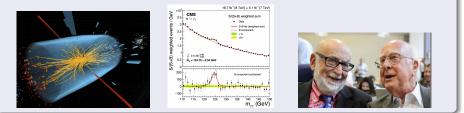
Strong gravitational radiation from a simple dark matter model

lason Baldes In collaboration with Camilo Garcia-Cely JHEP 1905 (2019) 190 arXiv:1809.01198

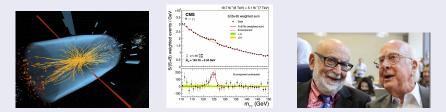


EPS-HEP2019 Ghent 11 July 2019

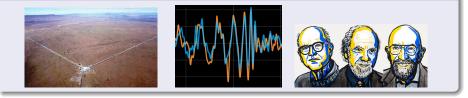
2012. Discovery of the Brout Englert Higgs boson



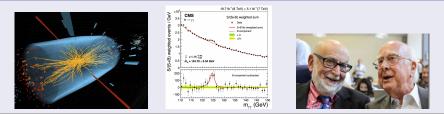
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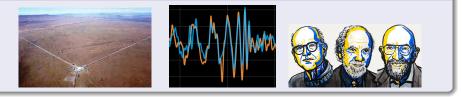
2016. Direct Detection of Gravitational Waves



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2016. Direct Detection of Gravitational Waves



Let us merge the two ideas.

Actually already done

by Witten '84, Hogan '86, ...

PHYSICAL REVIEW D

VOLUME 30, NUMBER 2

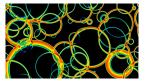
15 JULY 1984

Cosmic separation of phases

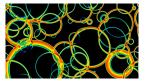
Edward Witten* Institute for Advanced Study, Princeton, New Jersey 08540 (Received 9 April 1984)

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- Symmetry is typically restored at high T.
- Violent events (e.g. cosmological phase transitions) produce gravitational waves.



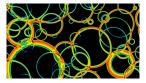
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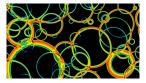
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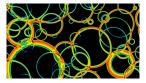
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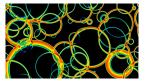
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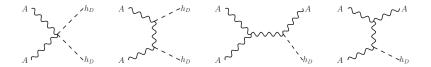


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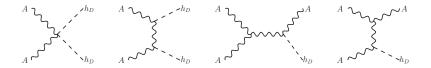
- Detected Higgs and GWs.
- Quantitative understanding of the predicted GW spectra has improved.
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- Concrete future proposals such as LISA have been developed.

The idea here is to explore a simple case study as to the feasibility of using GWs to detect SSB in a dark sector. $_{4/17}$



The Model: $SU(3)_C \times SU(2)_L \times U(1)_Y \times SU(2)_D$

$$\mathcal{L} \supset -\frac{1}{4} F_D \cdot F_D + (\mathcal{D}H_D)^{\dagger} (\mathcal{D}H_D) - \mu_2^2 H_D^{\dagger} H_D - \lambda_\eta (H_D^{\dagger} H_D)^2 - \lambda_{h\eta} H_D^{\dagger} H_D H^{\dagger} H_D$$

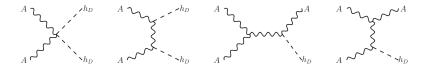


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Custodial SO(3) symmetry

Dark gauge bosons, A, are stable and form the DM!



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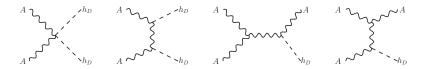
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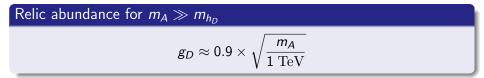
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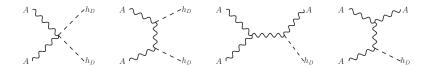
Potential possibilities

- Standard Potential with Mass terms Hambye 0811.0172
- ② Classically Scale Invariant

- Hambye, Strumia 1306.2329, - Hambye, Strumia, Teresi 1805.01473





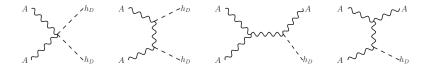


Relic abundance for $m_A \gg m_{h_D}$

$$g_D pprox 0.9 imes \sqrt{rac{m_A}{1~{
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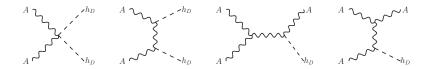
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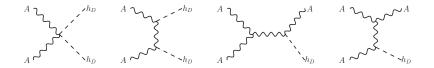
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- Determines relic abundance.
- Generates a thermal barrier \rightarrow first order PT.



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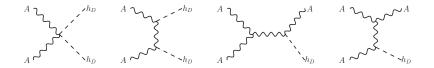
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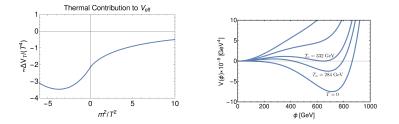
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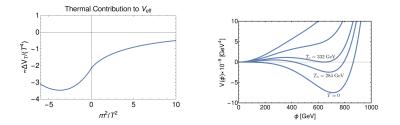
Close link between $\Omega_{\rm DM}$ and SSB \rightarrow Test using GWs! $$_{6/17}$$

Finite temperature effective potential



$$V_{\text{eff}} = V_{\text{tree}}(\phi) + V_1^0(\phi) + V_1^T(\phi, T) + V_{\text{Daisy}}(\phi, T)$$

Finite temperature effective potential



$$V_{\text{eff}} = V_{\text{tree}}(\phi) + V_1^0(\phi) + V_1^T(\phi, T) + V_{\text{Daisy}}(\phi, T)$$

Thermal Contribution

$$\frac{2\pi^2}{T^4} V_1^T(\phi, T) = \int_0^\infty y^2 \operatorname{Log} \left(1 - e^{-\sqrt{y^2 + m_i^2(\phi)/T^2}} \right) \mathrm{d}y$$
$$\approx -\frac{\pi^4}{45} + \frac{\pi^2 m^2}{12T^2} - \frac{\pi m^3}{6T^3} - \frac{m^4}{32T^4} \operatorname{Ln} \left(\frac{m^2}{220T^2} \right)$$

Euclidean Action

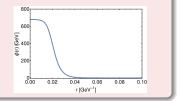
$$S_3 = 4\pi \int r^2 \left(\frac{1}{2} \left(\frac{d\phi_i}{dr} \right)^2 + \Delta V(\phi, \eta, T) \right) dr$$

Nucleation when $\Gamma/V \sim T^4 e^{-S_3/T} \sim H^4$.

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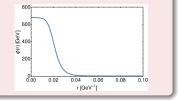
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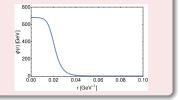
Find the latent heat and timescale of the PT

$$\alpha = \frac{1}{\rho_{\rm rad}} \left(1 - T \frac{\partial}{\partial T} \right) \left(V[\phi_0, \eta_0] - V[\phi_n, \eta_n] \right) \Big|_{T_n}$$
$$\beta = -\frac{d}{dt} \left(\frac{S_3}{T} \right) = H T_n \frac{d}{dT} \left(\frac{S_3}{T} \right) \Big|_{T_n}$$

Euclidean Action

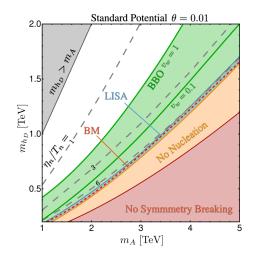
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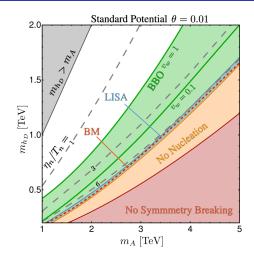


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Results



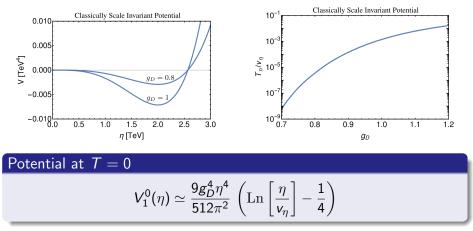
Results



LISA can test only limited parameter space of standard, polynomial type, potentials. BBO can do somewhat better. But we are really after a scenario which generically returns a lot of supercooling.

Classically Scale Invariant Potential

- Hambye, Strumia 1306.2329



The thermal contribution of the gauge bosons is added to this. Universe generically becomes vacuum dominated before PT. For $T_n < \Lambda_{\rm QCD}$ need to add effects of QCD - Iso, Serpico, Shimada 1704.04955

DM relic density

DM relic density

DM and PT possibilities

• Regime (i): standard freeze-out.

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Super-cool DM - Hambye, Strumia, Teresi 1805.01473

$$Y_{\rm DM}|_{\rm super-cool} = Y_{\rm DM}^{\rm eq} \frac{T_{\rm RH}}{T_{\rm infl}} \left(\frac{T_{\rm end}}{T_{\rm infl}}\right)^3$$

DM and PT possibilities

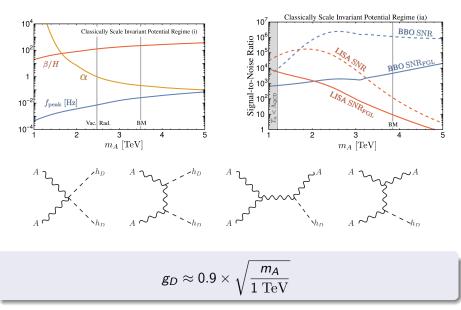
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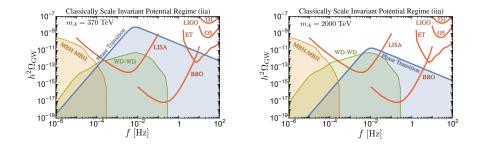
$$|Y_{
m DM}|_{
m super-cool} = |Y_{
m DM}^{
m eq} rac{T_{
m RH}}{T_{
m infl}} \left(rac{T_{
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m infl}}
ight)^3$$

Regime (ia) and (iia) are ameable for testing using GWs!

GW signal Regime (ia) - Freezeout



GW signal Regime (iia) - Super-cool DM

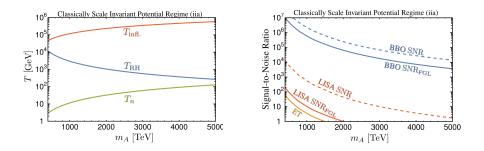


Super-cool DM

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Here $g_D \simeq 1$ and $m_A \gtrsim 370$ TeV.

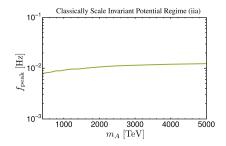
GW signal Regime (iia) - Super-cool DM



We correct for the period of matter domination after the PT.

$$f_{
m peak}
ightarrow \left(rac{T_{
m RH}}{T_{
m infl}}
ight)^{1/3} f_{
m peak} \qquad \Omega_{
m GW}
ightarrow \left(rac{T_{
m RH}}{T_{
m infl}}
ight)^{4/3} \Omega_{
m GW}$$

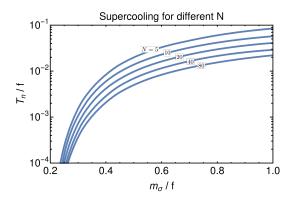
Peak Frequency Regime (iia) - Super-cool DM



Key prediction of the model

We find the peak frequency here is $\sim 10^{-2}$ Hz almost independent of m_A .

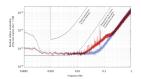
Another Possibility



- Composite Higgs with Dilaton Portal Dark Matter
 - IB, Gouttenoire, Sala, Servant. In Preparation.
- DM production from string breaking after supercooling/confinement.







	J



Summary

• Extensively studied the PTs for spin-one DM.



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- Case study for sensitivity of future GW observatories to DM models.



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- LISA, which will launch in 2034, will test scenarios with significant supercooling.
- More advanced instruments needed for polynomial potentials.
- Phase transitions: another pheno avenue to explore in your favourite models.
- Much work still needed \rightarrow exciting times ahead.

Backup

The terms of the one-loop effective potential

Effective Potential

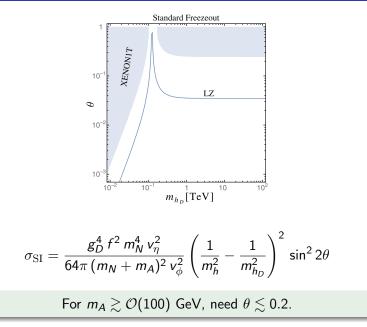
$$V_{\text{eff}} = V_{\text{tree}}(\phi) + V_1^0(\phi) + V_1^T(\phi, T) + V_{\text{Daisy}}(\phi, T)$$

$$V_1^{0}(\phi) = \sum_{i} \frac{g_i(-1)^F}{64\pi^2} \left\{ m_i^4(\phi) \left(\text{Log}\left[\frac{m_i^2(\phi)}{m_i^2(v)}\right] - \frac{3}{2} \right) + 2m_i^2(\phi)m_i^2(v) \right\}$$

$$V_1^T(\phi, T) = \sum_i \frac{g_i(-1)^F T^4}{2\pi^2} \times \int_0^\infty y^2 \operatorname{Log}\left(1 - (-1)^F e^{-\sqrt{y^2 + m_i^2(\phi)/T^2}}\right) dy$$

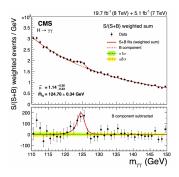
$$V_{\text{Daisy}}^{\phi}(\phi, T) = rac{T}{12\pi} \Big\{ m_{\phi}^{3}(\phi) - \big[m_{\phi}^{2}(\phi) + \Pi_{\phi}(\phi, T) \big]^{3/2} \Big\}$$

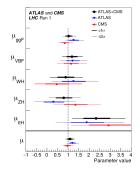
Direct Detection - Limit on Mixing



3/15

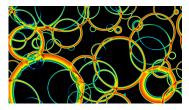
LHC constraints - Limit on Mixing



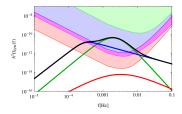


 $heta \lesssim \mathcal{O}(0.1)$

Predicted GW spectra



From a simulation by Weir et. al.



LISA working group 1512.06239

$$h^2 \Omega_{
m GW}(f) \equiv h^2 rac{f}{
ho_c} rac{d
ho_{
m GW}}{df}$$

Three contributions

- Scalar field contribution
- Sound waves in the plasma
- Magnetohydrodynamic Turbulence.

Predicted GW spectra

The spectra depend on the macroscopic properties

- Latent heat α
- Timescale of the transition β^{-1}
- The Hubble scale (or almost equivalently T_n)
- The wall velocity vw

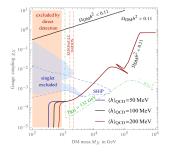
These are all calculable from microphysics (although v_w is technically challenging).

We can calculate these quantities and then match onto results from simulations/semi-analytic studies.

If enough of a plasma is present - Bodeker, Moore 1703.08215

- Runaway wall is prevented by $P_{
 m LO} \sim T^2 \Delta M^2$ or $P_{
 m NLO} \sim \gamma g^2 T^3 \Delta M$
- Scalar field contribution is suppressed.

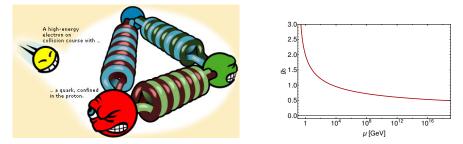
Super-cool DM relic density



Super-cool DM - Hambye, Strumia, Teresi 1805.01473

$$Y_{\rm DM}|_{\rm super-cool} = Y_{\rm DM}^{\rm eq} \frac{T_{\rm RH}}{T_{\rm infl}} \left(\frac{T_{\rm n}}{T_{\rm infl}}\right)^3$$
$$Y_{\rm DM}|_{\rm sub-thermal} = M_{\rm Pl} M_{\rm DM} \langle \sigma_{\rm ann} v_{\rm rel} \rangle \sqrt{\frac{\pi g_*}{45}} \int_{z_{\rm RH}}^{\infty} \frac{dz}{z^2} Y_{\rm eq}^2$$

Taking into account QCD

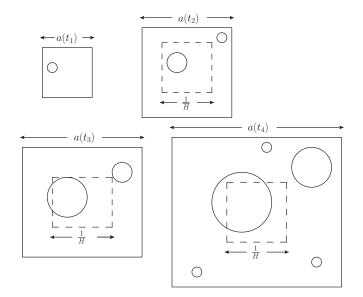


If $T_n \leq \Lambda_{QCD}$, QCD confinement must be taken into account.

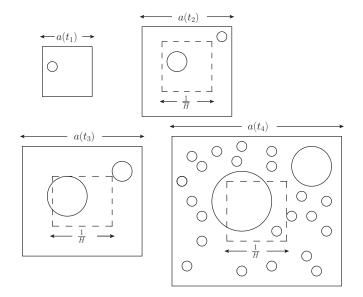
- When QCD confines a mass scale enters the potential.
- EW Symmetry is broken by the quark condensate.
- The Higgs gets a VEV $\langle h \rangle \sim \Lambda_{\rm QCD}$ induced by $y_t h \langle \overline{t_L} t_R \rangle$. - Witten '81
- This gives a mass term $V_{\rm eff} \supset -\lambda_{h\eta} \Lambda^2_{QCD} \eta^2$.
- The thermal barrier disappears at $T \sim m_h \Lambda_{QCD}/m_A$.
 - Iso, Serpico, Shimada 1704.04955

- \bullet With massless quarks QCD PT is first order at ${\it T} \sim \Lambda_{QCD}:$ GW signal
 - Helmboldt, Kubo, van der Woude 1904.07891
- However inflation continues until $T \sim m_h \Lambda_{QCD}/m_A$ \rightarrow suppresses signal.
- $SU(2)_D$ PT is also first order.
- But due to mass term $V_{\rm eff} \supset -\lambda_{h\eta} \Lambda^2_{QCD} \eta^2$ signal is weak.

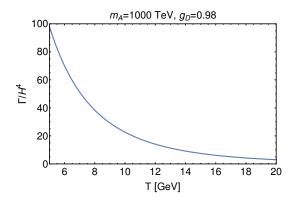
So we focus on $T_n > \Lambda_{\text{QCD}}$ instead.



If nucleation rate is low, we can form bubbles which never meet.

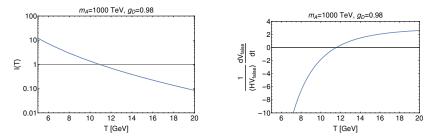


If nucleation grows enough, sufficient bubbles to meet will nucleate. 11/15



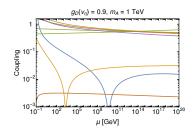
In the classically scale invariant potential we have a slow transition but an exponentially growing nucleation rate.

We can explicitly check the volume of false vacuum decreases and the bubbles will percolate.



$$\begin{split} P(T) &\equiv e^{-I(T)} \lesssim 1/e \implies I(T) = \frac{4\pi}{3} \int_{t_c}^t dt' \Gamma(t') a(t')^3 r(t,t')^3 \gtrsim 1 \\ &\frac{1}{H \mathcal{V}_{\text{false}}} \frac{d \mathcal{V}_{\text{false}}}{dt} = 3 + T \frac{dI}{dT} \lesssim -1. \end{split}$$

Radiative Symmetry Breaking



We start with a classically scale invariant theory

The dark gauge coupling drives the exotic quartic negative in the IR

$$\beta_{\lambda_{\eta}} = \frac{1}{(4\pi)^2} \left(\frac{9}{8} g_D^4 - 9 g_D^2 \lambda_{\eta} + 2\lambda_{h\eta}^2 + 24\lambda_{\eta}^2 \right)$$

- This signals radiative symmetry breaking Coleman, E. Weinberg '73
- The potential is approximated in the flat direction in field space - Gildener, S. Weinberg '76

