

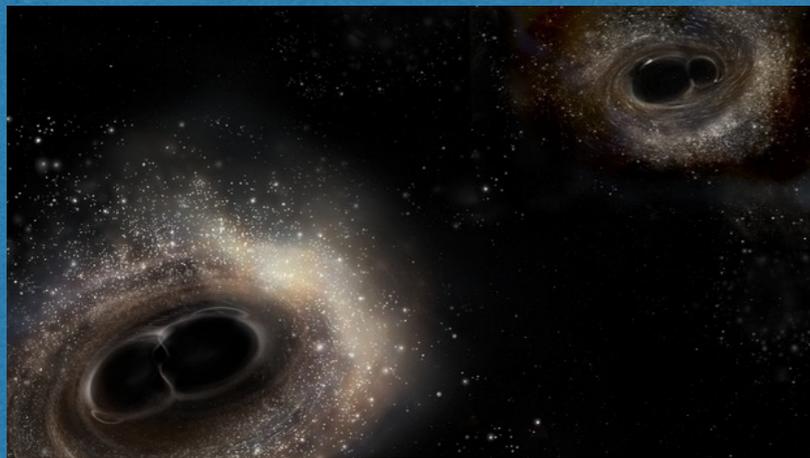
# Searching for the stochastic gravitational-wave background with Advanced LIGO and Advanced Virgo

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Albert Einstein Institute, Potsdam  
EPS-HEP 2019, 13 July 2019

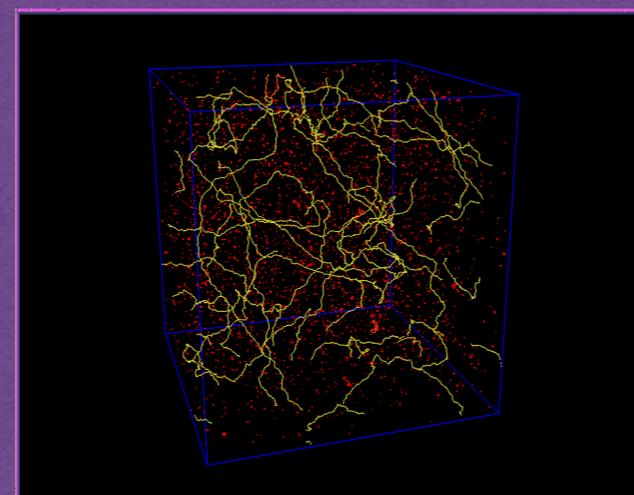
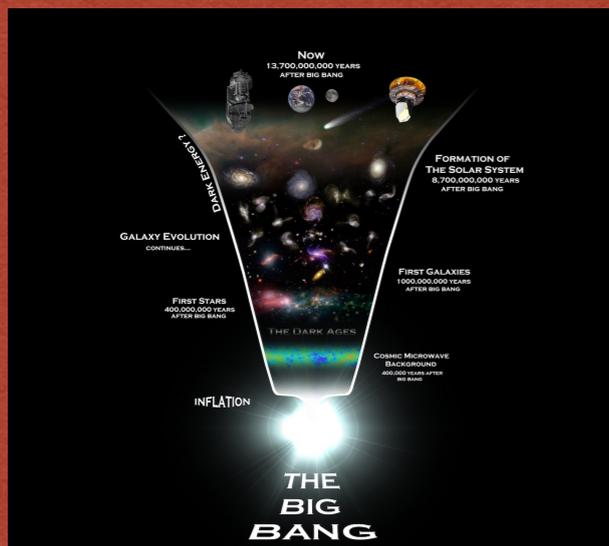
# Stochastic gravitational wave background

A superposition of astrophysical and cosmological sources, including...



Unresolved astrophysical sources (binaries, supernovae, NS, ...)

Early Universe  
(inflation, pre big-bang, ...)



Cosmic Strings

Cosmological  
Phase Transitions



# Data analysis technique

Cross correlate the time series from 2+ detectors

The signal is long duration and non-deterministic

$$s_1 = h_1 + n_1$$

$$s_2 = h_2 + n_2$$

signal and noise  
are uncorrelated

$$\langle s_1 s_2 \rangle = \langle h_1 h_2 \rangle + \langle h_2 n_1 \rangle + \langle h_1 n_2 \rangle + \langle n_1 n_2 \rangle$$

signal

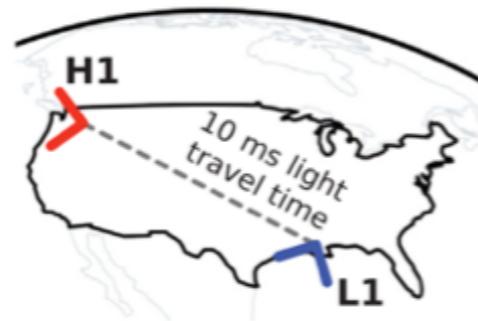
noise at 2 widely  
separated detectors is  
uncorrelated

# Analysis of LIGO's first two observing runs

We analyzed data at H1 and L1 from the first two observing runs  
(O1) September 2015—January 2016  
(O2) December 2016-August 2017



Hanford, Washington (H1)



## O2 Results papers

Abbott *et al*, 1903.02886

Abbott *et al*, 1903.08844

Livingston, Louisiana (L1)

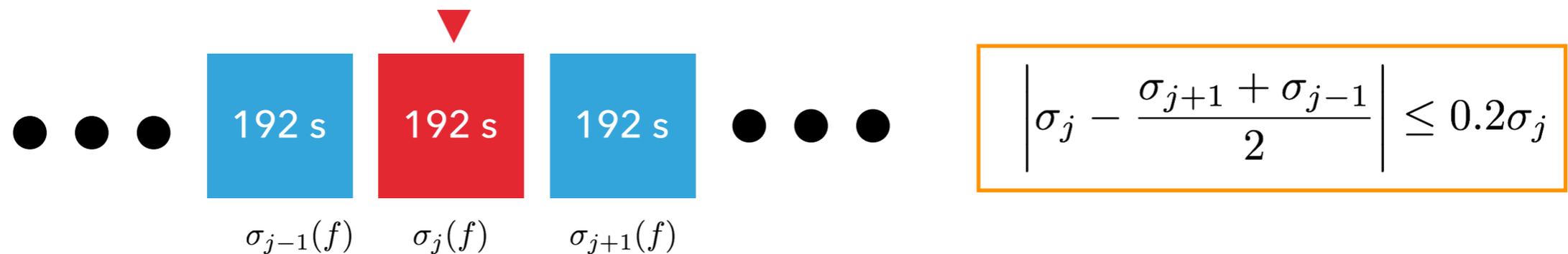


# Analysis cuts

Abbott *et al*, Phys.Rev.Lett. 118 (2017) no.12, 121101

Abbott *et al*, 1903.02886

1. We remove times where data is known to be corrupt (for example: interferometer not operational)
2. We remove time segments where noise is non-stationary



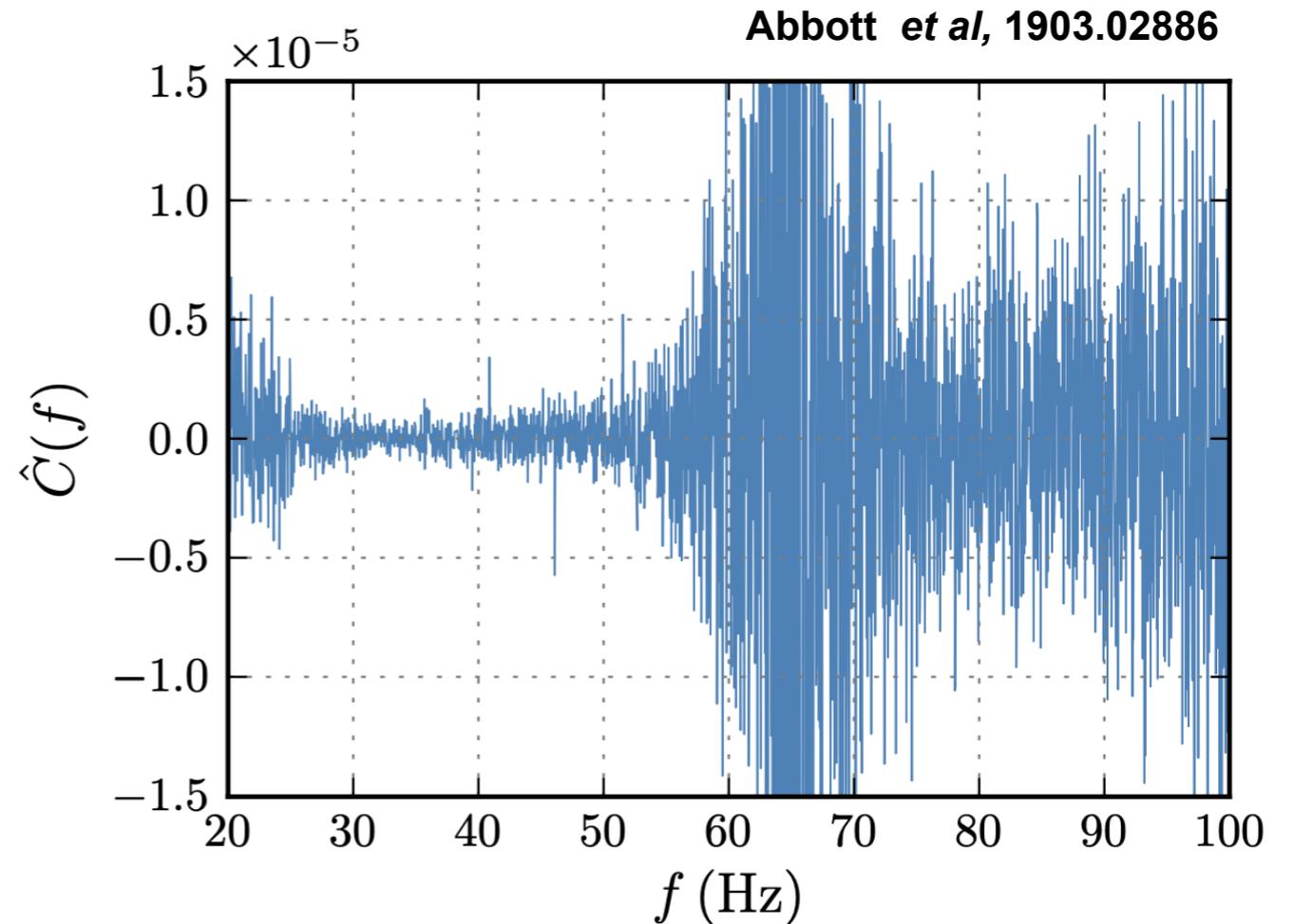
3. We remove frequency bins which display coherence with instrumental (auxiliary) channels

Covas *et al*, Phys.Rev. D97 (2018) no.8, 082002

# Cross-correlation spectrum

Representation of data in form  
useful for stochastic searches

Spectrum consistent with  
Gaussian, un-correlated noise

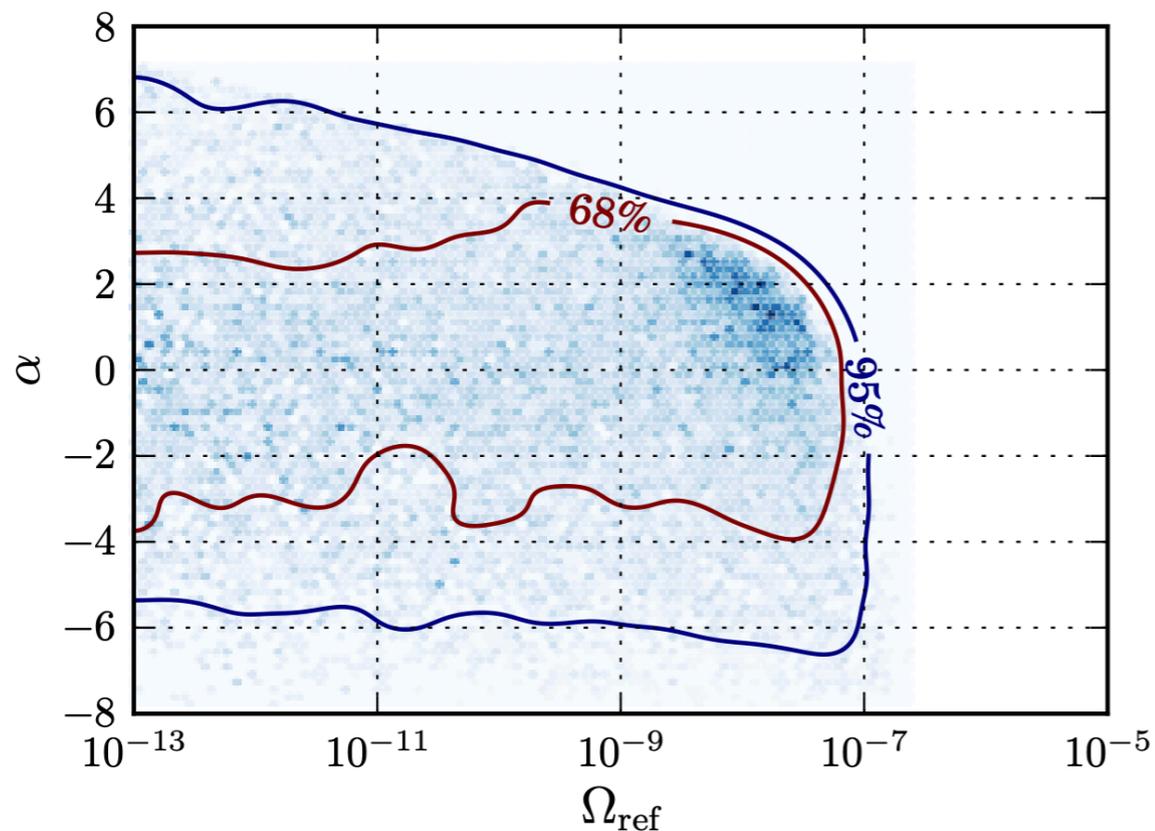


$\alpha$	$\hat{\Omega}_{\text{ref}} (\text{O2})$	$\hat{\Omega}_{\text{ref}} (\text{O1})$	O2 Sensitive band
0	$(2.2 \pm 2.2) \times 10^{-8}$	$(4.4 \pm 6.0) \times 10^{-8}$	20-85.8 Hz
2/3	$(2.0 \pm 1.6) \times 10^{-8}$	$(3.5 \pm 4.4) \times 10^{-8}$	20-98.2 Hz
3	$(3.5 \pm 2.8) \times 10^{-9}$	$(3.7 \pm 6.6) \times 10^{-9}$	20-305 Hz

\* Increase in sensitivity is more than  
“O1 + longer integration time”

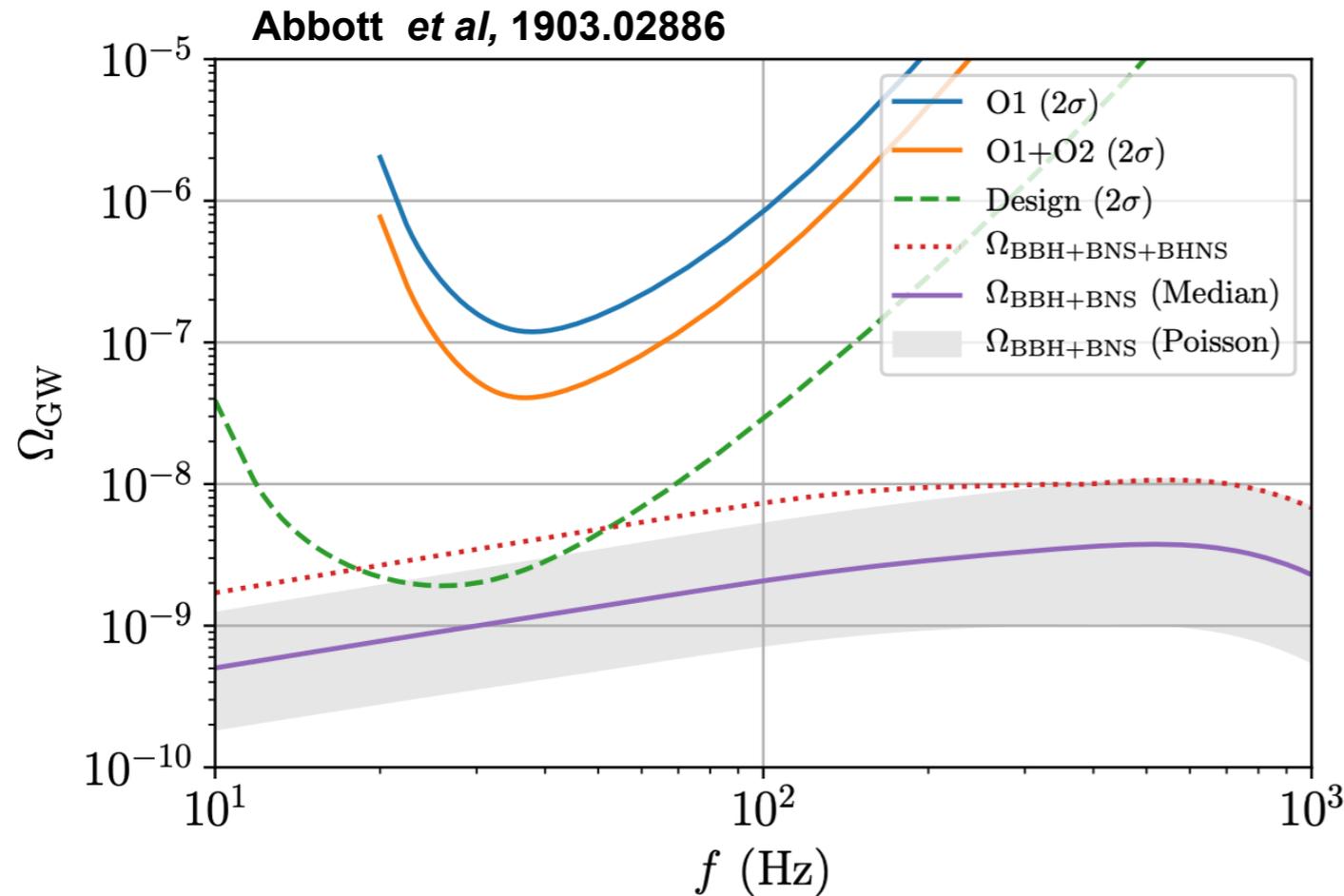
# Upper limits

$\alpha$	Uniform prior		Log-uniform prior	
	O1+O2	O1	O1+O2	O1
0	$6.0 \times 10^{-8}$	$1.7 \times 10^{-7}$	$3.5 \times 10^{-8}$	$6.4 \times 10^{-8}$
2/3	$4.8 \times 10^{-8}$	$1.3 \times 10^{-7}$	$3.0 \times 10^{-8}$	$5.1 \times 10^{-8}$
3	$7.9 \times 10^{-9}$	$1.7 \times 10^{-8}$	$5.1 \times 10^{-9}$	$6.7 \times 10^{-9}$
Marg.	$1.1 \times 10^{-7}$	$2.5 \times 10^{-7}$	$3.4 \times 10^{-8}$	$5.5 \times 10^{-8}$



\* Improvement over O1 by about a factor of 2.8

# Implications for CBC background



## ***predictions***

$$\Omega_{\text{BBH}}(25 \text{ Hz}) = 5.3_{-2.5}^{+4.2} \times 10^{-10}$$

$$\Omega_{\text{BNS}}(25 \text{ Hz}) = 3.6_{-3.1}^{+8.4} \times 10^{-10}$$

$$\Omega_{\text{BBH+BNS}}(25 \text{ Hz}) = 8.9_{-5.6}^{+12.6} \times 10^{-10}$$

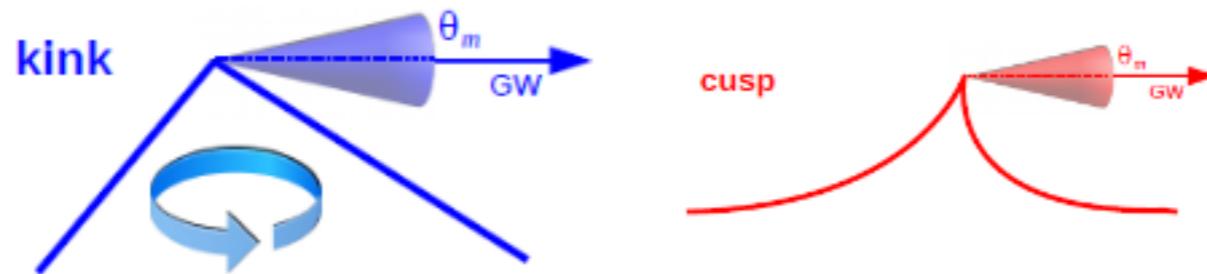
*upper limit*  $\Omega_{\text{BHNS}}(25 \text{ Hz}) = 9.1 \times 10^{-10}$

$$\Omega_{\text{GW}}(f, \theta_k) = \frac{f}{\rho_c H_0} \int_0^{z_{\text{max}}} dz \frac{R_m(z, \theta_k) \frac{dE_{\text{GW}}(\theta_k)}{df}}{(1+z)E(\Omega_M, \Omega_\Lambda, z)}$$

May detect background at design sensitivity

# Implications for cosmic string background

- Cusps and kinks in network of cosmic strings can produce gravitational waves



c/o Florent Robinet

- Place upper limits on string tension within the context of 2 different models of string network

Blanco-Pillado et al

$$G\mu/c^2 \leq 1.1 \times 10^{-6}$$

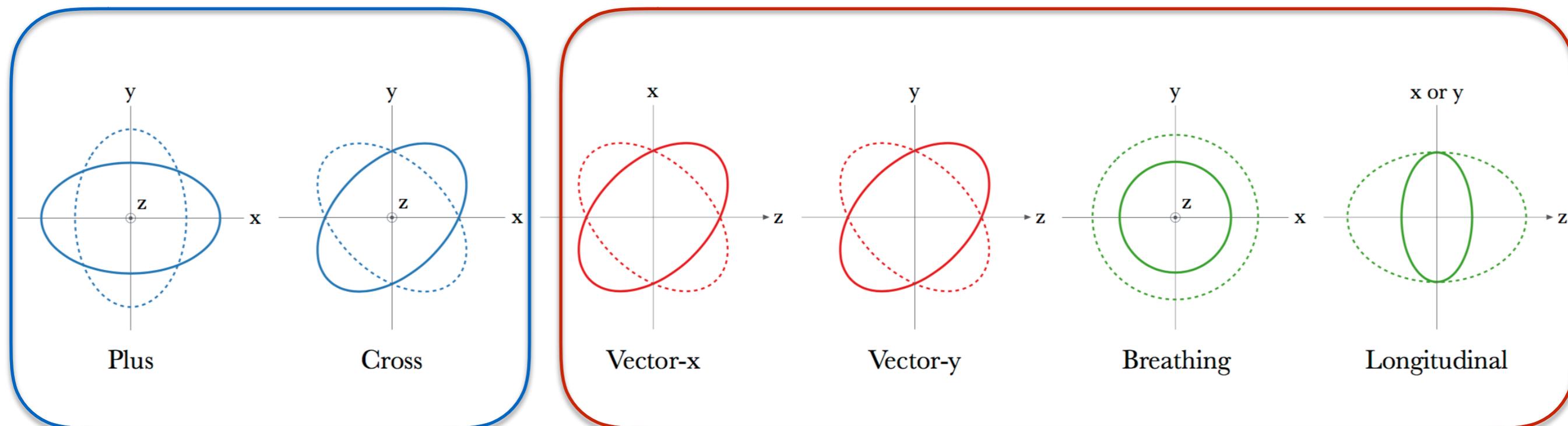
Lorenz et al

$$G\mu/c^2 \leq 2.1 \times 10^{-14}$$

# Non-tensor polarizations

Abbott *et al*, 1903.02886

6 polarizations for a symmetric 3x3 tensor



**Predicted by GR**

**Modification of GR**

With uniform prior, obtain limits on backgrounds of each polarization

$$\Omega_T < 8.2 \times 10^{-8} \quad \Omega_S < 4.2 \times 10^{-7}$$

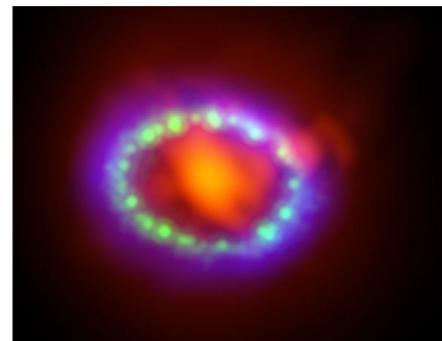
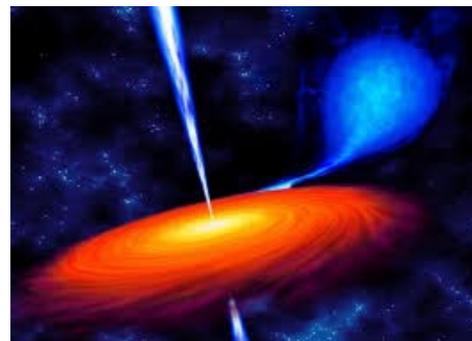
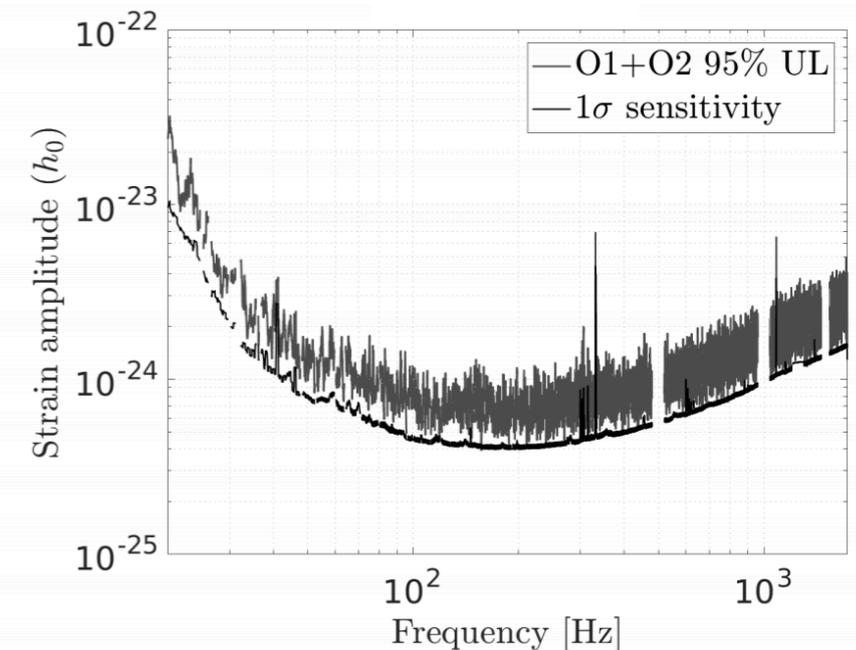
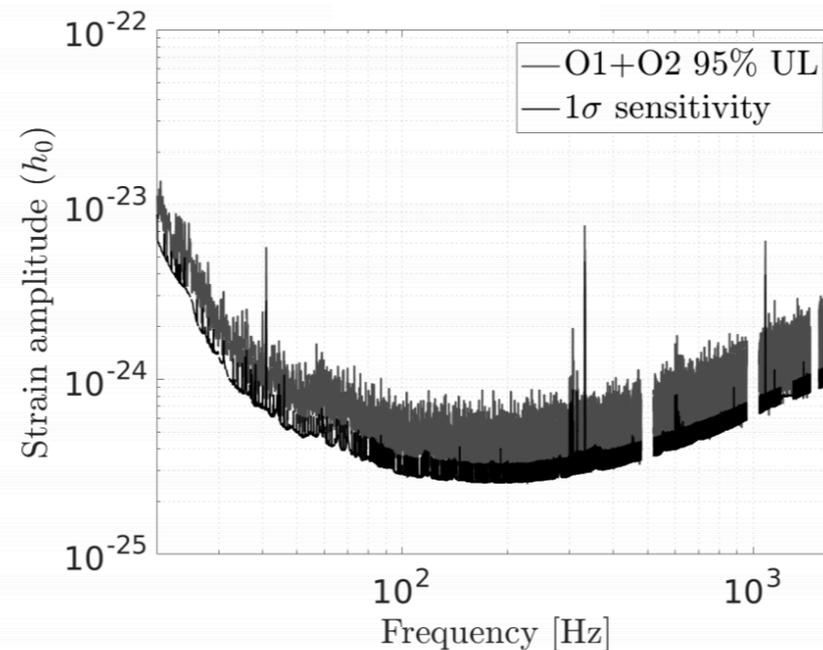
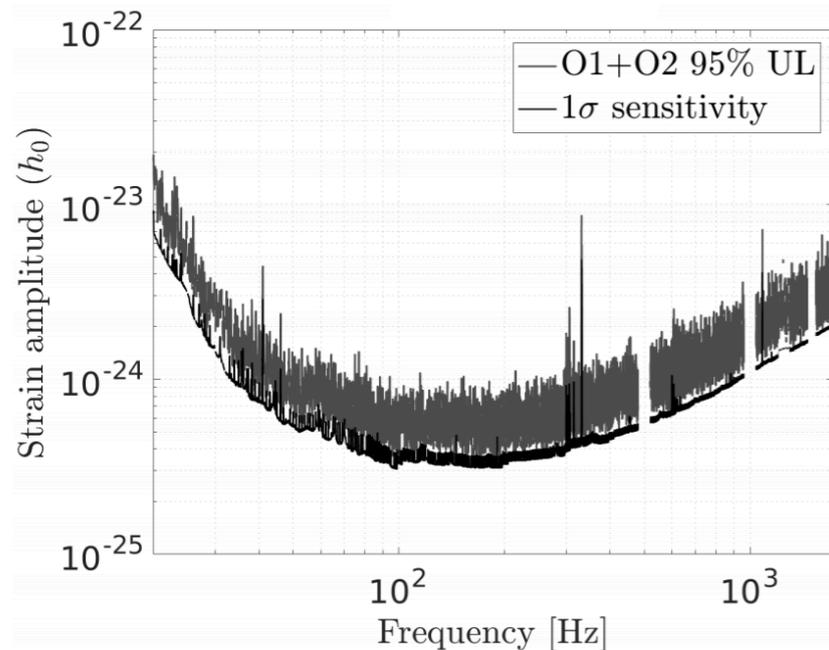
$$\Omega_V < 1.2 \times 10^{-7}$$

# Directional searches: narrowband sources

Abbott *et al*, 1903.08844

## Narrowband Radiometer Results

Direction	Max SNR	$p$ -value (%)	Frequency (Hz) ( $\pm 0.016$ Hz)	Best UL ( $\times 10^{-25}$ )	Frequency band (Hz)
Sco X-1	4.80	4.5	1602.09	4.2	183.6 – 184.6
SN 1987A	4.95	1.7	181.81	3.6	247.75 – 248.75
Galactic Center	3.80	98	20.28	4.7	156.8 – 157.8

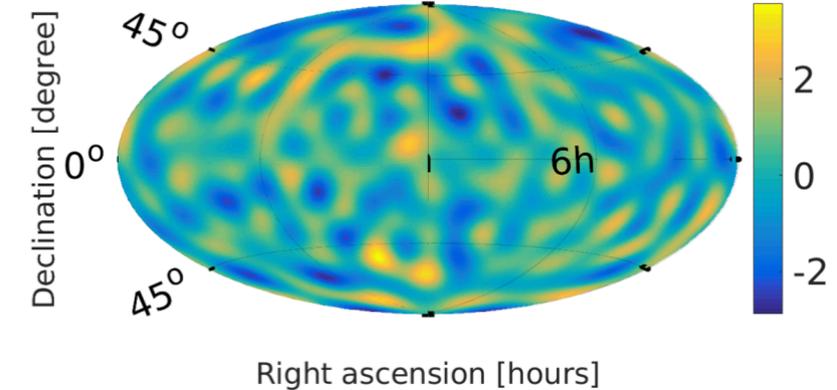
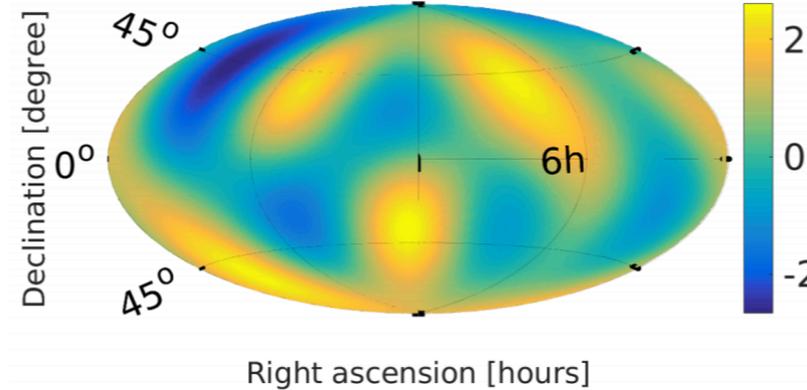
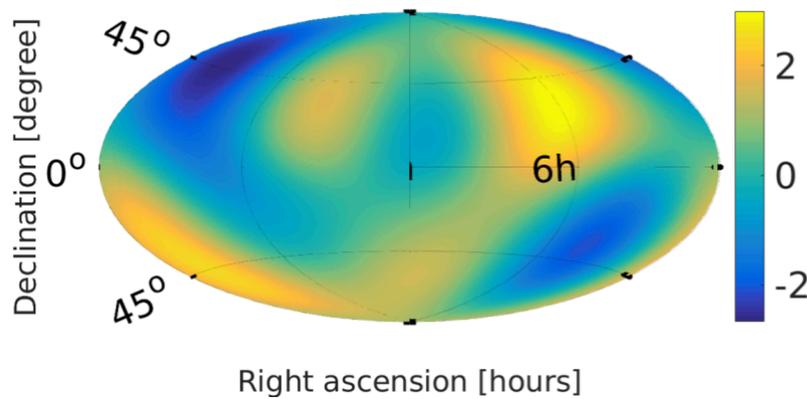


36.06 Hz frequency bin marginally significant in ScoX-1 direction in O2 (but not O1+O2) 11

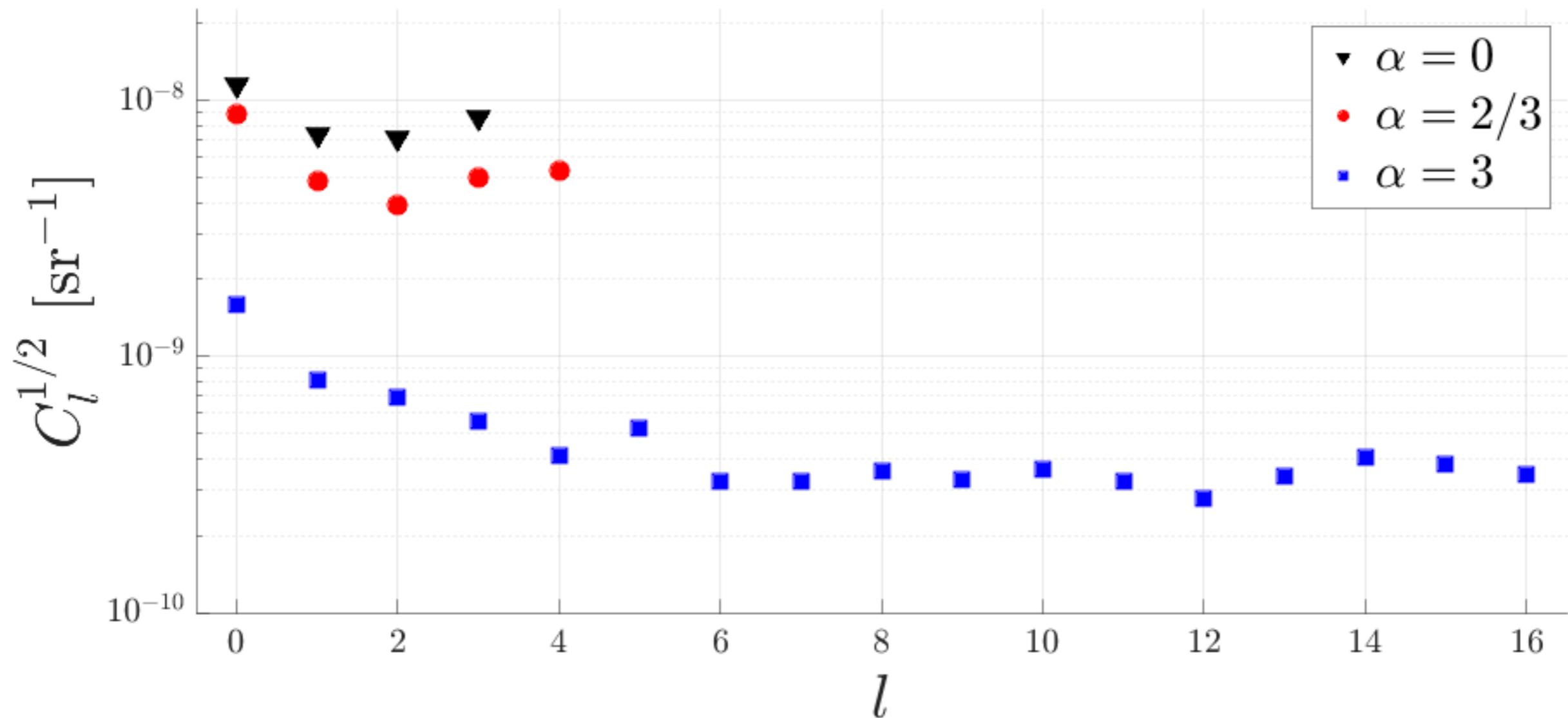
# Directional search: broadband sources

## All-sky (broadband) Results

$\alpha$	$\Omega_{\text{gw}}$	$H(f)$	Max SNR (% $p$ -value)		Upper limit ranges		O1 Upper limit ranges	
			BBR	SHD	BBR ( $\times 10^{-8}$ )	SHD ( $\times 10^{-8}$ )	BBR ( $\times 10^{-8}$ )	SHD ( $\times 10^{-8}$ )
0	constant	$\propto f^{-3}$	3.09 (9)	2.98 (9)	4.4 – 25	0.78 – 2.90	15 – 65	3.2 – 8.7
2/3	$\propto f^{2/3}$	$\propto f^{-7/3}$	3.09 (20)	2.61 (31)	2.3 – 14	0.64 – 2.47	7.9 – 39	2.5 – 6.7
3	$\propto f^3$	constant	3.27 (66)	3.57 (27)	0.05 – 0.33	0.19 – 1.1	0.14 – 1.1	0.5 – 3.1



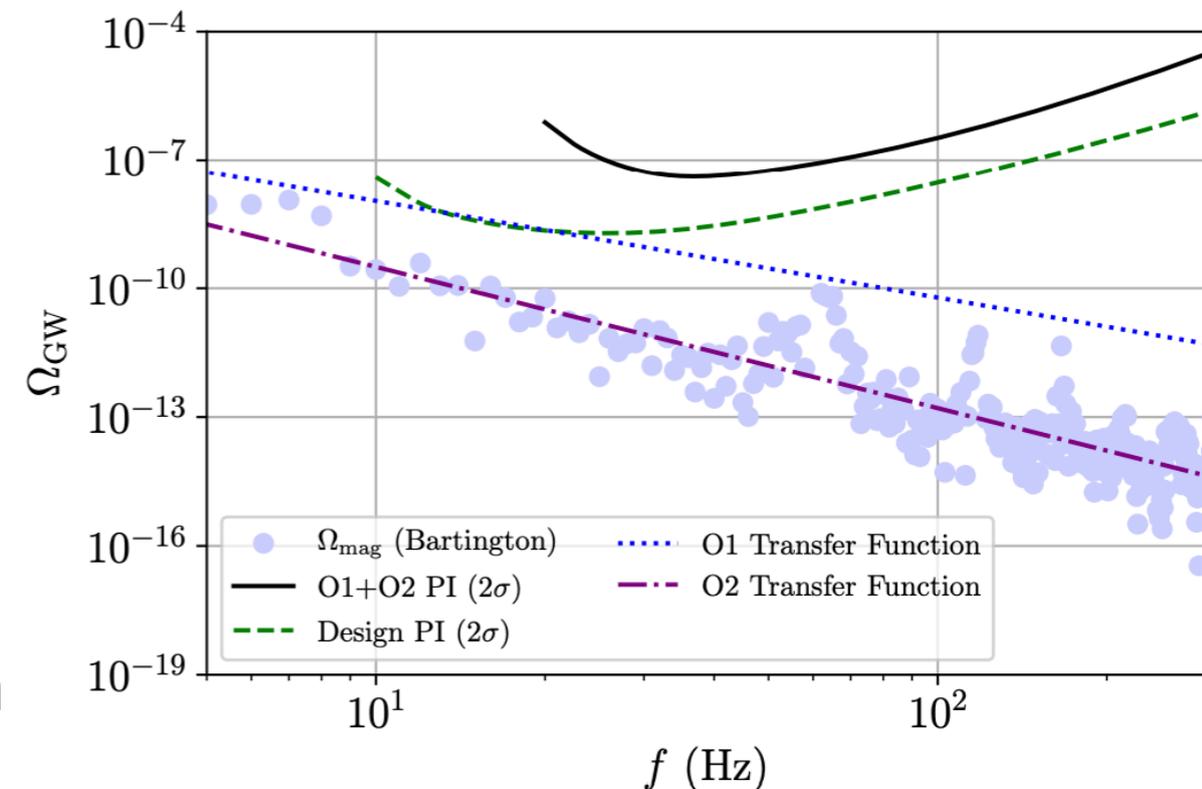
# Directional searches: Upper limits on CL



Abbott *et al*, 1903.08844

# Magnetic noise

- \* Global scale Schumann resonances lead to correlated magnetic noise.
  - \* We construct budget using magnetic transfer functions and cross-correlation spectrum between magnetic fields
- $$\Omega_{\text{mag}}(f) = \frac{|T_1(f)||T_2(f)|\text{Re}[M_{12}(f)]}{\gamma_T(f)S_0(f)}$$
- \* Upper limits indicate that this is not an issue in O2, could be in issue in future runs.
  - \* Mitigation strategies being developed including Wiener filtering and Bayesian estimation.



# Summary

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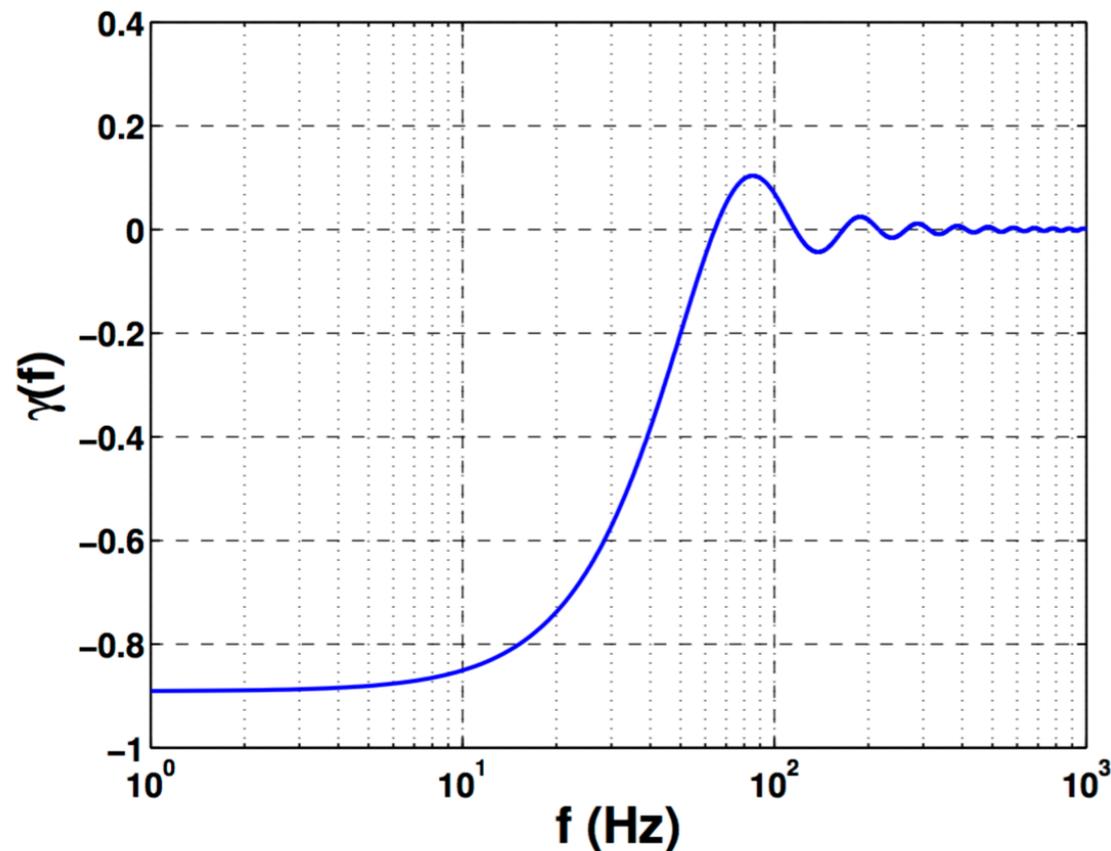
- Searched O1 and O2 data for stochastic background, did not detect
- Upper limits placed on the stochastic background
  - isotropic for different spectral shapes
  - non-tensor modes
- Studied implications of results for cosmic string and CBC models
- Detection of CBC background possible at design sensitivity

Extras

# Overlap reduction function

Cross correlation of detector outputs is related to  $\Omega_{\text{GW}}$

$$\langle \tilde{s}_1(f)^* \tilde{s}_2(f) \rangle = \frac{3H_0^2}{20\pi^2} \delta(f - f') |f|^{-3} \Omega_{\text{GW}}(|f|) \gamma(|f|)$$



Allen and Romano, Phys.Rev. D59 (1999) 102001

Overlap reduction function

$$\gamma(f) := \frac{5}{8\pi} \sum_A \int_{S^2} d\hat{\Omega} \underbrace{e^{i2\pi f \hat{\Omega} \cdot \Delta \vec{x} / c}}_{\text{time delay}} \underbrace{F_1^A(\hat{\Omega}) F_2^A(\hat{\Omega})}_{\text{detector response}}$$

Geometric factor controlling  
sensitivity

# Anisotropic background

$$\langle h_A^*(f, \hat{\Omega}) h_{A'}(f', \hat{\Omega}') \rangle = \frac{1}{4} \mathcal{P}(f, \hat{\Omega}) \delta(f - f') \delta_{AA'} \delta(\hat{\Omega}, \hat{\Omega}')$$

Typically assume  $\mathcal{P}(f, \hat{\Omega}) = \mathcal{P}(\hat{\Omega}) \bar{H}(f)$

Expand  $\mathcal{P}(\Theta)$  in a basis

$$\mathcal{P}(\Theta) = \mathcal{P}_\alpha \mathbf{e}_\alpha(\Theta)$$

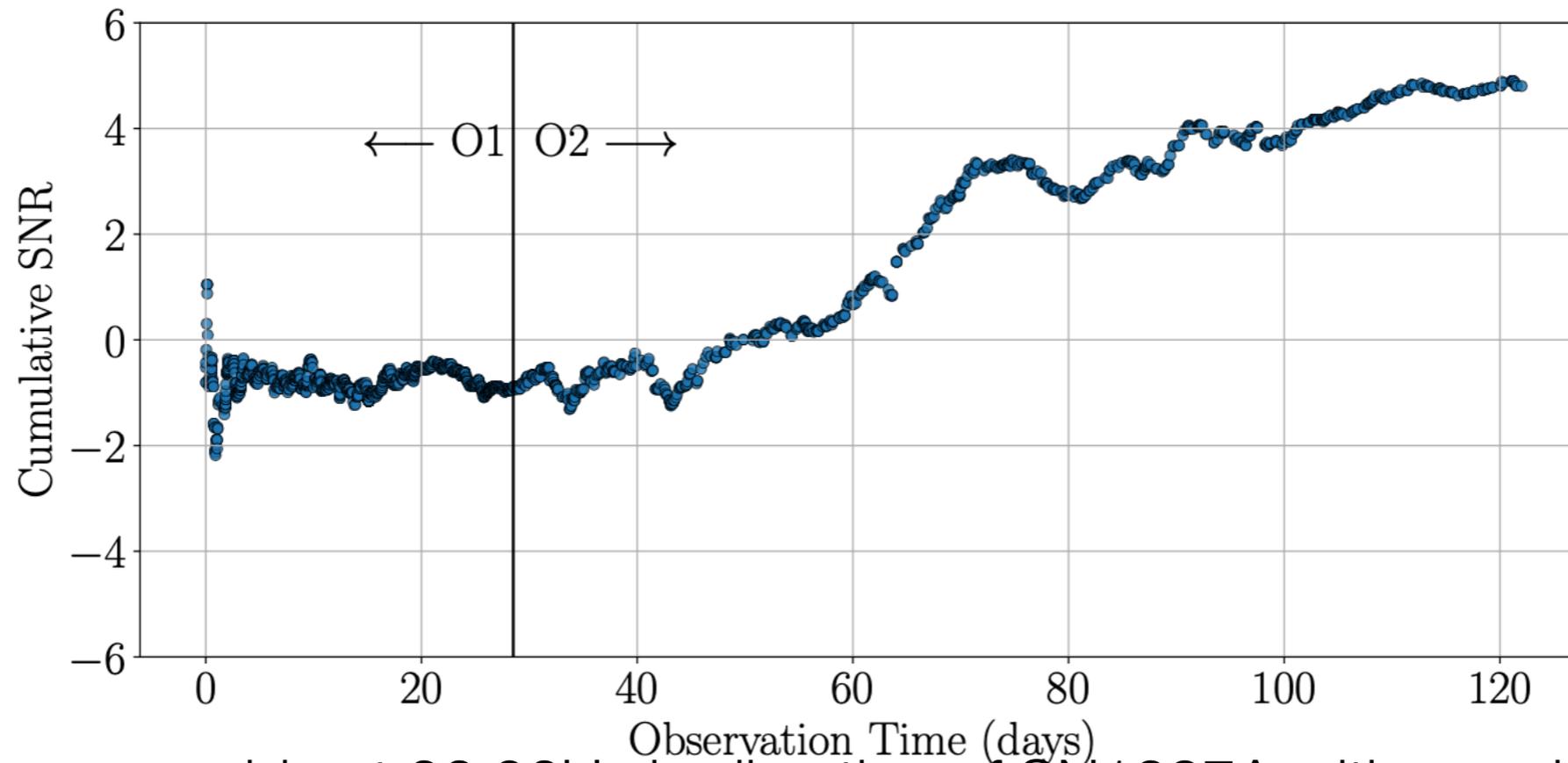
$$\mathbf{e}_\alpha(\Theta) = \delta^2(\Theta, \Theta_\alpha)$$

Radiometer search  
point sources

$$\mathbf{e}_\alpha(\Theta) = Y_{\ell m}(\Theta)$$

Spherical harmonic search

# Radiometer outlier



- \* 1 frequency bin at 36.06Hz in direction of SN1987A with marginal significance (3 sigma) in O2
- \* Not significant combining O1 and O2 (we will learn more in O3)
- \* If we interpret result as a neutron star at distance of SN1987A, infer ellipticity  $3 \times 10^{-2}$