

# Physics at FCC-ee



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## Outline

1. The Future Circular Collider Study
2. FCC-ee Electroweak Studies at the Z Pole, ZH,  $W^+W^-$  and  $t\bar{t}$  thresholds
3. QCD Physics at FCC-ee





# FCC – Future Circular Collider



**FCC - international collaboration hosted at CERN,  
goal: construction of ~100 km circumference  
tunnel infrastructure in Geneva area**

**to host:**

- ✓ **e<sup>-</sup>-e<sup>+</sup> collider:** FCC-ee – potential first step, preceding the FCC-pp
- ✓ **p-p collider:** FCC-hh – flagship, 100 TeV p-p, 16T Nb<sub>3</sub>Sn magnets
- ✓ **e-p collider:** FCC-he – additional option of e-p collisions; e<sup>-</sup> from ERL



- 136 institutes
  - 34 countries
  - 32 industrial partners
- EC H2020**
- EuroCirCol project
  - EASITrain ITN

**The Conceptual Design Report issued in January, 2019:**

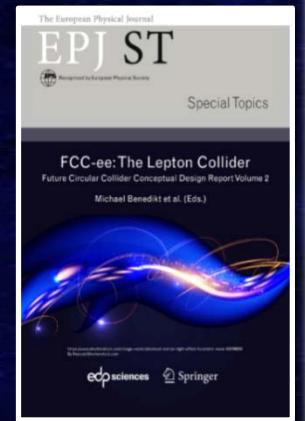
(~1364 contributors, 351 institutes – a truly global collaboration and effort – as suggested by the EPPSU'13): <https://fcc-cdr.web.cern.ch/>

**The FCC-ee European Particle Physics Strategy Update (EPPSU) document:**

**FCC week 2019, Brussels, 24-28, June**

<https://cds.cern.ch/record/2653669>

<http://fccweek2019.web.cern.ch/>

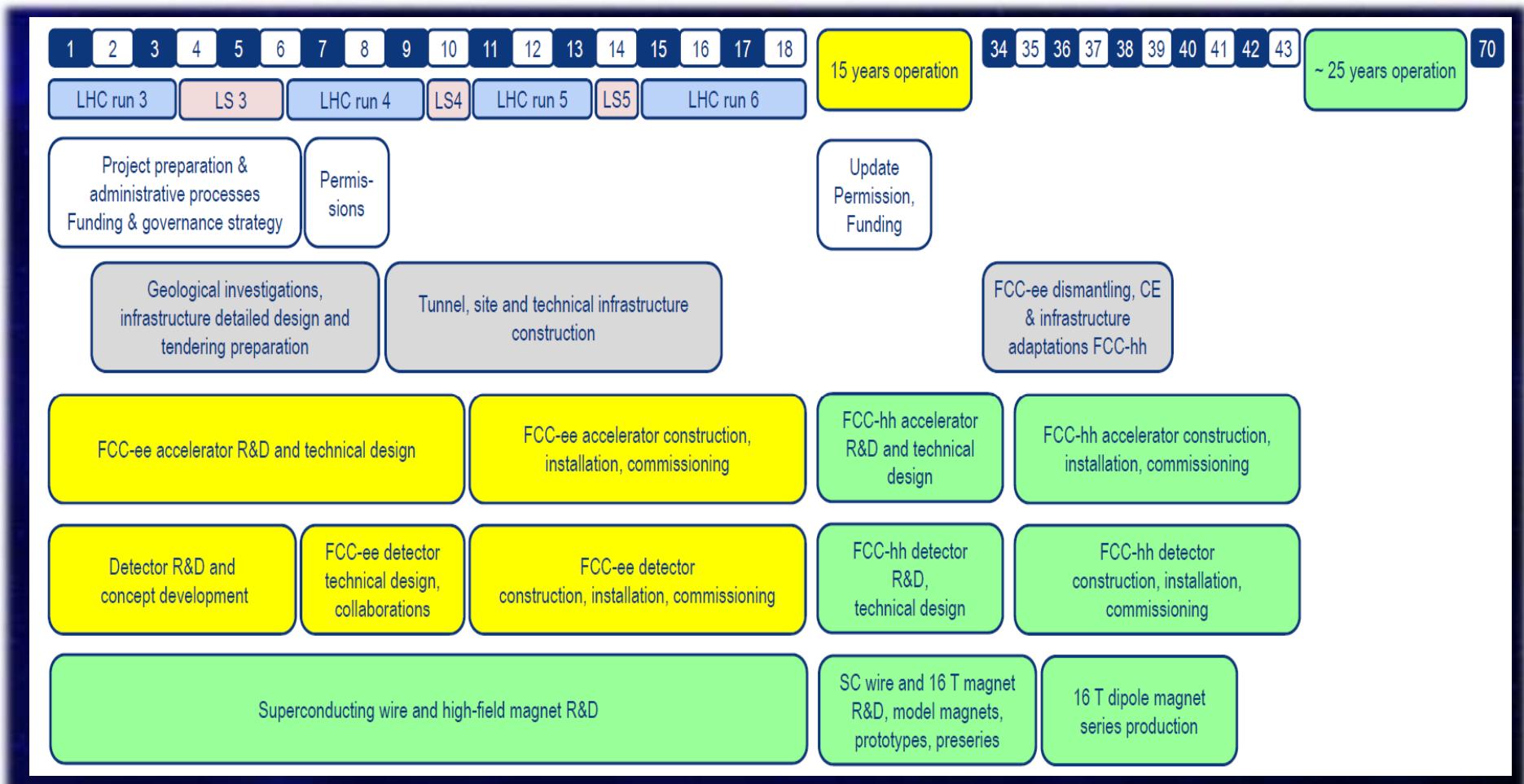




# FCC Integrated Project Technical Schedule



The FCC project plan is fully integrated with HL-LHC exploitation and provides for seamless further continuation of particle physics in Europe





# FCC-ee Operation Model



working point	Design luminosity/IP [ $10^{34} \text{ cm}^{-2}\text{s}^{-1}$ ]	total luminosity (2 IPs)/ yr	physics goal	run time [years]
Z first 2 years	115 (50% nominal)	24 $\text{ab}^{-1}$ /year	150 $\text{ab}^{-1}$	4
Z later	230	48 $\text{ab}^{-1}$ /year		
W	28	6 $\text{ab}^{-1}$ /year	10 $\text{ab}^{-1}$	2
H	8.5	1.7 $\text{ab}^{-1}$ /year	5 $\text{ab}^{-1}$	3
machine modification for RF installation & rearrangement: <b>1 year</b>				
top 1st year (350 GeV)	0.95 (50% nominal)	0.2 $\text{ab}^{-1}$ /year	0.2 $\text{ab}^{-1}$	1
top later (365 GeV)	1.55	0.34 $\text{ab}^{-1}$ /year	1.5 $\text{ab}^{-1}$	4

**total program duration: 15 years (including machine modifications)**

**phase 1 (Z, W, H): 9 years,  
phase 2 (top): 6 years**

(Total luminosity calculation based on 185 physics days per year, 75% efficiency, design luminosities and 10% overall contingency)



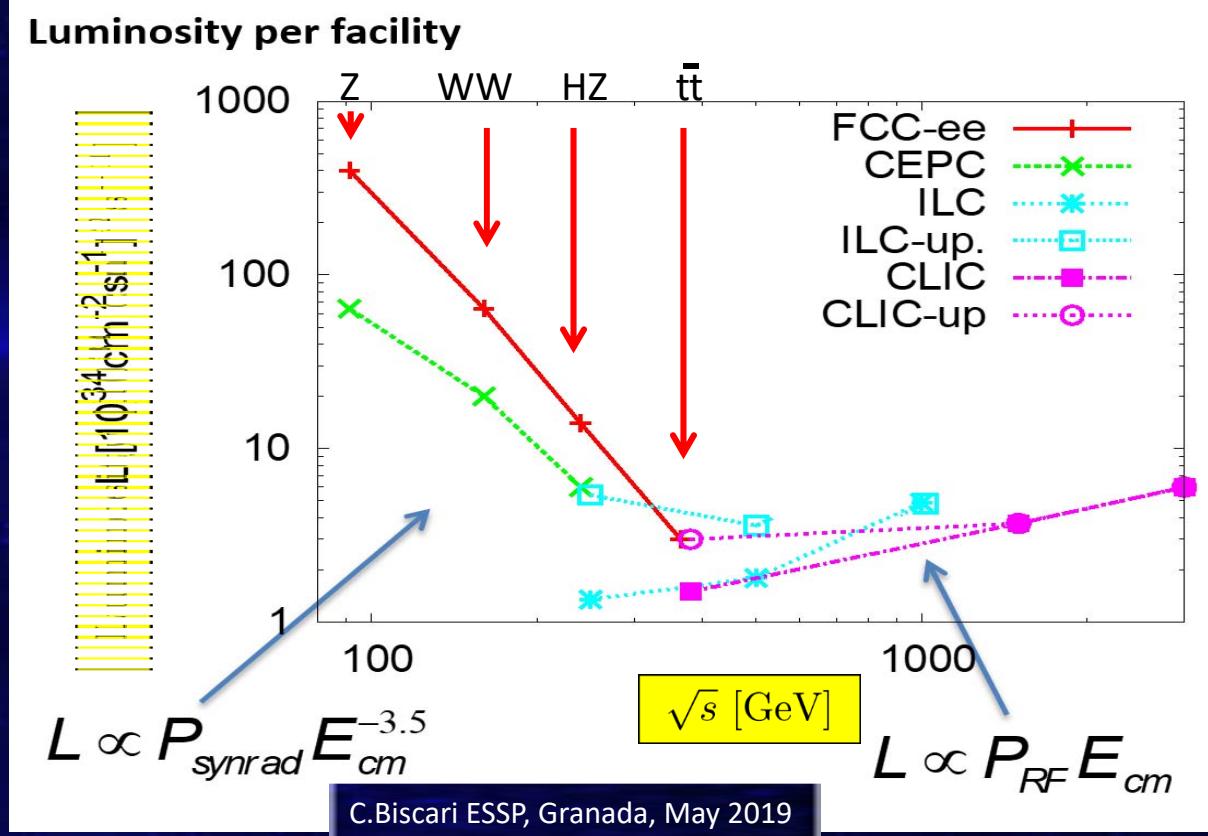
# FCC-ee Collider Parameters



- two rings (separate for  $e^+$  and  $e^-$ ); two interaction points (3 & 4 IPs under study), flat beams with very strong focusing ( $\beta^*_y \approx 1\text{mm}$ ); top-up injection (booster), crab waist crossing optics, non-zero (30 mrad) crossing angle;  $P_{SR} = 100\text{ MW}$ , four working points:

➤

Parameter	$\sqrt{s} = M_Z$	$\sqrt{s} = M(WW)$	$\sqrt{s} = M(ZH)$	$\sqrt{s} = M(t\bar{t})$	LEP2
$E_{beam} [\text{GeV}]$	45.6	80	120	175 - 182.5	104.5
Beam current [mA]	1390	147	29	5.4	4
No. Bunches/beam	16 640	2 000	393	48	4
SR energy loss/turn [GeV]	0.036	0.34	1.72	9.21	3.34
SR power [MW]	100	100	100	100	22
SR energy loss/turn [GeV]	0.036	0.34	1.72	9.21	3.4
RF Voltage [GV]	0.1	0.44	2.0	10.9	3.5
$\beta^*_x [\text{m}]$	0.15	0.2	0.3	1	1.5
$\beta^*_y [\text{mm}]$	0.8	1	1	1.6	50
$\epsilon_x [\text{nm}]$	0.27	0.28	0.63	1.46	19.3
$\epsilon_y [\text{pm}]$	1	1.7	1.3	2.9	230
$L (10^{34} \text{ cm}^{-2}\text{s}^{-1})/\text{IP}$	230	28	8.5	1.55	0.012
Statistics (2expts)	$5 \times 10^{12} Z / 6\text{ yrs}$	$3 \times 10^7 WW/2\text{yr}$	$10^6 ZH/5\text{yrs}$	$10^6 t\bar{t} / 5\text{yrs}$	
LEP1 :	$2.1 \times 10^{31} \text{ cm}^{-2}\text{s}^{-1}$	LEP2 :	$3.6 \times 10^{31} \text{ cm}^{-2}\text{s}^{-1}$		



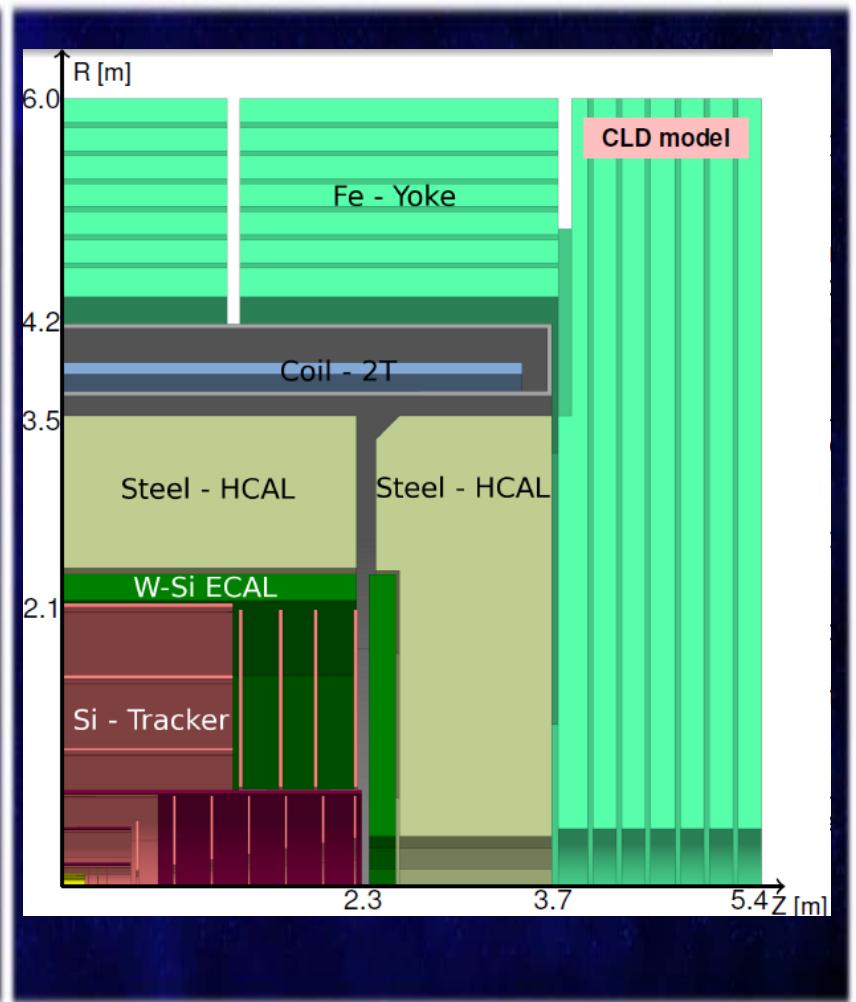
Event statistics:

$E_{cm}$   
errors:

Z peak	$E_{cm}$ : 91 GeV	$5 \cdot 10^{12}$	$e+e^- \rightarrow Z$	$LEP \times 10^5$	100 keV
WW threshold	$E_{cm}$ : 161 GeV	$3 \cdot 10^7$	$e+e^- \rightarrow WW$	$LEP \times 10^3$	300 keV
ZH threshold	$E_{cm}$ : 240 GeV	$10^6$	$e+e^- \rightarrow ZH$	Never done	5 MeV
tt threshold	$E_{cm}$ : 350 GeV	$10^6$	$e+e^- \rightarrow tt\bar{t}$	Never done	10 MeV

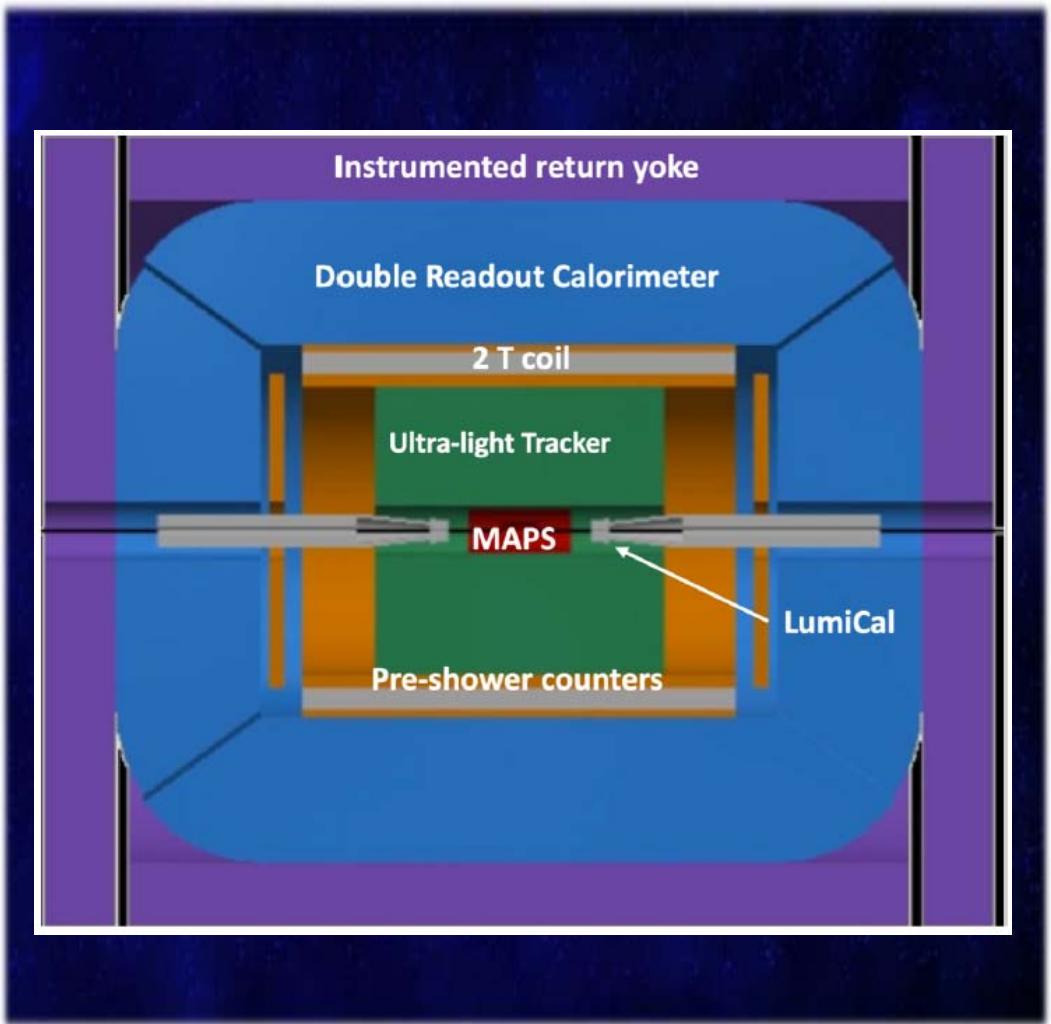
**CLD - detector model for FCC-ee derived from CLICdp model  
and optimized for FCC-ee experimental conditions**

- Full silicon tracking system (  $\geq 12$  hits/track )
- High granularity calorimeters optimized for particle flow reconstruction
- Superconducting coil (2T) located outside the calorimeters
- Steel return yoke containing muon chambers
- Forward region reserved for Machine-Detector Interface and LumiCal
- Tracking fully efficient from 700 MeV
- $\delta p_T \approx 4 \times 10^{-5} \text{ GeV}^{-1}$  ( for muons  $p=100 \text{ GeV}$  )
- $\Delta E/E = (3-5)\%$  ( barrel region )
- Efficiency for electrons and gammas  $> 95\%$



## IDEA – new, innovative, possibly more cost-effective design

- **Silicon vertex detector**  
(5 layers of pixels (MAPS)  $30 \times 30 \mu\text{m}^2$ , point resolution of 5  $\mu\text{m}$ )
- **Short-drift, ultra light wire chamber** (90%/10% He/iC<sub>4</sub>H<sub>10</sub>, momentum resolution 0.25%, impact parameter resolution 4  $\mu\text{m}$ )
- **Dual-readout calorimeter**  
(scintillating fibers sensitive to all charged particles, clear fibers sensitive only to Cherenkov light;  $\frac{\sigma}{E} = \frac{11\%}{\sqrt{E}} + 1\%$  )
- **Thin and light solenoid coil inside calorimetric system**  
(2T, stored energy 170 MJ)



The ZH threshold never studied in  $e^+e^-$

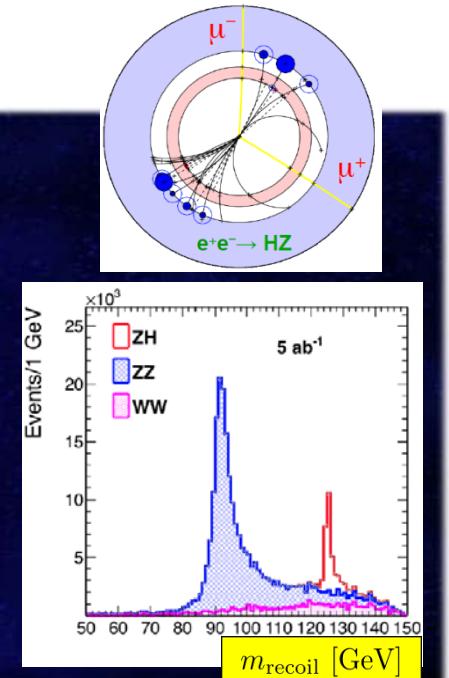
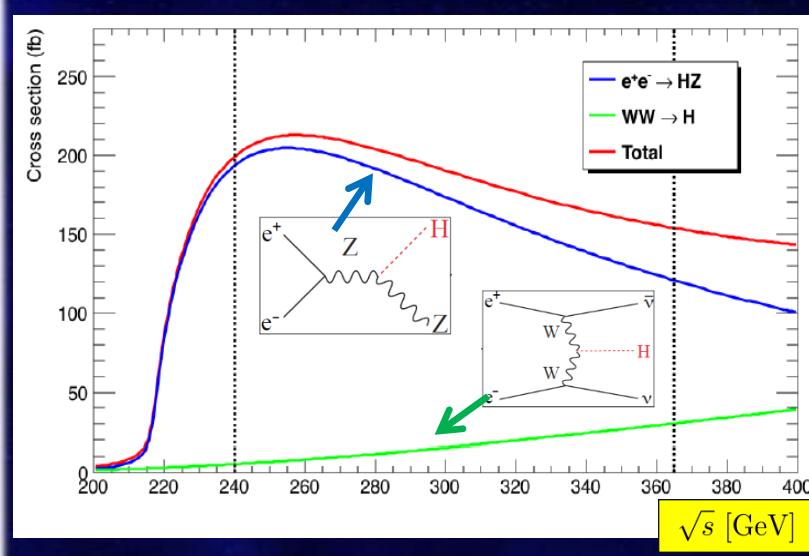
FCC-ee

$N_{ZH} \sim 10^6$

- ✓ The Higgs production measured inclusively from its presence as a recoil to the Z in the process  $e^+e^- \rightarrow ZH$

$$m_{\text{recoil}}^2 = (\sqrt{s} - E_Z)^2 - p_Z^2$$

- ✓  $\Delta m_H = 10$  MeV
- ✓ Absolute measurement of the  $g_{HZZ} \rightarrow \Gamma_H \rightarrow$  other couplings  $g_{ZXZ}$  ( $Z = b, c, \tau, \mu, W, g, \gamma, \dots$ )



- ✓ The couplings of the 3rd and 2nd generation fermions accessible (most with sub-percent precision )
- ✓ This precision yields the New Physics (NP) sensitivity  $\sim 10$  TeV
- ✓ A possible pattern of deviations can discriminate between different BSM models
- ✓ See the talks: *Higgs measurements at the FCC-ee* (abstract 280)  
*Global EFT fits from Higgs at the FCC-ee* (abstract 283)

Luminosity [ $\text{ab}^{-1}$ ]	6.5
No. of years	7
$\delta \Gamma_H / \Gamma_H [\%]$	1.6
$\delta g_{HZZ} / g_{HZZ} [\%]$	0.22
$\delta g_{HWW} / g_{HWW} [\%]$	0.47
$\delta g_{Hb\bar{b}} / g_{Hb\bar{b}} [\%]$	0.68
$\delta g_{H\bar{c}\bar{c}} / g_{H\bar{c}\bar{c}} [\%]$	1.23
$\delta g_{Hgg} / g_{Hgg} [\%]$	1.03
$\delta g_{H\tau\tau} / g_{H\tau\tau} [\%]$	0.80
$\delta g_{H\mu\mu} / g_{H\mu\mu} [\%]$	8.6
$\delta g_{H\gamma\gamma} / g_{H\gamma\gamma} [\%]$	3.8

LEP

$N_Z = 1.7 \times 10^7$



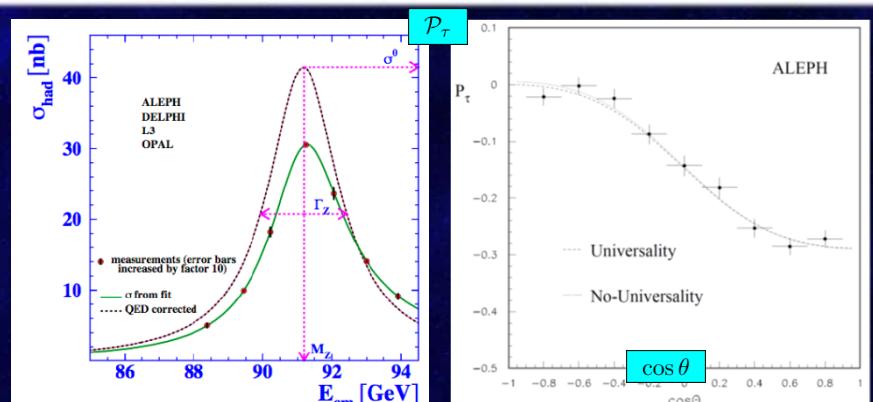
FCC-ee

$N_Z \sim 5 \times 10^{12}$



Extreme precision  
of EW observables

- ✓ Z pole scan:
- ✓ Beam energy calibration is crucial
- ✓ Precision limited by beam energy calibration and theoretical uncertainties



$$\mathcal{P}_\tau(\cos \theta) = \frac{\mathcal{A}_\tau(1 + \cos^2 \theta) + 2\mathcal{A}_e \cos \theta}{(1 + \cos^2 \theta) + \mathcal{A}_e \mathcal{A}_\tau \cos \theta}$$

Observable	present value ±error	FCC – ee Stat.	FCC – ee Syst.	Improvement factor
$m_Z$ [keV/c <sup>2</sup> ]	$91186700 \pm 2200$	5	100	22
$\Gamma_Z$ [keV]	$2495200 \pm 2300$	8	100	23
$R_l^Z$ [ $\times 10^3$ ]	$20767 \pm 25$	0.06	0.2 – 1	125 – 25
$\alpha_S(m_Z)$ [ $\times 10^4$ ]	$1196 \pm 30$	0.1	0.4 – 1.6	75 – 19
$R_b$ [ $\times 10^6$ ]	$216290 \pm 660$	0.3	< 60	11
$N_\nu$ [ $\times 10^3$ ]	$2991 \pm 7$	0.005	1	7
$\sin^2 \theta_W^{\text{eff}}$ [ $\times 10^6$ ]	$231480 \pm 160$	3	2 – 5	44 – 28
$1/\alpha_{\text{QED}}(m_Z)$ [ $\times 10^3$ ]	$128952 \pm 14$	4	small	3.5
$A_{FB,0}^b$ [ $\times 10^4$ ]	$992 \pm 16$	0.02	1 – 3	16 – 5
$A_{FB}^{\text{pol},\tau}$ [ $\times 10^4$ ]	$1498 \pm 49$	0.15	< 2	25

$$R_l = \frac{\Gamma_{\text{had}}}{\Gamma_{l\bar{l}}} \quad N_\nu = \left( \frac{\Gamma_l}{\Gamma_\nu} \right)_{\text{SM}} \cdot \left( \sqrt{\frac{12\pi R_l}{M_Z^2 \sigma_{\text{peak},0}^{\text{had}}}} - R_l - 3 \right)$$

$$\mathcal{A}_f = \frac{2g_V^f g_A^f}{(g_V^f)^2 + (g_A^f)^2} \quad \sin^2 \theta_W^{\text{eff}} = \frac{1}{4} \left( 1 - \frac{g_V^f}{g_A^f} \right)$$

$$A_{FB}^f = \frac{\sigma_F - \sigma_B}{\sigma_F + \sigma_B} = \frac{3}{4} \mathcal{A}_e \mathcal{A}_f$$

- ✓ The direct measurement of  $\alpha_{\text{QED}}(m_Z^2)$  from the muon FB asymmetry just below and just above the Z pole (as part of Z resonance scan – no need of extrapolation from  $\alpha_{\text{QED}}(0)$  )

P.Janot JHEP 02 (2016) 053

- ✓ See the talk „Electroweak physics at FCC-ee” (abstract 281)

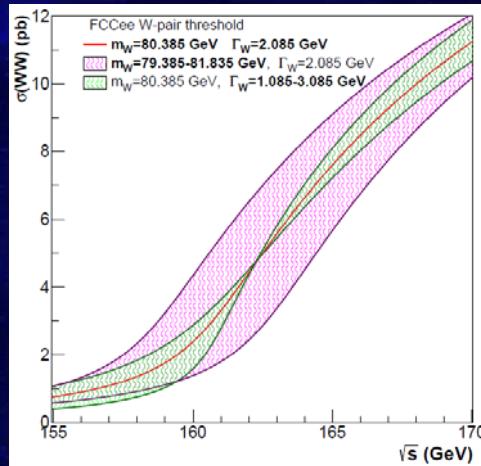
The WW threshold scan

LEP

$$N_{WW} = 1.1 \times 10^4$$

FCC-ee

$$N_{WW} \sim 3 \times 10^7$$



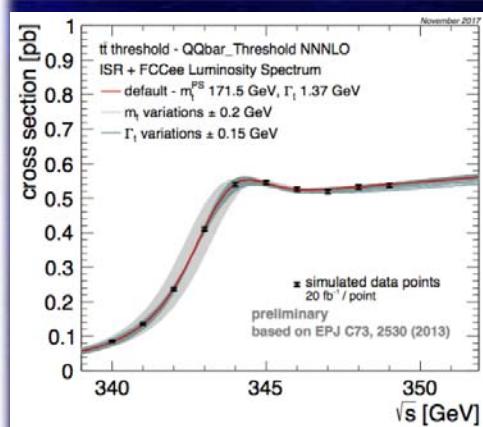
Observable	present value ±error	FCC – ee Stat.	FCC – ee Syst.	Improvement factor
$m_W$ [MeV/c <sup>2</sup> ]	$80379 \pm 12$	0.6	0.3	18
$\Gamma_W$ [MeV]	$2085 \pm 42$	1.5	0.3	27

See the talk „Electroweak physics at FCC-ee” (abstract 281)

The t-tbar threshold never studied in e<sup>+</sup>e<sup>-</sup>

FCC-ee

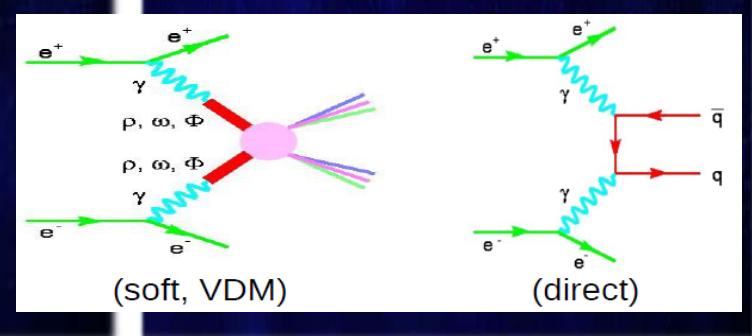
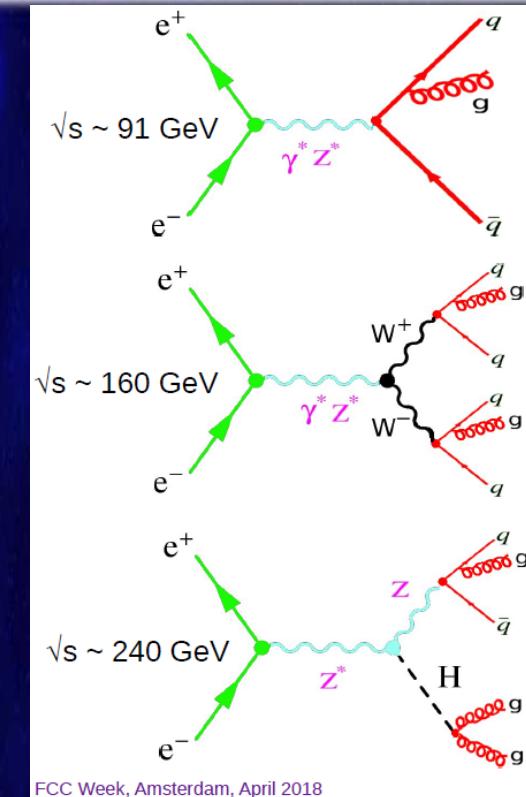
$$N_{t\bar{t}} \sim 10^6$$



Observable	present value ±error	FCC – ee Stat.	FCC – ee Syst.	Improvement factor
$m_t$ [MeV/c <sup>2</sup> ]	$172900 \pm 400$	20	small	20
$\Gamma_t$ [MeV]	$1420 \pm 190$	40	small	5

See the talk „Top quark physics at the FCC-ee” (abstract 284)

- ✓ Extremely clean environment
- ✓ Fully controlled QED initial-state with known kinematics
- ✓ Controlled QCD radiation - only from the final state
- ✓ Well defined quark, gluon and heavy-quark jets
- ✓ Relatively small non-perturbative QCD uncertainties (lack of QCD underlying event, no PDFs....)
- ✓ Fragmentation and hadronization - direct and clean
- ✓ Large statistical samples
- ✓ Studies of  $\gamma\gamma$  SM and BSM collisions  
(in Equivalent Photon Approximation (EPA))
- ✓ ...





# Reminder: QCD Studies at LEP



- ✓ The successful running of LEP yielded a crucial impact on the understanding of QCD (~240 publications)
- ✓ **The QCD highlights from LEP:**
  - Studies of hadronic event shapes
  - Measurements of  $\alpha_s$
  - Determinations of QCD colour factors and tests of the non-Abelian gauge structure of QCD
  - Studies of differences between quark and gluon jets
  - Tests of Monte Carlo shower and hadronization models
  - Studies of QCD with heavy quarks
  - Advances in two-photon scattering processes
  - ...

No. of hadronic events	LEP	FCC-ee
$\sqrt{s} \sim 91 \text{ GeV}$	$10^7$	$10^{12}$
$\sqrt{s} \sim 160 \text{ GeV}$	$10^4$	$10^7$
$\sqrt{s} \sim 240 \text{ GeV}$	-	$10^5$



# The QCD Objectives of FCC-ee



- ✓ **High precision  $\alpha_s$  determination** (with the accuracy at the ‰ level) from
  - hadronic  $\tau$  decays
  - Jet rates, event shapes
  - hadronic Z decays
  - hadronic W decays
- ✓ **High precision studies of perturbative parton radiation including:**
  - jet rates and event shapes
  - jet substructure,
  - quark/gluon/heavy-quark discrimination
  - g,q,b,c parton-to-hadron fragmentation functions
- ✓ **High precision non-perturbative QCD studies including:**
  - colour reconnection
  - final-state multiparticle correlations
- ✓ **High precision hadronization studies**
  - very rare hadron production and decays

- ✓ The  $\alpha_s$  determines the strength of the strong interaction at a given scale
- ✓ The unique free parameter of QCD in the limit  $m_q \rightarrow 0$

- ✓ The  $\alpha_s$  is the least precisely measured of all four couplings of fundamental interactions:

$$\Delta\alpha \sim 10^{-10}$$

$$\Delta G_F \sim 10^{-7}$$

$$\Delta G \sim 10^{-5}$$

$$\boxed{\Delta\alpha_S \sim 10^{-2}}$$

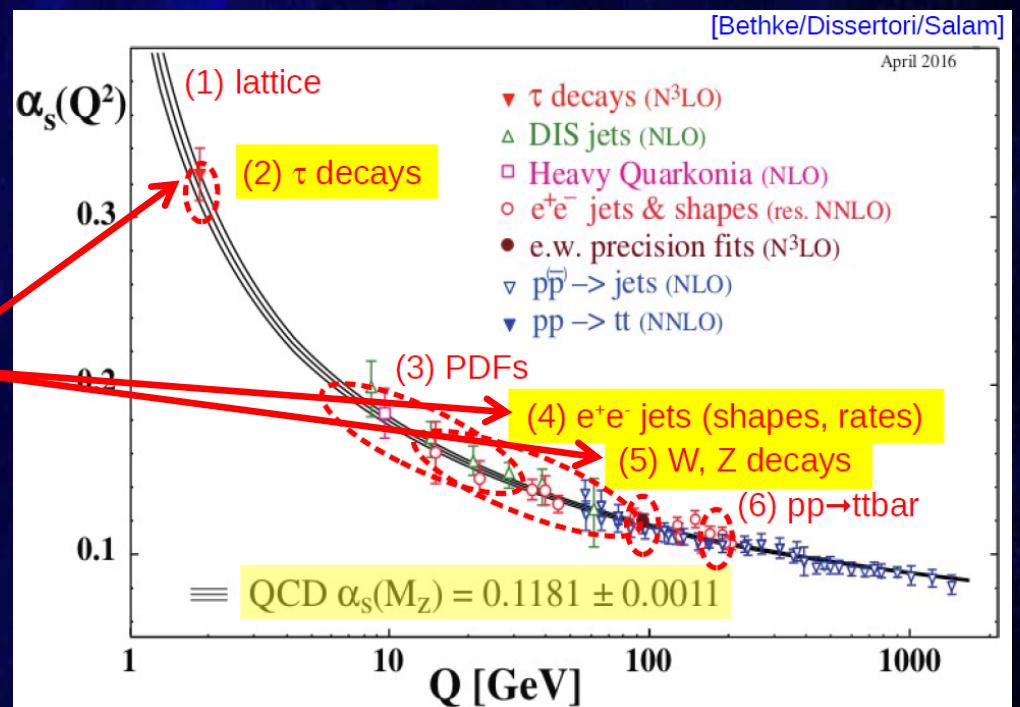
- ✓ huge statistics of hadronic  $\tau$ ,  $W$  and  $Z$  decays
- ✓  $N^3LO$  perturbative QCD calculations



$$\boxed{\Delta\alpha_S \sim 10^{-3}}$$

- ✓ The  $\alpha_s$  is determined by comparing now 6 groups of experimental observables to pQCD NNLO and  $N^3LO$  predictions

- ✓ The global average is provided at the  $Z$  pole





# The QCD Coupling Constant $\alpha_s$ at FCC-ee



- ✓  **$\tau$  decays:** The relevant quantity:

$$R_\tau = \frac{\Gamma(\tau^- \rightarrow \nu_\tau + \text{hadrons})}{\Gamma(\tau^- \rightarrow \nu_\tau e^- \bar{\nu}_e)}$$

computable at N<sup>3</sup>LO:

$$R_\tau = S_{EW} N_C \left( 1 + \sum_{n=1}^4 c_n \left( \frac{\alpha_S}{\pi} \right)^n + \mathcal{O}(\alpha_S^5) + \delta_{np} \right)$$

- ✓ The current experimental value:

$$R_{\tau, \text{exp}} = 3.4697 \pm 0.0080 \quad (\pm 0.23\%)$$

- ✓ The current determination of the  $\alpha_s$ :

$$\alpha_S(m_Z) = 0.1192 \pm 0.0018 \quad (\pm 1.5\%)$$

FCC-ee

$$N(Z \rightarrow \tau^+ \tau^-) \sim 10^{11}$$

& theoretical progress

$$\delta \alpha_S(m_Z)/\alpha_S(m_Z) < 1\%$$

- ✓ **The event shapes**, like e.g. thrust (T), C-parameter...

$$T = \max_{\vec{n}} \left( \sum_{i=1}^n |\vec{p}_i \cdot \vec{n}| \right) / \left( \sum_{i=1}^n |\vec{p}_i| \right)$$

$$C = \frac{3}{2} \frac{\sum_{i,j=1}^n |\vec{p}_i| |\vec{p}_j| \sin^2 \theta_{ij}}{(\sum_{i=1}^n |\vec{p}_i|)^2}$$

**and N jet cross sections**  
are computed at  
N<sup>2,3</sup>LO+N<sup>2</sup>LL accuracy

- ✓ The current combination of LEP results yields

$$\delta \alpha_S(m_Z)/\alpha_S(m_Z) < 2.9\%$$

FCC-ee

$$N(Z \rightarrow \text{hadrons}) \sim 10^{12}$$



$$\delta \alpha_S(m_Z)/\alpha_S(m_Z) < 1\%$$

& theoretical progress

## Hadronic Z decays:

- ✓ at LEP, the  $\alpha_s$  was extracted from the fits to the three Z-peak observables

$$\sigma_l^0 = \frac{12\pi}{m_Z} \frac{\Gamma_l^2}{\Gamma_Z^2} \quad \sigma_{\text{had}}^0 = \frac{12\pi}{m_Z} \frac{\Gamma_e \Gamma_{\text{had}}}{\Gamma_Z^2}$$

$$R_l^0 = \frac{\Gamma(Z \rightarrow \text{had})}{\Gamma(Z \rightarrow l)} = \frac{\Gamma_{\text{had}}}{\Gamma_l}$$

- ✓ computable at  $N^3\text{LO}$ :

$$R_l^0 = R_Z^{\text{EW}} N_C \left( 1 + \sum_{n=1}^4 c_n \left( \frac{\alpha_S}{\pi} \right)^n + \mathcal{O}(\alpha_S^5) + \delta_m + \delta_{np} \right)$$

- ✓ The current  $\alpha_s$  value:

$$\alpha_s(m_Z) = 0.1196 \pm 0.0030 \quad (\pm 2.5\%)$$

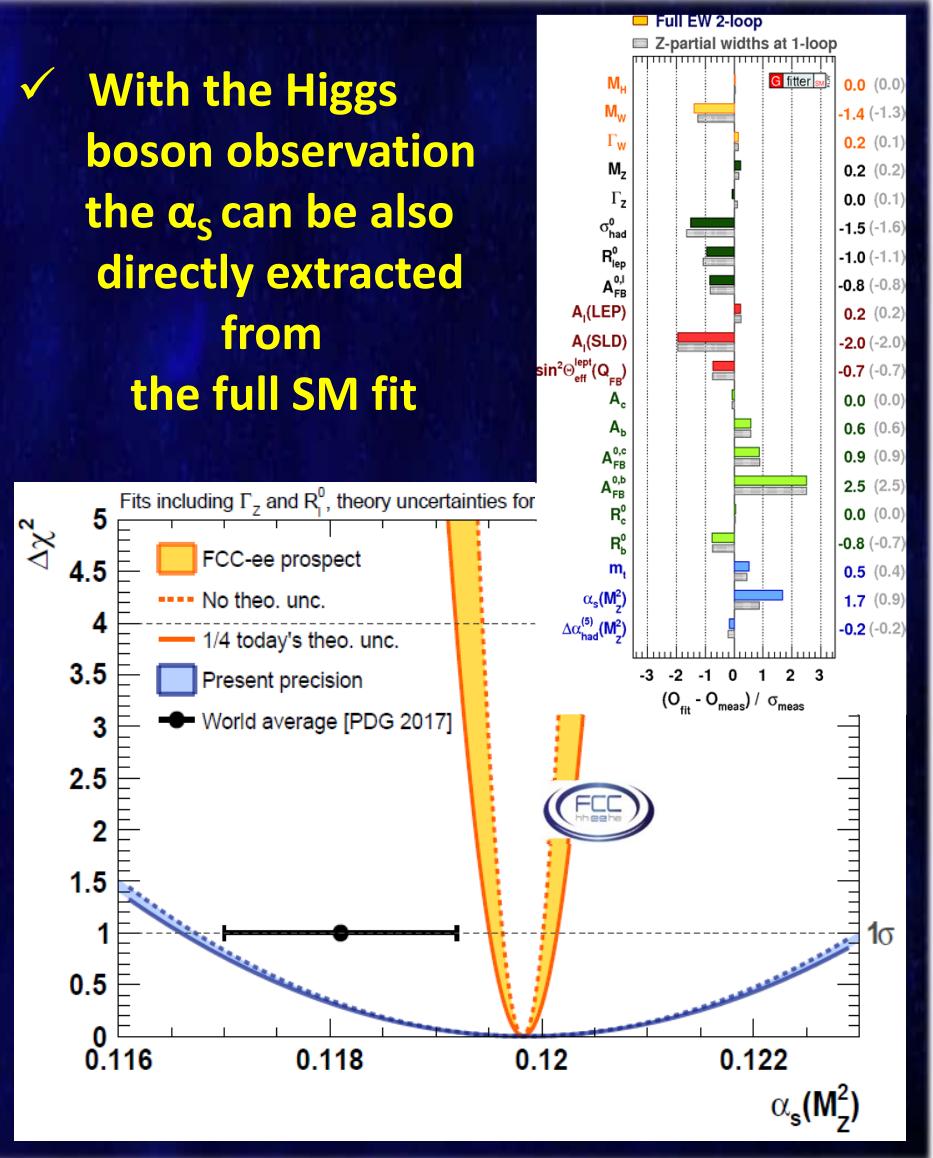
FCC-ee

$$N_Z \sim 5 \times 10^{12}$$

and theoretical progress

$$\rightarrow \delta \alpha_s(m_Z)/\alpha_s(m_Z) < 0.2\%$$

- ✓ **With the Higgs boson observation the  $\alpha_s$  can be also directly extracted from the full SM fit**



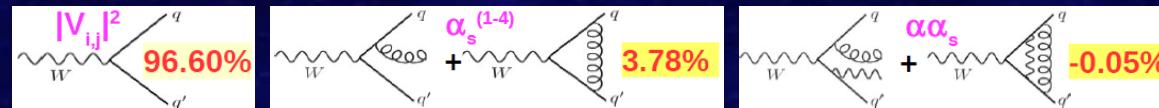
## Hadronic W decays:

- ✓ The observable: ratio of hadronic to leptonic W decay widths

$$\Gamma_{W,\text{had}} = \frac{\sqrt{2}}{4\pi} G_F m_W^3 \sum_{\text{quarks } i,j} |V_{i,j}|^2 \left[ 1 + \sum_{k=1}^4 \left( \frac{\alpha_S}{\pi} \right)^k + \delta_{\text{EW}}(\alpha_{\text{QED}}) + \delta_{\text{mixed}}(\alpha_{\text{QED}} \alpha_S) \right]$$

[EWK: -0.35%]

- ✓ computable at  $N^{2,3}\text{LO}$ :



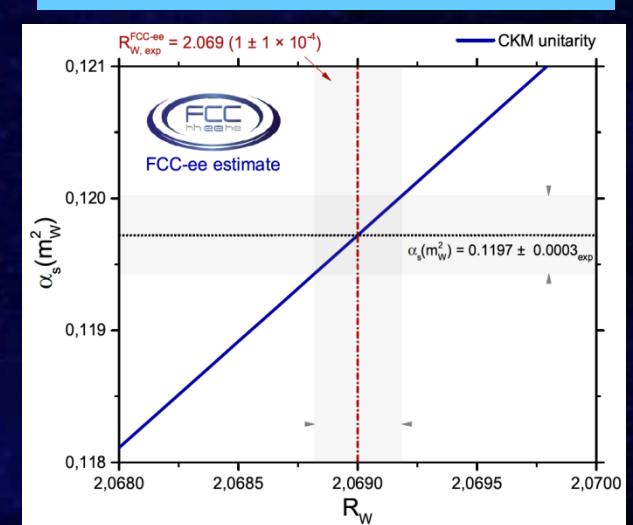
- ✓ The LEP  $\alpha_S$  value:  $\alpha_S(m_Z) = 0.117 \pm 0.040$  ( $\pm 35\%$ )

FCC-ee  $N_{WW} \sim 3 \times 10^7$   $\delta\alpha_S(m_Z)/\alpha_S(m_Z) < 0.3\%$

and theoretical progress

$$R_W = \frac{\Gamma_{\text{had}}^W}{\Gamma_l^W}$$

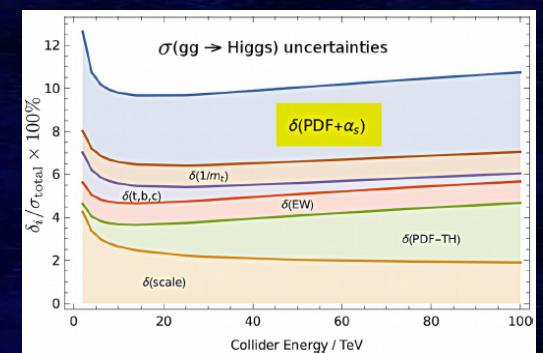
D.d'Enterria, M.Srebre, arXiv:1603.06501



**The precision on  $\alpha_s$  influences all QCD cross-sections and decays ...**

Quantity	FCC-ee	future param.unc.	Main source
$\Gamma_Z$ [MeV]	0.1	0.1	$\delta\alpha_s$
$R_b$ [ $10^{-5}$ ]	6	< 1	$\delta\alpha_s$
$R_\ell$ [ $10^{-3}$ ]	1	1.3	$\delta\alpha_s$

David d'Enterria FCC Phys. Workshop, CERN, Jan 2018





# High Precision Studies of Perturbative Parton Radiation – Jet Rates and Event Shapes



- ✓ **Jet rates** are expected to be measured with the accuracy  $10^{-6}$  (at the Z pole), including:

Rate of	up to $k_T$ [GeV]	$ ln(y) $
4-jet events	~30	~2
5-jet-events	~20	~3
6-jet events	~12	~4
7-jet events	~7.5	~5

(jet resolution parameter:  $y = \frac{k_T^2}{s}$  )



Comparison with theoretical calculations  
with accuracy beyond the NNLO+NNLL  
( $\rightarrow \alpha_s$  extraction)

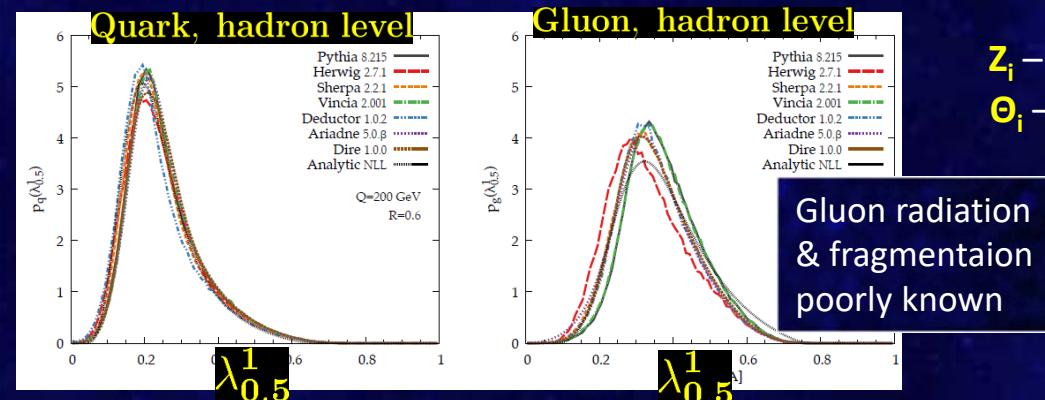
- ✓ Event shapes are affected by logarithmic enhancements (resummed up to  $N^3LL$ : pQCD, SCET,...) and hadronization corrections (estimated from MC generators)
- ✓ **The FCC-ee operating at different CM energies will provide much tighter control on resummation and hadronization effects in event shape distributions**



$\sqrt{s} = 91.2$  GeV → non-perturbative uncertainties reduced from 9% to 2%

- ✓ **Goal:** parton flavour discrimination (PFD): quark – gluon; (u,d,s) – c – b
- ✓ Such separation crucial for precision SM measurements and BSM searches
- ✓ The PFD is based on the comparison of jet substructure properties to MC predictions
- ✓ Quark-gluon PFD at LEP: studies of  $Z \rightarrow b\bar{b}g$  (statistically limited)
  
- ✓ -  **$10^5$  more Zs**  
- **a unique sample of  $10^4$   $H \rightarrow gg$  events - FCC-ee as a „pure gluon” factory**

- ✓ The current level of discrepancies between MC generators (hadron level distributions):



**The generalized angularities:**

$$\lambda_{\beta}^{\kappa} = \sum_{i \in \text{jet}} Z_i^{\kappa} \theta_i^{\beta}$$

$Z_i$  – the momentum fraction of particle i

$\theta_i$  – the angular fraction of part. i w.r.t. the jet radius

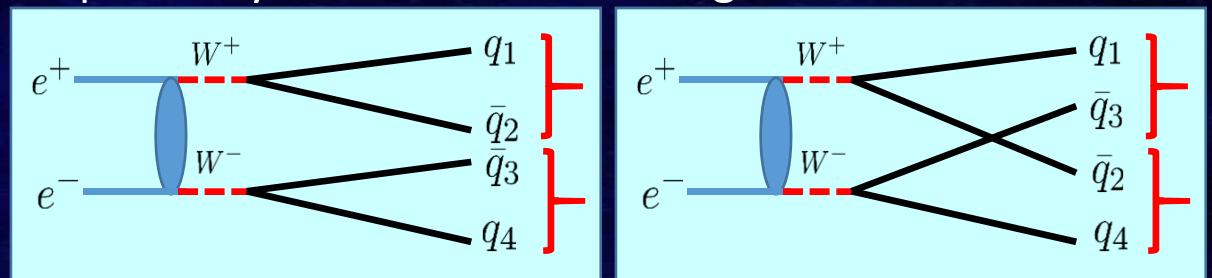
**Significant variations between generators for gluon distributions  
new insight from the FCC-ee**

→ : large samples of top, W, Z, H decays to b and c quarks; important progress in heavy-quark fragmentation and in gluon fragmentation  $g \rightarrow b\bar{b}$  ( $c\bar{c}$ )

- ✓ The uncertainties due to non-perturbative QCD effects (colour reconnection, hadronization, final state interactions...) impact many high-precision SM studies
- ✓  $e^+e^-$  collisions offer favourable conditions to control them

- ✓ **Colour Reconnection (CR):** strong interaction (colour flow) between colour singlet parton systems of different origin

- ✓ LEP2: exclusion (99.5% CL) of the no-CR null hypothesis but statistics insufficient for more quantitative results



- ✓ **FCC-ee:**  $\Delta m_W \sim 1$  MeV (threshold scan) & the  $3 \times 10^3$  gain in the number of WW pairs
- ✓ The shift in the reconstructed  $m_W$  expected from different PYTHIA 8 CR models:

small (S):  
maximal (L):  
medium size (M):

$E_{\text{cm}}$ (GeV)	$\langle \delta \bar{m}_W \rangle$ (MeV)						
	I	II	II'	GM-I	GM-II	GM-III	CS
170	+18	-14	-6	-41	+49	+2	+7
240	+95	+29	+25	-74	+400	+104	+9
350	+72	+18	+16	-50	+369	+60	+4



discrimination  
between CR  
models

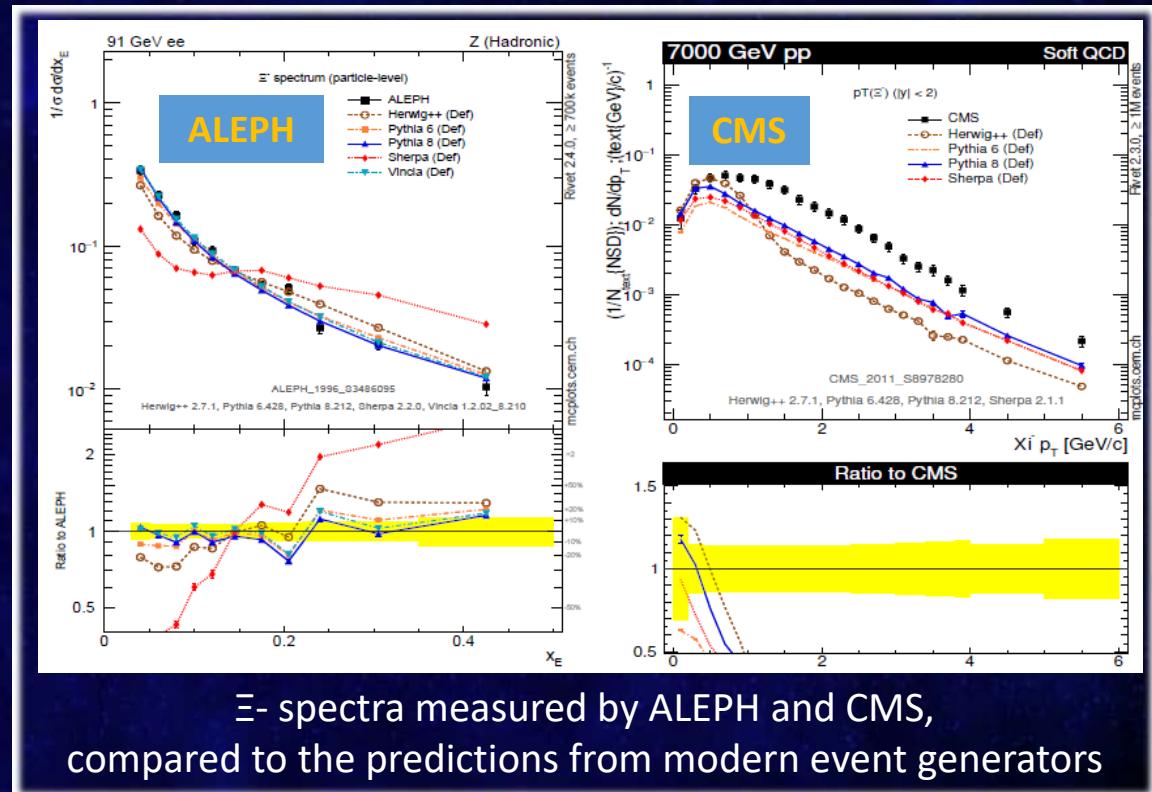
✓ **Parton Hadronization (PH) – phenomenological models – MC generators**

✓ **The understanding of many aspects of PH like**

- baryon production
- strangeness production
- final state correlations
- colour string dynamics
- ....

✓ **can profit significantly from the FCC-ee (hadronic) data samples:**

- large statistics
- excellent tracking and calorimetry
- efficient hadron identification
- ...



- ✓ The FCC-ee project aims at collection of huge data samples at the four relevant working points: Z-pole, ZH, WW and ttbar thresholds
- ✓ The uncertainties of the most important electroweak observables are expected to be improved by a factor of at least 10
- ✓ The QCD program of the FCC-ee encompasses
  - High precision  $\alpha_s$  determination
  - High precision studies of perturbative parton radiation
  - High precision non-perturbative QCD studies
  - High precision hadronization studies



# BACKUP



# EU H2020 Design Study EuroCirCol

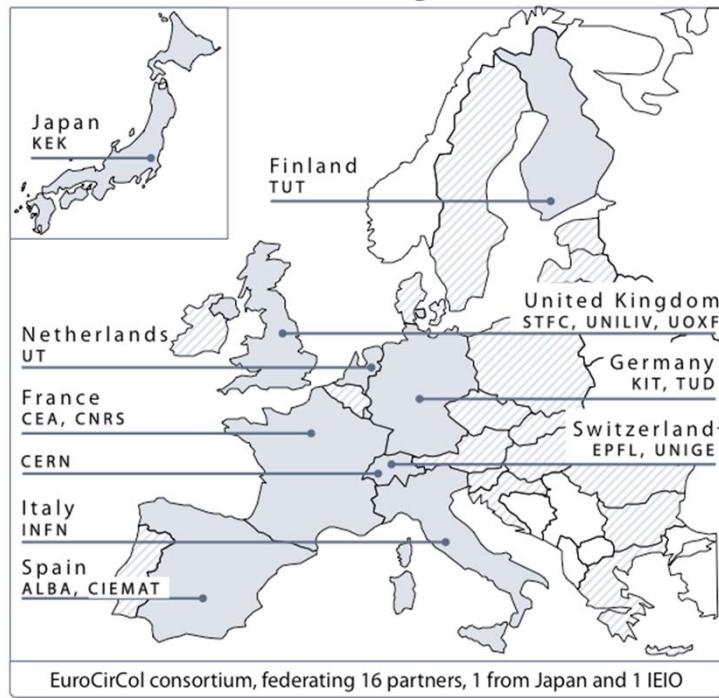


## European Union Horizon 2020 program:

UNIVERSITY OF TWENTE.



TAMPERE  
UNIVERSITY OF  
TECHNOLOGY



Ciemat  
Centro de Investigaciones  
Energéticas, Medioambientales  
y Tecnológicas



MANCHESTER  
1824

- 3 MEURO co-funding
- Started June 2015, ends in Dec 2019
- 15 European beneficiaries & KEK & associated FNAL, BNL, LBL, NHFML

## Covers FCC-hh key work packages:

- Optics design (arc & IR)
- Cryogenic beam vacuum system design including beam tests at ANKA
- 16 T dipole design, construction folder for demonstrator magnets



# EU H2020 Marie Curie ITN EASITrain



European Advanced Superconductivity Innovation and Training Network  
Funding 15 Early Stage Researchers over 3 years & training in key areas

- SC wires at low temperatures for magnets (Nb<sub>3</sub>Sn, MgB<sub>2</sub>, HTS)
  - Superconducting thin films for RF and beam screen (Nb<sub>3</sub>Sn, Ti)
  - Electrohydraulic forming for RF structures
  - Turbocompressor for Nelium refrigeration
  - Magnet cooling architectures
- started 1 October 2017

13  
Beneficiaries



12 Partners



# FCC-ee basic design choices

**double ring  $e^+e^-$  collider  $\sim 100$  km**

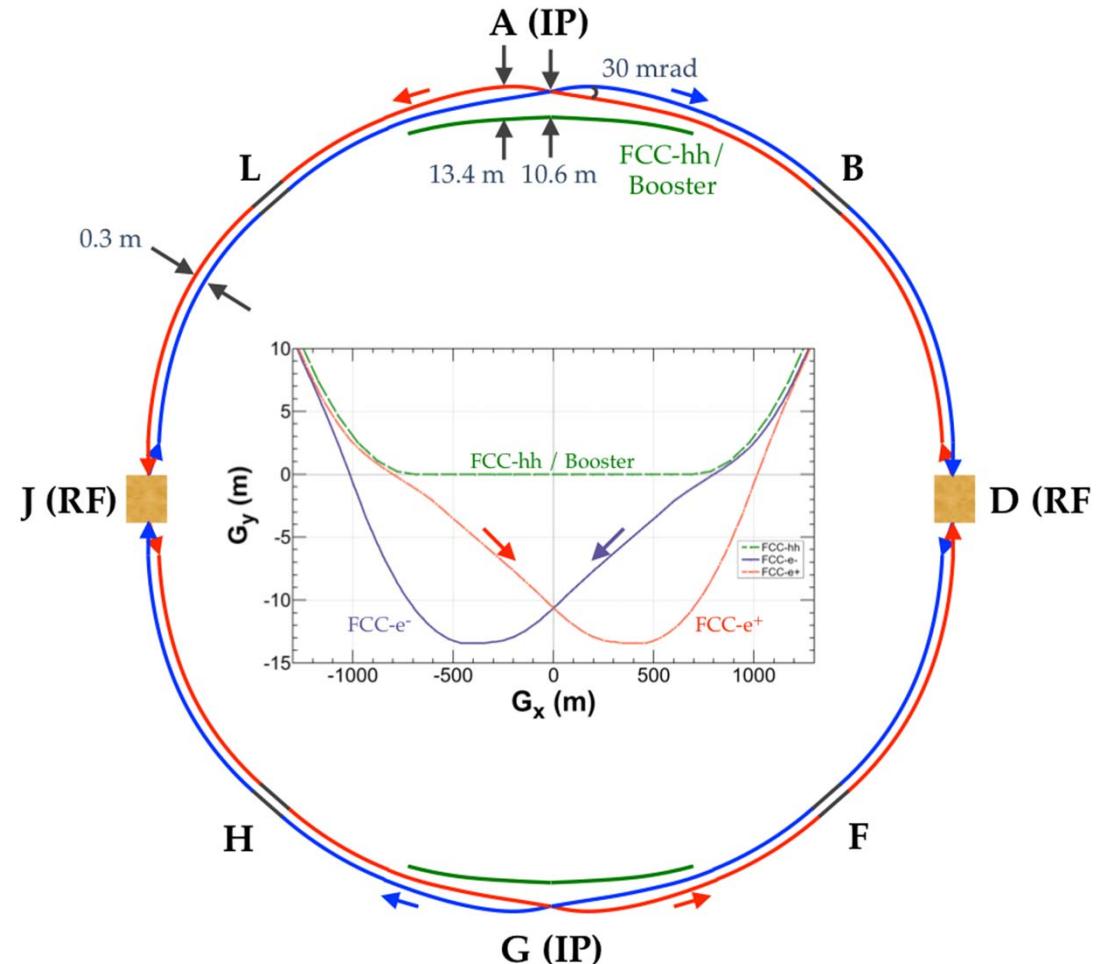
**follows footprint of FCC-hh, except around IPs**

**asymmetric IR layout & optics** to limit synchrotron radiation towards the detector

**presently 2 IPs** (alternative layouts with 3 or 4 IPs under study), **large horizontal crossing angle 30 mrad, crab-waist optics**

**synchrotron radiation power 50 MW/beam** at all beam energies; tapering of arc magnet strengths to match local energy

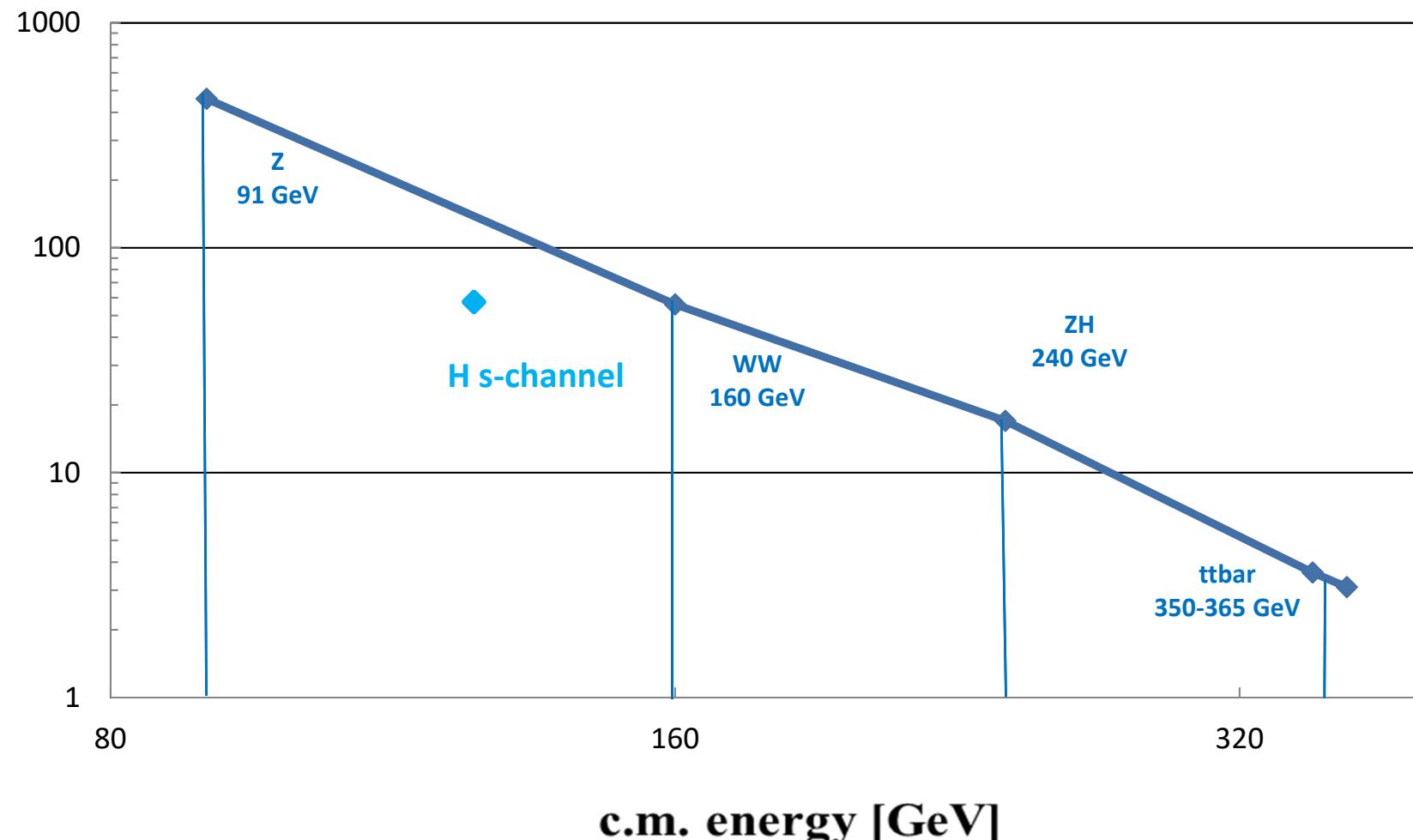
**top-up injection scheme;** requires **booster synchrotron in collider tunnel**



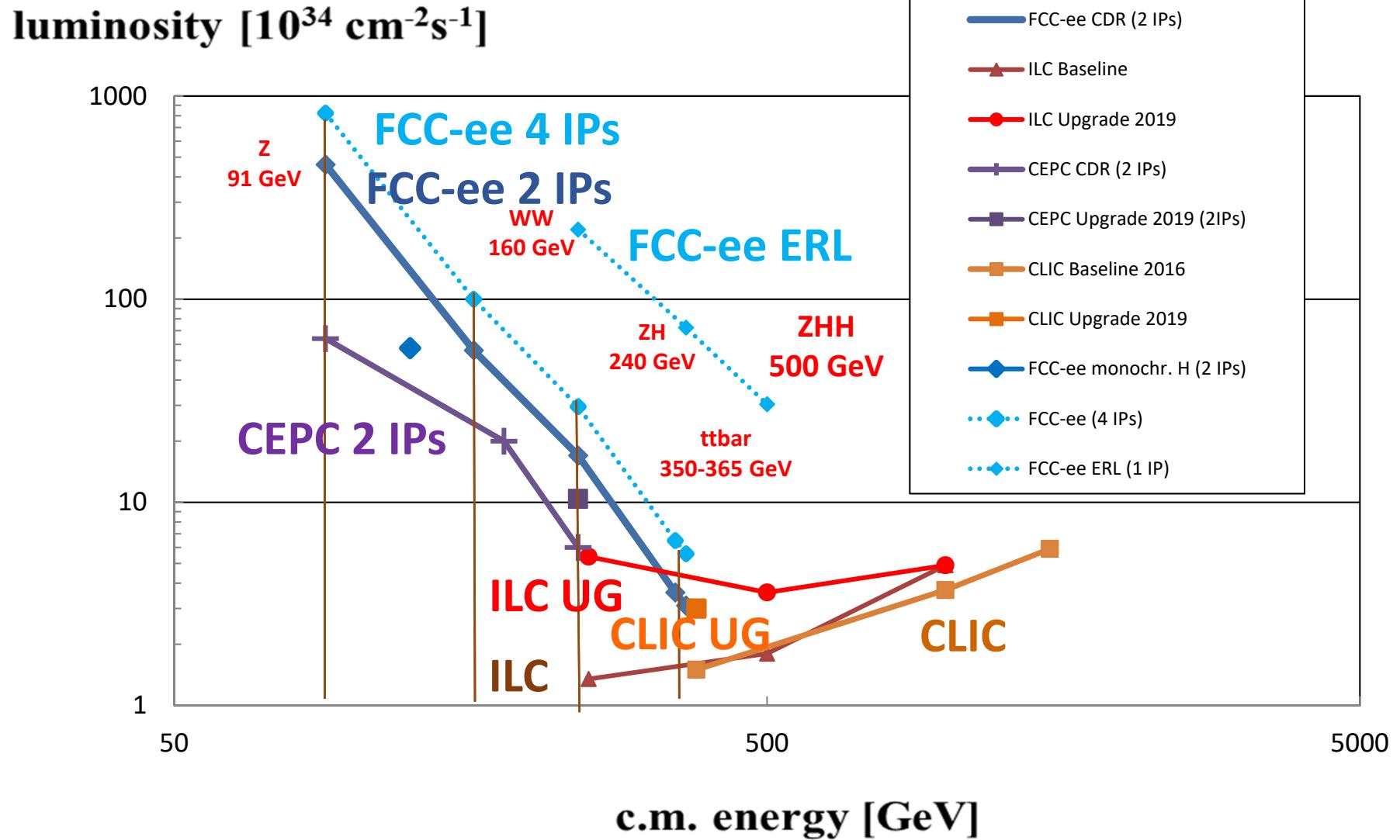


# FCC-ee luminosity versus energy

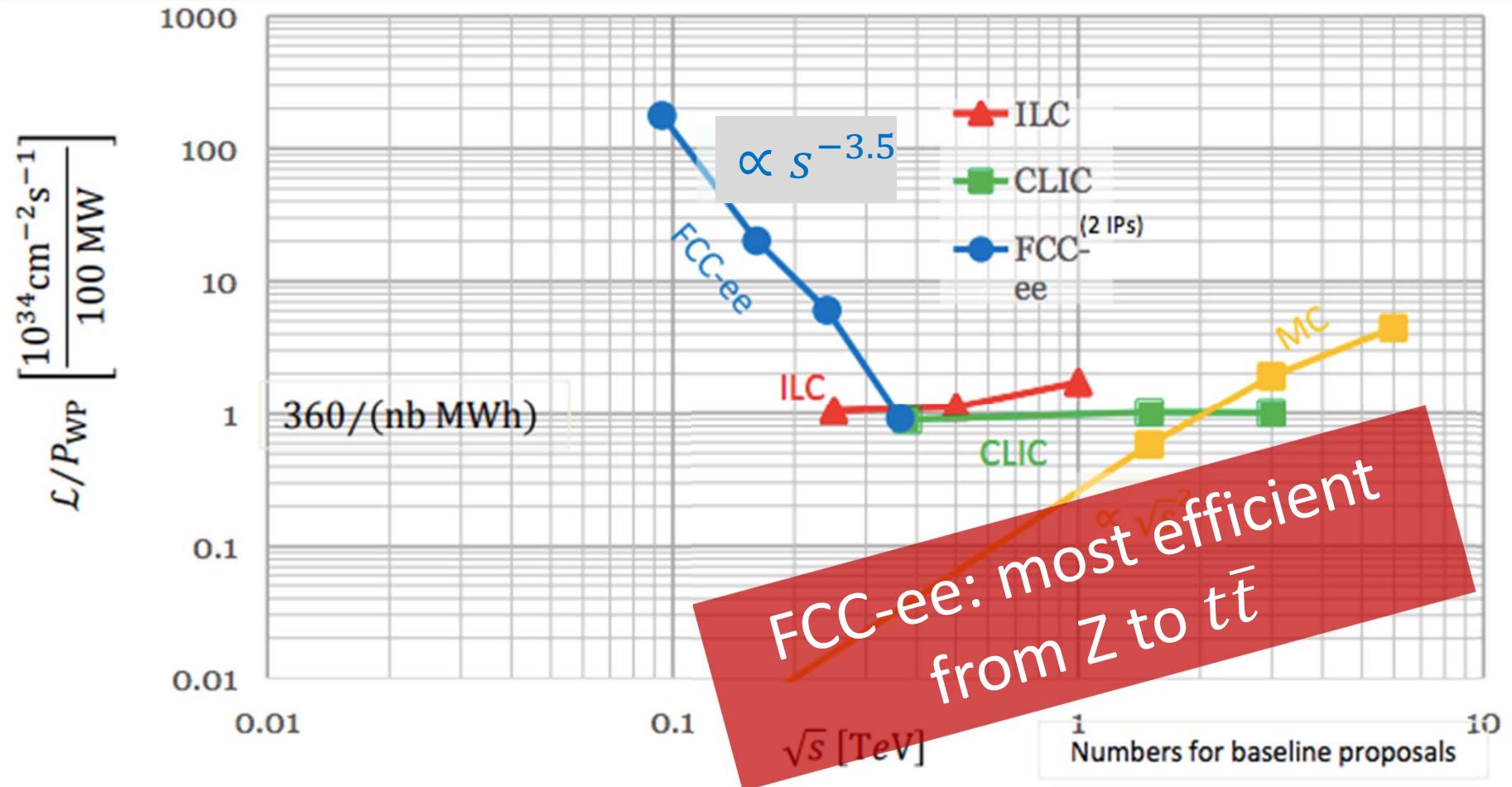
**luminosity [ $10^{34} \text{ cm}^{-2}\text{s}^{-1}$ ] (2 IPs)**



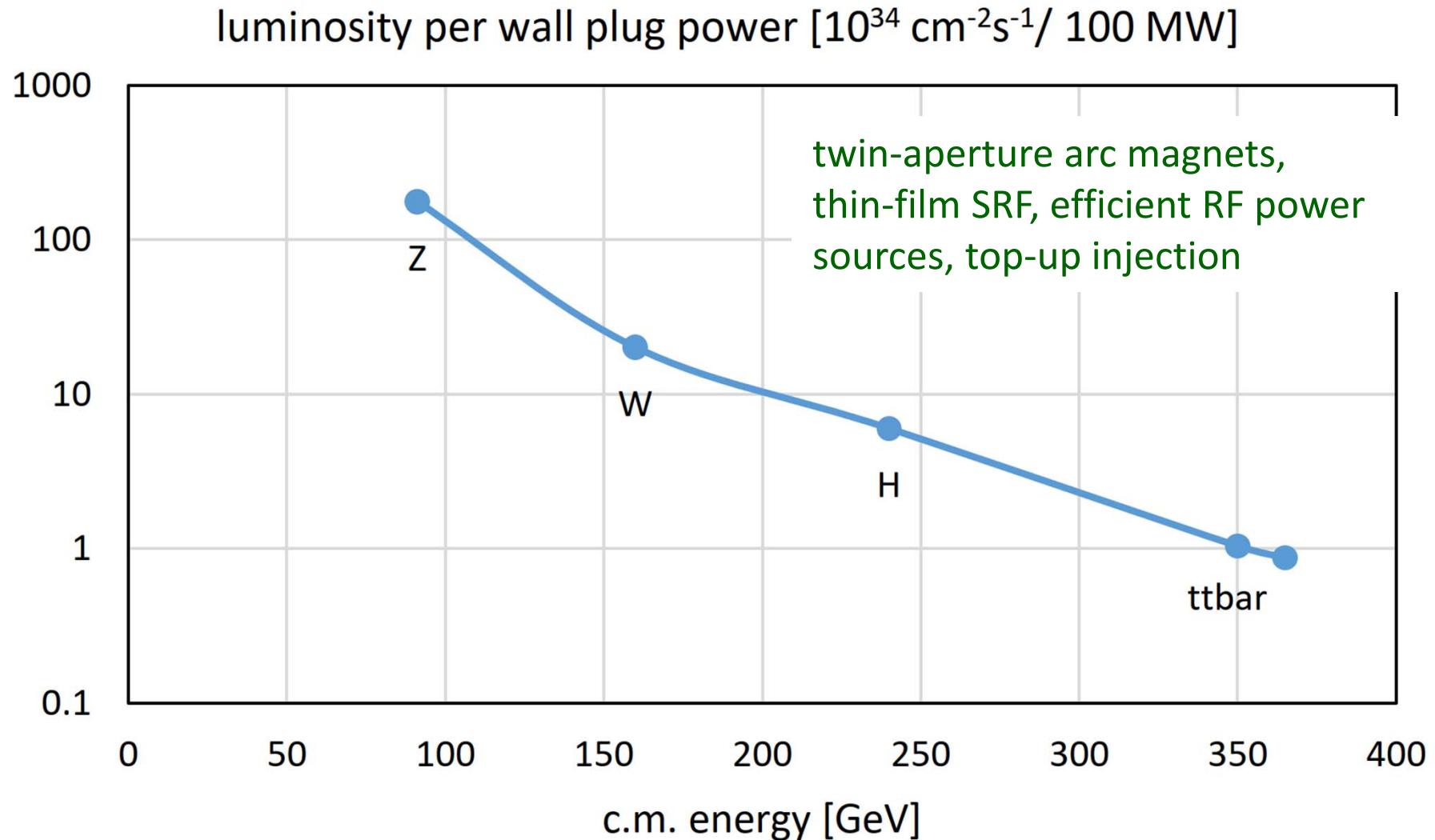
# FCC-ee luminosity in perspective



# figure of merit for lepton colliders



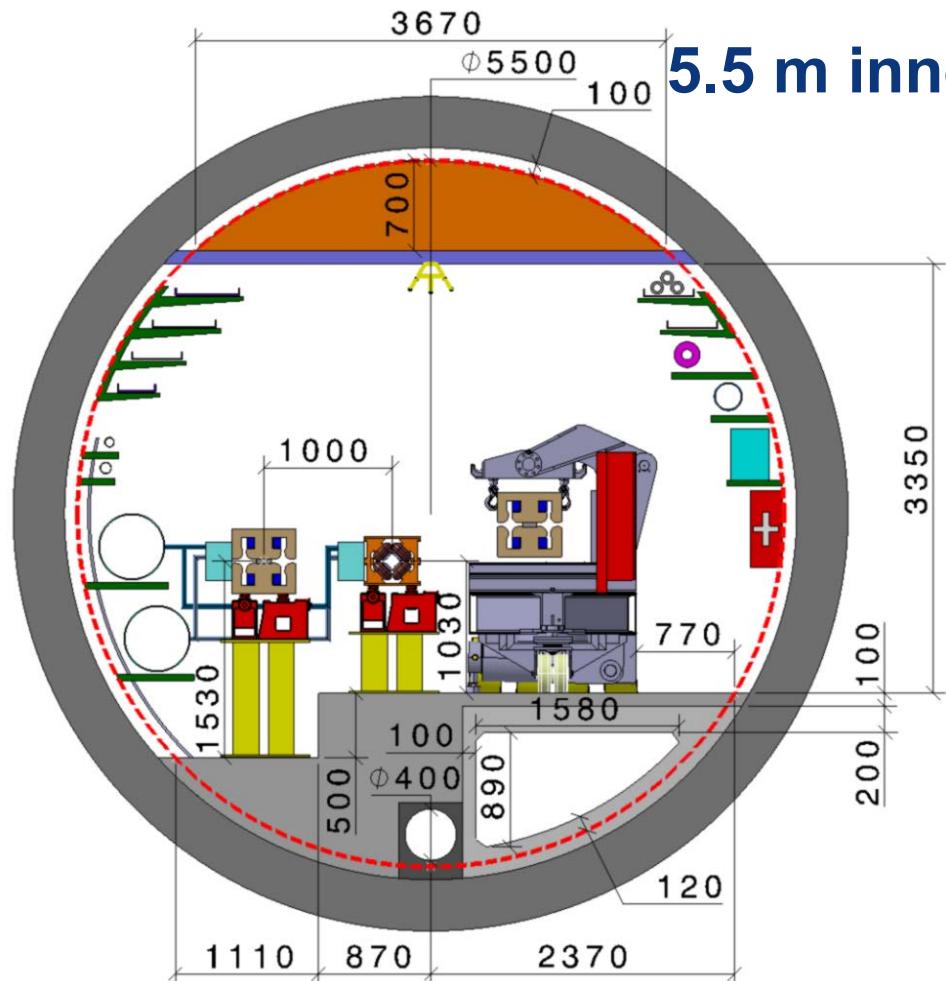
# FCC-ee: a sustainable accelerator



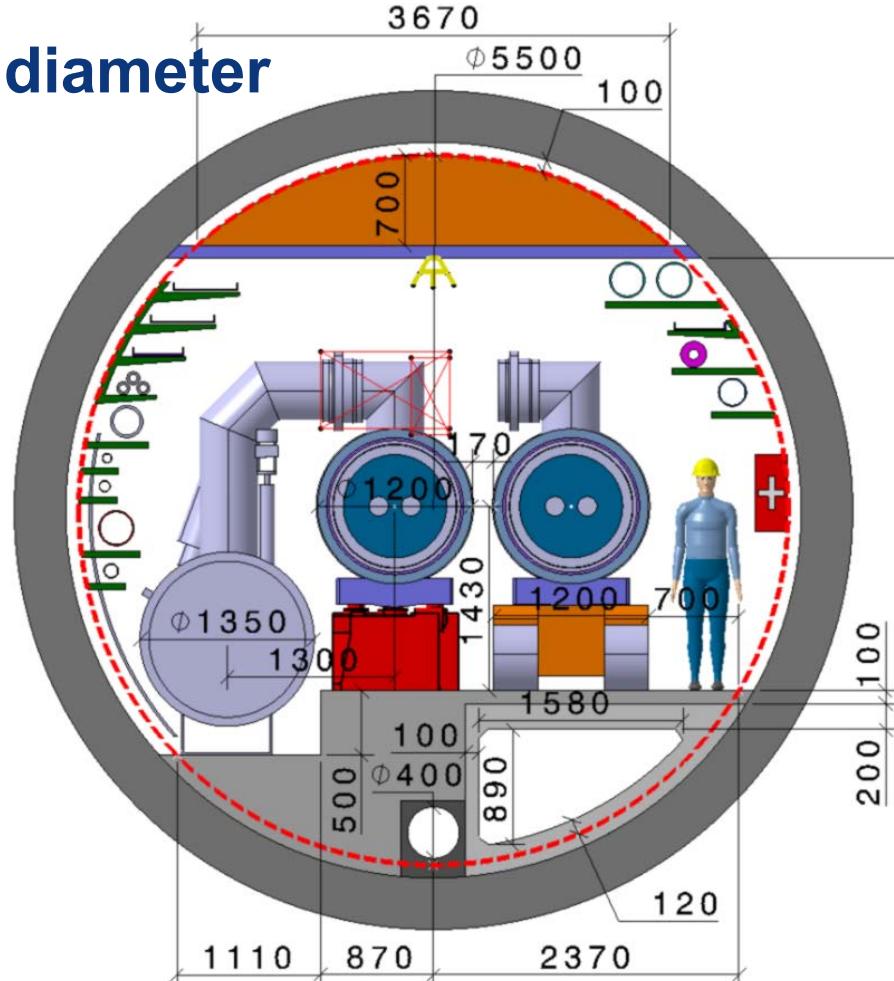
**electricity cost ~200 euro per Higgs boson**

# Tunnel integration in arcs

FCC-ee

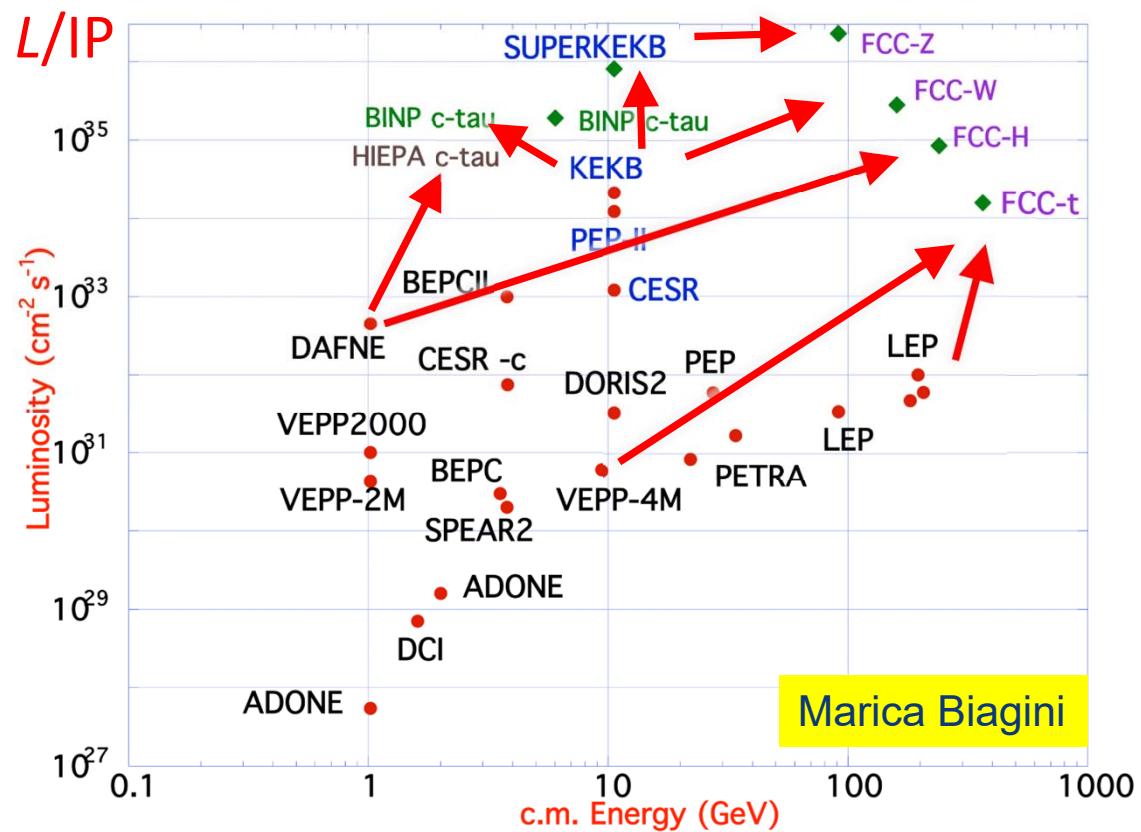


FCC-hh



# FCC-ee – EW factory: performance

FCC-ee reaches highest luminosities & energies  
by combining ingredients and well-proven concepts of several recent colliders:



**B-factories:** KEKB & PEP-II:  
double-ring lepton colliders,  
high beam currents,  
top-up injection

**DAFNE:** crab waist, double ring

**Super B-fact., S-KEKB:** low  $\beta_y^*$

**LEP high energy, SR effects**

**VEPP-4M, LEP:**  
precision E calibration

**KEKB:**  $e^+$  source

**HERA, LEP, RHIC:** spin gymnastics

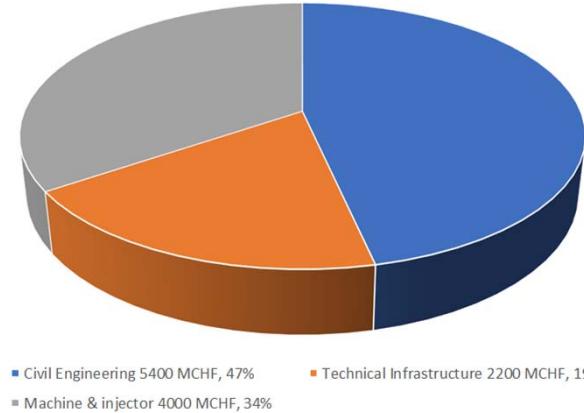


# FCC integrated project cost estimate

## Construction cost phase1 (FCC-ee) is 11,6 BCHF

- 5,4 BCHF for civil engineering (47%)
- 2,2 BCHF for technical infrastructure (19%)
- 4,0 BCHF accelerator and injector (34%)

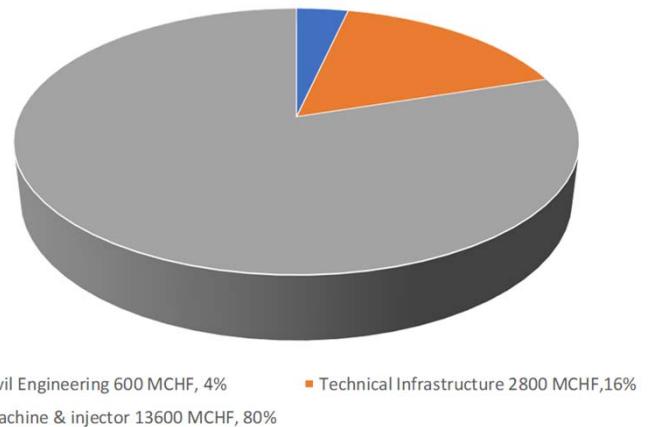
FCC-ee (Z, W, H, t): capital cost per domain



## Construction cost phase 2 (FCC-hh) is 17,0 BCHF.

- 13,6 BCHF accelerator and injector (57%)
  - Major part for 4,700 Nb<sub>3</sub>Sn 16 T main dipole magnets, totalling 9,4 BCHF, targeting 2 MCHF/magnet.
- CE and TI from FCC-ee re-used, 0,6 BCHF for adaptation
- 2,8 BCHF for additional TI, driven by cryogenics  
(Cost FCC-hh stand alone would be 24,0 BCHF.)

FCC-hh - combined mode: capital cost per domain





# Higgs Mass and H-Z-Z Coupling

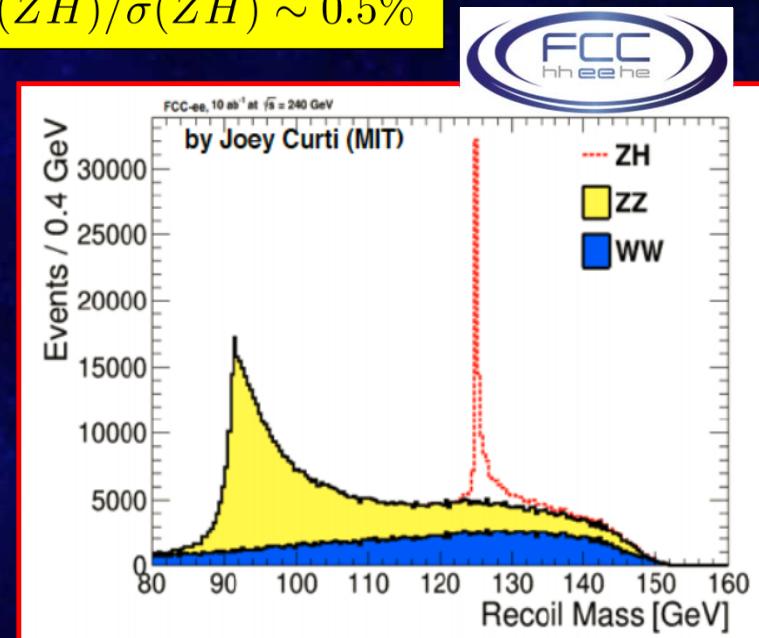
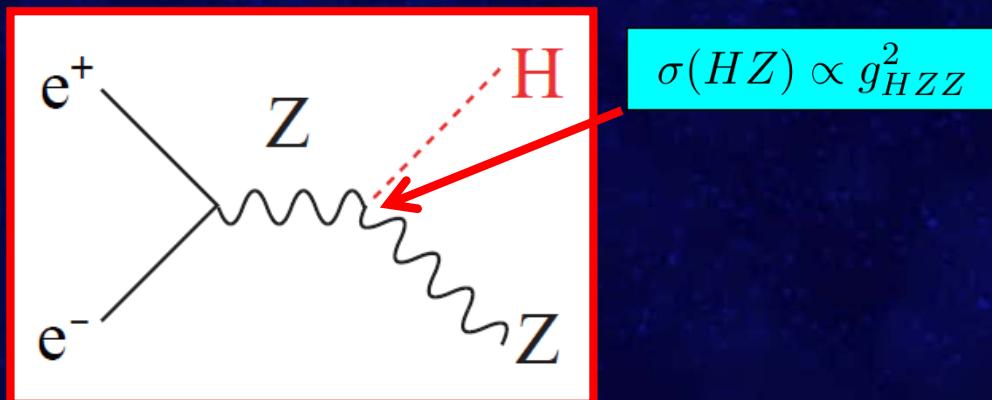


➤ The recoil technique in  $e^+e^- \rightarrow ZH$  - unique for lepton colliders :

- Look just at the Z and reconstruct its decay products
- ZH events are tagged independently of Higgs decay mode (include invisible decay modes)
- Very clean Higgs mass determination:  $m_{\text{recoil}}^2 = (\sqrt{s} - E_{\text{ll}})^2 - |\tilde{p}_{\text{ll}}|^2$

$$\Delta m_H \sim 10 \text{ MeV}$$

- Precise determination of the ZH cross-section  $\Delta\sigma(ZH)/\sigma(ZH) \sim 0.5\%$
- Precise measurement of the H-Z-Z coupling ( $g_{HZZ}$ ):





# Higgs Total Width and HWW Coupling



## ➤ Determination of the H-W-W coupling ( $g_{HWW}$ ):

- Measure the rate of WW Fusion to HZ processes – preferably at 350 GeV, using Higgs decays to the given final state e.g.

$$\frac{\sigma(e^+e^- \rightarrow H\nu_e\bar{\nu}_e) \times BR(H \rightarrow b\bar{b})}{\sigma(e^+e^- \rightarrow HZ) \times BR(H \rightarrow b\bar{b})} \propto \frac{g_{HWW}^2}{g_{HZZ}^2} \quad \rightarrow g_{HWW} \text{ measured}$$

## ➤ Determination of the Higgs total width ( $\Gamma_H$ ):

- Use the HZ proces and  $H \rightarrow ZZ^*$

$$\sigma(e^+e^- \rightarrow HZ) \times BR(H \rightarrow ZZ^*) \propto \frac{g_{HZZ}^4}{\Gamma_H}$$



$\Gamma_H$  measured

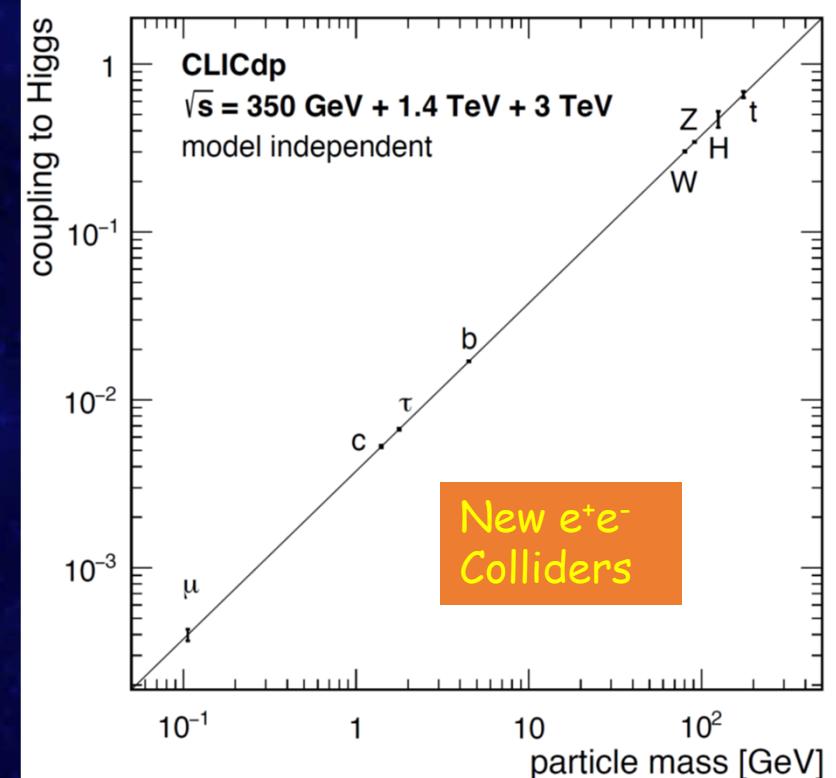
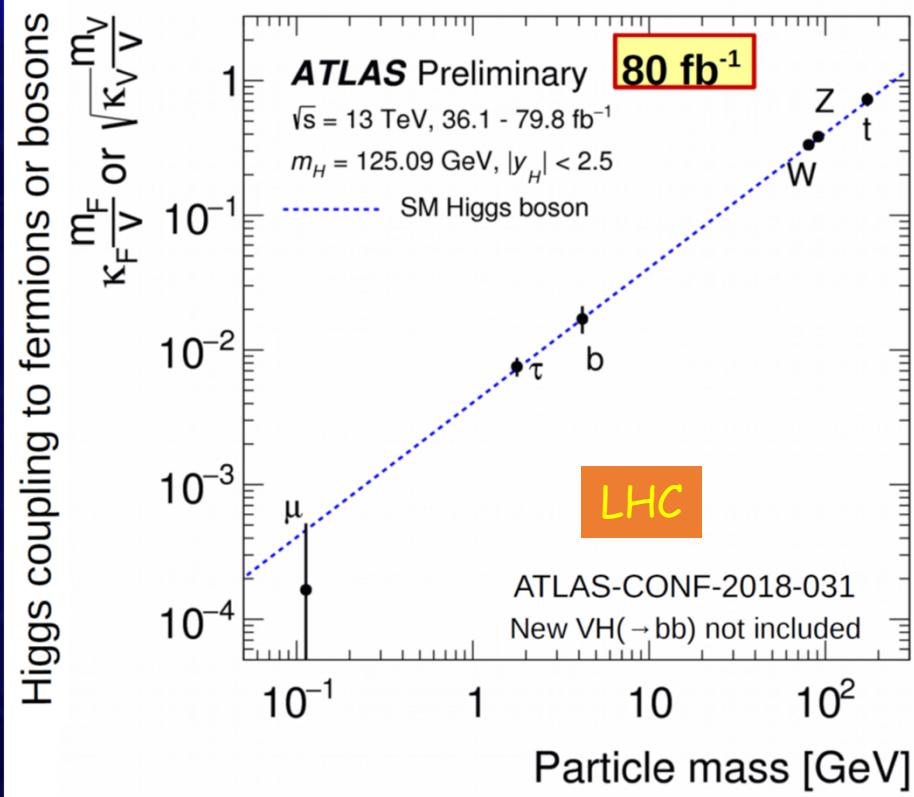
- Use the WW Fusion proces and  $H \rightarrow WW^*$ :

$$\sigma(e^+e^- \rightarrow H\nu_e\bar{\nu}_e) \times BR(H \rightarrow WW^*) \propto \frac{g_{HWW}^4}{\Gamma_H}$$





# Higgs Couplings: Post Factum



$$\Delta k_f \sim 15\%$$

$$\Delta k_f \sim 1\%$$

3rd generation only  
(qualitative precision level)

3rd AND 2nd generations accessible



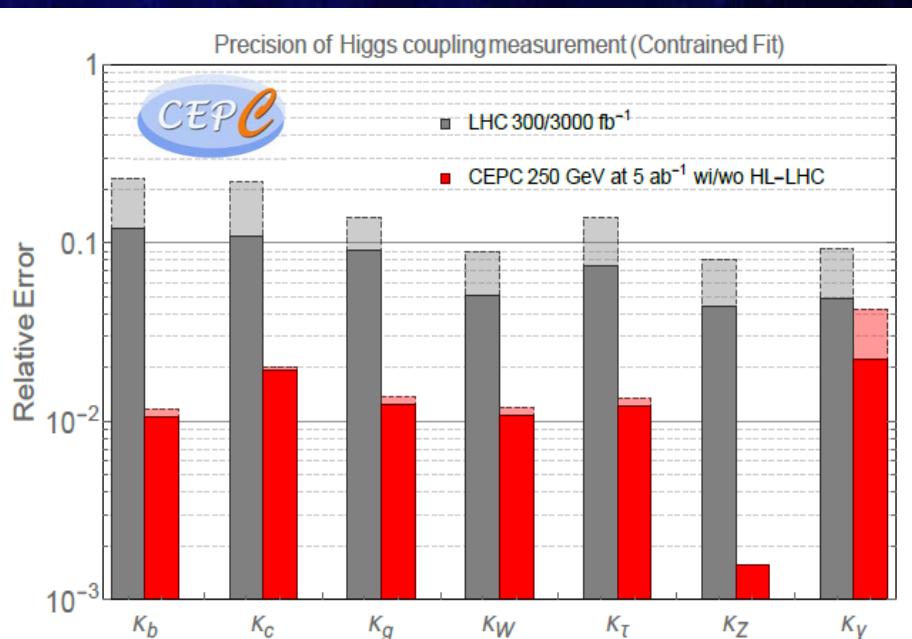
# Normalized Higgs Couplings



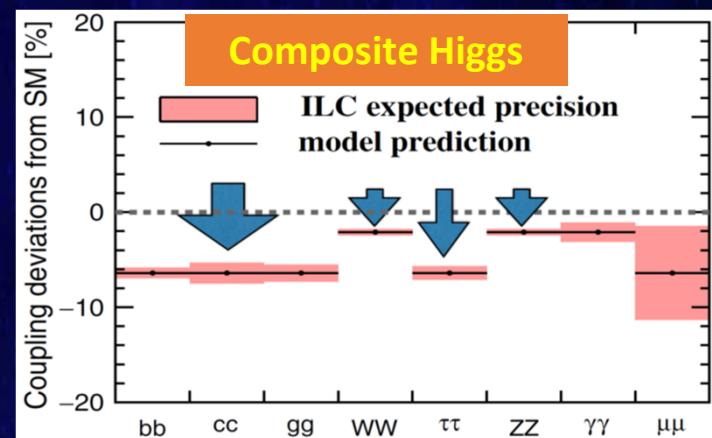
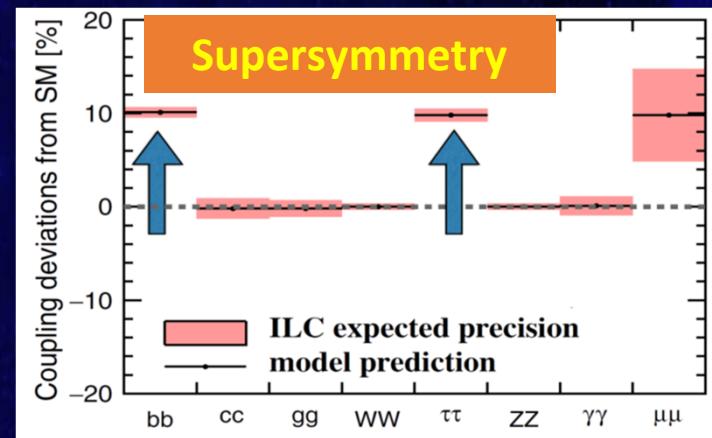
- Higgs couplings normalized to the Standard Model predictions:

$$k_f = \frac{g_{Hff}}{g_{Hff}^{SM}}, \quad f = b, c, \tau$$

$$k_V = \frac{g_{HVV}}{g_{HVV}^{SM}}, \quad V = W, Z, \gamma, g$$



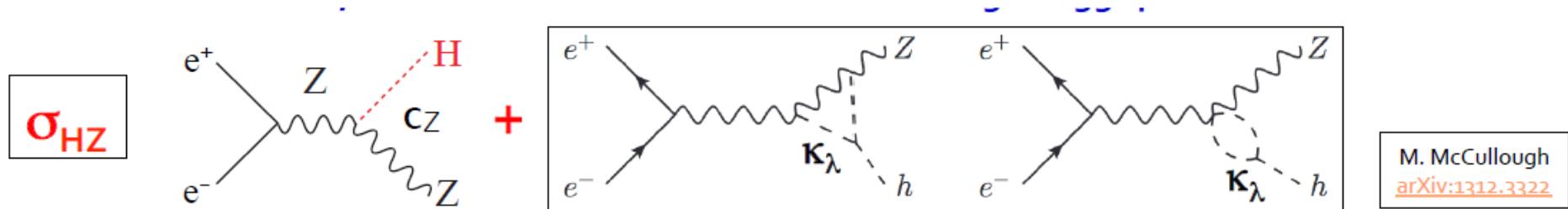
- Fingerprinting NP: different BSM models predict different pattern of deviations from the SM:



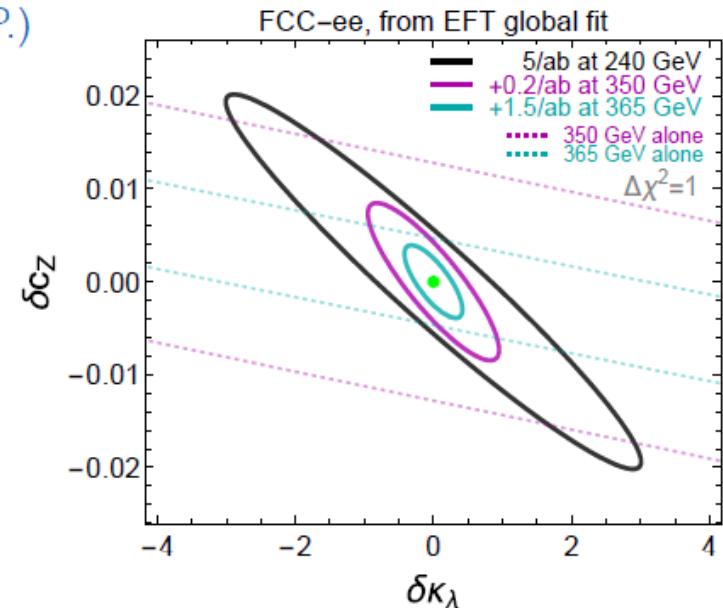
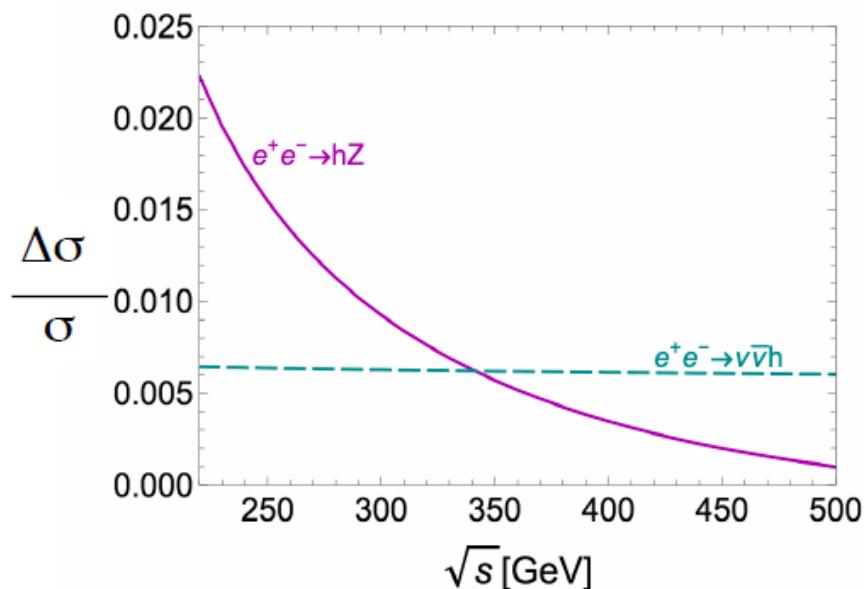
Phys Rev. D 97, 053003 (2018)



# Measurements of the Higgs self-coupling



- assuming all other couplings at MS,  $\Delta\kappa/\kappa \sim 12\%$  (9% 4 I.P.)
- maximum sensitivity at the threshold production



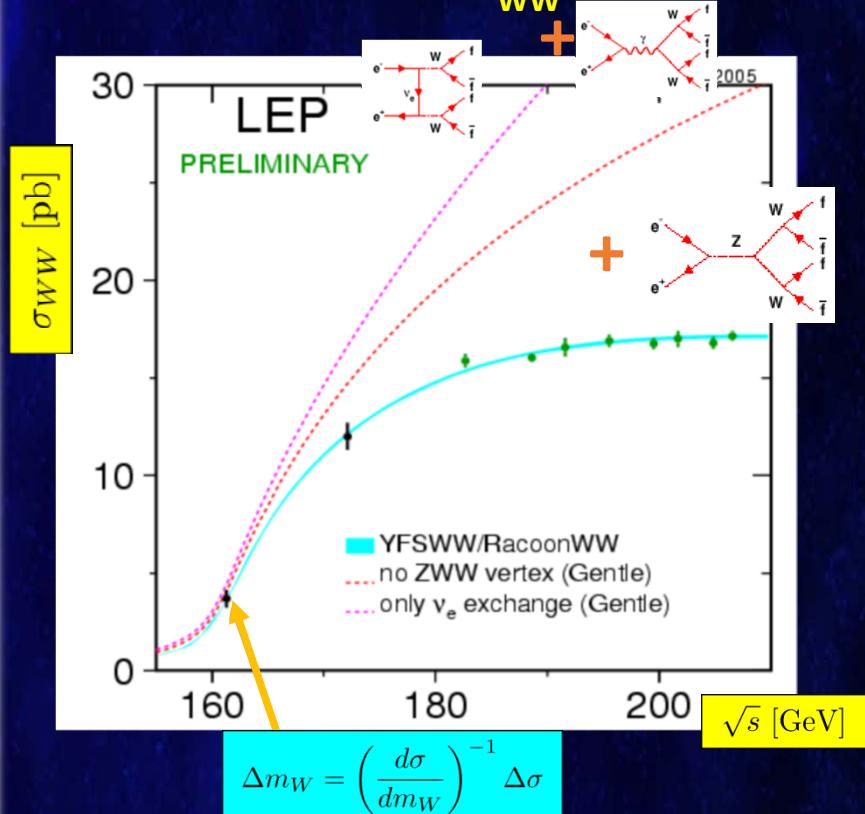
- from a global EFT fit  $\Delta\kappa/\kappa \sim 25\%$  (4 IPs)
- changing CMS energy helps in reducing correlations



# WW Threshold Scan: the W Mass and Width



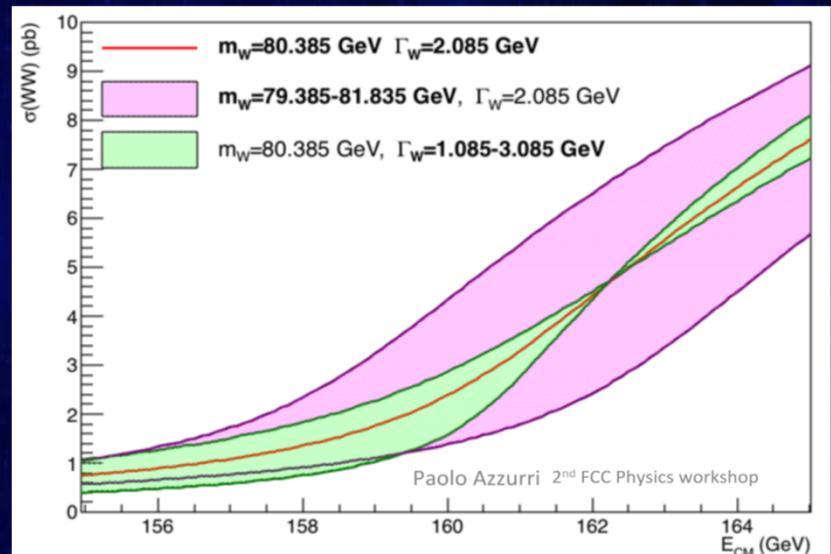
## ➤ The W mass from $\sigma_{WW}$ :



	LEP2 Stat./Prec.	FCC - ee stat (syst)
$N_{WW}$	$4 \times 10^4$	$3 \times 10^7$
$M_W [\text{MeV}]$	$80376 \pm 33 \pm 4$	$0.3 (< \pm 1)$

$$\Delta m_W = 1 \text{ MeV}$$

## ➤ The W width from $\sigma_{WW}$ :



- Measure  $\sigma_{WW}$  in two energy points  $E_1$  and  $E_2$ , with the fractions of luminosity  $f$  and  $(1-f)$   
→ evaluation of both  $m_W$  and  $\Gamma_W$
- Choose the parameters  $E_1$ ,  $E_2$  and  $f$  in order to minimize the errors:  $\Delta\Gamma_W$  and  $\Delta m_W$ :

$$E_1 = 157.1 \text{ GeV} \quad E_1 = 162.3 \text{ GeV} \quad f = 0.4$$

$$\rightarrow \Delta\Gamma_W = 1.5 \text{ MeV} \quad \Delta m_W^{\text{stat}} = 0.6 \text{ MeV}$$



# W Physics: Branching Ratios, TGCs...



➤ **WW samples  
(FCC-ee)**

$\sqrt{s}$ [GeV]	161	240	350
$N_{WW} [\times 10^6]$	30	80	15

➤ **W Branching ratios (%)**

LEP2

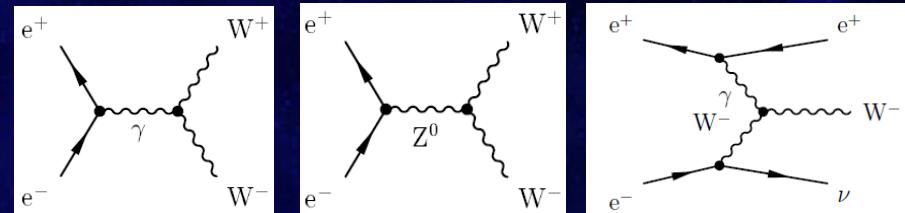
$BR(W \rightarrow e\nu)$	$10.65 \pm 0.17$
$BR(W \rightarrow \mu\nu)$	$10.59 \pm 0.15$
$BR(W \rightarrow \tau\nu)$	$11.44 \pm 0.22$
$BR(W \rightarrow l\nu)$	$10.84 \pm 0.09$
$BR(W \rightarrow \text{hadrons})$	$67.48 \pm 0.28$

- Lepton universality tested at 2% level (2.7 $\sigma$  discrepancy between  $\tau$  and  $\mu/e$ )
- Quark-lepton universality tested at 0.6%

FCC-ee

- Lepton universality test at 0.04% level
- Quark-lepton universality test at 0.01%
- Flavour tagging  $\rightarrow V_{cs} V_{cb} \dots$

➤ **Triple Gauge Couplings**



- Selected LEP limits (95% C.L.)

$\Delta k_\gamma$	$[-9.9, 6.6] \times 10^{-2}$
$\lambda_\gamma$	$[-5.9, 1.7] \times 10^{-2}$
$\Delta k_Z$	$[-7.4, 5.1] \times 10^{-2}$
$\lambda_z$	$[-5.9, 1.7] \times 10^{-2}$
$\Delta g_1^Z$	$[-5.4, 2.1] \times 10^{-2}$

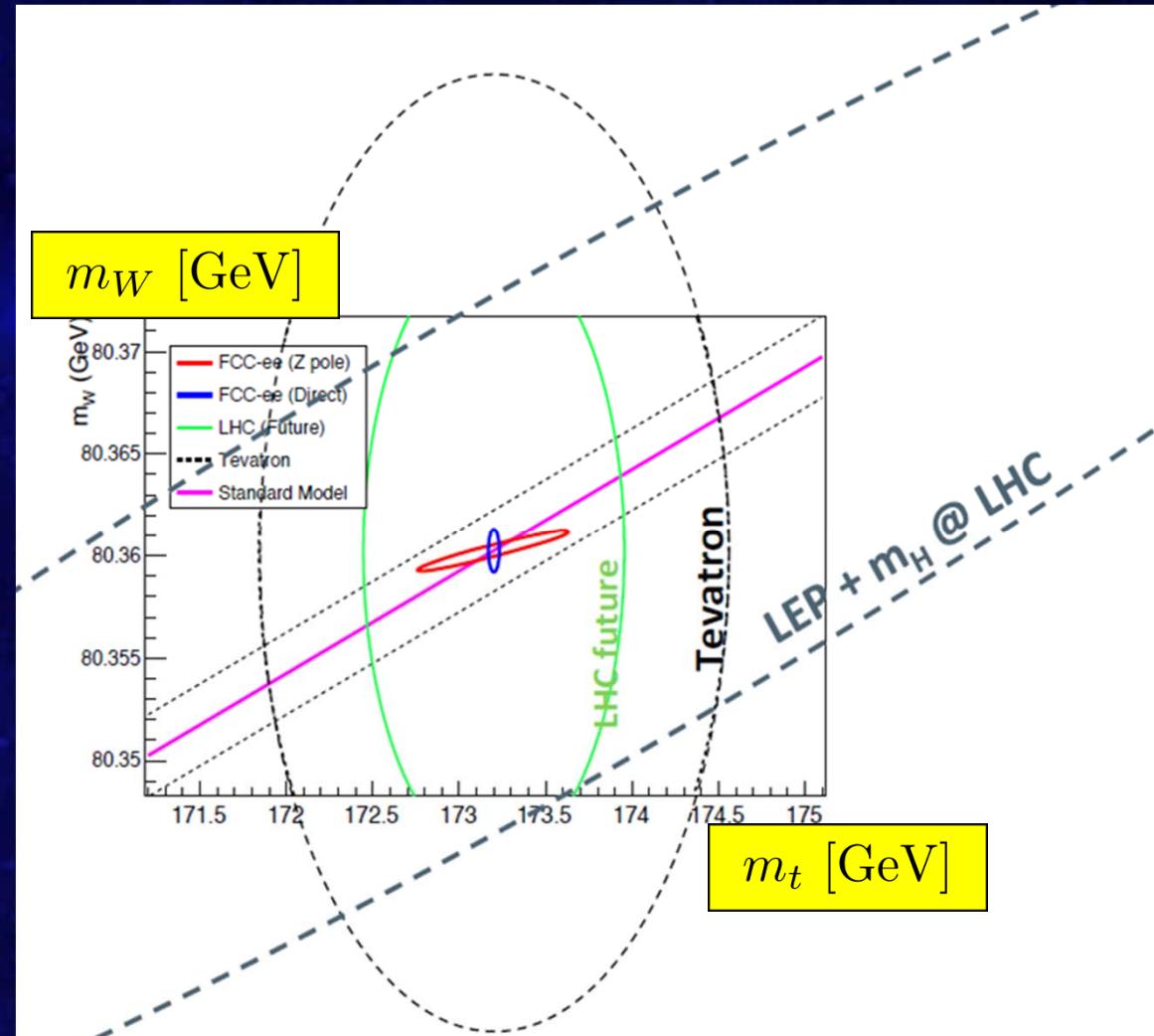
- FCC-ee: overall improvements by a factor of 50 to compare with LEP

➤ **The strong coupling constant:**

- FCC-ee:  $\Delta_{\text{rel}}\alpha_S(m_W^2) = 3 \times 10^{-3}$  from hadronic W decays ( $\Gamma_W$  and  $BR_{W,\text{had}}$ )
- LEP2 precision: 37%



# $m_W$ vs $m_t$





# Electroweak Physics at the Z pole



LEP

$$N_Z = 1.7 \times 10^7$$



FCC-ee

$$N_Z \sim 5 \times 10^{12}$$



**Extreme precision  
of EW observables**

- **Z mass and width (from Z pole scan):**

**The crucial factor:** continuous  $E_{CM}$  calibration (resonant depolarization)

$$\Delta E_{CM} \approx (10 \text{ (stat)} + 100 \text{ (syst)}) \text{ keV}$$

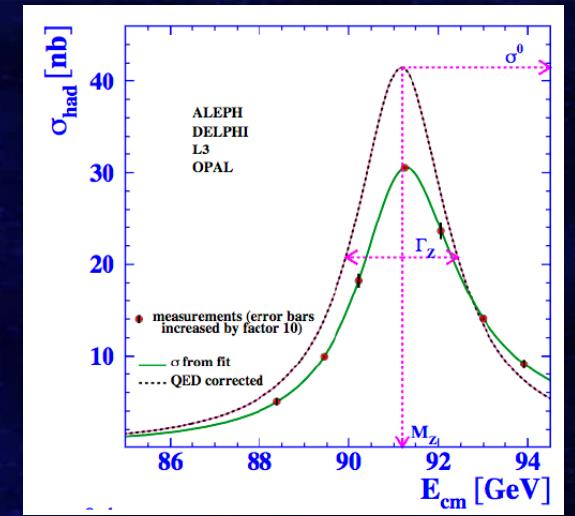
	$\Delta_{rel}$ (LEP)	Improvement factor
Z mass	$1 \times 10^{-6}$	20
Z width	$5 \times 10^{-5}$	20

(~300 (stat)  $\oplus$  ~10 (syst))



$$2.1 \text{ MeV} \rightarrow 100 \text{ keV}$$

$$2.3 \text{ MeV} \rightarrow 100 \text{ keV}$$



- **Normalized partial widths:**

$$R_l = \frac{\Gamma_{had}}{\Gamma_{l\bar{l}}}, \quad l = e, \mu, \tau$$

$$\Gamma_{f\bar{f}} \propto (g_V^f)^2 + (g_A^f)^2 \quad f = l, q$$

$$R_q = \frac{\Gamma_{q\bar{q}}}{\Gamma_{had}}, \quad q = b, c$$

	PDG (LEP) value	PDG (LEP) rel. precision	FCC – ee Improvement factor
$R_e$	$20.804 \pm 0.050$	$2.4 \times 10^{-3}$	20
$R_\mu$	$20.785 \pm 0.033$	$1.6 \times 10^{-3}$	20
$R_\tau$	$20.764 \pm 0.045$	$2.2 \times 10^{-3}$	20
$R_b$	$0.21629 \pm 0.00066$	$3.1 \times 10^{-3}$	10
$R_c$	$0.1721 \pm 0.0030$	$1.7 \times 10^{-2}$	10

necessary input for a precise measurement of EW couplings (next slide)

and  $\alpha_S(m_Z^2)$  (from hadronic Z decays). FCC-ee precision:  $\Delta_{rel}\alpha_S(m_Z^2) = 2 \times 10^{-3}$  LEP: 2.5%

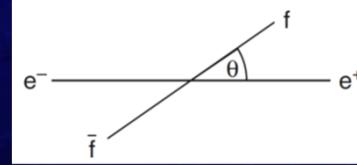


# Electroweak Physics at the Z pole



## Z asymmetries:

$$\frac{d\sigma_{f\bar{f}}}{d\cos\theta} = \frac{3}{8}\sigma_{f\bar{f}}^{\text{tot}} [(1 - \mathcal{P}_e)\mathcal{A}_e(1 + \cos^2\theta) + 2(\mathcal{A}_e - \mathcal{P}_e)\mathcal{A}_f \cos\theta]$$



The forward-backward asymmetry:

$$A_{FB}^f = \frac{\sigma_F - \sigma_B}{\sigma_F + \sigma_B} = \frac{3}{4}\mathcal{A}_e\mathcal{A}_f$$

The left-right asymmetry:

$$A_{LR}^f = \frac{\sigma_L - \sigma_R}{\sigma_L + \sigma_R} = \mathcal{A}_e$$

$\mathcal{P}_e$  - polarization  
of the initial state  $e^-$

$$\mathcal{A}_f = \frac{2g_V^f g_A^f}{(g_V^f)^2 + (g_A^f)^2}$$

LEP & SLC: longstanding discrepancies between different asymmetry measurements; uncertainties dominated by statistics

tau lepton case:

the final state helicity can be measured

$$\mathcal{P}_\tau(\cos\theta) = \frac{\mathcal{A}_\tau(1 + \cos^2\theta) + 2\mathcal{A}_e \cos\theta}{(1 + \cos^2\theta) + \mathcal{A}_e\mathcal{A}_\tau \cos\theta}$$

$$\mathcal{P}_\tau(\cos\theta) = \frac{d(\sigma_r - \sigma_l)}{d\cos\theta} \cdot \left( \frac{d(\sigma_r + \sigma_l)}{d\cos\theta} \right)^{-1}$$

$$A_{FB}^\tau = \frac{(\sigma_r - \sigma_l)_F - (\sigma_r - \sigma_l)_B}{(\sigma_r + \sigma_l)_F + (\sigma_r + \sigma_l)_B}$$

Experimentally accessible observables:

$$\langle \mathcal{P}_\tau \rangle = -\mathcal{A}_\tau$$

$$A_{FB}^\tau = -\frac{3}{4}\mathcal{A}_e$$

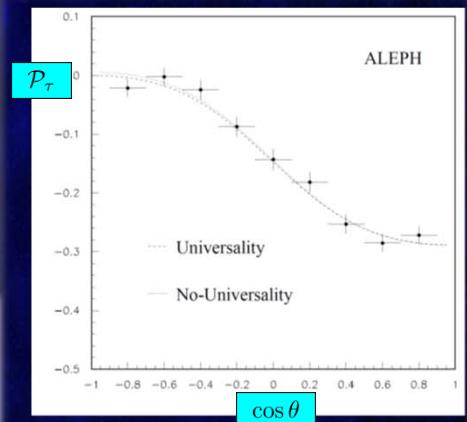
$\mathcal{A}_f$  measured  
( $f = e, \mu, \tau, b, c$ )



$g_V^f g_A^f$  extracted



$$\sin^2 \theta_{W,\text{eff}}^f = \frac{1}{4} \left( 1 - \frac{g_V^f}{g_A^f} \right)$$



	$\Delta_{\text{rel}}^{\text{stat}}$ (FCC - ee)	$\Delta_{\text{rel}}^{\text{syst}}$ (FCC - ee)	Improvement factor w.r.t. LEP
$\mathcal{A}_e$	$5.0 \times 10^{-5}$	$1.0 \times 10^{-4}$	50
$\mathcal{A}_\mu$	$2.5 \times 10^{-5}$	$1.5 \times 10^{-4}$	30
$\mathcal{A}_\tau$	$4.0 \times 10^{-5}$	$3.0 \times 10^{-4}$	15
$\mathcal{A}_b$	$2.0 \times 10^{-4}$	$3.0 \times 10^{-3}$	5
$\mathcal{A}_c$	$3.0 \times 10^{-4}$	$8.0 \times 10^{-3}$	4

Systematic uncertainties dominate

Precision on vector and axial couplings from  $R_f$  and  $A_f$ :

Improvement w.r.t. LEP: 10-100

fermion	$\Delta g_V$	$\Delta g_A$
$e$	$2.5 \times 10^{-4}$	$1.5 \times 10^{-4}$
$\mu$	$2.0 \times 10^{-4}$	$2.5 \times 10^{-5}$
$\tau$	$3.5 \times 10^{-4}$	$0.5 \times 10^{-4}$
$b$	$1.0 \times 10^{-2}$	$1.5 \times 10^{-3}$
$c$	$1.0 \times 10^{-2}$	$2.0 \times 10^{-3}$



# Electroweak Physics at the Z pole



→  $\sin^2 \theta_{W,\text{eff}}$  (absolute) uncertainties:

	stat	syst	Improvement w.r.t. LEP
from muon FB	$10^{-7}$	$5.0 \times 10^{-6}$	100
from tau pol	$10^{-7}$	$6.6 \times 10^{-6}$	75

## ➤ Measurement of $\alpha_{\text{QED}}(m_Z^2)$ - better precision necessary for future precision SM tests !

- Current uncertainty:  $\Delta \alpha_{\text{QED}}(m_Z^2) = 10^{-4}$  from running coupling constant formula: 
$$\alpha_{\text{QED}}(m_Z^2) = \frac{\alpha_{\text{QED}}(0)}{1 - \Delta \alpha_l(m_Z^2) - \Delta \alpha_{\text{had}}^{(5)}(m_Z^2)}$$
 dominated by the experimental determination of the hadronic vacuum polarization, obtained from dispersion integral with expt. input from low energies (KLOE, Belle, BaBar, CLEO, BES CMD-2...)

## ➤ Alternative: the direct measurement of $\alpha_{\text{QED}}(m_Z^2)$ from the muon FB asymmetry just below and just above the Z pole (as part of Z resonance scan) – no need of extrapolation from $\alpha_{\text{QED}}(0)$

- The  $A_{FB}^{\mu\mu}$  - self normalized quantity 
$$A_{FB}^{\mu\mu} = \frac{\sigma_{\mu\mu}^F - \sigma_{\mu\mu}^B}{\sigma_{\mu\mu}^F + \sigma_{\mu\mu}^B}$$
 (no need for measurement of  $L_{\text{int}}$ ; most uncertainties (sel. efficiency, det. acceptance) cancel in the ratio

$$\frac{\Delta \alpha_{\text{QED}}}{\alpha_{\text{QED}}} \simeq \frac{\Delta A_{FB}^{\mu\mu}}{A_{FB}^{\mu\mu}} \times \frac{\mathcal{Z} + \mathcal{G}}{\mathcal{Z} - \mathcal{G}}$$

$\mathcal{Z}(\mathcal{G})$  - Z(photon)-exchange terms

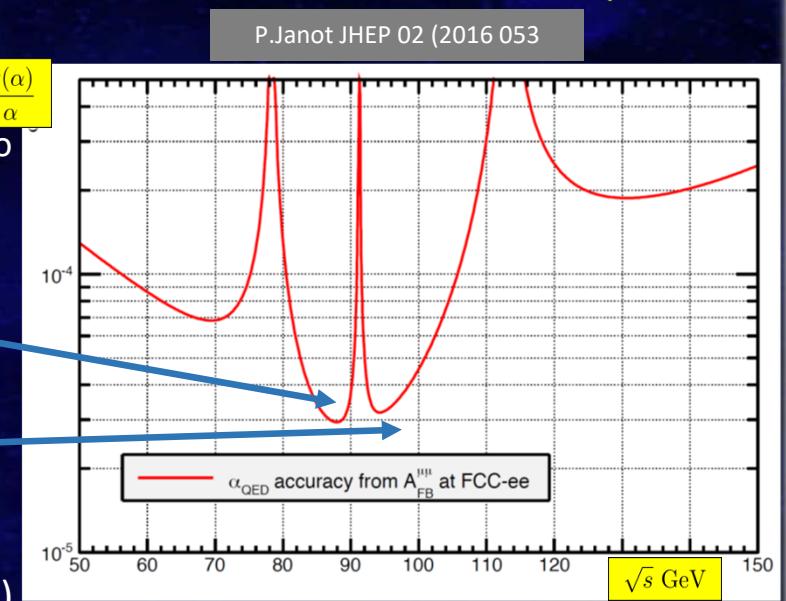
Optimal CMS energies:

$$\sqrt{s_-} = 87.9 \text{ GeV}$$

$$\sqrt{s_+} = 94.3 \text{ GeV}$$

$$\frac{1}{\alpha_{\text{QED}}(m_Z^2)} = \frac{1}{\alpha_\pm} + \beta_{\text{QED}} \log \frac{s_\pm}{m_Z^2} \quad \rightarrow \quad \Delta \alpha_{\text{QED}}(m_Z^2) = 3 \times 10^{-5}$$

(adequate for future precision EW fits)





# The Z Invisible Width – Number of Light Neutrino Species



1)  $N_\nu$  determined at LEP1 from the Z line-shape scan:

$$N_\nu = 2.991 \pm 0.007$$

$$N_\nu \cdot \Gamma_\nu = \Gamma_Z - \Gamma_h - 3\Gamma_l$$

$$N_\nu = \left( \frac{\Gamma_l}{\Gamma_\nu} \right)_{\text{SM}} \cdot \left( \sqrt{\frac{12\pi R_l}{M_Z^2 \sigma_{\text{had}}^{\text{peak},0}}} - R_l - 3 \right)$$

theory

all measured at the peak

Only small room for improvements:

precision limited mainly by the theoretical uncertainty on luminosity determination

i.e. on small angle Bhabha cross section

(LEP1:  $\Delta L/L = 0.00061$ ,  $\Delta N_\nu^{\text{lumi}} = 0.0046 \rightarrow \Delta N_\nu^{\text{lumi}} = 0.0001$  @FCC-ee ).  $\Delta N_\nu^{\text{FCC-ee}} = 0.00008(\text{stat}) \pm 0.0001(\text{syst})$

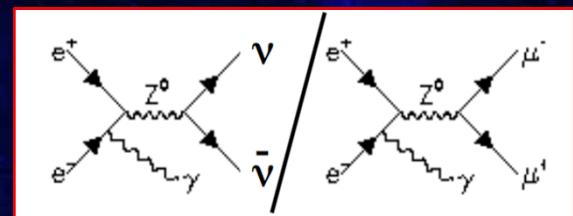
2)  $N_\nu$  from the radiative return process

$$e^+ e^- \rightarrow Z\gamma, \quad Z \rightarrow \nu\bar{\nu}$$

from the higher masses  
than the Z resonance

Monophoton events (normalized  
to photon-lepton-lepton events):

$$N_\nu = \left[ \frac{(e^+ e^- \rightarrow \gamma Z_{\text{inv}})^{\text{meas}}}{(e^+ e^- \rightarrow \gamma Z_{\text{lept}})} \right] \left( \frac{\Gamma_{\nu\bar{\nu}}}{\Gamma_{\text{lept}}} \right)^{\text{SM}}$$



- LEP1:  $N_\nu = 2.92 \pm 0.05$  (statistics too scarce).
- Photon selection common for both final states  $\rightarrow$  cancellations of systematics.
- $N_\nu$  can be measured vs  $\text{sqrt}(s)$   $\rightarrow$  sensitivity to NP at high energy scales.
- FCC-ee sensitivity:

$\sqrt{s}$ [GeV]	years of running	$\Delta N_\nu$ (stat)
161	1	0.0011
240 & 340	5	0.0008
125	1	0.0004

$3 \times 10^7 \gamma Z(\text{inv})$  ev.  
(running parasitically)

$$\Delta N_\nu \leq 4 \times 10^{-4}$$

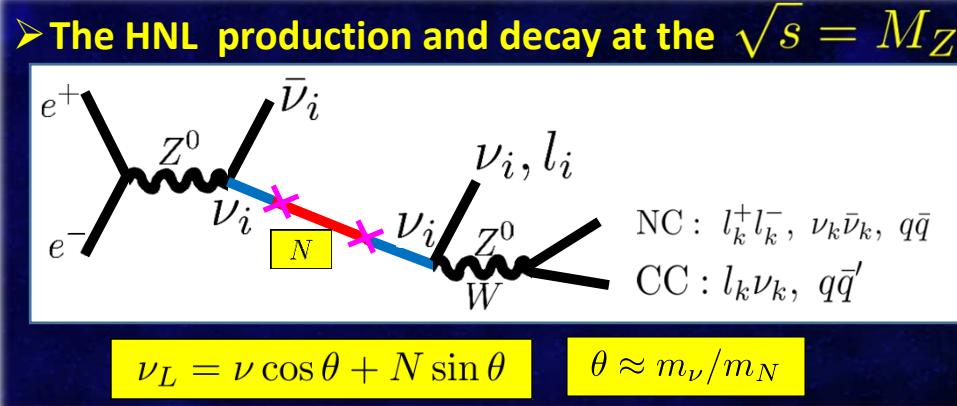




# Heavy Neutral Leptons (HNL) Searches



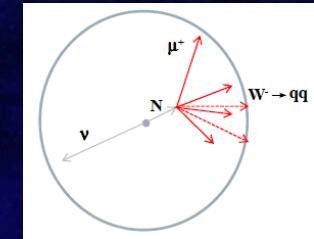
- Sterile, right-handed neutrinos (N) are common in extensions of the SM; they couple to Higgs and SM ν
- Substantial part of them are HNLs: very massive and characterised by macroscopic decay length



## ➤ Experimental signatures

NC: 2 leptons/jets +  $E_{\text{miss}}$

CC: 2 jets + lepton/ $E_{\text{miss}}$



Search for (highly) displaced vertices;  
very clean events

- FCC-ee sensitivity  
to HNLs up to  $10^{-11}$

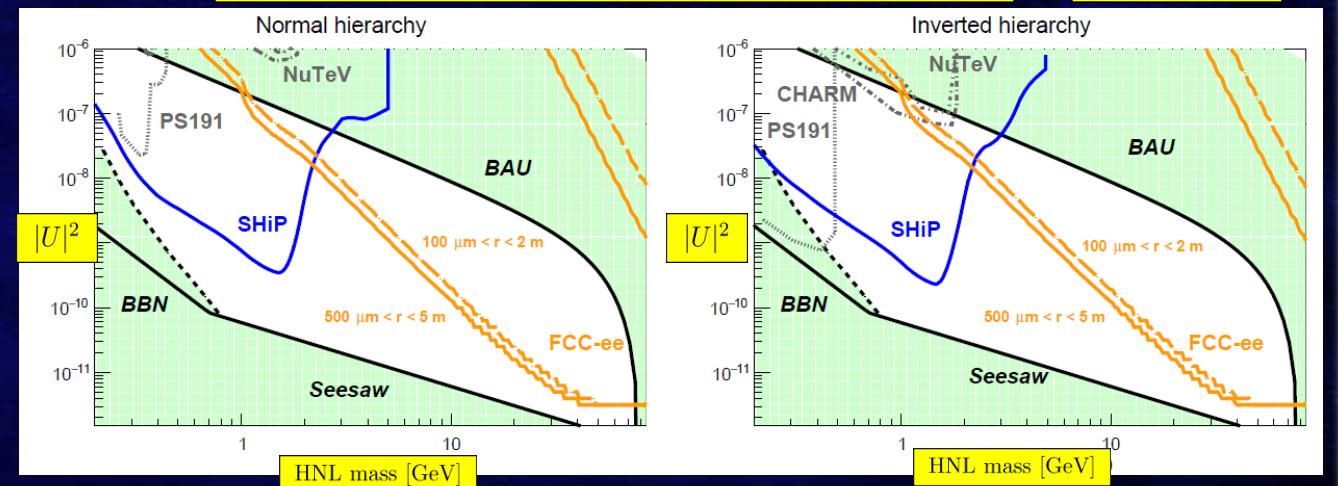
A.Blondel et al., arXiv: 1411.5230 [hep-ex]

- Complementary to  
beam dump facilities

- The upper limits of LEP  
searches:  $10^{-4}$

$$|U|^2 = |U_e|^2 + |U_\mu|^2 + |U_\tau|^2 \quad (N - \nu \text{ couplings})$$

$$|U|^2 \propto \theta^2$$





# Flavour Physics



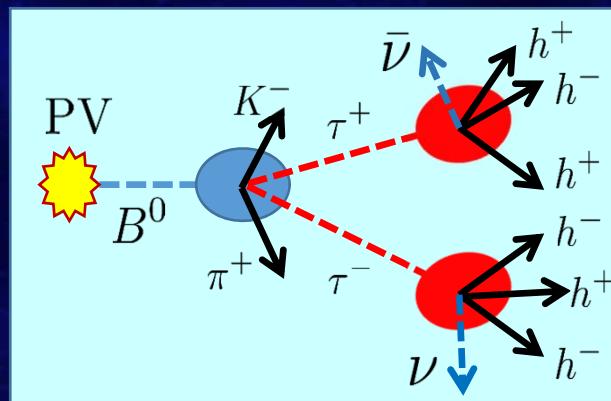
## ➤ The sheer power of statistics:

Particles	$B^0/B^+$	$B_s^0$	$\Lambda_b$	$B_c$	$Z \rightarrow \tau^+\tau^-$
Yields (FCC-ee 150 $ab^{-1}$ )	$10^{12}$	$2.5 \cdot 10^{11}$	$2.5 \cdot 10^{11}$	$2.5 \cdot 10^9$	$5 \cdot 10^{11}$
Yields (Belle II 50 $ab^{-1}$ )	$10^{11}$	$10^{7-8}$	—	—	$5 \cdot 10^{10}$

LEP :  $\sim 6 \times 10^6$       S.Monteil [2nd FCC Physics workshop]

## ➤ Example: $B \rightarrow K^*(892)\tau^+\tau^-$ decay

- Excellent vtx reconstruction ( $\tau \rightarrow 3$  prongs)



- FCC-ee: 1000 signal events expected,  
Belle2: 10 events expected
- The amplitude analysis feasible

