



# Precision QCD at the LHeC and FCC-eh

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on behalf of the LHeC and FCC-eh WGs

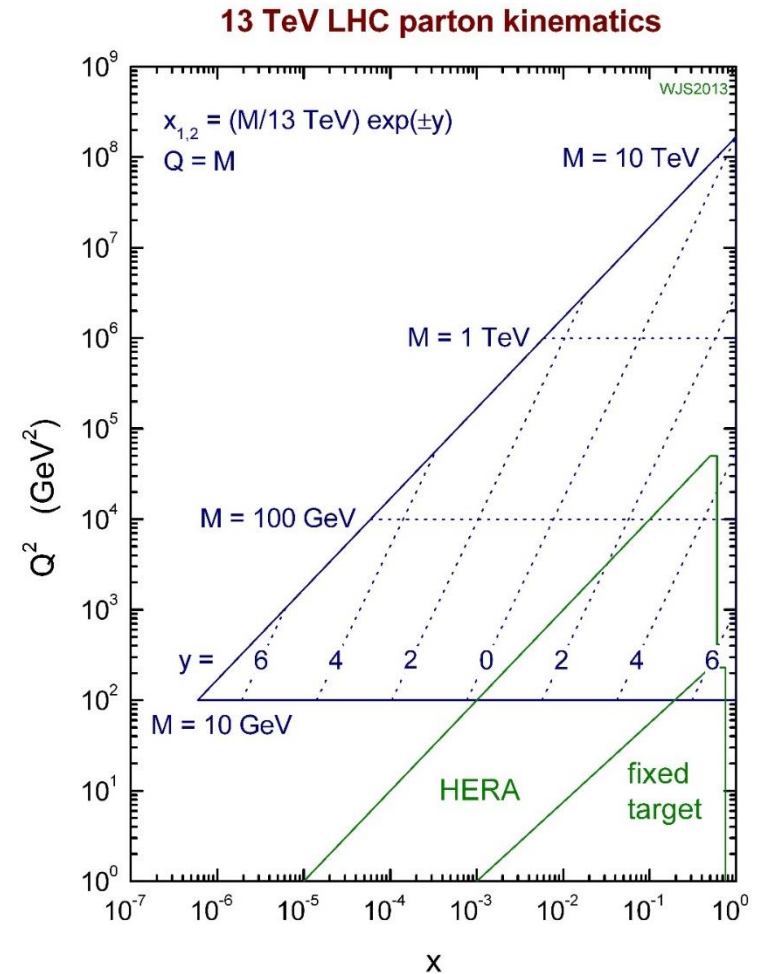
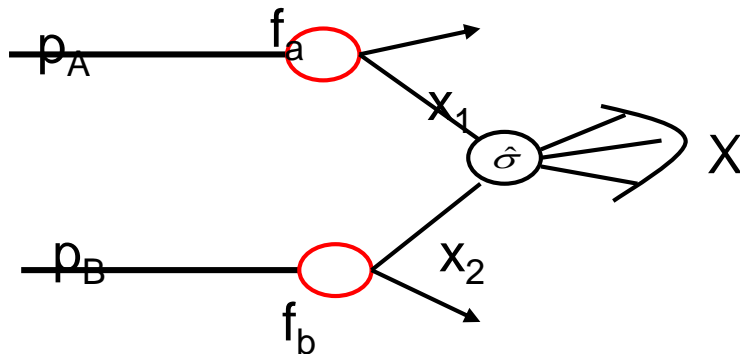


# The Standard Model is not as well known as you might think

In the QCD sector the uncertainties on Parton Distribution Functions (PDFs) limit our knowledge of cross sections-

$$\sigma_X = \sum_{a,b} \int_0^1 dx_1 dx_2 f_a(x_1, \mu_F^2) f_b(x_2, \mu_F^2) \times \hat{\sigma}_{ab \rightarrow X} \left( x_1, x_2, \{P_i^\mu\}; \alpha_S(\mu_R^2), \alpha(\mu_R^2), \frac{Q^2}{\mu_R^2}, \frac{Q^2}{\mu_F^2} \right)$$

where  $X=W, Z, D\text{-}Y, H, \text{high-}E_T \text{ jets, prompt-}\gamma$  and  $\sigma$  is known to some fixed order in pQCD and EW or in some leading logarithm approximation (LL, NLL, ...) to all orders via resummation



Our knowledge of PDFs in the LHC kinematic region mostly comes from evolving the results from HERA and other Deep Inelastic Scattering experiments in  $Q^2$  using the QCD DGLAP formalism

# How well do we know PDFs today ?

This is best evaluated in terms of parton-parton luminosities, which are the convolution of the purely partonic part of the sub-process cross-section.

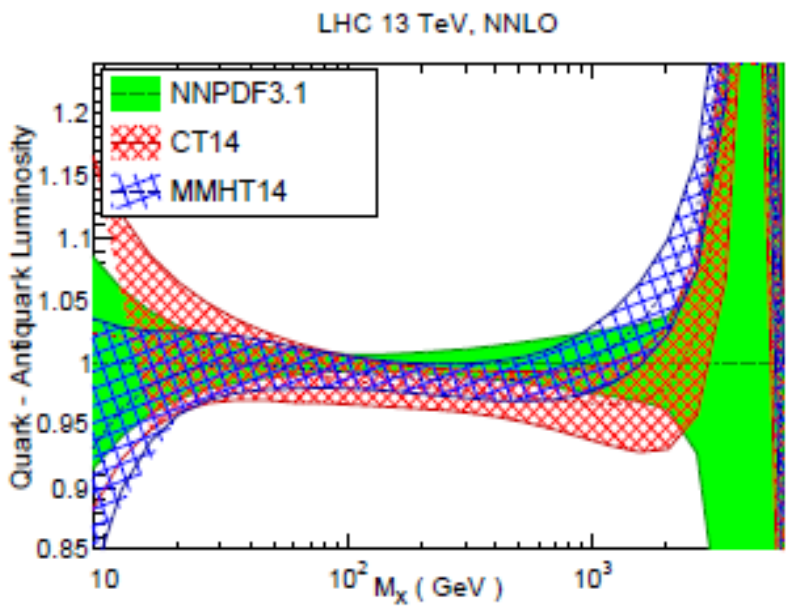
The quark-antiquark and gluon-gluon luminosities for various PDFs are compared here for 13 TeV LHC running in terms of the centre of mass energy of the parton sub- process  $M_x$

So for Drell-Yan production of W or Z at  $M_x \sim 80,90$  GeV

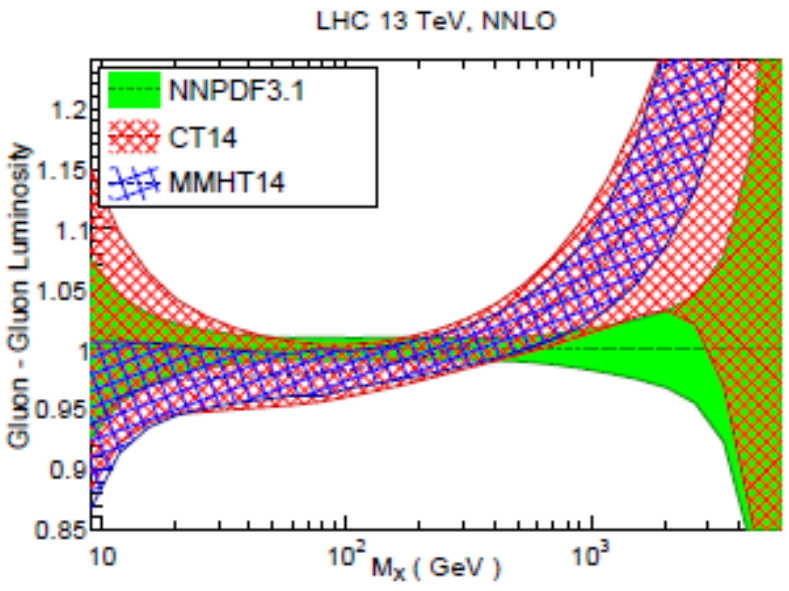
Or for gluon-gluon production of Higgs at  $M_x \sim 125$  GeV

the parton-parton luminosities are fairly well known

- This is not so for higher mass BSM particles where we need improved PDFs at high-x
- It is also not so for low-scales/ low-x where we may learn more about QCD in the non-linear regime
- We also need to know PDFs better in the regions where they are best known today in order to reduce the uncertainty on precision SM measurements like  $M_W$  and  $\sin^2\theta_W$

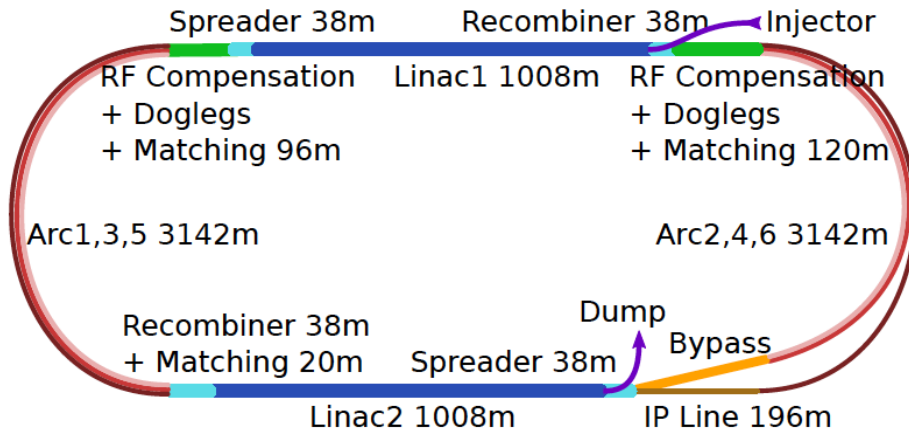


$$\mathcal{L}_{ij}(M^2, s) = \int_{\tau}^1 \frac{dx}{x} x f_i(x, M^2) \frac{\tau}{x} f_j\left(\frac{\tau}{x}, M^2\right) \quad \tau \equiv \frac{M^2}{s}$$



# How could one improve knowledge?

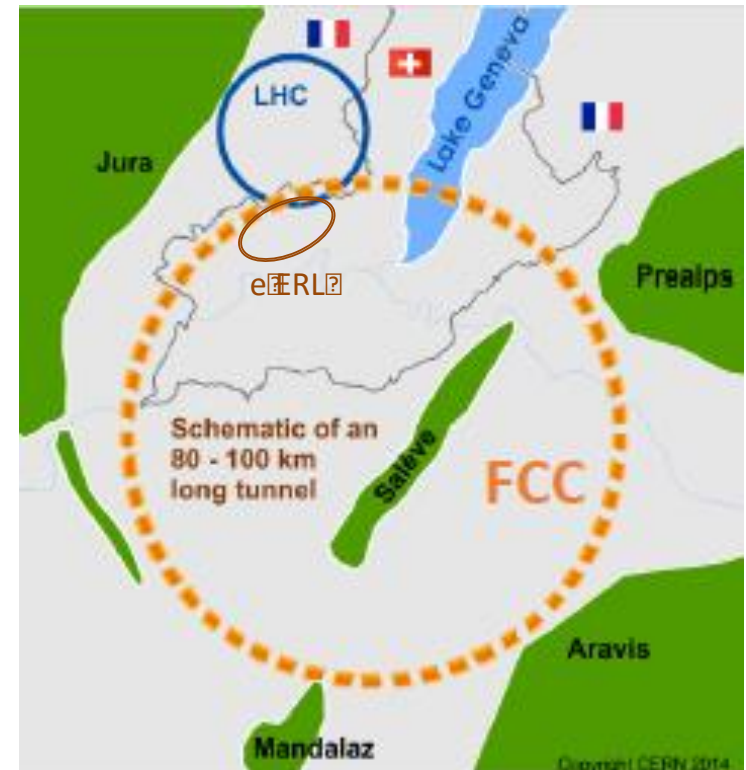
## LHeC and FCC-eh



energy recovery LINAC

e beam: up to 60 GeV

Lint  $\rightarrow$  1 ab<sup>-1</sup> (1000× HERA ; per 10 yrs)



operating **synchronously** :

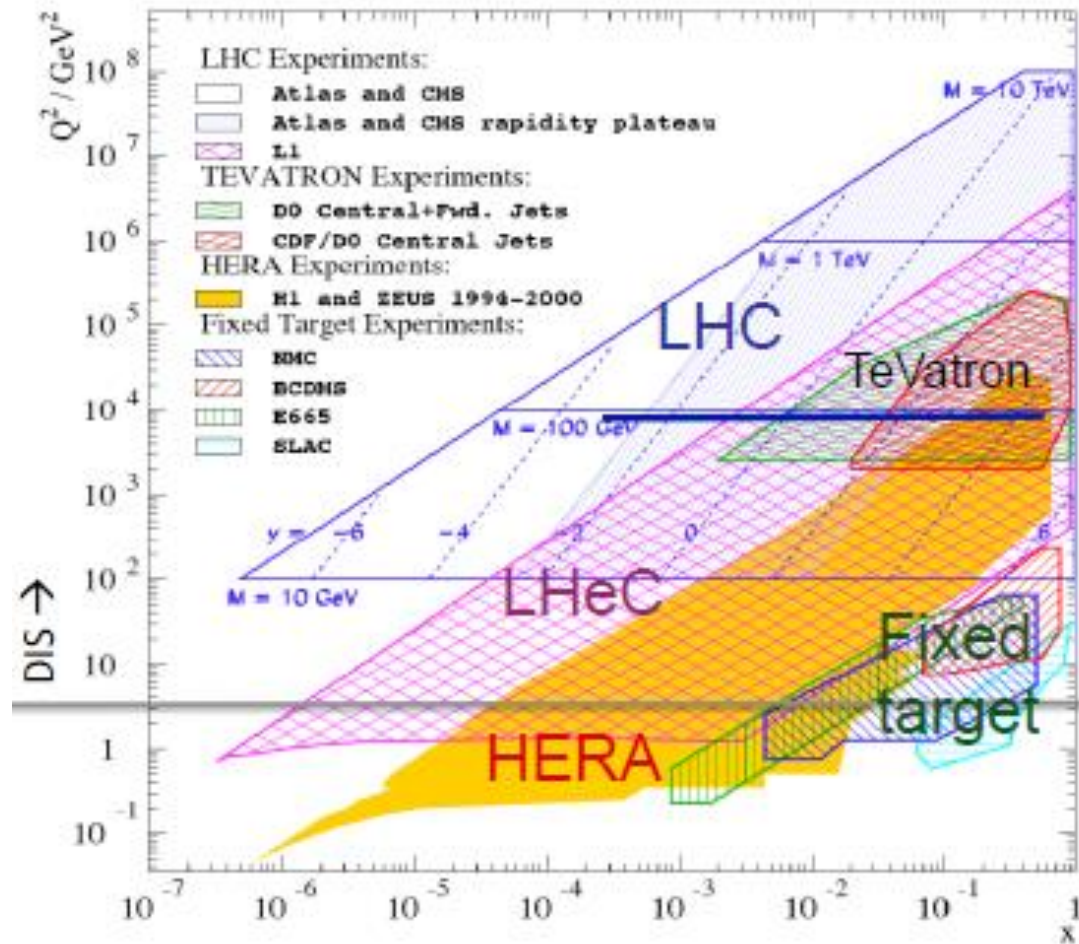
- with **HL-LHC** (or HE-LHC)  
**p: 7 (14) TeV,  $\sqrt{s} \approx 1.3$  (1.8) TeV**
- and/or later with an **FCC (A)**  
**p: 50 (20) TeV,  $\sqrt{s} \approx 3.5$  (2.2) TeV**

† **FCC (A)**: a lower energy configuration that could operate earlier, in an FCC tunnel, using current magnet technology

# Kinematic coverage

The LHeC option represents an increase in the kinematic reach of Deep Inelastic Scattering and an increase in the luminosity  $\sim 500$  fold

- This represents a tremendous potential for the increase in the precision of Parton Distribution Functions
- And the exploration of a kinematic region at low-x where we learn more about QCD- e.g. is there gluon saturation?
- Precision PDFs are needed for BSM physics



But can't we get precision PDFs from the LHC itself?

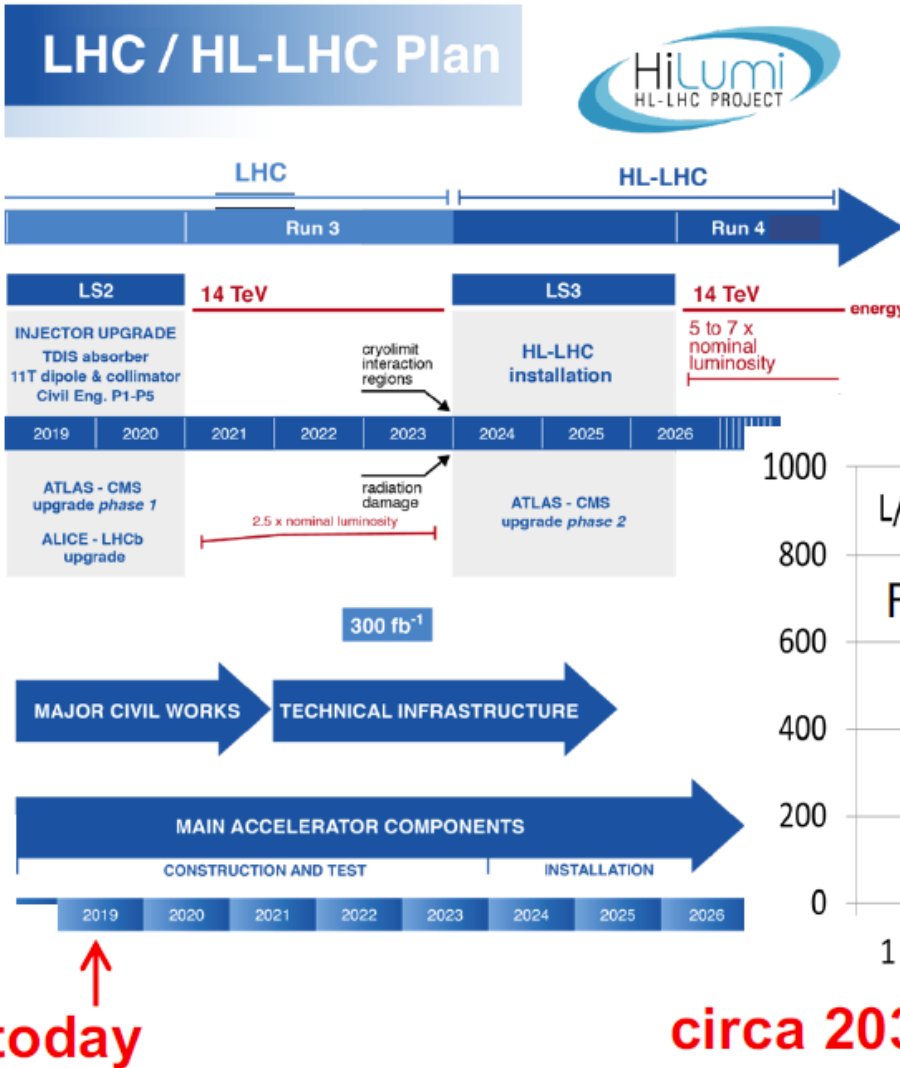
Future projections suggest we may get some way towards it.

But future projections live in an ideal world where many different types of data from the LHC have completely well understood systematics, well understood correlations and no inconsistencies.

The single consistent data set of deep inelastic scattering at an LHeC is a tried and tested reliable way to achieve this.

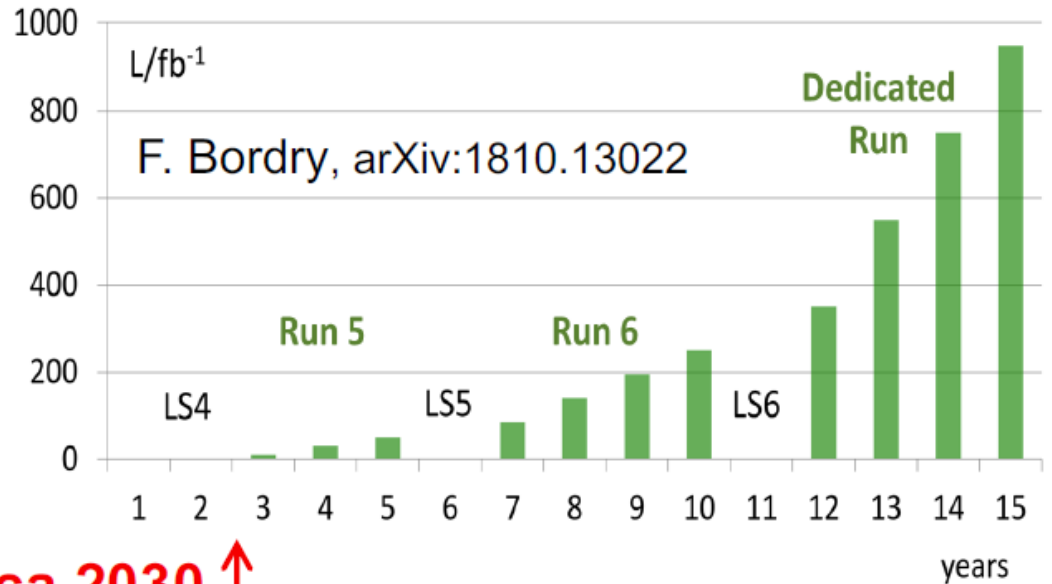
Plus there are questions of timing.....

# Timelines



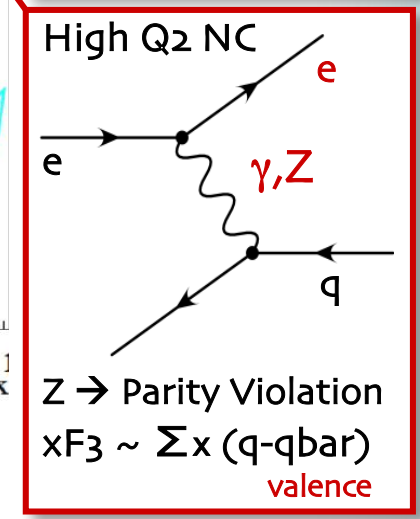
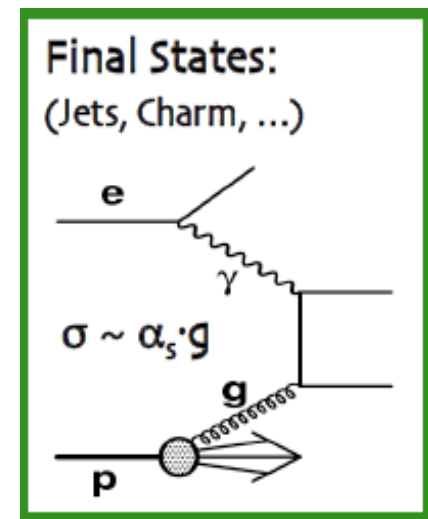
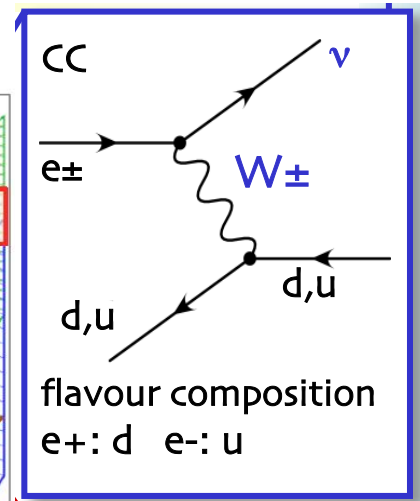
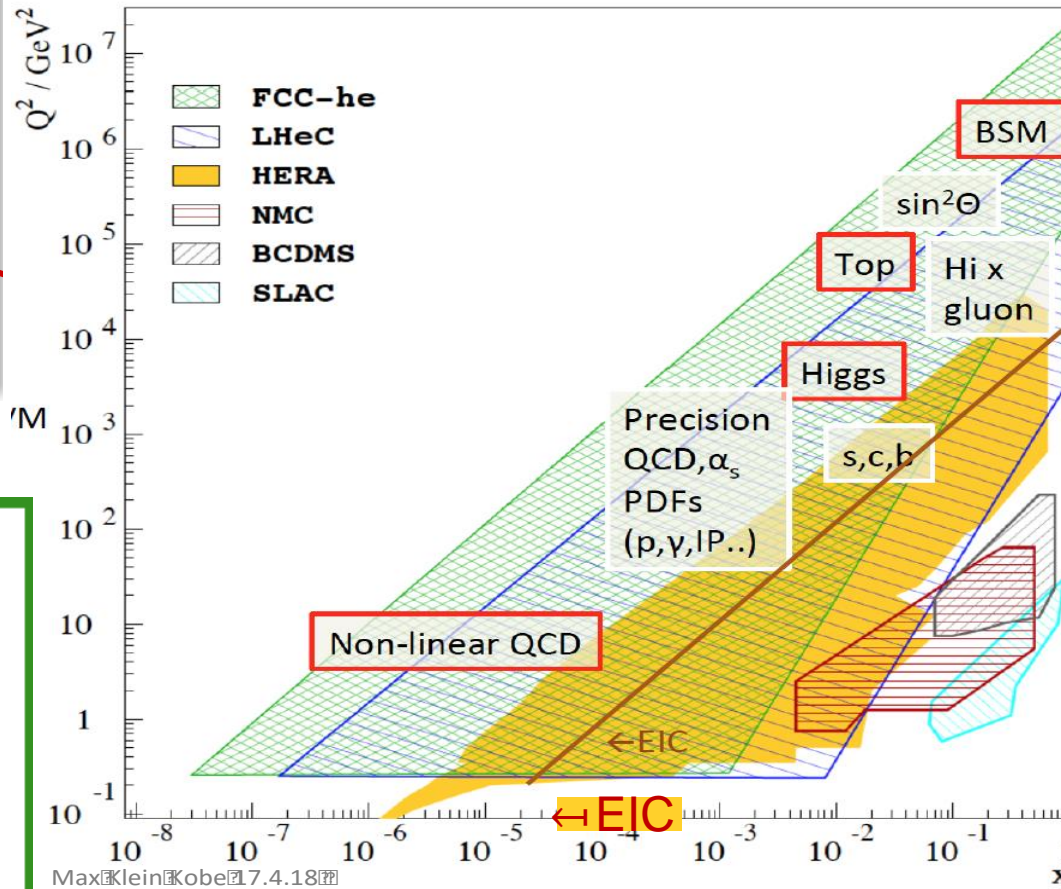
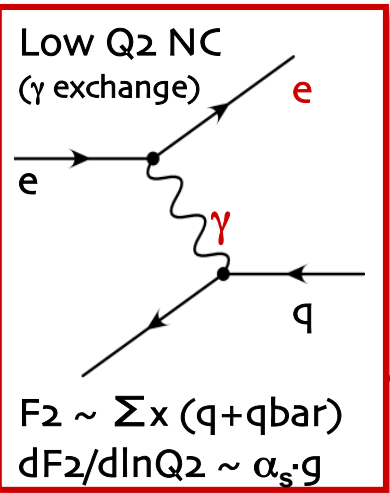
**LHeC** 1<sup>st</sup> run, Lint approx. 50 fb<sup>-1</sup>  
total Lint → 1 ab<sup>-1</sup>

**LHeC** projected Integrated Luminosity:



50 fb<sup>-1</sup> can be achieved in 3 years before LS5 and long before the end of HL-LHC running

# Where does the information come from?



$\times 15/120$  extension in  $Q^2, 1/x$  reach vs HERA

# LHeC pdf programme

simulation and  
pdf fit studies:

M. Klein,  
C. Gwenlan

completely resolve all **proton pdfs**, and  $\alpha_s$  to permille precision

→ **ubar, uv, dbar, dv, s, c, b, t, xg** and  $\alpha_s$

unprecedented kinematic range;  
no higher twist, no nuclear corr.,  
free of symmetry assumptions,  
N3LO theory possible, ...

**NEW LHeC simulations (e: 50 GeV, p: 7TeV)**

dataset	e charge	e pol.	lumi (fb-1)	
NC/CC	–	–0.8	5,50,1000	luminosity
NC/CC	+	0	1,10	positron
NC/CC	–	0	50	polarisation
NC/CC	–	+0.8	10,50	

**uncert. assumptions:**  
elec. scale: 0.1%;  
hadr. scale 0.5%;  
radcor: 0.3%;  
 $\gamma p$  at high y: 1%  
uncorrelated extra eff.: 0.5%  
CC syst: 1.5%  
luminosity: 0.5%

NB, I will frequently refer to the following:

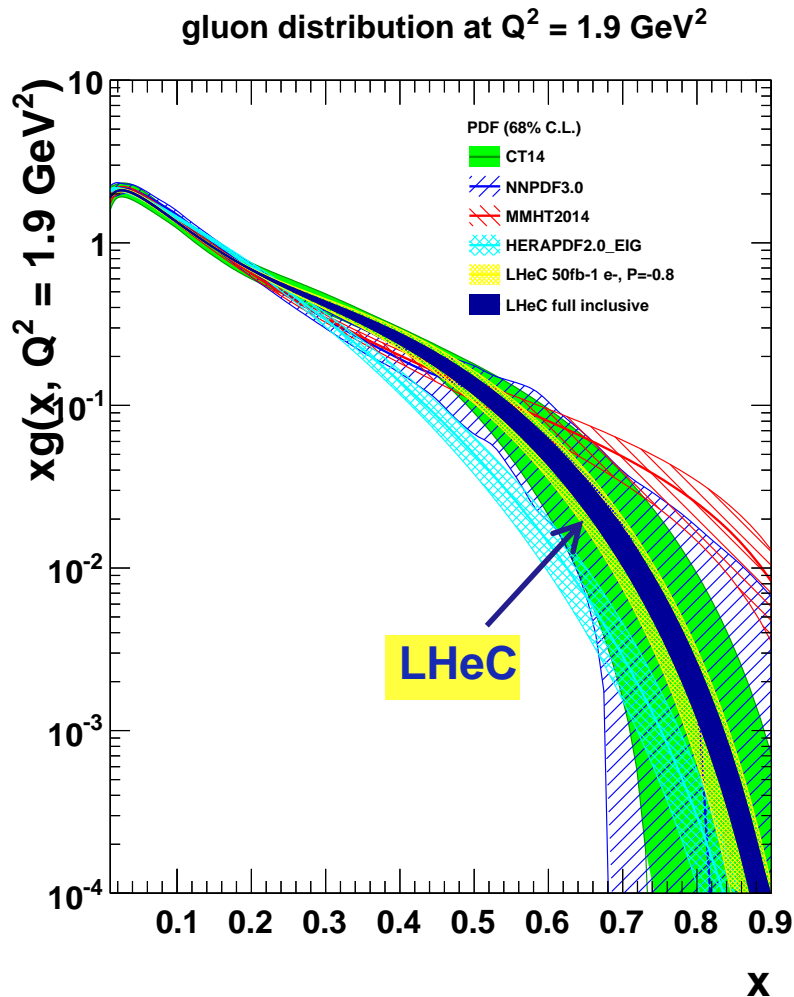
LHeC 1<sup>st</sup> Run (e-, 50 fb-1, P=-0.8)

LHeC full inclusive (e-, 1000 fb-1, P=-0.8) + (e-, 50 fb-1, P=+0.8) + (e+, 10 fb-1)

**QCD analysis a la HERAPDF**, BUT no constraint that  $d\bar{u} = u\bar{d}$  at small x;  
4+1 xuv, xdv, xUbar, xDbar and xg



# Gluon at large x



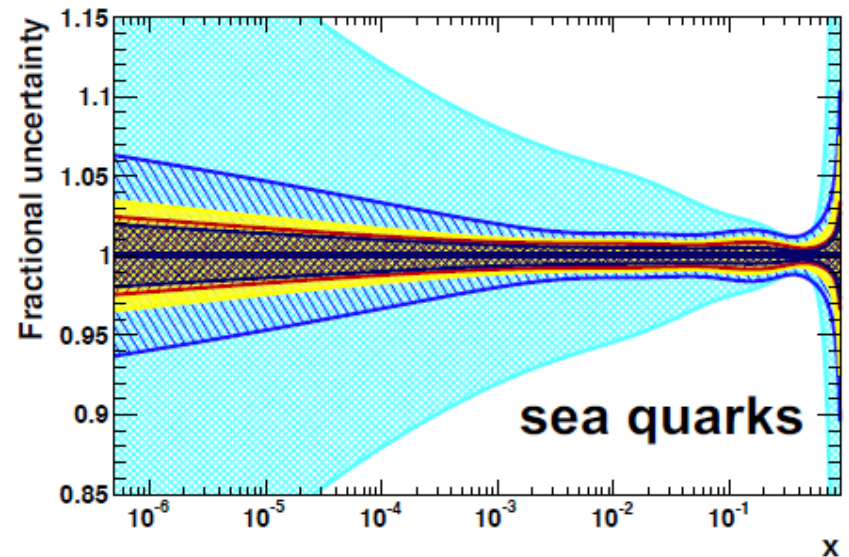
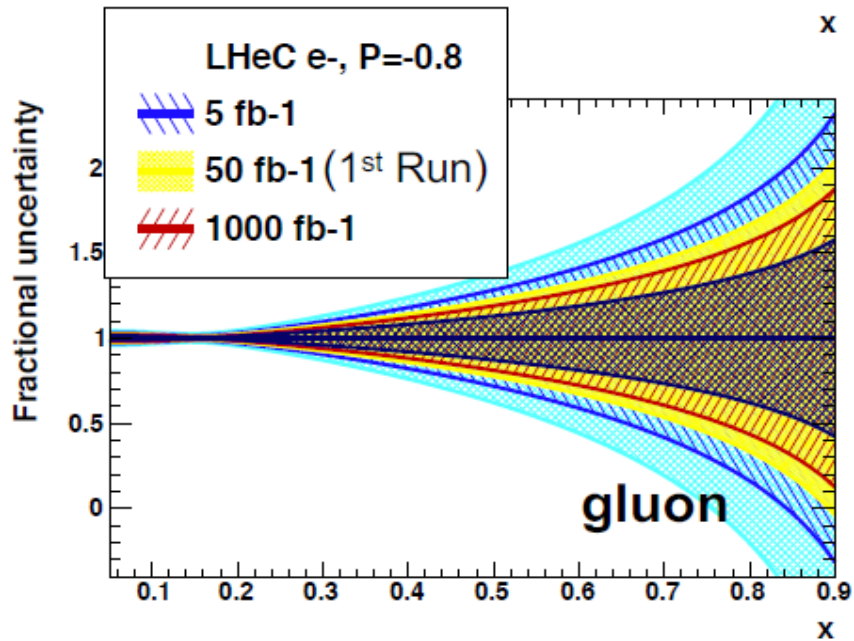
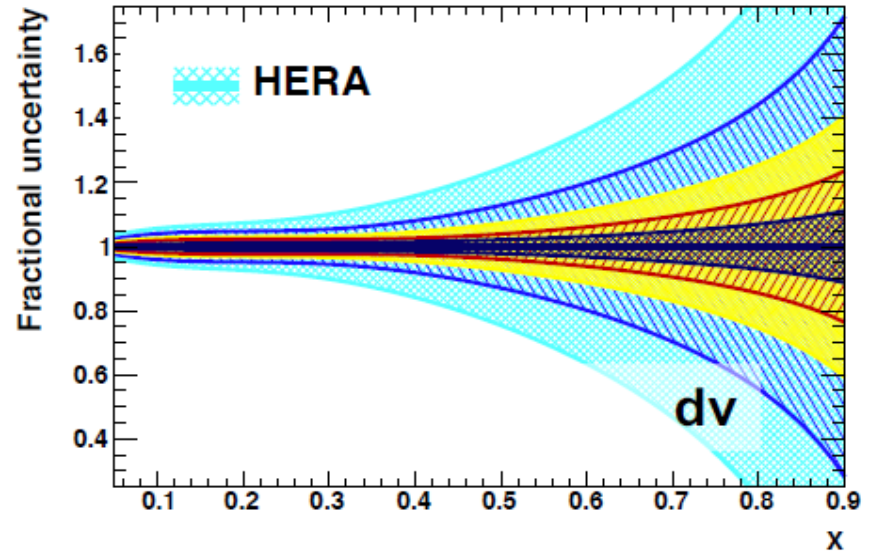
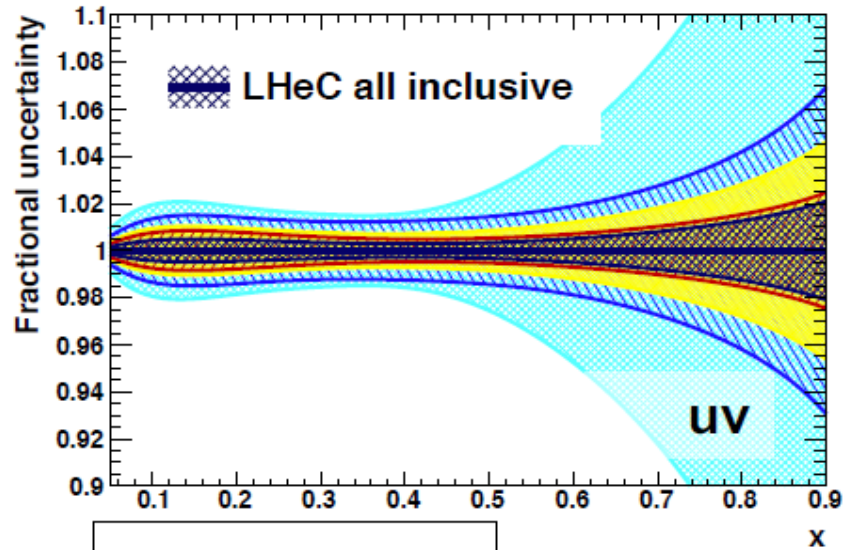
gluon at large x is small and currently  
very poorly known;  
**crucial for new physics searches**

**LHeC** sensitivity at large x comes as  
part of overall package

- high luminosity ( $\times 50-1000$  HERA);
- fully constrained quark pdfs; small x;
- momentum sum rule

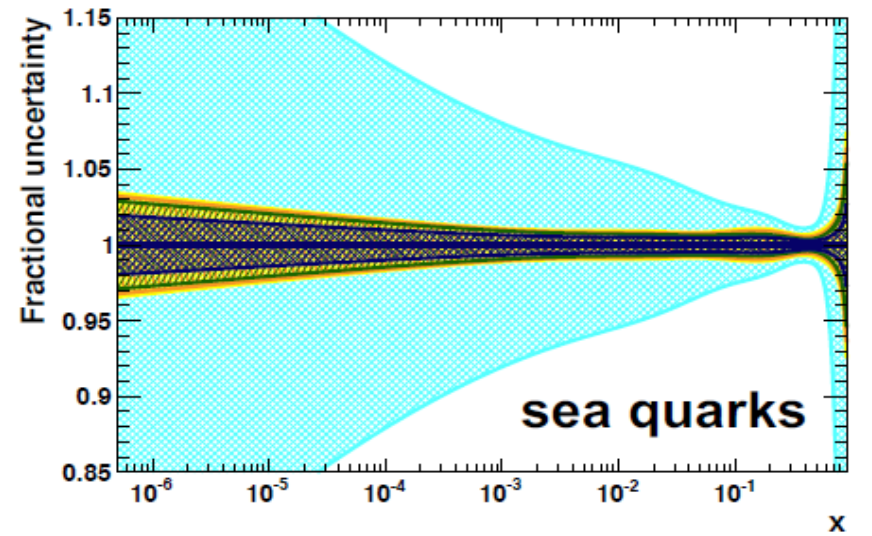
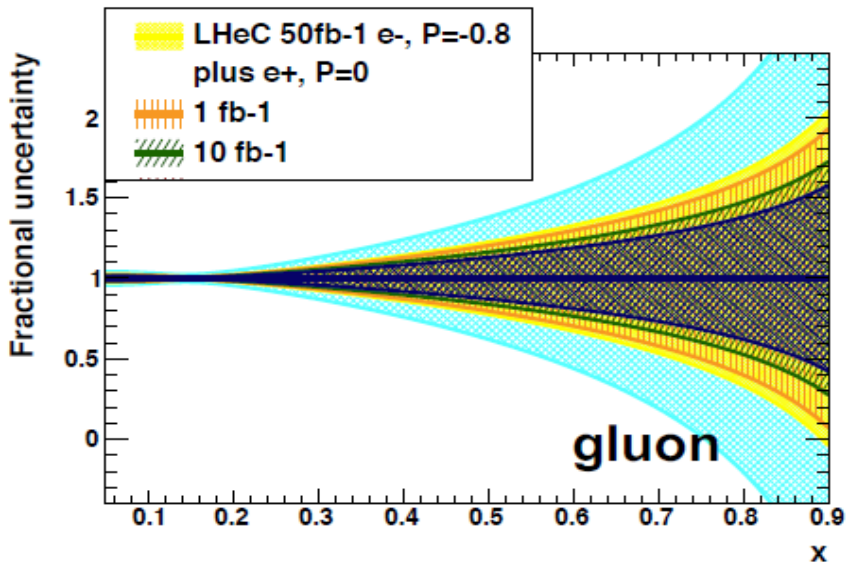
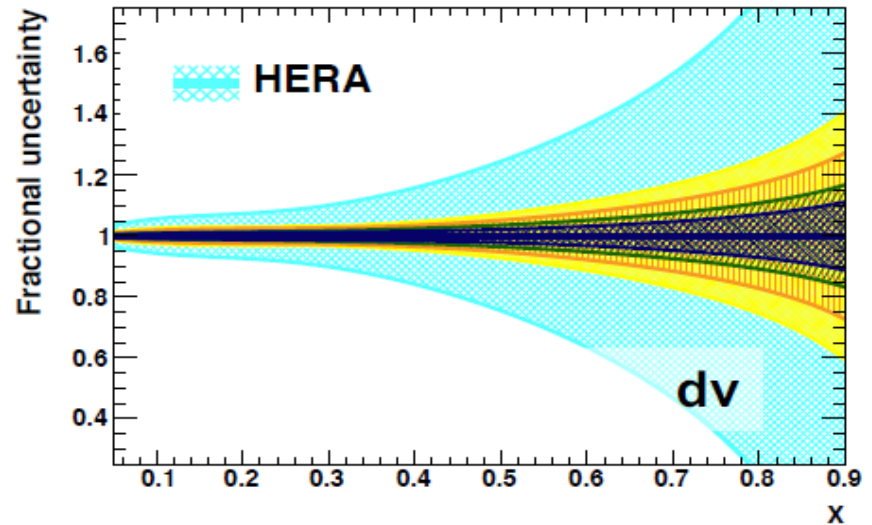
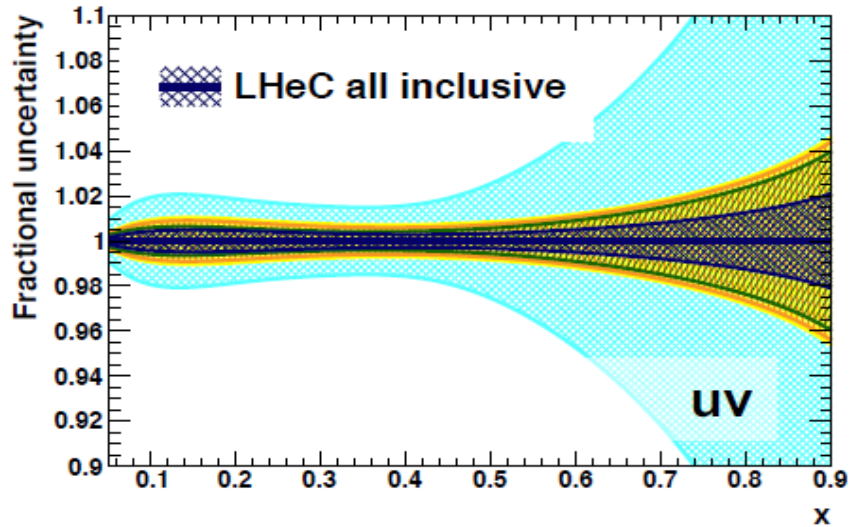
gluon and sea intimately related  
**LHeC** can disentangle sea from  
valence quarks at large x, with precision  
measurements of **CC** and **NC**  $F_2^{YZ}$ ,  $xF_3^{YZ}$

# Impact of luminosity on PDFs



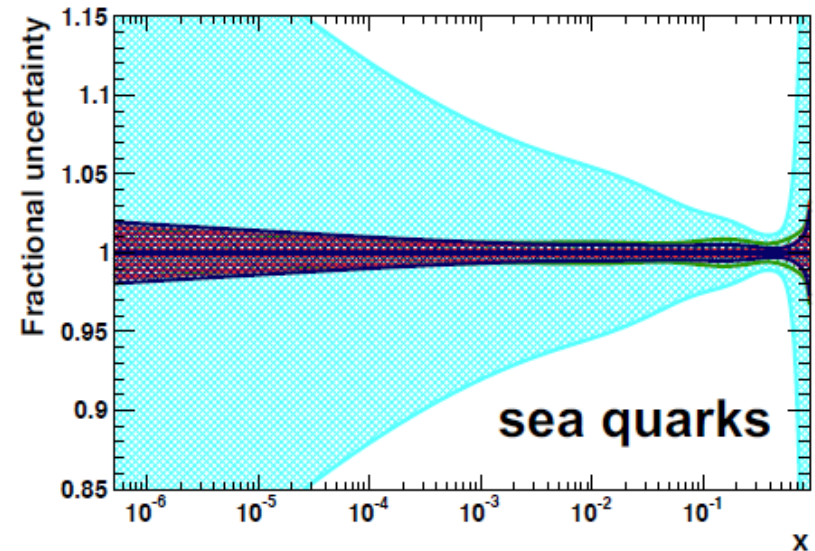
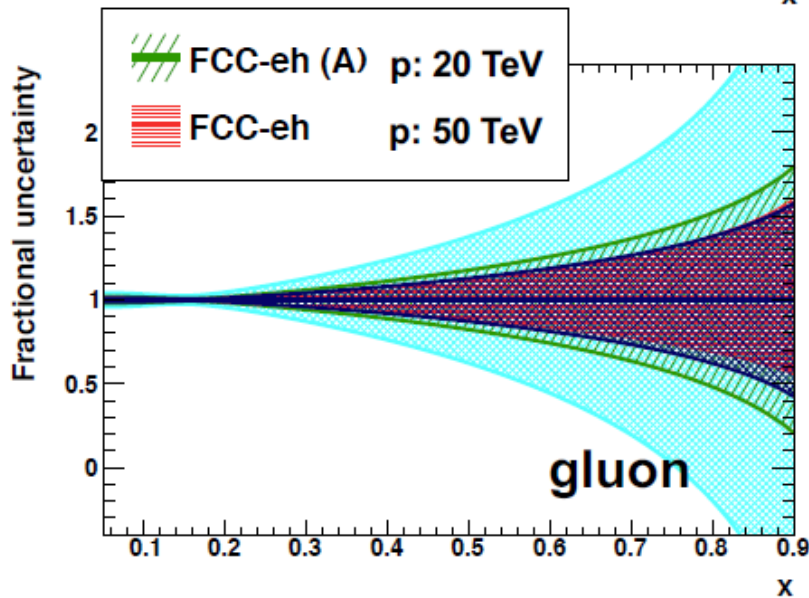
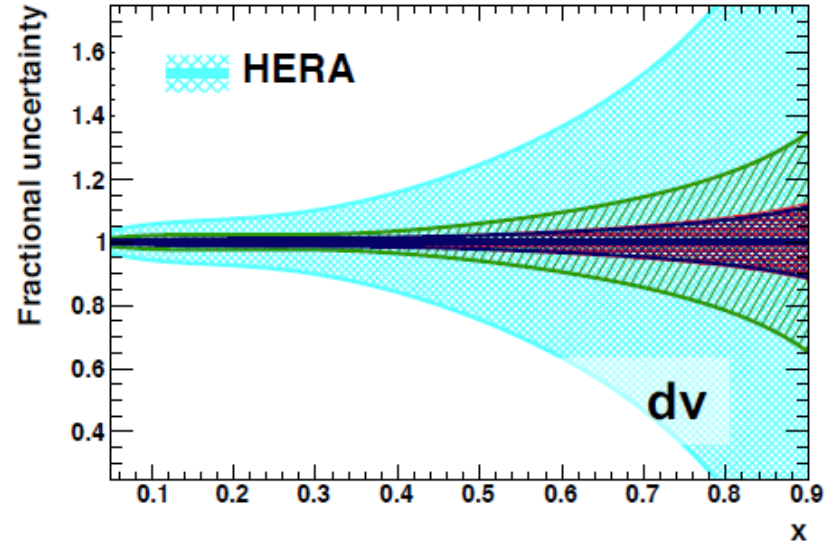
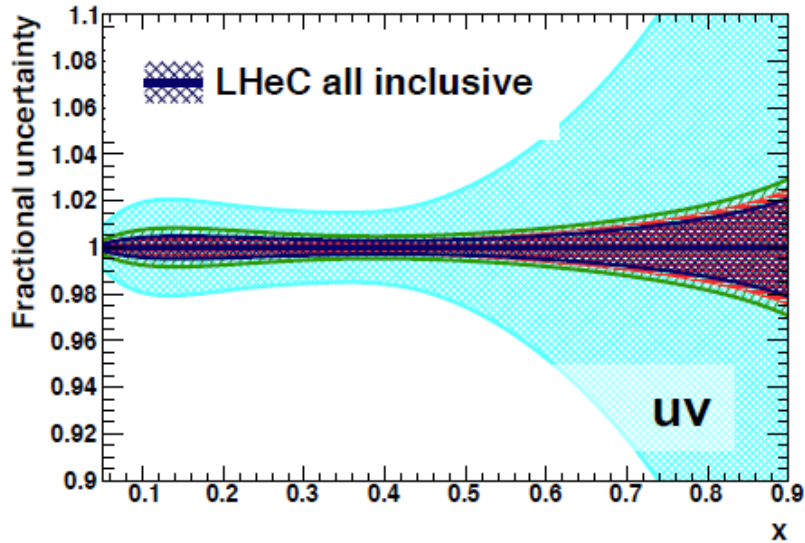
**small and medium  $x$**  quickly constrained (5 fb-1  $\equiv$   $\times 5$  HERA  $\equiv$  1 year LHeC)

# Impact of positrons on PDFs



**CC:**  $e^+$  sensitive to  $d$ ; **NC:**  $e^\pm$  asymmetry gives  $xF_3^{\nu Z}$ , sensitive to valence

# Collider configurations



**FCC-eh (A):** new preliminary simulation with  $2 \text{ ab}^{-1}$  polarised  $e^-$  (NO  $e^+$  yet; impact especially in  $d$  at large  $x$ )

# And why do we want to improve high-x gluon and quarks?

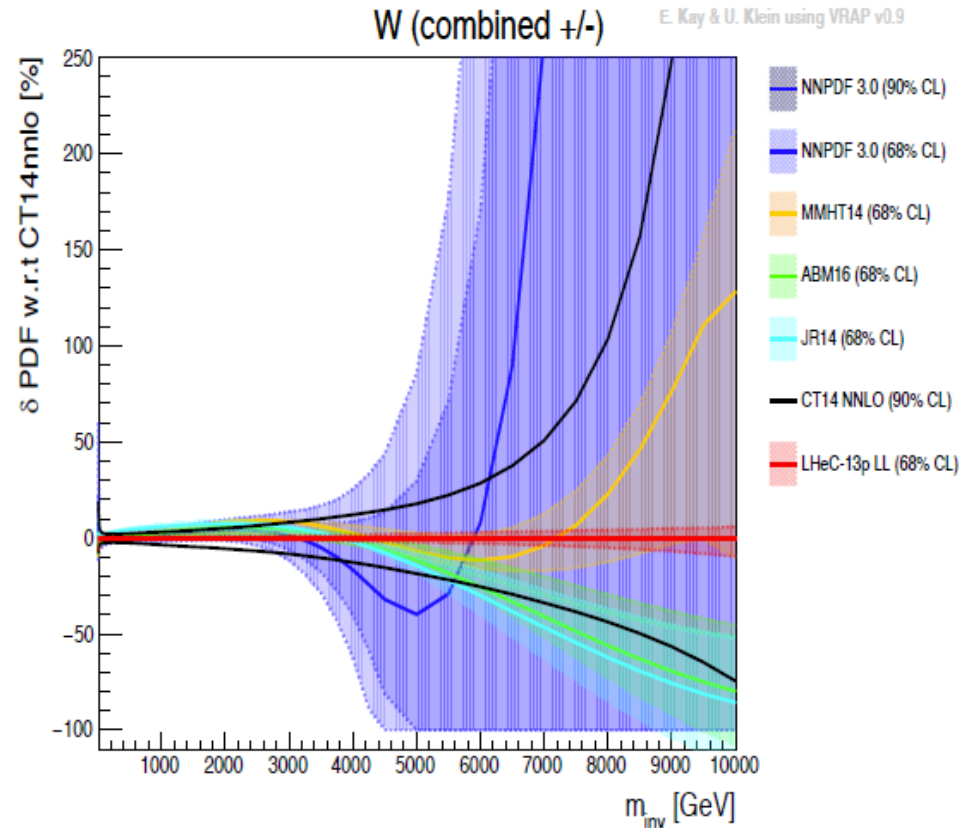
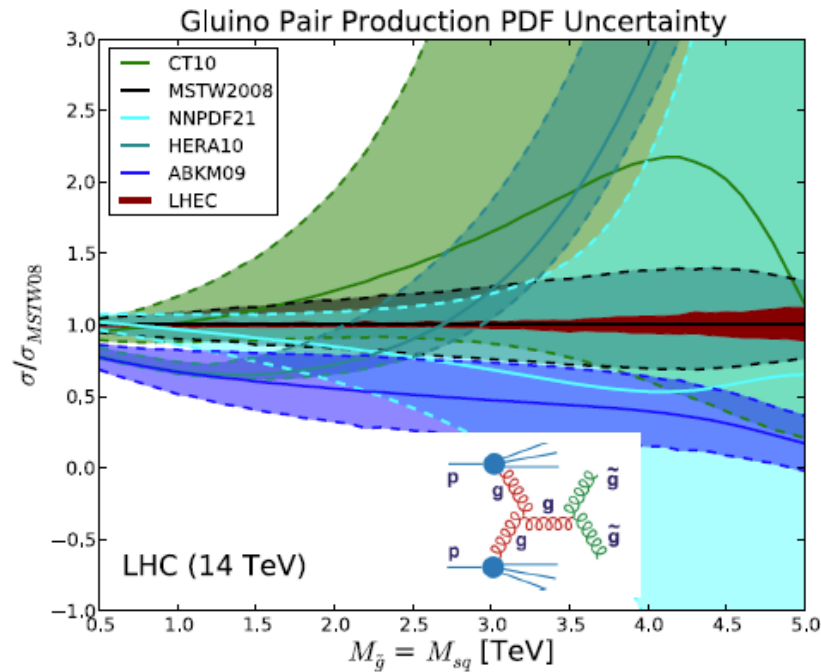
**external**, reliable **pdfs** needed for range extension and interpretation

**gluons**

SUSY (RPC, RPV), LQs, ...

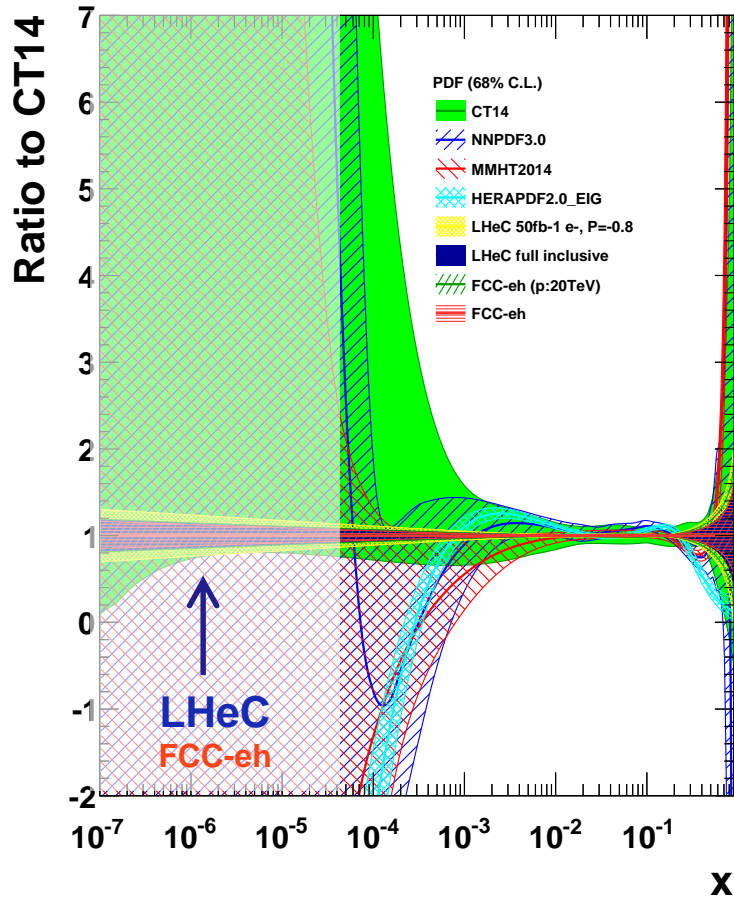
**quarks**

exotic and extra boson searches at high mass



# Gluon at small x

gluon distribution at  $Q^2 = 1.9 \text{ GeV}^2$



no current data much below  $x=5 \times 10^{-5}$

**LHeC** provides single, precise and unambiguous dataset down to  $x=10^{-6}$

**FCC-eh** probes to even smaller  $x=10^{-7}$

explore low x QCD:

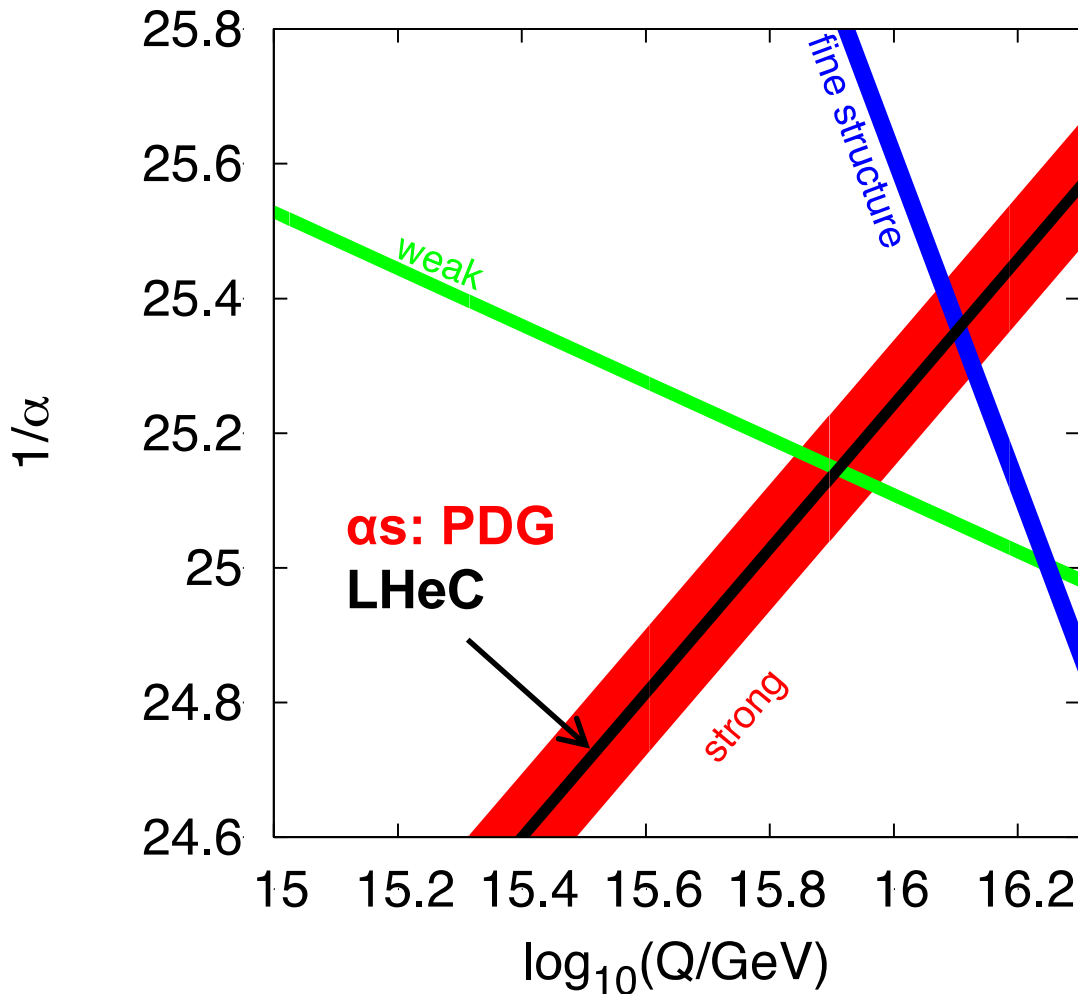
DGLAP vs BFKL; non-linear evolution;

gluon saturation; implications

for ultra high energy neutrino cross sections



# strong coupling, $\alpha_s$ (MZ)



**$\alpha_s$  is least known  
coupling constant**

**PDG2018:**

**$\alpha_s = 0.1174 \pm 0.0016$**   
(w/o lattice QCD, 1.5% uncertainty)

**precise  $\alpha_s$  needed:**  
to constrain GUT  
scenarios; for cross  
section predictions,  
including Higgs; ...

**LHeC:** permille  
precision possible in  
**combined QCD fit for  
pdfs+ $\alpha_s$**

# Summary

**Precision determination of quark and gluon structure of proton and  $\alpha_s$**  of fundamental importance for future hadron collider physics programme (Higgs, BSM, ...)

**Deep inelastic scattering e-p colliders essential for full exploitation**

**External precision pdf input**; complete q,g unfolding, high luminosity  $x \rightarrow 1$ , s, c, b, (t); N3LO; small x; strong coupling to permille precision; ...

**NEW pdf studies presented (all work in progress)**

All critical pdf information can be obtained early with LHeC ( $\sim 50 \text{ fb}^{-1} \equiv \times 50 \text{ HERA}$ ), in parallel with HL-LHC operation studies for potential new collider configurations underway

**LHeC, PERLE and FCC documents submitted to european strategy update**

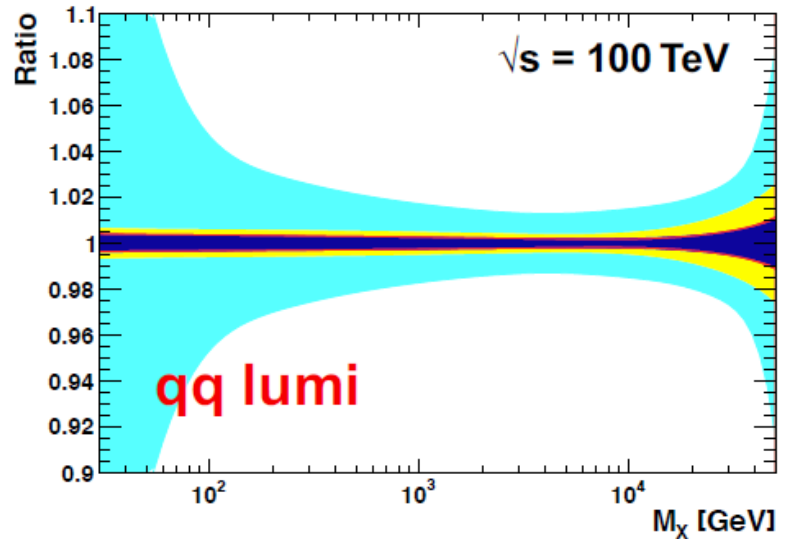
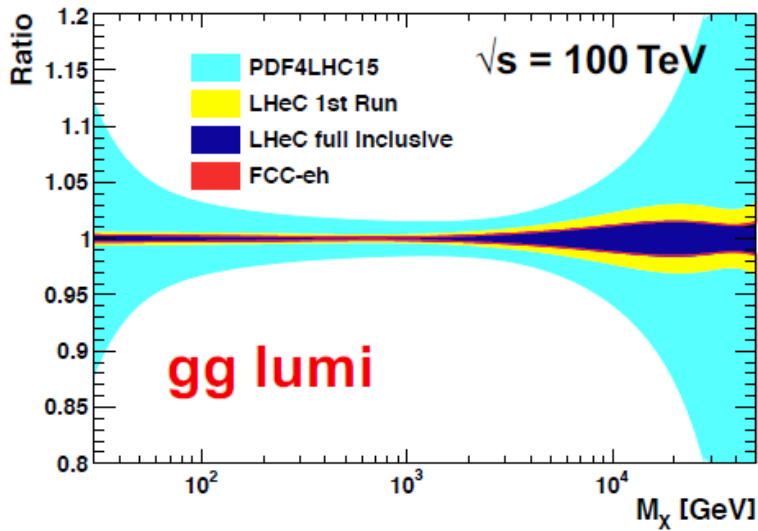
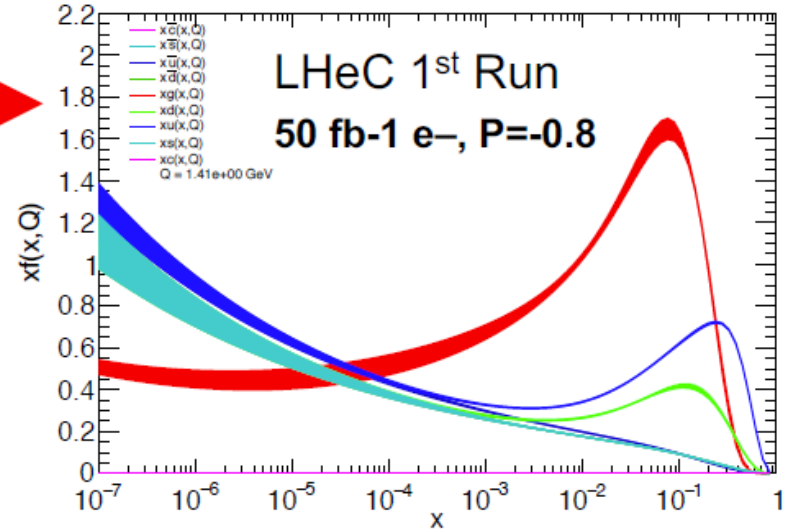
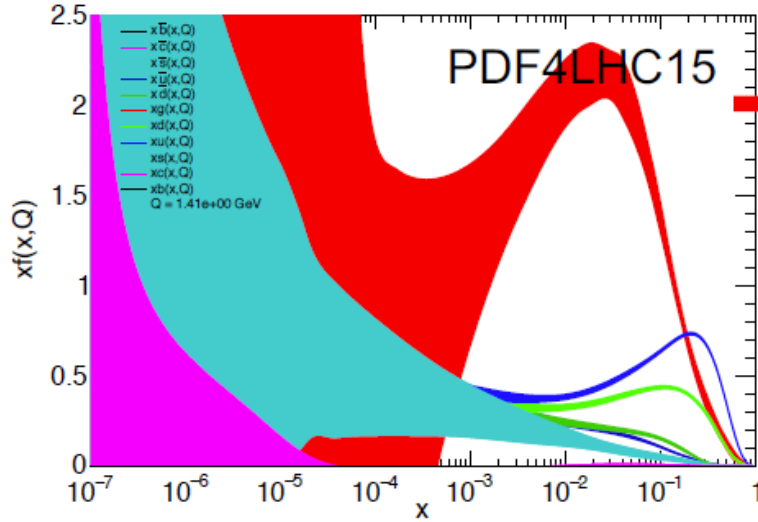
**Next steps:** ongoing parallel and complementary studies EG. arXiv:1906.10127; major new summary paper later this year; workshop in the autumn, 24 – 25 Oct 2019



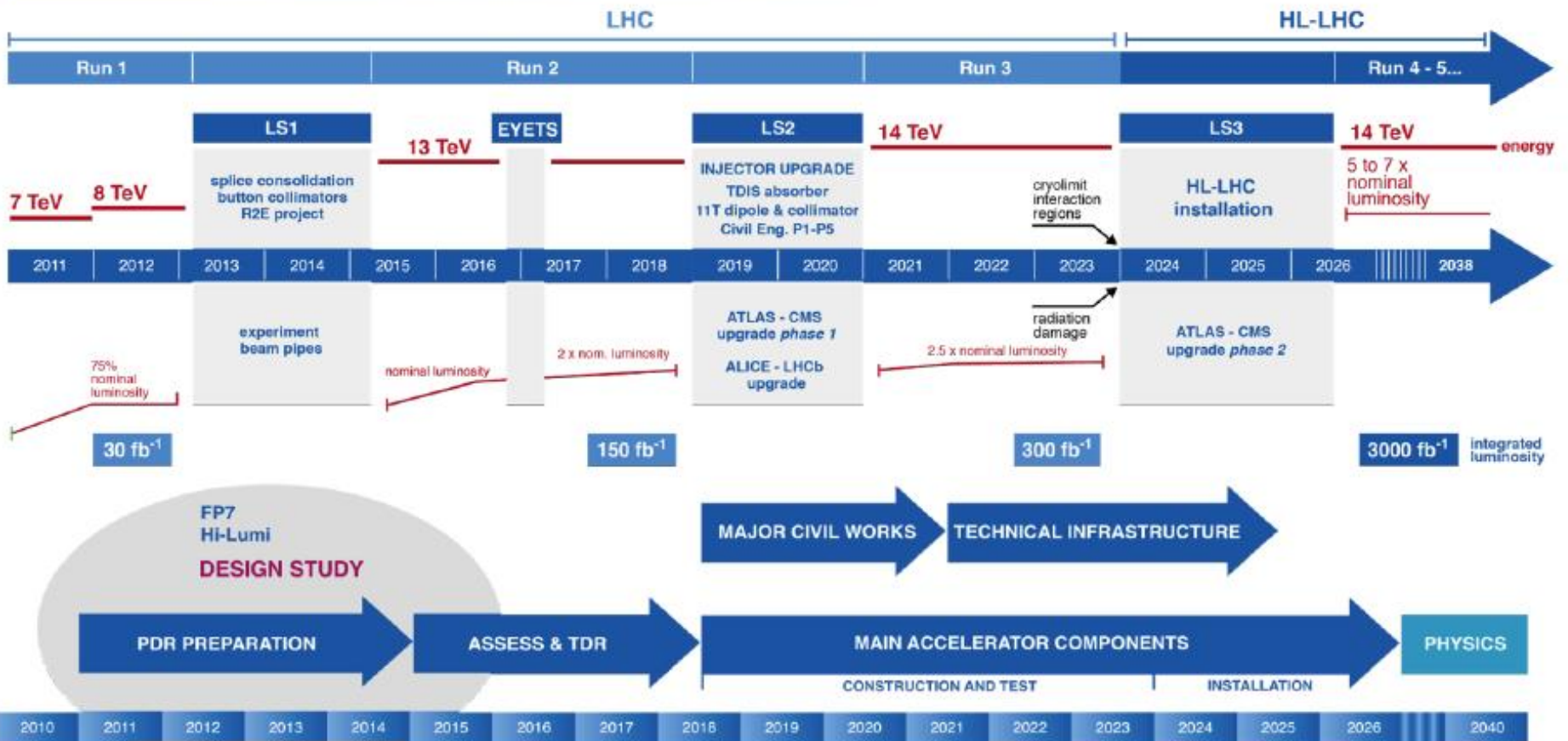


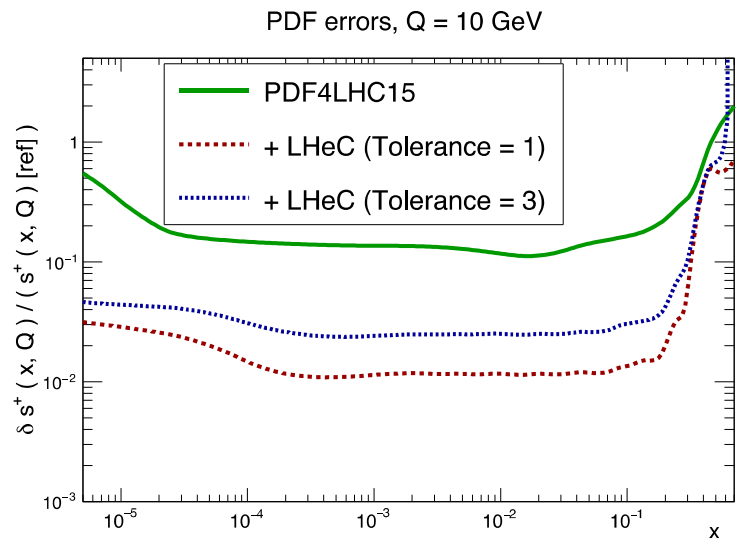
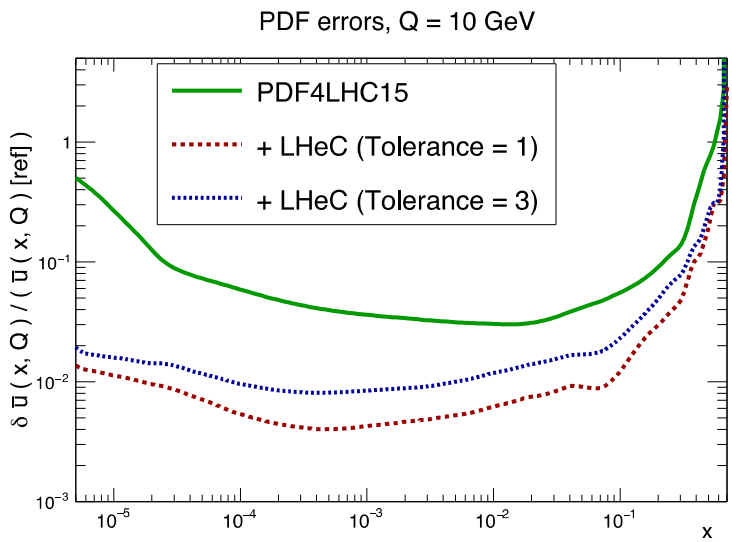
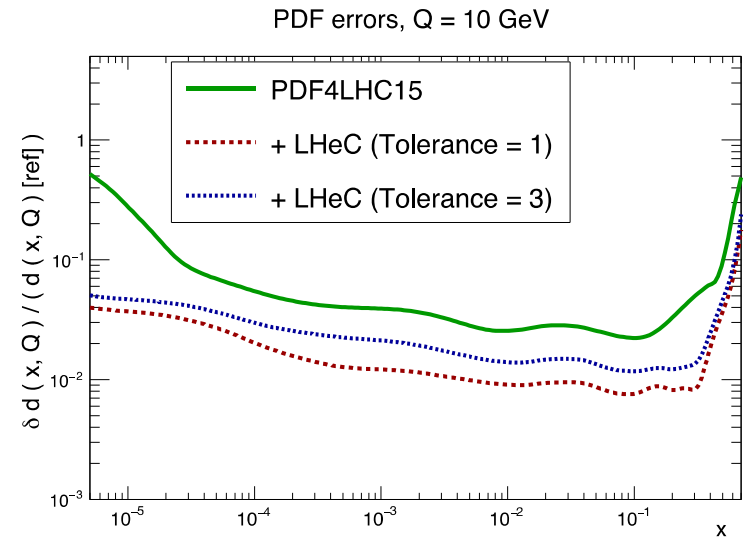
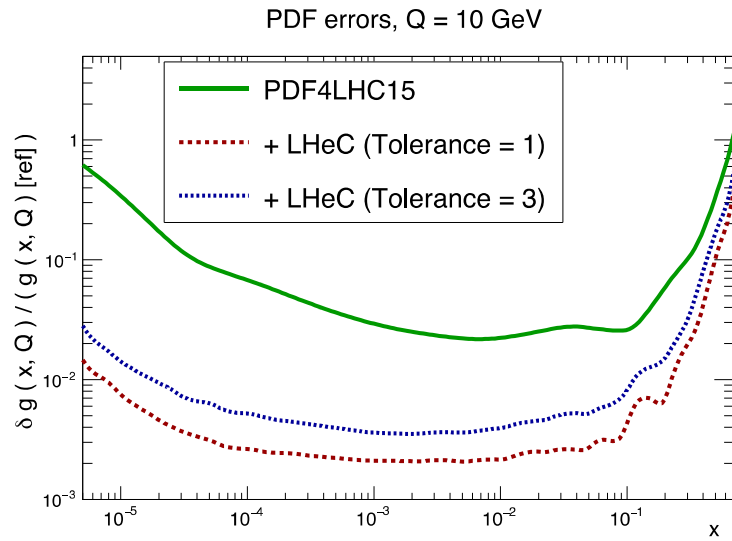
extras

# summary of pdfs



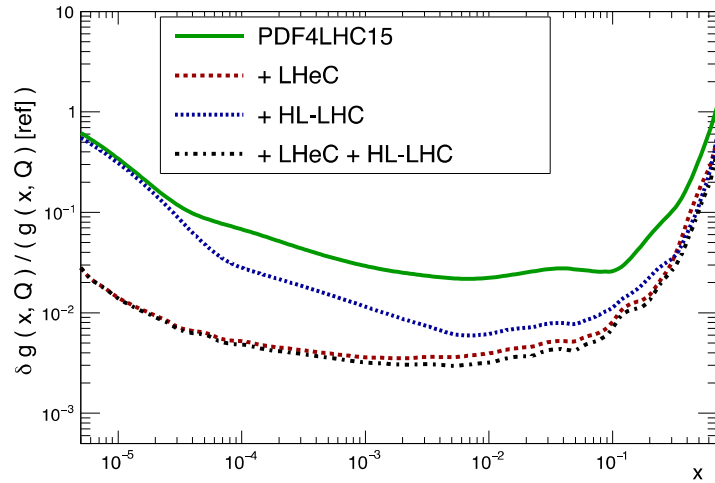
# LHC / HL-LHC Plan



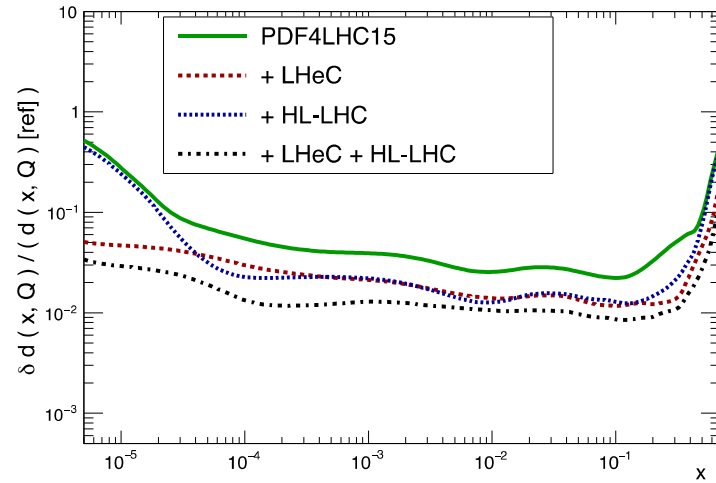


PDF4LHC15 profiled with (previous iteration of) LHeC inclusive+HQ simulated data

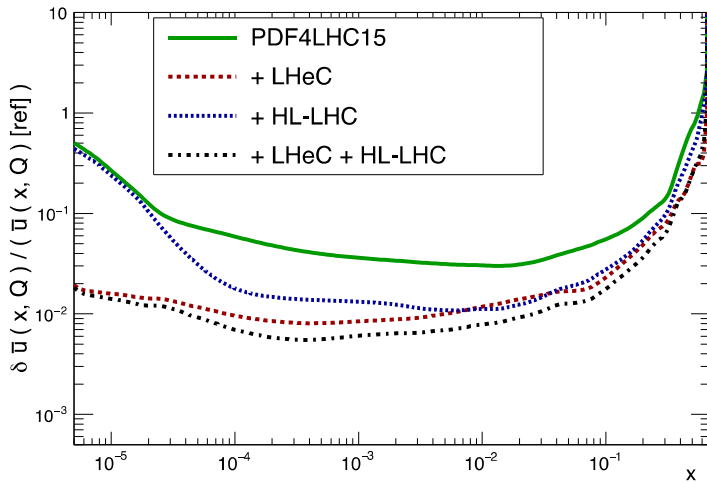
PDFs at the HL-LHC ( Q = 10 GeV )



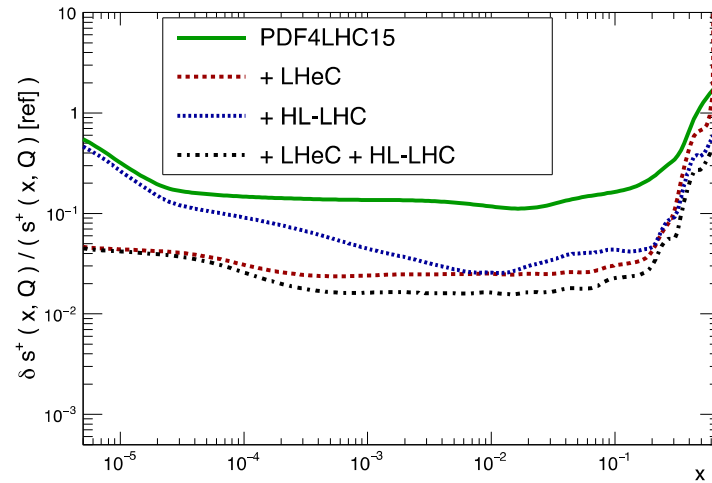
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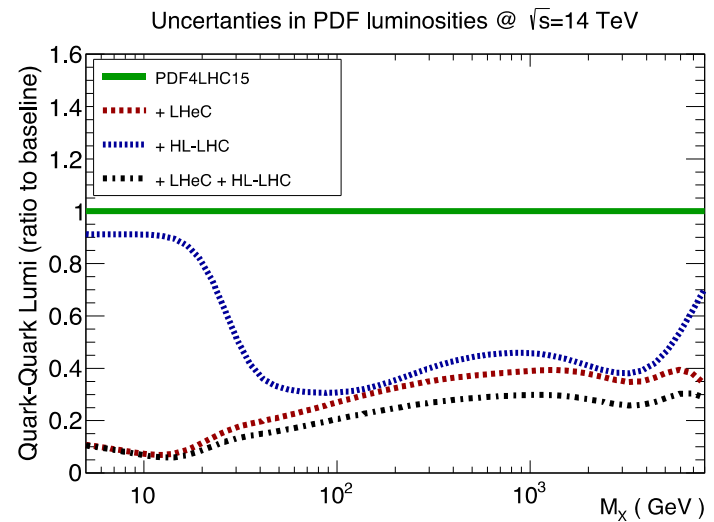
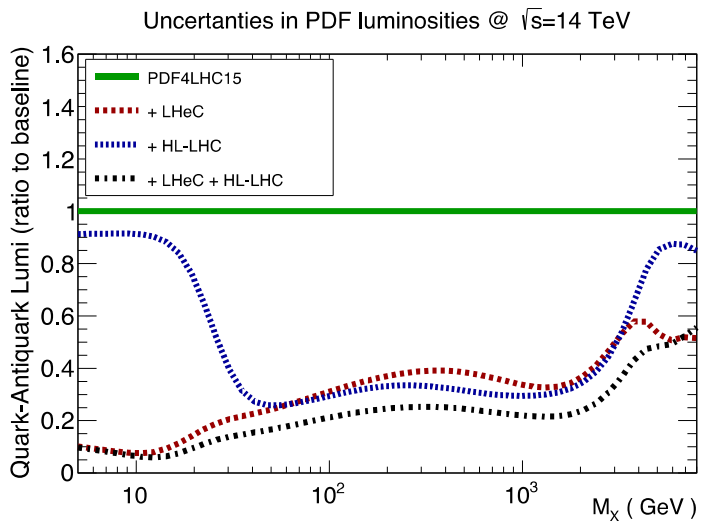
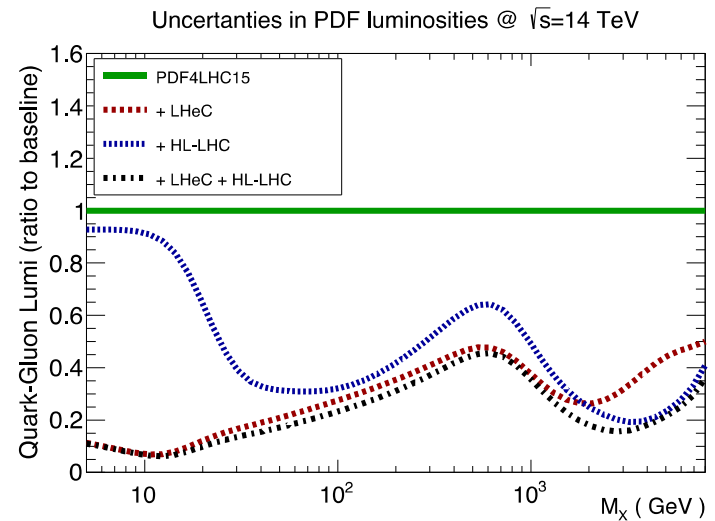
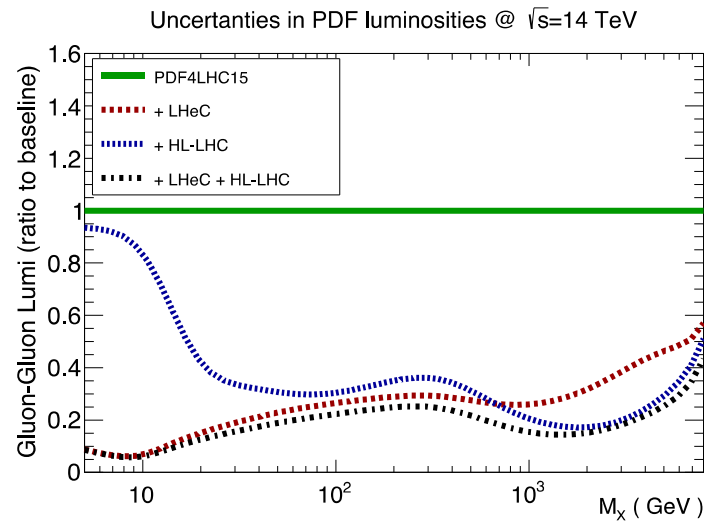


PDFs at the HL-LHC ( Q = 10 GeV )

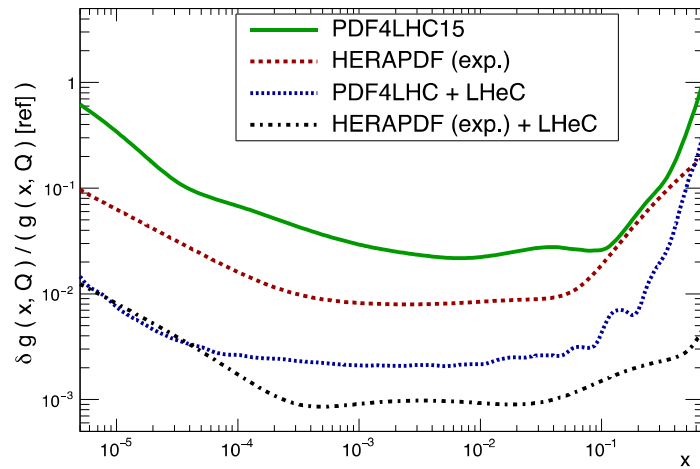
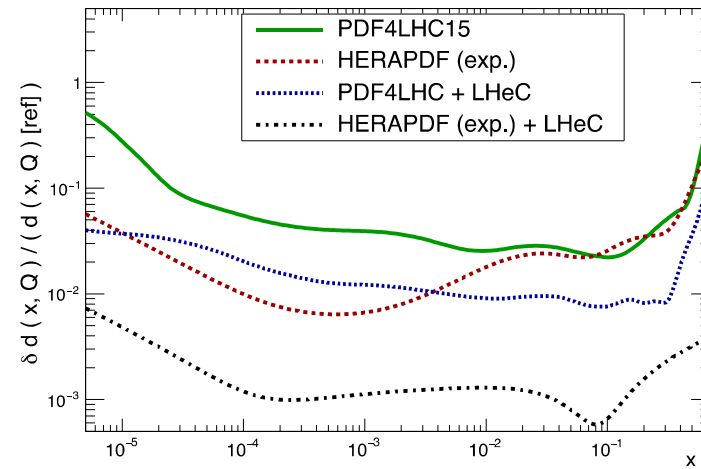
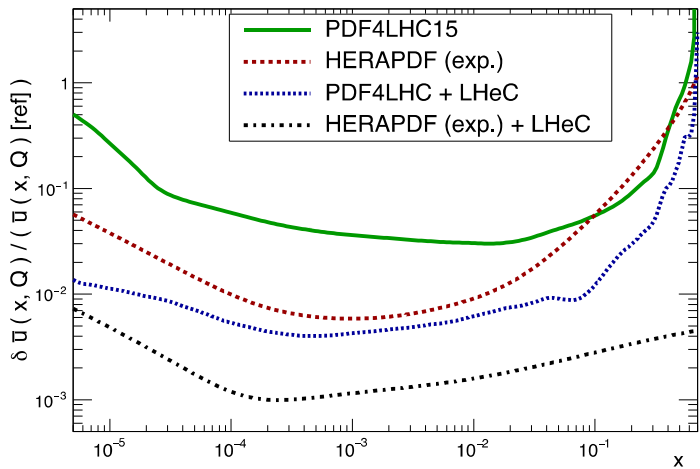
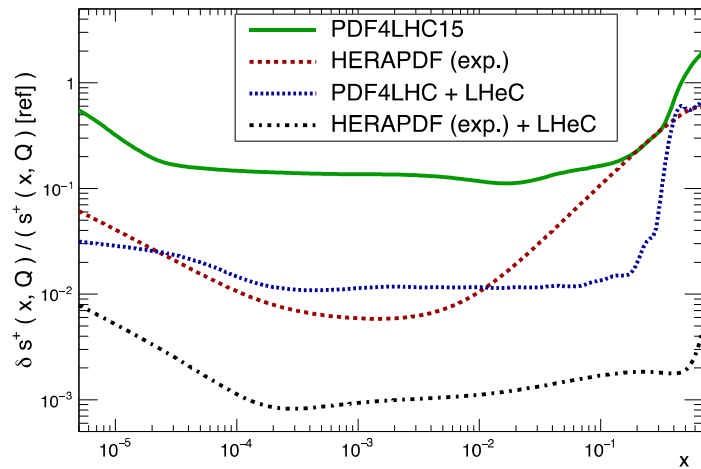


PDFs at the HL-LHC ( Q = 10 GeV )

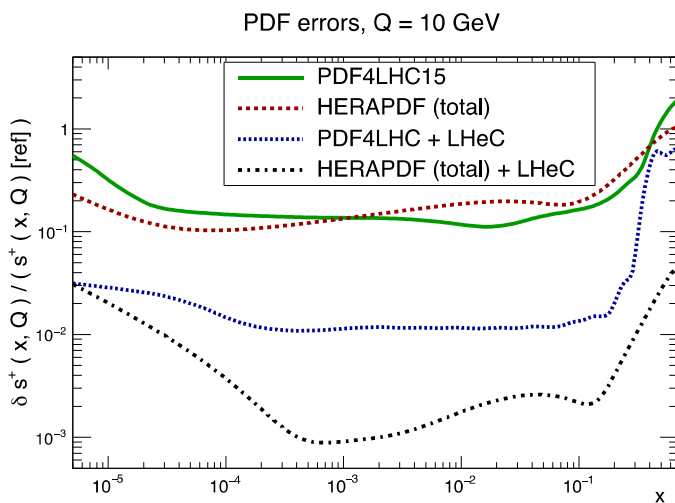
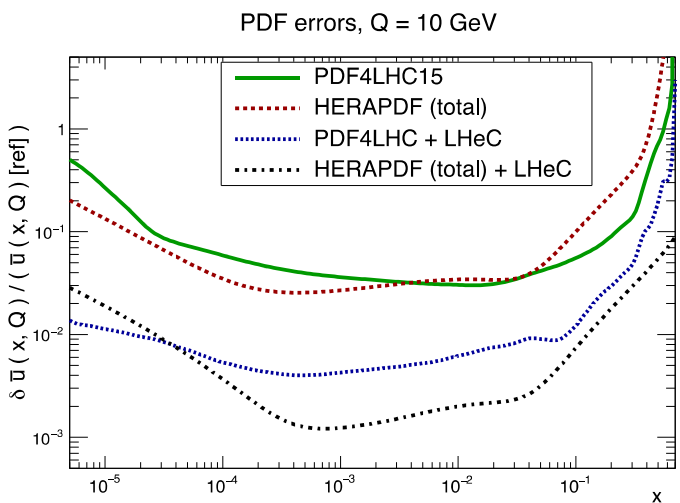
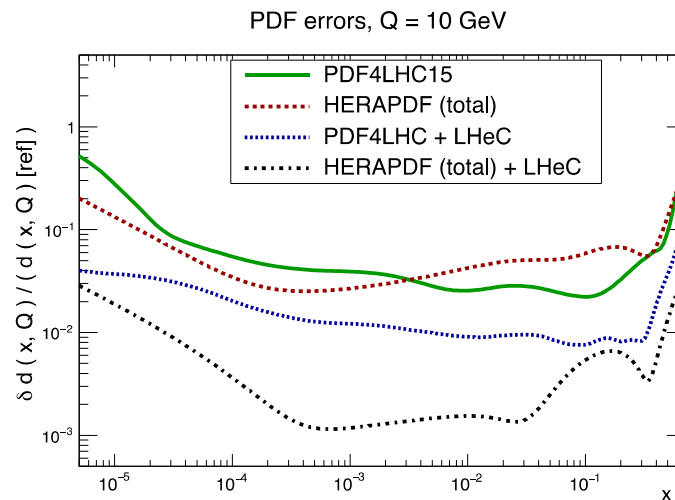
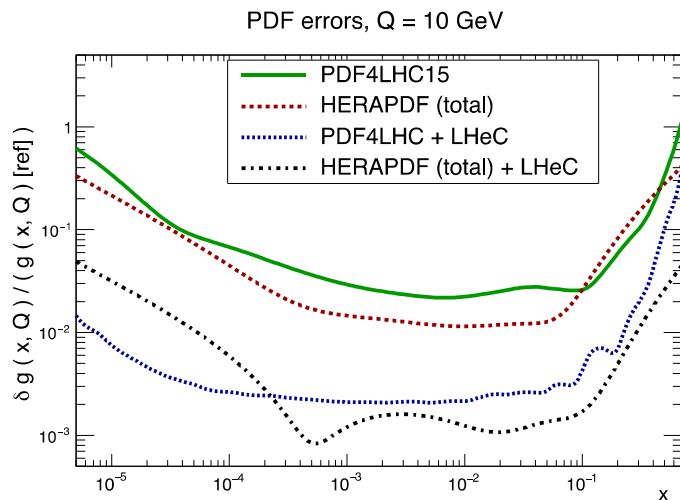




PDF4LHC15 profiled with LHeC inclusive+HQ and HL-LHC simulated data

PDF errors,  $Q = 10$  GeVPDF errors,  $Q = 10$  GeVPDF errors,  $Q = 10$  GeVPDF errors,  $Q = 10$  GeV

PDF4LHC15 and HERAPDF profiled with LHeC inclusive+HQ simulated data



PDF4LHC15 and HERAPDF (total uncersts) profiled with LHeC inclusive+HQ simulated data



# QCD fit parameterisation

## QCD fit ansatz based on HERAPDF2.0, with following differences

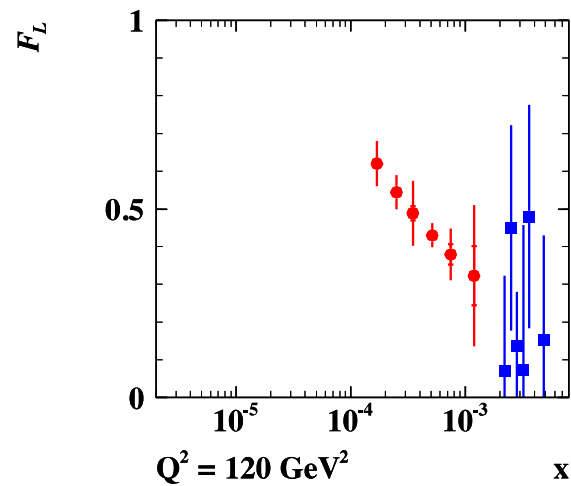
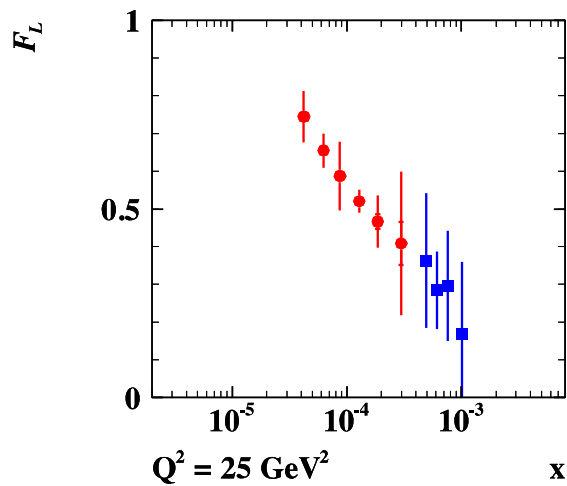
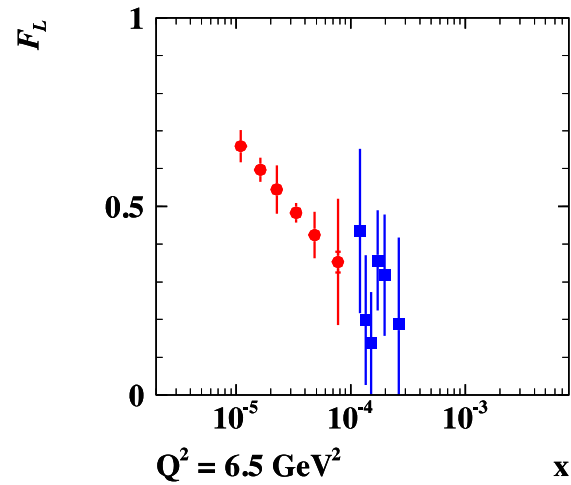
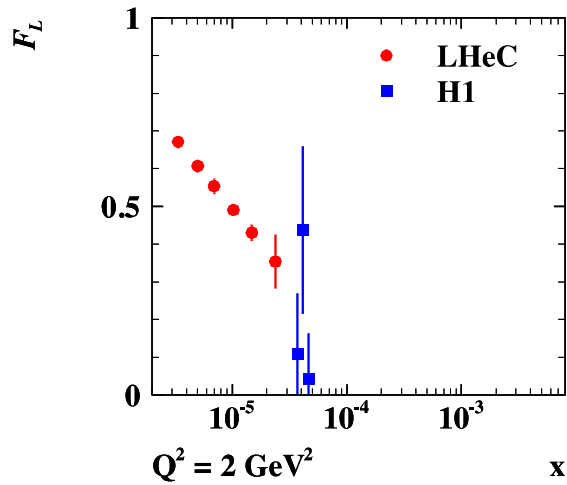
much more relaxed sea ie. no requirement that  $\bar{u}=\bar{d}$  at small  $x$   
no negative gluon term (simply for the aesthetics of ratio plots – it has been checked that this does not impact size of projected uncertainties)

$$\begin{aligned}xg(x) &= A_g x^{B_g} (1-x)^{C_g} (1 + D_g x) \\xu_v(x) &= A_{u_v} x^{B_{u_v}} (1-x)^{C_{u_v}} (1 + E_{u_v} x^2) \\xd_v(x) &= A_{d_v} x^{B_{d_v}} (1-x)^{C_{d_v}} \\x\bar{U}(x) &= A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}} \\x\bar{D}(x) &= A_{\bar{D}} x^{B_{\bar{D}}} (1-x)^{C_{\bar{D}}}\end{aligned}$$

**4+1 pdf fit (above) has 14 free parameters**

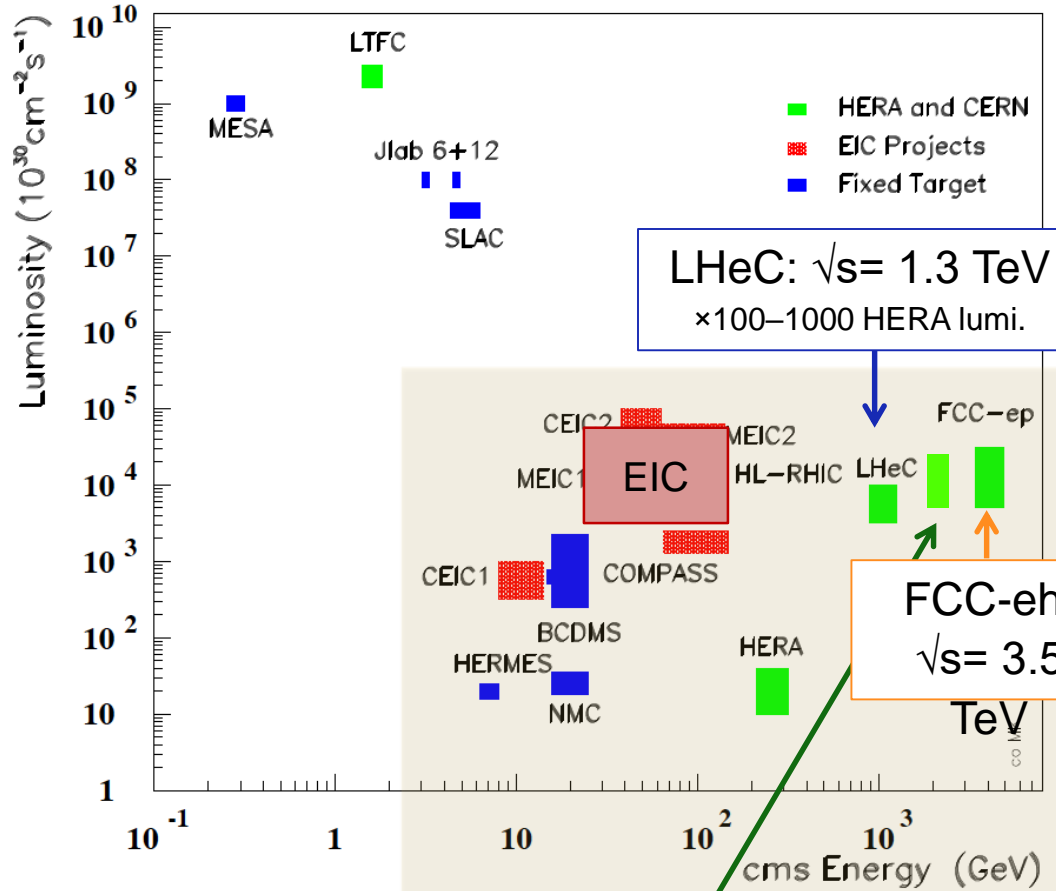
**5+1 pdf fit for HQ studies parameterises  $\bar{d}$  and  $\bar{s}$  separately, and has 17 free parameters**

# FL at LHeC



# ep colliders

Lepton-Proton Scattering Facilities

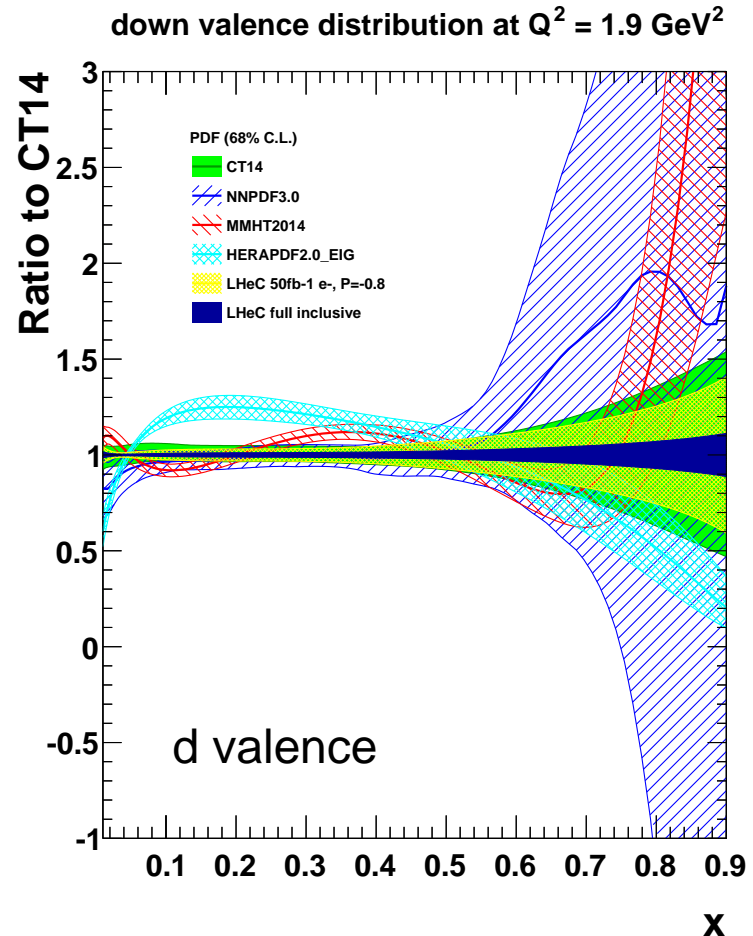
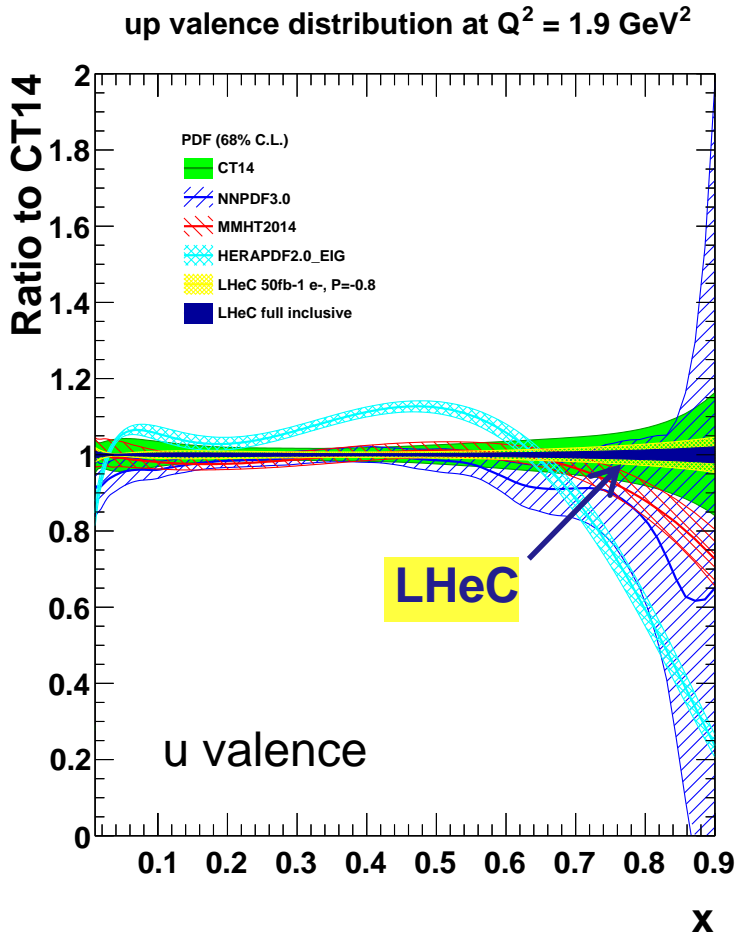


**HERA:** world's first and still only ep collider ( $\sqrt{s} \approx 300 \text{ GeV}$ )

**LHeC:** future ep (eA) collider, proposed to run concurrently with HL/HE-LHC; CDR arXiv:1206.2913 (complementary to LHC; extra discovery channels; Higgs; precision pdfs and  $\alpha_s$ )

**FCC-eh:** further future ep (eA) collider, integrated with FCC; CDR, volume 1, EPJ C79 (2019) no.6, 474 (further kinematic extension wrt **LHeC**)

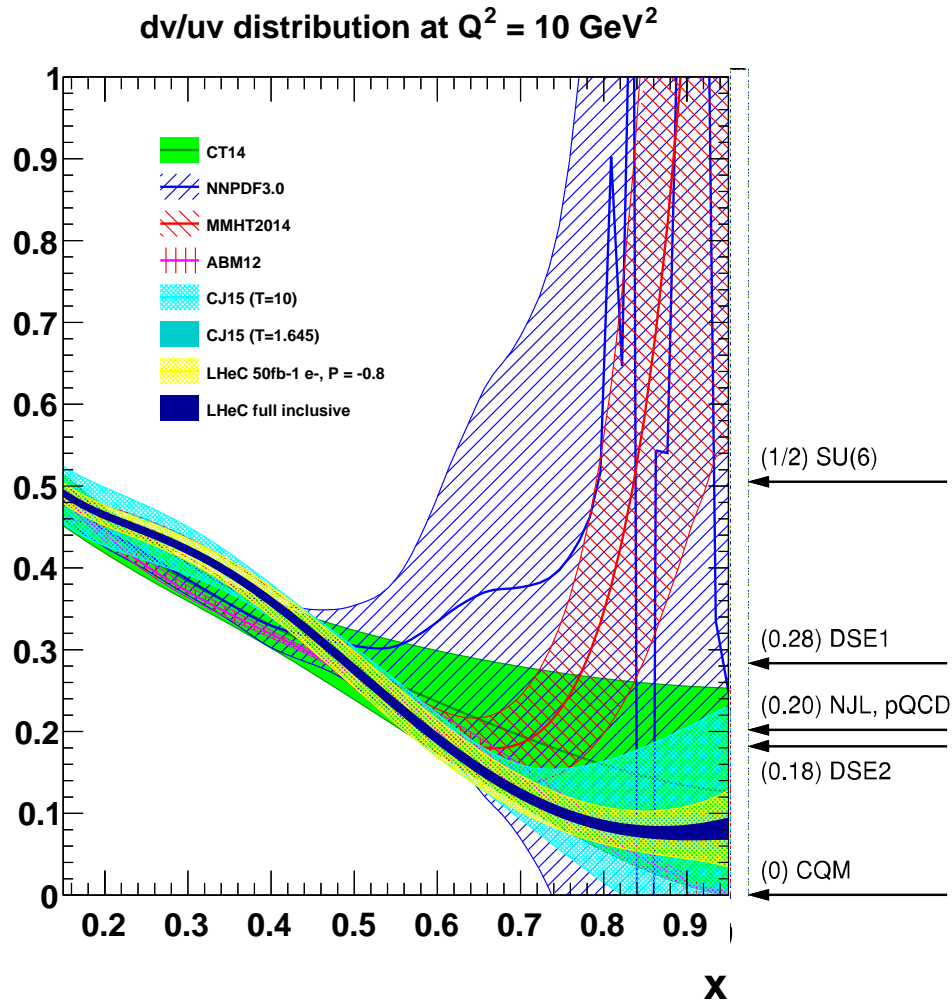
# valence quarks from LHeC



precision determination, free from higher twist corrections and nuclear uncertainties

**large x crucial for HL/HE-LHC and FCC searches;** also relevant for DY, MW etc.

# d/u at large x



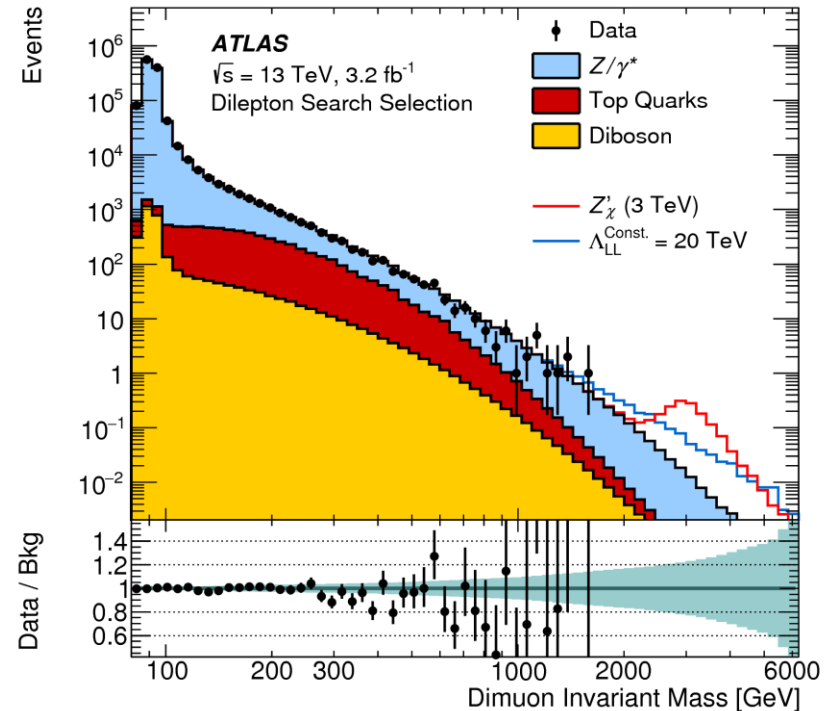
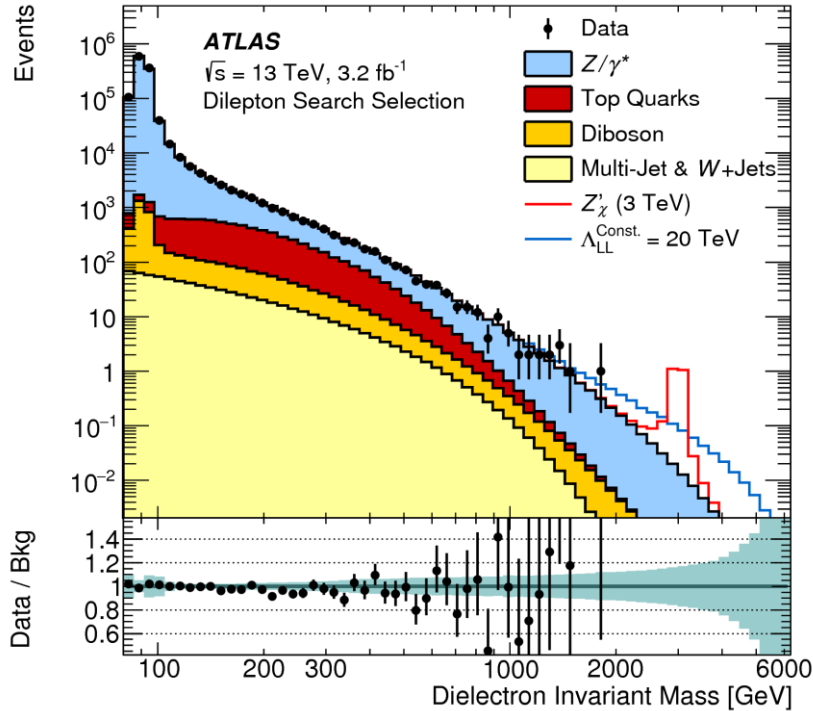
**d/u essentially unknown at large x**

no predictive power from current pdfs;  
conflicting theory pictures;  
data inconclusive, large nuclear  
uncerts.

**resolve long-standing mystery  
of d/u ratio at large x**

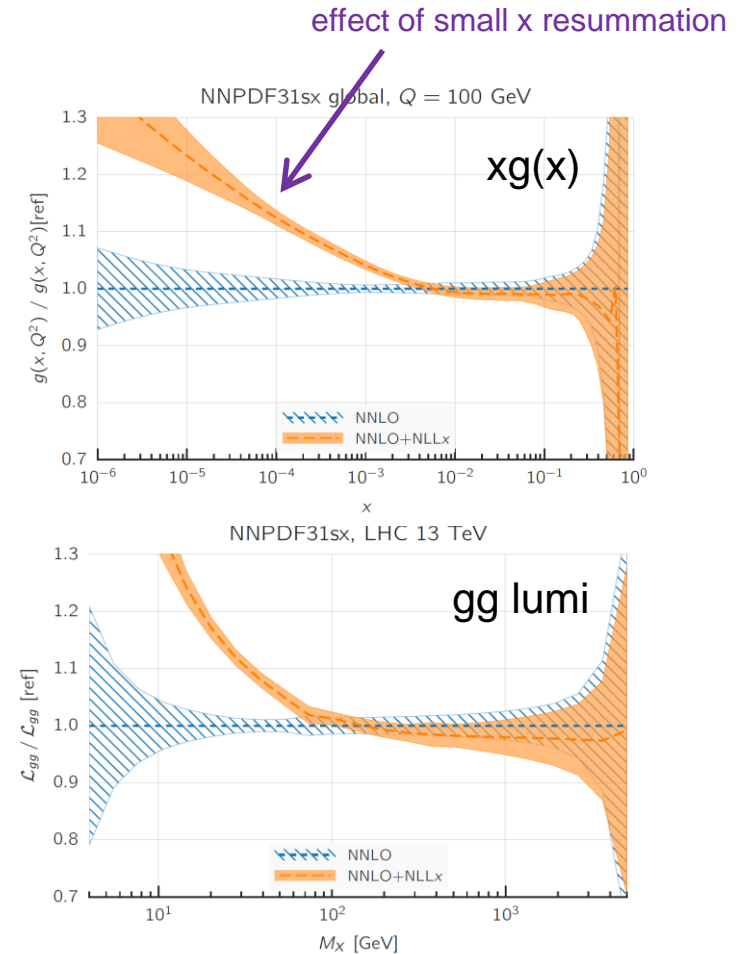
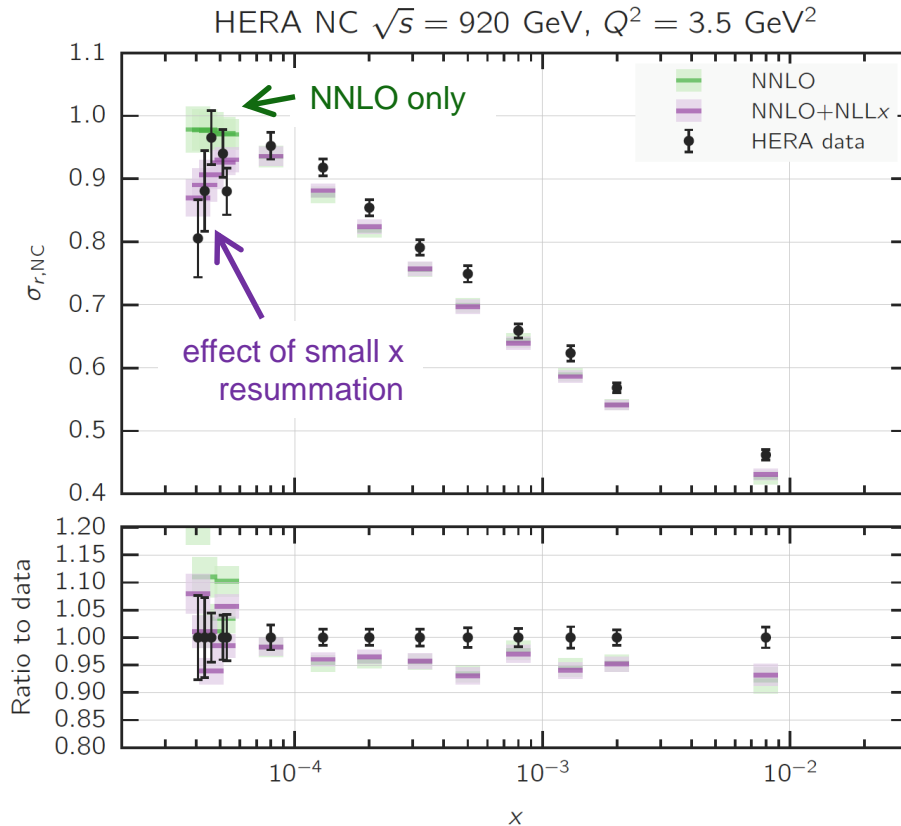
# Why are we interested in the high-x sea?-one example

Current BSM searches in High Mass Drell-Yan are limited by high-x antiquark uncertainties as well as by high-x valence uncertainties



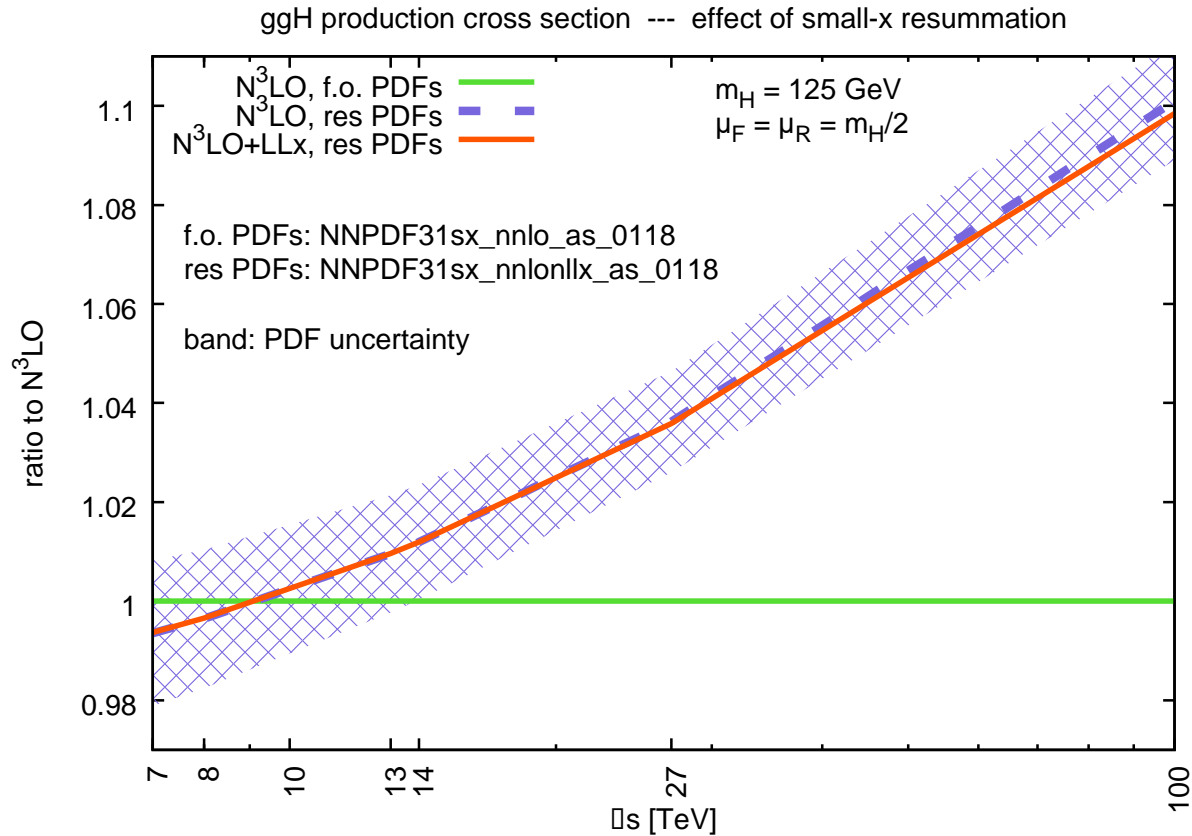
# gluon at small x

R. Ball et al, arXiv:1710.05935



- recent evidence for onset of BFKL dynamics in HERA inclusive data
- impact for LHC and most certainly at ultra low  $x$  values probed at FCC**

# gluon at small x matters

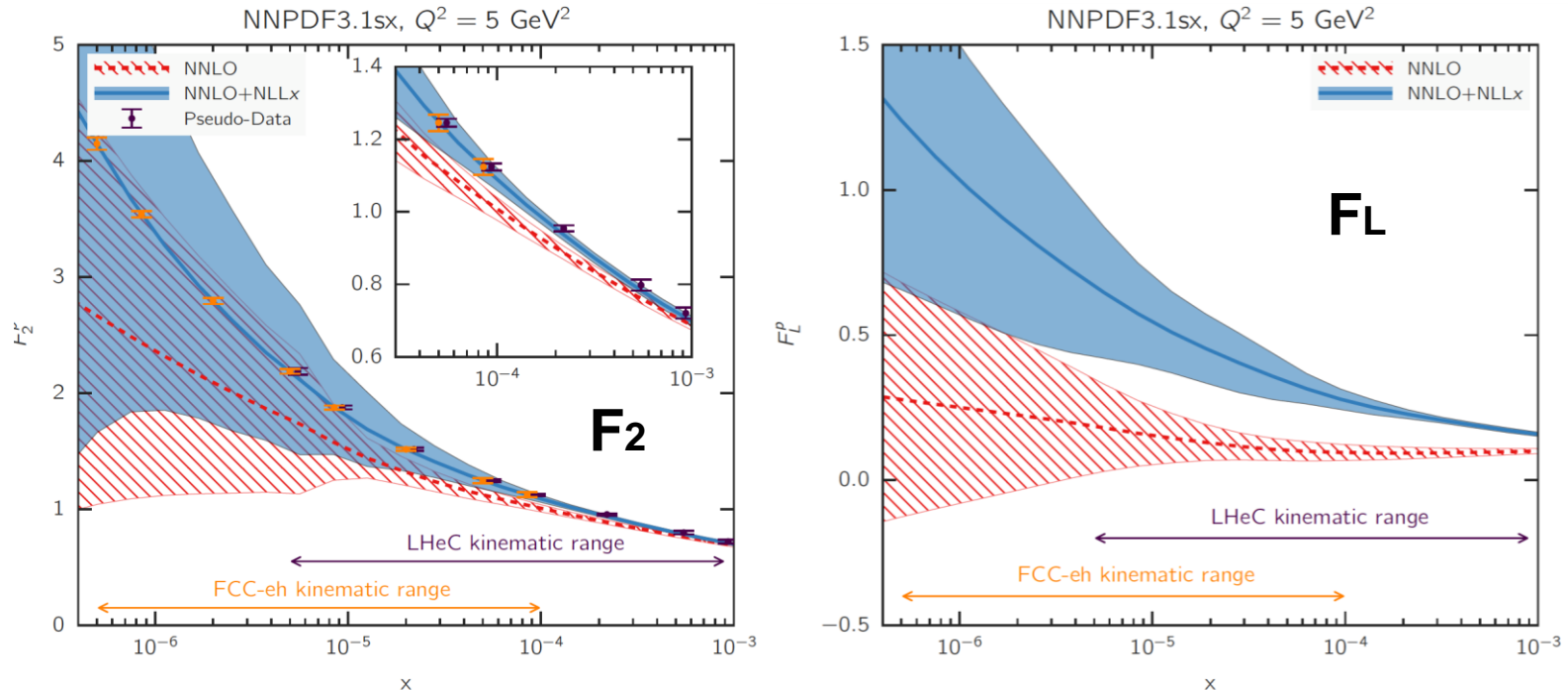


effect of small x resummation on ggH cross section for LHC, HE-LHC, FCC  
impact on other EW observables could be of similar size



# gluon at small x

arXiv:1710.05935



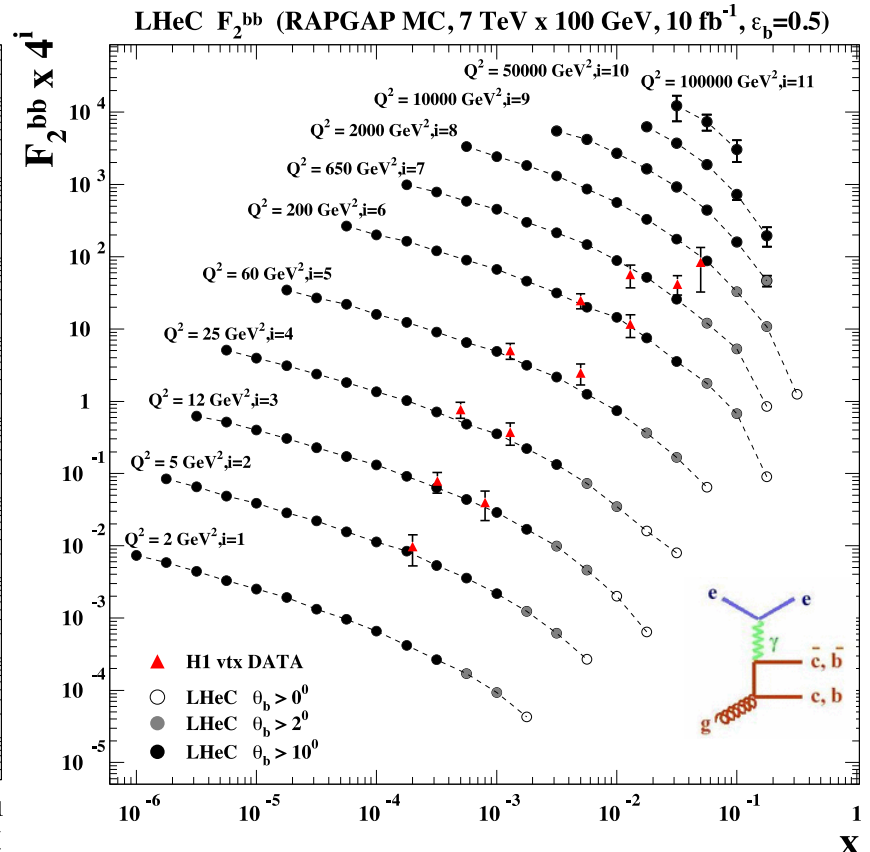
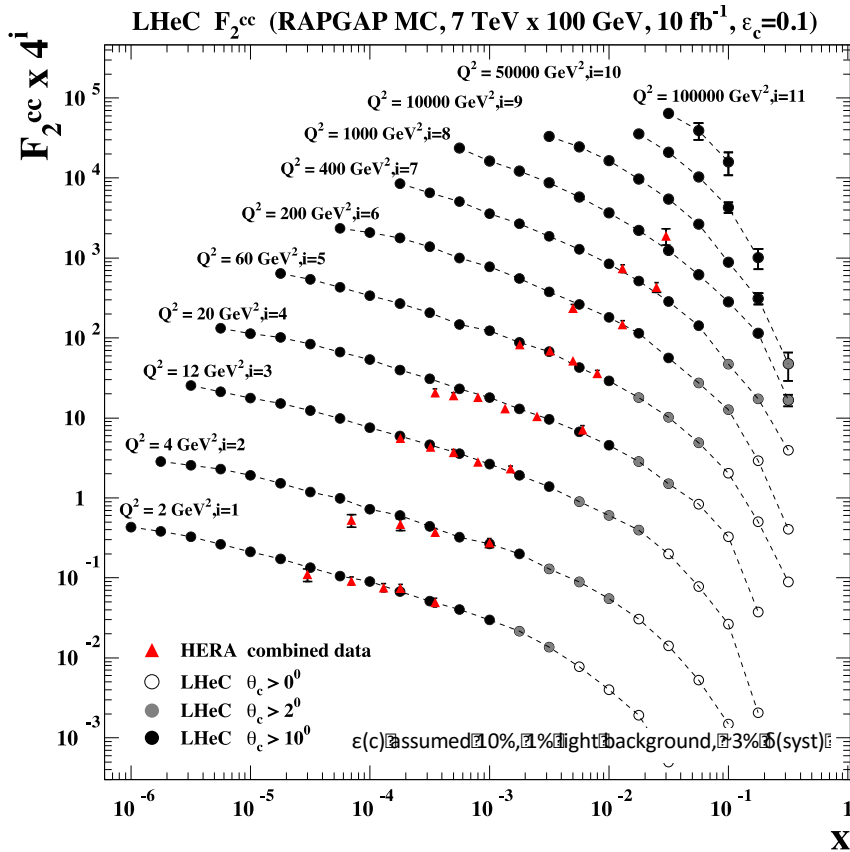
$F_2$  and  $F_L$  predictions for simulated kinematics of **LHeC** and **FCC-eh**

**ep simulated data very precise** – significant constraining power to discriminate between theoretical scenarios of small  $x$  dynamics

**measurement of  $F_L$  has a critical role to play**

see also M. Klein, arXiv:1802.04317

# c, b quarks

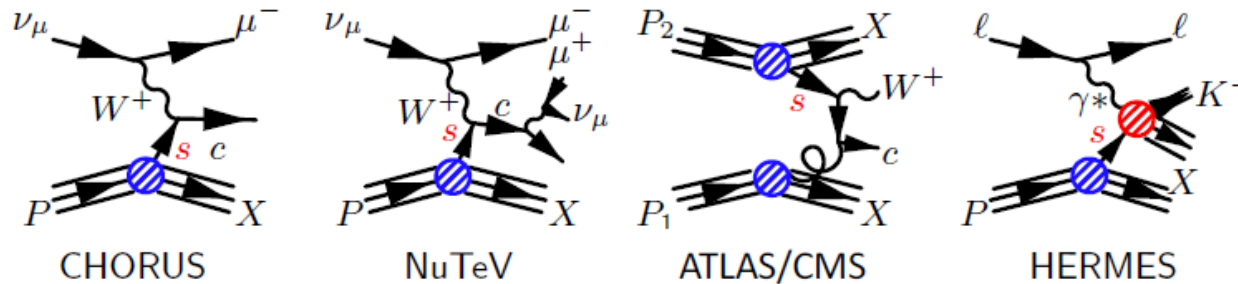


**LHeC: enormously extended range and much improved precision c.f. HERA**

- $\delta M_c = 50$  (HERA) to 3 MeV: impacts on  $\alpha_s$ , regulates ratio of charm to light, crucial for precision t, H
- $\delta M_b$  to 10 MeV; MSSM: Higgs produced dominantly via  $b\bar{b} \rightarrow A$

# strange

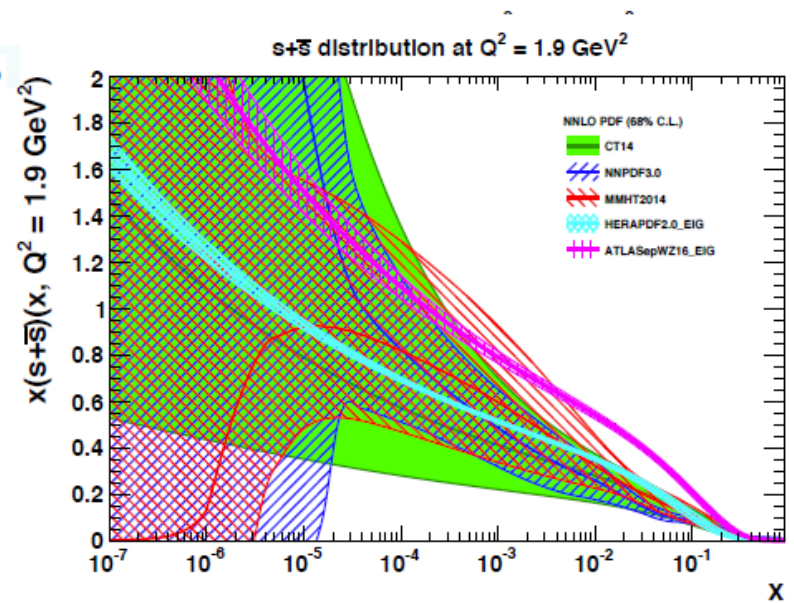
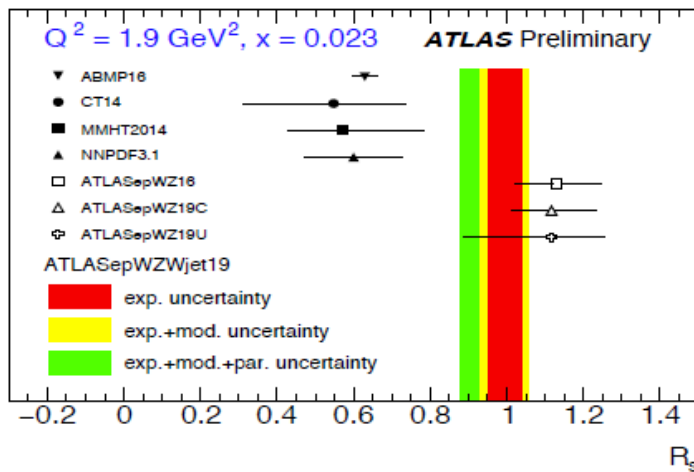
strange pdf poorly known; suppressed cf. other light quarks? strange valence?



EG.

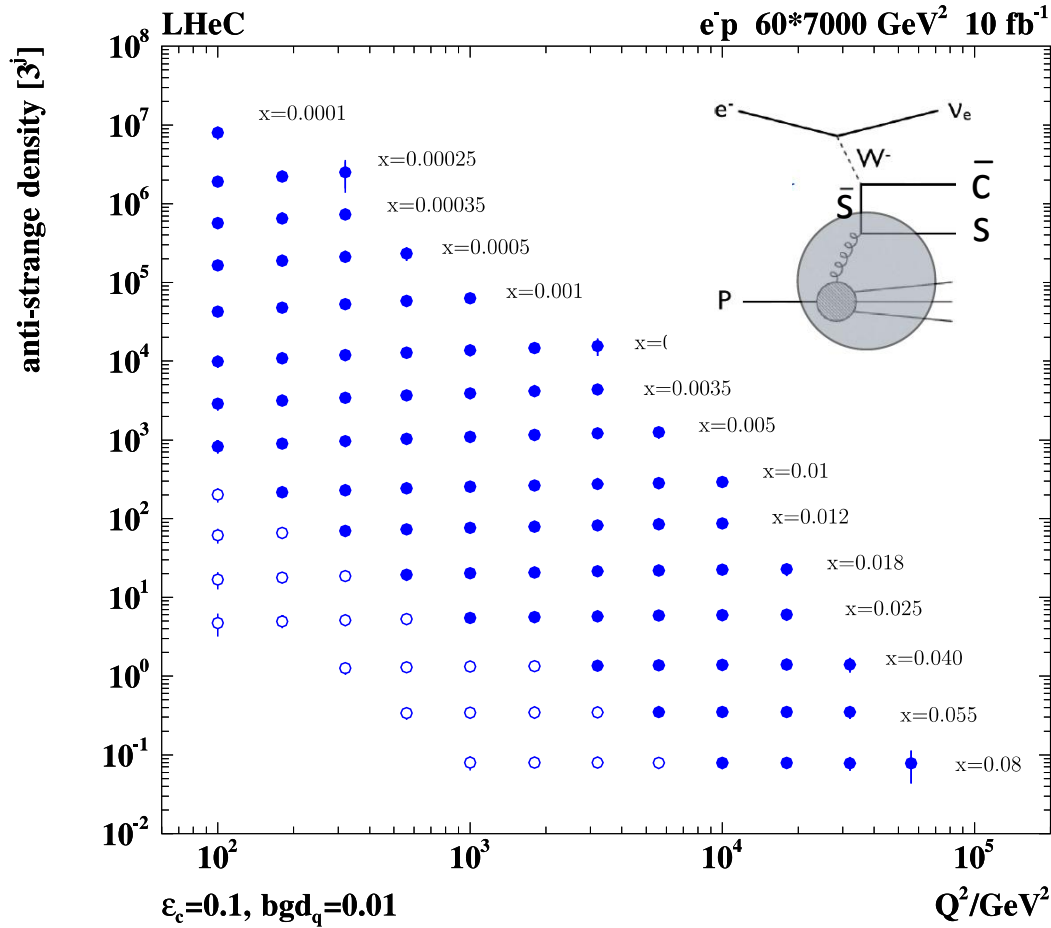
ATLAS<sup>†</sup> observe large strange fraction at mean Bjorken  $x$  around 0.01

$$R_s(x, Q^2) = \frac{s(x, Q^2) + \bar{s}(x, Q^2)}{\bar{u}(x, Q^2) + \bar{d}(x, Q^2)} \begin{cases} \approx 0.5 \text{ (from neutrino)} \\ \approx 1.0 \text{ (from ATLAS W,Z)} \end{cases}$$



<sup>†</sup>ATLAS arXiv:1203.4051, confirmed in 1612.03016, ATL-PHYS-PUB-2019-016; and by global fitters EG. 1706.00428, 1708.00047

# strange

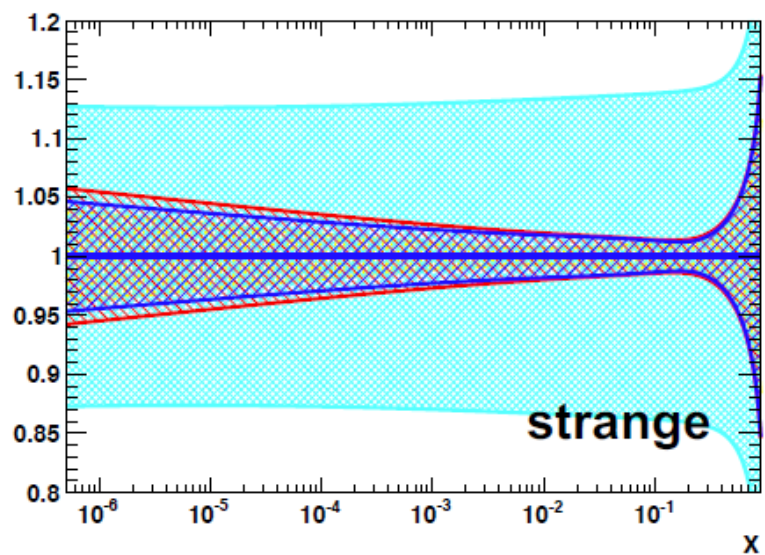
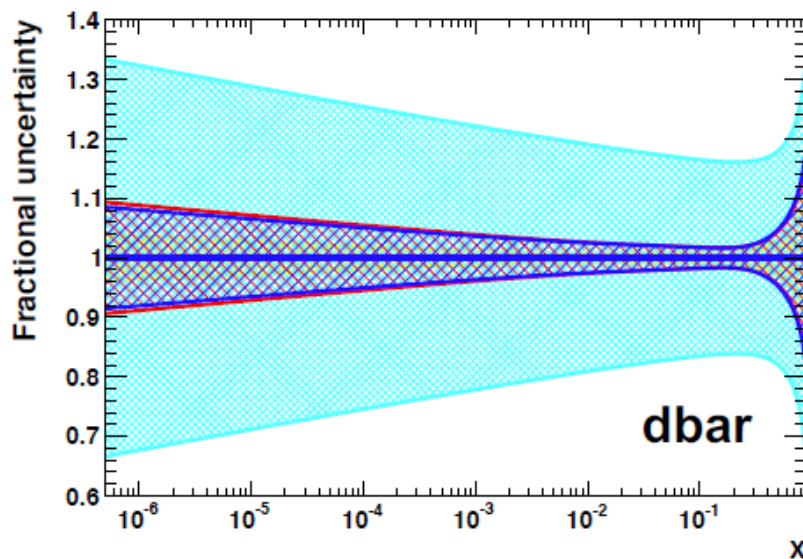
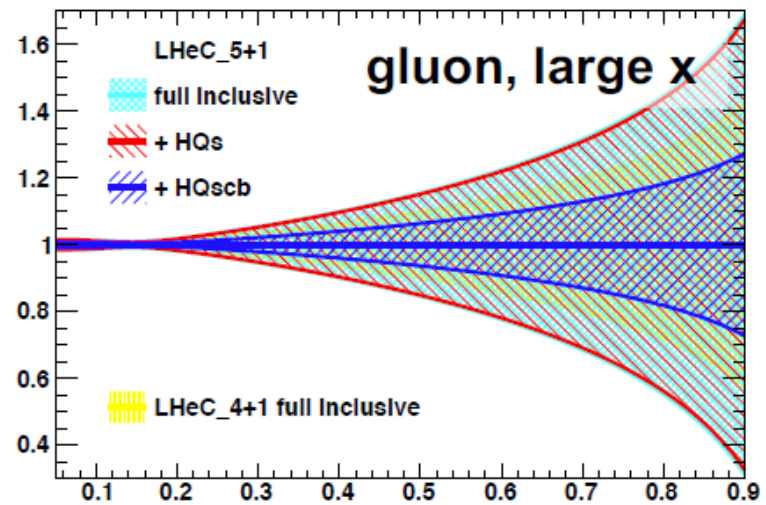
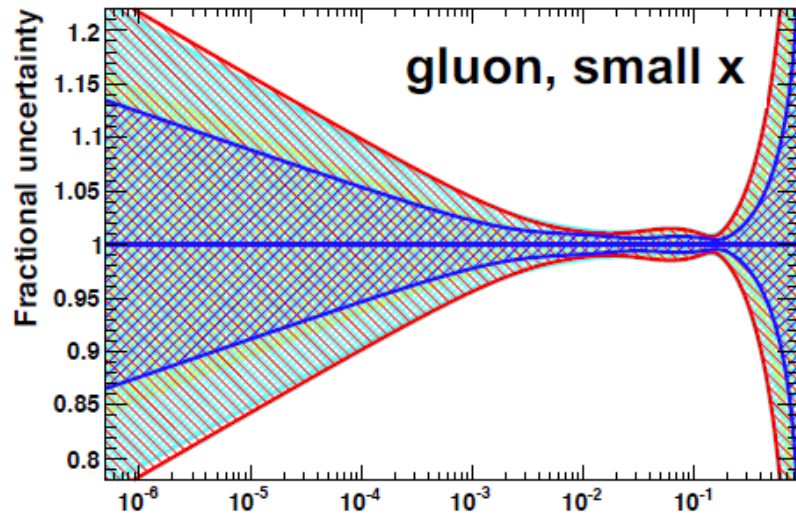


**LHeC:** direct sensitivity to **strange** via  $W+s \rightarrow c$   
 ( $x, Q^2$ ) mapping of (anti) strange for first time

**also top PDF**  
 top quark becomes light at large  $Q^2$ :  
 new field of research opens for top PDFs!

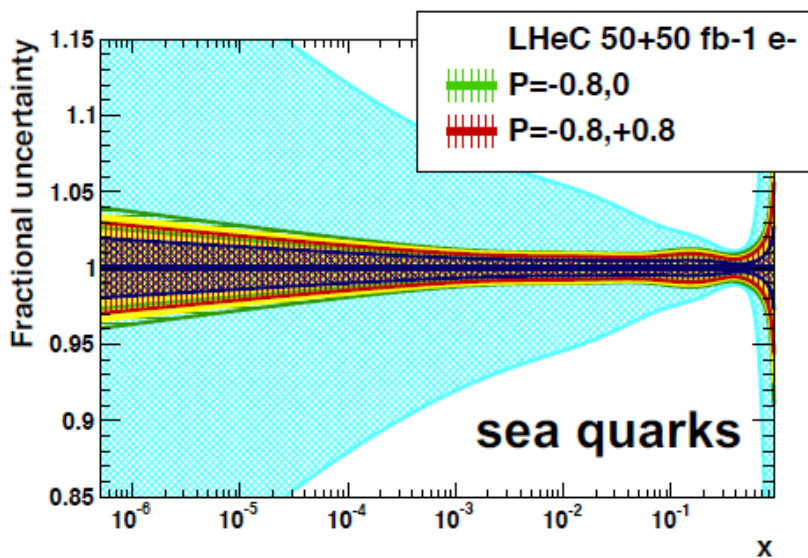
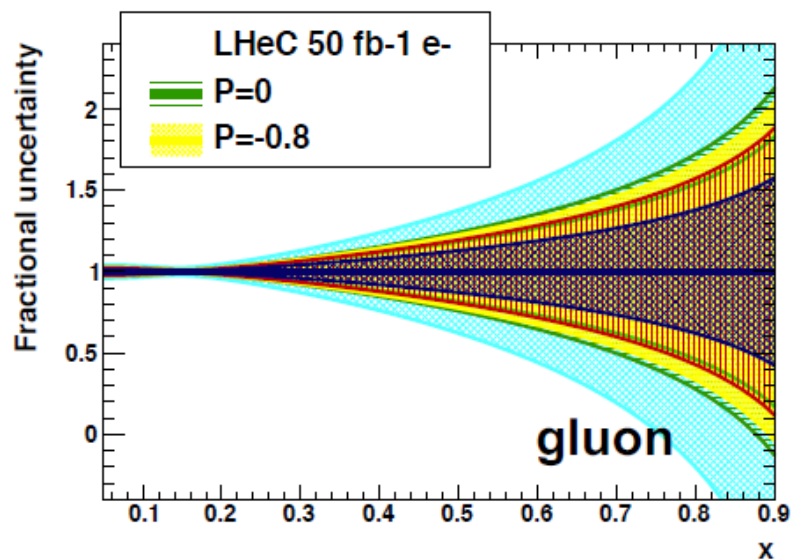
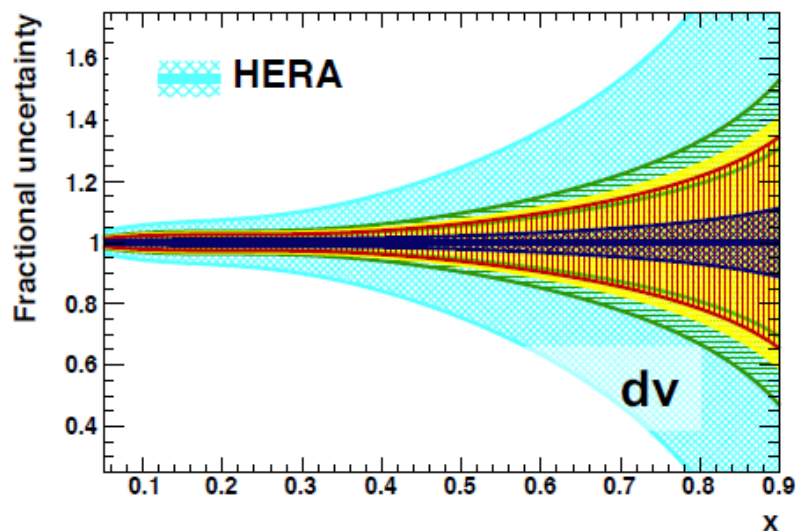
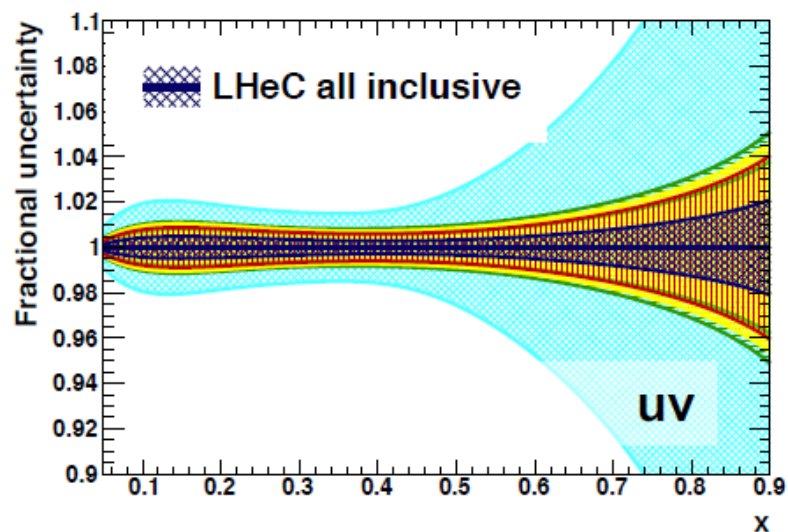
G.R. Boroun, PLB 744 (2015) 142  
 G.R. Boroun, PLB 741 (2015) 197

# impact of HQ data on LHeC pdfs



more flexible parameterisation (5+1):  $x_{u\bar{v}}$ ,  $x_{d\bar{v}}$ ,  $x_{\bar{u}}$ ,  $x_{\bar{d}}$ ,  $x_{\bar{s}}$  and  $x_g$

# impact of polarisation on LHeC pdfs



impact of polarisation on pdfs generally small (but pol. important for ew)

(**CC**:  $\sigma(e\pm)$  scales as  $(1\pm P)$ ; **NC**: effects subtle; pol. asym. gives access to  $F_2^{\nu Z}$ , new quark combinations)