

# Photoproduction of dijets with PYTHIA 8

Initial Stages 2017

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September 20, 2017

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# Motivation & Outline

## Motivation

- $\gamma\gamma$  interactions in future  $e^+e^-$  colliders
- Photoproduction in  $e+p/A$  colliders
- Ultra-peripheral collisions (UPCs) at the LHC

⇒ **Aim:** Robust simulations of photoproduction in different collision systems with PYTHIA 8

## Outline

1. Event generation in PYTHIA 8
2. Photon-hadron collisions
3. Photo-production in ep collisions at HERA
4. Photo-nuclear dijets in UPCs at the LHC
5. Summary & Outlook

- A general-purpose Monte-Carlo event generator
- Main focus has been in pp (LHC), now several extensions
- Current public version 8.226, 8.228 to be released soon

## Team:

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- Peter Skands Monash University

## 1. Hard process

- Sample the (LO) hard process according to

$$d\sigma^X = \sum_{i,j} f_i(x_1, Q^2) \otimes f_j(x_2, Q^2) \otimes d\hat{\sigma}^{i+j \rightarrow X}$$

- where PDFs from global DGLAP analysis

## 2. Partonic evolution

- Final state radiation (FSR)
  - Splitting probabilities from DGLAP

$$d\mathcal{P}_{a \rightarrow b} = \frac{dQ^2}{Q^2} \frac{\alpha_s}{2\pi} P_{a \rightarrow bc}(z) dz$$

- Initial state radiation (ISR)
  - Backwards evolution, conditional probability

$$d\mathcal{P}_{a \leftarrow b} = \frac{df_b}{f_b} = \frac{dQ^2}{Q^2} \frac{\alpha_s}{2\pi} \frac{x' f_a(x', Q^2)}{x f_b(x, Q^2)} P_{a \rightarrow bc}(z) dz \quad (x' = x/z)$$

# Event generation in PYTHIA 8

- Multiple partonic interactions (MPIs) and soft processes
  - Screening parameter  $p_{T0}$  regulates  $p_T \rightarrow 0$  divergence

$$\frac{d\mathcal{P}_{\text{MPI}}}{dp_T} = \frac{1}{\sigma_{\text{nd}}} \frac{d\sigma}{dp_T} \propto \frac{\alpha_s(p_T^2)}{p_T^4} \rightarrow \frac{\alpha_s(p_{T0}^2 + p_T^2)}{(p_{T0}^2 + p_T^2)^2}$$

- Parameter energy-dependent:  $p_{T0}(\sqrt{s}) = p_{T0}^{\text{ref}}(\sqrt{s}/7 \text{ TeV})^\alpha$
- Tuned to data (Monash:  $p_{T0}^{\text{ref}} = 2.28 \text{ GeV}/c$ ,  $\alpha = 0.215$ )
- Common evolution scale ( $p_T$ ) for FSR, ISR and MPIs

$$\begin{aligned} \frac{d\mathcal{P}}{dp_T} &= \left( \frac{d\mathcal{P}_{\text{MPI}}}{dp_T} + \sum \frac{d\mathcal{P}_{\text{ISR}}}{dp_T} + \sum \frac{d\mathcal{P}_{\text{FSR}}}{dp_T} \right) \\ &\times \exp \left[ - \int_{p_T}^{p_T^{\text{max}}} dp'_T \left( \frac{d\mathcal{P}_{\text{MPI}}}{dp'_T} + \sum \frac{d\mathcal{P}_{\text{ISR}}}{dp'_T} + \sum \frac{d\mathcal{P}_{\text{FSR}}}{dp'_T} \right) \right] \end{aligned}$$

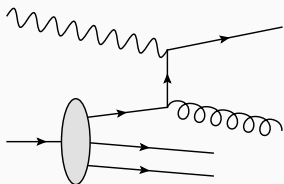
where  $\exp[...]$  is a Sudakov factor

## 3. Hadronization see C. Bierlich's talk

# Photon-hadron collisions

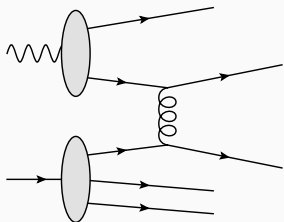
## Direct processes

- Unresolved photons initiators of the process
- No MPIs
- FSR and ISR for hadron



## Resolved processes

- Photons fluctuate to hadronic state (VMD)
- Partonic content from PDFs
- Full parton-level evolution (ISR, FSR, MPI)



Photoproduction  $\Rightarrow Q^2 \lesssim 1.0 \text{ GeV}^2$  (unlike in DIS)

# Resolved photons

- PDFs for resolved photons from global DGLAP analysis
- Data from  $\gamma^*\gamma$  events in  $e^+e^-$  (LEP)

## DGLAP equations for photons

- Additional term due to  $\gamma \rightarrow q\bar{q}$  splittings

$$\frac{\partial f_i^\gamma(x, Q^2)}{\partial \log(Q^2)} = \frac{\alpha_{\text{em}}}{2\pi} e_i^2 P_{i\gamma}(x) + \frac{\alpha_s(Q^2)}{2\pi} \sum_j \int_x^1 \frac{dz}{z} P_{ij}(z) f_j(x/z, Q^2)$$

where  $P_{i\gamma}(x) = 3(x^2 + (1-x)^2)$  for quarks, 0 for gluons (LO)

- Solution has two components:

$$f_i^\gamma(x, Q^2) = f_i^{\gamma, \text{pl}}(x, Q^2) + f_i^{\gamma, \text{had}}(x, Q^2)$$

Non-perturbative input for hadron-like part fixed by data

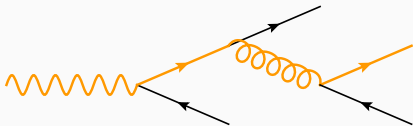
$$f_i^{\gamma, \text{had}}(x, Q_0^2) = N_i x^{a_i} (1-x)^{b_i}$$

# ISR with photon beams

- ISR probability based on DGLAP equations
- Add a term corresponding to  $\gamma \rightarrow q\bar{q}$  splitting

$$d\mathcal{P}_{a \leftarrow b} = \frac{dQ^2}{Q^2} \frac{\alpha_s}{2\pi} \frac{x' f_a^\gamma(x', Q^2)}{x f_b^\gamma(x, Q^2)} P_{a \rightarrow bc}(z) dz + \frac{dQ^2}{Q^2} \frac{\alpha_{em}}{2\pi} \frac{e_b^2 P_{\gamma \rightarrow bc}(x)}{f_b^\gamma(x, Q^2)}$$

- Corresponds to finding the beam photon during evolution
  - No further ISR
  - No MPIs below the scale
  - No need for beam remnants





# Photon flux from leptons

- Flux of photons from leptons using equivalent photon approximation (EPA)

$$f_{\gamma}^e(x, Q_{\max}^2) = \frac{\alpha_{\text{em}}}{2\pi} \int_{Q_{\min}^2(x)}^{Q_{\max}^2} \frac{dQ_{\gamma}^2}{Q_{\gamma}^2} \frac{(1 + (1-x)^2)}{x}$$

where  $x$  is the energy fraction of the photon wrt. lepton

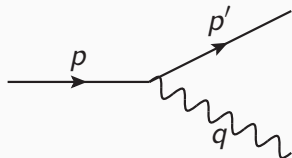
- Virtuality of the photon

$$Q_{\gamma}^2 = -q^2 = -(p - p')^2$$

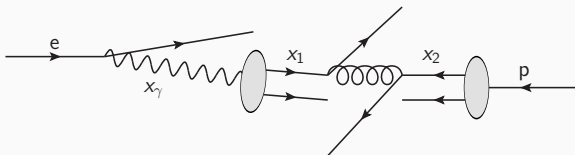
is related to lepton scattering angle  $\theta$  as

$$Q_{\gamma}^2 \approx 2 E_l^2 (1-x)(1 - \cos \theta)$$

and  $Q_{\min}^2(x) \approx m_l^2 x^2 / (1-x)$



## Resolved processes

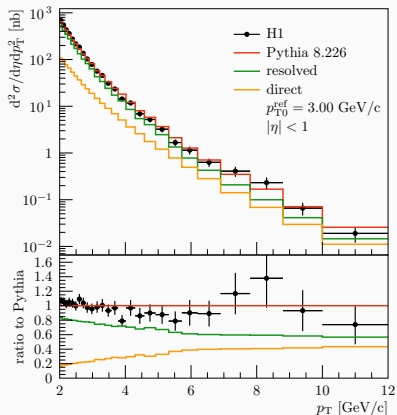


- PDFs required for hard-process sampling  
⇒ Define parton-inside-photon-inside-lepton PDFs

$$xf_i^l(x, Q^2) = \int_x^1 \frac{dx_\gamma}{x_\gamma} x_\gamma f_l^{\gamma}(x_\gamma, Q_{\max}^2) \frac{x}{x_\gamma} f_\gamma^i(x/x_\gamma, Q^2)$$

- Sample  $x_\gamma$  and  $Q_\gamma^2$  for each accepted event
- Set up  $\gamma p$  sub-collision according to sampled  $\gamma$  kinematics
- Perform parton-level evolution for the sub-system

# Charged particle $p_T$ spectra in ep collisions at HERA



[Eur.Phys.J. C10 (1999) 363-372]

## H1 measurement

- $E_p = 820 \text{ GeV}$ ,  $E_e = 27.5 \text{ GeV}$
- $\langle W_{\gamma p} \rangle \approx 200 \text{ GeV}$
- $Q_\gamma^2 < 0.01 \text{ GeV}^2$

## Comparison to PYTHIA 8

- Resolved contribution dominates
  - Data best described with  $p_{T0}^{\text{ref}} = 3.00 \text{ GeV}/c$
- $\Rightarrow$  Lower MPI probability than in pp ( $p_{T0}^{\text{ref}} = 2.28 \text{ GeV}/c$ )

# Dijet photoproduction in ep collisions at HERA

## ZEUS dijet measurement

- $Q_\gamma^2 < 1.0 \text{ GeV}^2$
- $134 < W_{\gamma p} < 277 \text{ GeV}$
- $E_T^{\text{jet}1} > 14 \text{ GeV}, E_T^{\text{jet}2} > 11 \text{ GeV}$
- $-1 < \eta^{\text{jet}1,2} < 2.4$

## Different contributions

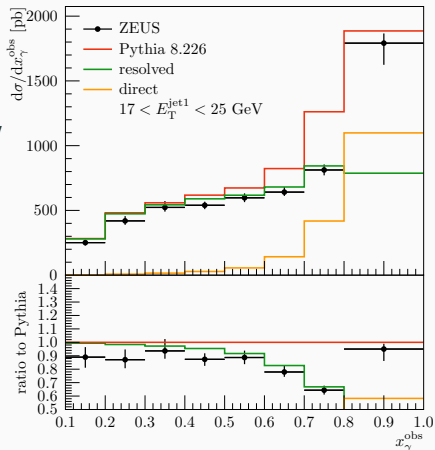
- Define

$$x_\gamma^{\text{obs}} = \frac{E_T^{\text{jet}1} e^{\eta^{\text{jet}1}} + E_T^{\text{jet}2} e^{\eta^{\text{jet}2}}}{2yE_e}$$

to discriminate direct and resolved processes

( $=x_\gamma$  at LO parton level)

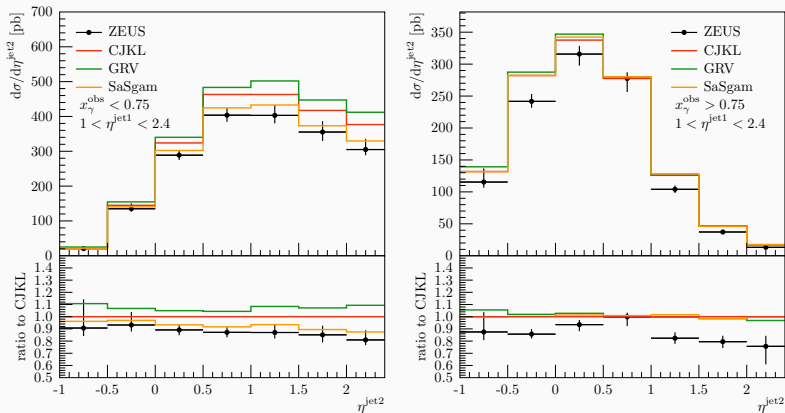
- At high- $x_\gamma^{\text{obs}}$  direct processes dominate



[Eur.Phys.J. C23 (2002) 615-631]

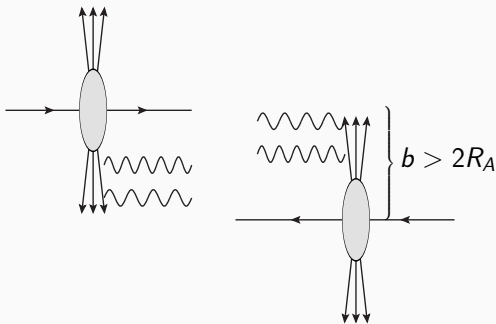
# Dijet in ep collisions at HERA

Pseudorapidity dependence of dijets [Eur.Phys.J. C23 (2002) 615-631]



- Simulations tend to overshoot the dijet data by  $\sim 10\%$
- $\sim 10\%$  uncertainty from photon PDFs for  $x_\gamma^{\text{obs}} < 0.75$  (default in PYTHIA 8 is CJKL)

# Ultra-peripheral heavy-ion collisions



- Large impact parameter  $b \Rightarrow$  No strong interaction
- EM-field of nuclei described with quasi-real photons (EPA)
  - Photon-photon (dileptons, light-by-light)  
 $\Rightarrow$  Useful to calibrate the photon flux
  - Photon-nucleus (dijets, incl. hadrons, heavy flavours, ...)  
 $\Rightarrow$  Can be used to probe nuclear PDFs

# Photon flux from nuclei

## Photon flux in impact-parameter $b$ space

- Obtained by a Fourier transformation of the time-dependent EM-field

$$f_{\gamma}^A(x, b) = \frac{\alpha_{EM} Z^2}{\pi^2} \left[ \frac{xm}{\hbar c} K_1 \left( \frac{xbm}{\hbar c} \right) \right]^2,$$

where  $Z$  is nuclear charge and  $K_1$  modified Bessel function

## Photon-nucleus interactions

- Integrate over  $b > 2R_A$  to reject hadronic interactions

$$f_{\gamma}^A(x) = \frac{2\alpha_{EM} Z^2}{\pi} \left[ \xi K_1(\xi) K_0(\xi) - \frac{\xi^2}{2} (K_1^2(\xi) - K_0^2(\xi)) \right],$$

where  $\xi = 2R_A xm / \hbar c$

- Primitive approach, does not account for the tails of the nuclear density

- No internal implementation of the photon flux from nuclei
- However, possibility to feed in external photon flux
- Implementation of nuclear PDFs, default EPS09LO  
 ⇒ Can study UPC sensitivity to nuclear PDFs at the LHC

### Photo-nuclear dijet production

- ATLAS analysis [ATLAS-CONF-2017-011]  
 anti- $k_T$ ,  $R = 0.4$ ,  $p_T^{\text{lead}} > 20$  GeV,  $p_T^{\text{jets}} > 15$  GeV,  $|\eta| < 4.4$
- Event-level variables:

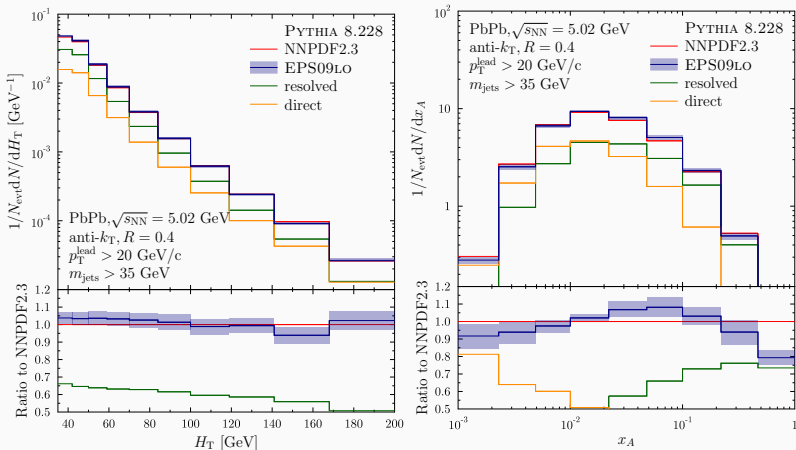
$$m_{\text{jets}} = \sqrt{(\sum_i E_i)^2 - |\sum_i \vec{p}_i|^2}, \quad H_T = \sum_i p_{Ti}$$

$$y_{\text{jets}} = \frac{1}{2} \log \left( \frac{\sum_i E_i + \sum_i p_{zi}}{\sum_i E_i - \sum_i p_{zi}} \right), \quad x_A = \frac{m_{\text{jets}}}{\sqrt{s}} e^{-y_{\text{jets}}}$$



# Results for UPC dijets

## Differential photo-nuclear dijet distributions (Preliminary)



- The expected nPDF features visible in  $x_A$
- Small- $x$  gluon uncertainties underestimated in EPS09

# Summary & Outlook

## Present: PYTHIA 8.226

- Full simulations of  $\gamma\gamma$  and  $\gamma$ -hadron collisions
- Automatic mixing of direct and resolved contributions
- Implementation of photon flux from leptons (EPA)
  - ⇒ Ready for FCC-ee studies
  - ⇒ Can simulate photoproduction in ep collisions

## Soon: PYTHIA 8.228

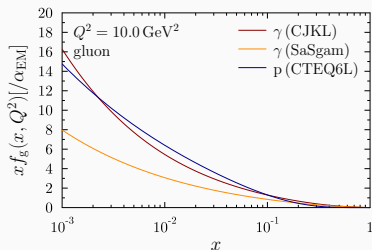
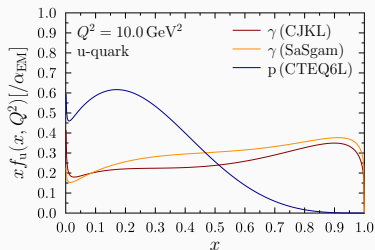
- Nuclear PDFs for hard processes to study  $\gamma A$
- Possibility to feed in external photon flux (e.g. from nuclei)
  - ⇒ Allow simulations photo-nuclear interactions in UPCs and to study sensitivity to nuclear PDFs (e.g. dijets)

## Future

- A detailed implementation of the photon flux from hadrons

Backup slides

# Photon PDFs



- More large- $x$  quarks due to  $\gamma \rightarrow q\bar{q}$  splittings
- CJKL and SASGAM analysis agree for quarks
- CJKL includes also data from LEP-II and is used for PYTHIA 8
- Similar behaviour as with protons
- CJKL  $\sim 2$  more gluons than SASGAM

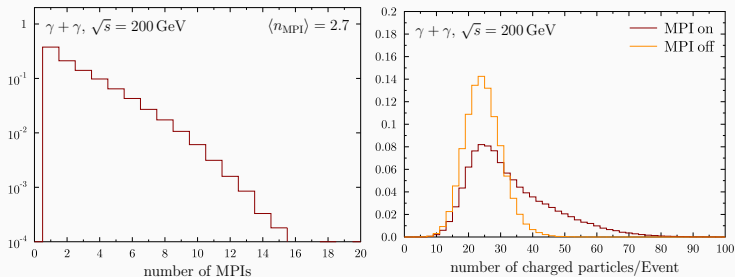
# MPIs with photon beams

- Parametrization for  $\sigma_{\text{tot}}(s)$

$$\sigma_{\text{tot}}^{\gamma\gamma}(s) \approx 211 s^{0.0808} + 215 s^{-0.4525} \quad [\text{nb}]$$

[Schuler, Sjöstrand, Z. Phys. C73 (1997)]

- We use  $\sigma_{\text{nd}}^{\gamma\gamma}(s) \sim 0.7 \sigma_{\text{tot}}^{\gamma\gamma}(s)$  (based on PYTHIA 6)
- Otherwise use the same parameters as for protons

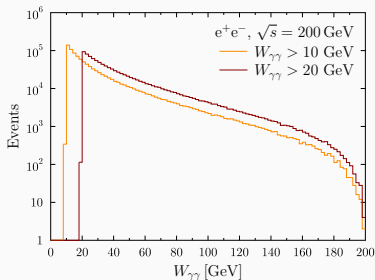


# Soft processes

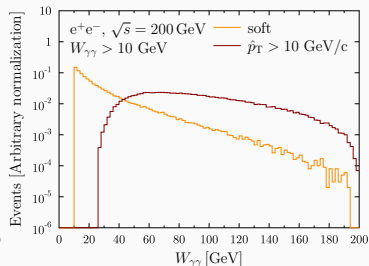
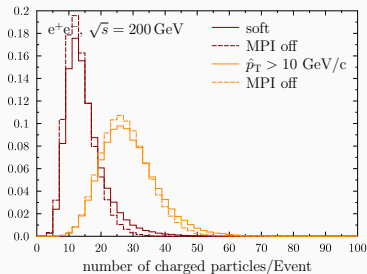
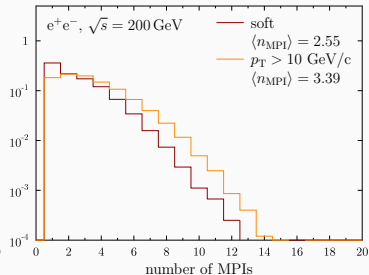
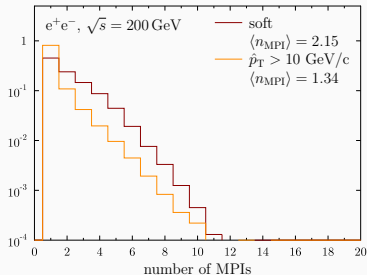
- Soft processes generated with MPI machinery

$$\sigma_{\text{nd}} = \left(\frac{\alpha_{\text{em}}}{2\pi}\right)^2 \int_{x_1^{\text{min}}}^1 dx_1 \int_{x_2^{\text{min}}}^1 dx_2 \frac{1 + (1 - x_1)^2}{x_1} \frac{1 + (1 - x_2)^2}{x_2} \log\left(\frac{Q_{\text{max}}^2}{Q_{\text{min}}^2(x_1)}\right) \log\left(\frac{Q_{\text{max}}^2}{Q_{\text{min}}^2(x_2)}\right) \sigma_{\text{nd}}^{\gamma\gamma}(W_{\gamma\gamma}^2)$$

- $x_i^{\text{min}}$  from lower cut for invariant mass ( $W_{\gamma\gamma}^2 \approx x_1 x_2 s$ )
- Sub-collisions biased towards low  $W_{\gamma\gamma}$

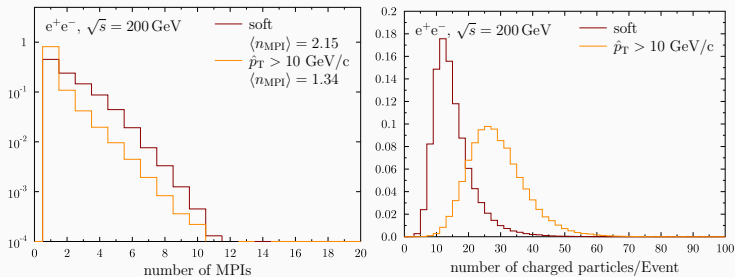


# MPIs in $e^+e^-$



# MPIs in $e^+e^-$

- The evolution of  $\gamma\gamma$  system is done as before



- Hard processes generate less MPIs than soft ones
  - $\gamma \rightarrow q\bar{q}$  splittings in ISR eliminate further MPIs

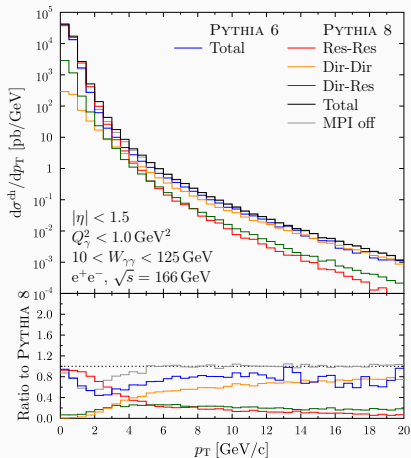
$$d\mathcal{P}_{\text{ISR}} \propto \frac{dp_T^2}{p_T^2} \quad d\mathcal{P}_{\text{MPI}} \propto \frac{dp_T^2}{p_T^4}$$

- Still more charged particles for hard processes



# Charged particle $p_T$ spectra

## Combination of direct and resolved processes



- Resolved processes dominate at low  $p_T$
- Direct processes take over above  $p_T \sim 5 \text{ GeV}/c$

## Comparison with PYTHIA 6:

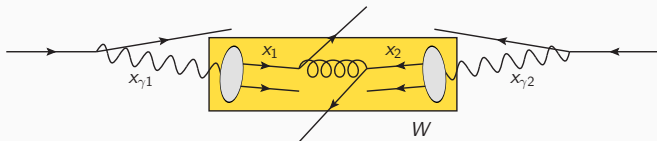
- Difference at  $p_T \sim 2 \text{ GeV}/c$  due to MPIs
- high- $p_T$  difference mainly from PDF sets

# Photoproduction of charged hadrons in LEP

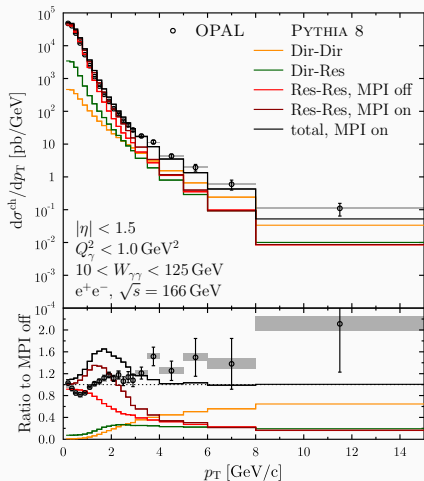
- $e^+e^-$  collisions at  $\sqrt{s} = 161$  and  $172$  GeV

## OPAL measurement

- “Anti-tagged events” = Scattered leptons not seen  
⇒ Quasi-real photons ( $Q^2 < 1 \text{ GeV}^2$ )
- Sum of ECAL and HCAL less than 45 GeV to remove  $e^+e^- \rightarrow q\bar{q}$  background
- Cuts in  $W$  (= invariant mass of hadronic final state)



# Charged particle $p_T$ spectra



[Eur. Phys. J. C6 (1999) 253-264]

## Combination of Direct and Resolved processes

- Resolved processes dominate at low  $p_T$
- Direct processes take over above  $p_T \sim 5 \text{ GeV}/c$

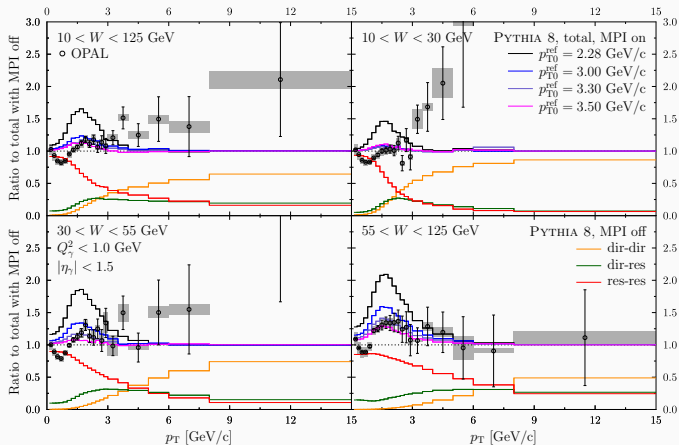
## Compare with OPAL data

- Agreement without MPIs
- “Out of the box” MPIs generates too much hadrons at  $p_T \sim 2 \text{ GeV}/c$

⇒ Value of  $p_{T0}^{\text{ref}}$  in  $\gamma\gamma$  ?

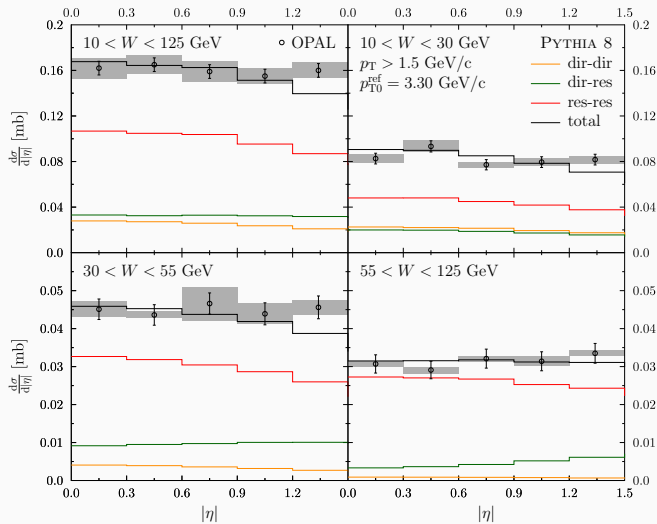
# Invariant mass dependence

- Constrain  $p_{T0}^{\text{ref}}$  with data binned in  $W$



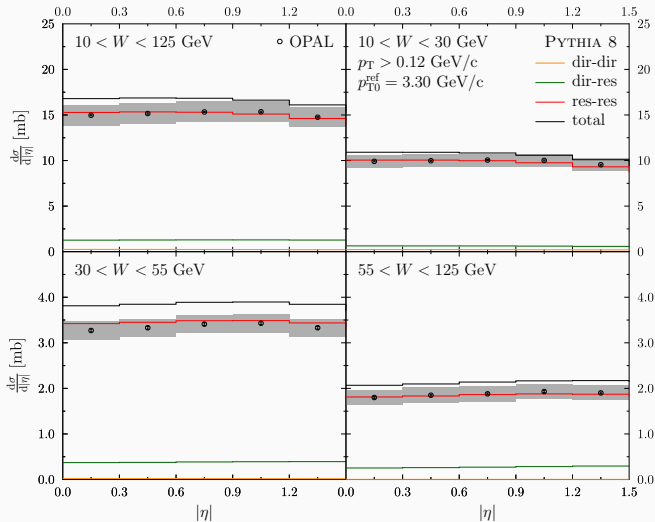
- Good agreement with the data using  $p_{T0}^{\text{ref}} = 3.3$  GeV/c
- More hadrons from MPIs with higher  $W$

# Pseudorapidity dependence



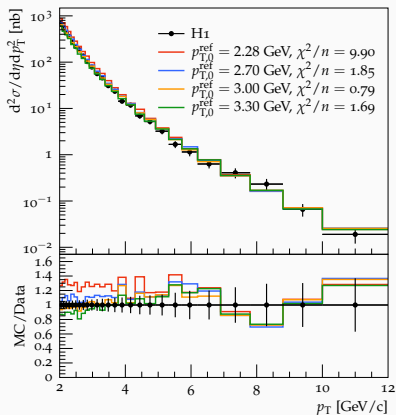
- Also  $\eta$  dependence looks good

# Pseudorapidity dependence



- PYTHIA 8 result slightly above the data with  $p_T > 0.12$  GeV/c

# Charged particle $p_T$ spectra in ep collisions at HERA



[Eur.Phys.J. C10 (1999) 363-372]

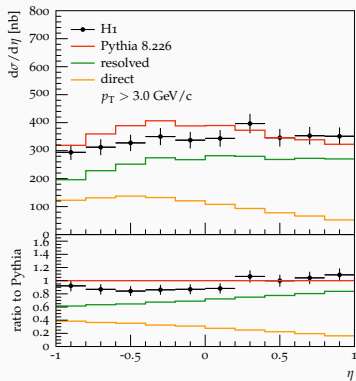
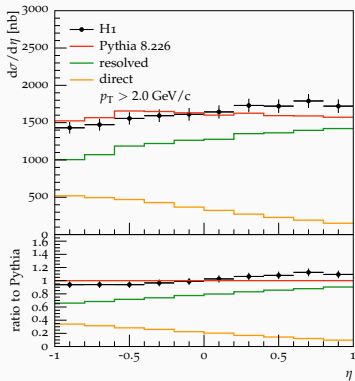
## H1 measurement

- $E_p = 820 \text{ GeV}, E_e = 27.5 \text{ GeV}$
- $\langle W_{\gamma p} \rangle \approx 200 \text{ GeV}$

## Comparison to PYTHIA 8

- Resolved contribution dominates
- Data best described with  $p_{T,0}^{\text{ref}} = 3.00 \text{ GeV}/c$   
(Between 2.28 GeV/c (pp) and 3.30 GeV/c ( $\gamma\gamma$ ))

# Charged particle $\eta$ dependence in ep collisions at HERA

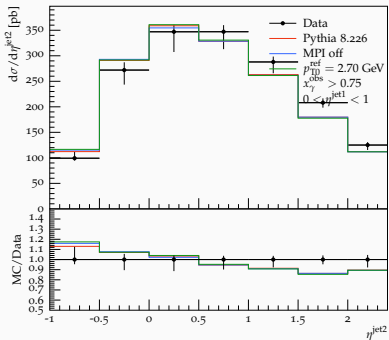
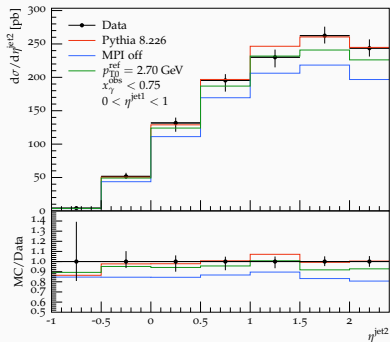


[Eur.Phys.J. C10 (1999) 363-372]



# Dijet in ep collisions at HERA

Pseudorapidity dependence of dijets [Eur.Phys.J. C23 (2002) 615-631]



- Good agreement with the data
- Some sensitivity to MPIs with  $x_\gamma^{obs} < 0.75$