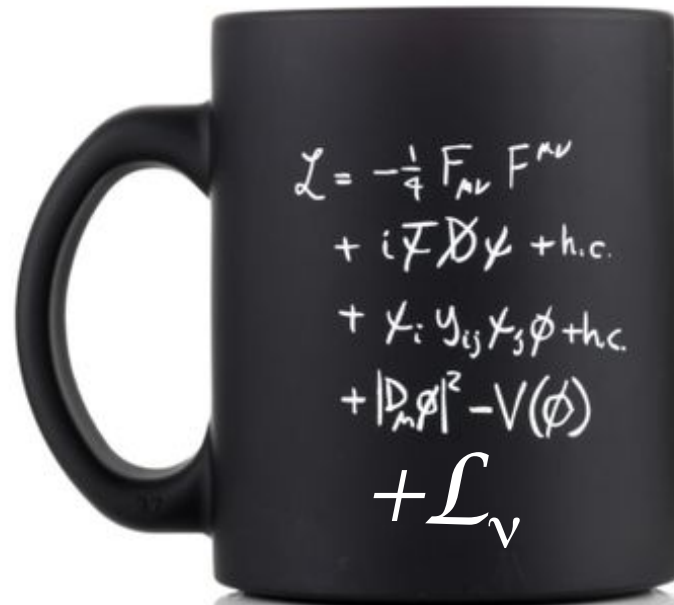


Towards a standard model with massive neutrinos

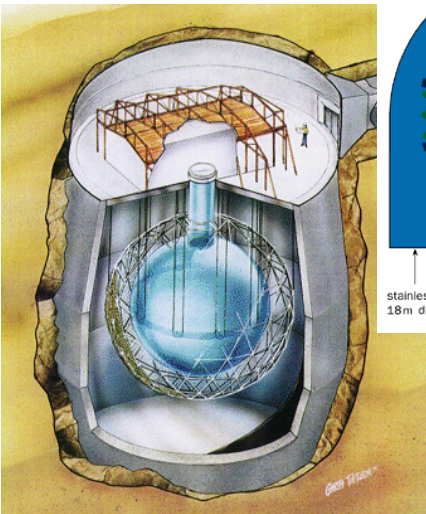
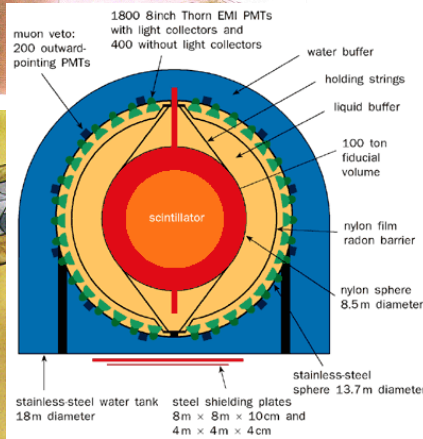
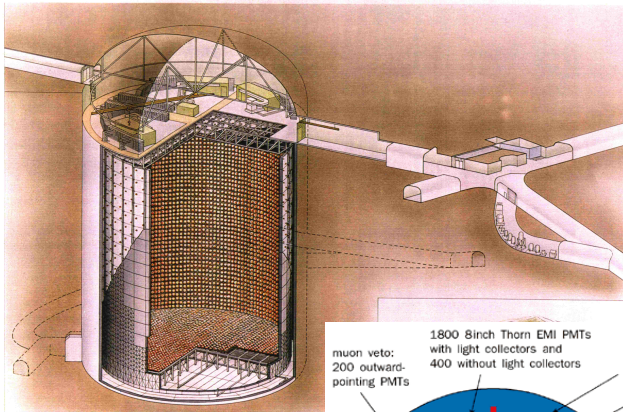
Pilar Hernández

CERN & University of Valencia/IFIC



Two decades of revolutionary neutrino experiments have revealed a new flavour sector, which does not quite fit in the Standard Model

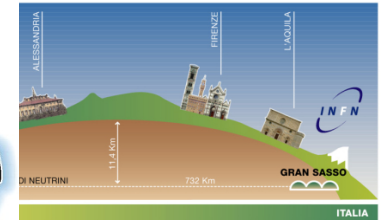
SuperKamiokande



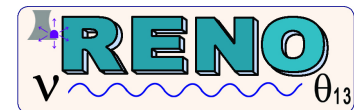
SNO Borexino



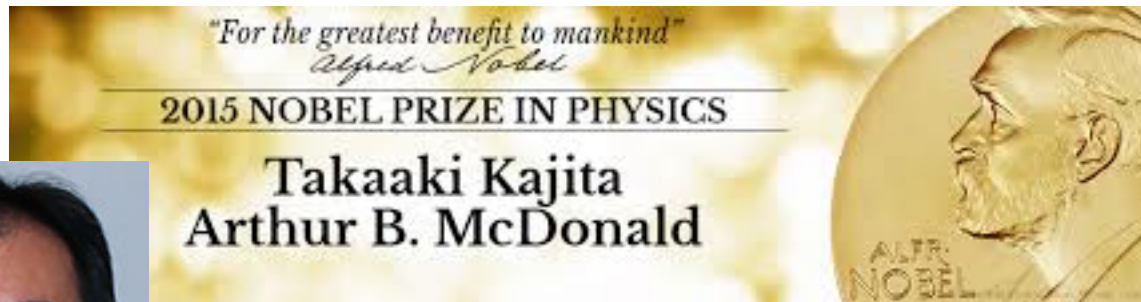
MINOS, Opera



...and more



“For the discovery of **neutrino oscillations**,
which shows that **neutrinos have mass**”

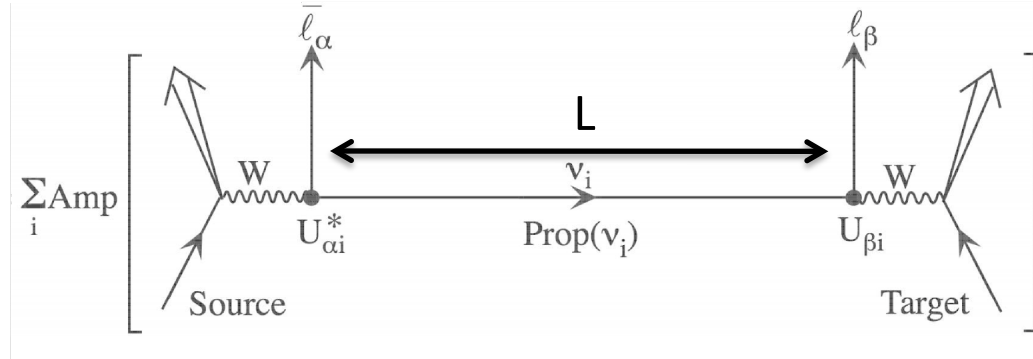


Neutrino Mixing

Mass eigenstates \neq flavour eigenstates

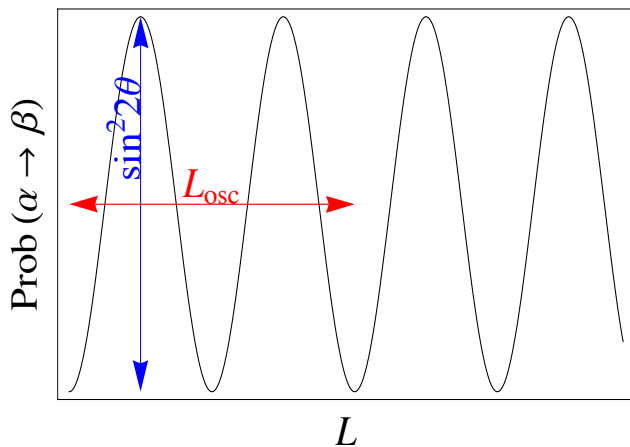
$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = U_{PMNS}(\theta_{12}, \theta_{23}, \theta_{13}, \delta, \dots) \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

Neutrino Interferometry



Бруно Понтекорво

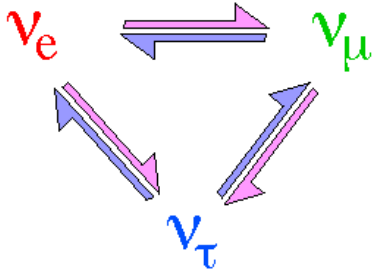
A neutrino experiment is an interferometer in flavour space, because neutrinos are so weakly interacting that can keep coherence over very long distances !



$$P(\nu_\alpha \rightarrow \nu_\beta) = \sum_{ij} U_{\alpha i} U_{\beta i}^* U_{\alpha j}^* U_{\beta j} e^{-i \frac{(m_i^2 - m_j^2)L}{2E}}$$

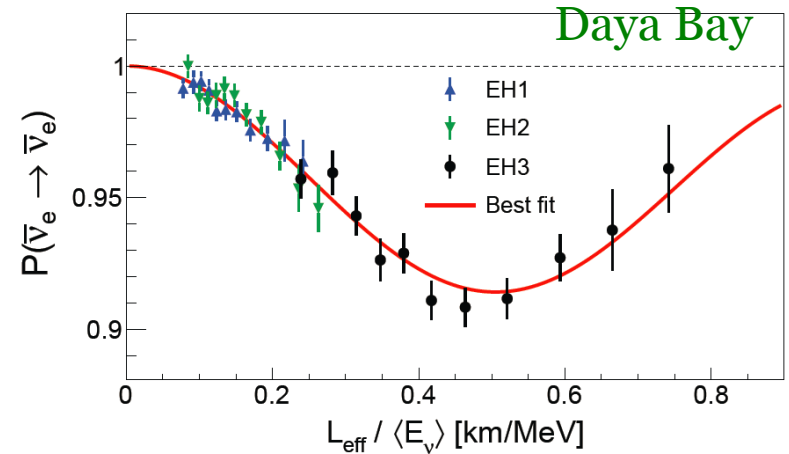
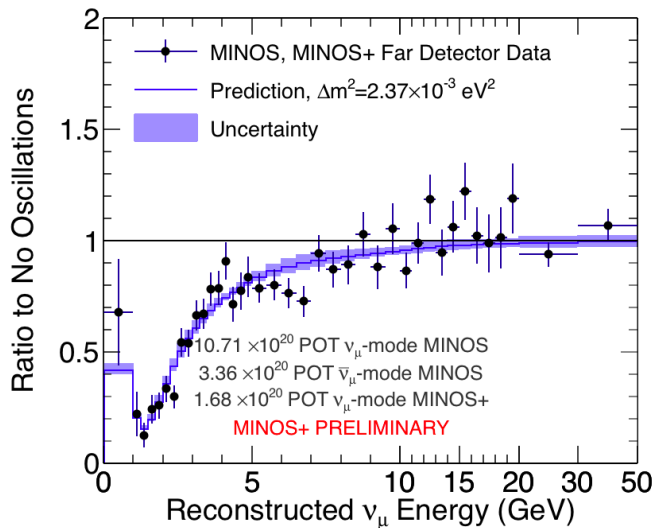
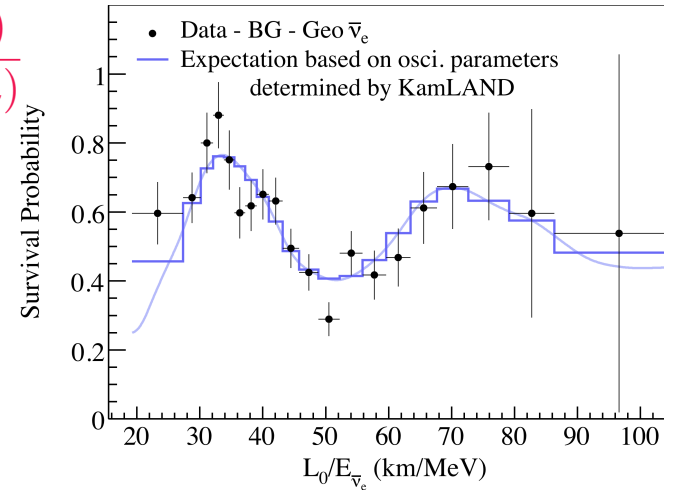
$$L_{osc} \sim \frac{E}{m_i^2 - m_j^2}$$

Two frequencies precisely measured



$$\Delta m_{\text{sol}}^2 \sim \frac{\mathcal{O}(\text{MeV})}{\mathcal{O}(100\text{km})}$$

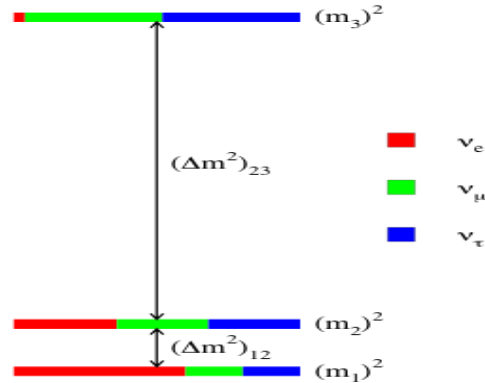
$$|\Delta m_{\text{atm}}^2| \sim \frac{\mathcal{O}(\text{GeV})}{\mathcal{O}(1000\text{km})} \sim \frac{\mathcal{O}(\text{MeV})}{\mathcal{O}(1\text{km})}$$



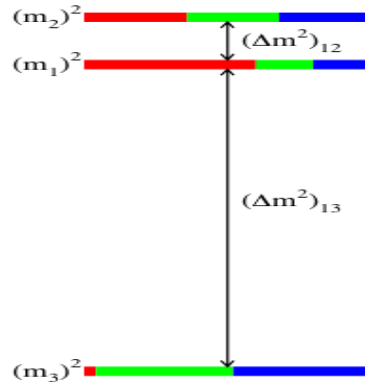
SM+3 massive neutrinos: Global Fits

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = U_{PMNS}(\theta_{12}, \theta_{23}, \theta_{13}, \delta, \dots) \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

normal hierarchy



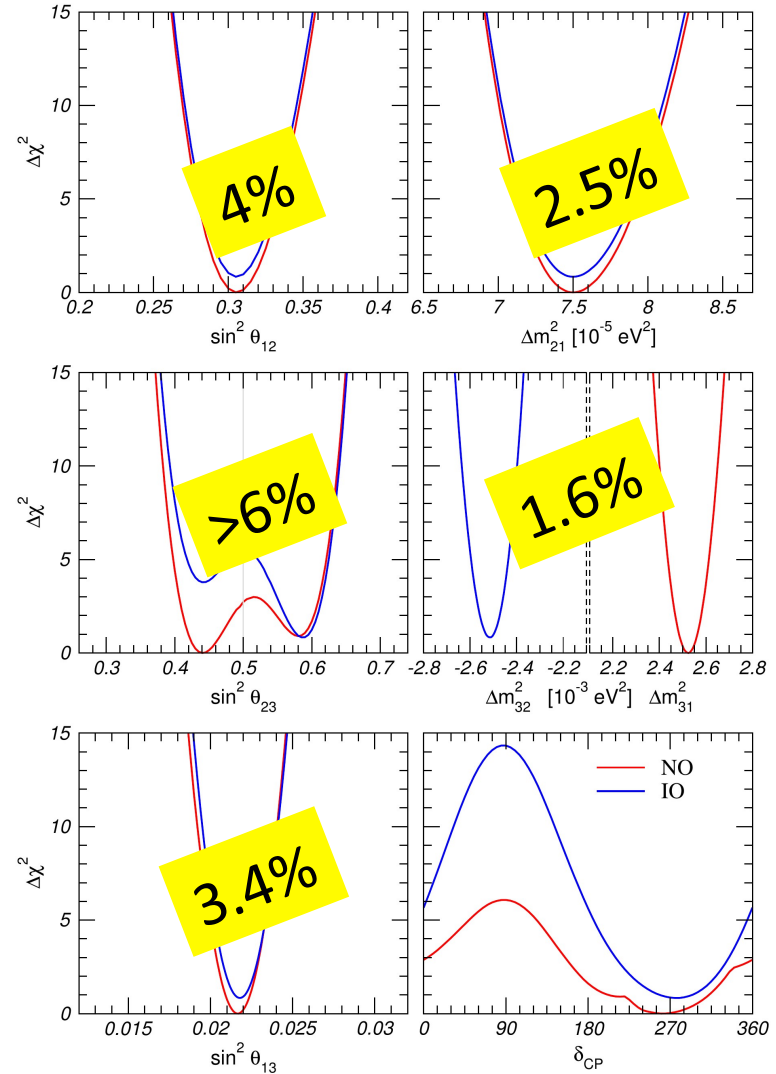
inverted hierarchy



$$\Delta m_{13}^2 > 0$$

$$\Delta m_{13}^2 < 0$$

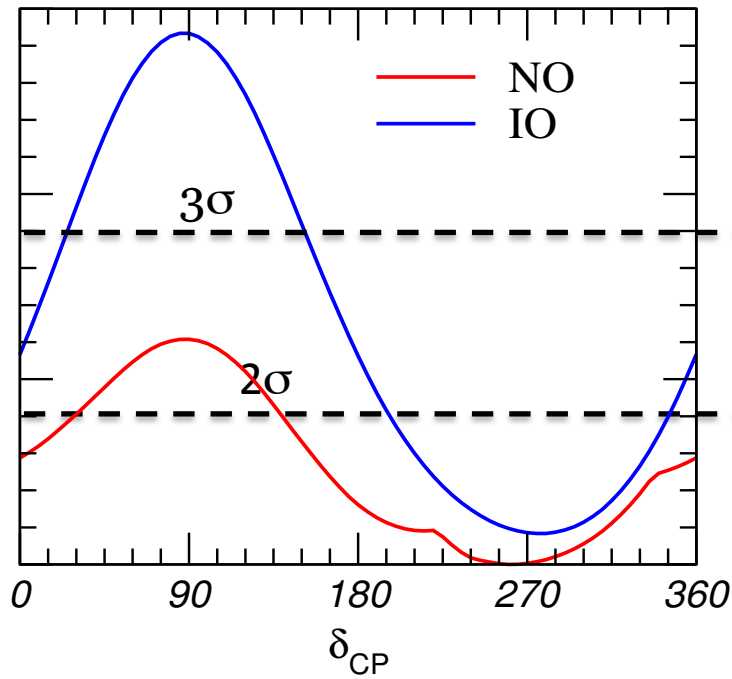
NuFIT 3.0 (2016)



Gonzalez-Garcia et al

See also Capozzi et al, & Forero et al

Leptonic CP violation

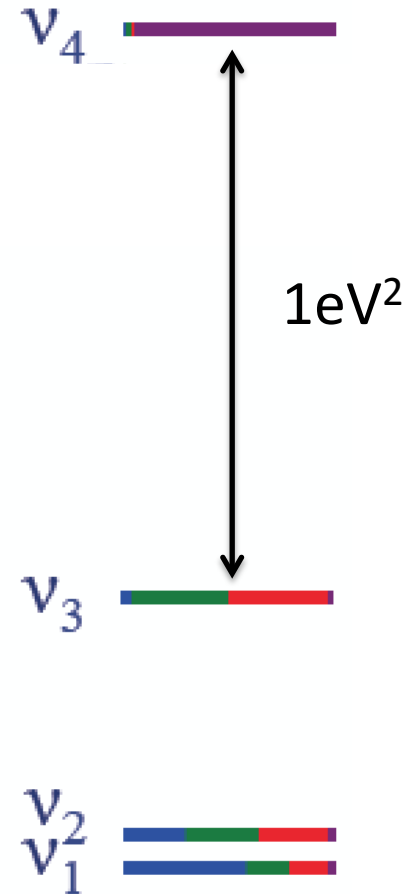
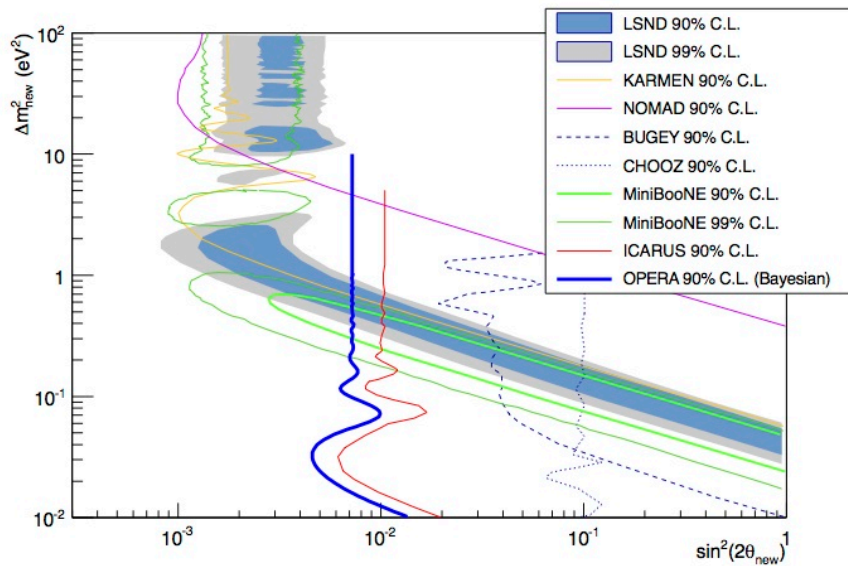


Preference for $\delta > 180^\circ$ driven mostly by combination of reactor/T2K, atmospheric add positively

Outliers: SBL anomalies

LSND

$$P(\nu_\mu \rightarrow \nu_e) = O(|U_{ei}|^2 |U_{\mu i}|^2)$$

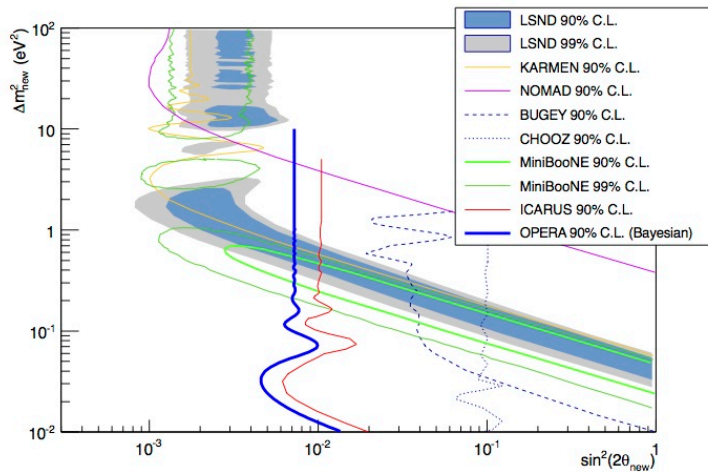


+Gallium anomaly+ MiniBOONE low-energy excess...

Outliers: SBL anomalies

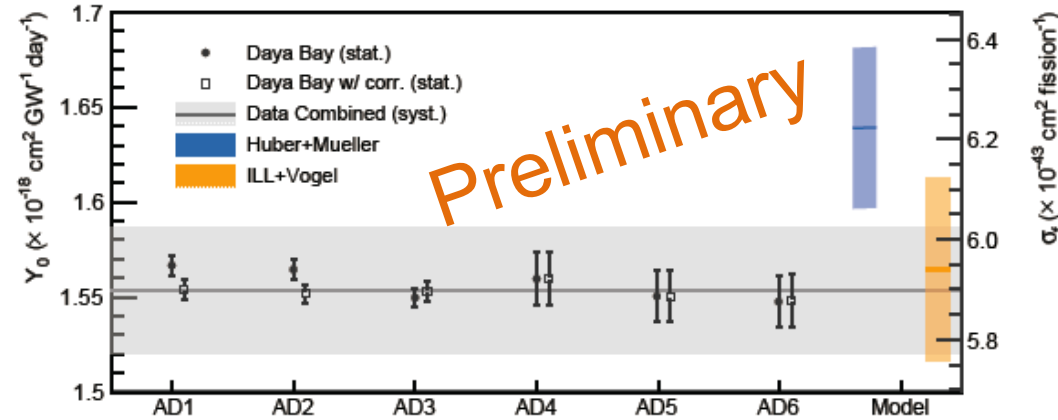
LSND

$$P(\nu_\mu \rightarrow \nu_e) = O(|U_{ei}|^2 |U_{\mu i}|^2)$$



Reactors

$$P(\nu_e \rightarrow \nu_e) = O(|U_{ei}|^2)$$



T. A. Mueller et al; P. Huber

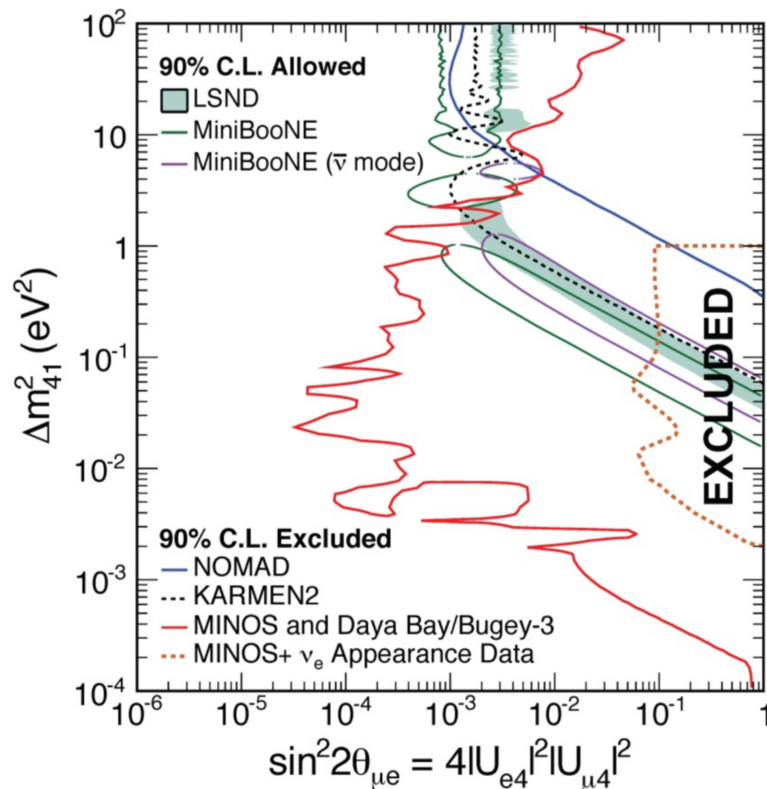
+Gallium anomaly+ MiniBOONE low-energy excess...

$O(eV)$ sterile neutrinos ?

Two other necessary conditions have not been found

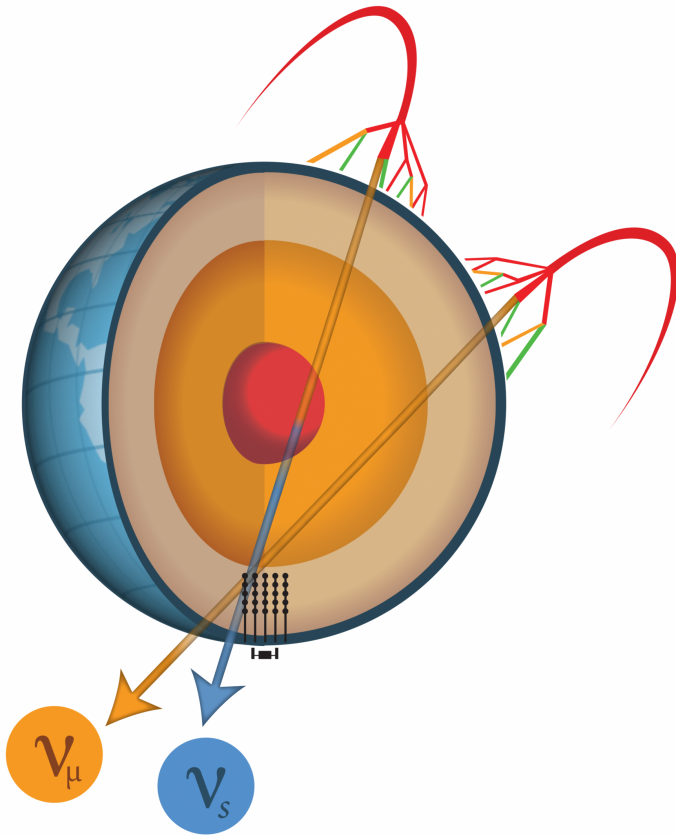
Neutrino muons must disappear also $P(\nu_\mu \rightarrow \nu_\mu) = O(|U_{\mu i}|^2)$

MINOS+Daya Bay

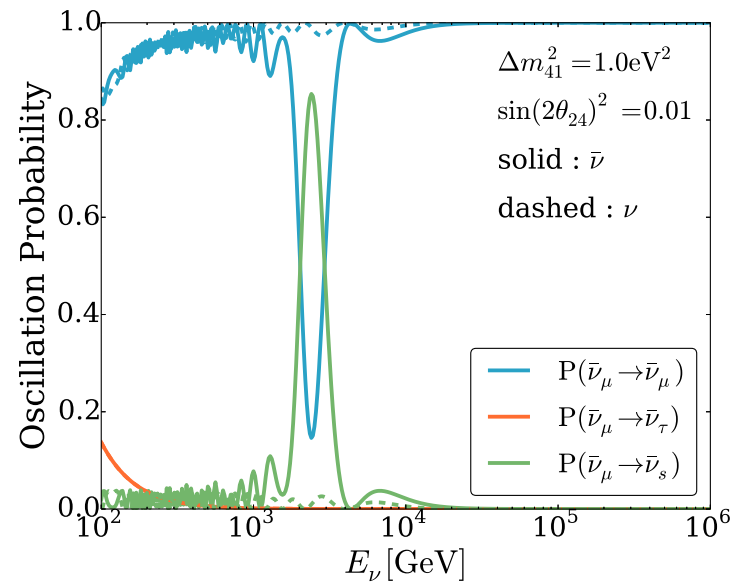


$O(eV)$ sterile neutrinos?

TeV atmospheric neutrinos must resonate into steriles when crossing the nucleus of the Earth

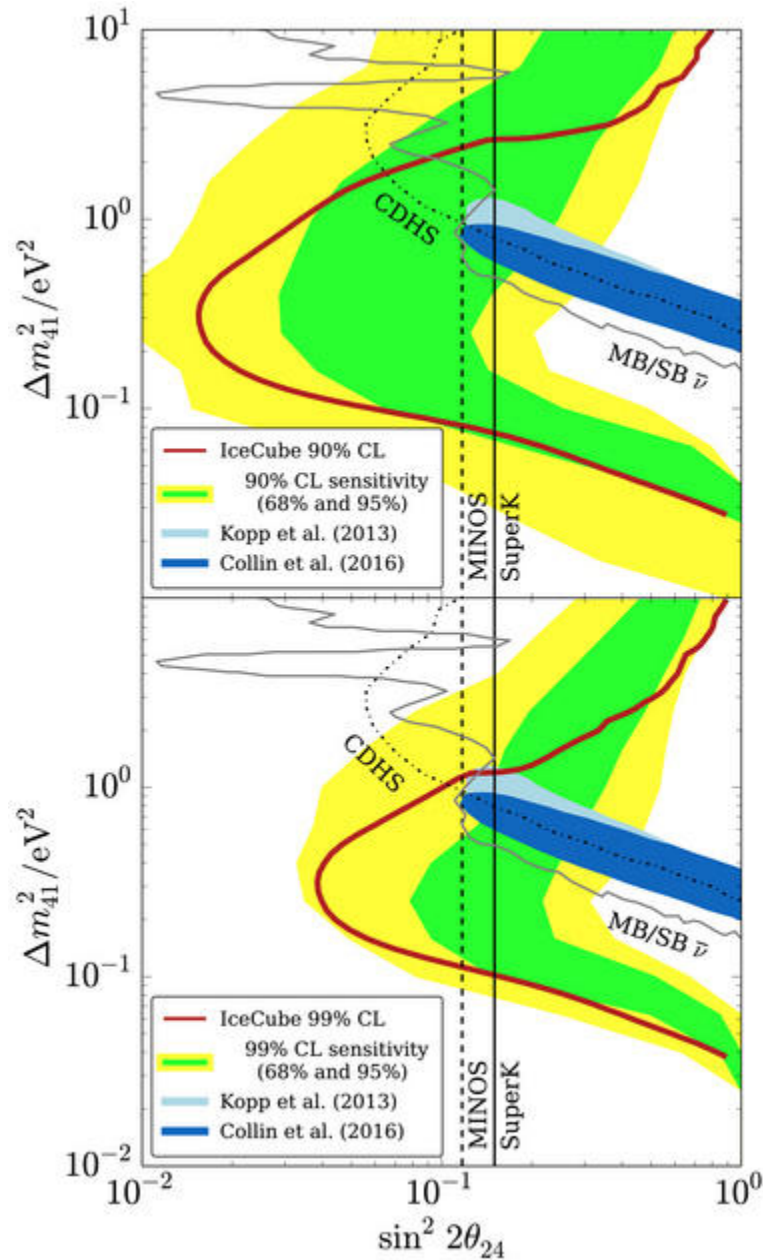


$$E_\nu^{\text{res}} \equiv \frac{\Delta m^2 \cos 2\theta}{2\sqrt{2}G_F N_e} \sim \mathcal{O}(TeV)$$



Chizhov, Petcov; Nunokawa et al; Barger et al; Esmaili et al;

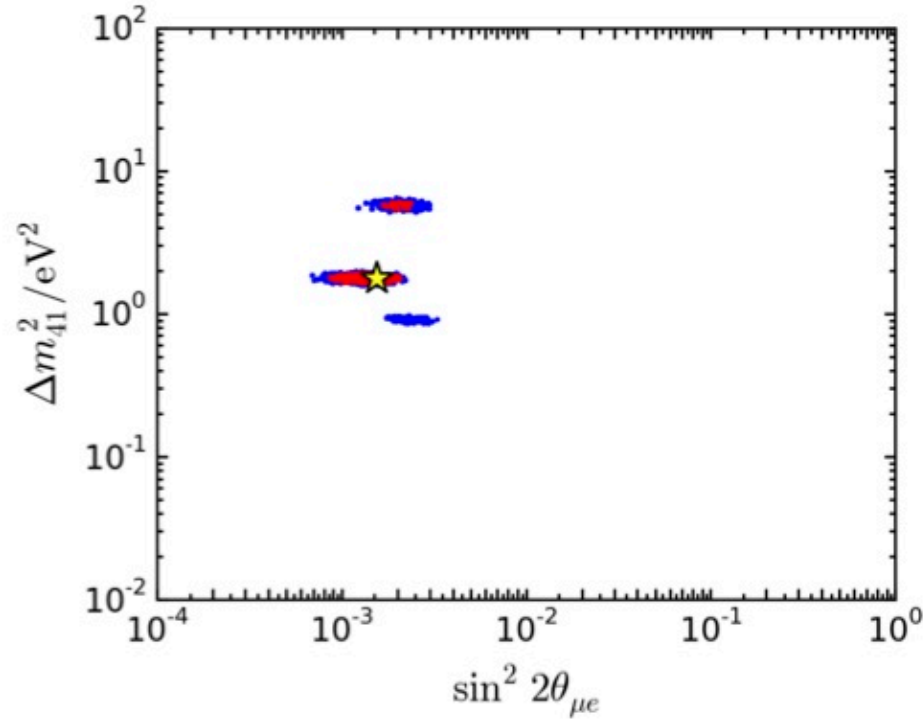
$O(eV)$ sterile neutrinos ?



IceCube coll. '16

O(eV) sterile neutrinos ?

Getting squeezed into inexistence...

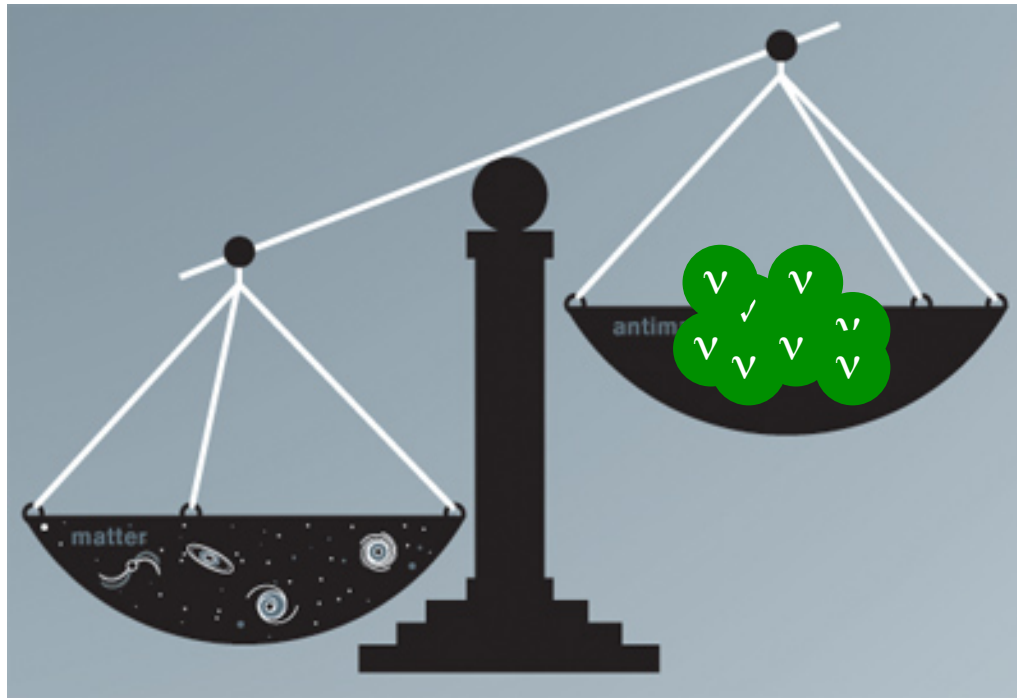


Collin, Argüelles, Conrad, Shaevitz '16

Probably a rather bad fit to all data...

Absolute mass scale

Best constraints at present from cosmology



Neutrinos as light as 0.1-1eV modify the large scale structure and CMB

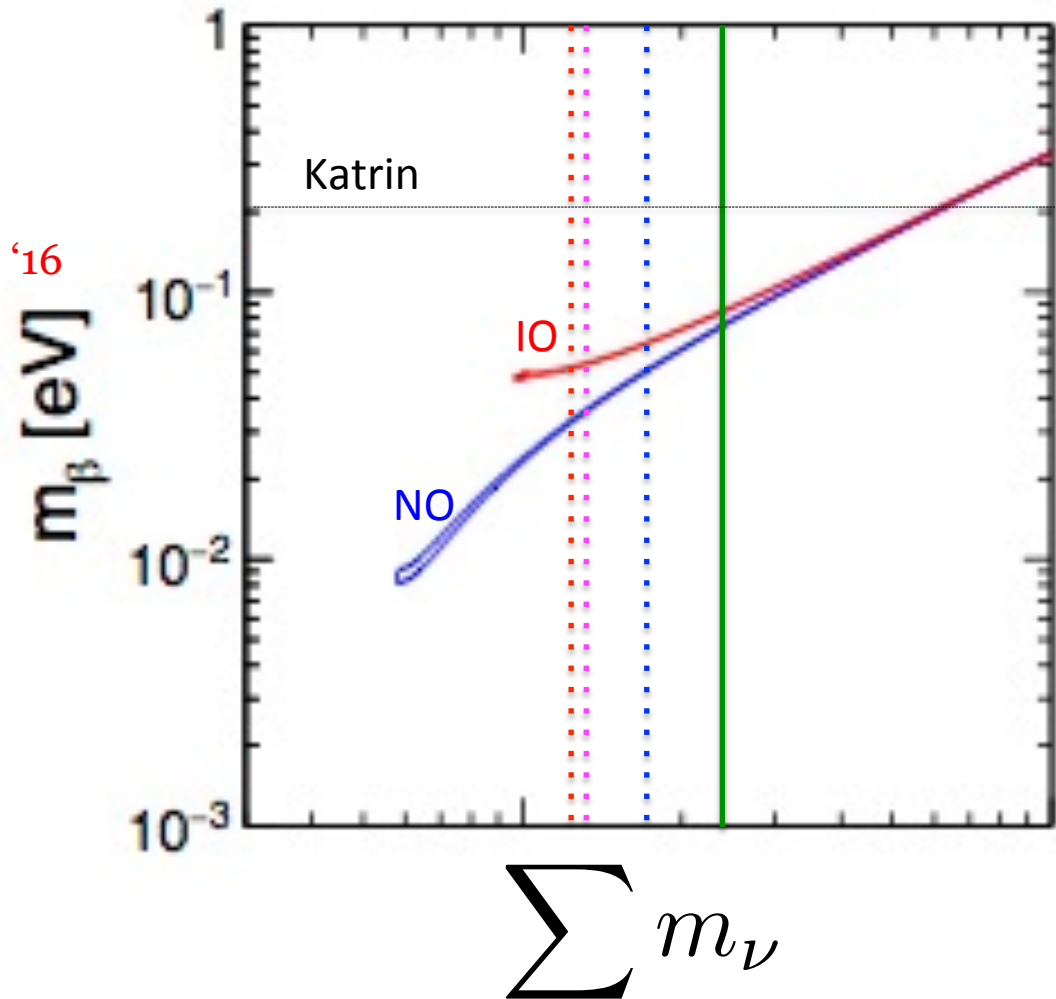
Absolute mass scale

Planck '15

Giusarma et al '16

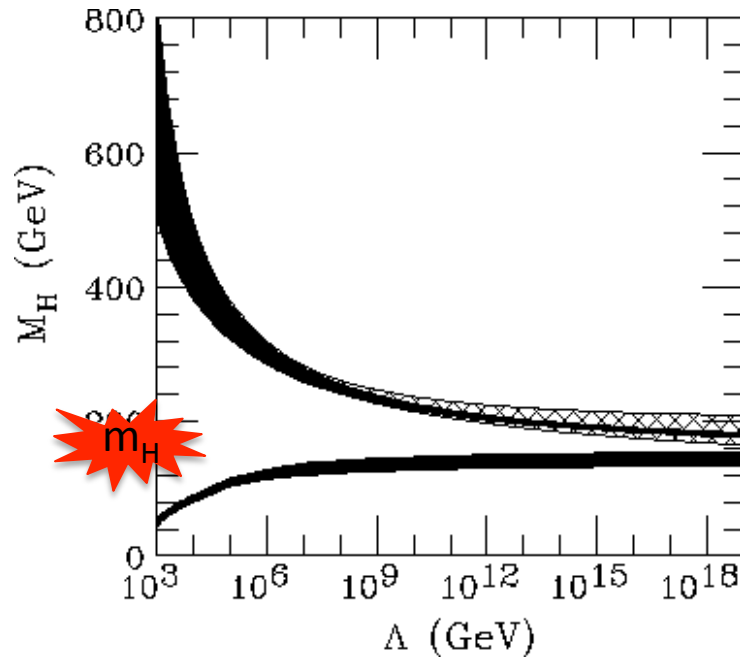
Palanque-DeLabrouille et al '16

Cuesta et al '16



After the discovery of the Brout-Englert-Higgs particle

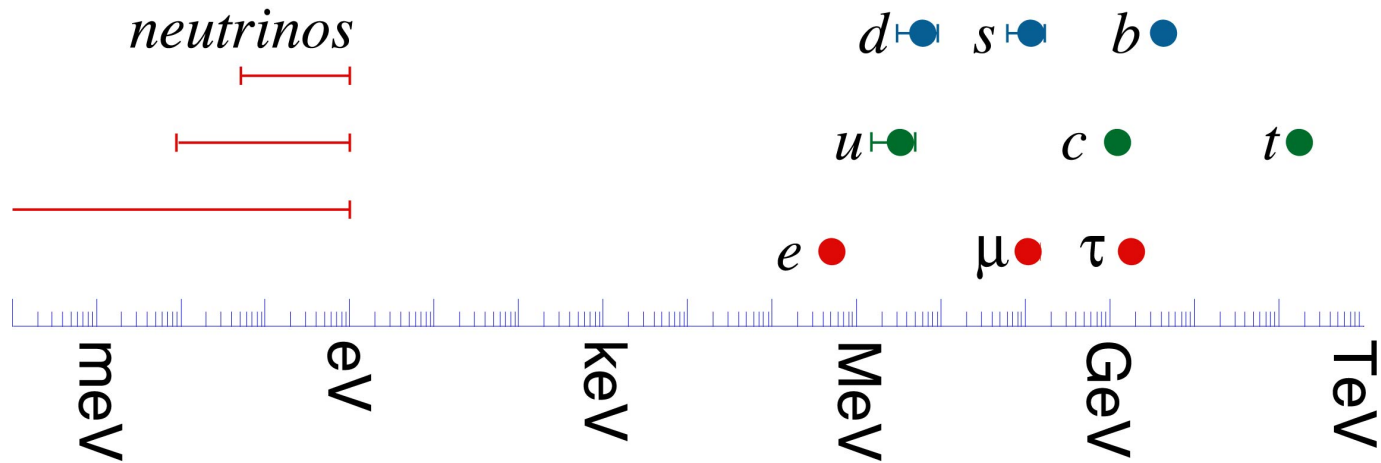
The Standard Model is healthy as far as we can see...



Health up to huge scales strongly suggests:

minimality as guiding principle in BSM

A new flavour perspective



How do we give neutrinos a mass ? Why are neutrinos so much lighter ?

Why do they mix so differently ?

CKM

$$|V|_{\text{CKM}} = \begin{pmatrix} 0.97427 \pm 0.00015 & 0.22534 \pm 0.0065 & (3.51 \pm 0.15) \times 10^{-3} \\ 0.2252 \pm 0.00065 & 0.97344 \pm 0.00016 & (41.2_{-5}^{+1.1}) \times 10^{-3} \\ (8.67_{-0.31}^{+0.29}) \times 10^{-3} & (40.4_{-0.5}^{+1.1}) \times 10^{-3} & 0.999146_{-0.000046}^{+0.000021} \end{pmatrix}$$

PMNS

3σ

NuFIT 3.0 (2016)

$$|U|_{3\sigma} = \begin{pmatrix} 0.800 \rightarrow 0.844 & 0.515 \rightarrow 0.581 & 0.139 \rightarrow 0.155 \\ 0.229 \rightarrow 0.516 & 0.438 \rightarrow 0.699 & 0.614 \rightarrow 0.790 \\ 0.249 \rightarrow 0.528 & 0.462 \rightarrow 0.715 & 0.595 \rightarrow 0.776 \end{pmatrix}$$

A new physics scale ?

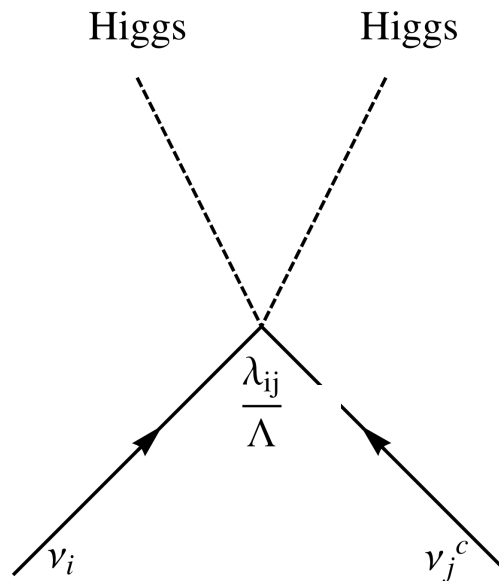
Neutrinos are different...they can have majorana masses:

$$-\mathcal{L}_{\text{Majorana}} = \bar{\nu}_L m_\nu \nu_L^c + h.c. \leftrightarrow \bar{L} \tilde{\Phi} \alpha \tilde{\Phi} L^c + h.c.$$

Weinberg

$$[\alpha] = -1$$

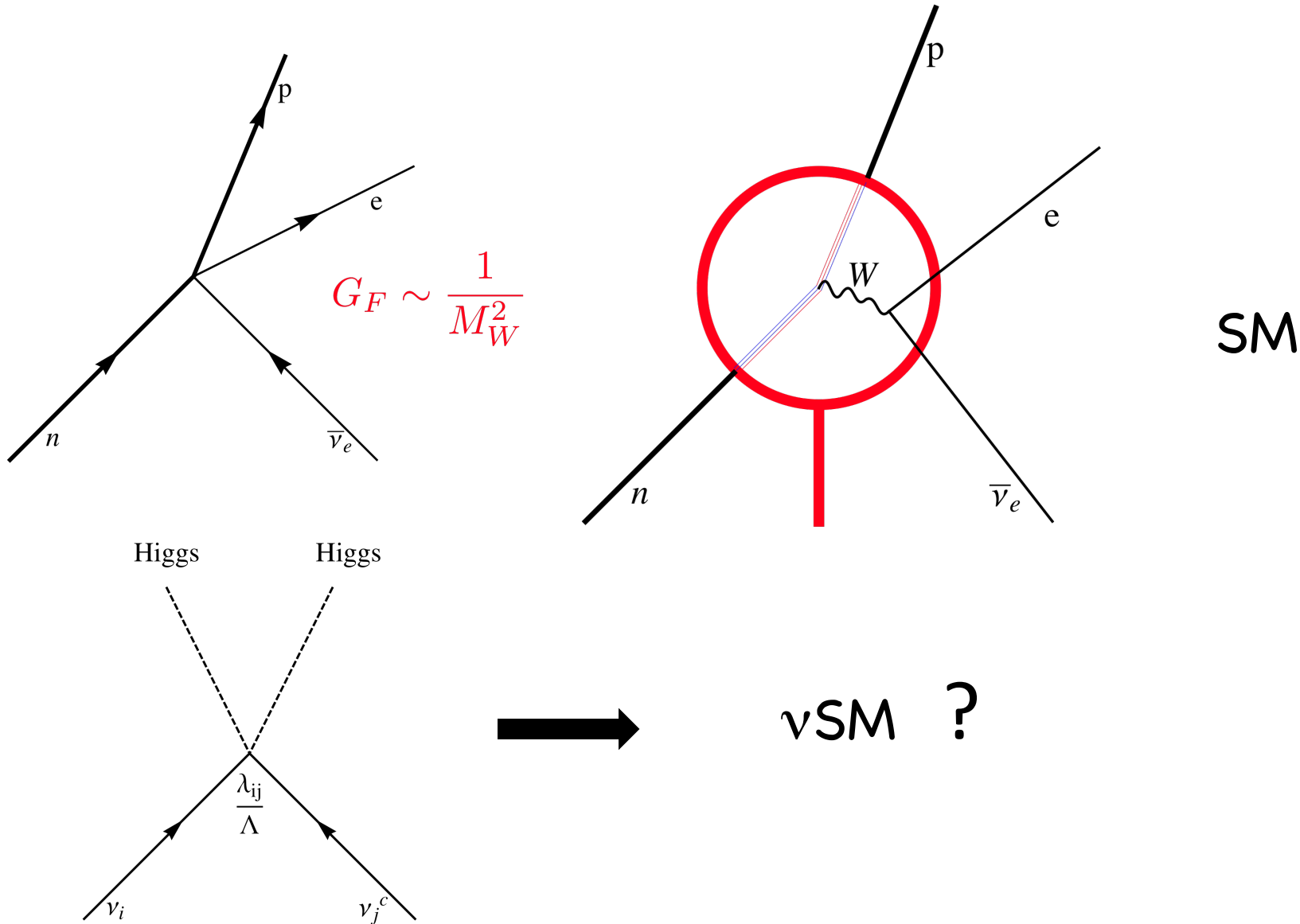
$$\alpha = \frac{\lambda}{\Lambda}$$



$$m_\nu = \lambda \frac{v^2}{\Lambda}$$

Scale at which new particles will show up

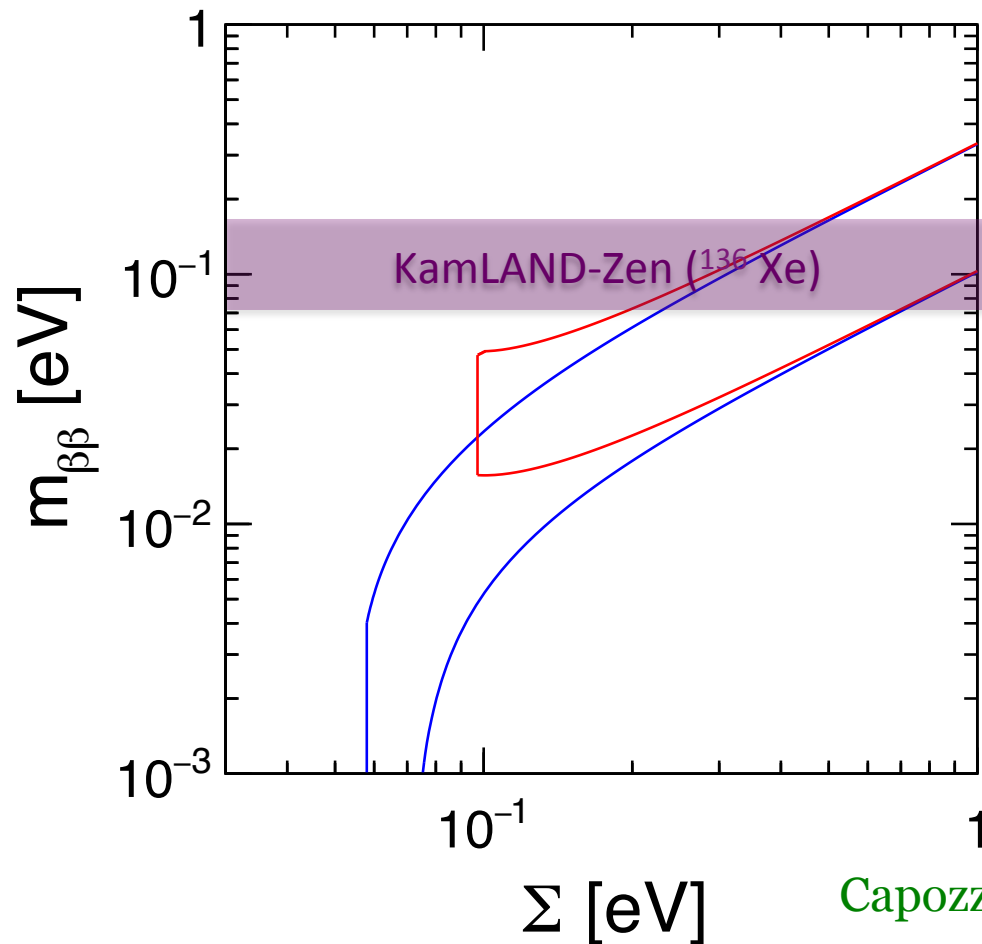
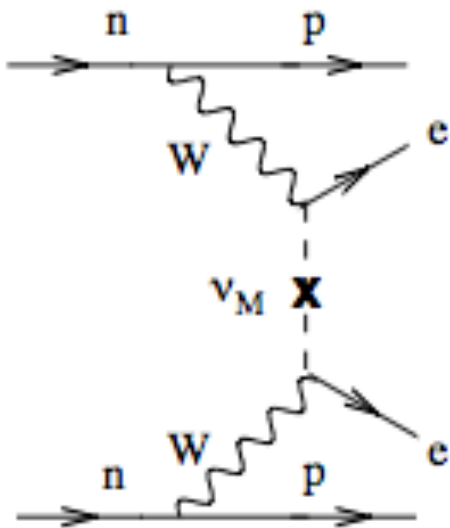
Fermi-era of neutrino physics



Neutrinoless $\beta\beta$ decay: Majorana nature ?

$\Lambda > 100 \text{ MeV}$

$$m_{\beta\beta} = \sum_{i=1}^3 [(U_{PMNS})_{ei}]^2 m_i$$



Capozzi et al '16

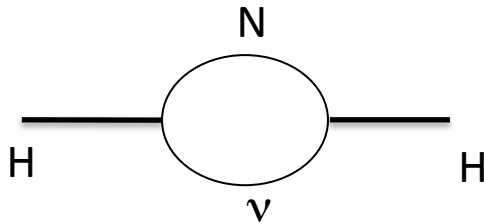
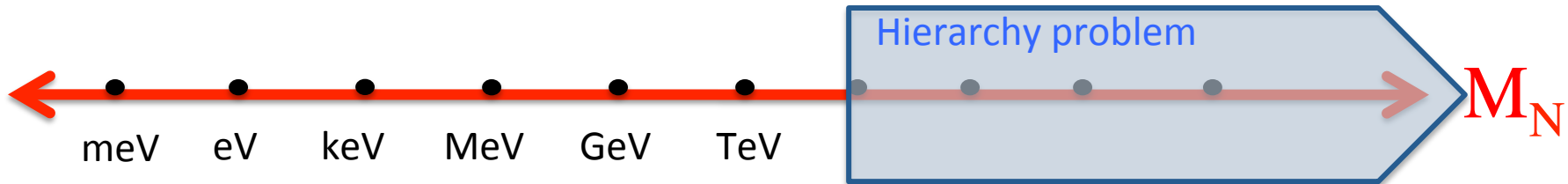
What originates Weinberg's operator?

Could be $\Lambda \gg v \dots$ the standard lore (theoretical prejudice ?)

$$\left. \begin{array}{l} \Lambda = M_{\text{GUT}} \\ \lambda \sim \mathcal{O}(1) \end{array} \right\} m_\nu \checkmark$$

To avoid fine-tuning

The new scale is stable under radiative corrections due to Lepton Number symmetry but the EW is not!



$$\delta m_H^2 = \frac{Y^\dagger Y}{4\pi^2} M_N^2 \log \frac{M_N}{\mu}$$

Vissani

$M_N \gg m_H$ not natural in the absence of SUSY

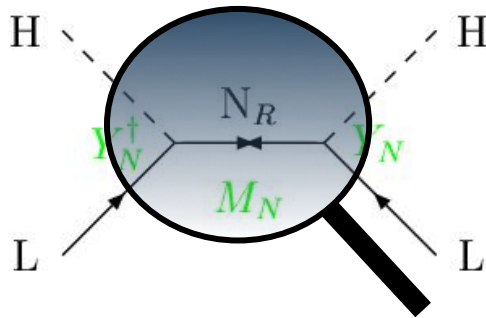
What originates Weinberg's operator?

- sensitivity to neutrino masses comes from very low-energy processes: Weinberg's operator description OK for neutrino masses even if $\Lambda < v \dots$
- λ in front of Weinberg operator might be naturally different to SM Yukawa couplings

Resolving Weinberg's operator at tree level

E. Ma

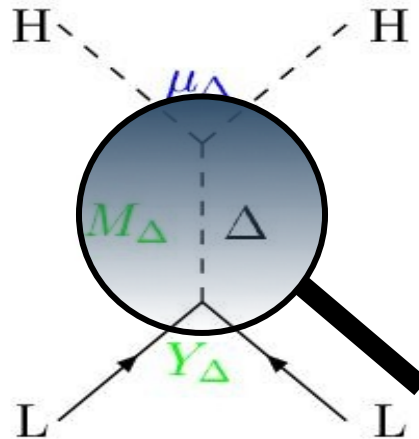
Type I see-saw:
a heavy singlet scalar



$$m_\nu = \frac{\alpha v^2}{\Lambda} \equiv Y_N^T \frac{v^2}{M_N} Y_N$$

Minkowski; Yanagida;
Glashow;
Gell-Mann, Ramond Slansky;
Mohapatra, Senjanovic...

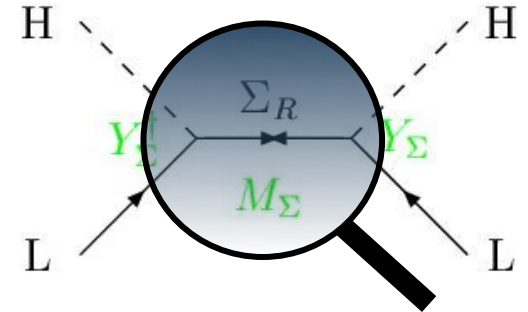
Type II see-saw:
a heavy triplet scalar



$$m_\nu = \frac{\alpha v^2}{\Lambda} \equiv Y_\Delta \frac{\mu_\Delta}{M_\Delta^2} v^2$$

Konetschny, Kummer;
Cheng, Li;
Lazarides, Shafi, Wetterich ...

Type III see-saw:
a heavy triplet fermion

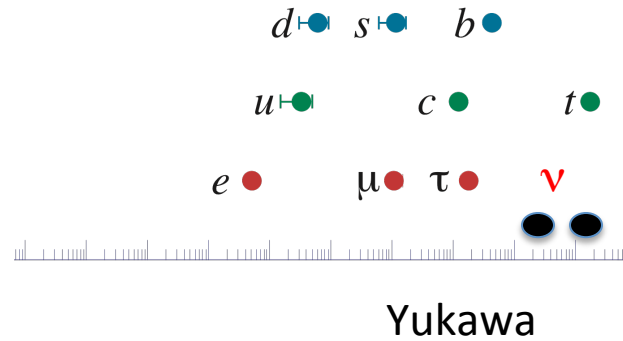


$$m_\nu = \frac{\alpha v^2}{\Lambda} \equiv Y_\Sigma^T \frac{v^2}{M_\Sigma} Y_\Sigma$$

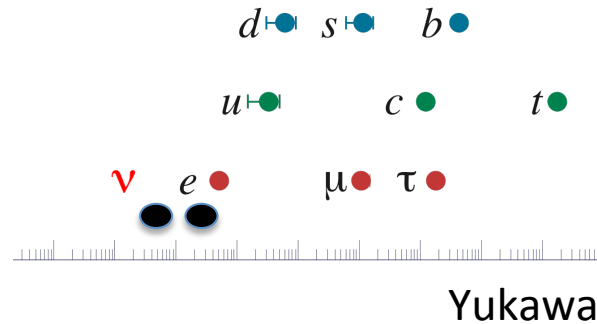
Foot et al; Ma;
Bajc, Senjanovic...

Pinning down the new physics scale: naturalness

$M \leq \text{GUT}$

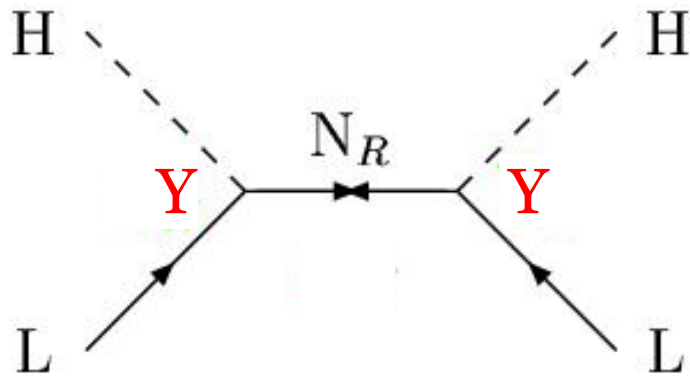


$M = \text{TeV}$

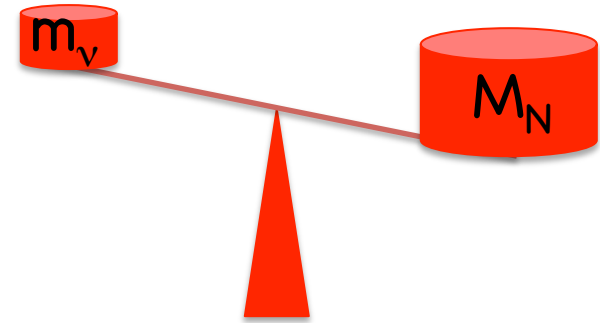


Minimality: SM+right-handed neutrinos

$$\mathcal{L}_\nu = -\bar{l}Y\tilde{\Phi}N_R - \frac{1}{2}\bar{N}_RMN_R + h.c.$$



$$n_R \geq 2$$

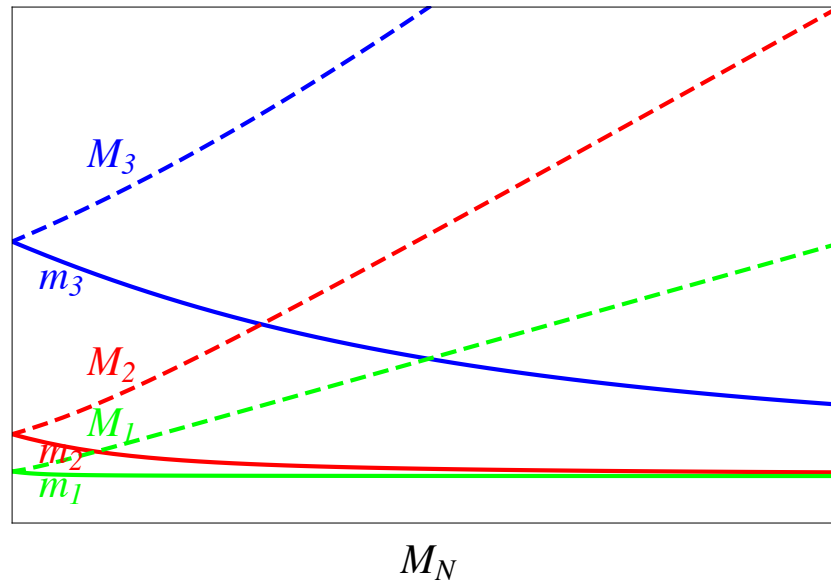


$$m_\nu = \lambda \frac{v^2}{\Lambda} \equiv Y^T \frac{v^2}{M} Y$$

Minkowski; Yanagida; Glashow; Gell-Mann, Ramond Slansky; Mohapatra, Senjanovic...

Type I seesaw models

$n_R = 3$: 18 free parameters (6 masses+6 angles+6 phases) out of which we have measured 2 masses and 3 angles...

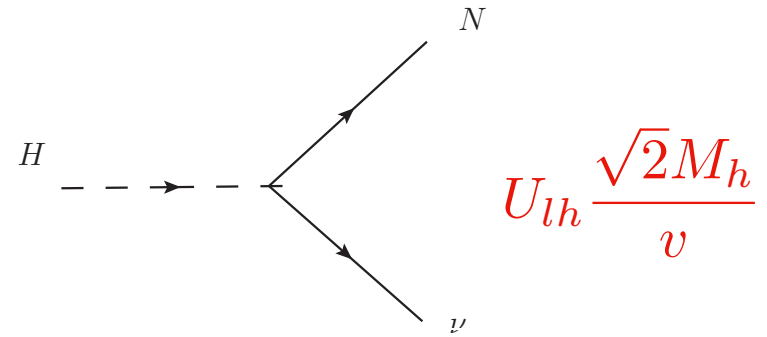
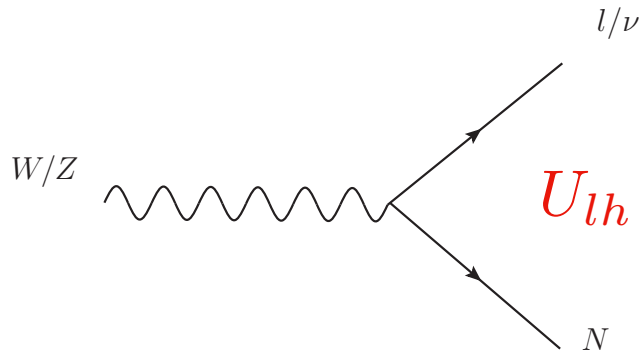


Type I seesaw models

Phenomenology (beyond neutrino masses) of these models depends on the heavy spectrum and the size of active-heavy mixing:

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = U_{ll} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix} + U_{lh} \begin{pmatrix} N_1 \\ N_2 \\ N_3 \end{pmatrix}$$

Type I seesaw models



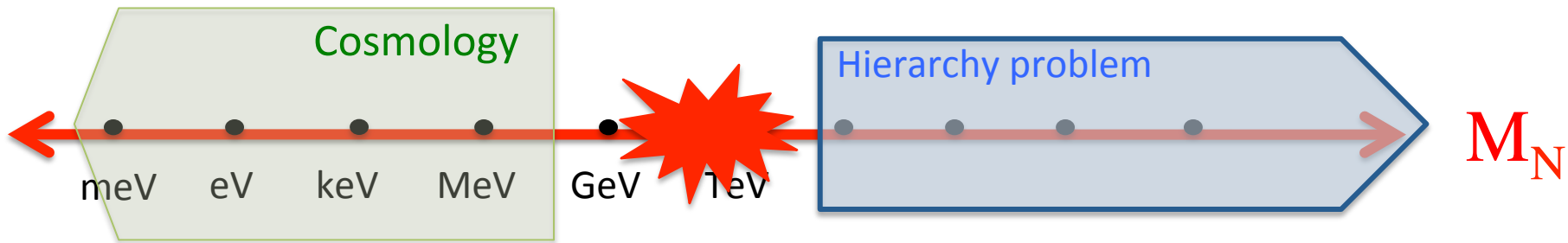
$$U_{lh} \simeq iU_{\text{PMNS}} \sqrt{m_l} R \frac{1}{\sqrt{M_h}}$$

Casas-Ibarra

R: general orthogonal complex matrix (contains all the parameters we cannot measure in neutrino experiments)

Strong correlation between active-heavy mixing and neutrino masses, but the naive scaling ($|U_{lh}|^2 \sim m_l/M_h$) too naive...

Pinning down the New physics scale



Sterile neutrinos below 100MeV can strongly modify

Big-Bang Nucleosynthesis

Cosmic Microwave background

Large Scale structure

Notzold, Raffelt; Barbieri&Dolgov; Kainulainen....;
Dolgov, Hansen, Raffelt, Semikoz;
Ruchayskiy, Ivashko; Vincent et al;

Either they contribute too much radiation or too much matter, modifying in unacceptable ways the expansion history and/or growth of perturbations

Sterile neutrinos @ early Universe

The extra states contribute to the energy density of the Universe:

$T < T_{EW}$ produced via mixing...

$$\Gamma_{s_i} \simeq \sum_{\alpha} \langle P(\nu_{\alpha} \rightarrow \nu_{s_i}) \rangle \times \Gamma_{\nu_{\alpha}}$$

Barbieri&Dolgov; Kainulainen

Thermalisation will occur if for some T:

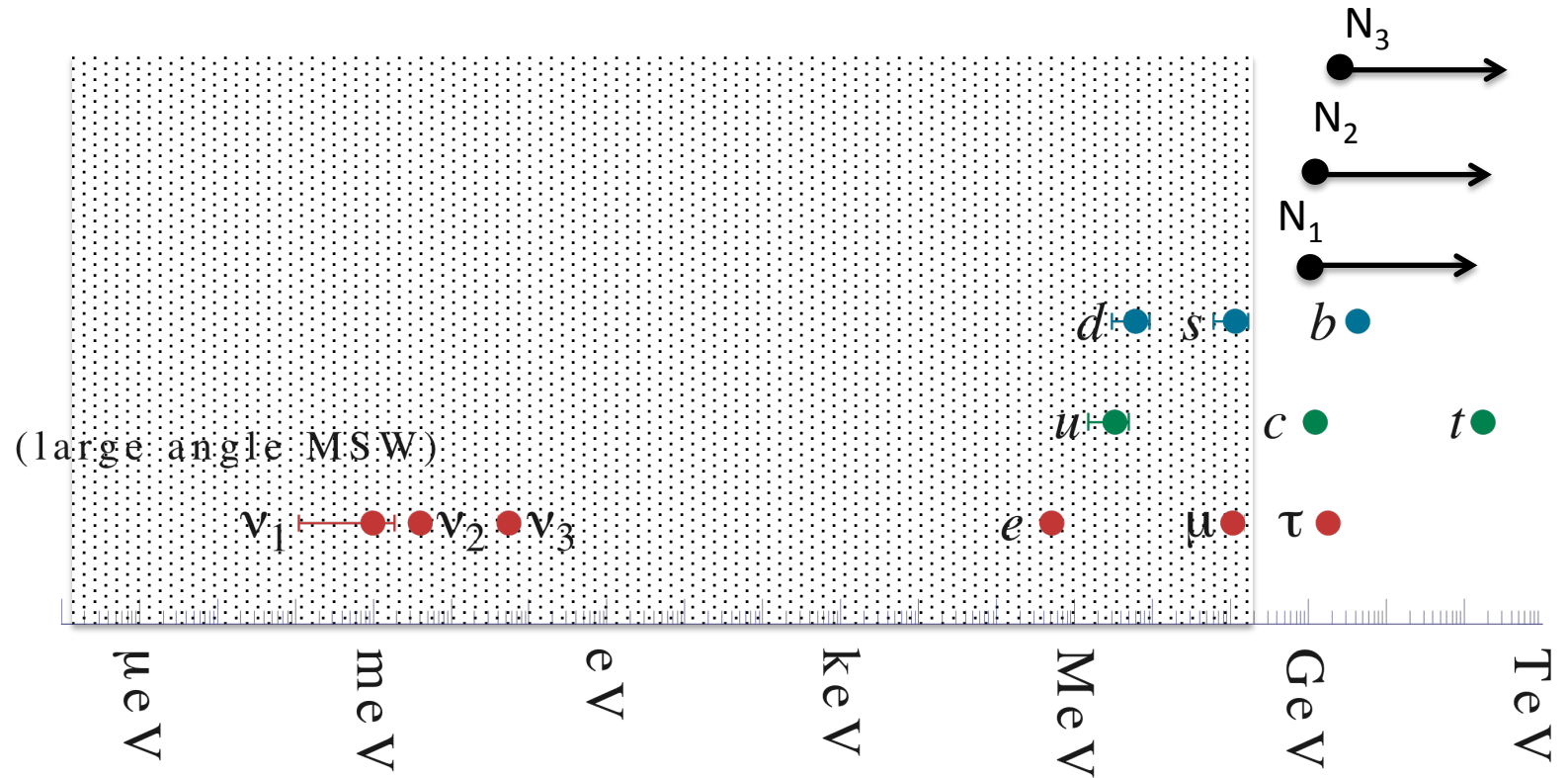
$$\frac{\Gamma_{s_i}(T)}{H(T)} \geq 1$$

$$\frac{\Gamma_{s_i}(T_{\max})}{H(T_{\max})} \sim \frac{\sum_{\alpha} |U_{\alpha s_i}|^2 M_i}{\sqrt{g_*(T_{\max})}}$$

independent of M ?

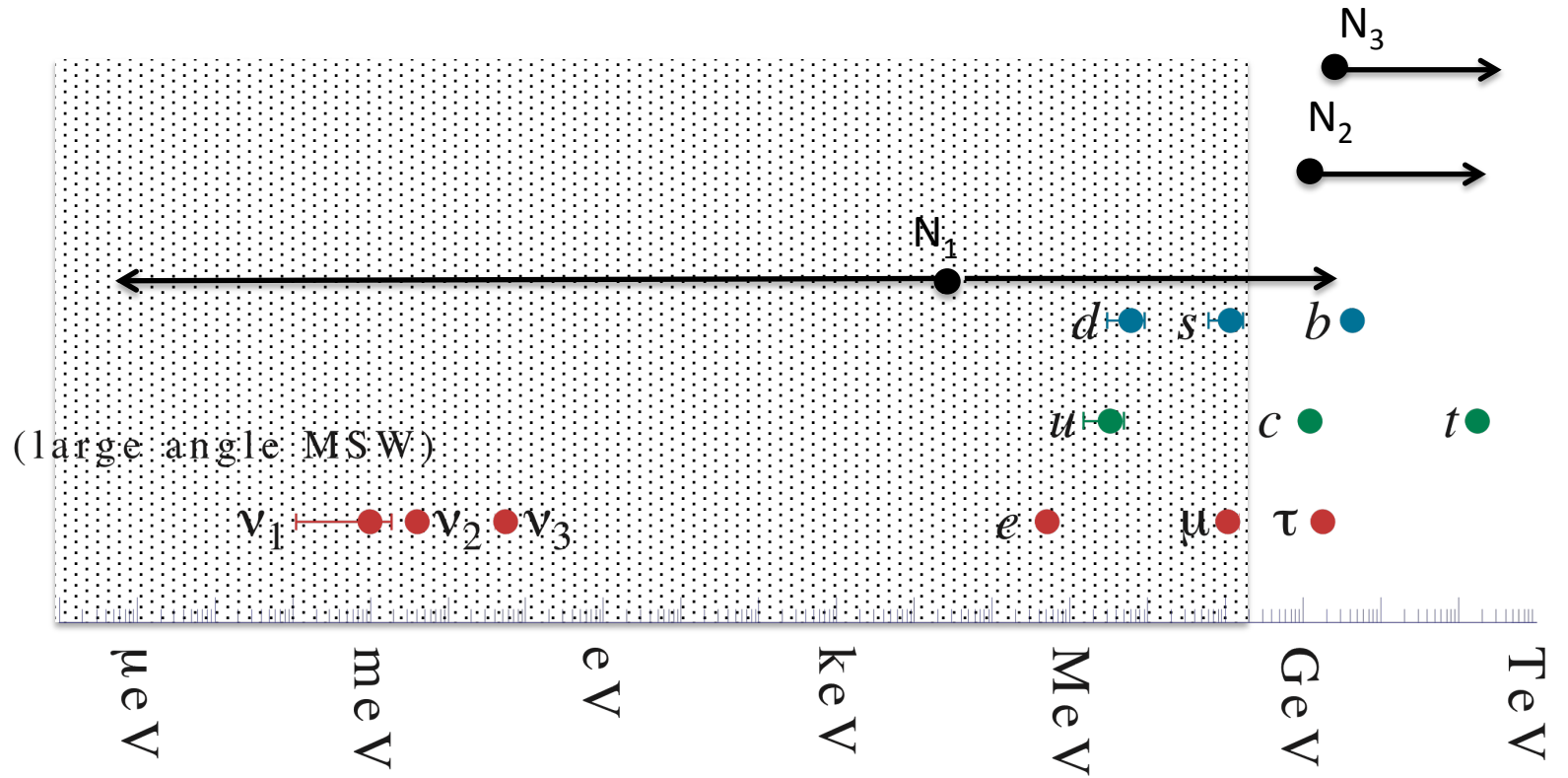
Seesaw scale vs cosmology

Type I seesaw $N = 3$ that explains neutrino masses



$$m_{\text{lightest}} > 3.2 \times 10^{-3} \text{ eV}$$

Type I seesaw N = 3 that explains neutrino masses

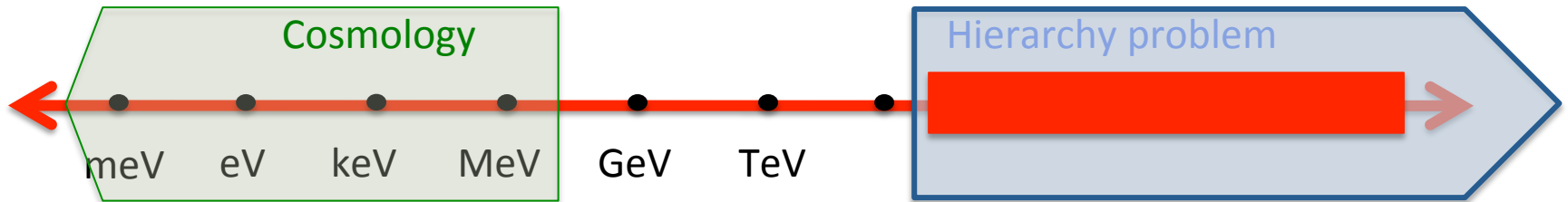


$$m_{\text{lightest}} < 3.2 \times 10^{-3} \text{ eV}$$

PH, M. Kevic, J. López-Pavon

$M_1 = O(\text{keV})$ WDM candidate! **νMSM** Shaposhnikov et al

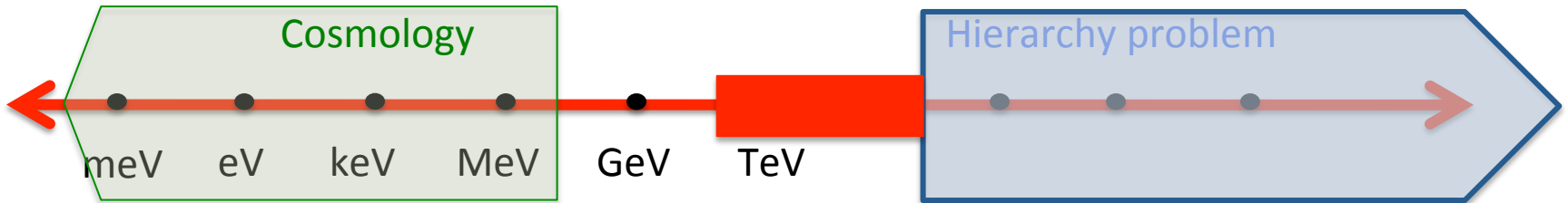
Leptogenesis



Standard leptogenesis in out-of-equilibrium
decay $M > 10^7 \text{ GeV}$

Fukuyita, Yanagida;....

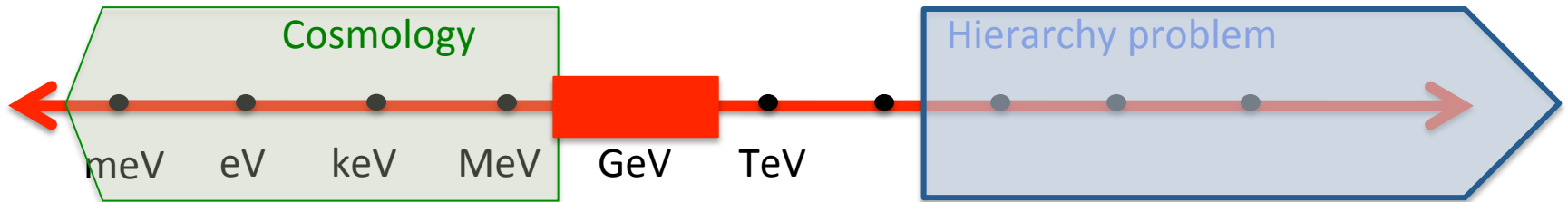
Leptogenesis



Resonant leptogenesis $M > 100 \text{ GeV}$

Pilaftsis...

Leptogenesis



Leptogenesis from neutrino oscillations
 $0.1\text{GeV} < M < 100\text{GeV}$

Akhmedov, Rubakov, Smirnov

Sakharov conditions

- ✓ CP violation (up to 6 new CP phases in the lepton sector)

$$Y = V^\dagger \text{Diag}(y_1, y_2, y_3) W$$

(V, W : 3 phases each)

Sakharov conditions

- ✓ CP violation (up to 6 new CP phases in the lepton sector)

$$Y = U_{\text{PMNS}}^* \sqrt{m_\nu} R \sqrt{M_h} \frac{\sqrt{2}}{v}$$

Casas-Ibarra

(R : 3 complex angles + U_{PMNS} : 3 phases)

Sakharov conditions

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Casas-Ibarra

(R : 3 complex angles + U_{PMNS} : 3 phases)

- ✓ B+L violation from sphalerons $T > T_{\text{EW}}$

Sakharov Conditions

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Casas-Ibarra

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- ✓ B+L violation from sphalerons $T > T_{\text{EW}}$

$$\cancel{L}_\alpha \oplus B \mp \cancel{L}$$

(in contrast with standard leptogenesis in the decay of the heavy states:
the violation of L from Majorana masses is not relevant $M/T \ll 1$)

Sakharov conditions

- ✓ CP violation (up to 6 new CP phases in the lepton sector)

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Casas-Ibarra

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(in contrast with standard leptogenesis in the decay of the heavy states:
the violation of L from Majorana masses is not relevant $M/T \ll 1$)

- ✓ Out of equilibrium: some states have not reached equilibration at T_{EW}

ARS Leptogenesis

Akhmedov, Rubakov, Smirnov

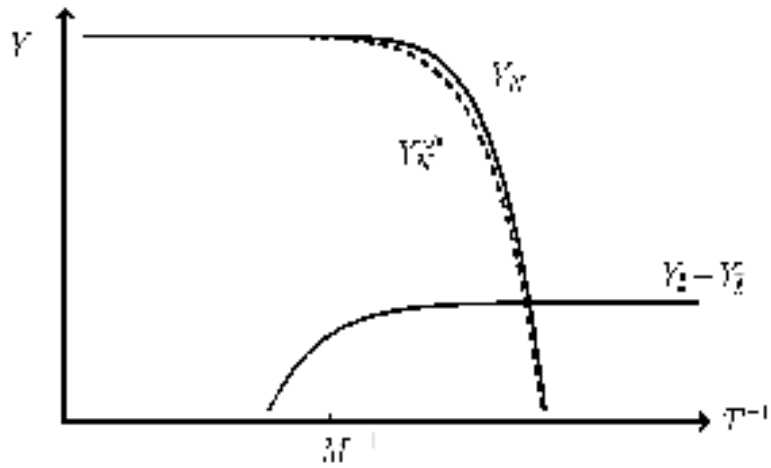
$$\Gamma_s(T) \sim y^2 T \sim \frac{M_N m_\nu}{v^2} T \qquad H(T) = \sqrt{\frac{4\pi^3 g_*(T)}{45}} \frac{T^2}{M_P}$$

$$\frac{\Gamma_s(T_{EW})}{H(T_{EW})} \sim 5 \left(\frac{M}{1\text{GeV}} \right) \left(\frac{m_\nu}{0.05\text{eV}} \right)$$

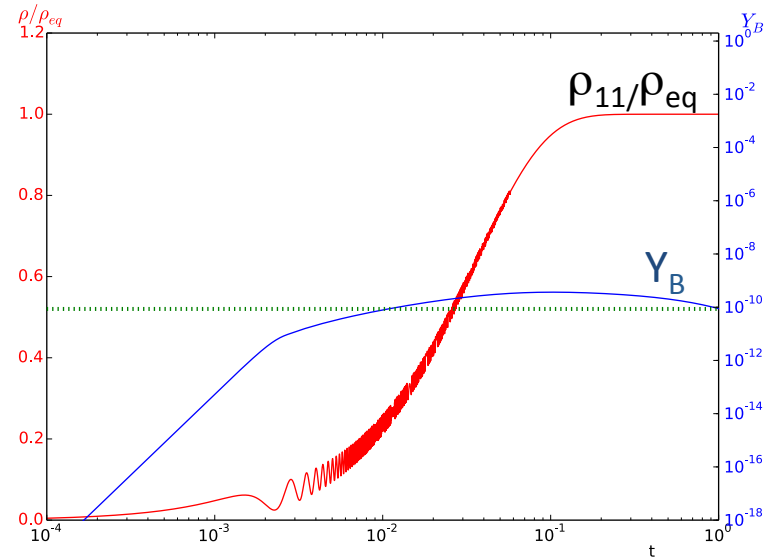
$$y_3 \ll y_1, y_2$$

CP asymmetries arise in production of sterile states via the interference of CP-odd phases and CP-even phases from oscillations

High-scale leptogenesis



Low-scale leptogenesis



T_{EW}

Courtesy of M. Kekic

Low-scale Leptogenesis

Asaka, Shaposhnikov; Shaposhnikov, Asaka, Eijima, Ishida; Canetti, Drewes, Frossard, Shaposhnikov; Drewes, Garbrecht; Shuve, Yavin; Abada, Arcadi, Domcke, Lucente; PH, Kekic, Lopez-Pavón, Racker, Rius

Raffelt-Sigl kinetic equations: quantum evolution of number density matrices of the sterile species:

$$\rho_{ss'}(\mathbf{p}) = \langle \hat{a}_s^\dagger(\mathbf{p}, t) \hat{a}_{s'}(\mathbf{p}, t) \rangle \quad \mathbf{M}/\mathbf{T} \ll 1$$

$$\frac{d\rho(k)}{dt} = -i \underbrace{[H, \rho(k)]}_{\text{oscillations}} - \underbrace{\frac{1}{2} \{ \Gamma_N^a, \rho(k) \} + \frac{1}{2} \{ \Gamma_N^p, 1 - \rho(k) \}}_{\text{scatterings}}$$

$$H \equiv \frac{\Delta M^2}{2k_0} + V_N$$

$$\Gamma_N^a / \Gamma_N^p \propto \mathcal{O}(Y^2)$$

annihilation/production

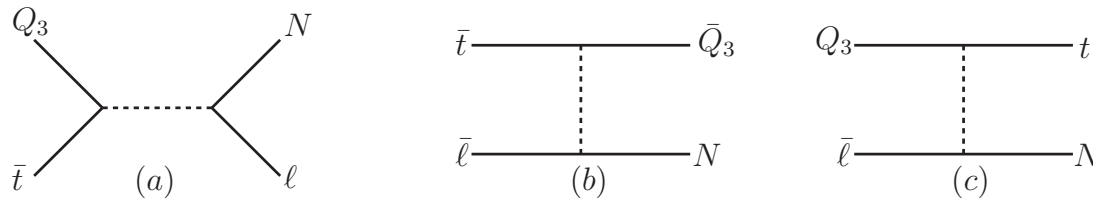
+eq. for $\bar{\rho}$ + evolution of $\mu_{\text{B}/3-\text{L}\alpha}$

Scattering rates

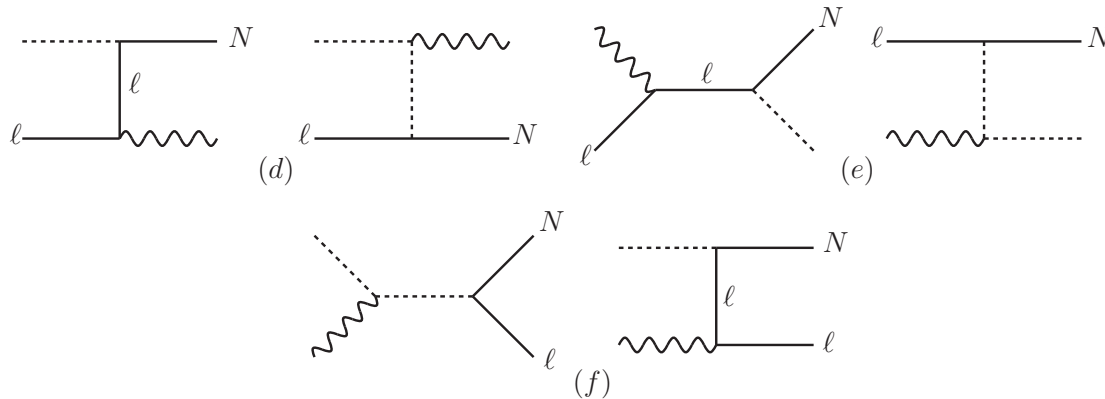
Include all the scattering processes that are believed to be relevant and have been computed

Besak, Bodeker, 1202.1288; Ghisoiu and M. Laine 1411.1765

top



gauge

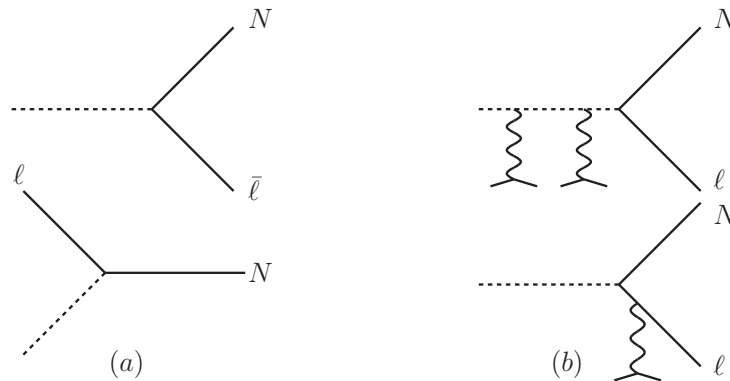


Scattering rates

Include all the scattering processes that are believed to be relevant and have been computed

Besak, Bodeker, 1202.1288; Ghisoiu and M. Laine 1411.1765

Decays+ID



Washouts: Re-evaluated in the presence of μ_α

PH, Kekic, Lopez-Pavon, Racker, Salvado '16

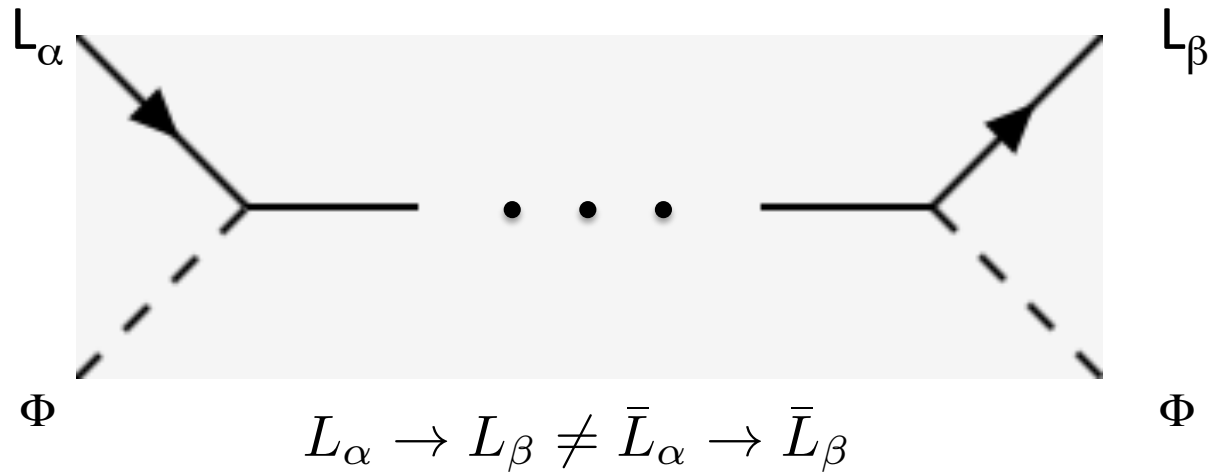
Two time scales relevant in evolution of asymmetries:

$$t_{\text{osc}}(ij) \propto (\Delta M_{ij}^2 M_P^*)^{-1/3} \quad t_{\text{eq}}(\alpha) \propto (Y^2 M_P^*)^{-1}$$

Natural choices of parameters: $t_{\text{osc}} \ll t_{\text{eq}}(\alpha) \lesssim t_{\text{EW}} < t_{\text{eq}}(\beta)$

Stiff differential equations: hard to treat numerically...

CP asymmetries build up in different flavours though “oscillations”:

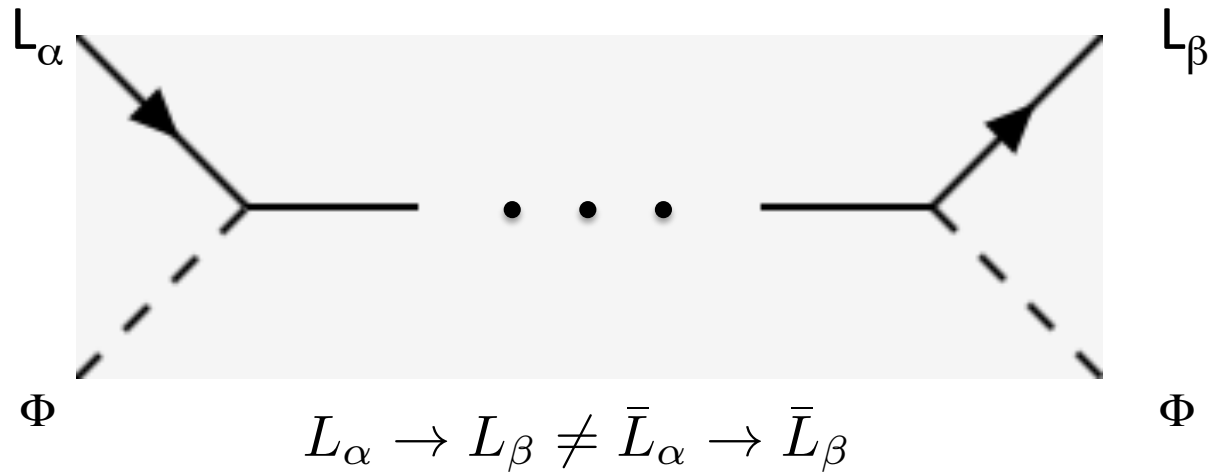


$$Y_B \propto \sum_{\alpha} \Delta_{CP}^{\alpha} \eta_{\alpha} \quad \sum_{\alpha} \Delta_{CP}^{\alpha} = 0$$

$$t > t_{\text{osc}}(ij) : \Delta_{CP}^{\alpha} \propto \text{Im} \left((Y^{\dagger} Y)_{ji} Y_{i\alpha}^{\dagger} Y_{\alpha j} \right)$$

$$\eta_{\alpha} \propto \frac{t}{t_{\text{eq}}(\alpha)}$$

CP asymmetries build up in different flavours though “oscillations”:



$$Y_B \propto \sum_{\alpha} \Delta_{CP}^{\alpha} \eta_{\alpha} \quad \sum_{\alpha} \Delta_{CP}^{\alpha} = 0$$

$$t > t_{eq}(\alpha) : \eta_{\alpha} \propto \exp(-t/t_{eq}(\alpha))$$

Analytical results in GeV Leptogenesis

PH, Kekic, Lopez-Pavón, Racker, Rius 1508.03676

Equations can be solved analytically quite accurately in a perturbative expansion **in mixing angles** of V, W to third order for $y_3 \ll y_1, y_2$

$$Y_B \propto \sum_{I_{CP}} I_{CP} A_{I_{CP}}(t), \quad I_{CP} = \underbrace{I_1^{(2)}, I_2^{(3)}, I_2^{(3)}, J_W}_{\text{Rephasing invariants (like } J_{ckg})}$$

Rephasing invariants (like J_{ckg})

One example (first vMSM invariant)

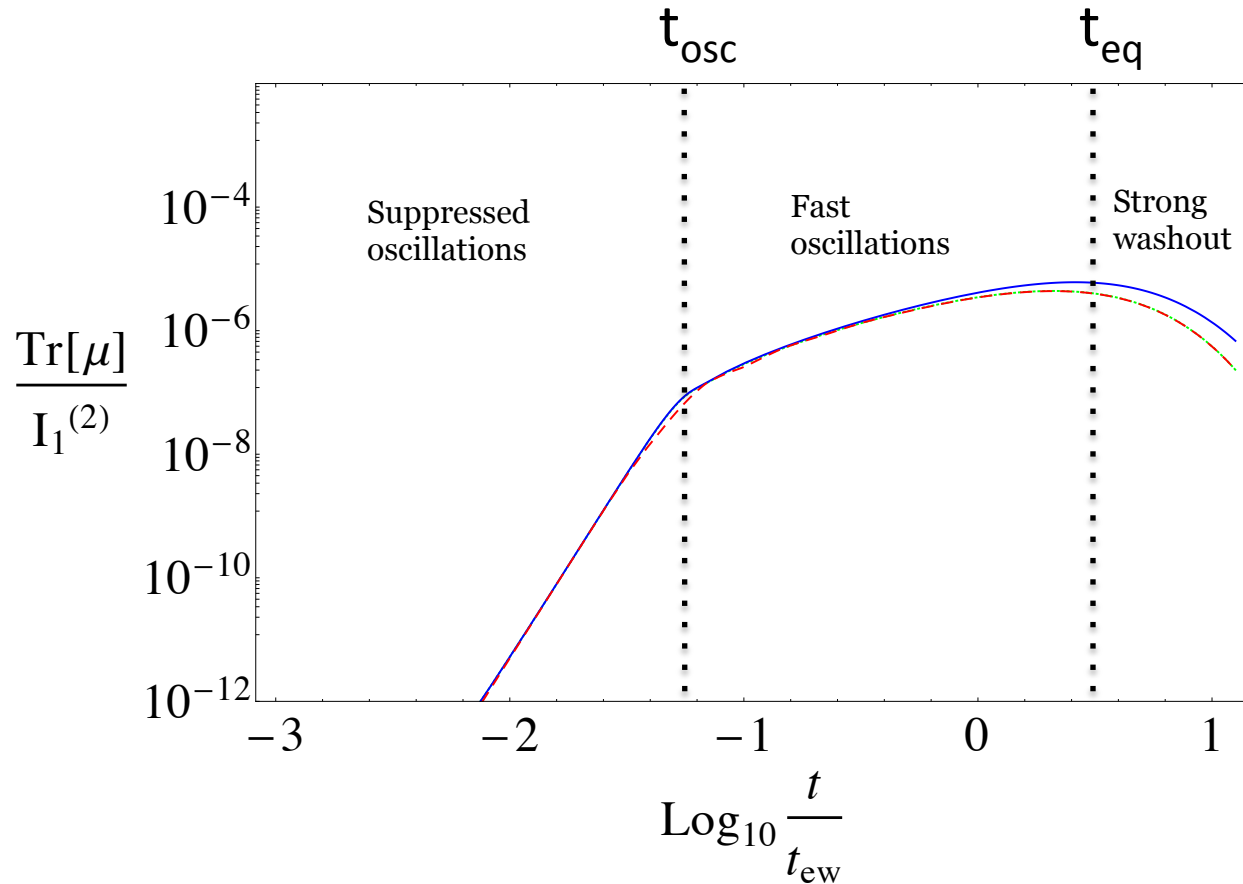
$$A_{I_1^{(2)}}(t) = y_1 y_2 (y_2^2 - y_1^2) \left(1 - \frac{\gamma_N}{\bar{\gamma}_N} \right) \gamma_N^2 G_1(t),$$

$$G_1(t) \equiv \left(e^{-\bar{\gamma}_2 t} - e^{-\bar{\gamma}_1 t} \right) \text{Re} [i J_{20}(\Delta_{12}, -\Delta_{12}, t) + 2\Delta_v J_{201}(\Delta_{12}, -\Delta_{12}, t)] \\ + \frac{1}{2} \sum_{k=1}^2 (-1)^k e^{-\bar{\gamma}_k t} \text{Re} [J_{210}(\Delta_{12}, -\Delta_{12}, t) (-2\Delta_v + i(2\bar{\gamma}_k - \gamma_1 - \gamma_2))],$$

washouts

$$\bar{\gamma}_i \propto y_i^2 \bar{\gamma}_N$$

Analytical vs numerical results



Full exploration of the minimal model N=2

PH, Kekic, López-Pavón, Racker, Salvadó 1606.06719

Bayesian posterior probabilities (using nested sampling Montecarlo Multinest)

$$\mathcal{L} = - \left(\frac{Y_B(\text{param}) - Y_B^{\text{obs}}}{\sigma_{Y_B}} \right)^2$$

Use Casas-Ibarra parametrization: fix light neutrino masses and mixings to the best fit oscillation points (IH/NH) and vary

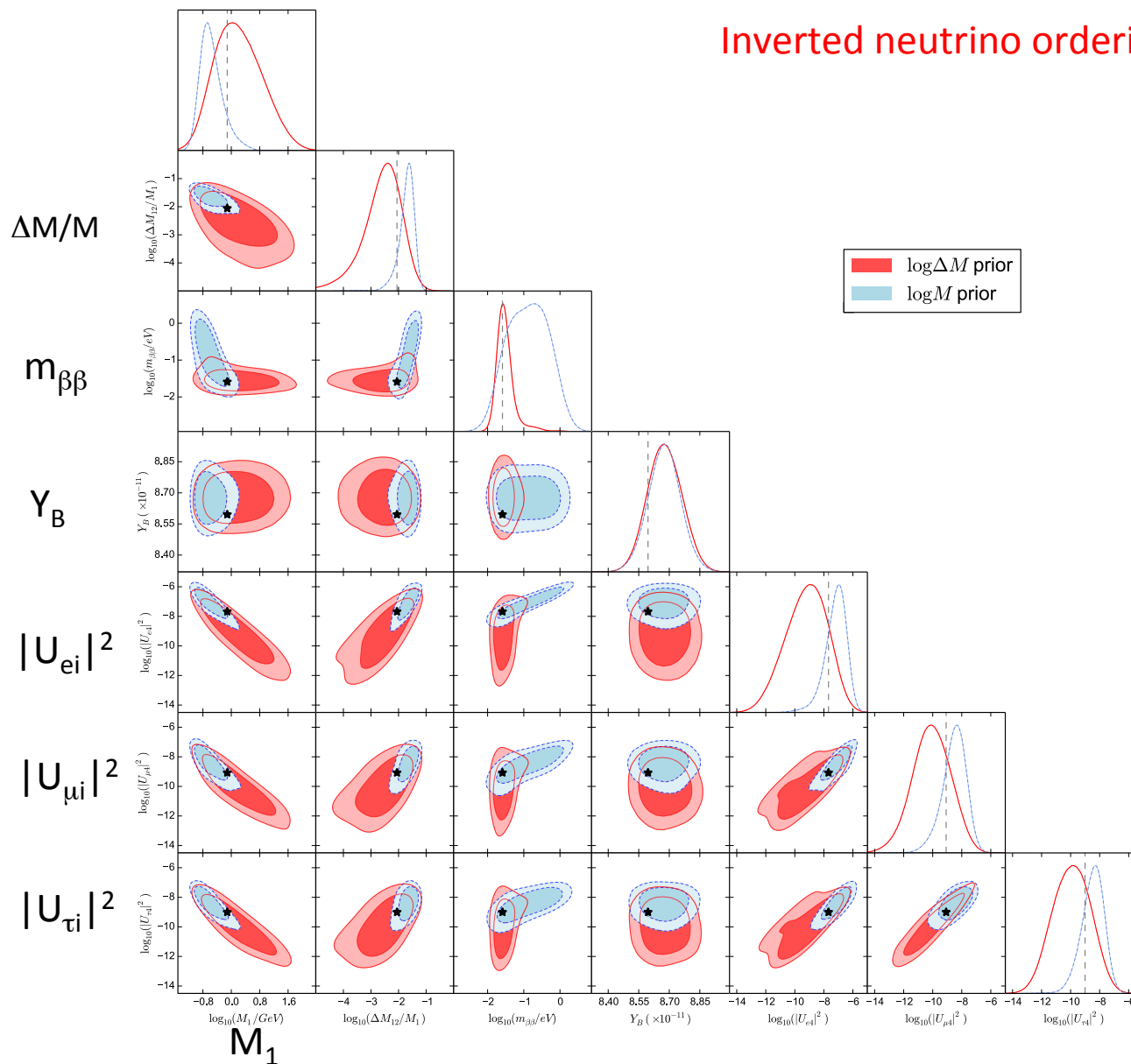
$$R(\theta + i\gamma); U_{PMNS}(\delta, \phi_1); M_1, M_2$$

Flat priors in:

$$\theta = [0, \pi]; \delta = [0, 2\pi]; \phi_1 = [0, 2\pi]; \gamma = [-9, 9]; \\ \log_{10} M_1 \text{ and } \log_{10} M_2 / \log_{10}(M_2 - M_1)$$

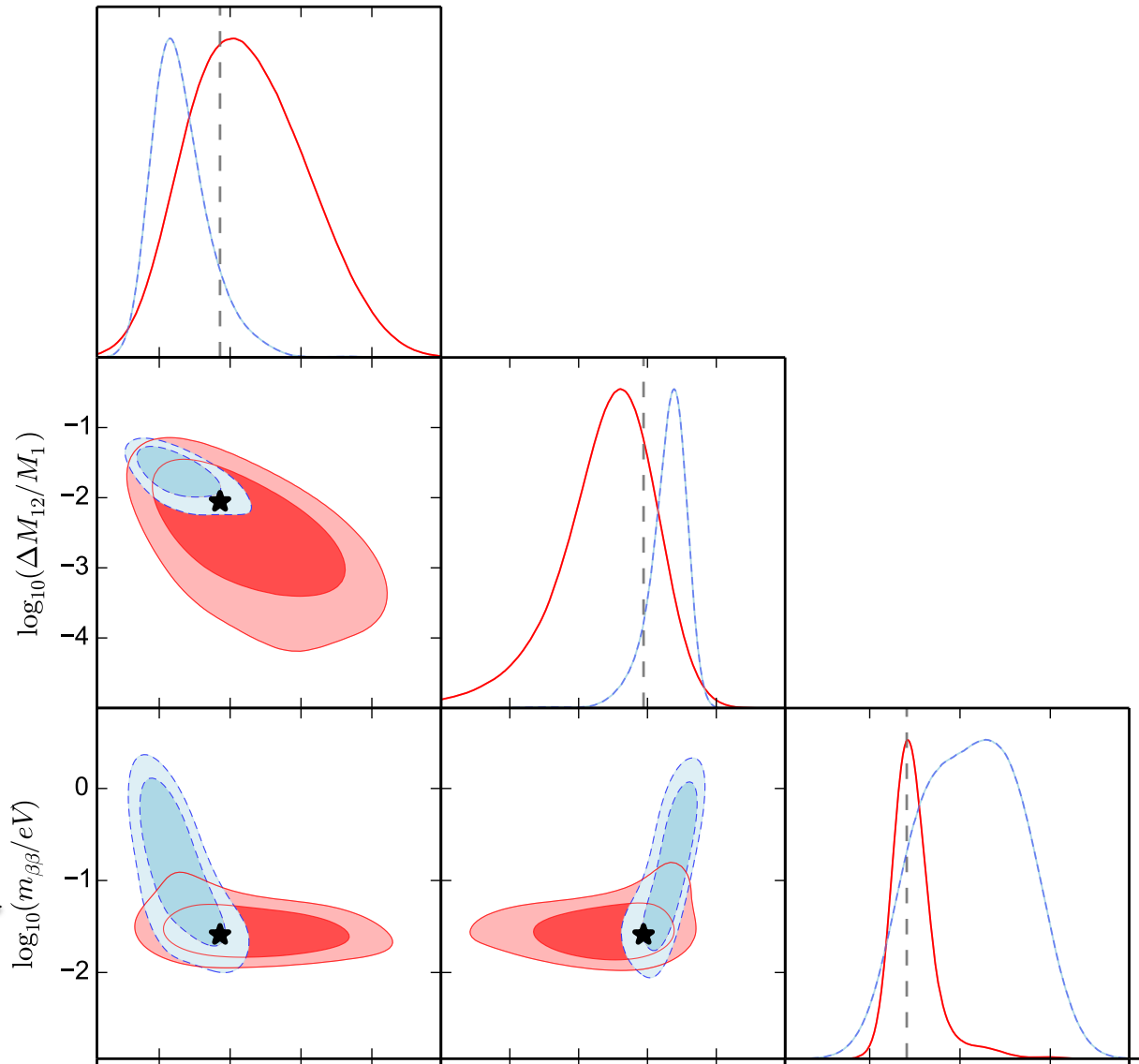
Full exploration of the minimal model N=2

Inverted neutrino ordering (IH)



Full exploration of the minimal model N=2

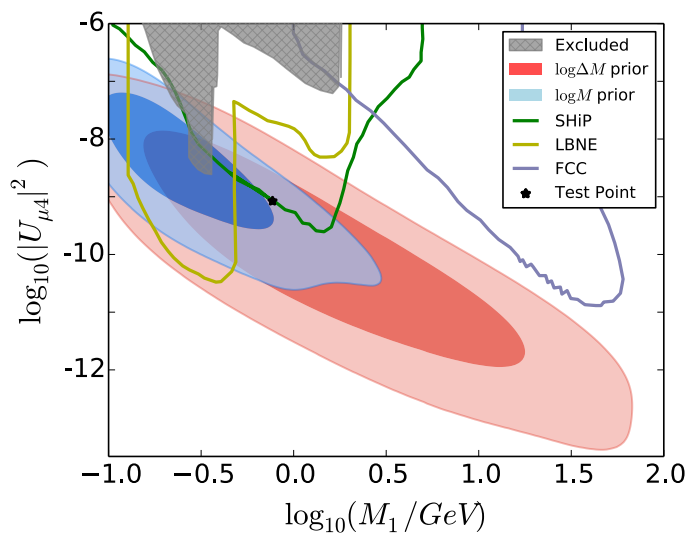
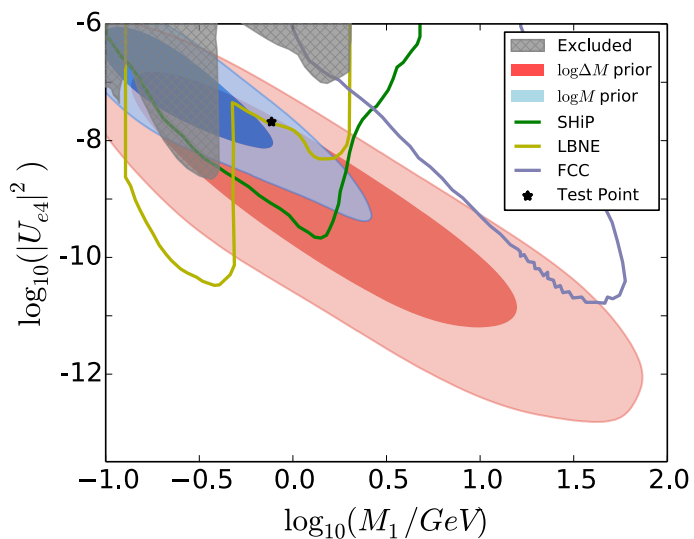
Fine tuning
in masses



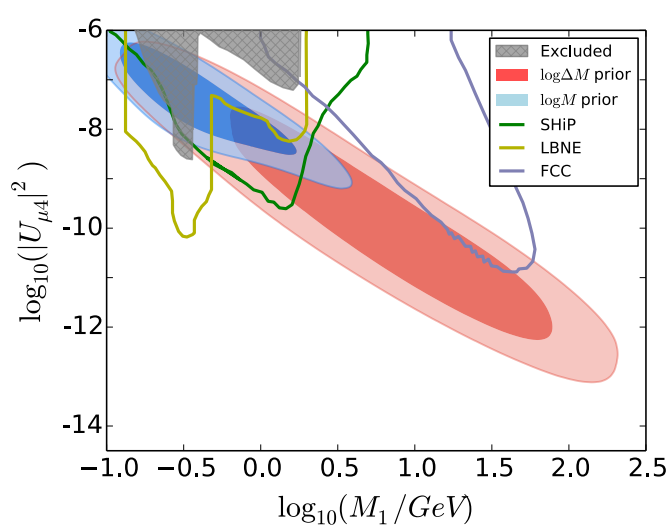
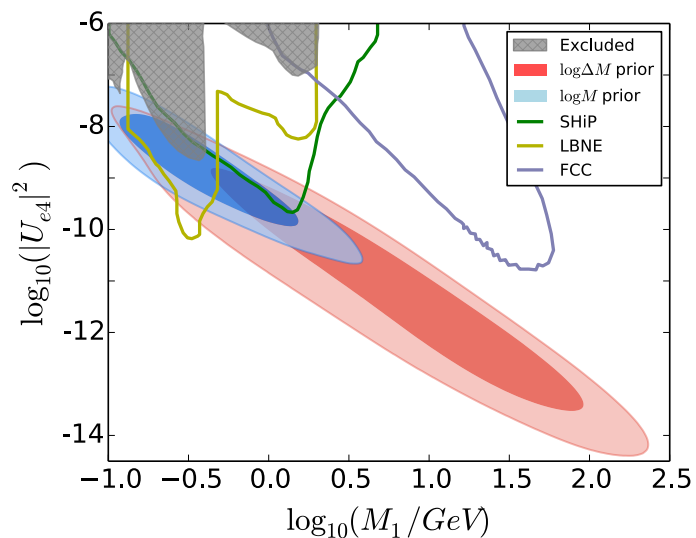
Generically large
non-standard
effect in $\beta\beta 0\nu$



Full exploration of the minimal model N=2



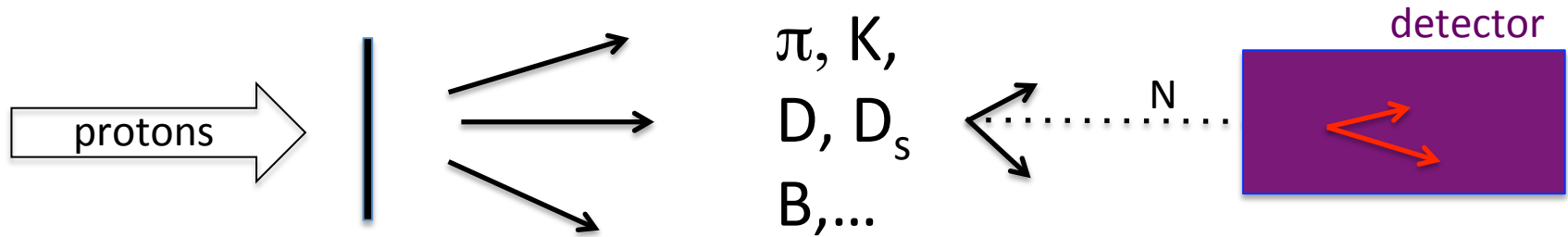
IH



NH

Less fine-tuned region prefers the range of SHiP & DUNE!

Searches in rare meson decays

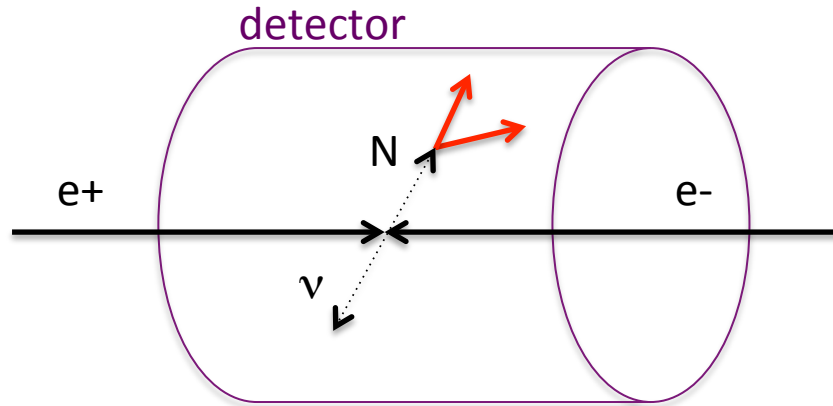


$M < M_K$



$M < M_D$

Searches in $e^+e^- @ Z$



Golden signal: displaced vertex

Predicting Y_B in the minimal model $N=2$ (IH) ?

If the heavy sterile neutrinos would be within reach of SHIP to what extent can we predict the baryon asymmetry from experiment ?

- SHIP measurement could provide (if states not too degenerate)

$$M_1, M_2, |U_{e1}|^2, |U_{\mu1}|^2, |U_{e2}|^2, |U_{\mu2}|^2$$

- Neutrinoless double beta decay amplitude: $|m_{\beta\beta}|$
- Neutrino oscillations: δ phase in the U_{PMNS}

Predicting Y_B in the minimal model N=2 (IH) ?

If the heavy sterile neutrinos would be within reach of SHIP to what extent can we predict the baryon asymmetry from experiment ?

It can be shown that Y_B depends sizeably on every one of the unknown parameters of the model !

Light sector: $U_{\text{PMNS}}(\phi_1, \delta), \Delta m^2_{\text{atm}}, \Delta m^2_{\text{sol}}$

Heavy sector: $M_1, M_2, z = \theta + i \gamma$

Predicting Y_B in the minimal model $N=2$?

From SHIP for **IH**:

$$\epsilon \sim e^{-\gamma} \sim \theta_{13} \sim x \equiv \sqrt{\frac{\Delta m_{\text{sol}}^2}{\Delta m_{\text{atm}}^2}}$$

$$|U_{e4}|^2 M_1 \simeq |U_{e5}|^2 M_2 \simeq A \left[(1 + \sin \phi_1 \sin 2\theta_{12})(1 - \theta_{13}^2) + \frac{1}{2} x^2 s_{12} (c_{12} \sin \phi_1 + s_{12}) + \mathcal{O}(\epsilon^3) \right],$$

$$|U_{\mu 4}|^2 M_1 \simeq |U_{\mu 5}|^2 M_2 \simeq A \left[\left(1 - \sin \phi_1 \sin 2\theta_{12} \left(1 + \frac{1}{4} x^2 \right) + \frac{1}{2} x^2 c_{12}^2 \right) c_{23}^2 \right. \\ \left. + \theta_{13} (\cos \phi_1 \sin \delta - \sin \phi_1 \cos 2\theta_{12} \cos \delta) \sin 2\theta_{23} \right. \\ \left. + \theta_{13}^2 (1 + \sin \phi_1 \sin 2\theta_{12}) s_{23}^2 + \mathcal{O}(\epsilon^3) \right], \quad A \equiv \frac{e^{2\gamma} \sqrt{\Delta m_{\text{atm}}^2}}{4},$$

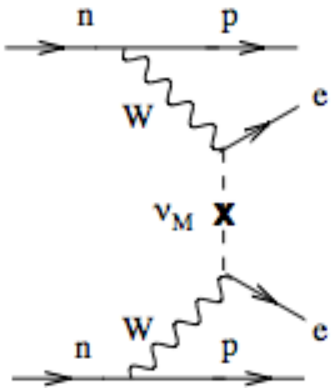
Ratios of e/μ mixings depend on the two phases of the U_{PMNS} matrix: δ, ϕ_1

Amplitude of either: γ

But the baryon asymmetry also depends on the last unknown θ

Predicting Y_B in the minimal model N=2 (IH)

Neutrinoless double beta decay comes to rescue...



$$m_{\beta\beta} = \underbrace{\sum_{i=1}^3 [(U_{PMNS})_{ei}]^2 m_i}_{\text{Light states}} + \underbrace{\sum_{i=j}^3 U_{ej}^2 M_j \frac{\mathcal{M}^{0\nu\beta\beta}(M_j)}{\mathcal{M}^{0\nu\beta\beta}(0)}}_{\text{Heavy states}}$$

$$M_j \rightarrow \infty \quad \frac{\mathcal{M}^{0\nu\beta\beta}(M_j)}{\mathcal{M}^{0\nu\beta\beta}(0)} \propto \left(\frac{100 \text{ MeV}}{M_j} \right)^2$$

The heavy contribution is sizeable for M_i of O(GeV) !

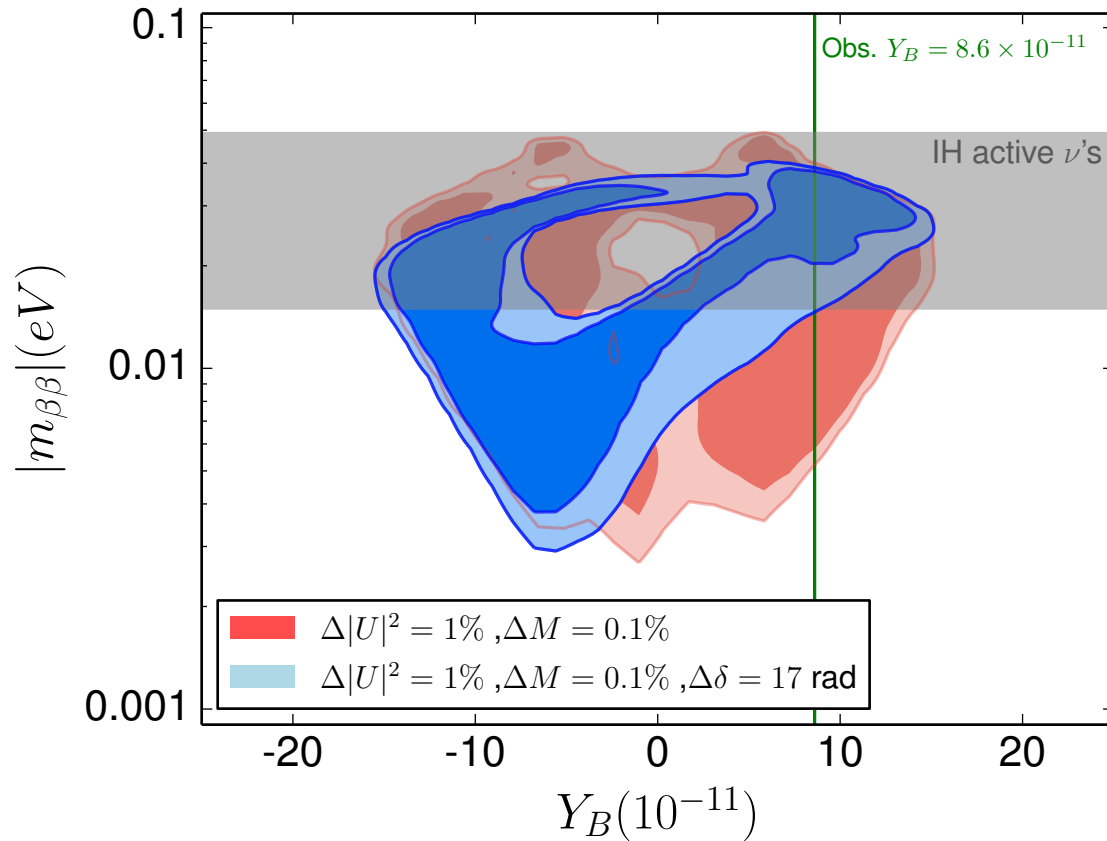
Blennow, Fernandez-Martinez, Lopez-Pavon, Menendez;
Lopez-Pavon, Pascoli, Wong; Lopez-Pavon, Molinaro, Petcov

Predicting Y_B in the minimal model N=2 (IH)

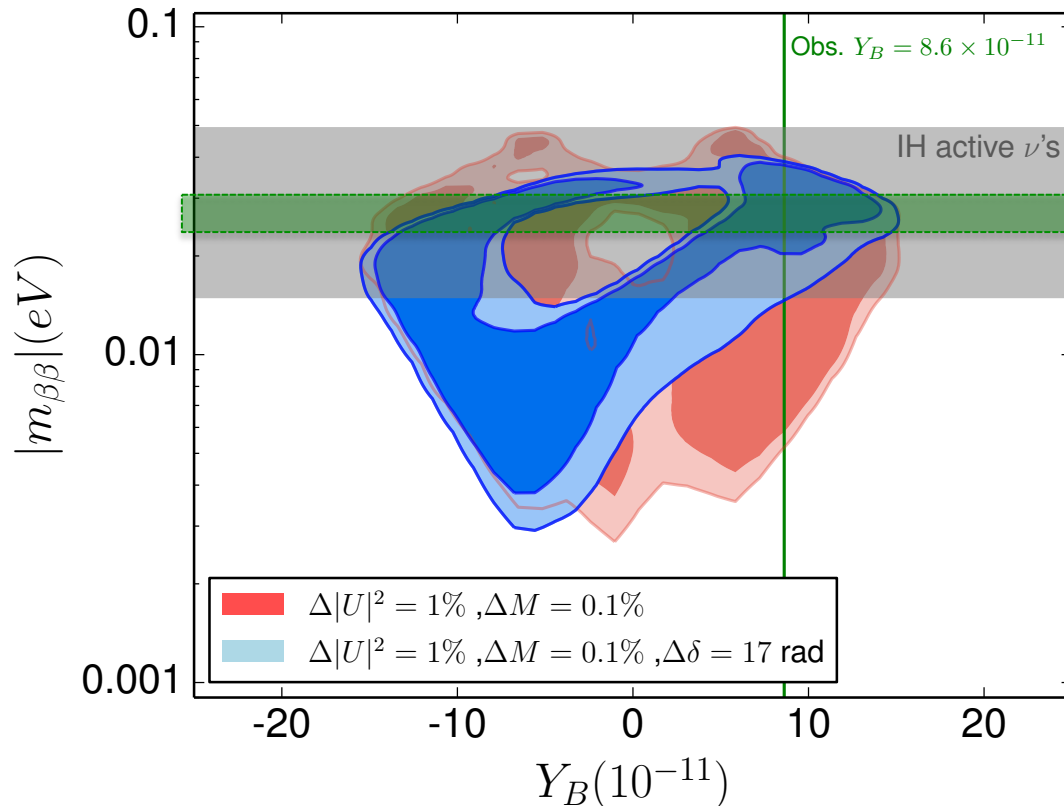
$$\begin{aligned}
 |m_{\beta\beta}|_{IH} \simeq & \sqrt{\Delta m_{atm}^2} \left[\overbrace{c_{13}^2 \left(c_{12}^2 + e^{2i\phi_1} s_{12}^2 \left(1 + \frac{x^2}{2} \right) \right)}^{\text{Light neutrino contribution}} \right. \\
 & \left. - \underbrace{f(A) e^{2i\theta} e^{2\gamma} (c_{12} - ie^{i\phi_1} s_{12})^2 (1 - 2e^{i\delta} s_{23} \theta_{13}) \frac{(0.9 \text{ GeV})^2}{4M_1^2} \left(1 - \left(\frac{M_1}{M_1 + \Delta M_{12}} \right)^2 \right)}_{\text{Heavy neutrino contribution}} \right], \quad (4.13)
 \end{aligned}$$

θ controls the interference of heavy and light contributions !

Predicting Y_B in the minimal model N=2 (IH)

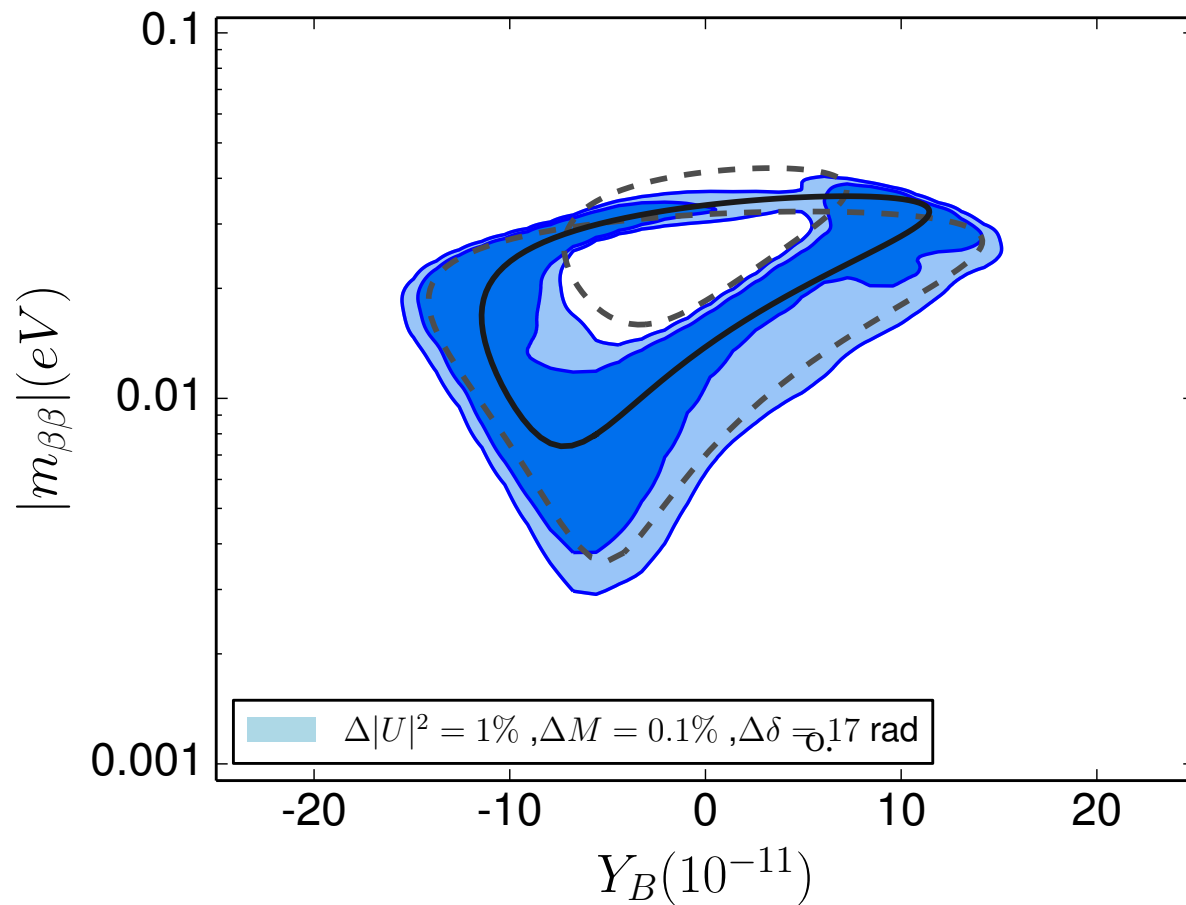


Predicting Y_B in the minimal seesaw model $M \sim \text{GeV}$



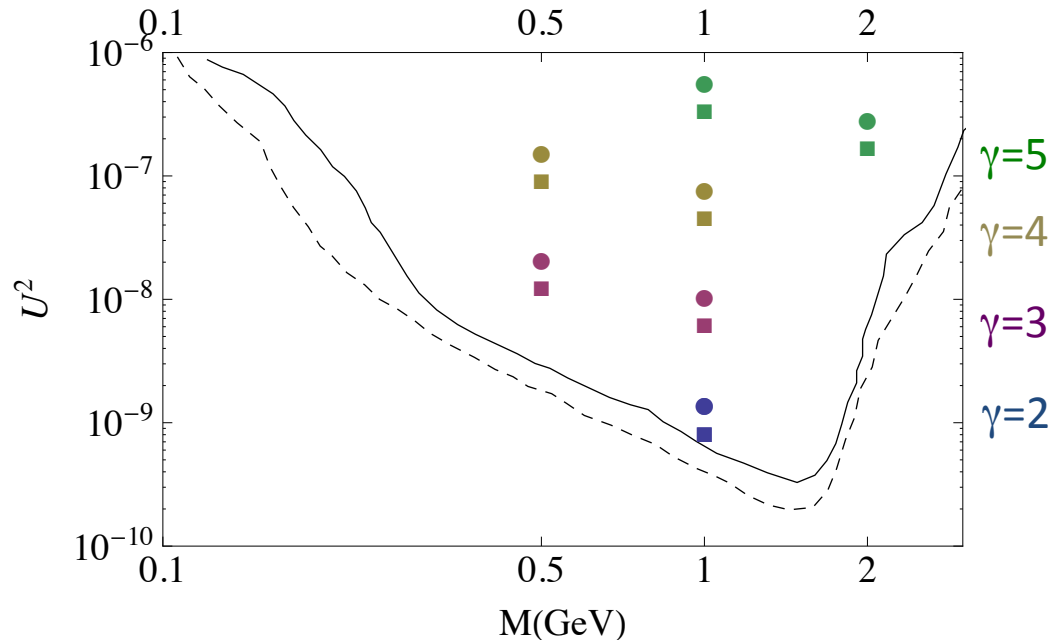
PH, Kekic, López-Pavón, Racker, Salvadó

The GeV-miracle: the measurement of the mixing to e/μ of the sterile states, neutrinoless double-beta decay and δ in neutrino oscillations have a chance to give a prediction for Y_B if IH



Shape can be understood from the residual error in δ :
precision in δ is important !

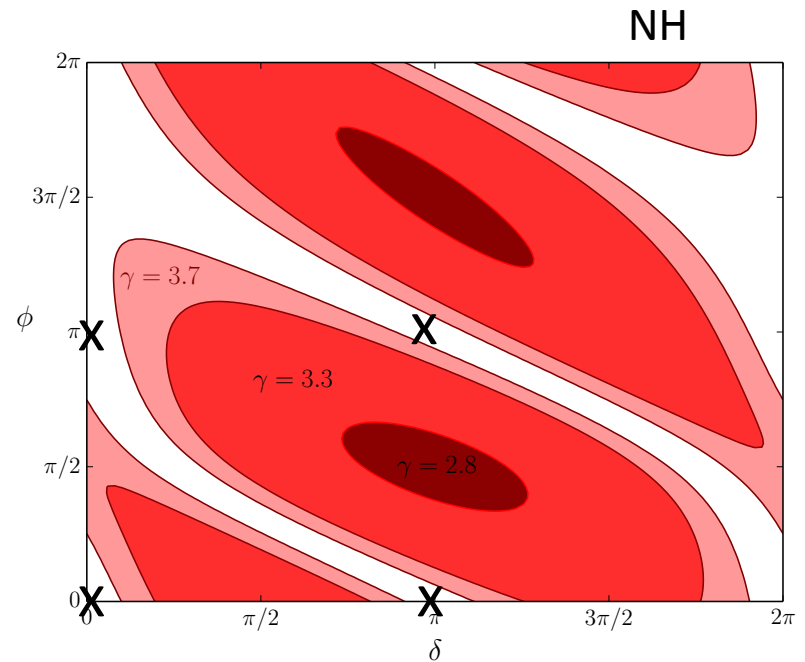
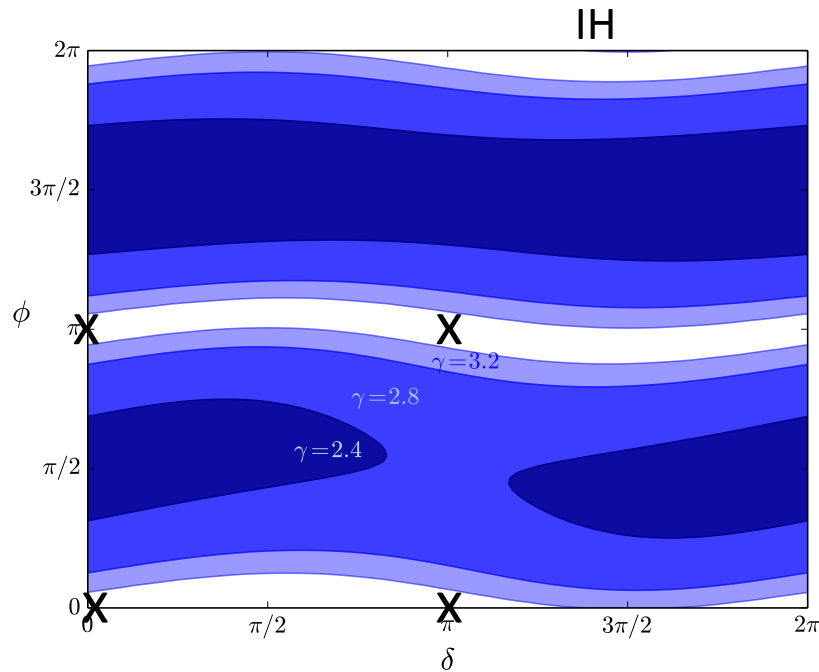
If SHIP measures the heavy neutrinos and their mixings to e/μ :



Can we exclude a real U_{PMNS} matrix ie. discover leptonic CP violation in mixing ?

$$(\delta, \phi_1) \neq (0/\pi, 0/\pi)$$

Leptonic CP violation in U_{PMNS} 5σ CL SHIP discovery regions



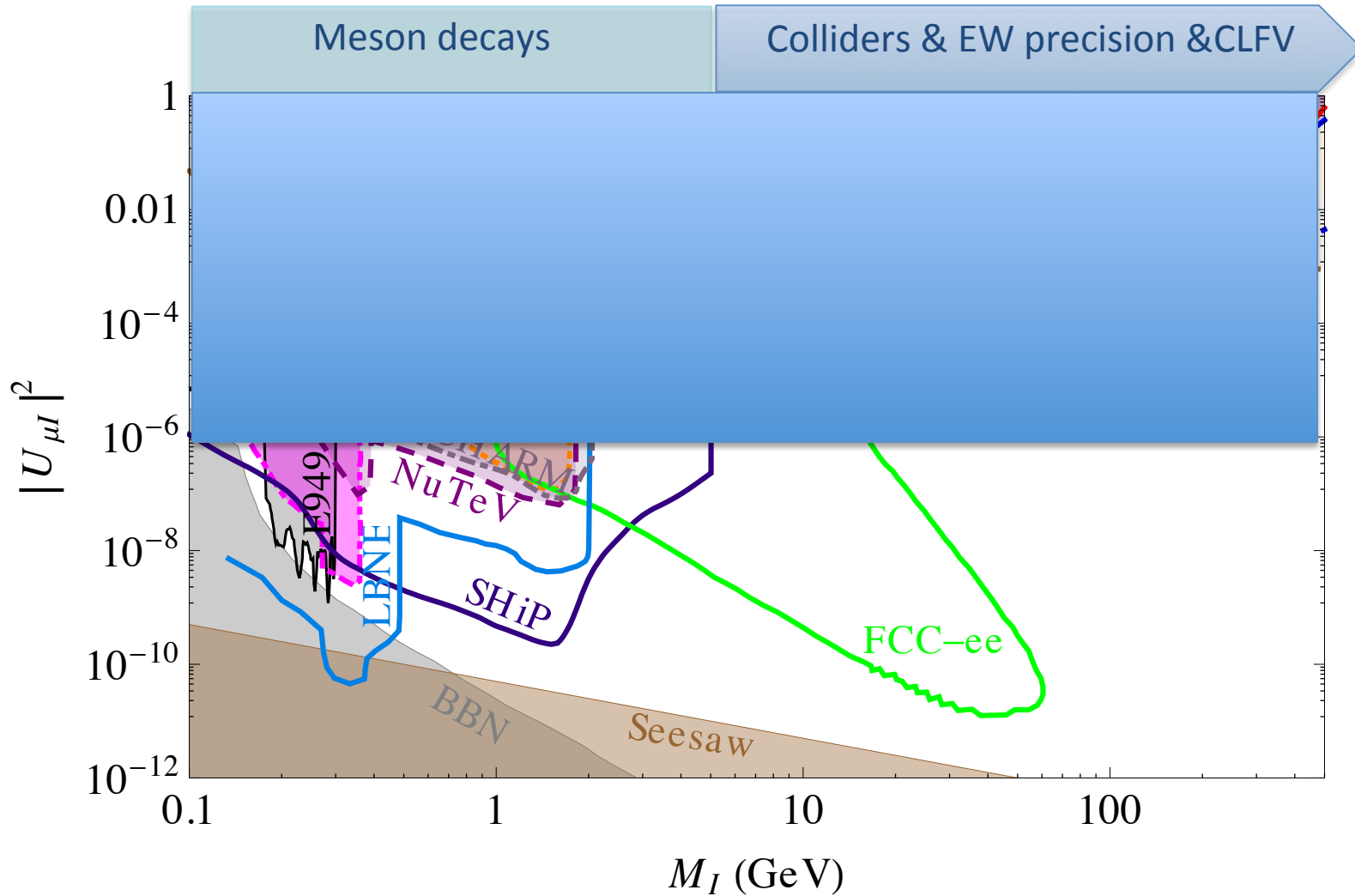
(no systematic error included)

Caputo, PH, Kekic, Lopez-Pavon, Salvado

5σ sensitivity to CP-violation in a large fraction of the CP rectangle !

Larger Mixings ?

Reviews Atre, Han, Pascoli, Zhang; Gorbunov, Shaposhnikov; Ruchayskiy, Ivashko



Bounds only relevant if $|U_{\alpha i}|^2 \gg \frac{m_\nu}{M_i} \leftrightarrow R \gg 1$

Is this natural ?

- In some cases **unnatural**:
cancellation between tree level and 1 loop contribution to neutrino masses
- But also technically-natural textures: Lopez-Pavon, Pascoli, Wang
protected by an approximate global $U(1)_L$

Example N=2: $L(N_1) = +1, L(N_2) = -1$

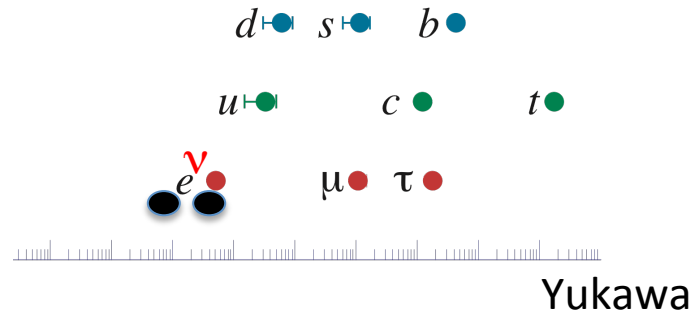
$$-\mathcal{L}_\nu \supset \bar{N}_1 M N_2^c + Y \bar{L} \tilde{\Phi} N_1 + h.c.$$

Eg: inverse, direct seesaw models

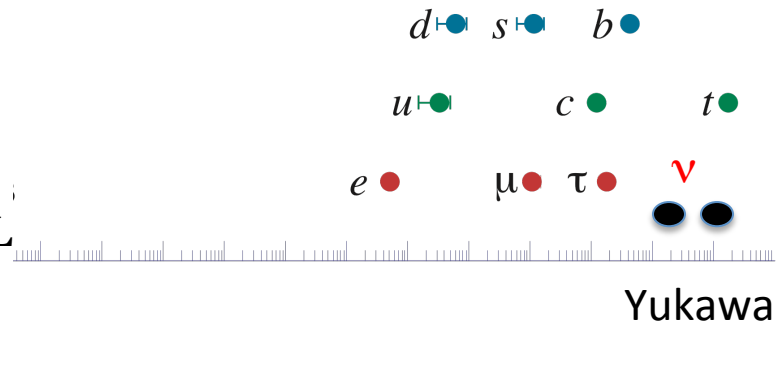
Wyler, Wolfenstein; Mohapatra, Valle; Branco, Grimus, Lavoura, Malinsky, Romao; Kersten, Smirnov; Abada et al; Gavela et al...many others

Charged/neutral hierarchy in seesaw

$$M_N = \text{TeV}$$



$$M_N \leq \text{TeV} + \text{aprox. } U(1)_L$$



Room for improvement in searches at LHC, LFV, future colliders: but must look for **not** lepton number violating processes

Conclusions

- The results of many beautiful experiments have demonstrated that ν are the less standard of the SM particles
- A new scale $\Lambda < \nu$ could explain the smallness of neutrino masses without increasing significantly the flavour hierarchies already existing in the SM
- Low-scale seesaw models can seed the baryon asymmetry in the Universe and do so in a testable way (**GeV region particularly interesting!**)
- Complementarity of different experimental approaches: **$\beta\beta\nu$** , **CP violation in neutrino oscillations**, **direct searches in meson decays**, **colliders...**