

High-Precision Measurement of the Hypertriton Mass








motivation, ideas, concepts, experimental limitations, ...

Patrick Achenbach

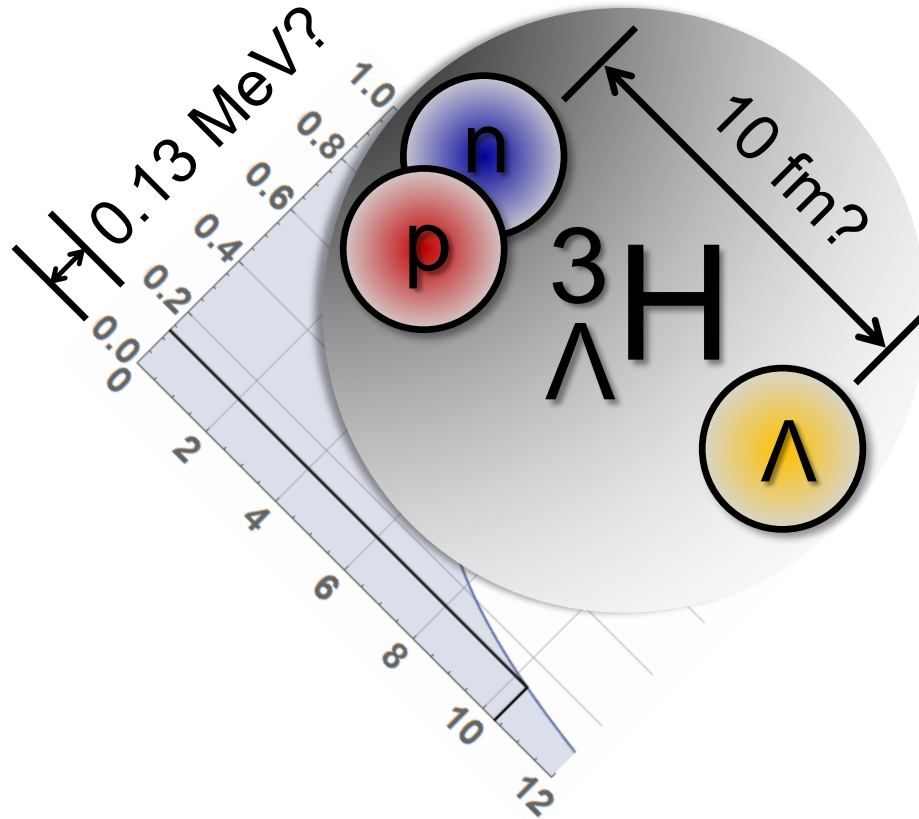
U Mainz

Sept. 2017

The story from hypernuclear halos to optical interferences

- a hypernuclear halo system

- the puzzle of its lifetime vs B_{Λ}

- emulsion data limitations

- need for new precision measurements

- decay-pion spectroscopy at MAMI

- limitation by absolute beam energy precision

- interferometry of optical undulator radiation

- ongoing activities and future projects

A hypernuclear halo system



The Λ -hypernuclear three-body system

the hypertriton

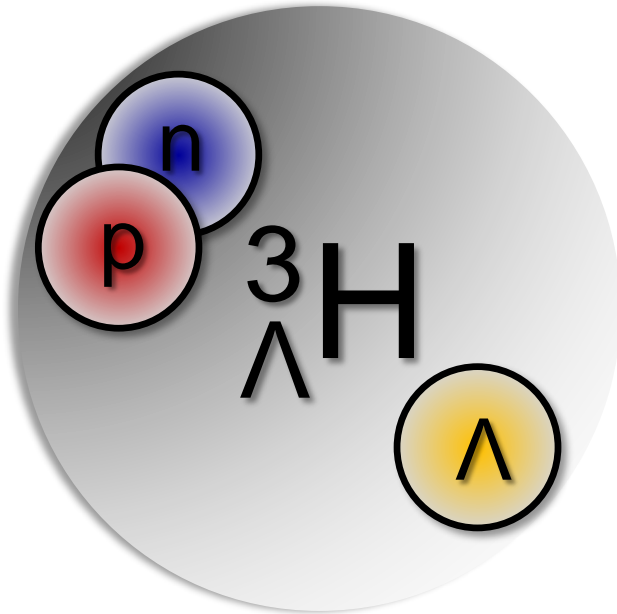
- lightest hypernuclear bound state:
 $S = -1$, $J^P = 1/2^+$, $T = 0$

- simplest system in which Λ particle interacts with nucleons at low energy

- Λ separation = binding energy
 $B_\Lambda = 130 \pm 50$ (stat.) ± 50 (syst.) keV

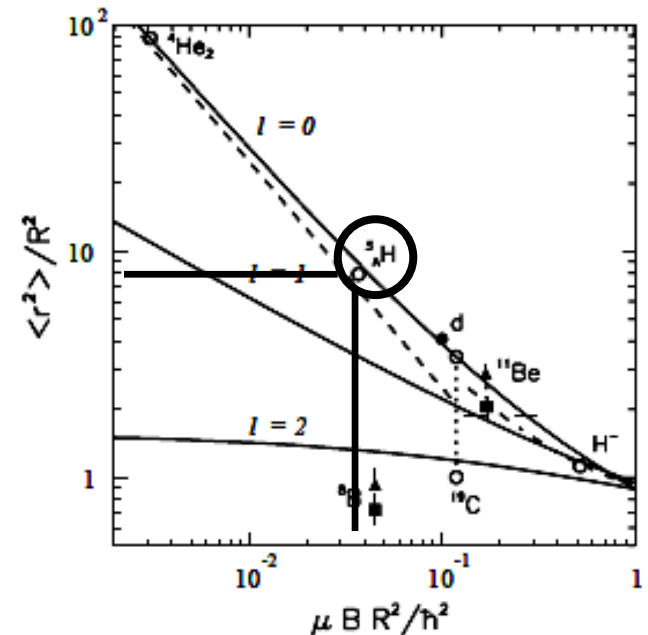
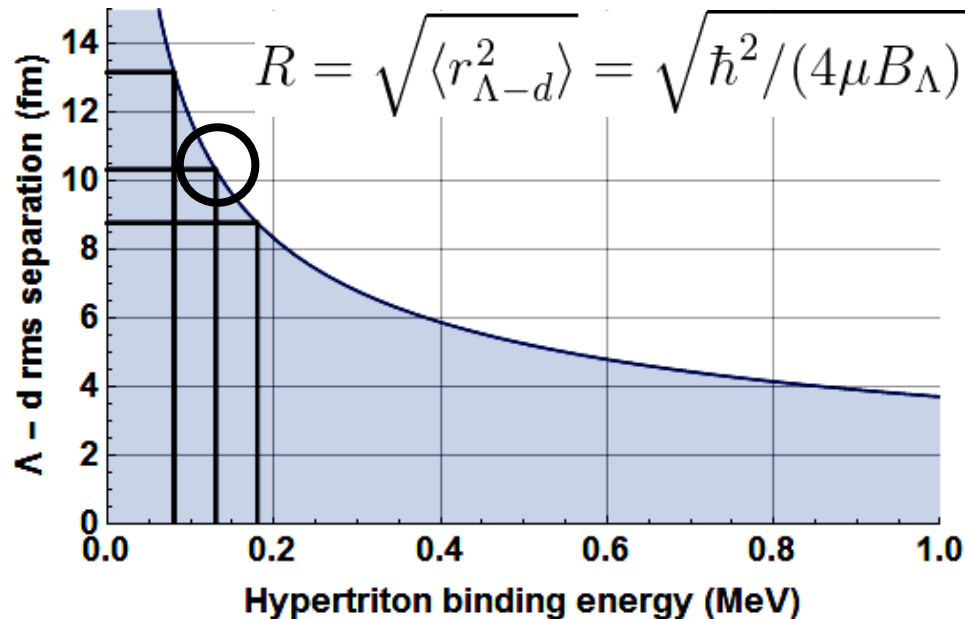
- short ranges of NN and Λ N interactions & small total binding energy (~ 2.3 MeV) imply S states for relative motions and very loose structure

- mesonic weak decay (MWD) is expected to dominate over non-MWD



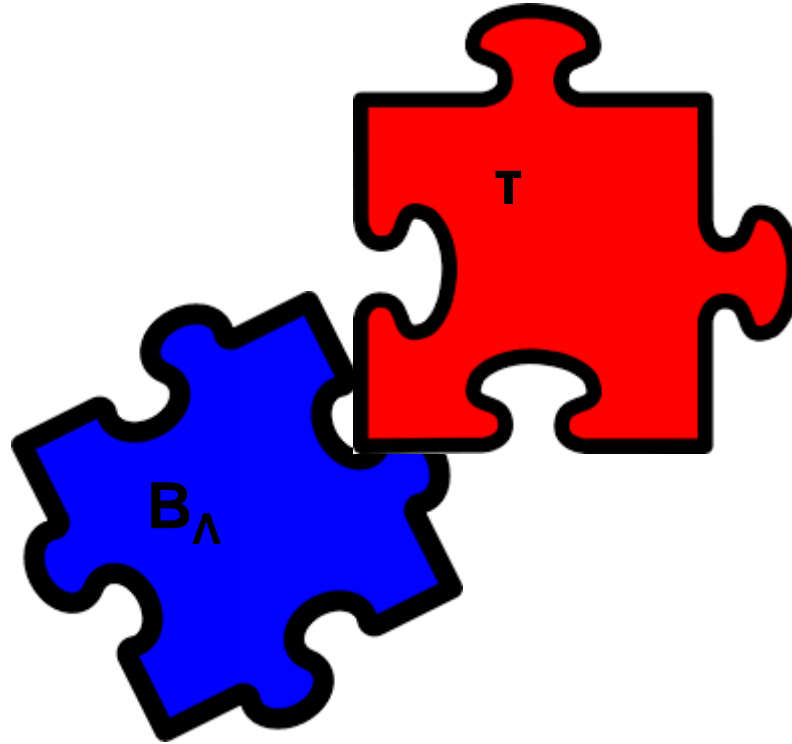
Hypertriton as a halo system

- 1n & 2n halos known for small n separation energies near dripline
- universal scaling relations derived for nuclear systems with low binding
- hypertriton effective two-body $d\Lambda$ system (?)
- in hypertriton no centrifugal barrier, no Coulomb repulsion
- when pair of particles is close, the third particle is, on average, far away
- for a spatially extended nuclear state (compared to core size) most of wave function tunneled into classically forbidden region

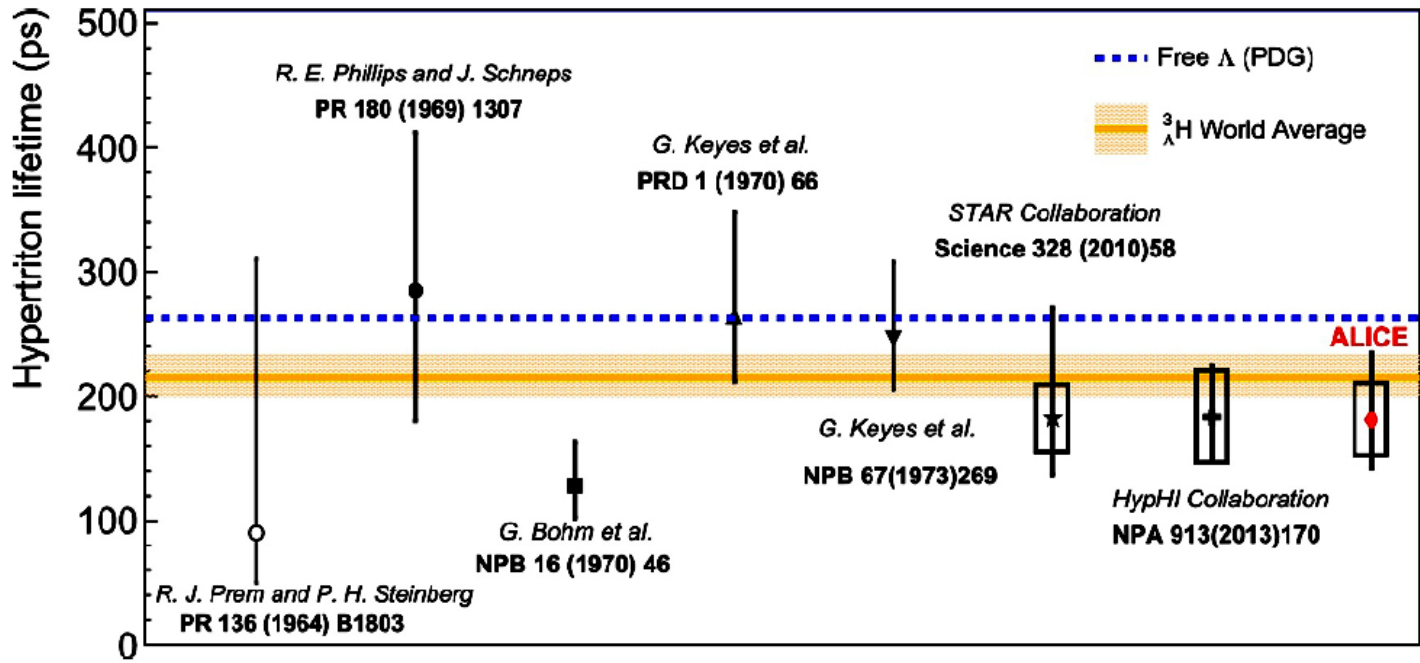


[Riisager et al., *Europhys. Lett.* 49 (2000)]

The puzzle of its lifetime vs B_{Λ}



$^3_\Lambda\text{H}$ lifetime measurements



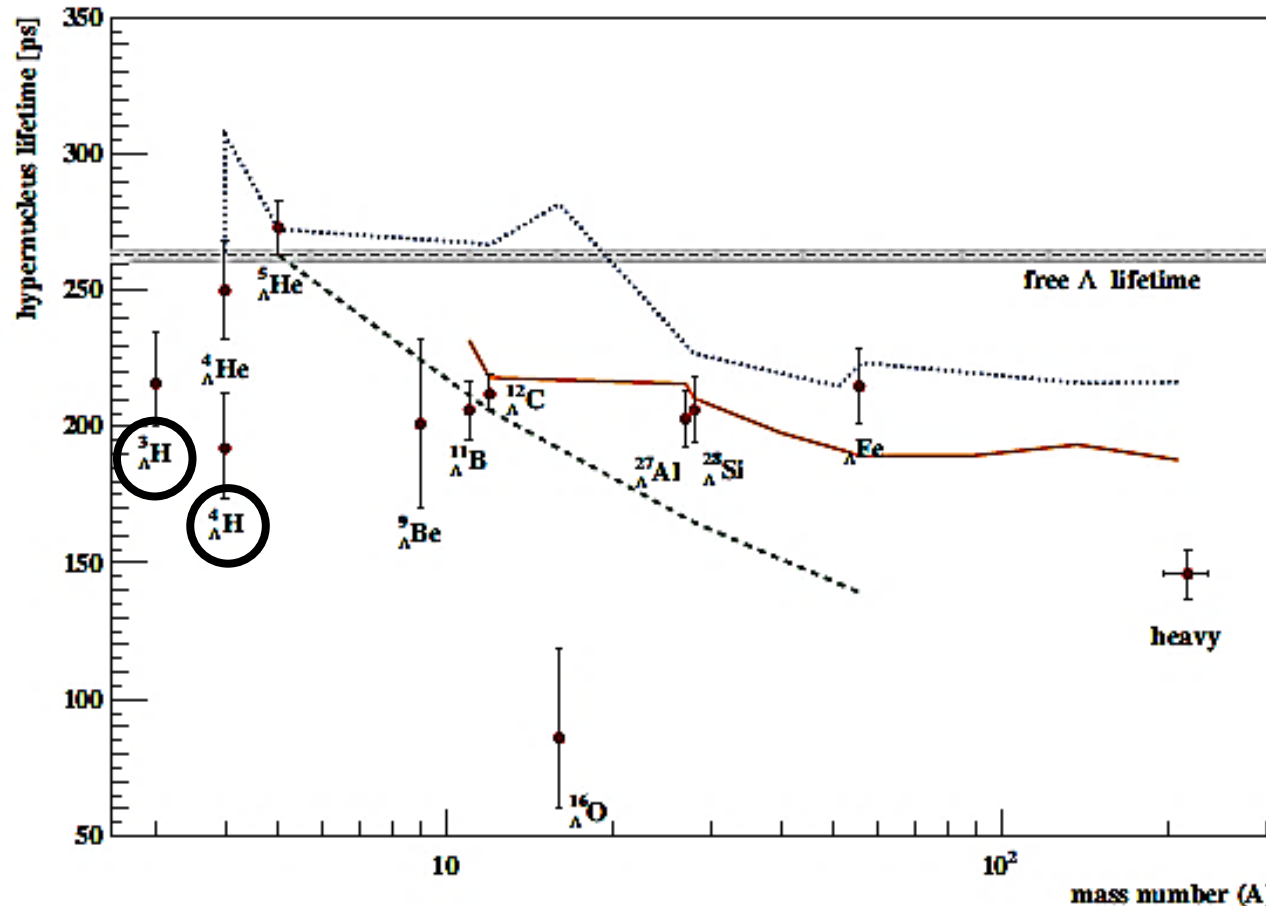
[ALICE Collab. PLB 754 (2016)]

- lifetimes of light ($A \leq 4$) hypernuclei expected to be similar to free Λ , if Λ in the hypernucleus is weakly bound
- hypernuclear lifetimes are not known as precisely as the Λ lifetime
- world average of $^3_\Lambda\text{H}$ lifetime measurements $\tau = 215^{+18}_{-16}$ ps
- comparison with $\tau_\Lambda = 263.2 \pm 2$ ps

values from heavy ion experiments are surprisingly small

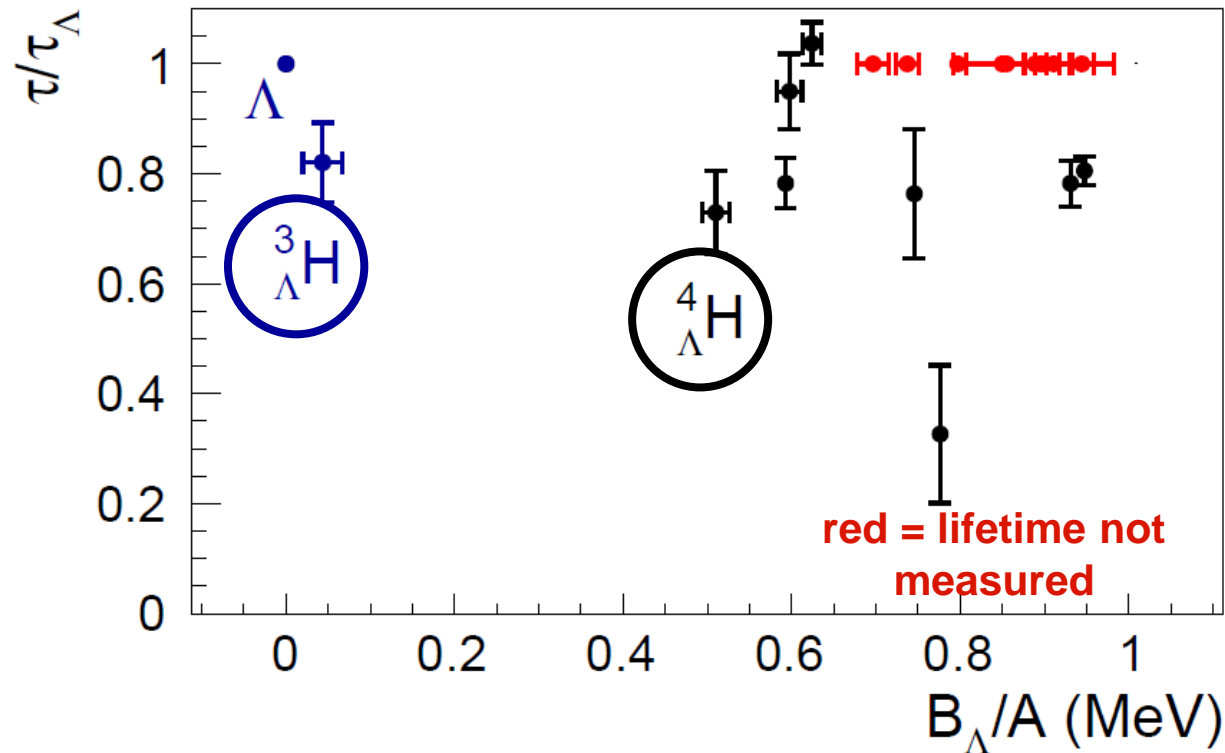
Other hypernuclear lifetimes

- only ~ 10 hypernuclear lifetimes known
- theoretical predictions are scattered over a large range
- calculations hyperhydrogen lifetimes predict no more than 10% deviation



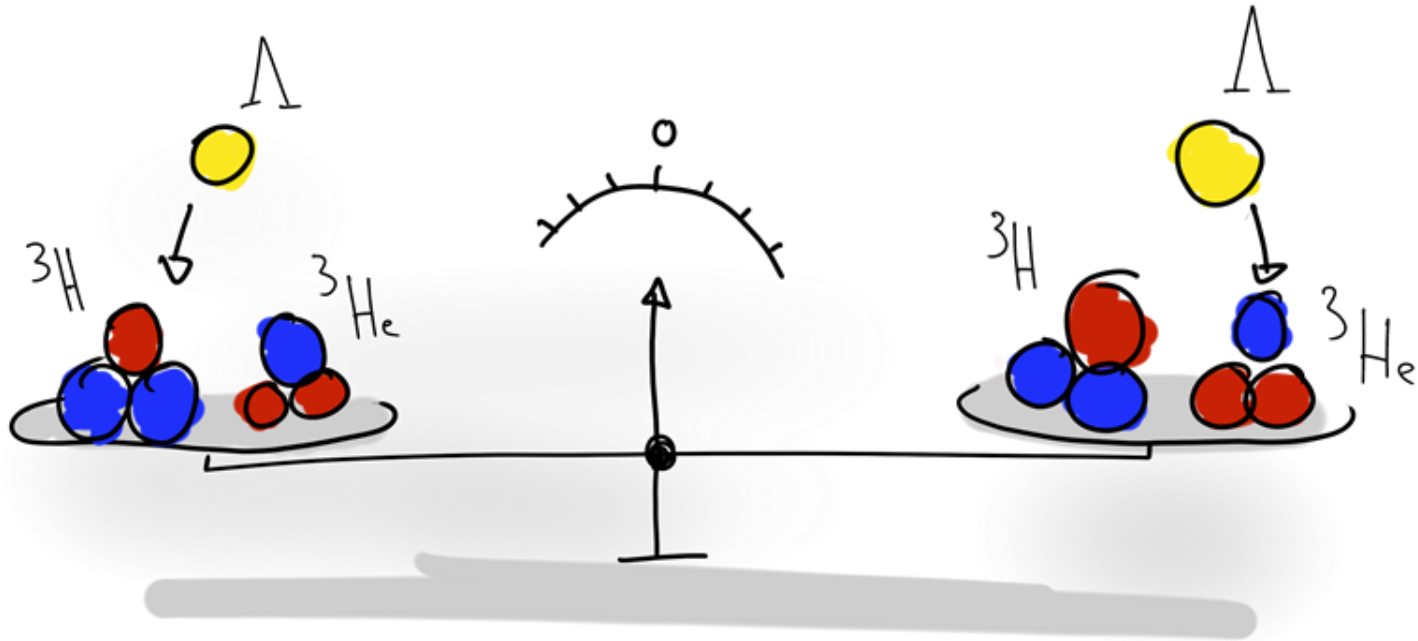
[E. Botta et al. Riv. N. Cim. 38 (2015)]

Scaled lifetime vs scaled B_Λ



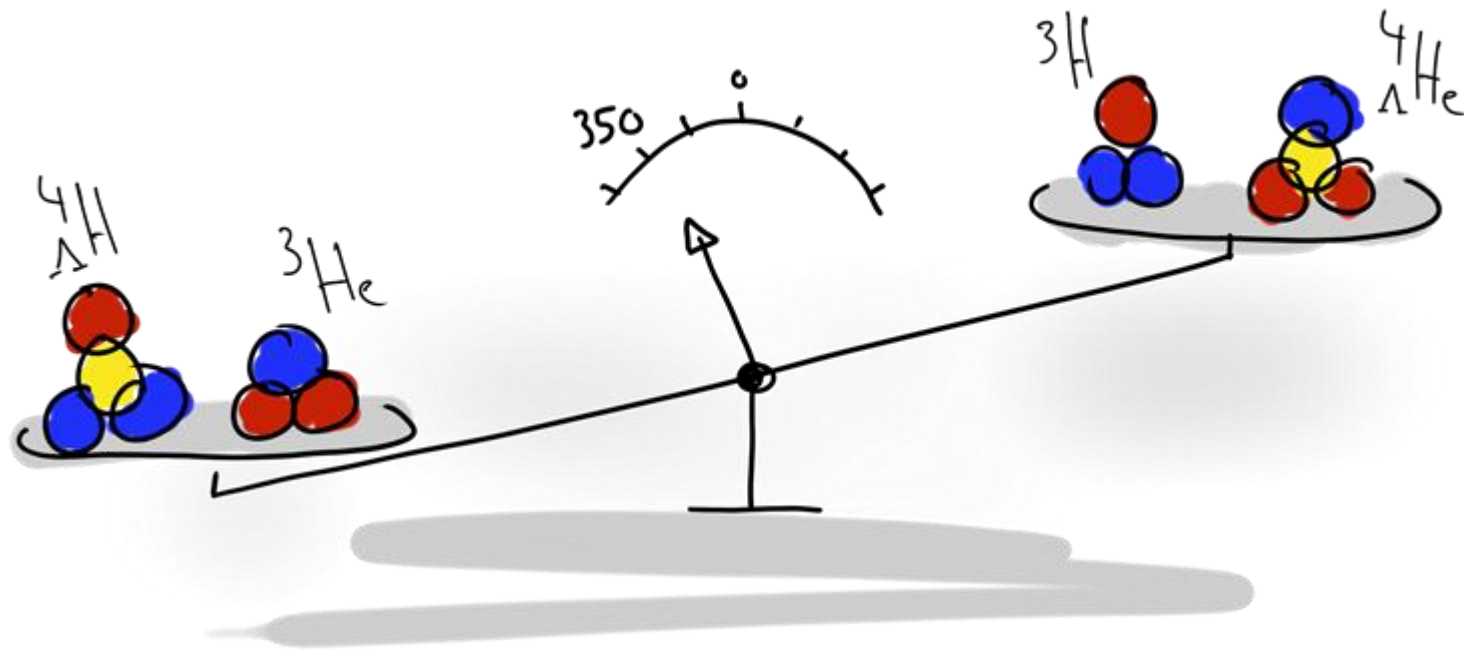
- small Λ binding energy implies extended wave function \rightarrow lifetime puzzle connected to precision of B_Λ measurement
- unique location of ${}^3_\Lambda\text{H}$ compared to all other known hypernuclei
- lifetime of hydrogen hyperisotopes $\sim 30\%$ shorter with respect to Λ
- B_Λ of ${}^4_\Lambda\text{H}$ $\sim 15\%$ smaller with respect to ${}^4_\Lambda\text{He}$
- strong charge symmetry breaking only in light hypernuclear systems

Charge symmetry in light hypernuclei



$$-B_{\Lambda} = M_{\text{HYP}} - (M_{\text{Core}} + M_{\Lambda})$$

Charge symmetry in light hypernuclei

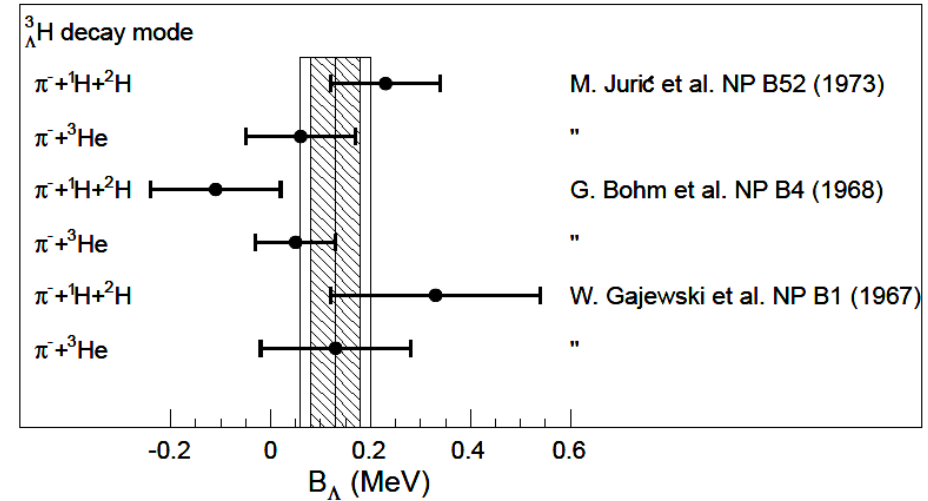
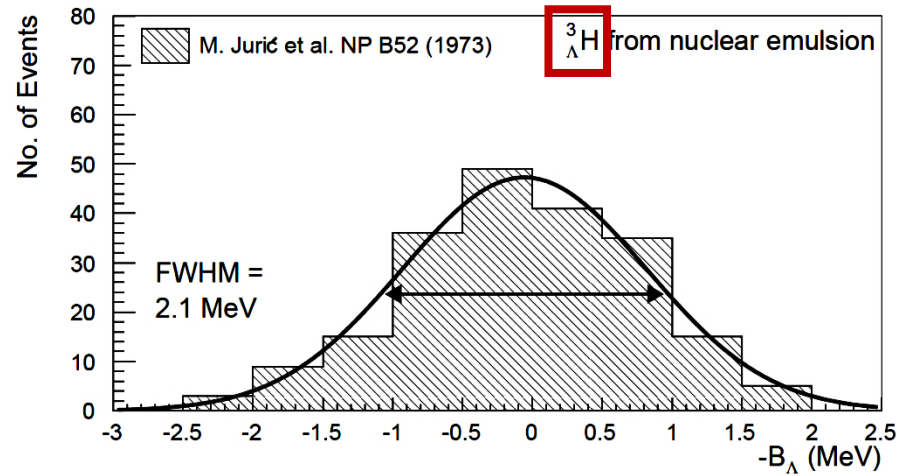


$$-B_{\Lambda} = M_{HYP} - (M_{Core} + M_{\Lambda})$$

Emulsion data limitations

The emulsion data for ${}^3_{\Lambda}\text{H}$

only about 200 analyzed events from emulsion:



these data (from 2 decay modes): only source of binding energy information

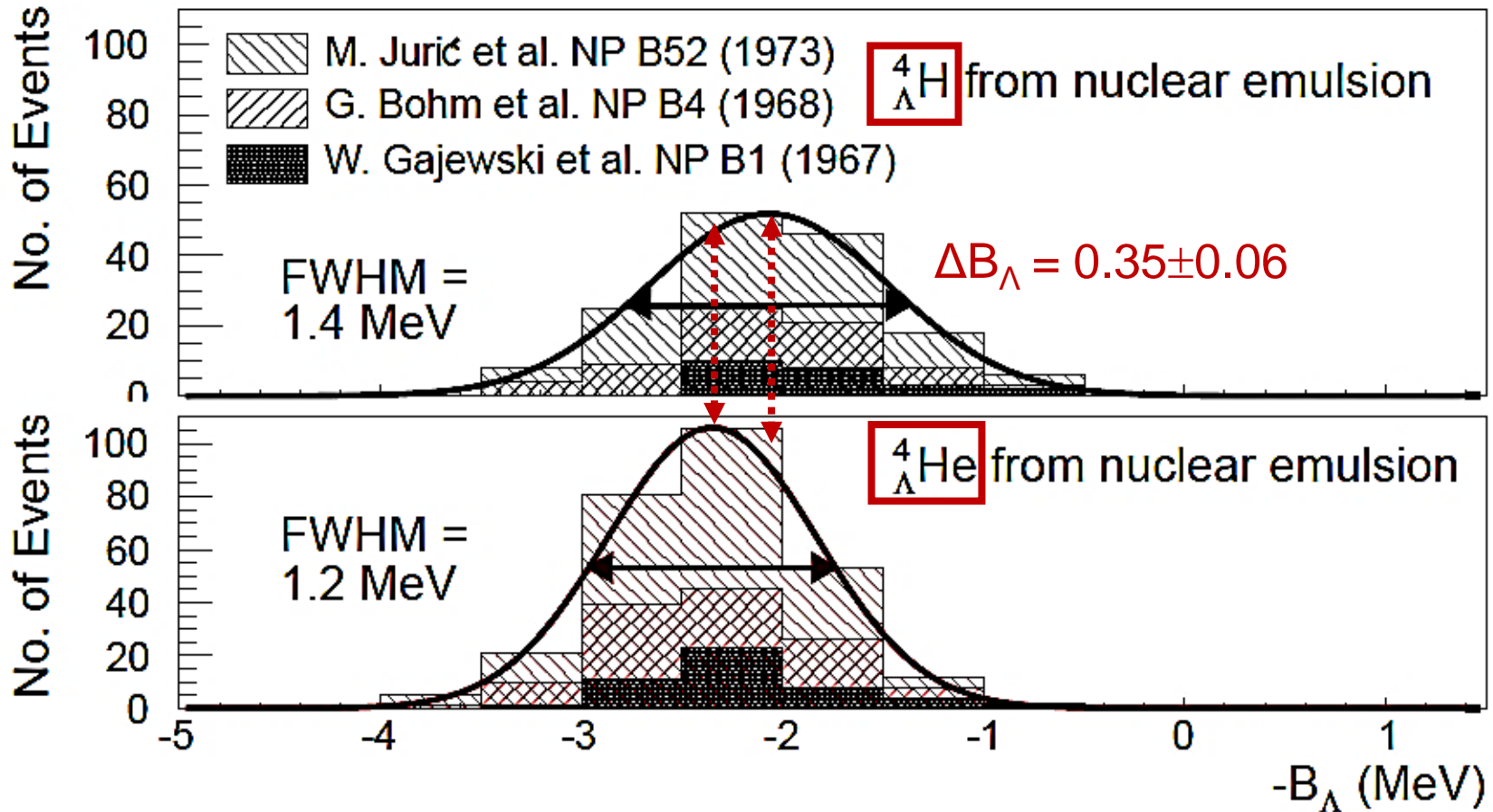
$$\begin{aligned}
 {}^3_{\Lambda}\text{H}^{\text{decay}} &\rightarrow \pi^- + {}^3\text{He}: & B_{\Lambda} &= 70 \pm 60 \text{ keV} \\
 {}^3_{\Lambda}\text{H}^{\text{decay}} &\rightarrow \pi^- + {}^1\text{H} + {}^2\text{H}: & B_{\Lambda} &= 120 \pm 80 \text{ keV}
 \end{aligned}$$

} 50 keV difference

$$\text{Total: } B_{\Lambda} = 130 \pm 50 \text{ keV}$$

[M. Juric et al. NP B52 (1973)]

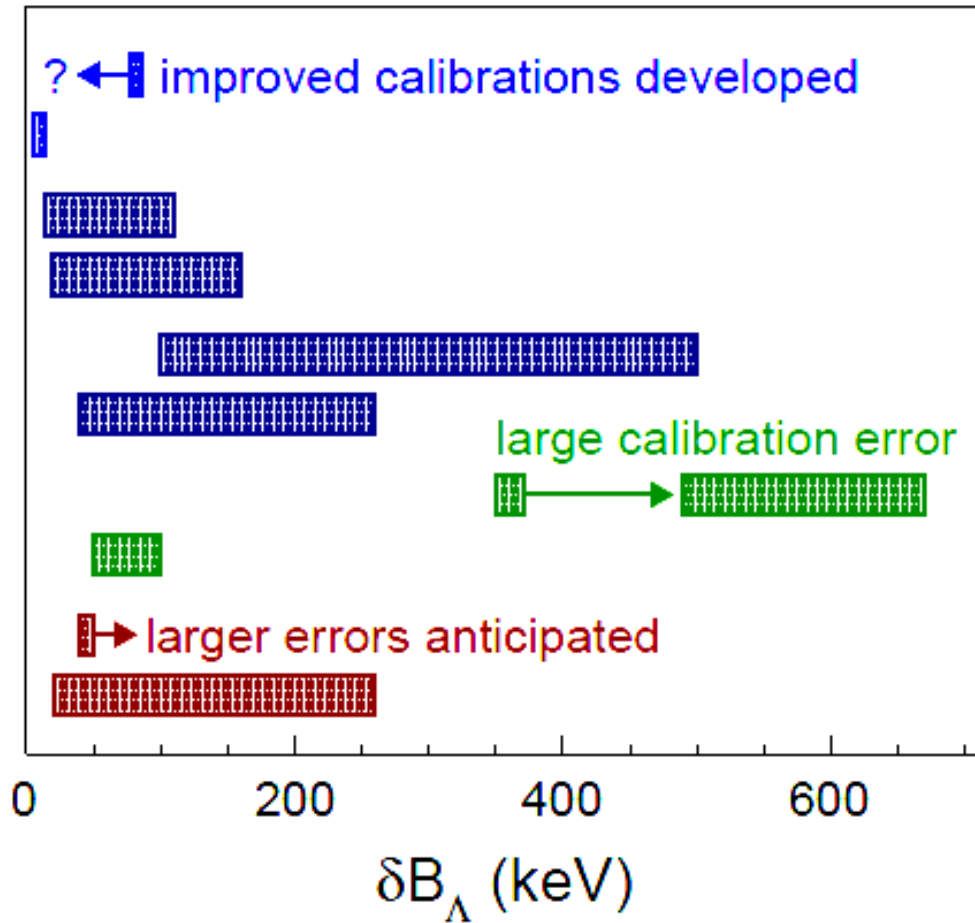
Emulsion results on ${}_{\Lambda}^4\text{H}$ and ${}_{\Lambda}^4\text{He}$



- only three-body decay modes used for hyperhydrogen
- 155 events for hyperhydrogen, 279 events for hyperhelium

Need for new precision measurements

Errors on binding energy by method

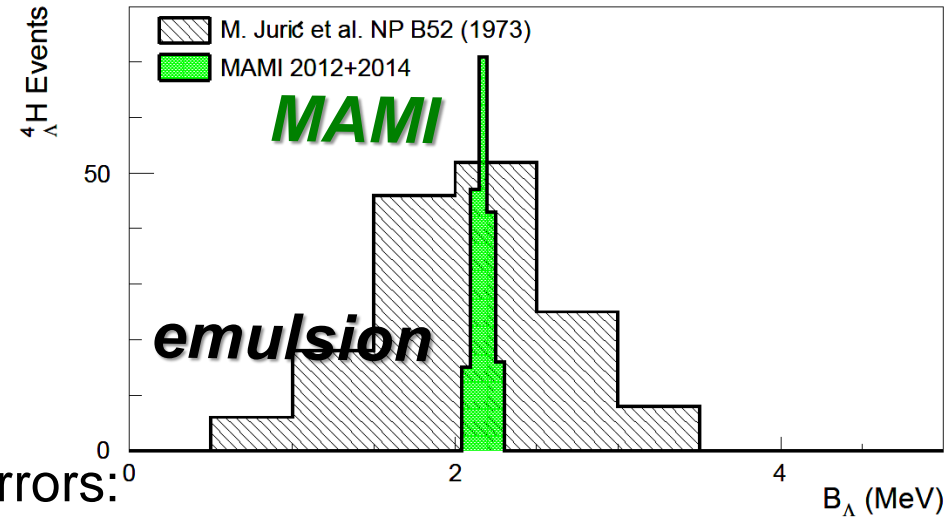


$(e, K^+ \pi^-)$ MAMI syst. error
 $(e, K^+ \pi^-)$ MAMI stat. error
 $(e, e' K^+)$ JLab syst. error
 $(e, e' K^+)$ JLab stat. error
 $(K_{\text{stop}}^-, \pi^-)$ FINUDA syst. error
 $(K_{\text{stop}}^-, \pi^-)$ FINUDA stat. error
 (π^+, K^+) KEK-SKS syst. error
 (π^+, K^+) KEK-SKS stat. error
 emulsion syst. error
 emulsion stat. error

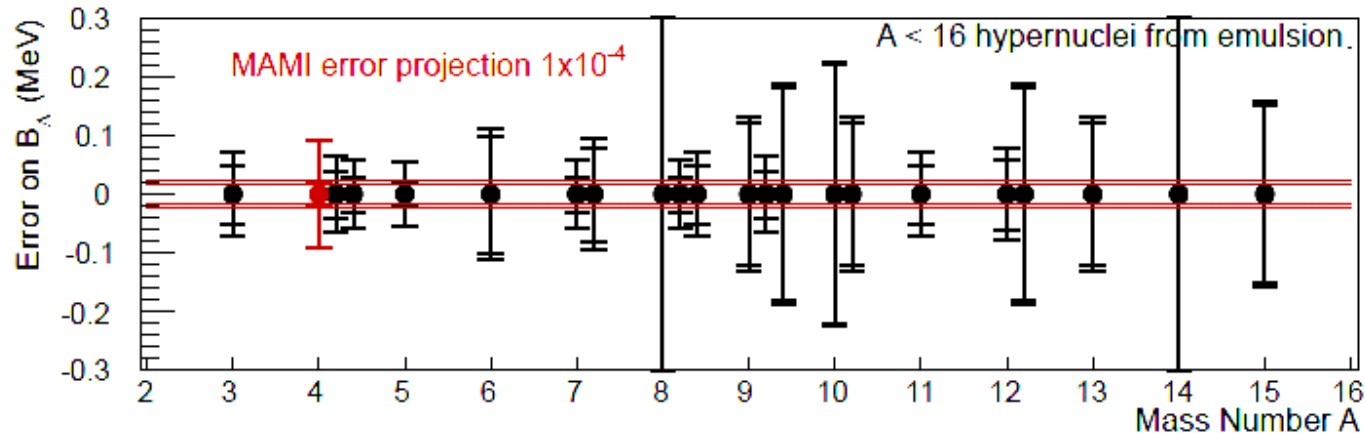
- goal of calibrations is syst. error comparable to stat. error < 20 keV
- decay-pion spectroscopy will be the most precise method of all

High-precision mass measurements at MAMI

requirements: calibration and beam energy with $O(10^{-4})$ precision



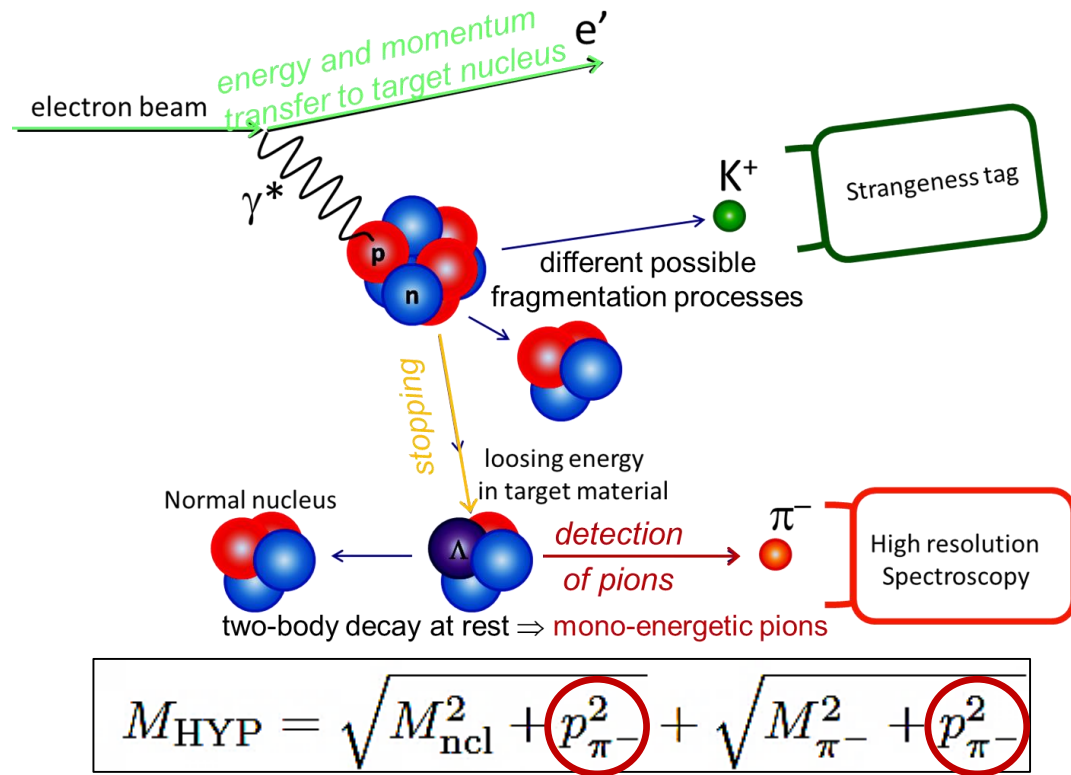
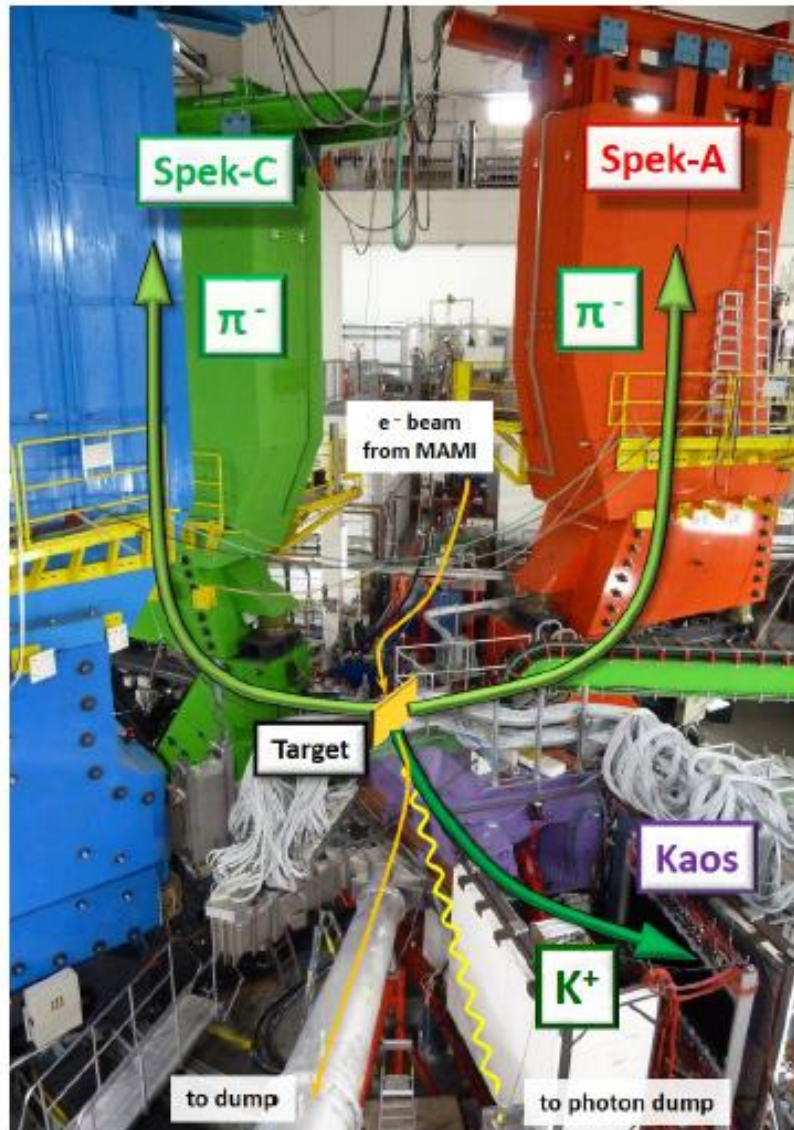
projected error compared to emulsion errors:



binding energies of light hyperisotopes could be measured with improved precision by decay-pion spectroscopy

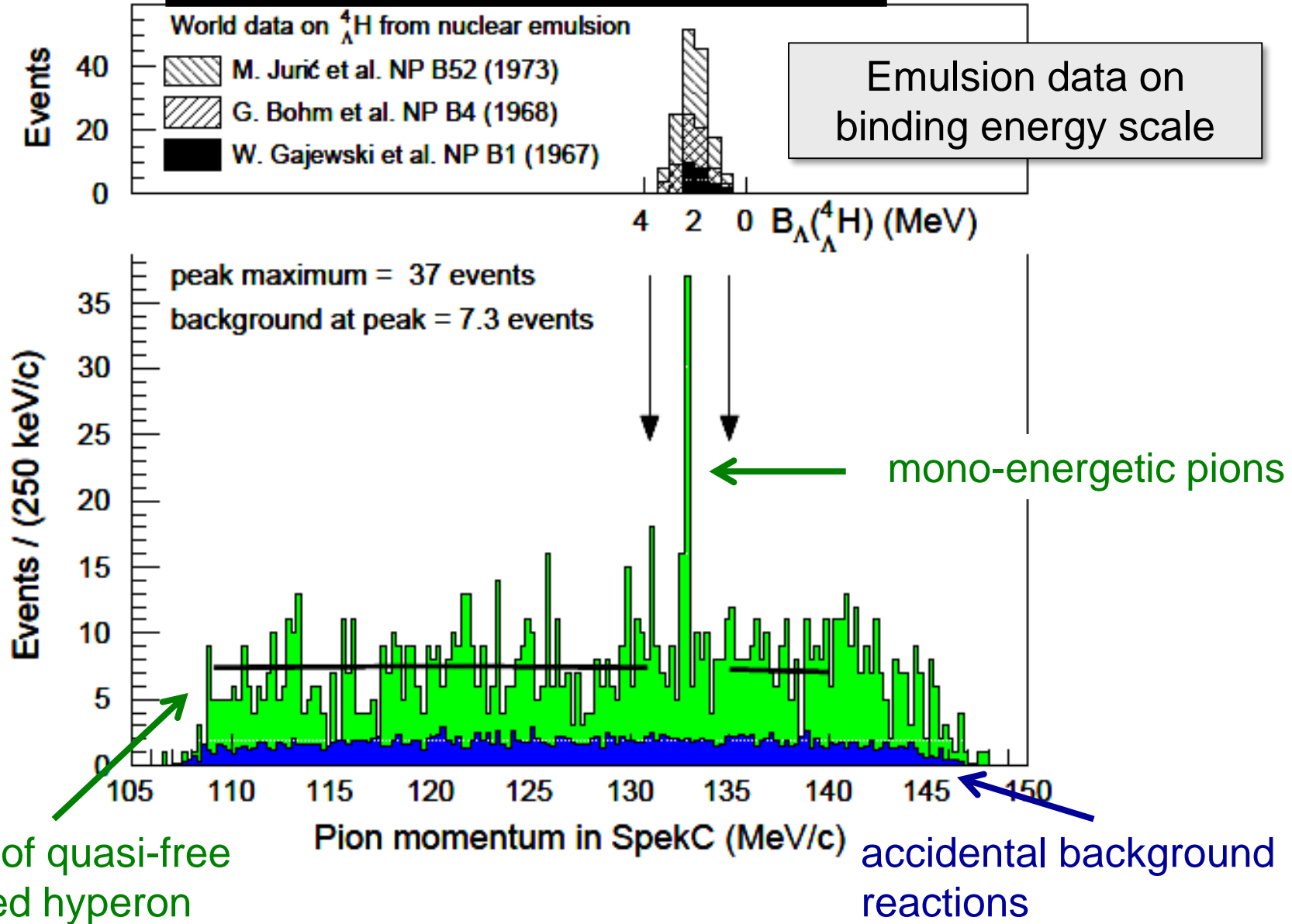
Decay-pion spectroscopy at MAMI

Hyperfragment decay-pion spectroscopy with electron beams



Hypernuclear experiments at MAMI done in Collaboration with Tohoku University (S.N.N. Nakamura et al.)

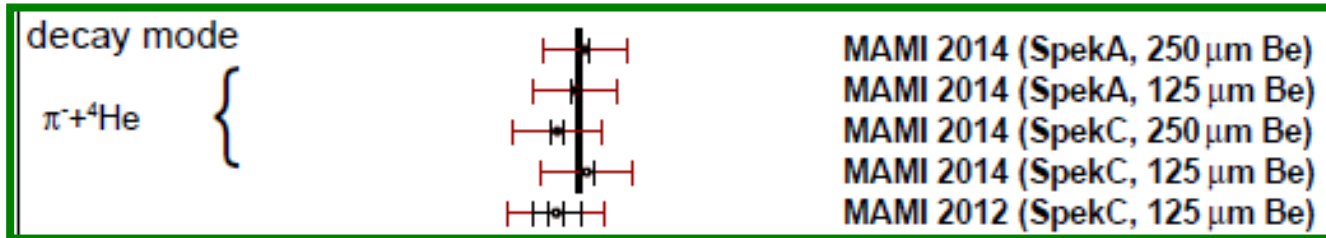
Decay-pion spectrum



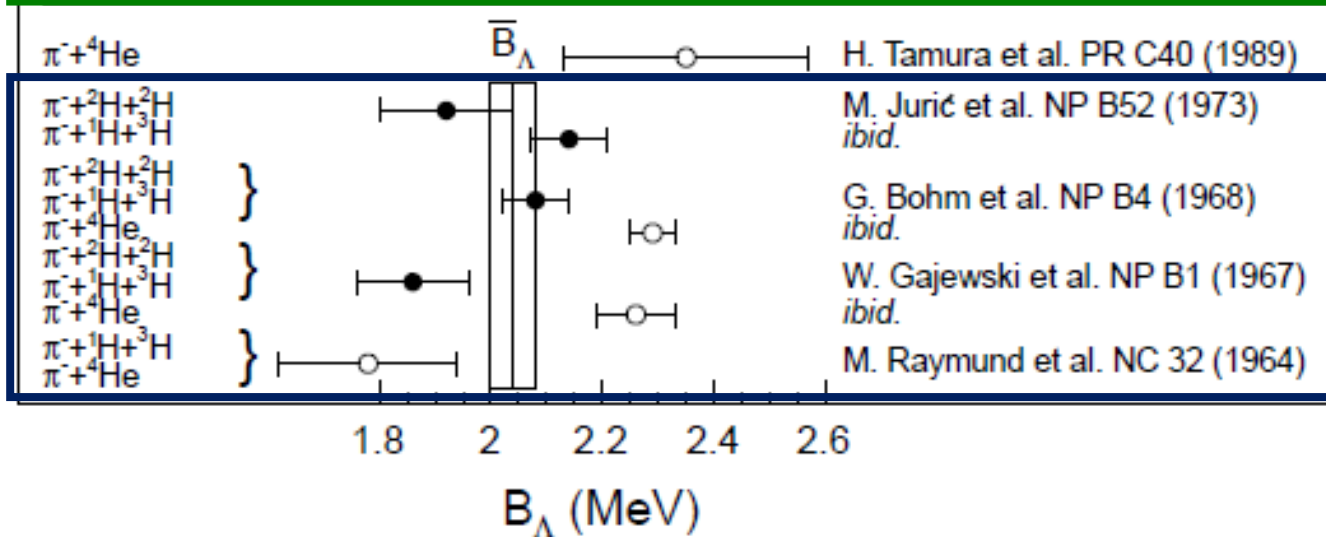
World data on ${}^4_{\Lambda}\text{H}$ mass

outer error bars correlated from calibration

MAMI



emulsion

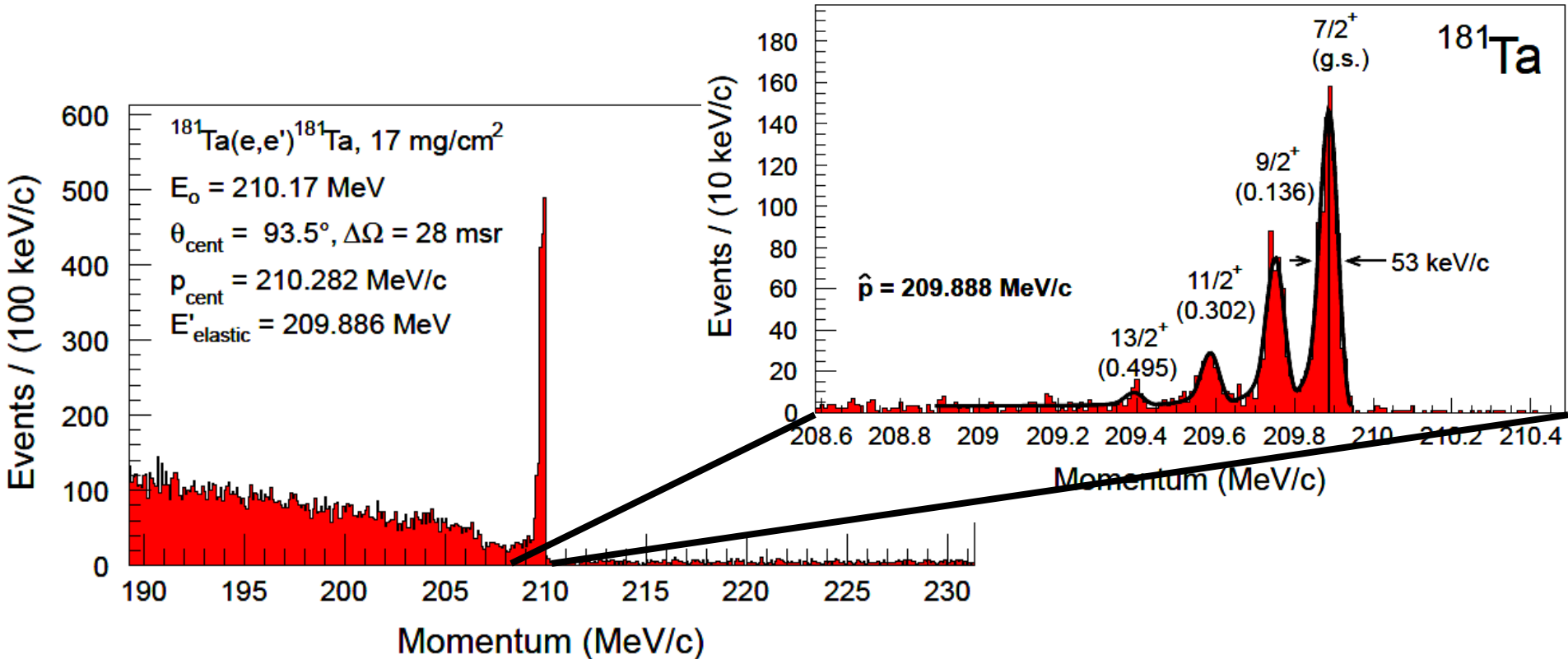


	$B_{\Lambda}({}^4_{\Lambda}\text{H})$	(stat.)	(syst.)	
emulsion:	2.04	± 0.04	± 0.05 MeV	[M. Juric et al. NP B52 (1973)]
MAMI 2012:	2.12	± 0.01	± 0.09 MeV	[A. Esser et al., PRL 114 (2015)]
MAMI 2014:	2.16	± 0.01	± 0.08 MeV	[F. Schulz et al., NPA (2016)]

Limitation by absolute beam energy precision

Absolute momentum calibration

scattering off thin tantalum foil



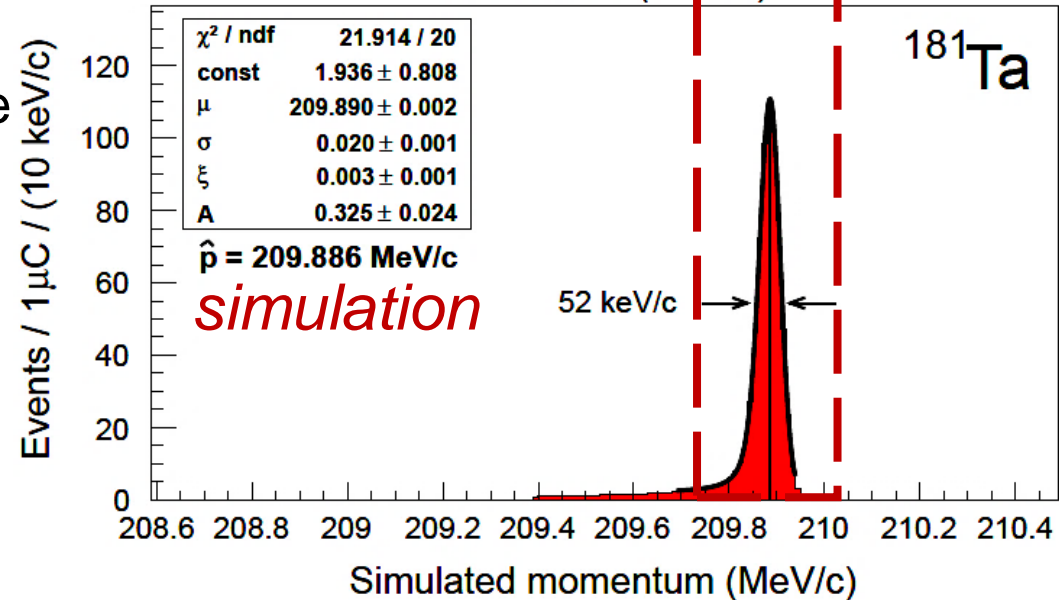
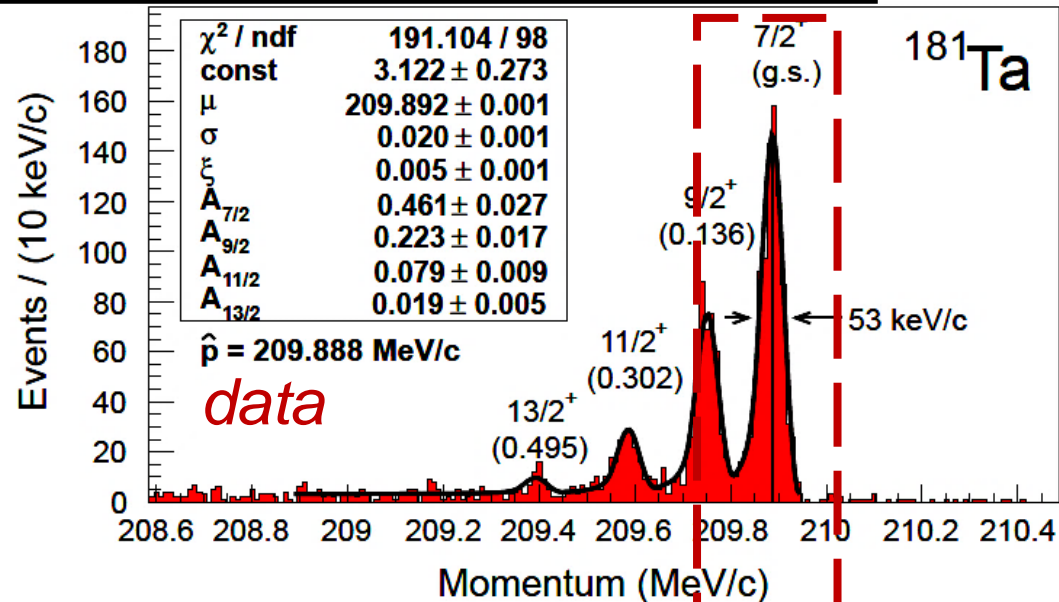
- spectrometer FWHM of 53 keV/c $\rightarrow \delta p/p \sim 2 \cdot 10^{-4}$
- beam energy absolute accuracy $\delta p_{\text{beam}} \pm 160$ keV/c $\rightarrow \delta E/E \sim 7 \cdot 10^{-4}$
- repeated calibrations at different momenta reveal $\delta p_{\text{calib}} \sim 5$ keV/c

Simulation of scattering process and spectrometer

comparison of
simulation vs. data
reveals highest precision

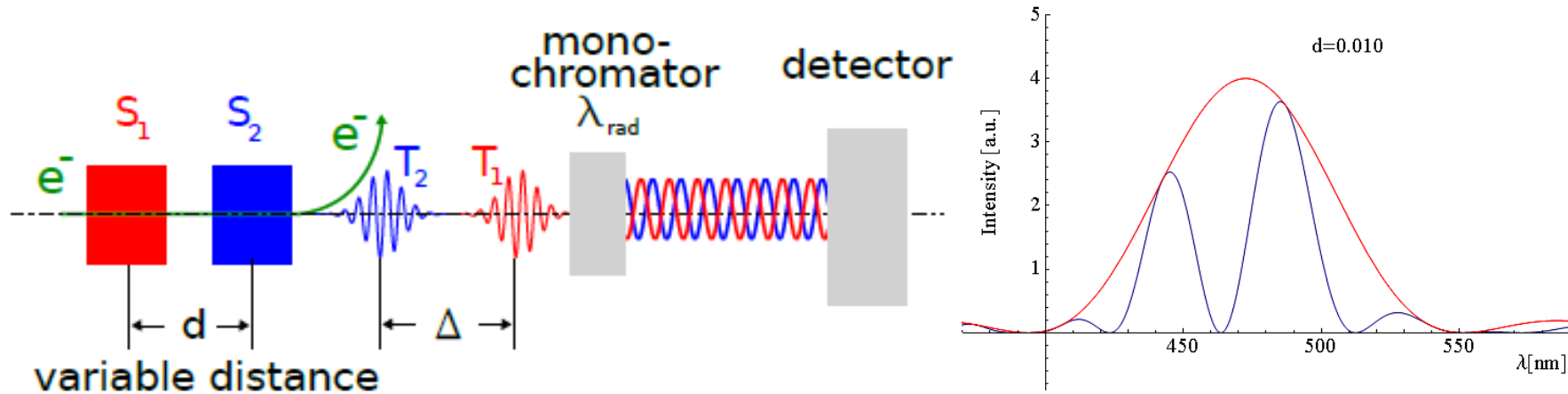
Monte Carlo code for
...**energy-loss** of incoming beam,
...reaction **vertex distribution**,
...**reaction kinematics**, and
...**energy-loss** of outgoing particle
→ **shape & width well reproduced**

calibration fixed at relative
momentum closest to decay-pion
line of ${}^4_{\Lambda}\text{H}$, data here shifted 7%
→ **difference of only 2 keV/c**



Interferometry of optical undulator radiation

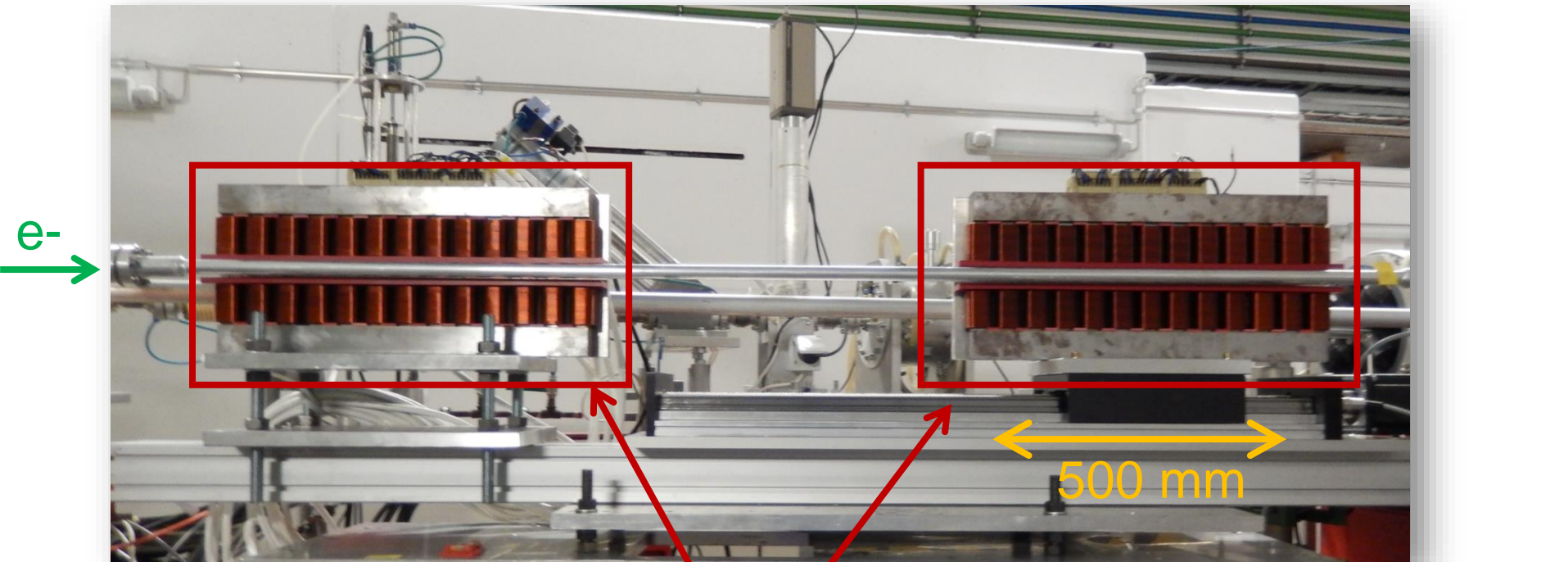
Novel absolute beam energy measurements



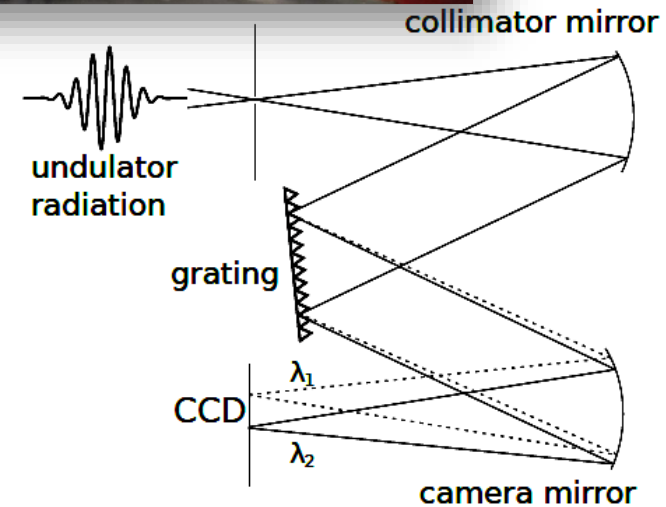
- two spatially separated sources of coherent synchrotron light
- two separated wave trains show interference in optical detector
- monochromator serves as Fourier analyzer of wave trains
- intensity for a selected wavelength shows a periodical variation
- intensity oscillation length directly related to beam energy

$$\gamma_{\text{beam}}^2 = \frac{\lambda_{\text{osc}}}{2\lambda_{\text{rad}}}$$

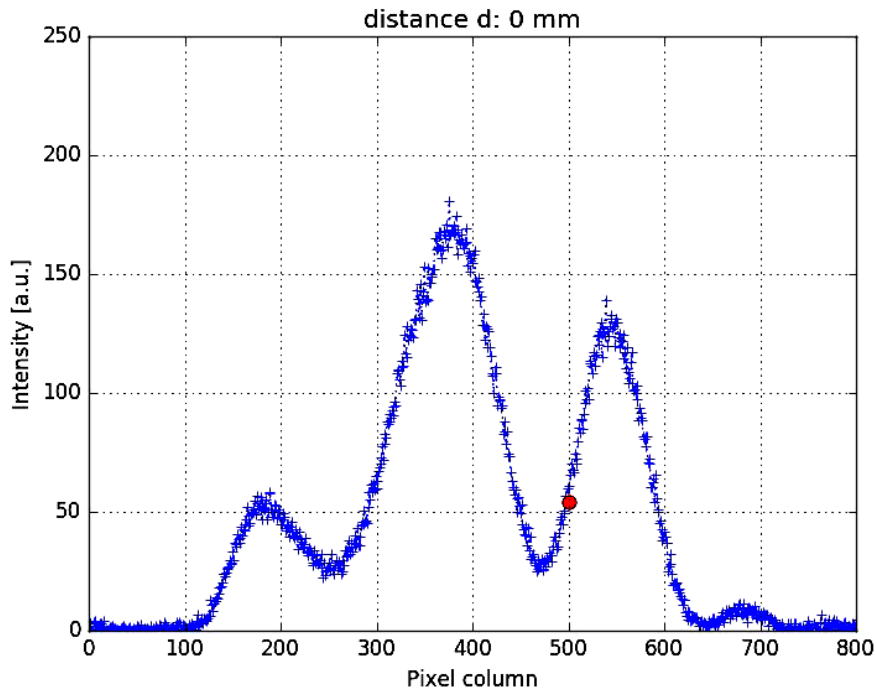
Pioneering run with undulator setup at MAMI



- two 50 cm long undulators
- variable distance of 500 mm
- monochromator and CCD system



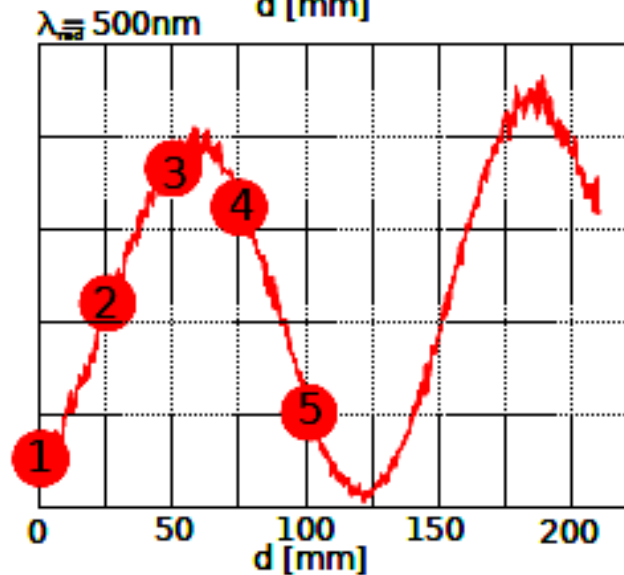
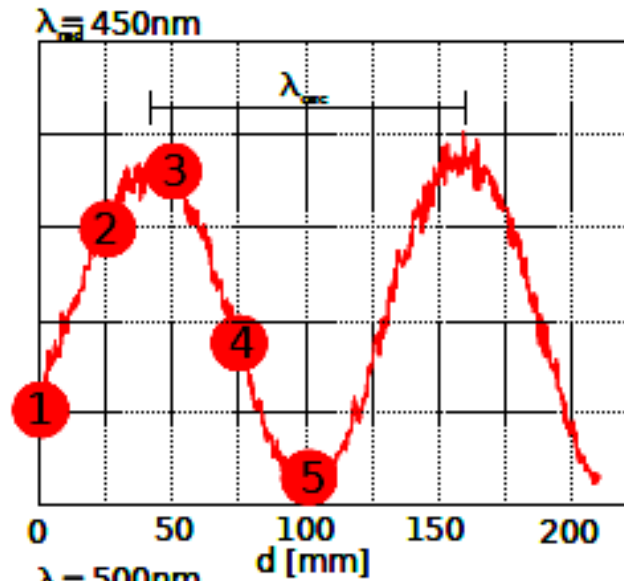
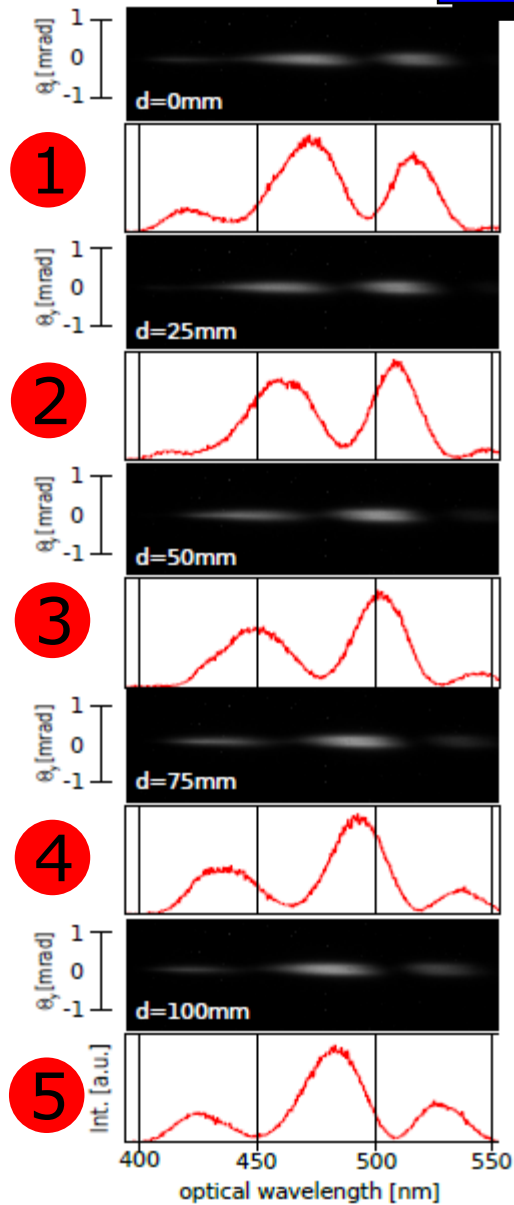
Evolution of synchrotron spectrum with distance



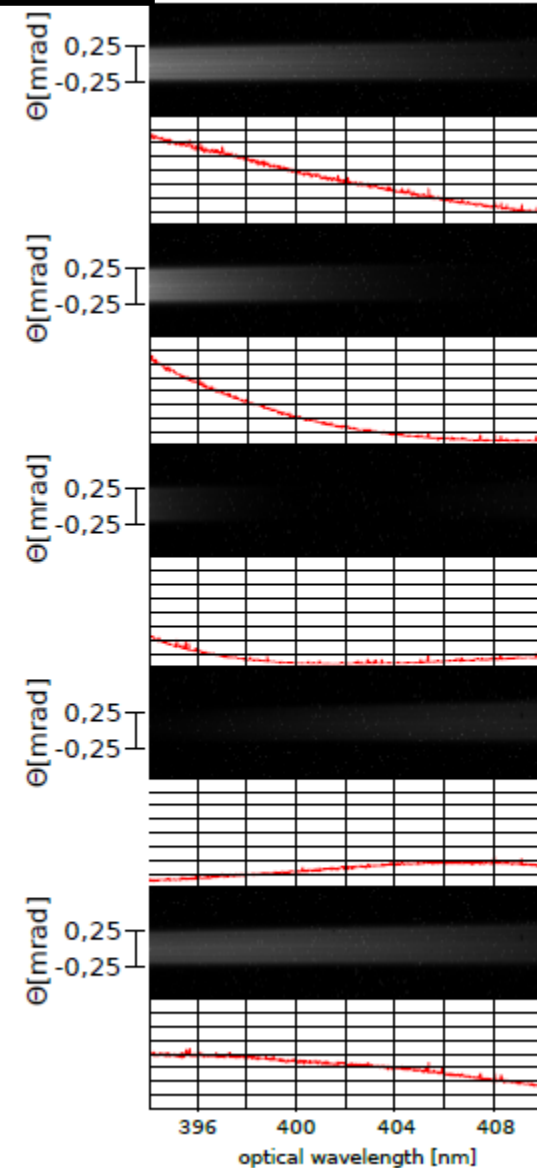
- clean spectra observed at center of radiation cone
- intensity at one wavelength varies periodically
- low counting noise
⇒ high statistical precision

proof of principle demonstrated with this measurement

Proof of principle demonstrated



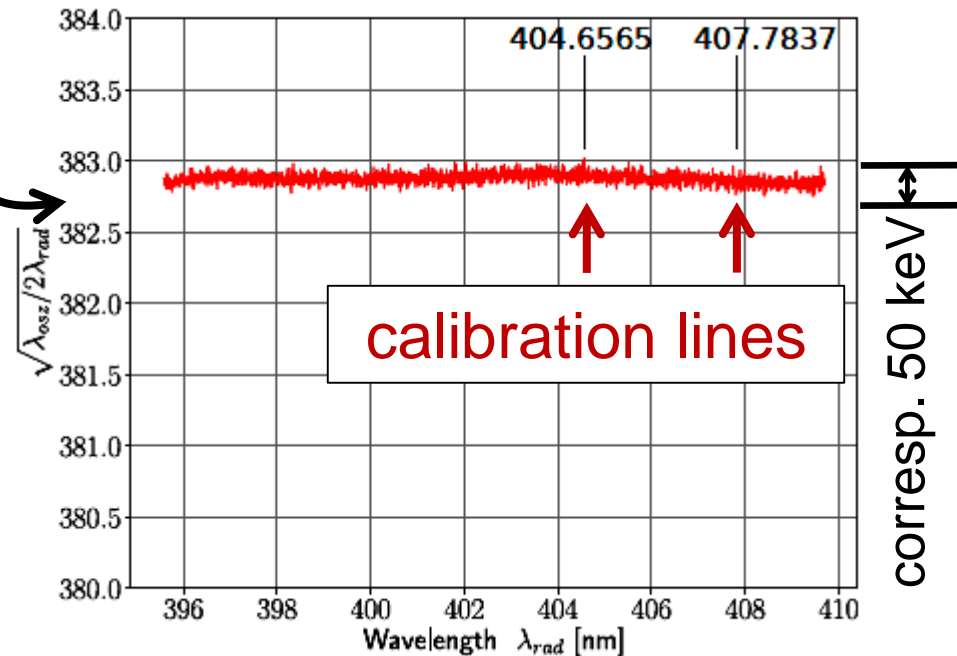
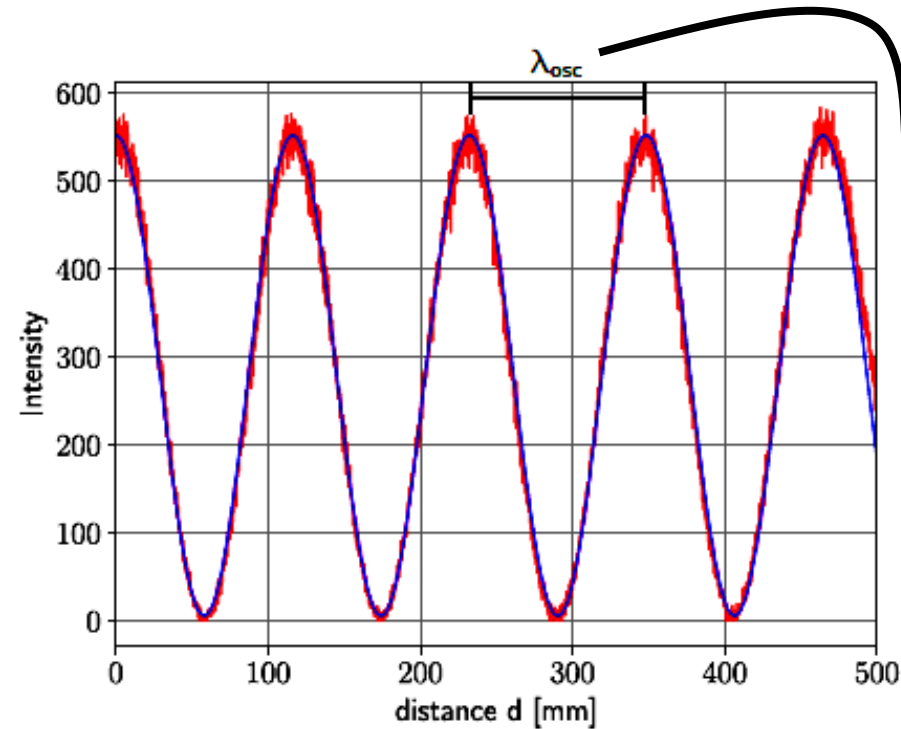
change of
monochromator



Highest-precision beam energy measurement achieved

intensity oscillation for one selected wavelength:

simultaneous measurement for 2328 wavelengths in CCD:

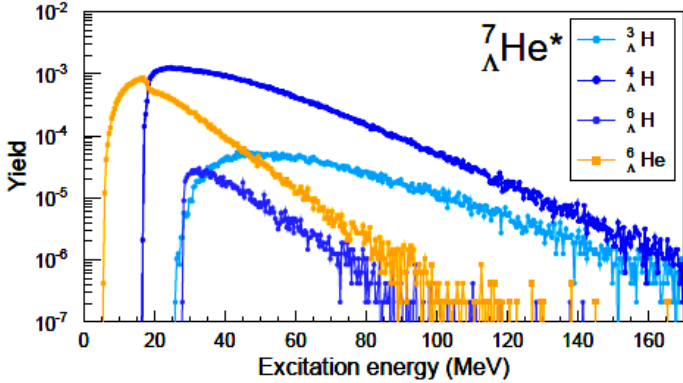
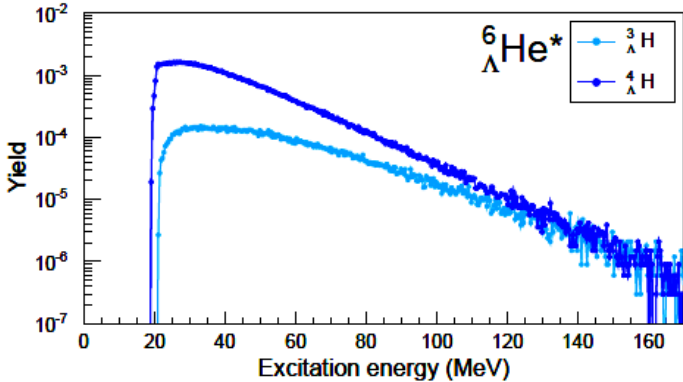


$$\gamma_{beam} = 382.2 \pm 0.002 \text{ (stat.)} \pm 1.3 \text{ (syst. } \delta_{\Theta}) \pm 0.1 \text{ (syst. } \delta_{\lambda})$$

$$E_{beam} = 194.8 \pm 0.001 \text{ (stat.)} \pm 0.7 \text{ (syst. } \delta_{\Theta}) \pm 0.05 \text{ (syst. } \delta_{\lambda}) \text{ MeV}$$

Ongoing activities and future projects

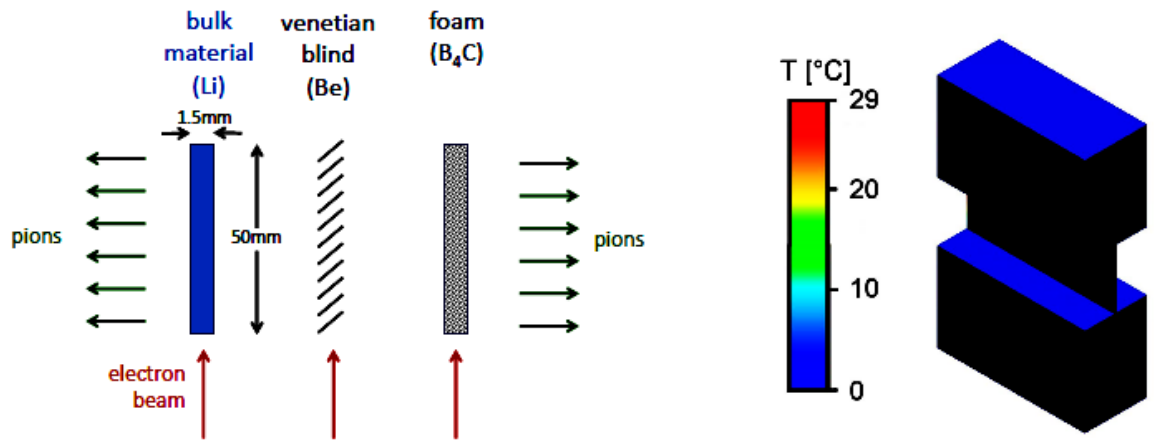
Li: an ideal target for ${}^3_{\Lambda}\text{H}$ production










statistical decay simulations:

hyper-nucleus	π^- momentum (MeV/c)	${}^9\text{Be}$ target			${}^7\text{Li}$ target	${}^6\text{Li}$ target
		direct Λ capture ${}^9_{\Lambda}\text{Li}^*$	Λ +neutron kick out ${}^8_{\Lambda}\text{Li}^*$	Λ +proton kick out ${}^8_{\Lambda}\text{He}^*$	direct Λ capture ${}^7_{\Lambda}\text{He}^*$	direct Λ capture ${}^6_{\Lambda}\text{He}^*$
${}^3_{\Lambda}\text{H}$	114.37 ± 0.08	0.56	1.18	0.67	1.49	2.48
${}^4_{\Lambda}\text{H}$	132.87 ± 0.06	3.56	3.74	7.51	12.61	8.81
${}^6_{\Lambda}\text{H}$	135.13 ± 1.52	0.03	<0.01	0.23	0.10	—
${}^6_{\Lambda}\text{He}$	108.47 ± 0.18	2.44	1.25	1.47	3.53	—
${}^7_{\Lambda}\text{He}$	$114.97 \pm 0.15_{stat} \pm 0.17_{sys}$	2.12	0.44	1.35	—	—
${}^8_{\Lambda}\text{He}$	116.50 ± 1.08	0.04	—	—	—	—
${}^7_{\Lambda}\text{Li}$	108.11 ± 0.05	1.54	1.68	—	—	—
${}^8_{\Lambda}\text{Li}$	124.20 ± 0.05	0.85	—	—	—	—

possible experiments:
2019/2020



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