

Heavy-quark spin-symmetry partners of hadronic molecules

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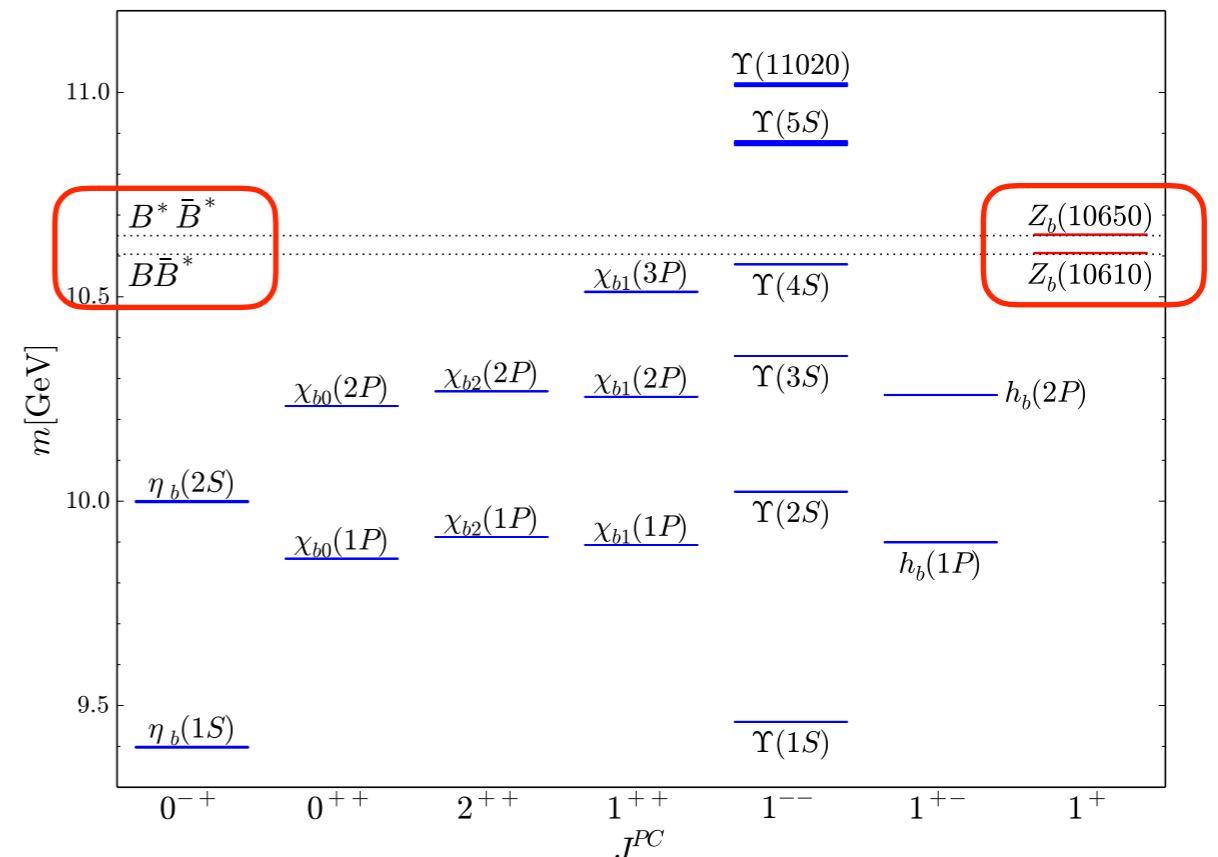
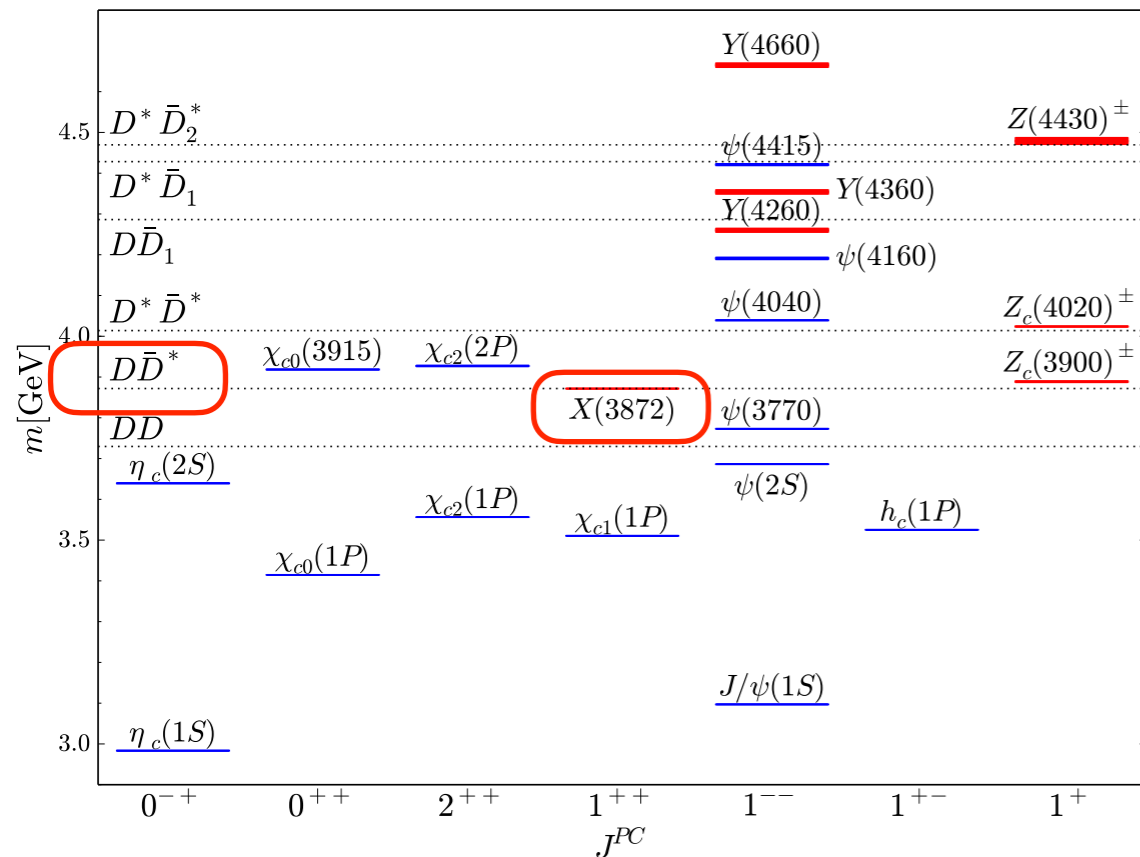
in collaboration with

E. Epelbaum, A.A. Filin, C. Hanhart, U.-G. Meißner and A.V. Nefediev

Key Refs: PLB 763, 20 (2016) and JHEP 1706, 158 (2017)

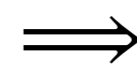
Introduction

- Plenty of experimentally observed XYZ states do not fit in quark model picture



Enigmatic examples: $J^{PC} = 1^{++}$ $X(3872)$ and 1^{+-} $Z_b(10610)/Z_b(10650)$ Belle (2010-2016)

decay predominantly to open-flavour channels



large molecule component!

reside very close to hadronic thresholds
and couple to them in S-wave

But very precise measurements and sophisticated line shape analyses are needed to unambiguously disentangle from tetraquarks!

Esposito et al. (2014)

Heavy-quark spin symmetry

The XYZ states contain heavy quark and antiquark \implies employ heavy-quark spin symmetry

➤ Heavy-quark spin symmetry (HQSS):

- In the limit $\Lambda_{\text{QCD}}/m_Q \rightarrow 0$ strong interactions are independent of HQ spin
- Approximate but quite accurate symmetry of QCD

➤ Consequences of HQSS — number of spin-partner states, location and decay properties — are different for different interpretations [Cleven et al. \(2015\)](#)

\implies Search for spin partner states \implies useful insights into the nature of XYZ states

This Talk: **Discuss HQSS predictions for the molecular scenario**

Impact of the charmonium component in the mixed interpretation [Cincioglu et al. \(2016\)](#)

Molecular partners: S-wave short-range interactions

- Basis states $\mathbf{J}^{\mathbf{PC}}$ made of a Pseudoscalar (P) and a Vector (V):

C-parity states: $C = \pm$ $PV(\pm) = \frac{1}{\sqrt{2}} (P\bar{V} \pm V\bar{P})$

$P = D$ or B , $V = D^*$ or B^*

0^{++}	: $\{P\bar{P}(^1S_0), V\bar{V}(^1S_0)\}$,
1^{+-}	: $\{P\bar{V}(^3S_1, -), V\bar{V}(^3S_1)\}$,
1^{++}	: $\{P\bar{V}(^3S_1, +)\}$,
2^{++}	: $\{V\bar{V}(^5S_2)\}$.

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- Consequences of HQSS for S-wave contact interactions

Grinstein et al. (1992),
AlFiky et al. (2006),
Nieves and Valderrama (2012)

☞ only two parameters at LO: LECs C and C'

☞ $V_{\text{LO}}^{(1^{++})}$ and $V_{\text{LO}}^{(2^{++})}$ are the same!

☞ C and C' –different for isoscalars and isovectors

$$\begin{aligned} V_{\text{LO}}^{(0^{++})} &= \frac{1}{4} \begin{pmatrix} 3C + C' & -\sqrt{3}(C - C') \\ -\sqrt{3}(C - C') & C + 3C' \end{pmatrix}, \\ V_{\text{LO}}^{(1^{+-})} &= \frac{1}{2} \begin{pmatrix} C + C' & C - C' \\ C - C' & C + C' \end{pmatrix}, \\ V_{\text{LO}}^{(1^{++})} &= V_{\text{LO}}^{(2^{++})} \equiv C \end{aligned}$$

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- strict HQSS limit: V - P mass splitting much smaller than all other scales

$$\delta = m_* - m \ll E_{\text{Bound}} \ll m$$

⇒ solutions of coupled-channel problem: two decoupled sets of partner states

$$E_{1^{++}}^{(0)} = E_{2^{++}}^{(0)} = E_{1^{+-}}^{(0)} = E_{0^{++}}^{(0)} \quad \text{and} \quad E_{0^{++}}^{(0)'} = E_{1^{+-}}^{(0)'}$$

Hidalgo-Duque et al. (2013)
our work (2016)

Contact theory with HQSS breaking

- Bondar et al. (2011), Voloshin (2011), Mehen and Powell (2011) propose a different expansion to account for HQSS breaking

$$E_{\text{Bound}} \ll \delta \ll m \quad \text{with}$$

$$\delta \simeq 140 \text{ MeV} \quad \delta/m \simeq 7\% \quad \text{in the c-sector}$$

$$\delta \simeq 45 \text{ MeV} \quad \delta/m \simeq 1\% \quad \text{in the b-sector}$$

- Leading effect — the states reside near their thresholds: $P\bar{P}$, $P\bar{V}$ and $V\bar{V}$

For example:

$$M_{2^{++}} = M_{1^{++}} + \delta$$

- Next-to-leading terms $O(\delta)$ and $o\left(\frac{\gamma^2}{\sqrt{m\delta}}\right) \simeq o\left(\sqrt{\frac{E_{\text{bound}}}{\delta}}\gamma\right)$ our work (2016)

➡ States 1^{+-} and 0^{++} acquire finite widths due to coupled channels:
 $D^* \bar{D}^* \rightarrow D \bar{D}^* \rightarrow D^* \bar{D}^*$
 $B^* \bar{B}^* \rightarrow B \bar{B}^* \rightarrow B^* \bar{B}^*$

➡ 2^{++} tensor state is uncoupled in the contact problem \implies no width

Contact + one-pion exchange (OPE) interactions

- Extended basis states:

$$0^{++} : \{P\bar{P}(^1S_0), V\bar{V}(^1S_0), V\bar{V}(^5D_0)\},$$

$$1^{+-} : \{P\bar{V}(^3S_1, -), P\bar{V}(^3D_1, -), V\bar{V}(^3S_1), V\bar{V}(^3D_1)\},$$

$$1^{++} : \{P\bar{V}(^3S_1, +), P\bar{V}(^3D_1, +), V\bar{V}(^5D_1)\},$$

$$2^{++} : \{P\bar{P}(^1D_2), P\bar{V}(^3D_2), V\bar{V}(^5S_2), V\bar{V}(^1D_2), V\bar{V}(^5D_2), V\bar{V}(^5G_2)\}$$

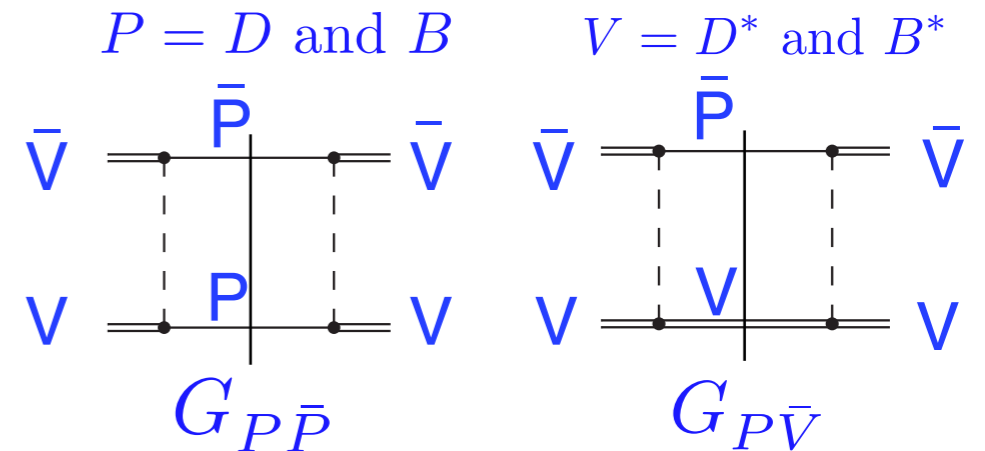
- Coupled-channel transitions in S, D and even G-waves

- coupled-channel dynamics is very important: inconsistent omission our work (2016)
 \implies strongly cutoff dependent results

- Pions enhance HQSS violation due to V-P mass splitting

$P\bar{P}$ and $P\bar{V}$ intermediate states can go on shell

\implies also 2^{++} $V\bar{V}$ states acquire finite widths



- pionic (S-D) tensor forces have non-trivial impact on the observables due to relatively large momentum scales involved

\implies Non-perturbative pion dynamics is to be important

Chiral EFT based approach for hadronic molecules

Our works: PLB 763, 20 (2016), JHEP 1706, 158 (2017)

- A systematic approach for studying various molecular candidates with special focus on:
 - pionic dof, coupled-channel dynamics, HQSS and the pattern of its breaking
 - three-body effects ($P\bar{P}\pi$) and the η -meson from SU(3) GB octet are included also
 - leading HQSS violation is included via the V - P mass splitting

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- nonperturbative solutions of the LS integral Eqs. for various $J^{PC} = 1^{++}, 2^{++}, 0^{++}$ and 1^{+-}

➡ Potential: contact operators (2 parameters) + π and η -meson \Rightarrow input is needed!

input in c-quark sector: 1^{++} $X(3872) \Rightarrow$ output : 2^{++} partner state X_{c2}

To predict other partners of the $X(3872)$ one more experimental input is needed! $X(3915)?$

input in b-quark sector: 1^{+-} $Z_b(10610)/Z_b(10650) \Rightarrow$ output: $W_{b0} (0^{++}), W'_{b0} (0^{++}),$
 $W_{b1} (1^{++})$ and $W_{b2} (2^{++})$

Some technical details

- Pionic Lagrangian: $\mathcal{L} = \frac{g_b}{2f_\pi} \left(\mathbf{B}^{*\dagger} \cdot \nabla \pi^a \tau^a \mathbf{B} + \mathbf{B}^\dagger \tau^a \nabla \pi^a \cdot \mathbf{B}^* + i[\mathbf{B}^{*\dagger} \times \mathbf{B}^*] \cdot \nabla \pi^a \tau^a \right)$

with $g_b = g_c \approx 0.57$ from $D^* \rightarrow D\pi$ width and HQSS

- Exemplary potential:

$$V_{B\bar{B}^* \rightarrow B^*\bar{B}}(\mathbf{p}, \mathbf{p}') = -\frac{2g_b^2}{(4\pi f_\pi)^2} \tau_1 \cdot \tau_2^c (\epsilon_1 \cdot \mathbf{q})(\epsilon_2'^* \cdot \mathbf{q}) \left(\frac{1}{D_{BB\pi}(\mathbf{p}, \mathbf{p}')} + \frac{1}{D_{B^*B^*\pi}(\mathbf{p}, \mathbf{p}')} \right)$$

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- ➡ 3-body propagators with NR heavy mesons and relativistic pions

$$D_{BB\pi}(\mathbf{p}, \mathbf{p}') = 2E_\pi(\mathbf{q}) \left(m + m + \frac{\mathbf{p}^2}{2m} + \frac{\mathbf{p}'^2}{2m} + E_\pi(\mathbf{q}) - \sqrt{s} \right) \quad E_\pi(\mathbf{q}) = \sqrt{\mathbf{q}^2 + m_\pi^2}$$

$$D_{B^*B^*\pi}(\mathbf{p}, \mathbf{p}') = 2E_\pi(\mathbf{q}) \left(m_* + m_* + \frac{\mathbf{p}^2}{2m_*} + \frac{\mathbf{p}'^2}{2m_*} + E_\pi(\mathbf{q}) - \sqrt{s} \right)$$

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- **Scattering amplitude from coupled-channel integral Eqs:**

$$a_{ij}^{(JPC)}(p, p') = V_{ij}^{(JPC)}(p, p') - \sum_n \int dk k^2 V_{in}^{(JPC)}(p, k) G_n(k) a_{nj}^{(JPC)}(k, p')$$

- ➔ $V_{ij}^{(JPC)}(p, p')$ stands for the **partial wave projected $\pi + \eta$ -meson exchanges +contact terms**

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➡ For D-mesons: $D_{DD\pi}(\mathbf{p}, \mathbf{p}')$ and $G_n(k)$ contain 3-body cuts

Sign of the OPE potential

$$V_{B\bar{B}^* \rightarrow B^*\bar{B}}^C(\mathbf{p}, \mathbf{p}') = -C \frac{2g_b^2}{(4\pi f_\pi)^2} \tau_1 \cdot \tau_2^c (\boldsymbol{\epsilon}_1 \cdot \mathbf{q})(\boldsymbol{\epsilon}'_2{}^* \cdot \mathbf{q}) \left(\frac{1}{D_{BB\pi}(\mathbf{p}, \mathbf{p}')} + \frac{1}{D_{B^*B^*\pi}(\mathbf{p}, \mathbf{p}')} \right)$$

- Isospin coefficient: $\tau_1 \cdot \tau_2^c = 3 - 2I(I + 1) = \begin{cases} 3 & I=0 \\ -1 & I=1 \end{cases}$ — different signs
- sign also depends on C-parity: $C = \pm$
- ➡ central (S-wave) OPE for **isospin-1** $0^{++}, 1^{++}$ and 2^{++} states is repulsive for 1^{+-} — attractive
- ➡ central (S-wave) OPE for **isospin-0** $0^{++}, 1^{++}$ and 2^{++} states is attractive for 1^{+-} — repulsive

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☞ central (S-wave) OPE for **isospin-1** $0^{++}, 1^{++}$ and 2^{++} states is repulsive for 1^{+-} — attractive

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⇒ central (S-wave) OPE is attractive for the $X(3872)$ and Z_b 's

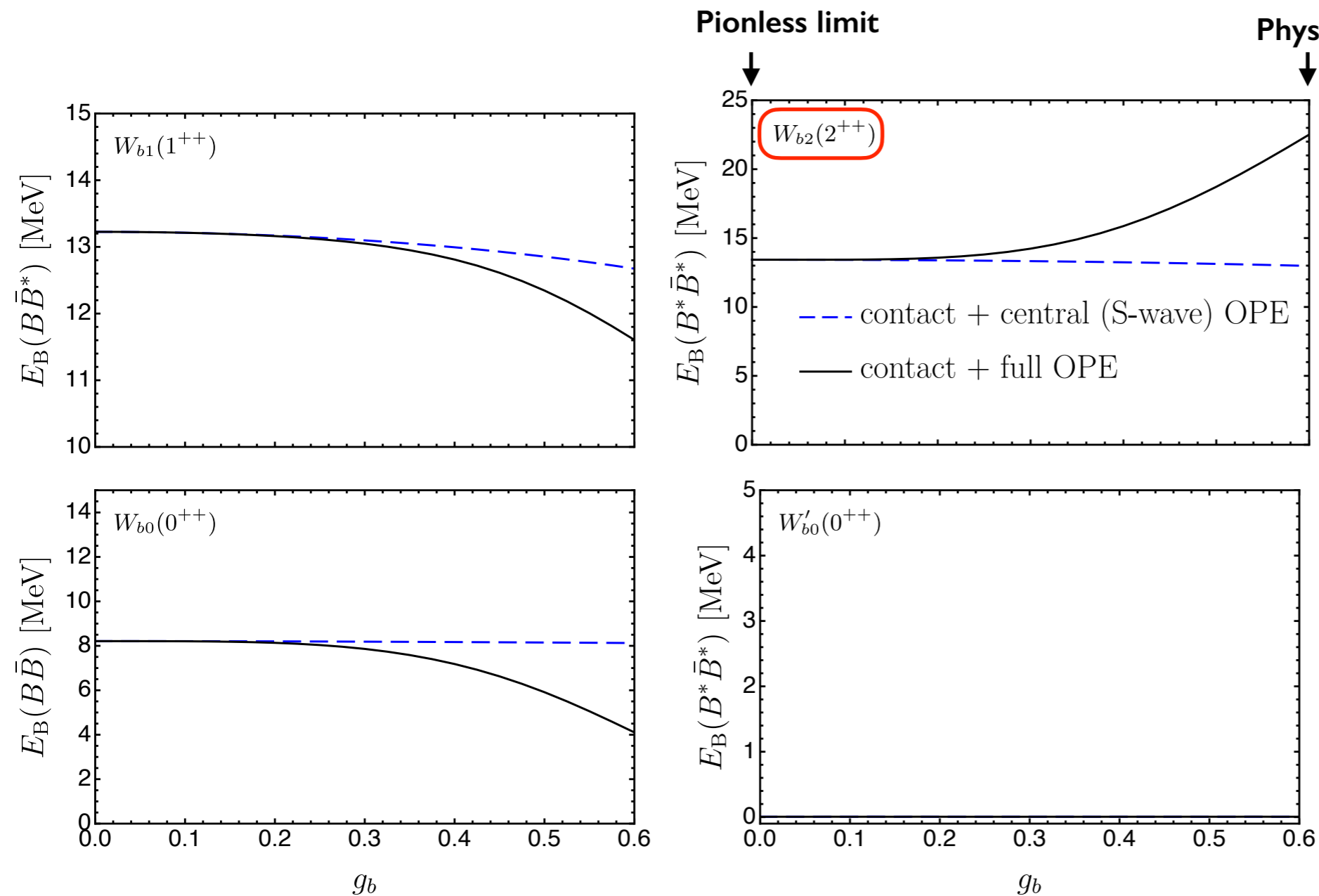
⇒ Naively, repulsive OPE should reduce the binding energies of the Z_b 's partner states

But too naive:

- tensor forces (off diagonal S-D transitions) bring additional attraction!
- when OPE is added LECs must be refitted to reproduce the exp.input

⇒ effect of OPE is nontrivial

Z_b 's partner states BE (E_B) vs pion coupling constant g_B



Input for binding energies:

$$E_B(Z_b) = 5 \text{ MeV}$$

$$E_B(Z_b') = 1 \text{ MeV}$$

consistent with data by Belle

Cleven et al. (2011)

Physical value of g_B :

$$g_B = g_C = 0.57$$

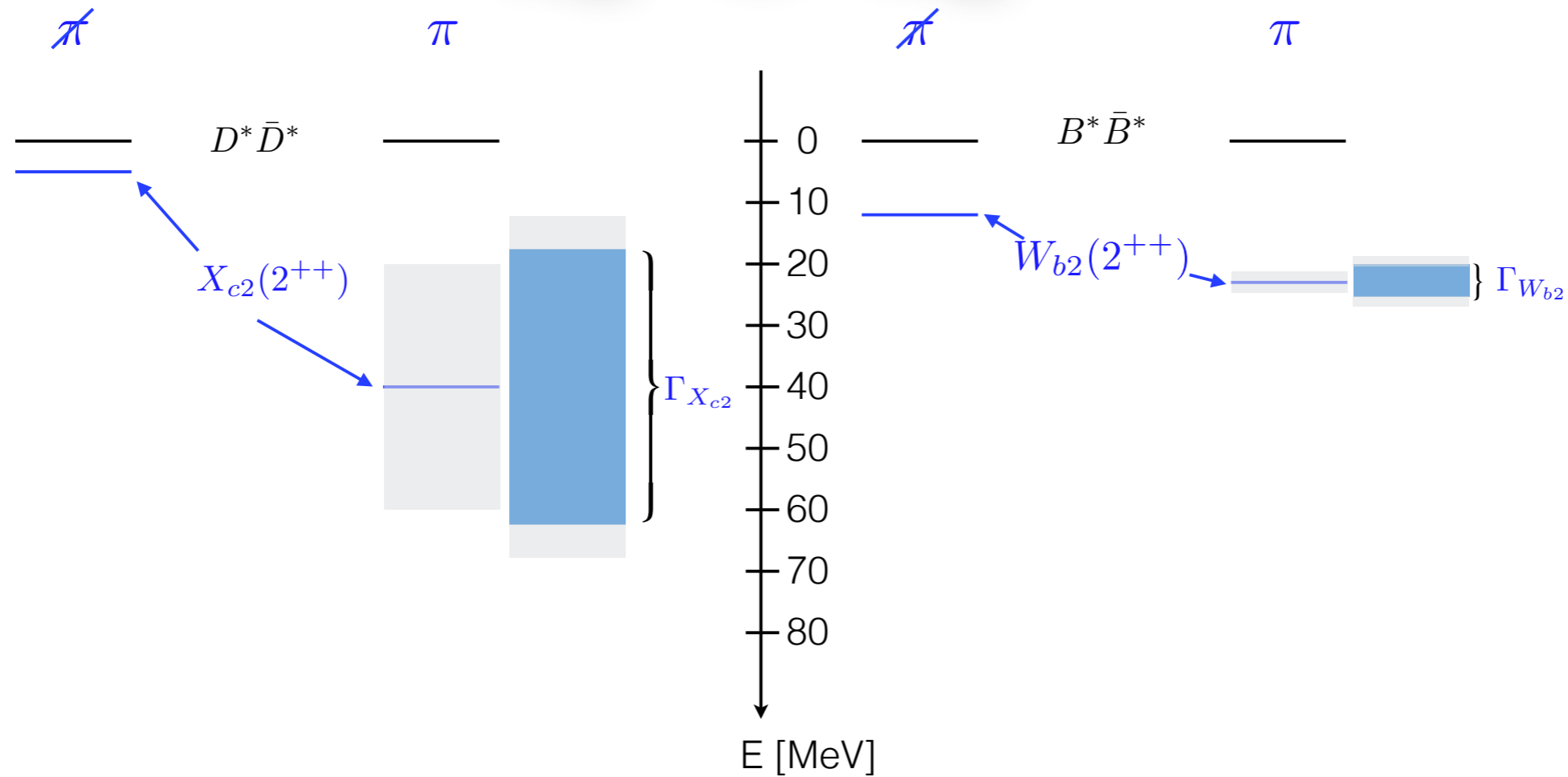
👉 For each g_B — refit the contact terms to reproduce the input values for the Z_b 's

- For $g_B < 0.3$ pions can be absorbed into redefinitions of the contact terms
- OPE Tensor forces: sizeable contributions at the physical value of g_B
- OPE Central (S-wave) force — almost no influence on the results

HQSS implications: $X(3872)$ vs $Z_b(10610)/Z_b(10650)$

2^{++} tensor partners:

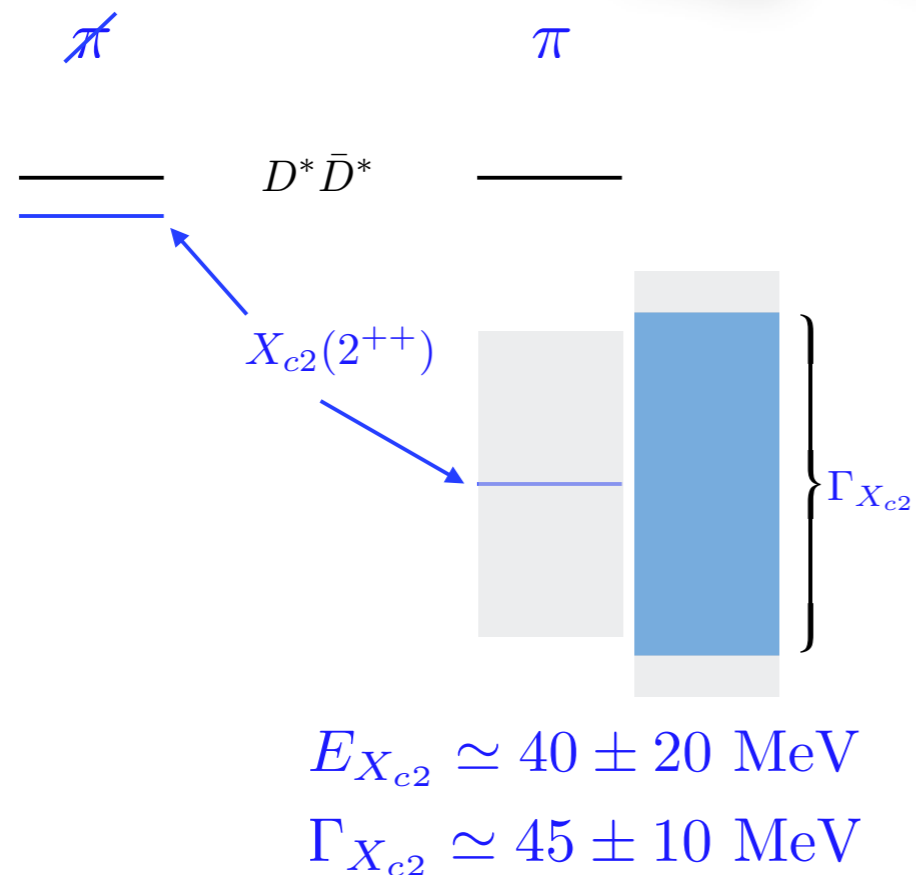
X_{c2} vs W_{b2}



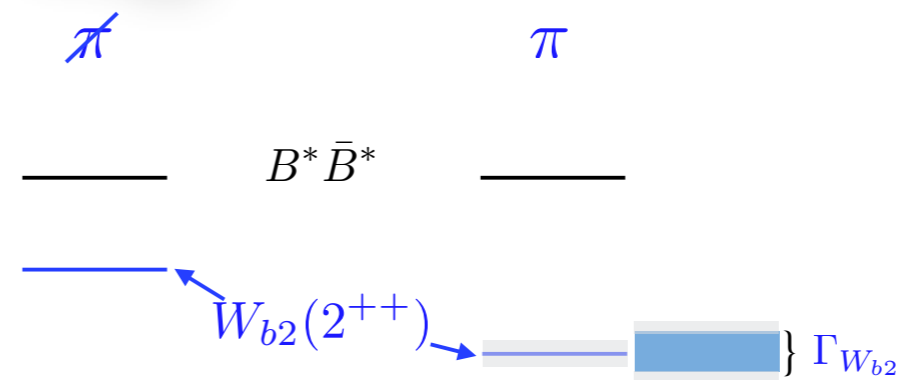
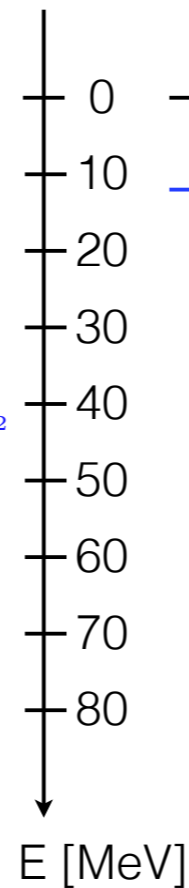
HQSS implications: $X(3872)$ vs $Z_b(10610)/Z_b(10650)$

2^{++} tensor partners:

X_{c2} vs W_{b2}



Largest uncertainty: UV regulator dependence



$$E_{W_{b2}} \simeq 22.5 \pm 2 \text{ MeV}$$

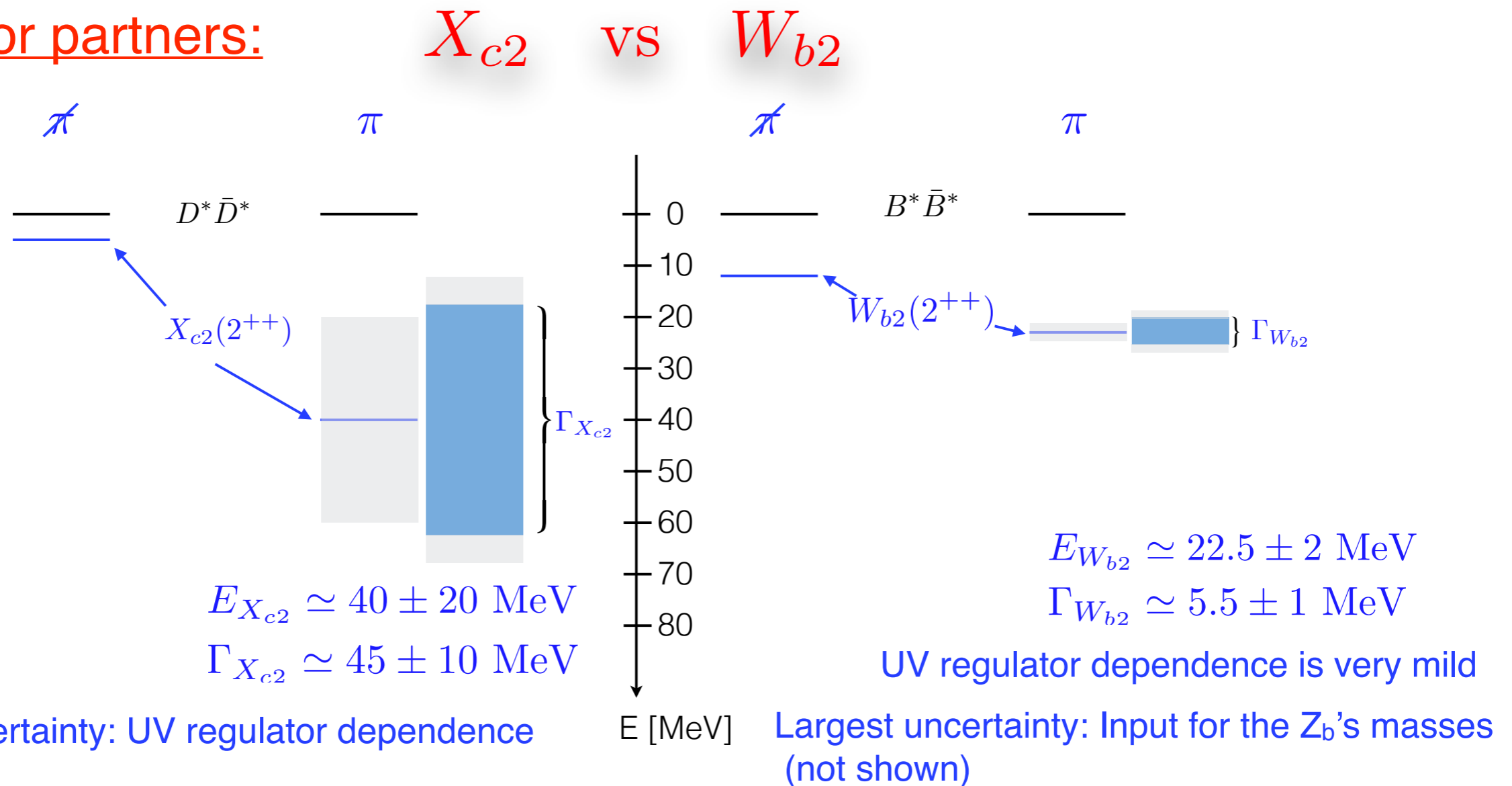
$$\Gamma_{W_{b2}} \simeq 5.5 \pm 1 \text{ MeV}$$

UV regulator dependence is very mild

Largest uncertainty: Input for the Z_b 's masses (not shown)

HQSS implications: $X(3872)$ vs $Z_b(10610)/Z_b(10650)$

2^{++} tensor partners:



● Impact of HQSS violation enhanced by nonperturbative pions on the tensor:

- ➡ stronger in the c-sector than in the b-sector
- ➡ larger than with perturbative pions

For a perturbative approach
see [Albaladejo et al. \(2015\)](#)

- **Role of 3-body effects:** sizeable in the c-sector (reduce E_B and Γ up to 20%)
marginal in the b-sector

Summary and conclusions

- We propose a systematic approach consistent with chiral and heavy quark symmetries to probe various molecular candidates in c and b -sectors
- It can be applied to study various aspects of light quark dynamics in $D^{(*)}D^{(*)}$ and $B^{(*)}B^{(*)}$
- Generalisation to other systems involving $\{D_1, D_2\}$ and $\{B_1, B_2\}$ doublets is straight fwd

Applied in this talk to predict HQSS partners of $X(3872)$ and $Z_b(10610)/Z_b(10650)$

- HQSS breaking and non-perturbative pions have significant impact on the partner states
- ➡ The effect from OPE is stronger in the c -quark sector, than in the b -quark one.
- ➡ Accurate predictions of the Z_b partners: relatively weak HQSS breaking, no $b\bar{b}$ admixture

$X_{c2^{++}}$ is significantly shifted from $D^*\bar{D}^*$ threshold and has the width $\Gamma_{X_{c2}} \simeq 45 \pm 10$ MeV

$W_{b2^{++}}$ is still located around $B^*\bar{B}^*$ threshold and has a few MeV width

should be detectable in $BB^{(*)}$ and also in $\chi_{b1}\pi$ and $\chi_{b2}\pi$ channels