

Are the X(4260) and X(4360) Molecular State?

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XVII International Conference on Hadron Spectroscopy and Structure
Salamanca, 25 September, 2017

OVERVIEW

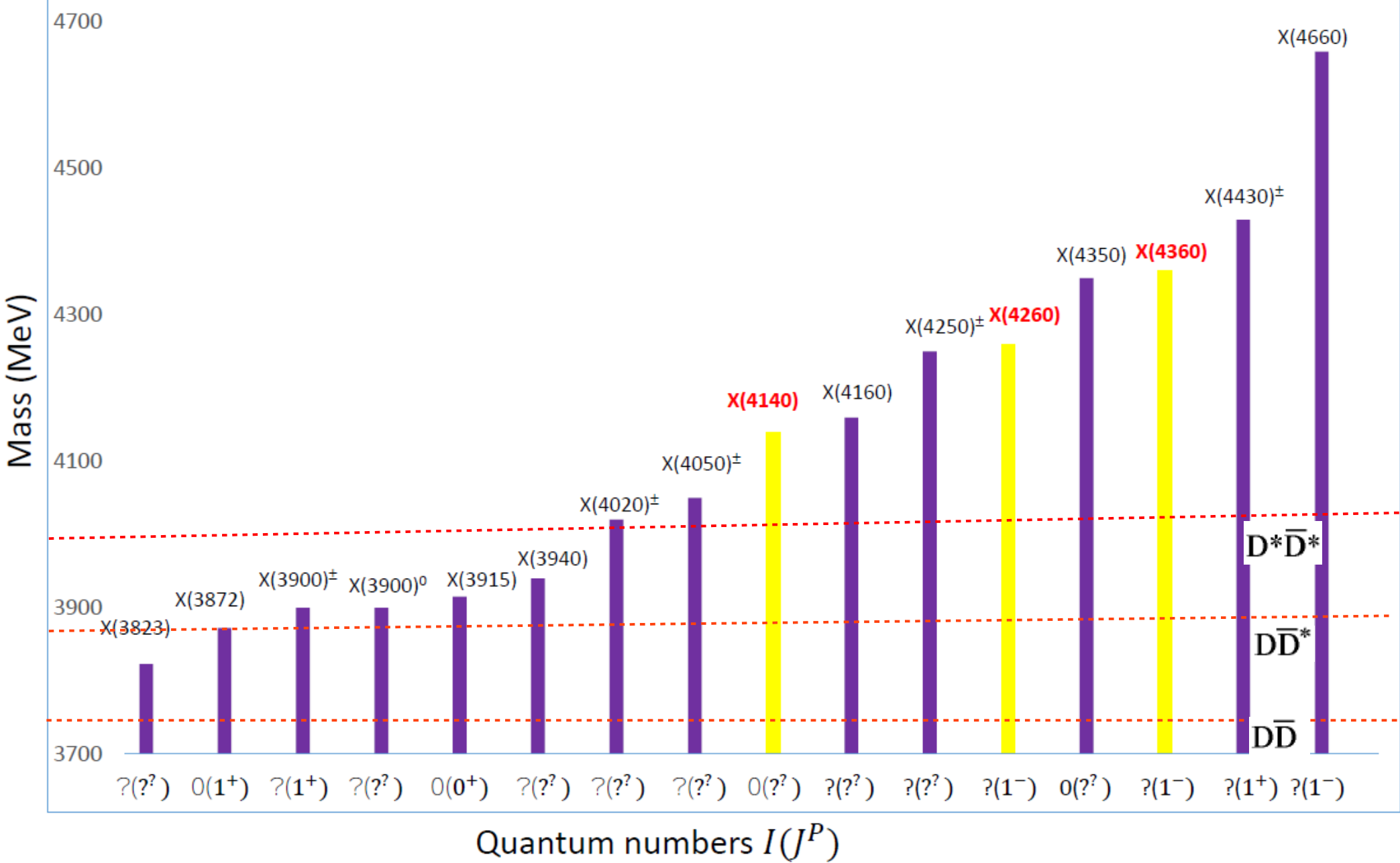
★ *Introduction*

★ *Formalism*

★ *Results and Discussion*

★ *Summary*

Spectrum of **XHADRONS**



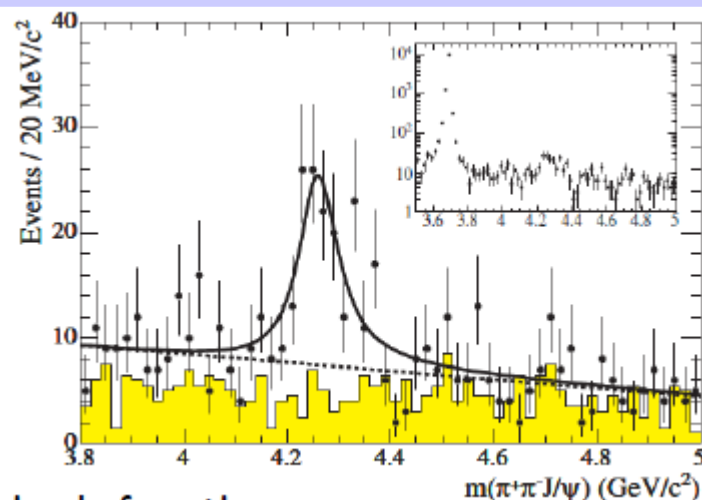
$X(4260) \quad I^G(J^{PC})=?^?(1^-)$

- In 2005, BABAR, the process $e^+e^- \rightarrow \pi\pi J/\Psi$ cross section

(B. Aubert et al. [BaBar Collaboration], Phys Rev. Lett. 95,142001, 2005)

$$m \sim 4260 \text{ MeV}/c^2$$

$$\Gamma \sim 90 \text{ MeV}/c^2$$

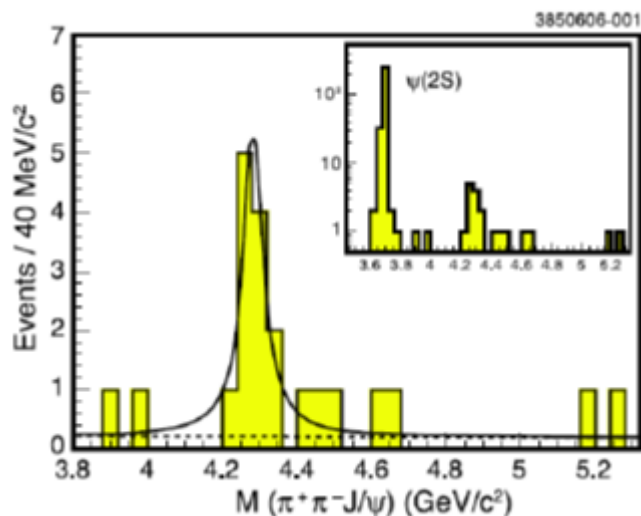


- The Cleo Collaboration searched for the new resonances $X(4260)$

(Q. He et al. [CLEO Collaboration], Phys Rev. D 74, 091104, 2006)

$$m \sim 4284_{-16}^{+17} \text{ (stat)} \pm 4 \text{ (syst)} \text{ MeV}/c^2$$

$$\Gamma \sim 73_{-25}^{+39} \text{ (stat)} \pm 5 \text{ (syst)} \text{ MeV}/c^2$$

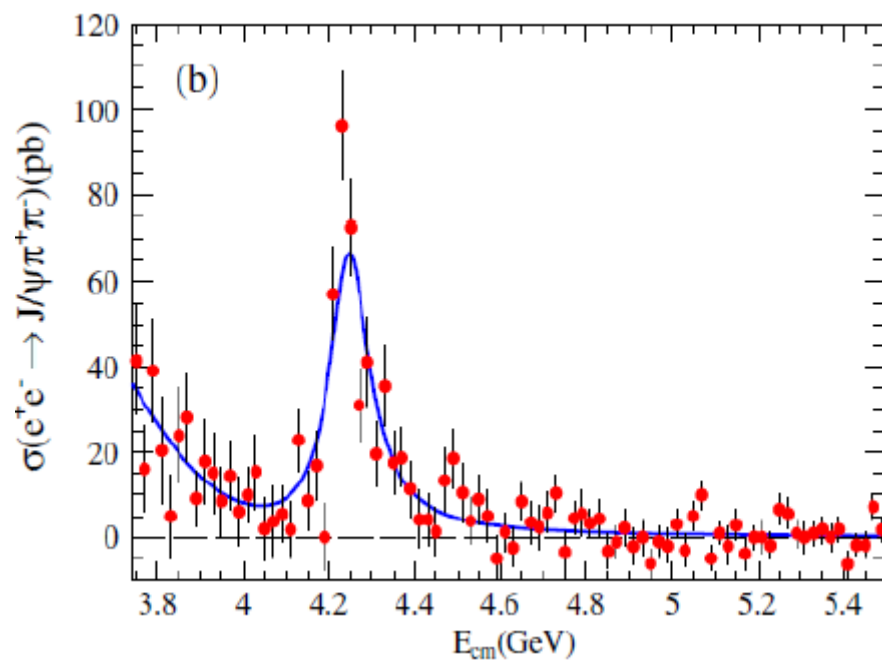


- Again, BABAR Collaboration studied $e^+e^- \rightarrow \pi\pi J/\Psi$ in the c.m. Energy range 3.74-5.50 GeV using ISR events

(J. P. Leset al. [BaBar Collaboration], Phys Rev. D 86, 051102, 2012)

$$m \sim 4245 \pm \text{(stat)} \pm 4 \text{ (syst)} \text{ MeV}/c^2$$

$$\Gamma \sim 114_{-15}^{+16} \text{ (stat)} \pm 7 \text{ (syst)} \text{ MeV}/c^2$$



$X(4360)$ $I^G(J^{PC}) = ??(1^{--})$

- In 2007, BABAR observed a structure

(B. Aubert et al. [BaBar Collaboration], Phys Rev. Lett. 98,212001, 2007)

$$m \sim 4324.0 \pm 24 \text{ MeV}/c^2$$
$$\Gamma \sim 172 \pm 33 \text{ MeV}$$

- Belle, measured $e^+e^- \rightarrow \pi\pi\Psi(2S)$ cross section between threshold and 5.5 GeV. This state is in a good agreement with structure observed by BABAR in mass but with a much narrower width

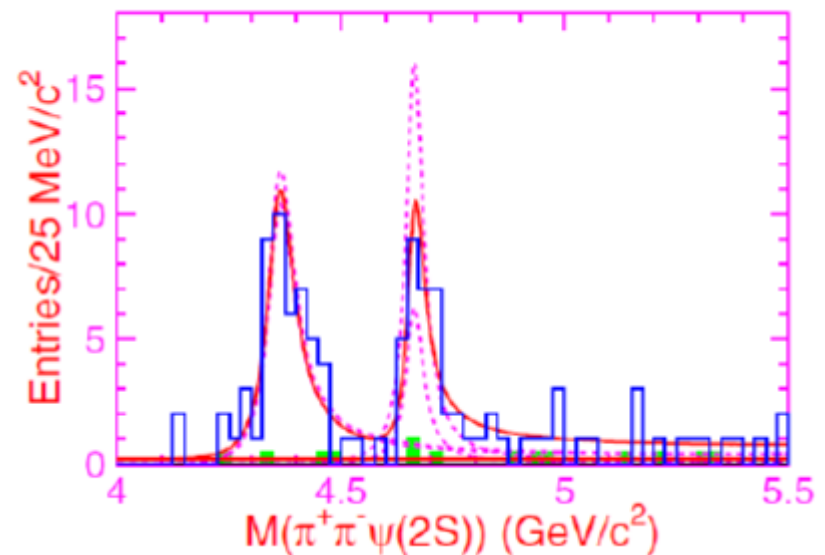
(X. L. Wang et al. [Belle Collaboration], Phys. Rev. Lett., 99, 142002, 2007)

$$m \sim 4361.0 \pm 9 \pm 9 \text{ MeV}/c^2$$

$$\Gamma \sim 74 \pm 15 \pm 15 \text{ MeV}/c^2$$

$$m \sim 4664.0 \pm 11 \pm 5 \text{ MeV}/c^2$$

$$\Gamma \sim 48 \pm 15 \pm 3 \text{ MeV}/c^2$$



$X(4260)$ and $X(4360) \rightarrow$ Molecular State??

ρ $D\bar{D}$ Three Body System

Fixed Center Approximation (FCA) to the Faddeev equations is an effective tool to deal with the three-body hadronic interactions.

*This method is technically **simple** and **accurate** when dealing with **bound states**.*

$\bar{K}NK$, $\bar{K}NN$, DNN , multi- ρ , ... (M.Bayar, J. Yamagata, L. Roca, C.W.Xiao, J.J.Xie, A. Martines Torres, W.H. Liang, E. Oset: PRC84(2011)015209, PRD84(2011)0340037, NPA833(2012)57, PRD82(2010)054013, PRD82(2010)094017.)

$\pi(\Delta\rho) \Rightarrow$ solved the $\Delta_{\frac{5}{2}^+}$ (2000) puzzle (J.J. Xie, A. Martines Torres, E. Oset, PRC83(2011)055204)

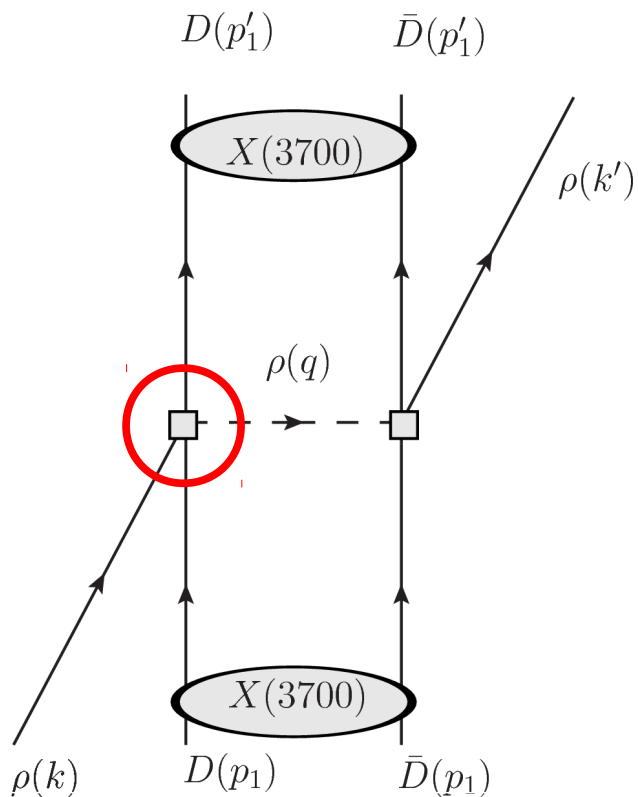
Limits to the FCA to the Faddeev equations (A. Martines Torres, E.J. Garzon, E. Oset PRD83(2011)116002; M.Bayar, J. Yamagata, E. Oset PRC84(2012)015209.)

THREE BODY INTERACTION

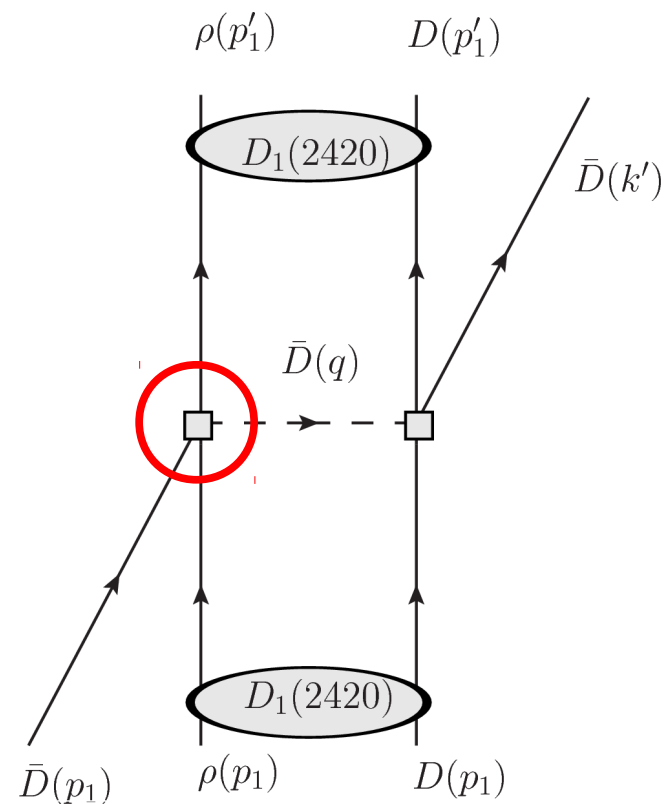
the $\rho D \bar{D}$ system

- ★ A cluster of two bound particles $D\bar{D}$, ($I=0$), $X(3700)$ and ρD , ($I=1/2$), $D_1(2420)$
- ★ Third particle interacts with the cluster

the $\rho - X(3700)$



the $\bar{D} - D_1(2420)$



ρD (vector - pseudoscalars mesons) two body scattering :

Channel content in each sector for the pseudoscalar vector

meson interaction *D. Gamermann and E. Oset Eur. Phys. J. A 33, 119–131*

(2007)

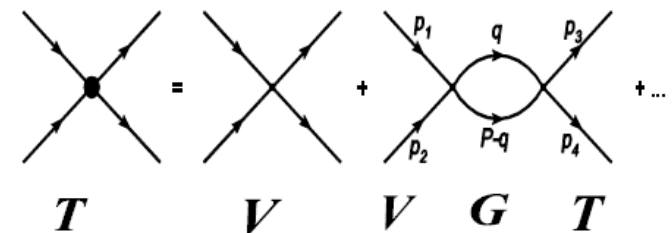
Charm	Strangeness	$I^G(J^{PC})$	Channels
1	1	1(1 ⁺)	$\pi D_s^*, D_s \rho$ $K D^*, DK^*$
		0(1 ⁺)	$DK^*, KD^*, \eta D_s^*$ $D_s \omega, \eta_c D_s^*, D_s J/\psi$
	0	$\frac{1}{2}(1^+)$	$\pi D^*, D \rho, K D_s^*, D_s K^*$ $\eta D^*, D \omega, \eta_c D^*, DJ/\psi$
	-1	0(1 ⁺)	DK^*, KD^*
0	1	$\frac{1}{2}(1^+)$	$\pi K^*, K \rho, \eta K^*, K \omega$ $\bar{D} D_s^*, D_s \bar{D}^*, K J/\psi, \eta_c K^*$
		0	1 ⁺ (1 ⁺⁻)
		1 ⁻ (1 ⁺⁺)	$\pi \rho, \frac{1}{\sqrt{2}}(\bar{K} K^* - c.c.), \frac{1}{\sqrt{2}}(\bar{D} D^* - c.c.)$
		0 ⁺ (1 ⁺⁺)	$\frac{1}{\sqrt{2}}(\bar{K} K^* + c.c.), \frac{1}{\sqrt{2}}(\bar{D} D^* + c.c.), \frac{1}{\sqrt{2}}(\bar{D}_s D_s^* - c.c.)$
		0 ⁻ (1 ⁺⁻)	$\pi \rho, \eta \omega, \frac{1}{\sqrt{2}}(D D^* - c.c.), \eta_c \omega$ $\eta J/\psi, \frac{1}{\sqrt{2}}(\bar{D}_s D_s^* + c.c.), \frac{1}{\sqrt{2}}(\bar{K} K^* - c.c.), \eta_c J/\psi$

TABLE II. The C^I coefficients in Eq. (2) for the $I = 3/2$ case.

Channels	πD^*	$D \rho$
πD^*	1	1
$D \rho$	1	1

$\rho D, (I=1/2), D_1(2420)$

$$T = -(\hat{1} + V\hat{G})^{-1}V\vec{\epsilon} \cdot \vec{\epsilon}'$$



ρD (vector - pseudoscalars mesons) two body scattering :

The potentials, projected over s-wave:

$$V_{ij}^I(s) = \frac{1}{2} \int_{-1}^1 d(\cos\theta) \tilde{V}_{ij}^I(s, t(s, \cos\theta), u(s, \cos\theta))$$

The loop function:

$$\begin{aligned} G_l &= i \int \frac{dq^4}{(2\pi)^4} \frac{1}{q^2 - m_l^2 + i\epsilon} \frac{1}{(P - q)^2 - M_l^2 + i\epsilon} \\ &= \frac{1}{16\pi^2} \left(\alpha_l + \text{Log} \frac{m_l^2}{\mu^2} + \frac{M_l^2 - m_l^2 + s}{2s} \text{Log} \frac{M_l^2}{m_l^2} \right. \\ &\quad \left. + \frac{p}{\sqrt{s}} \left(\text{Log} \frac{s - M_l^2 + m_l^2 + 2p\sqrt{s}}{-s + M_l^2 - m_l^2 + 2p\sqrt{s}} + \text{Log} \frac{s + M_l^2 - m_l^2 + 2p\sqrt{s}}{-s - M_l^2 + m_l^2 + 2p\sqrt{s}} \right) \right) \end{aligned}$$

The Unitarized T-matrix for DD

D. Gamermann, E. Oset, D. Strottman and M. J. Vicente Vacas, Phys. Rev. D 76, 074016 (2007)

$DD, K\bar{K}, \pi\bar{\pi}, \eta\eta, \eta_c\eta, D_s\bar{D}_s$, in the $I = 0$

$DD, K\bar{K}, \pi\bar{\pi}, \pi\eta, \eta_c\pi$, in the $I = 1$ case

Bethe-Salpeter equation for DD: $T = (\hat{1} - V\hat{G})^{-1}V$

FIXED-CENTER FORMALISM FOR THE THREE BODY SYSTEM

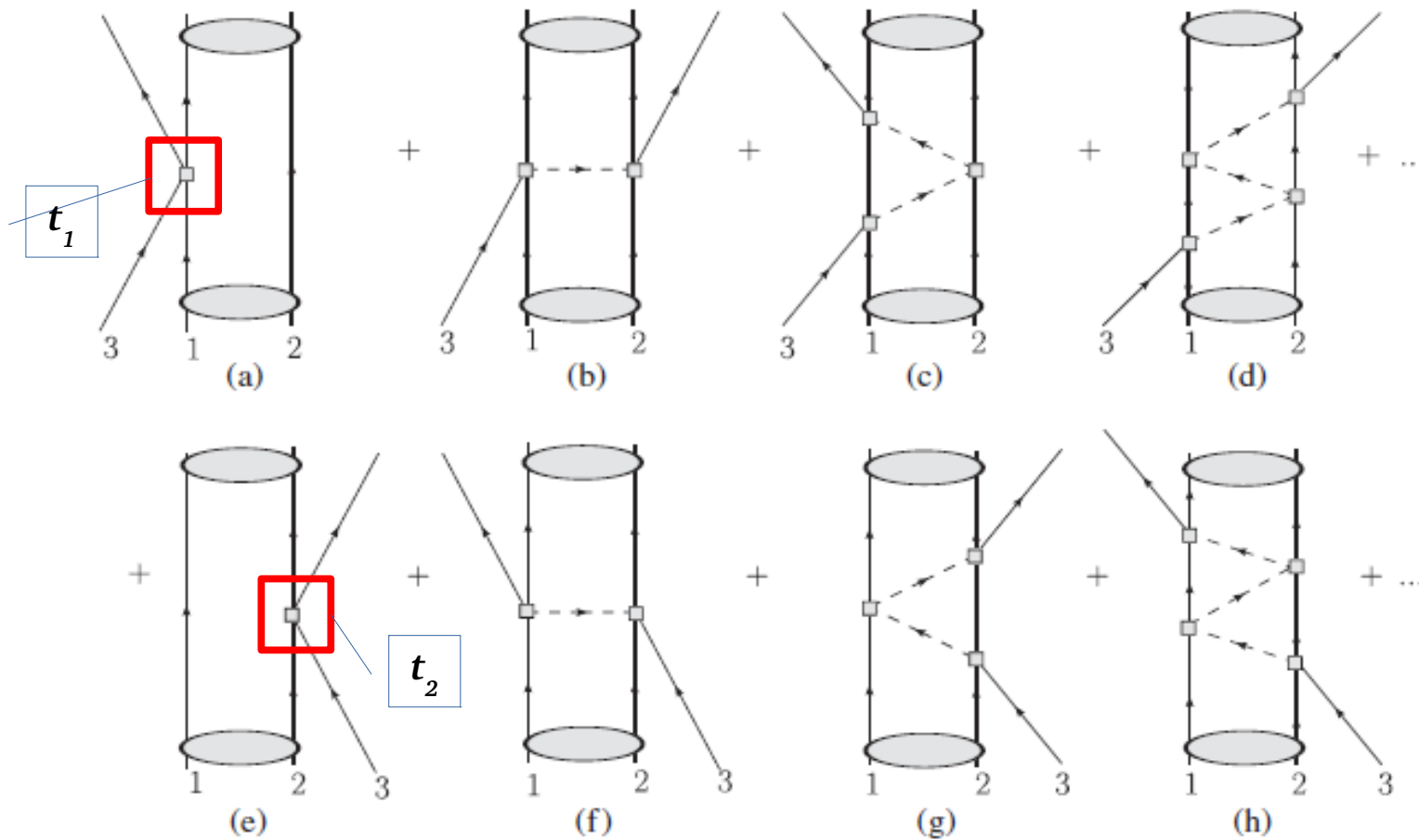


FIG. Diagrammatic representation of the fixed-center approximation to Faddeev equations

- ★ ***T1***: all diagrams beginning with interaction in 1 meson.
- ★ ***T2***: all diagrams beginning with interaction in 2 meson.

$$T_1 = t_1 + t_1 G_0 T_2,$$

$$T_2 = t_2 + t_2 G_0 T_1.$$

$$T = T_1 + T_2$$

For the normalization

The S -matrix for the single scattering:

$$S_1^{(1)} = -it_1 \frac{1}{\mathcal{V}^2} (2\pi)^4 \delta^4(k_3 + k_{\text{cls}} - k'_3 - k'_{\text{cls}}) \\ \times \frac{1}{\sqrt{2\omega_3}} \frac{1}{\sqrt{2\omega'_3}} \frac{1}{\sqrt{2\omega_1}} \frac{1}{\sqrt{2\omega'_1}},$$

S -matrix for the double scattering:

$$S^{(2)} = -i(2\pi)^4 \frac{1}{\mathcal{V}^2} \delta^4(k_3 + k_{\text{cls}} - k'_3 - k'_{\text{cls}}) \\ \times \frac{1}{\sqrt{2\omega_3}} \frac{1}{\sqrt{2\omega'_3}} \frac{1}{\sqrt{2\omega_1}} \frac{1}{\sqrt{2\omega'_1}} \frac{1}{\sqrt{2\omega_2}} \frac{1}{\sqrt{2\omega'_2}} \\ \times \int \frac{d^3q}{(2\pi)^3} F_{\text{cls}}(q) \frac{1}{q^{02} - \vec{q}^2 - m_3^2 + i\epsilon} t_1 t_2,$$

Using the low energy reduction

$$\sqrt{2\omega} \sim \sqrt{2m}$$

$$\tilde{t}_1 = \frac{m_{\text{cls}}}{m_1} t_1, \quad \tilde{t}_2 = \frac{m_{\text{cls}}}{m_2} t_2$$

The full three-body scattering:

$$S = -iT \frac{1}{\mathcal{V}^2} (2\pi)^4 \delta^4(k_3 + k_{\text{cls}} - k'_3 - k'_{\text{cls}}) \\ \times \frac{1}{\sqrt{2\omega_3}} \frac{1}{\sqrt{2\omega'_3}} \frac{1}{\sqrt{2\omega_{\text{cls}}}} \frac{1}{\sqrt{2\omega'_{\text{cls}}}}.$$

For the normalization

The S -matrix for the single scattering:

$$S_1^{(1)} = -it_1 \frac{1}{\mathcal{V}^2} (2\pi)^4 \delta^4(k_3 + k_{\text{cls}} - k'_3 - k'_{\text{cls}}) \\ \times \frac{1}{\sqrt{2\omega_3}} \frac{1}{\sqrt{2\omega'_3}} \frac{1}{\sqrt{2\omega_1}} \frac{1}{\sqrt{2\omega'_1}},$$

S -matrix for the double scattering:

$$S^{(2)} = -i(2\pi)^4 \frac{1}{\mathcal{V}^2} \delta^4(k_3 + k_{\text{cls}} - k'_3 - k'_{\text{cls}}) \\ \times \frac{1}{\sqrt{2\omega_3}} \frac{1}{\sqrt{2\omega'_3}} \frac{1}{\sqrt{2\omega_1}} \frac{1}{\sqrt{2\omega'_1}} \frac{1}{\sqrt{2\omega_2}} \frac{1}{\sqrt{2\omega'_2}} \\ \times \int \frac{d^3q}{(2\pi)^3} F_{\text{cls}}(q) \frac{1}{q^{02} - \vec{q}^2 - m_3^2 + ie} t_1 t_2,$$

The full three-body scattering:

$$S = -iT \frac{1}{\mathcal{V}^2} (2\pi)^4 \delta^4(k_3 + k_{\text{cls}} - k'_3 - k'_{\text{cls}}) \\ \times \frac{1}{\sqrt{2\omega_3}} \frac{1}{\sqrt{2\omega'_3}} \frac{1}{\sqrt{2\omega_{\text{cls}}}} \frac{1}{\sqrt{2\omega'_{\text{cls}}}}.$$

Using the low energy reduction

$$\sqrt{2\omega} \sim \sqrt{2m}$$

$$\tilde{t}_1 = \frac{m_{\text{cls}}}{m_1} t_1, \quad \tilde{t}_2 = \frac{m_{\text{cls}}}{m_2} t_2$$

we get:

$$T = T_1 + T_2 = \frac{\tilde{t}_1 + \tilde{t}_2 + 2\tilde{t}_1\tilde{t}_2 G_0}{1 - \tilde{t}_1\tilde{t}_2 G_0^2}.$$

The function G_0 is the meson exchange propagator

The Function G_0

$$G_0 = \frac{1}{2m_{\text{cls}}} \int \frac{d^3 q}{(2\pi)^3} F_{\text{cls}}(q) \frac{1}{q^0{}^2 - \vec{q}^2 - m_3^2 + i\epsilon}$$

The Form factor:

$$F_{\text{cls}}(q) = \frac{1}{\mathcal{C}} \int_{\substack{p < k_{\text{max}} \\ |\vec{p} - \vec{q}| < k_{\text{max}}}} d^3 p \frac{1}{2\omega_1(\vec{p})} \frac{1}{2\omega_2(\vec{p})} \frac{1}{m_{\text{cls}} - \omega_1(\vec{p}) - \omega_2(\vec{p})} \\ \times \left(\frac{1}{2\omega_1(\vec{p} - \vec{q})} \right) \left(\frac{1}{2\omega_2(\vec{p} - \vec{q})} \right) \frac{1}{m_{\text{cls}} - \omega_1(\vec{p} - \vec{q}) - \omega_2(\vec{p} - \vec{q})},$$

$$\mathcal{C} = \int_{p < k_{\text{max}}} d^3 p \left[\frac{1}{2\omega_1(\vec{p})} \frac{1}{2\omega_2(\vec{p})} \frac{1}{m_{\text{cls}} - \omega_1(\vec{p}) - \omega_2(\vec{p})} \right]^2$$

The arguments of the three body amplitude $T(s)$ and two body amplitudes $t_j(s_j)$

- ★ $s \rightarrow$ the total invariant mass of the three body system
- ★ $s_j \rightarrow$ the invariant masses of the two body systems

→ the binding energy among the three particles, proportionally to their masses:

the total energy of the two body system:

$$E_1 = \frac{\sqrt{s}}{(m_{\text{cls}} + m_3)} \frac{m_1 m_{\text{cls}}}{(m_1 + m_2)}$$

$$E_2 = \frac{\sqrt{s}}{(m_{\text{cls}} + m_3)} \frac{m_2 m_{\text{cls}}}{(m_1 + m_2)}$$

$$E_3 = m_3 \frac{\sqrt{s}}{(m_{\text{cls}} + m_3)}$$

$$\begin{aligned} s_{1(2)} &= (p_3 + p_{1(2)})^2 \\ &= \left(\frac{\sqrt{s}}{m_{\text{cls}} + m_3} \right)^2 \left(m_3 + \frac{m_{1(2)} m_{\text{cls}}}{m_1 + m_2} \right)^2 - \vec{P}_{2(1)}^2 \end{aligned}$$

with an approximate value of $\vec{P}_{2(1)}$,

$$\frac{\vec{P}_{2(1)}^2}{2m_{2(1)}} \simeq B_{2(1)} \equiv \frac{m_{2(1)} m_{\text{cls}}}{(m_1 + m_2)} \frac{(m_{\text{cls}} + m_3 - \sqrt{s})}{(m_{\text{cls}} + m_3)},$$

↓
the binding energy of particle 2 (1)

The Isospin

the $\rho - X(3700)$

the cluster of $X(3700)$, $I_{D\bar{D}} = 0$

$$|D\bar{D}\rangle^{I=0} = \frac{1}{\sqrt{2}} \left| \frac{1}{2}, -\frac{1}{2} \right\rangle - \frac{1}{\sqrt{2}} \left| -\frac{1}{2}, \frac{1}{2} \right\rangle \quad \text{with the nomenclature } |I_{z_1}, I_{z_2}\rangle \text{ for the } D\bar{D} \text{ system}$$

The total isospin of the three body system $I_{\rho(D\bar{D})} = 1$

$$\begin{aligned} \langle \rho D\bar{D} | t | \rho D\bar{D} \rangle &= \langle \rho^+ (D\bar{D})^{I=0} | (\hat{t}_{\rho D} + \hat{t}_{\rho \bar{D}}) | \rho^+ (D\bar{D})^{I=0} \rangle \quad \text{with nomenclature } |D\bar{D}, I, I_z\rangle \otimes |\rho, I, I_z\rangle \\ &= -\langle 1, +1 | \otimes \frac{1}{\sqrt{2}} \left(\left\langle \frac{1}{2}, \frac{1}{2} \right| \left\langle \frac{1}{2}, -\frac{1}{2} \right| - \left\langle \frac{1}{2}, -\frac{1}{2} \right| \left\langle \frac{1}{2}, \frac{1}{2} \right| \right) (\hat{t}_{\rho D} + \hat{t}_{\rho \bar{D}}) \\ &\quad \times \frac{1}{\sqrt{2}} \left(\left| \frac{1}{2}, \frac{1}{2} \right\rangle \left| \frac{1}{2}, -\frac{1}{2} \right\rangle - \left| \frac{1}{2}, -\frac{1}{2} \right\rangle \left| \frac{1}{2}, \frac{1}{2} \right\rangle \right) \otimes (-) |1, +1\rangle \\ &= \left(\frac{2}{3} t_{\rho D}^{I=3/2} + \frac{1}{3} t_{\rho D}^{I=1/2} \right) + \left(\frac{2}{3} t_{\rho \bar{D}}^{I=3/2} + \frac{1}{3} t_{\rho \bar{D}}^{I=1/2} \right) \end{aligned}$$

The Isospin

the $\rho - X(3700)$

the cluster of $X(3700)$, $I_{D\bar{D}} = 0$

$$|D\bar{D}\rangle^{I=0} = \frac{1}{\sqrt{2}} \left| \frac{1}{2}, -\frac{1}{2} \right\rangle - \frac{1}{\sqrt{2}} \left| -\frac{1}{2}, \frac{1}{2} \right\rangle \quad \text{with the nomenclature } |I_{z_1}, I_{z_2}\rangle \text{ for the } D\bar{D} \text{ system}$$

The total isospin of the three body system $I_{\rho(D\bar{D})} = 1$

$$\begin{aligned} \langle \rho D\bar{D} | t | \rho D\bar{D} \rangle &= \langle \rho^+ (D\bar{D})^{I=0} | (\hat{t}_{\rho D} + \hat{t}_{\rho \bar{D}}) | \rho^+ (D\bar{D})^{I=0} \rangle \quad \text{with nomenclature } |D\bar{D}, I, I_z\rangle \otimes |\rho, I, I_z\rangle \\ &= -\langle 1, +1 | \otimes \frac{1}{\sqrt{2}} \left(\left\langle \frac{1}{2}, \frac{1}{2} \right| \left\langle \frac{1}{2}, -\frac{1}{2} \right| - \left\langle \frac{1}{2}, -\frac{1}{2} \right| \left\langle \frac{1}{2}, \frac{1}{2} \right| \right) (\hat{t}_{\rho D} + \hat{t}_{\rho \bar{D}}) \\ &\quad \times \frac{1}{\sqrt{2}} \left(\left| \frac{1}{2}, \frac{1}{2} \right\rangle \left| \frac{1}{2}, -\frac{1}{2} \right\rangle - \left| \frac{1}{2}, -\frac{1}{2} \right\rangle \left| \frac{1}{2}, \frac{1}{2} \right\rangle \right) \otimes (-) |1, +1\rangle \\ &= \left(\frac{2}{3} t_{\rho D}^{I=3/2} + \frac{1}{3} t_{\rho D}^{I=1/2} \right) + \left(\frac{2}{3} t_{\rho \bar{D}}^{I=3/2} + \frac{1}{3} t_{\rho \bar{D}}^{I=1/2} \right) \end{aligned}$$

the $\bar{D}(\rho D)_{D_1(2420)}$ system

$$I_{\rho D} = \frac{1}{2}$$

$$I_{\bar{D}(\rho D)} = 1$$

$$I_{\bar{D}(\rho D)} = 0$$

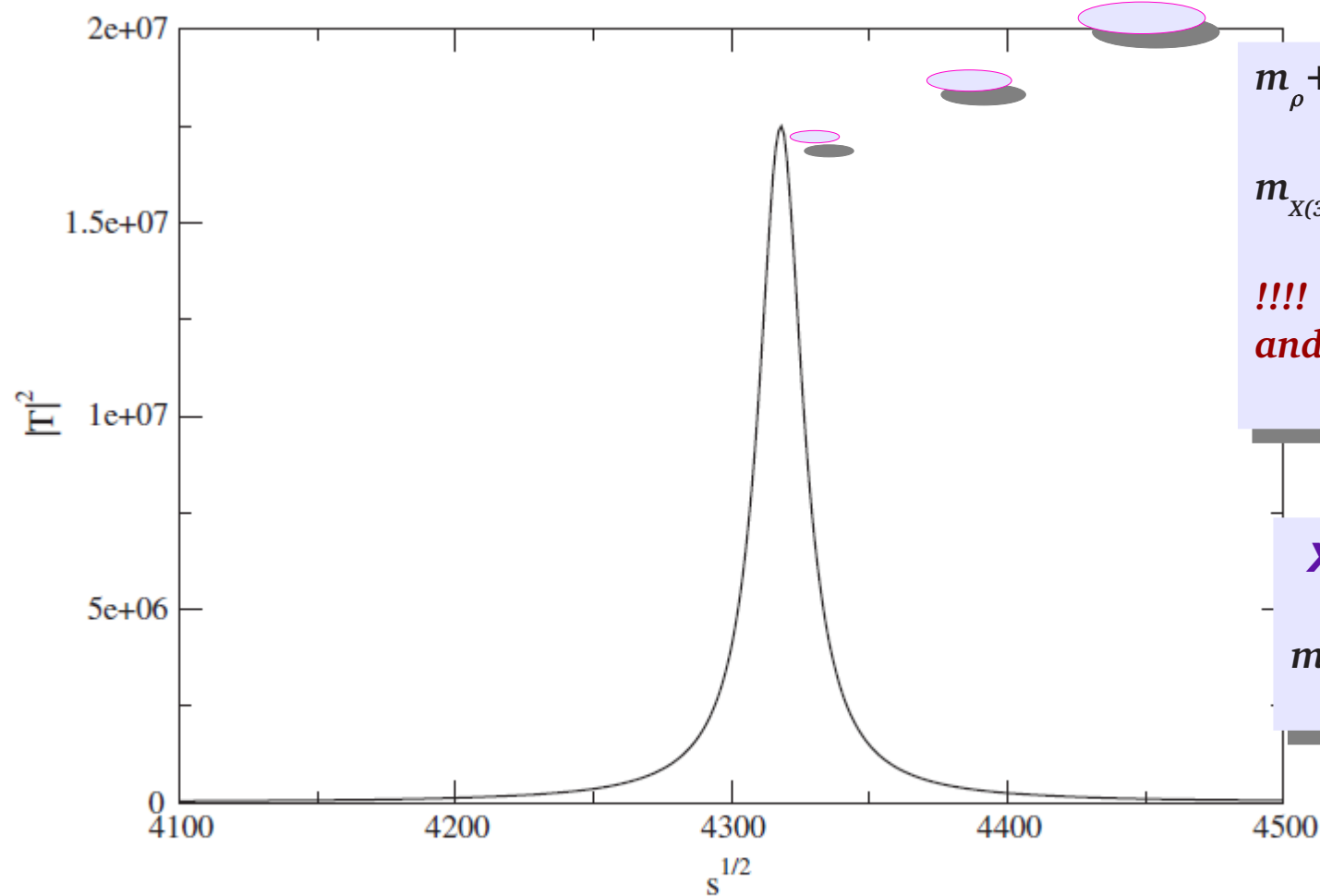
$$t = (t_{D\rho}^{I=1/2}) + (t_{D\bar{D}}^{I=1})$$

$$\begin{aligned} \langle \rho D\bar{D} | t | \rho D\bar{D} \rangle &= \langle \bar{D}(\rho D)^{I=1/2} | (\hat{t}_{D\rho} + \hat{t}_{D\bar{D}}) | \bar{D}(\rho D)^{I=1/2} \rangle \\ &= \frac{1}{\sqrt{2}} \left\langle \frac{1}{2} \right| \otimes \left(\frac{1}{\sqrt{3}} \left\langle 0, -\frac{1}{2} \right| - \sqrt{\frac{2}{3}} \left\langle -1, \frac{1}{2} \right| \right) + \frac{1}{\sqrt{2}} \left\langle -\frac{1}{2} \right| \otimes \left(\sqrt{\frac{2}{3}} \left\langle 1, -\frac{1}{2} \right| - \frac{1}{\sqrt{3}} \left\langle 0, +\frac{1}{2} \right| \right) (\hat{t}_{D\rho} + \hat{t}_{D\bar{D}}) \\ &\quad \times \frac{1}{\sqrt{2}} \left| \frac{1}{2} \right\rangle \otimes \left(\frac{1}{\sqrt{3}} \left| 0, -\frac{1}{2} \right\rangle - \sqrt{\frac{2}{3}} \left| -1, \frac{1}{2} \right\rangle \right) + \frac{1}{\sqrt{2}} \left| -\frac{1}{2} \right\rangle \otimes \left(\sqrt{\frac{2}{3}} \left| 1, -\frac{1}{2} \right\rangle - \frac{1}{\sqrt{3}} \left| 0, +\frac{1}{2} \right\rangle \right) \\ &= \left(\frac{8}{9} t_{D\rho}^{I=3/2} + \frac{1}{9} t_{D\rho}^{I=1/2} \right) + \left(\frac{2}{3} t_{D\bar{D}}^{I=1} + \frac{1}{3} t_{D\bar{D}}^{I=0} \right) \quad \text{with the nomenclature } |\rho\bar{D}, I_{z_1}, I_{z_2}\rangle \otimes |D, I_z\rangle \end{aligned}$$

RESULTS AND DISCUSSION

B. Durkaya and M. Bayar, Phys. Rev. D 92, 036006 (2015)

$m \sim 4320 \text{ MeV}, \Gamma \sim 25 \text{ MeV}$



$$m_{\rho} + m_D + m_{\bar{D}} = 4535 \text{ MeV}$$

$$m_{X(3700)} + m_{\rho} \sim 4475 \text{ MeV}$$

!!!! $\sim 160 \text{ MeV}$ below the $X(3700)$ and ρ meson threshold

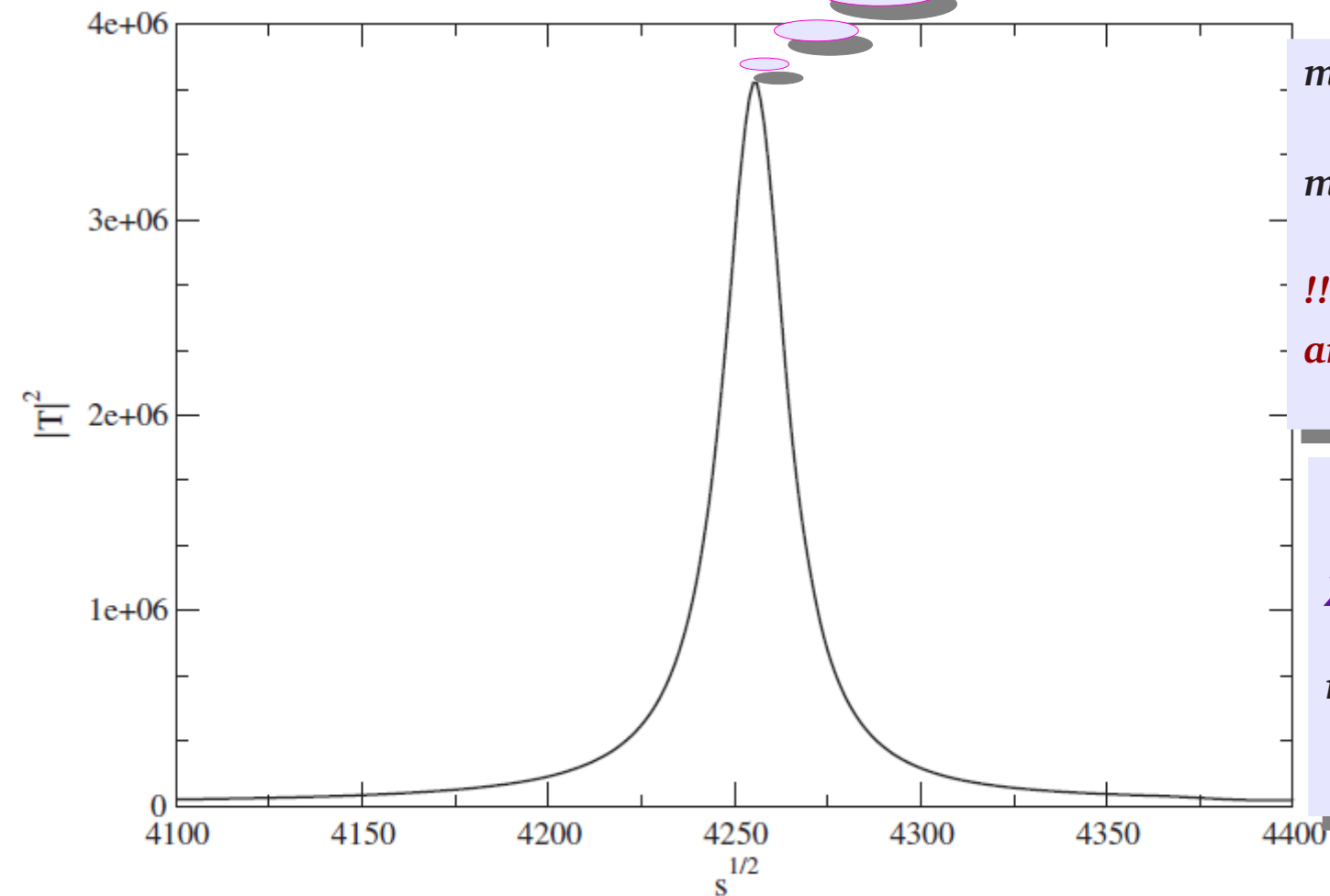
$X(4360) \quad I^G(J^{PC}) = ?^?(1^-)$

$m \sim 4361 \text{ MeV}, \Gamma \sim 74 \text{ MeV}$

FIG. 2. Modulus squared of the $\rho(D\bar{D})_{X(3700)}$ scattering amplitude with total isospin $I = 1$.

$\bar{D}D_1(2420)$ system

$m \sim 4256 \text{ MeV}, \Gamma \sim 25\text{-}30 \text{ MeV}$



$$m_\rho + m_D + m_D = 4535 \text{ MeV}$$

$$m_{D_1(2420)} + m_D \sim 4290 \text{ MeV}$$

!!!! $\sim 40 \text{ MeV}$ below the $D_1(2420)$ and D meson threshold

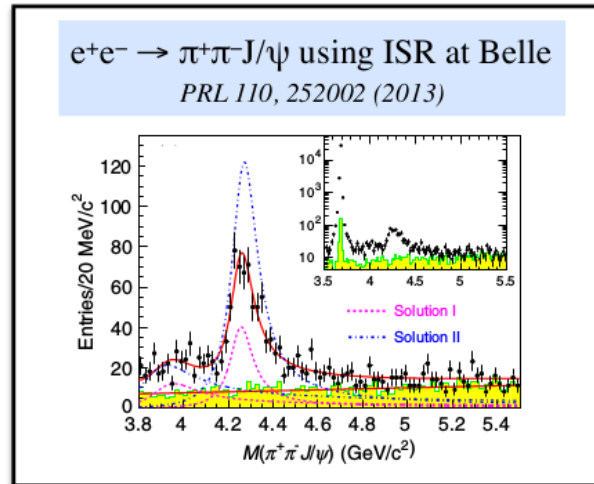
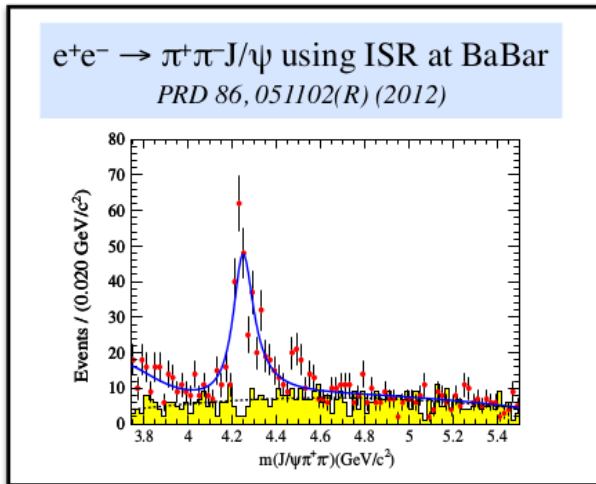
$X(4260) \quad I^G(J^{PC}) = ??(1^-)$

$m \sim 4251 \text{ MeV}, \Gamma \sim 44 \text{ MeV}$

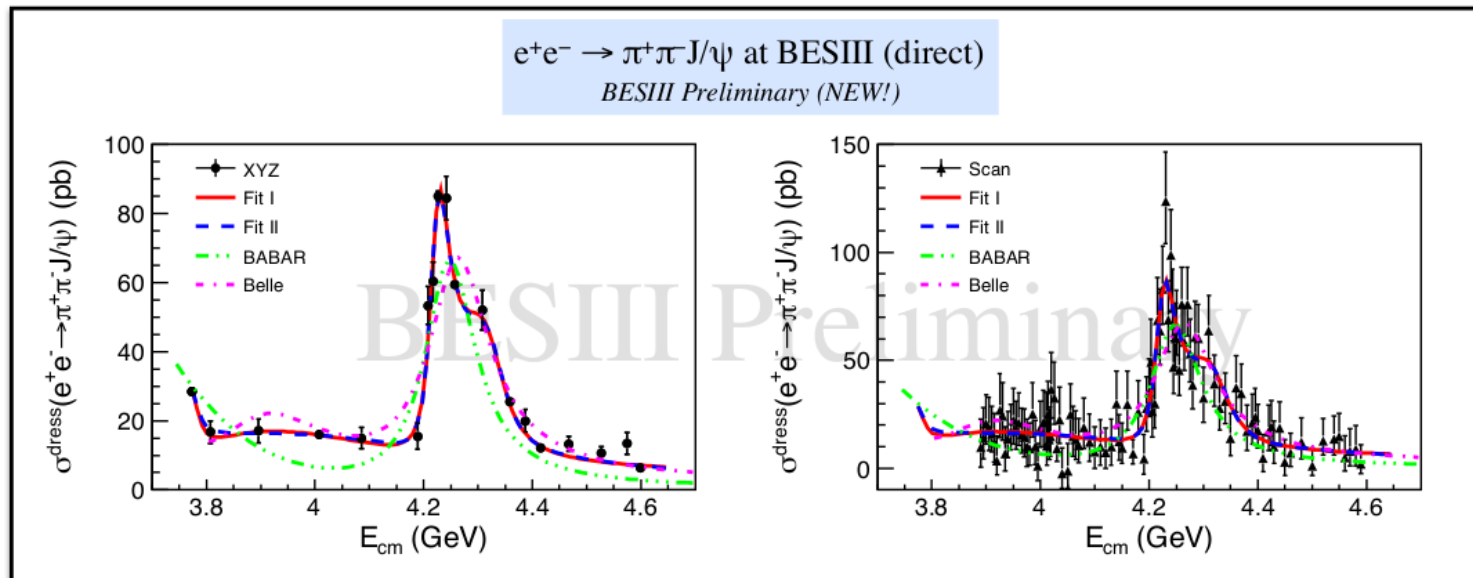
BESIII, Phys.Rev.Lett. 118 (2017) no.9, 092001

FIG. 3. Modulus squared of the $\bar{D}(\rho D)_{D_1(2420)}$ scattering amplitude with total isospin $I = 1$.

(4) $e^+e^- \rightarrow \pi^+\pi^-J/\psi, \pi^+\pi^-\psi(2S), \pi^+\pi^-h_c$ and the “Y” States



\Rightarrow asymmetric shape?
a low-mass peak (“Y(4008)”)?



Conclusion 1: The cross section is inconsistent with a single peak for the Y(4260)!
Two peaks are favored over one peak by $> 7\sigma$.

Conclusion 2: The Y(4008) is not needed to describe the BESIII data.
Fit I with a wide low-mass Breit-Wigner is equivalent to Fit II with an interfering non-resonant exponential shape.

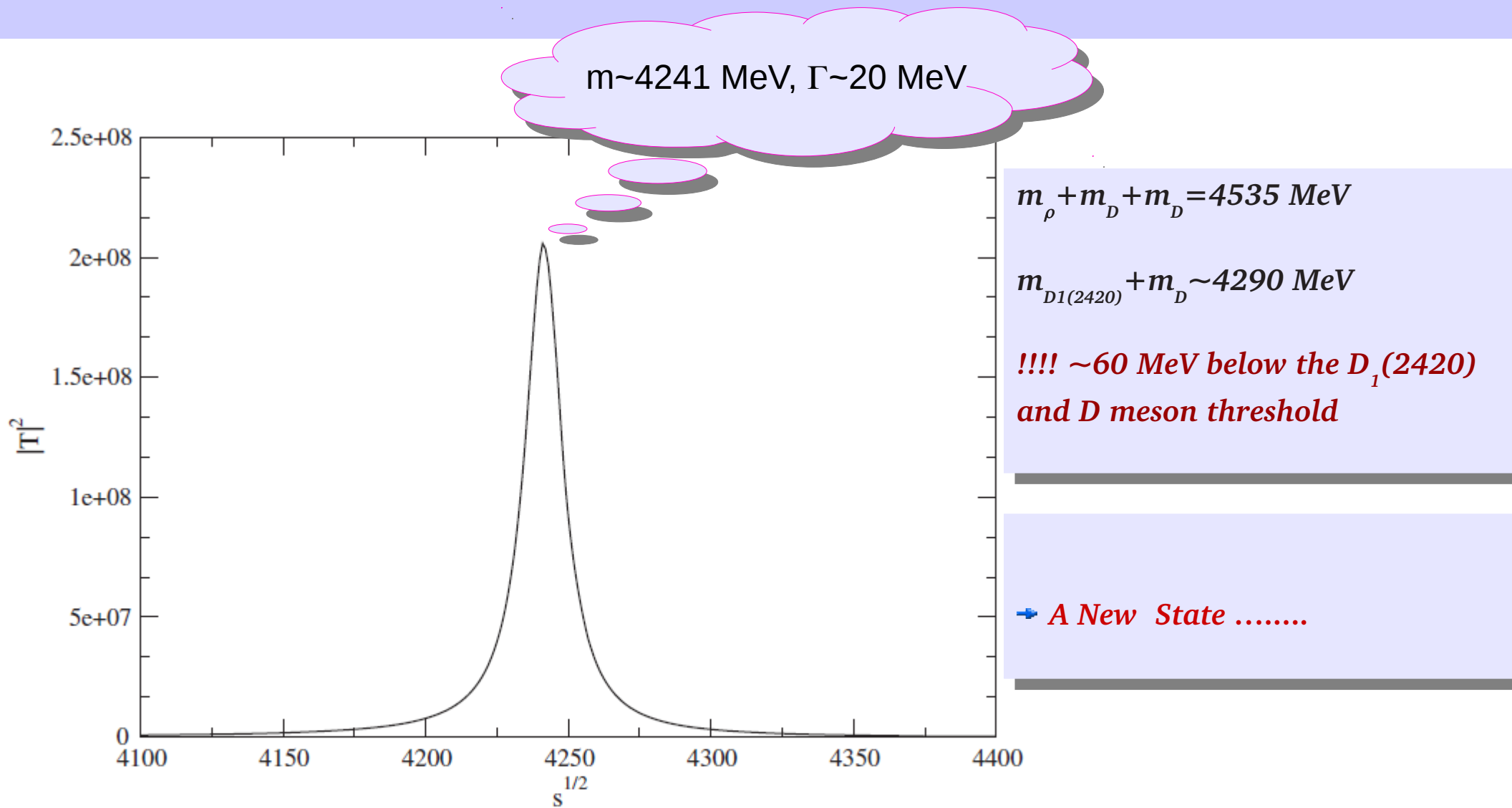


FIG. 4. Modulus squared of the $\bar{D}(\rho D)_{D_1(2420)}$ scattering amplitude with total isospin $I = 0$.

SUMMARY

- ★ *We investigate the three-body systems of ρDD by taking the fixed center approximation to Faddeev equations, and find*
 - *A bound states around 4320 MeV and 4256 MeV associated to $X(4360)$ and $X(4260)$ with $I=1$*
 - *Predict a new state: mass about 4241 MeV with $I=0$*

Thank you for your attention!