Testable Leptogenesis & CP violation

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Motivation

• The LHC results indicate that the Higgs mechanism is the responsible for the mass generation of the SM particles.

 The origin of light neutrino masses, which existence is supported by neutrino oscillation experiments, still remains unknown.

Minimal Model: Seesaw Model



Heavy fermion singlet: ν_R . Type I seesaw. Minkowski 77; Gell-Mann, Ramond, Slansky 79; Yanagida 79; Mohapatra, Senjanovic 80.

We will focus on the simplest extension of SM able to account for neutrino masses:

$$\mathcal{L} = \mathcal{L}_{SM} + \mathcal{L}_{K} - \frac{1}{2}\overline{N_{i}}M_{ij}N_{j} - Y_{i\alpha}\overline{N_{i}}\widetilde{\phi}^{\dagger}L_{\alpha} + h.c.$$

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$$\begin{split} \mathcal{L} &= \mathcal{L}_{\mathcal{S}\mathcal{M}} + \mathcal{L}_{\mathcal{K}} - \frac{1}{2} \overline{N_i} \overline{M_{ij}} N_j - Y_{i\alpha} \overline{N_i} \widetilde{\phi}^{\dagger} L_{\alpha} + h.c. \\ & \text{New Physics Scale} \quad \left(m_{\nu} \sim Y^2 v^2 / M \right) \end{split}$$



The New Physics Scale



• Type-I seesaw with N_R=3 & $m_{lightest} \lesssim 10^{-3} eV \begin{cases} M_2, M_3>100 \text{ MeV} \\ M_1 \text{ unbounded} \end{cases}$

P. Hernandez, M. Kekic, JLP 1311.2614;1406.2961

The New Physics Scale



- Resonant Leptogenesis M>100GeV Pilaftsis
- Leptogenesis via Oscillations M=0.1-100GeV Akhmedov, Rubakov, Smirnov (ARS); Asaka, Shaposnikov (AS)

GeV Scale Leptogenesis

Hernandez, Kekic, JLP, Racker, Rius 1508.03676; Hernandez, Kekic, JLP, Racker, Salvado 1606.06719

Asaka, Shaposhnikov;Shaposhnikov; Asaka, Eijima, Ishida; Canetti, Drewes, Frossard, Shaposhnikov;Drewes, Garbrecht; Shuve, Yavin; Abada, Arcadi, Domcke, Lucente...

Kinematic Equations

We have solved the equations for the density matrix in the Raffelt-Sigl formalism

$$\frac{d\rho_N(k)}{dt} = -i[H, \rho_N(k)] - \frac{1}{2} \{\Gamma_N^a, \rho_N\} + \frac{1}{2} \{\Gamma_N^p, 1 - \rho_N\}$$

- Fermi-Dirac or Bose-Einstein statistics is kept throughout
- Collision terms include 2 ↔ 2 scatterings at tree level with top quarks and gauge bosons, as well as 1 ↔ 2 scatterings, including the resummation of scatterings mediated by soft gauge bosons
- Leptonic chemical potentials are kept in all collision terms to linear order
- Include spectator processes

Kinematic Equations

We have solved the equations for the density matrix in the Raffelt-Sigl formalism using the code SQuIDS

Arguelles Delgado, Salvado, Weaver 2015 https://github.com/jsalvado/SQuIDS

$$\begin{split} xH_{u}\frac{dr_{+}}{dx} &= -i[\langle H_{\mathrm{re}}\rangle, r_{+}] + [\langle H_{\mathrm{im}}\rangle, r_{-}] - \frac{\langle \gamma_{N}^{(0)}\rangle}{2} \{\mathrm{Re}[Y^{\dagger}Y], r_{+} - 1\} \\ &\quad + i\langle \gamma_{N}^{(1)}\rangle\mathrm{Im}[Y^{\dagger}\mu Y] - i\frac{\langle \gamma_{N}^{(2)}\rangle}{2} \{\mathrm{Im}[Y^{\dagger}\mu Y], r_{+}\} - i\frac{\langle \gamma_{N}^{(0)}\rangle}{2} \{\mathrm{Im}[Y^{\dagger}Y], r_{-}\}, \\ xH_{u}\frac{dr_{-}}{dx} &= -i[\langle H_{\mathrm{re}}\rangle, r_{-}] + [\langle H_{\mathrm{im}}\rangle, r_{+}] - \frac{\langle \gamma_{N}^{(0)}\rangle}{2} \{\mathrm{Re}[Y^{\dagger}Y], r_{-}\} \\ &\quad + \langle \gamma_{N}^{(1)}\rangle\mathrm{Re}[Y^{\dagger}\mu Y] - \frac{\langle \gamma_{N}^{(2)}\rangle}{2} \{\mathrm{Re}[Y^{\dagger}\mu Y], r_{+}\} - i\frac{\langle \gamma_{N}^{(0)}\rangle}{2} \{\mathrm{Im}[Y^{\dagger}Y], r_{+} - 1\}, \\ \frac{d\mu_{B/3-L_{\alpha}}}{dx} &= \frac{\int_{k}\rho_{F}}{\int_{k}\rho_{F}'} \{\langle \gamma_{N}^{(0)}\rangle\mathrm{Tr}[r_{-}\mathrm{Re}(Y^{\dagger}I_{\alpha}Y) + ir_{+}\mathrm{Im}(Y^{\dagger}I_{\alpha}Y)] \\ &\quad + \mu_{\alpha}\left(\langle \gamma_{N}^{(2)}\rangle\mathrm{Tr}[r_{+}\mathrm{Re}(Y^{\dagger}I_{\alpha}Y)] - \langle \gamma_{N}^{(1)}\rangle\mathrm{Tr}[YY^{\dagger}I_{\alpha}]\right)\}, \\ \mu_{\alpha} &= -\sum_{\beta}C_{\alpha\beta}\mu_{B/3-L_{\beta}}, \end{split}$$

Full parameter space exploration Nr=2 $Y_B^{\rm exp}\simeq 8.65(8)\times 10^{-11}$

Bayesian posterior probabilities (using nested sampling Montecarlo MultiNest)

$$\log \mathcal{L} = -\frac{1}{2} \left(\frac{Y_B(t_{\rm EW}) - Y_B^{\rm exp}}{\sigma_{Y_B}} \right)^2.$$
Casas-Ibarra
$$\frac{R(\theta + i\gamma)}{R(\theta + i\gamma)}$$
Parameters of the
model
$$\theta_{23}, \theta_{12}, \theta_{13}, m_2, m_3, M_1, M_2, \delta, \phi_1, \theta, \gamma$$
Fixed by neutrino
oscillation experiments
Free
parameters



Leptogenesis in Minimal Model Nr=2

Non degenerated solutions



Inverted light neutrino ordering (IH)

Hernandez, Kekic, JLP, Racker, Salvado 2016 arXiv:1606.06719

Leptogenesis in Minimal Model Nr=2

Non very degenerate solutions



Inverted light neutrino ordering (IH)

Hernandez, Kekic, JLP, Racker, Salvadò 2016 arXiv:1606.06719

Leptogenesis in Minimal Model Nr=2

SHIP



Inverted light neutrino ordering

Hernandez, Kekic, JLP, Racker, Salvadò 2016 arXiv:1606.06719 What if the sterile ν are within reach of ShiP?

Can we estimate YB from the experiments?

• Baryon asymmetry for IH and in the weak wash out regime:

$$[Y_B]_{IH} \propto e^{4\gamma} \frac{(\Delta m_{atm}^2)^{3/2}}{4v^6} M_1 M_2 (M_1 + M_2) \left[(\sin 2\theta \cos 2\theta_{12} - \cos \phi_1 \cos 2\theta \sin 2\theta_{12}) \left(\sin^2 2\theta_{23} + (4 + \cos 4\theta_{23}) \sin \phi_1 \sin 2\theta_{12} \right) + \mathcal{O}(\epsilon) \right]$$

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• Baryon asymmetry depends on all the unknown parameters (also on δ at $\mathcal{O}\left(\epsilon\right)$)

• **SHIP** can measure (if sterile states not too degenerate)

 $M_1, M_2, |U_{e4}|, |U_{e5}|, |U_{\mu4}|, |U_{\mu5}|$

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$$\begin{split} M_1, M_2, |U_{e4}|, |U_{e5}|, |U_{\mu4}|, |U_{\mu5}| \\ & \text{SHIP sensitive to} \\ \bullet |U_{e4}|^2 / |U_{\mu4}|^2 \simeq |U_{e5}|^2 / |U_{\mu5}|^2 \simeq & \delta, \phi_1 \\ & (1 + s_{\phi_1} \sin 2\theta_{12})(1 - \theta_{13}^2) + \frac{1}{2}r^2 s_{12}(c_{12}s_{\phi_1} + s_{12}) \\ \hline (1 - \sin 2\theta_{12}s_{\phi_1} \left(1 + \frac{r^2}{4}\right) + \frac{r^2 c_{12}^2}{2} c_{23}^2 + \theta_{13}(c_{\phi_1}s_{\delta} - \cos 2\theta_{12}s_{\phi_1}c_{\delta}) \sin 2\theta_{23} + \theta_{13}^2(1 + \sin 2\theta_{12})s_{23}^2 s_{\phi_1} \end{split}$$

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• $|U_{e4}|^2, |U_{\mu4}|^2, |U_{e5}|^2, |U_{\mu5}|^2 \propto e^{2\gamma}$

•SHIP sensitive to $M_1,\ M_2,\ \phi_1,\ \delta,\ \gamma$



• Great but...

...how about θ which is essential to predict Y_B ?

• Neutrinoless double beta decay effective mass in the IH case

 $|m_{\beta\beta}|_{IH} \simeq$

$$\simeq \sqrt{\Delta m_{atm}^2} \left| c_{13}^2 \left(c_{12}^2 + e^{2i\phi_1} s_{12}^2 \left(1 + \frac{r^2}{2} \right) \right) - f(A) e^{2i\theta} e^{2\gamma} (c_{12} - ie^{i\phi_1} s_{12})^2 (1 - 2e^{i\delta} s_{23} \theta_{13}) \frac{(0.9 \,\text{GeV})^2}{4M_1^2} \left(1 - \left(\frac{M_1}{M_1 + \Delta M_{12}} \right)^2 \right) \right|$$

• Neutrinoless double beta decay effective mass in the IH case

$$\begin{split} |m_{\beta\beta}|_{IH} \simeq & \underset{\text{contribution}}{\text{LIGHT NEUTRINO}} \\ \simeq & \sqrt{\Delta m_{atm}^2} \left[c_{13}^2 \left(c_{12}^2 + e^{2i\phi_1} s_{12}^2 \left(1 + \frac{r^2}{2} \right) \right) \right] \\ - & f(A) e^{2i\theta} e^{2\gamma} (c_{12} - ie^{i\phi_1} s_{12})^2 (1 - 2e^{i\delta} s_{23} \theta_{13}) \frac{(0.9 \,\text{GeV})^2}{4M_1^2} \left(1 - \left(\frac{M_1}{M_1 + \Delta M_{12}} \right)^2 \right) \end{split}$$

• Neutrinoless double beta decay effective mass in the IH case



- Heavy neutrino contribution can be sizable for $M \sim O\left(GeV\right)$ Mitra, Senjanovic, Vissani 2011 JLP, Pascoli, Wong 2012

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Hernandez, Kekic, JLP, Racker, Salvadò 2016 arXiv:1606.06719



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CP-violation in Minimal Model Measurment of PMNS phases from FCC and ShiP?

Caputo, Hernandez, Kekic, JLP, Salvado arXiv:1611.05000

CP-violation in minimal model

• SHIP and FCC can measure:

$$\begin{split} M_1, M_2, |U_{e4}|, |U_{e5}|, |U_{\mu4}|, |U_{\mu5}| & \text{Sensitivity to} \\ & \mathsf{PMNS CP-phases!} \\ \bullet |U_{e4}|^2 / |U_{\mu4}|^2 \simeq |U_{e5}|^2 / |U_{\mu5}|^2 \simeq & \delta, \phi_1 \\ & (1 + s_{\phi_1} \sin 2\theta_{12})(1 - \theta_{13}^2) + \frac{1}{2}r^2 s_{12}(c_{12}s_{\phi_1} + s_{12}) \\ \hline (1 - \sin 2\theta_{12}s_{\phi_1} \left(1 + \frac{r^2}{4}\right) + \frac{r^2 c_{12}^2}{2} \right) c_{23}^2 + \theta_{13}(c_{\phi_1}s_{\delta} - \cos 2\theta_{12}s_{\phi_1}c_{\delta}) \sin 2\theta_{23} + \theta_{13}^2(1 + \sin 2\theta_{12})s_{23}^2 s_{\phi_1} \end{split}$$

• $|U_{e4}|^2, |U_{\mu4}|^2, |U_{e5}|^2, |U_{\mu5}|^2 \propto e^{2\gamma}$



 5σ discovery CP-violation



 5σ discovery CP-violation



Summary and Conclusions

- Successful baryogenesis is possible with a mild heavy neutrino degeneracy in the minimal model (N=2)
- These less fine-tuned solutions prefer smaller masses M ≤ 1GeV (target region of SHiP) and significant non-standard contributions to neutrinoless double beta decay.
- SHiP, neutrinoless double beta decay and searches for leptonic CP violation in neutrino oscillations are complementary searches regarding the baryon asymmetry prediction.
- If O(GeV) heavy neutrinos would be discovered in SHiP and the neutrino ordering is inverted, predicting the baryon asymmetry looks in principle viable, in contrast with previous beliefs.
- 5σ measurement of leptonic CP violation from ShiP and FCC would be possible in a very significant fraction of parameter space!! (regardless the baryon asymmetry generation).



1FA



In order to quantify the discovery CP potential we consider that SHiP or FCC-ee will measure the number of electron and muon events in the decay of one of the heavy neutrino states (without loss of generality we assume to be that with mass M_1), estimated as explained in the previous section. We will only consider statistical errors.

The test statistics (TS) for leptonic CP violation is then defined as follows:

$$\Delta \chi^{2} \equiv -2 \sum_{\alpha = \text{channel}} N_{\alpha}^{\text{true}} - N_{\alpha}^{CP} + N_{\alpha}^{\text{true}} \log\left(\frac{N_{\alpha}^{CP}}{N_{\alpha}^{\text{true}}}\right) + \left(\frac{M_{1} - M_{1}^{\text{min}}}{\Delta M_{1}}\right)^{2}.$$
(10)

where $N_{\alpha}^{\text{true}} = N_{\alpha}(\delta, \phi_1, M_1, \gamma, \theta)$ is the number of events for the true model parameters, and $N_{\alpha}^{CP} = N_{\alpha}(CP, \gamma^{\min}, \theta^{\min}, M_1^{\min})$ is the number of events for the CP-conserving test hypothesis that minimizes $\Delta \chi^2$ among the four CP conserving phase choices $CP = (0/\pi, 0/\pi)$ and over the unknown test parameters. ΔM_1 is the uncertainty in the mass, which is assumed to be 1%.



Fig. 4 Distribution of the test statistics for $\mathcal{O}(10^7)$ number of experimental measurements of the number of events for true values of the phases $(\delta, \phi_1) = (0,0)$ for IH and $(\gamma, \theta, M_1) = (3.5,0,1)$ GeV, compared to the χ^2 distribution for 1 or 2 degrees-of-freedom.

SHIP sensitive to PMNS CP phases



Recall, neutrino oscillation experiments sensitive to $\,\delta$

Light New Physics scale

• Contrary to the high scale models, a low Majorana scale does not worsen the Higgs mass hierarchy problem.



 $[\delta M_H^2]_{N_R} \propto M^2$ Vissani 1998

• Drawback: small Yukawa couplings required.

• The lepton assymetry should be proportional to a combination of the following 4 independent CP-invariants

$$I_{1}^{(2)} = -\operatorname{Im}[W_{12}^{*}V_{11}V_{21}^{*}W_{22}]$$

$$I_{1}^{(3)} = \operatorname{Im}[W_{12}^{*}V_{13}V_{23}^{*}W_{22}]$$

$$I_{2}^{(3)} = \operatorname{Im}[W_{13}^{*}V_{12}V_{22}^{*}W_{23}]$$

$$J_{W} = -\operatorname{Im}[W_{23}^{*}W_{22}W_{32}^{*}W_{33}]$$

$$CP \text{ phases from V & W} (U_{PMNS & R})$$

$$CP \text{ phases from W} (only R)$$

$$Y = V^{\dagger} \text{Diag} \{y_1, y_2, y_3\} W$$

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$$N_{R} \ge 2$$

$$I_{2}^{(3)} = \operatorname{Im}[W_{13}^{*}V_{12}V_{22}^{*}W_{23}]$$

$$J_{W} = -\operatorname{Im}[W_{23}^{*}W_{22}W_{32}^{*}W_{33}]$$

$$N_{R} \ge 3$$

 $Y = V^{\dagger} \text{Diag} \{y_1, y_2, y_3\} W$

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$$ARS$$

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Hernandez, Kekic, JLP, Racker, Salvadò 2016 arXiv:1606.06719



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$$I_{1}^{(2)} = -\text{Im}[W_{12}^{*}V_{11}V_{21}^{*}W_{22}] \simeq \theta_{12}\bar{\theta}_{12}\sin\psi_{1}$$

$$I_{1}^{(3)} = \text{Im}[W_{12}^{*}V_{13}V_{23}^{*}W_{22}] \simeq \theta_{12}\bar{\theta}_{13}\bar{\theta}_{23}\sin(\bar{\delta}+\psi_{1})$$

$$I_{2}^{(3)} = \text{Im}[W_{13}^{*}V_{12}V_{22}^{*}W_{23}]] \simeq \bar{\theta}_{12}\theta_{13}\theta_{23}\sin(\delta-\psi_{1})$$

$$J_{W} = -\text{Im}[W_{23}^{*}W_{22}W_{32}^{*}W_{33}] \simeq \theta_{12}\theta_{13}\theta_{23}\sin\delta$$

$$Y = V^{\dagger}\text{Diag}\{y_{1}, y_{2}, y_{3}\}W$$

$$Y_B \simeq 1.3 \times 10^{-3} \sum_{\alpha} \mu_{B/3-L_{\alpha}}$$

Heavy New Physics scale

$$m_{\nu} = \frac{v^2}{2} Y M^{-1} Y^T \lesssim \mathcal{O} \left(1 \,\mathrm{eV} \right)$$

• $Y \sim 1$ suggests M close to the GUT scale.

• Drawback: New Physics effects at low energies very suppressed by the NP scale M.