

# Lepton Flavor Violation at high and low energies



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# 1. Introduction: leptonic FCNC

## ★ Why study flavor-changing neutral currents (FCNC)?

- ★ No trivial FCNC vertices in the Standard Model: sensitive NP tests
- ★ Possible experimental studies in a lepton sector

### - lepton-flavor violating processes

- $\mu \rightarrow e\gamma, \tau \rightarrow e\gamma, \text{etc.}$
- $\mu \rightarrow eee, \tau \rightarrow \mu ee, \text{etc.}$
- $\mu^+e^- \rightarrow e^-\mu^+$
- $Z^0 \rightarrow \mu e, \tau e, \text{etc.}$
- $H \rightarrow \mu e, \tau e, \text{etc.}$
- $K^0 (B^0, D^0, \dots) \rightarrow \mu e, \tau e, \text{etc.}$
- $K^+ (B^+, D^+, \dots) \rightarrow \pi^+\mu e, \pi^+\tau e, \text{etc.}$
- $\mu^- + (A, Z) \rightarrow e^- + (A, Z)$

Channel	Babar		BELLE	
	$\mathcal{L}$ ( $\text{fb}^{-1}$ )	$B_{\text{UL}}$ ( $10^{-8}$ )	$\mathcal{L}$ ( $\text{fb}^{-1}$ )	$B_{\text{UL}}$ ( $10^{-8}$ )
$\tau^\pm \rightarrow e^\pm \gamma$	232	11	535	12
$\tau^\pm \rightarrow \mu^\pm \gamma$	232	6.8	535	4.5
$\tau^\pm \rightarrow \ell^\pm \ell^\mp \ell^\pm$	92	11 - 33	535	2 - 4
$\tau^\pm \rightarrow e^\pm \pi^0$	339	13	401	8.0
$\tau^\pm \rightarrow \mu^\pm \pi^0$	339	11	401	12
$\tau^\pm \rightarrow e^\pm \eta$	339	16	401	9.2
$\tau^\pm \rightarrow \mu^\pm \eta$	339	15	401	6.5
$\tau^\pm \rightarrow e^\pm \eta'$	339	24	401	16
$\tau^\pm \rightarrow \mu^\pm \eta'$	339	14	401	13

### - lepton number and lepton-flavor violating processes

- $(A, Z) \rightarrow (A, Z_{\pm 2}) + e^\mp e^\mp$
- $\mu^- + (A, Z) \rightarrow e^+ + (A, Z-2)$

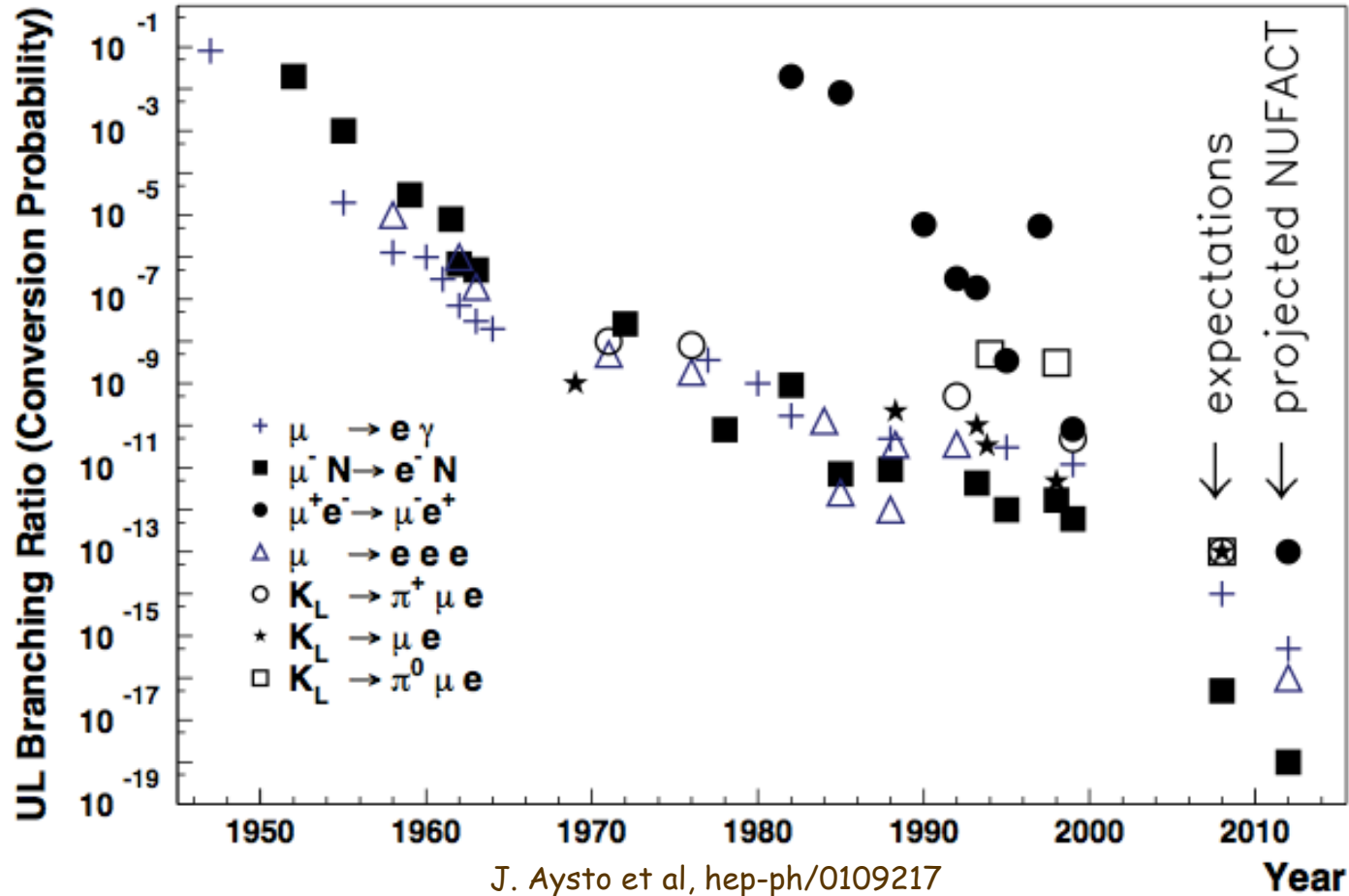
$$\text{BR}(K_L^0 \rightarrow \mu e) < 4.7 \times 10^{-12}$$

$$\text{BR}(B_d^0 \rightarrow \mu e) < 1.7 \times 10^{-7} \quad [\text{Belle}]$$

$$\text{BR}(B_s^0 \rightarrow \mu e) < 6.1 \times 10^{-6} \quad [\text{CDF}]$$

★ Highly suppressed in the Standard Model, e.g.  $Br(\mu \rightarrow e\gamma) = \frac{3\alpha}{32\pi} \left| \sum_i U_{\mu i}^* U_{ei} \frac{m_{\nu_i}^2}{M_W^2} \right|^2 < 10^{-54}$

# Searches for Lepton Number Violation



- ★ Let us be more systematic: consider LFV in quark processes
  - only one FCNC: flavor conservation on the quark side
  - use EFT to classify operators

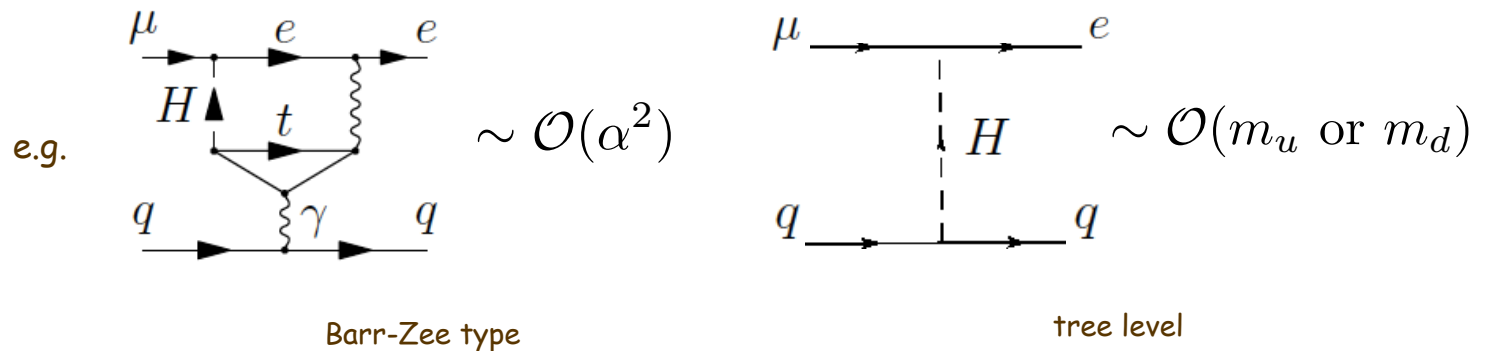
# High energy vs low energy

★ Leptonic FCNC could be generated by New Physics

★ E.g. FCNC Higgs decays  $H \rightarrow \mu e, \tau e, \text{etc.}$ :  $Y_{ij} = \frac{m_i}{v} \delta_{ij} + \frac{v^2}{\sqrt{2}\Lambda^2} \hat{\lambda}_{ij}$

Harnik, Kopp,  
Zupan

★ FCNC Higgs model & muon conversion/quarkonium decays



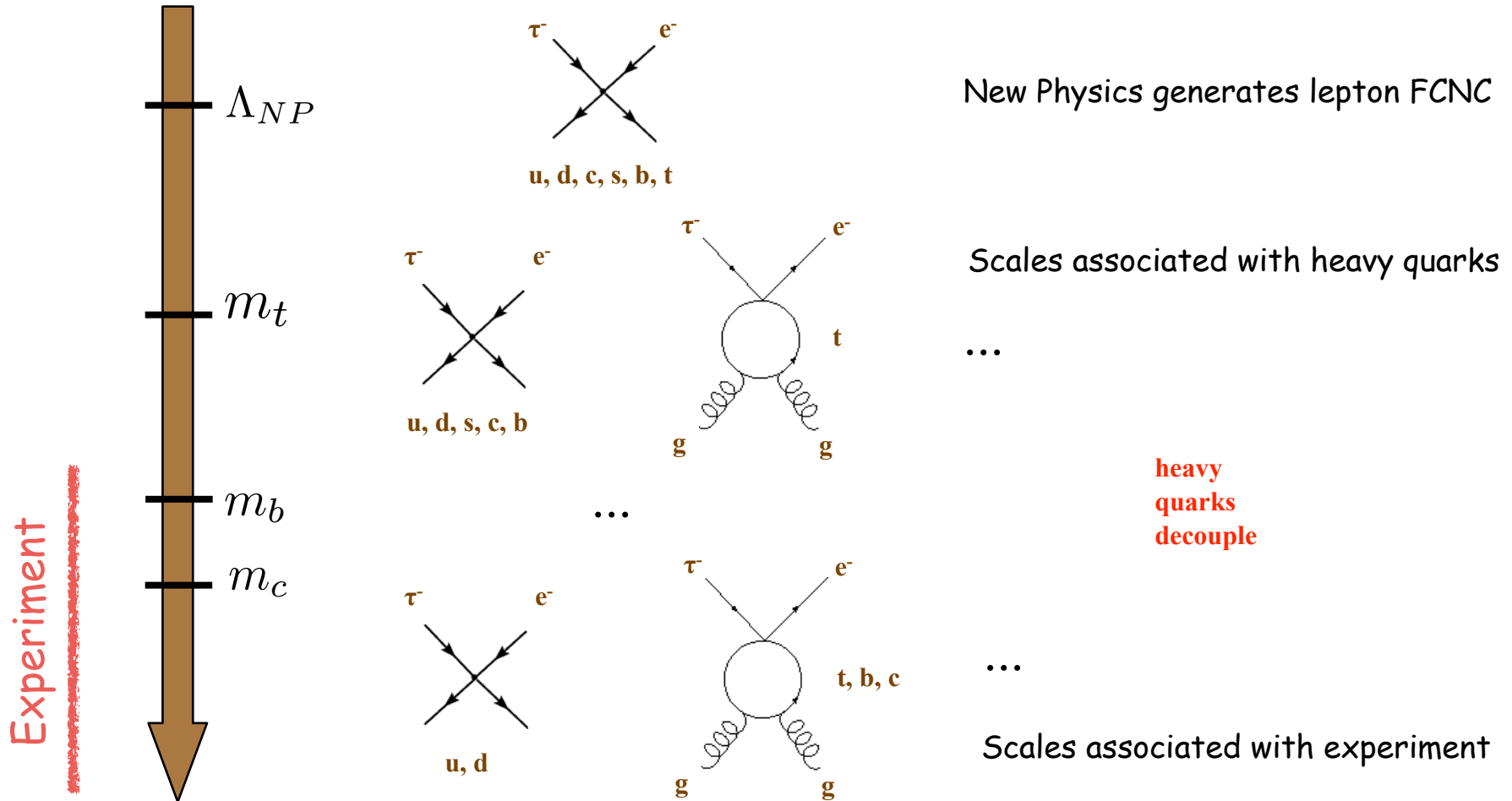
★ ... but note: couplings of new physics to light quarks are suppressed

Can we correlate low energy and high energy data?  
(will not discuss purely leptonic LFV interactions)

# 2. Effective Lagrangians for LFV transitions

★ Modern approach to flavor physics calculations: effective field theories

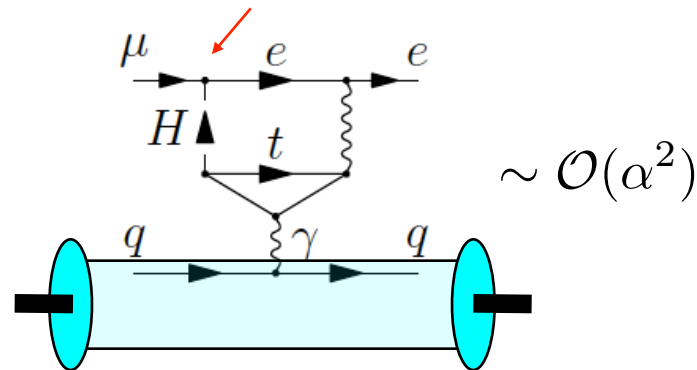
★ It is important to understand ALL relevant energy scales for the problem at hand



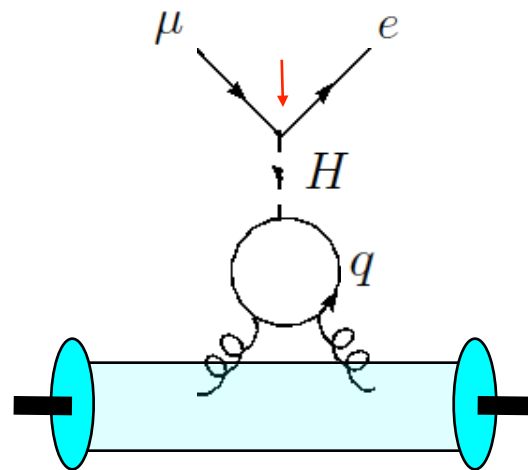
# All operators are important

★ Contribution of heavy quarks can, in principle, be large even at low energies

★ Two-loop sensitivity to NP in muon conversion experiment...



★ ... becomes one-loop!



- ➔ gluonic couplings to hadrons are not (always) suppressed!
- ➔ NP couplings to heavy quarks are not well constrained and could be large

# Effective Lagrangians

★ Naive power counting: largest contribution from lowest dimensional operators

★ Can write the most general LFV Lagrangian  $\mathcal{L}_{LFV} = \mathcal{L}_D + \mathcal{L}_{lq} + \mathcal{L}_G + \dots$

- dipole operators

$$\mathcal{L}_D = -\frac{m_2}{\Lambda^2} \left[ (C_{DR} \bar{l}_1 \sigma^{\mu\nu} P_L l_2 + C_{DR} \bar{l}_1 \sigma^{\mu\nu} P_R l_2) F_{\mu\nu} + h.c. \right]$$

- four-fermion operators

$$\begin{aligned} \mathcal{L}_{lq} = & -\frac{1}{\Lambda^2} \sum_q \left[ \left( C_{VR}^{q\ell_1\ell_2} \bar{l}_1 \gamma^\mu P_R l_2 + C_{VL}^{q\ell_1\ell_2} \bar{l}_1 \gamma^\mu P_L l_2 \right) \bar{q} \gamma_\mu q \right. \\ & + \left( C_{AR}^{q\ell_1\ell_2} \bar{l}_1 \gamma^\mu P_R l_2 + C_{AL}^{q\ell_1\ell_2} \bar{l}_1 \gamma^\mu P_L l_2 \right) \bar{q} \gamma_\mu \gamma_5 q \\ & + m_2 m_q G_F \left( C_{SR}^{q\ell_1\ell_2} \bar{l}_1 P_L l_2 + C_{SL}^{q\ell_1\ell_2} \bar{l}_1 P_R l_2 \right) \bar{q} q \\ & + m_2 m_q G_F \left( C_{PR}^{q\ell_1\ell_2} \bar{l}_1 P_L l_2 + C_{PL}^{q\ell_1\ell_2} \bar{l}_1 P_R l_2 \right) \bar{q} \gamma_5 q \\ & \left. + m_2 m_q G_F \left( C_{TR}^{q\ell_1\ell_2} \bar{l}_1 \sigma^{\mu\nu} P_L l_2 + C_{TL}^{q\ell_1\ell_2} \bar{l}_1 \sigma^{\mu\nu} P_R l_2 \right) \bar{q} \sigma_{\mu\nu} q + h.c. \right]. \end{aligned}$$

- gluonic operators

$$\begin{aligned} \mathcal{L}_G = & -\frac{m_2 G_F}{\Lambda^2} \frac{\beta_L}{4\alpha_s} \left[ \left( C_{GR} \bar{l}_1 P_R l_2 + C_{GL} \bar{l}_1 P_L l_2 \right) G_{\mu\nu}^a G^{a\mu\nu} \right. \\ & \left. + \left( C_{\bar{G}R} \bar{l}_1 P_R l_2 + C_{\bar{G}L} \bar{l}_1 P_L l_2 \right) G_{\mu\nu}^a \tilde{G}^{a\mu\nu} + h.c. \right] \end{aligned}$$

There are many effective operators, so a single operator dominance hypothesis (SODH) is usually applied to get constraints on relevant Wilson coefficients.

Is it necessary?

# Effective Lagrangians: designer states

★ By selecting appropriate quantum numbers of a decaying state we can probe all Wilson coefficients of LFV Lagrangian!

$$\begin{aligned}
 \mathcal{L}_{\ell q} = & -\frac{1}{\Lambda^2} \sum_q \left[ \left( C_{VR}^{q\ell_1\ell_2} \bar{\ell}_1 \gamma^\mu P_R \ell_2 + C_{VL}^{q\ell_1\ell_2} \bar{\ell}_1 \gamma^\mu P_L \ell_2 \right) \bar{q} \gamma_\mu q \right. \\
 & + \left( C_{AR}^{q\ell_1\ell_2} \bar{\ell}_1 \gamma^\mu P_R \ell_2 + C_{AL}^{q\ell_1\ell_2} \bar{\ell}_1 \gamma^\mu P_L \ell_2 \right) \bar{q} \gamma_\mu \gamma_5 q \\
 & + m_2 m_q G_F \left( C_{SR}^{q\ell_1\ell_2} \bar{\ell}_1 P_L \ell_2 + C_{SL}^{q\ell_1\ell_2} \bar{\ell}_1 P_R \ell_2 \right) \bar{q} q \\
 & + m_2 m_q G_F \left( C_{PR}^{q\ell_1\ell_2} \bar{\ell}_1 P_L \ell_2 + C_{PL}^{q\ell_1\ell_2} \bar{\ell}_1 P_R \ell_2 \right) \bar{q} \gamma_5 q \\
 & \left. + m_2 m_q G_F \left( C_{TR}^{q\ell_1\ell_2} \bar{\ell}_1 \sigma^{\mu\nu} P_L \ell_2 + C_{TL}^{q\ell_1\ell_2} \bar{\ell}_1 \sigma^{\mu\nu} P_R \ell_2 \right) \bar{q} \sigma_{\mu\nu} q + h.c. \right].
 \end{aligned}$$

- Can (partially) do away with SODH if designer initial/final states are used
- This can be done in case of restricted kinematics (e.g. 2-body decays)

# Effective Lagrangians: designer states

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 & + \left( C_{AR}^{q\ell_1\ell_2} \bar{\ell}_1 \gamma^\mu P_R \ell_2 + C_{AL}^{q\ell_1\ell_2} \bar{\ell}_1 \gamma^\mu P_L \ell_2 \right) \bar{q} \gamma_\mu \gamma_5 q \\
 & + m_2 m_q G_F \left( C_{SR}^{q\ell_1\ell_2} \bar{\ell}_1 P_L \ell_2 + C_{SL}^{q\ell_1\ell_2} \bar{\ell}_1 P_R \ell_2 \right) \bar{q} q \\
 & + m_2 m_q G_F \left( C_{PR}^{q\ell_1\ell_2} \bar{\ell}_1 P_L \ell_2 + C_{PL}^{q\ell_1\ell_2} \bar{\ell}_1 P_R \ell_2 \right) \bar{q} \gamma_5 q \\
 & \left. + \left( C_{TR}^{q\ell_1\ell_2} \bar{\ell}_1 \sigma^{\mu\nu} P_L \ell_2 + C_{TL}^{q\ell_1\ell_2} \bar{\ell}_1 \sigma^{\mu\nu} P_R \ell_2 \right) \bar{q} \sigma_{\mu\nu} q + h.c. \right].
 \end{aligned}$$

also dipole operators

**Vector** meson decays:  $\Upsilon(nS) \rightarrow \bar{\mu}\tau, \psi(nS) \rightarrow \bar{\mu}\tau, \rho \rightarrow \bar{\mu}e, \dots$

# Effective Lagrangians: designer states

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 & + m_2 m_q G_F \left( C_{PR}^{q\ell_1\ell_2} \bar{\ell}_1 P_L \ell_2 + C_{PL}^{q\ell_1\ell_2} \bar{\ell}_1 P_R \ell_2 \right) \bar{q} \gamma_5 q \\
 & \left. + m_2 m_q G_F \left( C_{TR}^{q\ell_1\ell_2} \bar{\ell}_1 \sigma^{\mu\nu} P_L \ell_2 + C_{TL}^{q\ell_1\ell_2} \bar{\ell}_1 \sigma^{\mu\nu} P_R \ell_2 \right) \bar{q} \sigma_{\mu\nu} q + h.c. \right].
 \end{aligned}$$

also gluonic operators

**Pseudoscalar** meson decays:  $\eta_b \rightarrow \bar{\mu}e, \eta_c \rightarrow \bar{\mu}\tau, \eta^{(\prime)} \rightarrow \bar{\mu}e, \dots$

# Effective Lagrangians: designer states

★ By selecting appropriate quantum numbers of a decaying state we can probe all Wilson coefficients of LFV Lagrangian!

$$\begin{aligned}
 \mathcal{L}_{\ell q} = & -\frac{1}{\Lambda^2} \sum_q \left[ \left( C_{VR}^{q\ell_1\ell_2} \bar{\ell}_1 \gamma^\mu P_R \ell_2 + C_{VL}^{q\ell_1\ell_2} \bar{\ell}_1 \gamma^\mu P_L \ell_2 \right) \bar{q} \gamma_\mu q \right. \\
 & + \left( C_{AR}^{q\ell_1\ell_2} \bar{\ell}_1 \gamma^\mu P_R \ell_2 + C_{AL}^{q\ell_1\ell_2} \bar{\ell}_1 \gamma^\mu P_L \ell_2 \right) \bar{q} \gamma_\mu \gamma_5 q \\
 & + m_2 m_q G_F \left( C_{SR}^{q\ell_1\ell_2} \bar{\ell}_1 P_L \ell_2 + C_{SL}^{q\ell_1\ell_2} \bar{\ell}_1 P_R \ell_2 \right) \bar{q} q \\
 & + m_2 m_q G_F \left( C_{PR}^{q\ell_1\ell_2} \bar{\ell}_1 P_L \ell_2 + C_{PL}^{q\ell_1\ell_2} \bar{\ell}_1 P_R \ell_2 \right) \bar{q} \gamma_5 q \\
 & \left. + m_2 m_q G_F \left( C_{TR}^{q\ell_1\ell_2} \bar{\ell}_1 \sigma^{\mu\nu} P_L \ell_2 + C_{TL}^{q\ell_1\ell_2} \bar{\ell}_1 \sigma^{\mu\nu} P_R \ell_2 \right) \bar{q} \sigma_{\mu\nu} q + h.c. \right].
 \end{aligned}$$

also gluonic operators

Scalar meson decays:  $\chi_{b0} \rightarrow \bar{\mu}\tau$ ,  $\chi_{c0} \rightarrow \bar{\mu}\tau$ , ...

# LFV vector quarkonia decays

★ Most LFV experimental data available  $V \rightarrow \mu e, \tau e, \text{etc.}$

$\ell_1 \ell_2$	$\mu\tau$	$e\tau$	$e\mu$
$\mathcal{B}(\Upsilon(1S) \rightarrow \ell_1 \ell_2)$	$6.0 \times 10^{-6}$	...	...
$\mathcal{B}(\Upsilon(2S) \rightarrow \ell_1 \ell_2)$	$3.3 \times 10^{-6}$	$3.2 \times 10^{-6}$	...
$\mathcal{B}(\Upsilon(3S) \rightarrow \ell_1 \ell_2)$	$3.1 \times 10^{-6}$	$4.2 \times 10^{-6}$	...
$\mathcal{B}(J/\psi \rightarrow \ell_1 \ell_2)$	$2.0 \times 10^{-6}$	$8.3 \times 10^{-6}$	$1.6 \times 10^{-7}$
$\mathcal{B}(\phi \rightarrow \ell_1 \ell_2)$	FPS	FPS	$4.1 \times 10^{-6}$
$\mathcal{B}(\ell_2 \rightarrow \ell_1 \gamma)$	$4.4 \times 10^{-8}$	$3.3 \times 10^{-8}$	$5.7 \times 10^{-13}$

★ Decay amplitude:  $\mathcal{A}(V \rightarrow \ell_1 \bar{\ell}_2) = \bar{u}(p_1, s_1) \left[ A_V^{\ell_1 \ell_2} \gamma_\mu + B_V^{\ell_1 \ell_2} \gamma_\mu \gamma_5 + \frac{C_V^{\ell_1 \ell_2}}{m_V} (p_2 - p_1)_\mu + \frac{i D_V^{\ell_1 \ell_2}}{m_V} (p_2 - p_1)_\mu \gamma_5 \right] v(p_2, s_2) \epsilon^\mu(p).$

★ Decay rate: 
$$\frac{\mathcal{B}(V \rightarrow \ell_1 \bar{\ell}_2)}{\mathcal{B}(V \rightarrow e^+ e^-)} = \left( \frac{m_V (1 - y^2)}{4\pi \alpha f_V Q_q} \right)^2 \left[ (|A_V^{\ell_1 \ell_2}|^2 + |B_V^{\ell_1 \ell_2}|^2) + \frac{1}{2} (1 - 2y^2) (|C_V^{\ell_1 \ell_2}|^2 + |D_V^{\ell_1 \ell_2}|^2) + y \text{Re}(A_V^{\ell_1 \ell_2} C_V^{\ell_1 \ell_2*} + i B_V^{\ell_1 \ell_2} D_V^{\ell_1 \ell_2*}) \right].$$

Form-factors depend on vector, tensor, and dipole Wilson coefficients



The secret of being a bore... is to tell everything.  
(Voltaire)

izquotes.com

*Le secret d'ennuyer est celui de tout dire*

# LFV vector quarkonia decays: dipoles

★ Constraints on Wilson coefficients of dipole low energy operators

Dipole Wilson coefficient [GeV <sup>-2</sup> ]	Leptons	Initial state					
	$\ell_1\ell_2$	$\Upsilon(1S)(b)$	$\Upsilon(2S)(b)$	$\Upsilon(3S)(b)$	$J/\psi(c)$	$\phi(s)$	$\ell_2 \rightarrow \ell_1\gamma$
$ C_{DL}^{\ell_1\ell_2}/\Lambda^2 $	$\mu\tau$	$2.0 \times 10^{-4}$	$1.6 \times 10^{-4}$	$1.4 \times 10^{-4}$	$2.5 \times 10^{-4}$	FPS	$2.6 \times 10^{-10}$
	$e\tau$	...	$1.6 \times 10^{-4}$	$1.6 \times 10^{-4}$	$5.3 \times 10^{-4}$	FPS	$2.7 \times 10^{-10}$
	$e\mu$	...	...	...	$1.1 \times 10^{-3}$	0.2	$3.1 \times 10^{-7}$
$ C_{DR}^{q\ell_1\ell_2}/\Lambda^2 $	$\mu\tau$	$2.0 \times 10^{-4}$	$1.6 \times 10^{-4}$	$1.4 \times 10^{-4}$	$2.5 \times 10^{-4}$	FPS	$2.6 \times 10^{-10}$
	$e\tau$	...	$1.6 \times 10^{-4}$	$1.6 \times 10^{-4}$	$5.3 \times 10^{-4}$	FPS	$2.7 \times 10^{-10}$
	$e\mu$	...	...	...	$1.1 \times 10^{-3}$	0.2	$3.1 \times 10^{-7}$

D. Hazard and A.A.P.,  
PRD94 (2016), 074023

★ Much tighter constraints are obtained from lepton radiative decays: drop from quarkonium decay analyses in what follows

# LFV vector quarkonia decays: 4f operators

★ Constraints on Wilson coefficients of four-fermion low energy operators

Wilson coefficient [GeV <sup>-2</sup> ]	Leptons	Initial state (quark)				
	$\ell_1 \ell_2$	$\Upsilon(1S)(b)$	$\Upsilon(2S)(b)$	$\Upsilon(3S)(b)$	$J/\psi(c)$	$\phi(s)$
$ C_{VL}^{q\ell_1\ell_2}/\Lambda^2 $	$\mu\tau$	$5.6 \times 10^{-6}$	$4.1 \times 10^{-6}$	$3.5 \times 10^{-6}$	$5.5 \times 10^{-5}$	FPS
	$e\tau$	...	$4.1 \times 10^{-6}$	$4.1 \times 10^{-6}$	$1.1 \times 10^{-4}$	FPS
	$e\mu$	...	...	...	$1.0 \times 10^{-5}$	$2 \times 10^{-3}$
$ C_{VR}^{q\ell_1\ell_2}/\Lambda^2 $	$\mu\tau$	$5.6 \times 10^{-6}$	$4.1 \times 10^{-6}$	$3.5 \times 10^{-6}$	$5.5 \times 10^{-5}$	FPS
	$e\tau$	...	$4.1 \times 10^{-6}$	$4.1 \times 10^{-6}$	$1.1 \times 10^{-4}$	FPS
	$e\mu$	...	...	...	$1.0 \times 10^{-5}$	$2 \times 10^{-3}$
$ C_{TL}^{q\ell_1\ell_2}/\Lambda^2 $	$\mu\tau$	$4.4 \times 10^{-2}$	$3.2 \times 10^{-2}$	$2.8 \times 10^{-2}$	1.2	FPS
	$e\tau$	...	$3.3 \times 10^{-2}$	$3.2 \times 10^{-2}$	2.4	FPS
	$e\mu$	...	...	...	4.8	$1 \times 10^4$
$ C_{TR}^{q\ell_1\ell_2}/\Lambda^2 $	$\mu\tau$	$4.4 \times 10^{-2}$	$3.2 \times 10^{-2}$	$2.8 \times 10^{-2}$	1.2	FPS
	$e\tau$	...	$3.3 \times 10^{-2}$	$3.2 \times 10^{-2}$	2.4	FPS
	$e\mu$	...	...	...	4.8	$1 \times 10^4$

D. Hazard and A.A.P.,  
PRD94 (2016), 074023

# LFV pseudoscalar/scalar quarkonia decays

★ Very scarce LFV experimental data available  $P/S \rightarrow \mu e, \tau e, \text{etc.}$

- no data for pseudoscalar heavy-flavored meson decays
- no data for any scalar meson decays

$\ell_1 \ell_2$	$e\mu$
$\mathcal{B}(\eta \rightarrow \ell_1 \ell_2)$	$6 \times 10^{-6}$
$\mathcal{B}(\eta' \rightarrow \ell_1 \ell_2)$	$4.7 \times 10^{-4}$
$\mathcal{B}(\pi^0 \rightarrow \ell_1 \ell_2)$	$3.6 \times 10^{-10}$

$$P = \eta_b, \eta_c, \eta^{(\prime)}, \dots$$

$$S = \chi_{b0}, \chi_{c0}, \dots$$

★ Decay amplitudes:  $\mathcal{A}(P \rightarrow \ell_1 \bar{\ell}_2) = \bar{u}(p_1, s_1)[E_P^{\ell_1 \ell_2} + iF_P^{\ell_1 \ell_2} \gamma_5]v(p_2, s_2)$

$$\mathcal{A}(S \rightarrow \ell_1 \bar{\ell}_2) = \bar{u}(p_1, s_1)[E_S^{\ell_1 \ell_2} + iF_S^{\ell_1 \ell_2} \gamma_5]v(p_2, s_2)$$

★ Decay rates:  $\mathcal{B}(P \rightarrow \ell_1 \bar{\ell}_2) = \frac{m_P}{8\pi\Gamma_P} (1 - y^2)^2 [ |E_P^{\ell_1 \ell_2}|^2 + |F_P^{\ell_1 \ell_2}|^2 ]$

$$\mathcal{B}(S \rightarrow \ell_1 \bar{\ell}_2) = \frac{m_S}{8\pi\Gamma_S} (1 - y^2)^2 [ |E_S^{\ell_1 \ell_2}|^2 + |F_S^{\ell_1 \ell_2}|^2 ]$$

Form-factors depend on axial, pseudoscalar, and gluonic operator Wilson coefficients (P)  
scalar and gluonic operator Wilson coefficients (S)

# LFV pseudoscalar/scalar quarkonia decays

## ★ Constraints on Wilson coefficients of low energy operators

D. Hazard and A.A.P.,  
PRD94 (2016), 074023

Wilson coefficient	Leptons	Initial state					
	$\ell_1\ell_2$	$\eta_b$	$\eta_c$	$\eta(u/d)$	$\eta(s)$	$\eta'(u/d)$	$\eta'(s)$
$ C_{AL}^{q\ell_1\ell_2}/\Lambda^2 $	$\mu\tau$	...	...	FPS	FPS	FPS	FPS
	$e\tau$	...	...	FPS	FPS	FPS	FPS
	$e\mu$	...	...	$3 \times 10^{-3}$	$2 \times 10^{-3}$	$2.1 \times 10^{-1}$	$1.9 \times 10^{-1}$
$ C_{AR}^{q\ell_1\ell_2}/\Lambda^2 $	$\mu\tau$	...	...	FPS	FPS	FPS	FPS
	$e\tau$	...	...	FPS	FPS	FPS	FPS
	$e\mu$	...	...	$3 \times 10^{-3}$	$2 \times 10^{-3}$	$2.1 \times 10^{-1}$	$1.9 \times 10^{-1}$
$ C_{PL}^{q\ell_1\ell_2}/\Lambda^2 $	$\mu\tau$	...	...	FPS	FPS	FPS	FPS
	$e\tau$	...	...	FPS	FPS	FPS	FPS
	$e\mu$	...	...	$2 \times 10^3$	$1 \times 10^3$	$3.9 \times 10^4$	$3.6 \times 10^4$
$ C_{PR}^{q\ell_1\ell_2}/\Lambda^2 $	$\mu\tau$	...	...	FPS	FPS	FPS	FPS
	$e\tau$	...	...	FPS	FPS	FPS	FPS
	$e\mu$	...	...	$2 \times 10^3$	$1 \times 10^3$	$3.9 \times 10^4$	$3.6 \times 10^4$

★ More data is needed: use radiative decays:  $\mathcal{B}(V \rightarrow \gamma \ell_1 \bar{\ell}_2) = \mathcal{B}(V \rightarrow \gamma M) \mathcal{B}(M \rightarrow \ell_1 \bar{\ell}_2)$

$$\mathcal{B}(\psi(2S) \rightarrow \gamma \chi_{c0}(1P)) = 9.99 \pm 0.27\%,$$

$$\mathcal{B}(\psi(3770) \rightarrow \gamma \chi_{c0}(1P)) = 0.73 \pm 0.09\%.$$

$$\mathcal{B}(J/\psi \rightarrow \gamma \eta_c) = 1.7 \pm 0.4\%,$$

$$\mathcal{B}(\psi(2S) \rightarrow \gamma \eta_c) = 0.34 \pm 0.05\%.$$

$$\mathcal{B}(\Upsilon(2S) \rightarrow \gamma \chi_{b0}(1P)) = 3.8 \pm 0.4\%,$$

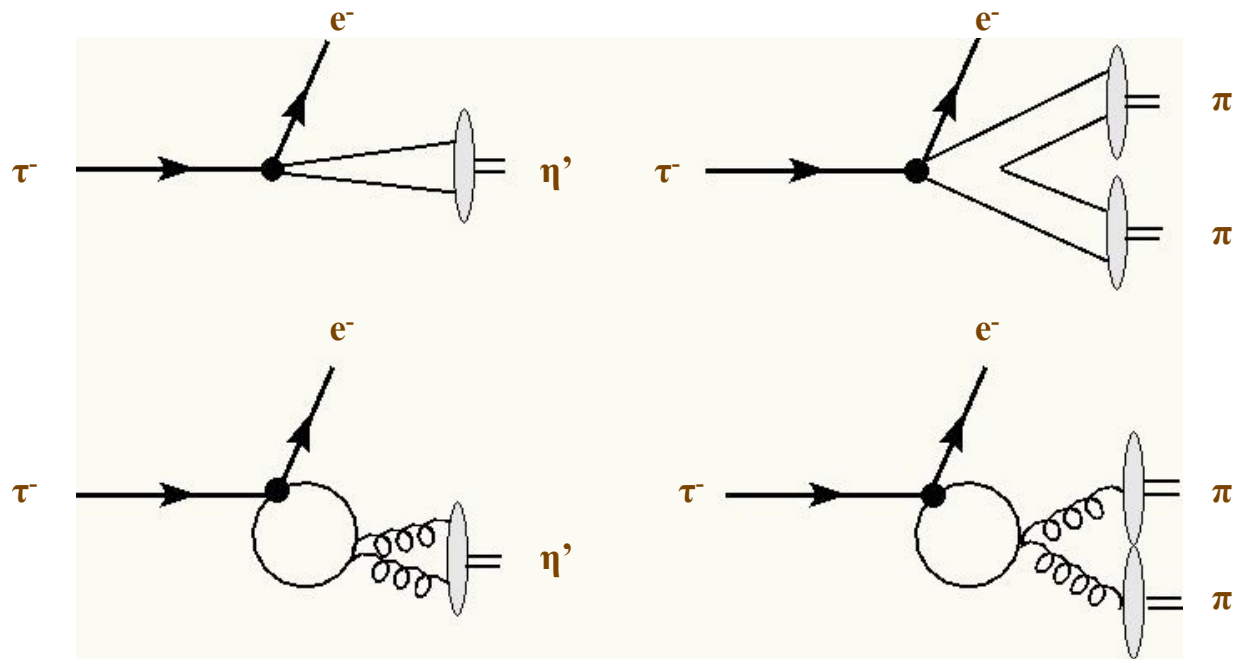
$$\mathcal{B}(\Upsilon(3S) \rightarrow \gamma \chi_{b0}(1P)) = 0.27 \pm 0.04\%,$$

$$\mathcal{B}(\Upsilon(3S) \rightarrow \gamma \chi_{b0}(2P)) = 5.9 \pm 0.6\%.$$

# Probing LFV gluonic operators in tau decays

★ Let's compute FCNC tau decays (concentrate on those sensitive to gluonic operators)

AAP and D. Zhuridov  
PRD89 (2014) 3, 033005



Parity-violating  
operators

Parity-conserving  
operators



# Hadronic physics I

★ To calculate FV tau decays we need a bit of hadronic physics

- matrix elements of parity-conserving operators

$$\langle \pi^+ \pi^- | \bar{q}q | 0 \rangle = \langle K^+ K^- | \bar{q}q | 0 \rangle = \delta_q^M B_0$$

$$\langle M^+ M^- | \bar{q} \gamma_\mu q | 0 \rangle = \delta_q^M G_M^{(q)}(Q^2) (p_+ - p_-)_\mu$$

$$\langle M^+ M^- | \frac{\alpha_s}{4\pi} G^{a\mu\nu} G_{\mu\nu}^a | 0 \rangle = -\frac{2}{9} q^2,$$

- ... where  $B_0 = 1.96 \text{ GeV}$  from  $m_\pi^2 = (m_u + m_d) B_0$

Black, Han, He, Sher

- ... and we used  $\theta_\mu^\mu = -\frac{b\alpha_s}{8\pi} G^{\mu\nu a} G_{\mu\nu}^a + \sum_{q=u,d,s} m_q \bar{q}q$

Voloshin

★ Can do better on hadronic side by using data

Celis, Cirigliano, Passemar

# Hadronic physics II

★ To calculate FV tau decays we need a bit of hadronic physics

- matrix elements of parity-violating operators

$$\langle M(p) | \bar{q} \gamma^\mu \gamma_5 q | 0 \rangle = -i b_q f_M^q p^\mu,$$

$$\langle M(p) | \bar{q} \gamma_5 q | 0 \rangle = -i b_q h_M^q,$$

$$\langle M(p) | \frac{\alpha_s}{4\pi} G^{a\mu\nu} \tilde{G}_{\mu\nu}^a | 0 \rangle = a_M,$$

- ... where  $q=u,d,s$  and  $b_{u,d}=1/2^{1/2}$ , while  $b_s=1$
- ... and in the FKS scheme of eta-eta' mixing

$$a_\eta = -\frac{m_{\eta'}^2 - m_\eta^2}{2} \sin 2\phi (-f_q b_q \sin \phi + f_s \cos \phi),$$

$$a_{\eta'} = -\frac{m_{\eta'}^2 - m_\eta^2}{2} \sin 2\phi (f_q b_q \sin \phi + f_s \cos \phi),$$

# Bounds: parity conserving

★ Looking at the scalar operators only

$$\frac{d\Gamma(\tau \rightarrow \ell M^+ M^-)}{dq^2} = \frac{m_\tau}{32(2\pi)^3 \Lambda^4} \left[ |A_{MM}|^2 + |B_{MM}|^2 \right] \times \sqrt{1 - \frac{4m_M^2}{q^2}} \left(1 - \frac{q^2}{m_\tau^2}\right)^2,$$

- ... with the following coefficients

$$A_{MM} = -\frac{2c_1^{\ell\tau}}{9} q^2 + \frac{1}{2} \sum_{q=u,d,s} \left( C_1^{q\ell\tau} + C_2^{q\ell\tau} \right) \delta_q^M B_0,$$

$$B_{MM} = -\frac{2c_3^{\ell\tau}}{9} q^2 + \frac{1}{2} \sum_{q=u,d,s} \left( C_3^{q\ell\tau} + C_4^{q\ell\tau} \right) \delta_q^M B_0.$$

Coef	Bound on $ c_i^{\ell\tau} /\Lambda^2$ , GeV <sup>-3</sup>							
	$\mathcal{B}(\tau \rightarrow \mu \pi^+ \pi^-)$ < $2.1 \times 10^{-8}$	$\mathcal{B}(\tau \rightarrow e \pi^+ \pi^-)$ < $2.3 \times 10^{-8}$	$\mathcal{B}(\tau \rightarrow \mu K^+ K^-)$ < $4.4 \times 10^{-8}$	$\mathcal{B}(\tau \rightarrow e K^+ K^-)$ < $3.3 \times 10^{-8}$	$\mathcal{B}(\tau \rightarrow \mu \eta')$ < $1.3 \times 10^{-7}$	$\mathcal{B}(\tau \rightarrow e \eta')$ < $1.6 \times 10^{-7}$	$\mathcal{B}(\tau \rightarrow \mu \eta)$ < $1.3 \times 10^{-7}$	$\mathcal{B}(\tau \rightarrow e \eta)$ < $1.6 \times 10^{-7}$
$c_1$	$6.8 \times 10^{-8}$	$6.5 \times 10^{-8}$	$9.4 \times 10^{-8}$	$8.2 \times 10^{-8}$	–	–	–	–
$c_2$	–	–	–	–	$2.3 \times 10^{-7}$	$2.5 \times 10^{-7}$	$1.6 \times 10^{-7}$	$1.5 \times 10^{-7}$
$c_3$	$6.8 \times 10^{-8}$	$6.5 \times 10^{-8}$	$9.4 \times 10^{-8}$	$8.2 \times 10^{-8}$	–	–	–	–
$c_4$	–	–	–	–	$2.3 \times 10^{-7}$	$2.5 \times 10^{-7}$	$1.6 \times 10^{-7}$	$1.5 \times 10^{-7}$

# Bounds: parity violating

★ Again, looking at the scalar operators only

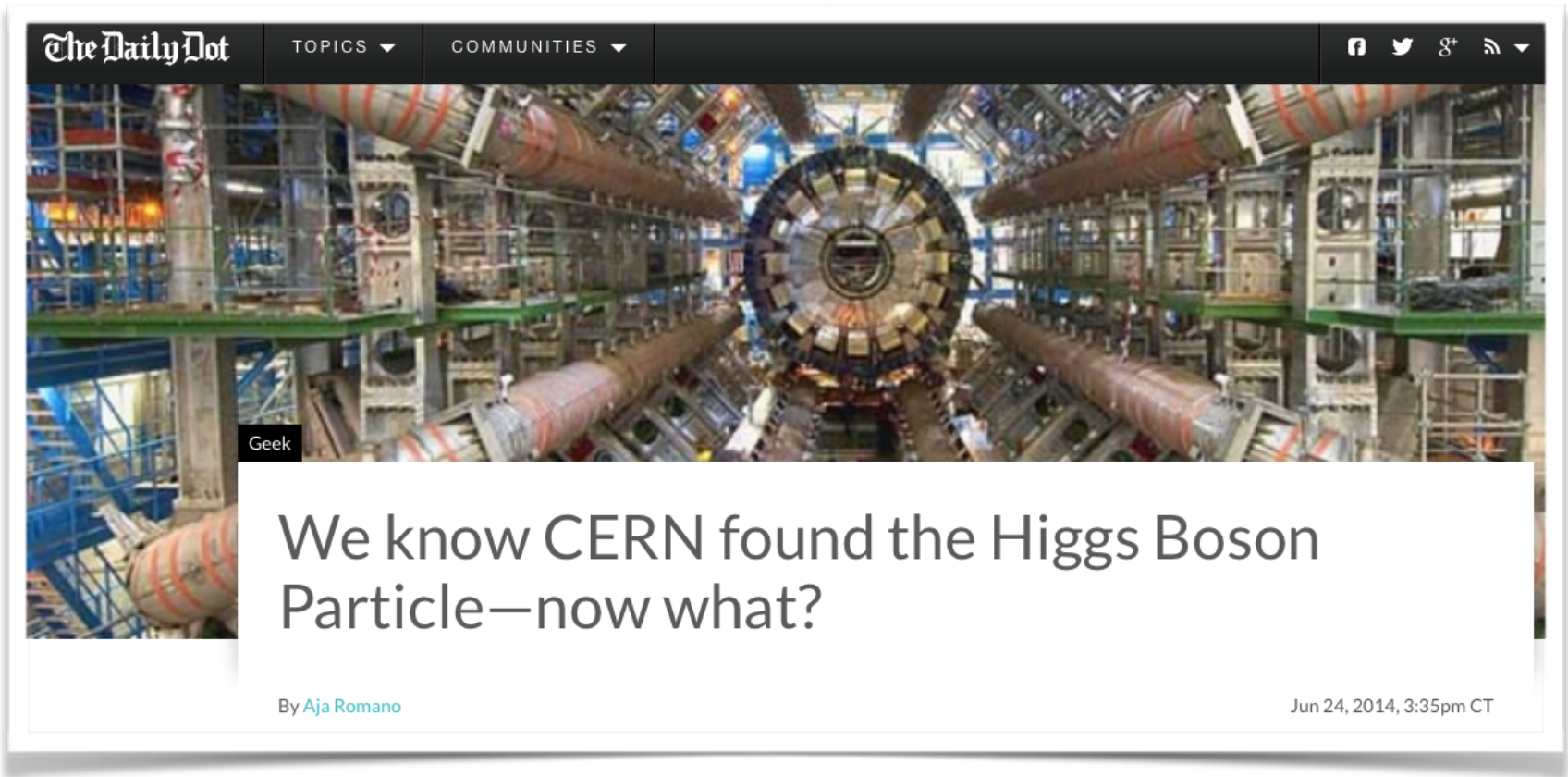
$$\Gamma(\tau \rightarrow \mu M) = \frac{m_\tau}{8\pi\Lambda^4} \left[ |A_M|^2 + |B_M|^2 \right] \left( 1 - \frac{m_M^2}{m_\tau^2} \right)^2$$

- ... with the following coefficients

$$\begin{aligned}
 A_M &= -\frac{2i}{9} c_2^{\ell\tau} a_M + \sum_{q=u,d,s} \left( C_2^{q\ell\tau} - C_1^{q\ell\tau} \right) \frac{b_q h_M^q}{4m_q} \\
 &\quad + \frac{1}{2} m_\mu \sum_{q=u,d,s} \left( C_5^{q\ell\tau} - C_6^{q\ell\tau} \right) b_q f_M^q \\
 &\quad - \frac{1}{2} m_\tau \sum_{q=u,d,s} \left( C_7^{q\ell\tau} - C_8^{q\ell\tau} \right) b_q f_M^q \\
 B_M &= -\frac{2i}{9} c_4^{\ell\tau} a_M + \sum_{q=u,d,s} \left( C_4^{q\ell\tau} - C_3^{q\ell\tau} \right) \frac{b_q h_M^q}{4m_q} \\
 &\quad - \frac{1}{2} m_\tau \sum_{q=u,d,s} \left( C_5^{q\ell\tau} - C_6^{q\ell\tau} \right) b_q f_M^q \\
 &\quad + \frac{1}{2} m_\mu \sum_{q=u,d,s} \left( C_7^{q\ell\tau} - C_8^{q\ell\tau} \right) b_q f_M^q
 \end{aligned}$$

Coef	Bound on $ c_i^{\ell\tau} /\Lambda^2$ , GeV <sup>-3</sup>							
	$\mathcal{B}(\tau \rightarrow \mu \pi^+ \pi^-)$ < $2.1 \times 10^{-8}$	$\mathcal{B}(\tau \rightarrow e \pi^+ \pi^-)$ < $2.3 \times 10^{-8}$	$\mathcal{B}(\tau \rightarrow \mu K^+ K^-)$ < $4.4 \times 10^{-8}$	$\mathcal{B}(\tau \rightarrow e K^+ K^-)$ < $3.3 \times 10^{-8}$	$\mathcal{B}(\tau \rightarrow \mu \eta')$ < $1.3 \times 10^{-7}$	$\mathcal{B}(\tau \rightarrow e \eta')$ < $1.6 \times 10^{-7}$	$\mathcal{B}(\tau \rightarrow \mu \eta)$ < $1.3 \times 10^{-7}$	$\mathcal{B}(\tau \rightarrow e \eta)$ < $1.6 \times 10^{-7}$
$c_1$	$6.8 \times 10^{-8}$	$6.5 \times 10^{-8}$	$9.4 \times 10^{-8}$	$8.2 \times 10^{-8}$	–	–	–	–
$c_2$	–	–	–	–	$2.3 \times 10^{-7}$	$2.5 \times 10^{-7}$	$1.6 \times 10^{-7}$	$1.5 \times 10^{-7}$
$c_3$	$6.8 \times 10^{-8}$	$6.5 \times 10^{-8}$	$9.4 \times 10^{-8}$	$8.2 \times 10^{-8}$	–	–	–	–
$c_4$	–	–	–	–	$2.3 \times 10^{-7}$	$2.5 \times 10^{-7}$	$1.6 \times 10^{-7}$	$1.5 \times 10^{-7}$

# Now what?



The Daily Dot

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Geek

## We know CERN found the Higgs Boson Particle—now what?

By [Aja Romano](#)

Jun 24, 2014, 3:35pm CT

The image shows a screenshot of a news article from The Daily Dot. The article title is "We know CERN found the Higgs Boson Particle—now what?". The author is Aja Romano, and the date is June 24, 2014, at 3:35pm CT. The background of the article is a photograph of the interior of the Large Hadron Collider (LHC) tunnel, showing the complex machinery and the central circular structure.

# 3. Matching to high scale physics

★ Consider example: leptoquark interactions

- scalar leptoquarks

$$\mathcal{L}_S = (\lambda_{LS_0} \bar{q}_L^c i\tau_2 \ell_L + \lambda_{RS_0} \bar{u}_R^c e_R) S_0^\dagger + \left( \lambda_{LS_{1/2}} \bar{u}_R \ell_L + \lambda_{RS_{1/2}} \bar{q}_L i\tau_2 e_R \right) S_{1/2}^\dagger + \text{H.c.},$$

- vector leptoquarks

$$\mathcal{L}_V = (\lambda_{LV_0} \bar{q}_L \gamma_\mu \ell_L + \lambda_{RV_0} \bar{d}_R \gamma_\mu e_R) V_0^{\mu\dagger} + \left( \lambda_{LV_{1/2}} \bar{d}_R^c \gamma_\mu \ell_L + \lambda_{RV_{1/2}} \bar{q}_L^c \gamma_\mu e_R \right) V_{1/2}^{\mu\dagger} + \text{H.c.},$$

Davidson, Bailey, Campbell

★ Matching to the general result above, get

$C_i^u / \Lambda^2$	Expression	$C_i^d / \Lambda^2$	Expression
$\frac{C_1^u}{\Lambda^2}$	$\frac{\lambda_{RS_{1/2}}^{\ell_1 u} \lambda_{LS_{1/2}}^{\ell_2 u}}{2M_{S_{1/2}}^2}$	$\frac{C_1^d}{\Lambda^2}$	$\frac{\lambda_{LV_{1/2}}^{\ell_2 b} \lambda_{RV_{1/2}}^{\ell_1 b}}{M_{V_{1/2}}^2}$
$\frac{C_2^u}{\Lambda^2}$	$\frac{\lambda_{RS_0}^{\ell_1 u} \lambda_{LS_0}^{\ell_2 u}}{2M_{S_0}^2}$	$\frac{C_2^d}{\Lambda^2}$	$\frac{\lambda_{LV_0}^{\ell_2 b} \lambda_{RV_0}^{\ell_1 b}}{M_{V_0}^2}$
$\frac{C_3^u}{\Lambda^2}$	$\frac{\lambda_{RS_0}^{\ell_2 u} \lambda_{LS_0}^{\ell_1 u}}{2M_{S_0}^2}$	$\frac{C_3^d}{\Lambda^2}$	$\frac{\lambda_{LV_0}^{\ell_1 b} \lambda_{RV_0}^{\ell_2 b}}{M_{V_0}^2}$
$\frac{C_4^u}{\Lambda^2}$	$\frac{\lambda_{RS_{1/2}}^{\ell_2 u} \lambda_{LS_{1/2}}^{\ell_1 u}}{2M_{S_{1/2}}^2}$	$\frac{C_4^d}{\Lambda^2}$	$\frac{\lambda_{LV_{1/2}}^{\ell_1 b} \lambda_{RV_{1/2}}^{\ell_2 b}}{M_{V_{1/2}}^2}$

# Leptoquarks as an example

★ Leptoquark interaction parameters for tau-mu transitions

$$\frac{|\lambda_{RS_0}^{\mu t} \lambda_{LS_0}^{\tau t}|}{M_{S_0}^2} = \frac{|\lambda_{RS_{1/2}}^{\mu t} \lambda_{LS_{1/2}}^{\tau t}|}{M_{S_{1/2}}^2} < 2.3 \times 10^{-4} \text{ GeV}^{-2},$$

$$\frac{|\lambda_{LV_0}^{\tau b} \lambda_{RV_0}^{\mu b}|}{M_{V_0}^2} = \frac{|\lambda_{LV_{1/2}}^{\tau b} \lambda_{RV_{1/2}}^{\mu b}|}{M_{V_{1/2}}^2} < 4.4 \times 10^{-6} \text{ GeV}^{-2}$$

★ ... and the same for tau-e

$$\frac{|\lambda_{RS_0}^{et} \lambda_{LS_0}^{\tau t}|}{M_{S_0}^2} = \frac{|\lambda_{RS_{1/2}}^{et} \lambda_{LS_{1/2}}^{\tau t}|}{M_{S_{1/2}}^2} < 2.2 \times 10^{-4} \text{ GeV}^{-2},$$

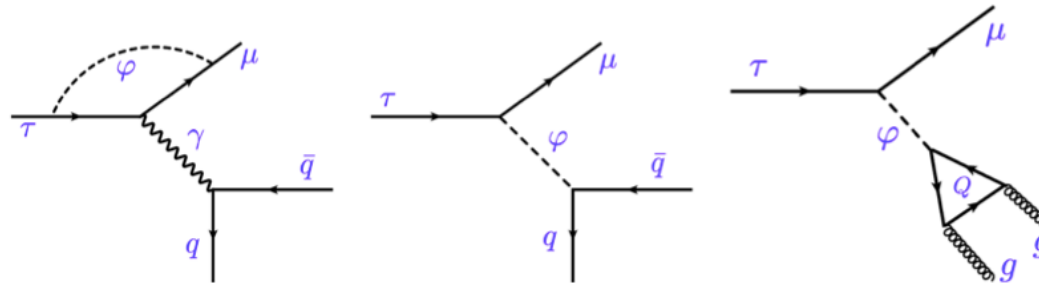
$$\frac{|\lambda_{LV_0}^{\tau b} \lambda_{RV_0}^{eb}|}{M_{V_0}^2} = \frac{|\lambda_{LV_{1/2}}^{\tau b} \lambda_{RV_{1/2}}^{eb}|}{M_{V_{1/2}}^2} < 4.2 \times 10^{-6} \text{ GeV}^{-2}$$

AAP and D. Zhuridov  
PRD89 (2014) 3, 033005

# FCNC Higgs as an example

Celis, Cirigliano, Passemar

★ FCNC Higgs gives another example



★ FCNC Higgs gives another example

Process	(BR × 10 <sup>8</sup> ) 90% C.L.	$\sqrt{ Y_{\mu\tau}^h ^2 +  Y_{\tau\mu}^h ^2}$	Operator(s)
$\tau \rightarrow \mu\gamma$	<4.4 [86]	<0.016	Dipole
$\tau \rightarrow \mu\mu\mu$	<2.1 [87]	<0.24	Dipole
$\tau \rightarrow \mu\pi^+\pi^-$	<2.1 [88]	<0.13	Scalar, gluon, dipole
$\tau \rightarrow \mu\rho$	<1.2 [89]	<0.13	Scalar, gluon, dipole
$\tau \rightarrow \mu\pi^0\pi^0$	<1.4 × 10 <sup>3</sup> [90]	<6.3	Scalar, gluon

Process	(BR × 10 <sup>8</sup> ) 90% CL	$\sqrt{ Y_{e\tau}^h ^2 +  Y_{\tau e}^h ^2}$	Operator(s)
$\tau \rightarrow e\gamma$	<3.3 [86]	<0.014	Dipole
$\tau \rightarrow eee$	<2.7 [87]	<0.12	Dipole
$\tau \rightarrow e\pi^+\pi^-$	<2.3 [88]	<0.14	Scalar, gluon, dipole
$\tau \rightarrow e\rho$	<1.8 [89]	<0.16	Scalar, gluon, dipole
$\tau \rightarrow e\pi^0\pi^0$	<6.5 × 10 <sup>2</sup> [90]	<4.3	Scalar, gluon

Celis, Cirigliano, Passemar

## 4. Conclusions

- Flavor-changing neutral current transitions provide great opportunities for studies of lepton flavor in the SM and BSM
    - charge lepton transitions offer practically SM-background-free playground
    - large contributions from New Physics are possible, but not seen
    - EFT approach can be useful in studies of quarkonium/tau FCNC decays
    - ... as current methods rarely go beyond dim-6 operators
    - ... and thus do not constrain NP-heavy fermion couplings very well
  - Need more data from Belle-II (or LHCb) on LFV quarkonia and tau decays!
    - there is NO DATA for LFV radiative decays, e.g.  $\psi(nS) \rightarrow \gamma \bar{\mu} e, \gamma \bar{\mu} \tau, \dots$
  - More data from ATLAS/CMS/(LHCb?) on  $pp \rightarrow \tau \mu + X$ 
    - possible effects from  $gg \rightarrow \tau \mu$  due to large gluon luminosity of LHC
- Bhattacharya, Morgan, AAP
- Maybe flavor physics will be the only place to see glimpses of New Physics
  - ...but then again, maybe not.



# Thank you for your attention!

JOURNAL OF APPLIED BEHAVIOR ANALYSIS

1974, 7, 497

NUMBER 3 (FALL 1974)

*THE UNSUCCESSFUL SELF-TREATMENT OF  
A CASE OF "WRITER'S BLOCK"<sup>1</sup>*

DENNIS UPPER

VETERANS ADMINISTRATION HOSPITAL, BROCKTON, MASSACHUSETTS

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REFERENCES

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<sup>1</sup>Portions of this paper were not presented at the 81st Annual American Psychological Association Convention, Montreal, Canada, August 30, 1973. Reprints may be obtained from Dennis Upper, Behavior Therapy Unit, Veterans Administration Hospital, Brockton, Massachusetts 02401.

*Received 25 October 1973.  
(Published without revision.)*

Hopefully, I did better than him...

# LFV vector quarkonia decays

★ Most general decay rate for  $V \rightarrow \mu e, \tau e, \text{etc.}$  ( $V = \Upsilon(nS), \psi(nS), \rho, \phi, \dots$ ):

$$\frac{\mathcal{B}(V \rightarrow \ell_1 \bar{\ell}_2)}{\mathcal{B}(V \rightarrow e^+ e^-)} = \left( \frac{m_V(1-y^2)}{4\pi\alpha f_V Q_q} \right)^2 [ (|A_V^{\ell_1 \ell_2}|^2 + |B_V^{\ell_1 \ell_2}|^2) + \frac{1}{2}(1-2y^2)(|C_V^{\ell_1 \ell_2}|^2 + |D_V^{\ell_1 \ell_2}|^2) + y \text{Re}(A_V^{\ell_1 \ell_2} C_V^{\ell_1 \ell_2*} + i B_V^{\ell_1 \ell_2} D_V^{\ell_1 \ell_2*}) ].$$

D. Hazard and A.A.P.,  
PRD94 (2016), 074023

... and the decay rate is

$$\begin{aligned} A_V^{\ell_1 \ell_2} &= \frac{f_V m_V}{\Lambda^2} [\sqrt{4\pi\alpha} Q_q y^2 (C_{DL}^{\ell_1 \ell_2} + C_{DR}^{\ell_1 \ell_2}) + \kappa_V (C_{VL}^{q\ell_1 \ell_2} + C_{VR}^{q\ell_1 \ell_2}) \\ &\quad + 2y^2 \kappa_V \frac{f_V^T}{f_V} G_F m_V m_q (C_{TL}^{q\ell_1 \ell_2} + C_{TR}^{q\ell_1 \ell_2})], \\ B_V^{\ell_1 \ell_2} &= \frac{f_V m_V}{\Lambda^2} [-\sqrt{4\pi\alpha} Q_q y^2 (C_{DL}^{\ell_1 \ell_2} - C_{DR}^{\ell_1 \ell_2}) - \kappa_V (C_{VL}^{q\ell_1 \ell_2} - C_{VR}^{q\ell_1 \ell_2}) \\ &\quad - 2y^2 \kappa_V \frac{f_V^T}{f_V} G_F m_V m_q (C_{TL}^{q\ell_1 \ell_2} - C_{TR}^{q\ell_1 \ell_2})], \\ C_V^{\ell_1 \ell_2} &= \frac{f_V m_V}{\Lambda^2} y [\sqrt{4\pi\alpha} Q_q (C_{DL}^{\ell_1 \ell_2} + C_{DR}^{\ell_1 \ell_2}) + 2\kappa_V \frac{f_V^T}{f_V} G_F m_V m_q (C_{TL}^{q\ell_1 \ell_2} + C_{TR}^{q\ell_1 \ell_2})], \\ D_V^{\ell_1 \ell_2} &= i \frac{f_V m_V}{\Lambda^2} y [-\sqrt{4\pi\alpha} Q_q (C_{DL}^{\ell_1 \ell_2} - C_{DR}^{\ell_1 \ell_2}) - 2\kappa_V \frac{f_V^T}{f_V} G_F m_V m_q (C_{TL}^{q\ell_1 \ell_2} - C_{TR}^{q\ell_1 \ell_2})]. \end{aligned}$$

# LFV pseudoscalar quarkonia decays

★ Most general decay rate for  $P \rightarrow \mu e, \tau e, \text{etc.}$  ( $P = \eta_b, \eta_c, \eta^{(\prime)}, \dots$ ):

$$\mathcal{B}(P \rightarrow \ell_1 \bar{\ell}_2) = \frac{m_P}{8\pi\Gamma_P} (1 - y^2)^2 [ |E_P^{\ell_1 \ell_2}|^2 + |F_P^{\ell_1 \ell_2}|^2 ].$$

D. Hazard and A.A.P.,  
PRD94 (2016), 074023

... and the decay rate is

$$\begin{aligned} E_P^{\ell_1 \ell_2} &= y \frac{m_P}{4\Lambda^2} [ -if_P [ 2(C_{AL}^{q\ell_1 \ell_2} + C_{AR}^{q\ell_1 \ell_2}) \\ &\quad - m_P^2 G_F (C_{PL}^{q\ell_1 \ell_2} + C_{PR}^{q\ell_1 \ell_2}) ] + 9G_F a_P (C_{\tilde{G}L}^{\ell_1 \ell_2} + C_{\tilde{G}R}^{\ell_1 \ell_2}) ], \\ F_P^{\ell_1 \ell_2} &= -y \frac{m_P}{4\Lambda^2} [ f_P [ 2(C_{AL}^{q\ell_1 \ell_2} - C_{AR}^{q\ell_1 \ell_2}) \\ &\quad - m_P^2 G_F (C_{PL}^{q\ell_1 \ell_2} - C_{PR}^{q\ell_1 \ell_2}) ] + 9iG_F a_P (C_{\tilde{G}L}^{\ell_1 \ell_2} - C_{\tilde{G}R}^{\ell_1 \ell_2}) ]. \end{aligned}$$

# LFV scalar quarkonia decays

★ Most general decay rate for  $S \rightarrow \mu e, \tau e, \text{etc.}$  ( $S = \chi_{b0}, \chi_{c0}, \dots$ ):

$$\mathcal{B}(S \rightarrow \ell_1 \bar{\ell}_2) = \frac{m_S}{8\pi\Gamma_S} (1 - y^2)^2 [ |E_S^{\ell_1 \ell_2}|^2 + |F_S^{\ell_1 \ell_2}|^2 ]$$

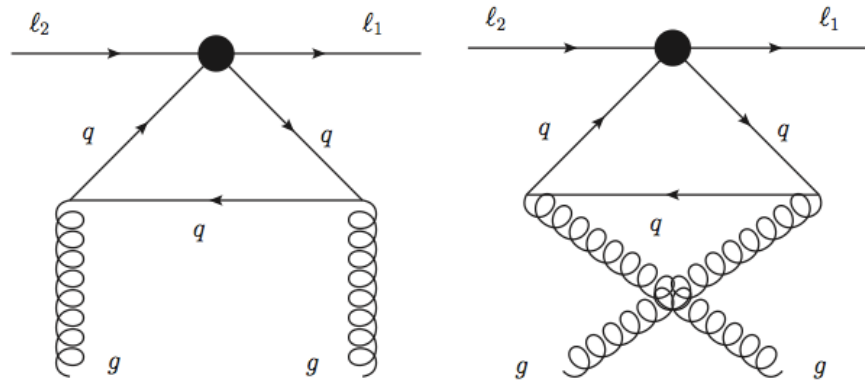
D. Hazard and A.A.P.,  
PRD94 (2016), 074023

... and the decay rate is

$$\begin{aligned} E_S^{\ell_1 \ell_2} &= y \frac{m_S G_F}{4\Lambda^2} [ 2if_S m_S m_q (C_{SL}^{q\ell_1 \ell_2} + C_{SR}^{q\ell_1 \ell_2}) \\ &\quad + 9a_S (C_{GL}^{q\ell_1 \ell_2} + C_{GR}^{q\ell_1 \ell_2}) ], \\ F_S^{\ell_1 \ell_2} &= y \frac{m_S G_F}{4\Lambda^2} [ 2f_S m_S m_q (C_{SL}^{q\ell_1 \ell_2} - C_{SR}^{q\ell_1 \ell_2}) \\ &\quad - 9ia_S (C_{GL}^{q\ell_1 \ell_2} - C_{GR}^{q\ell_1 \ell_2}) ]. \end{aligned}$$

# Effective Lagrangians: gluonic operators

★ Coefficients of gluonic operators depend on the number of active flavors



$$\mathcal{L}_G = -\frac{m_2 G_F}{\Lambda^2} \frac{\beta_L}{4\alpha_s} \left[ \left( C_{GR} \bar{\ell}_1 P_R \ell_2 + C_{GL} \bar{\ell}_1 P_L \ell_2 \right) G_{\mu\nu}^a G^{a\mu\nu} \right. \\ \left. + \left( C_{\bar{G}R} \bar{\ell}_1 P_R \ell_2 + C_{\bar{G}L} \bar{\ell}_1 P_L \ell_2 \right) G_{\mu\nu}^a \tilde{G}^{a\mu\nu} + h.c. \right]$$

- ★ we can calculate their contribution to meson or tau decay rates!
- ★ also relevant for muon conversion experiments
- ★  $c_i$  probe couplings of heavy quarks to New Physics

AAP and D. Zhuridov  
PRD89 (2014) 3, 033005

# Effective Lagrangians: gluonic operators

★ ... get an effective Lagrangian

$$\mathcal{L}_{\ell_1 \ell_2}^{(7)} = \frac{1}{\Lambda^2} \sum_{i=1}^4 c_i^{\ell_1 \ell_2} O_i^{\ell_1 \ell_2} + \text{H.c.},$$

AAP and D. Zhuridov  
PRD89 (2014) 3, 033005

...where we defined operators

$$O_1^{\ell_1 \ell_2} = \bar{\ell}_{1R} \ell_{2L} \frac{\beta_L}{4\alpha_s} G_{\mu\nu}^a G^{a\mu\nu},$$

$$O_2^{\ell_1 \ell_2} = \bar{\ell}_{1R} \ell_{2L} \frac{\beta_L}{4\alpha_s} G_{\mu\nu}^a \tilde{G}^{a\mu\nu},$$

$$O_3^{\ell_1 \ell_2} = \bar{\ell}_{1L} \ell_{2R} \frac{\beta_L}{4\alpha_s} G_{\mu\nu}^a G^{a\mu\nu},$$

$$O_4^{\ell_1 \ell_2} = \bar{\ell}_{1L} \ell_{2R} \frac{\beta_L}{4\alpha_s} G_{\mu\nu}^a \tilde{G}^{a\mu\nu},$$

...and Wilson coefficients

$$c_1^{\ell_1 \ell_2} = -\frac{2}{9} \sum_{q=c,b,t} \frac{I_1(m_q)}{m_q} (C_1^{q\ell_1 \ell_2} + C_2^{q\ell_1 \ell_2}),$$

$$c_2^{\ell_1 \ell_2} = \frac{2i}{9} \sum_{q=c,b,t} \frac{I_2(m_q)}{m_q} (C_1^{q\ell_1 \ell_2} - C_2^{q\ell_1 \ell_2}),$$

$$c_3^{\ell_1 \ell_2} = -\frac{2}{9} \sum_{q=c,b,t} \frac{I_1(m_q)}{m_q} (C_3^{q\ell_1 \ell_2} + C_4^{q\ell_1 \ell_2}),$$

$$c_4^{\ell_1 \ell_2} = \frac{2i}{9} \sum_{q=c,b,t} \frac{I_2(m_q)}{m_q} (C_3^{q\ell_1 \ell_2} - C_4^{q\ell_1 \ell_2}),$$

$$I_1 = \frac{1}{3}, \quad I_2 = \frac{1}{2}.$$