

Physical Cosmology I

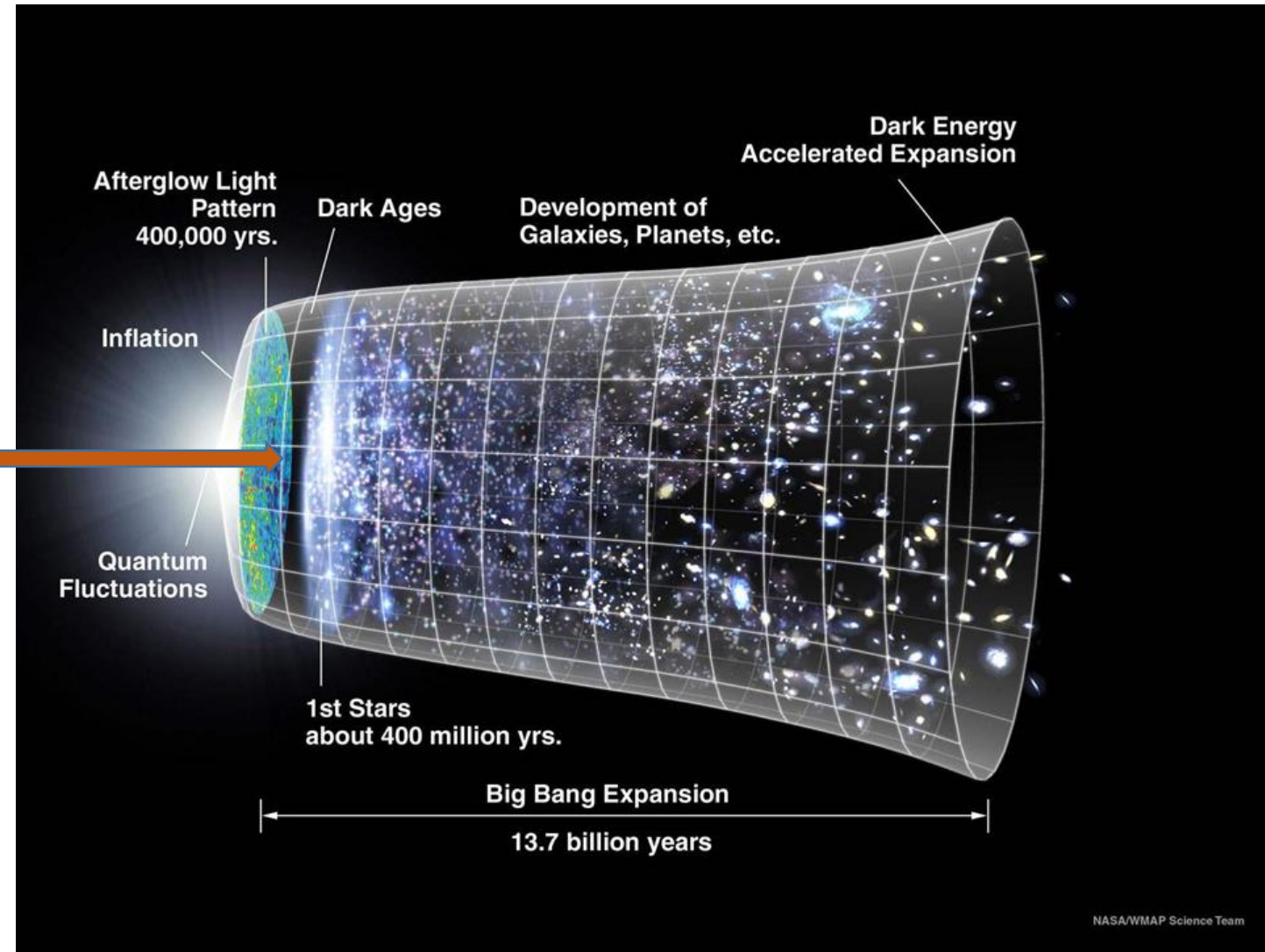
6th Egyptian School for HEP

Thermal History

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Google 'Cosmic History' → Images: Things Like

This talk



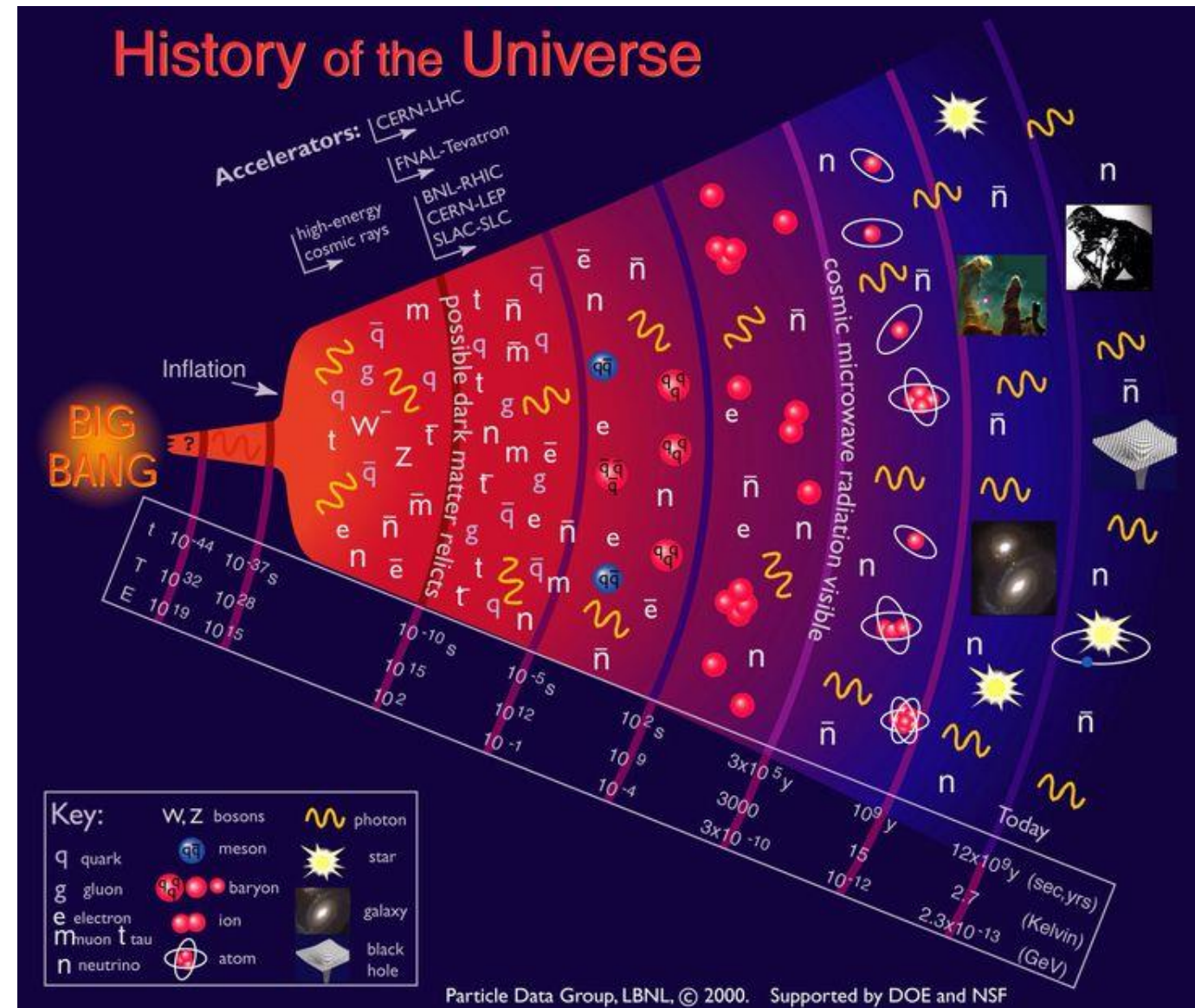
Subject Matter

- Our universe is expanding → Should have been ‘hot’ in the past
- As T rises:
 - Atoms ionize
 - Nuclei disassociate → individual protons neutrons → quarks-gluons
 - SM phase transitions (electroweak, QCD) expected. Others (GUT) predicted
- At some level universe is **testing ground for HEP**


mass


nuclei

Google some more: A **Thermal Bath** of **Particles and Antiparticles** that Leaves Relics



Tightly coupled, highly interacting, system

Couple of proper refs

Kolb & Turner: The Early Universe (standard text)

Daniel Baumann Tripos lectures Chapter 3
www.damtp.cam.ac.uk/user/db275/Cosmology.pdf
(which I follow to some extent)

The Cosmic Microwave Background

- Tells us of prior **thermal equilibrium**
- Current temperature of spectrum: **2.728 Kelvin**
- Current energy density of CMB:

$$(4\sigma/c)T^4 = 4.19 \times 10^{-14} \text{ J m}^{-3}$$

- The average energy per photon

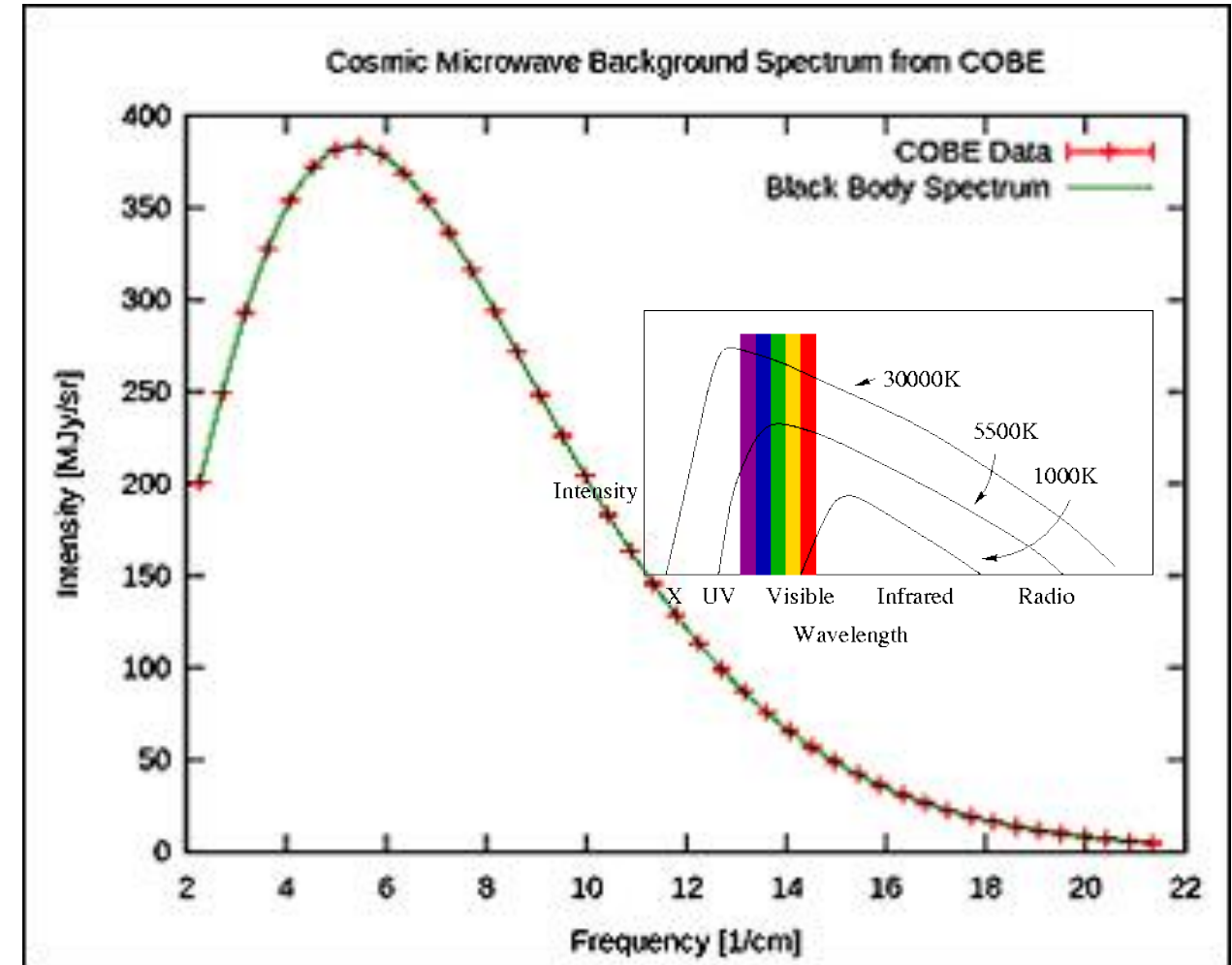
$$\sim kT \sim h\nu \quad (\text{since distn} \sim e^{-\frac{E}{kT}})$$

→ photon number density $\sim 10^8 \text{ m}^{-3}$

Compare with < one proton per cubic meter!

Entropy ~ large ratio; well conserved

→ in comoving vol



Units, rates (and ‘~convention’!)

- Using ‘**natural units**’: $c = \hbar = G = k_B = 1$
- Temperature, energy, momentum and mass are in electron volts
- Length and time are in inverse electron volts
- In these units, during radiation era gives

Expansion rate

$$H \sim T^2 / M_{\text{pl}}$$

Using Stefan-Boltzmann and $H \sim \sqrt{\rho}/M_{\text{pl}}$. law Natural units

The reduced Planck mass $M_{Pl} = \sqrt{\hbar/8\pi G}$

- Already twiddle ‘~’ sign reappearing!
- we will be making mainly order of magnitude (factor ten) estimates

Relativistic Degrees of Freedom g_*

$$\frac{T}{1 \text{ MeV}} \simeq 1.5 g_*^{-1/4} \left(\frac{1 \text{ sec}}{t} \right)^{1/2}$$

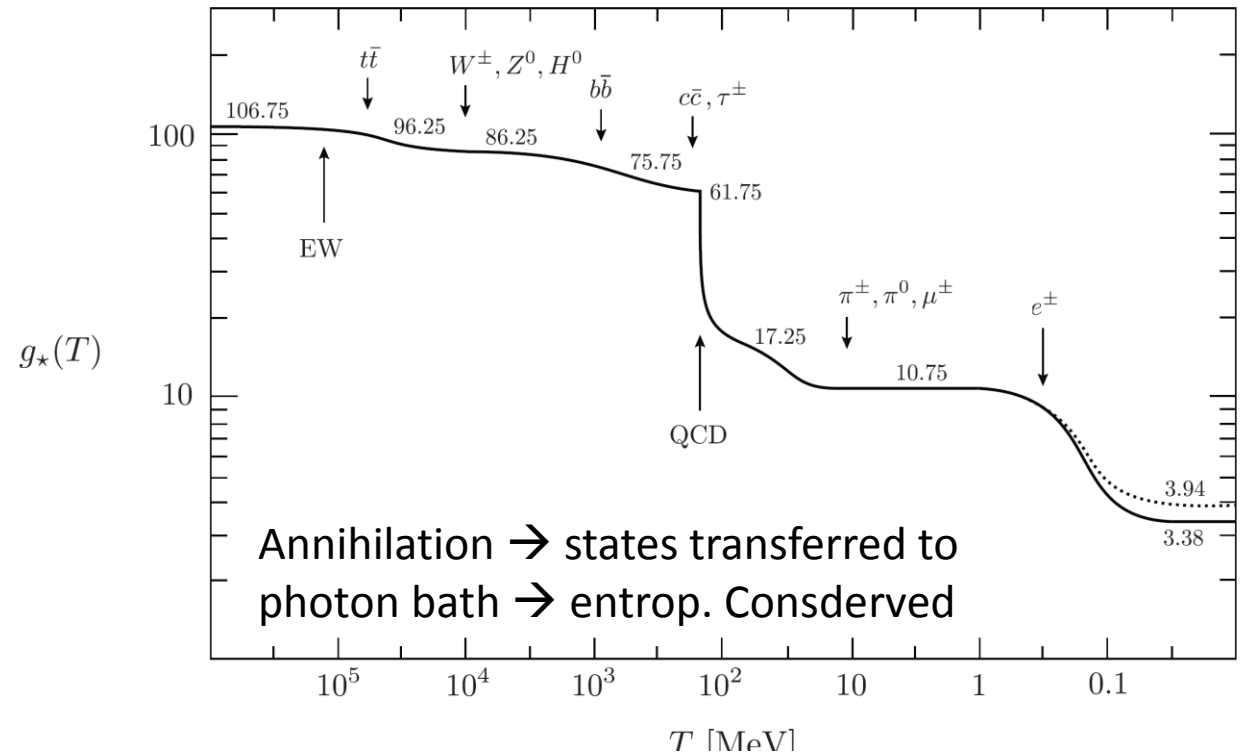
Expansion influenced by number of relativistic degrees of freedom (essentially number of species and their internal degrees of freedom; e.g. spin)

The total **energy density of relativistic species** is (using Stefan-Boltzmann again in natural units)

$$\rho_r = \sum_i \rho_i = \frac{\pi^2}{30} g_*(T) T^4$$

(similar relation for entropy $s \sim \rho/T$)

These act as 'radiation' with pressure $1/3 \rho$



A thermal particle is **relativistic** if $(m \ll T)$

A particle is in the thermal equilibrium if: **interaction rate** with thermal bath **> expansion rate**

Number densities in Thermal Equilibrium

- Spatially homogeneous system with phase space density $f(p) \rightarrow$

$$d n = g f(p) d p_x d p_y d p_z \rightarrow n = 4 \pi g \int f(p) p^2 d p$$

(isotropic momenta and number of internal deg. freed., e.g. spin, g)

$$f(p) \sim \frac{1}{e^{\frac{E(p)}{T}} \pm 1}$$

$$n = 4 \pi g \int_0^\infty d p \frac{p^2}{\exp [\sqrt{p^2 + m^2}/T] \pm 1}$$

Chemical equilib. \rightarrow particles are created – annihilated so as to keep these distn

\rightarrow

Non-relativistic parts \rightarrow more difficult to make \rightarrow lose out and suppressed

Relativistic

$(m \ll T)$

$$n \sim g T^3$$

Non-relativistic

$(m \gg T)$

$$n \sim g (mT)^{\frac{3}{2}} e^{-\frac{m}{T}}$$

\rightarrow As $T \rightarrow 0$ a massive particles should vanish... !

‘Normal matter’; should vanish; it’s existence suggests violations of baryon number and charge parity conservation

\rightarrow **Baryogenesis** through particle antipart asymmetry (probably BSM)

Era of Tightly Coupled Plasma

- Currently interaction rate of CMB photons with matter negligible, **but**
- As universe changes scale **a** \rightarrow

Number density of photons $n \sim \frac{1}{a^3} \sim T^3$

$$\rightarrow T \sim \frac{1}{a} \quad (\sim h \nu \sim 1/\lambda)$$

Back in time \rightarrow higher density and temperature \rightarrow universe ionised

*Number of neutral atoms (\sim Hydrogen) suppressed by
factor Boltzmann factor $e^{-\frac{B_H}{T}}$ ($B_H = 13.6$ eV is Hydrogen's binding energy)*

There are $\sim 10^9$ *photons per proton* $\rightarrow T_{\text{rec}} \sim 14/\ln 10^9 = 0.7$ eV (proper calc gives 0.3)

3600 Kelvin $\rightarrow a(\text{rec}) = 1/1300 \rightarrow z(\text{rec.}) = 1300 \rightarrow t(\text{rec}) \sim 300\,000$ yr for $a(t) = (t/t_0)^{2/3}$

Cosmic Plasma Coupling

- **Gas fully ionized** \rightarrow strongly interacts with photons by **Thompson scattering**:

- Electron placed in EM field $\rightarrow m_e \frac{d^2 z}{dt^2} = -e E_0 \sin(\omega t)$, \rightarrow oscillates

- radiates back $\frac{dP}{d\Omega} = \frac{e^4 E_0^2}{32\pi^2 \epsilon_0 c^3 m_e^2} \sin^2 \theta$.

Crosssection \sim power radiated / mean incident energy flux

\sim Square of classical electron radius $r_e = \frac{e^2}{4\pi \epsilon_0 m_e c^2} = 2.82 \times 10^{-15} \text{ m}$

$$\sigma_T \approx 2 \times 10^{-3} \text{ MeV}^{-2}$$

$$e^- + \gamma \leftrightarrow e^- + \gamma \quad \text{interaction rate} \quad \Gamma_\gamma \approx n_e \sigma_T \quad (\text{note relative vely } \sim c = 1 \text{ here!})$$

Interaction Rate of Coupled Plasma


- Electron dens. \sim Baryon dens $\sim 10^{-9}$ photon dens $\sim 0.1 T^3$

→

Photon electron Interaction rate at decoupling $\sim \sigma_T T_{dec}^3$

$$\underset{n}{\sim 10^{-10}} \cdot \underset{\sigma}{0.3^3 10^{-18}} \cdot 2 \cdot 10^{-3} \text{ MeV} = 10^{-10} \cdot 0.3^3 10^{-18} \cdot 2 \cdot 10^{-15} \text{ eV}$$

$$\text{Interaction Time} \sim 2 \cdot 10^{26} \text{ eV}^{-1} \sim 1.4 \cdot 10^{11} \text{ s} \sim 4400 \text{ years} \quad (<< \text{age of uni at recom.})$$

 $6.582119 \times 10^{-16} \text{ s}$

→ Timescale for interaction much smaller than age of universe

→ Plasma tightly coupled in (kinetic) equilib. Before recom.

Similar process of binding in QCD phase trans. And BBN

Rough rule of thumb for equilibrium:

Interaction rate > expansion rate (interaction time < age of universe)

Neutrino Decoupling

- Neutrinos are coupled to electrons through **weak interactions**
→ Much looser than Thompson coupling → **early decoupling**

Below electroweak scale (~ 100 GeV) but
In relativistic limit → cross section

(‘four Fermion’ interaction)

$$\sigma \sim \left| \begin{array}{c} \diagup \quad \diagdown \\ \diagdown \quad \diagup \end{array} \right|^2 \sim G_F^2 T^2$$

$$G_F \sim \alpha / M_W^2 \sim 1.17 \times 10^{-5} \text{ GeV}^{-2}$$

Neutrinos thus decouple at
$$\frac{\Gamma}{H} \sim \frac{\alpha^2 M_{\text{pl}} T^3}{M_W^4} \sim \left(\frac{T}{1 \text{ MeV}} \right)^3 \quad (\text{recall } H \sim T^2 \text{ in rad era})$$

→ When scales ~ 3 million times smaller than recombination ~ 1 s after start of expansion

Cosmological Element Production (BBN)

- Elements beyond hydrogen need neutrons, these are in equilibrium with protons before weak scale freeze out

Post QCD

$$\begin{array}{l} n + \nu_e \leftrightarrow p^+ + e^- \\ n + e^+ \leftrightarrow p^+ + \bar{\nu}_e \end{array} \rightarrow \left(\frac{n_n}{n_p} \right)_{\text{eq}} = e^{-Q/T} \quad Q \equiv m_n - m_p = 1.30 \text{ MeV}.$$

At Freeze out (1 MeV) neutron fraction $\sim 1/6$ ++ decay $\sim 1/8$

Elements cannot form until Boltzmann suppression $\sim 10^{-9} e^{\frac{B_E}{T}}$ overcome

Virtually all neutrons go to Helium \rightarrow abundance $\sim 1/16 \rightarrow$ by mass $1/4$

Heavier elements absent due to low densities (process ends after three min...)

Of BBN and BSM

****Dependence on baryon dens. →**

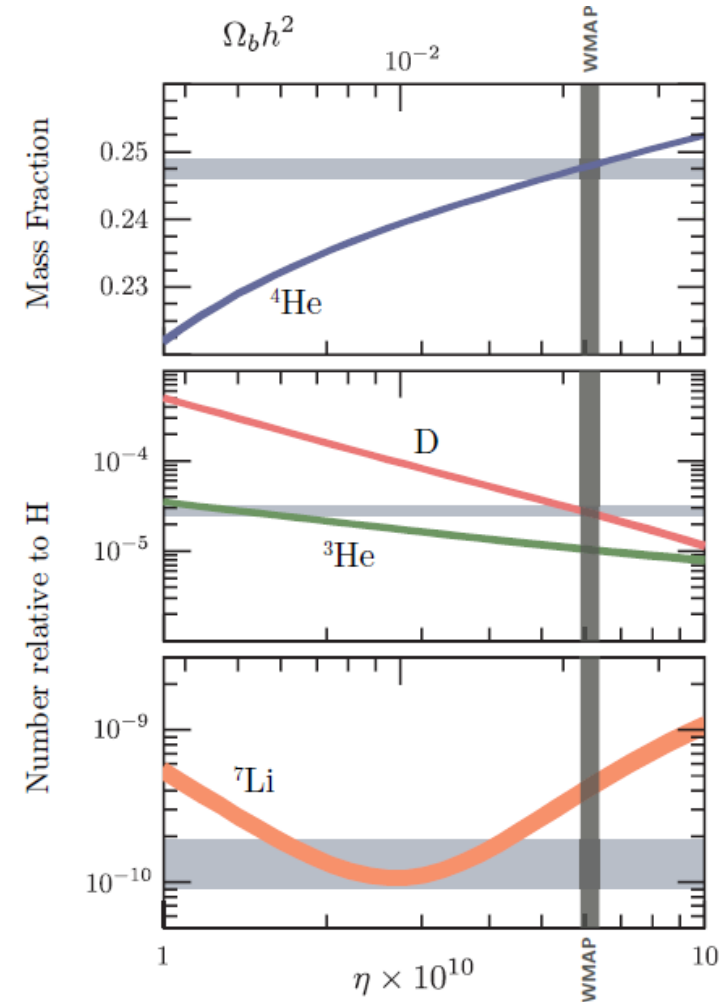
Non-Baryonic Dark Matter dominant

**** Dependence on expansion rate →**
number of relativistic species (with $m \ll T$)
(Recall the expansion rate $H^2 \sim \rho \sim g_*$)

→ puts bounds on neutrino species
(and any other relativistic species prior to $T \sim \text{MeV}$)

****Places constraints on G and G_F at early times**

++ Constraints on non-standard cosmology



Vertical line Baryon fraction $\sim 5\%$

What Then is the DM: A WIMP Miracle?

- Assume DM is composed of weakly interacting massive particles
- Mass of order 100 proton mass ~ 1 GeV, consistent with BSM models

Rough feasibility estimate

Freeze out at **interaction rate** \sim **expansion rate**

Recall for neutrinos this gave $\frac{\Gamma}{H} \sim \frac{\alpha^2 M_{\text{pl}} T^3}{M_W^4} \sim \left(\frac{T}{1 \text{ MeV}} \right)^3$

Density of DM $\sim 1/20$ baryon density for ~ 100 GeV particle

++ baryons less dense than neutrinos by a factor 10^{-9}

And in non relativistic lim $\sigma \rightarrow \text{const}$

\rightarrow T of non-relativistic relic $n \sigma \sim 10^{-10} T^3 \sigma \sim \frac{T^2}{M_{\text{pl}}} \rightarrow$

$T_{\text{dec}} \sim 10^{10} \sigma^{-1} M_{\text{pl}}^{-1} \sim \text{few GeV for } \sigma \sim 10^{-8} \text{ GeV}^{-2} \rightarrow \text{characteristic of weak interaction...}$

The Miracle **more precisely**

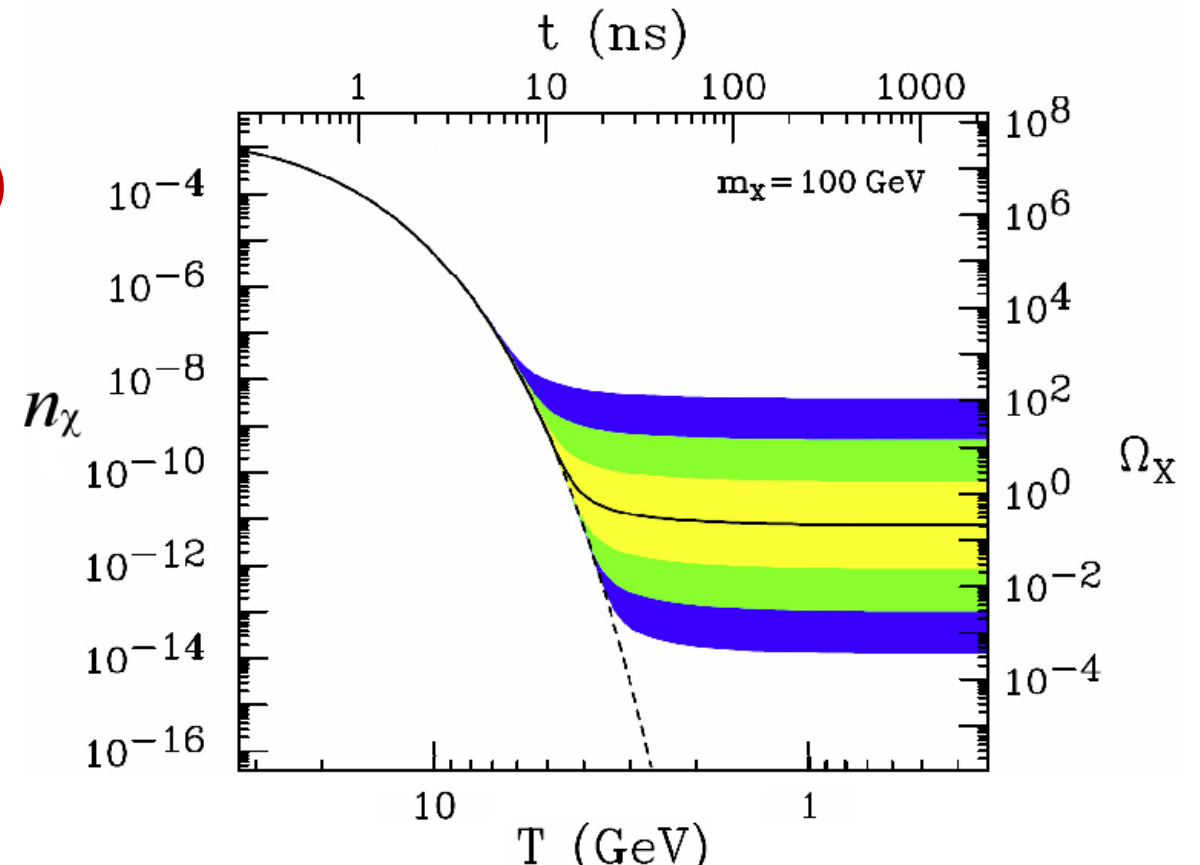
- Use Boltzmann equation for *comoving* number density

$$\frac{dN_X}{dt} = -s\langle\sigma v\rangle\left[N_X^2 - (N_X^{\text{eq}})^2\right]$$

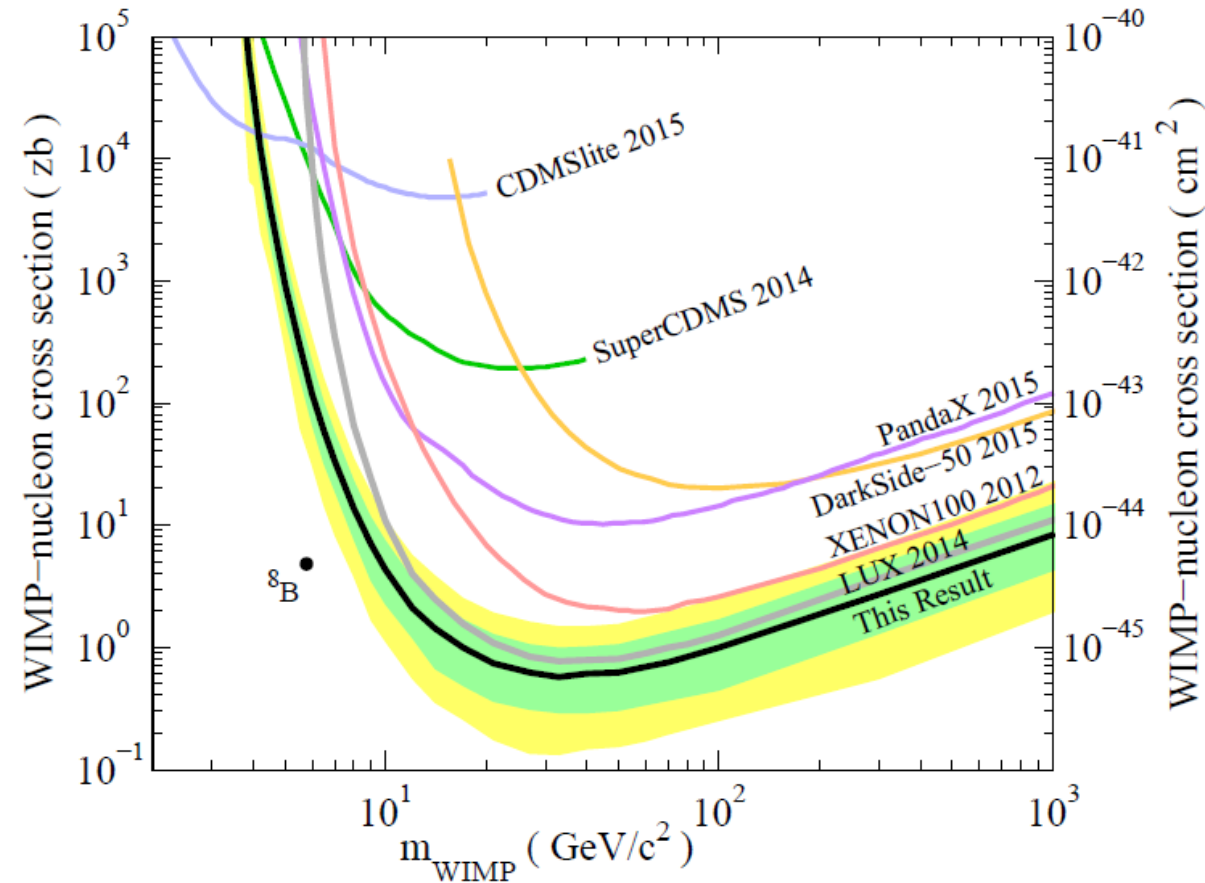
- The **equilibrium** abundance is Boltzmann suppressed

(Recall non-relativistic $n \sim g (mT)^{\frac{3}{2}} e^{-\frac{m}{T}}$)

- **It is suppressed in the right way** →
proper abundance for weak decoupling



Nevertheless...



Direct detection constraints from Akerib et. al. (2016)

$$\text{Cm}^2 \sim 4 * 10^{-28} \text{ GeV}^{-2}$$

Experimental constraints → WIMP miracle wither away?

(Also appears withering at LHC...)

Some Alternatives

- Sterile neutrinos (can be produced from oscillations with regular ones)

→ 'Warm dark matter' in keV range

- Axions (introduced to solve CP violation problem in QCD re neutron's electric dipole moment)

→ Tiny mass but dynamical friction effect leads to similar behavior as cold dark matter

- Non-thermal production of WIMPS or WDM

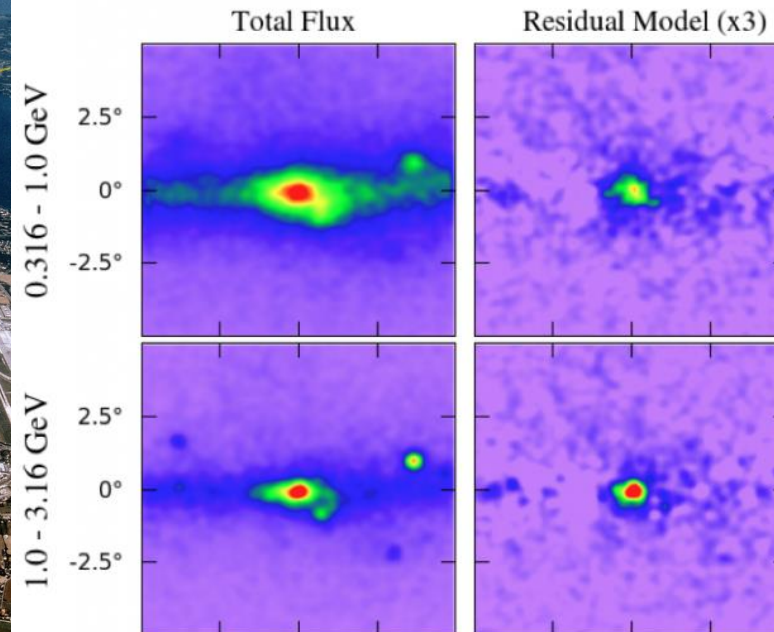
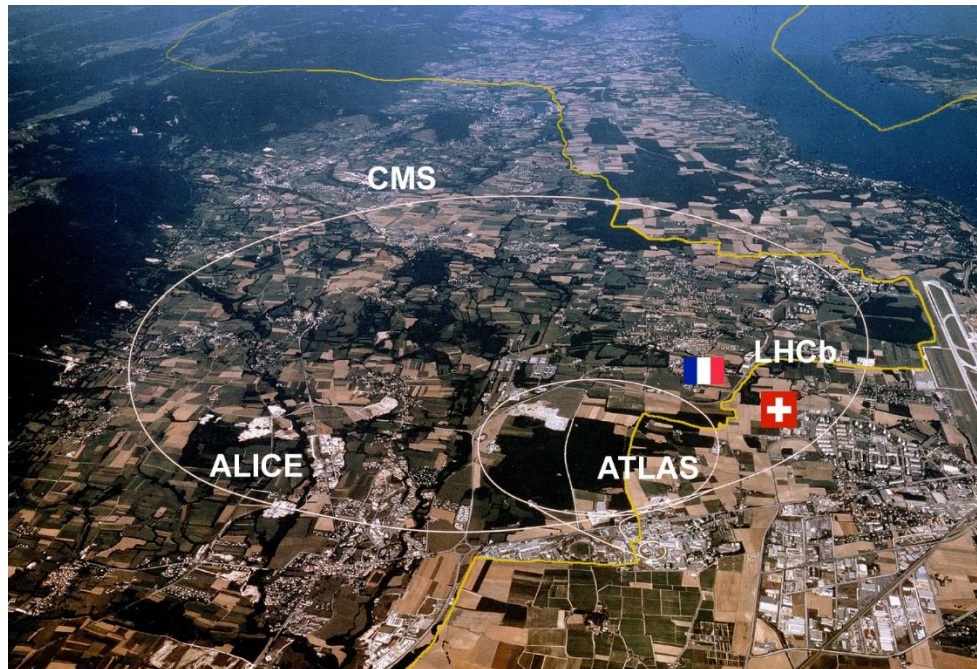
e.g., from direct decay of Inflaton like field → escapes thermal constraints if equilibrium is not established (e.g., produced after T_{decoup} .)

This is normally accompanied by 'entropy production' (decay of field into relativistic particles) which can adjust expansion rate and thus the DM abundance (diluting it)

→ Constrained by BBN and CMB

Searching for Dark Matter

- Detection experiments (DM in the room!)
- LHC (at CERN)
- Annihilation Signals (in the sky)



Overview of Evolution

Event	time t	redshift z	temperature T
Inflation	10^{-34} s (?)	–	–
Baryogenesis	?	?	?
EW phase transition	20 ps	10^{15}	100 GeV
QCD phase transition	$20 \mu\text{s}$	10^{12}	150 MeV
Dark matter freeze-out	?	?	?
Neutrino decoupling	1 s	6×10^9	1 MeV
Electron-positron annihilation	6 s	2×10^9	500 keV
Big Bang nucleosynthesis	3 min	4×10^8	100 keV
Matter-radiation equality	60 kyr	3400	0.75 eV
Recombination	260–380 kyr	1100–1400	0.26–0.33 eV
Photon decoupling	380 kyr	1000–1200	0.23–0.28 eV
Reionization	100–400 Myr	11–30	2.6–7.0 meV
Dark energy-matter equality	9 Gyr	0.4	0.33 meV
Present	13.8 Gyr	0	0.24 meV

From lecture notes by Daniel Baumann

