

# Assessing the Higgs (self-)couplings

*"What's going on at the weak scale"*  
CERN-CKC workshop, Jeju island, June 3, 2017



*Christophe Grojean*

DESY (Hamburg)  
Humboldt University (Berlin)

( [christophe.grojean@desy.de](mailto:christophe.grojean@desy.de) )

# This talk is based upon...

## A global view on the Higgs self-coupling

---

S. Di Vita,<sup>a</sup> C. Grojean,<sup>1a,b</sup> G. Panico,<sup>c</sup> M. Riembau,<sup>a,c</sup> T. Vantalon<sup>a,c</sup>

<sup>a</sup> DESY, Notkestraße 85, D-22607 Hamburg, Germany

<sup>b</sup> Institut für Physik, Humboldt-Universität zu Berlin, D-12489 Berlin, Germany

<sup>c</sup> IFAE, Barcelona Institute of Science and Technology (BIST) Campus UAB, E-08193 Bellaterra, Spain

E-mail: [stefano.divita@desy.de](mailto:stefano.divita@desy.de), [christophe.grojean@desy.de](mailto:christophe.grojean@desy.de),  
[gpanico@ifae.es](mailto:gpanico@ifae.es), [marc.riembau@desy.de](mailto:marc.riembau@desy.de), [tvantalon@ifae.es](mailto:tvantalon@ifae.es)

arXiv:1704.01953v1 [hep-ph]

## The leptonic future of the Higgs

Gauthier Durieux,<sup>a</sup> Christophe Grojean,<sup>a,b</sup> <sup>1</sup> Jiayin Gu,<sup>a,c</sup> Kechen Wang<sup>a,c</sup>

<sup>a</sup> DESY, Notkestraße 85, D-22607 Hamburg, Germany

<sup>b</sup> Institut für Physik, Humboldt-Universität zu Berlin, D-12489 Berlin, Germany

<sup>c</sup> Center for Future High Energy Physics, Institute of High Energy Physics,  
Chinese Academy of Sciences, Beijing 100049, China

[gauthier.durieux@desy.de](mailto:gauthier.durieux@desy.de), [christophe.grojean@desy.de](mailto:christophe.grojean@desy.de), [jiayin.gu@desy.de](mailto:jiayin.gu@desy.de), [kechen.wang@desy.de](mailto:kechen.wang@desy.de)

arXiv:1704.02333v1 [hep-ph]

and on-going work with

N. Craig, S. Di Vita, G. Durieux, C. Grojean, J. Gu, Z. Liu, G. Panico, M. Riembau, T. Vantalon

**see also**

Gorbahn et al '16  
arXiv:1607.03773 [hep-ph]

Degrassi et al '16  
arXiv:1607.04251 [hep-ph]

Bizon et al '16  
arXiv:1610.05771 [hep-ph]

# How to report Higgs data: from $\kappa$ to EFT

LHCHSWG '12

M. Zuckerberg created FaceMash before Facebook

J.K. Rowling got rejected 12 times by editors before she published Harry Potter

Beyonce wrote hundreds of songs before 'Halo'

... Physicists used signal strengths to report Higgs data before ...

one doesn't have to succeed on the first try  
“the success comes from the freedom to fail”

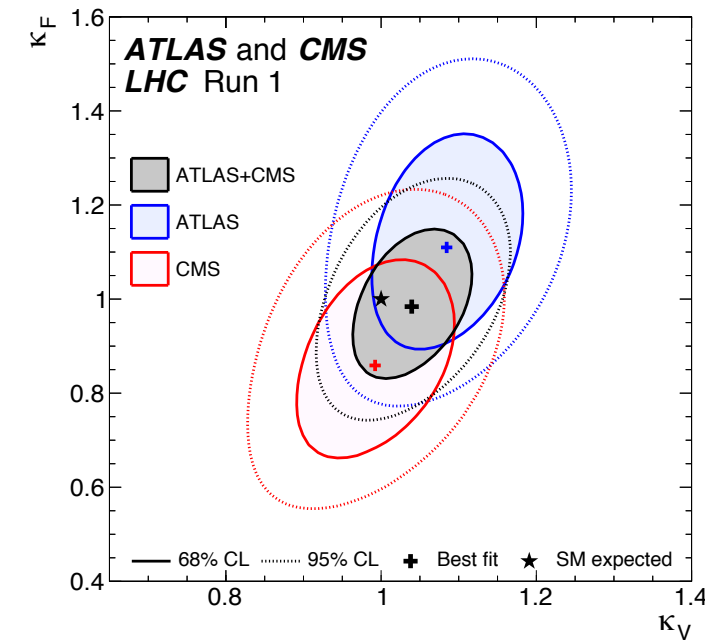
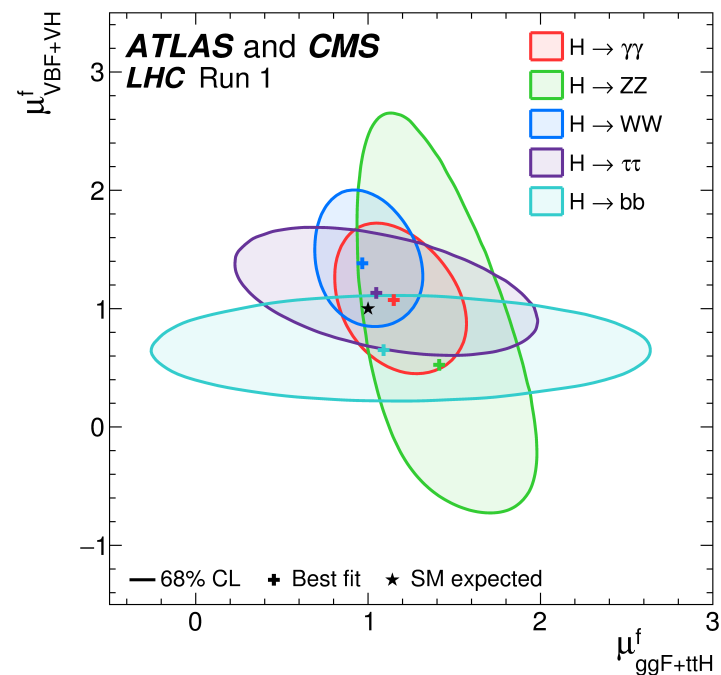
M. Zuckerberg, Harvard graduation ceremony speech, May 25, 2017

# How to report Higgs data: from $\kappa$ to EFT

LHCHSWG '12

$$\mu_i = \frac{\sigma[i \rightarrow h]}{(\sigma[i \rightarrow h])_{\text{SM}}}$$

$$\mu_f = \frac{\text{BR}[h \rightarrow f]}{(\text{BR}[h \rightarrow f])_{\text{SM}}}$$

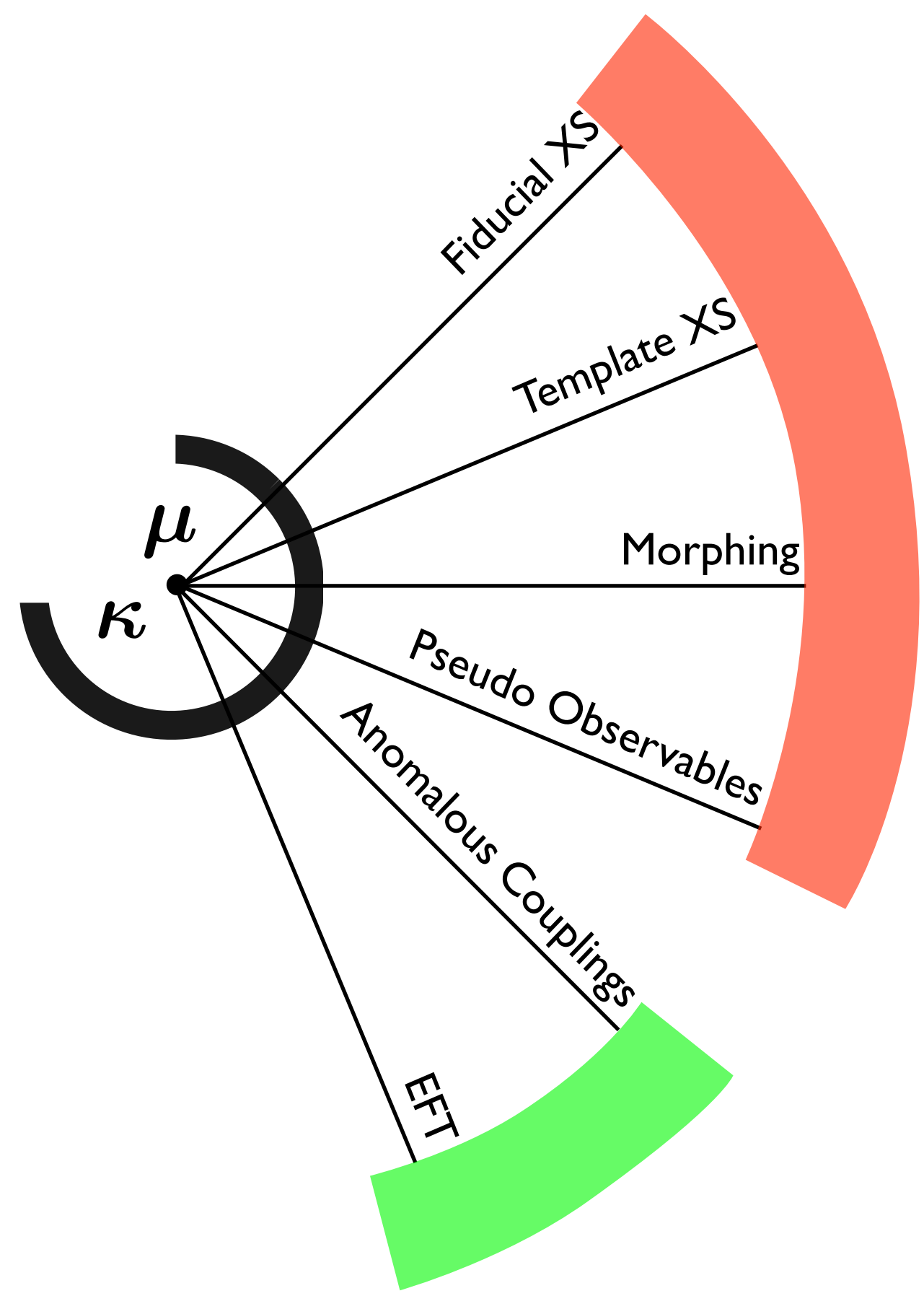


$$(\sigma \cdot \text{BR})(gg \rightarrow H \rightarrow \gamma\gamma) = \sigma_{\text{SM}}(gg \rightarrow H) \cdot \text{BR}_{\text{SM}}(H \rightarrow \gamma\gamma) \cdot \frac{\kappa_g^2 \cdot \kappa_\gamma^2}{\kappa_H^2}$$

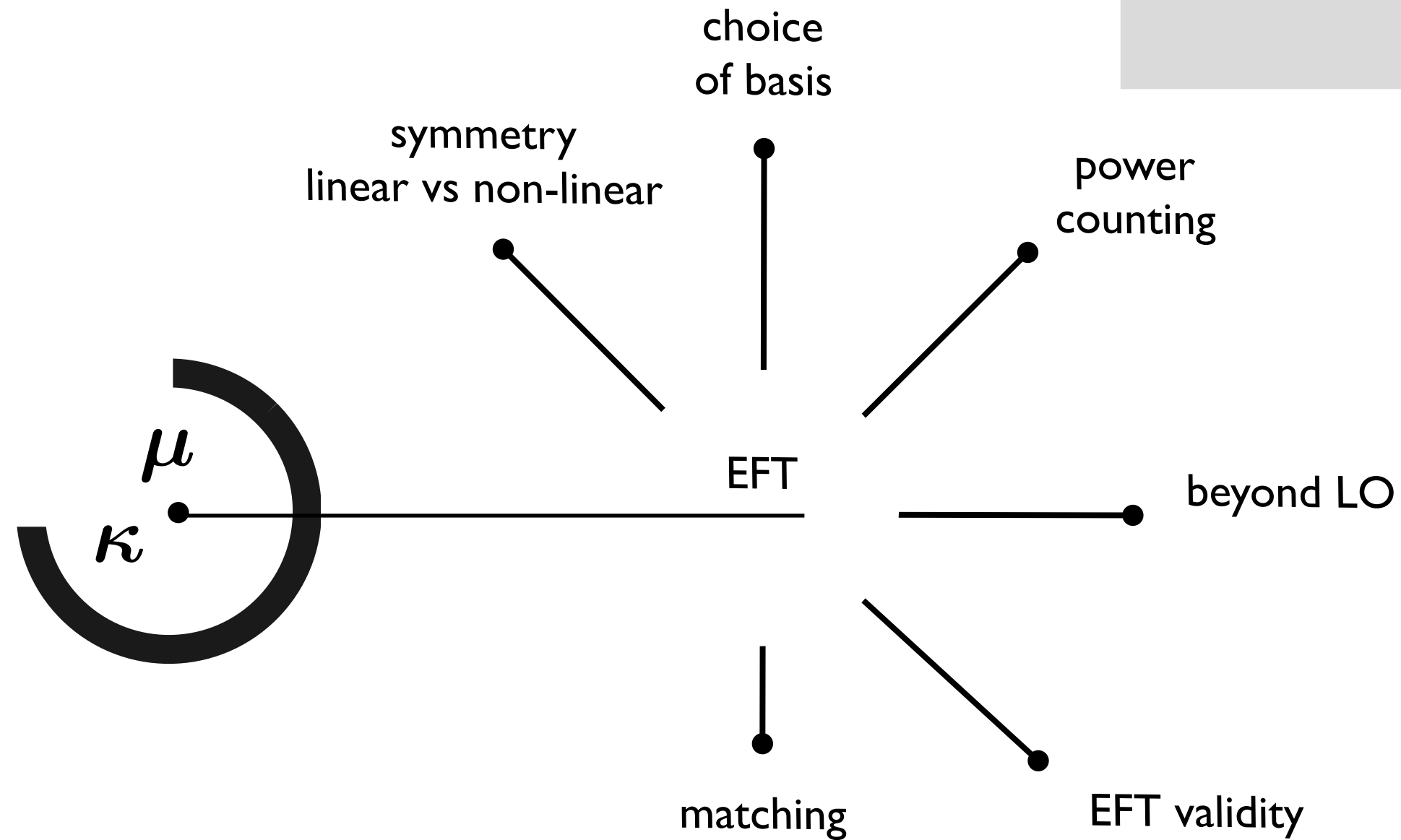
**individual coupling rescaling factors**

Well suited parametrization for inclusive measurements  
but doesn't do justice to full possible deformations of SM & other rich diff. information

# EFT



# EFT



## Pros:

- ▶ correlations between different channels/observables
- ▶ combination of measurements at different energies  
e.g. EW precision data and Higgs measurements
- ▶ test of self-consistency



## unique to EFT

allow to focus on channels yet unconstrained and more likely to offer new discovery opportunities

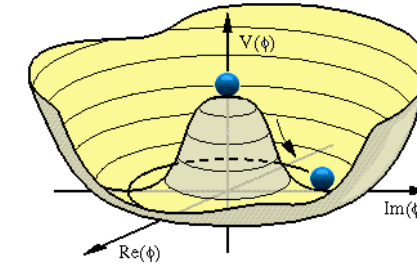
# Higgs physics vs BSM

(assuming EW symmetry linearly realized and that new physics is heavy)

Several deformations away from the SM affecting Higgs properties are already probed in the vacuum

$$\phi = v+h$$

vacuum



Potentially new BSM-effects in h physics could have been already tested in the vacuum

e.g.

$$= \frac{1}{2v} \times$$

(assuming that the Higgs boson is part of a doublet)

$$H^\dagger D_\mu H \bar{f} \gamma^\mu f$$

Modifications in  $h \rightarrow Zff$  related to  $Z \rightarrow ff$

consistency check  
not discovery mode



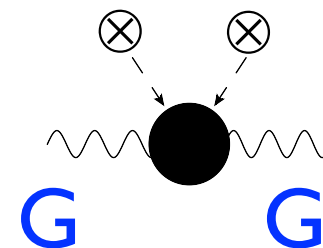
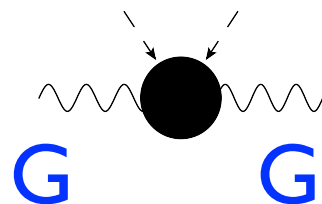
One can use  $h \rightarrow ZZ \rightarrow 4l$  to probe this deformation but hard time to compete with LEP bounds

courtesy of A. Pomarol@Moriond2014

# Higgs/BSM Primaries

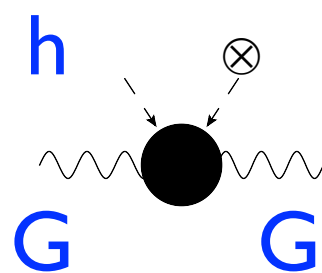
There are others deformations away from the SM that are harmless in the vacuum and need a Higgs field to be probed

e.g. 
$$\frac{1}{g_s^2} G_{\mu\nu}^2 + \frac{|H|^2}{\Lambda^2} G_{\mu\nu}^2 \rightarrow \left( \frac{1}{g_s^2} + \frac{v^2}{\Lambda^2} \right) G_{\mu\nu}^2$$



operator  
not visible in the vacuum  
(redefinition of input parameter)

But can affect h physics:



affects  $GG \rightarrow h!$

operator  
visible in Higgs physics

(courtesy of A. Pomarol@HiggsHunting2014)



# Higgs/BSM Primaries

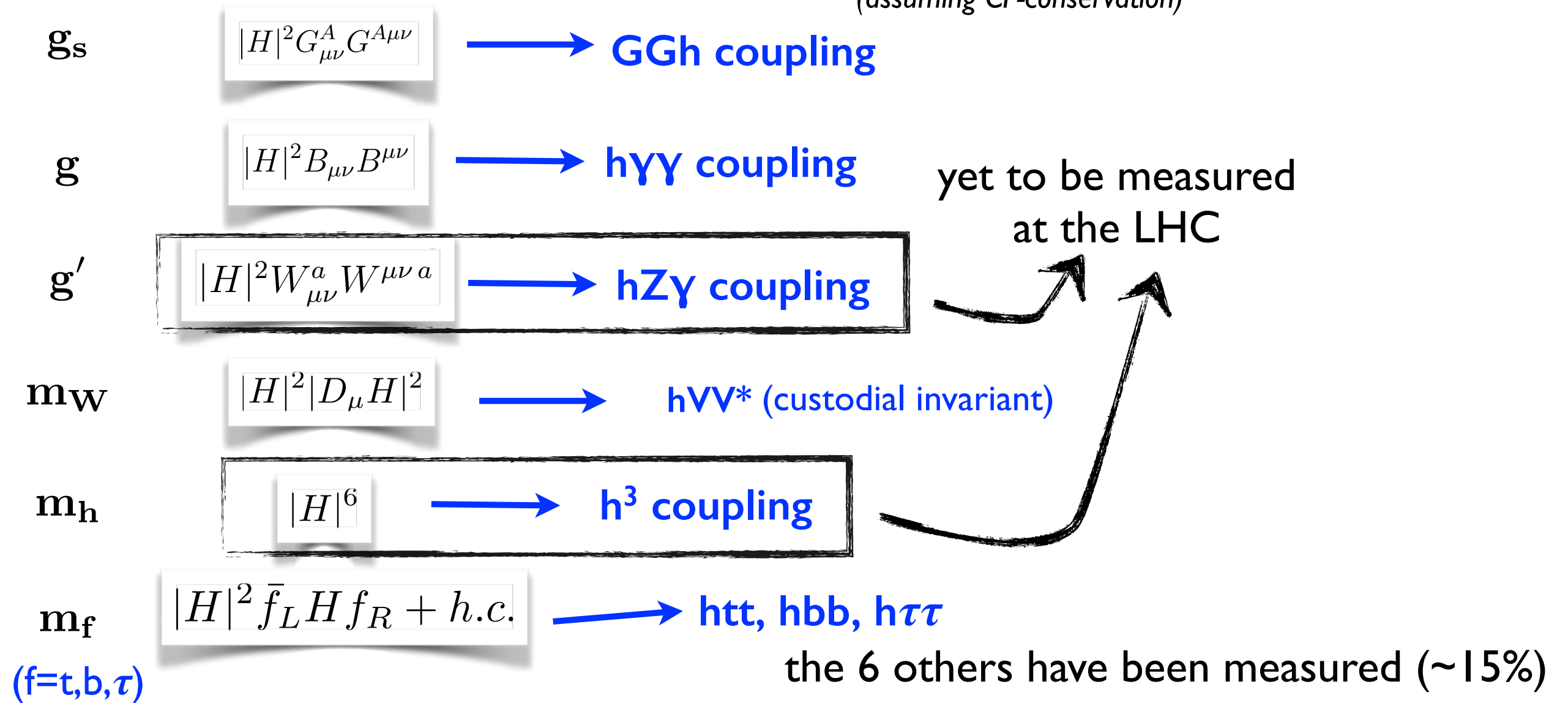
Pomarol, Riva '13

Elias-Miro et al '13

Gupta, Pomarol, Riva '14

How many of these effects can we have?

As many as parameters in the SM: **8** for one family  
(assuming CP-conservation)



(courtesy of A. Pomarol@HiggsHunting2014)

# Higgs/BSM Primaries

Pomarol, Riva '13

Elias-Miro et al '13

Gupta, Pomarol, Riva '14

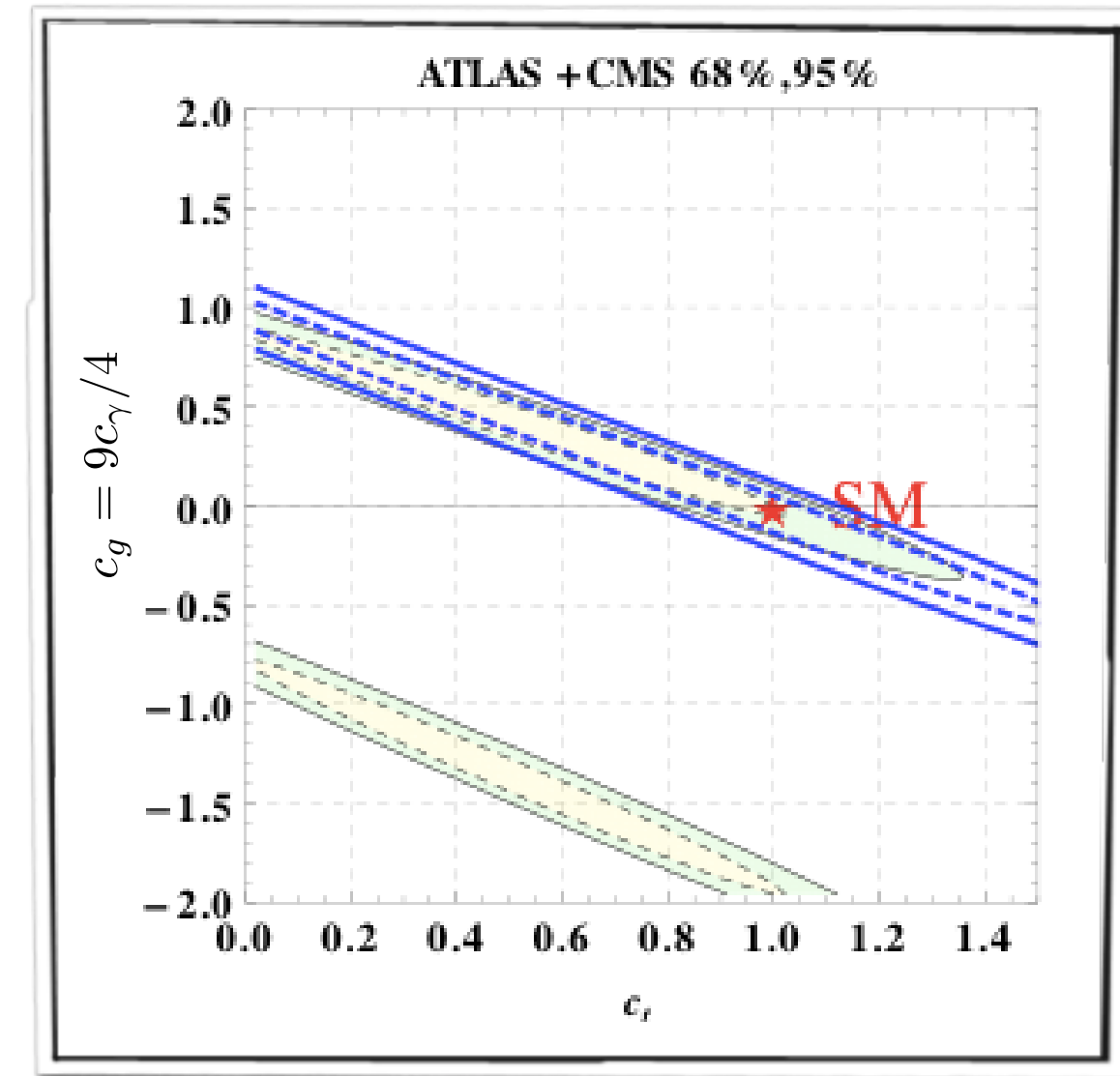
Almost a 1-to-1 correspondence with the 8  $\kappa$ 's in the Higgs fit

Coupling	300 fb <sup>-1</sup> Theory unc.:			3000 fb <sup>-1</sup> Theory unc.:		
	All	Half	None	All	Half	None
$\kappa_Z$	8.1%	7.9%	7.9%	4.4%	4.0%	3.8%
$\kappa_W$	9.0%	8.7%	8.6%	5.1%	4.5%	4.2%
$\kappa_t$	22%	21%	20%	11%	8.5%	7.6%
$\kappa_b$	23%	22%	22%	12%	11%	10%
$\kappa_\tau$	14%	14%	13%	9.7%	9.0%	8.8%
$\kappa_\mu$	21%	21%	21%	7.5%	7.2%	7.1%
$\kappa_g$	14%	12%	11%	9.1%	6.5%	5.3%
$\kappa_\gamma$	9.3%	9.0%	8.9%	4.9%	4.3%	4.1%
$\kappa_{Z\gamma}$	24%	24%	24%	14%	14%	14%

Atlas projection

With some important differences:

- 1) width hypothesis built-in
- 2)  $\kappa_W/\kappa_Z$  is not a primary (constrained by  $\Delta\rho$  and TGC)
- 3)  $\kappa_g, \kappa_\gamma, \kappa_{Z\gamma}$  do not separate UV and IR contributions



Azatov '15

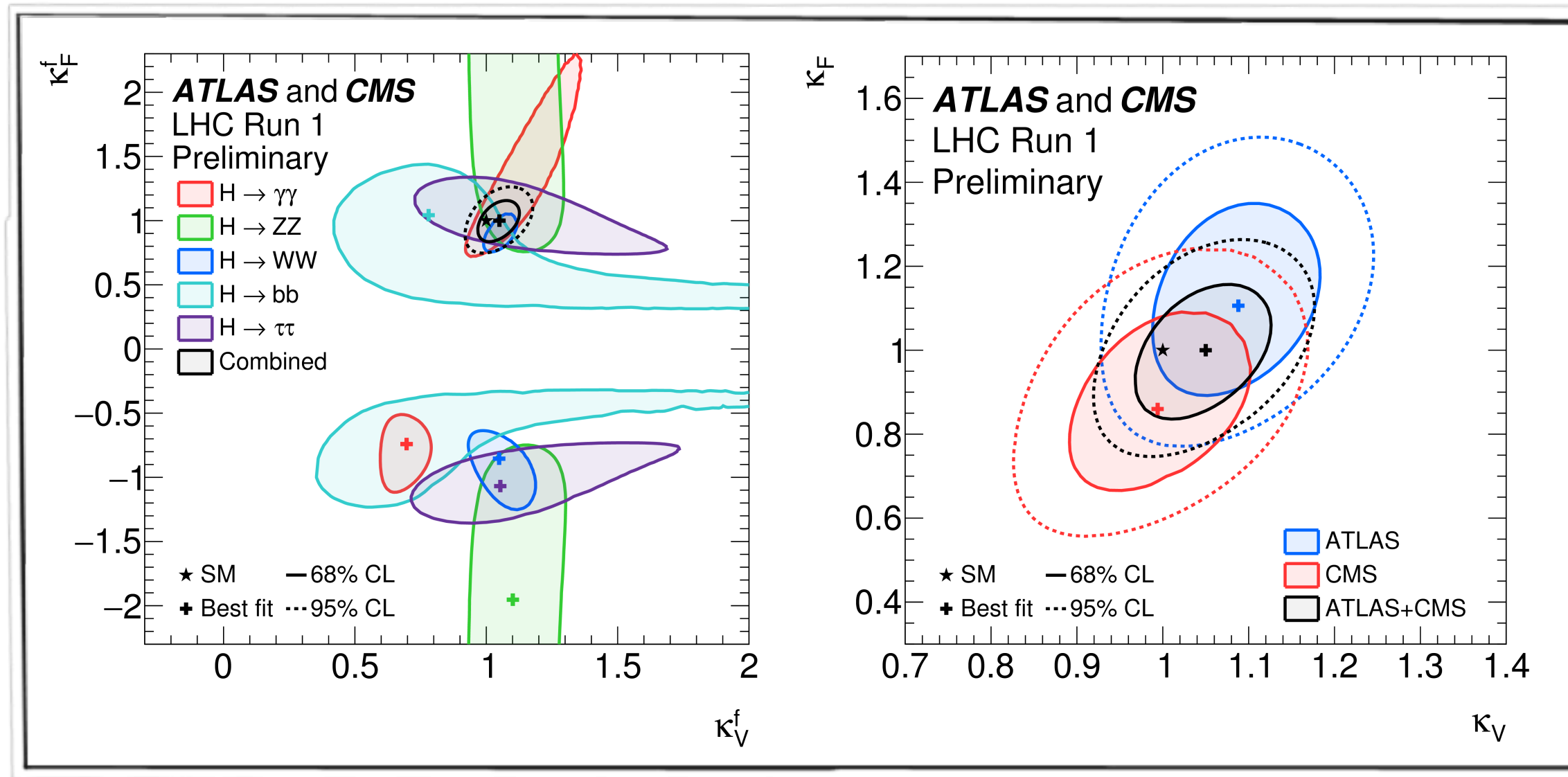
the 6 others have been measured (~15%) up to a flat direction between between the top/gluon/photon couplings

(courtesy of A. Pomarol@HiggsHunting2014)

# Why going beyond inclusive Higgs processes?

So far the LHC has mostly produced Higgses on-shell  
in processes with a characteristic scale  $\mu \approx m_H$

access to Higgs couplings @  $m_H$



# Why going beyond inclusive Higgs processes?

So far the LHC has mostly produced Higgses on-shell  
in processes with a characteristic scale  $\mu \approx m_H$

  
access to Higgs couplings @  $m_H$

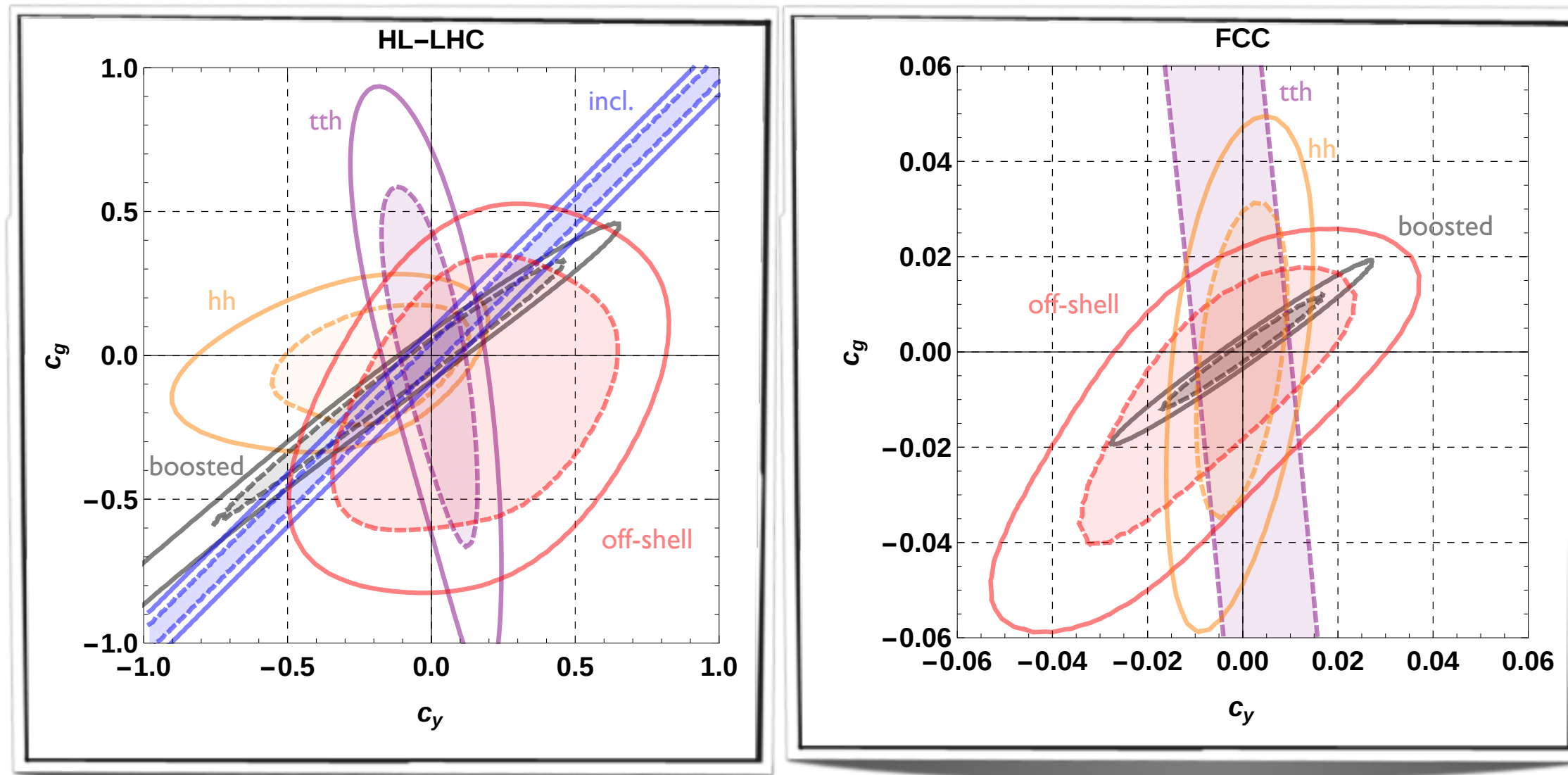
Producing a Higgs with boosted additional particle(s)  
probe the Higgs couplings @ large energy  
(important to check that the Higgs boson ensures perturbative unitarity)

Examples of interesting channels to explore further:

1. off-shell  $gg \rightarrow h^* \rightarrow ZZ \rightarrow 4l$
2. boosted Higgs: Higgs+ high- $p_T$  jet
3. double Higgs production

# Why going beyond inclusive Higgs processes?

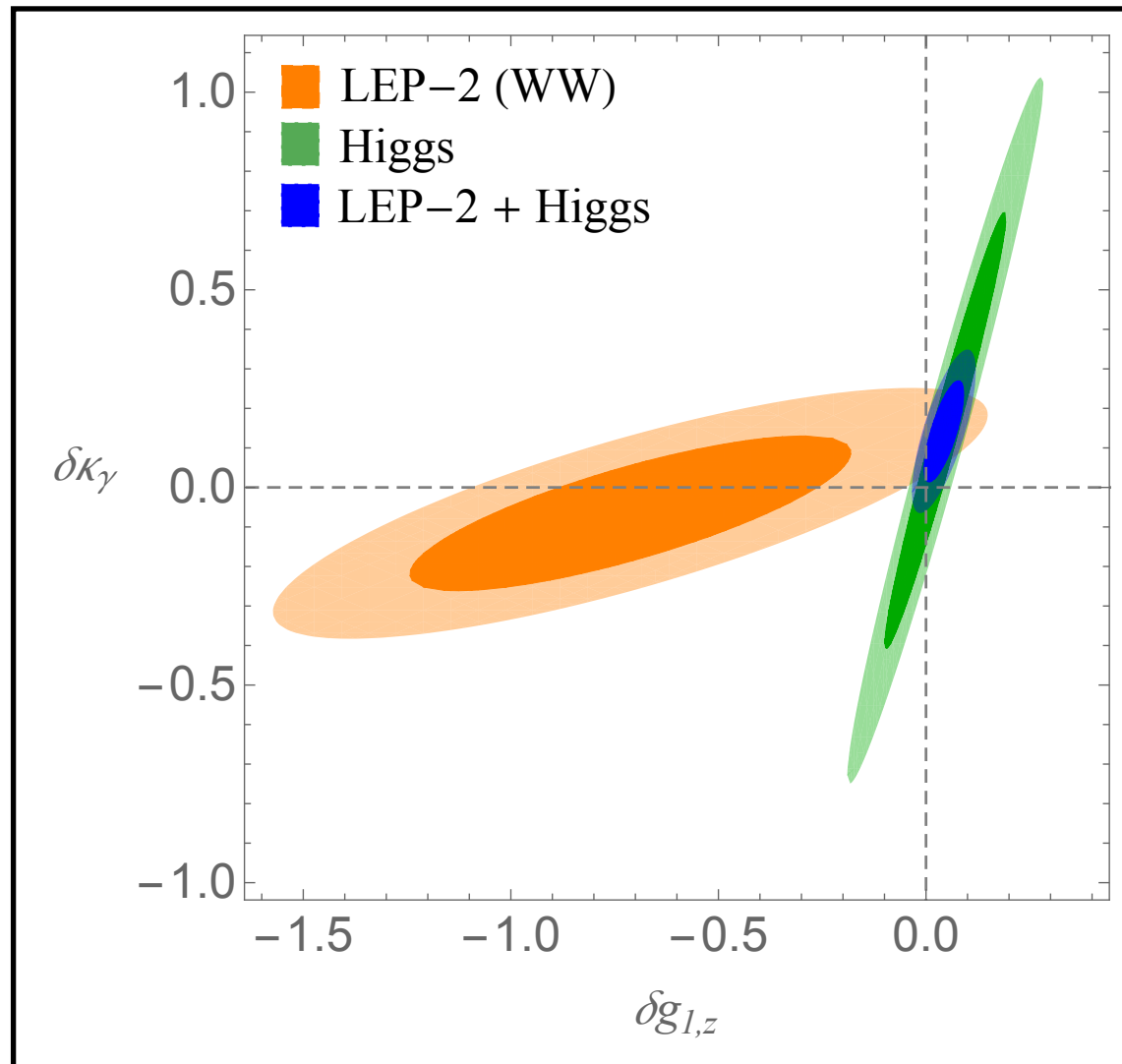
So far the LHC has mostly produced Higgses on-shell  
in processes with a characteristic scale  $\mu \approx m_H$



Azatov, Grojean, Paul, Salvioni '16

# Synergy Higgs and diboson

Falkowski et al '15



(TGC+Higgs) > (TGC)  $\cup$  (Higgs)

In EFT<sub>(dim-6)</sub>

8 deformations affecting Higgs physics alone  
2 deformations affecting Higgs and diboson data

diboson (1%) are a priori more constraining than Higgs (10%)

Is there any value in doing a global fit?

Strong correlations between 2 data sets

**Better to do a (8+2) parameter fit!**

Impact of HL-LHC WW data?

we assumed 1% syst. and also studied the impact of this assumption

# One missing beast: $h^3$

## The Higgs self-couplings plays important roles

- 1) controls the **stability** of the EW vacuum
- 2) dictates the dynamics of EW **phase transition** and potentially conditions the generation of a matter-antimatter asymmetry via **EW baryogenesis**

## Does it need to be measured with high accuracy?

difficult to design new physics scenarios that dominantly affect the Higgs self-couplings and leave the other Higgs coupling deviations undetectable

## Higgs self-coupling prospects

M. Son, Washington '15

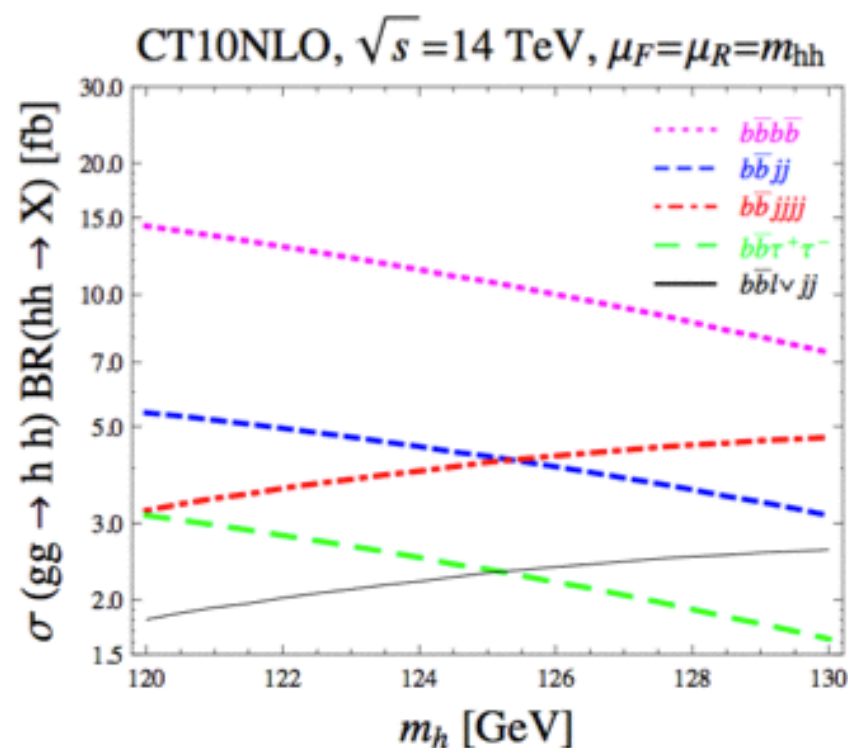
	HL LHC 3/ab	ILC/CLIC	FCC 100TeV
Precision on $\lambda_{HHH}$	$b\bar{b}\gamma\gamma$ : poor, only $\sim O(1)$ determination Other channels: needs more detailed studies	ILC <ul style="list-style-type: none"> <li>• DHS alone at 500 GeV and 1TeV gives only <math>\sim O(1)</math> determination</li> <li>• <math>\sim 28\%</math> via VBF at 1TeV, 1/ab</li> </ul> CLIC at 3TeV, 2/ab <ul style="list-style-type: none"> <li>• <math>\sim 12\%</math> via VBF</li> </ul>	$b\bar{b}\gamma\gamma$ : golden channel. 5-10% determination might be possible with 30/ab. $\sim 3x$ less sensitivity with 3/ab
Comments	Combining various channels might be important	The role of VBF is important High CM energy and high luminosity are crucial	Improvements on heavy flavor tagging, fakes, mass resolution etc are crucial to achieve our goal

# h<sup>3</sup> from hh@LHC

Measuring this small cross section in an inclusive search is very challenging at the HL-LHC: compromise between branching ratio and cleanliness of the signal

M. Spannowsky, Mainz '15

Channel	BR (%)	Events/3 ab
<i>bbWW</i>	24.7	30000
<i>bbττ</i>	7.3	9000
<i>WWWW</i>	4.3	5200
<i>bbγγ</i>	0.27	330
<i>bbZZ</i> (→ e <sup>+</sup> e <sup>-</sup> μ <sup>+</sup> μ <sup>-</sup> )	0.015	19
<i>γγγγ</i>	0.00052	1

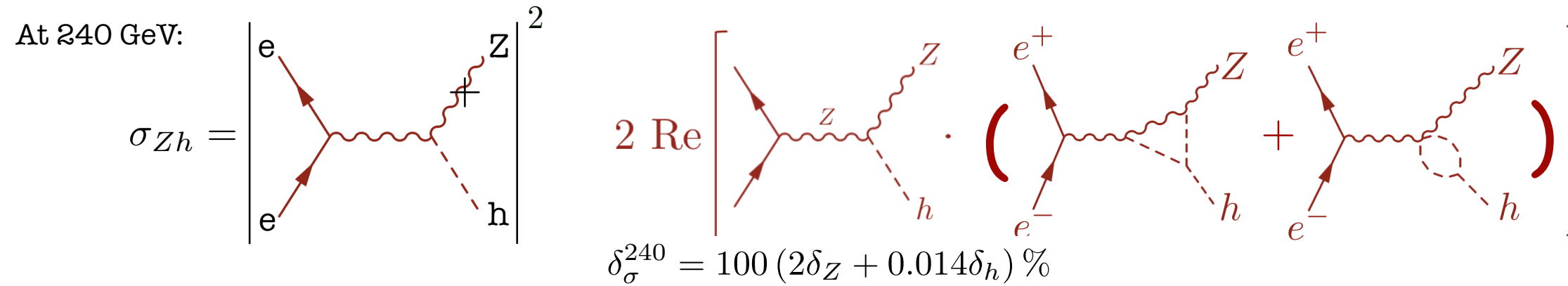


Decay	Issues	Expectation 3000 ifb	References
<i>b<math>\bar{b}</math>γγ</i>	<ul style="list-style-type: none"> <li>• Signal small</li> <li>• BKG large &amp; difficult to asses</li> <li>• Simple reconst.</li> </ul>	$S/B \simeq 1/3$ $S/\sqrt{B} \simeq 2.5$	[Baur, Plehn, Rainwater] [Yao 1308.6302] [Baglio et al. JHEP 1304]
<i>b<math>\bar{b}</math>τ<sup>+</sup>τ<sup>-</sup></i>	<ul style="list-style-type: none"> <li>• tau rec tough</li> <li>• largest bkg tt</li> <li>• Boost+MT2 might help</li> </ul>	<b>differ a lot</b> $S/B \simeq 1/5$ $S/\sqrt{B} \simeq 5$	[Dolan, Englert, MS] [Barr, Dolan, Englert, MS] [Baglio et al. JHEP 1304]
<i>b<math>\bar{b}</math>W<sup>+</sup>W<sup>-</sup></i>	<ul style="list-style-type: none"> <li>• looks like tt</li> <li>• Need semilep. W to rec. two H</li> <li>• Boost + BDT proposed</li> </ul>	<b>differ a lot</b> <b>best case:</b> $S/B \simeq 1.5$ $S/\sqrt{B} \simeq 8.2$	[Dolan, Englert, MS] [Baglio et al. JHEP 1304] [Papaefstathiou, Yang, Zurita 1209.1489]
<i>b<math>\bar{b}</math>b<math>\bar{b}</math></i>	<ul style="list-style-type: none"> <li>• Trigger issue (high pT kill signal)</li> <li>• 4b background large difficult with MC</li> <li>• Subjets might help</li> </ul>	$S/B \simeq 0.02$ $S/\sqrt{B} \leq 2.0$	[Dolan, Englert, MS] [Ferreira de Lima, Papaefstathiou, MS] [Wardrope et al, 1410.2794]
others	<ul style="list-style-type: none"> <li>• Many taus/W not clear if 2 Higgs</li> <li>• Zs, photons no rate</li> </ul>		



# $h^3$ from $h@NLO@LHC$

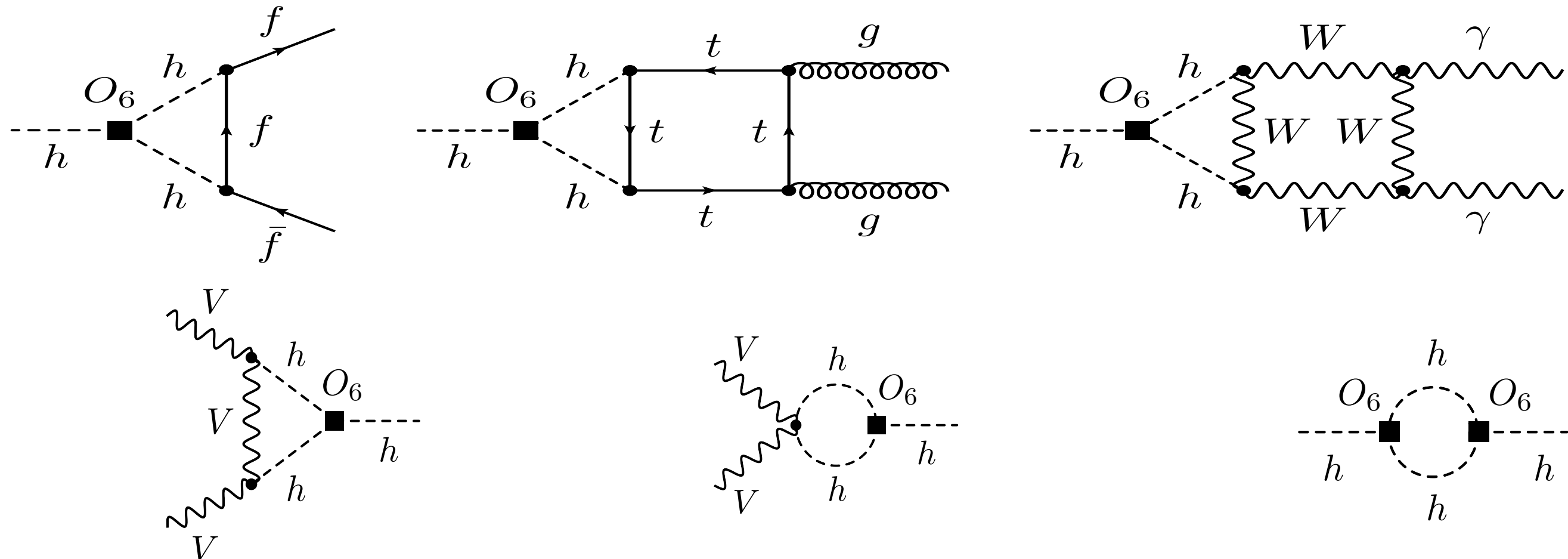
M. McCullough '14



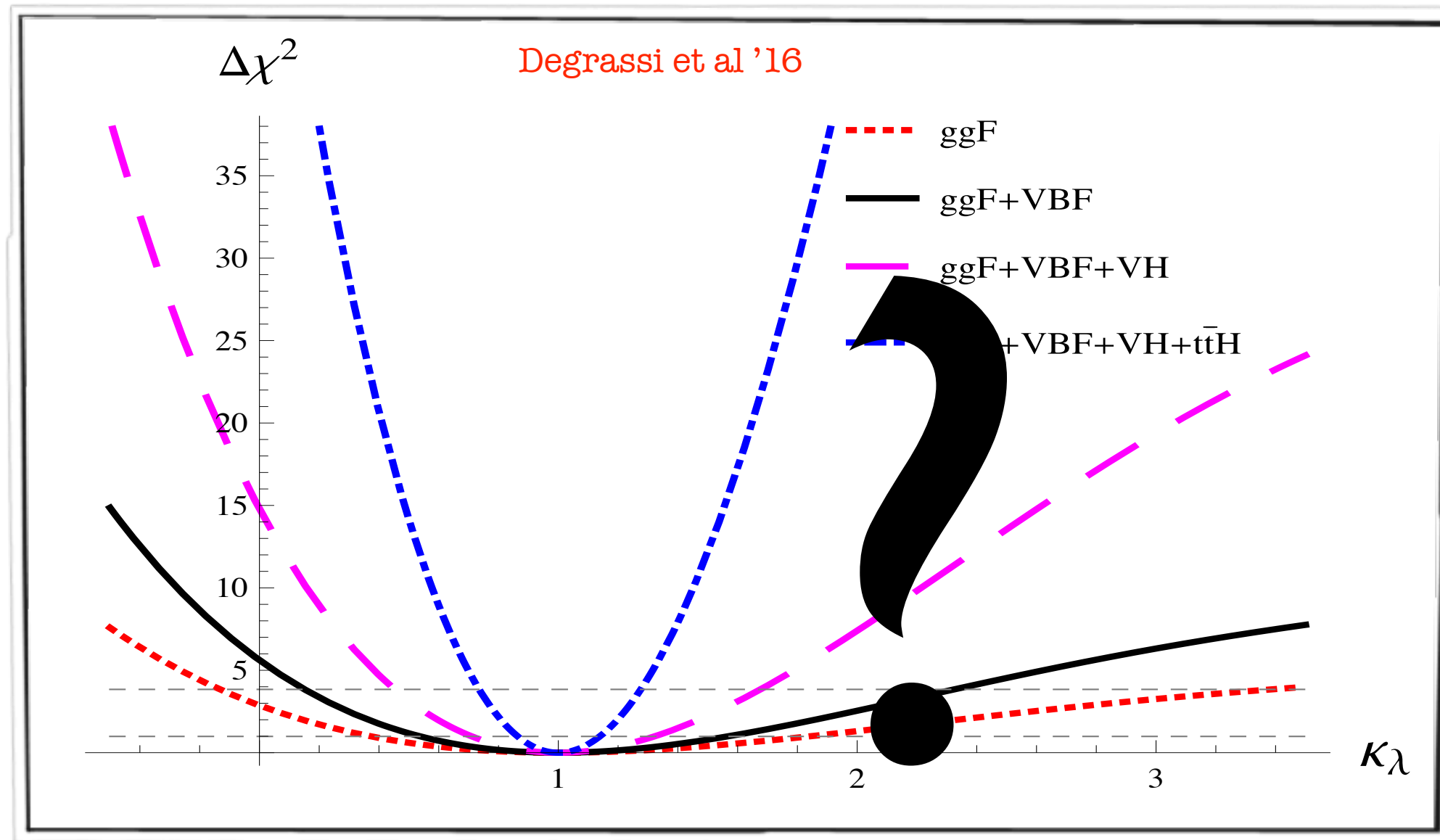
Gorbahn et al '16

Degrassi et al '16

Bizon et al '16



# $h^3$ from $h@NLO@LHC$



$$\kappa_\lambda \in [-0.7, 4.2]$$

$$\kappa_\lambda = \frac{g_{h^3}}{g_{h^3}^{\text{SM}}}$$

$$\mathcal{L} \supset \frac{c_6}{\Lambda^2} |H|^6 \iff \kappa_\lambda = 1 + \frac{c_6 G_F^{-2}}{m_H^2 \Lambda^2}$$

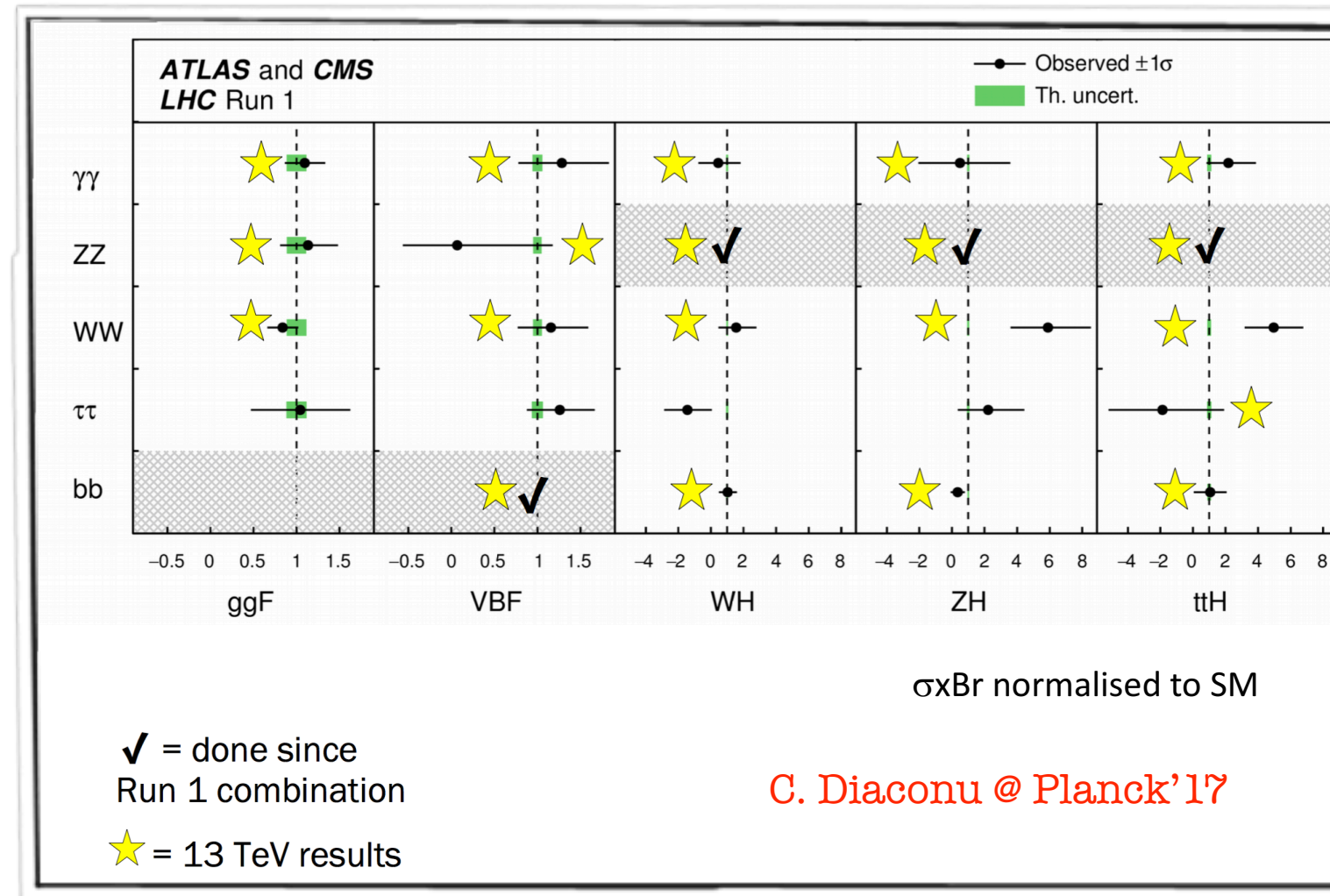
(a bit worse but)  
in the same ballpark  
of bounds obtained  
from double Higgs production

# $h^3$ @NLO vs $h$ @ LO in global fit

## The fabulous $5^2$ channels

5 main production modes: ggF, VBF, WH, ZH, ttH

5 main decay modes: ZZ, WW,  $\gamma\gamma$ ,  $\tau\tau$ , bb



# $h^3$ @NLO vs $h$ @ LO in global fit

## The fabulous $5^2$ channels

Good sensitivity (O(5-10-20)%) on 16 channels @ **HL-LHC**

Process	Combination	Theory	Experimental
$H \rightarrow \gamma\gamma$	ggF	0.07	0.05
	VBF	0.22	0.16
	$t\bar{t}H$	0.17	0.12
	$WH$	0.19	0.08
	$ZH$	0.28	0.07
$H \rightarrow ZZ$	ggF	0.06	0.05
	VBF	0.17	0.10
	$t\bar{t}H$	0.20	0.12
	$WH$	0.16	0.06
	$ZH$	0.21	0.08
$H \rightarrow WW$	ggF	0.07	0.05
	VBF	0.15	0.12
$H \rightarrow Z\gamma$	incl.	0.30	0.13
$H \rightarrow b\bar{b}$	$WH$	0.37	0.09
	$ZH$	0.14	0.05
$H \rightarrow \tau^+\tau^-$	VBF	0.19	0.12

Estimated relative uncertainties on the determination of single-Higgs production channels at the HL-LHC(14 TeV center of mass energy, 3/ab integrated luminosity and pile-up 140 events/bunch-crossing).

ATL-PHYS-PUB-2014-016

ATL-PHYS-PUB-2016-008

ATL-PHYS-PUB-2016-018

# $h^3$ @NLO vs $h$ @ LO in global fit

## The fabulous $5^2$ channels

5 main production modes: ggF, VBF, WH, ZH, ttH

5 main decay modes: ZZ, WW,  $\gamma\gamma$ ,  $\tau\tau$ , bb

a priori up to **25** measurements

but for on-shell particles, at most **10** physical quantities

since only products  $\sigma \times \text{BR}$  are measured  $\Rightarrow$  only **9** independent constraints

$$\mu_i^f = \mu_i \times \mu^f = \frac{\sigma_i}{(\sigma_i)_{\text{SM}}} \times \frac{\text{BR}[f]}{(\text{BR}[f])_{\text{SM}}}$$

$$\mu_i^f \simeq 1 + \delta\mu_i + \delta\mu^f$$

linearized BSM perturbations

$$\mu_i \rightarrow \mu_i + \delta$$

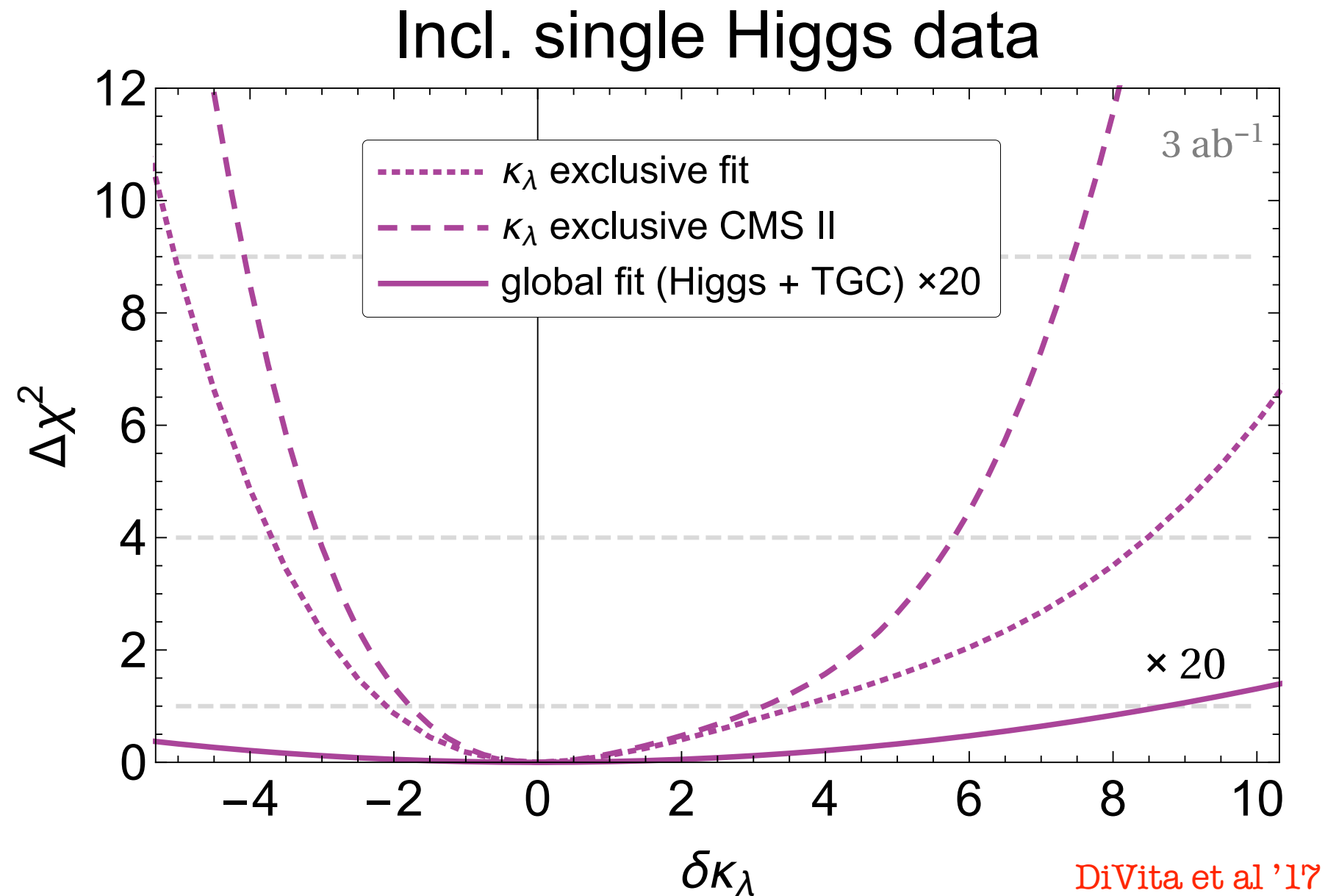
$$\mu^f \rightarrow \mu^f - \delta.$$

cannot determine univocally 10 EFT parameters!

**one flat direction is expected!**

# $h^3$ @NLO vs $h$ @ LO in global fit

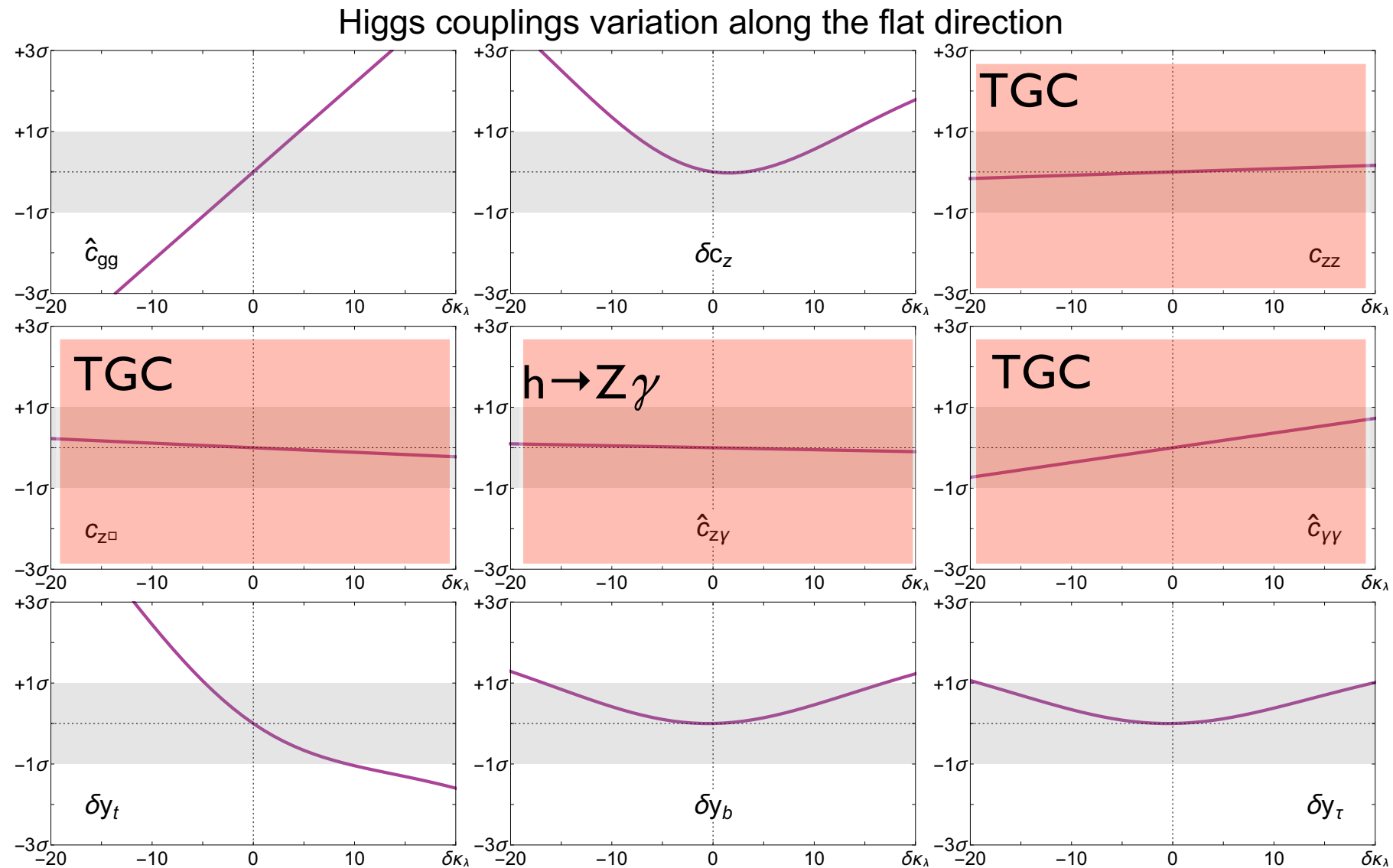
## The fabulous $5^2$ channels



**one flat direction is expected!**

# $h^3$ @NLO vs $h$ @ LO in global fit

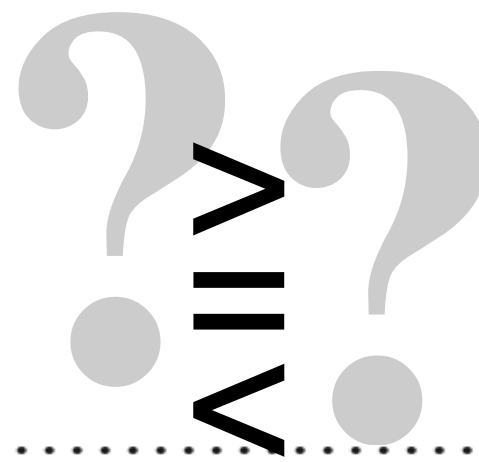
## The fabulous $5^2$ channels



The particular structure of this flat direction tells that adding new data on diboson or  $h \rightarrow Z\gamma$  won't help much

**one flat direction is expected!**

# $h^3$ @NLO vs $h$ @ LO in global fit



NLO w/ dominant  $h^3$

LO w/ subdominant other  $h$

Minimal Composite Higgs

SILH

$$\xi = \frac{v^2}{f^2} \ll 1$$

$$\frac{1}{f^2} (\partial_\mu |H|^2)^2$$

$$\frac{\lambda_4}{f^2} |H|^6$$

$$\kappa_V \equiv \frac{g_{hVV}}{g_{hVV}^{\text{SM}}} = 1 + \xi$$

$$\kappa_3 \equiv \frac{g_{hhh}}{g_{hhh}^{\text{SM}}} = 1 + \xi$$

NLO  $h^3$   
irrelevant

Partly Composite Higgs

$$\xi = \frac{v^2}{f^2} \ll 1$$

$$\frac{\varepsilon^4}{f^2} (\partial_\mu |H|^2)^2$$

$$\frac{\varepsilon^6}{f^2} |H|^6$$

$$\kappa_V \equiv \frac{g_{hVV}}{g_{hVV}^{\text{SM}}} = 1 + \varepsilon^4 \xi$$

$$\kappa_3 \equiv \frac{g_{hhh}}{g_{hhh}^{\text{SM}}} = 1 + \varepsilon^2 \frac{g_*^2 v^2}{m_h^2} \varepsilon^4 \xi$$

NLO  $h^3$   
could be relevant

Bosonic Technicolor

Induced EWSB

$$\varepsilon = \frac{f}{v} \ll 1$$

$$\frac{\varepsilon^4}{f^2} (\partial_\mu |H|^2)^2$$

$$\frac{\varepsilon^6}{f^2} |H|^6$$

$$\kappa_V \equiv \frac{g_{hVV}}{g_{hVV}^{\text{SM}}} = 1 + \varepsilon^2$$

$$\kappa_3 \equiv \frac{g_{hhh}}{g_{hhh}^{\text{SM}}} = 1 + \mathcal{O}(1)$$

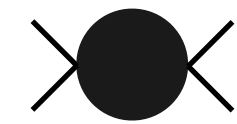
NLO  $h^3$   
a priori relevant



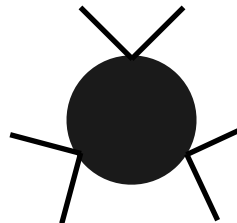
# Make $h^3$ great again: Higgs portal models

$$\mathcal{L} \supset \theta g_* m_* H^\dagger H \varphi - \frac{m_*^4}{g_*^2} V(g_* \varphi / m_*)$$

$$\varphi \sim \frac{\theta g_* |H|^2}{m_*}$$



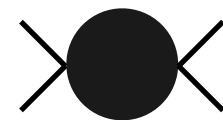
$$\frac{\theta^2 g_*^2}{m_*^2} \partial_\mu (H^\dagger H) \partial^\mu (H^\dagger H) \Rightarrow \delta c_z \sim \theta^2 g_*^2 \frac{v^2}{m_*^2}$$



$$\frac{m_*^4}{g_*^2} \frac{g_*^3}{m_*^3} \left( \frac{\theta g_*}{m_*} \right)^3 (H^\dagger H)^3 \Rightarrow \delta \kappa_\lambda \sim \theta^3 g_*^4 \frac{1}{\lambda_3^{SM}} \frac{v^2}{m_*^2}$$

**parametric  
enhancement  
of  $h^3$**

but also **tuning** of Higgs quartic coupling



$$\frac{m_*^4}{g_*^2} \frac{g_*^2}{m_*^2} \left( \frac{\theta g_*}{m_*} \right)^2 |H|^4 \Rightarrow \Delta \sim \frac{\theta^2 g_*^2}{\lambda_3^{SM}}$$

$$\delta \kappa_\lambda \sim \varepsilon \Delta$$

where  $\varepsilon$  controls validity of  $h$  expansion

$$\varepsilon \equiv \frac{\theta g_*^2 v^2}{m_*^2}$$

**~~ large  $h^3$  ~~**  
either tuning ( $\Delta > 1$ )

or

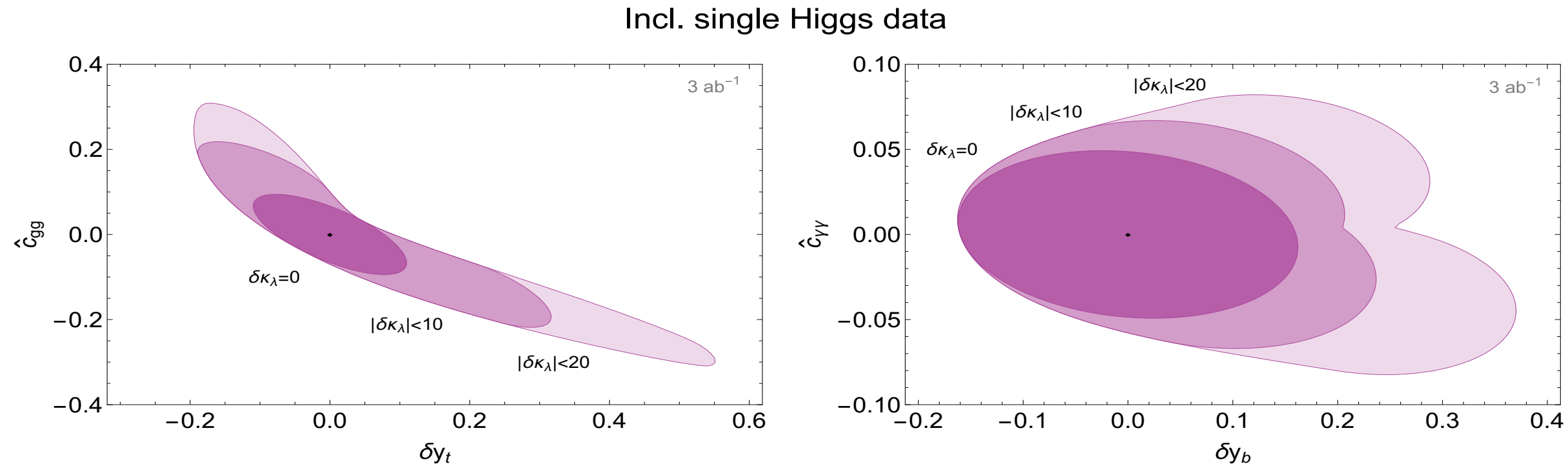
give-up on linear  $h$ -expansion ( $\varepsilon > 1$ )

a possible benchmark of large  $h^3$

$$\theta \simeq 1, g_* \simeq 3 \text{ and } m_* \simeq 2.5 \text{ TeV}$$

$$\varepsilon \simeq 0.1, \quad 1/\Delta \simeq 1.5\%, \quad \delta c_z \simeq 0.1, \quad \delta \kappa_\lambda \simeq 6$$

# Does $h^3$ modify the fit to other couplings?



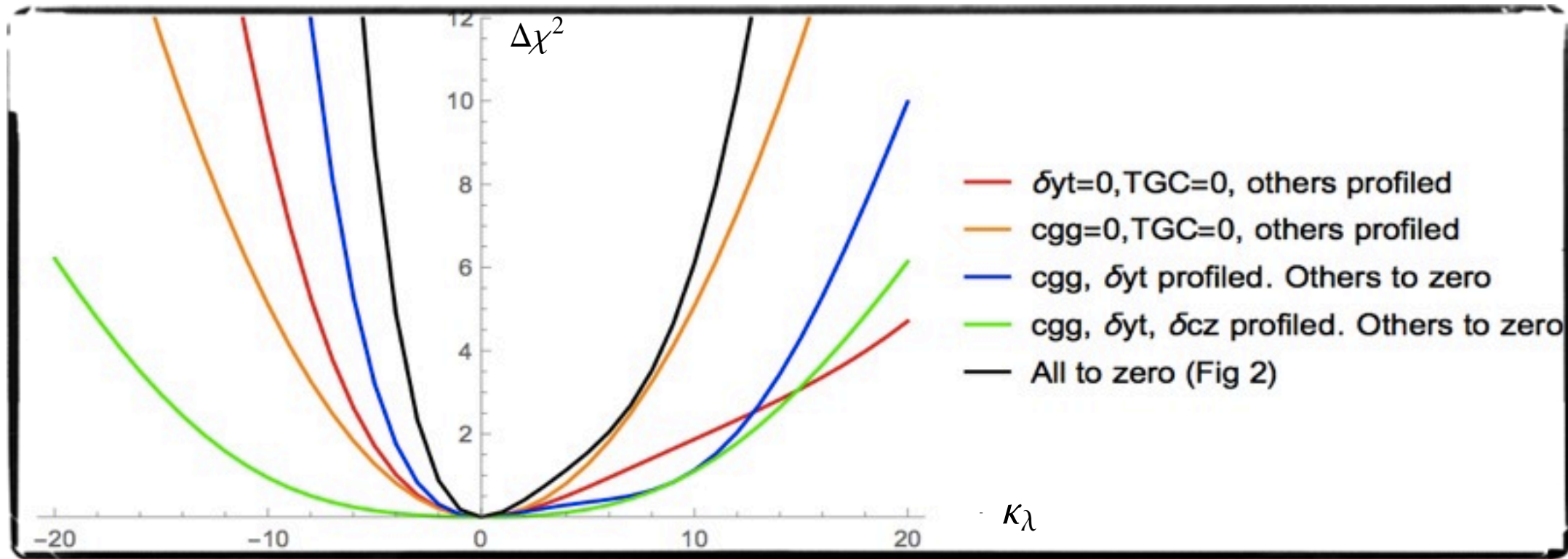
**Figure 3.** Constraints in the planes  $(\delta y_t, \hat{c}_{gg})$  (left panel) and  $(\delta y_b, \hat{c}_{\gamma\gamma})$  (right panel) obtained from a global fit on the single-Higgs processes. The darker regions are obtained by fixing the Higgs trilinear to the SM value  $\kappa_\lambda = 1$ , while the lighter ones are obtained through profiling by restricting  $\delta\kappa_\lambda$  in the ranges  $|\delta\kappa_\lambda| \leq 10$  and  $|\delta\kappa_\lambda| \leq 20$  respectively. The regions correspond to 68% confidence level (defined in the Gaussian limit corresponding to  $\Delta\chi^2 = 2.3$ ).

in models with parametrically large  $h^3$

a LO fit to single Higgs couplings done omitting  $\kappa_\lambda$  could be erroneous

# Intermediate scenarios?

DiVita et al '17



NLO single Higgs  
might do well  
(w/o the need for HH)  
in intermediate  
scenarios  
with a subset of relevant  
deformations of Higgs couplings

single Higgs couplings

simple dynamics = few parameters ( $\kappa_F/\kappa_V, \kappa_g/\kappa_\gamma$ )

more dynamics = more parameters

... model building required ...

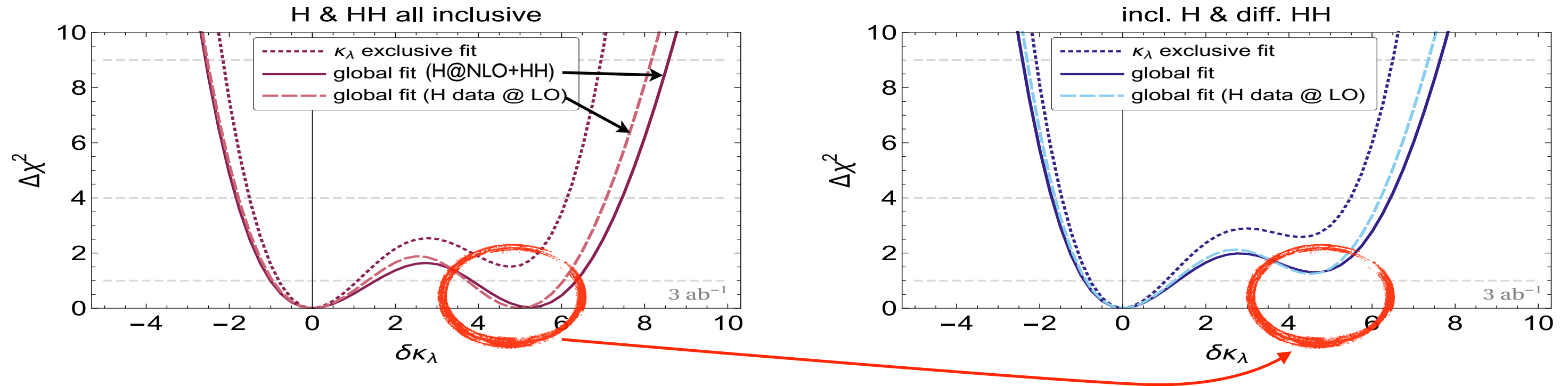
h3 fit

simple dynamics = flat direction

more dynamics (e.g. twin portal) = fewer parameters = less degeneracy

# NLO single H vs double Higgs

DiVita et al '17



**Figure 4.** *Left:* The solid curve shows the global  $\chi^2$  as a function of the corrections to the Higgs trilinear self-coupling obtained from a fit exploiting inclusive single Higgs and inclusive double Higgs observables. The dashed line shows the fit obtained by neglecting the dependence on  $\delta\kappa_\lambda$  in single-Higgs observables. The dotted line is obtained by exclusive fit in which all the EFT parameters, except for  $\delta\kappa_\lambda$ , are set to zero. *Right:* The same but using differential observables for double Higgs.

**double Higgs data first!**

single Higgs observables at NLO play a marginal role in determining  $h^3$

$$\kappa_\lambda \in [0.0, 2.5] \cup [4.9, 7.4]$$

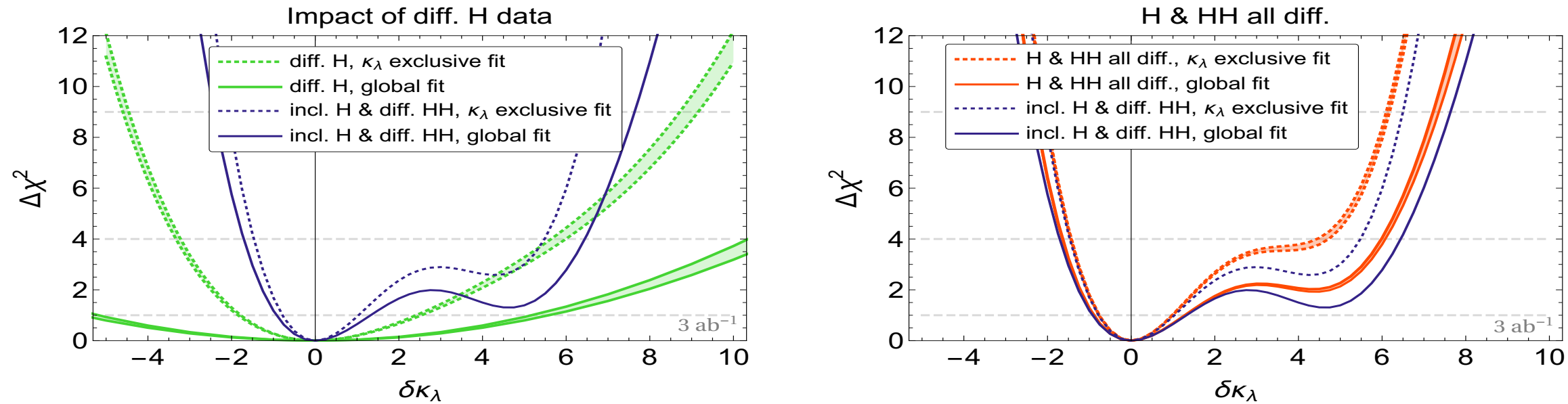
differential double Higgs removes degenerate minimum but doesn't improve much the bound around SM

Azatov et al '15

Jeju, June 3, 2017

# Is differential single H @ NLO a good option?

DiVita et al, 17



**Figure 5.** *Left:*  $\chi^2$  as a function of the Higgs trilinear self-coupling. The green bands are obtained from the differential analysis on single-Higgs observables and are delimited by the fits corresponding to the optimistic and pessimistic estimates of the experimental uncertainties. The dotted green curves correspond to a fit performed exclusively on  $\delta\kappa_\lambda$  setting to zero all the other parameters, while the solid green lines are obtained by a global fit profiling over the single-Higgs coupling parameters. *Right:* The red lines show the fits obtained by a combination of single-Higgs and double-Higgs differential observables. In both panels the dark blue curves are obtained by considering only double-Higgs differential observables and coincide with the results shown in fig. 4.

**diff. single Higgs** observables to asses  $h^3$  = interesting potential option

h incl. @ NLO: flat direction

h diff. @ NLO:  $\kappa_\lambda \in [-4,7]$

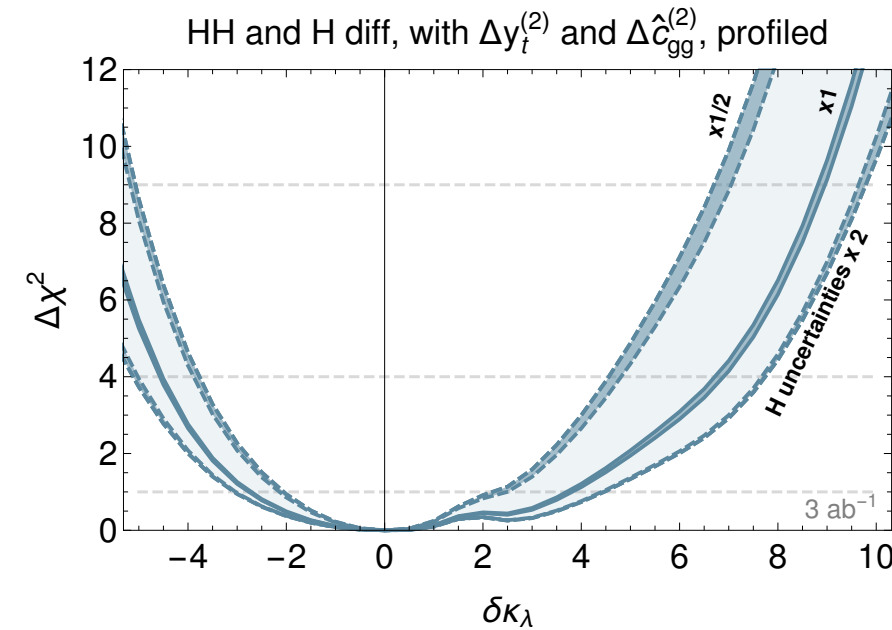
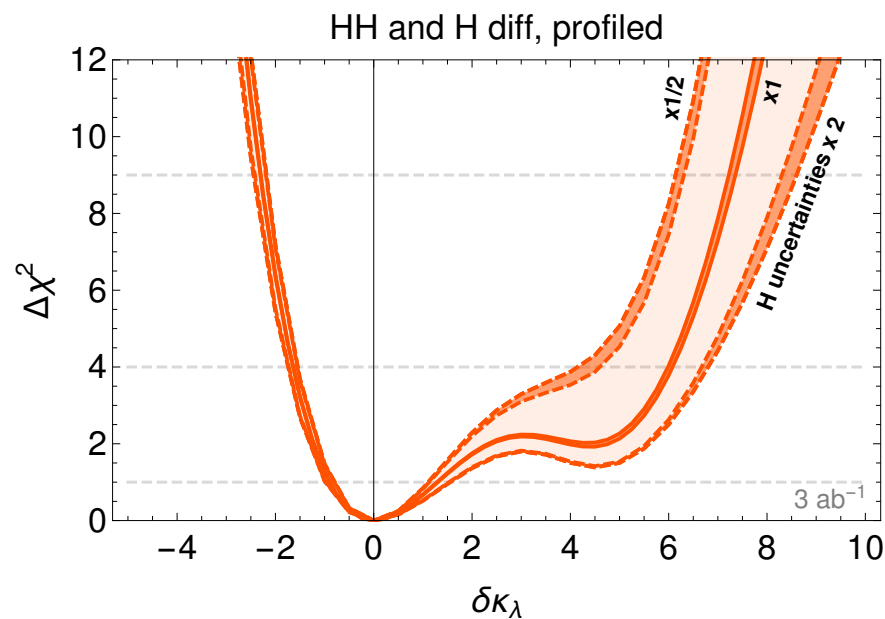
w/ hh data:  $\kappa_\lambda \in [0,2.5]$

~~ synergy between diff. single Higgs and double Higgs channels ~~

more detailed estimates of exp. uncertainties are required to fully asses the potential of diff. channels

# Is the fit robust against systematics?

doubling the uncertainties doesn't affect much the bounds on  $h^3$



bounds on  $h^3$  become looser in non-linear realization of SU(2)

**Figure 6.** Band of variation of the global fit on the Higgs self-coupling obtained by rescaling the single-Higgs measurement uncertainties by a factor in the range  $x \in [1/2, 2]$ . The lighter shaded bands show the full variation of the fit due to the rescaling. The darker bands show how the fits corresponding to the ‘optimistic’ and ‘pessimistic’ assumptions on the systematic uncertainties (compare fig. 5) change for  $x = 1/2, 1, 2$ . The left panel shows the fit in the linear Lagrangian, while the right panel corresponds to the non-linear case in which  $\Delta y_f^{(2)}$  and  $\Delta \hat{c}_{gg}^{(2)}$  are treated as independent parameters.

in scenarios where  $h^3$  can be naturally large,  
Higgs expansion could break down & more parameters need to be fitted  
(in particular due do fewer constraints from EW precision data)  
**no robust determination of  $h^3$  possible yet in these scenarios**

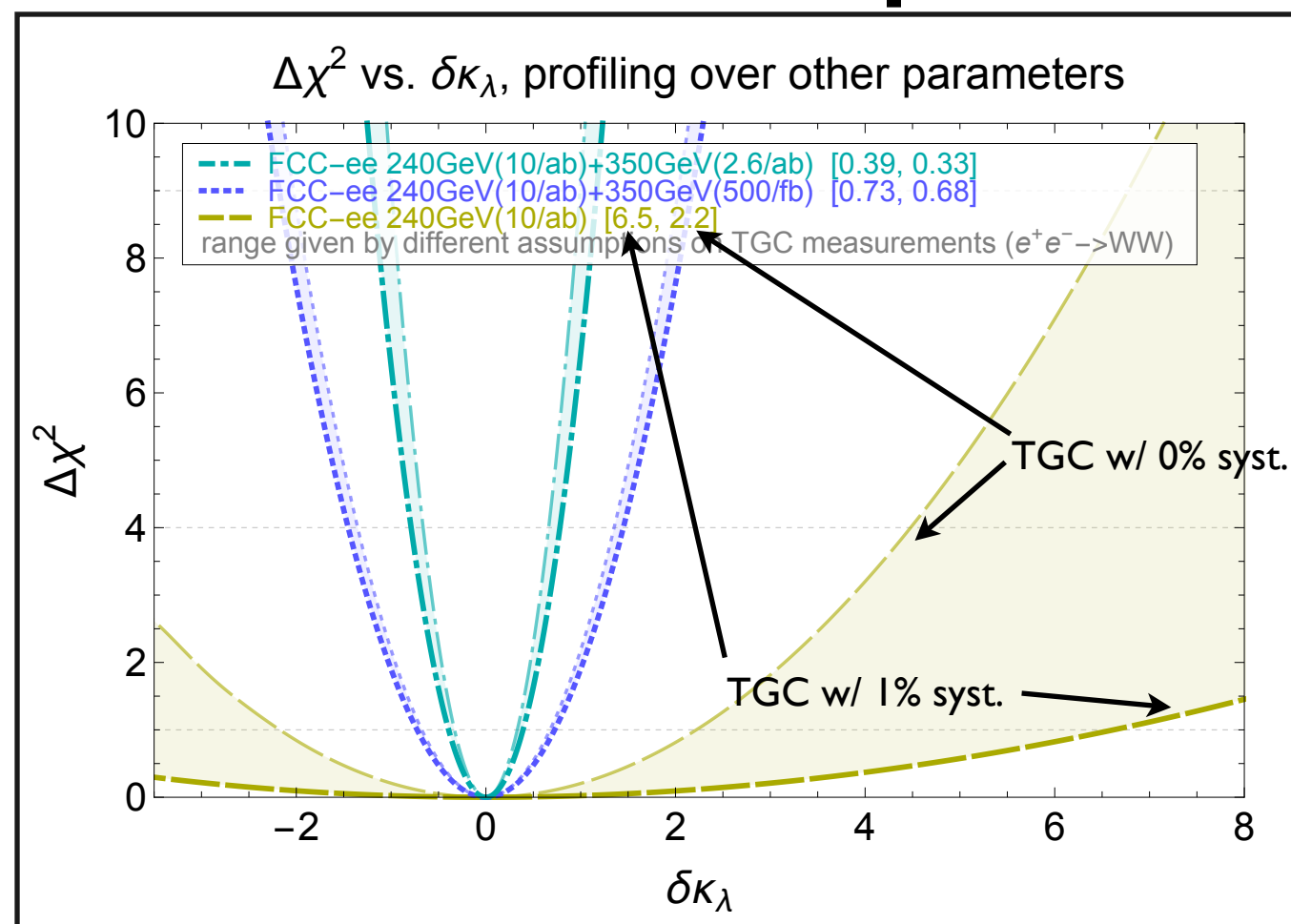
# What about (low energy) $e^+e^-$ colliders?

I main production mode: ZH & I subdominant production: VBF  
+ access to full angular distributions (4) and/or beam polarizations (2)

7 (+2) accessible decay modes: ZZ, WW,  $\gamma\gamma$ ,  $Z\gamma$ ,  $\tau\tau$ , bb, gg, (cc,  $\mu\mu$ )

at least **10** solid independent constraints to fit **10** parameters

**a priori no flat direction is expected!**



I) with a run at 240 GeV only, bound starts to become meaningful only if perfect control of di-boson

N. Craig, S. Di Vita, G. Durieux, C. Grojean, J. Gu, Z. Liu, G. Panico, M. Riembau, T. Vantalou 'in progress

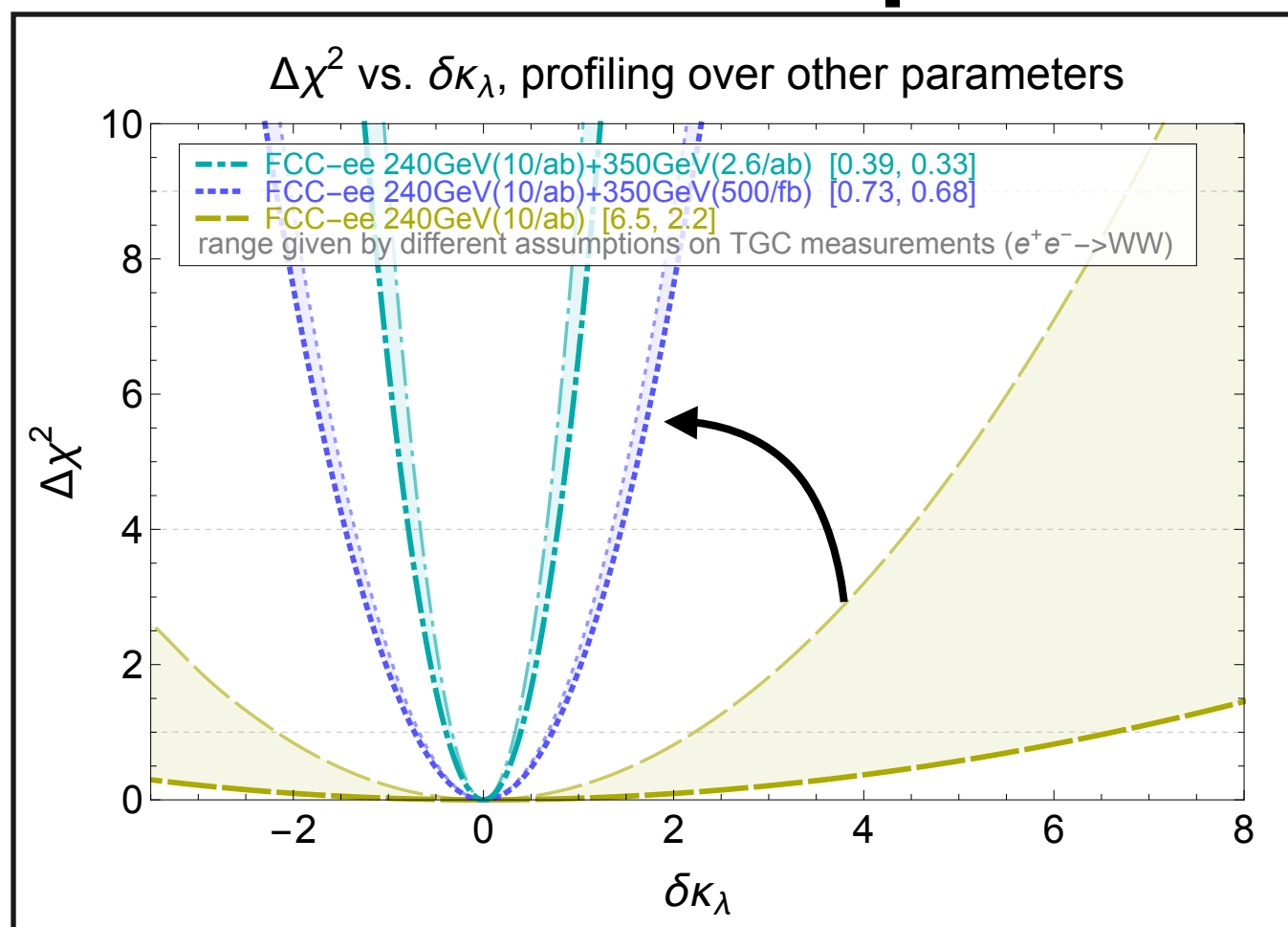
# What about (low energy) $e^+e^-$ colliders?

1 main production mode: ZH & 1 subdominant production: VBF  
+ access to full angular distributions (4) and/or beam polarizations (2)

7 (+2) accessible decay modes: ZZ, WW,  $\gamma\gamma$ ,  $Z\gamma$ ,  $\tau\tau$ , bb, gg, (cc,  $\mu\mu$ )

at least **10** solid independent constraints to fit **10** parameters

**a priori no flat direction is expected!**



- 1) with a run at 240 GeV only, bound starts to become meaningful only if perfect control of di-boson
- 2) combining 240+350 improves significantly the bounds on  $h^3$

N. Craig, S. Di Vita, G. Durieux, C. Grojean, J. Gu, Z. Liu, G. Panico,  
M. Riembau, T. Vantalou 'in progress



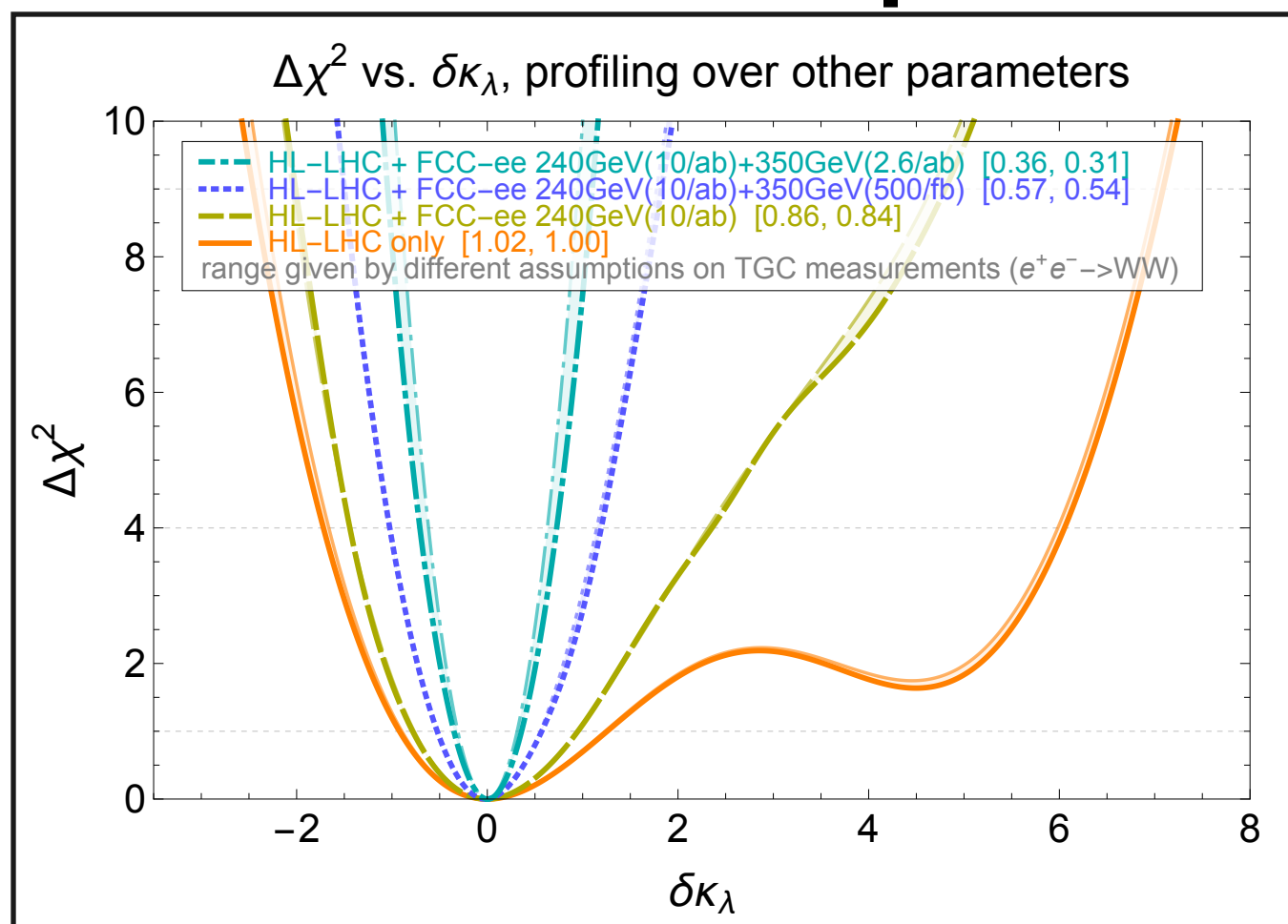
# What about (low energy) $e^+e^-$ colliders?

1 main production mode: ZH & 1 subdominant production: VBF  
+ access to full angular distributions (4) and/or beam polarizations (2)

7 (+2) accessible decay modes: ZZ, WW,  $\gamma\gamma$ ,  $Z\gamma$ ,  $\tau\tau$ , bb, gg, (cc,  $\mu\mu$ )

at least **10** solid independent constraints to fit **10** parameters

**a priori no flat direction is expected!**



- 1) with a run at 240 GeV only, bound starts to become meaningful only if perfect control of di-boson
- 2) combining 240+350 improves significantly the bounds on  $h^3$
- 3) combination FCC-ee and HL-LHC is very powerful (especially if cannot afford FCC-ee @ 350 GeV)

N. Craig, S. Di Vita, G. Durieux, C. Grojean, J. Gu, Z. Liu, G. Panico, M. Riembau, T. Vantalou 'in progress

# Conclusions

It is often claimed that  $h^3$  measurement is needed

- 1) to understand EW symmetry breaking
- 2) to probe new physics at the origin of EWVSB

$h^3$  is not a precise measurement to access to new physics  
but order one determination is within HL-LHC reach and it can help figure out  
the thermodynamics of EW phase transition and the Higgs thermal potential  
with important consequences:

- 1) EW baryogenesis**
- 2) stochastic GW background**

Let us try and help the experimentalists telling us its value!

# Backup

# Higgs Basis

A. Falkowski '15  
LHCHXSWG YR4 '16

$$\begin{aligned} \mathcal{L} \supset & \frac{h}{v} \left[ \delta c_w \frac{g^2 v^2}{2} W_\mu^+ W^{-\mu} + \delta c_z \frac{(g^2 + g'^2) v^2}{4} Z_\mu Z^\mu \right. \\ & + c_{ww} \frac{g^2}{2} W_{\mu\nu}^+ W^{-\mu\nu} + c_{w\Box} g^2 (W_\mu^- \partial_\nu W^{+\mu\nu} + \text{h.c.}) + \hat{c}_{\gamma\gamma} \frac{e^2}{4\pi^2} A_{\mu\nu} A^{\mu\nu} \\ & \left. + c_{zz} \frac{g^2 + g'^2}{4} Z_{\mu\nu} Z^{\mu\nu} + \hat{c}_{z\gamma} \frac{e \sqrt{g^2 + g'^2}}{2\pi^2} Z_{\mu\nu} A^{\mu\nu} + c_{z\Box} g^2 Z_\mu \partial_\nu Z^{\mu\nu} + c_{\gamma\Box} g g' Z_\mu \partial_\nu A^{\mu\nu} \right] \\ & + \frac{g_s^2}{48\pi^2} \left( \hat{c}_{gg} \frac{h}{v} + \hat{c}_{gg}^{(2)} \frac{h^2}{2v^2} \right) G_{\mu\nu} G^{\mu\nu} - \sum_f \left[ m_f \left( \delta y_f \frac{h}{v} + \delta y_f^{(2)} \frac{h^2}{2v^2} \right) \bar{f}_R f_L + \text{h.c.} \right] \\ & - (\kappa_\lambda - 1) \lambda_3^{SM} v h^3, \end{aligned}$$

with

$$\begin{aligned} \delta c_w &= \delta c_z, \\ c_{ww} &= c_{zz} + 2 \frac{g'^2}{\pi^2 (g^2 + g'^2)} \hat{c}_{z\gamma} + \frac{g'^4}{\pi^2 (g^2 + g'^2)^2} \hat{c}_{\gamma\gamma}, \\ c_{w\Box} &= \frac{1}{g^2 - g'^2} \left[ g^2 c_{z\Box} + g'^2 c_{zz} - e^2 \frac{g'^2}{\pi^2 (g^2 + g'^2)} \hat{c}_{\gamma\gamma} - (g^2 - g'^2) \frac{g'^2}{\pi^2 (g^2 + g'^2)} \hat{c}_{z\gamma} \right], \\ c_{\gamma\Box} &= \frac{1}{g^2 - g'^2} \left[ 2g^2 c_{z\Box} + (g^2 + g'^2) c_{zz} - \frac{e^2}{\pi^2} \hat{c}_{\gamma\gamma} - \frac{g^2 - g'^2}{\pi^2} \hat{c}_{z\gamma} \right], \\ \hat{c}_{gg}^{(2)} &= \hat{c}_{gg}, \\ \delta y_f^{(2)} &= 3\delta y_f - \delta c_z. \end{aligned}$$

10 parameters

6 deformations of Higgs couplings to gauge bosons

$$\delta c_z, c_{zz}, c_{z\Box}, \hat{c}_{z\gamma}, \hat{c}_{\gamma\gamma}, \hat{c}_{gg}.$$

3 deformations of Higgs couplings to fermions

$$\delta y_t, \delta y_b, \delta y_\tau,$$

1 deformations of Higgs self-couplings

$$\kappa_\lambda$$

# Single Higgs observables @ NLO in $h^3$

$$\frac{\sigma_{ZH}}{\sigma_{ZH}^{SM}} = 1 + \delta c_z \begin{pmatrix} 2.0 \\ 2.0 \\ 2.0 \\ 2.0 \\ 2.0 \\ 2.0 \end{pmatrix} + c_{z\Box} \begin{pmatrix} 7.6 \\ 7.8 \\ 8.3 \\ 8.4 \\ 9.1 \\ 10.0 \end{pmatrix} + c_{zz} \begin{pmatrix} 3.4 \\ 3.4 \\ 3.5 \\ 3.6 \\ 3.7 \\ 4.0 \end{pmatrix} - \hat{c}_{z\gamma} \begin{pmatrix} 0.060 \\ 0.061 \\ 0.067 \\ 0.068 \\ 0.077 \\ 0.086 \end{pmatrix} - \hat{c}_{\gamma\gamma} \begin{pmatrix} 0.028 \\ 0.028 \\ 0.030 \\ 0.032 \\ 0.034 \\ 0.037 \end{pmatrix}$$

$$\frac{\sigma_{WH}}{\sigma_{WH}^{SM}} = 1 + \delta c_z \begin{pmatrix} 2.0 \\ 2.0 \\ 2.0 \\ 2.0 \\ 2.0 \\ 2.0 \end{pmatrix} + c_{z\Box} \begin{pmatrix} 9.3 \\ 9.4 \\ 10.0 \\ 10.1 \\ 11.1 \\ 12.1 \end{pmatrix} + c_{zz} \begin{pmatrix} 4.4 \\ 4.4 \\ 4.6 \\ 4.6 \\ 5.0 \\ 5.3 \end{pmatrix} - \hat{c}_{z\gamma} \begin{pmatrix} 0.082 \\ 0.084 \\ 0.094 \\ 0.095 \\ 0.110 \\ 0.126 \end{pmatrix} - \hat{c}_{\gamma\gamma} \begin{pmatrix} 0.044 \\ 0.045 \\ 0.048 \\ 0.049 \\ 0.054 \\ 0.060 \end{pmatrix}$$

$$\frac{\sigma_{VBF}}{\sigma_{VBF}^{SM}} = 1 + \delta c_z \begin{pmatrix} 2.0 \\ 2.0 \\ 2.0 \\ 2.0 \\ 2.0 \\ 2.0 \end{pmatrix} - c_{z\Box} \begin{pmatrix} 2.2 \\ 2.2 \\ 2.5 \\ 2.5 \\ 3.0 \\ 3.7 \end{pmatrix} - c_{zz} \begin{pmatrix} 0.81 \\ 0.83 \\ 0.89 \\ 0.90 \\ 1.04 \\ 1.27 \end{pmatrix} + \hat{c}_{z\gamma} \begin{pmatrix} 0.029 \\ 0.030 \\ 0.033 \\ 0.034 \\ 0.041 \\ 0.051 \end{pmatrix} + \hat{c}_{\gamma\gamma} \begin{pmatrix} 0.0113 \\ 0.0117 \\ 0.0129 \\ 0.0131 \\ 0.0156 \\ 0.0193 \end{pmatrix}$$

$$\frac{\sigma_{ggF}}{\sigma_{ggF}^{SM}} = 1 + 2\hat{c}_{gg} + 2.06\delta y_t - 0.06\delta y_b$$

$$\frac{\sigma_{ttH}}{\sigma_{ttH}^{SM}} = 1 + 2\delta y_t.$$

$$\frac{\Gamma_{\gamma\gamma}}{\Gamma_{\gamma\gamma}^{SM}} = 1 + 2.56\delta c_z + 2.15c_{z\Box} + 0.98c_{zz} - 0.066\hat{c}_{z\gamma} - 2.47\hat{c}_{\gamma\gamma} - 0.56\delta y_t,$$

$$\frac{\Gamma_{Z\gamma}}{\Gamma_{Z\gamma}^{SM}} = 1 + 2.11\delta c_z - 3.4\hat{c}_{z\gamma} - 0.113\delta y_t,$$

$$\frac{\Gamma_{WW}}{\Gamma_{WW}^{SM}} = 1 + 2.0\delta c_z + 0.67c_{z\Box} + 0.05c_{zz} - 0.0182\hat{c}_{z\gamma} - 0.0051\hat{c}_{\gamma\gamma},$$

$$\frac{\Gamma_{ZZ}}{\Gamma_{ZZ}^{SM}} = 1 + 2.0\delta c_z + 0.33c_{z\Box} + 0.19c_{zz} - 0.0081\hat{c}_{z\gamma} - 0.00111\hat{c}_{\gamma\gamma},$$

$$\frac{\Gamma_{\tau\tau}}{\Gamma_{\tau\tau}^{SM}} = 1 + 2.0\delta y_\tau,$$

$$\frac{\Gamma_{bb}}{\Gamma_{bb}^{SM}} = 1 + 2.0\delta y_b,$$

$$\frac{\Gamma_H}{\Gamma_H^{SM}} = 1 + 0.171\hat{c}_{gg} + 0.006c_{zz} - 0.0091\hat{c}_{z\gamma} + 0.15c_{z\Box} - 0.0061\hat{c}_{\gamma\gamma} + 0.48\delta y_t + 1.15\delta y_b + 0.23\delta y_t + 0.13\delta y_\tau,$$

LHCHSWG YR4 '16

$$\frac{\sigma}{\sigma_{SM}} = 1 + (\kappa_\lambda - 1)C^\sigma + \frac{(\kappa_\lambda^2 - 1)\delta Z_H}{1 - \kappa_\lambda^2\delta Z_H},$$

$$\frac{\Gamma}{\Gamma_{SM}} = 1 + (\kappa_\lambda - 1)C^\Gamma + \frac{(\kappa_\lambda^2 - 1)\delta Z_H}{1 - \kappa_\lambda^2\delta Z_H}.$$

$$\delta Z_H = -\frac{9}{16} \frac{G_\mu m_H^2}{\sqrt{2}\pi^2} \left( \frac{2\pi}{3\sqrt{3}} - 1 \right) \simeq 0.0015$$

Degrassi et al '16

$C^\Gamma$ [%]	$\gamma\gamma$	$ZZ$	$WW$	$f\bar{f}$	$gg$
H	0.49	0.83	0.73	0	0.66

$C^\sigma$ [%]	ggF	VBF	WH	ZH	$t\bar{t}H$
7 TeV	0.66	0.65	1.06	1.23	3.87
8 TeV	0.66	0.65	1.05	1.22	3.78
13 TeV	0.66	0.64	1.03	1.19	3.51
14 TeV	0.66	0.64	1.03	1.18	3.47

# TGC

$$\begin{aligned} \mathcal{L} \supset & i g c_w \delta g_{1,z} (W_{\mu\nu}^+ W^{\mu-} - W_{\mu\nu}^- W^{\mu+}) Z^\nu \\ & + i e \delta \kappa_\gamma A^{\mu\nu} W_\nu^+ W_\nu^- + i g c_w \delta \kappa_z Z^{\mu\nu} W_\mu^+ W_\nu^- \\ & + i \frac{e \lambda_\gamma}{m_w^2} W_\nu^{\mu+} W_\rho^{\nu-} A^\rho_\mu + \frac{g c_w \lambda_z}{m_w^2} W_\nu^{\mu+} W_\rho^{\nu-} Z^\rho_\mu \end{aligned}$$

$$\delta g_{1,z} = \frac{g'^2}{2(g^2 - g'^2)} \left[ \hat{c}_{\gamma\gamma} \frac{e^2}{\pi^2} + \hat{c}_{z\gamma} \frac{g^2 - g'^2}{\pi^2} - c_{zz} (g^2 + g'^2) - c_{z\Box} \frac{g^2}{g'^2} (g^2 + g'^2) \right],$$

$$\delta \kappa_\gamma = - \frac{g^2}{2(g^2 + g'^2)} \left[ \hat{c}_{\gamma\gamma} \frac{e^2}{\pi^2} + \hat{c}_{z\gamma} \frac{g^2 - g'^2}{\pi^2} - c_{zz} (g^2 + g'^2) \right]$$

$$\delta \kappa_z = \delta g_{1,z} - \frac{g'^2}{g^2} \delta \kappa_\gamma,$$

$$\lambda_\gamma = \lambda_z.$$