

# MSTW Parton Distributions and $\alpha_S$

Robert Thorne

May 29th, 2009



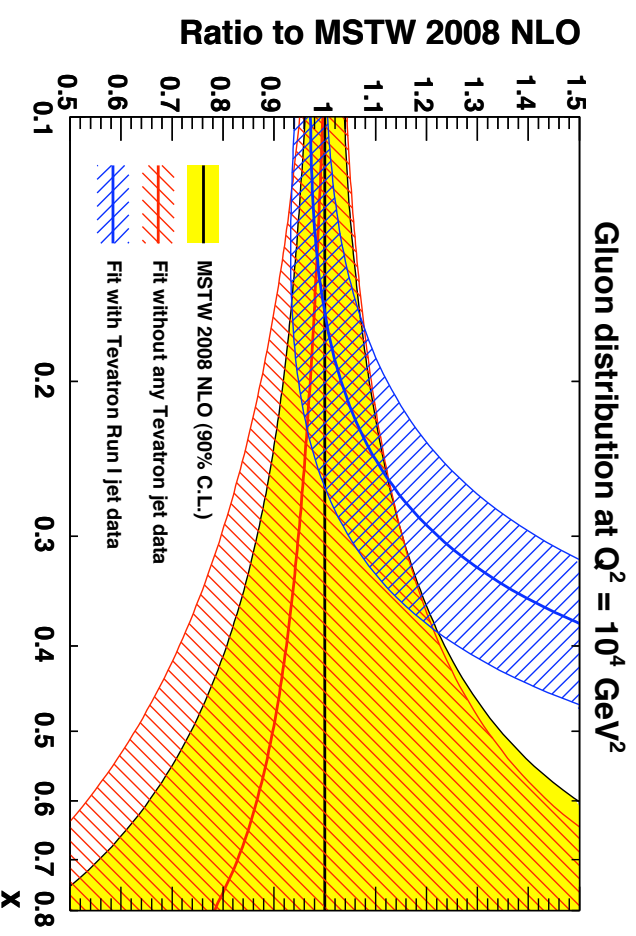
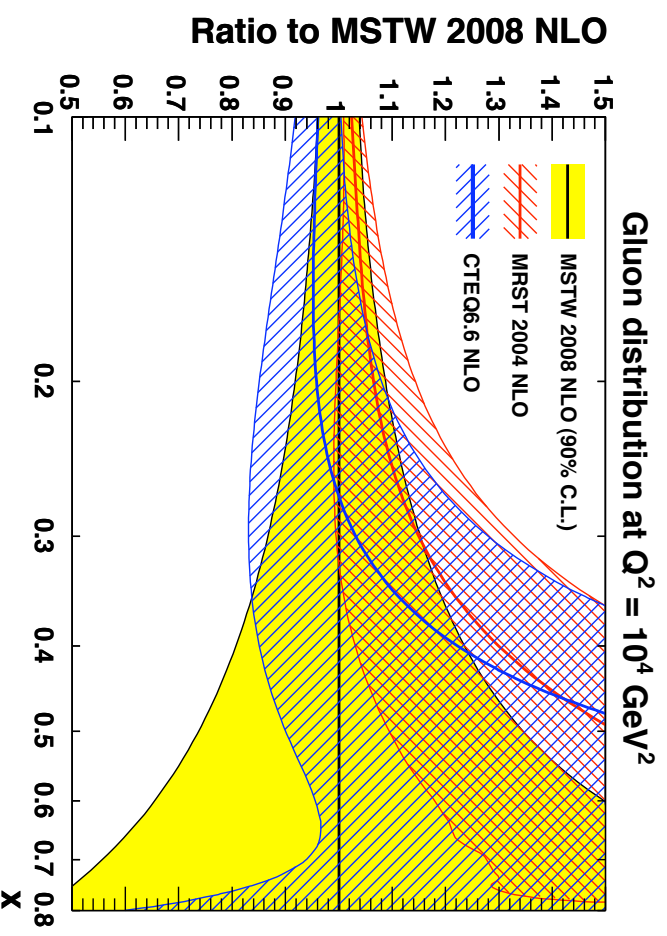
University College London

(In collaboration with A.D. Martin, W.J. Stirling and G. Watt)

(arXiv:0905.3531)

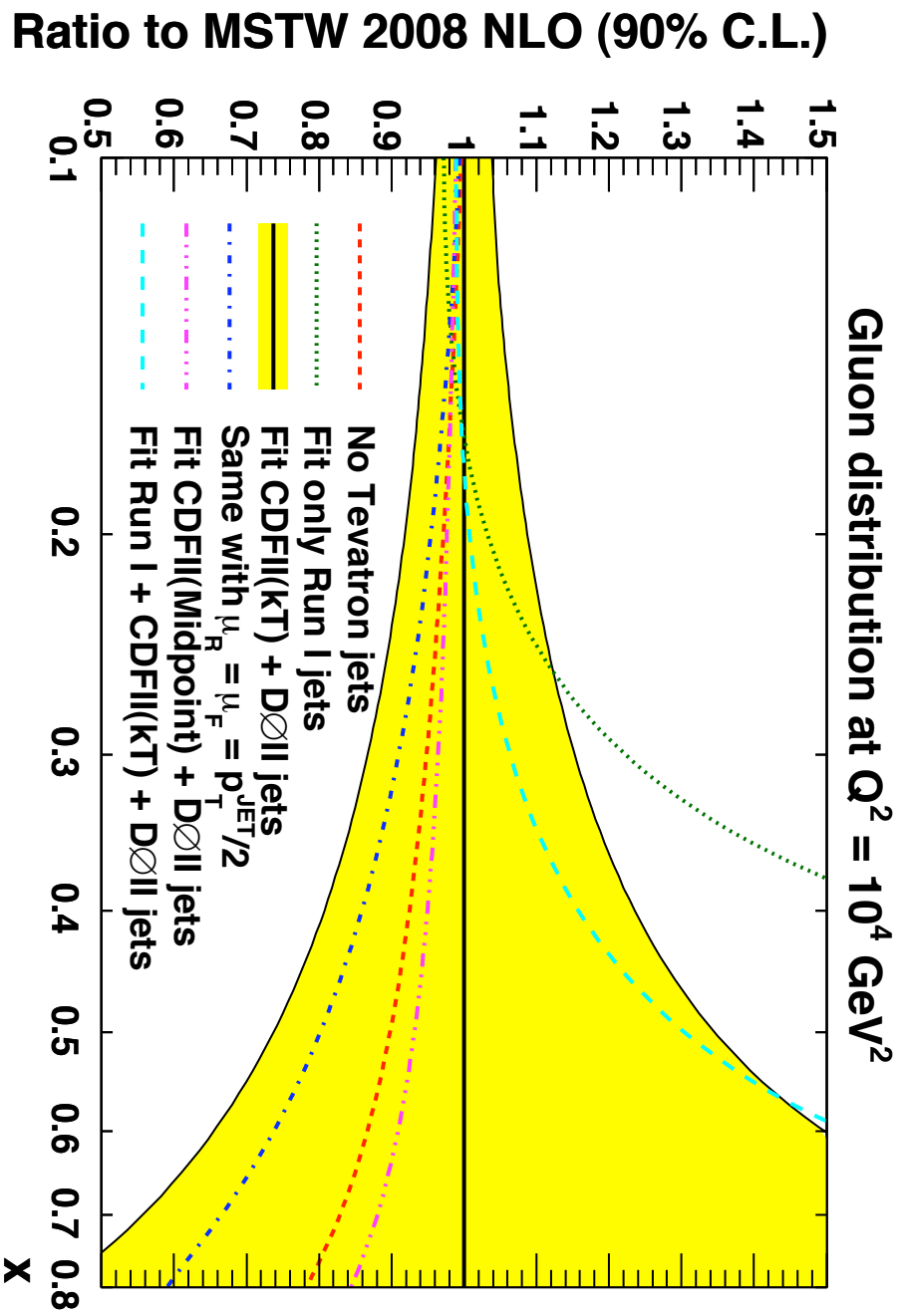
Begin by considering the gluon.  
Affects many LHC predictions.

Inclusion of Run II Tevatron jet  
data instead of Run I softens gluon  
at high  $x$  significantly.



Unlike CT09G do not find good consistency between fits to Run I and Run II.

Little change in conclusions if CDFII  $k_T$ -algorithm or (corrected) midpoint algorithm data used.

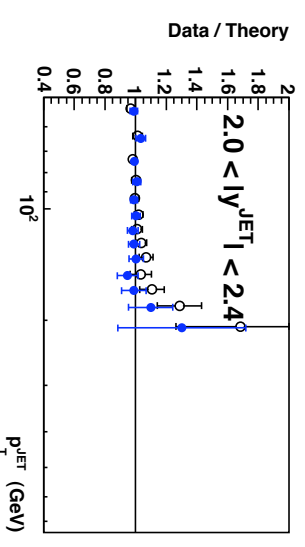
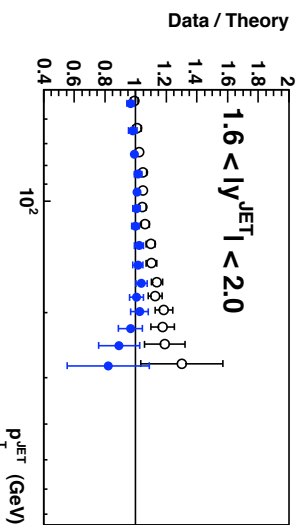
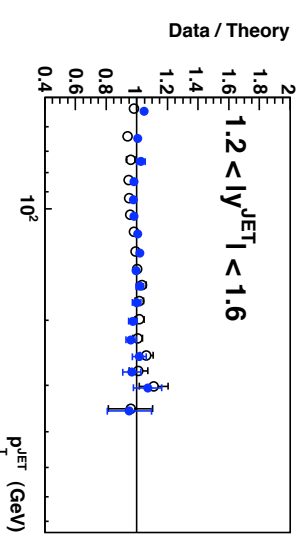
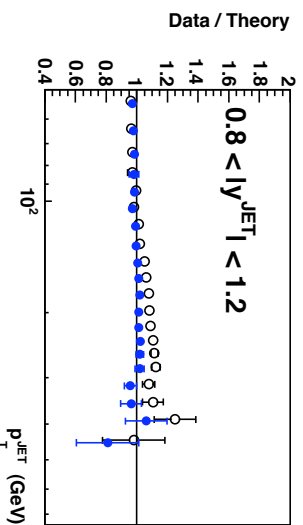
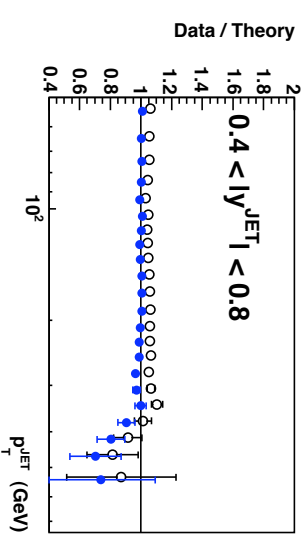
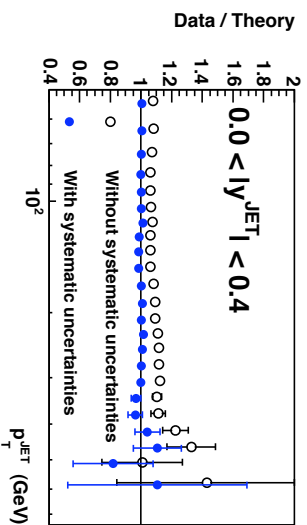


Note different gluons correspond to  $\alpha_S$  variation of  $\sim 0.002$ .

Fit to D0 Run II data excellent.

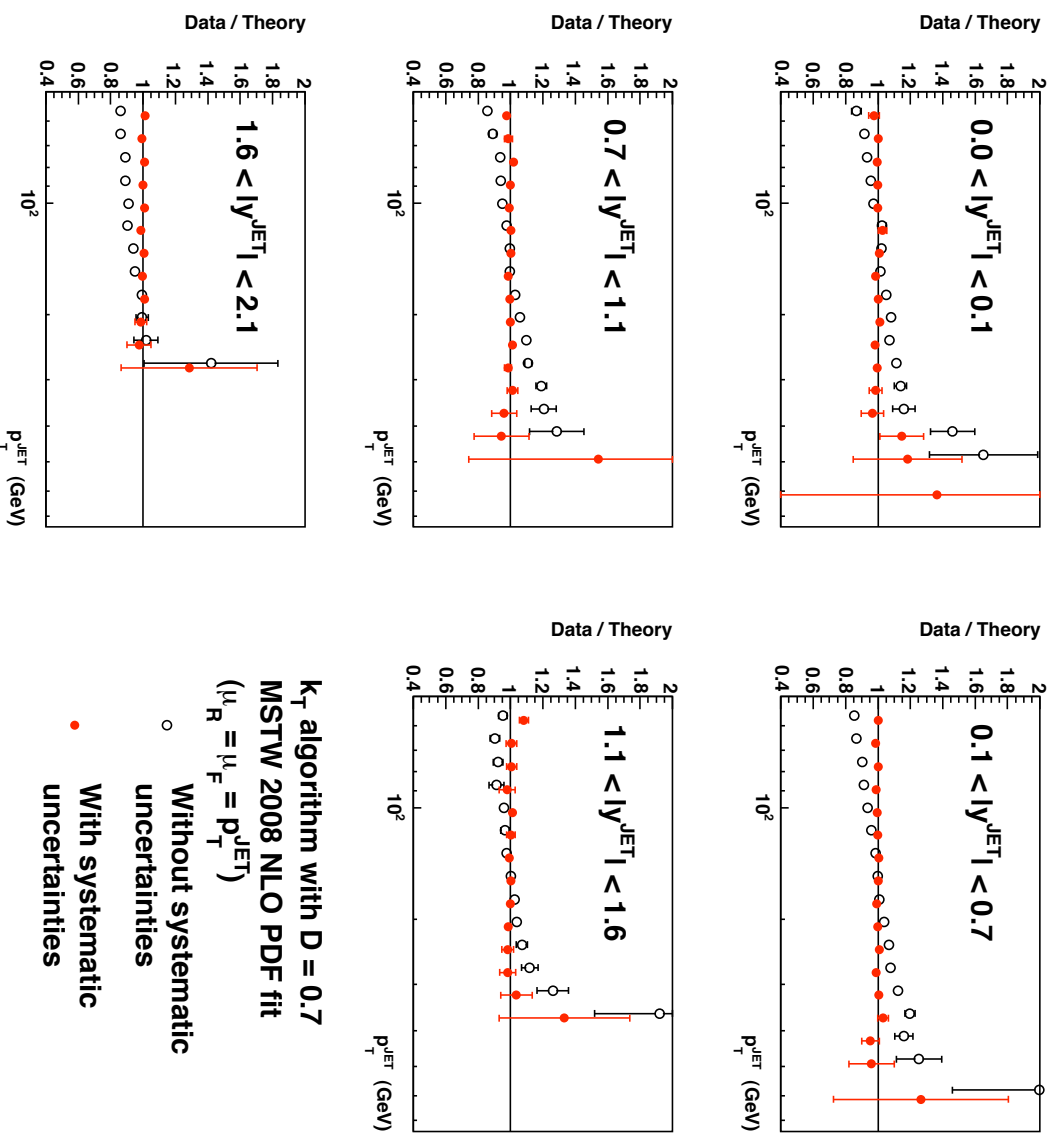
No large shifts of data relative to theory required.

**$\text{D}\bar{\text{D}}$  Run II inclusive jet data (cone,  $R = 0.7$ )**  
MSTW 2008 NLO PDF fit ( $u_R = u_F = p_T^{\text{JET}}$ ),  $\chi^2 = 114$  for 110 pts.



Fit to CDF Run II data similarly good.

## CDF Run II inclusive jet data, $\chi^2 = 56$ for 76 pts.



- Without systematic uncertainties
  - With systematic uncertainties
- $K_T$  algorithm with  $D = 0.7$   
MSTW 2008 NLO PDF fit  
 $(\mu_R = \mu_F = p_T^{\text{JET}})$

Quality of fit to various combinations of jet data by **MSTW**.

CDF <sub>I</sub> [179] (33 pts.)		D0 <sub>I</sub> [176] (90 pts.)		CDF <sub>II</sub> [54] (76 pts.)		D0 <sub>II</sub> [56] (110 pts.)		$\Delta\chi^2_{\text{non-jet}}$ (2513 pts.)	$\alpha_S(M_Z^2)$
53	119	48	117	64	180	0	0.1197		
<b>51</b>	<b>48</b>	132	114	132	114	9	0.1214		
56	110	56	117	56	117	2	0.1202		
<b>53</b>	<b>85</b>	68	117	68	117	1	0.1204		

Quality of fit to various combinations of jet data by **CTEQ**.

CDF <sub>I</sub> (33 pts) Wt $\chi^2$		D0 <sub>I</sub> (90 pts) Wt $\chi^2$		CDF <sub>II</sub> (72 pts) Wt $\chi^2$		D0 <sub>II</sub> (110 pts) Wt $\chi^2$		$\Delta\chi^2_{\text{non-jet}}$
0	55.4	0	115.3	0	99.5	0	134.0	0.0
1	52.6	1	47.0	0	105.6	0	138.3	11.8
0	56.6	0	82.2	1	85.6	1	124.1	6.2
1	52.1	1	59.4	1	88.5	1	121.5	9.6

Quality of fit to combinations of jet data by **CTEQ** with restricted gluon parameterization – far worse. Therefore not obvious source of discrepancy.

CDF <sub>I</sub> (33 pts) Wt $\chi^2$		D0 <sub>I</sub> (90 pts) Wt $\chi^2$		CDF <sub>II</sub> (72 pts) Wt $\chi^2$		D0 <sub>II</sub> (110 pts) Wt $\chi^2$		$\Delta\chi^2_{\text{non-jet}}$
0	55.8	0	145.9	0	120.6	0	155.2	2.0
1	53.2	1	124.0	0	118.2	0	148.6	7.7
0	58.6	0	121.3	1	98.1	1	137.8	16.8
1	54.5	1	108.8	1	95.5	1	134.2	25.8

# Higgs predictions

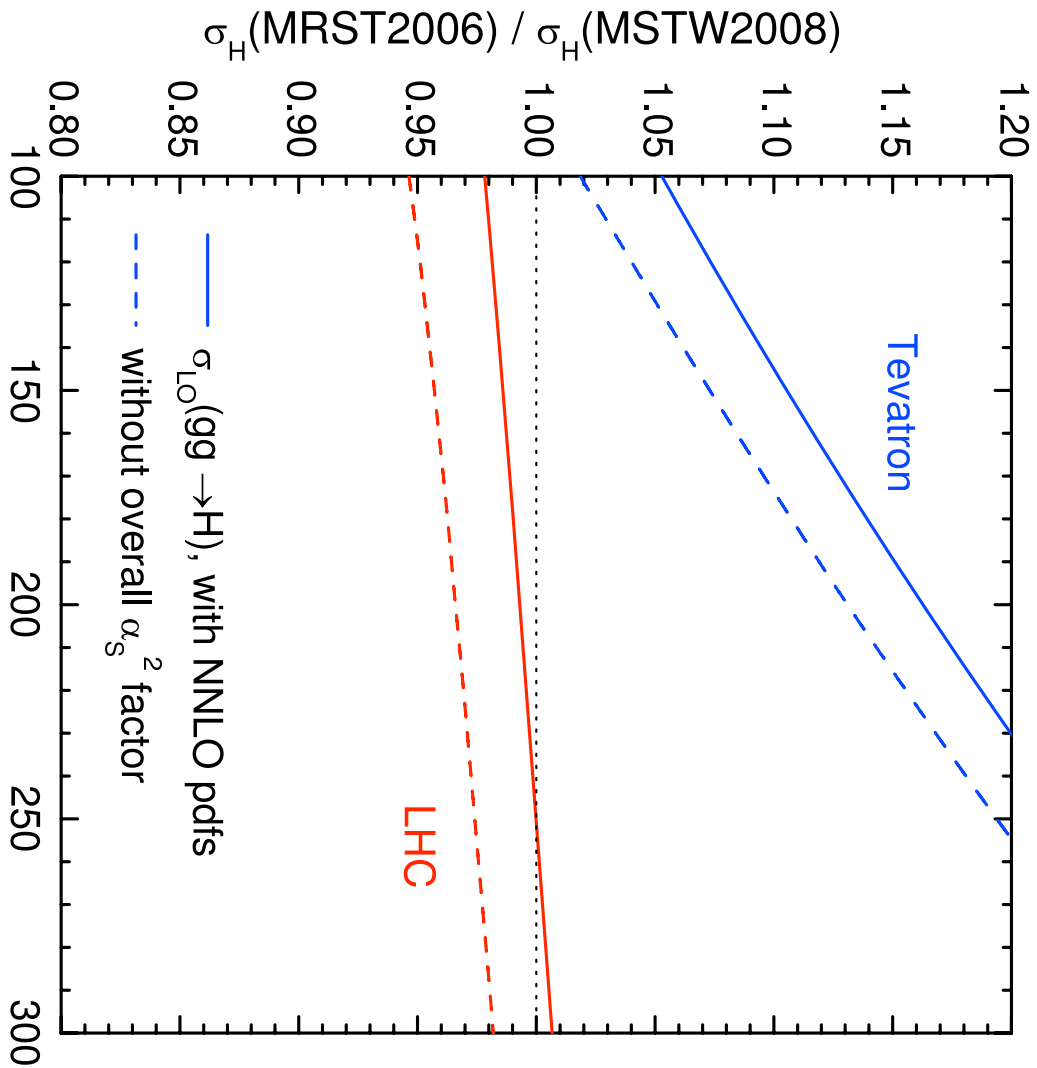
Also consider implications for new physics from updated PDFs.

In **MSTW2008** larger small- $x$  gluon, smaller high- $x$  gluon.

→ decrease in **Higgs** rate at **Tevatron**, slight increase at **LHC** (de Florian *et al*, Anastasiou *et al*).

But largely affected by change in central value of coupling – down **2%** – anticorrelated with small- $x$  gluon. Increases **Tevatron** effect, limits **LHC** effect.

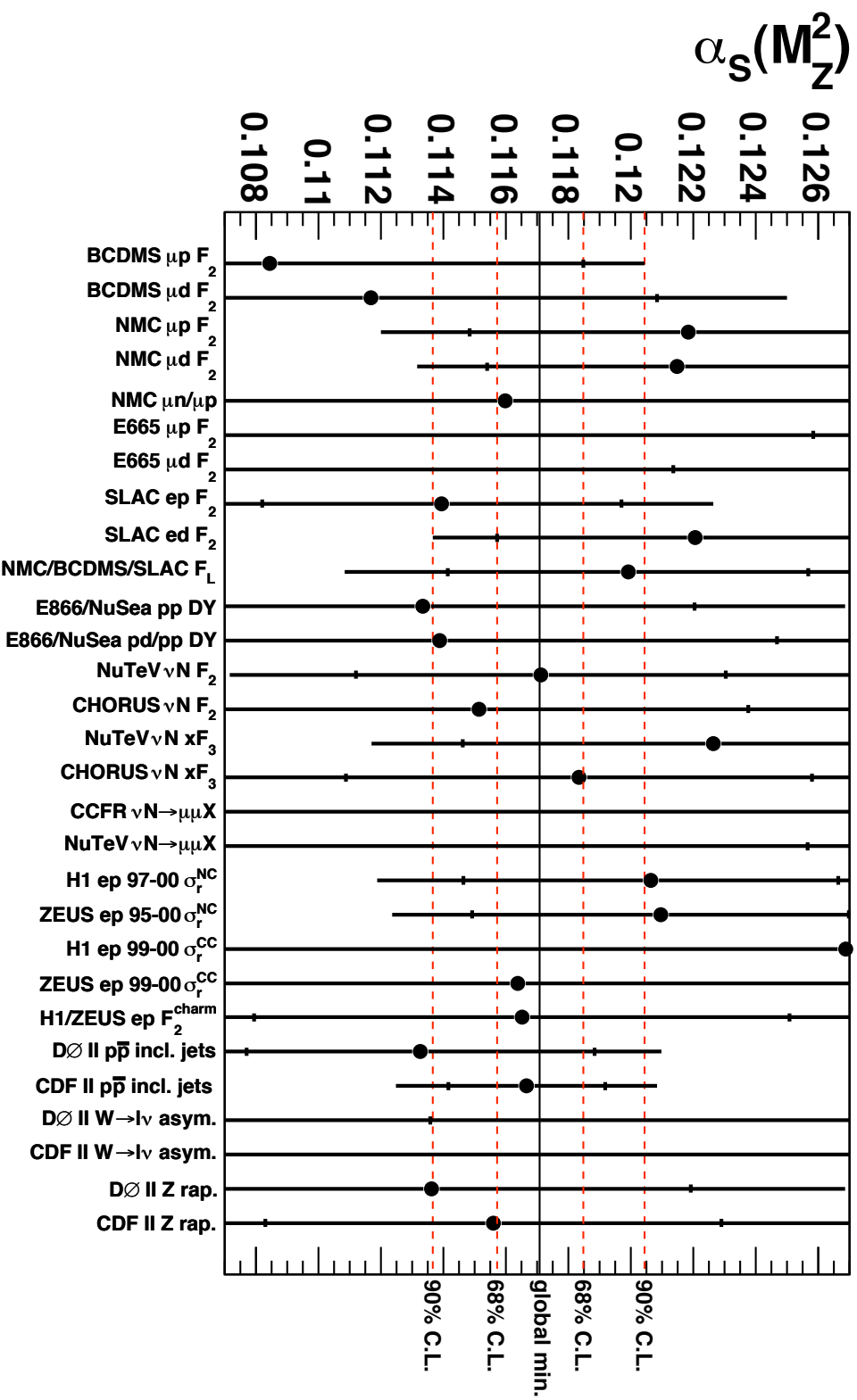
Shows importance of correlations of PDFs and  $\alpha_S(M_Z^2)$ . Not usually considered.



# Uncertainties on PDFs and $\alpha_s(M_Z^2)$ .

Determine uncertainties by scanning over fit quality to different data sets, as with eigenvectors.

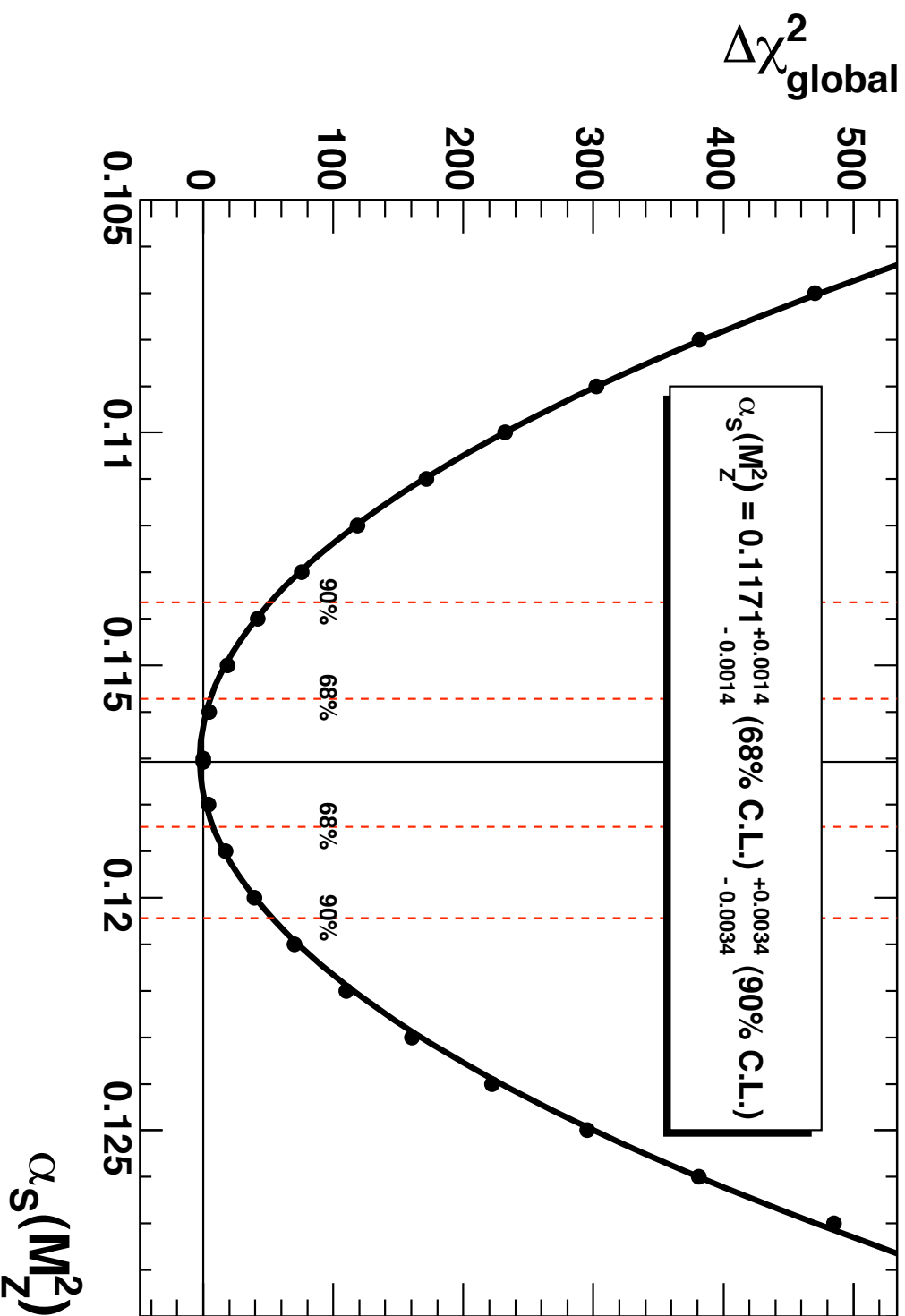
## MSTW 2008 NNLO ( $\alpha_s$ ) PDF fit





Leads to competitive looking uncertainties.

### MSTW 2008 NNLO ( $\alpha_s$ ) PDF fit



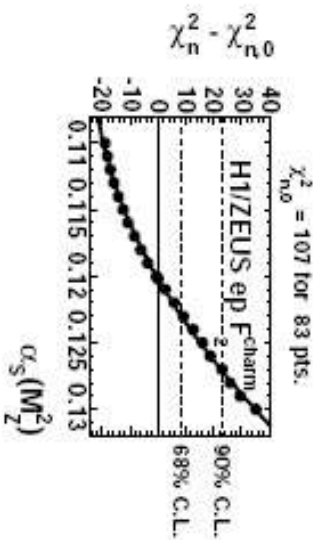
The  $\Delta\chi^2$  profiles for some data sets are stabilised by NNLO corrections.

High- $x$   $F_L(x, Q^2)$  data receive large positive NNLO corrections, mimicked by large  $\alpha_S$  at NLO.

HERA  $F_2^{cc}(x, Q^2)$  data prefer slope predicted at NNLO – difficult to achieve at NLO.

E866 Drell-Yan data more complicated. Prefer NLO normalisation but NNLO shape.

MSTW 2008 NLO ( $\alpha_S$ )



MSTW 2008 NNLO ( $\alpha_S$ )

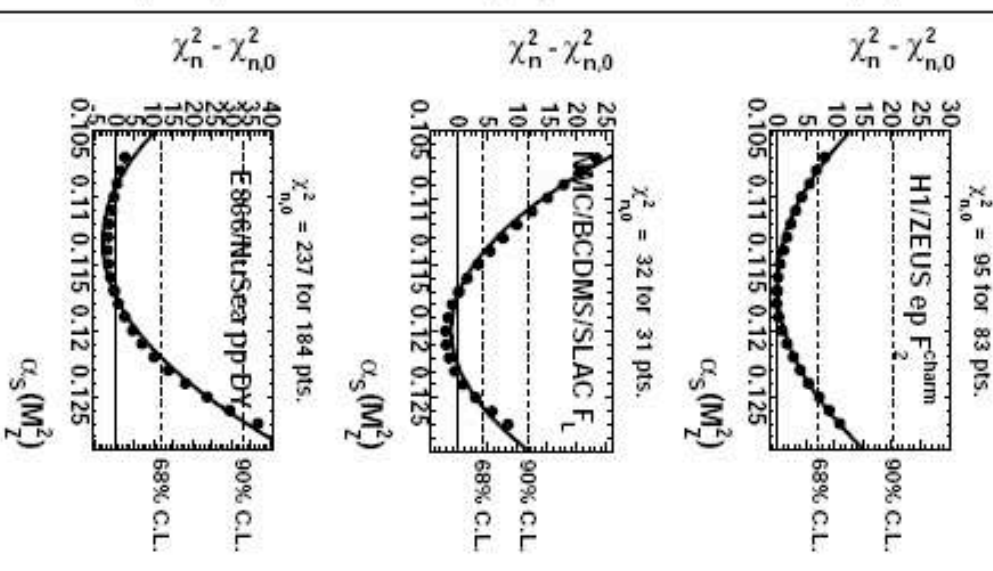
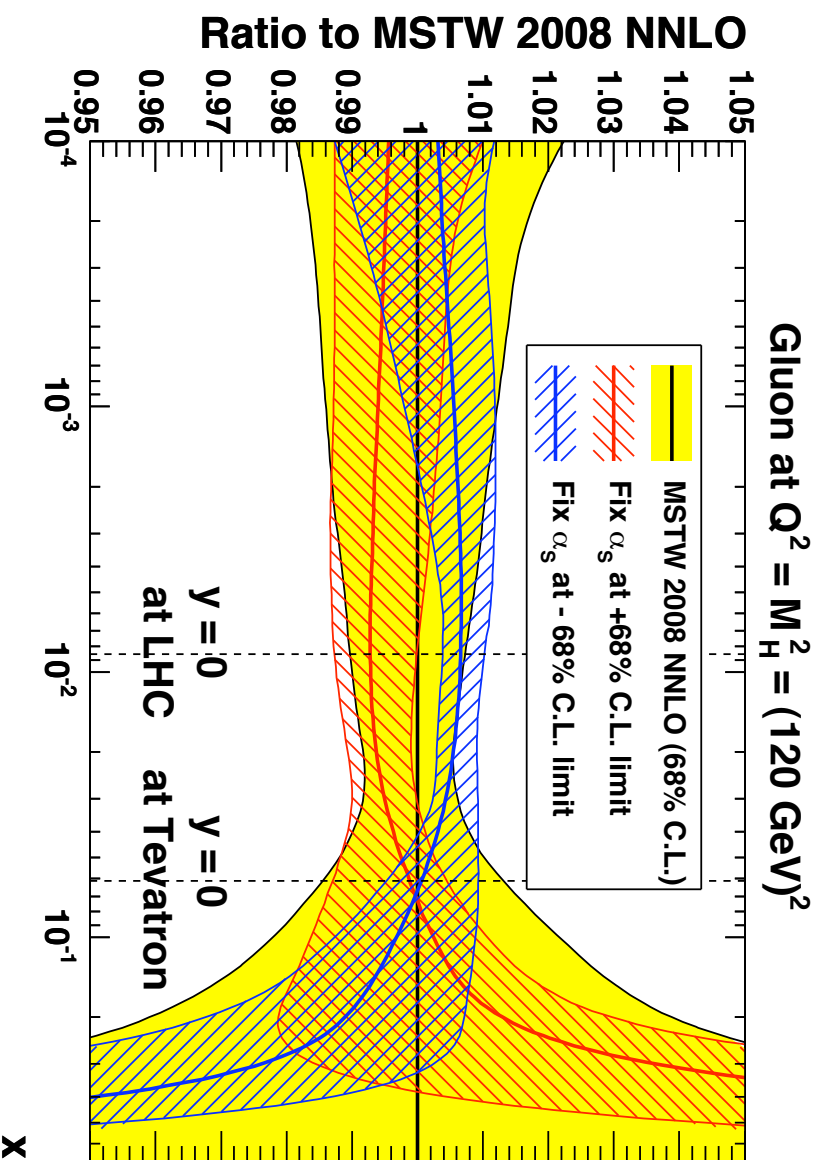


Figure 5: Comparison of selected  $\chi_n^2$  profiles in the NLO (left) and NNLO (right) fits.

Can also look at PDF changes and uncertainties at different  $\alpha_s(M_Z^2)$  values using same technique as before.

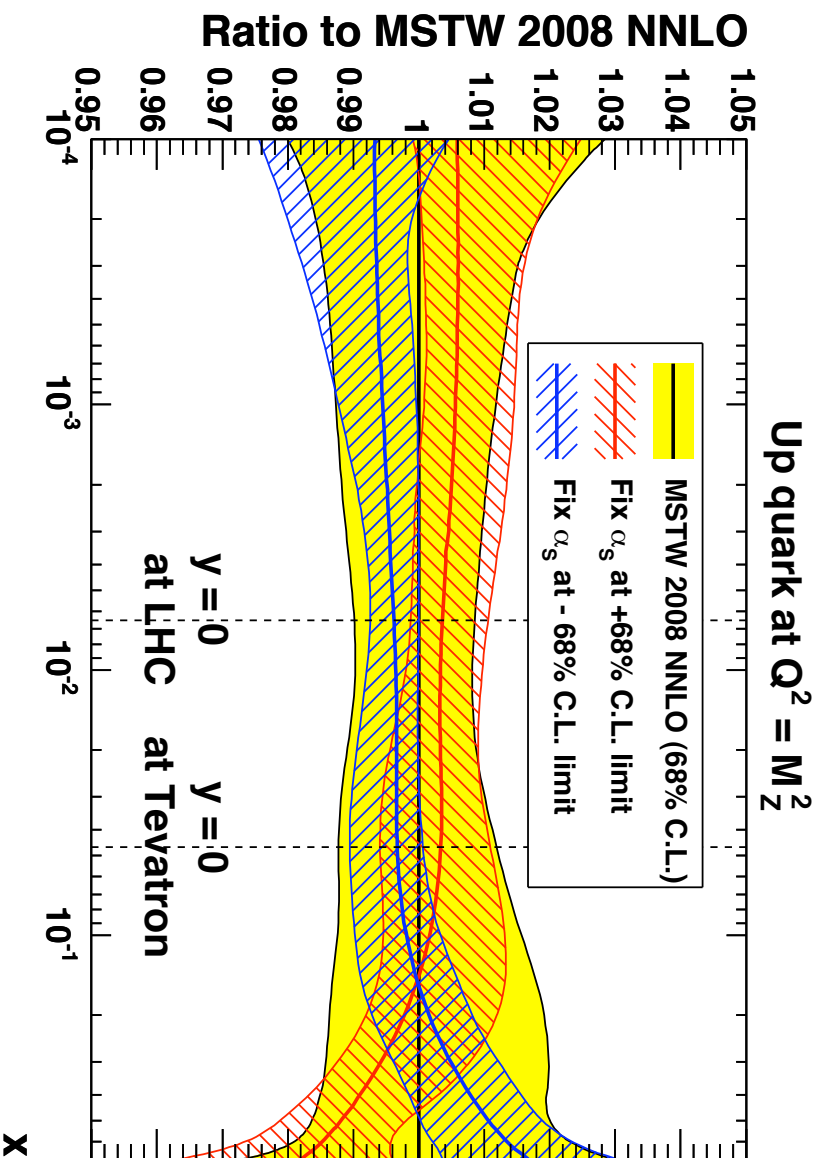
PDF uncertainties reduced since quality of fit already worse than best fit.



Expected gluon— $\alpha_s(M_Z^2)$  small— $x$  anti-correlation  $\rightarrow$  high- $x$  correlation from sum rule.

Variation of gluon largely within central uncertainty band.

Gluon feeds into evolution of quarks, but change in  $\alpha_S(M_Z^2)$  just outweighs gluon change, i.e. larger  $\alpha_S(M_Z^2)$   $\rightarrow$  slightly more evolution.



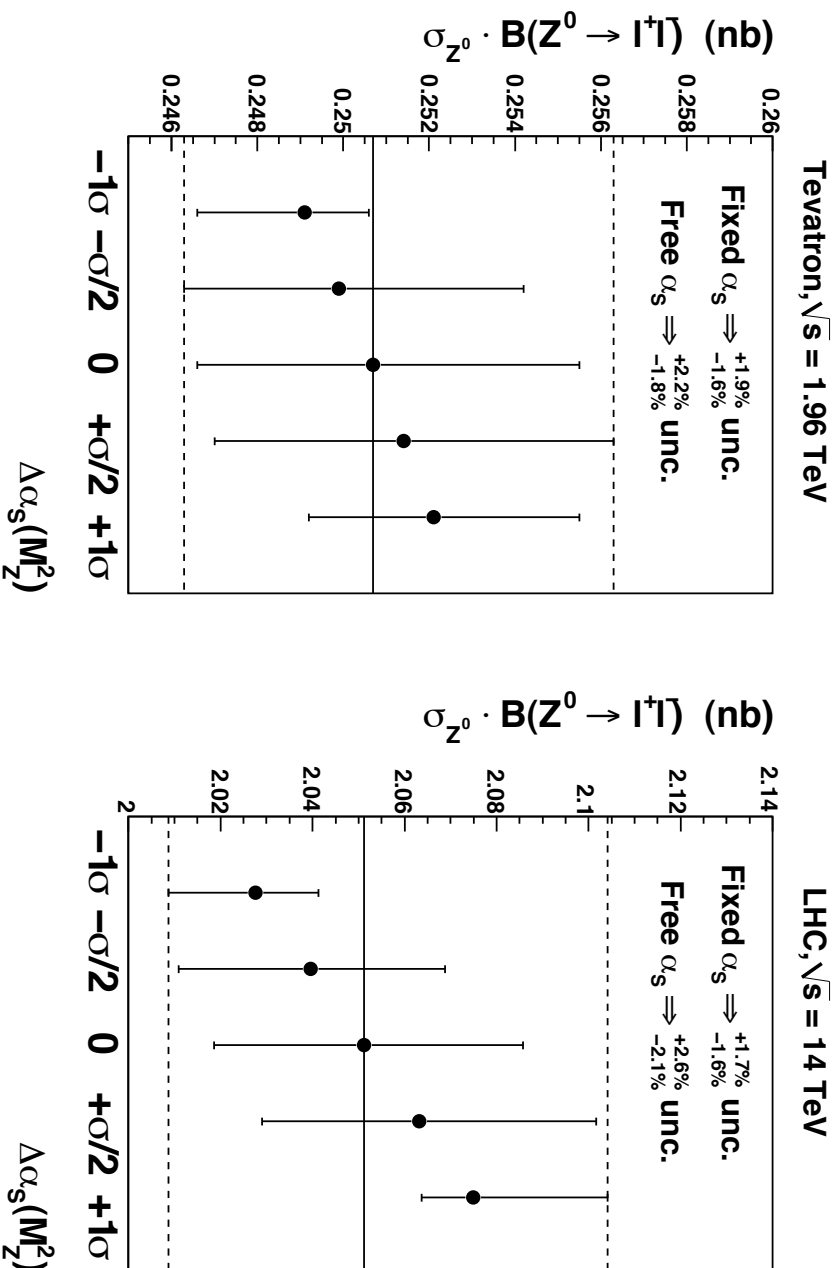
Strong anticorrelation at high- $x$  due to evolution and positive coefficient functions.

Again, changes within, or close to within, initial uncertainties.

Additional uncertainty from  $\alpha_s(M_Z^2)$  variation for quantities depends on how PDFs and coupling are correlated.

NNLO predictions for  $Z$  production for allowed  $\alpha_s(M_Z^2)$  values and their uncertainties.

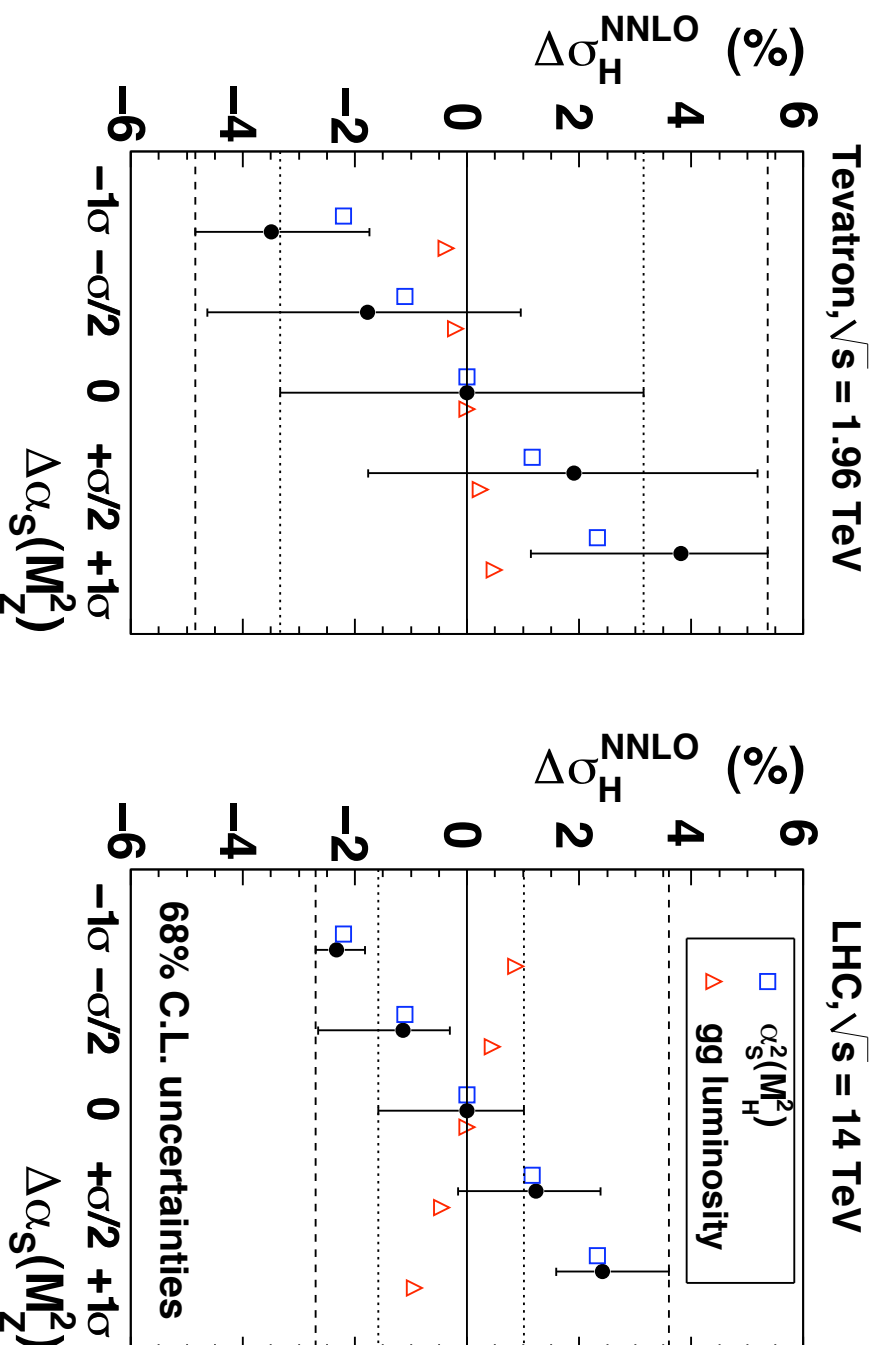
### $Z^0$ cross sections with MSTW 2008 NNLO PDFs



Total uncertainty envelope of set of uncertainties. Increases by up to 50% at LHC. Largely due to effect of PDFs.

NNLO predictions for Higgs (120 GeV) production for different allowed  $\alpha_S(M_Z^2)$  values and their uncertainties.

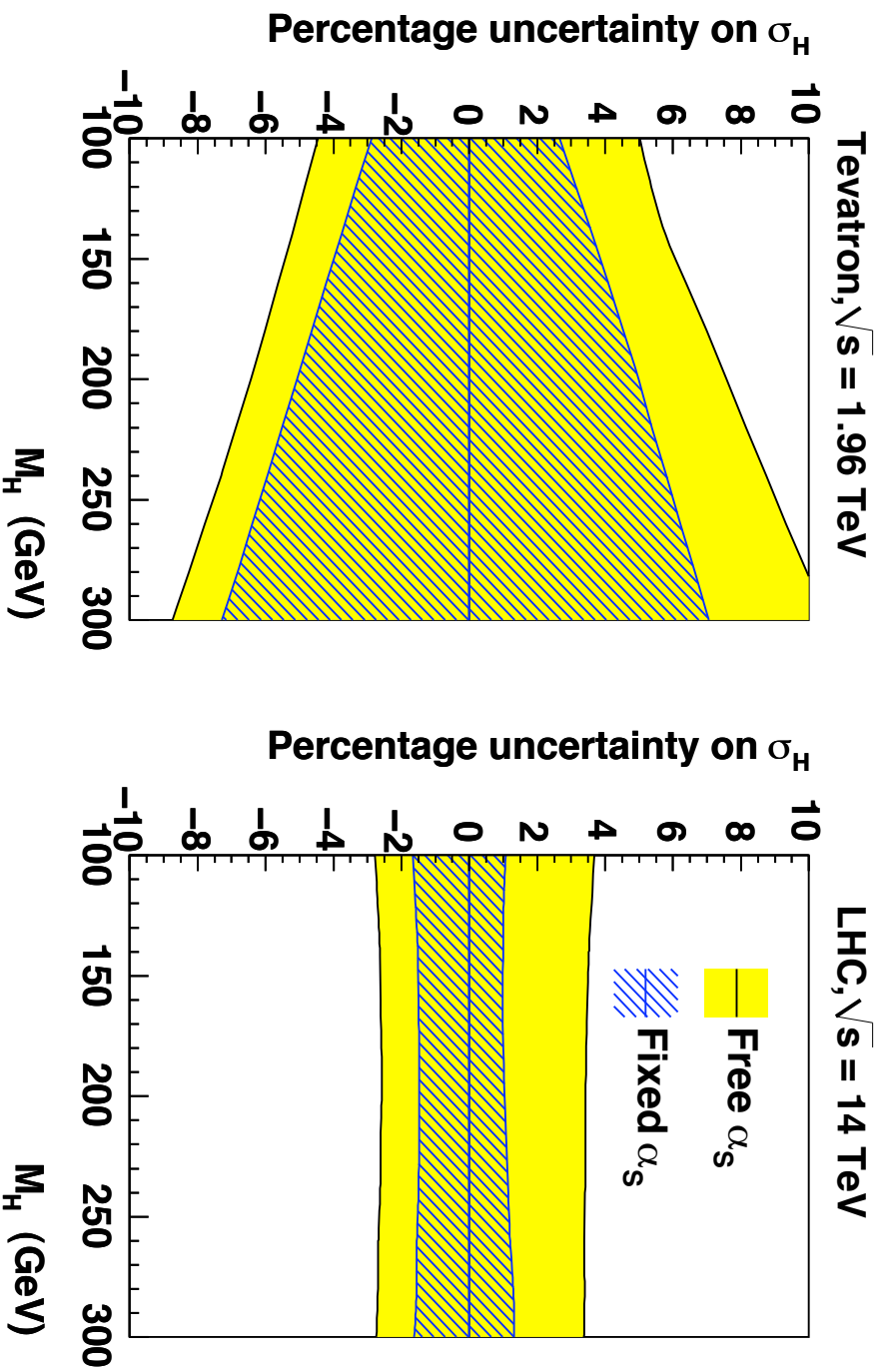
### Higgs ( $M_H = 120$ GeV) with MSTW 2008 NNLO PDFs



Increases by a factor of 2–3 (up more than down) at LHC. Direct  $\alpha_S(M_Z^2)$  dependence mitigated somewhat by anti-correlated small- $x$  gluon (asymmetry feature of *minor* problems in fit to HERA data). At Tevatron intrinsic gluon uncertainty dominates.

Can extend study to a range of Higgs masses. See same features, i.e. intrinsic PDF uncertainty most important at Tevatron and increases with mass (high- $x$  gluon). Roughly constant at LHC with coupling effect large.

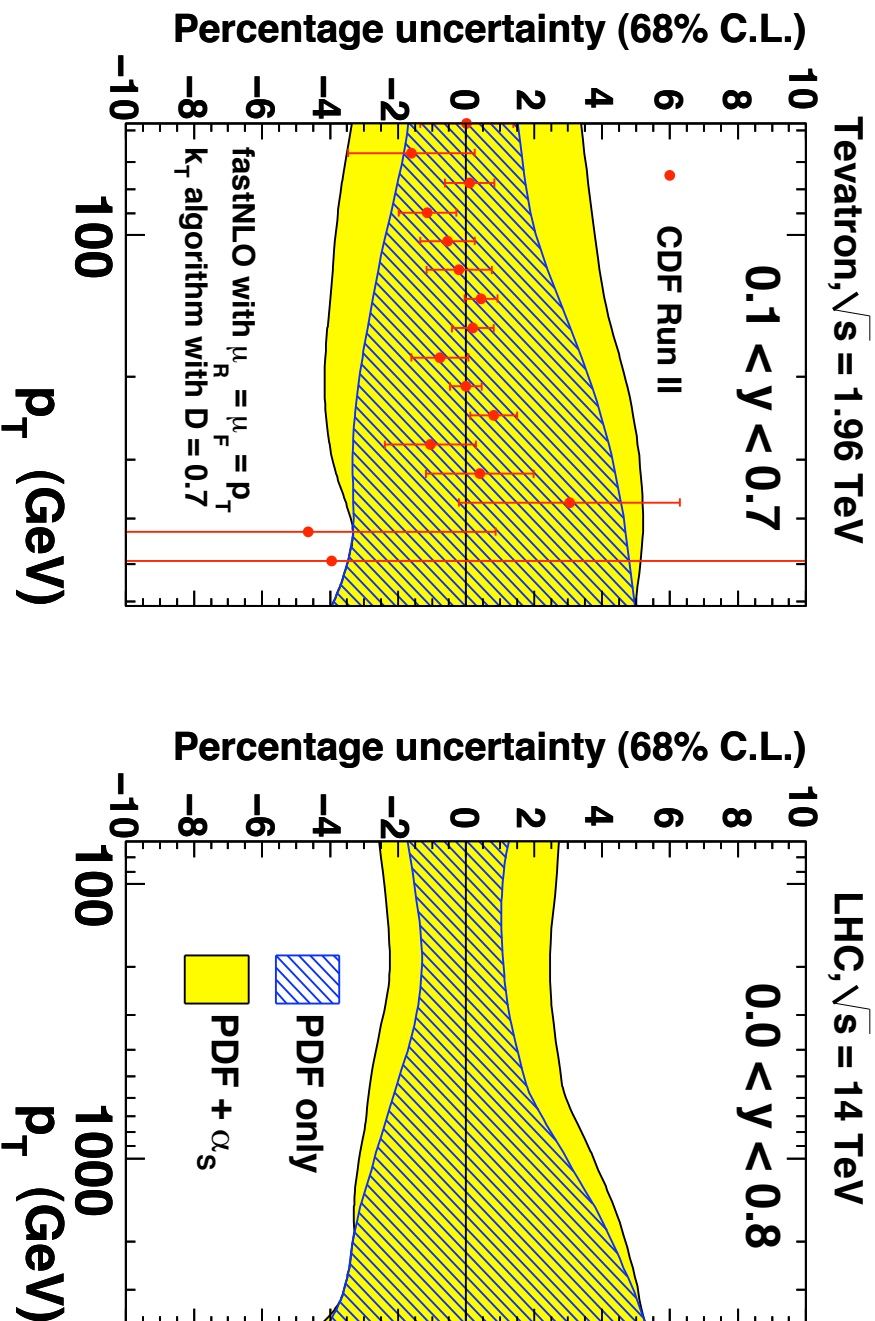
### Higgs cross sections with MSTW 2008 NNLO PDFs



Consistently more PDF- $\alpha_s$  anti-correlation in downwards direction.

Can also investigate uncertainties for inclusive jets at [Tevatron](#) and at [LHC](#).

### Inclusive jet cross sections with MSTW 2008 NLO PDFs



At lower  $p_T$  gluons dominate and  $\alpha_S$  correlated. At higher  $p_T$  quarks become more important and high- $x$  quarks anticorrelated to  $\alpha_S$  so no additional  $\alpha_S$  uncertainty.



## Conclusions

HERA and Tevatron jets now fit using fastNLO. New run II CDF and D0 jet data included. Smaller high- $x$  gluon, larger small- $x$  gluon – impacts on Higgs predictions.

No not find very good agreement between fits including run I and run II Tevatron jet data, 90% uncertainty bands do not overlap at highest  $x$ .

Change in best fit values of  $\alpha_S(M_Z^2)$ . At NLO 0.120 compared to 0.121 in unofficial MRST06 set. At NNLO 0.117 compared to 0.119 in MRST06 set.

Find uncertainty on coupling itself due to experimental errors  $\alpha_S(M_Z^2) = 0.1202^{+0.0012}_{-0.0015}$  at NLO and  $\alpha_S(M_Z^2) = 0.1171^{+0.0014}_{-0.0014}$  at NNLO.

PDF uncertainty approach now being applied with additional  $\alpha_S(M_Z^2)$  variation. As  $\alpha_S(M_Z^2)$  moves away from best-fit value PDF uncertainty band shrinks.

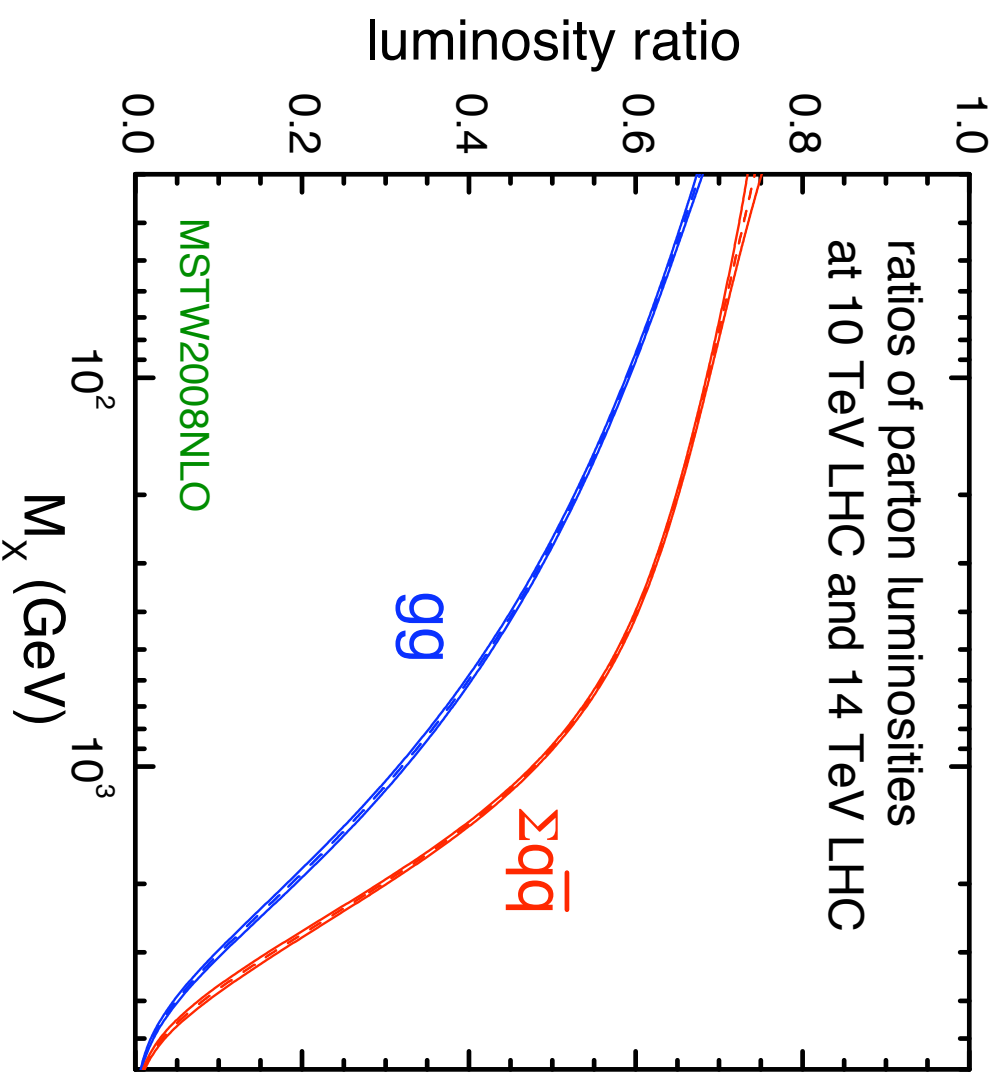
Some PDFs highly correlated, or anti-correlated with  $\alpha_S(M_Z^2)$ .

Full study of correlated PDF and  $\alpha_S$  uncertainty leads to uncertainties at LHC often about 1.5, and up to 3 – 4 times bigger. Correlations vitally important.

## Initial Running

Of course, will be starting the LHC running at 10 TeV rather than the full 14 TeV.

Roughly 60 – 70% the full cross-sections for most standard model (including light Higgs) processes.

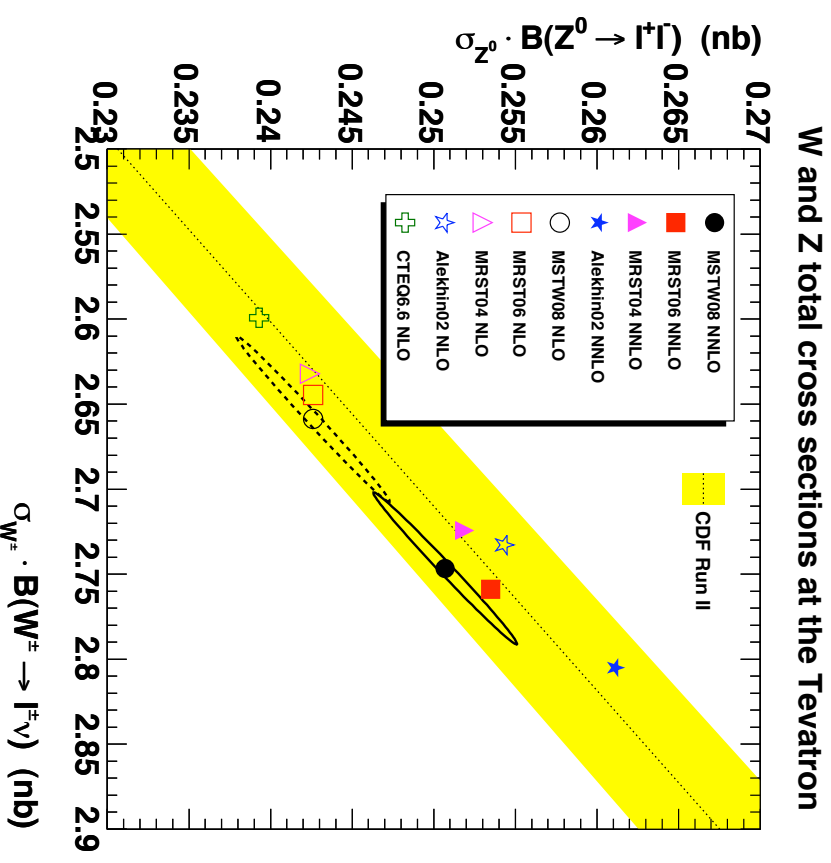


## Predictions – Cross-sections

Predictions for  $W$  and  $Z$  cross-sections for Tevatron with common fixed order  $QCD$  and vector boson width effects, and common branching ratios.

Fairly significant change from NLO to NNLO mainly due to hard cross-section correction.

Other than this reasonable agreement in predictions.

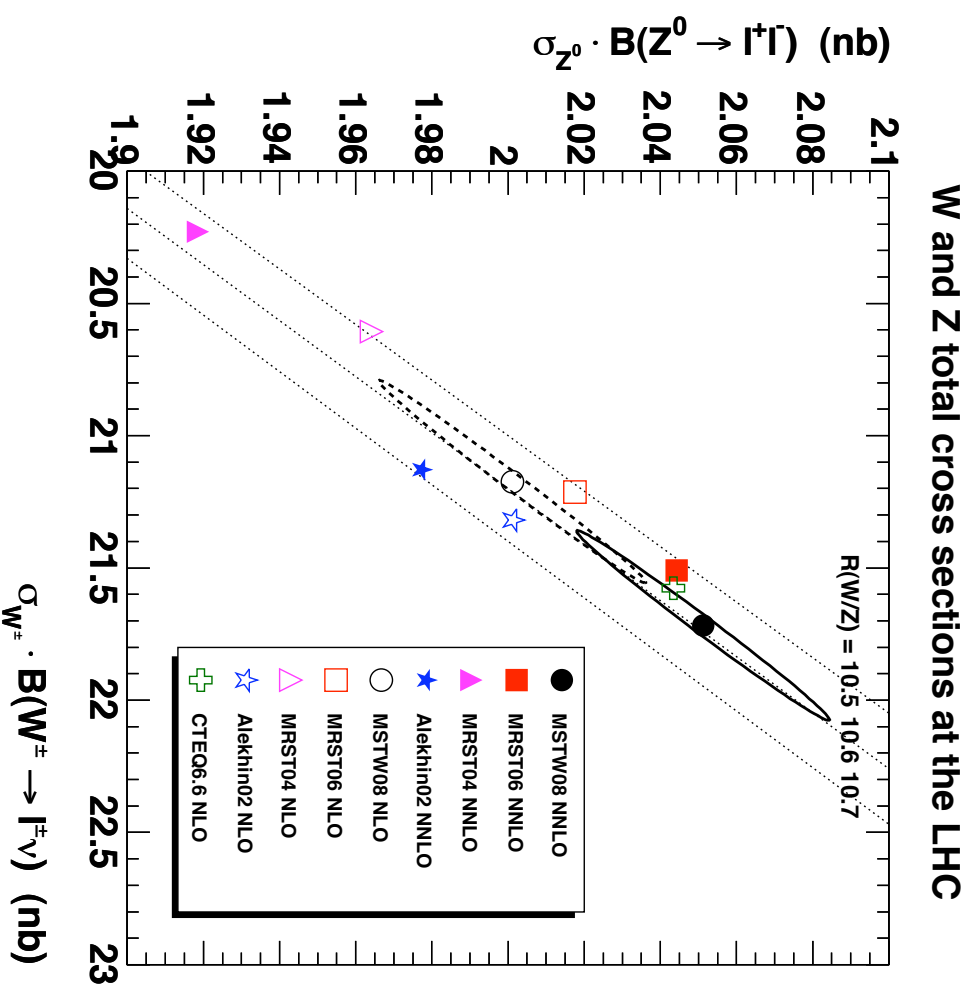


Predictions for  $W$  and  $Z$  cross-sections for Tevatron with common fixed order  $QCD$  and vector boson width effects, and common branching ratios.

Increases from MRST2006 compared to MRST2004 due to changes due to improved (NLO) or completed (NNLO) heavy flavour prescription.

Virtually no change from MRST2006  $\rightarrow$  MRST2008. Ratio changes due to change in strange distribution.

Reasonable agreement at NLO with CTEQ6.6, but systematic difference mirrors shape of gluon/quarks.

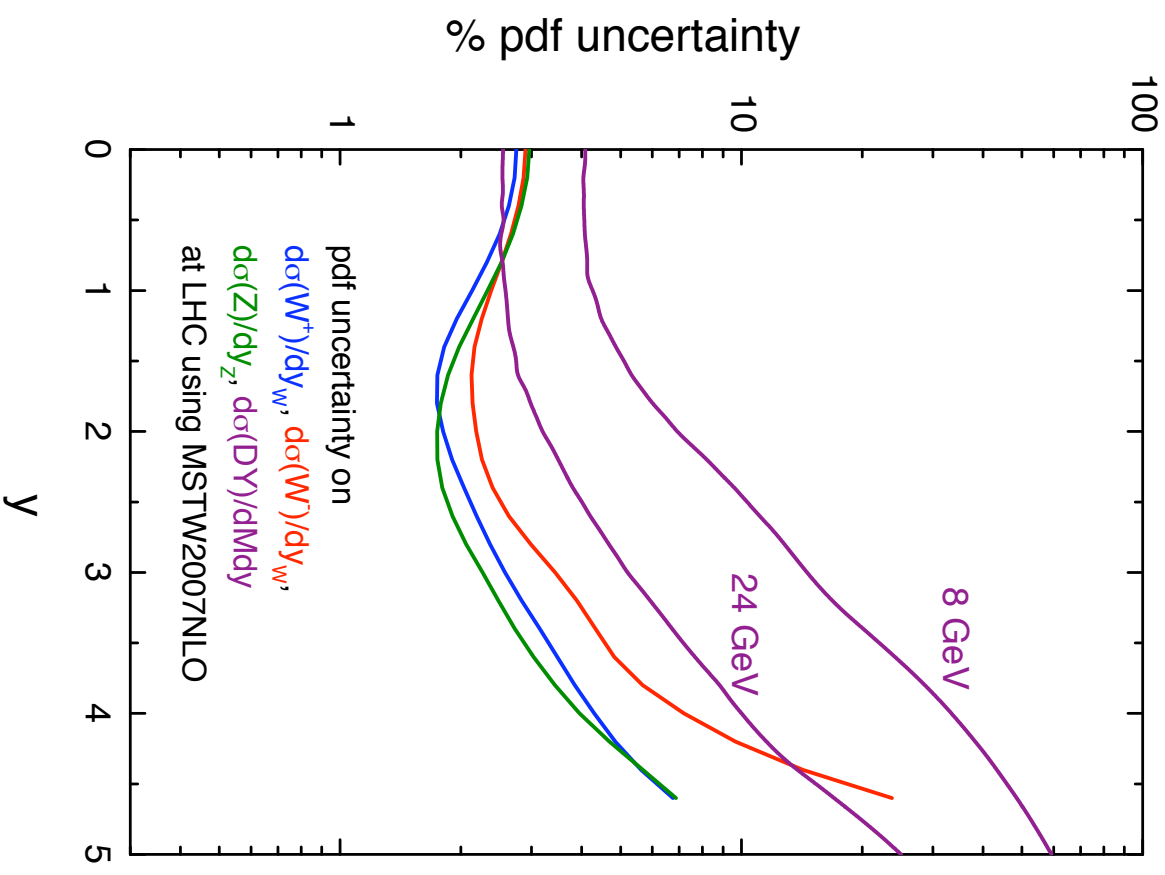


## Uncertainty – more details

Uncertainty on  $\sigma(Z)$  and  $\sigma(W^+)$  grows at high rapidity.

Uncertainty on  $\sigma(W^-)$  grows more quickly at very high  $y$  – depends on less well-known down quark.

Uncertainty on  $\sigma(\gamma^*)$  is greatest as  $y$  increases. Depends on partons at very small  $x$ .



More information from ratios including  $\sigma(Z)$ ,  $\sigma(W^-)$  and  $\sigma(W^+)$ .

Cleaner experimentally.

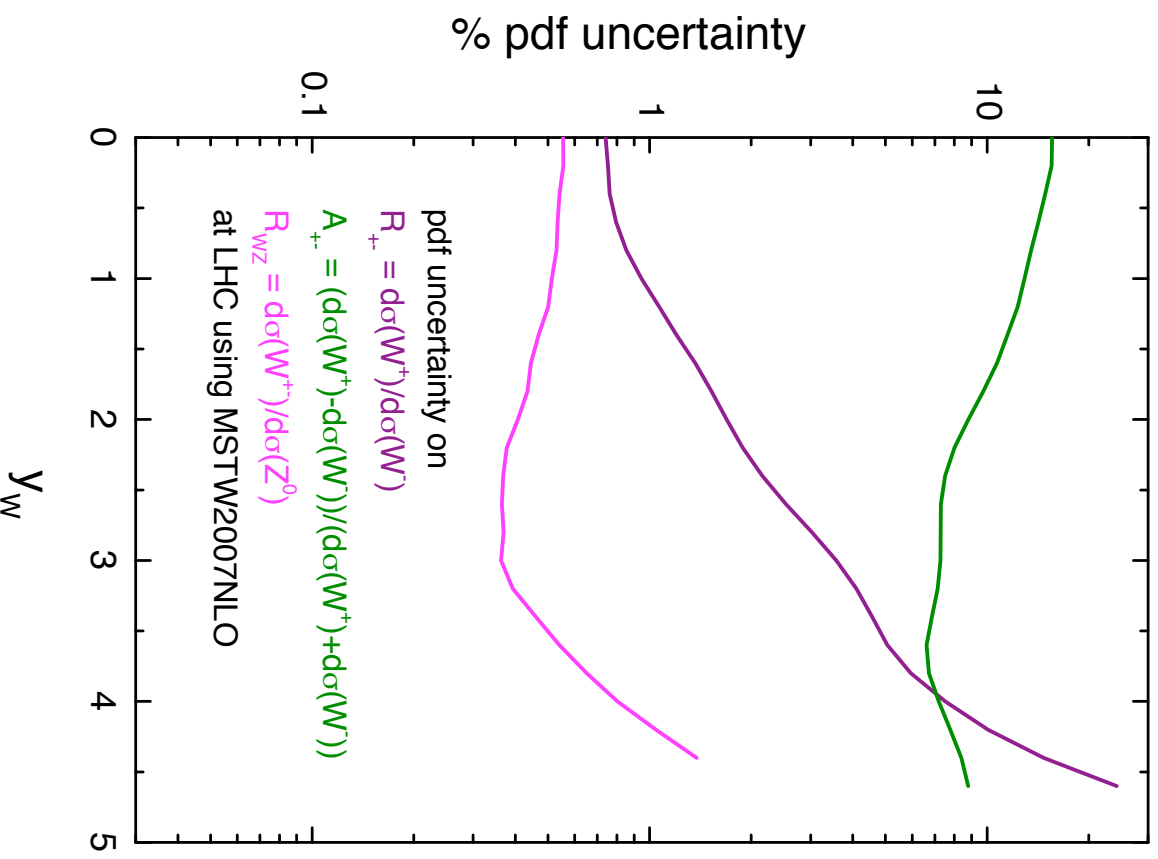
Uncertainty on  $A_W$  large even just from experimental sources.

But  $y = 0$  is  $x_1 = x_2 = 0.006$

– range of extrapolation of valence quarks. Differences in different PDF extractions.

One of most useful inputs to PDFS with very little data.

Extremely small uncertainty on ratios  $W/Z$  and  $W^+/W^-$ .

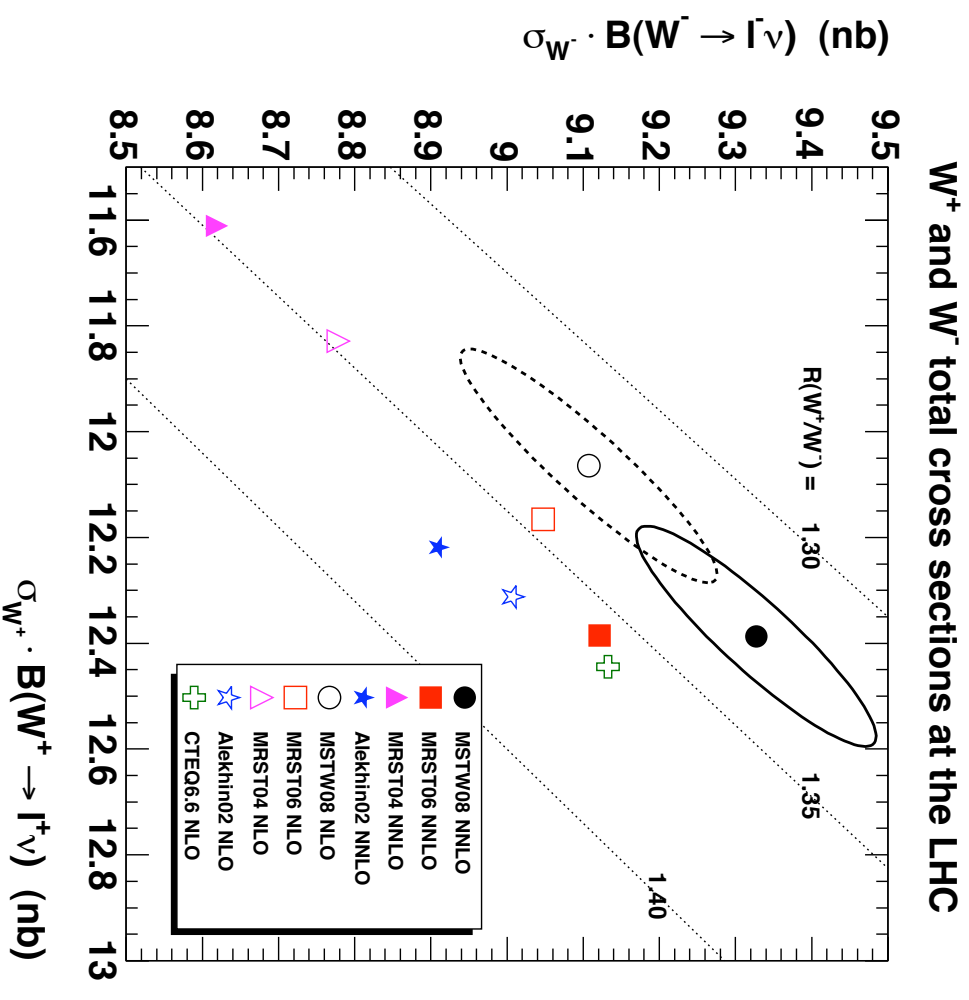


Predictions for  $W^+$  and  $W^-$  cross-sections for LHC with common fixed order  $QCD$  and vector boson width effects, and common branching ratios.

Quoted uncertainty for ratio very small, i.e.  $\approx 0.8\%$ .

Significantly more difference in this from other PDFs, including MRST.

Again very interesting for early data.



# Perturbative Stability at the LHC

Now have **QCD** calculations at **LO**, **NLO** and **NNLO** in the coupling constant  $\alpha_S$  for  $Z, W$  and  $\gamma^*$  production **Anastasiou, Dixon, Melnikov, Petriello**).

Good stability in predictions for e.g.  $Z$  and  $\gamma^*$  cross-sections for very high virtuality.

Becomes worse at lower scales where  $\alpha_S$  larger and large  $\ln(s/M^2)$  terms appear in expansion (equivalent to  $\ln(1/x)$ ) and large threshold  $\ln(1-x)$  terms.

## $\gamma^*/Z$ rapidity distributions at LHC

