



General treatment of theory uncertainties in kinematic bins

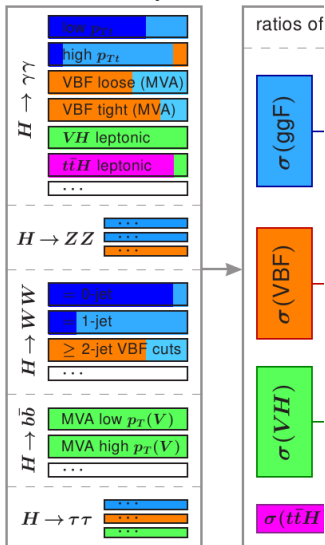
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WG1 ggF subgroup meeting: uncertainties in kinematic regions

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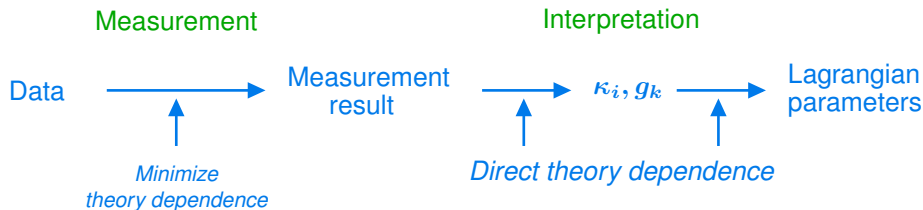
Treatment of theoretical uncertainties in Run1 coupling measurements.

Schematically



- Higgs coupling measurements extract signal strengths (μ) or cross sections per production mode (Run1 combination paper)
 - Main sources of theoretical uncertainty from missing higher order QCD corrections, PDFs, underlying event and parton shower modeling, Higgs BRs
 - In practice estimated from variations of predicted signal yield for the different experimental event categories or global scaling of $(\sigma \cdot \mathcal{B})^{\text{SM}}$
 - Uncertainties implemented as nuisance parameters that can be
 - ★ 100% correlated (“yield”)
 - ★ 100% anticorrelated (“migration”)
 - ★ uncorrelated
- between different event categories (across decay channels)

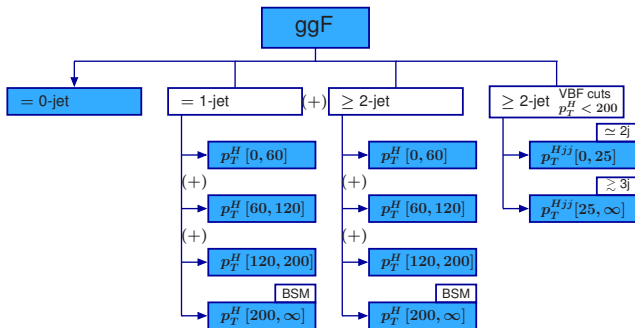
Separating uncertainties in measurement and interpretation.



- Run1 coupling measurements: theory uncertainties folded into the measurement
 - ★ Cross section measurements not affected by uncertainties that are a global scaling of $(\sigma \cdot \mathcal{B})^{\text{SM}}$
 - ★ Uncertainties related to event categorization (e.g. jet bins) completely entangled into measurement
- Define “intermediate layer” between data and interpretation with reduced theory dependence
 - ★ Improvements in theoretical predictions and uncertainties can be more easily taken advantage of

Simplified template cross sections (STXS).

- Measurement of cross sections per production mode in kinematic “bins”
- Most relevant for ggF: jet bin uncertainties, Higgs p_T shape, ggF with VBF topology (background in VBF selection)
- Reducing these uncertainties in the measurement is what guided the definitions of the bins
- Residual theoretical uncertainties related to “unfolding” experimental event categories to STXS “bins”



Treatment of theoretical uncertainties kinematic bins.

- Implementation of uncertainties (in measurement or interpretation) requires to have uncertainties per bin, and their correlations
 - ★ Particularly important when binning introduces source of uncertainties that affects each bin but cancels in their sum
 - ★ Implementation of $\pm 100\%$ correlated or uncorrelated nuisance parameters
- Identify and distinguish different sources of uncertainties and evaluate also their corrections between kinematic bins
- Discussion follows YR4 Section 1.4.2a
 - ★ Use jet bins as example
 - ★ Single bin boundary
 - ▶ Familiar from Run1
 - ★ Extension to multiple bin boundaries

Single bin boundary.

- Jet bin example: split total cross section into exclusive 0-jet ($\sigma_0(p_T^{\text{cut}})$) and inclusive 1-jet ($\sigma_{\geq 1}(p_T^{\text{cut}})$) by $p_T^{\text{jet}} \geq p_T^{\text{cut}}$:

$$\sigma_{\geq 0} = \sigma_0(p_T^{\text{cut}}) + \sigma_{\geq 1}(p_T^{\text{cut}})$$

- Uncertainties can be described in terms of fully correlated and fully anticorrelated components:

$$C(\{\sigma_0, \sigma_{\geq 1}\}) = \begin{pmatrix} (\Delta_0^y)^2 & \Delta_0^y \Delta_{\geq 1}^y \\ \Delta_0^y \Delta_{\geq 1}^y & (\Delta_{\geq 1}^y)^2 \end{pmatrix} + \begin{pmatrix} \Delta_{\text{cut}}^2 & -\Delta_{\text{cut}}^2 \\ -\Delta_{\text{cut}}^2 & \Delta_{\text{cut}}^2 \end{pmatrix}$$

- General parametrization of a 2×2 symmetric matrix, not specific to any particular calculation or framework
- Straightforward implementation in terms of nuisance parameters κ for $\{\sigma_{\geq 0}, \sigma_0, \sigma_{\geq 1}\}$:

$$\kappa^y : \quad \{\Delta_{\geq 0}^y, \Delta_0^y, \Delta_{\geq 1}^y\} \quad \kappa_{\text{cut}} : \quad \{0, \Delta_{\text{cut}}, -\Delta_{\text{cut}}\},$$

- Physical interpretation: (correlated) yield and (anticorrelated) migration uncertainties

Single bin boundary: application to jet bins at FO.

- No unambiguous way to identify different sources for Δ^y and Δ_{cut} for fixed-order predictions
- Different frameworks make different assumptions

FO-ST

$$\Delta_0^y = \Delta_{\geq 0}^y = \Delta_{\geq 0}^{\text{FO}}, \quad \Delta_{\geq 1}^y = 0, \quad \Delta_{\text{cut}} = \Delta_{\geq 1}^{\text{FO}}$$

- Migration uncertainty is approximated by perturbative uncertainty of $\sigma_{\geq 1}(p_T^{\text{cut}})$, motivated by structure of perturbative series
- Perturbative uncertainties in $\sigma_{\geq 0}$ and $\sigma_{\geq 1}$ treated as independent sources

JVE

- Perturbative uncertainties of $\epsilon_0 = \sigma_0(p_T^{\text{cut}})/\sigma_{\geq 0}$ and $\sigma_{\geq 0}$ treated as independent sources

$$\Delta_{\geq 0}^y = \Delta_{\geq 0}^{\text{FO}}, \quad \Delta_0^y = \epsilon_0 \Delta_{\geq 0}^{\text{FO}}$$

$$\Delta_{\geq 1}^y = (1 - \epsilon_0) \Delta_{\geq 0}^{\text{FO}}, \quad \Delta_{\text{cut}} = \sigma_{\geq 0} \Delta(\epsilon_0)$$

Multiple bin boundaries.

- Each bin can have multiple boundaries, and each boundary can be shared by different bins
- 2×2 covariance matrix decomposition applied to any single bin boundary when all additional subdivisions are removed
- Consider binning cut “a/b” with $\sigma_{ab} = \sigma_a + \sigma_b$ and associated $\Delta_{\text{cut}}^{a/b}$ (anticorrelated between σ_a and σ_b)
- Allow for additional subbins such that $\sigma_a = \sum_i \sigma_a^i$ and $\sigma_b = \sum_j \sigma_b^j$
- Consider binning uncertainty as fully correlated among subbins and implement with a single nuisance parameter

$$\kappa_{\text{cut}}^{a/b} : \Delta_{\text{cut}}^{a/b} \times \{ \{x_a^i\}, -\{x_b^j\} \} \quad \text{with} \quad \sum_i x_a^i = \sum_j x_b^j = 1$$

where x_a^i and x_b^j specify how $\Delta_{\text{cut}}^{a/b}$ gets distributed among the subbins

- Consider each binning cut/bin boundary as source for migration cut
- In addition, one or more correlated yield uncertainties

Multiple bin boundaries: example.

- 3 mutually exclusive jet bins: $\{\sigma_0, \sigma_1, \sigma_{\geq 2}\}$
- Identify 2 boundaries: $\sigma_{\geq 0} = \sigma_0 + \sigma_{\geq 1}$ and $\sigma_{\geq 1} = \sigma_1 + \sigma_{\geq 2}$
- Nuisance parameters for five observables $\{\sigma_{\geq 0}, \sigma_0, \sigma_{\geq 1}, \sigma_1, \sigma_{\geq 2}\}$

$$\kappa^y : \{\Delta_{\geq 0}^y, \Delta_0^y, \Delta_{\geq 1}^y, \Delta_1^y, \Delta_{\geq 2}^y\} \text{ with}$$

$$\Delta_{\geq 0}^y = \Delta_0^y + \Delta_{\geq 1}^y, \quad \Delta_{\geq 1}^y = \Delta_1^y + \Delta_{\geq 2}^y$$

$$\kappa_{\text{cut}}^{0/1} : \Delta_{\text{cut}}^{0/1} \times \{0, 1, -1, -(1 - x_1), -x_1\}$$

$$\kappa_{\text{cut}}^{1/2} : \Delta_{\text{cut}}^{1/2} \times \{0, x_2, -x_2, 1 - x_2, -1\}$$

- ★ x_1 determines how $\Delta_{\text{cut}}^{0/1}$ is split between σ_1 and $\sigma_{\geq 2}$
- ★ x_2 determines how $\Delta_{\text{cut}}^{1/2}$ is split between σ_0 and σ_1
- Independent of particular theory framework, and maintains interpretation in terms of underlying physical sources
 - ★ Allows to judge correlations between different observables
 - ★ Associate each source with one nuisance parameter