

# Jet-vetoed Higgs cross section in gluon fusion at $N_3\text{LO}+\text{NNLL}+\text{LL}_R$

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Work in collaboration with A. Banfi, F. Caola, F. Dreyer, F. Dulat, G. Salam and G. Zanderighi  
[1511.02886]

# Outline: the 0-jet cross section

[Anastasiou, Duhr, Dulat, Herzog, Mistlberger 1503.06056]

[Anastasiou et al. 1602.00695]

[Boughezal, Caola, Melnikov, Petriello, Schulze 1504.07922]

[Boughezal, Focke, Giele, Liu, Petriello 1505.03893]

[Chen, Cruz-Martinez, Gehrmann, Glover, Jaquier 1607.08817]

total cross section  
@ N3LO

~3% increase at 13 TeV  
for  $\mu_R = \mu_F = m_H/2$

H+1jet @ NNLO

~5% increase at veto  
scales for  $\mu_R = \mu_F = m_H/2$

NNLL resummation

[Banfi, PM, Salam, Zanderighi 1206.4998]

[Becher, Neubert, Rothen 1307.0025]

[Stewart, Tackmann, Walsh, Zuberi 1307.1808]

Quark-mass  
effects

[Banfi, PM, Zanderighi 1308.4634]

[Mantler, Wiesemann 1210.8263]

[Grazzini, Sargsyan 1306.4581]

LL small-R  
resummation

[Dasgupta, Dreyer, Salam, Soyez 1411.5182]

# Uncertainties with the JVE method

- Matched predictions for the 0-jet cross section have a more reliable error estimate. Different sources of uncertainty can be probed independently through variations of the appropriate scales (i.e. renorm./factor. scales vs. resummation scale  $Q$ )
- However, one would like a method for the determination of the uncertainties of exclusive cross sections which is:
  - robust against the inclusion of sizeable unknown effects, for instance exact quark-mass effects
  - reliable (i.e. resilient to accidental cancellations) even when the resummation is not available (e.g. combination of different jet multiplicities)
  - Not overly conservative in any kinematic regime

# Uncertainties with the JVE method

- Jet Veto Efficiency (JVE) method's synopsis:

[Banfi, Salam, Zanderighi 1203.5773]

- **JVE is a ratio of perturbative quantities** - i.e. it admits a number of possible definitions at each perturbative order

$$\sigma_{\text{tot},n} = \sum_{i=0}^n \sigma^{(i)}, \quad \Sigma(p_{t,\text{veto}}) = \sigma^{(0)} + \sum_{i=1}^n \Sigma^{(i)}(p_{t,\text{veto}})$$

$$\Sigma^{(i)}(p_{t,\text{veto}}) = \sigma^{(i)} + \bar{\Sigma}^{(i)}(p_{t,\text{veto}}) \quad \bar{\Sigma}^{(i)}(p_{t,\text{veto}}) = - \int_{p_{t,\text{veto}}}^{\infty} dp_t \frac{d\Sigma^{(i)}(p_t)}{dp_t}$$

- In the large-logarithms region, **JVE's uncertainty is dominated by Sudakov effects** - i.e. uncertainties uncorrelated with the error in the total cross section

$$\Sigma(p_{t,\text{veto}}) = \epsilon(p_{t,\text{veto}})\sigma_{\text{tot}} \quad \delta\Sigma(p_{t,\text{veto}}) = \sqrt{\epsilon^2 \delta^2 \sigma_{\text{tot}} + \delta^2 \epsilon \sigma_{\text{tot}}^2}$$

# Uncertainties with the JVE method

- e.g. at NNLO, three different efficiency schemes are available

$$\epsilon_{\text{NNLO}}^{(a)}(p_{\text{t,veto}}) = 1 + \frac{1}{\sigma_{\text{tot},2}} \sum_{i=1}^2 \bar{\Sigma}^{(i)}(p_{\text{t,veto}}),$$

Spread between schemes sensitive to the convergence of *all* previous orders

$$\epsilon_{\text{NNLO}}^{(b)}(p_{\text{t,veto}}) = 1 + \frac{1}{\sigma_{\text{tot},1}} \sum_{i=1}^2 \bar{\Sigma}^{(i)}(p_{\text{t,veto}}),$$

$$\epsilon_{\text{NNLO}}^{(c)}(p_{\text{t,veto}}) = 1 + \frac{1}{\sigma_{\text{tot},0}} \left[ \sum_{i=1}^2 \bar{\Sigma}^{(i)}(p_{\text{t,veto}}) - \frac{\sigma^{(1)}}{\sigma_{\text{tot},0}} \bar{\Sigma}^{(1)}(p_{\text{t,veto}}) \right]$$

- Resummation fits in naturally (each efficiency scheme corresponds to a different matching scheme), providing a better control of Sudakov effects, i.e. **reducing the spread between different efficiency schemes (separation of uncertainty sources)**

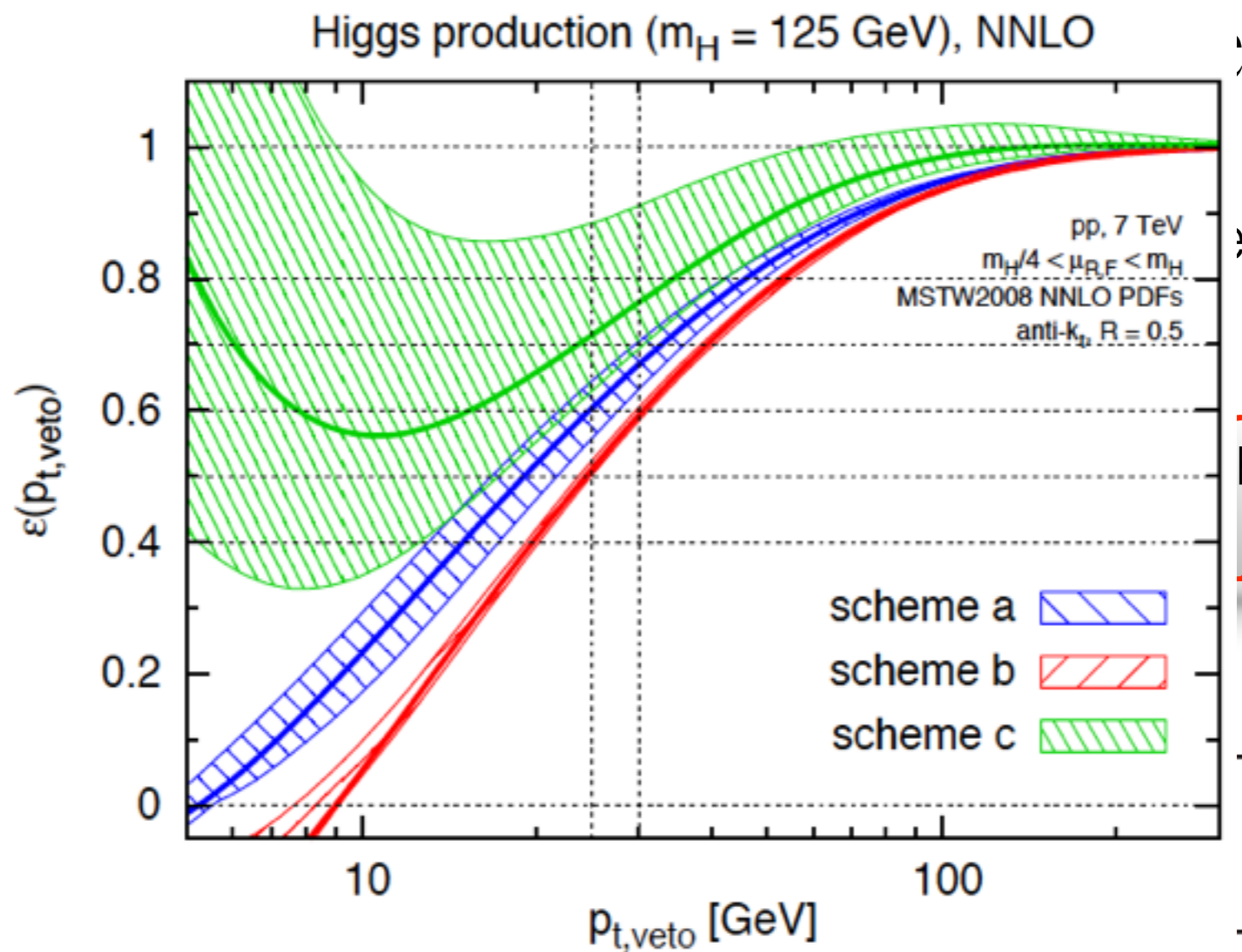
$U_1$

- e.g. a

$$\epsilon_{\text{NNLO}}^{(a)}(p_{t,\text{veto}})$$

$$\epsilon_{\text{NNLO}}^{(b)}(p_{t,\text{veto}})$$

$$\epsilon_{\text{NNLO}}^{(c)}(p_{t,\text{veto}})$$



Method

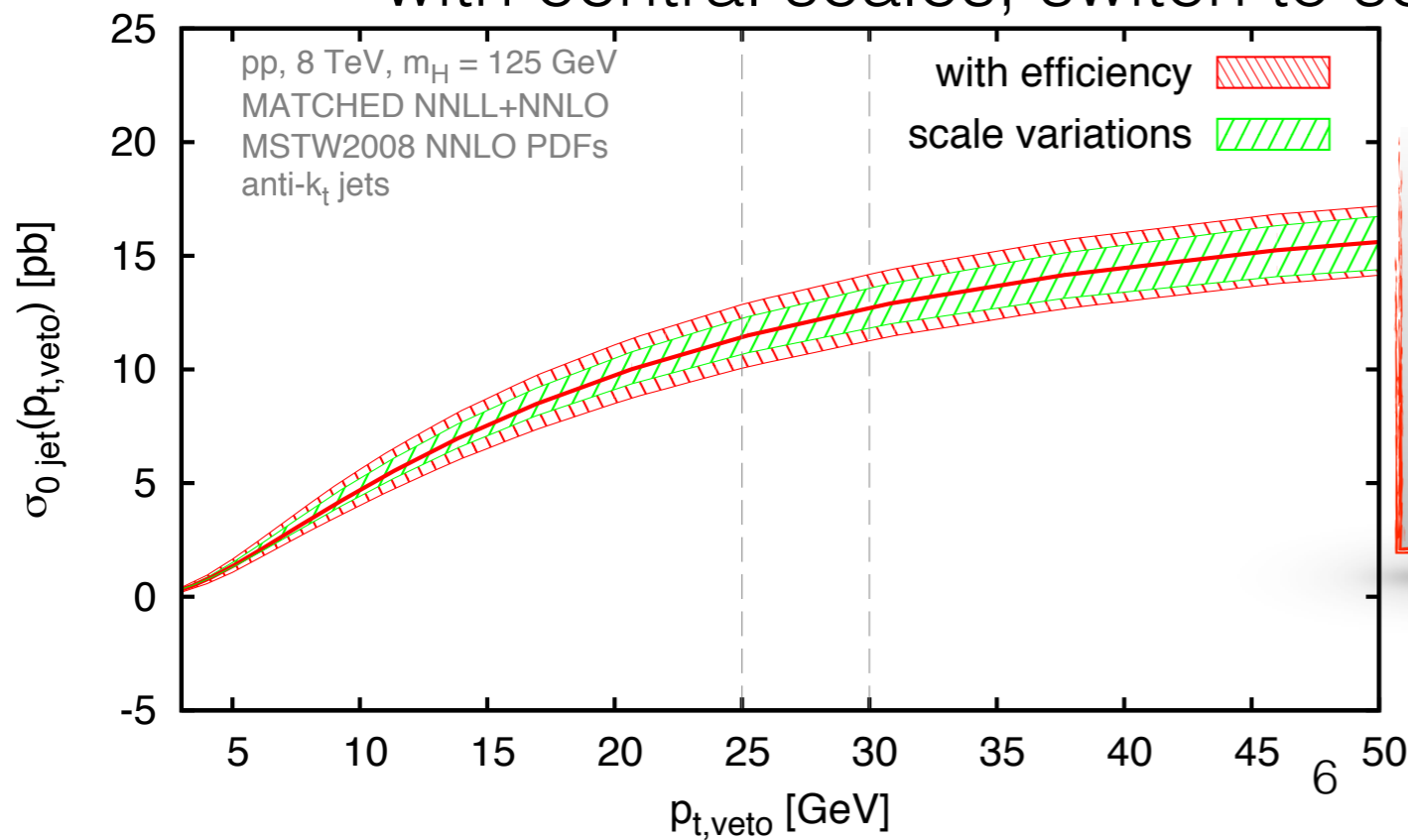
is available

Schemes sensitive to the *all* previous orders

- Resummation fits in naturally (each efficiency scheme corresponds to a different matching scheme), providing a better control of Sudakov effects, i.e. **reducing the spread between different efficiency schemes (separation of uncertainty sources)**

# OLD JVE prescription

- Prescription at NNLO+NNLL (a.k.a. old JVE method): uncertainty for JVE as the envelope of the following variations
  - with scheme (a), vary scales  $\mu_R/\mu_F$  by a factor of 2 in either direction while keeping  $1/2 \leq \mu_R/\mu_F \leq 2$
  - with central  $\mu_R/\mu_F$ , vary the resummation scale Q by a factor of 2
  - with central scales, switch to schemes (b), (c)



Final uncertainty in the 0-jet cross section slightly larger (but not overly conservative) than the **Q, renorm./fact. scales variations**. Slightly conservative estimate **reasonable considering the large corrections at NNLO**

# Updated JVE prescription for 0-jet bin

## What's new

- Updated uncertainty prescription for the JVE:
  - with scheme (a), vary scales  $\mu_R/\mu_F$  by a factor of 2 in either direction while keeping  $1/2 \leq \mu_R/\mu_F \leq 2$  (7 points)
  - keeping renormalisation and factorisation scales to their respective central values, vary the resummation scale ( $Q_b = Q$ ) in the range  $2/3 \leq Q/Q_0 \leq 3/2$
  - keeping central scales, switch to matching scheme (b)
  - with scheme (a) and keeping central scales, vary  $R_0$  by a factor of 2
  - final uncertainty defined as the envelope of the above variations
- Uncertainty in the 0-jet cross section obtained by combining in quadrature with the error in the total cross section

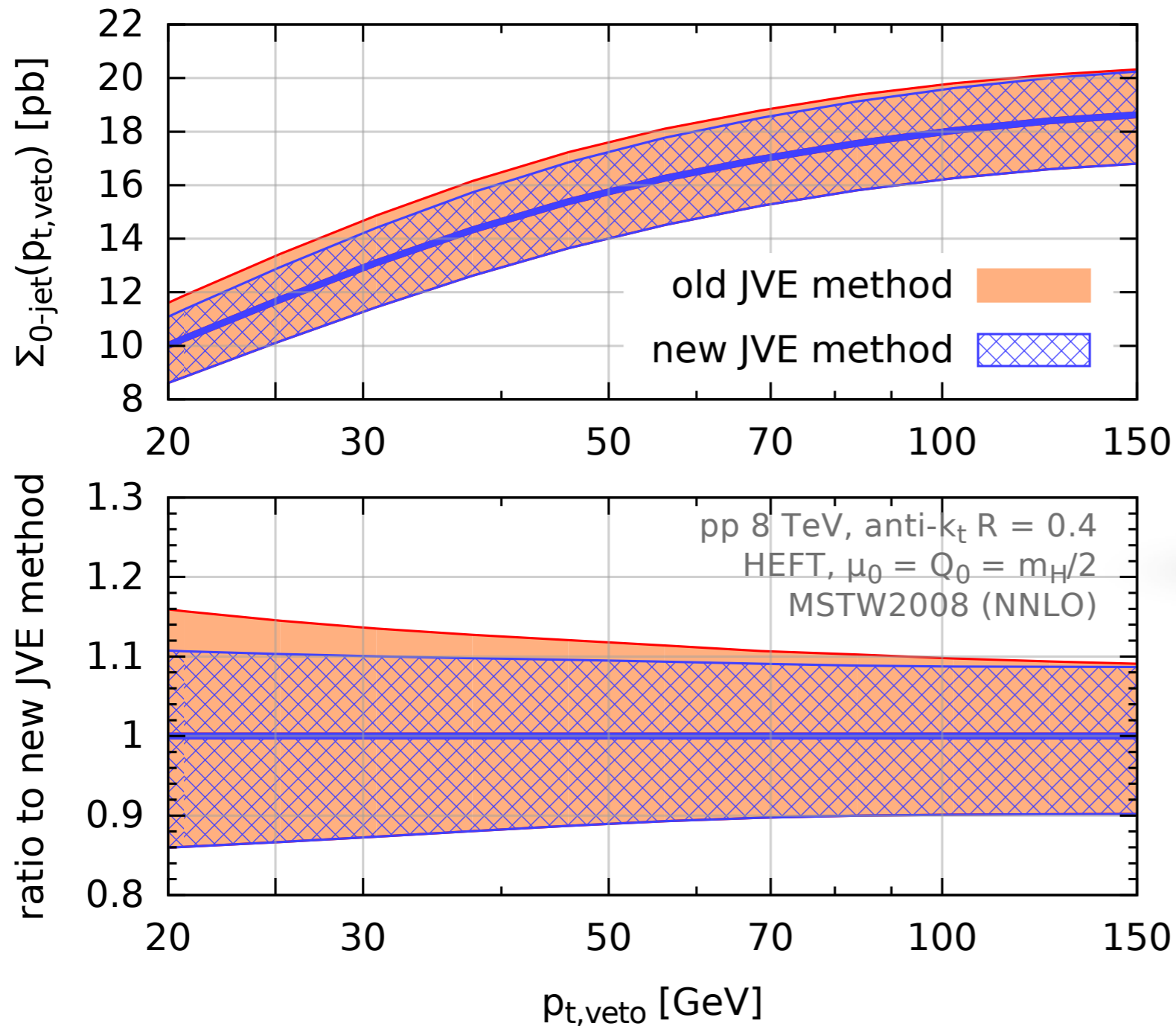
$$\Sigma(p_{t,\text{veto}}) = \epsilon(p_{t,\text{veto}})\sigma_{\text{tot}}$$

$$\delta\Sigma(p_{t,\text{veto}}) = \sqrt{\epsilon^2\delta^2\sigma_{\text{tot}} + \delta^2\epsilon\sigma_{\text{tot}}^2}$$



# Updated NNLO+NNLL results at 8 TeV

NNLO+NNLL jet veto cross section

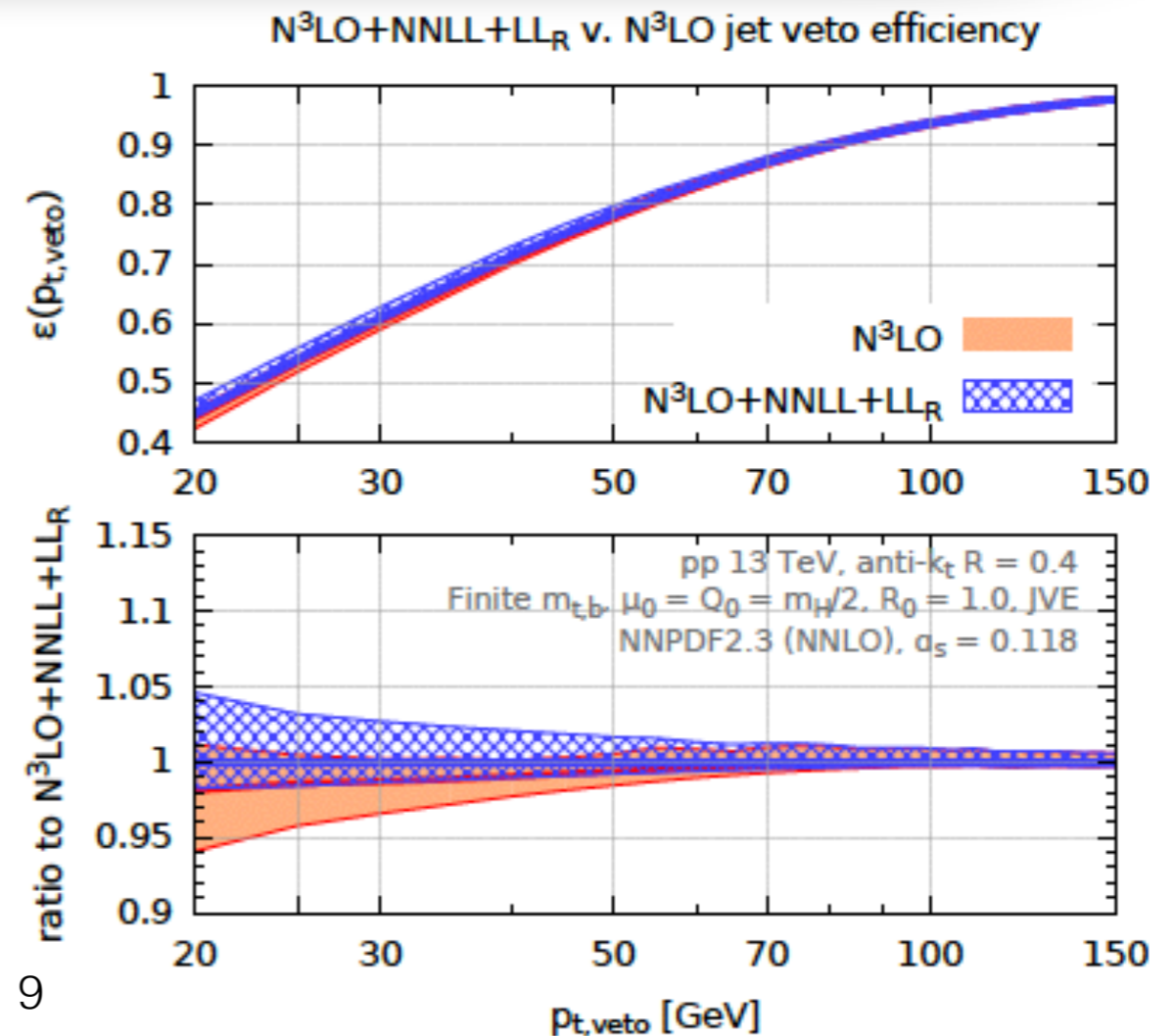
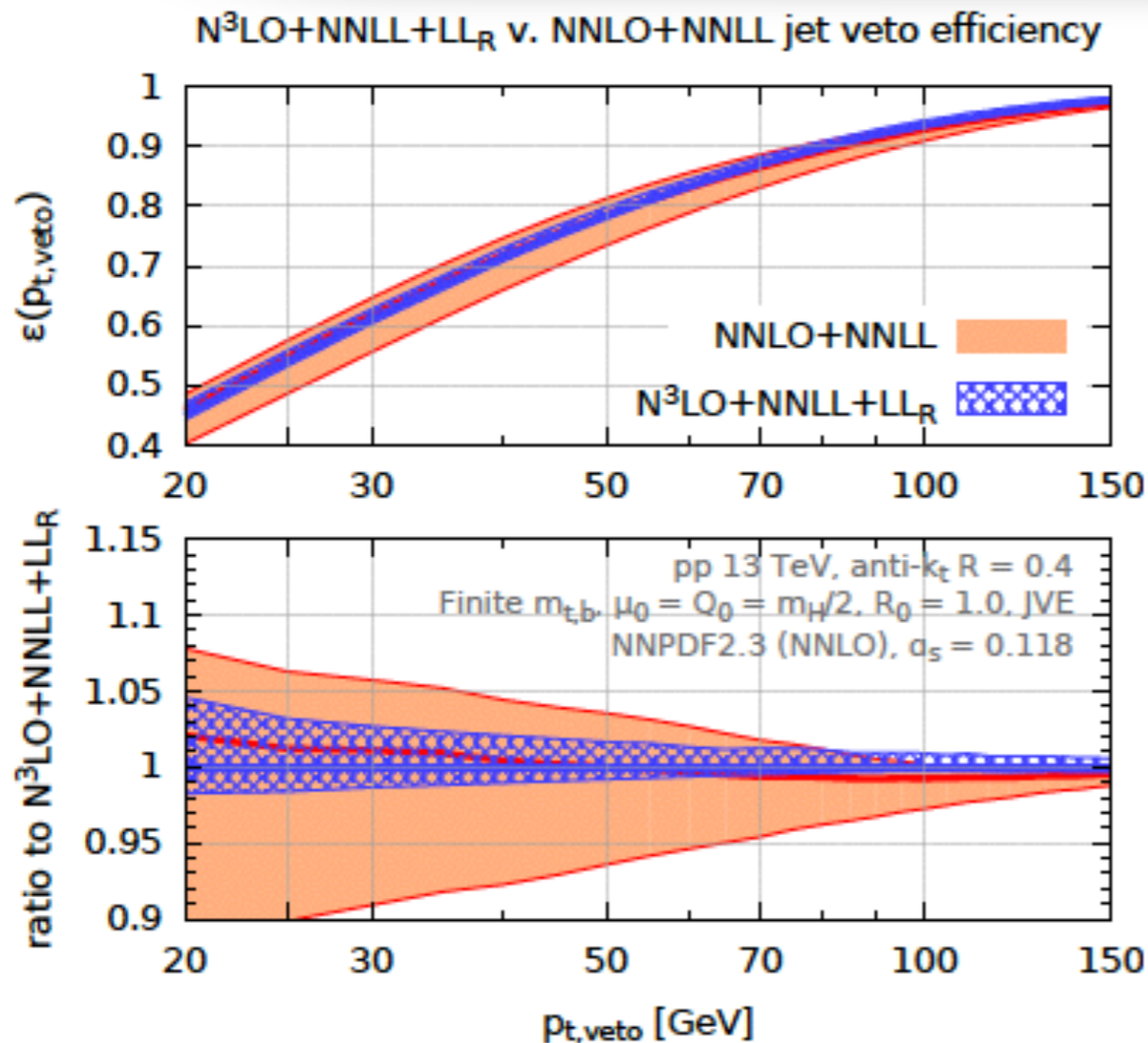


- Uncertainty reduction due to smaller range of Q variation at small  $p_t$ , and absence of scheme (c) at high  $p_t$

# Predictions at LHC13

- Jet-veto efficiency with  $\mu_R = \mu_F = m_H/2$  (see backup for mH)

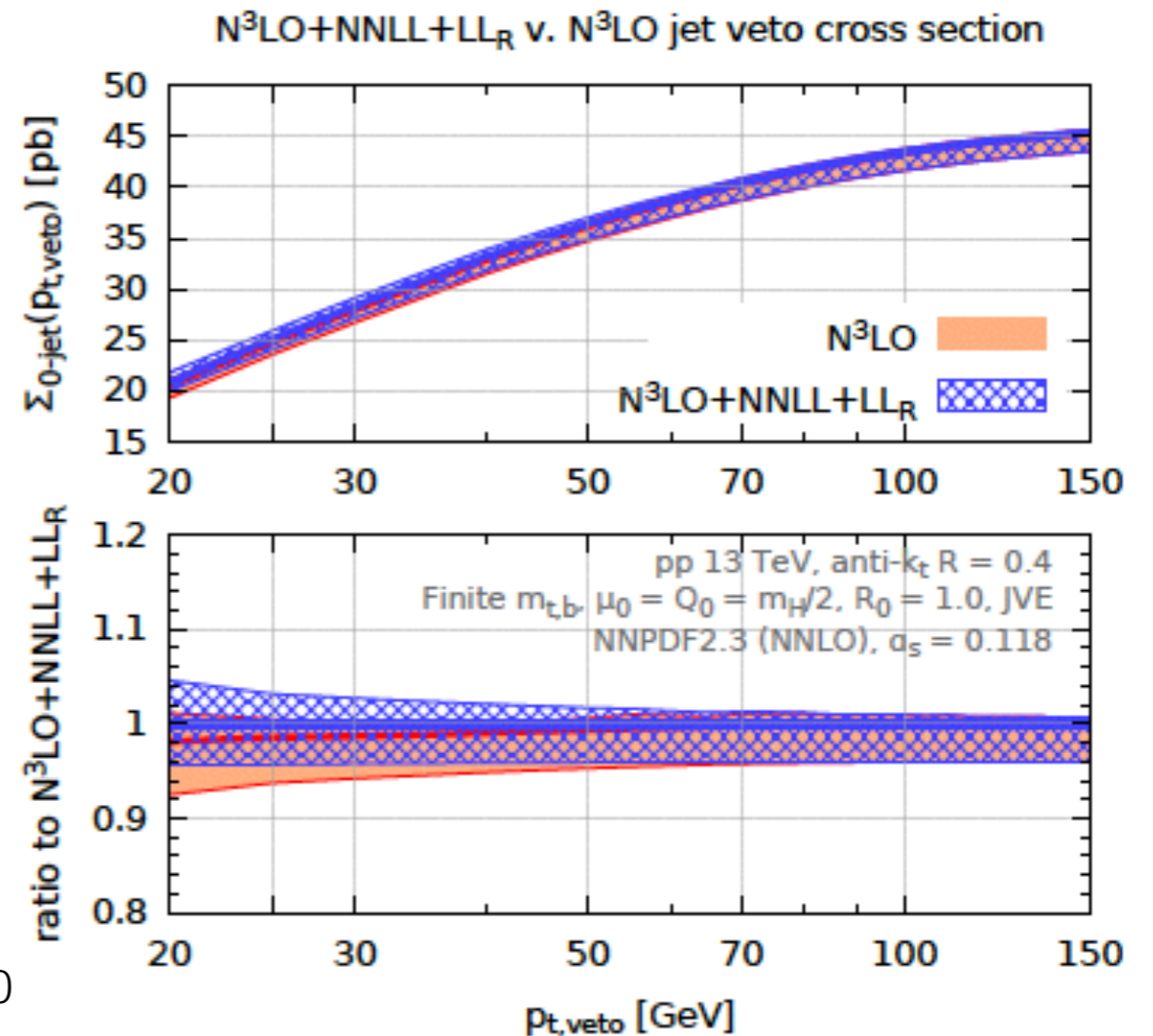
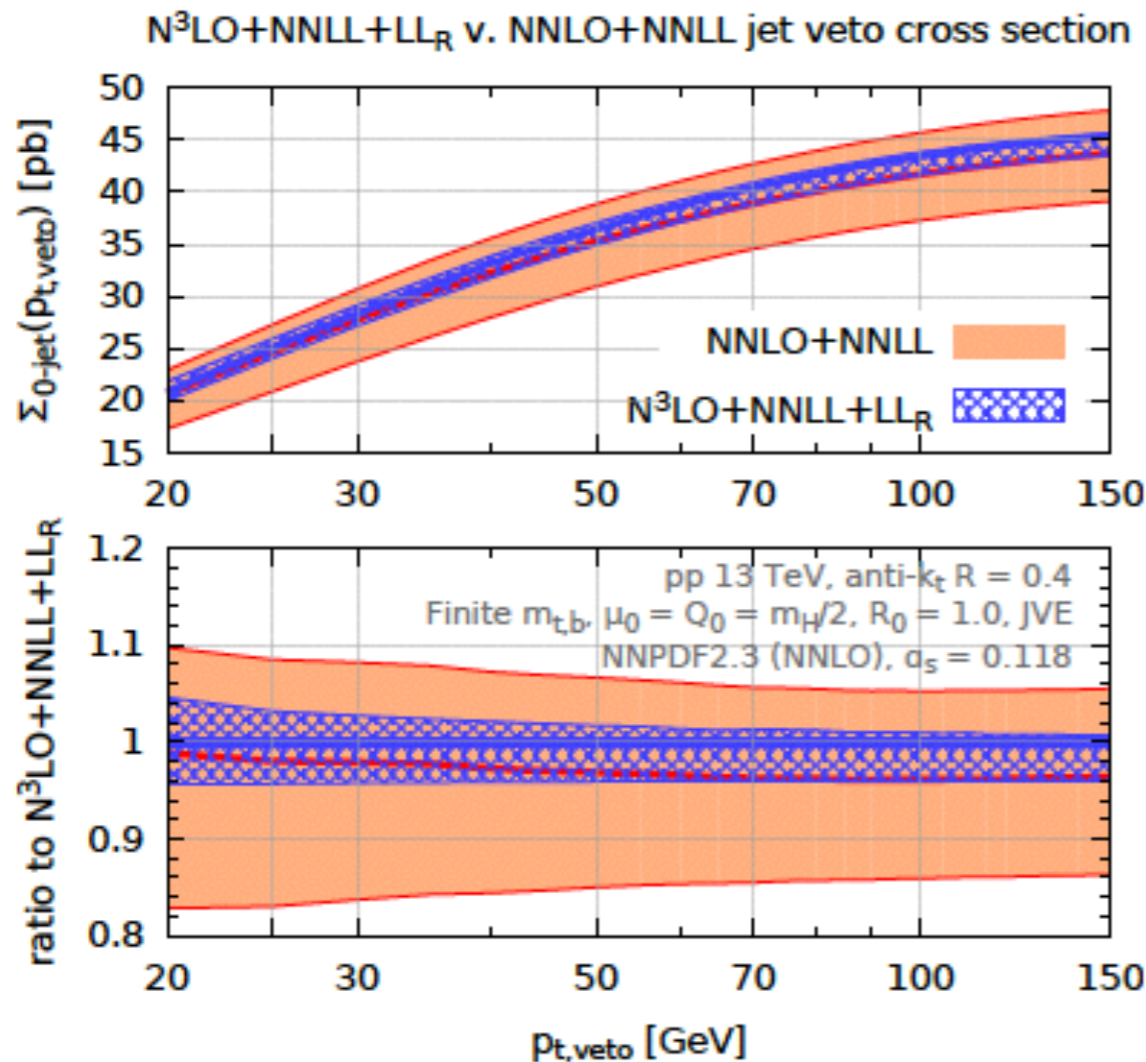
- Moderate corrections w.r.t. NNLO+NNLL ( $\sim 1-2\%$ ) - consistently, theory uncertainty reduced by more than a factor of two ( $\sim 8\% \rightarrow \sim 3\%$ )
- Impact of resummation w.r.t. N3LO at the 2% level - similar uncertainties (this is peculiar of this scale, doesn't occur at e.g. mH)



# Predictions at LHC13

- 0-jet cross section with  $\mu_R = \mu_F = m_H/2$

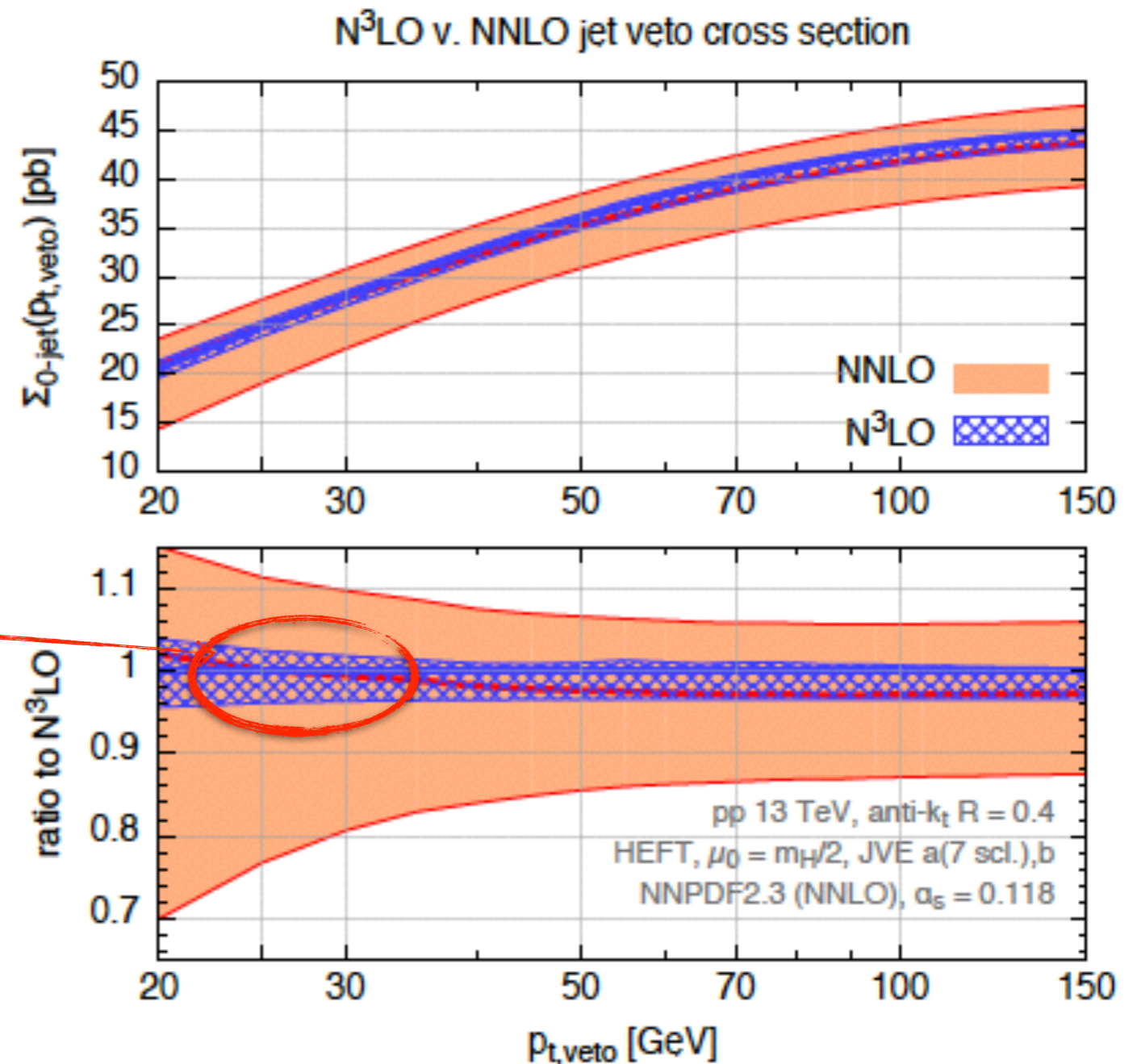
- Moderate increase in the 0-jet cross section ( $\sim 2\%$ ) w.r.t. NNLO+NNLL - significant reduction of the theory uncertainty



# Impact of NNLL resummation

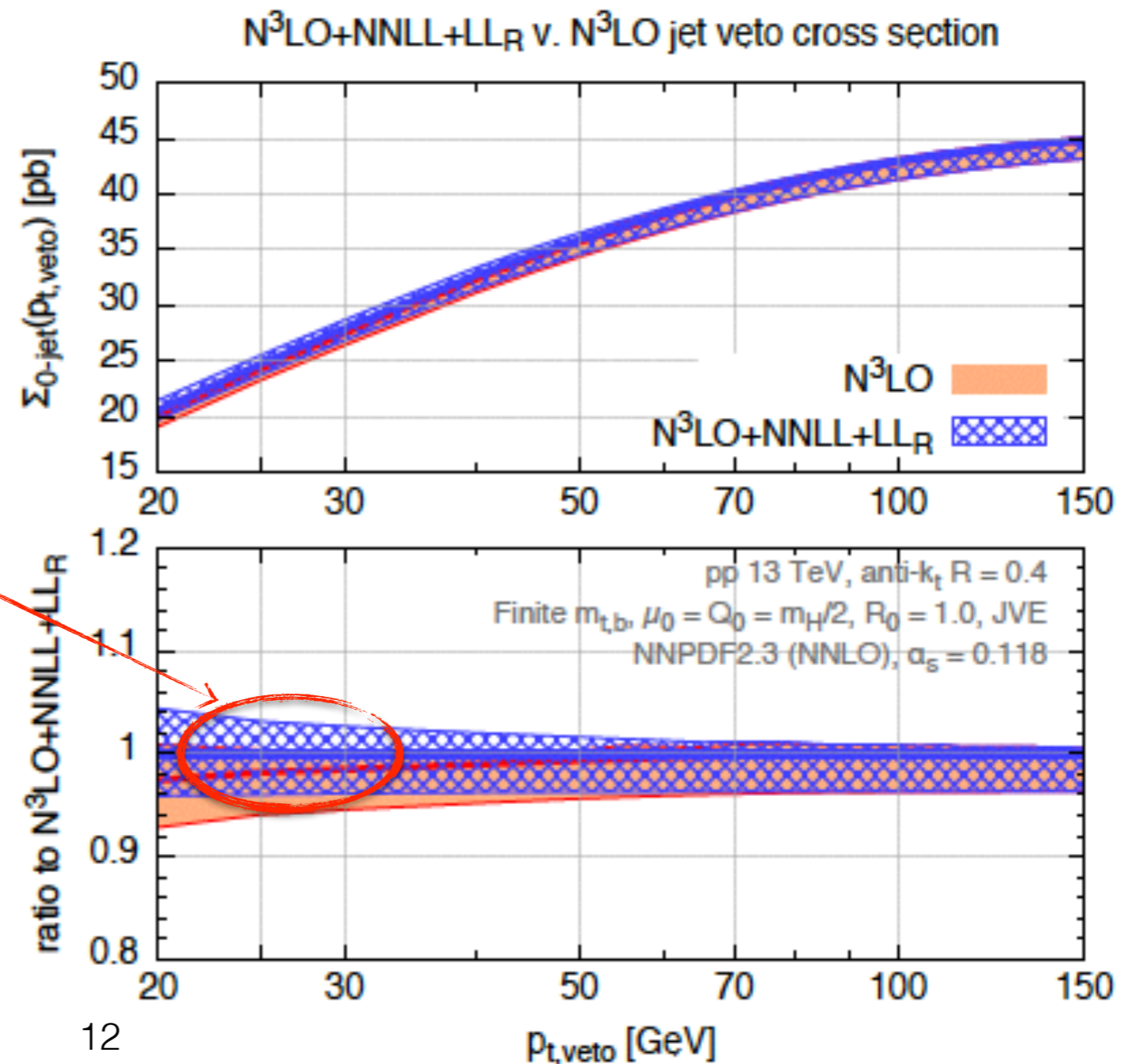
- Important to understand (a priori) where exactly resummation and fixed-order are reliable (and estimate the matching uncertainty)

at  $p_t \sim 25-30$  GeV  
N<sup>3</sup>LO (pure fixed order) corrections  
have a 1-2% impact  
(this varies with central scales)



# Impact of NNLL resummation

- Important to understand (a priori) where exactly resummation and fixed-order are reliable (and estimate the matching uncertainty)



Impact of the resummation is of the same order (~2%).  
How accurate is this statement ?

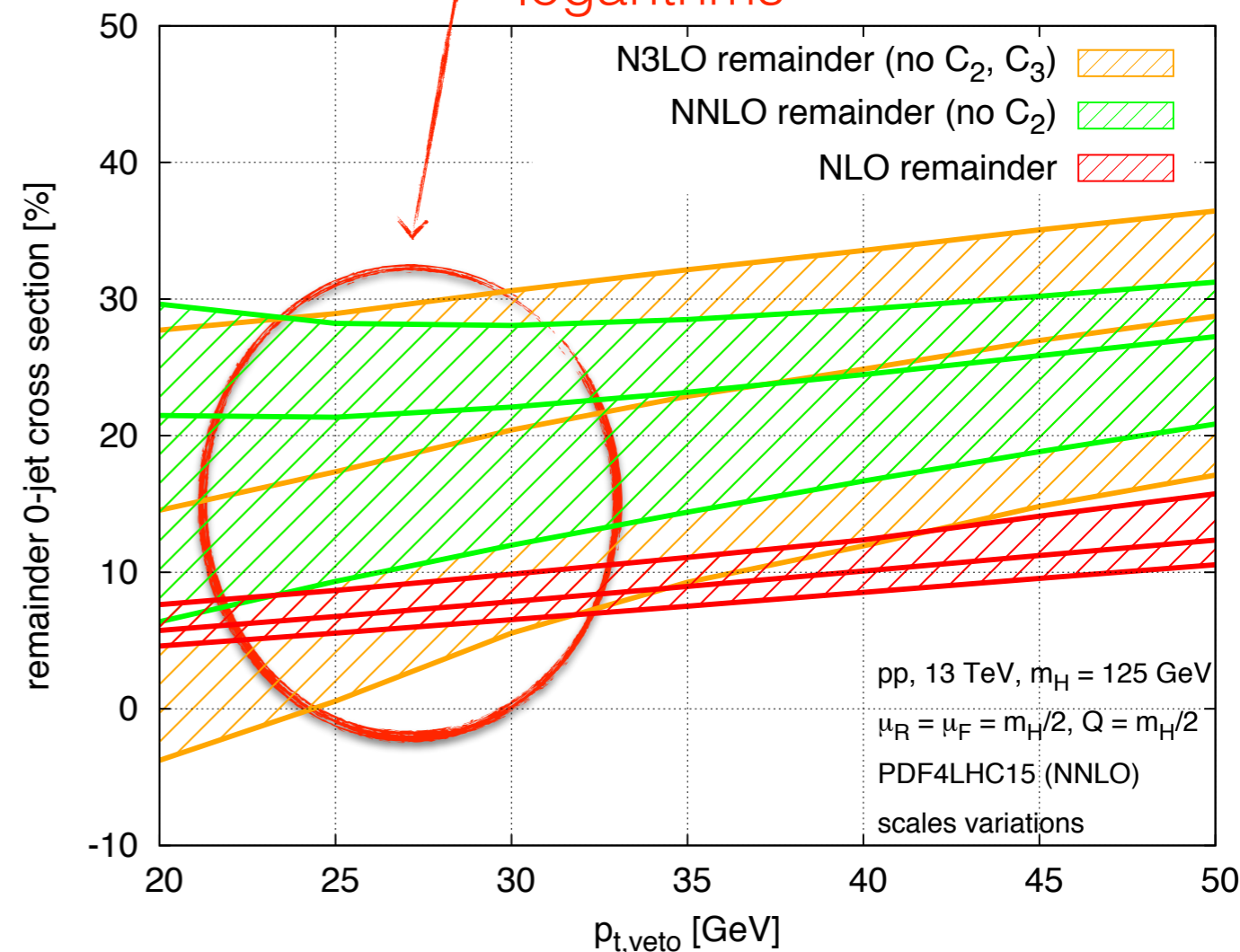
# Impact of NNLL resummation

- Important to understand (a priori) where exactly resummation and fixed-order are reliable (and estimate the matching uncertainty)

pt ~ 25-30 GeV is a transition region where logarithms are the dominant part of the perturbative expansion, although fixed-order still works fine (i.e. the coupling suppression is still effective) Resummation effects seem physical.

Some care is required with the uncertainties (impact of matching scheme and modified logarithms)

~ 70-80% of the perturbative expansion is made of logarithms

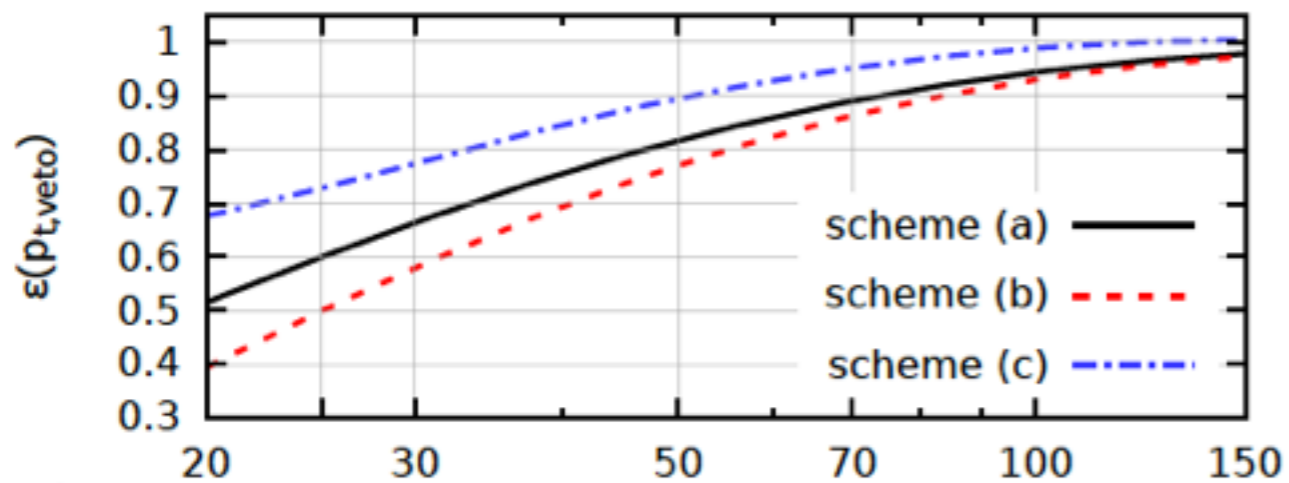


# Differences with the OLD JVE prescription

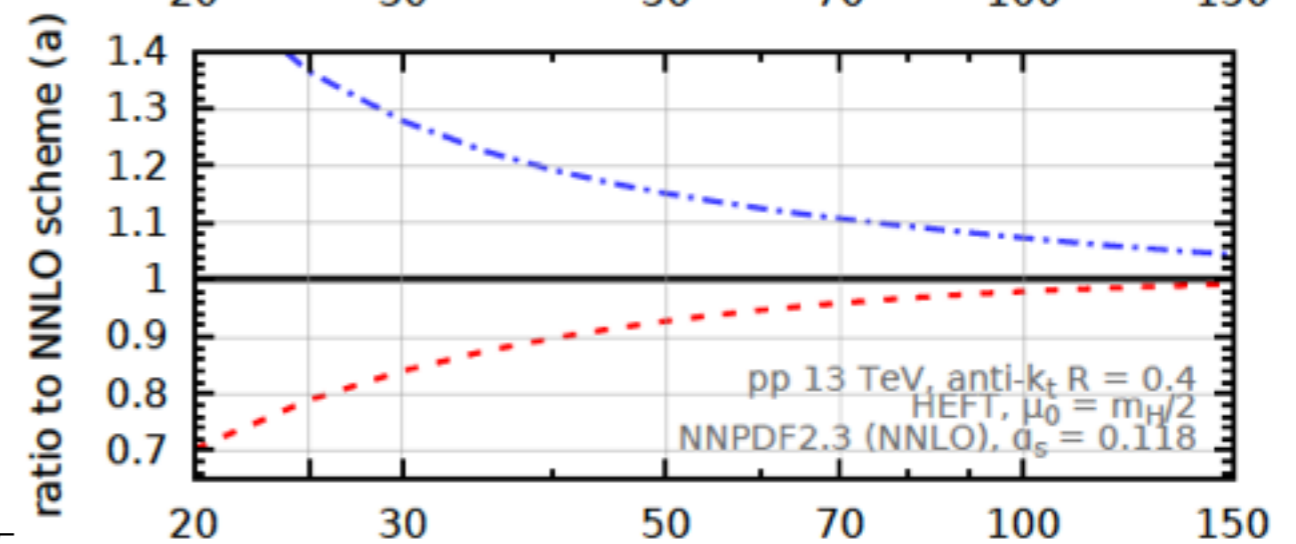
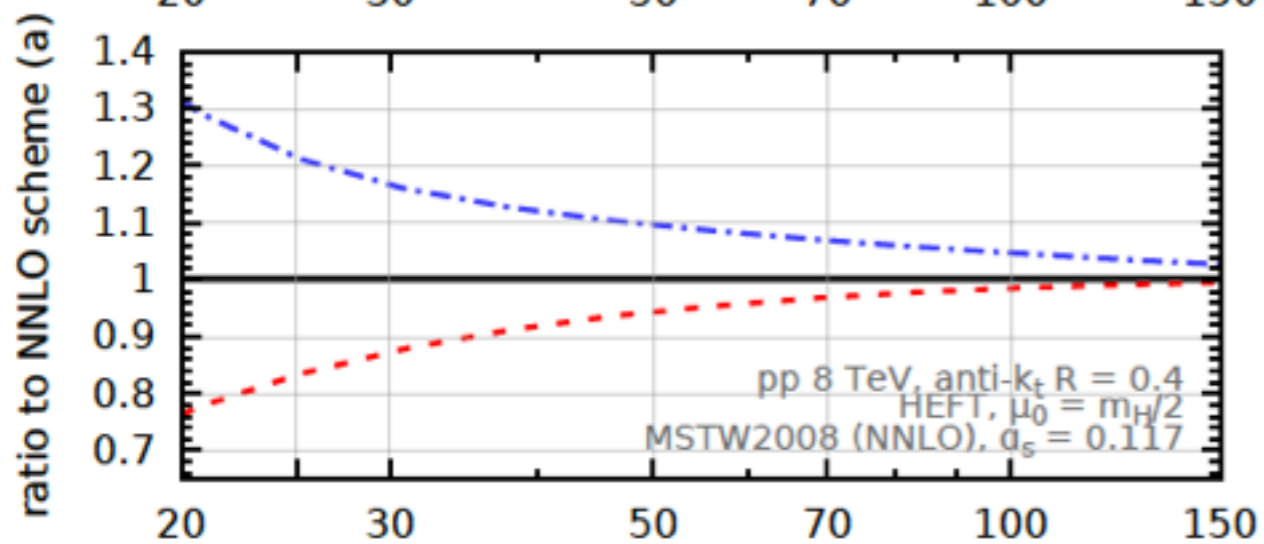
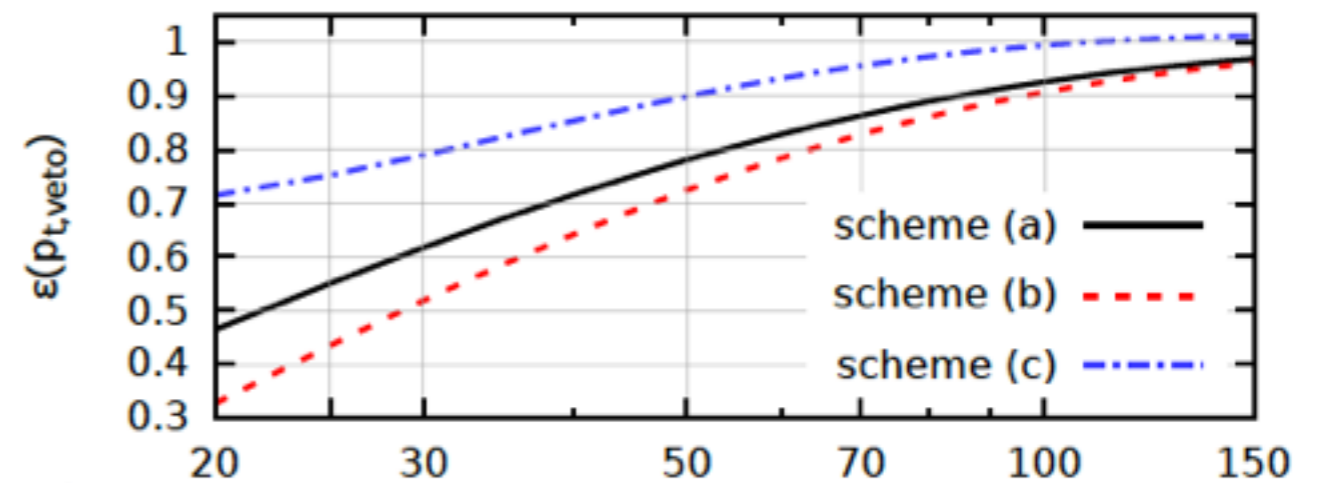
# Potential issues with efficiency schemes

- Possible issues can appear when the perturbative series for the total cross section features a very poor convergence, and the geometric expansion which defines the efficiency schemes can be badly defined
- This feature shows up already at NNLO for scheme (c) at larger c.o.m. energies  $\rightarrow$  NLO K factor grows from  $\sim 2.2$  (8 TeV) to  $\sim 2.3$  (13 TeV)

NNLO jet veto efficiency, 8 TeV



NNLO jet veto efficiency, 13 TeV





# Potential issues with efficiency schemes

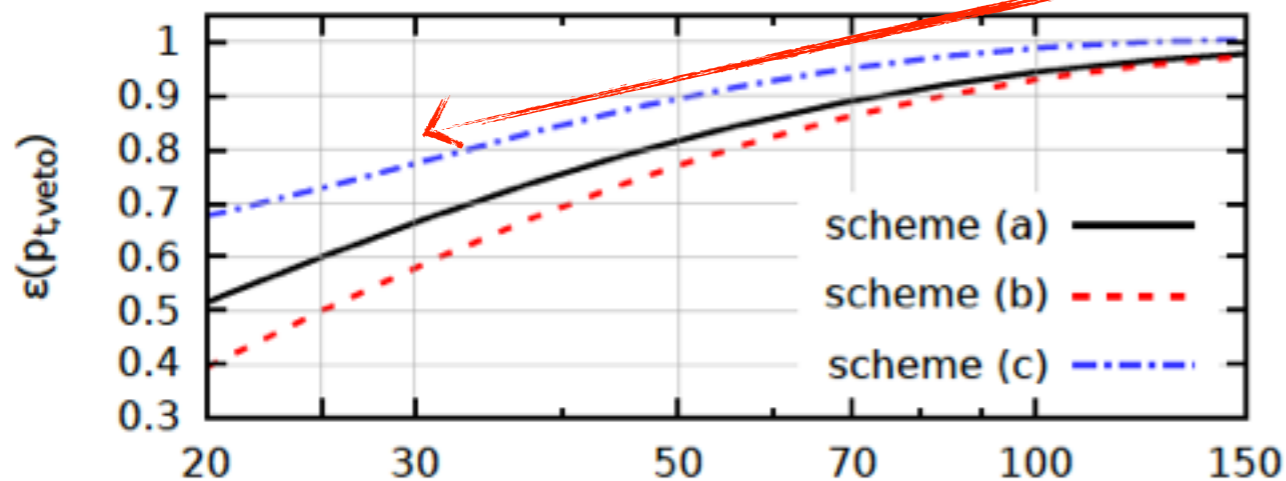
- Possible issues can appear when the perturbative series for the total cross section features a very poor convergence, and the geometric expansion which defines the efficiency schemes can be badly defined

- This feature shows that at higher energies  $\rightarrow$  NLO K-factor grows from  $\sim 1.5$  to  $\sim 2.5$  (13 TeV)

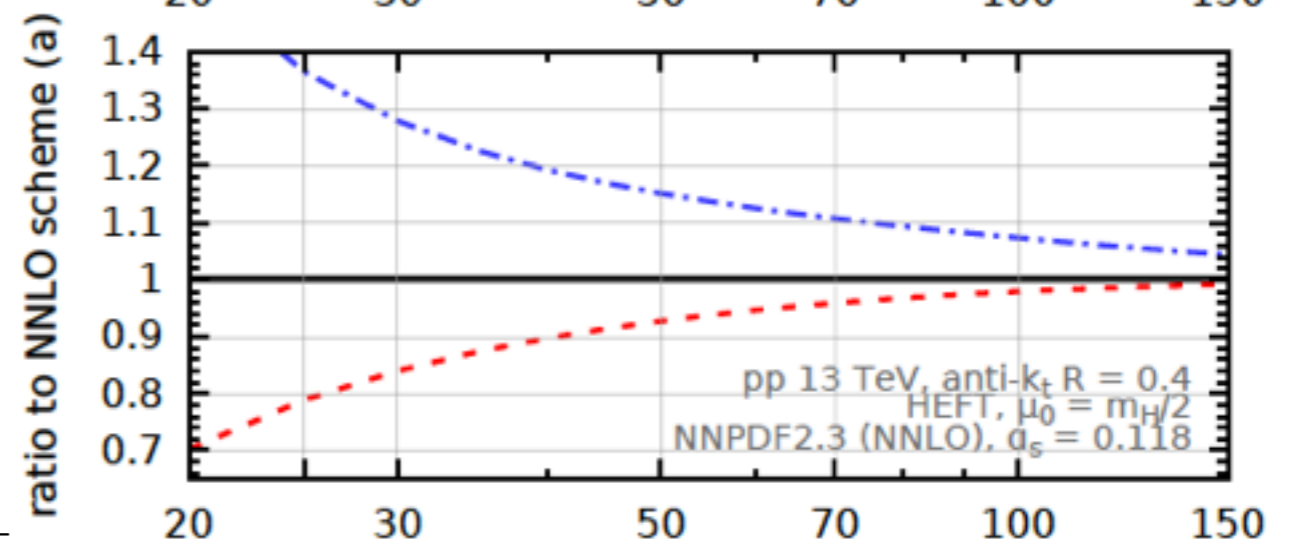
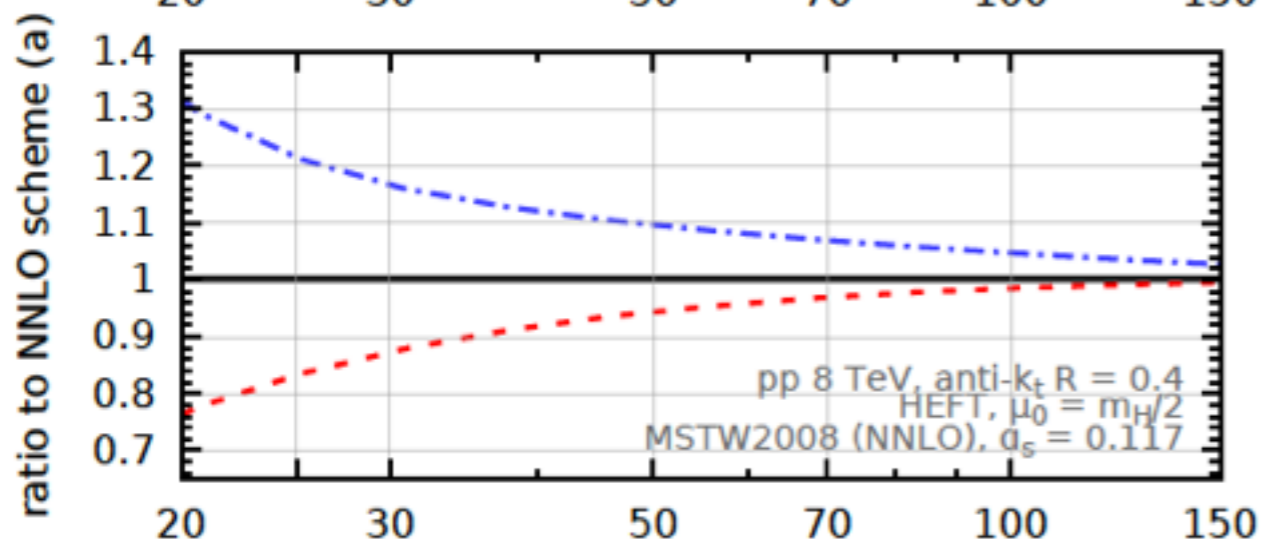
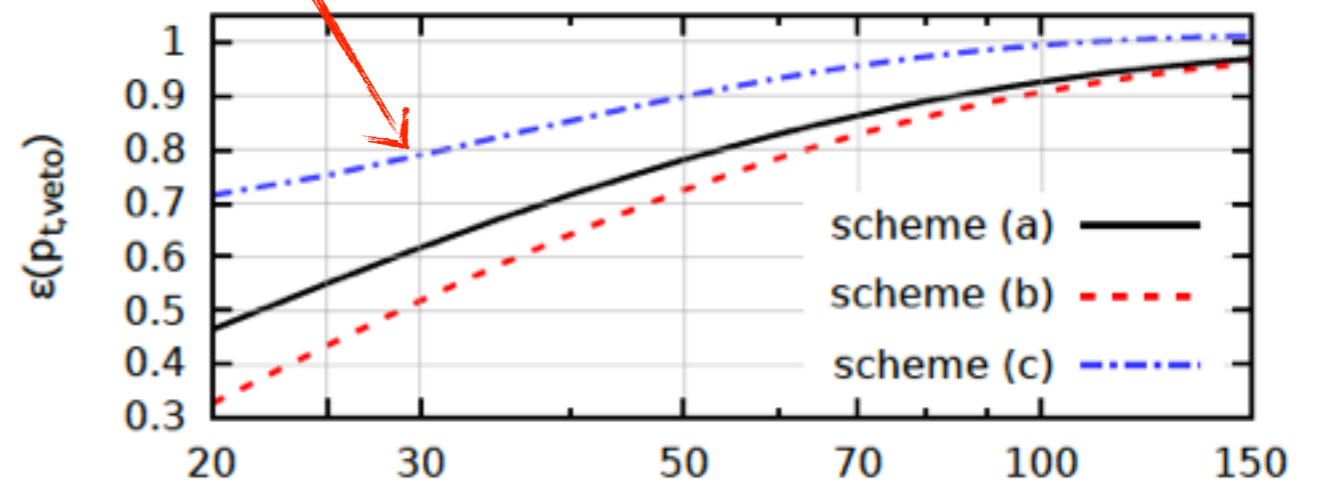
Scheme (c)'s efficiency increases with the energy (unphysical)

- larger c.o.m. (TeV)

NNLO jet veto efficiency, 8 TeV



NNLO jet veto efficiency, 13 TeV



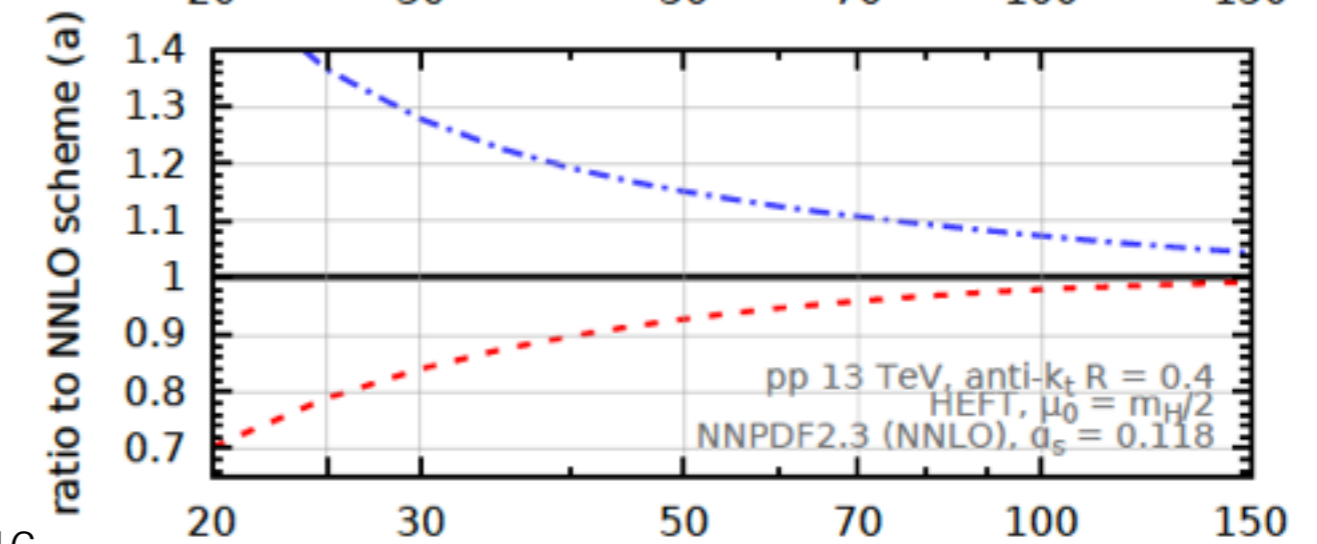
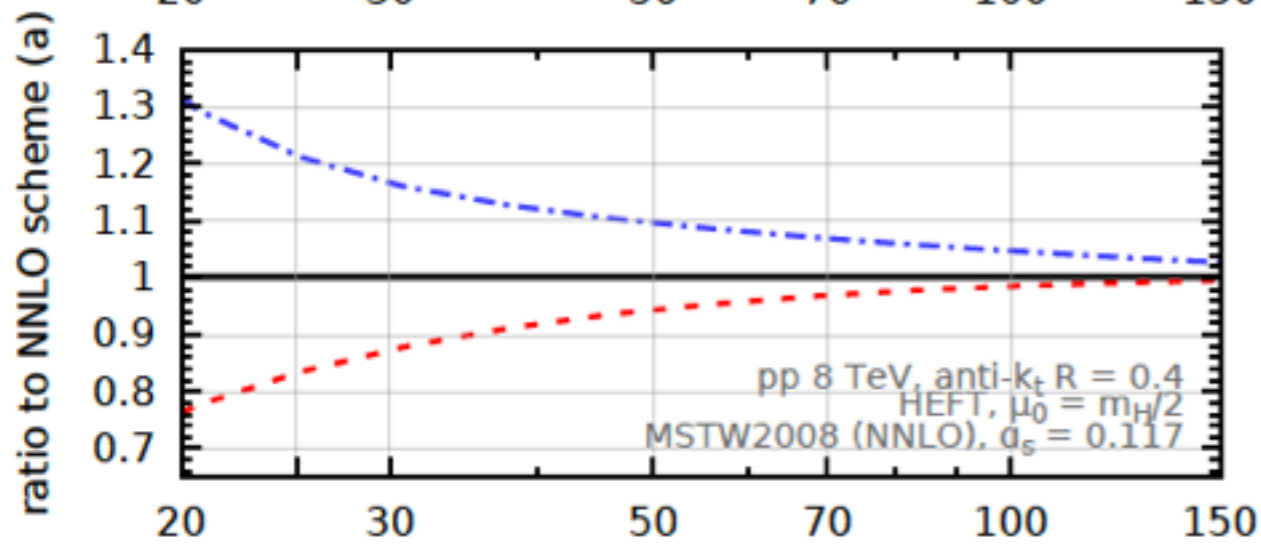
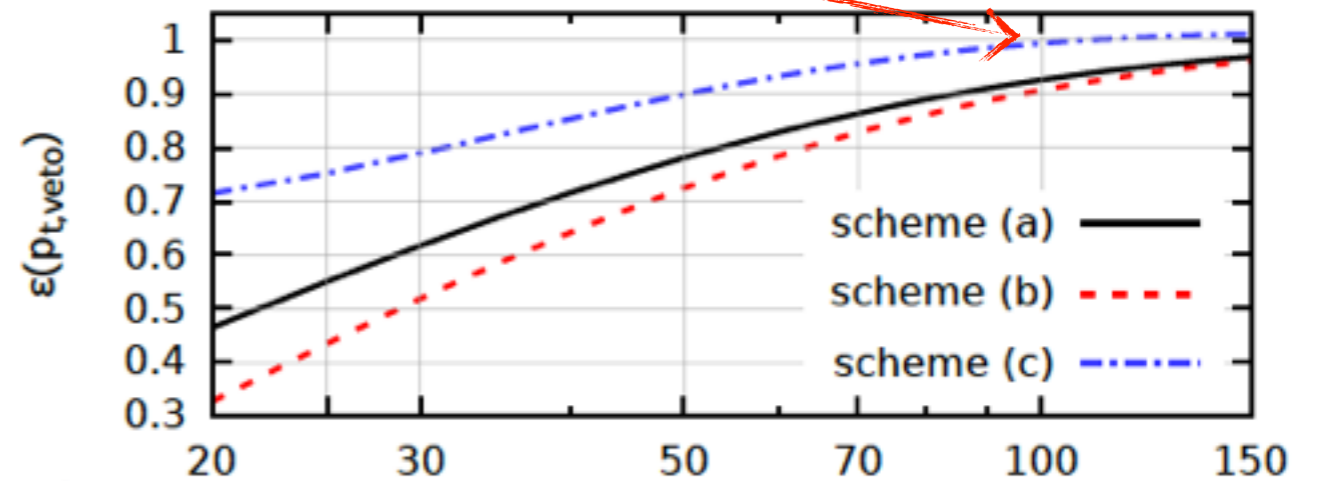
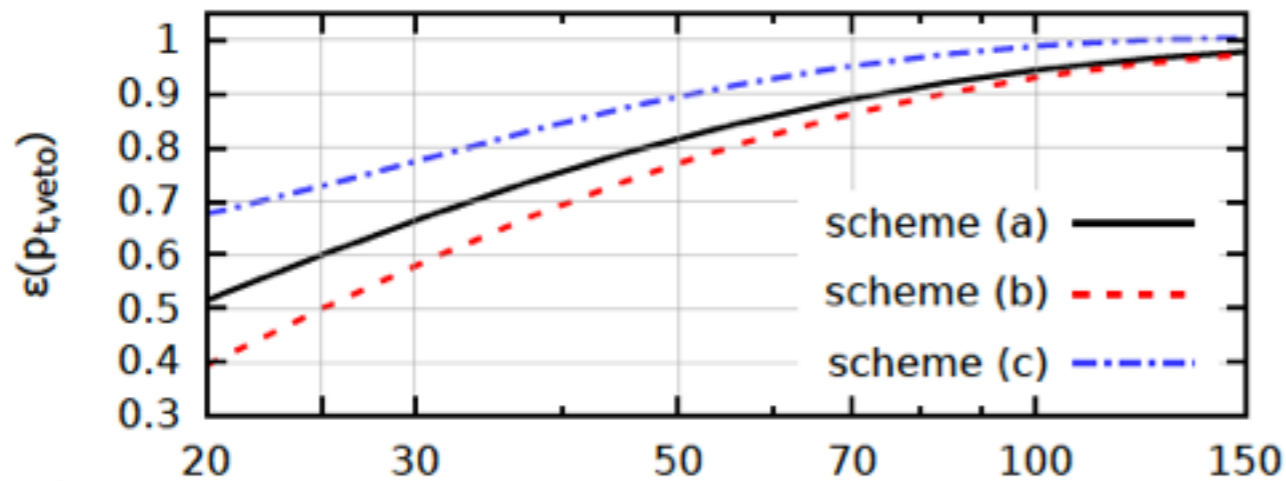
# Potential issues with efficiency schemes

- Possible issues can appear when the perturbative series for the total cross section expansion which is geometrically defined
- This feature shows up at larger c.o.m. energies  $\rightarrow$  NNLO jet veto grows from 41.2 (8 TeV) to 41.6 (13 TeV)

Scheme (c)'s efficiency becomes larger than one at high scales. Overly large uncertainty also in the tail of the leading jet's pt spectrum compared to NNLO

NNLO jet veto efficiency, 8 TeV

NNLO jet veto efficiency, 13 TeV



# Efficiency schemes at N<sub>3</sub>LO

- 5 schemes for the jet-veto efficiency available at this order for H

$\sigma^{(3)} \rightarrow$  [Anastasiou, Duhr, Dulat, Herzog, Mistlberger 1503.06056]

$\bar{\Sigma}^{(3)}(p_{t,\text{veto}}) \rightarrow$  [Boughezal, Caola, Melnikov, Petriello, Schulze 1504.07922]

$$\epsilon^{(a)}(p_{t,\text{veto}}) = 1 + \frac{1}{\sigma_{\text{tot},3}} \sum_{i=1}^3 \bar{\Sigma}^{(i)}(p_{t,\text{veto}})$$

$$\epsilon^{(b)}(p_{t,\text{veto}}) = 1 + \frac{1}{\sigma_{\text{tot},2}} \sum_{i=1}^3 \bar{\Sigma}^{(i)}(p_{t,\text{veto}}),$$

$$\epsilon^{(c)}(p_{t,\text{veto}}) = 1 + \frac{1}{\sigma_{\text{tot},1}} \left[ \sum_{i=1}^3 \bar{\Sigma}^{(i)}(p_{t,\text{veto}}) - \frac{\sigma^{(2)}}{\sigma_{\text{tot},0}} \bar{\Sigma}^{(1)}(p_{t,\text{veto}}) \right],$$

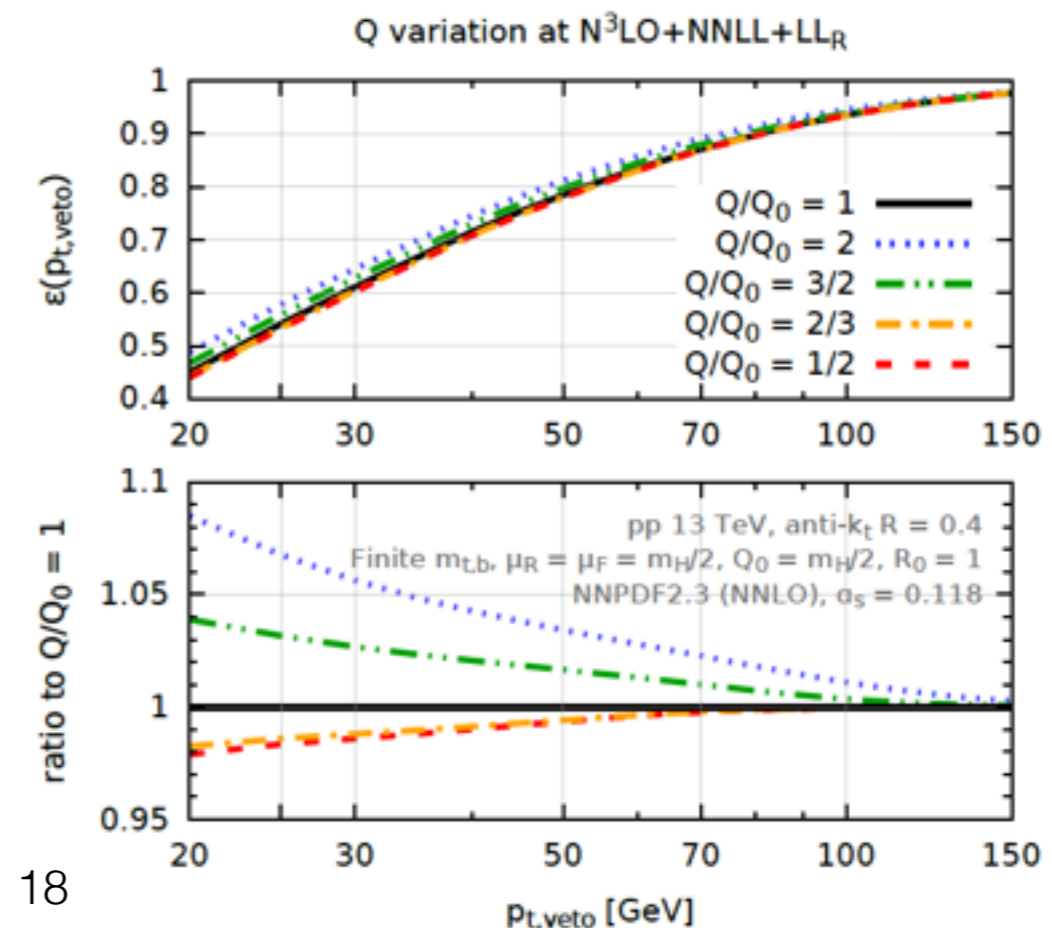
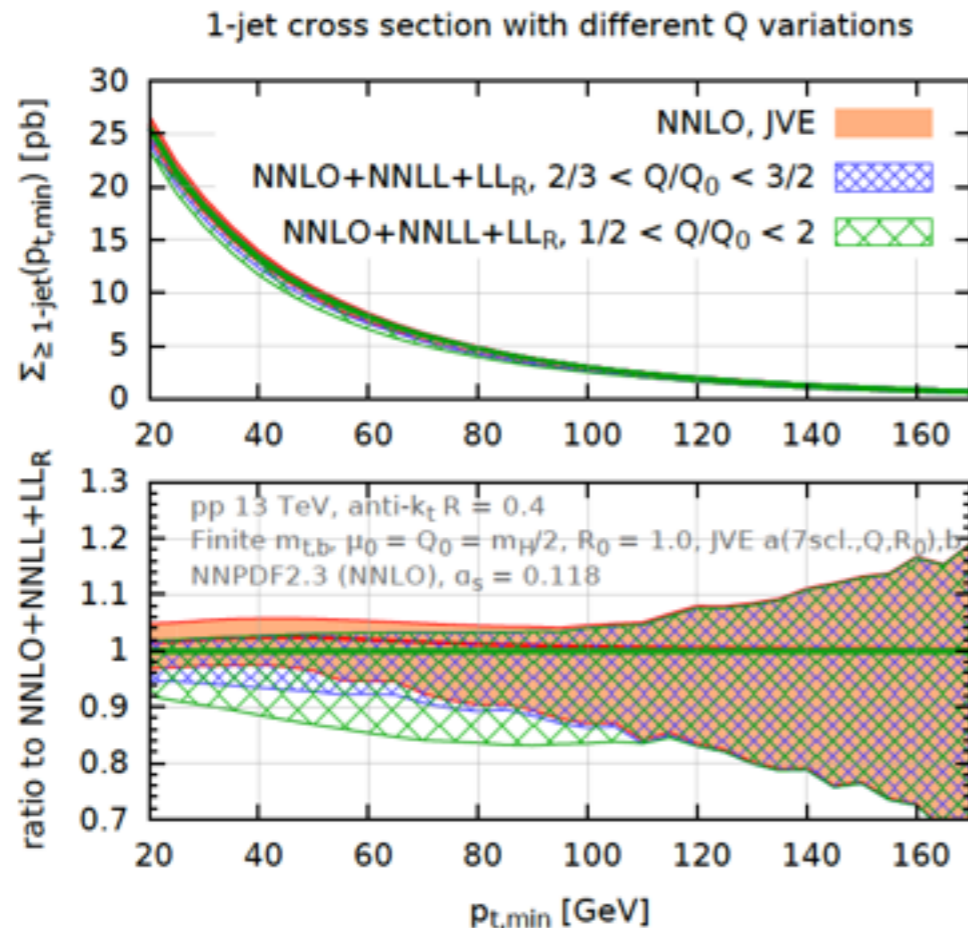
$$\epsilon^{(c')}(p_{t,\text{veto}}) = 1 + \frac{1}{\sigma_{\text{tot},1}} \left[ \sum_{i=1}^3 \bar{\Sigma}^{(i)}(p_{t,\text{veto}}) - \frac{\sigma^{(2)}}{\sigma_{\text{tot},1}} \bar{\Sigma}^{(1)}(p_{t,\text{veto}}) \right], \quad \rightarrow \sigma_{\text{tot},1} = \sigma^{(0)} + \sigma^{(1)}$$

$$\epsilon^{(d)}(p_{t,\text{veto}}) = 1 + \frac{1}{\sigma_{\text{tot},0}} \left[ \sum_{i=1}^3 \bar{\Sigma}^{(i)}(p_{t,\text{veto}}) - \frac{\sigma^{(1)}}{\sigma_{\text{tot},0}} (\bar{\Sigma}^{(1)}(p_{t,\text{veto}}) + \bar{\Sigma}^{(2)}(p_{t,\text{veto}})) \right. \\ \left. + \frac{\sigma^{(1)}\sigma^{(1)} - \sigma^{(0)}\sigma^{(2)}}{(\sigma_{\text{tot},0})^2} \bar{\Sigma}^{(1)}(p_{t,\text{veto}}) \right].$$

Schemes (c) and (d) are sensible only if the NLO K factor is small, therefore show the same issues as scheme (c) at NNLO

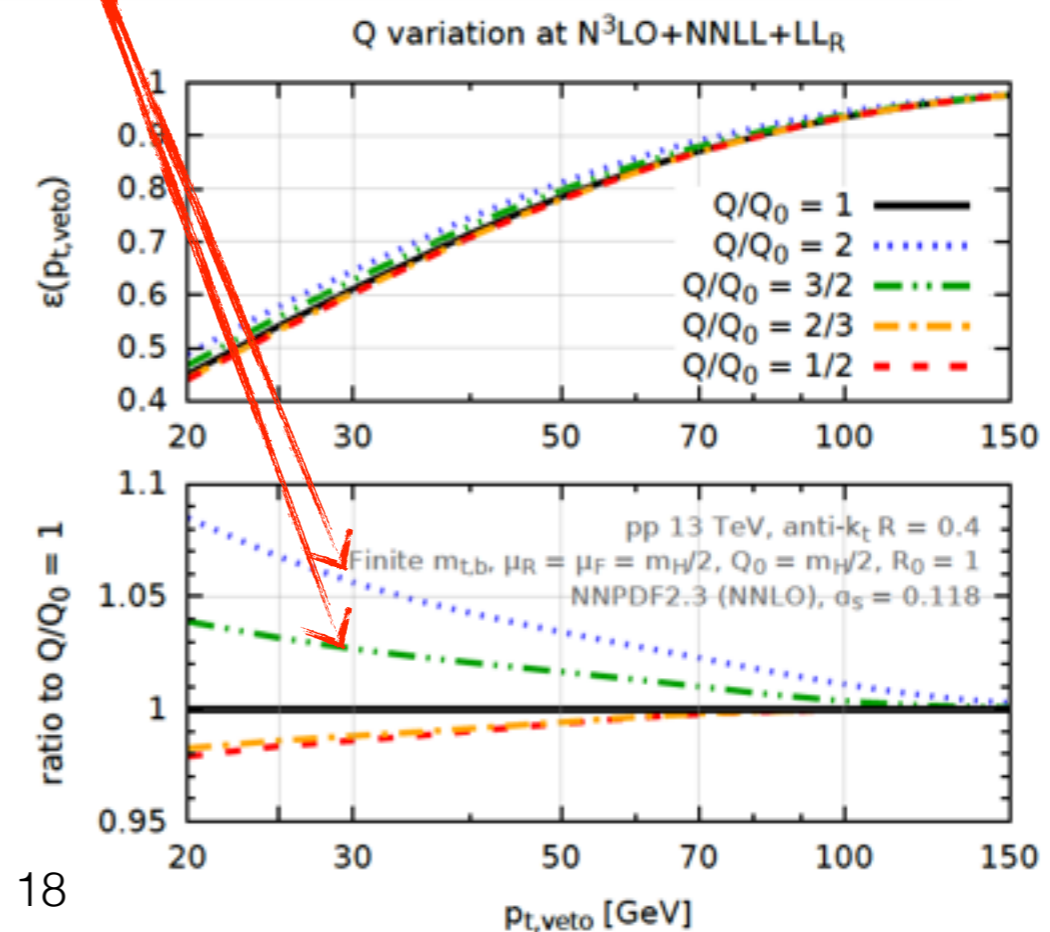
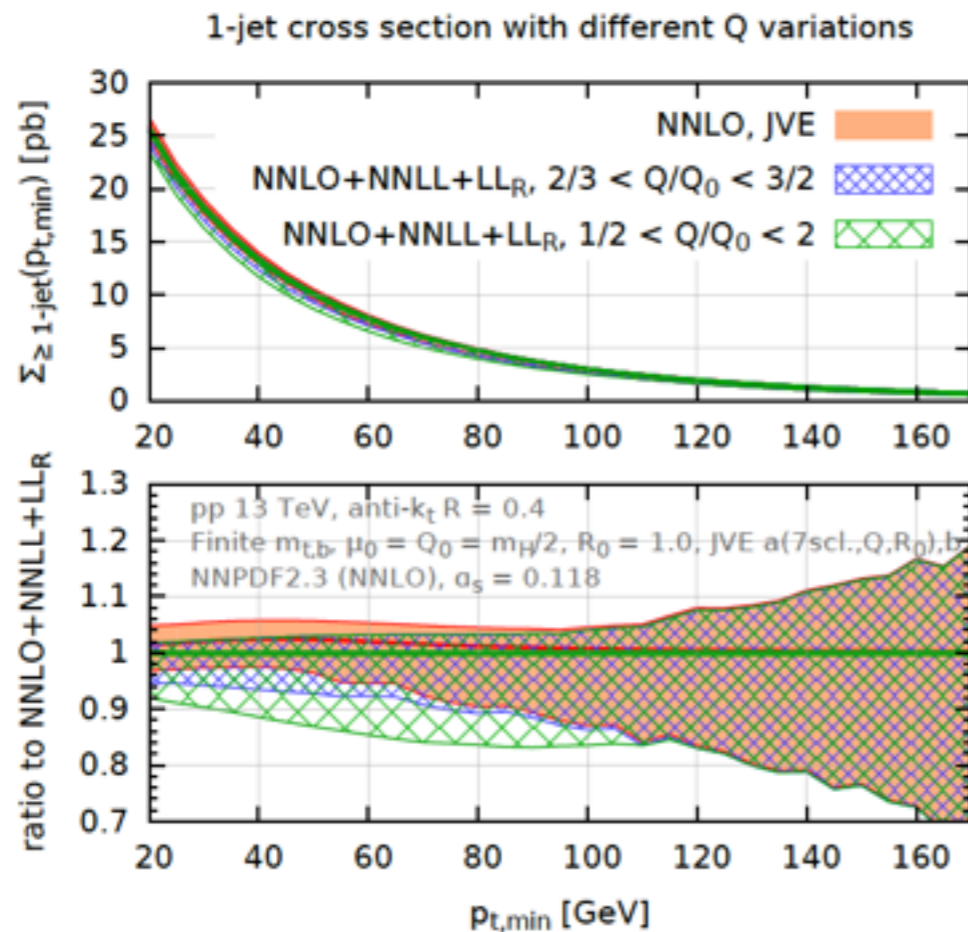
# Resummation uncertainties

- Matching to NNLL resummation of jet-veto logarithms is performed by means of two multiplicative matching schemes which correspond to the two efficiency schemes (a) and (b) respectively
- In addition to  $\mu_R/\mu_F$  scales ( $\times 2$ ) and schemes (a,b) variations, the size of subleading logarithmic terms is estimated by varying the resummation scale  $Q$  around its central value  $Q_0 = m_H/2$ :
 
$$\ln \frac{M}{p_{t,\text{veto}}} \rightarrow \ln \frac{Q}{p_{t,\text{veto}}} + \ln \frac{M}{Q}$$
  - The old variation range  $1/2 \leq Q/Q_0 \leq 2$  is conservative and allows for resummation effects up to  $\sim m_H$  (larger uncertainty band in tail of jet pt spectrum)



# Resummation uncertainties

- Matching to NNLL resummation of jet-veto logarithms is performed by means of two multiplicative matching schemes which correspond to the two efficiency schemes (a) and (b) respectively
- In • Given the good convergence observed with the inclusion of N3LO leading log corrections, we use the variation range  $2/3 \leq Q/Q_0 \leq 3/2$  which gives a less central conservative uncertainty at large  $p_t$
- • The Q dependence is reduced everywhere along the spectrum
- effects up to  $\sim m_H$  (larger uncertainty band in tail of jet  $p_t$  spectrum)

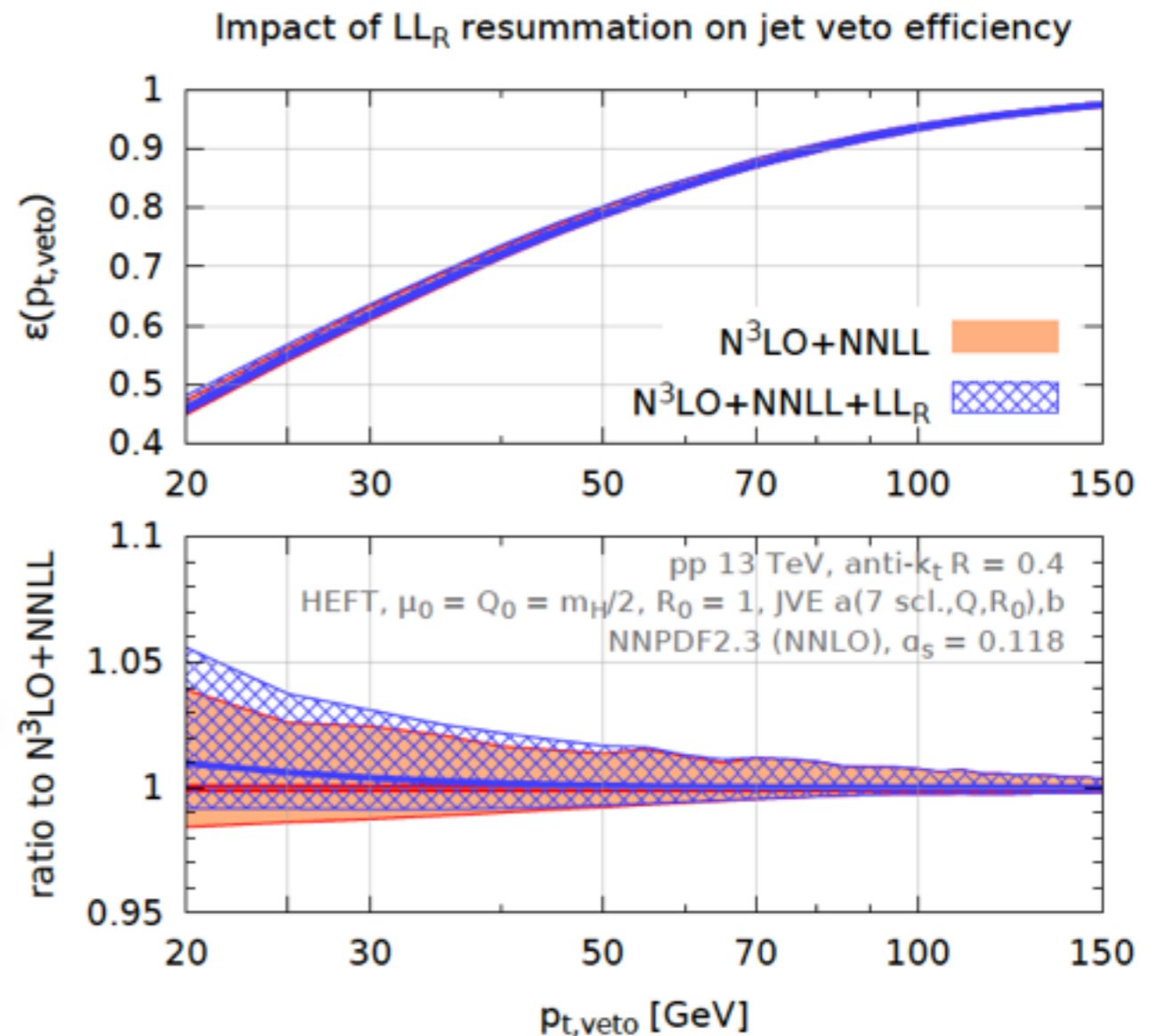


# Jet radius logarithms

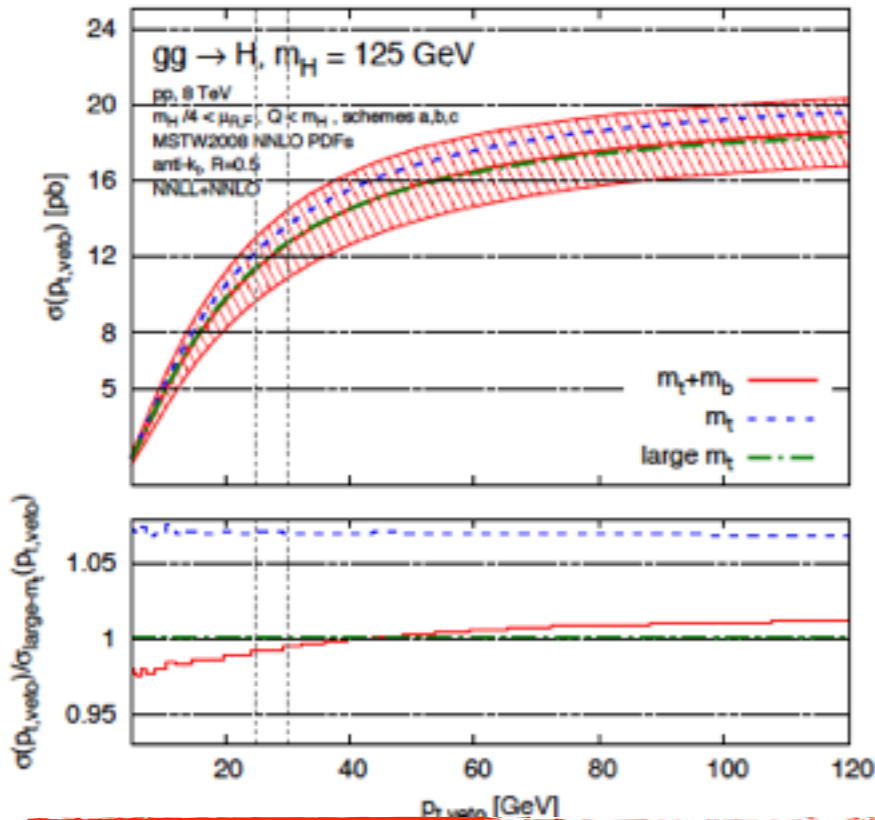
[Dasgupta, Dreyer, Salam, Soyez 1411.5182]

- In addition to the other theoretical uncertainties previously considered, the error associated with small-R resummation is estimated by varying  $1/2 \leq R_0 \leq 2$

- Small impact ( $\sim 1\%$ ) with  $R=0.4$
- Slight increase in uncertainty band due to larger  $Q$  dependence of the all-order correlated contribution (gluon splitting)
- $R_0$  dependence moderate (backup)



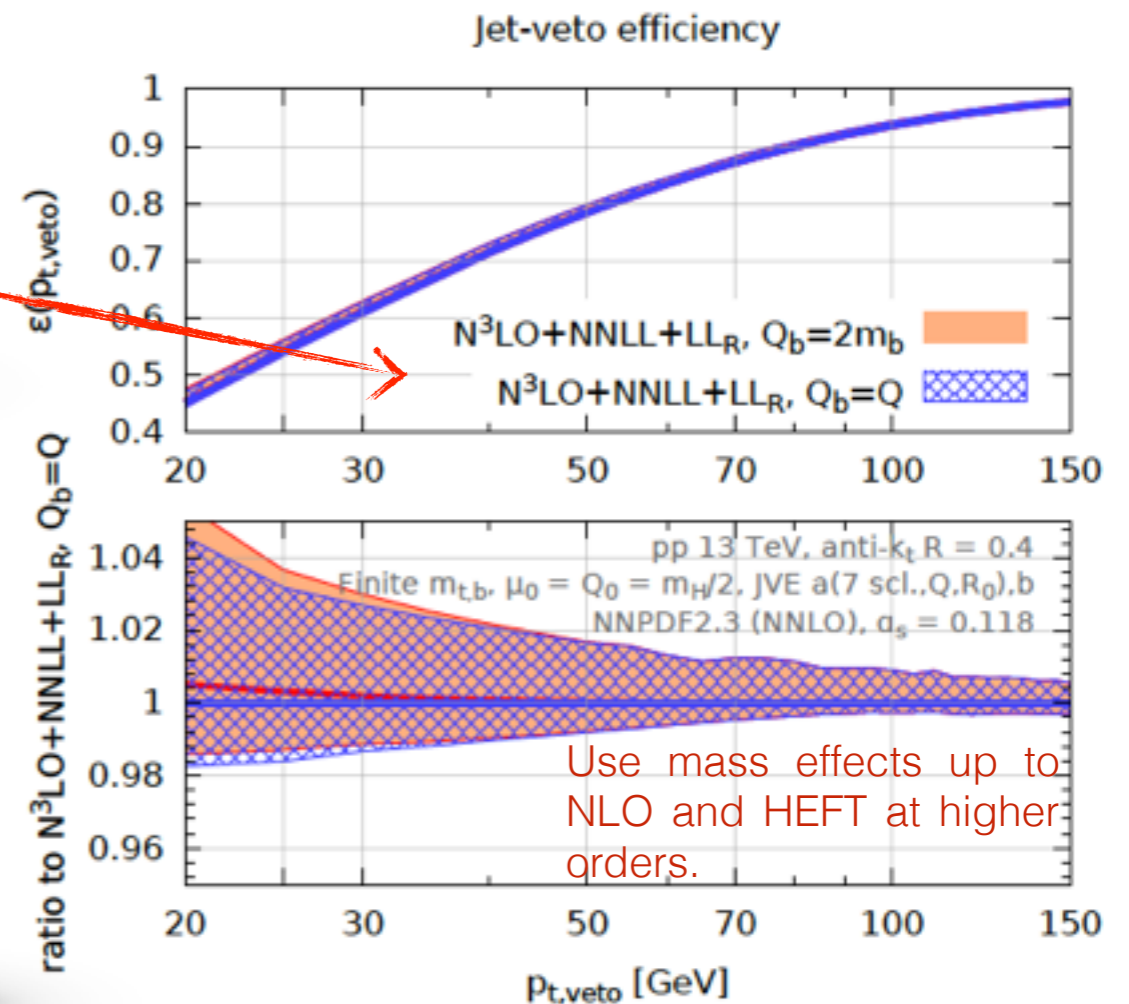
# Quark-mass effects



- Treat “bottom” logs on the same footing as other regular terms which vanish when  $p_t \rightarrow 0$   
 [Banfi, PM, Zanderighi 1308.4634]  
 [Mantler, Wiesemann 1210.8263]
- Switch off resummation around  $m_b$  for the bottom contribution (i.e. set  $Q_b \sim m_b$ )  
 [Grazzini, Sargsyan 1306.4581]

Here  $Q_b$  is varied by a factor of 2 in the  $Q_b = 2m_b$  case, while for the second case with  $Q_b = Q$  we stick to the nominal variation by a factor of 3/2

- Difference between the two prescriptions is negligible above 20 GeV therefore we choose to set  $Q_b = Q = m_H/2$
- resummation of mass logs moderate at DL (abelian lim)  
 [Melnikov, Penin 1602.09020]
- NNLO calculation desirable - will also help establish which prescription is more appropriate  
 [gg->hg in Melnikov, Tancredi, Wever 1610.03747]



Use mass effects up to NLO and HEFT at higher orders.

Including a one-jet bin

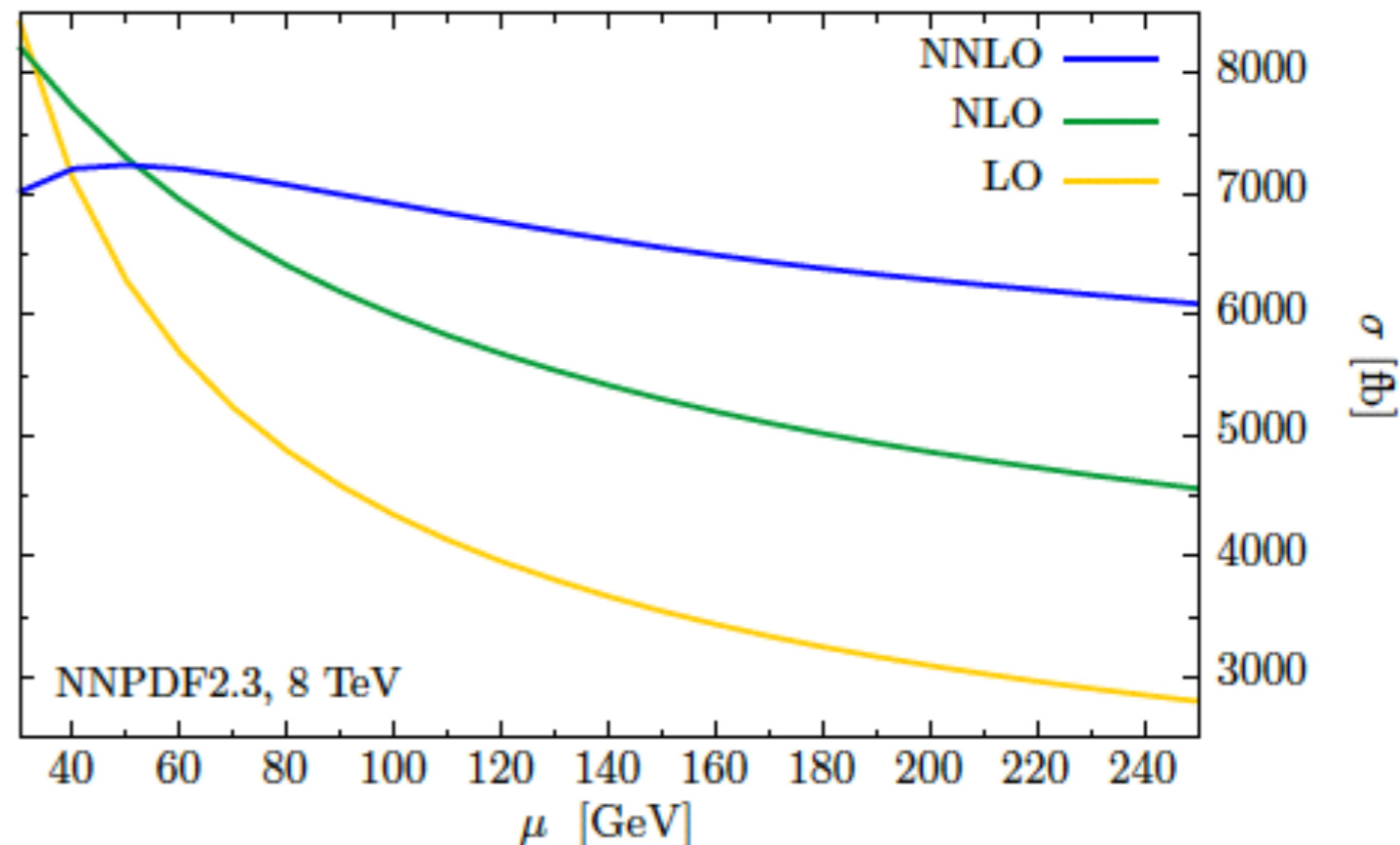


# The case with 3 jet bins

The (exclusive) 1-jet bin can be added - 3 schemes available at NNLO

$$\begin{aligned} \epsilon_1^{(a)} &= 1 - \frac{\sigma_{\geq 2\text{-jet}}^{\text{NLO}}}{\sigma_{\geq 1\text{-jet}}^{\text{NNLO}}}, \\ \epsilon_1^{(b)} &= 1 - \frac{\sigma_{\geq 2\text{-jet}}^{\text{NLO}}}{\sigma_{\geq 1\text{-jet}}^{\text{NLO}}}, \\ \epsilon_1^{(c)} &= 1 - \frac{\sigma_{\geq 2\text{-jet}}^{\text{NLO}}}{\sigma_{\geq 1\text{-jet}}^{\text{LO}}} + \left( \frac{\sigma_{\geq 1\text{-jet}}^{\text{NLO}}}{\sigma_{\geq 1\text{-jet}}^{\text{LO}}} - 1 \right) \frac{\sigma_{\geq 2\text{-jet}}^{\text{LO}}}{\sigma_{\geq 1\text{-jet}}^{\text{LO}}}. \end{aligned}$$

NLO K factor for the inclusive XS within the radius of convergence. Scheme (c) is sensible in this case



# The case with 3 jet bins

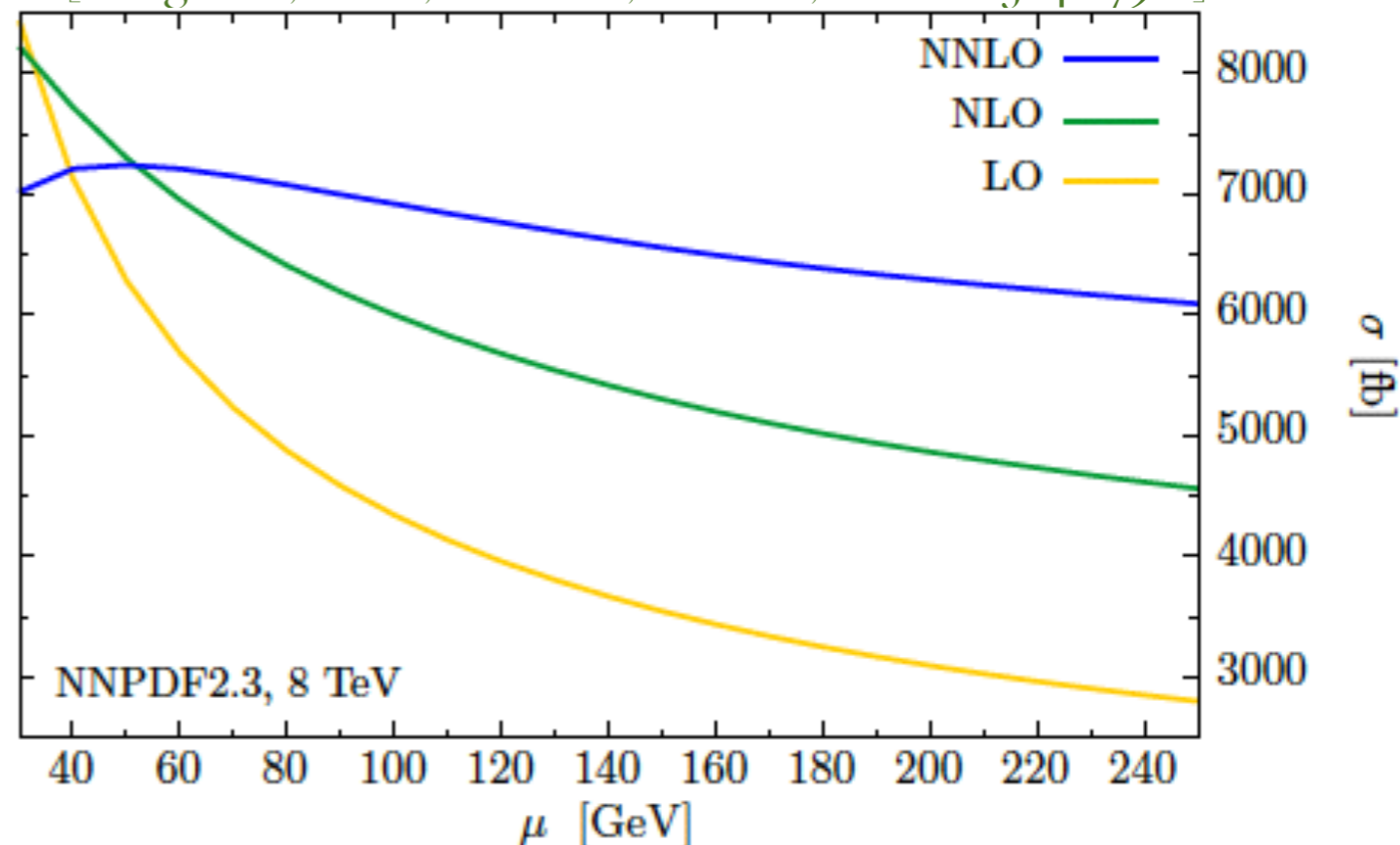
The (exclusive) 1-jet bin can be added - 3 schemes available at NNLO

[PM Les Houches proceedings 2013]

$$\begin{aligned} \epsilon_1^{(a)} &= 1 - \frac{\sigma_{\geq 2\text{-jet}}^{\text{NLO}}}{\sigma_{\geq 1\text{-jet}}^{\text{NNLO}}}, \\ \epsilon_1^{(b)} &= 1 - \frac{\sigma_{\geq 2\text{-jet}}^{\text{NLO}}}{\sigma_{\geq 1\text{-jet}}^{\text{NLO}}}, \\ \epsilon_1^{(c)} &= 1 - \frac{\sigma_{\geq 2\text{-jet}}^{\text{NLO}}}{\sigma_{\geq 1\text{-jet}}^{\text{LO}}} + \left( \frac{\sigma_{\geq 1\text{-jet}}^{\text{NLO}}}{\sigma_{\geq 1\text{-jet}}^{\text{LO}}} - 1 \right) \frac{\sigma_{\geq 2\text{-jet}}^{\text{LO}}}{\sigma_{\geq 1\text{-jet}}^{\text{LO}}}. \end{aligned}$$

NLO K factor for the inclusive XS within the radius of convergence. Scheme (c) is sensible in this case

[Boughezal, Caola, Melnikov, Petriello, Schulze 1504.07922]



# The case with 3 jet bins: covariance matrix

The (exclusive) 1-jet bin can be added - 3 schemes available at NNLO

$$\text{Cov}[\sigma_{0\text{-jet}}, \sigma_{1\text{-jet}}, \sigma_{\geq 2\text{-jet}}] = \begin{pmatrix} \Delta\sigma_{0\text{-jet}} \cdot \Delta\sigma_{0\text{-jet}} & \Delta\sigma_{0\text{-jet}} \cdot \Delta\sigma_{1\text{-jet}} & \Delta\sigma_{0\text{-jet}} \cdot \Delta\sigma_{\geq 2\text{-jet}} \\ \Delta\sigma_{1\text{-jet}} \cdot \Delta\sigma_{1\text{-jet}} & \Delta\sigma_{1\text{-jet}} \cdot \Delta\sigma_{\geq 2\text{-jet}} & \Delta\sigma_{\geq 2\text{-jet}} \cdot \Delta\sigma_{\geq 2\text{-jet}} \end{pmatrix}$$

$$\Delta\sigma_{0\text{-jet}} = (0, \sigma_{\text{tot}}\delta\epsilon_0, \epsilon_0\delta\sigma_{\text{tot}}),$$

$$\Delta\sigma_{1\text{-jet}} = ((1 - \epsilon_0)\sigma_{\text{tot}}\delta\epsilon_1, -\epsilon_1\sigma_{\text{tot}}\delta\epsilon_0, \epsilon_1(1 - \epsilon_0)\delta\sigma_{\text{tot}}),$$

$$\Delta\sigma_{\geq 2\text{-jet}} = (-(1 - \epsilon_0)\sigma_{\text{tot}}\delta\epsilon_1, -(1 - \epsilon_1)\sigma_{\text{tot}}\delta\epsilon_0, (1 - \epsilon_1)(1 - \epsilon_0)\delta\sigma_{\text{tot}}).$$

# The case with 3 jet bins: covariance matrix

The (exclusive) 1-jet bin can be added - 3 schemes available at NNLO

[PM Les Houches proceedings 2013]

$$\text{Cov}[\sigma_{0\text{-jet}}, \sigma_{1\text{-jet}}, \sigma_{\geq 2\text{-jet}}] = \begin{pmatrix} \Delta\sigma_{0\text{-jet}} \cdot \Delta\sigma_{0\text{-jet}} & \Delta\sigma_{0\text{-jet}} \cdot \Delta\sigma_{1\text{-jet}} & \Delta\sigma_{0\text{-jet}} \cdot \Delta\sigma_{\geq 2\text{-jet}} \\ \Delta\sigma_{1\text{-jet}} \cdot \Delta\sigma_{1\text{-jet}} & \Delta\sigma_{1\text{-jet}} \cdot \Delta\sigma_{\geq 2\text{-jet}} & \Delta\sigma_{\geq 2\text{-jet}} \cdot \Delta\sigma_{\geq 2\text{-jet}} \end{pmatrix}$$

$$\Delta\sigma_{0\text{-jet}} = (0, \sigma_{\text{tot}}\delta\epsilon_0, \epsilon_0\delta\sigma_{\text{tot}}),$$

$$\Delta\sigma_{1\text{-jet}} = ((1 - \epsilon_0)\sigma_{\text{tot}}\delta\epsilon_1, -\epsilon_1\sigma_{\text{tot}}\delta\epsilon_0, \epsilon_1(1 - \epsilon_0)\delta\sigma_{\text{tot}}),$$

$$\Delta\sigma_{\geq 2\text{-jet}} = (-(1 - \epsilon_0)\sigma_{\text{tot}}\delta\epsilon_1, -(1 - \epsilon_1)\sigma_{\text{tot}}\delta\epsilon_0, (1 - \epsilon_1)(1 - \epsilon_0)\delta\sigma_{\text{tot}}).$$

# Conclusions

- State-of-the-art predictions for the jet-veto efficiency and 0-jet cross section in H production includes:
  - N3LO corrections to the total cross section
  - NNLO corrections to the inclusive 1-jet cross section
  - NNLL resummation for jet-veto logarithms
  - small-R resummation effects at LL accuracy
  - heavy-quark mass effects

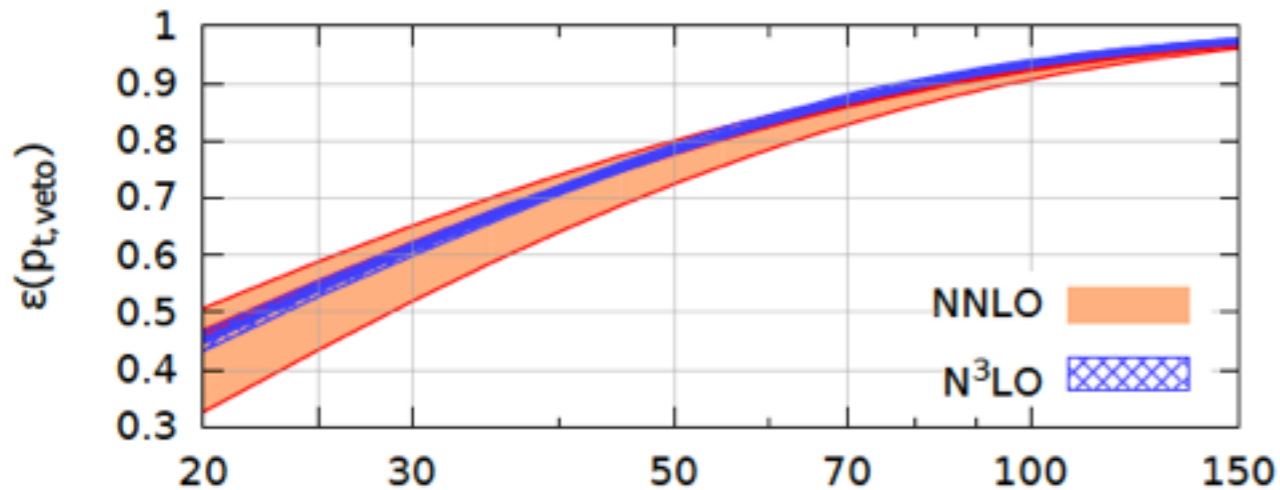
[Code `JetVHeto-v3.0` available at <https://jetvheto.hepforge.org/>]
- JVE method has been revisited to ameliorate some features that show up at higher energies and taking into account the good convergence of the perturbative series
- Corrections w.r.t. to the previous NNLO+NNLL predictions are at the few-percent level - theoretical uncertainties are reduced to  $\sim 3\%$  (efficiency)/ $\sim 4\%$  (0-jet cross section)
- At this level of precision other effects become as important (quark masses at NNLO, EW, non-perturbative corrections) - PDF and strong coupling uncertainties also of the same order

# Additional material

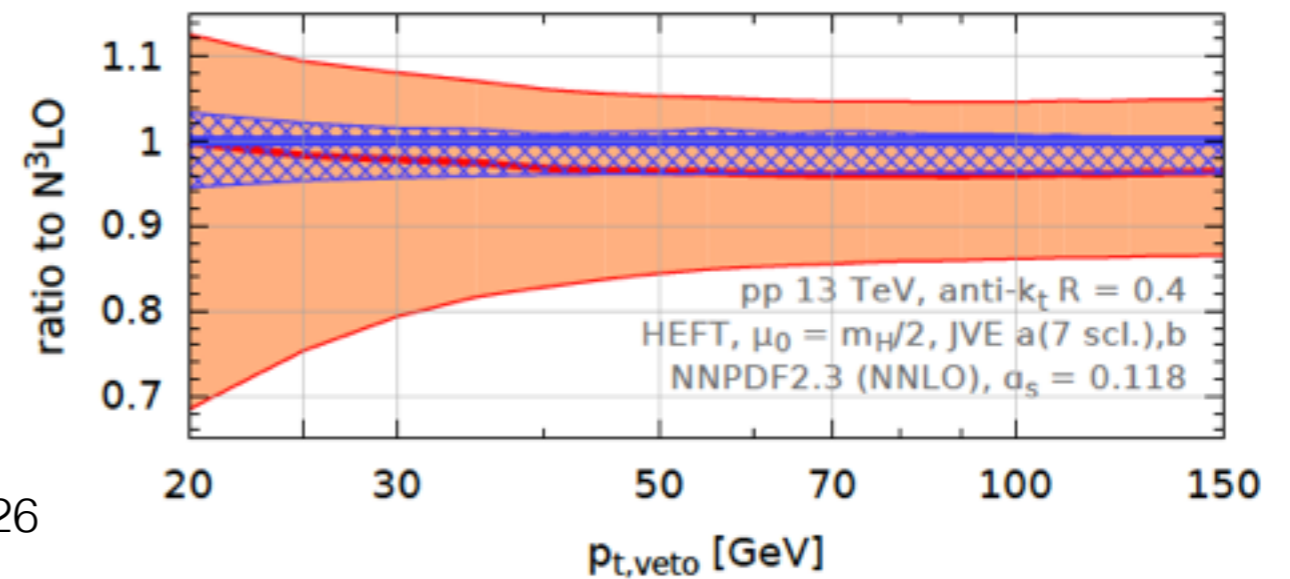
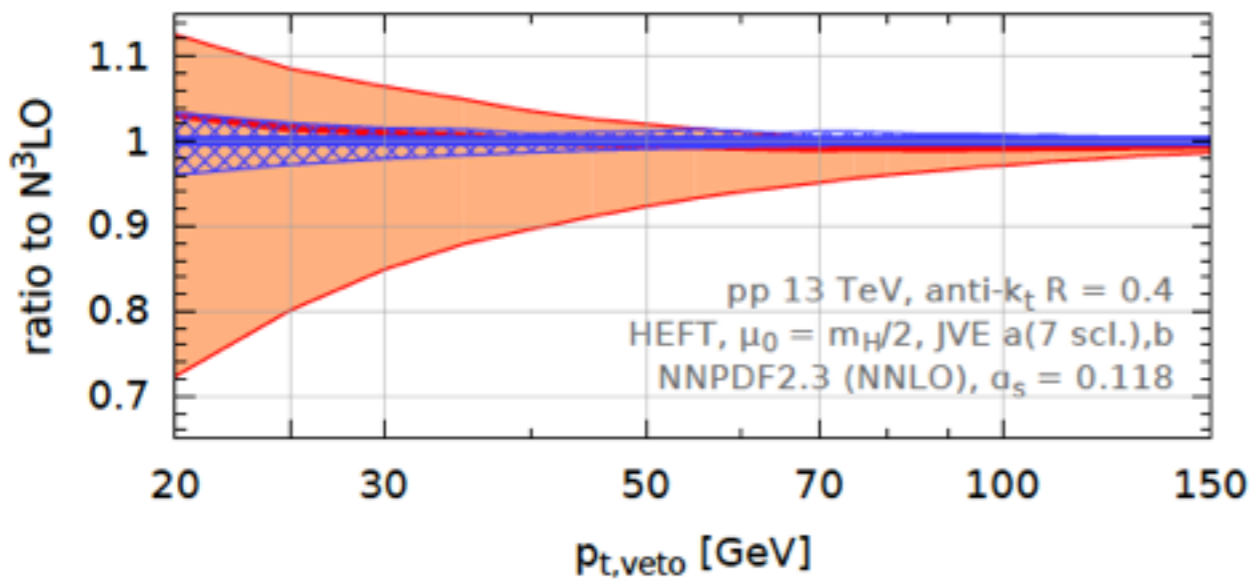
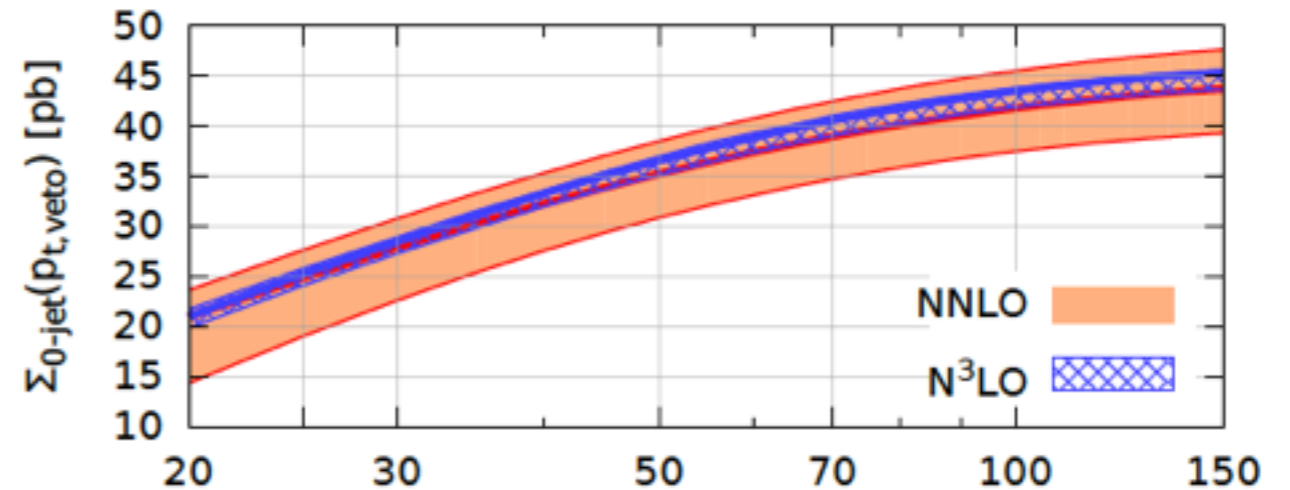
# Updated JVE prescription @ N<sup>3</sup>LO

- The same issue can show up in other processes with large NLO K factors - in these cases it is not safe to expand around  $K \rightarrow 0$
- Updated scheme prescription: we limit ourselves to schemes (a) and (b) (i.e. expand out the last perturbative order for the total cross section)
  - This provides useful information and it's not overly conservative at both small and large  $p_t$ .

N<sup>3</sup>LO v. NNLO jet veto efficiency



N<sup>3</sup>LO v. NNLO jet veto cross section



# Numerics at the 13 TeV LHC ( $\mu_0 = m_H/2$ )

LHC 13 TeV [pb]	$\sigma_{\text{tot},2}$	$\sigma_{\text{tot},3}$	$\sigma_{1j \geq 25\text{GeV}}^{\text{NLO}}$	$\sigma_{1j \geq 25\text{GeV}}^{\text{NNLO}}$	$\sigma_{1j \geq 30\text{GeV}}^{\text{NLO}}$	$\sigma_{1j \geq 30\text{GeV}}^{\text{NNLO}}$
EFT	$45.2^{+4.0}_{-4.6}$	$46.6^{+0.0}_{-1.7}$	$20.3^{+3.6}_{-3.4}$	$21.3^{+0.3}_{-1.3}$	$17.3^{+3.0}_{-2.9}$	$18.1^{+0.2}_{-1.1}$
<i>t</i> -only	$47.1^{+4.3}_{-4.9}$	$48.6^{+0.2}_{-2.0}$	$20.7^{+3.8}_{-3.5}$	$21.8^{+0.4}_{-1.4}$	$17.6^{+3.2}_{-3.0}$	$18.4^{+0.2}_{-1.2}$
<i>t, b</i>	$44.9^{+4.2}_{-4.7}$	$46.4^{+0.2}_{-1.9}$	$20.6^{+3.7}_{-3.5}$	$21.6^{+0.4}_{-1.4}$	$17.6^{+3.2}_{-3.0}$	$18.4^{+0.2}_{-1.2}$

Scale variation.  
N3LO total cross section updated after latest "bug"-fix

Full NLO and HEFT for NNLO N3LO corrections

LHC 13 TeV	$\epsilon^{\text{N}^3\text{LO}+\text{NNLL}+\text{LL}_R}$	$\Sigma_{0\text{-jet}}^{\text{N}^3\text{LO}+\text{NNLL}+\text{LL}_R}$ [pb]	$\Sigma_{0\text{-jet}}^{\text{N}^3\text{LO}}$	$\Sigma_{0\text{-jet}}^{\text{NNLO}+\text{NNLL}}$
$p_{t,\text{veto}} = 25 \text{ GeV}$	$0.541^{+0.017}_{-0.009}$	$25.1^{+0.8}_{-1.1}$	$24.7^{+0.5}_{-1.2}$	$24.6^{+2.6}_{-3.8}$
$p_{t,\text{veto}} = 30 \text{ GeV}$	$0.611^{+0.016}_{-0.008}$	$28.3^{+0.8}_{-1.2}$	$28.0^{+0.4}_{-1.3}$	$27.8^{+2.9}_{-4.0}$

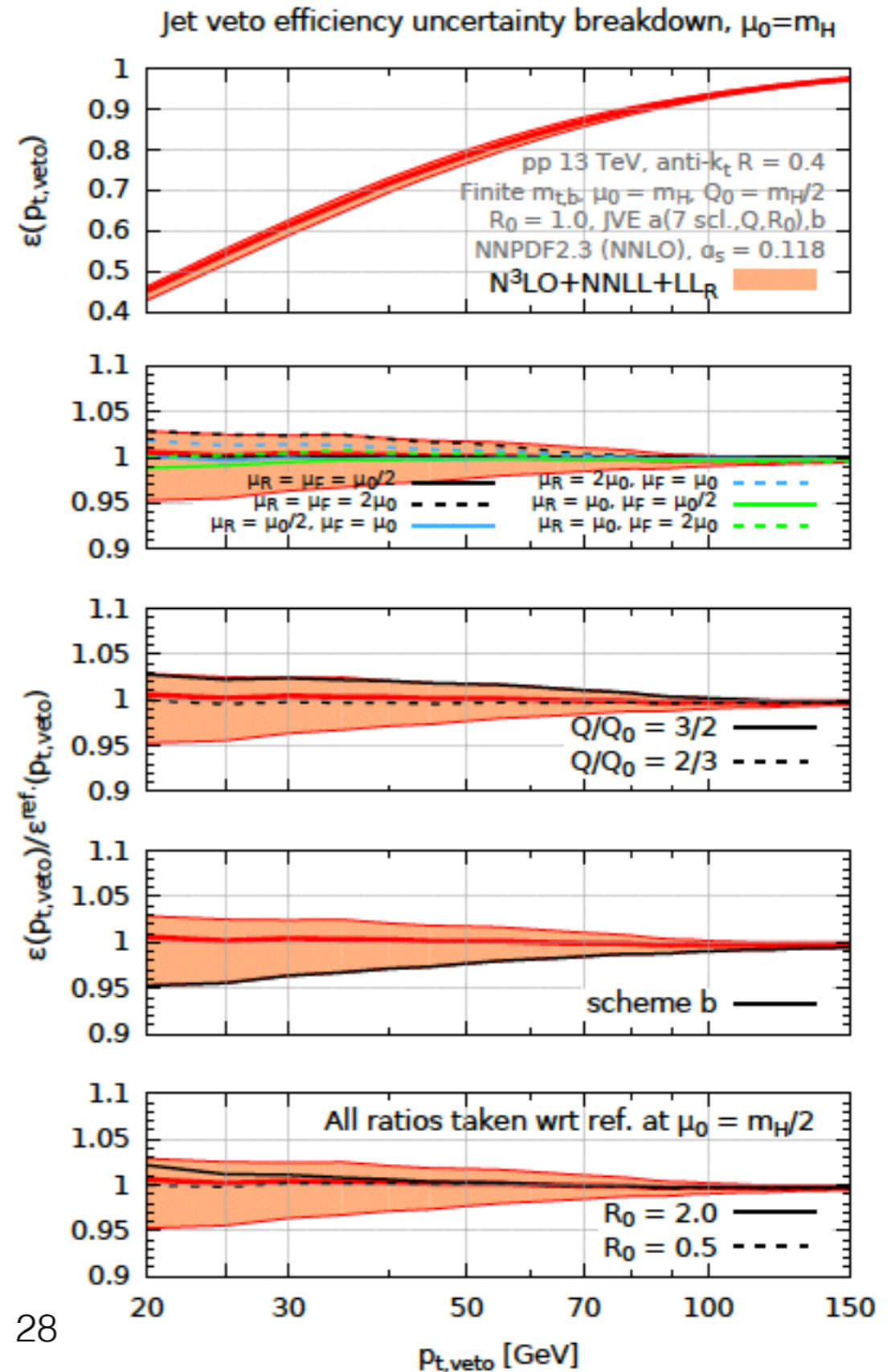
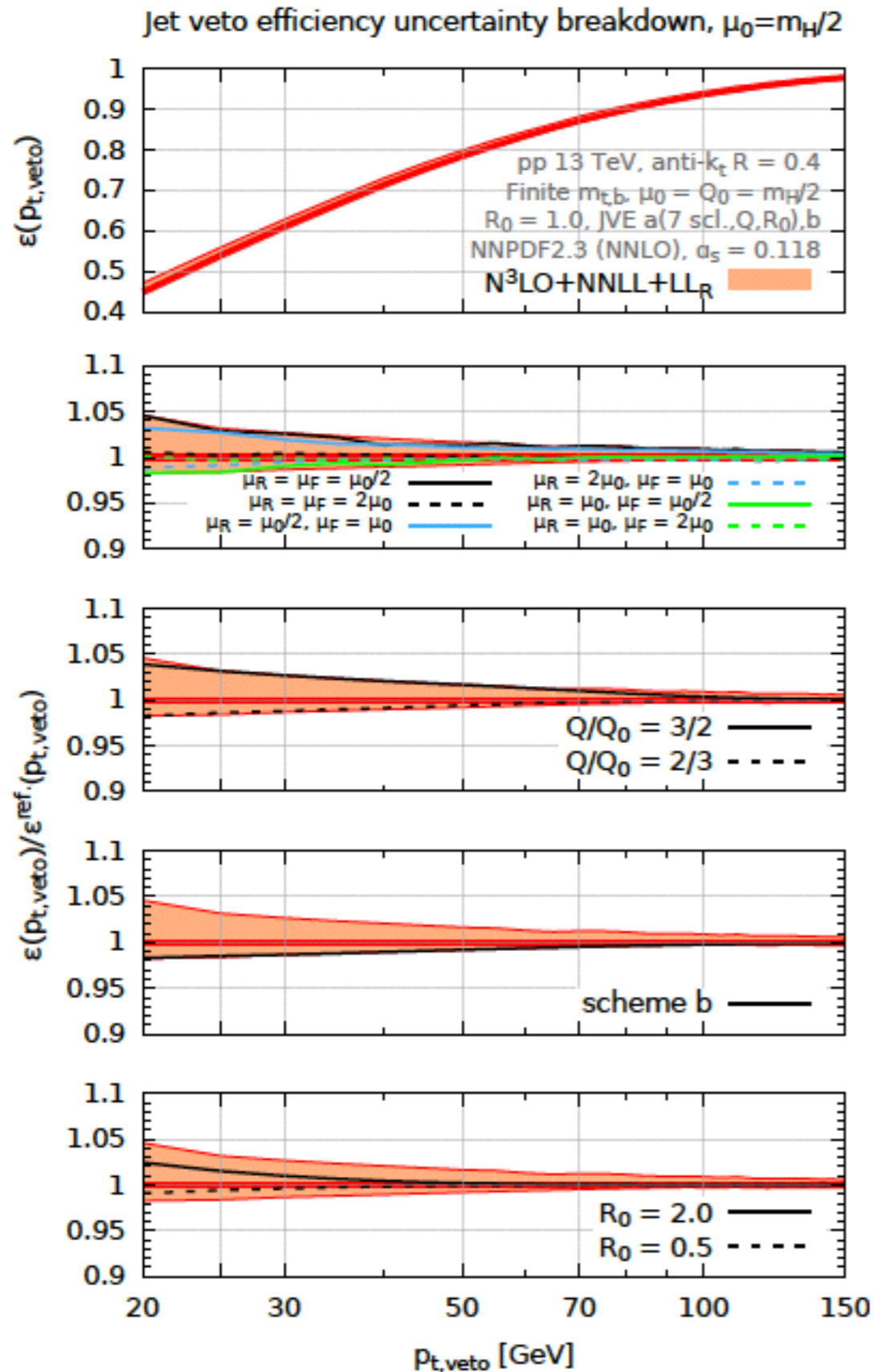
JVE

LHC 13 TeV	$\Sigma_{\geq 1\text{-jet}}^{\text{NNLO}+\text{NNLL}+\text{LL}_R}$ [pb]	$\Sigma_{\geq 1\text{-jet}}^{\text{NNLO}}$ [pb]
$p_{t,\text{min}} = 25 \text{ GeV}$	$21.3^{+0.4}_{-1.2}$	$21.6^{+0.7}_{-1.0}$
$p_{t,\text{min}} = 30 \text{ GeV}$	$18.0^{+0.4}_{-1.0}$	$18.4^{+0.6}_{-0.9}$

JVE



# Breakdown of uncertainties



# Quark-mass effects

- When exact mass loops are considered, the bottom-quark amplitude is enhanced by logarithms of the ratio  $p_t/m_b$  in the regime  $m_b^2 \ll p_t^2 \ll m_H^2$ 
  - e.g. at NLO (currently the state-of-the-art prediction for the full process), the 0-jet cross section features terms of the type

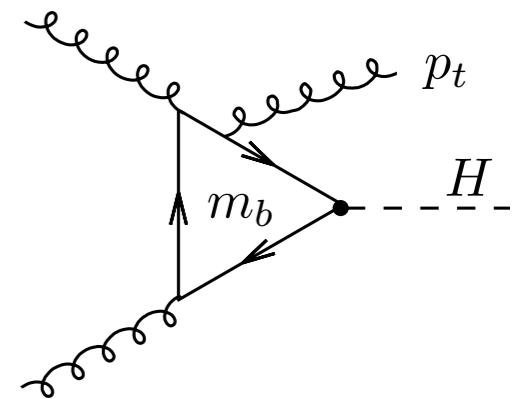
[Banfi, PM, Zanderighi 1308.4634]  
[Grazzini, Sargsyan 1306.4581]

$$\alpha_s \frac{m_b^2 m_t^2}{m_H^4} \ln^2 \frac{p_{t,\text{veto}}}{m_b} \ln \frac{p_{t,\text{veto}}}{m_H}$$

(interference)

$$\alpha_s \frac{m_b^4}{m_H^4} \ln^4 \frac{p_{t,\text{veto}}}{m_b} \ln^2 \frac{p_{t,\text{veto}}}{m_H}$$

(bottom squared)



- These logarithms **do not exist** for  $p_t \leq m_b$  (HQEFT picture) , therefore QCD factorisation is preserved in the limit  $p_t \rightarrow 0$  (i.e. the new logarithms are never divergent and come with a bunch of other regular terms  $\sim \mathcal{O}(p_t^2)$  )

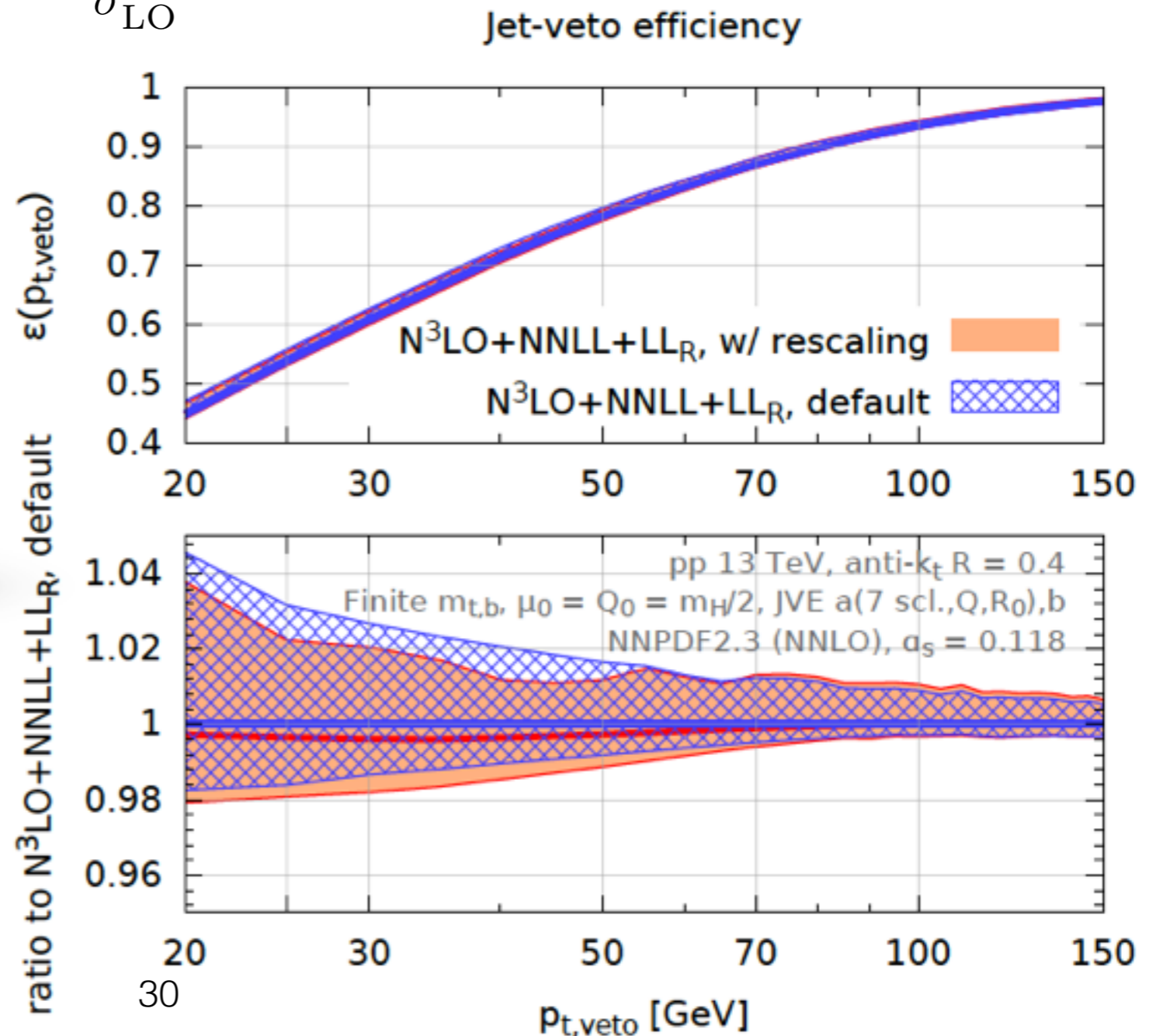
$$|\mathcal{M}(\{\tilde{p}\}, k_1, \dots, k_n)|^2 = |M_{\text{Born}}(\{\tilde{p}\})|^2 |M_{\text{div}}(k_1, \dots, k_n)|^2 + \text{regular terms}$$

- At normal jet-veto scales their contribution is potentially large, and an all-order treatment is preferable

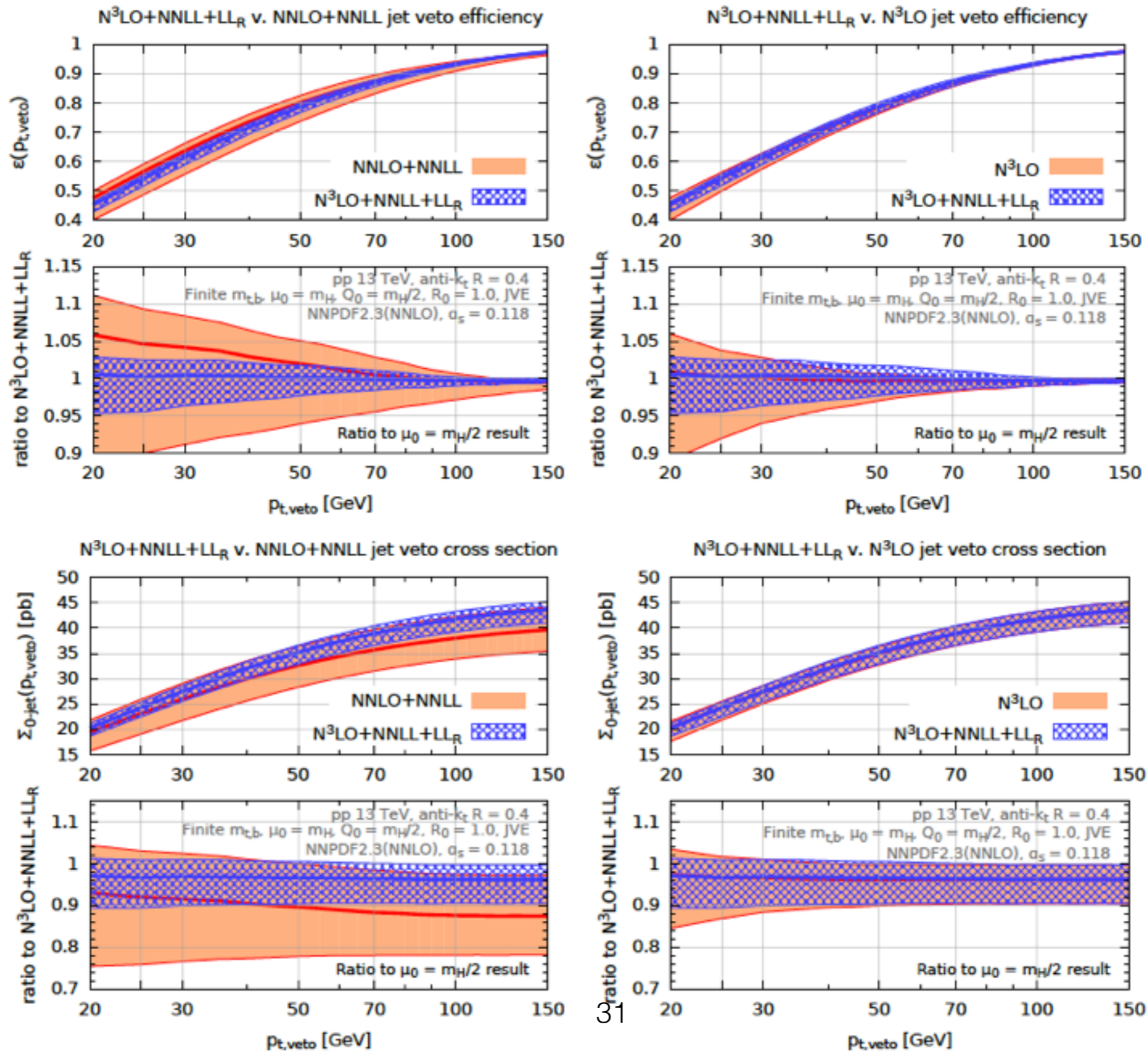
# Quark-mass effects

- Robustness against possible sizeable quark-mass effects beyond NLO is tested by rescaling the NNLO and N3LO 0-jet cross sections by the factor  $\frac{\sigma_{LO}^t}{\sigma_{LO}^{heft}}$

- Impact on the central value moderate
- Slight reduction of uncertainty at small pt

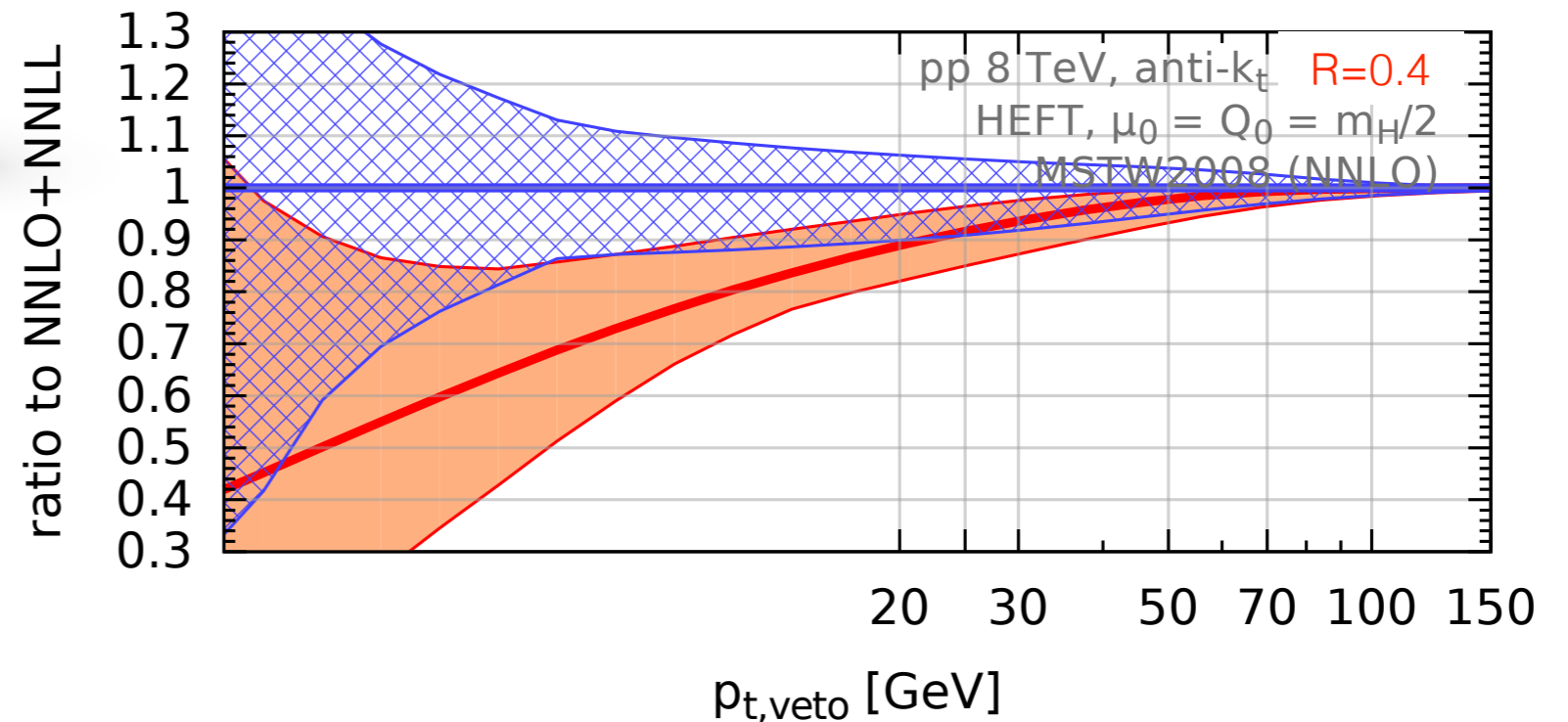
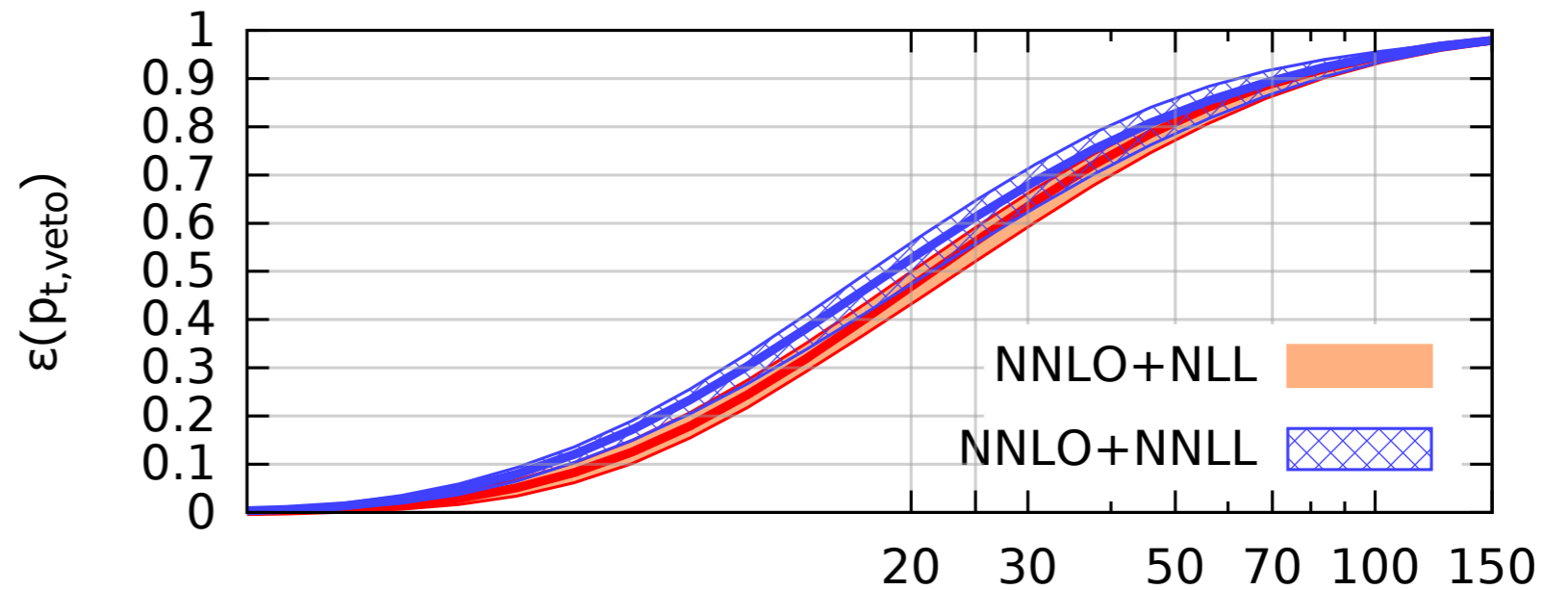


# Results at the 13 TeV LHC ( $\mu_0 = m_H$ )



# NNLL+NNLO v. NLL+NNLO

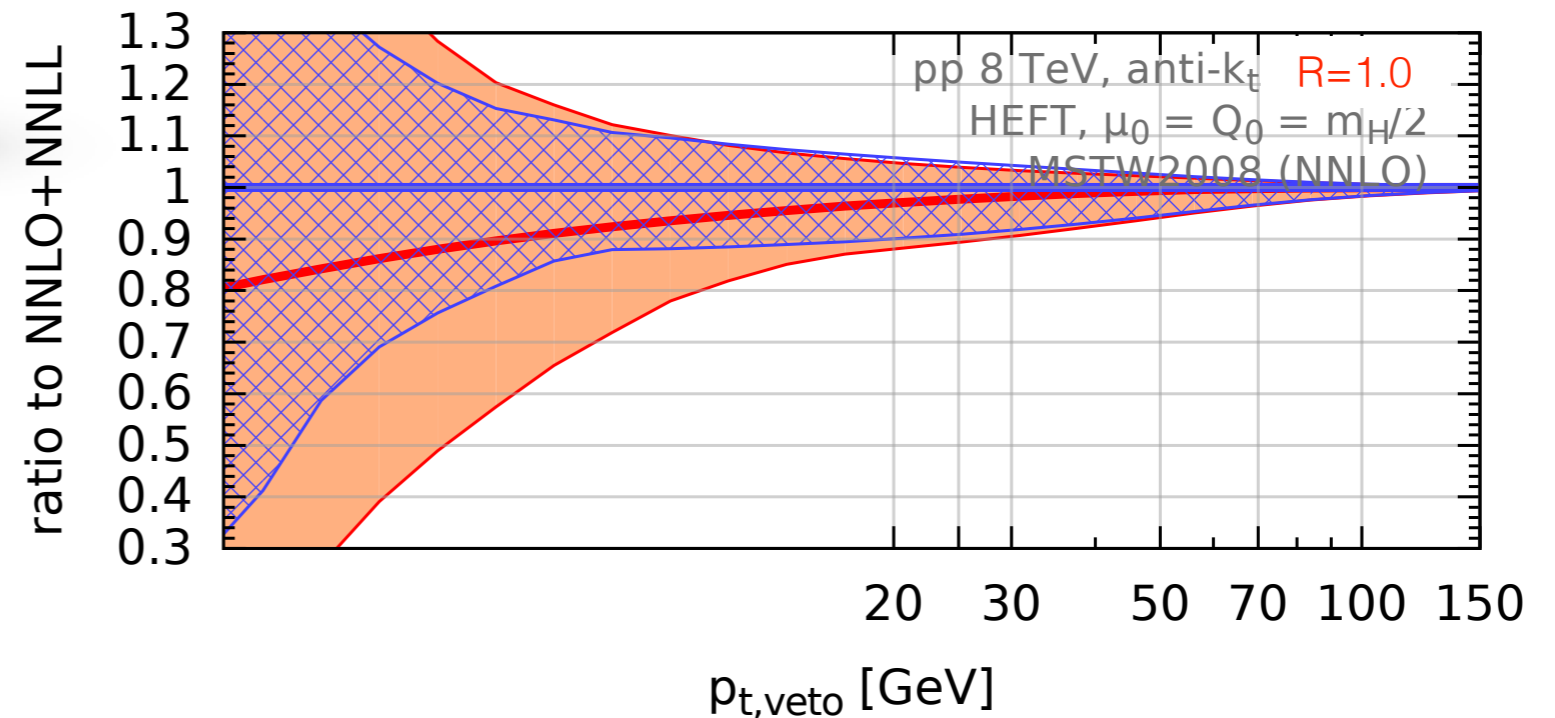
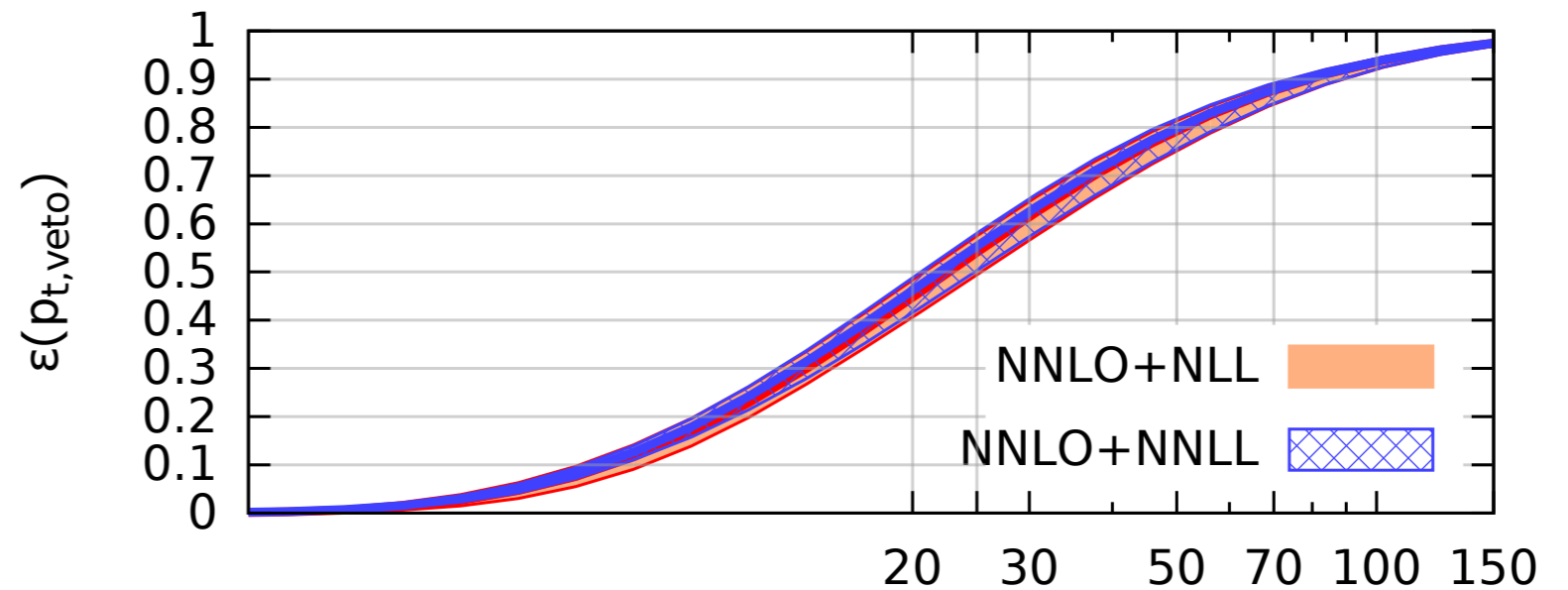
NNLO+NNLL v. NNLO+NLL jet veto efficiency



Moderate uncertainty reduction with  $R=0.4$  due to the large NNLL corrections associated with the soft gluon splitting

# NNLL+NNLO v. NLL+NNLO

NNLO+NNLL v. NNLO+NLL jet veto efficiency



Gluon splitting significantly reduced for  $R=1.0$ , NNLL corrections smaller.