



### Merging of jet-quenching with full event simulations

# Steffen A. Bass Duke University

- current status and open questions
- development of standardized interfaces:
  - the OSCAR2008H file format
  - common table format for hydro equation of state
- the PCM brick problem









# Motivation





### Jet-Medium Interactions

- Heavy-ion collisions at RHIC have produced a state of matter which behaves similar to an ideal fluid
- ➤ (3+1)D Relativistic Fluid Dynamics and hybrid macro+micro models are highly successful in describing the dynamics of bulk QCD matter
- ➤ A new generation of Parton Cascade Models is being developed for the same purpose (BAMPS...)
- Jet energy-loss calculations have reached a high level of technical sophistication (BDMPS, GLV, higher twist, AMY), yet they employ a variety of sometimes simple models for the evolution of the underlying deconfined medium...
- all conclusions to be drawn from jet energy-loss calculations are necessarily with respect to the nature of the medium assumed in the calculation
- need to treat medium and hard probes consistently and at same level of sophistication!
- same medium necessary for comparison of different energy-loss schemes and vice versa!





### **Current Status:**

Jet energy-loss and hydro

Hirano & Nara: Phys. Rev. **C66** (2002) 041901

Hirano & Nara: Phys. Rev. **C69** (2004) 034908

Renk, Ruppert, Nonaka & Bass: Phys. Rev. C75 (2007) 031902

Majumder, Nonaka & Bass: Phys. Rev. C76 (2007) 041902

Qin, Ruppert, Turbide, Gale, Nonaka & Bass: Phys. Rev. C76 (2007) 064907

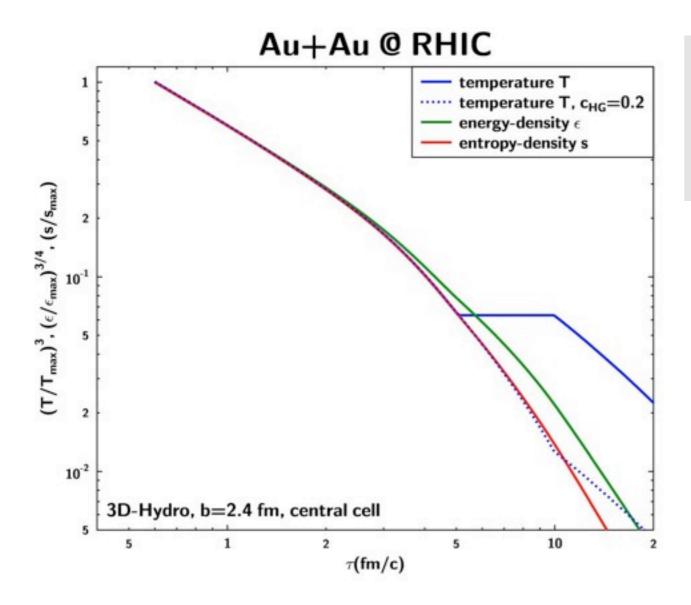
Bass, Gale, Majumder, Nonaka, Qin, Renk, Ruppert: Phys. Rev. C79 (2009) 024901



# Scaling with the Medium: T, $\varepsilon$ or s?



- how does the transport coefficient scale with the thermodynamic properties of the medium? Does the choice of T, ε or s matter? (a priori not known, but should be calculable)
- EoS for ideal QGP (ideal gas of ultrarelativistic bosons):  $\varepsilon = \frac{\pi^2}{30} g_{DOF} T^4$



common choices for scaling:

$$\hat{q} \sim T^3$$
  $\hat{q} \sim \varepsilon^{3/4}$   $\hat{q} \sim s$ 

- > identical results only for ideal QGP
- for non-ideal EoS, value of q will be affected by choice of scaling variable, in particular if energy-loss persists into hadronic phase
- choice of  $c_{HG}=0.2$  mimics scaling with entropy-density s



# Quantitative Comparison:



•define local transport coefficient along trajectory  $\xi$  for all three approaches and compare initial maximum value  $q_0$ :

$$\hat{q}(\xi) = \hat{q}_0 \cdot \Gamma(\xi) \quad \text{with } \Gamma = \left(\frac{T}{T_0}\right)^3, \left(\frac{\varepsilon}{\varepsilon_0}\right)^{3/4}, \left(\frac{S}{S_0}\right)^{3/4}$$

•for ASW, use Baier formula:

$$\hat{q}_0 = 2K \cdot \varepsilon_0^{\frac{3}{4}}$$

•For AMY use:

$$\hat{q}_0 = C \left( \frac{g^2}{4\pi} \right) T_0^3 \frac{8 \times 16\pi}{9}$$

q <sub>0</sub> [GeV <sup>2</sup> /fm]	ASW	НТ	AMY
T	10	2.3	4.1
3	18.5	4.5	X
S		4.3	X

(all values quoted for a gluon jet)

- different medium scaling can affect q by a factor of 2
- a clear difference persists among the different approaches, even when utilizing identical medium evolution & scaling and initial conditions
- the "correct" medium scaling relation is a priori not known, should hopefully be calculable from 1<sup>st</sup> principles QCD



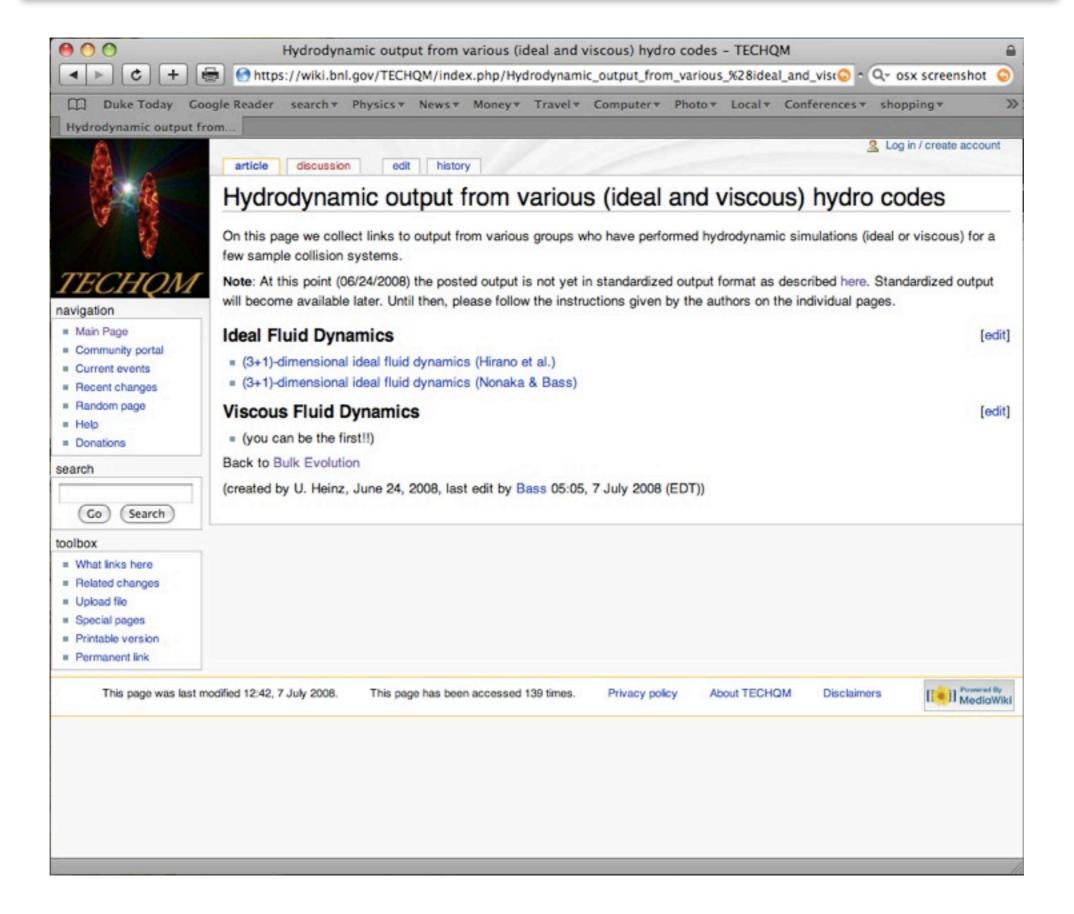


# A Common Output Format for Hydrodynamic Models



# Available Hydro Evolution Files









### The OSCAR2008H Standard

- follows the spirit of the OSCAR initiative
- •OSCAR1997A output format for particle based codes still in use
- 2 output file specifications:
  - •full time evolution file
  - final freeze-out hypersurface
- format needs to be flexible enough to accommodate different geometries, dimensionalities, ideal vs. viscous etc...
- should contain all relevant information on calculation (intial conditions, grid size, collision geometry) to allow for postprocessing and analysis

#### Prototype Developers:

- S.A. Bass & C. Nonaka
- H. Song & U. Heinz
- (T. Hirano)

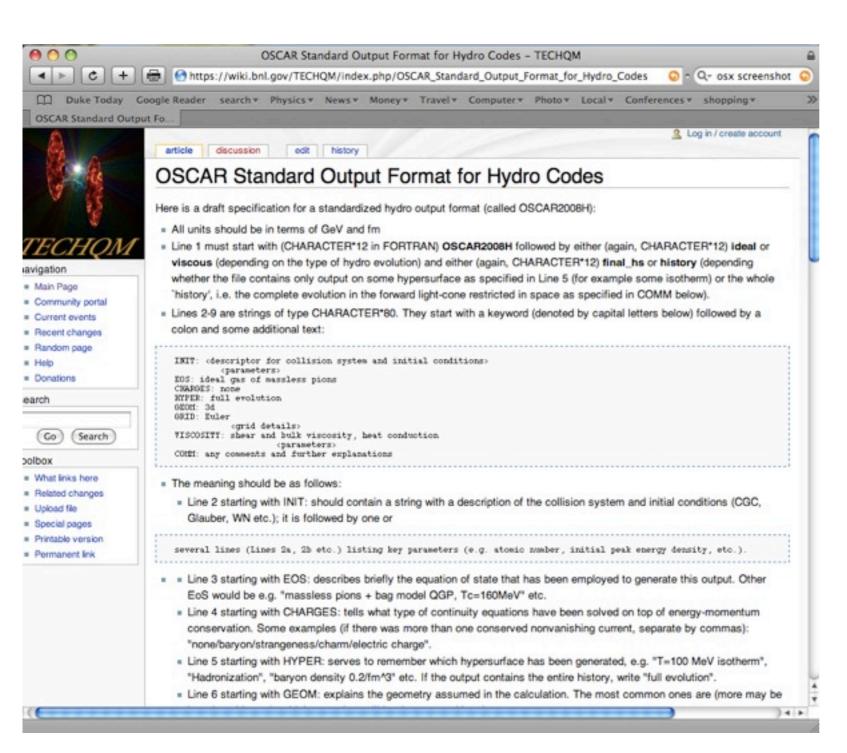
#### Pledged Supporters:

- D. Molnar & P. Huovinen
- P. Romatschke
- D. Teaney & K. Dusling
- Frankfurt Group



# OSCAR2008 Specifications





#### current status:

- posted on TECHQM website
- prototype implementations by Song/Heinz and Bass/Nonaka

#### next steps:

- need to use files in regular workflow to find shortcomings in specifications
- once usability has been established, specifications will be finalized





# Implementation

#### OSCAR2008H file header:

```
OSCAR2008H ideal final hs
INIT: Glauber + Wounded Nucleon
INIT: b= 2.4000 n_B,0= 0.0100 e_0= 300.0000
INIT: r_b/c= 0.8000 sigma_h 1.4000 eta_0= 2.0000
INIT: rad0 = 6.3800 rho0 = 0.1688 delta = 0.5400 sigma = 4.2000
EOS: Bag Model QGP + HRG
CHARGES: baryon
HYPER: T=110.0 MeV isotherm
GEOM: 3d
GRID: Lagrange
20000 101 101 121 1 0 0
    0.600 10000.600 -15.000 15.000 -15.000 15.000 -18.000
                                                                   18.000
VISCOSITY: none
COMM: (c) C. Nonaka & S.A. Bass
COMM: Phys.Rev.C75:014902 (2007)
```





```
OSCAR2008H ideal
                                             history
INIT: Glauber + Wounded Nucleon
INIT: b=
                      2.4000 n B,0=
                                                      0.1500 e 0= 40.0000
INIT: r b/c=
                             0.6000 sigma h
                                                               1.5000 eta_0=
                                                                                               0.5000
INIT: rad0 = 6.3800 rho0 = 0.1688 delta = 0.5400 sigma = 4.2000
EOS: smooth cross-over with tri-critical point
CHARGES: baryon
HYPER: full evolution
GEOM: 3d
GRID: Lagrange
100000 77 77 77 1 0
         0.600 10000.600
                                                               11.400
                                                                                -11.400
                                                                                                     11.400
                                                                                                                      -11.400
                                                                                                                                          11.400
                                        -11.400
VISCOSITY: none
COMM: (c) C. Nonaka & S.A. Bass
COMM: Phys.Rev.C75:014902 (2007)
                                   0 0.600000000000000E+00 -0.11400000000000E+02 -0.114000000000E+02 -0.11400000000E+02
                                                                                                                                                                                                                                                0.0000
                                                                                                                                                                                                                                                                 0.0350
                                                                                                                                                                                                                                                                                   0.0000 -0.57157676
                                                                                                                                                                                                                                0.0000
                1
                         0
                                   0 0.600000000000000E+00 -0.11100000000000E+02 -0.114000000000E+02 -0.114000000000E+02
                                                                                                                                                                                                                                0.0000
                                                                                                                                                                                                                                                0.0000
                                                                                                                                                                                                                                                                 0.0350
                                                                                                                                                                                                                                                                                   0.0000 -0.56141639
                2
                         0
                                   0 0.600000000000000E+00 -0.10800000000000E+02 -0.1140000000000E+02 -0.1140000000000E+02
                                                                                                                                                                                                                                0.0000
                                                                                                                                                                                                                                                0.0000
                                                                                                                                                                                                                                                                 0.0350
                                                                                                                                                                                                                                                                                   0.0000 -0.55098764
                                                                                                                                                                                                                                0.0000
                                                                                                                                                                                                                                                0.0000
       0
                3
                         0
                                   0 0.600000000000000E+00 -0.10500000000000E+02 -0.114000000000E+02 -0.1140000000000E+02
                                                                                                                                                                                                                                                                 0.0350
                                                                                                                                                                                                                                                                                   0.0000 -0.54028623
                          0
                                   0 0.600000000000000E+00 -0.10200000000000E+02 -0.114000000000E+02 -0.1140000000000E+02
                                                                                                                                                                                                                                0.0000
                                                                                                                                                                                                                                                 0.0000
                                                                                                                                                                                                                                                                 0.0350
                                                                                                                                                                                                                                                                                   0.0000 -0.52930809
       0
                                                                                                                                                                                                                                0.0000
                 5
                          0
                                   0 0.600000000000000E+00 -0.99000000000000E+01 -0.1140000000000E+02 -0.1140000000000E+02
                                                                                                                                                                                                                                                0.0000
                                                                                                                                                                                                                                                                 0.0350
                                                                                                                                                                                                                                                                                   0.0000 -0.51804959
       0
                 6
                          0
                                   0 0.600000000000000E+00 -0.96000000000000E+01 -0.1140000000000E+02 -0.1140000000000E+02
                                                                                                                                                                                                                                0.0000
                                                                                                                                                                                                                                                0.0000
                                                                                                                                                                                                                                                                 0.0350
                                                                                                                                                                                                                                                                                   0.0000 -0.50650734
                7
                          0
                                   0 0.600000000000000E+00 -0.9300000000000001E+01 -0.114000000000E+02 -0.11400000000000E+02
                                                                                                                                                                                                                                0.0000
                                                                                                                                                                                                                                                0.0000
                                                                                                                                                                                                                                                                 0.0350
                                                                                                                                                                                                                                                                                   0.0000 -0.49467838
                8
                                                                                                                                                                                                                                0.0000
                                                                                                                                                                                                                                                 0.0000
                                   0 0.600000000000000E+00 -0.90000000000000E+01 -0.1140000000000E+02 -0.1140000000000E+02
                                                                                                                                                                                                                                                                 0.0350
                                                                                                                                                                                                                                                                                   0.0000 -0.48256016
       0
                9
                          0
                                   0 0.6000000000000000E+00 -0.869999999999999E+01 -0.11400000000000E+02 -0.11400000000000E+02
                                                                                                                                                                                                                                0.0000
                                                                                                                                                                                                                                                0.0000
                                                                                                                                                                                                                                                                 0.0350
                                                                                                                                                                                                                                                                                   0.0000 -0.47015060
              10
                          0
                                   0 0.600000000000000E+00 -0.84000000000000E+01 -0.114000000000E+02 -0.1140000000000E+02
                                                                                                                                                                                                                                0.0000
                                                                                                                                                                                                                                                0.0000
                                                                                                                                                                                                                                                                 0.0350
                                                                                                                                                                                                                                                                                  0.0000 -0.45744816
              11
                          0
                                   0 0.600000000000000E+00 -0.81000000000000E+01 -0.1140000000000E+02 -0.1140000000000E+02
                                                                                                                                                                                                                                0.0000
                                                                                                                                                                                                                                                 0.0000
                                                                                                                                                                                                                                                                 0.0350
                                                                                                                                                                                                                                                                                   0.0000 -0.44445183
              12
                          0
                                   0.0000
                                                                                                                                                                                                                                                0.0000
                                                                                                                                                                                                                                                                 0.0350
                                                                                                                                                                                                                                                                                   0.0000 -0.43116122
              13
                                   0 0.600000000000000E+00 -0.750000000000000E+01 -0.1140000000000E+02 -0.11400000000000E+02
                                                                                                                                                                                                                                0.0000
                                                                                                                                                                                                                                                0.0000
                                                                                                                                                                                                                                                                 0.0350
                                                                                                                                                                                                                                                                                   0.0000 -0.4175765
              14
                          0
                                   0 0.600000000000000E+00 -0.72000000000000E+01 -0.1140000000000E+02 -0.1140000000000E+02
                                                                                                                                                                                                                                0.0000
                                                                                                                                                                                                                                                0.0000
                                                                                                                                                                                                                                                                 0.0350
                                                                                                                                                                                                                                                                                   0.0000 -0.40369883
                                   0 0.600000000000000E+00 -0.69000000000000E+01 -0.114000000000E+02 -0.1140000000000E+02
                                                                                                                                                                                                                                0.0000
                                                                                                                                                                                                                                                0.0000
                                                                                                                                                                                                                                                                 0.0350
                                                                                                                                                                                                                                                                                   0.0000 -0.38952966
              15
                          0
              16
                                   0 0.600000000000000E+00 -0.660000000000000E+01 -0.114000000000E+02 -0.1140000000000E+02
                                                                                                                                                                                                                                0.0000
                                                                                                                                                                                                                                                0.0000
                                                                                                                                                                                                                                                                 0.0350
                                                                                                                                                                                                                                                                                   0.0000 -0.37507152
                          0
              17
                          0
                                                                                                                                                                                                                                0.0000
                                                                                                                                                                                                                                                0.0000
                                                                                                                                                                                                                                                                 0.0350
                                                                                                                                                                                                                                                                                   0.0000 -0.3603276
                                   0 0.600000000000000E+00 -0.63000000000000E+01 -0.114000000000E+02 -0.1140000000000E+02
                                   \alpha = \alpha =
                                                                                                                                                                                                                               0 0000
                                                                                                                                                                                                                                                0 0000
                                                                                                                                                                                                                                                                 a asea
                                                                                                                                                                                                                                                                                  0 0000 0 2/E20211
```







- developers need to work with format to ensure its practicability/ usability
- OSCAR2008H should be finalized by next TECHQM workshop
- accepted use policy for output files needs to be defined
- •should TECHQM consider supplying analysis tools for the output?
- start work on interpolator routines:
  - use native or OSCAR2008 format?
  - which quantities should be provided?
  - which programming languages to support?
  - specify interpolation algorithm?





# Common Table Format for Hydro Equation of State



### Motivation



- ullet one of the main goals for the measurement of high  $p_T$  hadrons and/or jets is their capability to act as well-calibrated probes of the properties of the medium, aka the "full event"
- ambiguities arise from multiple sources, among them the sensitivity to the Equation of State
- only a controlled variation of individual modeling components will allow for the disentanglement of the different sensitivities and the unambiguous determination of the medium properties
- focus here on the sensitivity to the Equation of State in (v)RFD calculations:
  - a common format for tabulating the EoS would allow for easy interchange of different EoS in (v)RFD calculations and would thus enable systematic comparisons on the EoS sensitivity to the bulk evolution and to jet energy-loss calculations
  - such a format would also provide an efficient interface to the Lattice community for dissemination of their results to the transport community



### Current Status & To-Do List



#### current status:

- solicitation for description of current status on EoS treatment and proposals for a new standard treatment sent out to TECHQM community in 6/2009
- feedback received from a subset of practitioners (Ohio State, Purdue, Frankfurt)
- still waiting to hear from more community members

#### to-do list:

- develop prototype for common EoS table based on community feedback
  - needs to be able to work for ideal and viscous RFD
  - needs to be able to treat full chemical equilibrium and PCE
- create repository for different EoS tables on TECHQM website
- lobby for community-wide adoption of standard





### The PCM Brick Problem



### Motivation



- Parton Cascade Models are microscopic transport models based on the Boltzmann Equation - they describe the full time-evolution of a system of deconfined partons (quarks and gluons) at high density and temperature
- PCMs offer the unique ability to not only describe the evolution of the jet as it interacts with the medium, but also the response of the medium to the jet on a microscopic level
- a number of PCM implementations exist, each with their unique set of features and limitations, due to the algorithms employed to solve the Boltzmann eqn. and to deal with issues such as covariance, detailed-balance and radiative corrections
- the differences in the PCM implementations pose a challenge for the extraction of robust physics conclusions from these calculations
- a set of standard benchmarks will allow for
  - the comparison of the different PCM implementations among each other under controlled conditions
  - the comparison with analytic solutions, e.g. of the QGP brick problem
  - the verification of specific physics features, e.g. the implementation of the LPM effect

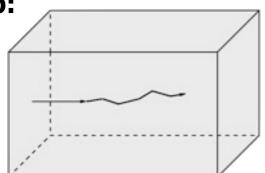
#### the PCM brick problem



### PCM Brick Problem: Setup



#### **Box Setup:**



- define a box of 5 fm length w/ periodic boundary conditions
- populate box with an ensemble of thermal gluons at T=300, 400, 500 or 600 MeV
- •insert a hard gluon w/ initial momentum  $p_x$ =50, 100, 200, 300, 400 GeV and track its evolution through the medium

#### **Cross Section:**

 use a Debye-screened elastic gg crosssection:

$$\frac{d\sigma}{dq_{\perp}^2} = \frac{9\pi\alpha_s^2}{\left(q_{\perp}^2 + m_D^2\right)^2}$$

choose Debye-mass to be:

$$m_D^2 = \frac{24}{\pi} \alpha_s T^2$$

•use a fixed coupling:  $\alpha_s = 0.3$ 

#### **Desired Calculations:**

- distribution of momentum transfers
- energy-loss as function of distance traveled
- energy-loss transport coefficient defined as:

$$\hat{q} = \frac{1}{l_x} \sum_{i=1}^{N_{coll}} (\Delta p_{\perp,i})^2$$

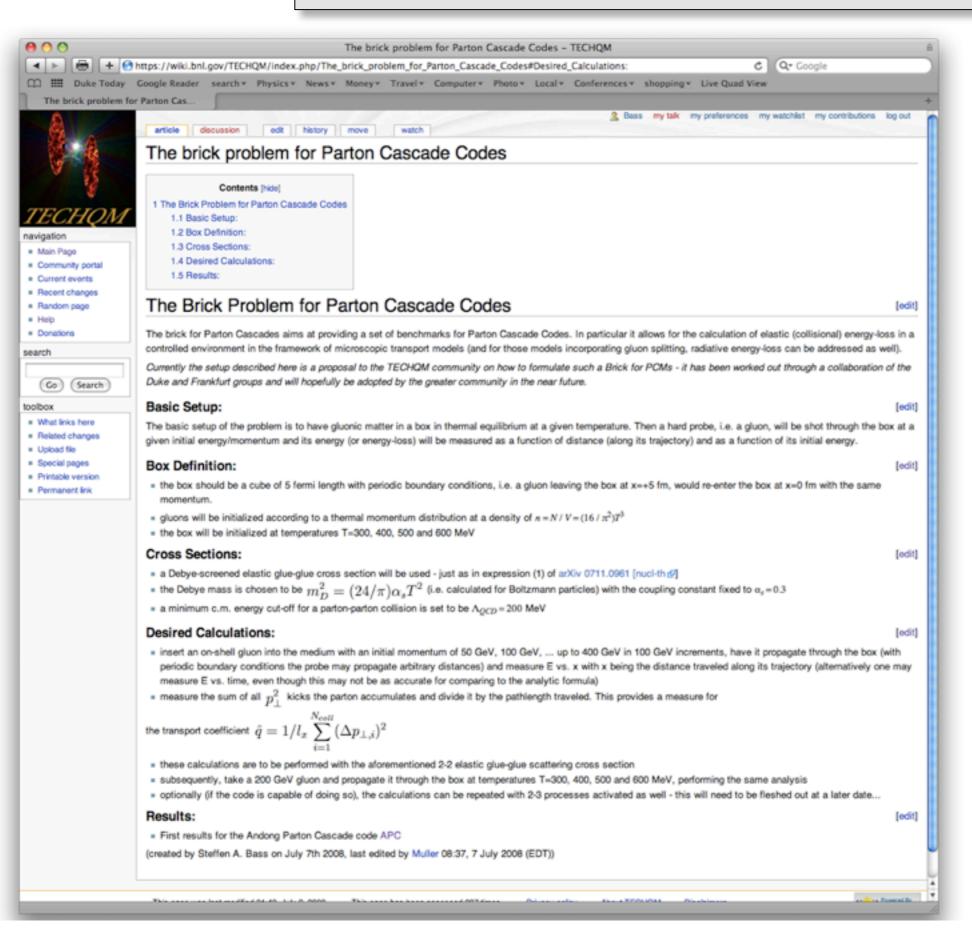
#### **Optional Extensions:**

- full QGP: study flavor-dependence
- heavy quark energy-loss
- radiative energy-loss
- medium response: conical flow, correlations



### **Current Status & To-Do List**



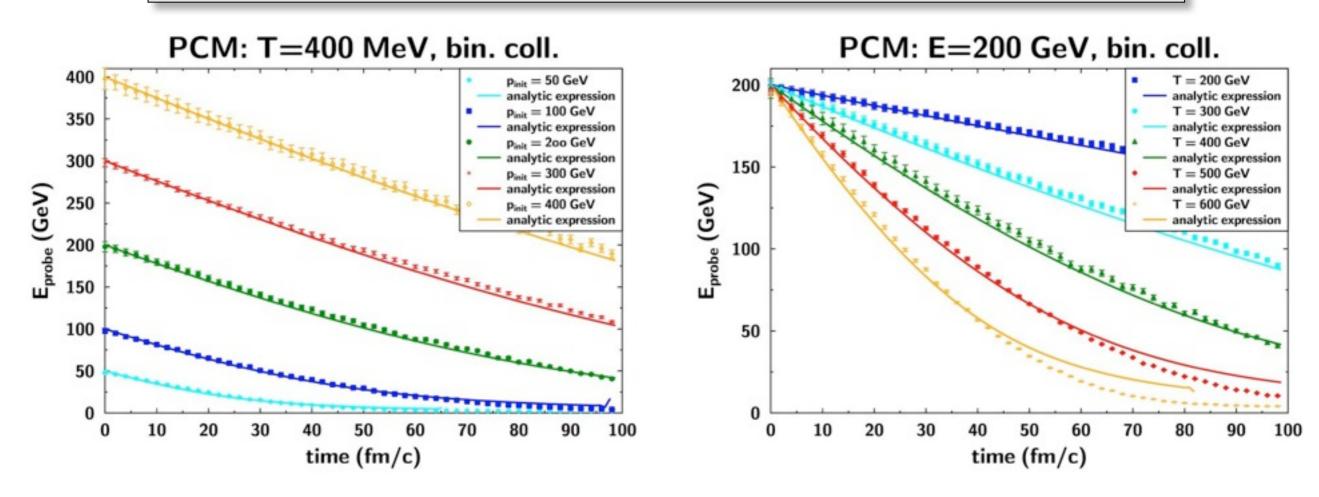


- •full specifications of the PCM brick problem have been posted on the TECHQM website
- several groups have pledged to undertake the calculations and compare results (Duke, Frankfurt, Andong)
- need to publicize this effort for wider adoption



## Energy- & Temperature Dependence





• the PCM brick calculations can be compared to the analytic expression for collisional energy-loss of light quarks/gluons:

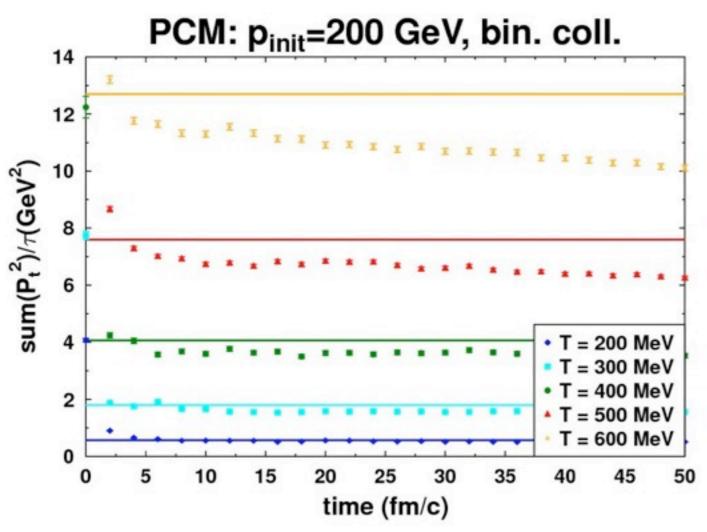
$$E_p(x) = E_p(0) - x \frac{\alpha_s C_2 m_D^2}{2} \ln \left| \frac{\sqrt{E_p(x)T}}{m_D} \right|$$

- excellent agreement with analytic expression over time-scale of 40+ fm/c
- caveat of current calculation: uses time instead of path-length this may account for deviations at longer times & high temperatures



# Energy-loss transport coefficient





 definition of q-hat for microscopic transport models:

$$\hat{q} = \frac{1}{l_x} \sum_{i=1}^{N_{coll}} (\Delta p_{\perp,i})^2$$

• the PCM brick calculations can be compared to the analytic expression of q-hat for

light quarks/gluons:

$$\hat{q} = \frac{C_2 g^2 T m_D^2}{2\pi} \ln \left[ \frac{\sqrt{E_p T}}{m_D} \right]$$

- good agreement with analytic expression for lower temperatures T=200-400 MeV
- caveat of current calculation: uses time instead of path-length this may account for deviations at higher temperatures



# Summary



The Merging of jet-quenching with full event simulations is greatly facilitated by the development of standardized interfaces and benchmarks:

#### the OSCAR2008H file format

- allows for a standard interface between jet energy-loss calculations and (v)RFD evolution files
- implementation nearly complete, awaits widespread adoption by community
- common table format for RFD equation of state
  - important for systematic comparisons on the sensitivity to the EoS of various observables, will help to disentangle ambiguities between different physics quantities characterizing the system
  - provides an interface to the Lattice-Gauge community

#### the PCM brick problem

- provides a benchmark for the comparison of the different PCM implementations among each other under controlled conditions
- allows for the comparison with analytic solutions, e.g. of the QGP brick problem
- enables the verification of specific physics features, e.g. the implementation of the LPM effect





# The End



### Motivation



- •one of the main goals for the measurement of high  $p_T$  hadrons and/or jets is their capability to act as well-calibrated probes of the properties of the medium, aka the "full event"
- ambiguities arise from multiple sources:
  - different formalisms for the treatment of hard probe medium interactions yield different values for characteristic medium properties, e.g. q-hat
  - sensitivity to the initial state (e.g. CGC vs. Glauber)
  - nature & treatment of pre-equilibrium phase of medium
  - sensitivity to the Equation of State
  - ideal vs. viscous treatment of medium in RFD, i.e. sensitivity to transport-coefficients, such as the bulk- and shear-viscosity
  - treatment of the hadronic phase: ideal RFD, PCE, hadronic afterburner...
- •only a controlled variation of individual modeling components will allow for the disentanglement of the different sensitivities and the unambiguous determination of the medium properties
- focus here on the sensitivity to the Equation of State in (v)RFD calculations:
  - a common format for tabulating the EoS would allow for easy interchange of different EoS in (v)RFD calculations and would thus enable systematic comparisons on the EoS sensitivity to the bulk evolution and to jet energy-loss calculations
  - such a format would also provide an efficient interface to the Lattice community for dissemination of their results to the transport community