

# Pitfalls in calculating charge response parameter from etch pit

Rupamoy Bhattacharyya

Research Fellow

Centre for Astroparticle Physics & Space Science,

Bose Institute, Kolkata



# Outline of talk

---

- ❑ Motivation.
- ❑ Formation of etch pit inside Nuclear Track Detector.
- ❑ Estimation of the region of applicability of two widely used methods of calculating charge response parameter.
- ❑ Experimental confirmation.
- ❑ Conclusion.

# Motivation

---

Nuclear Track Detectors (NTDs) are used to detect particles (size  $\sim$  nucleus) by observing their tracks inside detector material.

Currently two major experiments use NTDs as their detecting tool

**Magnetic Monopole search (MoEDAL experiment)** at LHCb, CERN

**Strangelet search at mountain altitude** at Bose Institute

In these two experiments, people use two different methods to calculate charge response parameter. Our aim is to study the region of applicability of these two methods.

Technical Design Report of the MoEDAL experiment CERN-LHC-2009-006, MoEDAL-TDR-1.1, September 21,2009

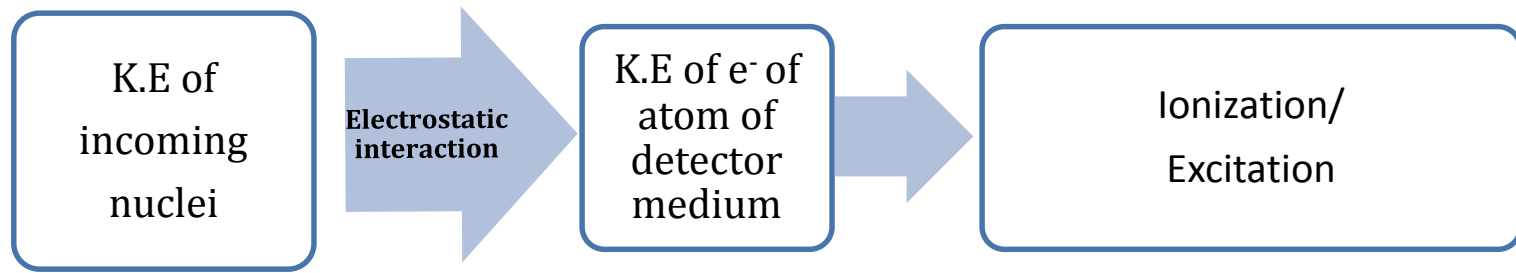
Strangelet Search at Mountain Altitude by R Bhattacharyya, S Dey, Sanjay K Ghosh, A Maulik, Sibaji Raha and D Syam. *Proc Indian Natn Sci Acad* **81** No. 1 February 2015 Special Issue, pp. 165-168.

# Formation of etch pit inside Nuclear Track Detector (NTD)

NTDs belong to a class of passive detectors.

Solid State Nuclear Track Detectors are dielectric solids.

Organic polymer : Polyethylene Terephthalate (PET)  
CR-39  
Makrofol



Electronic energy loss of charged particles follows Bethe-Bloch formula

$$-\frac{dE}{dx} = \frac{4\pi n Z^2}{m_e v^2} \left( \frac{e^2}{4\pi\epsilon_0} \right)^2 \left[ \ln \left( \frac{2m_e v^2}{I} \right) \right]$$

Ionizing particle produces 'permanent' damage trail along its direction of motion.  
Latent Track (diameter 3-10 nm)

# Etching : to make "latent track" visible under Optical Microscope

---

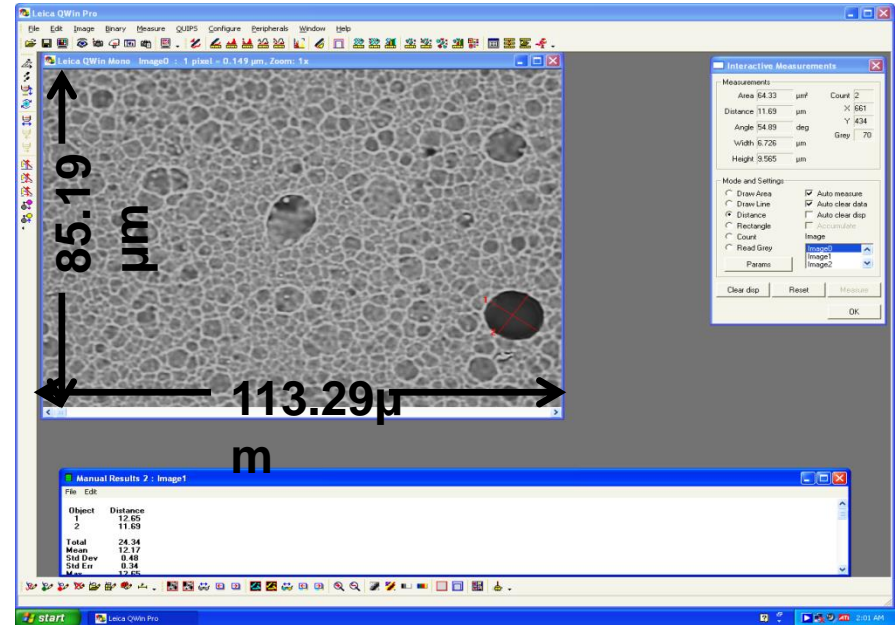
- ❑ Damaged region contains more chemically active zones than surrounding undamaged portion.
- ❑ Applying some chemical reagent ( here we use 6.25 N aqueous solution of NaOH ) makes the damaged portion etched out at a faster rate  $V_T$  (Track etch rate) than the undamaged portion  $V_B$  (Bulk etch rate) and after that size of the damaged portion increased to  $\sim \mu\text{m}$ .
- ❑ **Charge response parameter** ::  $(V_T/V_B)$  :: Necessary condition for the formation of etch-pit :  $V_T/V_B > 1$
- ❑ Now if the Detector (transparent) is kept under the microscope we can observe the etch pits.

Calibration of a solid state nuclear track detector (SSNTD) with high detection threshold to search for rare events in cosmic rays by S. Dey, D. Gupta, A. Maulik, Sibaji Raha, Swapan K. Saha, D. Syam, J. Pakarinen, D. Voulot, F. Wenander. *Astroparticle Physics* 34, 805-808 (2011).

# Images of etch pit

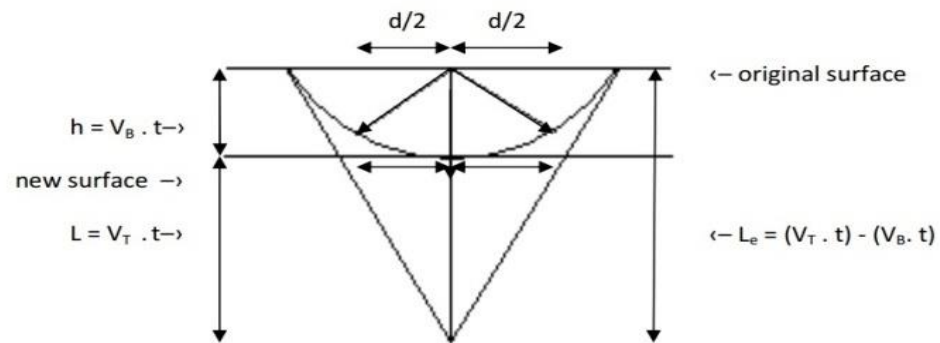
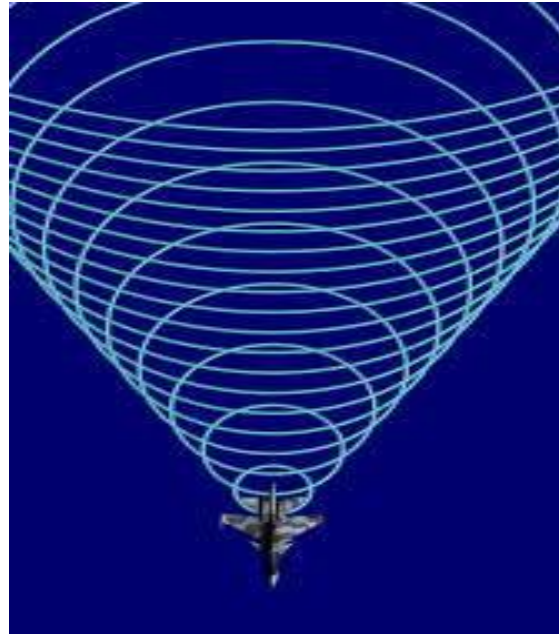


Leica DM 4000 optical microscope

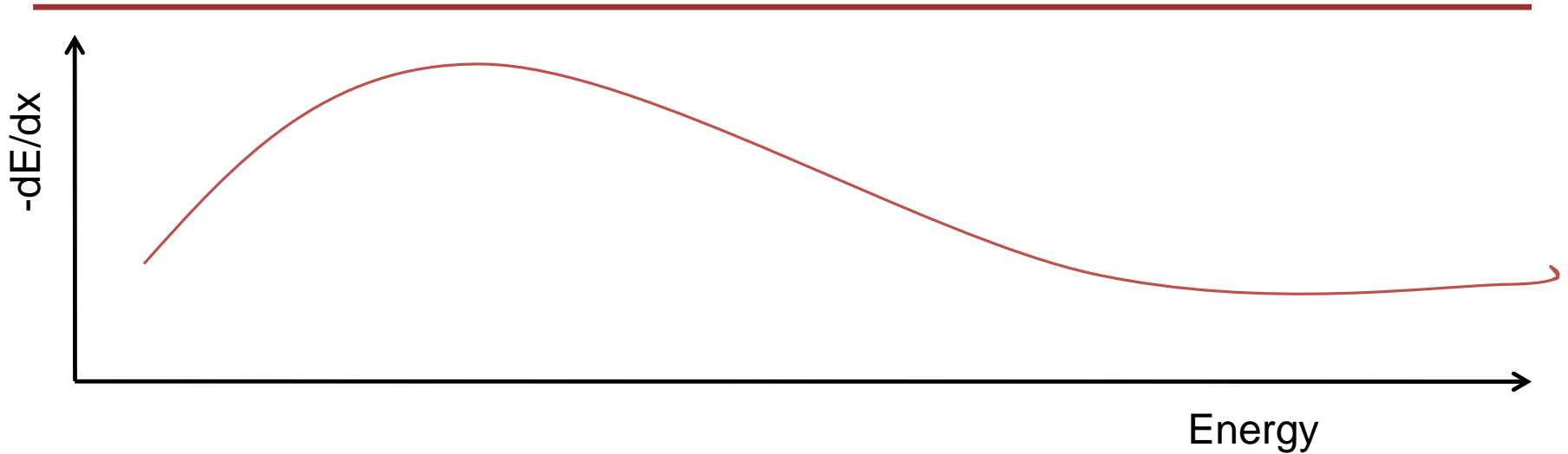


Screenshot during observation using QWin software under x100 dry objective

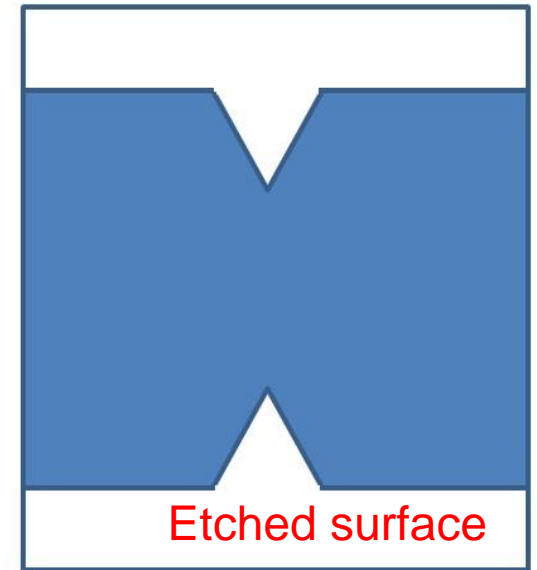
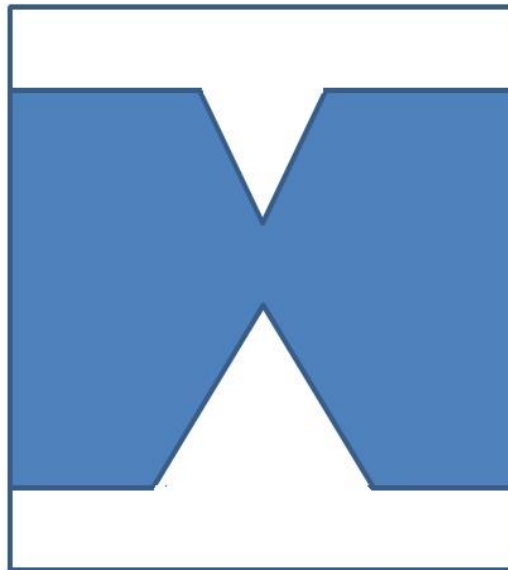
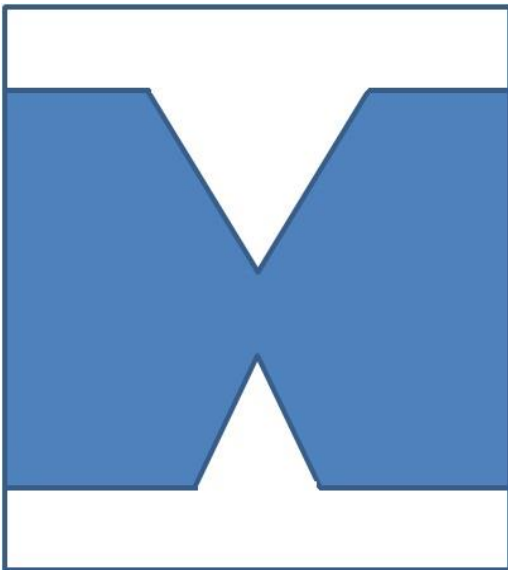
# Why the shape of the etch pit is conical



# Geometry of etch pit



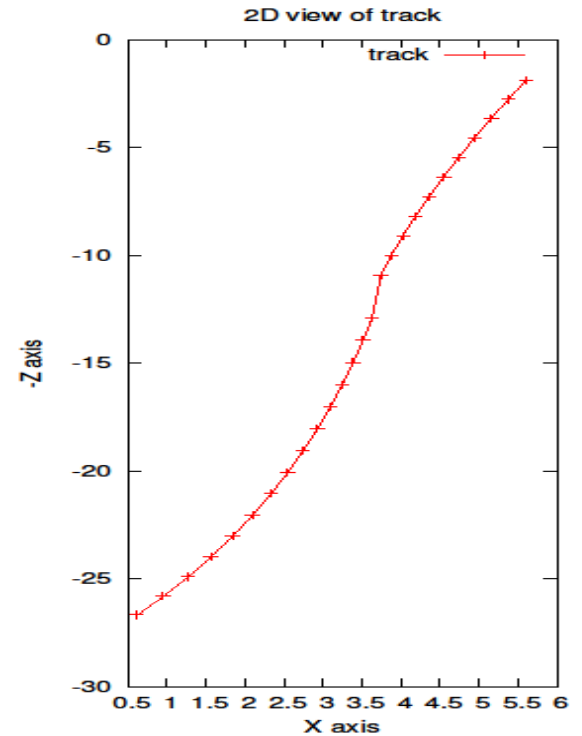
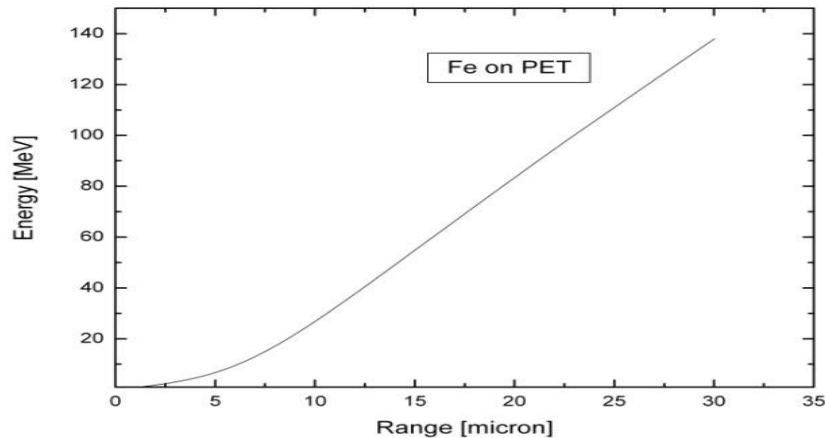
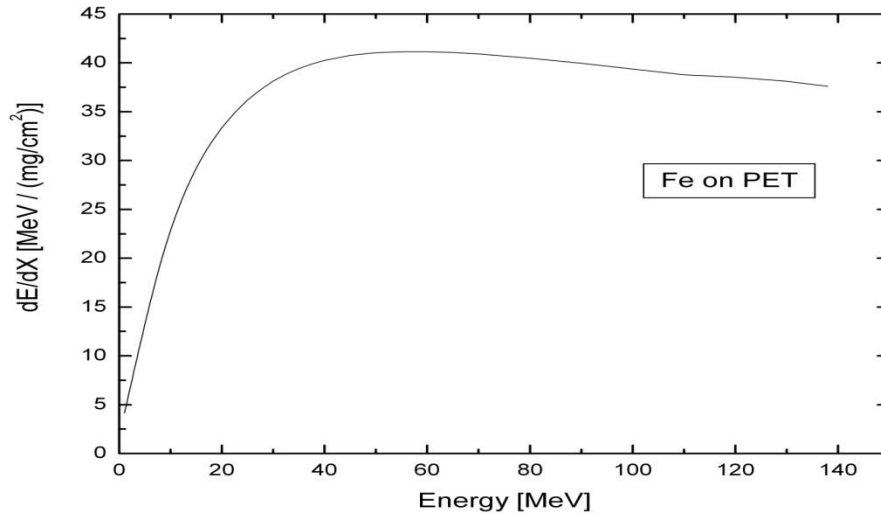
Original surface



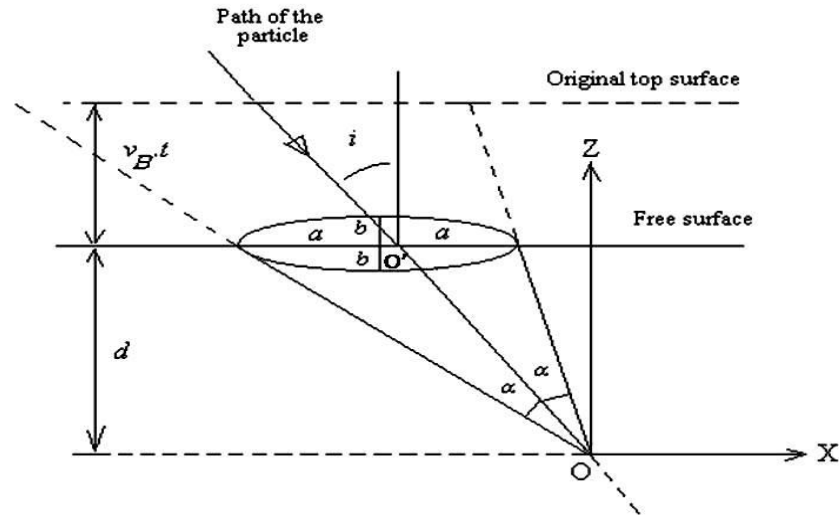
Etched surface



# Simulation of etch pit



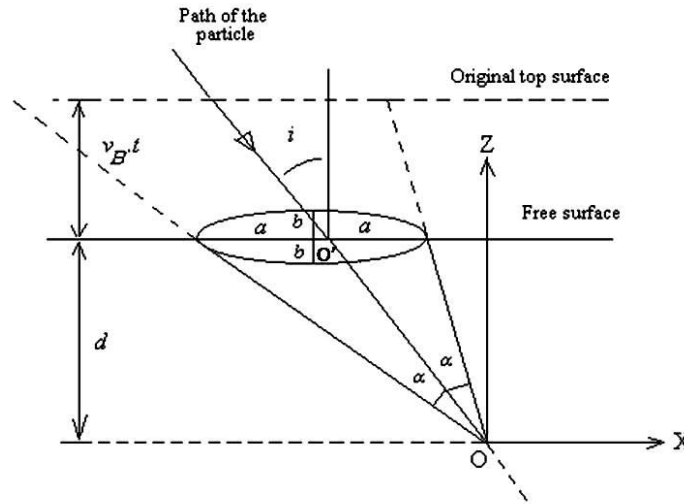
# Schematic diagram of etch pit inside the detector



Measurable quantities	Precision of measurement
Major axis diameter[2a]	0.4 $\mu\text{m}$
Minor axis diameter [2b]	0.4 $\mu\text{m}$
Height of the cone [d]	1.0 $\mu\text{m}$

# Formulae for calculating $V_T/V_B$

From depth measurement



From diameter measurement

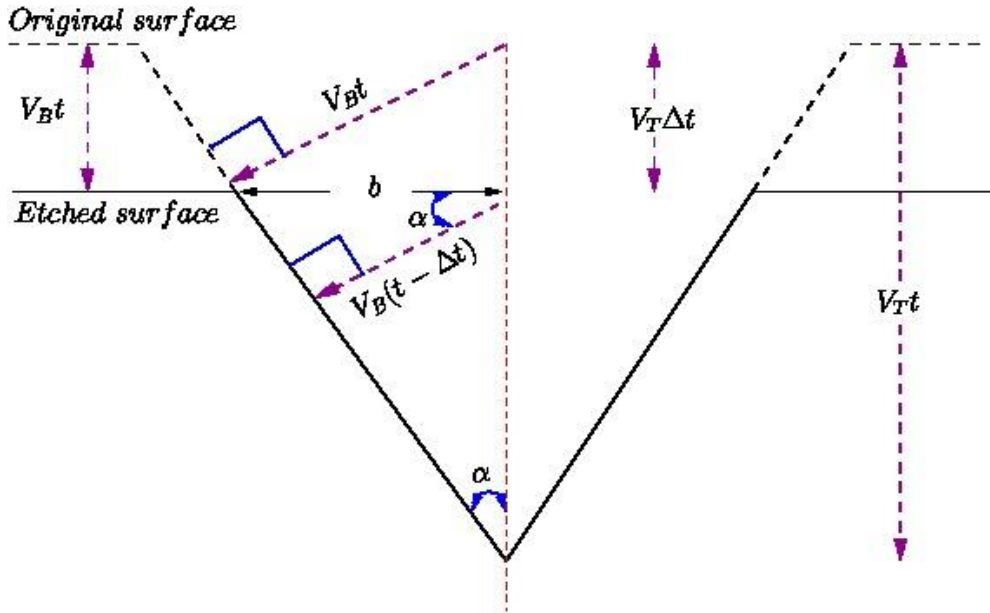
$$p = \frac{V_t}{V_b} = \frac{OO_1/t}{V_b} = \frac{\mu d + V_b \times t}{V_b \times t \times \cos i}$$

$$p = \frac{V_t}{V_b} = \sqrt{1 + \frac{4D^2}{(1-E^2)^2}}$$

Where,

$$E = \frac{b}{V_b \times t} \quad D = \frac{a}{V_b \times t}$$

# Condition for conical etch pit



$$V_B t = V_T \Delta t$$

$$\sin \alpha = \frac{V_B}{V_T} \quad \cos \alpha = \sqrt{1 - \left(\frac{V_B}{V_T}\right)^2}$$

$$b = \frac{V_B(t - \Delta t)}{\cos \alpha}$$

$$E = \frac{b}{V_B t} = \frac{V_B \left( t - \frac{V_B t}{V_T} \right)}{V_B t \cos \alpha} = \frac{\left( 1 - \frac{V_B}{V_T} \right)}{\sqrt{\left( 1 + \frac{V_B}{V_T} \right) \left( 1 + \frac{V_B}{V_T} \right)}} = \sqrt{\frac{\left( 1 - \frac{V_B}{V_T} \right)}{\left( 1 + \frac{V_B}{V_T} \right)}} < 1$$

# Ions on PET

Ion	Incident energy (MeV)	Energy at the surface after etching (MeV)	dE/dx after etching [MeV/(mg/cm <sup>2</sup> )]	$E=2b/2V_B t$	$V_T/V_B$ from depth measurement (eqn.1)	$V_T/V_B$ from diameter measurement (eqn.2)
<sup>238</sup> U	1724.5	2590.0	146.3	1.88±0.04	15.29±0.71	1.79±0.79
	2641.8	1680.0	136.6	1.31±0.03	14.32±0.67	3.89±0.29
<sup>129</sup> Xe	363.8	350.0	88.2	1.35±0.03	14.96±0.54	4.97±3.35
<sup>78</sup> Kr	220.0	194.5	53.6	1.25±0.05	12.21±0.42	6.7±7.2
<sup>56</sup> Fe	113.0	94.0	39.7	1.22±0.07	8.61±0.29	113±145
	129.8	111.2	38.7	1.24±0.05	8.53±0.27	28.7±67.4
	134.4	116.0	38.6	1.36±0.04	8.12±0.29	25.5±46.1
<sup>49</sup> Ti	138.2	130.0	30.2	1.14±0.03	6.26±0.24	12.5±24.7
<sup>32</sup> S	67.4	62.0	21.1	0.79±0.02	4.54±0.14	3.78±0.49
	70.4	63.8	20.9	0.73±0.05	4.23±0.19	3.63±0.50
	110.2	105.4	17.4	0.72±0.02	3.66±0.16	3.21±0.26
	115.6	110.0	17.1	0.61±0.07	3.29±0.18	3.08±0.21
<sup>12</sup> C	8.0	5.0	7.7	0.51±0.04	2.09±0.10	1.84±0.15
	11.0	5.7	7.6	0.34±0.04	1.78±0.19	1.40±0.08

# Experiment at IUAC

---

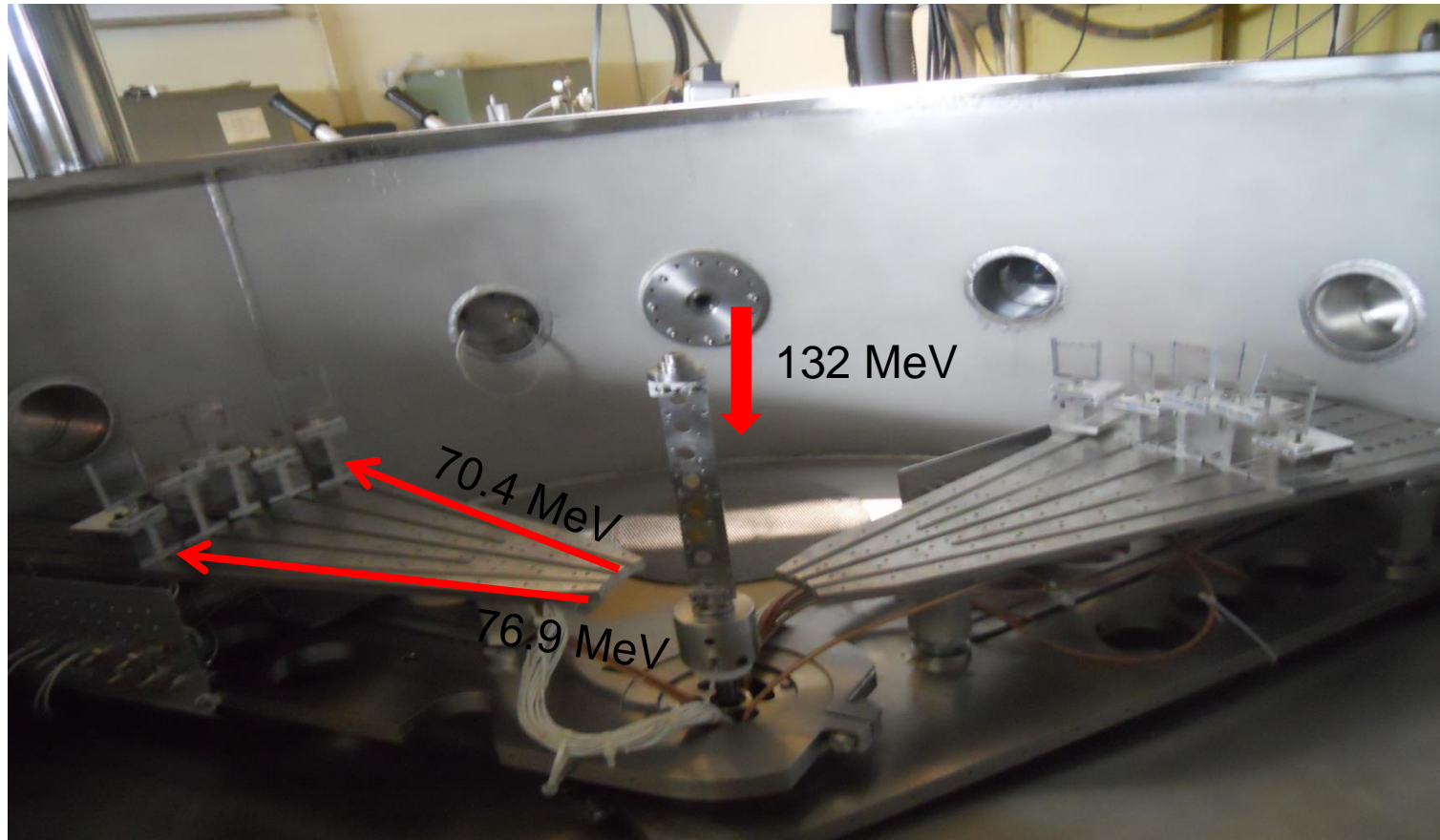


General Purpose Scattering Chamber (GPSC) at IUAC



PET films (5 cm × 5 cm) inside aluminium holders

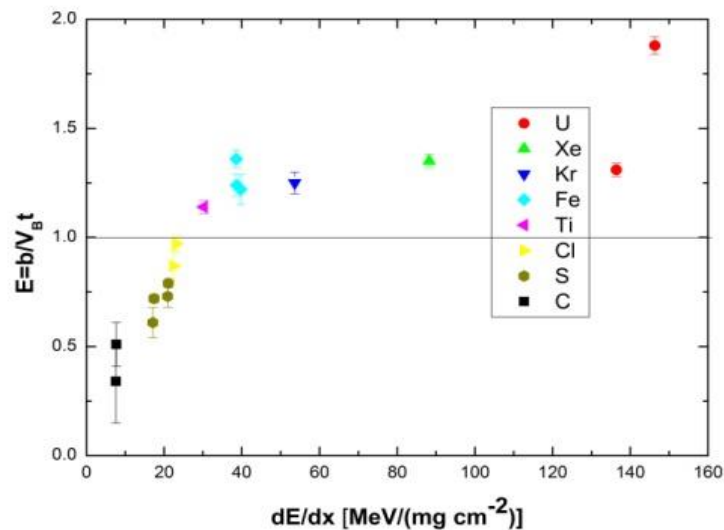
# Beam details



Ion	Energy (MeV)	Charge state	Beam current (pA)
$^{35}\text{Cl}$	132	$10^+$	1.5

# Updated table of PET

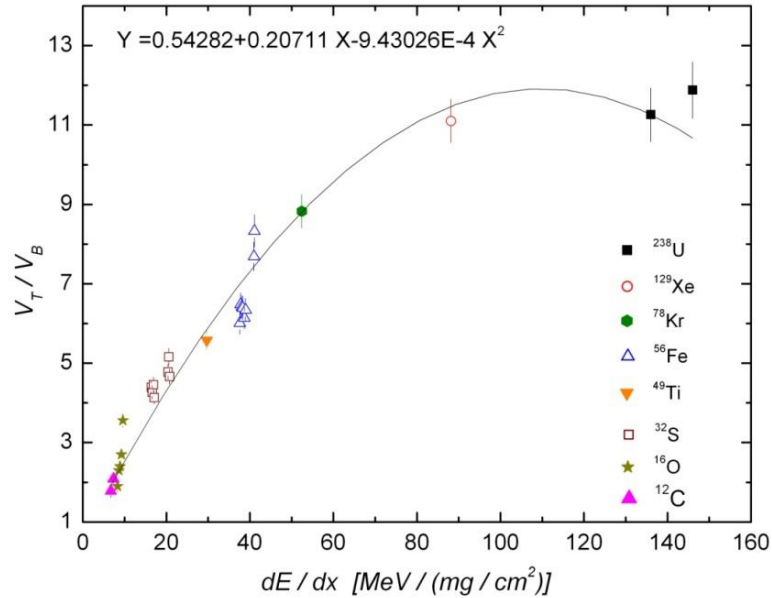
Ion	Incident energy (MeV)	Energy at the surface after etching (MeV)	dE/dx after etching [MeV/(mg/cm <sup>2</sup> )]	$E=2b/2V_B t$	$V_T/V_B$ from depth measurement	$V_T/V_B$ from diameter measurement
<sup>49</sup> Ti	138.2	130.0	30.2	1.14±0.03	6.26±0.24	12.5±24.7
<sup>35</sup> Cl	70.4	61.00	23.1	0.97±0.04	5.08±0.13	56.9±58.5
	76.9	67.50	22.4	0.87±0.07	4.58±0.19	7.97±1.68
<sup>32</sup> S	67.4	62.0	21.1	0.79±.02	4.54±0.14	3.78±0.49



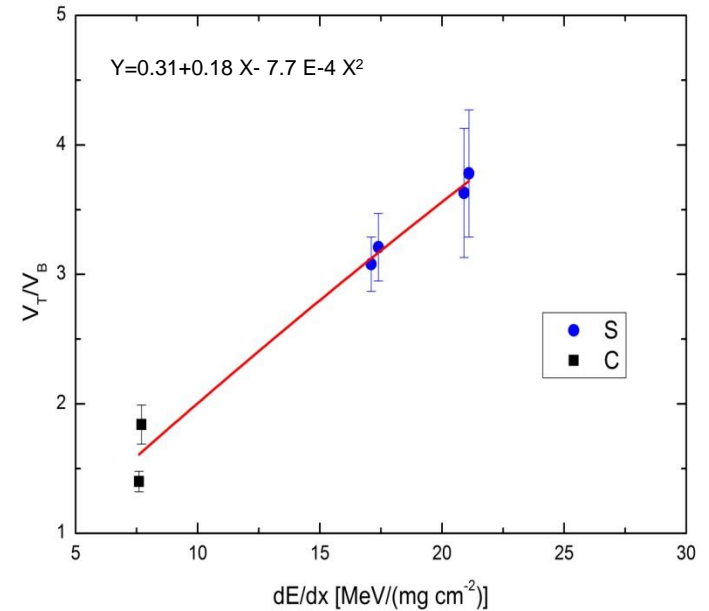
E vs. dE/dx plot for PET



# Calibration curve of PET

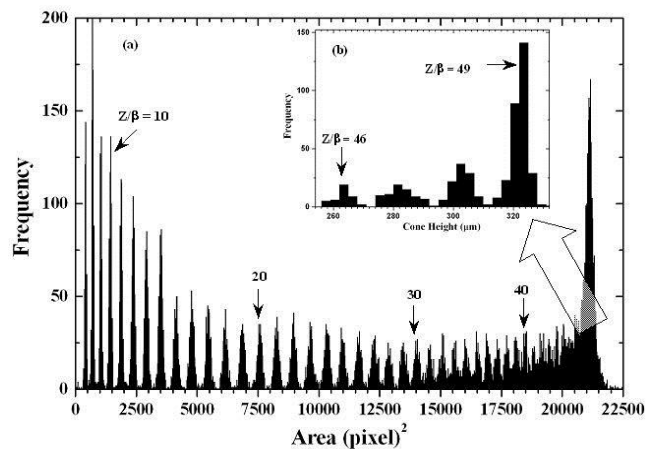


Using depth measurement method

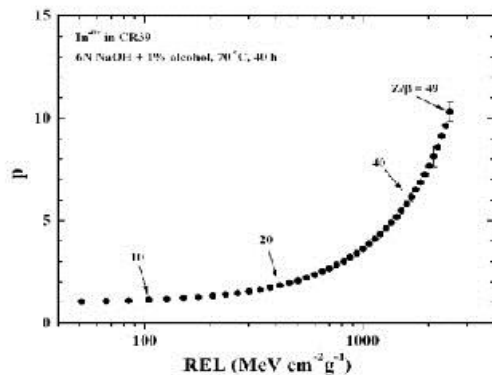


Using diameter measurement method

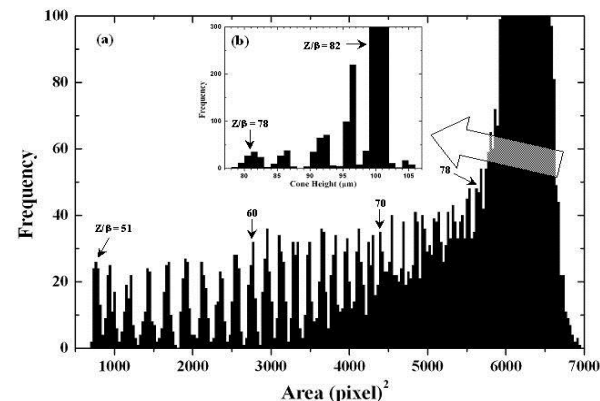
# Results from CR-39 and Makrofol detectors



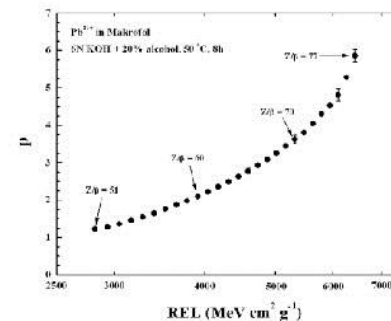
Base area distribution of etched cones in CR39 from 158 A GeV In<sup>49+</sup> ions and their fragments



p versus REL for CR39



Base area distribution of etched cones in Makrofol from 158 A GeV Pb<sup>82+</sup> ions and their fragment



p versus REL for Makrofol

# Conclusion

---

- ❑ Although by diameter measurement, one can easily get the value of 'p' at the surface we found that this formula can't be used blindly.
- ❑ For  $dE/dx > 23$  [MeV/(mg/cm<sup>2</sup>)] we observe that  $b > V_B \times t$  (so  $E > 1$ ); So in this region conical approximation of etch pits doesn't hold good. Moreover near  $E \sim 1$  this formula started giving absurd results and value of 'p' diverges.
- ❑ Above  $p \sim 4$  from diameter measurement method or above  $p \sim 5$  from depth measurement method, depth measurement method provides more reliable results.

# Acknowledgement

**Group members:** Sandhya Dey, Sanjay K. Ghosh, Atanu Maulik, Sibaji Raha, Debapriyo Syam

**Funding agency :** IRHPA (Intensification of Research in High Priority Areas) Project of the (SERC), DST, Government of India, New Delhi.

Thank  
you!