

# **PHENIX results on centrality and beam energy dependent Levy HBT analysis**

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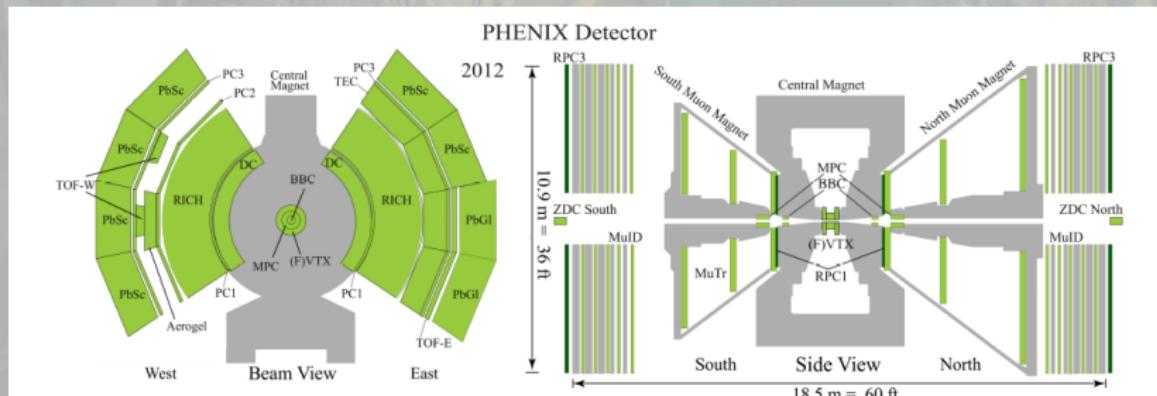
BGL 2017  
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# Outline

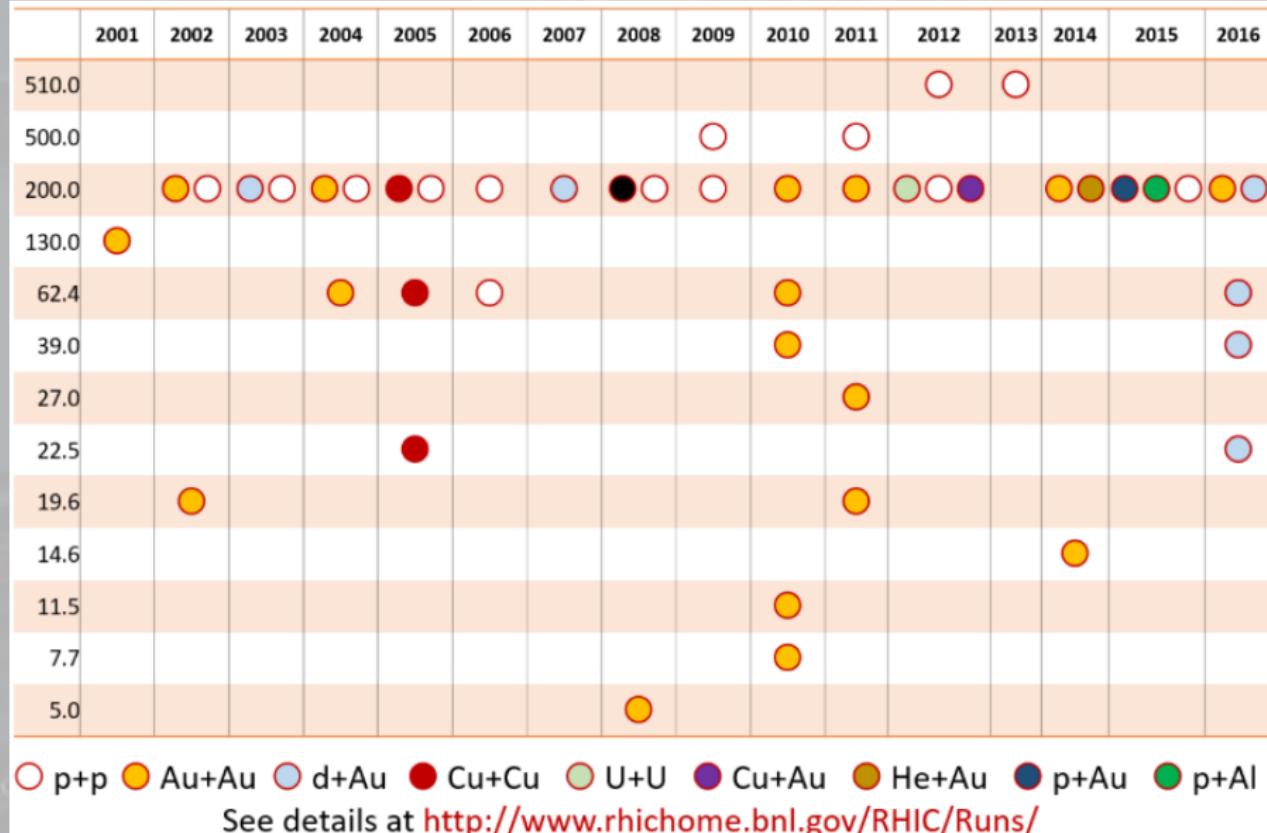
- The PHENIX experiment
- Bose-Einstein correlations
- Lévy-type distributions and the critical point
- Centrality dependent results at  $\sqrt{s_{NN}} = 200 \text{ GeV}, 62 \text{ GeV}$  and  $39 \text{ GeV}$
- Summary

# PHENIX experiment

- Observing collision of p+p, p+Al, p+Au, d+Au, h+Au, Cu+Cu, Cu+Au, Au+Au, U+U
- Charged pion ID from  $\sim 0.2$  to 2 GeV
- Typical Au+Au:  $\sqrt{s_{NN}} = 130$  GeV, 200 GeV
- Beam energy scan program: 62.4, 39.0, 27.0, 19.6, 14.5, 7.7 GeV



# Beam Energy Scan program



# Bose-Einstein correlations

- Correlation function from one- and two-particle invariant momentum distributions:

$$C_2(p_1, p_2) = \frac{N_2(p_1, p_2)}{N_1(p_1)N_2(p_2)}$$

- $N_1(p)$  norm.,  $N_2(p_1, p_2) = \int S(x_1, p_1)S(x_2, p_2)|\Psi_2(x_1, x_2)|^2 d^4x_1 d^4x_2$
- $S(x, p)$  usually assumed Gaussian  $\rightarrow$  we assumed it Lévy
- $\Psi_2$  – interaction free case –  $|\Psi_2|^2 = 1 + \cos(qx)$
- Introducing  $q = p_1 - p_2$  and  $K = (p_1 + p_2)/2$
- If  $k_1 \approx k_2 \rightarrow$  inverse Fourier-trf of the  $S$  source function

$$C_2(q, K) = 1 + \frac{|\tilde{S}(q, K)|^2}{|\tilde{S}(q = 0, K)|^2}$$

# Effects on correlation functions

Several effect could modify the correlation functions

- Like-charged pions → Coulomb corr. needed:  $C_{B-E} = K(q) \cdot C_m(q)$
- Strong final state interaction
- Effect of the resonance pions → core-halo model:
  - Split the source into two part:  $S = S_{\text{core}} + S_{\text{halo}}$
  - Long-lived resonances contribute to the halo
  - In-medium  $\eta'$  mass modification → specific,  $m_T$  dependent suppression
- Partial coherence (see the next presentation)
- Squeezed states
- Aharonov-Bohm-like effect
  - The hadron gas around the pair could reduce the strength of the correlation
  - Could be treated as an Aharonov-Bohm-like effect

# Lévy-type distribution and the critical point

- Generalized Gaussian – Lévy-distribution

– Anomalous diffusion  
– Generalized central limit th.

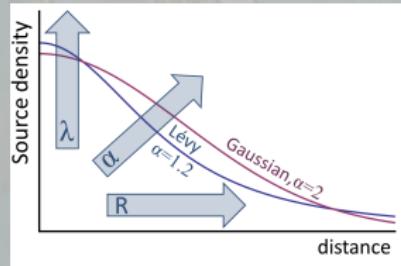
$$\left. \begin{array}{l} \\ \end{array} \right\} \mathcal{L}(\alpha, R, \mathbf{r}) = \frac{1}{(2\pi)^3} \int d^3 q e^{i\mathbf{qr}} e^{-\frac{1}{2}|\mathbf{q}R|^\alpha}$$

- $\alpha = 2$  Gaussian,  $\alpha = 1$  Cauchy,  $0 < \alpha \leq 2$  Lévy
- The  $C_2$  from a symmetric Lévy-source:

$$C_2(Q) = 1 + \lambda \cdot e^{-(RQ)^\alpha}$$

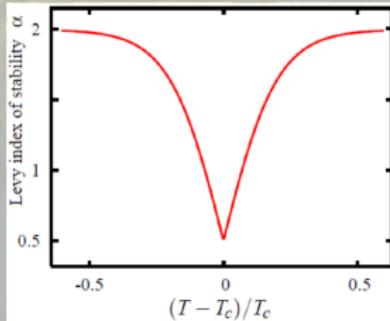
- Spatial corr.  $\sim r^{-1-\eta}$  in 3D  $\rightarrow$  defines  $\eta$  exponent
- Symmetric stable distribution (Lévy)  $\rightarrow$  spatial corr.  $\sim r^{-1-\alpha}$
- $\alpha$  identical to  $\eta$ !
- For details see e.g.:

- [1] Csörgő, Hegyi, Zajc, Eur.Phys.J. C36 (2004) 67, nucl-th/0310042
- [2] Csörgő, Hegyi, Novák, Zajc, AIP Conf.Proc. 828 (2006) 525, nucl-th/0512060
- [3] Csörgő, PoS HIGH-pTLHC08:027 (2008), nucl-th/0903.0669
- [4] Csanád, Csörgő, Nagy, Braz.J.Phys. 37 (2007) 1002-1013



# Searching for the critical point

- QCD universality class  $\leftrightarrow$  3D Ising [5],[6]
  - At the critical point:
    - random field 3D Ising model [7]:  $\eta = 0.5 \pm 0.05$
    - 3D Ising [8]:  $\eta = 0.03631(3)$
  - Change in  $\alpha \rightarrow$  vicinity of the CEP
  - Motivation for precise HBT measurements ...
    - ... with different multiplicity  $\rightarrow$  centrality dependence
    - ... with different energy: now 200 GeV, 62 GeV, 39 GeV
- 
- [5] Halasz et al., Phys.Rev.D58 (1998) 096007, hep-ph/9804290
  - [6] Stephanov et al., Phys.Rev.Lett.81 (1998) 4816, hep-ph/9806219
  - [7] Rieger, Phys.Rev.B52 (1995) 6659, cond-mat/9503041
  - [8] El-Showk et al., J.Stat.Phys.157 (4-5): 869, hep-th/1403.4545



# Analysis details

- Data used for the centrality dependent analysis:

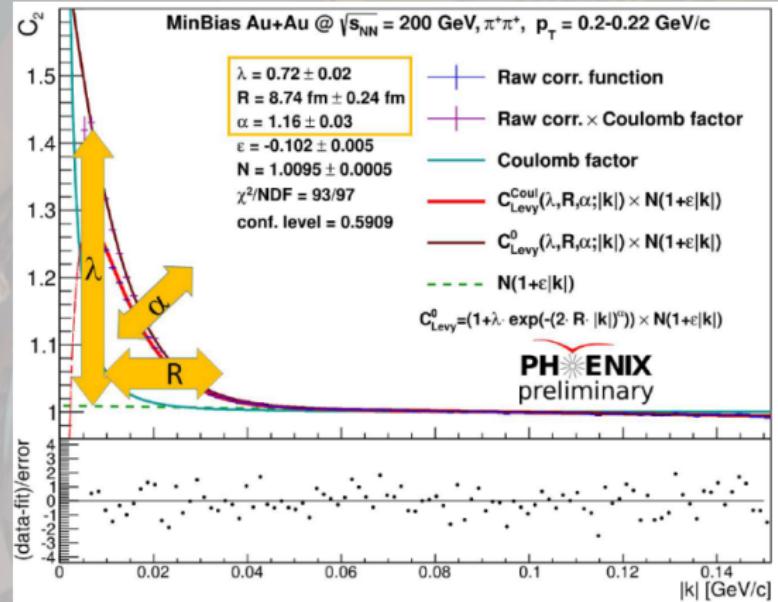
- Run-10, Au+Au at  $\sqrt{s_{\text{NN}}} = 200$  GeV
- 18  $m_T$  bin, 6 cent.bin by 10% steps

Data used for the  $\sqrt{s_{\text{NN}}}$  dependent analysis:

- Run-10, Au+Au at
  - $\sqrt{s_{\text{NN}}} = 62$  GeV with 8  $m_T$  bin, 4 cent.bin by 10% steps
  - $\sqrt{s_{\text{NN}}} = 39$  GeV with 8  $m_T$  bin, 2 cent.bin by 20% steps

- Yield the  $m_T$  and centrality dependence of the Lévy-parameters
- Estimate the systematical uncertainties (in progress):
  - Effect of single and pair cuts
  - Choice of PID arm (East or West)
  - Systematics from fit: choice of the  $Q_{\min}$  and  $Q_{\max}$
  - In Coulomb correction  $q_{\text{inv}} \leftrightarrow Q$  change

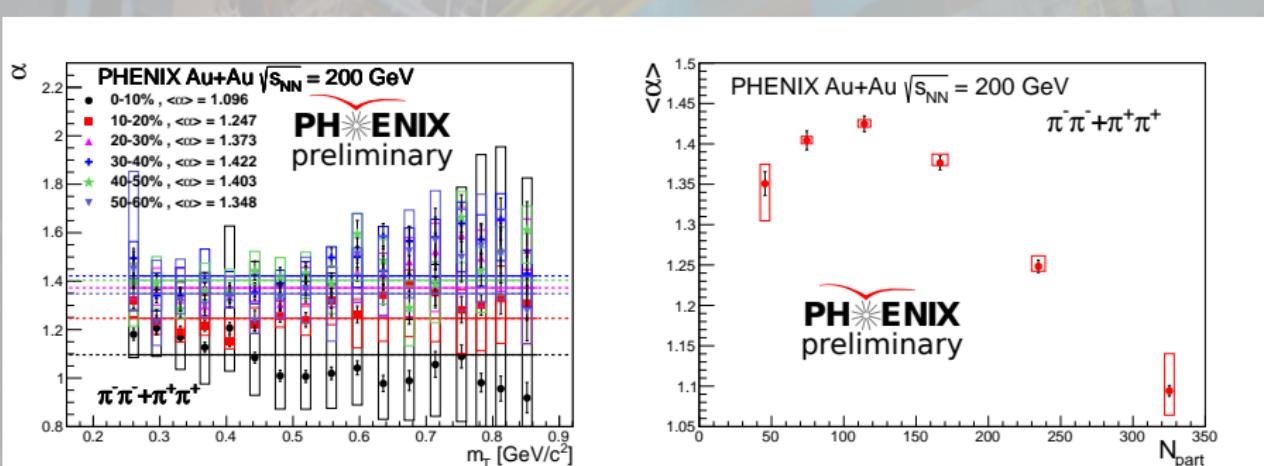
# Example fit



- Fitted with Coulomb-corrected function
- All fits converged and the conf.levels are acceptable
- Lévy parameters are measured versus  $m_T$

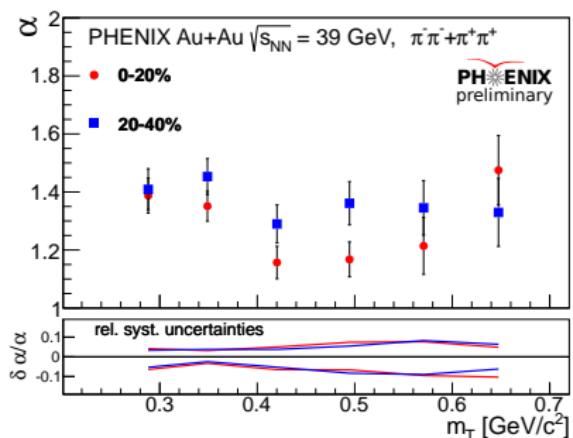
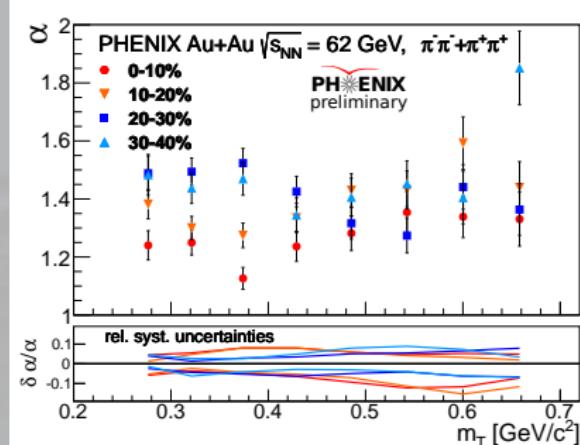
# Lévy exponent $\alpha$ at 200 GeV

- Slightly non-monotonic behavior as a function of  $m_T$
- Average has non-monotonic behavior at 200 GeV
- $\alpha = \langle \alpha \rangle$  constant fits were performed with centrality bin dependent value



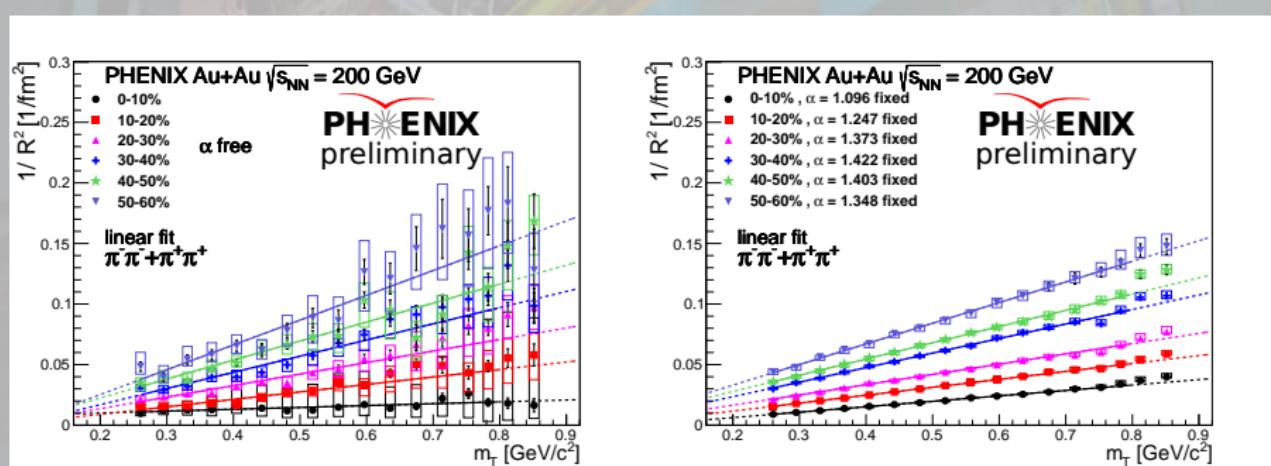
# Lévy exponent $\alpha$ at 62 and 39 GeV

- Lévy exponent  $\alpha$  does not seem to depend on  $\sqrt{s_{NN}}$
- Fewer centrality bins have to be used due to the statistics
- $\alpha = \langle \alpha \rangle$  constant fits were not done



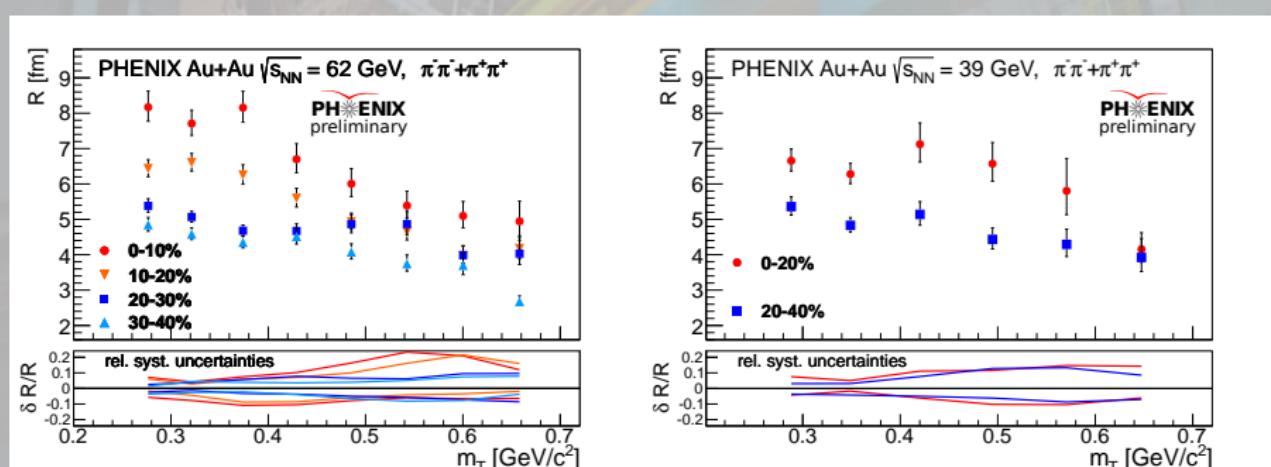
# Lévy scale $R$ at 200 GeV

- Not equivalent with the Gaussian width but show similar trends
- Linear scaling behavior is seen in  $1/R^2(m_T)$
- $\alpha$  fix fits reduce the systematic uncertainties



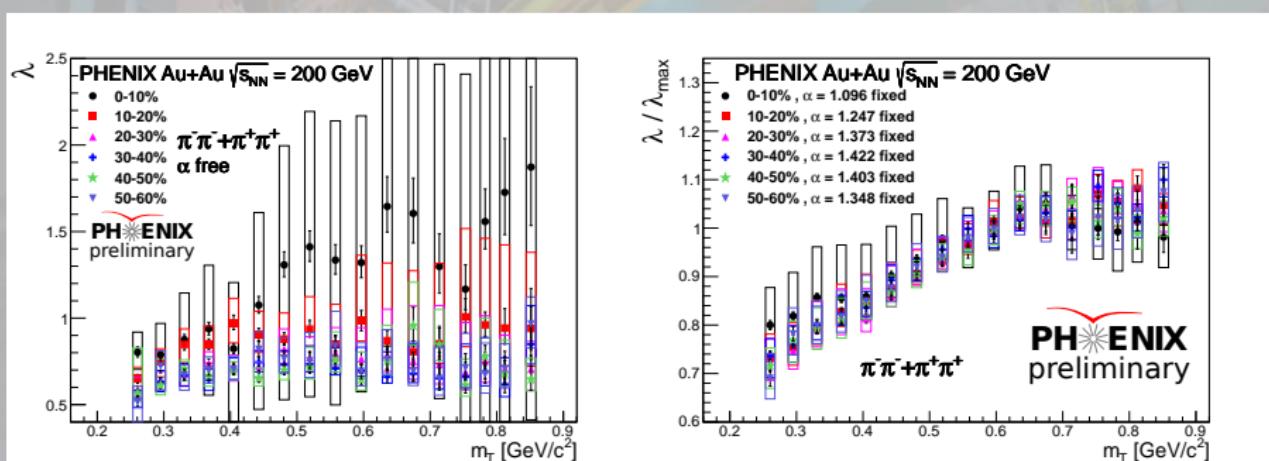
# Lévy scale $R$ at 62 and 39 GeV

- Similar decreasing trends with  $m_T$  as in the Gaussian case
- Similar trends as at 200 GeV
- Fewer centrality bins have to be used due to statistics



# Lévy strength $\lambda$ at 200 GeV

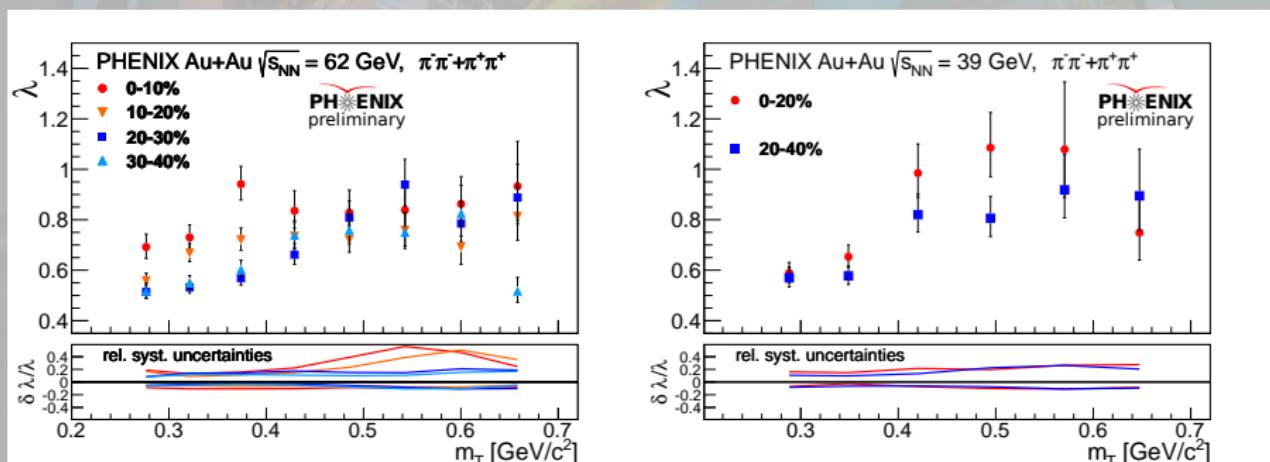
- Decreasing tendency at lower  $m_T$  not depend on centrality (as in [9])
- Can be observed clearly in  $\lambda/\lambda_{\max}$  with  $\alpha$  fix (r.h.s. figure)
- Partial coherence predicts strong centrality dependence
- No centrality dependence of the “hole”



[9] Abelev et al. [STAR collaboration] PRC80, 024905

# Lévy strength $\lambda$ at 62 and 39 GeV

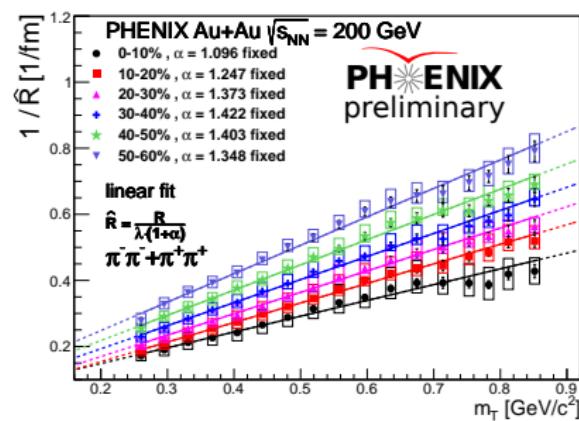
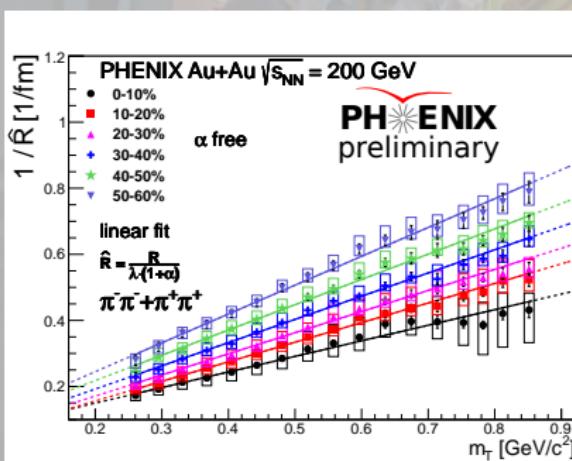
- Similar trends as at 200 GeV
- The characteristics of the “hole” do not depend strongly on  $\sqrt{s_{NN}}$
- At  $\sqrt{s_{NN}} \approx 19.4$  GeV the effect seems to disappear in S+Pb (see [10])



[10] Beker et al. [NA44 collaboration], PRL74, 3340

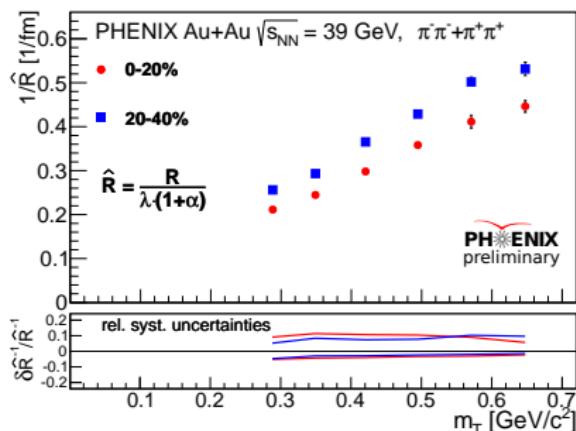
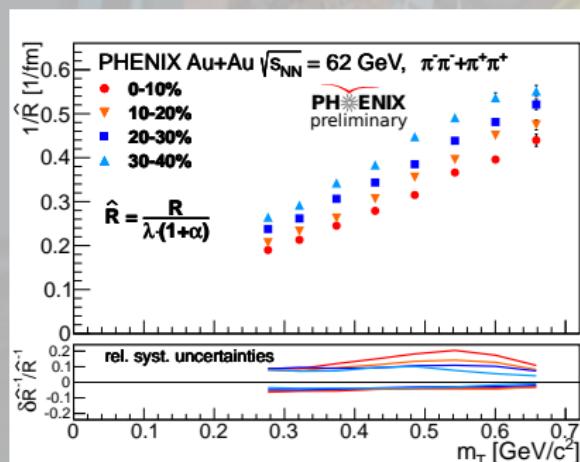
# New scaling parameter $\hat{R}$ at 200 GeV

- $\frac{1}{\hat{R}} = \frac{\lambda(1+\alpha)}{R}$  scales with  $m_T$
- Not sensitive to the  $\alpha$  fixation
- May correspond to the area under the correlation function
- Experimentally observed, no theoretical explanation as far as we know



# New scaling parameter $\hat{R}$ at 62 and 39 GeV

- Surprisingly good behavior at lower energy
- Linear behavior does still hold

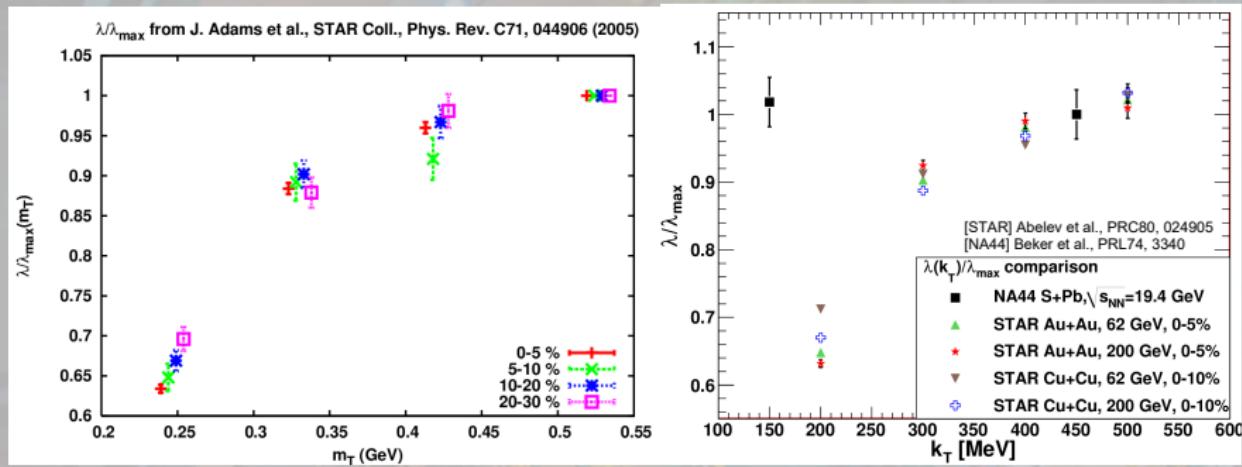


# Summary

- Experimentally, a significant deviation from the Gaussian ( $\alpha = 2$ ) case
- Symmetric Lévy shape is a statistically acceptable description
- Lévy parameters connected to rescattering, core/halo model and size
- Lévy exponent  $\alpha$ : non-monotonic in  $N_{\text{part}}$ , almost independent of  $\sqrt{s_{NN}}$
- Lévy scale  $R$ : geometric/hydro scaling, similar to Gaussian
- Lévy strength: low- $m_T$  “hole” for  $\sqrt{s_{NN}} \geq 39$  GeV, weak centrality dep.
- New par  $\hat{R}$ : linear scaling for  $\sqrt{s_{NN}} \geq 39$  GeV, all investigated centrality

Thank you for your attention!

# Backup slides



STAR centrality dependent results (left) and the comparison of STAR results in different  $\sqrt{s_{NN}}$  with NA44 data (right)