

# Offshell Higgs production and interference effects at NLO

Raoul Röntsch

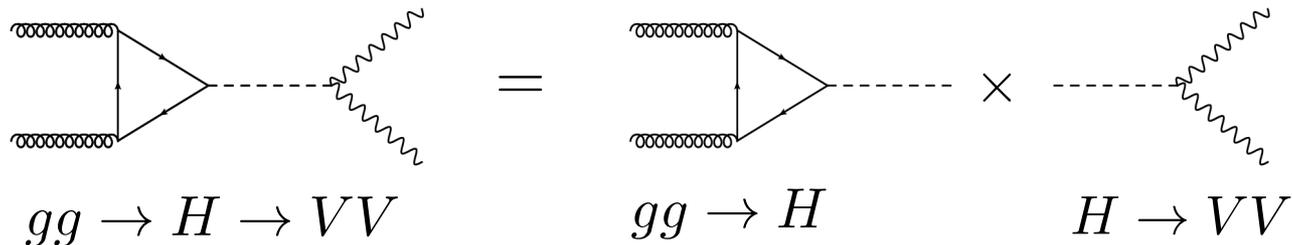
KARLSRUHE INSTITUTE OF TECHNOLOGY

Zurich Phenomenology Workshop: The second run of the LHC

11 January 2017

# Higgs on- and offshell

- Higgs discovery was the highlight of Run I.
- Higgs physics continues to be focus during Run II – precise measurements of properties
- $H \rightarrow VV$  important decay channel
- Higgs properties mostly probed using **onshell Higgs**
  - Factorize production and decay



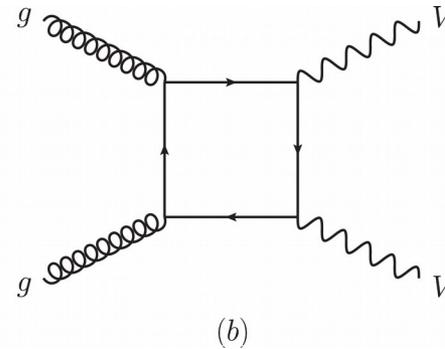
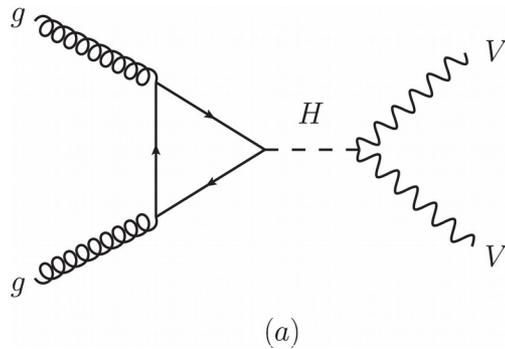
- Treat signal and background separately

**BUT:** 10% of events in  $H \rightarrow VV$  **above  $2m_V$  threshold** (Kauer, Passarino '12)

**➡** NWA **not sufficient** to describe behavior of  $H \rightarrow VV$

# Offshell interference

Consistent treatment in **high mass region** requires both **signal** and **background** amplitudes



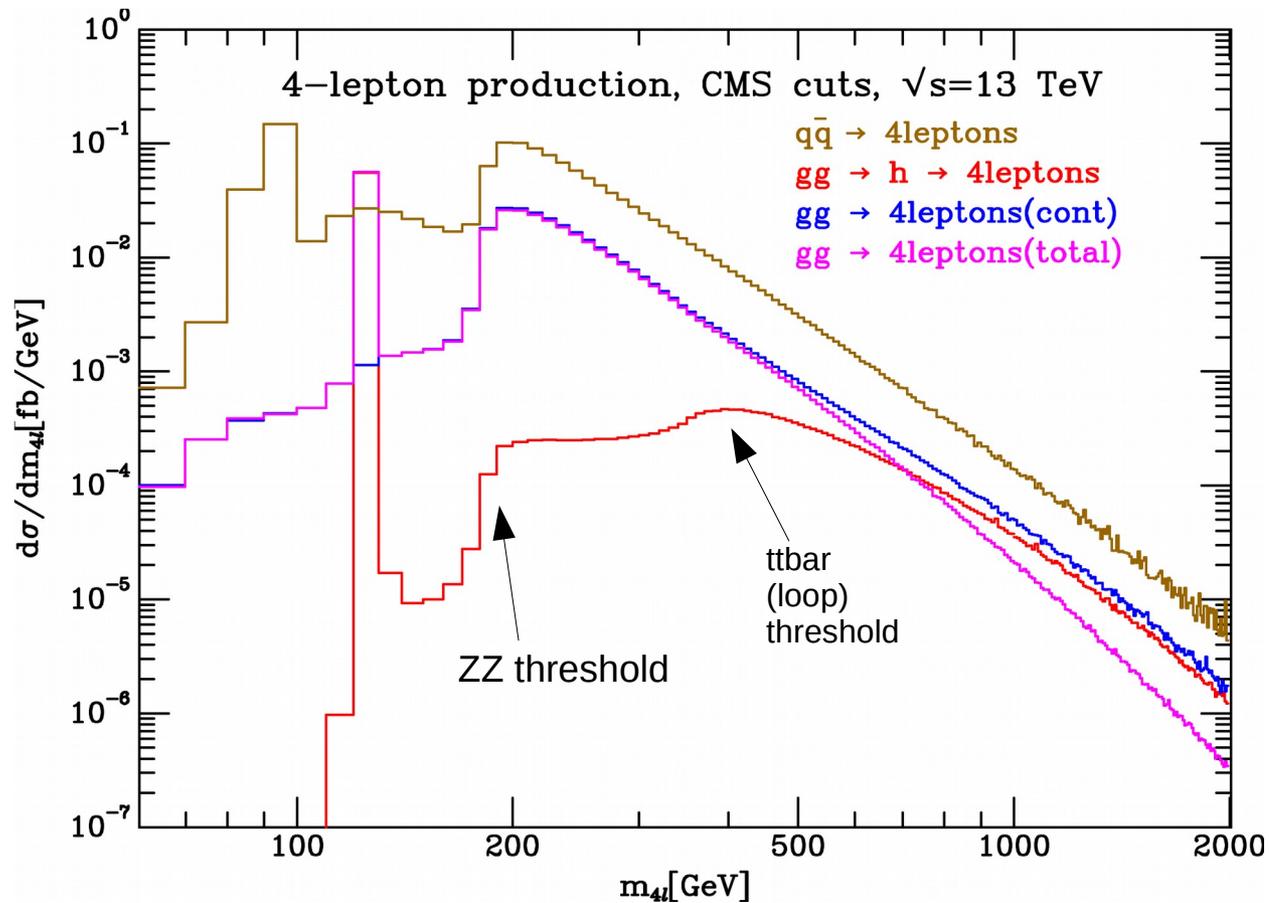
“signal”  $A_H$

“background”  $A_b$

$$|A_{ZZ}|^2 = |A_H|^2 + |A_b|^2 + 2\text{Re}[A_H A_b^*]$$

$$\rightarrow \sigma_{\text{full}} = \sigma_{\text{sigl}} + \sigma_{\text{bkgd}} + \sigma_{\text{intf}}$$

# Interference effect and line shape

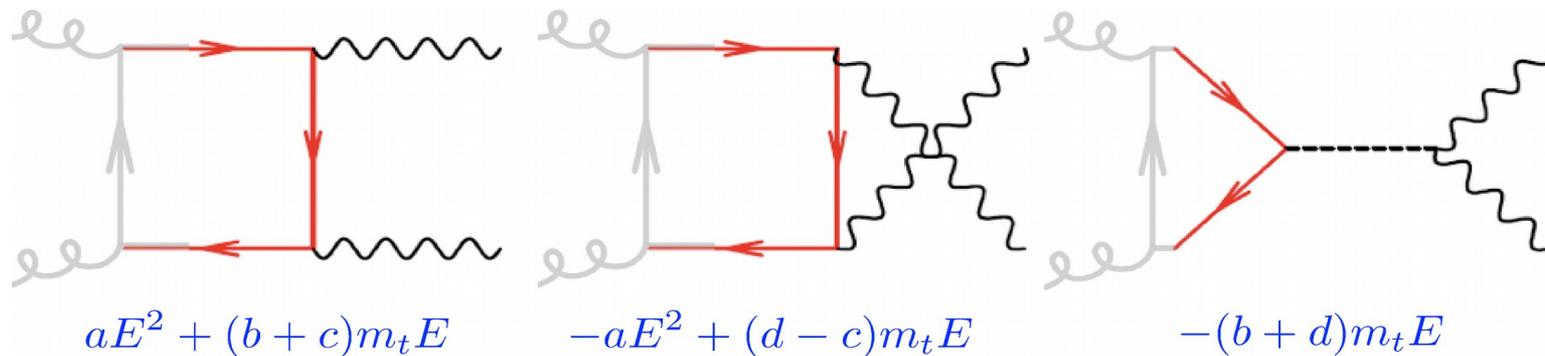


Interference is **strong** and **destructive**, especially at high invariant mass

Campbell, Ellis, Williams '13

# Understanding high energy behavior

Cut open top loop – have  $t\bar{t} \rightarrow VV$



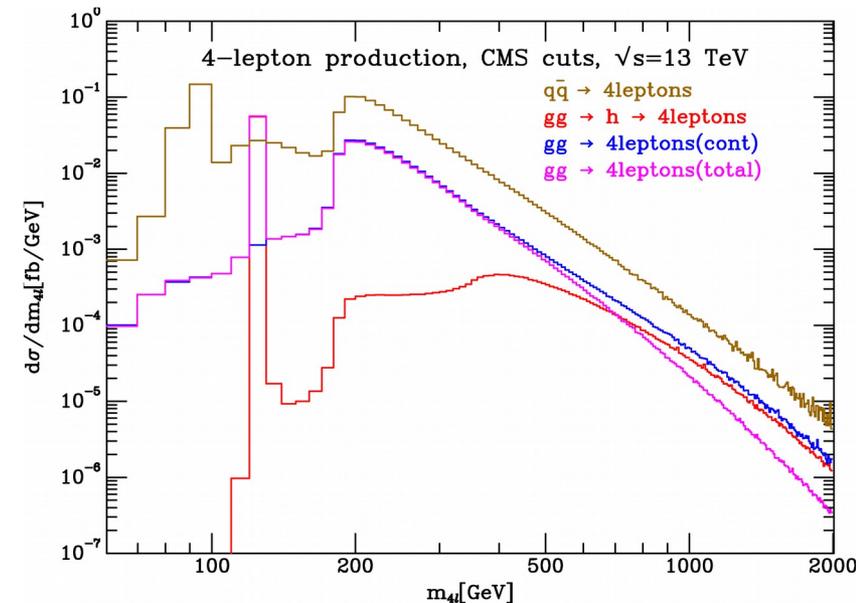
J. Campbell

- **Signal** and **background** amplitudes-squared grow like  $E^2$
- **Interference** grows like  $-E^2 \rightarrow$  cancels  $E^2$  terms of signal and background
- **Higgs unitarizing massive scattering amplitude** – connected to its role in EWSB and mass generation

# Using off-shell Higgs

We have **a new tool** for studying Higgs physics!

- High mass behavior probes **unitarization properties** of Higgs
  - Important for understanding EWSB
  - Cross sections small  $\rightarrow$  HL-LHC
- Higgs couplings **more sensitive to NP** at high energies



Campbell, Ellis, Williams '13

# Using off-shell Higgs: indirect width constraints

- Observation of Caola & Melnikov:

$$\sigma_{\text{on}} \propto g_i^2 g_f^2 / \Gamma_H \quad \sigma_{\text{off}} \propto g_i^2 g_f^2$$

$$\Rightarrow \Gamma_H \propto \frac{\sigma_{\text{off}}}{\sigma_{\text{on}}} \quad \longrightarrow \quad \text{indirect constraint on width}$$

- CMS:  $\Gamma_H < 13 \text{ MeV}$  ATLAS:  $\Gamma_H < 23 \text{ MeV}$
- Direct constraints  $\sim 1 \text{ GeV}$
- Compare with SM value:  $\Gamma_H \approx 4 \text{ MeV}$

# Indirect Higgs width constraint: *caveat emptor*

Indirect constraints not model-independent:

- **Assume same couplings on- & off-shell**
- Can construct models with  $\Gamma_H > \Gamma_H^{\text{SM}}$  but no sensitivity from off-shell measurements (Englert, Spannowsky '14)
- Possible option:
  - Introduce energy-dependent couplings in  $\kappa$ -framework / EFT (Englert, Soreq, Spannowsky '14)
  - Constrain couplings and width simultaneously
  - Highly non-trivial dependence of **signal**, **background** and **interference** on these couplings! (see e.g. Azatov, Grojean, Paul, Salvioni '16)
  - CMS: simultaneous constraints on width &  $HVV$  coupling (hep-ex/1507.06656)

# Impact of higher order corrections

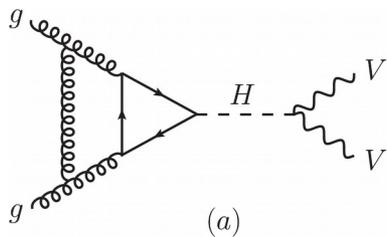
- Signal (incl. top mass effects) known at **NLO**
  - **NLO corrections large**, k-factor  $\sim 1.7$
- Experimental analyses use background and interference at **LO only**
  - NLO corrections approximated by corrections from signal  
→ **adds uncertainties to analysis**
- Recent work has extended background and interference to **NLO**

Campbell, Czakon, Ellis, Kirchner, hep-ph/1605.01380

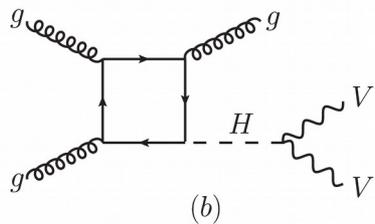
Caola, Dowling, Melnikov, R.R., Tancredi, hep-ph/1605.04610

# Higgs Interference Effects at NLO

Known

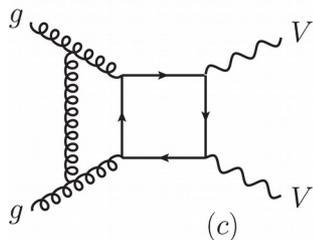


Known



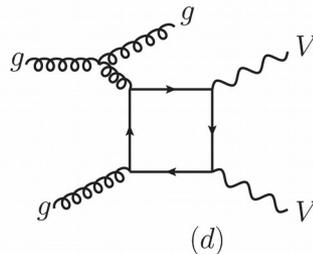
Massless: known

Massive: extremely difficult / impossible

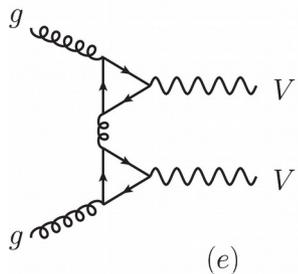


Massless: easy

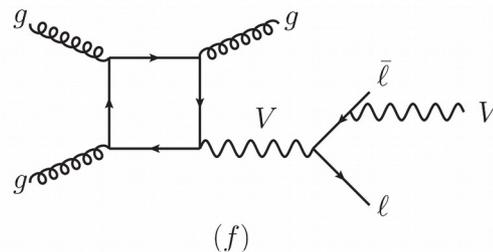
Massive: moderate



Known



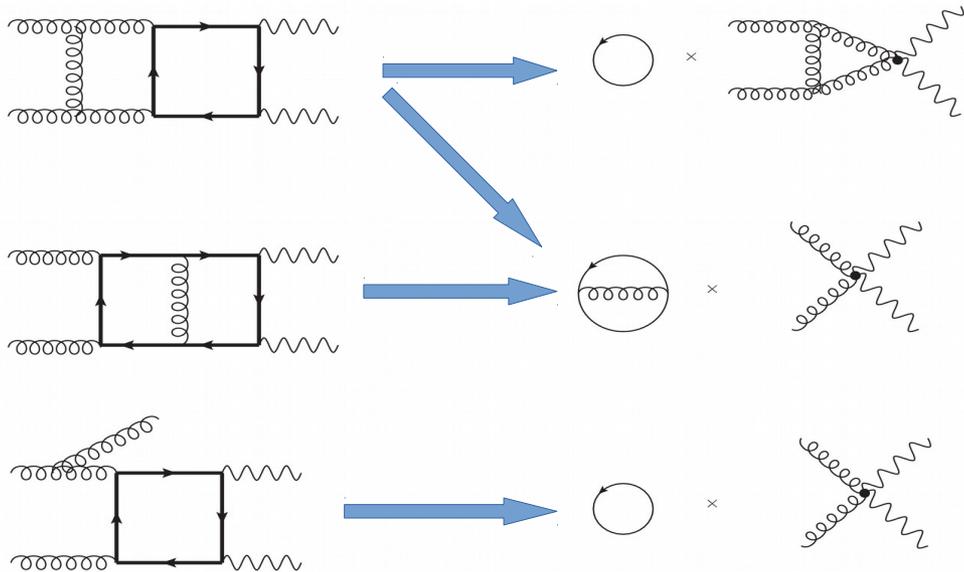
Known



Spira, Djouadi, Graudenz, Zerwas '95; Harlander, Kant '05; Aglietti, Bonciani, Degrassi, Vicini '07;  
 Ellis, Hinchliffe, Soldate, v.d. Bij '88;  
 Caola et al '15, v. Manteuffel, Tancredi '15  
 Hagiwara, Kuruma, Yamada '91; Campbell, Ellis, Zanderighi '07;  
 v.d. Bij, Glover '89;

# $gg \rightarrow (H) \rightarrow ZZ$ : Top Mass Expansion

Expand in  $s/m_t^2$



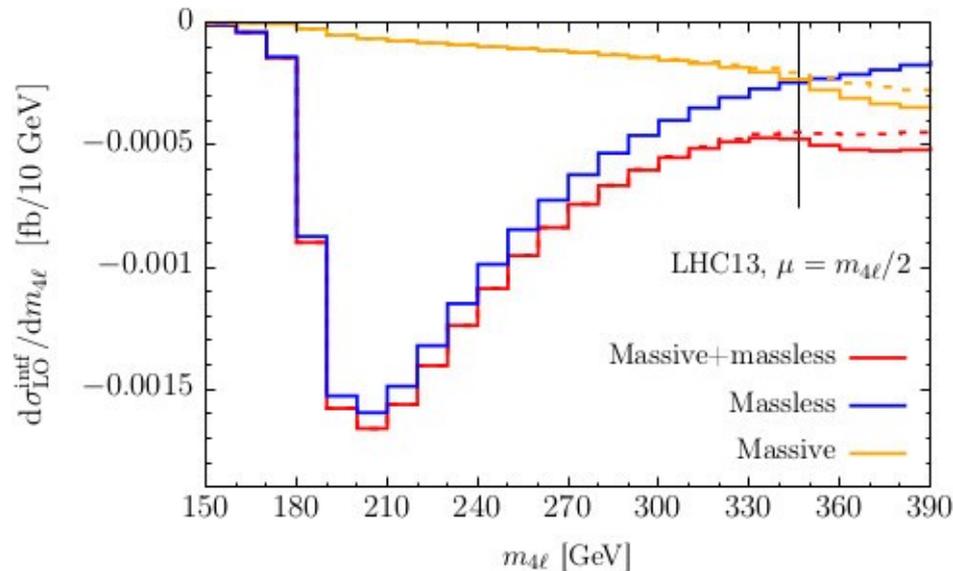
- Keep terms to  $(s/m_t^2)^4$
- Expect to be valid for partonic energies

$$s \lesssim 4m_t^2$$

Dowling, Melnikov '15

# Validity of top mass expansion

Can check validity at LO – Interference for exact  $m_t$  dependence vs mass expansion



Good approximation below  $2m_t$  threshold

Restricted to  
 $m_{4\ell} \leq 2m_t$   
 $p_{T,j} < 150 \text{ GeV}$

- Cannot probe unitarization effects :(

- Large window  $150 \text{ GeV} \lesssim m_{4\ell} \leq 2m_t$  where Higgs is off-shell and we can study **interference effects at NLO**

# Parameters

- $gg \rightarrow ZZ \rightarrow e^+e^-\mu^+\mu^-$  at 13 TeV LHC
- Dynamical scale  $\mu_F = \mu_R = \{m_{4\ell}/4, m_{4\ell}/2, m_{4\ell}\}$
- Minimal cuts:
  - $150 \text{ GeV} \leq m_{4\ell} \leq 340 \text{ GeV}$
  - $p_{T,j} < 150 \text{ GeV}$
  - $60 \text{ GeV} \leq m_{\ell\ell} \leq 120 \text{ GeV}$

# $gg \rightarrow (H) \rightarrow ZZ$ Results: Cross Sections

$$\sigma_{\text{LO}}^{\text{signal}} = 0.043_{-0.009}^{+0.012} \text{ fb}, \quad \sigma_{\text{NLO}}^{\text{signal}} = 0.074_{-0.008}^{+0.008} \text{ fb}$$

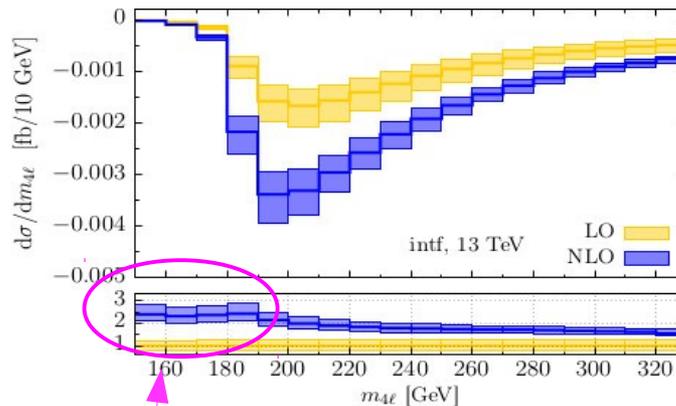
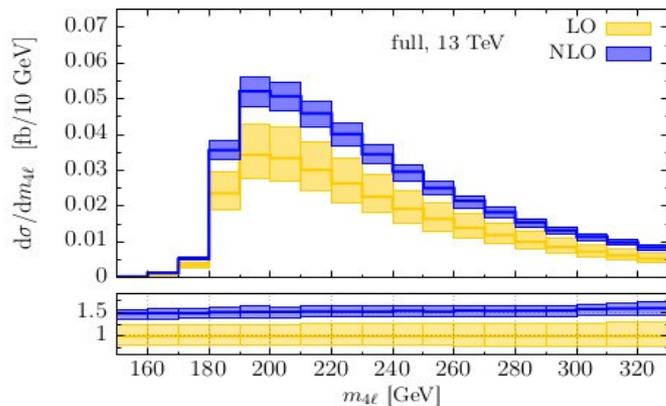
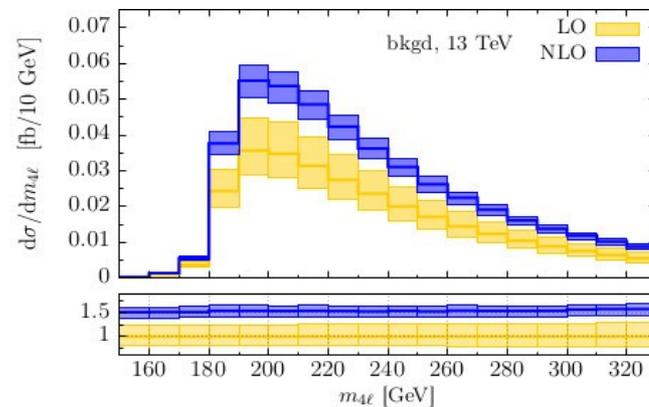
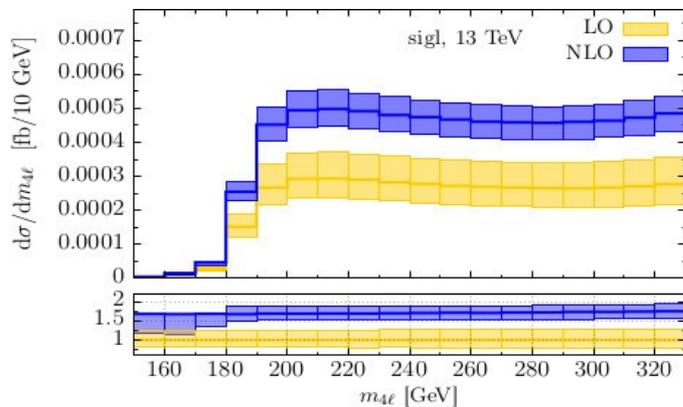
$$\sigma_{\text{LO}}^{\text{bkgd}} = 2.90_{-0.58}^{+0.77} \text{ fb}, \quad \sigma_{\text{NLO}}^{\text{bkgd}} = 4.49_{-0.38}^{+0.34} \text{ fb}$$

$$\sigma_{\text{LO}}^{\text{intf}} = -0.154_{-0.04}^{+0.031} \text{ fb}, \quad \sigma_{\text{NLO}}^{\text{intf}} = -0.287_{-0.037}^{+0.031} \text{ fb}$$

$$\sigma_{\text{LO}}^{\text{full}} = 2.79_{-0.56}^{+0.74} \text{ fb}, \quad \sigma_{\text{NLO}}^{\text{full}} = 4.27_{-0.35}^{+0.32} \text{ fb},$$

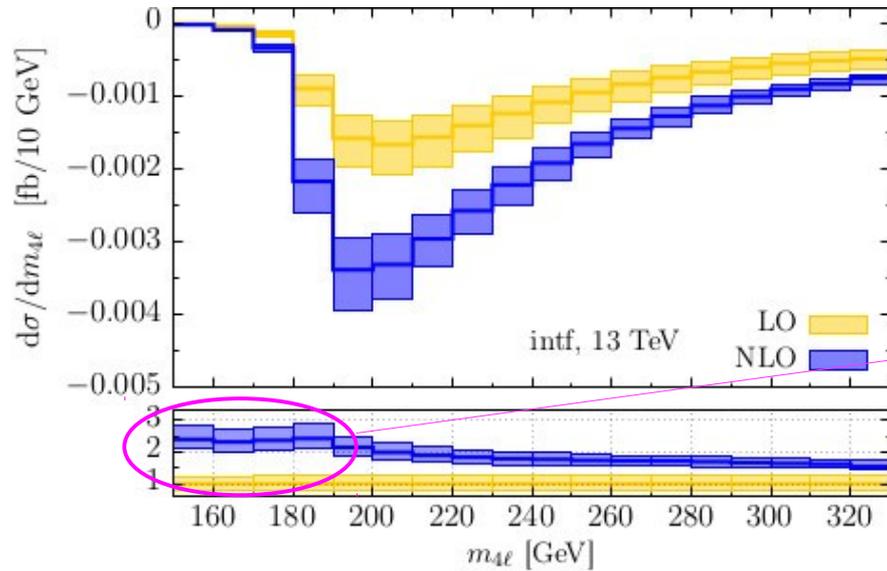
- **~ 13k events** at HL-LHC ( $3 \text{ ab}^{-1}$ )
- **Destructive interference ~ 5%**
  - ~ 4 x larger than signal, order of magnitude smaller than background
  - Can use specialized cuts needed to enhance relative to signal and background
- Scale uncertainty: **20%-30% at LO**, **10% at NLO**
- $K_{\text{sigl}} = 1.72$      $K_{\text{bkgd}} = 1.55$      $K_{\text{intf}} = 1.65 \simeq \sqrt{K_{\text{sigl}} K_{\text{bkgd}}}$

# $gg \rightarrow (H) \rightarrow ZZ$ Results: Mass distributions

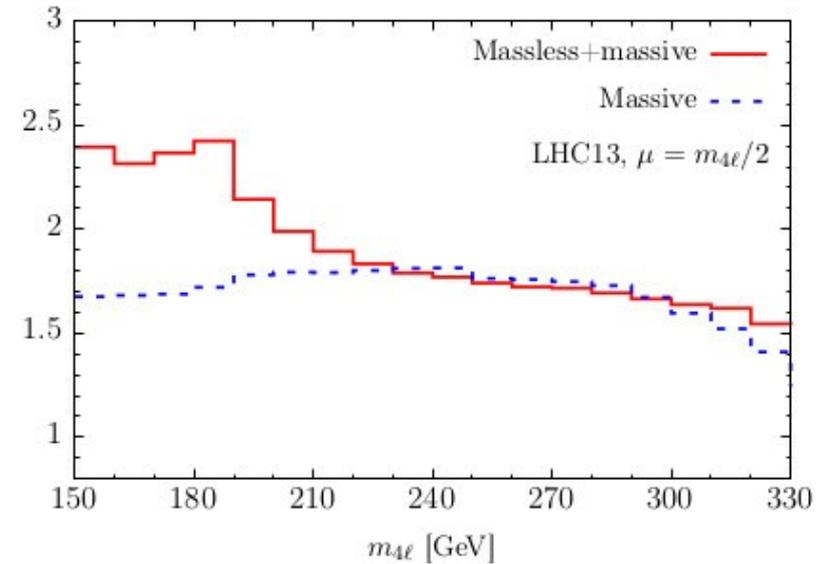


- Differential k-factors **relatively flat**...
- Except for interference near  $2m_Z$  threshold

# $gg \rightarrow (H) \rightarrow ZZ$ Results: Differential k-factor



$K_{\text{intf}}$



- **Massless loop** dominates near  $2m_Z$  threshold, **drives k-factor behavior**

# Comparison with similar work

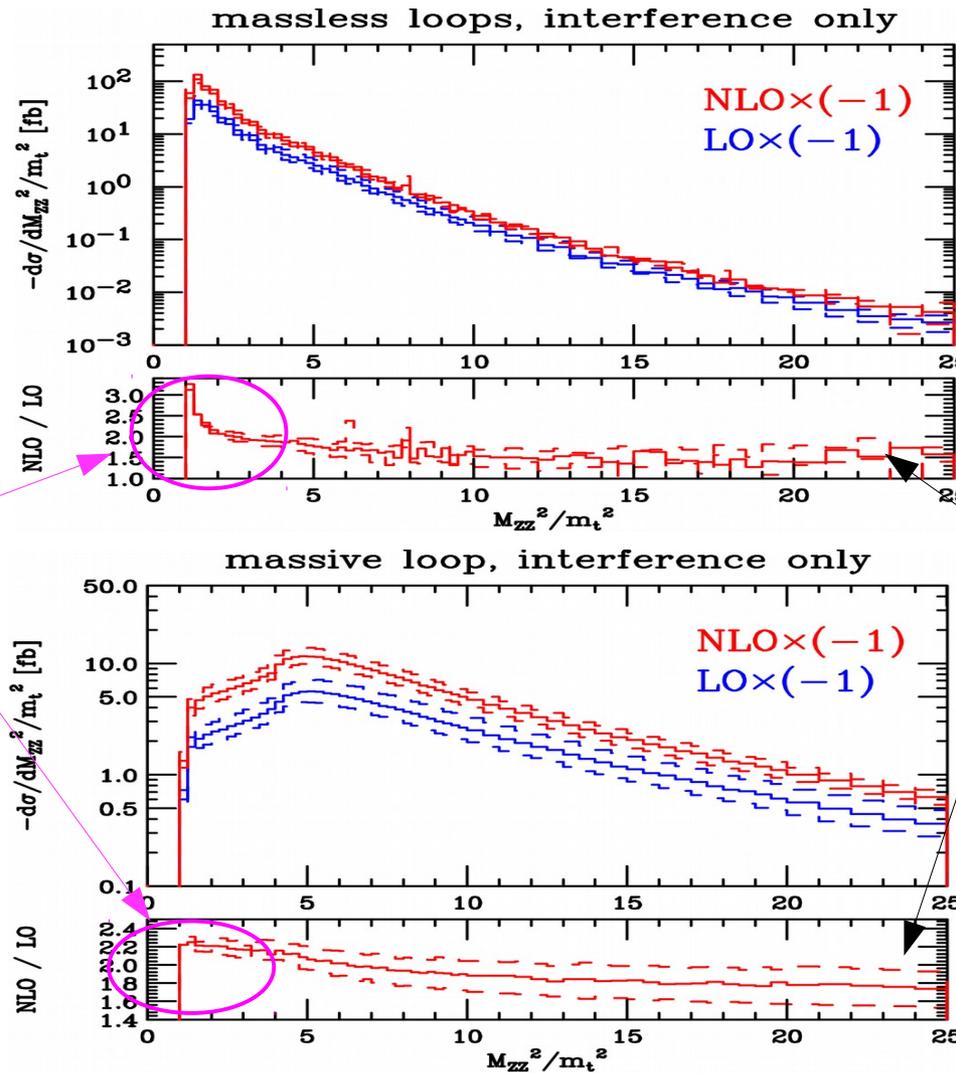
Campbell, Czakon, Ellis, Kirchner, hep-ph/1605.01380

- Only **interference** contribution considered
- On-shell Z bosons, so  $m_{ZZ} > 2m_Z$
- Massive two-loop amplitudes computed in mass expansion to  $(s/m_t^2)^6$
- Massive real emission amplitudes computed exactly – no need for jet cut
- **Results extended beyond  $2m_t$  threshold using Padé approximations – look at high-mass tail**

# Comparison with similar work

Campbell, Czakon, Ellis,  
Kirchner, hep-ph/1605.01380

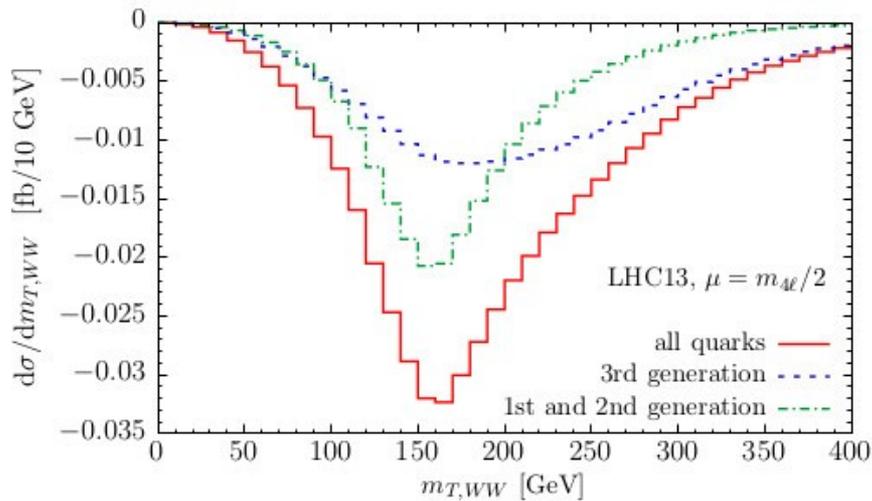
Qualitatively similar  
behavior of k-factors  
near  $2m_Z$  threshold



k-factor flat  
in high-  
energy tail

# $gg \rightarrow (H) \rightarrow WW$

- Analogous to  $gg \rightarrow (H) \rightarrow ZZ$
- Mass expansion more complicated since **top and bottom quarks mix** in loop
- $\rightarrow$  neglect 3<sup>rd</sup> generation altogether
  - **Comparable** to massless contribution at low-intermediate  $m_{T,WW}$
  - **Dominate** at high  $m_{T,WW}$
- **Partial results only**



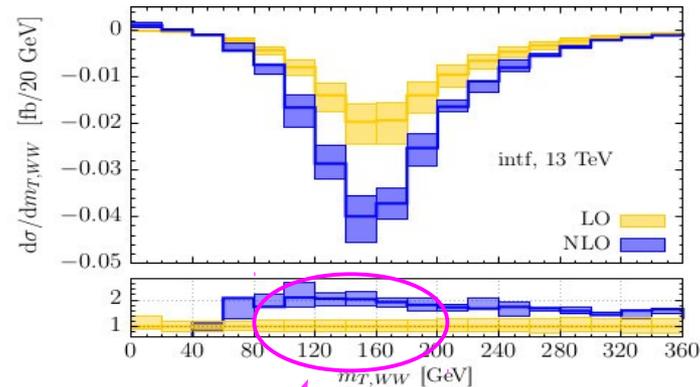
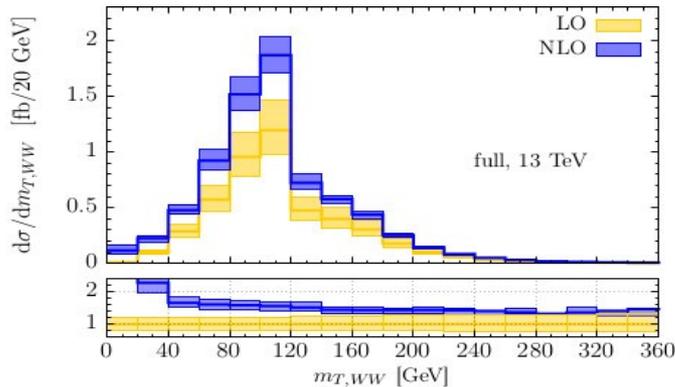
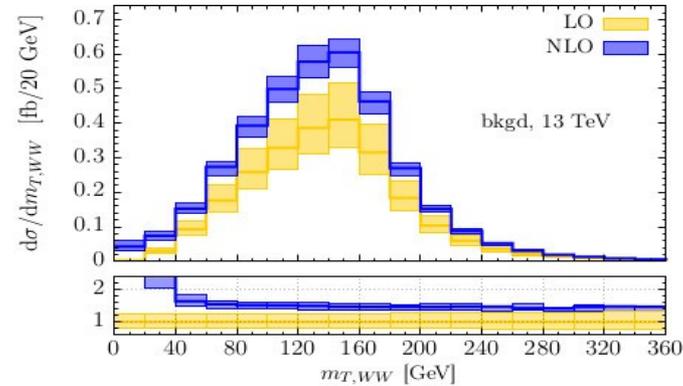
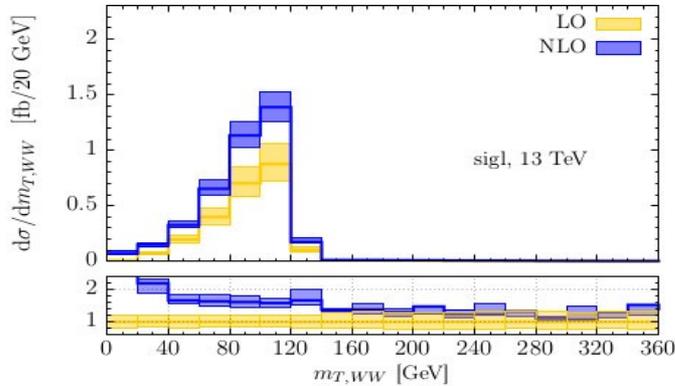
- $gg \rightarrow W^+W^- \rightarrow \nu_e e^+ \mu^- \bar{\nu}_\mu$
- No kinematic cuts imposed
- Scales as for ZZ

# $gg \rightarrow (H) \rightarrow WW$ Results: Cross Sections

$$\begin{aligned}
 \sigma_{\text{LO}}^{\text{signal}} &= 48.3_{-8.4}^{+10.4} \text{ fb}, & \sigma_{\text{NLO}}^{\text{signal}} &= 81.0_{-8.2}^{+10.5} \text{ fb} \\
 \sigma_{\text{LO}}^{\text{bkgd}} &= 49.0_{-9.7}^{+12.8} \text{ fb}, & \sigma_{\text{NLO}}^{\text{bkgd}} &= 74.7_{-6.2}^{+5.5} \text{ fb} \\
 \sigma_{\text{LO}}^{\text{intf}} &= -2.24_{-0.59}^{+0.44} \text{ fb}, & \sigma_{\text{NLO}}^{\text{intf}} &= -4.15_{-0.54}^{+0.47} \text{ fb} \\
 \sigma_{\text{LO}}^{\text{full}} &= 95.0_{-17.6}^{+22.6} \text{ fb}, & \sigma_{\text{NLO}}^{\text{full}} &= 151.6_{-13.9}^{+15.4} \text{ fb}.
 \end{aligned}$$

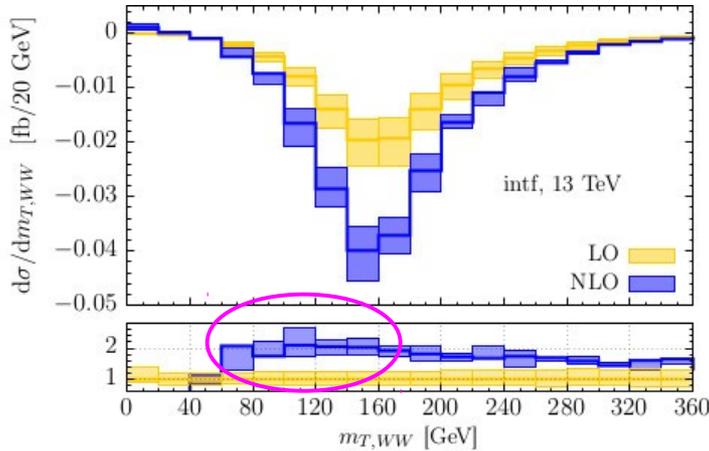
- **Destructive interference** ~ 2%
  - Higgs peak present → interference smaller than signal and background
- Scale uncertainty reduced by factor ~ 2
- $K_{\text{sigl}} = 1.68$      $K_{\text{bkgd}} = 1.53$      $K_{\text{intf}} = 1.85$ 
  - slightly above geometric mean

# $gg \rightarrow (H) \rightarrow WW$ Results: Mass distributions



- Differential k-factors **relatively flat...**
- ... except for interference near  $2m_W$  threshold – as in ZZ case

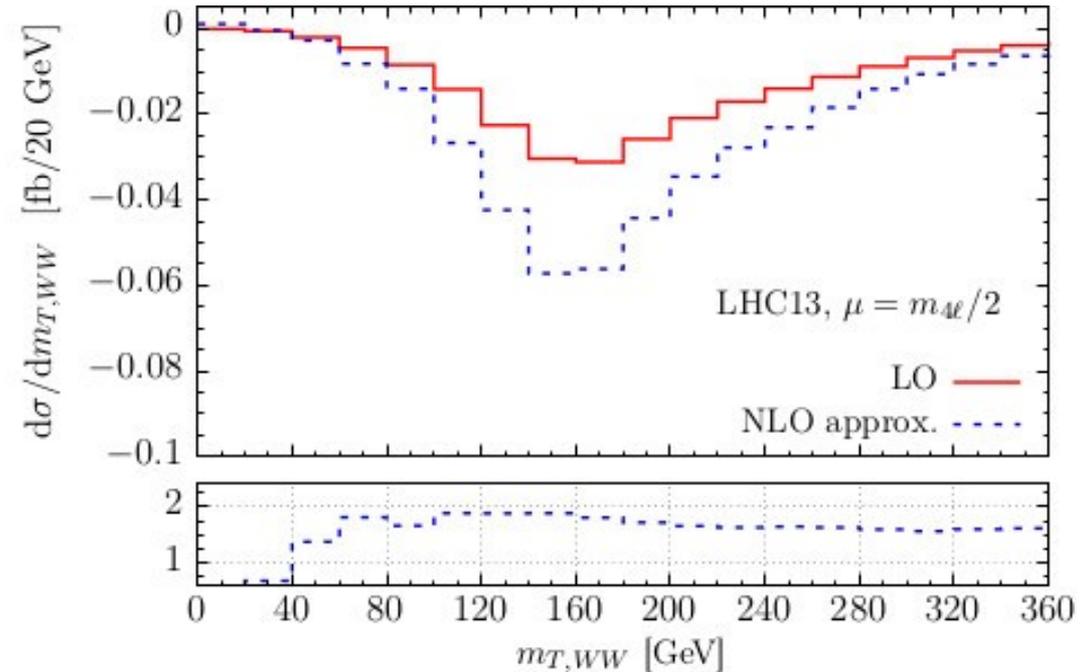
# $gg \rightarrow (H) \rightarrow WW$ Results: Estimating effect of 3<sup>rd</sup> generation



- As in ZZ case, enhancement from **massless loops**
- **3<sup>rd</sup> generation loops** give relatively flat differential k-factor

→ estimate by using LO results scaled by approximate k-factor

$$\sqrt{K_{\text{sigl}} K_{\text{bkgd}}}$$



# Nice job...

Impact of NLO calculation on width constraints:

- K-factor known, can remove systemic uncertainty
- **Exact impact not obvious** – will wait for experimental analysis

## ...but is it good enough?

- NLO is known to be insufficient for onshell Higgs – **is it okay for offshell?**
  - NLO results lie **outside** LO scale uncertainty bands
  - Do we trust the **NLO scale uncertainty?**
  - **Offshell NNLO** impossible at present
  - Use NNLO results for infinite  $m_t$  to get **approximate NNLO** k-factor offshell?
- Can we understand effectiveness of Padé approximants (e.g. how well do they do for  $HH$  production)?

# Conclusions

- Higgs off-shell behavior provides a rich environment to study Higgs physics:
  - Probe **unitarizing behavior** of the Higgs
  - **Indirect constraints** on Higgs width
  - **Test couplings** at high energies
- NLO corrections to **interference** in  $gg \rightarrow ZZ$  and  $gg \rightarrow WW$ , are now known, at least below  $2m_t$  threshold
- Difficulty of computing two-loop massive corrections
  - **top mass expansion** for  $ZZ$
  - **neglect 3<sup>rd</sup> generation** for  $WW$
- $ZZ$  in window  $150 \text{ GeV} \leq m_{4\ell} \leq 340 \text{ GeV}$ 
  - Moderate k-factors  $\sim 1.6$ - $1.7$
  - $K_{\text{intf}} \simeq \sqrt{K_{\text{sigl}} K_{\text{bkgd}}}$  **except near  $2m_z$  threshold** – driven by massless amplitudes
- $WW$ :
  - Interference k-factor slightly larger than signal and background k-factors
  - Effect of 3<sup>rd</sup> generation at NLO approximated assuming uniform contribution to k-factor

# THANK YOU!