

# ABMP16 PDFs

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(*in collaboration with J.Blümlein, S.Moch, and R.Plačákytė*)

- HERA I+II data:  $\alpha_s(M_Z)$ ,  $m_c$ , and  $m_b$
  - Drell-Yan data from the LHC and Tevatron: Isospin asymmetry and d/u at large x  
sa, Blümlein, Moch, Plačákytė, hep-ph/1508.07923
  - t-quark data:  $m_t$  and gluon distribution
  - Charm production data from NOMAD and CHORUS: strange sea  
sa, Blümlein, Caminada, Lipka, Lohwasser,  
Moch, Petti, Plačákytė hep-ph/1404.6469
- sa, Blümlein, Moch, Plačákytė, hep-ph/1701.05838

# The fit ingredients

## DATA:

DIS NC/CC inclusive (HERA I+II added, no deuteron data included)  
DIS NC charm production (HERA)  
DIS CC charm production (HERA, NOMAD, CHORUS, NuTeV/CCFR)  
fixed-target DY  
LHC DY distributions (ATLAS, CMS, LHCb)  
t-quark data from the LHC and Tevatron  
deuteron data are excluded

## QCD:

NNLO evolution  
NNLO massless DIS and DY coefficient functions  
NLO+ massive DIS coefficient functions (**FFN scheme**)

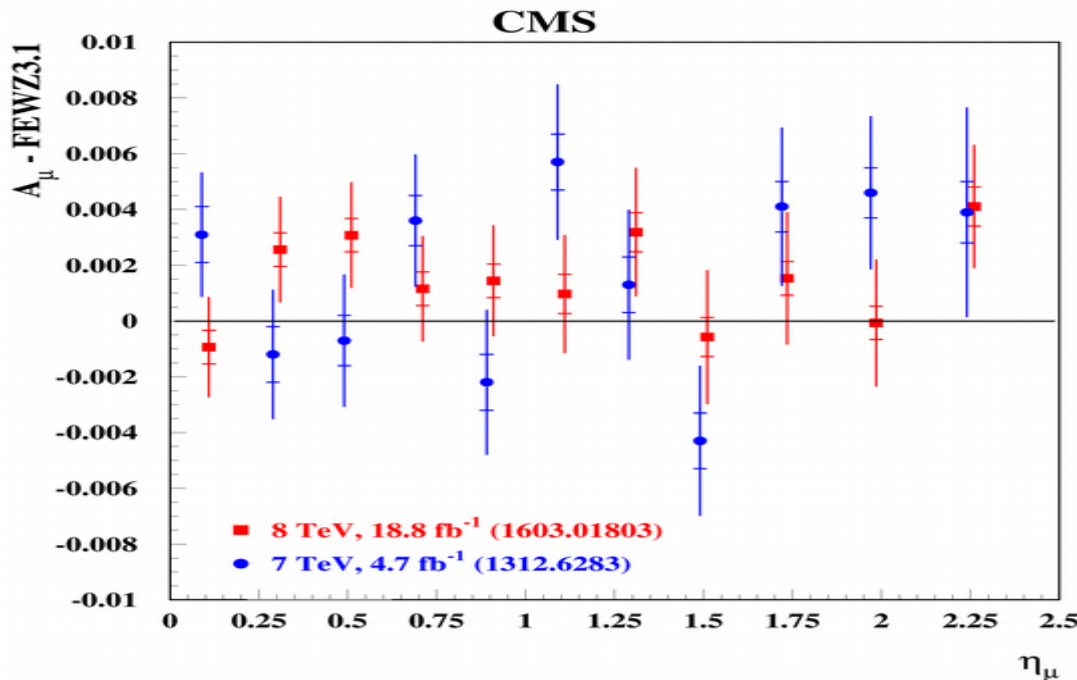
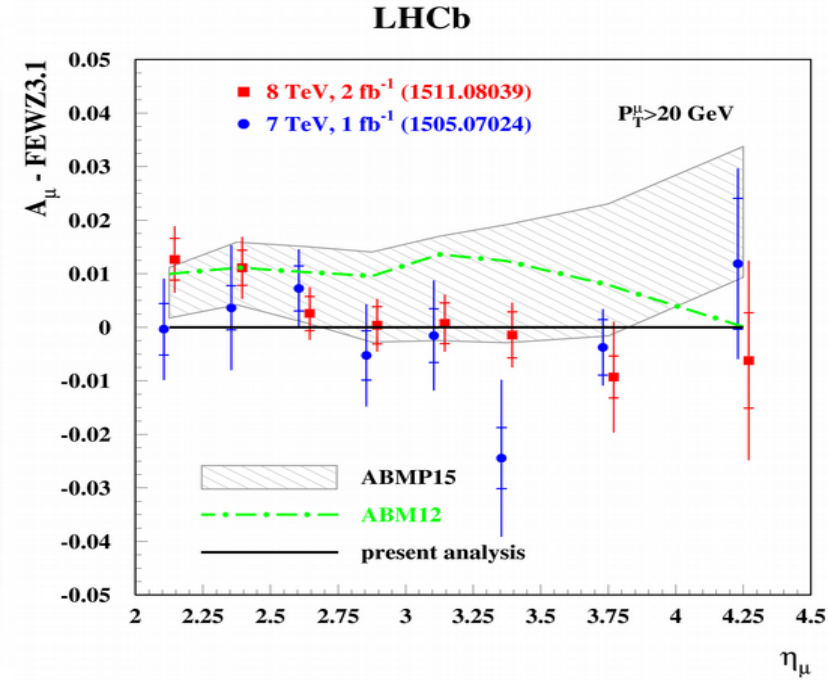
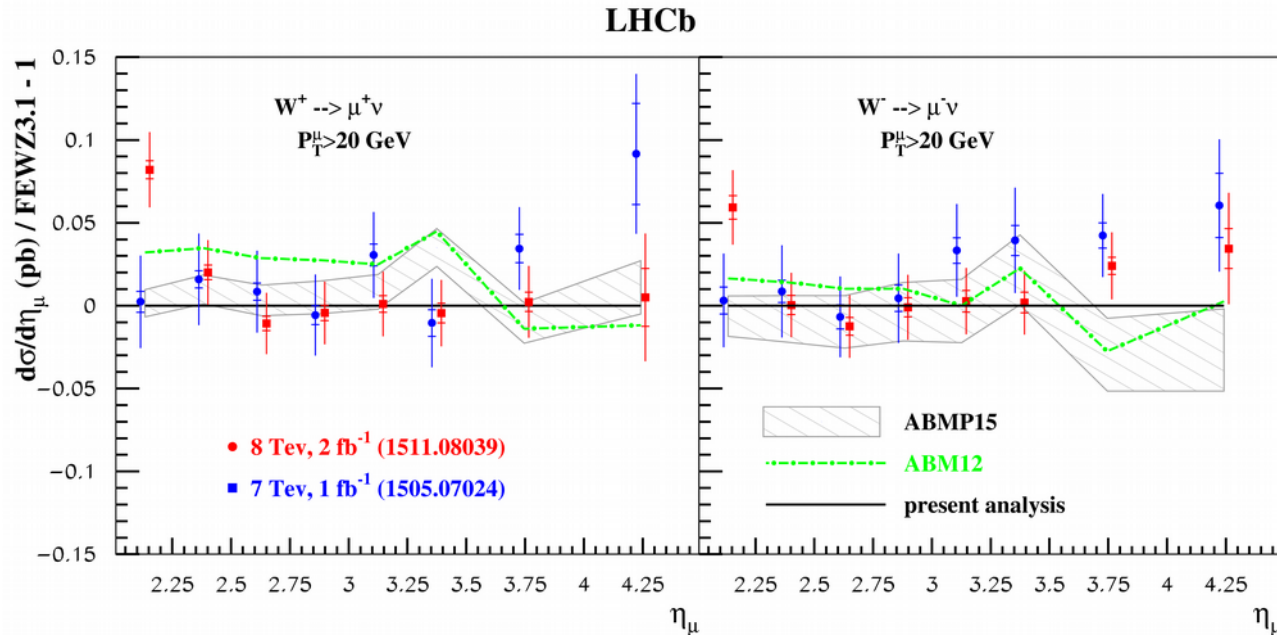
- NLO + NNLO(approx.) corrections for NC
- NNLO CC at  $Q \gg m_c$
- running mass

NNLO exclusive DY (FEWZ 3.1)  
NNLO inclusive  $t\bar{t}$  production ( pole / running mass )  
Relaxed form of  $(d\bar{d}-u\bar{u})$  at small  $x$

## Power corrections in DIS:

target mass effects  
dynamical twist-4 terms

# Most recent DY inputs



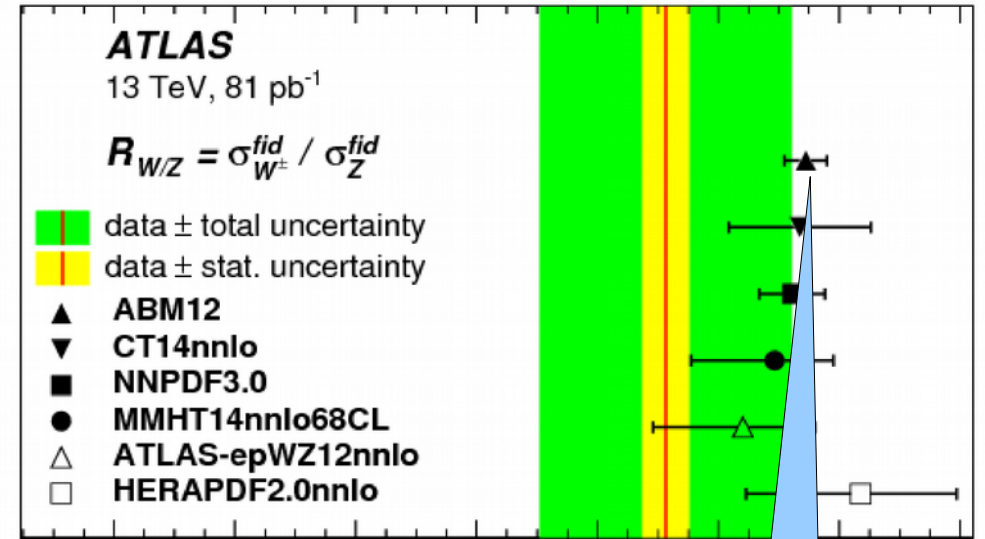
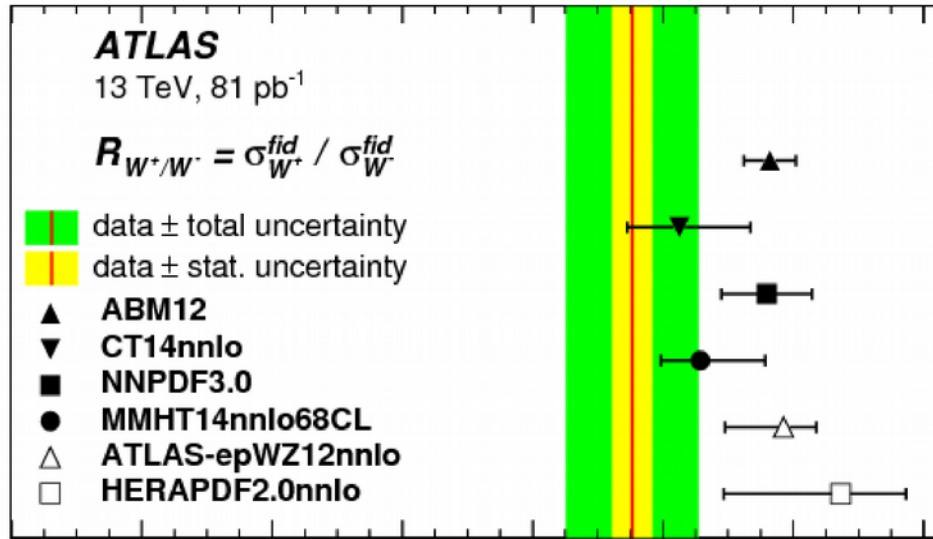
Filtering of the LHCb data has been performed:

- a bump at 7 TeV and  $Y=3.275$  (not confirmed by the LHCb data at 8 TeV)
- and excess at 8 TeV and  $Y=2.125$  (not confirmed by the CMS data at 8 TeV)

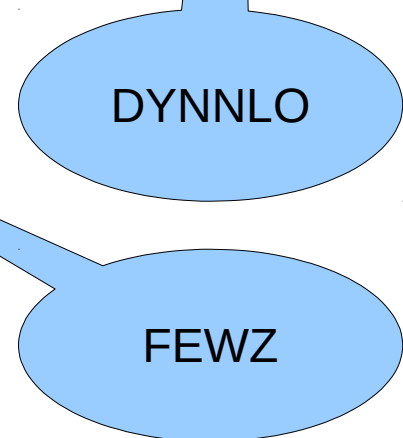
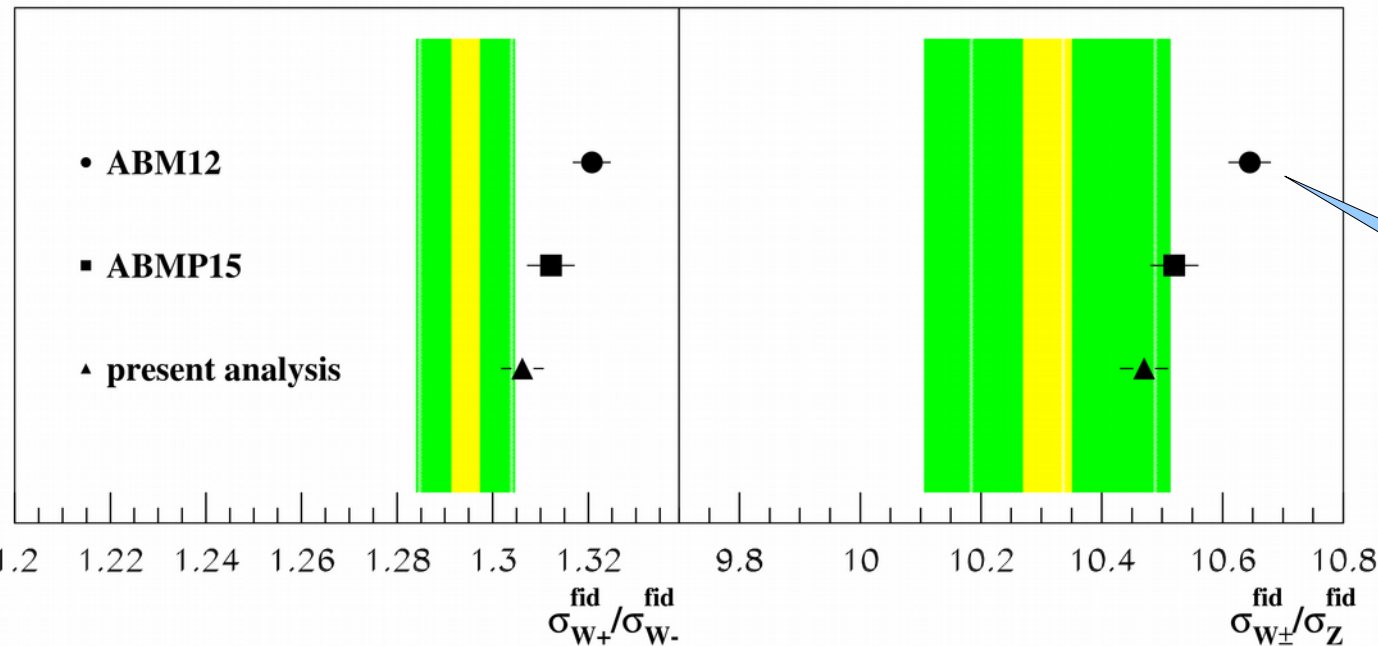
The CMS data at 8 TeV are much smoother than the ones at 7 TeV:  
 $\chi^2=17/22$  versus  $22/11$

# ATLAS W&Z at 13 TeV

ATLAS, hep-ex/1603.09222



ATLAS (13 TeV, 81 pb<sup>-1</sup>) 1603.09222



Data are well accommodated into the fit  $\chi^2/NDP=9/6$



# Collider W&Z data used in the fit

Experiment	ATLAS		CMS		DØ		LHCb			
$\sqrt{s}$ (TeV)	7	13	7	8	1.96		7	8		
Final states	$W^+ \rightarrow l^+ \nu$ $W^- \rightarrow l^- \nu$ $Z \rightarrow l^+ l^-$	$W^+ \rightarrow l^+ \nu$ $W^- \rightarrow l^- \nu$ $Z \rightarrow l^+ l^-$	$W^+ \rightarrow \mu^+ \nu$ $W^- \rightarrow \mu^- \nu$ (asym)	$W^+ \rightarrow \mu^+ \nu$ $W^- \rightarrow \mu^- \nu$	$W^+ \rightarrow \mu^+ \nu$ $W^- \rightarrow \mu^- \nu$ (asym)	$W^+ \rightarrow e^+ \nu$ $W^- \rightarrow e^- \nu$ (asym)	$W^+ \rightarrow \mu^+ \nu$ $W^- \rightarrow \mu^- \nu$ $Z \rightarrow \mu^+ \mu^-$	$Z \rightarrow e^+ e^-$	$W^+ \rightarrow \mu^+ \nu$ $W^- \rightarrow \mu^- \nu$ $Z \rightarrow \mu^+ \mu^-$	
Cut on the lepton $P_T$	$P_T^l > 20$ GeV	$P_T^e > 25$ GeV	$P_T^\mu > 25$ GeV	$P_T^\mu > 25$ GeV	$P_T^\mu > 25$ GeV	$P_T^e > 25$ GeV	$P_T^\mu > 20$ GeV	$P_T^e > 20$ GeV	$P_T^\mu > 20$ GeV	
Luminosity (1/fb)	0.035	0.081	4.7	18.8	7.3	9.7	1	2	2.9	
Reference	[66]	[26]	[24]	[25]	[23]	[22]	[19]	[21]	[20]	
NDP	30	6	11	22	10	13	31	17	32	
$\chi^2$	present analysis <sup>a</sup>	31.0	9.2	22.4	16.5	17.6	19.0	45.1	21.7	40.0
	CJ15 [6]	–	–	–	–	20	29	–	–	–
	CT14 [7]	42	–	– <sup>b</sup>	–	–	34.7	–	–	–
	JR14 [8]	–	–	–	–	–	–	–	–	–
	HERAFitter [197]	–	–	–	–	13	19	–	–	–
	MMHT14 [9]	39	–	–	–	21	–	–	–	–
	NNPDF3.0 [10]	35.4	–	18.9	–	–	–	–	–	–

<sup>a</sup> The ABM12 [1] analysis has used older data sets from CMS and LHCb.

<sup>b</sup> For the statistically less significant data with the cut of  $P_T^\mu > 35$  GeV the value of  $\chi^2 = 12.1$  was obtained.

*Obsolete/superseded/low-accuracy Tevatron and LHC data are not used*

Thorne, QCD@LHC2016

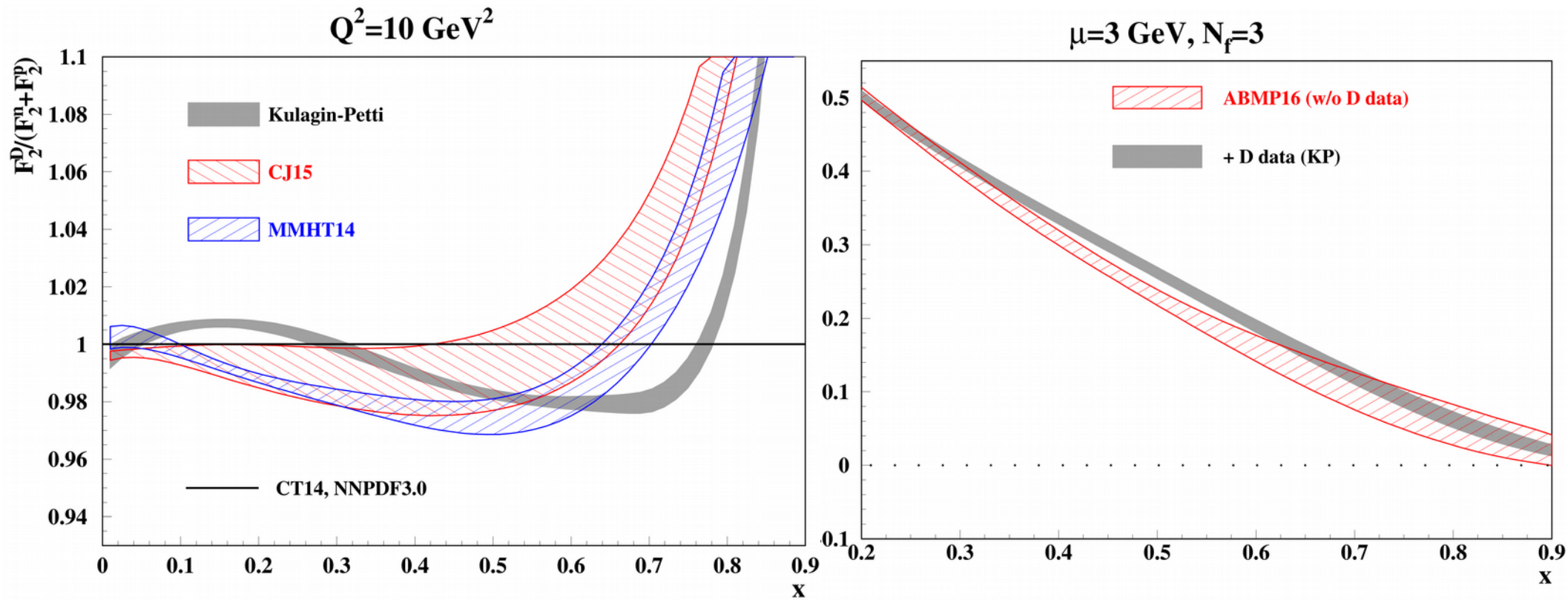
	no. points	NLO $\chi_{pred}^2$	NLO $\chi_{new}^2$	NNLO $\chi_{pred}^2$	NNLO $\chi_{new}^2$
$\sigma_{tt}$ Tevatron +CMS+ATLAS	18	19.6	20.5	14.7	15.5
LHCb 7 TeV $W + Z$	33	50.1	45.4	37.1	36.7
LHCb 8 TeV $W + Z$	34	77.0	58.9	76.1	67.2
LHCb 8TeV $e$	17	37.4	33.4	30.0	27.8
CMS 8 TeV $W$	22	32.6	18.6	57.6	29.4
CMS 7 TeV $W + c$	10	8.5	10.0	8.7	8.0
DØ $e$ asymmetry	13	22.2	21.5	27.3	22.9
total	3738/3405	4375.9	4336.1	3768.0	3739.3

The sum of  $\chi^2$ /NDP for the DY data by LHCb, CMS, and DØ:

184/119 (MMHT16)  
171/119 (ABMP16, no filtering)

account of other DY data increases the difference

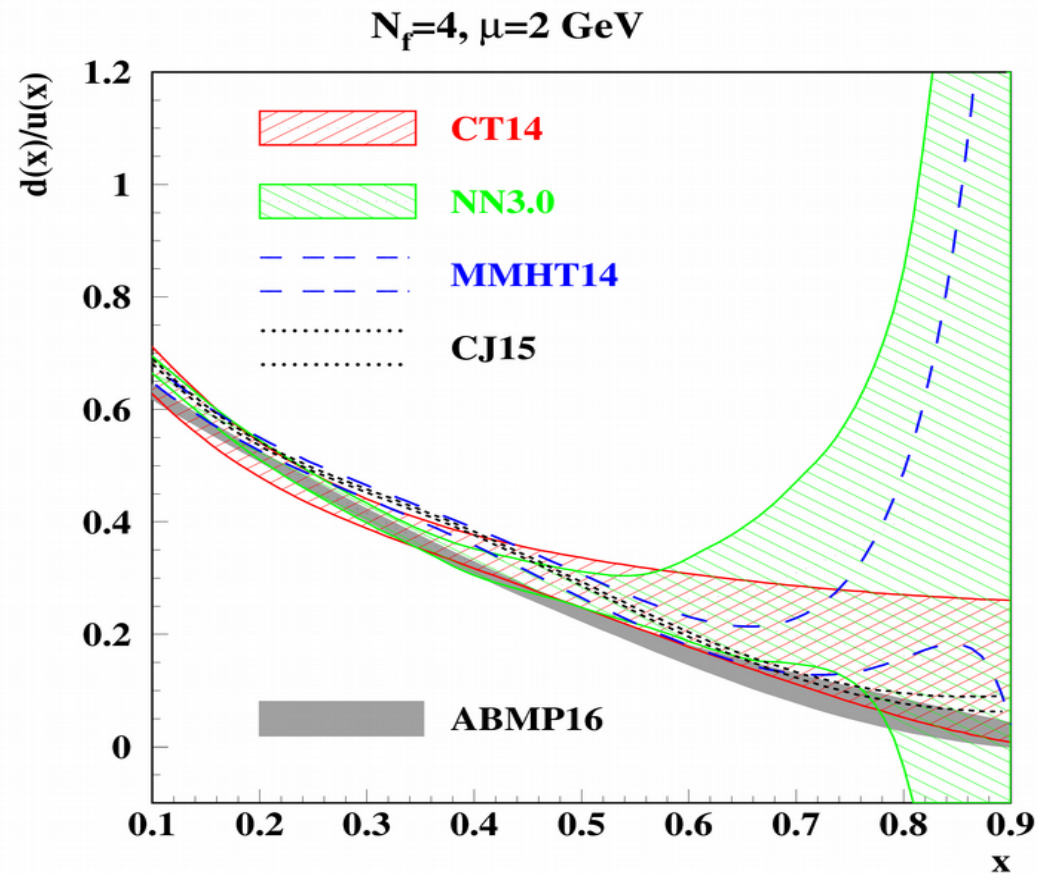
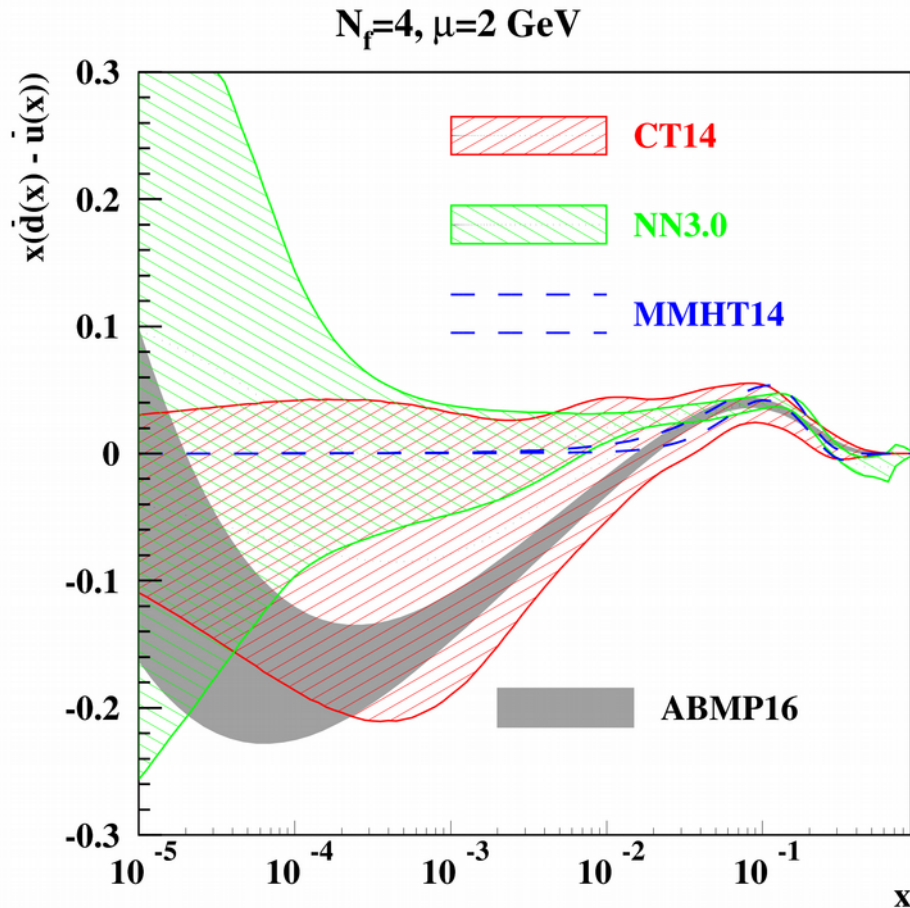
# Deuteron corrections in the PDF fits



*Spread between different deuteron models  $O(\%)$ ; quite big for the purposes of precision measurements*

*DY data help to keep accuracy of the PDF determination avoiding uncertainty due to the modeling of nuclear effects*

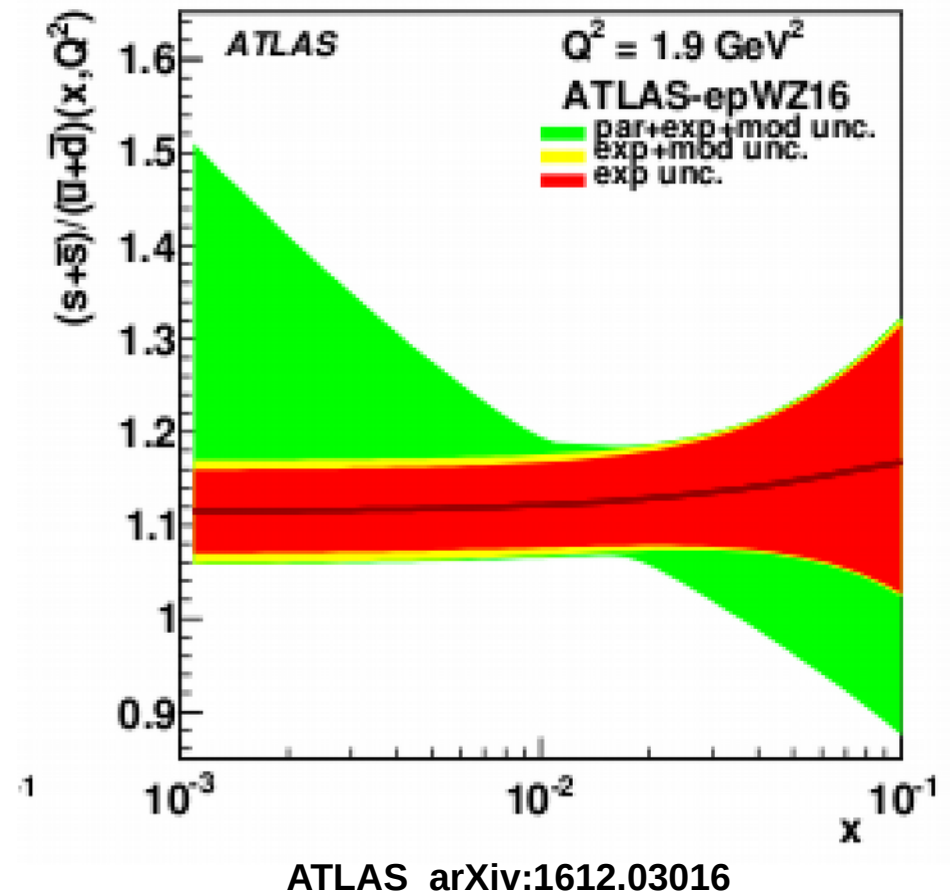
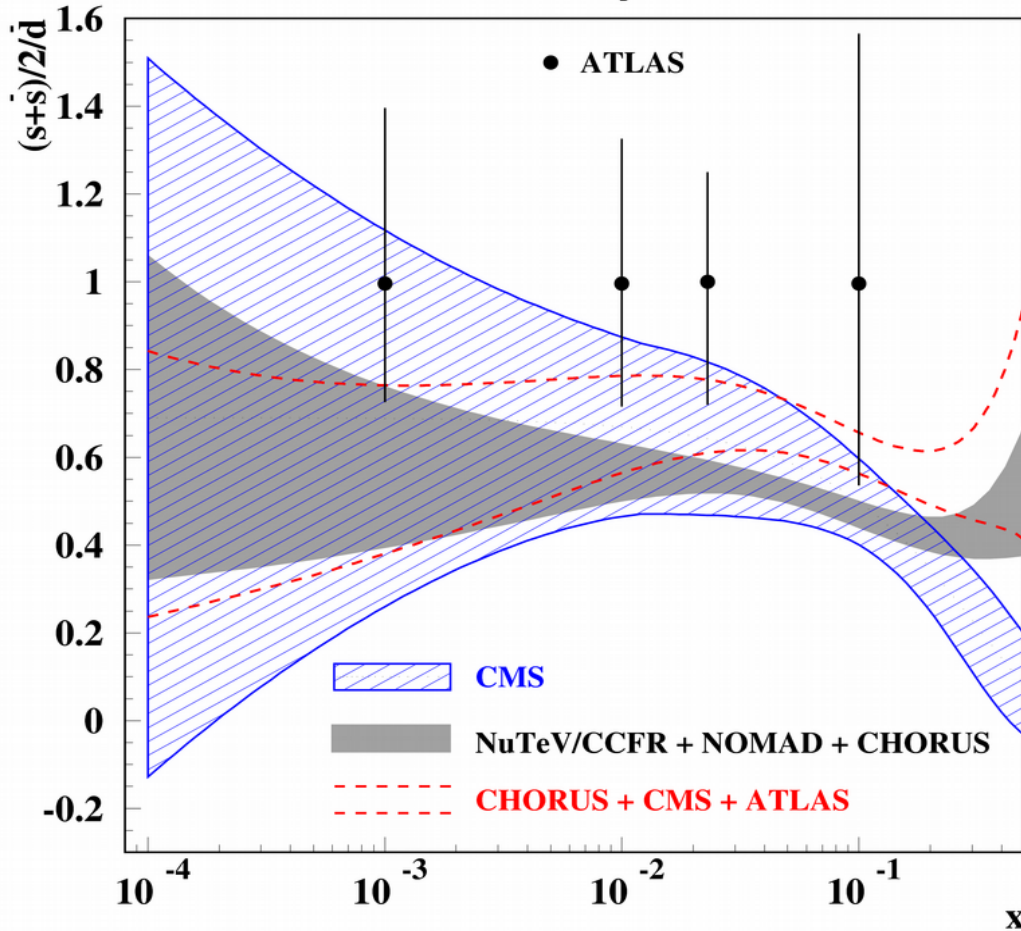
# Impact of the forward Drell-Yan data



- Relaxed form of the sea iso-spin asymmetry  $I(x)$  at small  $x$ ; Regge-like behaviour is recovered only at  $x \sim 10^{-6}$ ; at large  $x$  it is still defined by the phase-space constraint
- Good constraint on the  $d/u$  ratio w/o deuteron data  $\rightarrow$  independent extraction of the deuteron corrections Accardi, Brady, Melnitchouk, Owens, Sato hep-ph/1602.03154;
- Big spread between different PDF sets, up to factor of 30 at large  $x$   $\rightarrow$  poor control of the background to BSM effects without constraints from the DY data

# ATLAS strange sea determinations

$\mu^2 = 1.9 \text{ GeV}^2, n_f = 3$



- ABM update (NuTeV/CCFR+NOMAD+CHORUS) demonstrate good agreement with the CMS result
- The ATLAS(2011) strange-sea is enhanced, however it is correlated with the d-quark sea suppression → disagreement with the FNAL-E-866 data

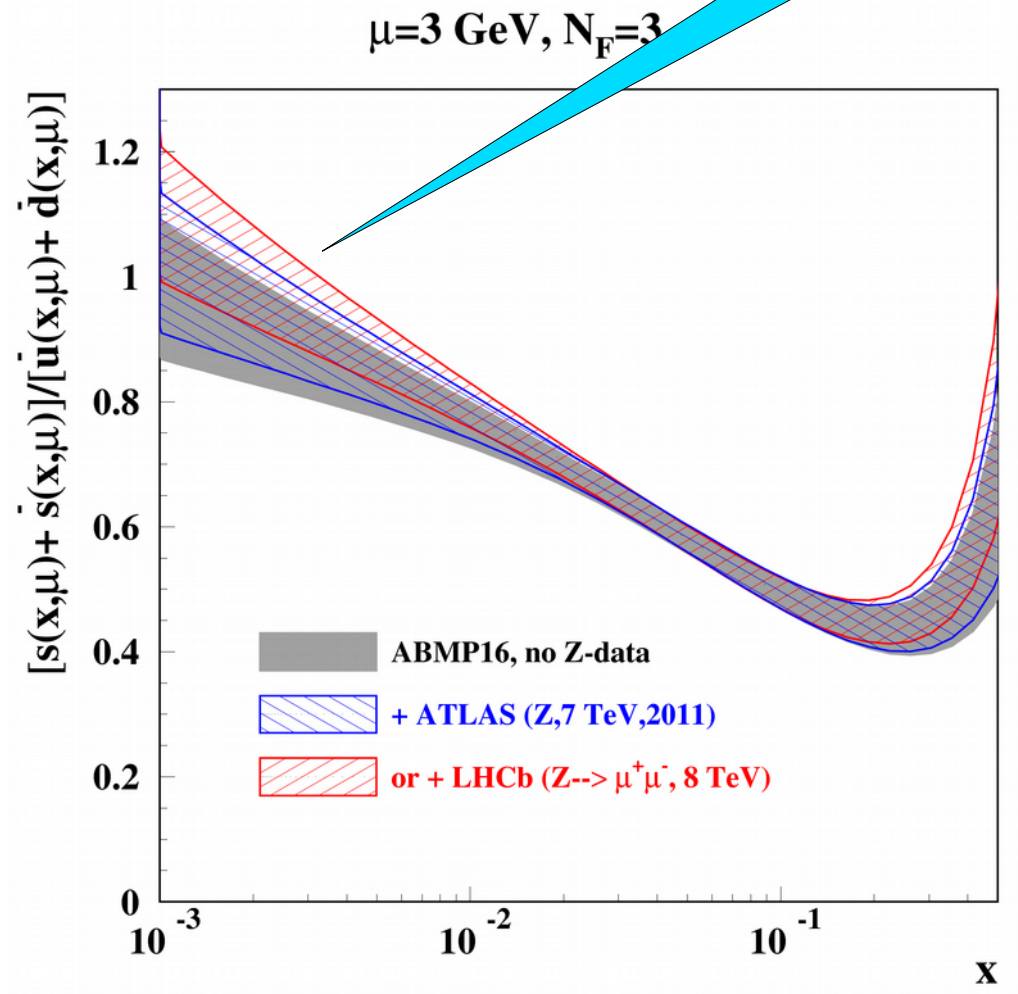
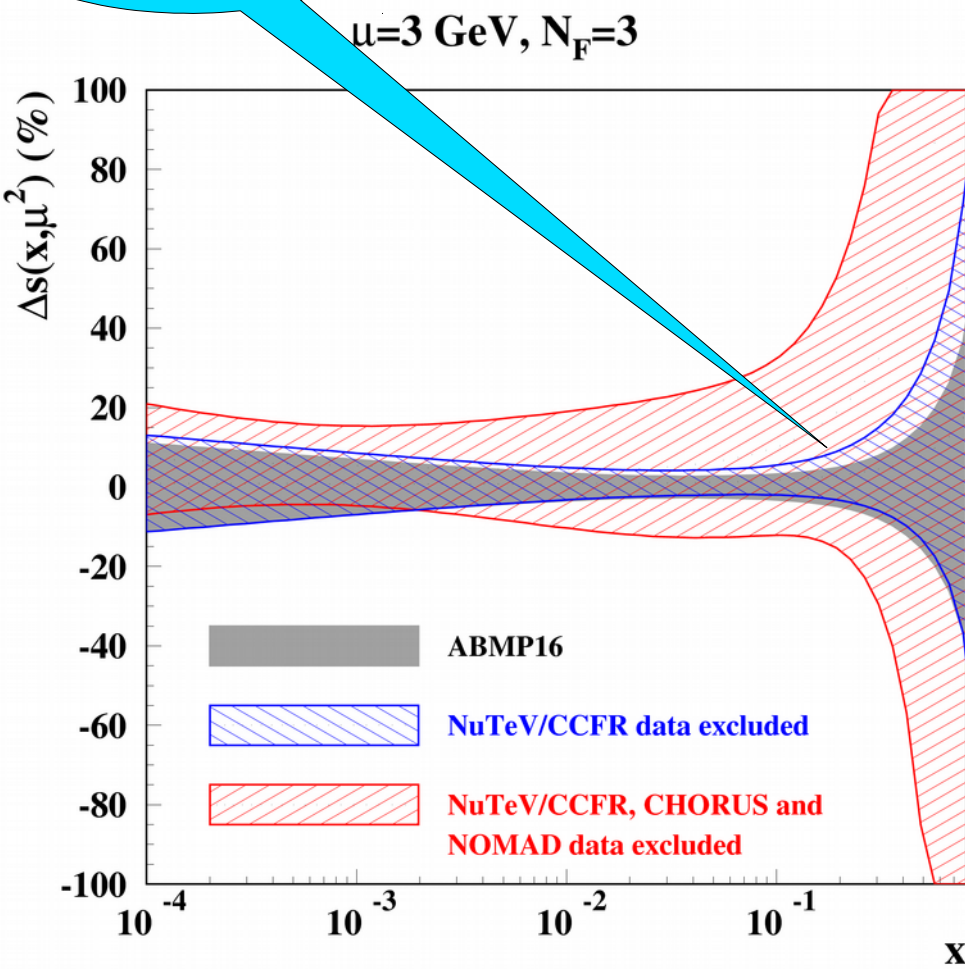
The result is confirmed with improved accuracy → disagreement with the neutrino-beam results??



# Constraints on strange sea

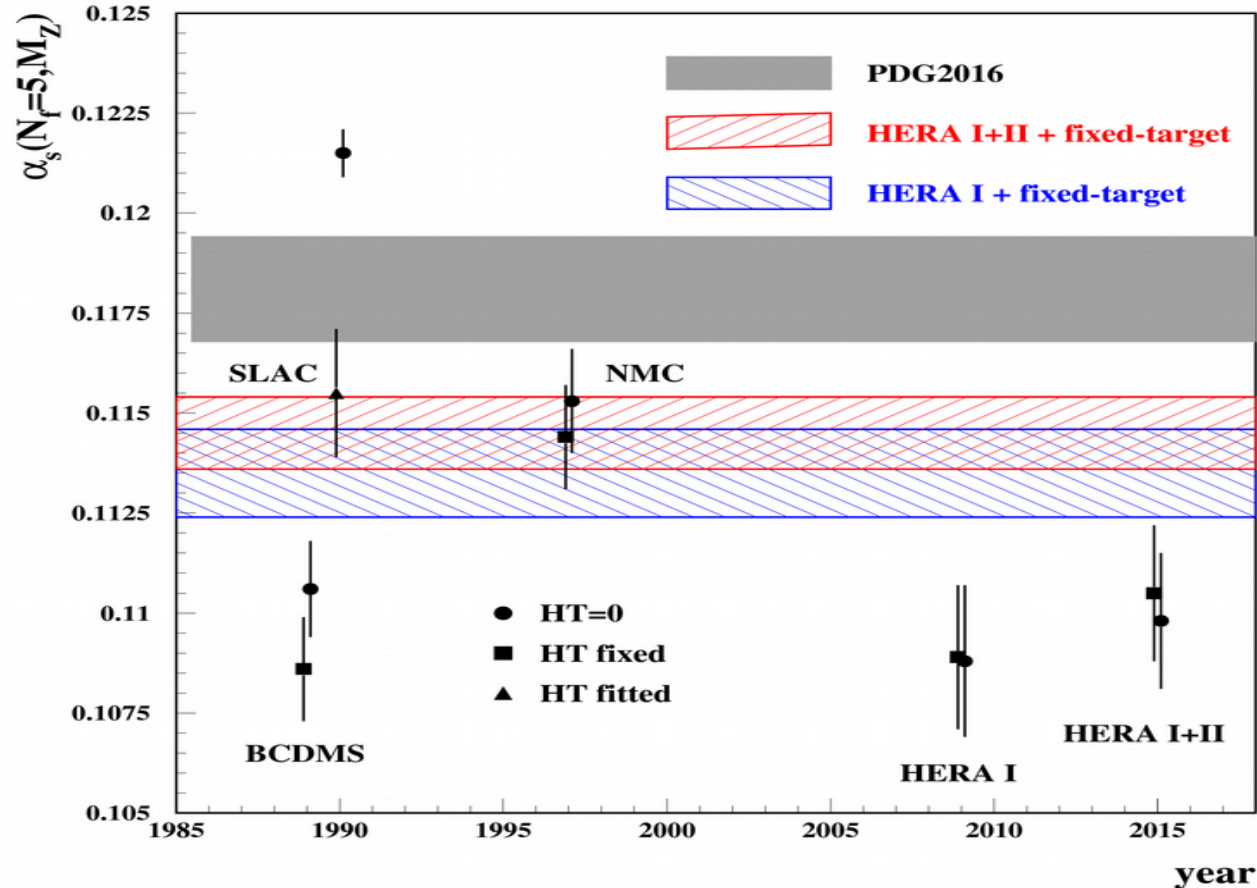
Controlled by  
NOMAD

Controlled by  
DY&DIS(incl.)

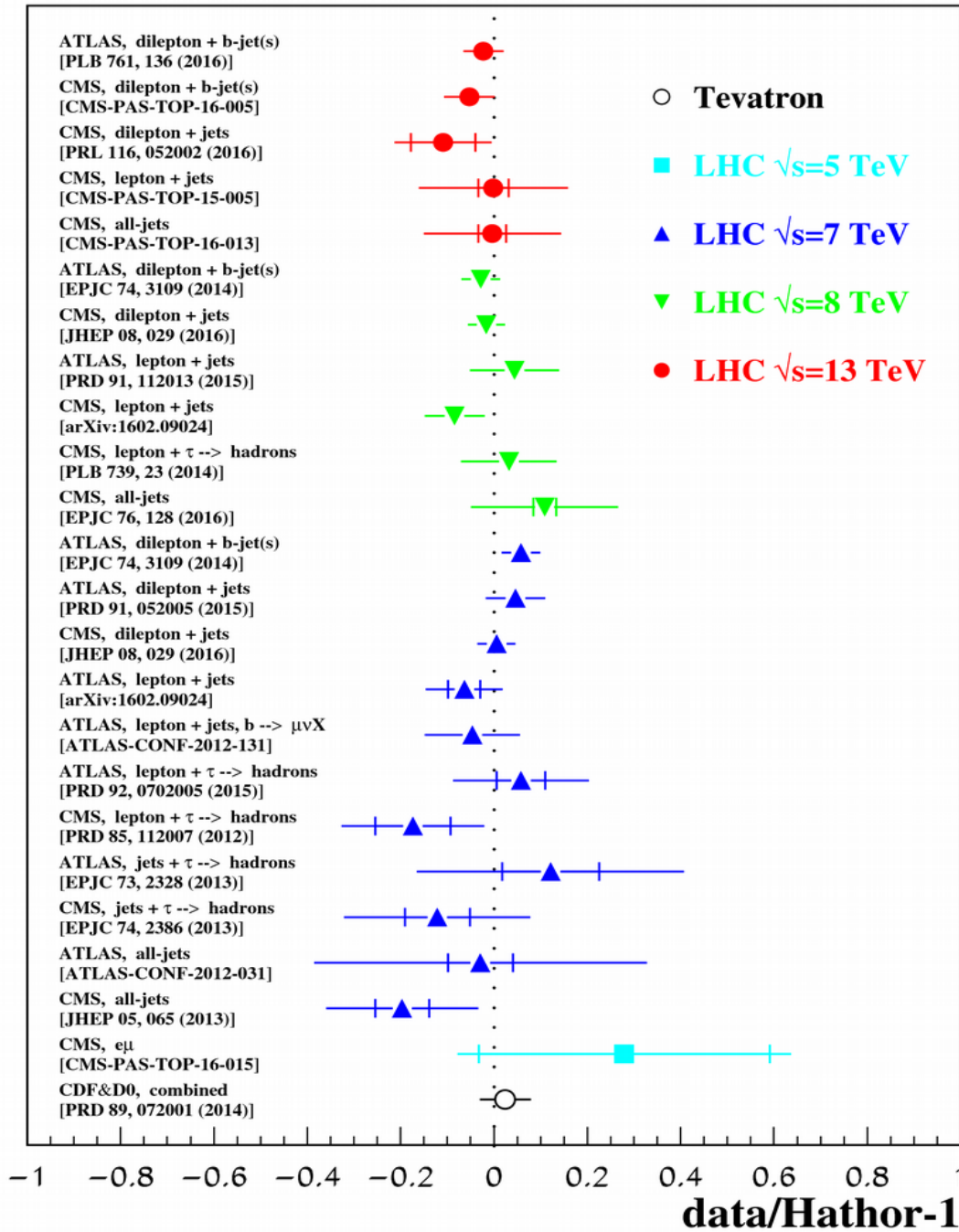
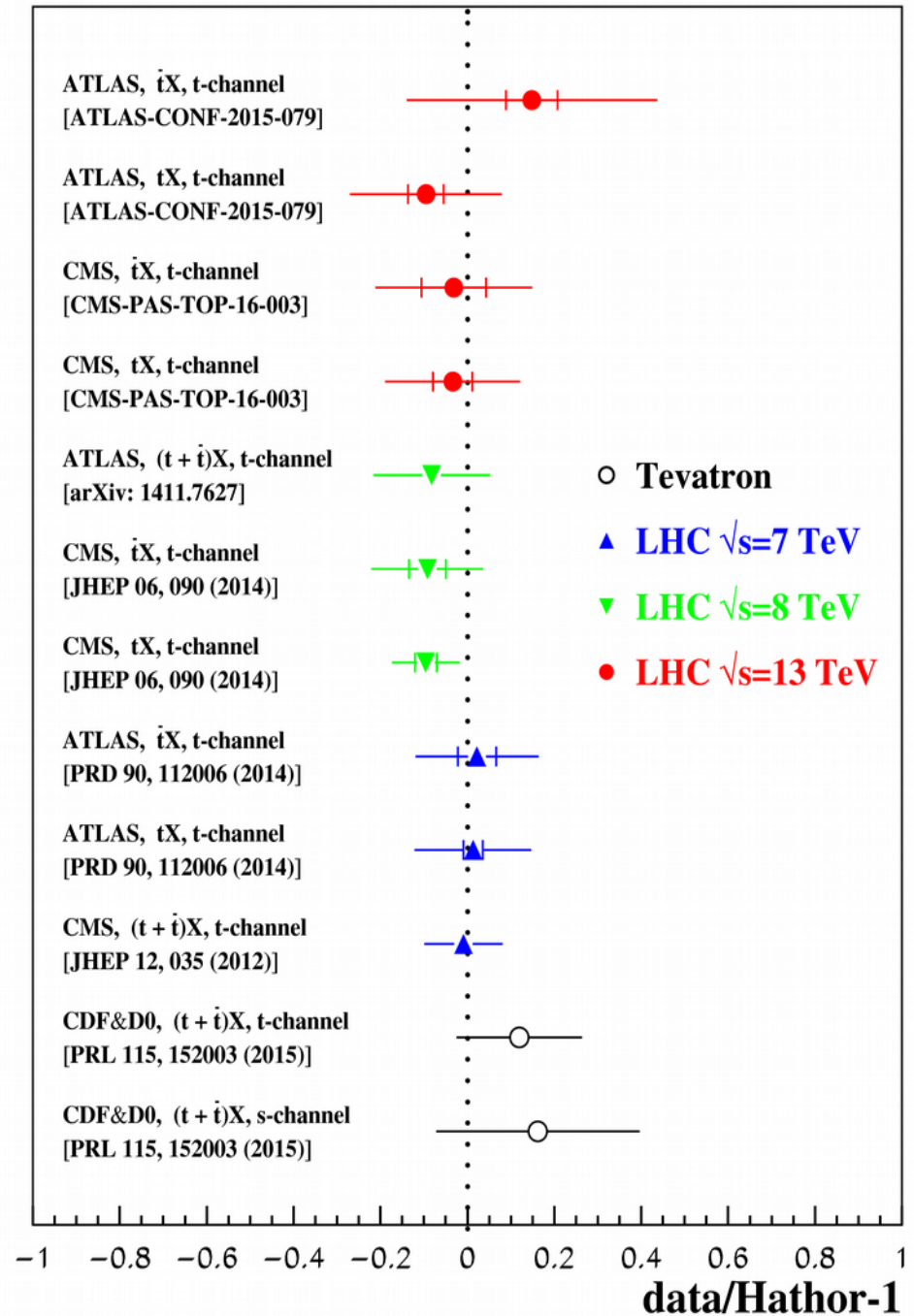


- Uncertainty of  $\sim 5\%$  is achieved at  $x$  around 0.1
- NuTeV/CCFR data play no essential role  $\rightarrow$  impact of the nuclear corrections is greatly reduced (NOMAD and CHORUS give the ratio CC/incl.)

# Strong coupling constant



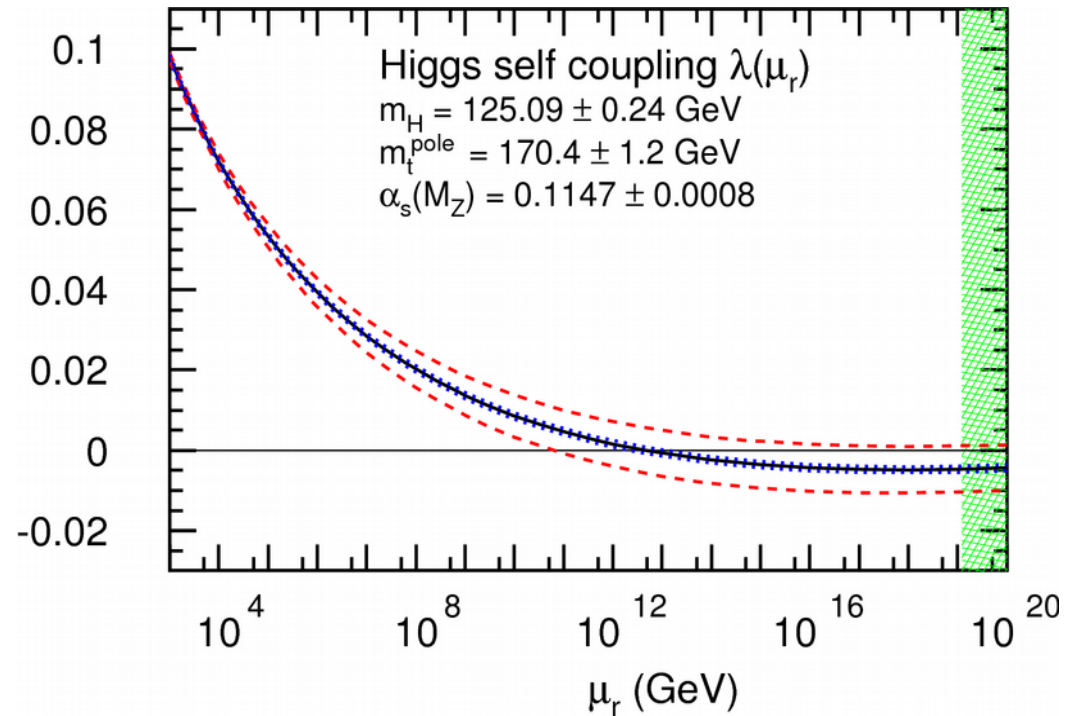
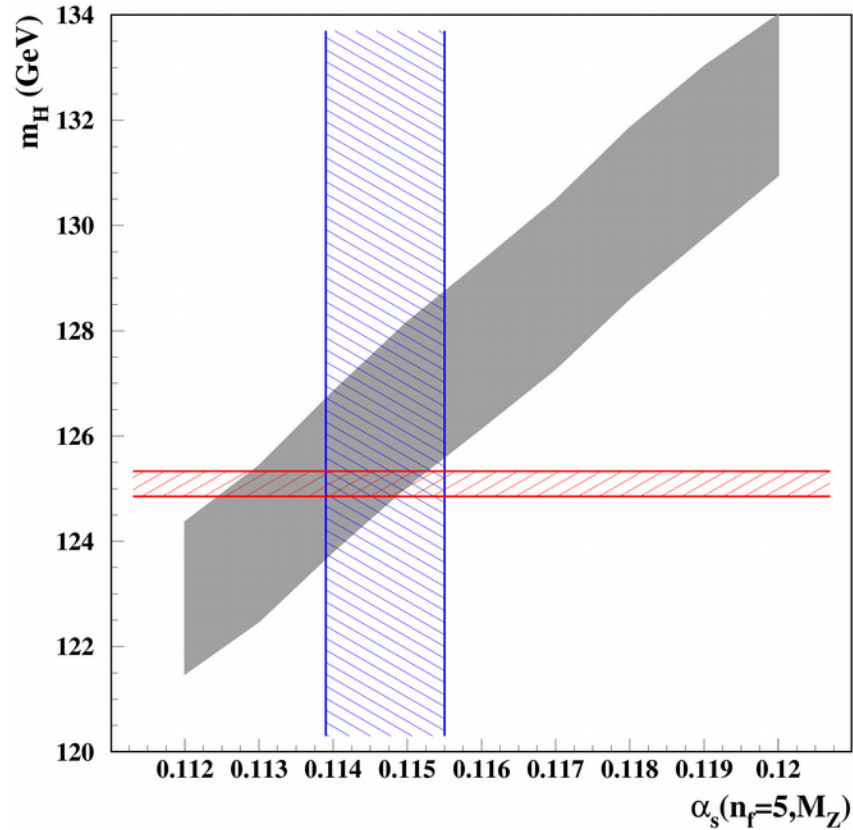
- Combination of the DY data (disentangle PDFs) and the DIS ones (constrain  $\alpha_s$ )
- Run-II data pull  $\alpha_s$  up by 0.001
- the value of  $\alpha_s$  is still lower than the PDG one: pulled up by the SLAC and NMC data; pulled down by the BCDMS and HERA ones
- only SLAC determination overlap with the PDG band provided the high-twist terms are taken into account

$\sigma(t\bar{t}X)$  $\sigma(t/\bar{t} X)$ 

$$m_t(m_t) = 160.9 \pm 1.1 \text{ GeV}$$



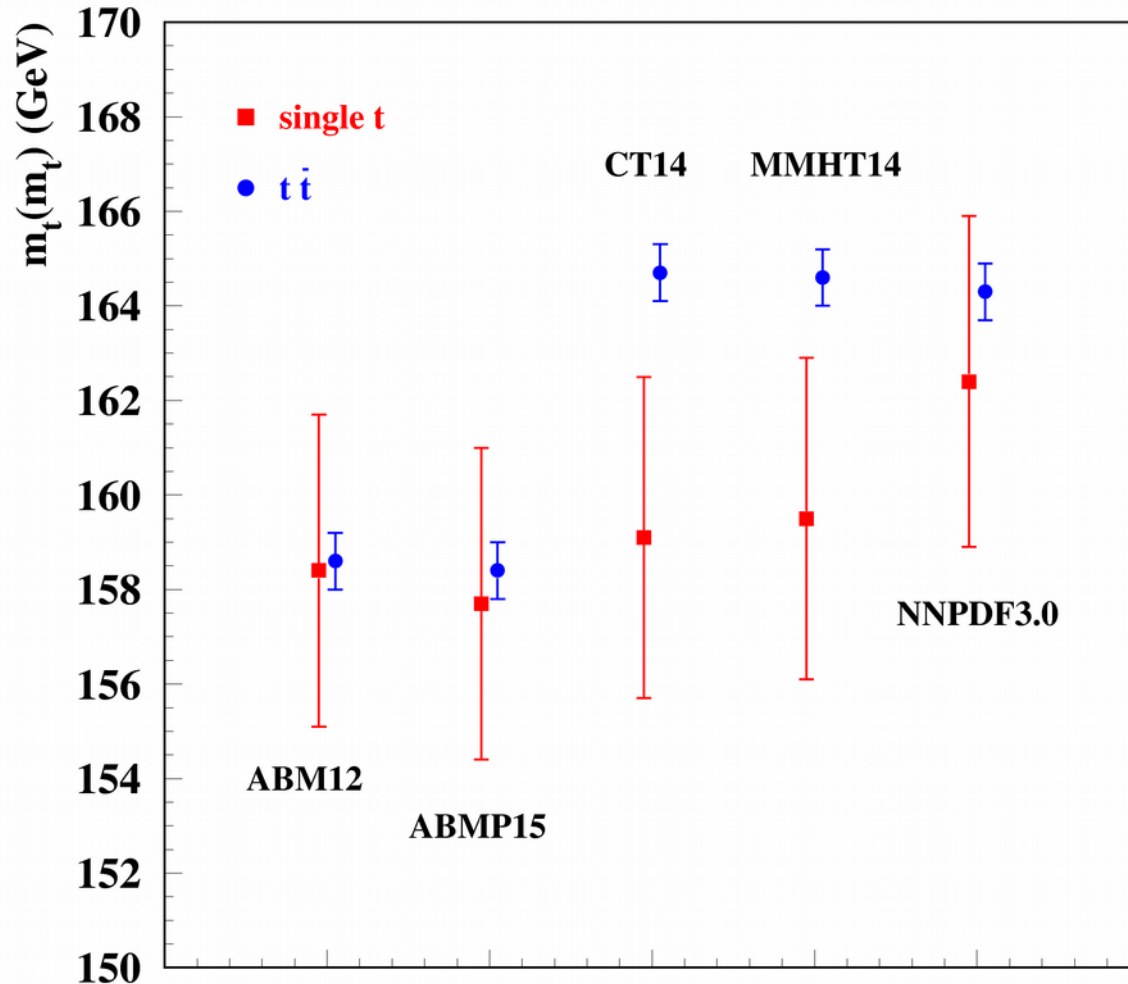
# Electroweak vacuum stability



mr: Kniehl, Pikelner, Veretin CPC 206, 84 (2016)

Vacuum stability is quite sensitive to the t-quark mass

# t-quark mass from the single-top data



- Electroweak production  $\rightarrow$  reduced impact of  $\alpha_s$  and the PDF uncertainties
- HATHOR framework  
t-channel: NNLO  
Brucherseifer, Caola, Melnikov PLB 736, 58 (2014)  
s-channel: NNLO threshold. resum.  
sa, Moch, Thier hep-ph/1608.05212
- Different PDFs prefer value of  
 $m_t(m_t) \sim 160 \pm 3.5$  GeV  
NNPDF goes higher by 3 GeV.
- The CT14 and MMHT14 go higher by 3 GeV with the t t-bar channel

# Summary

The improvements summarized in the new PDF set:

- deuteron data are replaced by the Drell-Yan ones from the LHC and Tevatron → reduced theoretical uncertainties in PDFs, in particular in d/u at large x
- the small-x iso-spin sea asymmetry is relaxed and turns negative at  $x \sim 10^{-3}$ ; an onset of the Regge asymptotics still may occur at  $x < 10^{-5}$
- improved strange sea determination, particularly at large x
- moderate increase in the large-x gluon distribution due to impact of the ttbar data
- HERA I+II data included → improved determination of  $m_c(m_c)$ ;

$$m_c(m_c) = 1.252 \pm 0.018 \text{ GeV}$$

$$m_b(m_b) = 3.83 \pm 0.12 \text{ GeV}$$

$$m_t(m_t) = 160.9 \pm 1.1 \text{ GeV}$$

$$\alpha_s(M_Z) = 0.1145(9)$$

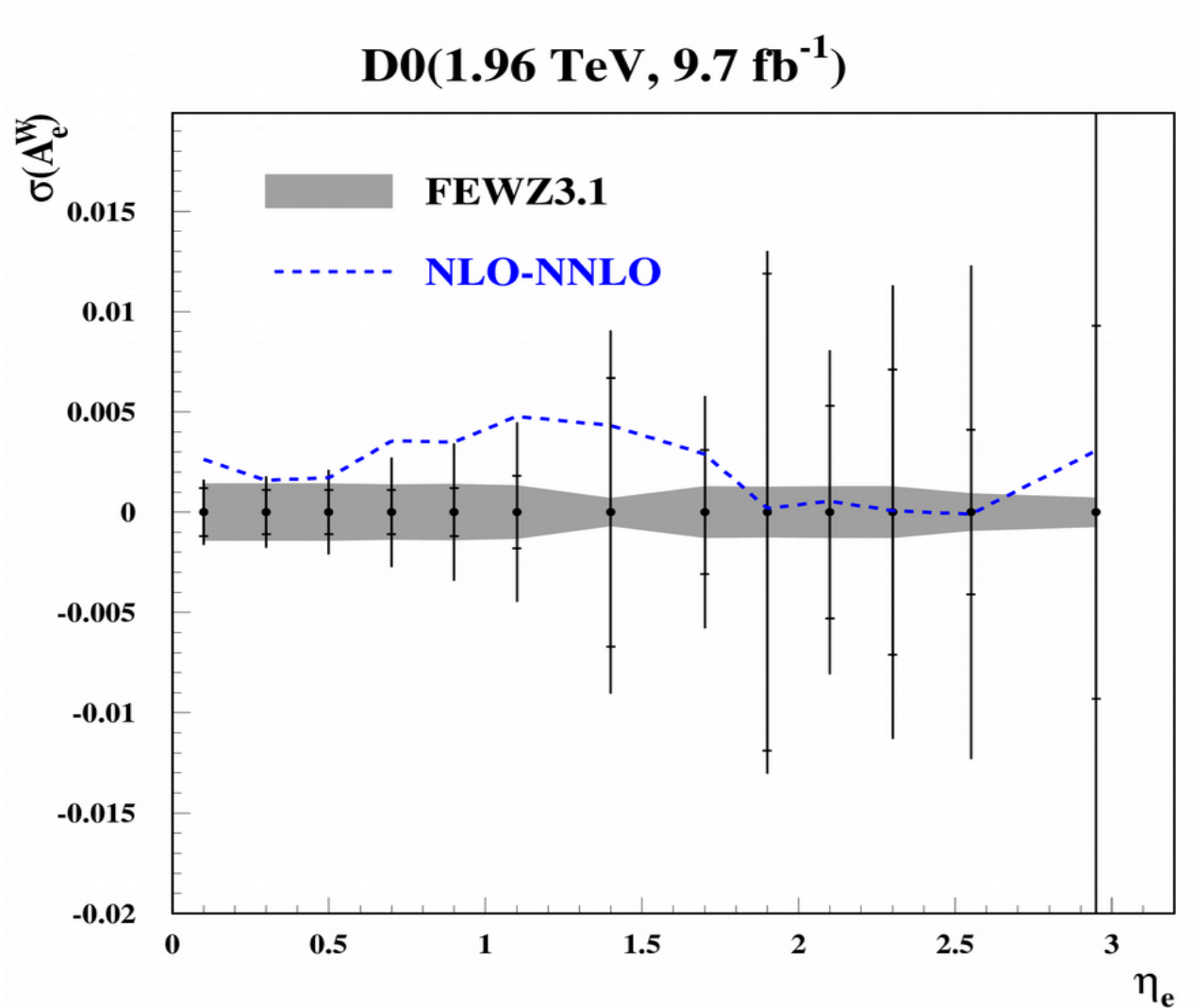
DIS

$$\alpha_s(M_Z) = 0.1147(8)$$

DIS+ttbar

**EXTRAS**

# Computation accuracy



- Accuracy of O(1 ppm) is required to meet uncertainties in the experimental data → O(10<sup>4</sup> h) of running FEWZ 3.1 in NNLO
- An interpolation grid a la FASTNLO is used

# NNLO DY corrections in the fit

The existing NNLO codes (DYNNLO, FEWZ) are quite time-consuming → fast tools are employed (FASTNLO, Applgrid,.....)

- the corrections for certain basis of PDFs are stored in the grid
- the fitted PDFs are expanded over the basis
- the NNLO c.s. in the PDF fit is calculated as a combination of expansion coefficients with the pre-prepared grids

The general PDF basis is not necessary since the PDFs are already constrained by the data, which do not require involved computations → *use as a PDF basis the eigenvalue PDF sets obtained in the earlier version of the fit*

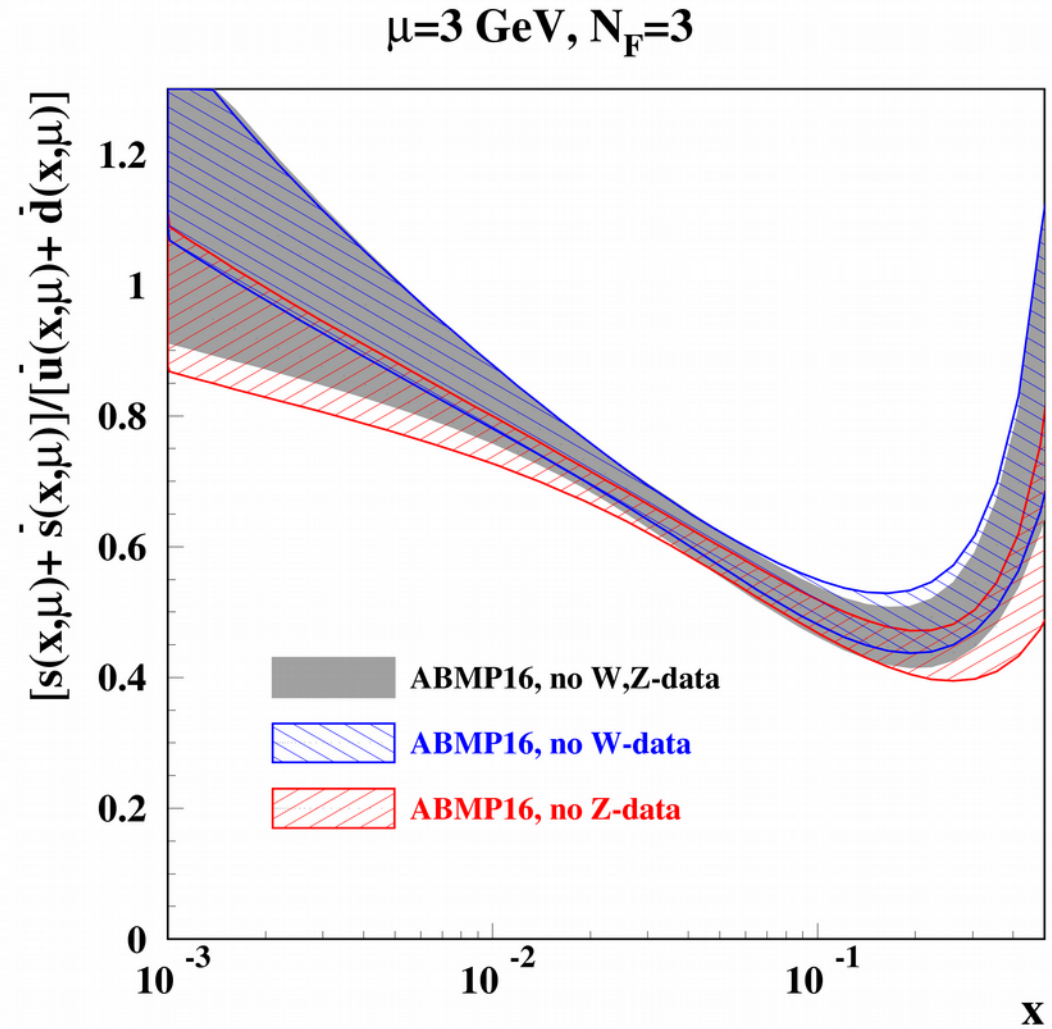
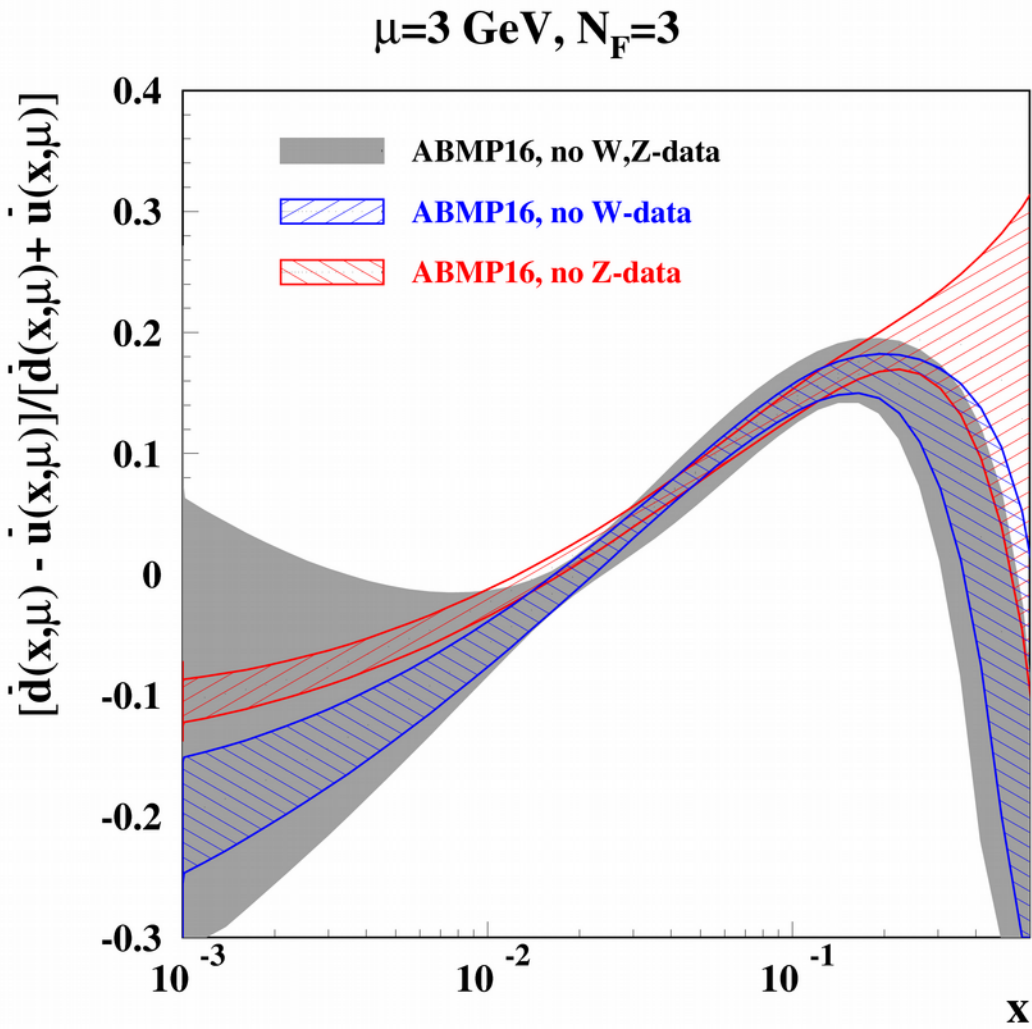
$\mathbf{P}_0 \pm \Delta\mathbf{P}_0$  – vector of PDF parameters with errors obtained in the earlier fit

$\mathbf{E}$  – error matrix

$\mathbf{P}$  – current value of the PDF parameters in the fit

- store the DY NNLO c.s. for all PDF sets defined by the eigenvectors of  $\mathbf{E}$
- the variation of the fitted PDF parameters ( $\mathbf{P} - \mathbf{P}_0$ ) is transformed into this eigenvector basis
- the NNLO c.s. in the PDF fit is calculated as a combination of transformed ( $\mathbf{P} - \mathbf{P}_0$ ) with the stored eigenvector values

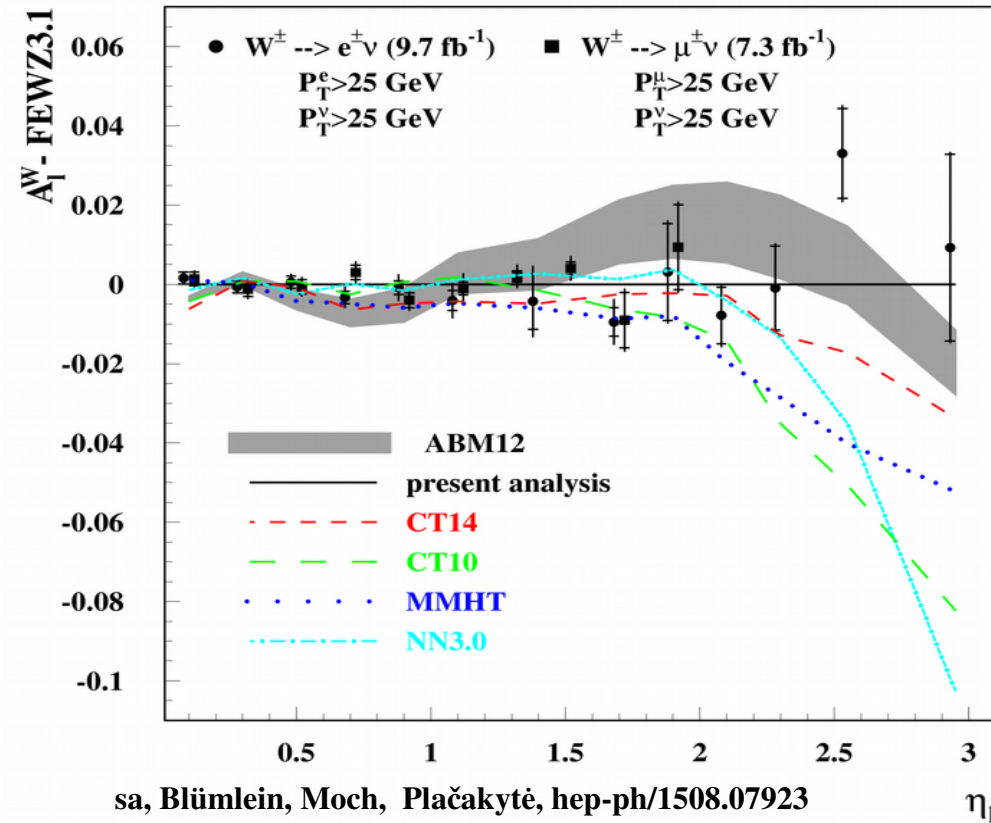
# Impact of the W-, Z-data



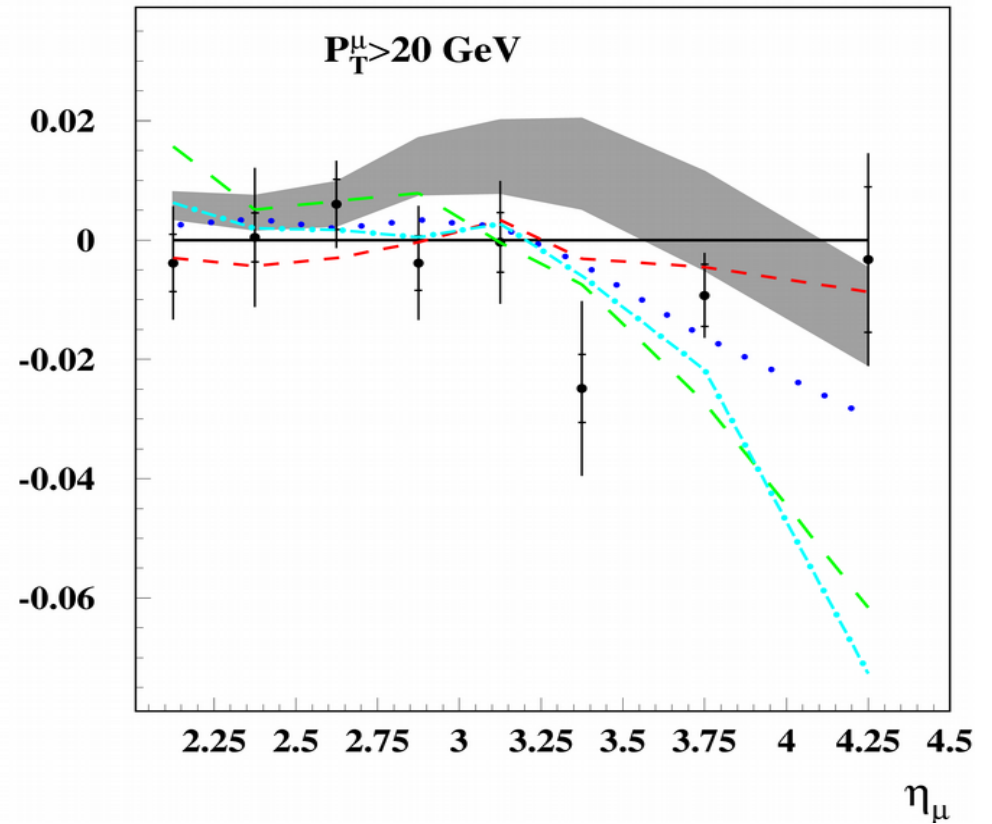


# DY at large rapidity

D0 (1.96 TeV)



LHCb (7 TeV,  $1 \text{ fb}^{-1}$ )



- The data can be evidently used for consolidation of the PDFs, however, unification of the theoretical accuracy is also needed

ABM

Interpolation of accurate NNLO grid (a la FASTNLO)

CT

NNLL (ResBos)

MMHT

NLO + NNLO K-factor

NNPDF

NLO + NNLO C-factors (y-dependent K-factors)

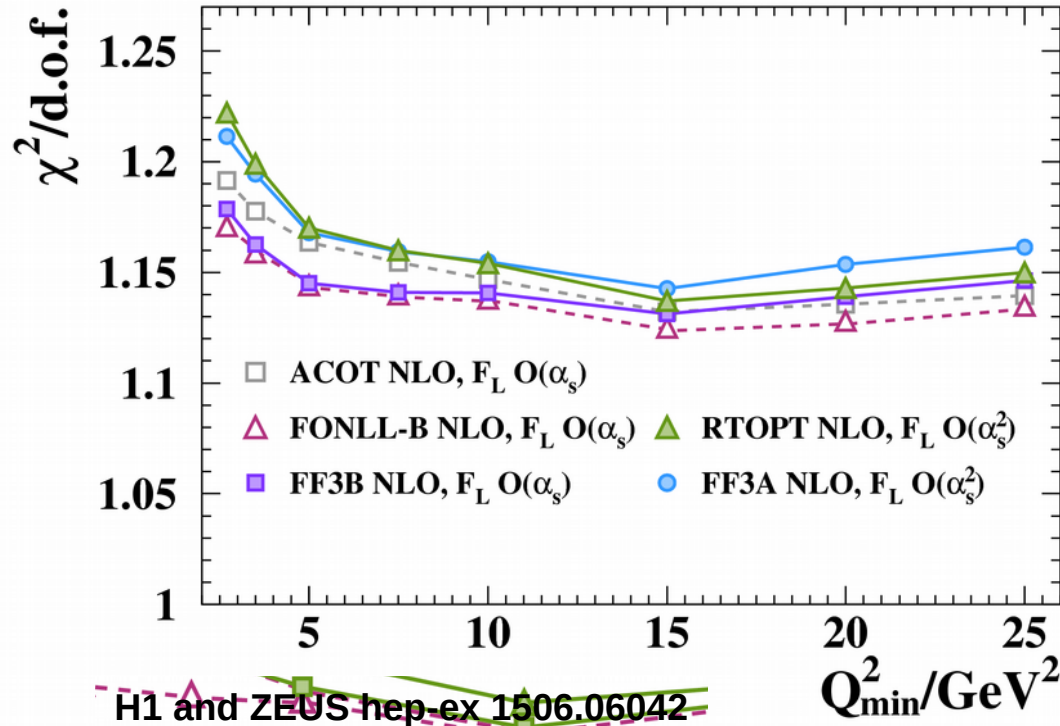
PDF sets	$m_c$ [GeV]	$m_c$ renorm. scheme	theory method ( $F_2^c$ scheme)	theory accuracy for heavy quark DIS Wilson coeff.	$\chi^2$ /NDP for HERA data [127] with xFitter [128, 129]	
ABM12 [2] <sup>a</sup>	$1.24^{+0.05}_{-0.03}$	$\overline{\text{MS}}$ $m_c(m_c)$	FFNS ( $n_f = 3$ )	NNLO <sub>approx</sub>	65/52	66/52
CJ15 [1]	1.3	$m_c^{\text{pole}}$	SACOT [122]	NLO	117/52	117/52
CT14 [3] <sup>b</sup>						
(NLO)	1.3	$m_c^{\text{pole}}$	SACOT( $\chi$ ) [123]	NLO	51/47	70/47
(NNLO)	1.3	$m_c^{\text{pole}}$	SACOT( $\chi$ ) [123]	NLO	64/47	130/47
HERAPDF2.0 [4]						
(NLO)	1.47	$m_c^{\text{pole}}$	RT optimal [125]	NLO	67/52	67/52
(NNLO)	1.43	$m_c^{\text{pole}}$	RT optimal [125]	NLO	62/52	62/52
JR14 [5] <sup>c</sup>	1.3	$\overline{\text{MS}}$ $m_c(m_c)$	FFNS ( $n_f = 3$ )	NNLO <sub>approx</sub>	62/52	62/52
MMHT 14 [6]						
(NLO)	1.4	$m_c^{\text{pole}}$	RT optimal [125]	NLO	72/52	78/52
(NNLO)	1.4	$m_c^{\text{pole}}$	RT optimal [125]	NLO	71/52	83/52
NNPDF3.0 [7]						
(NLO)	1.275	$m_c^{\text{pole}}$	FONLL-B [124]	NLO	58/52	60/52
(NNLO)	1.275	$m_c^{\text{pole}}$	FONLL-C [124]	NLO	67/52	69/52
PDF4LHC15 [8] <sup>d</sup>	–	–	FONLL-B [124]	–	58/52	64/52
	–	–	RT optimal [125]	–	71/52	75/52
	–	–	SACOT( $\chi$ ) [123]	–	51/47	76/47

*No advantage of the GMVFN schemes: the VFN  $\chi^2$  values are systematically bigger than the FFN ones*

Accardi, et al. hep-ph/1603.08906

# Factorization scheme benchmarking

## H1 and ZEUS



- Data allow to discriminate factorization schemes
- FFN scheme works very well in case of correct setting (running mass definition and correct value of  $m_c$ ) → no traces of big logs due to resummation

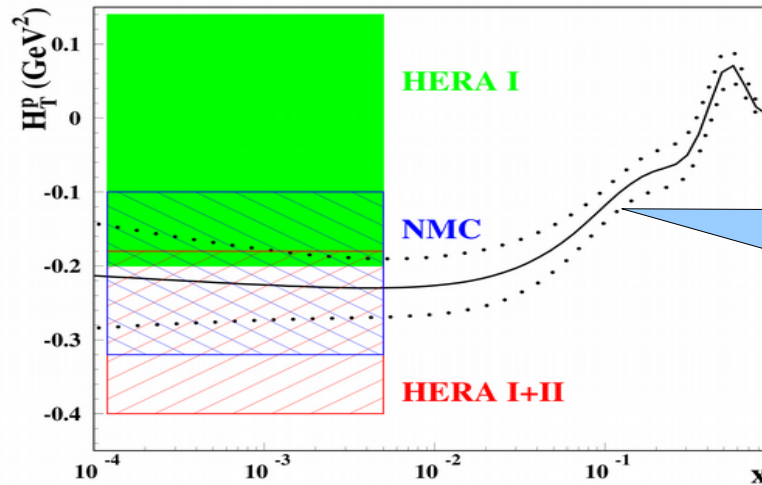
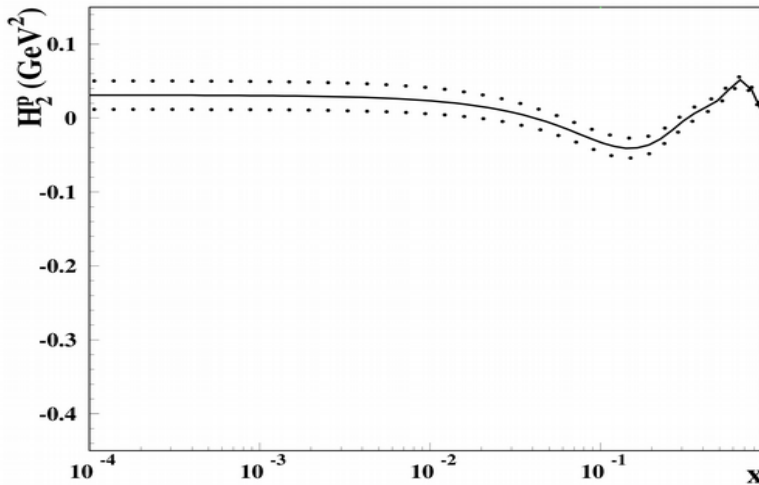
$x_{\min}$	$x_{\max}$	$Q_{\min}^2$ (GeV)	$Q_{\max}^2$ (GeV)	$\Delta\chi^2$ (DIS)	$N_{\text{dat}}^{\text{DIS}}$	$\Delta\chi^2$ (HERA-I)	$N_{\text{dat}}^{\text{hera-I}}$
$4 \cdot 10^{-5}$	1	3	$10^6$	72.2	2936	77.1	592
$4 \cdot 10^{-5}$	0.1	3	$10^6$	87.1	1055	67.8	405
$4 \cdot 10^{-5}$	0.01	3	$10^6$	40.9	422	17.8	202
$4 \cdot 10^{-5}$	1	10	$10^6$	53.6	2109	76.4	537
$4 \cdot 10^{-5}$	1	100	$10^6$	91.4	620	97.7	412
$4 \cdot 10^{-5}$	0.1	10	$10^6$	84.9	583	67.4	350
$4 \cdot 10^{-5}$	0.1	100	$10^6$	87.7	321	87.1	227

We conclude that the FFN fit is actually based on a less precise theory, in that it does not include full resummation of the contribution of heavy quarks to perturbative PDF evolution, and thus provides a less accurate description of the data

# High twists at small x

$$F_{2,L} = F_{2,L}(\text{leading twist}) + H_{2,L}(x)/Q^2$$

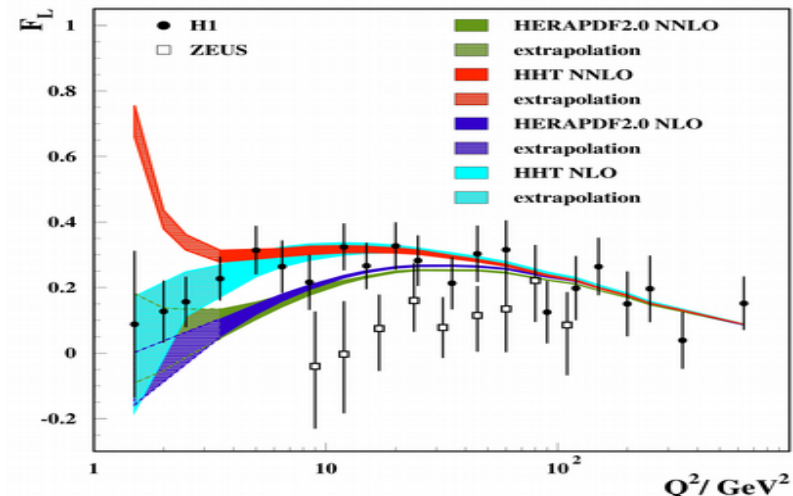
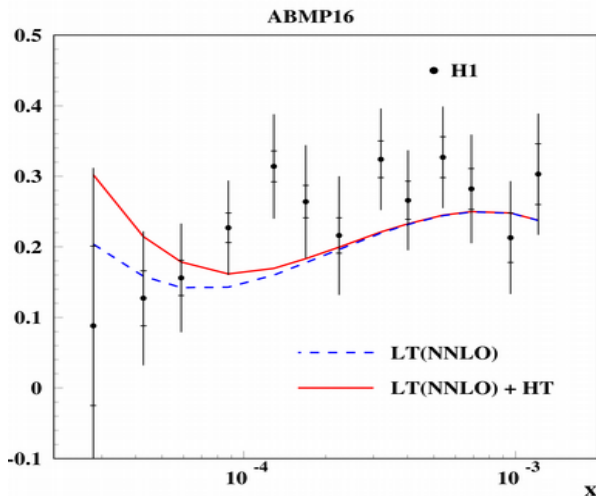
$$H(x) = x^h P(x)$$



Controlled by  
SLAC and NMC  
data

sa, Blümlein, Moch  
PRD 86, 054009 (2012)

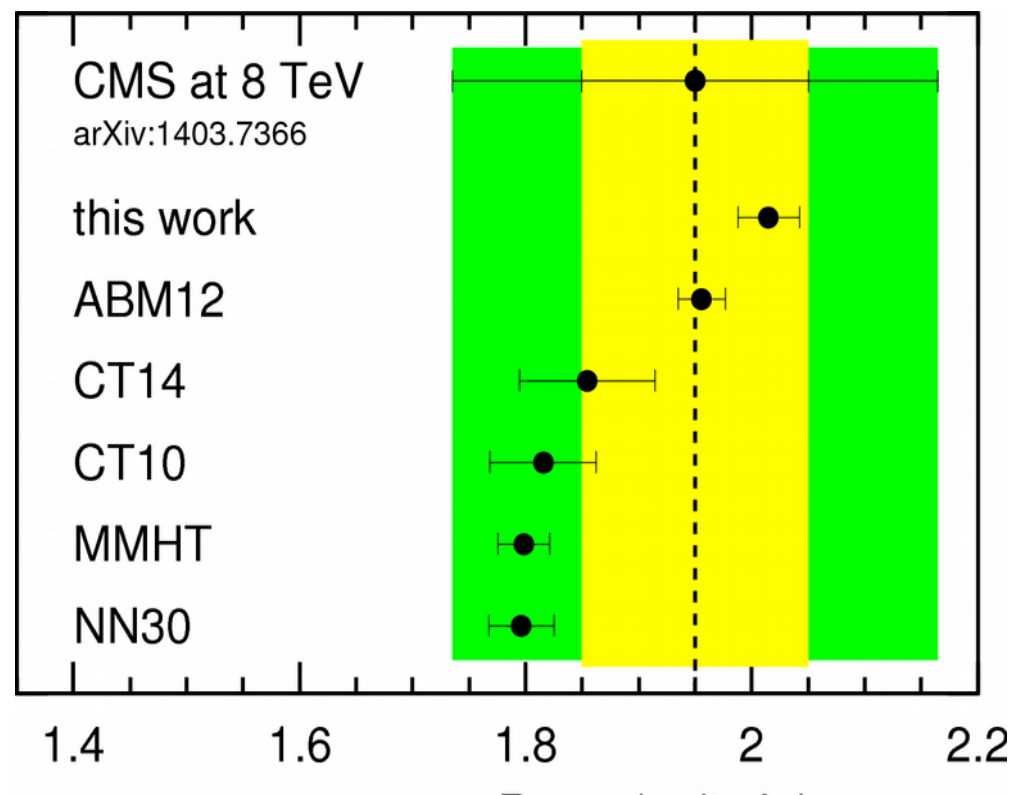
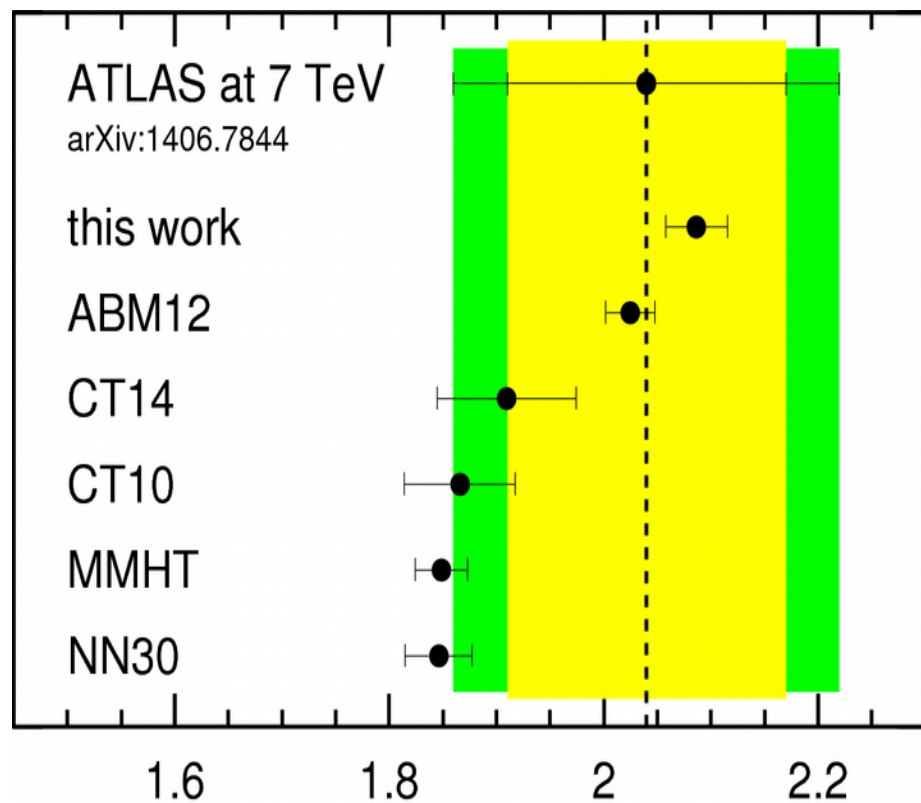
- $H_T(x)$  continues a trend observed at larger  $x$ ;  $H_2(x)$  is comparable to 0 at small  $x$
  - $h_T = 0.05 \pm 0.07 \rightarrow$  slow vanishing at  $x \rightarrow 0$
  - $\Delta\chi^2 \sim -40$
- Harland-Lang, Martin, Motylinski, Thorne hep-ph/1601.03413



No dramatic increase of  $F_L$  at small  $x$

Abt, et al. hep-ex/1604.02299

# Implication for(of) the single-top production



$$R_t = \sigma_t / \sigma_{\bar{t}} \text{ (t-ch.) } \text{ sa, Blümlein, Moch, Plačákytė hep-ph/1508.07923}$$

$$R_t = \sigma_t / \sigma_{\bar{t}} \text{ (t-ch.)}$$

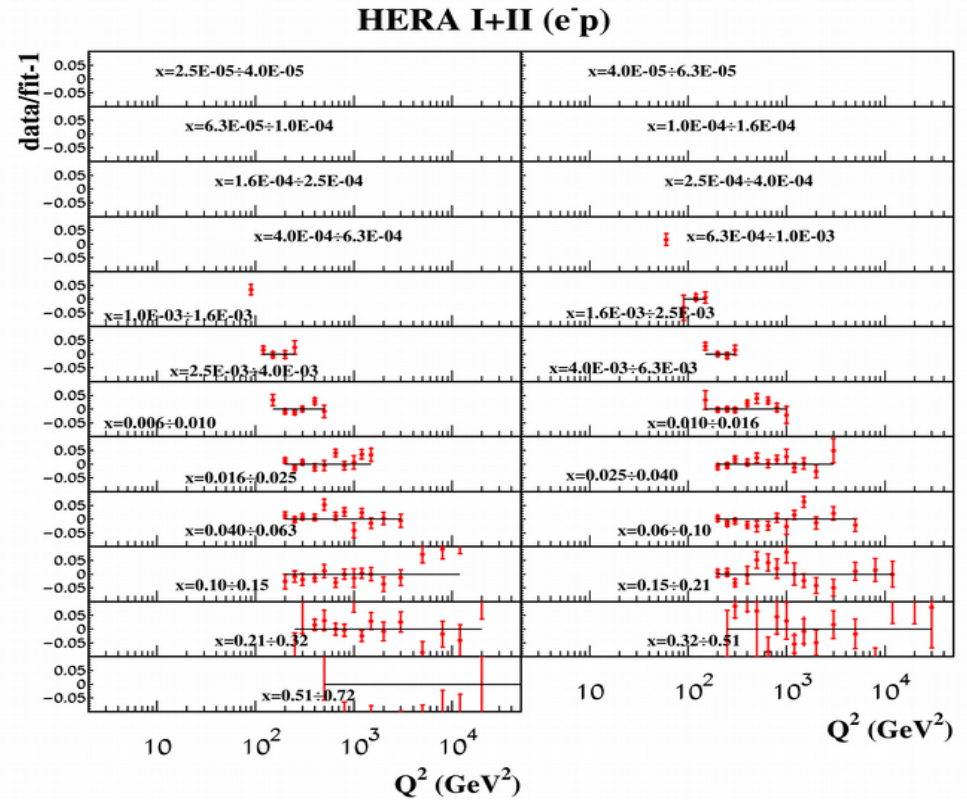
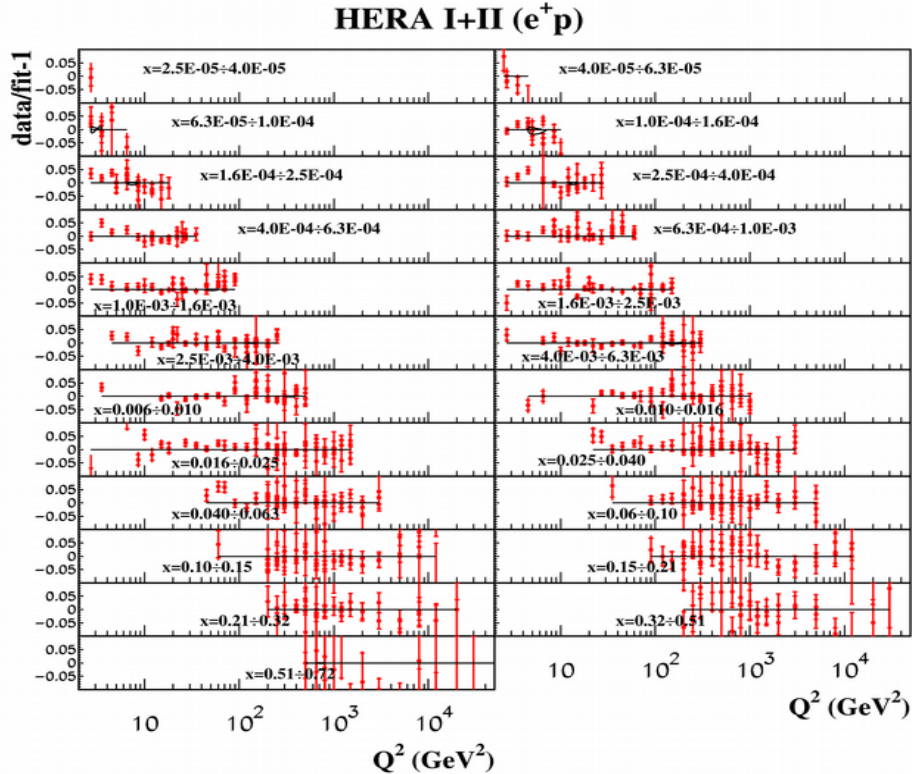
- ATLAS and CMS data on the ratio  $t/\bar{t}$  are in a good agreement
- The predictions driven by the forward DY data are in a good agreement with the single-top data (N.B.: ABM12 is based on the deuteron data → consistent deuteron correction was used) talks by Petti at DIS2016

*Single-top production discriminate available PDF sets and can serve as a standard candle process*

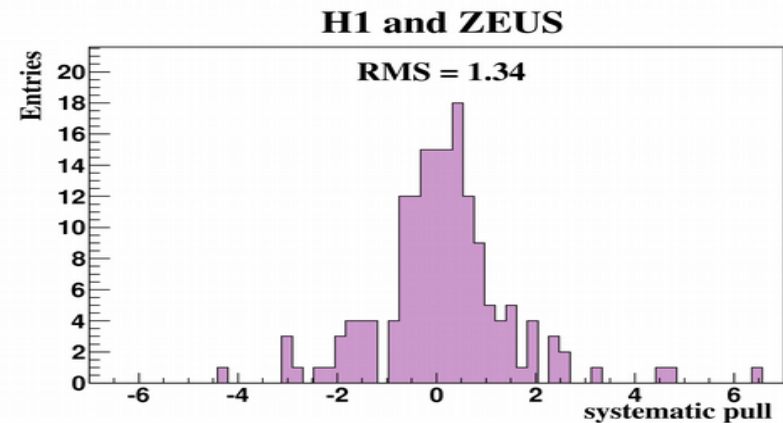


# Inclusive HERA I+II data

H1 and ZEUS hep-ex/1506.06042



$Q^2$ (HERA)	$\chi^2$ /NDP(HERA)
$>2.5 \text{ GeV}^2$	$1509/1168=1.29$
$>5 \text{ GeV}^2$	$1354/1092=1.24$
$>10 \text{ GeV}^2$	$1228/1007=1.22$

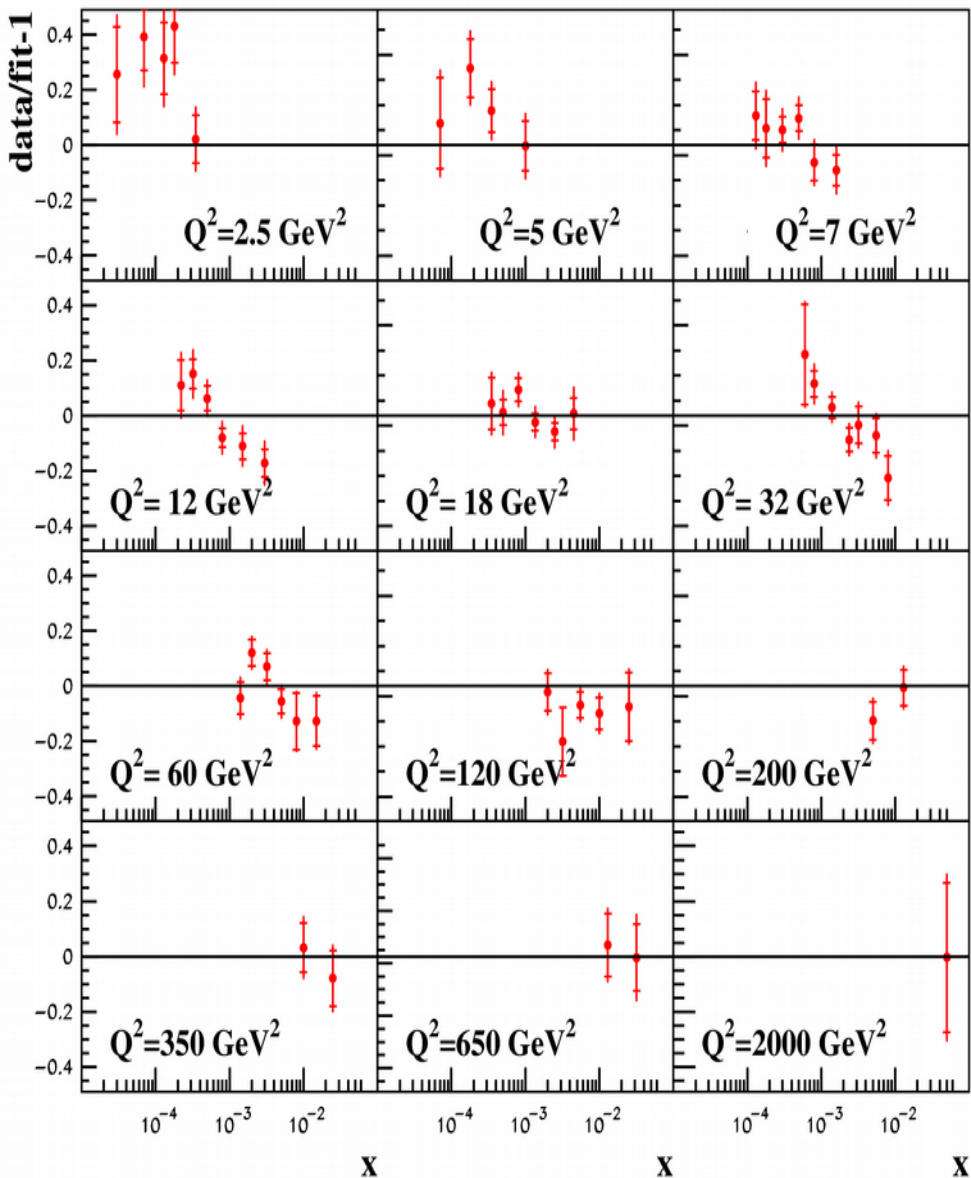


The value of  $\chi^2$ /NDP is bigger than 1, however still comparable to the pull distribution width

# HERA charm data and $m_c(m_c)$

H1/ZEUS ZPC 73, 2311 (2013)

HERA I+II (ep  $\rightarrow$  e charm X)



$m_c(m_c) = 1.246 \pm 0.023$  (h.o.) GeV NNLO

Kiyo, Mishima, Sumino hep-ph/1510.07072

- Approximate NNLO massive Wilson coefficients (combination of the threshold corrections, high-energy limit, and the NNLO massive OMEs)

Kawamura, Lo Presti, Moch, Vogt NPB 864, 399 (2012)

Update with the pure singlet massive OMEs

Ablinger et al. NPB 890. 48 (2014)

$\rightarrow$  improved theoretical uncertainties

- Running-mass definition of  $m_c$

$X^2/NDP = 66/52$

$m_c(m_c) = 1.252 \pm 0.018$  (exp.) GeV

ABMP16

$m_c(m_c) = 1.24 \pm 0.03$  (exp.) GeV

ABM12

- RT optimal

$X^2/NDP = 82/52$

$m_c(\text{pole}) = 1.25$  GeV

NNLO

~~MMHT14 EPJC 75, 204 (2015)~~

- FONLL

$X^2/NDP = 60/47$

$m_c(\text{pole}) = 1.275$  GeV

NNLO

~~NNPDF3.0 JHEP 1504, 040 (2015)~~

- S-ACOT- $\chi$

$X^2/NDP = 59/47$

$m_c(\text{pole}) = 1.3$  GeV

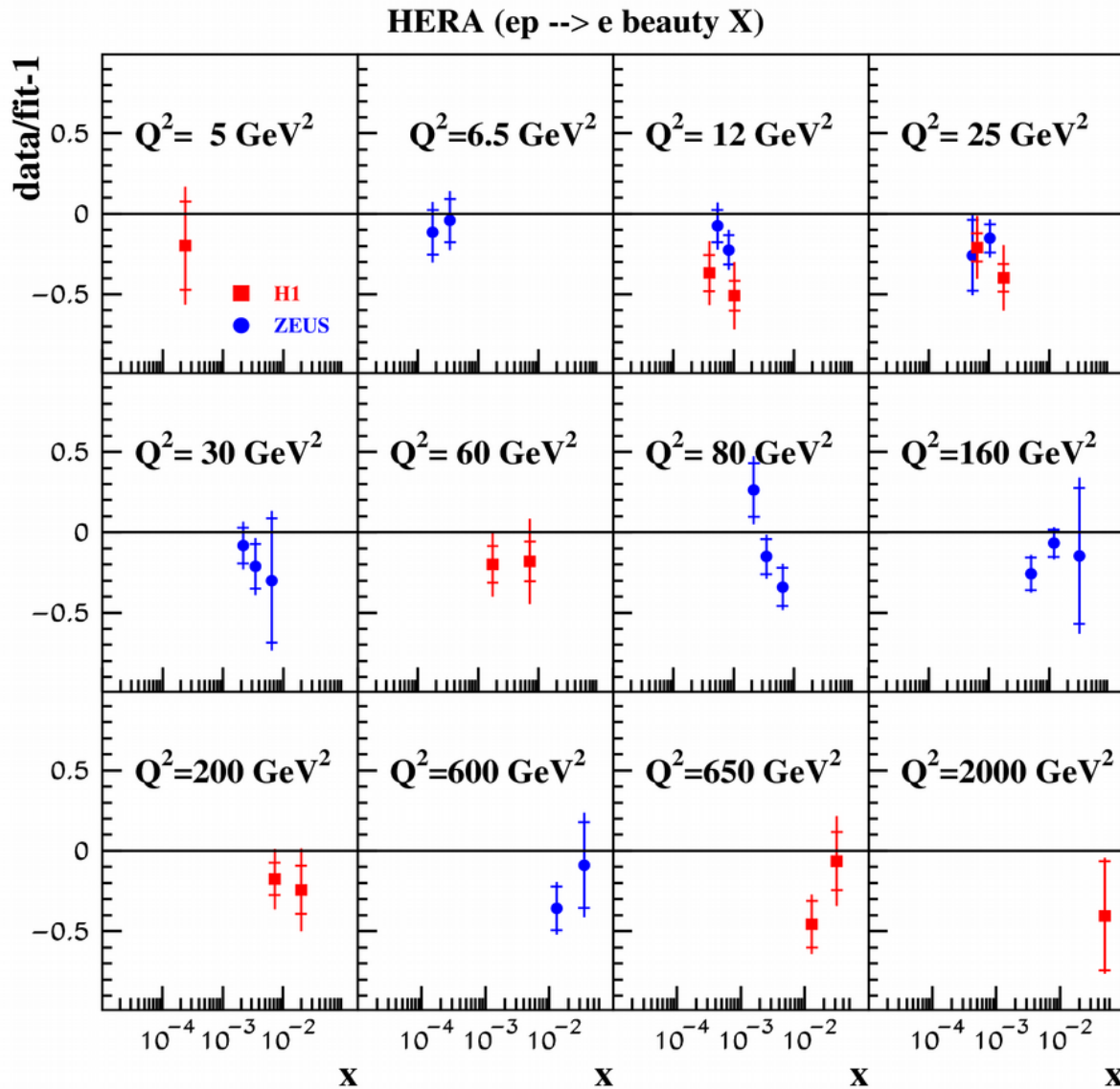
NNLO

~~CT14 hep-ph 1506.07443~~

Accardi, et al. hep-ph/1603.08906



# HERA bottom data and $m_b(m_b)$



ZEUS JHEP 1409, 127 (2014)

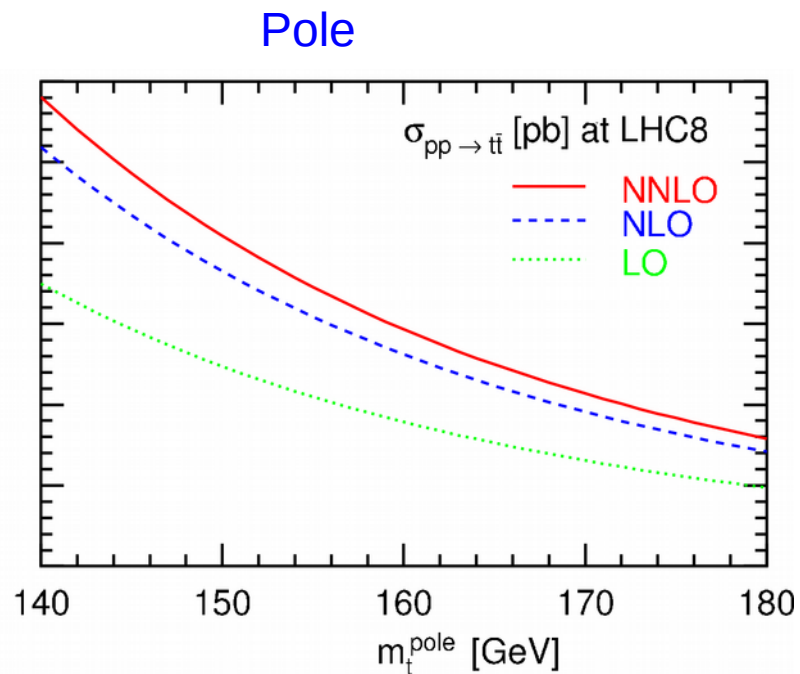
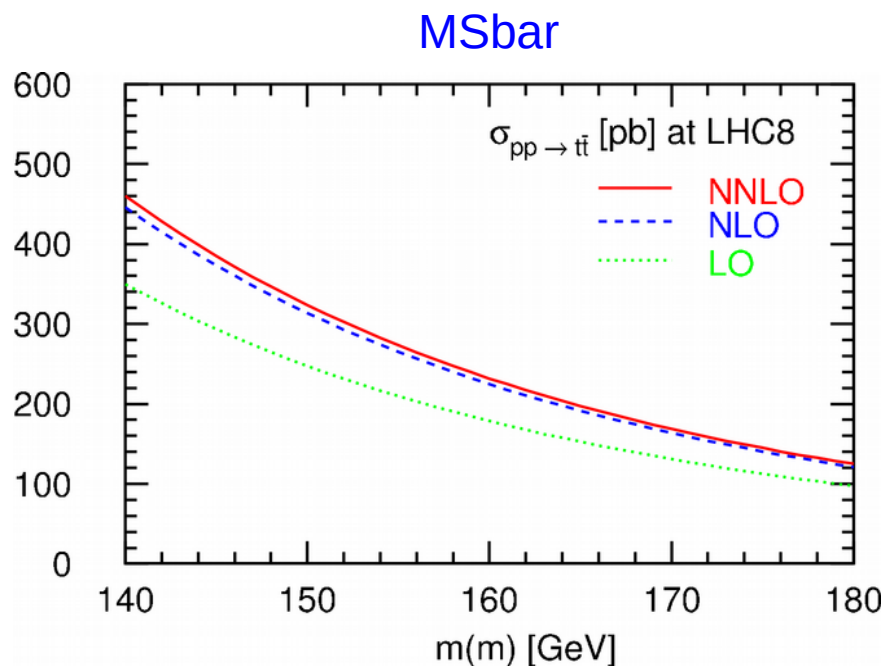
$$\chi^2/\text{NDP} = 16/17$$

H1 EPJC 65, 89 (2010)

$$\chi^2/\text{NDP} = 5/12$$

$$m_b(m_b) = 3.83 \pm 0.12 (\text{exp.}) \text{ GeV}$$

# ttbar production with pole and $\overline{MS}$ mass

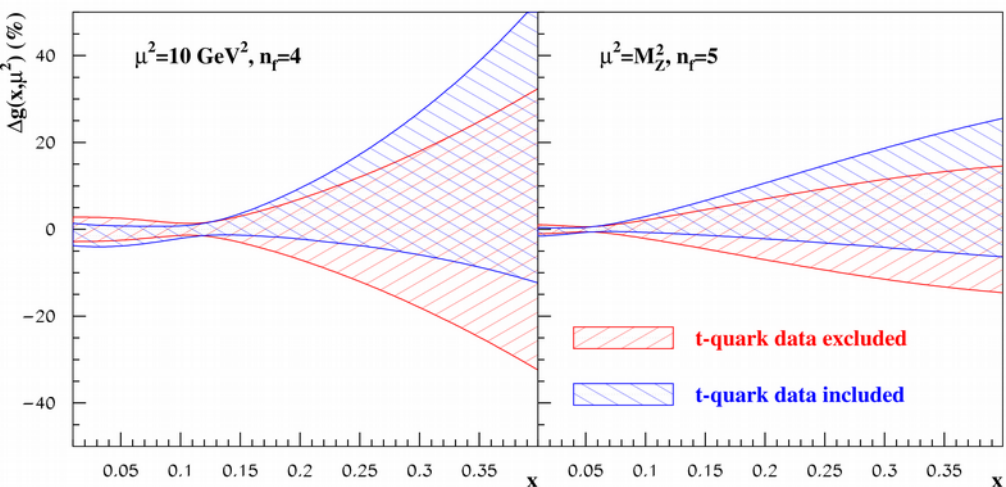


**HATHOR** (NNLO terms are checked with TOP++)

Langenfeld, Moch, Uwer PRD 80, 054009 (2009)

*Running mass definition provides nice perturbative stability*

Czakon, Fiedler, Mitov hep-ph/1303.6254



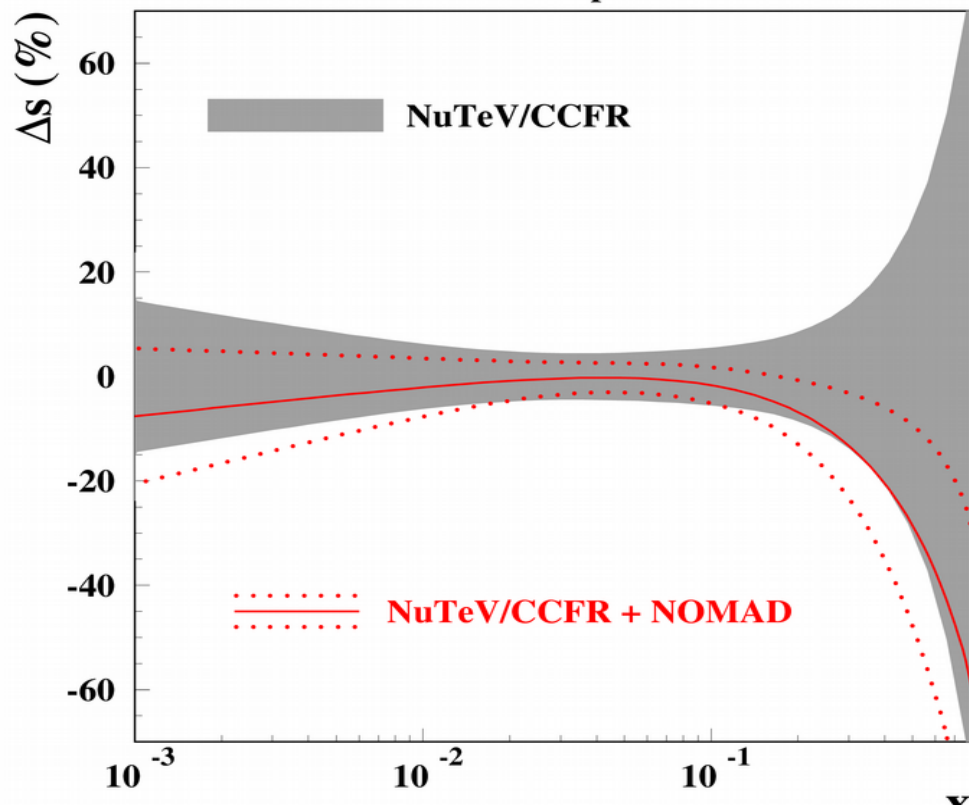
•  $m_t(m_t) = 160.9 \pm 1.1$  (exp.) GeV      NNLO

•  $\alpha_s(M_Z) = 0.1145(9) \rightarrow 0.1147(8)$       NNLO

• moderate change in the large- $x$  gluon distribution

# NOMAD charm data

$\mu=3 \text{ GeV}, n_f=3$



The data on ratio  $2\mu/\text{incl. CC ratio}$  with the  $2\mu$  statistics of 15000 events (much bigger than in earlier CCFR and NuTeV samples).

NOMAD NPB 876, 339 (2013)

Systematics, nuclear corrections, etc. cancel in the ratio

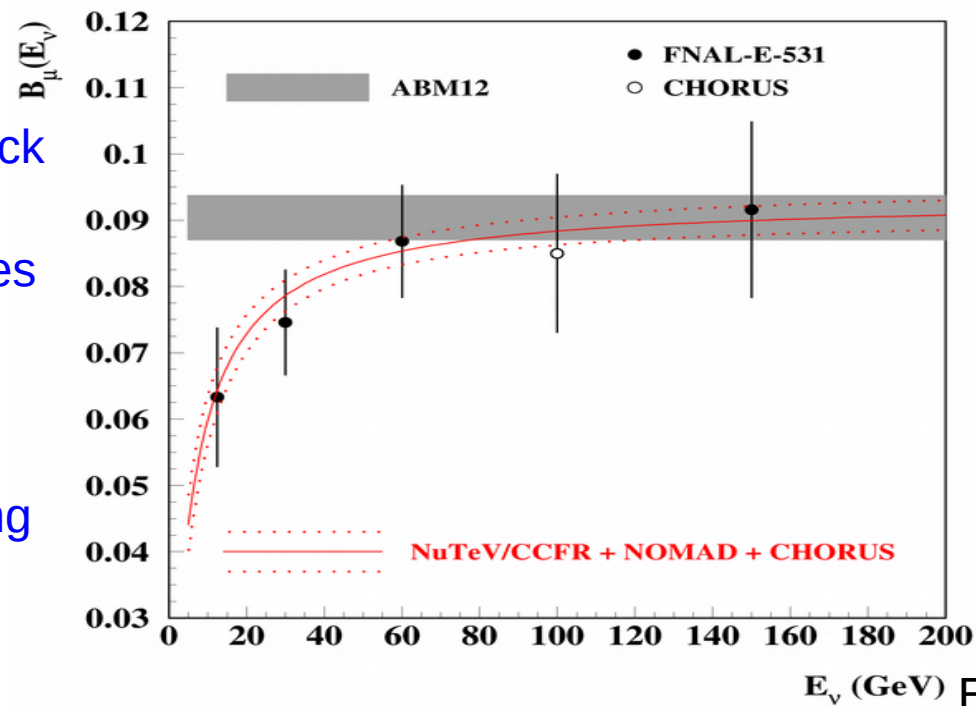
- pull down strange quarks at  $x > 0.1$  with a sizable uncertainty reduction
- $m_c(m_c) = 1.23 \pm 0.03(\text{exp.}) \text{ GeV}$  is comparable to the ABM12 value

The semi-leptonic branching ratio  $B_\mu$  is a bottleneck

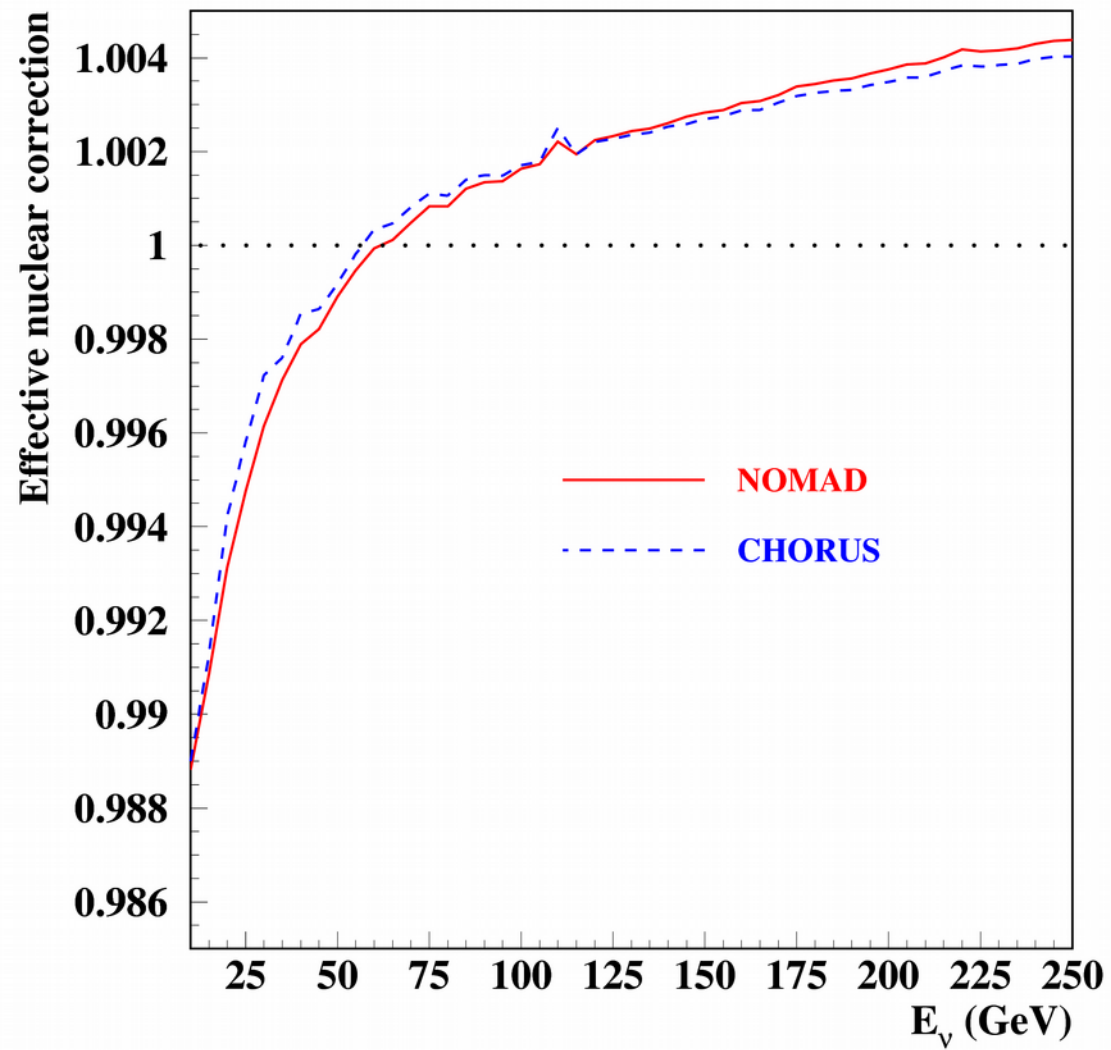
- weighted average of the charmed-hadron rates

$$B_\mu(E_\nu) = \sum_h r^h(E_\nu) B^h = a / (1 + b/E_\nu)$$

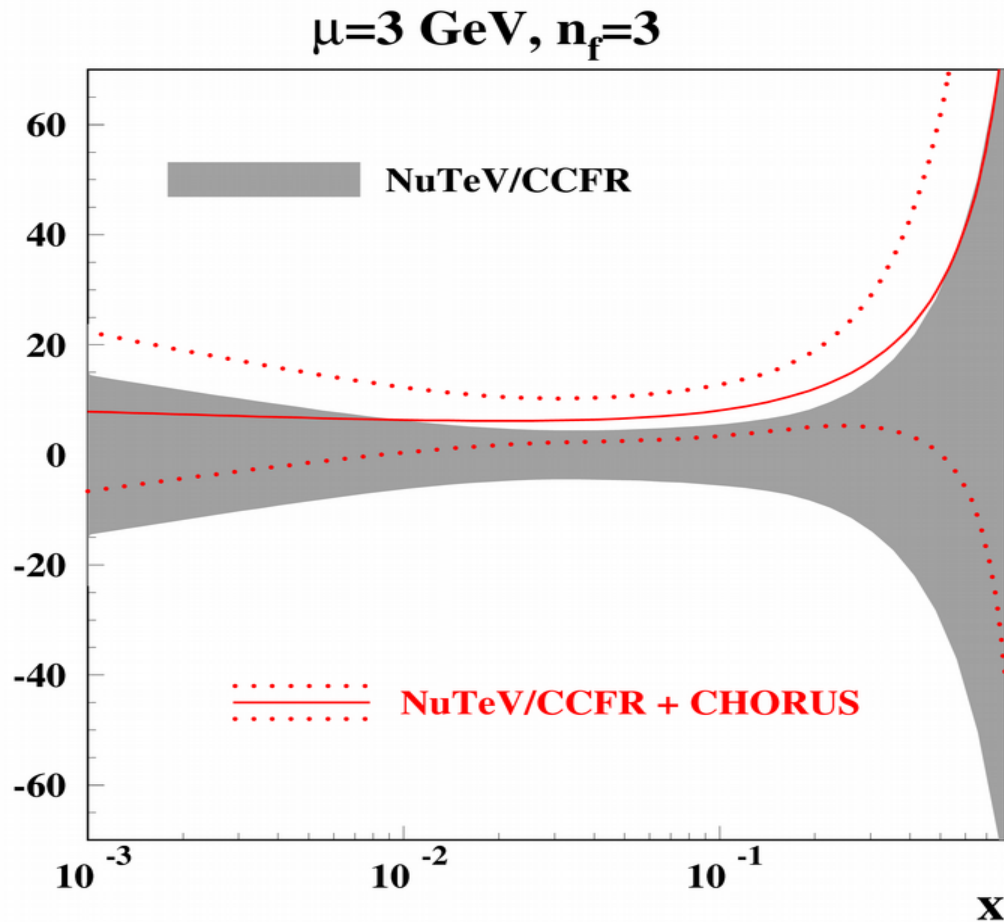
- fitted simultaneously with the PDFs, etc. using the constraint from the emulsion data



sa, Blümlein, Caminadac, Lipka, Lohwasser, Moch, Petti, Placakyte hep-ph/1404.6469



# CHORUS charm data

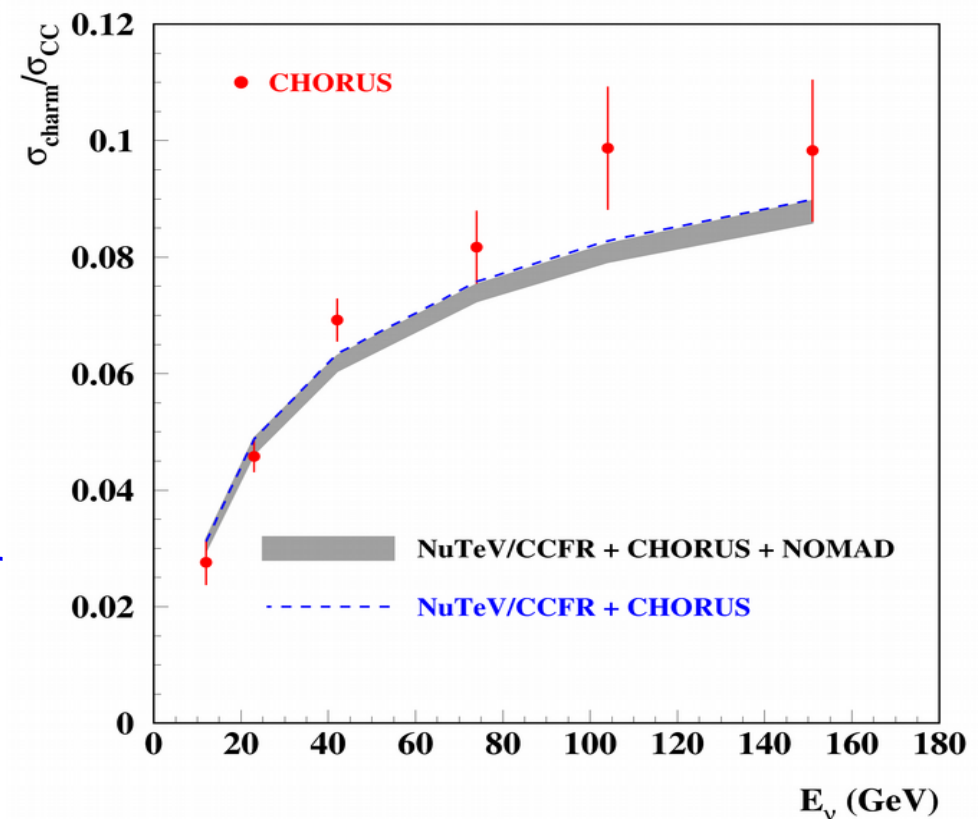


Emulsion data on charm/CC ratio with the charmed hadron vertex measured

CHORUS NJP 13, 093002 (2011)

- full phase space measurements
- no sensitivity to  $B_\mu$
- low statistics (2013 events)

CHORUS data pull strangeness up, however the statistical significance of the effect is poor

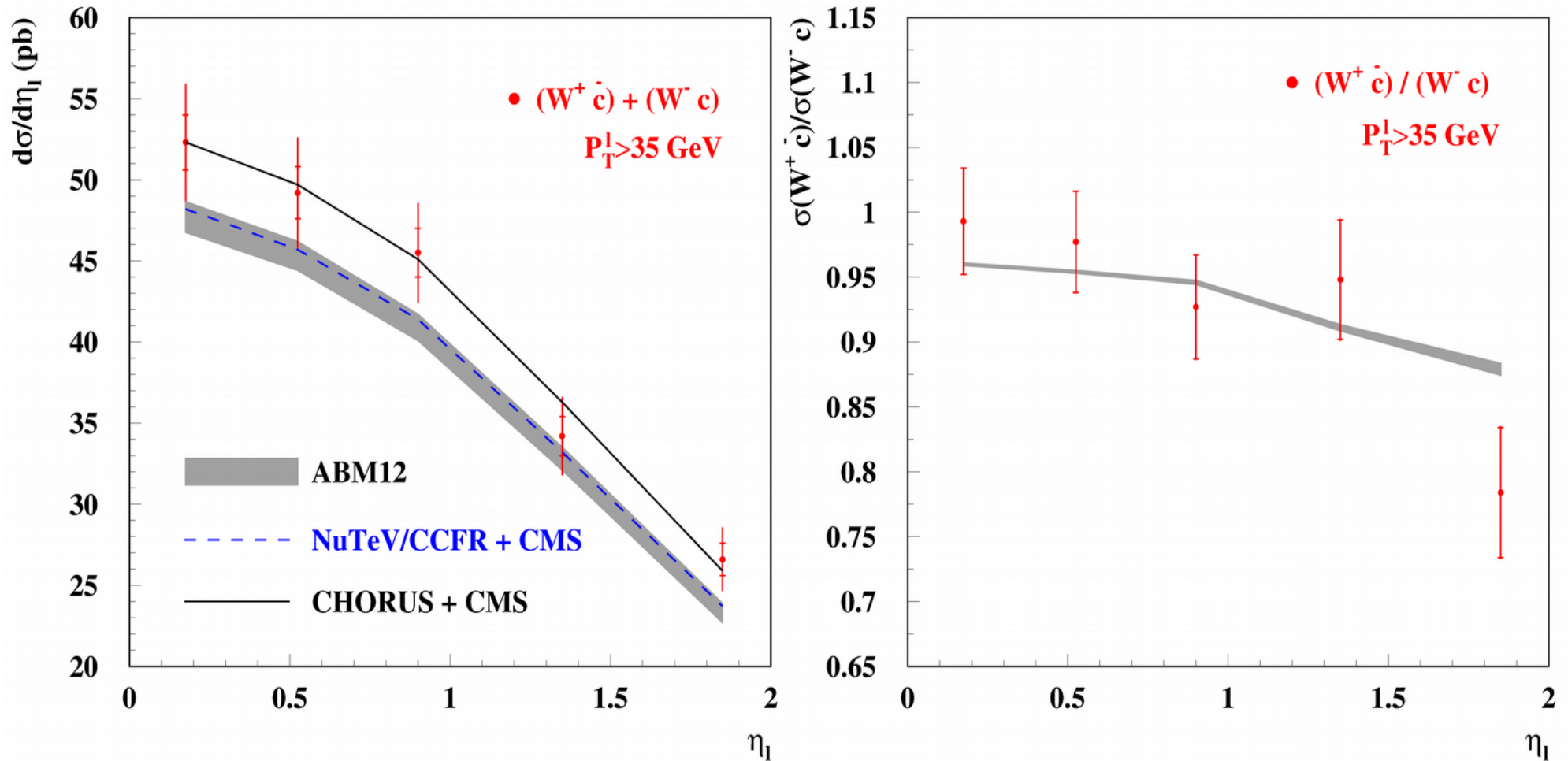


sa, Blümlein, Caminadac, Lipka, Lohwasser,  
 Moch, Petti, Placakyte hep-ph/1404.6469

# CMS W+charm data

CMS Collaboration JHEP 02, 013 (2014)

CMS (7 TeV, 5 1/fb)

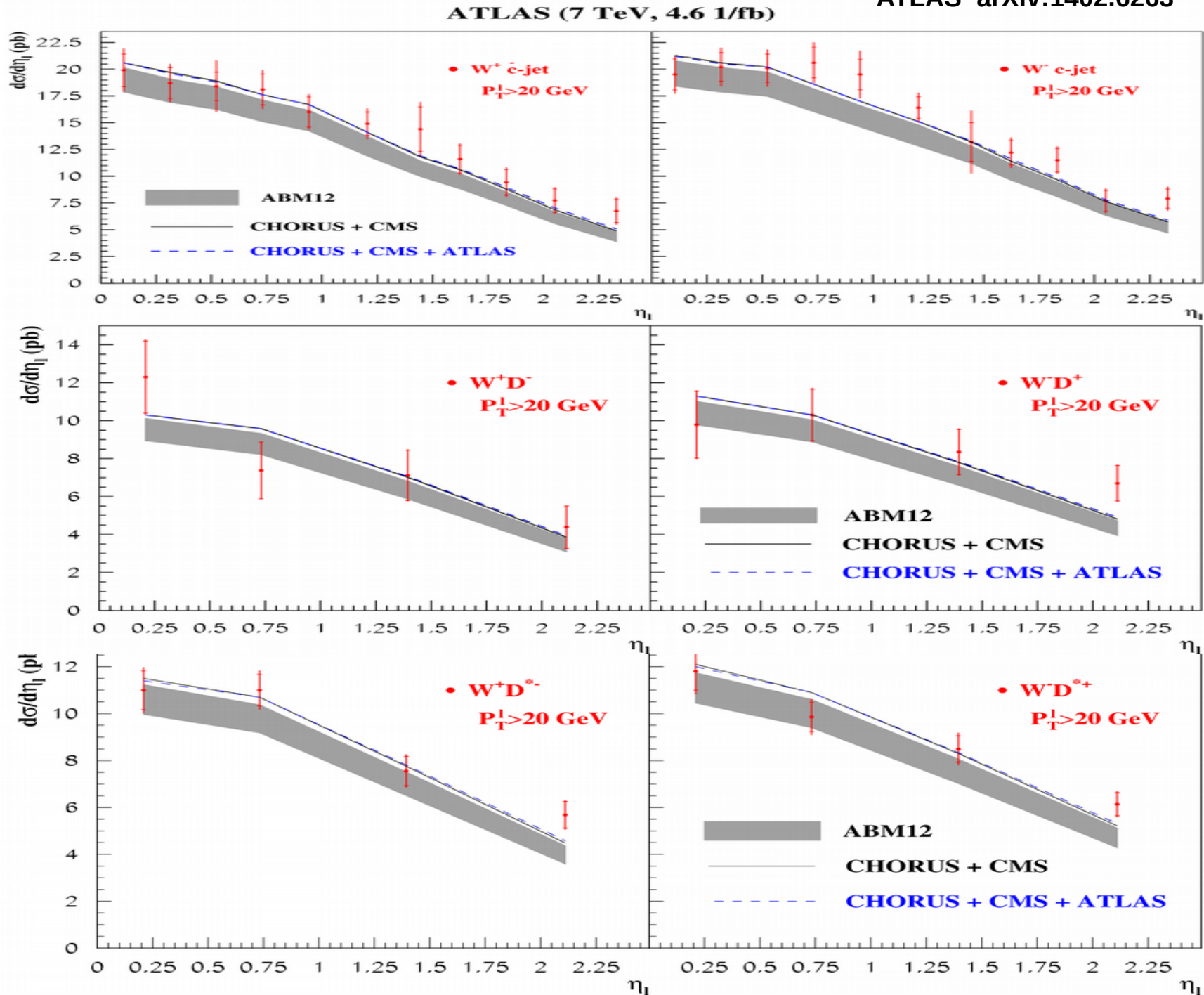


- CMS data go above the NuTeV/CCFR by  $1\sigma$ ; little impact on the strange sea
- The charge asymmetry is in a good agreement with the charge-symmetric strange sea
- Good agreement with the CHORUS data



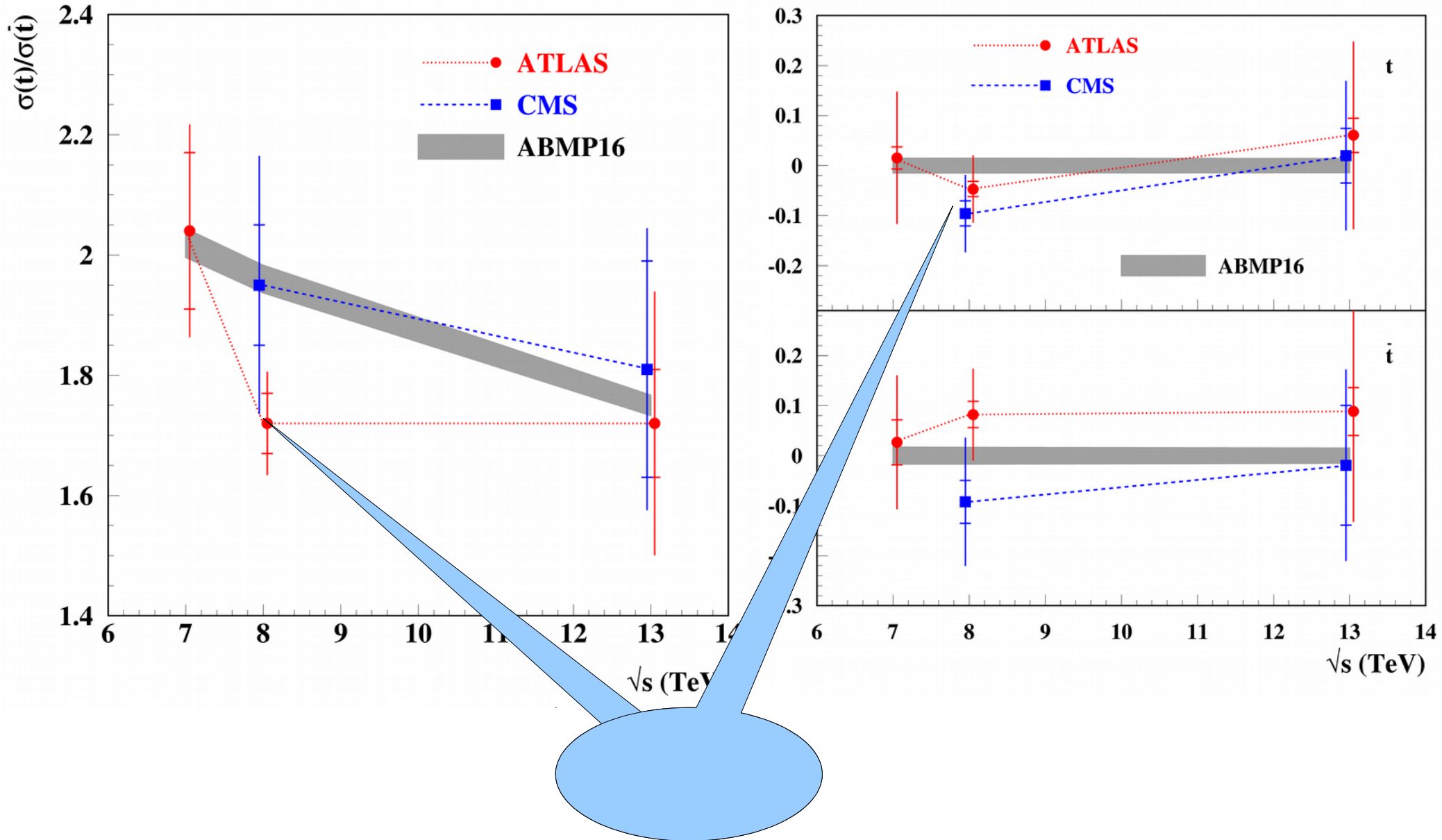
# ATLAS W+charm data

ATLAS arXiv:1402.6263

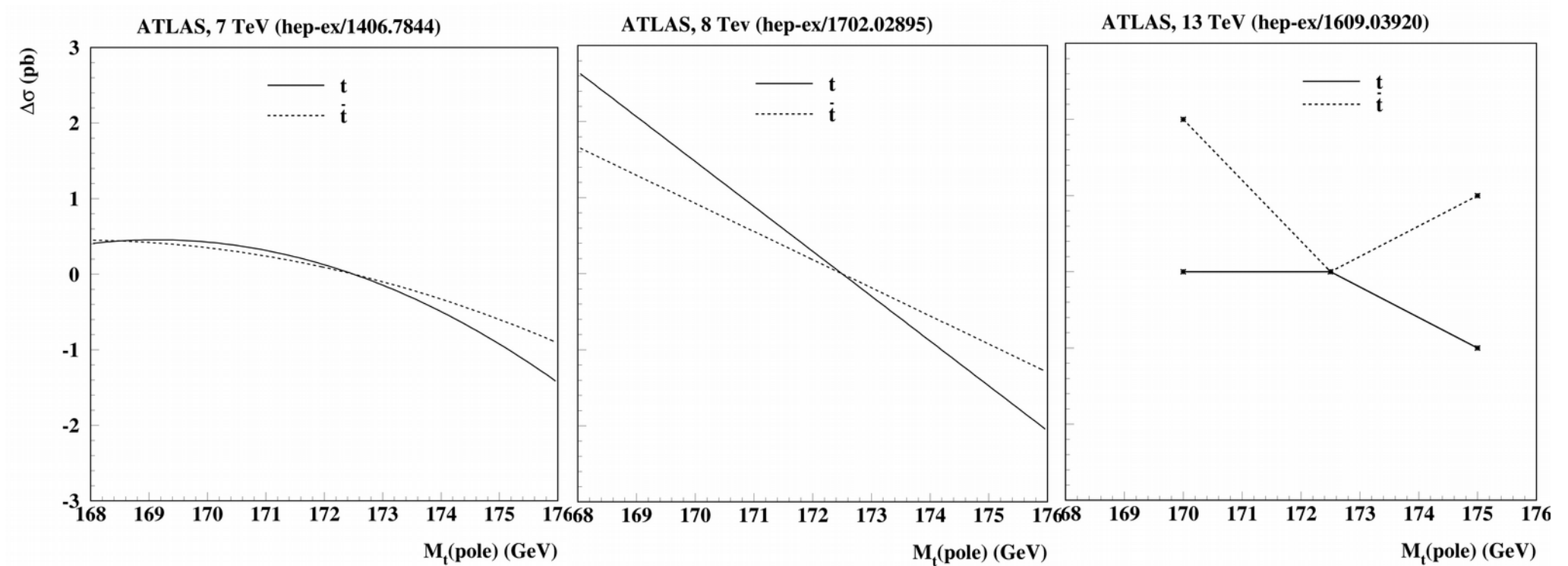




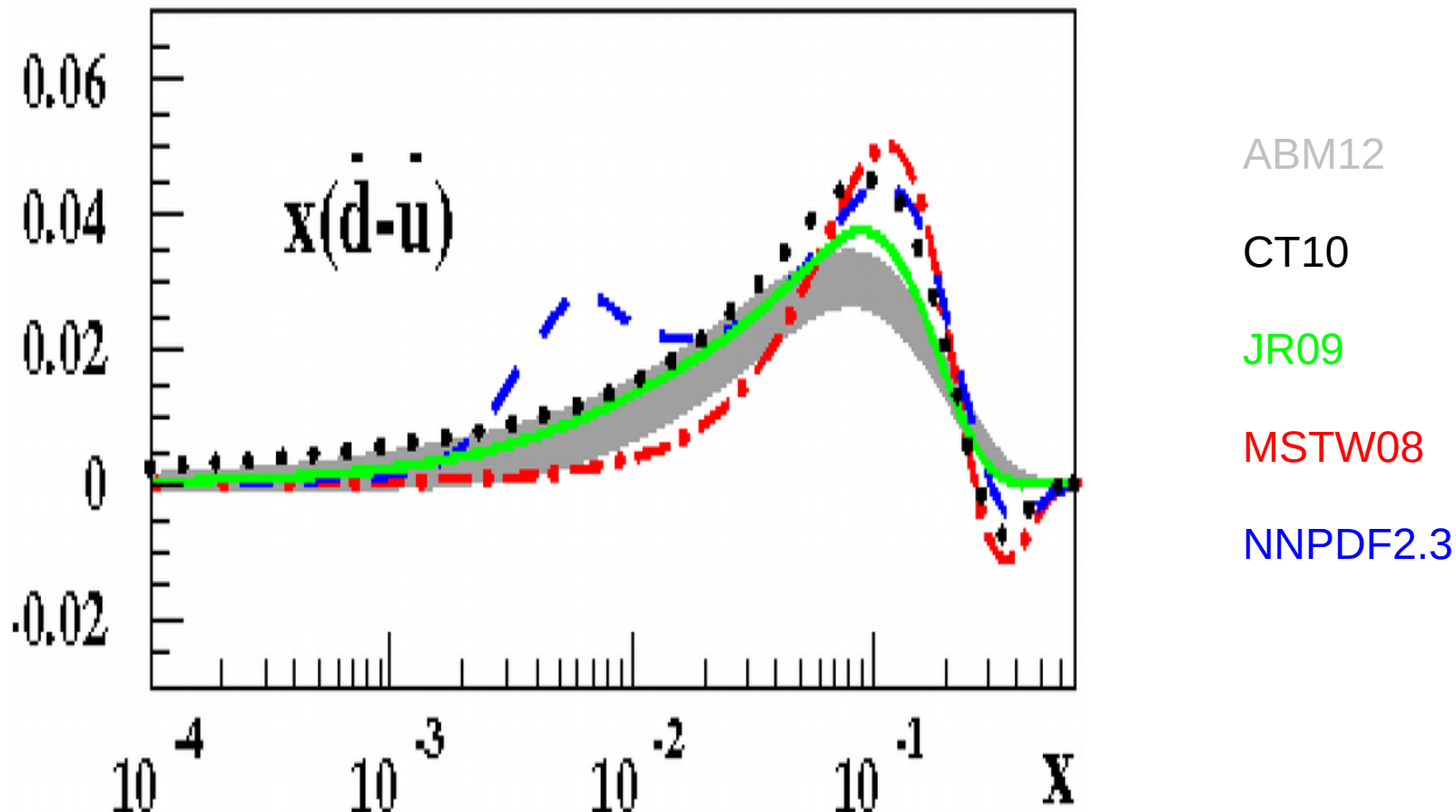
# Single-top: s.c.m. energy dependence



# Single-top: mass dependence



# Sea quark iso-spin asymmetry



osä, Blümlein, Moch PRD 89, 054028 (2014) -

- At  $x \sim 0.1$  the sea quark iso-spin asymmetry is controlled by the fixed-target DY data (E-866), weak constraint from the DIS (NMC)
- At  $x < 0.01$  Regge-like constraint like  $x^{(a-1)}$ , with a close to the meson trajectory intercept; the “unbiased” NNPDF fit follows the same trend

*Onset of the Regge asymptotics is out of control*