



U.S. DEPARTMENT OF  
**ENERGY**

Office of  
Science

# *On “Ultimate” Energy Frontier Colliders*

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# “Dream” Collider: Choices

- Far Future “Energy Frontier” assumes

- ❖ 300-1000 TeV (20-100 × LHC)

- ❖ “decent luminosity” (TBD)

- Surely we know:

circular collider

1. For the same reason there is no circular  $e^+e^-$  collider above Higgs-F there will be no circular  $pp$  colliders beyond 100 TeV → LINEAR

$$L \propto \frac{\eta P_{wall}}{E^3} \frac{\xi_y}{\beta_y}$$

2. Electrons radiate 100% **linear collider** *beam-strahlung* (<3 TeV) and in focusing channel (<10 TeV) →  $\mu^+\mu^-$  or  $pp$

$$L \propto \frac{\eta_{linac} P_{wall}}{E} \frac{N_\gamma}{\sigma_y}$$

# “Phase-Space” is Further Limited

- “Cost Feasibility”: for 20-100 × LHC

- ❖ < 10 B\$

- ❖ < 10 km

- ❖ < 10 MW (beam power, ~100MW total)

→ New technology should provide **>30 GeV/m @**

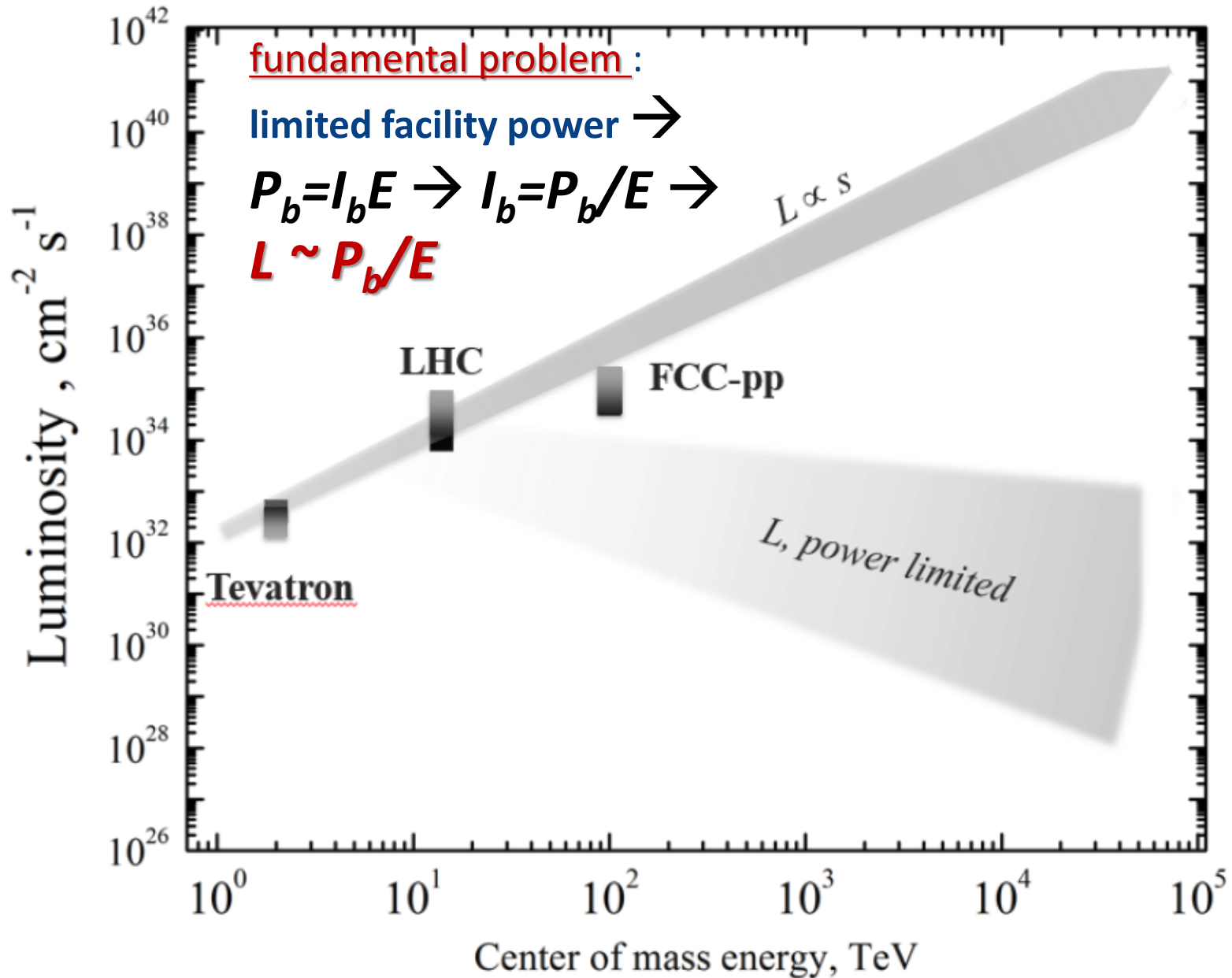
**total component cost <1M\$/m ( ~NC magnets now)**

SC magnets equiv. ~ 0.5 GeV per meter (LHC)

**3. Only one option for >30 GeV/m known now:**

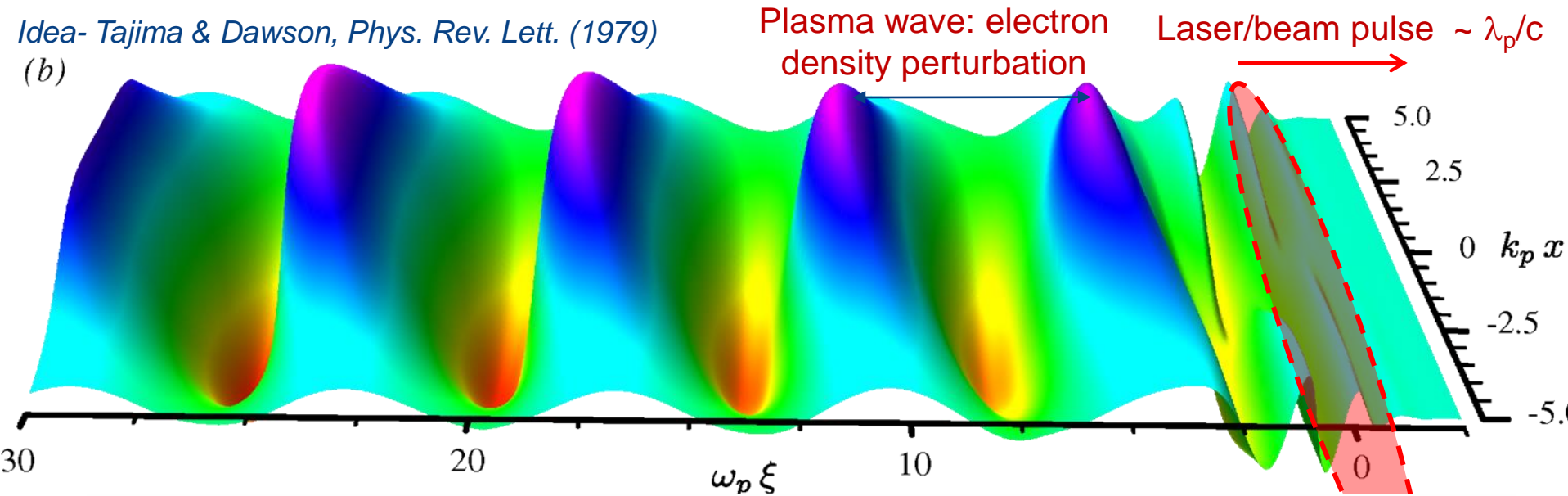
**dense plasma → that excludes *protons* → only muons**

# Paradigm Shift : *Energy vs Luminosity*



# New Technology- Plasma

Idea- Tajima & Dawson, Phys. Rev. Lett. (1979)  
(b)



$$E_0 = \frac{m_e c \omega_p}{e} \approx 100 \left[ \frac{\text{GeV}}{m} \right] \cdot \sqrt{n_0 [10^{18} \text{ cm}^{-3}]}$$

**Option A:**

Short intense e-/e+/p bunch  
Few  $10^{16} \text{ cm}^{-3}$ , **6 GV/m** over 0.3m

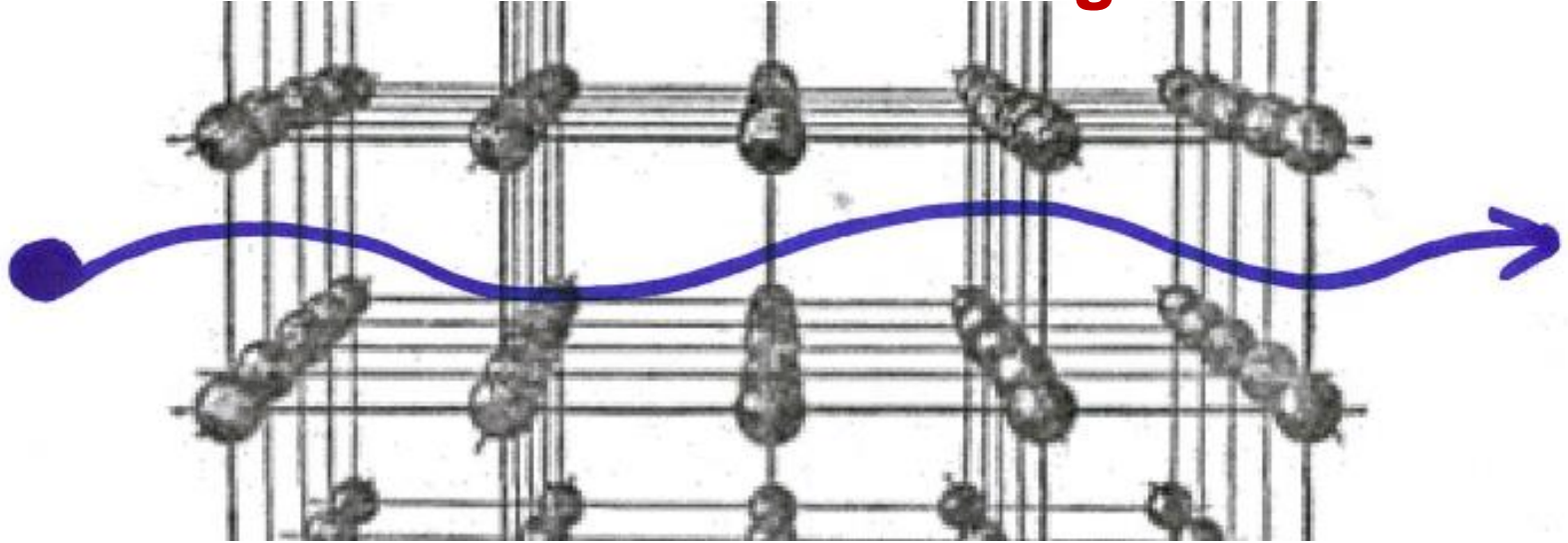
**Option B:**

Short intense laser pulse  
 $\sim 10^{18} \text{ cm}^{-3}$ , **50 GV/m** over 0.1m

First looks into "Plasma-Collider": **staging kills !  $\langle E \rangle \sim 2 \text{ GV/m}, \varepsilon$**

# New Approach:

## Acceleration in Continuous Focusing Channel



$$E_0 = \frac{m_e c \omega_p}{e} \approx 100 \left[ \frac{\text{GeV}}{m} \right] \cdot \sqrt{n_0 [10^{18} \text{ cm}^{-3}]}$$

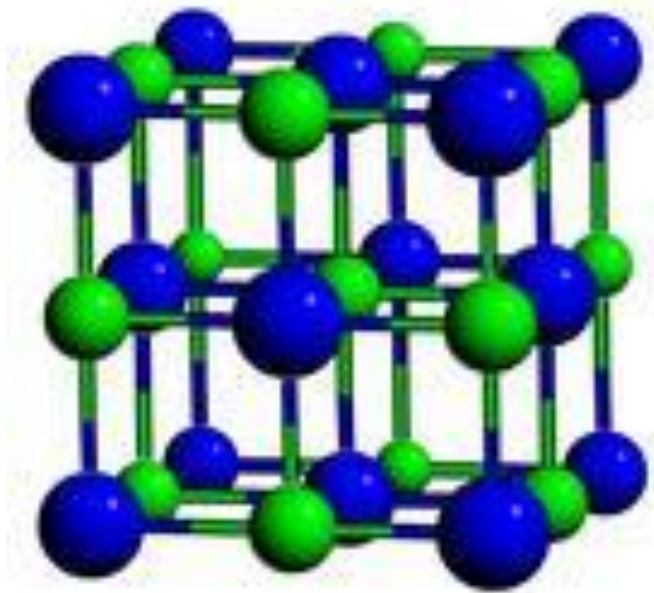
$10^{22} \text{ cm}^{-3} \rightarrow 10 \text{ TV/m}, \lambda_p \sim 0.3 \mu\text{m}$

$10^{24} \text{ cm}^{-3} \rightarrow 100 \text{ TV/m}, \lambda_p \sim 0.03 \mu\text{m}$

Synchrotron radiation  
losses balance energy gain:  
0.3 TeV for positrons  
10 000 TeV for muons (+)  
1000 000 TeV for protons



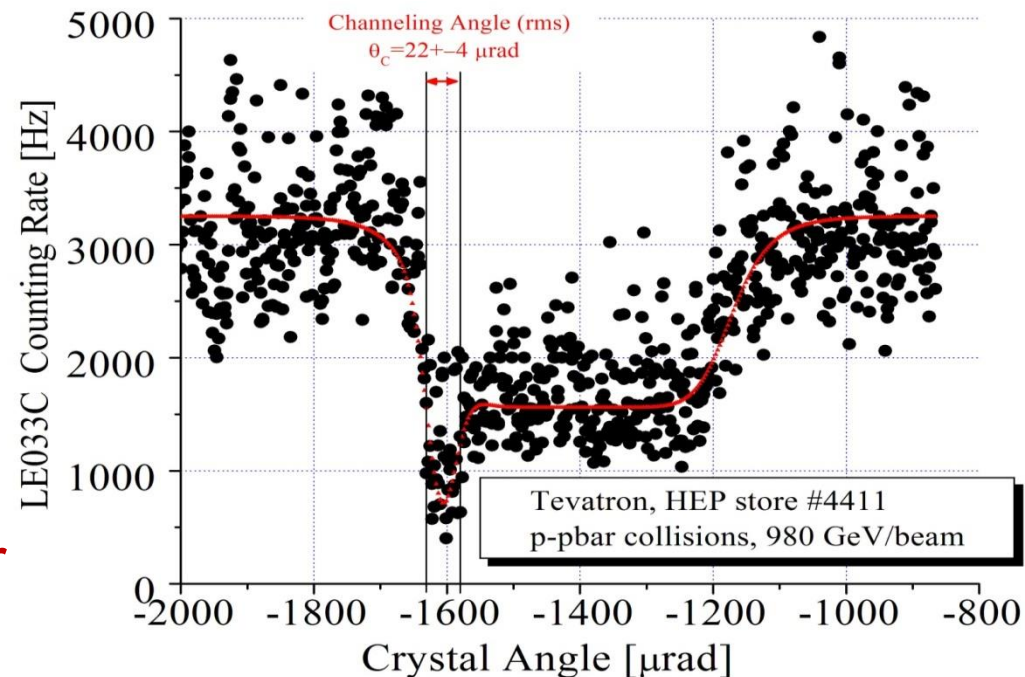
# What Do We Know about Crystals?



- Strong inter-planar electric fields  $\sim 10\text{V}/\text{\AA}=1\text{GV}/\text{cm}$
- **Very stable, can be used for**
  - deflection/bending (*works*)
  - focusing (*works*)
  - acceleration (*if excited*)

$$l_d [\text{m}] \sim E [\text{TeV}]$$

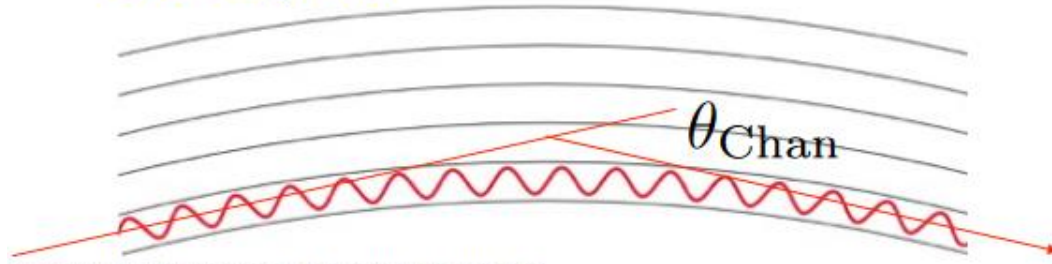
**T980 experiment at Tevatron, N.Mokhov et al JINST 6 T08005 (2011)**



$\sim 92.5 \pm 5\%$  efficiency  
Or  $l_d \sim 5\text{mm}/0.025 < 0.2\text{m}$

# 4 mm Si in LHC

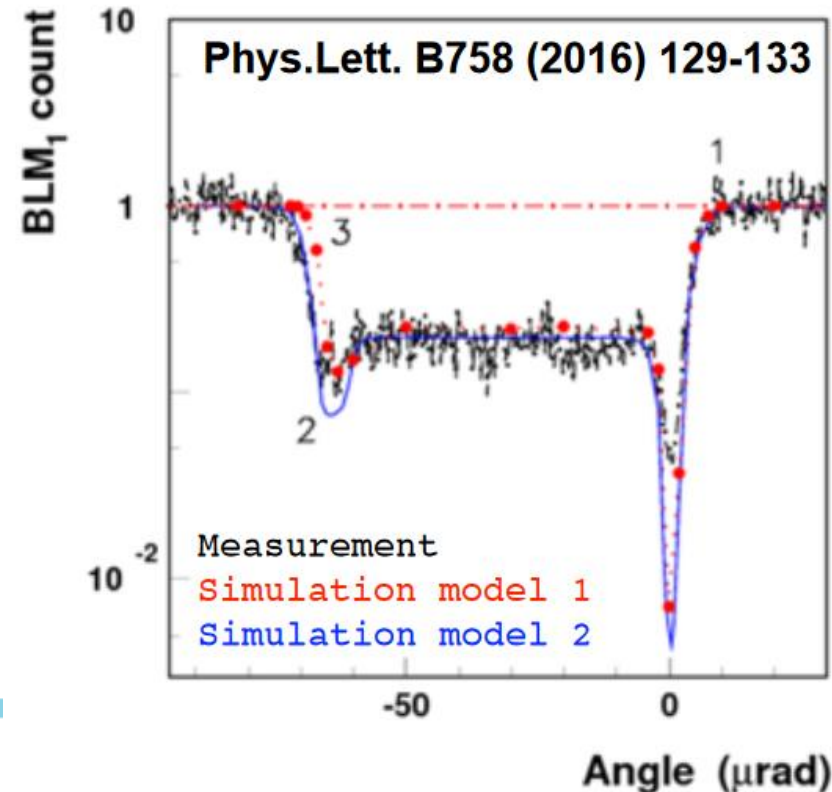
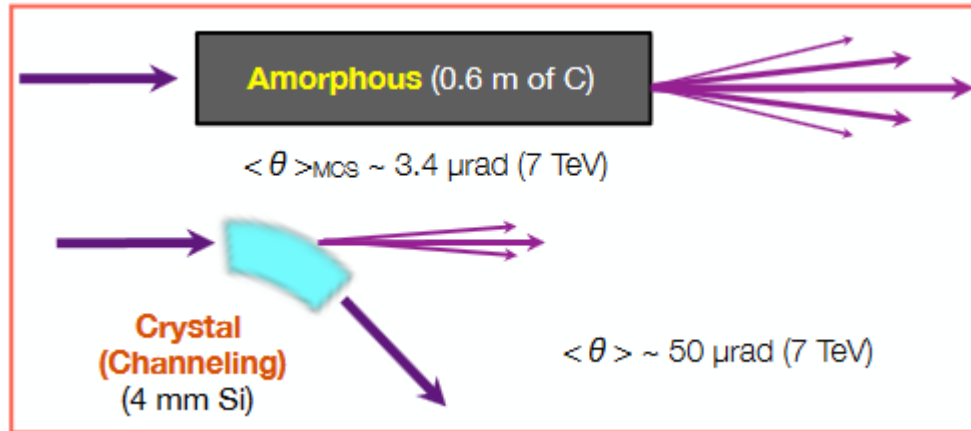
## Bent crystal



S. Redaelli, *Physics Beyond Colliders*, 06/09/2016

~2 mrad at 7 TeV

Equivalent magnetic field for  
**50  $\mu\text{rad}$**  at 7 TeV proton  
beams: **310 T** (4 mm crystal)



~99.5% efficiency

Or  $l_d \sim 4\text{mm}/0.005 = 0.8\text{m}$



# Collider considerations

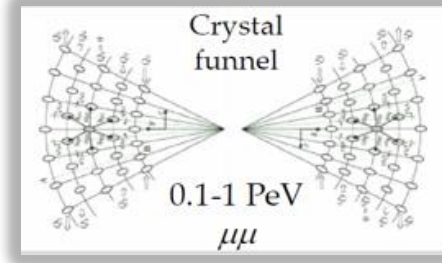
$$\frac{dN}{dt} = -N/\gamma\tau_0 \quad \frac{N}{N_0} \approx \left(\frac{m_\mu c^2}{E}\right)^\kappa$$

$$\kappa = (m_\mu c/\tau_0 G) \ll 1/\ln(\dot{E}/m_\mu c^2)$$

i.e. irrelevant

$$A \sim 1 \text{ \AA}^2 = 10^{-16} \text{ cm}^2 \quad N_0 \sim 10^3 \text{ particles}$$

$$L = fN^2/A = f \times 10^{16} \times 10^6 n_{\text{ch}} [\text{cm}^{-2} \text{ s}^{-1}]$$



$$L [\text{sm}^{-2} \text{ s}^{-1}] \approx 4 \times 10^{33-35} \frac{P^2 [\text{MW}]}{E^2 [\text{TeV}] f n_{\text{ch}} [10^8 \text{ Hz}]}$$

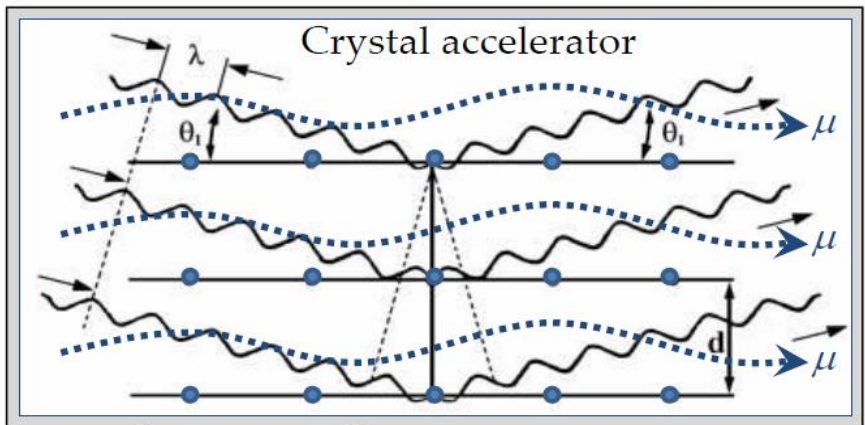
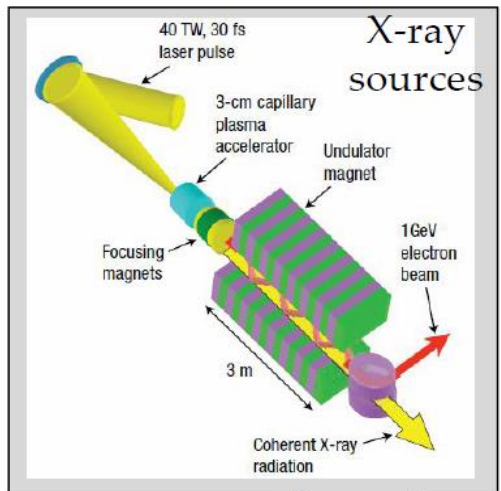
**Table 4.** Options for future particle colliders.

Collider type	Dielectric based	Plasma based	Crystal channeling
Accelerating media	Microstructures	Ionized plasma	Solid crystals
Energy source: option 1 option 2	Optical laser e <sup>-</sup> bunch	e <sup>-</sup> bunch Optical laser	X-ray laser
Preferred particles	Any stable	e <sup>-</sup> , μ <sup>-</sup>	μ <sup>+</sup> , p <sup>+</sup>
Max accelerating gradient, GeV m <sup>-1</sup>	1–3	30–100	100–10 <sup>4</sup>
CM energy reach in 10 km	3–10	3–50	10 <sup>3</sup> –10 <sup>5</sup>
Number of stages/10 km: option 1 option 2	10 <sup>5</sup> –10 <sup>6</sup> 10 <sup>4</sup> –10 <sup>5</sup>	~ 100 10 <sup>3</sup> –10 <sup>4</sup>	~ 1

# “Dream” Collider = Muons + Acceleration in Crystals + Continuous Focusing (Channeling)

V.Shiltsev, Phys. Uspekhy 55 965 (2012)

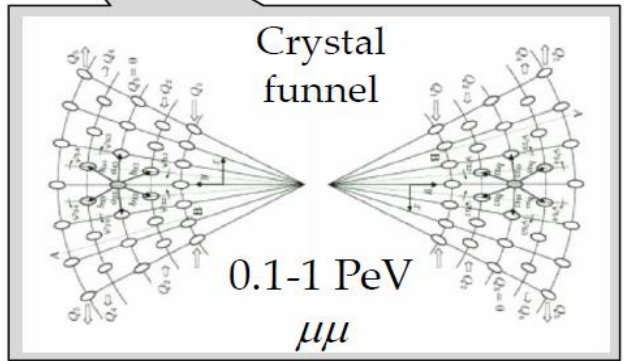
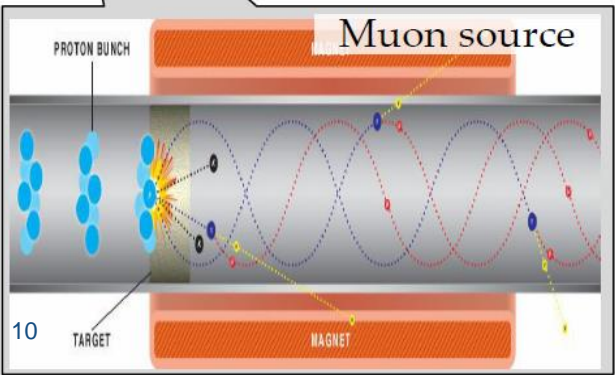
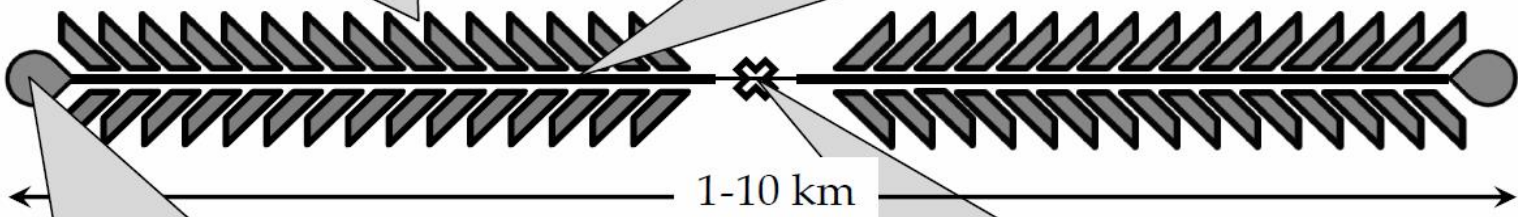
$$E_0 = \frac{m_e c \omega_p}{e} \approx 100 \left[ \frac{\text{GeV}}{m} \right] \cdot \sqrt{n_0 [10^{18} \text{ cm}^{-3}]}$$



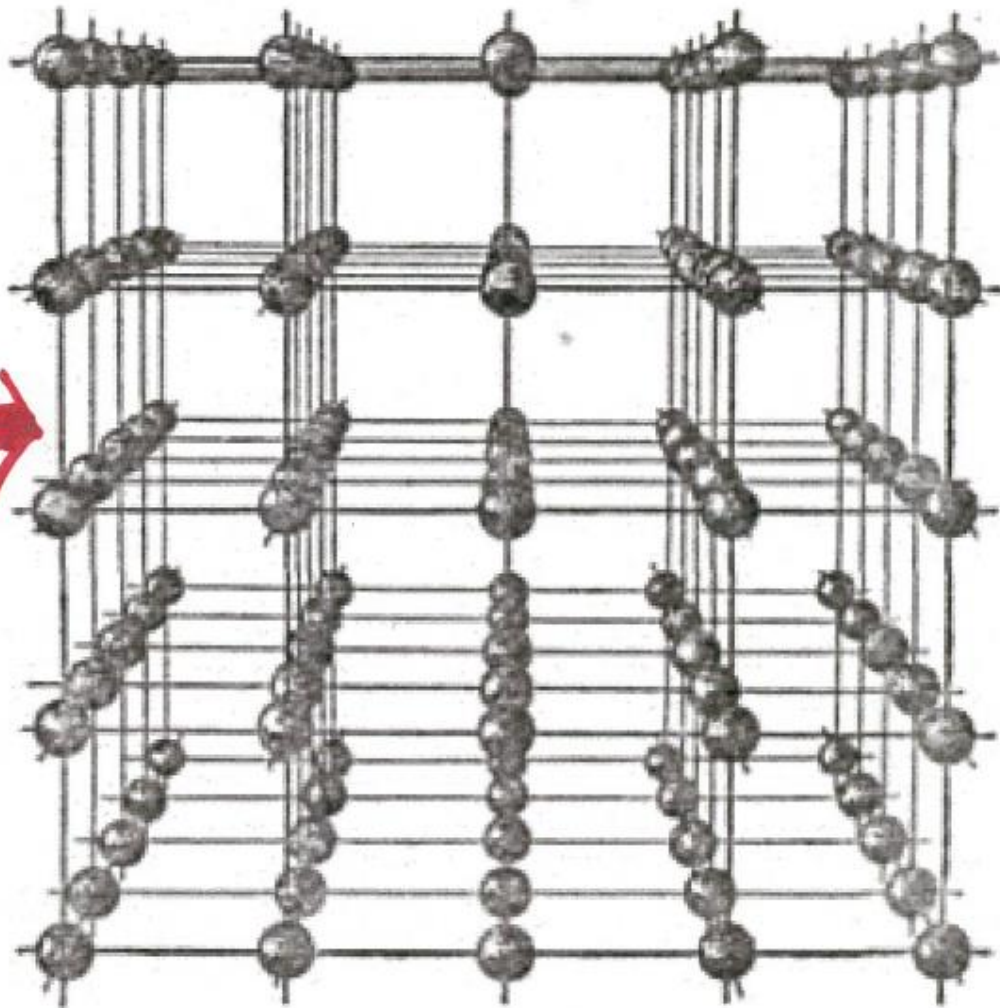
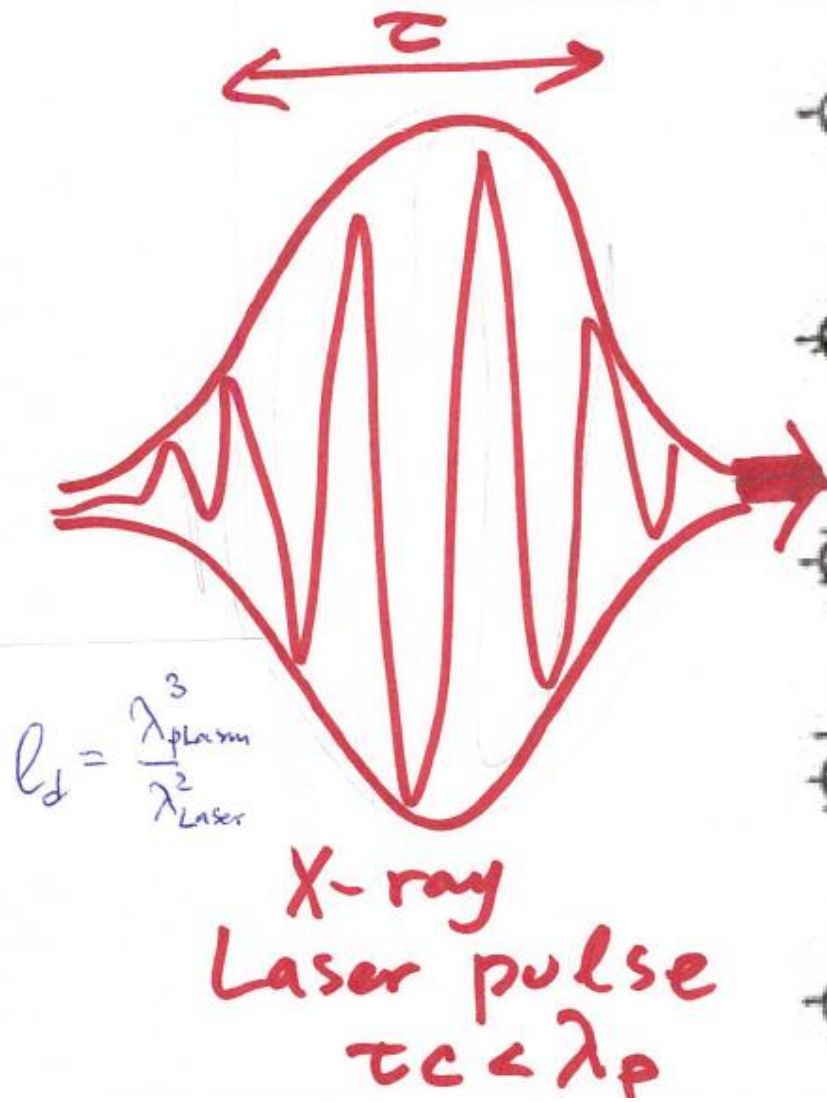
$n \sim 10^{22} \text{ cm}^{-3}$ ,  
**10 TeV/m**  
 $\rightarrow$

**1 PeV = 1000 TeV**

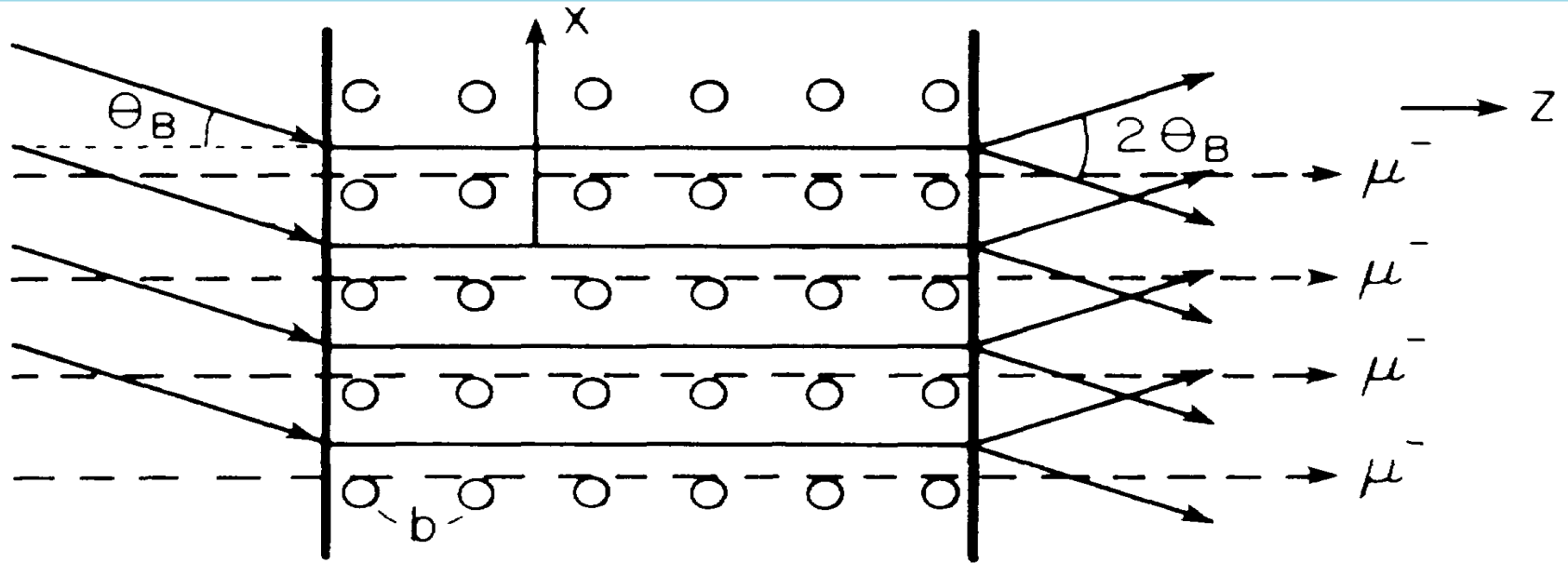
$n_\mu \sim 1000$   
 $n_B \sim 100$   
 $f_{rep} \sim 10^6$   
 $L \sim 10^{30-32}$



# Ways to excite the crystal (1)



# Crystal Excitation by X-Rays



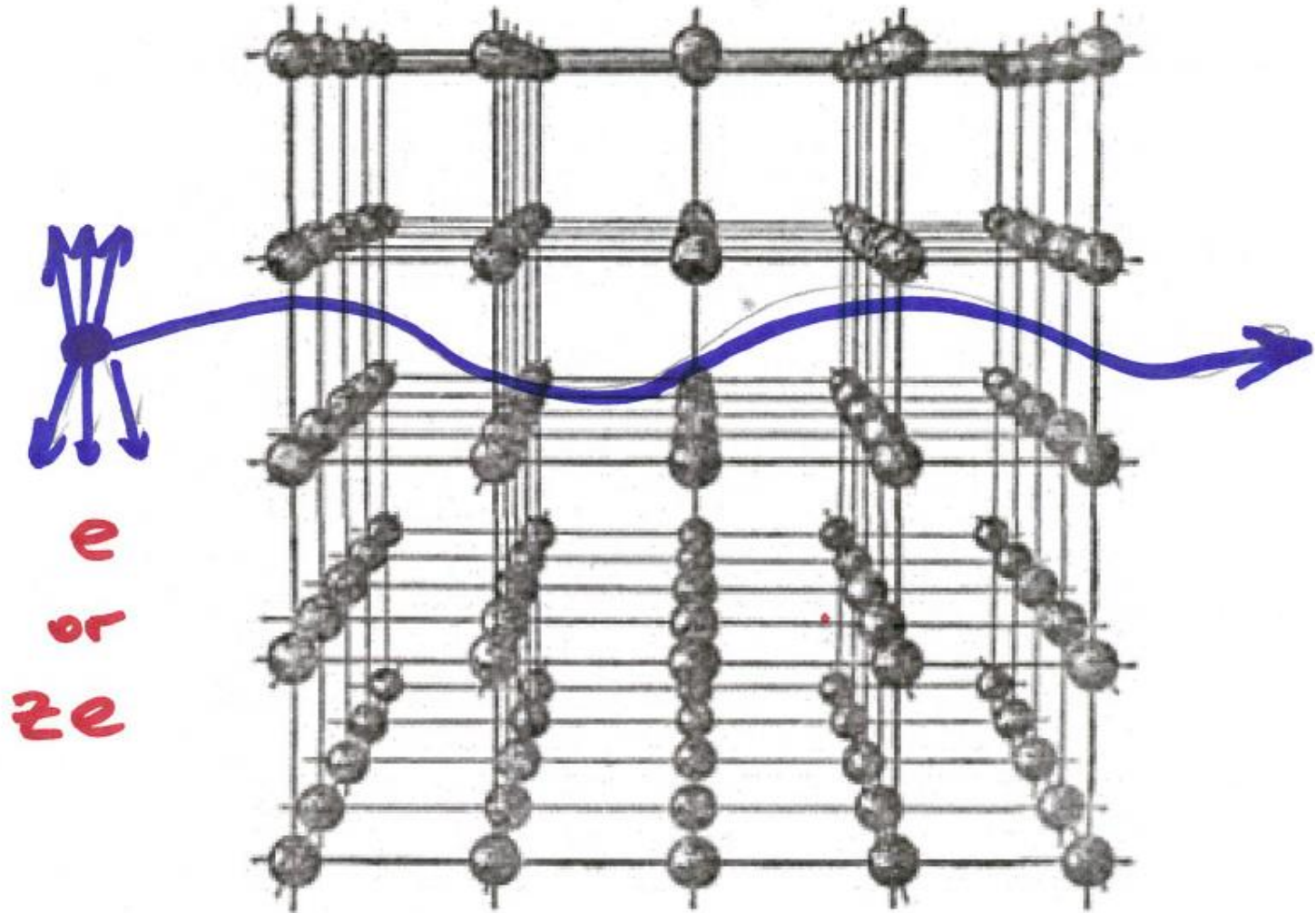
Tajima, Cavenago, *Phys. Rev. Lett.* 59 (1987), 1440

FIG. 1. Bormann anomalous transmission. When the x rays are injected at the Bragg angle, the Bormann effect takes place. Particle beams are injected along the crystal axis.

- Need 40keV high peak power x-rays
  - now available from SASE FELs like LCLS
- Gradients  $>1\text{GV/cm}$
- Muons preferred
  - No bremsstrahlung, no nucl.
- $\mu^+$  rad length  $10^9\text{ cm}$ 
  - total energy  $\sim 10^9\text{ GeV}$

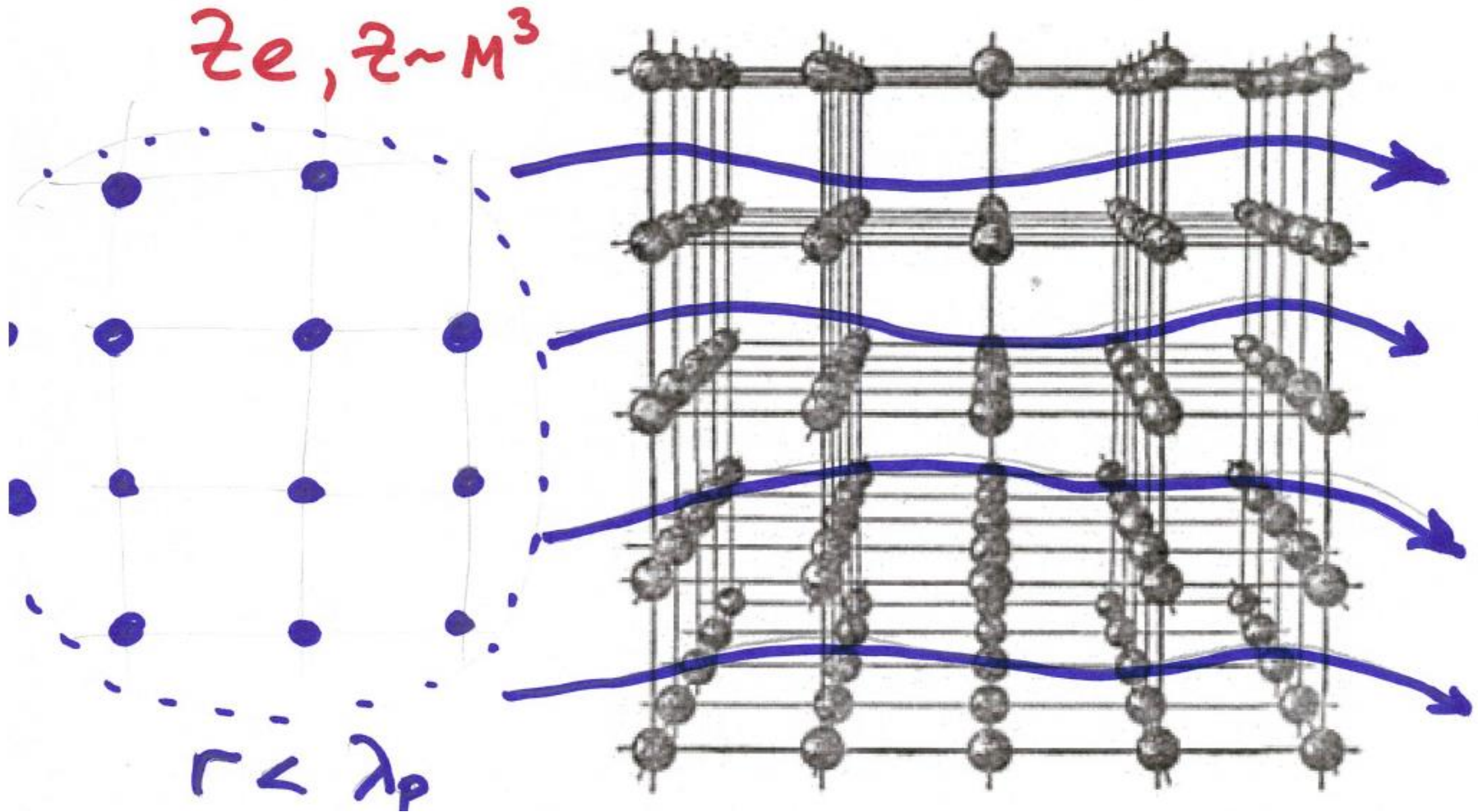


# Ways to excite the crystal (2)



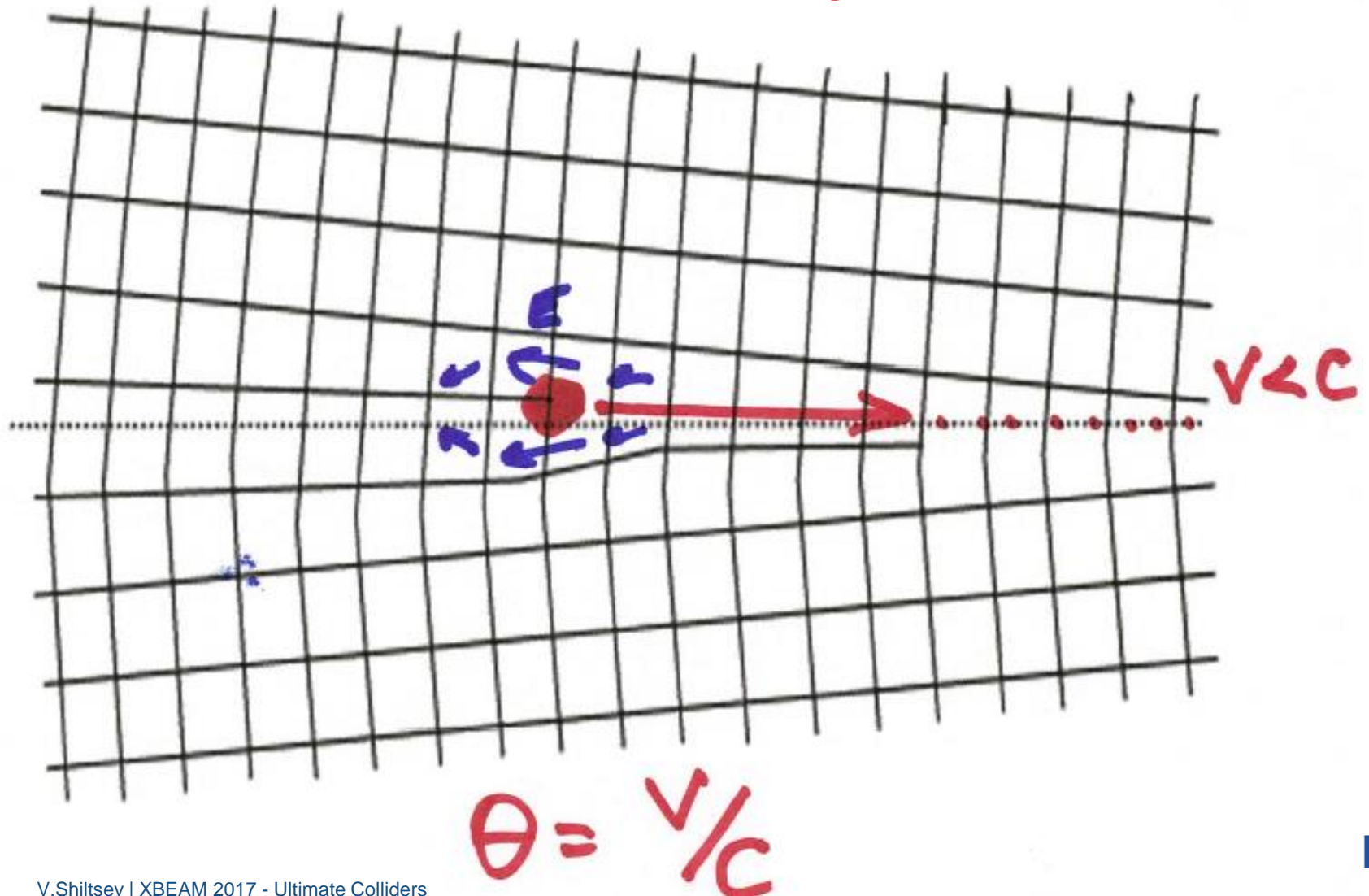


# Ways to excite the crystal (3)



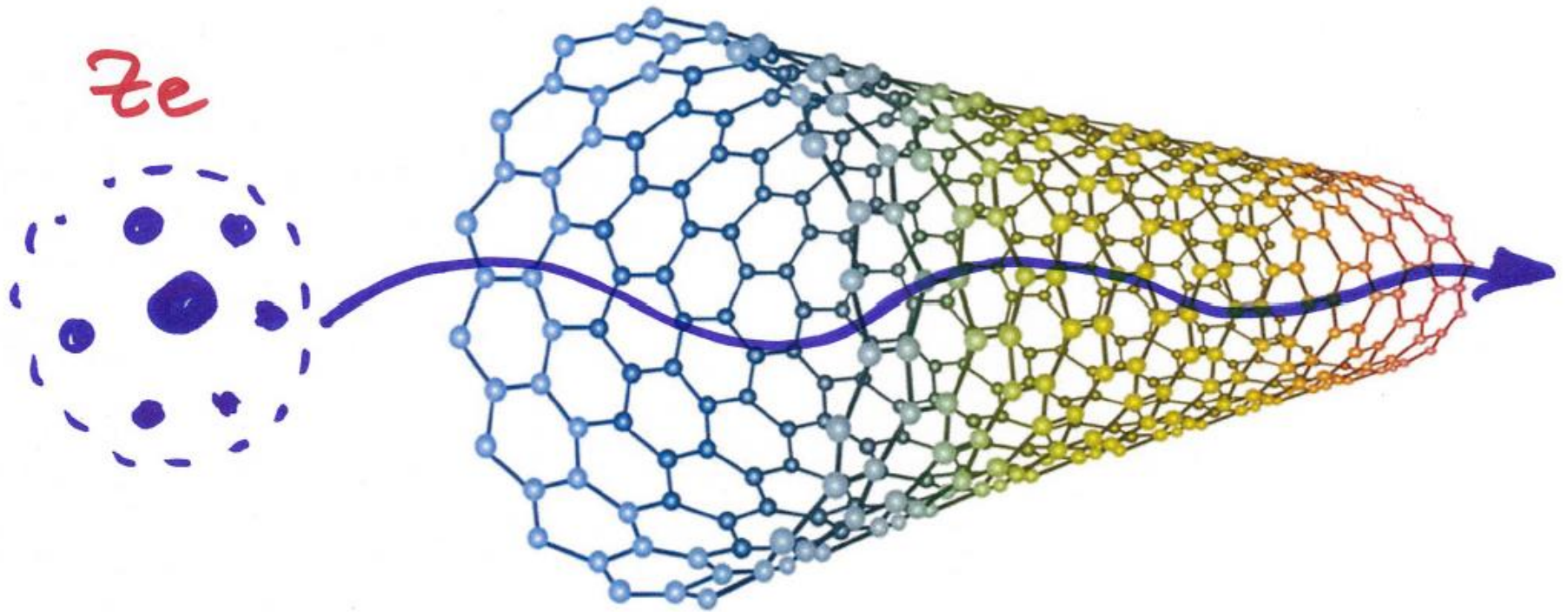
# Ways to excite the crystal (4)

Controlled generation of dislocations



# Nanotubes(1)

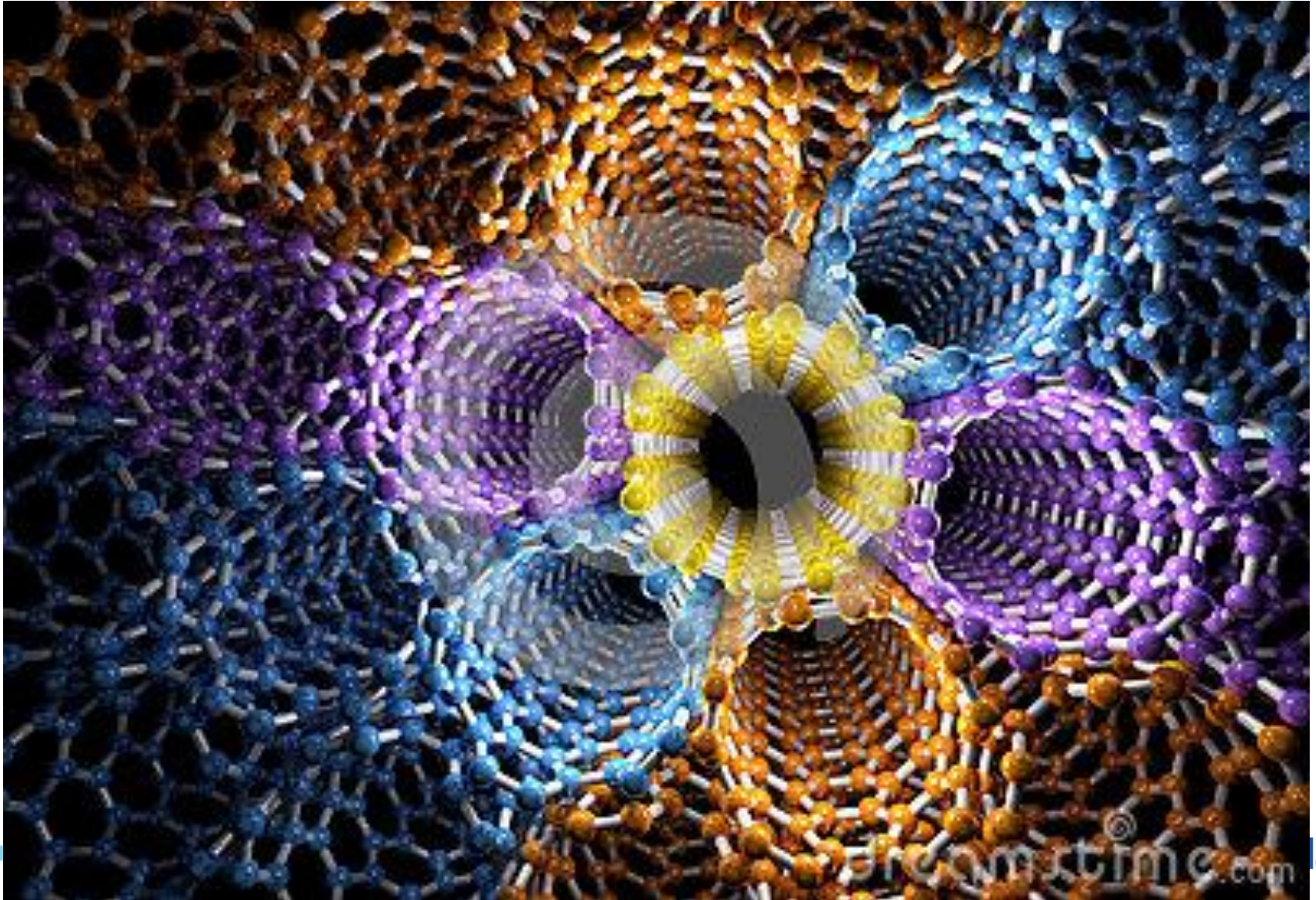
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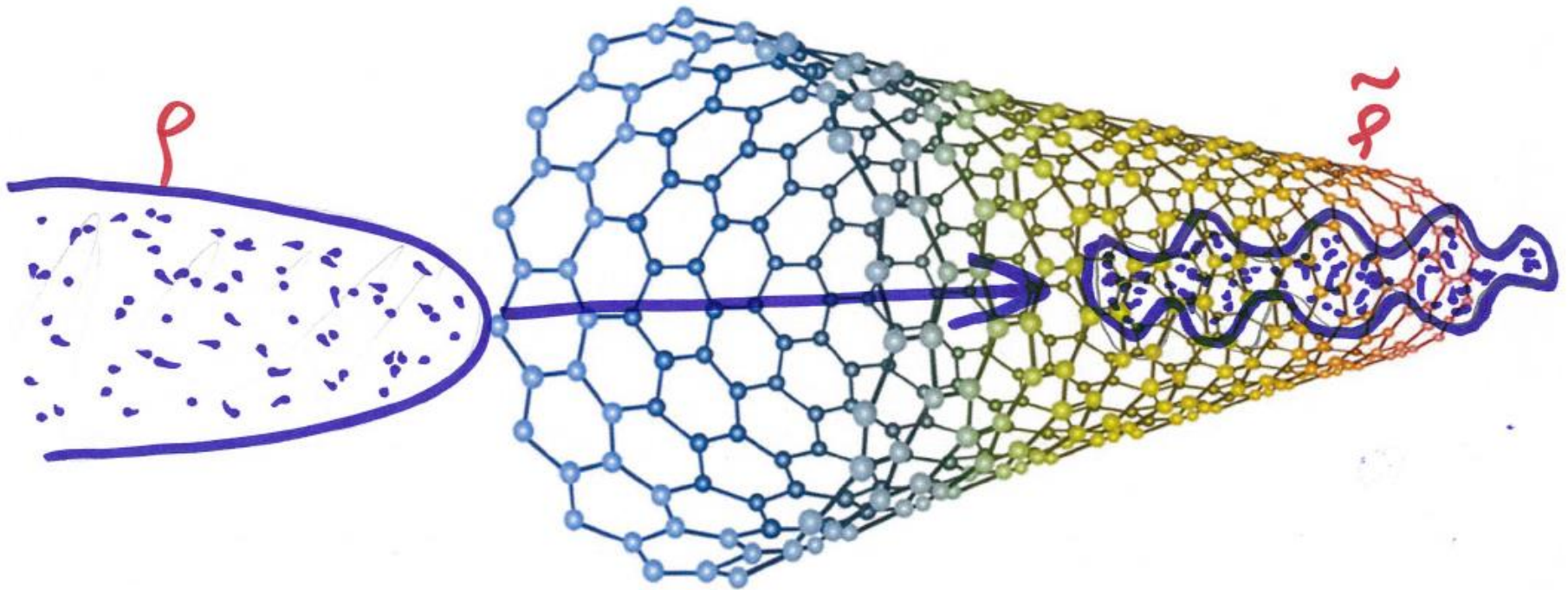


# Nanotubes (2)

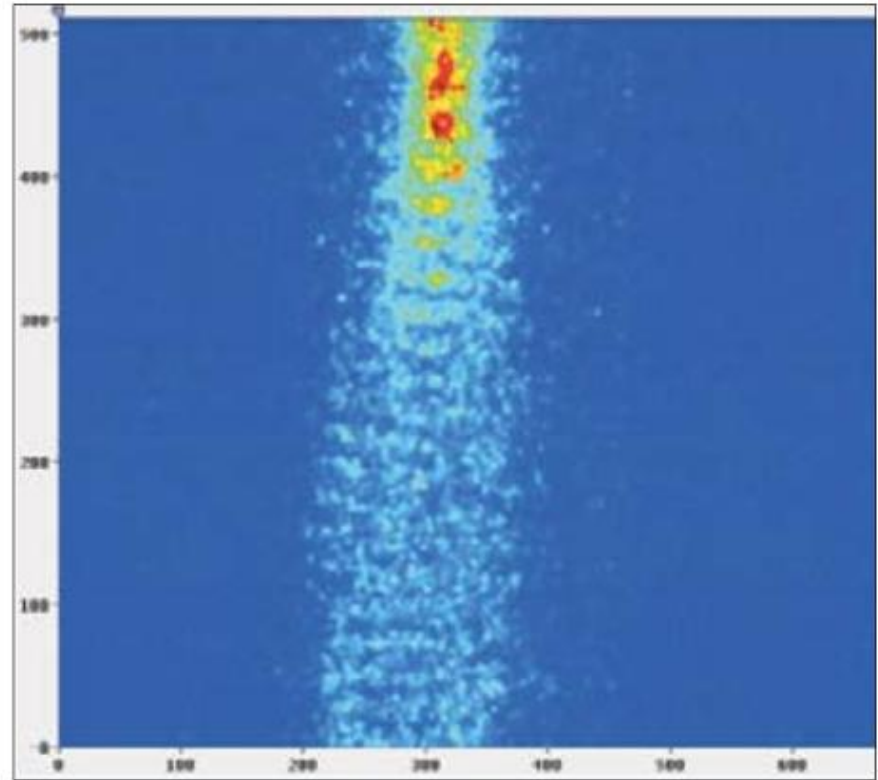
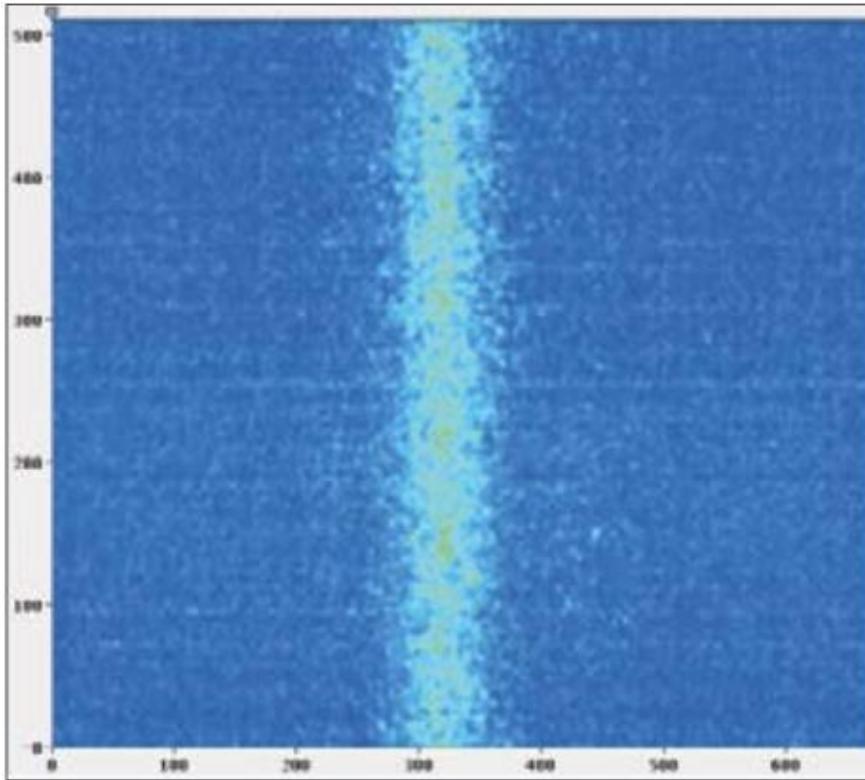
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# Excite nanotubes





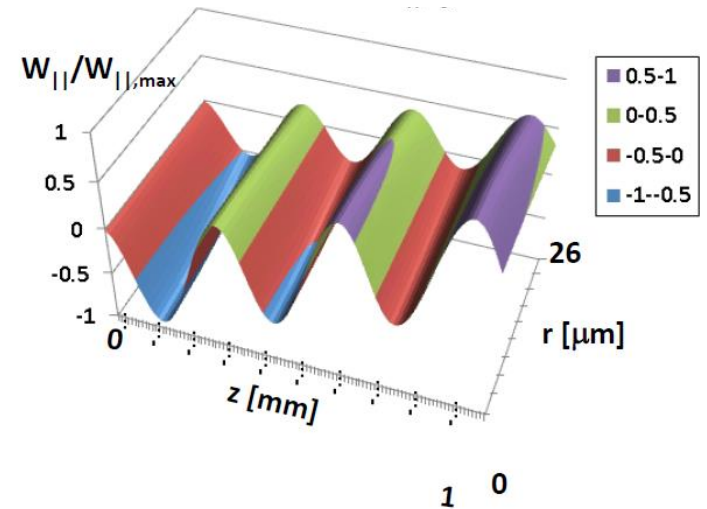
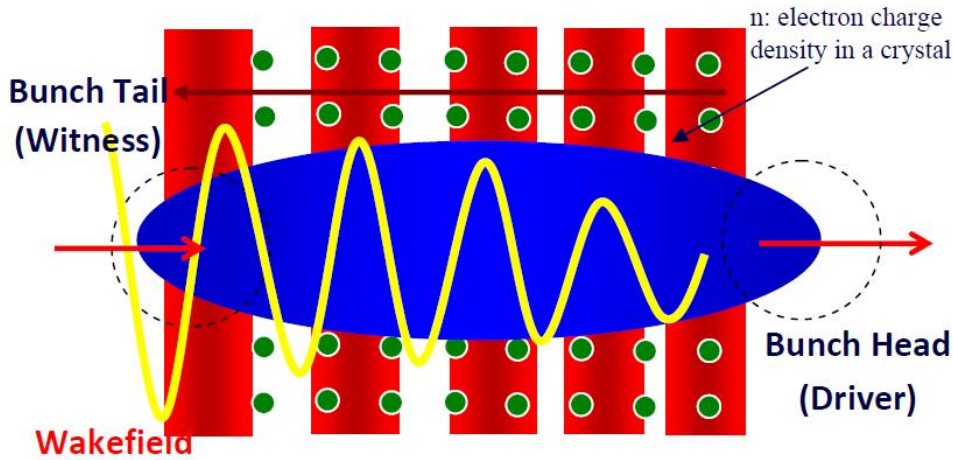


A Petrenko/CERN

*Comparison of the proton-bunch longitudinal profile (left, no plasma) with the profile for a bunch passing through plasma (right), showing the strong modulation of the bunch.*

# Proof-of-principle test of acceleration in Crystals/Carbon Nano Tubes (CNTs)

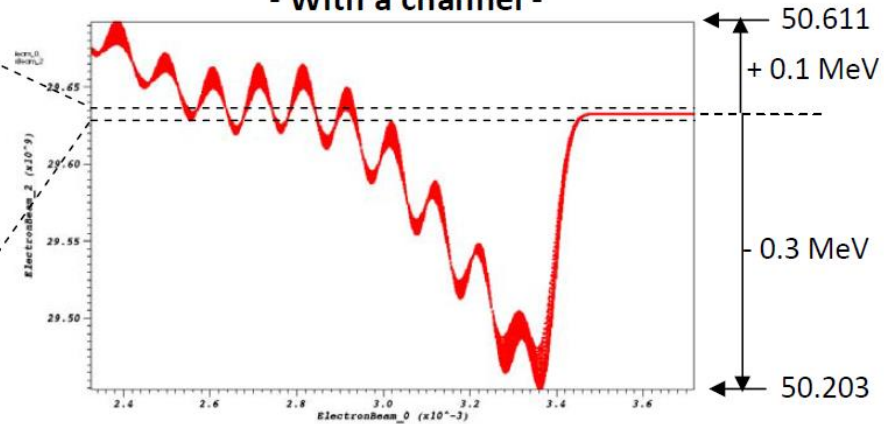
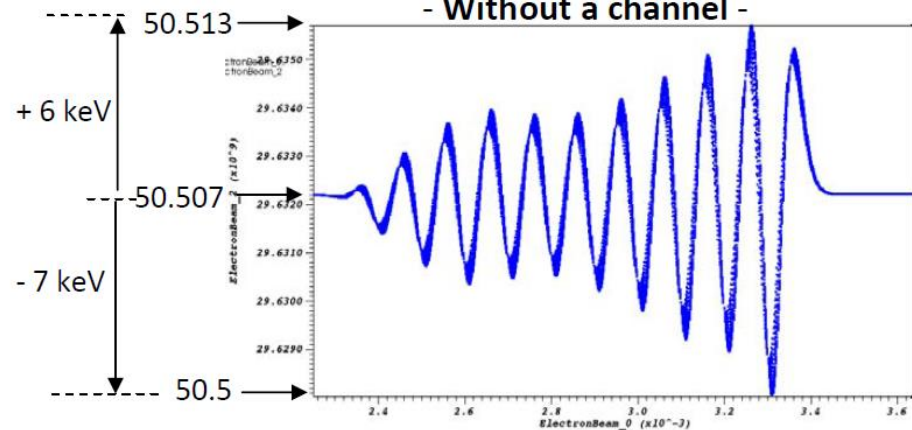
Y.M.Shin(NIU/FNAL), V,Shiltsev, C.Thangaraj (FNAL), et al



- 50 MeV (1 nC)

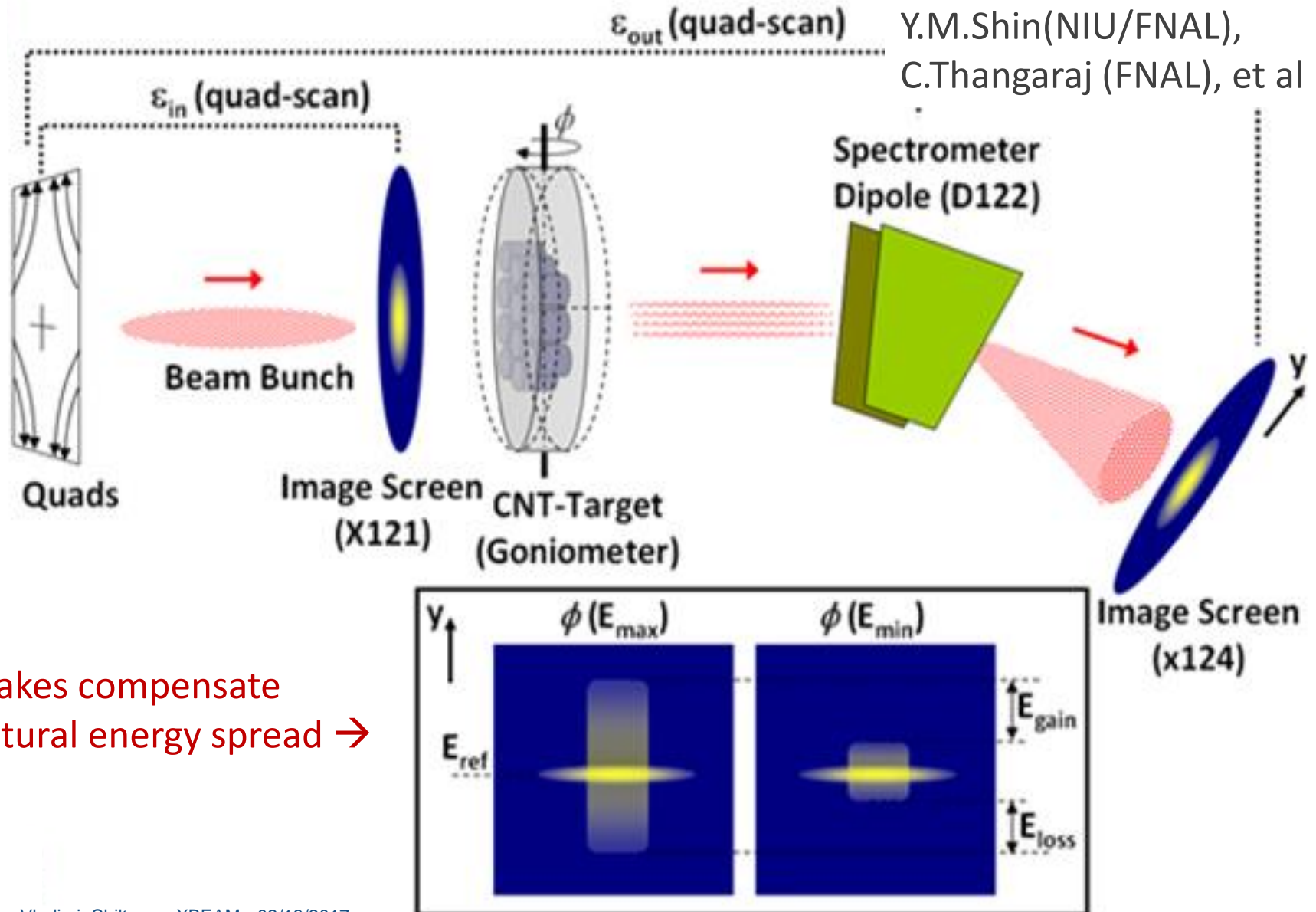
- Without a channel -

- With a channel -



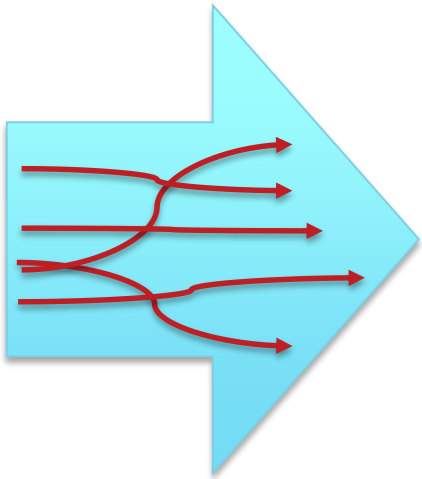
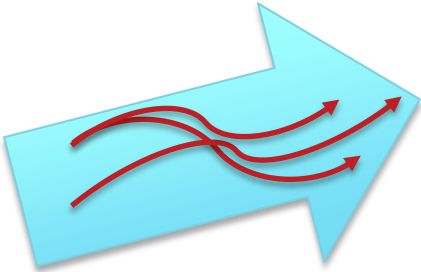
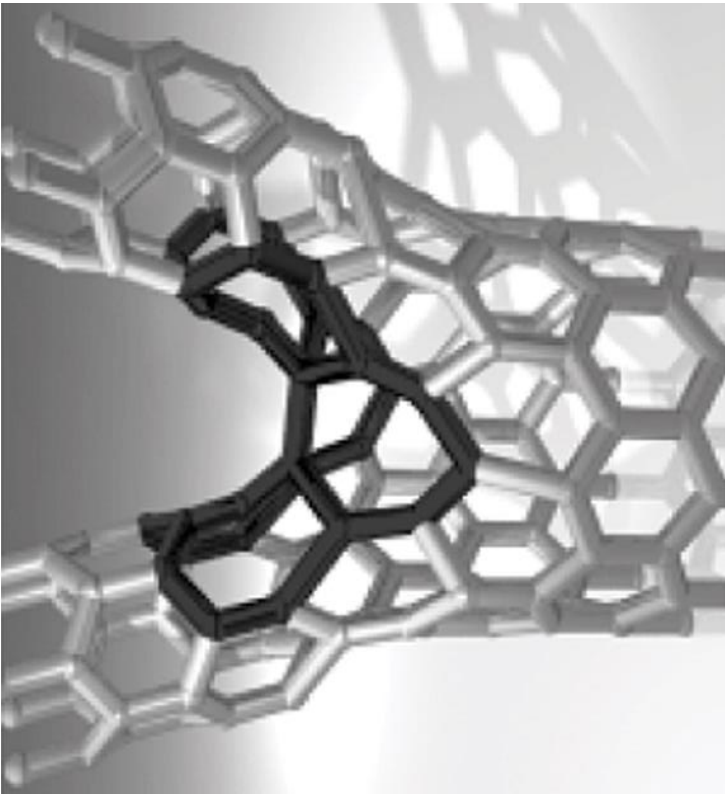
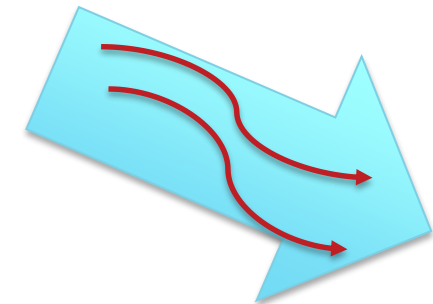
# Outline of Proposed Experiment at ASTA

Y.M.Shin(NIU/FNAL),  
C.Thangaraj (FNAL), et al



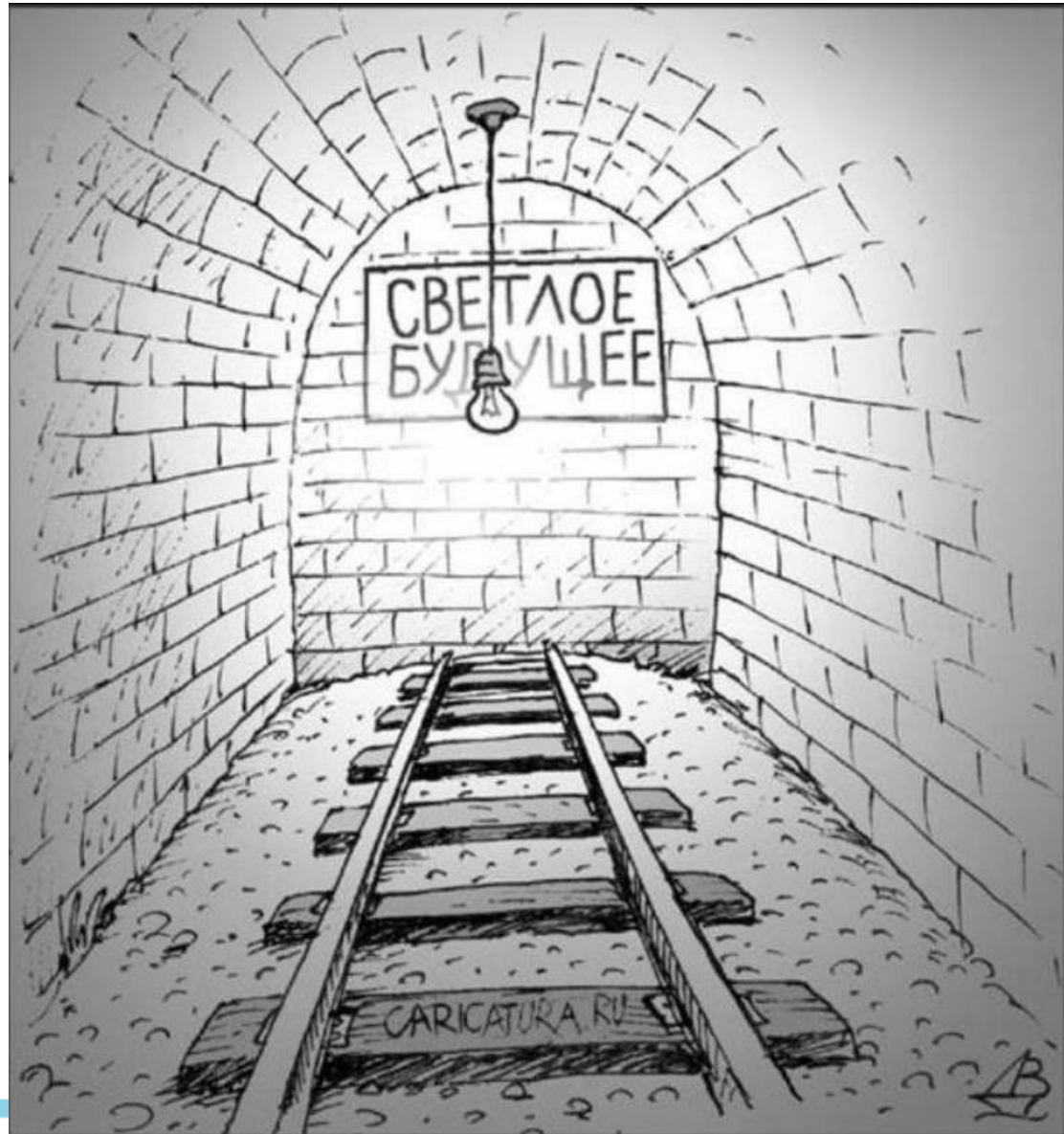
Wakes compensate  
natural energy spread →

# Combine (funnel) Channels





# Bright Future





# HEP's "Far" Future

- **Good News**

- options **EXIST**

- 300-1000 TeV muons in plasma/crystals

- **Bad News**

- It will be

**H**igh

**E**nergy

**L**ow

**L**uminosity

*Thank You for Your  
Attention!*

