



U.S. DEPARTMENT OF  
**ENERGY**

Office of  
Science

# *On Cost of Future Colliders and Options/Preemptive Measures*

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**Vladimir Shiltsev**

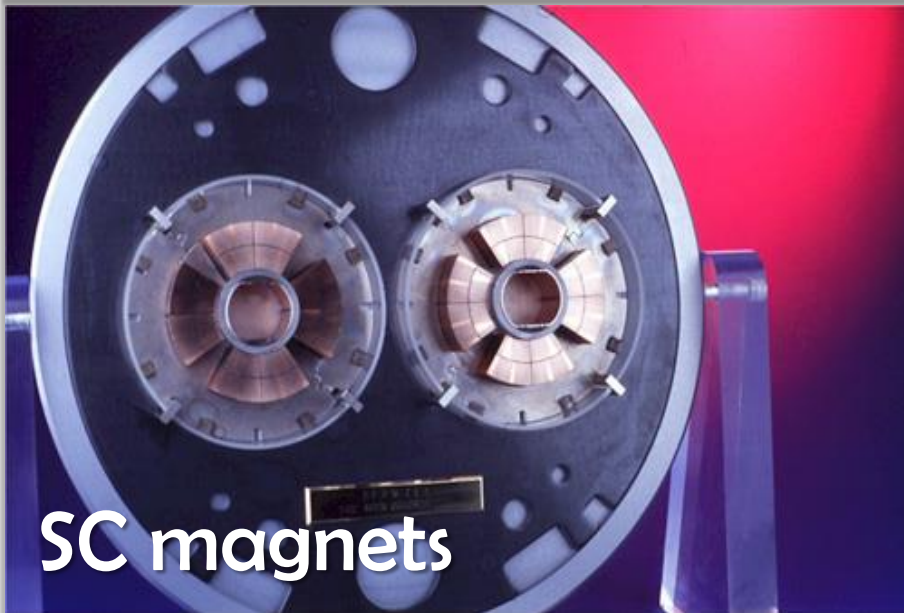
Fermilab \*, Batavia, IL , USA

Accelerator Physics Center

February 15, 2016



# Four “Feasible” Technologies



# Analysis:

2014 JINST 9 T07002

## 17 “Data Points” - Costs of Big Accelerators:

- Actually built:
  - RHIC, MI, SNS, LHC
- Under construction:
  - XFEL, FAIR, ESS
- Not built but costed:
  - SSC, VLHC, NLC
  - ILC, TESLA, CLIC, Project-X, Beta-Beam, SPL, v-Factory

## Wide range :

- 4 orders in Energy, >1 order in Power, >2 orders in Length
- Almost 2 orders in cost
  - (normalized to US TPC)

	Cost (B\$) Year	Energy (TeV)	Accelerator technology	Comments	Length (km)	Site power (MW)	TPC range (Y14 B\$)
SSC	11.8 B\$ (1993)	40	SC Mag	Estimates changed many times [6–8]	87	~ 100	19–25
FNAL MI	260M\$ (1994)	0.12	NC Mag	“old rules”, no OH, existing injector [9]	3.3	~ 20	0.4–0.54
RHIC	660M\$ (1999)	0.5	SC Mag	Tunnel, some infrastructure, injector re-used [10]	3.8	~ 40	0.8–1.2
TESLA	3.14 B€ (2000)	0.5	SC RF	“European accounting” [11]	39	~ 130	11–14
VLHC-I	4.1 B\$ (2001)	40	SC Mag	“European accounting”, existing injector [12]	233	~ 60	10–18
NLC	~ 7.5 B\$ (2001)	1	NC RF	~ 6 B\$ for 0.5 TeV collider, [13]	30	250	9–15
SNS	1.4 B\$ (2006)	0.001	SC RF	[14]	0.4	20	1.6–1.7
LHC	6.5 BCHF (2009)	14	SC Mag	collider only — existing injector, tunnel & infrstr., no OH, R&D [15]	27	~ 40	7–11
CLIC	7.4–8.3B CHF(2012)	0.5	NC RF	“European accounting” [16]	18	250	12–18
Project X	1.5 B\$ (2009)	0.008	SC RF	[17]	0.4	37	1.2–1.8
XFEL	1.2 B€ (2012)	0.014	SC RF	in 2005 prices, “European accounting” [18]	3.4	~ 10	2.9–4.0
NuFactory	4.7–6.5 B€ (2012)	0.012	NC RF	Mixed accounting, w. contingency [19]	6	~ 90	7–11
Beta-Beam	1.4–2.3 B€ (2012)	0.1	SC RF	Mixed accounting, w. contingency [19]	9.5	~ 30	3.7–5.4
SPL	1.2–1.6 B€ (2012)	0.005	SC RF	Mixed accounting, w. contingency [19]	0.6	~ 70	2.6–4.6
FAIR	1.2 B€ (2012)	0.003–0.08	SC Mag	“European accounting” [20], 6 rings, existing injector	~ 3	~ 30	1.8–3.0
ILC	7.8 B\$ (2013)	0.5	SC RF	“European accounting” [21]	34	230	13–19
ESS	1.84 B€ (2013)	0.0025	SC RF	“European accounting” [22, 23]	0.4	37	2.5–3.8



# ! WARNING !

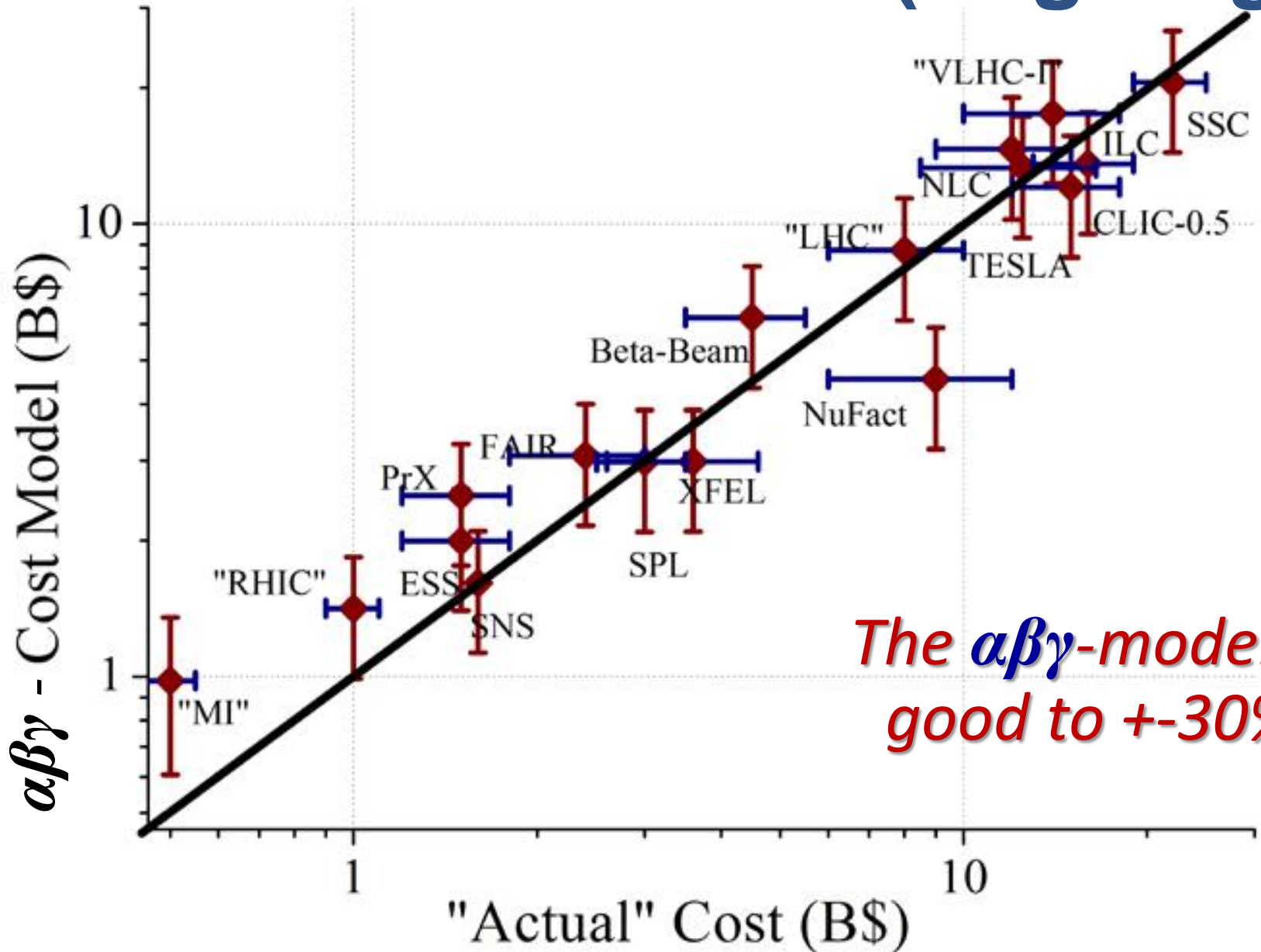
$\alpha\beta\gamma$  - Cost Estimate Model:

$$\text{Cost(TPC)} = \alpha L^{1/2} + \beta E^{1/2} + \gamma P^{1/2}$$

- a)  $\pm 33\%$  estimate, for a “green field” accelerators
- b) “US-Accounting” = TPC ! (  $\sim 2 \times$  *European Accounting* )
- c) Coefficients ( units: 10 km for  $L$ , 1 TeV for  $E$ , 100 MW for  $P$  )
  - $\alpha \approx 2\text{B}\$/\text{sqrt}(L/10 \text{ km})$
  - $\beta \approx 10\text{B}\$/\text{sqrt}(E/\text{TeV})$  for SC/NC RF
  - $\beta \approx 2\text{B}\$ /\text{sqrt}(E/\text{TeV})$  for SC magnets
  - $\beta \approx 1\text{B}\$ /\text{sqrt}(E/\text{TeV})$  for NC magnets
  - $\gamma \approx 2\text{B}\$/\text{sqrt}(P/100 \text{ MW})$

USE AT YOUR OWN RISK!

# Total Cost vs Model (Log-Log)



# Illustrations

## Comment:

*Sqrt*-functions are quite accurate over wide range because such dependence well approximates the “initial cost” – effect :

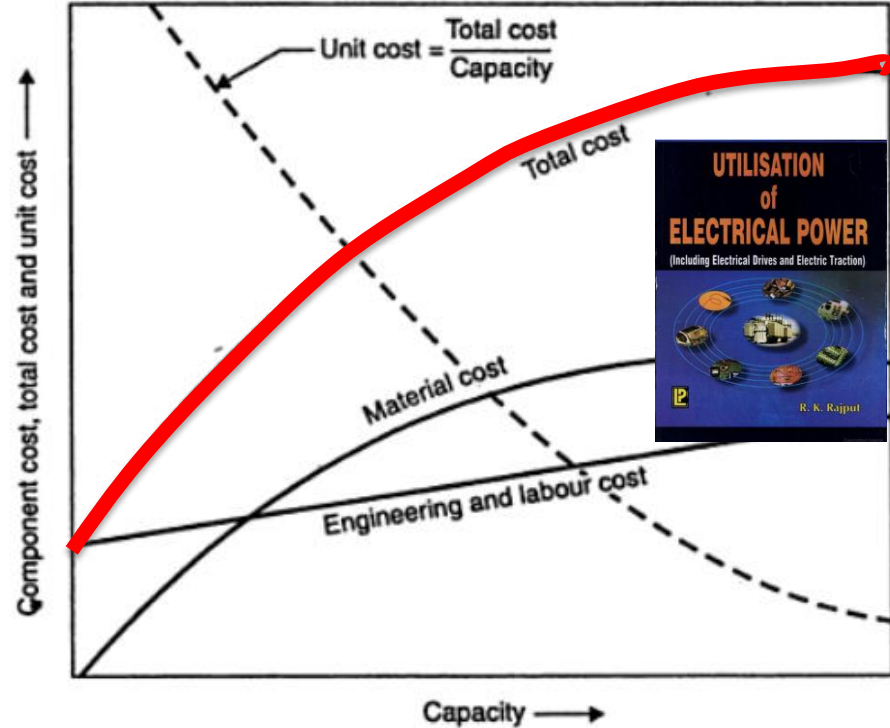
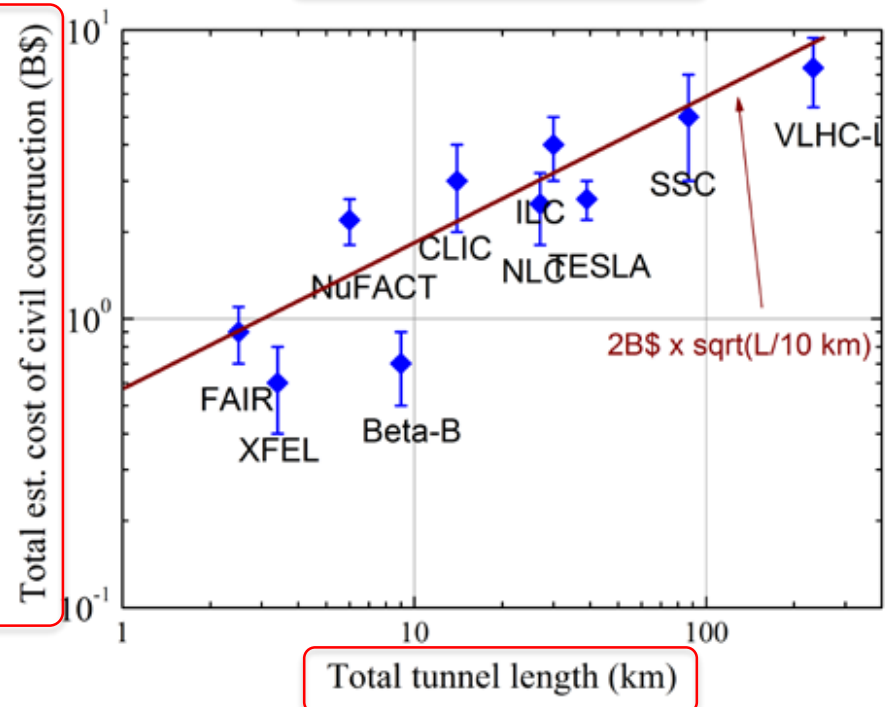
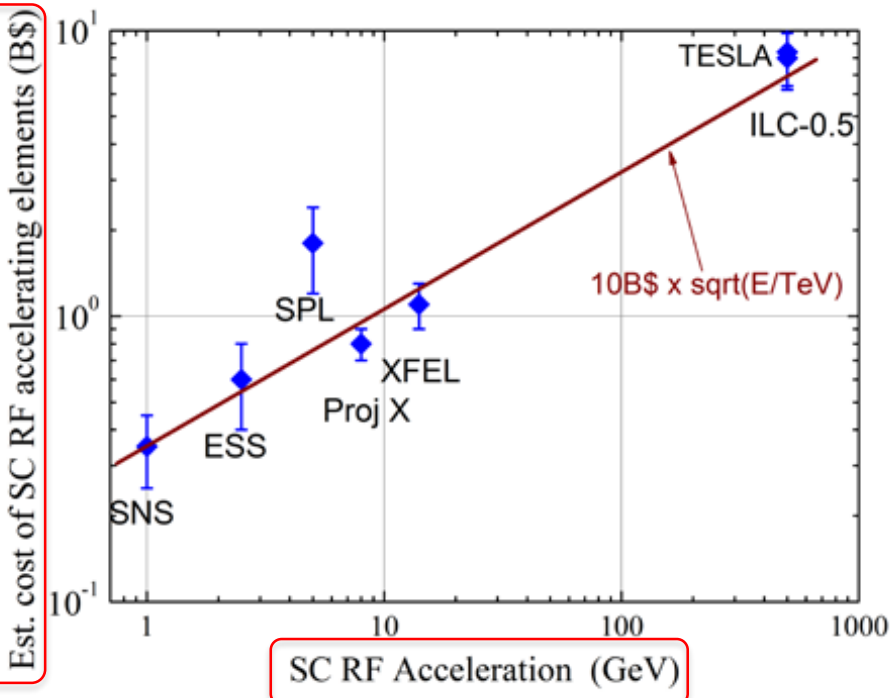


Fig. 9.5. Variation of costs of power plant versus its capacity.

# Take LHC as an Example:

- **$\alpha\beta\gamma$  – Model:**

- 40 km of tunnels
- 14 TeV c.o.m SC magnets
- ~150 MW of site power

$$2\sqrt{40/10} = 4$$

$$2\sqrt{14} = 7.5$$

$$2\sqrt{150/100} = 2.5$$

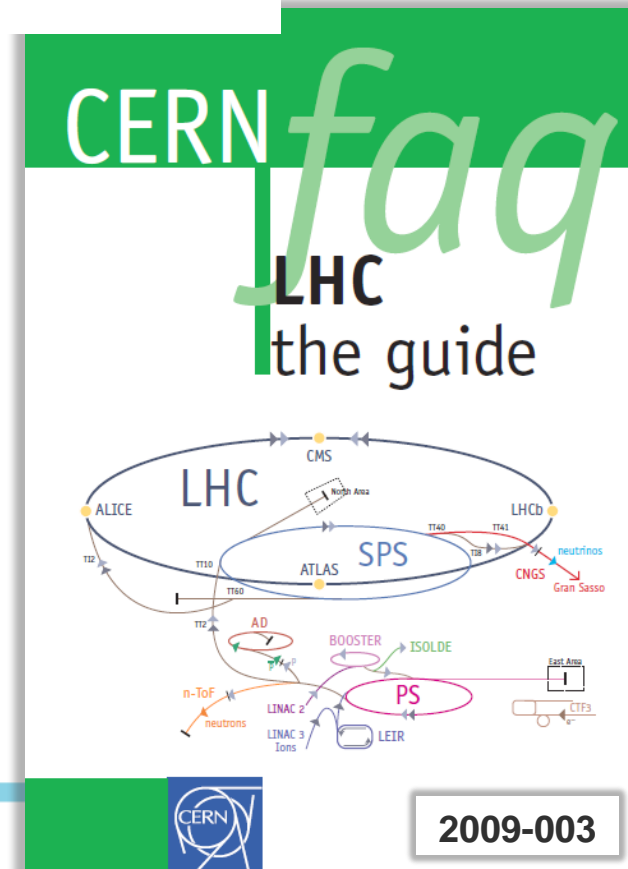
TOTAL PROJECT COST : **14B\$ ± 4.5B\$**

- **CERN LHC Factbook (2009):**

- 6.5 BCHF, incl. **5 BCHF** for accelerator (European Accounting)
- x 2 to US TPC → **10 BCHF=10B\$**
- Cost of existing injector complex ~30-40% **3-4 B\$**

**TPC : ~13-14B\$**

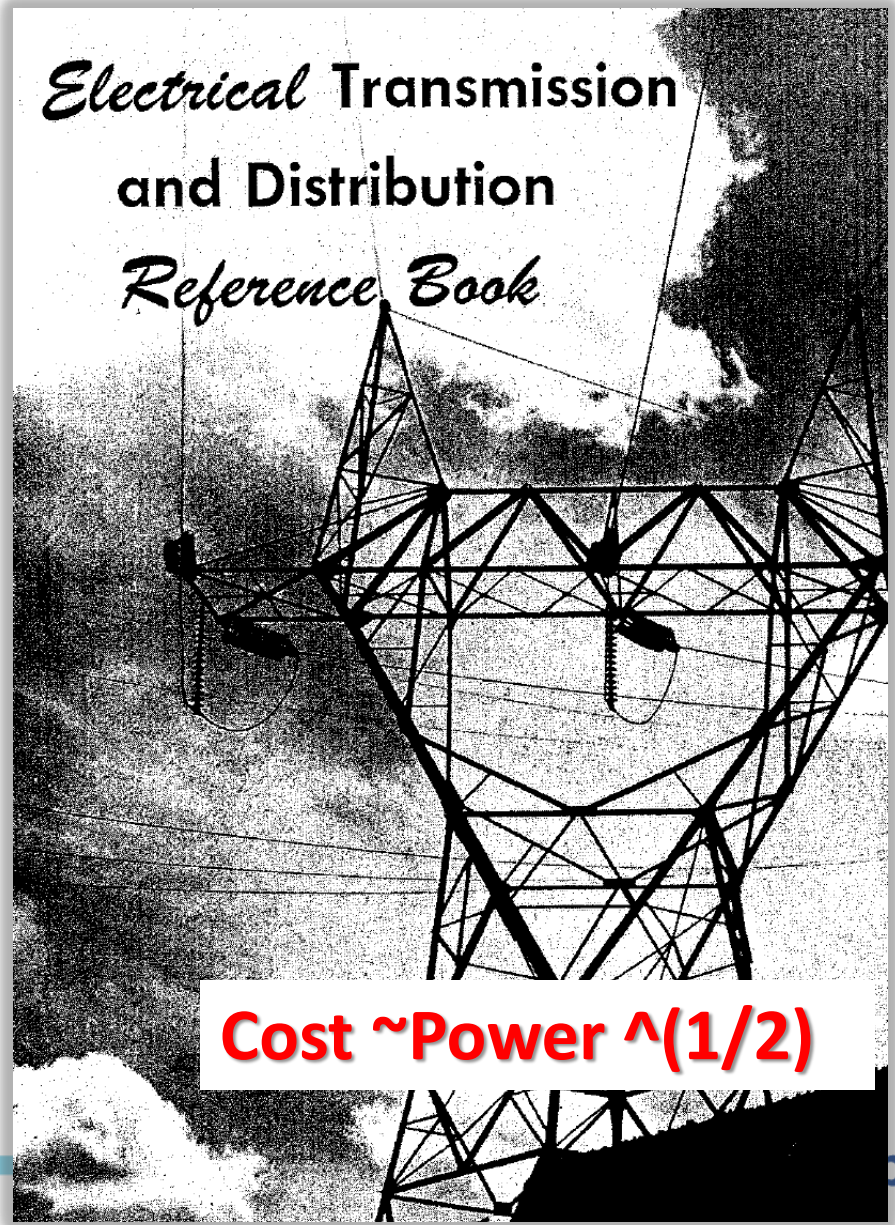
**(of which CERN paid 10 over ~8 yrs)**





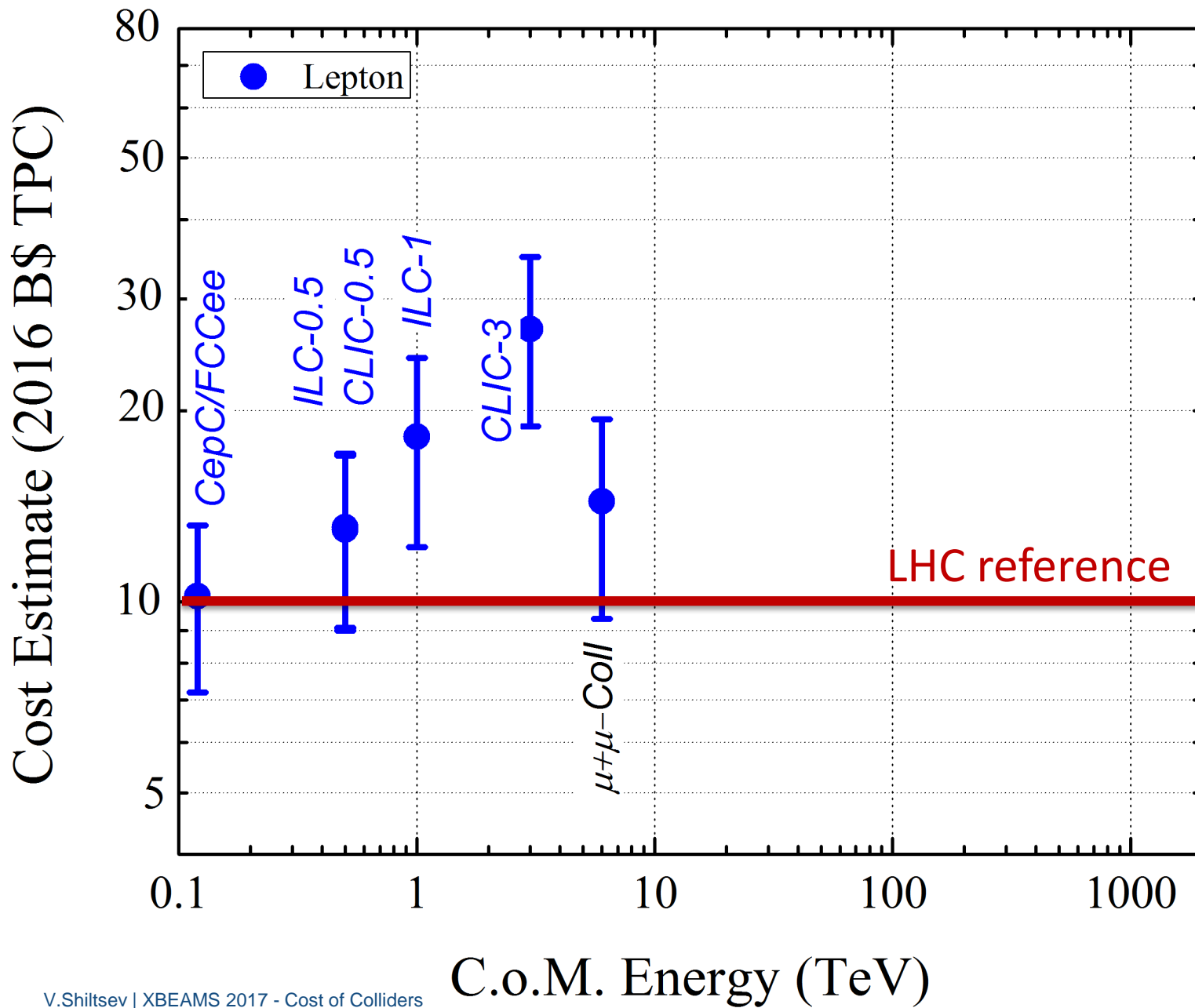
# Important Note: Two out of Three Factors in the Model are Independent from Our R&D Efforts – Tunneling, Power Infrastructure

Do not expect Cost  $\sim (L \times D^2) = \text{meter}^3$  !

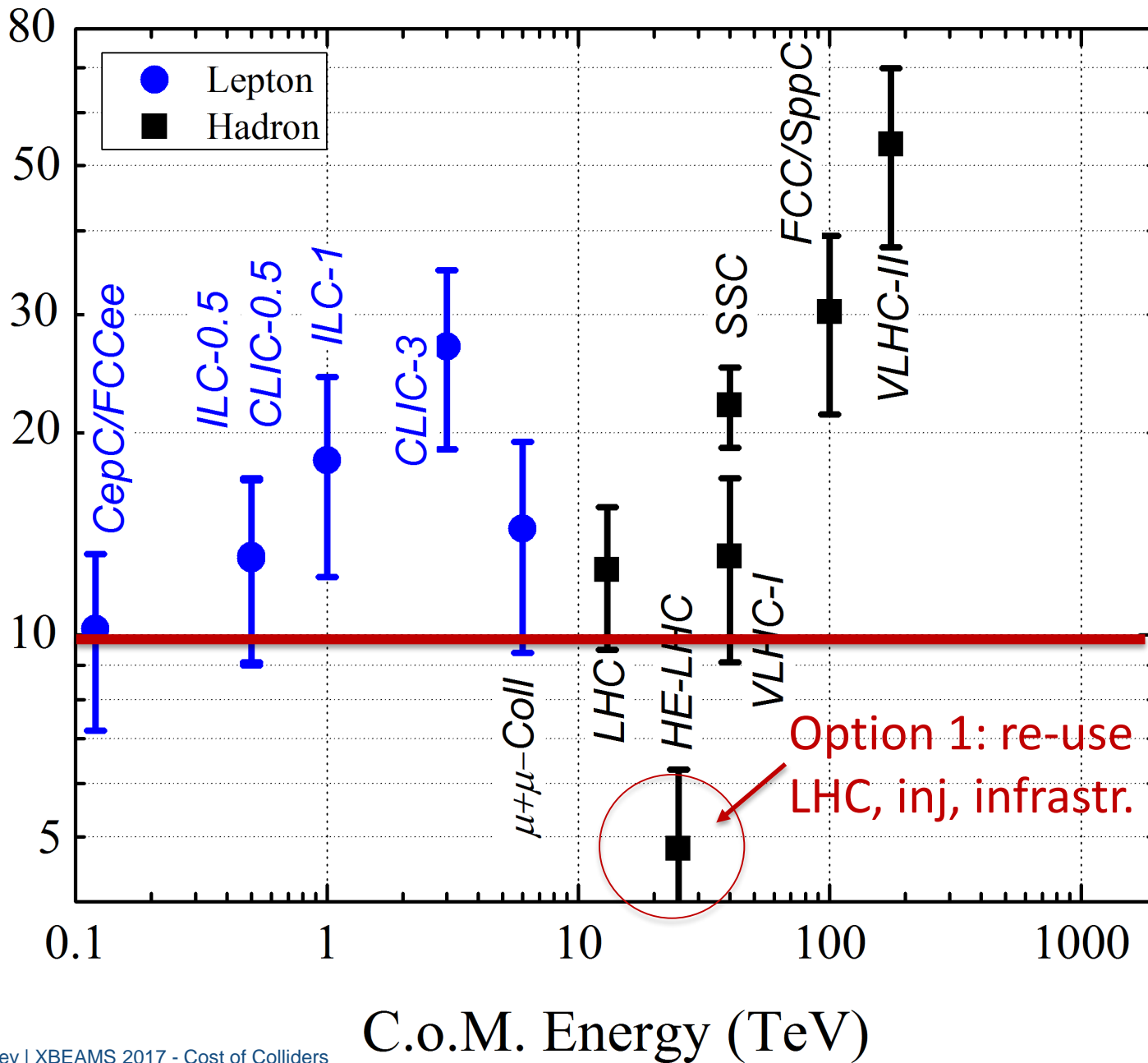


Cost  $\sim L^{(0.4-1)} D^{(0.6-1.5)}$



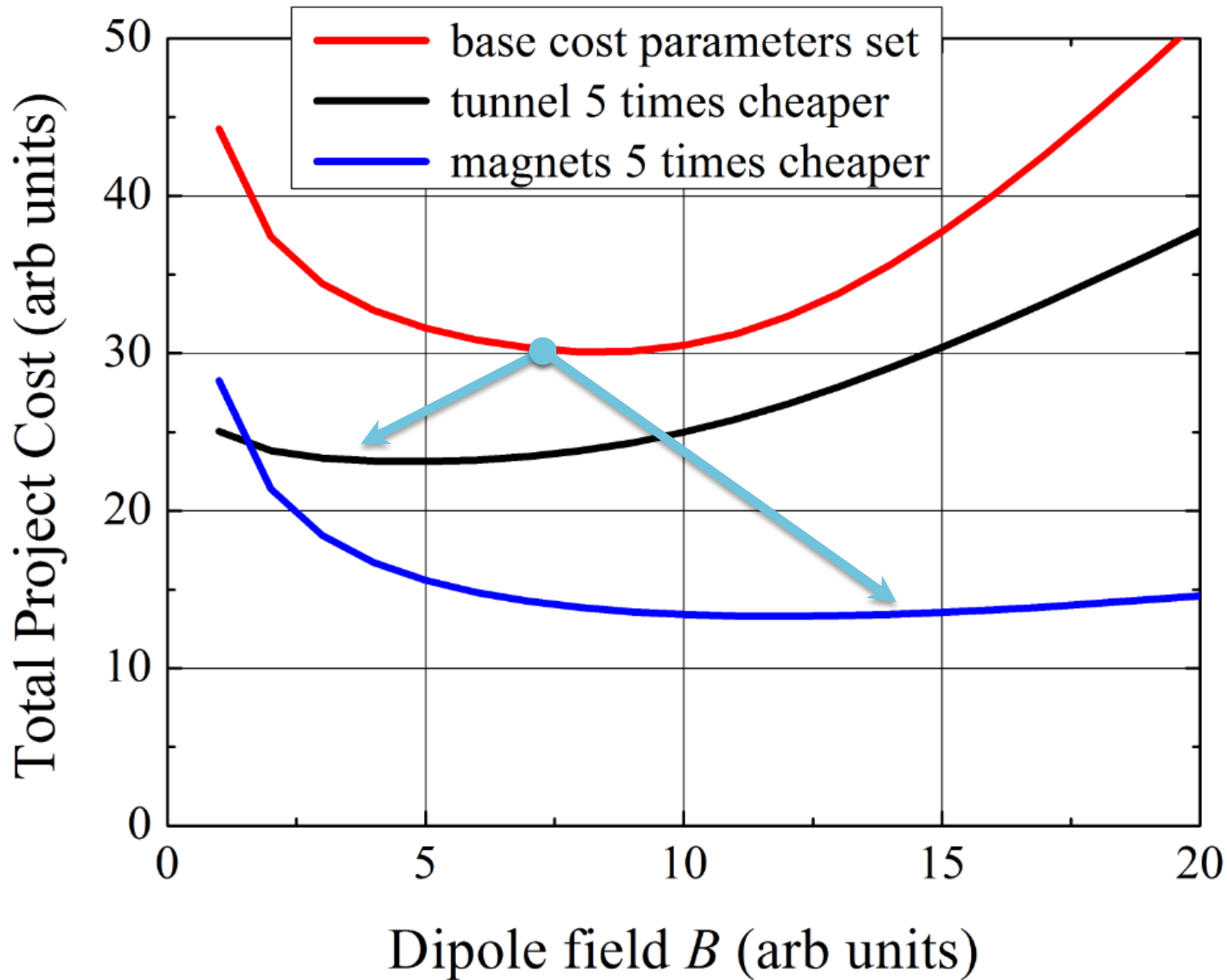


Cost Estimate (2016 B\$ TPC)



# Option 2 : Develop Technology to Lower Cost

## 100 TeV $pp$ : Qualitative Cost Dependencies

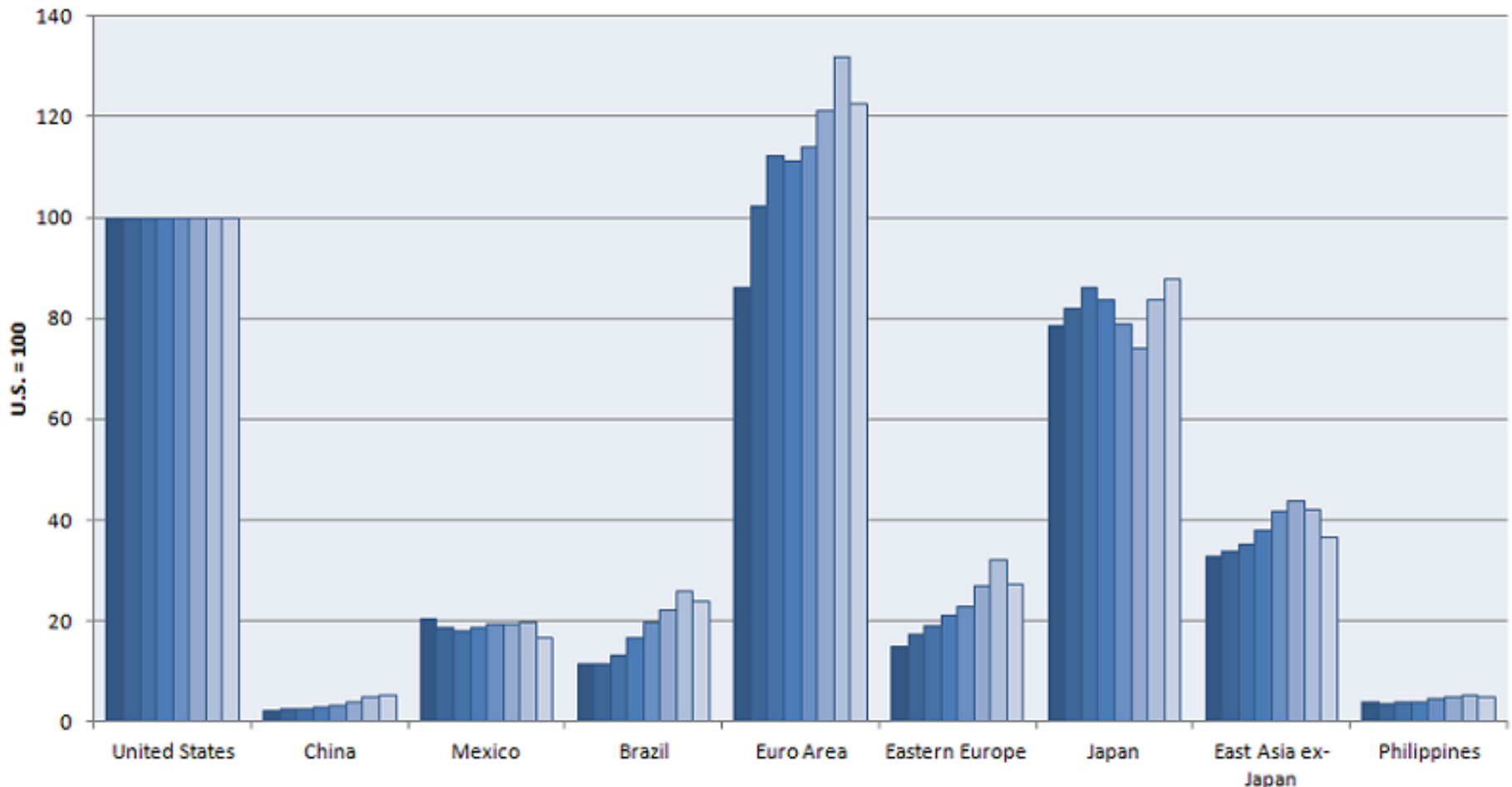


\* for illustration purposes only



# Option 3: “Move to China !”

Average hourly compensation costs of manufacturing employees, selected economies and regions, 2002-2009



Note: For a description of the economic groups, see the technical notes at [www.bls.gov/ilc/ichcctn.pdf](http://www.bls.gov/ilc/ichcctn.pdf), Table 2.

Source: U.S. Bureau of Labor Statistics, International Labor Comparisons.

# SSRF *China*



- 432 m
  - 3.5 GeV
  - 1.2B RMB
- 2007

# Spring-8 *Japan*



- 1436 m
  - 8 GeV
  - 11 BY
- 1997

# Diamond *UK*



- 562 m
  - 3 GeV
  - 383 M £
- 2007

# NSLSII *USA*



- 792 m
  - 3 GeV
  - 912 M\$
- 2015

***Account infl'n, convert to USD and scale to sqrt(1 km):***

***350 M\$***

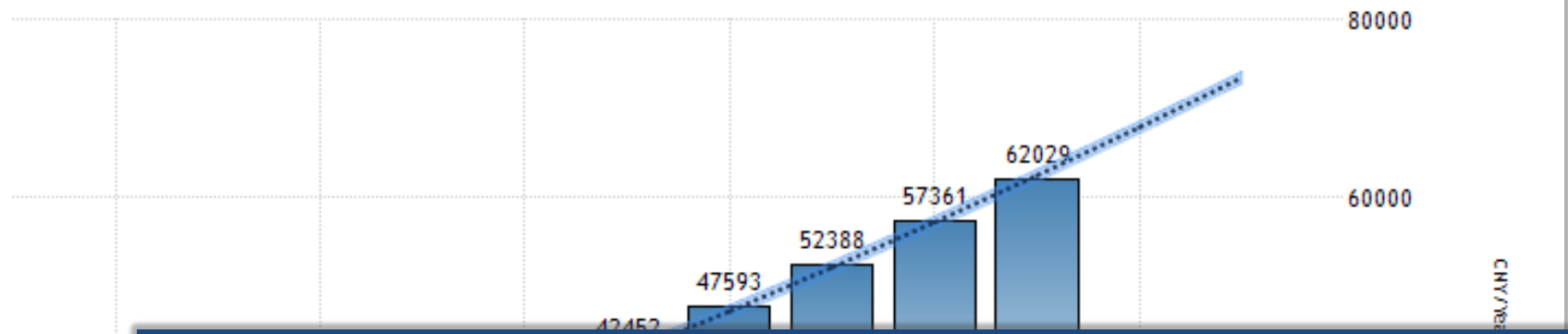
***772 M\$***

***1040 M\$***

***1024 M\$***

# “Move to China !” - Caveats

CHINA AVERAGE YEARLY WAGES



Historical Niobium Price Performance

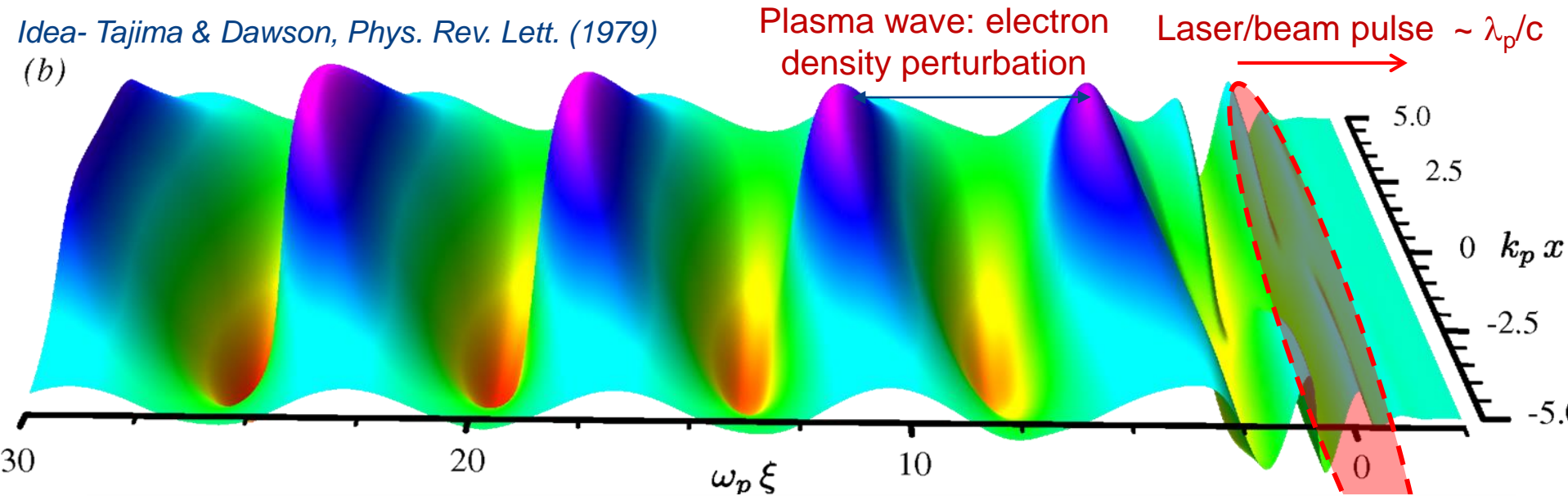


Source: DataStream, Roskill, Sumario Mineral, Departamento Nacional de Produção Mineral, República Federativa do Brasil



# Option 4: New Technology- Plasma

Idea- Tajima & Dawson, Phys. Rev. Lett. (1979)  
(b)



$$E_0 = \frac{m_e c \omega_p}{e} \approx 100 \left[ \frac{\text{GeV}}{m} \right] \cdot \sqrt{n_0 [10^{18} \text{ cm}^{-3}]}$$

**Option A:**

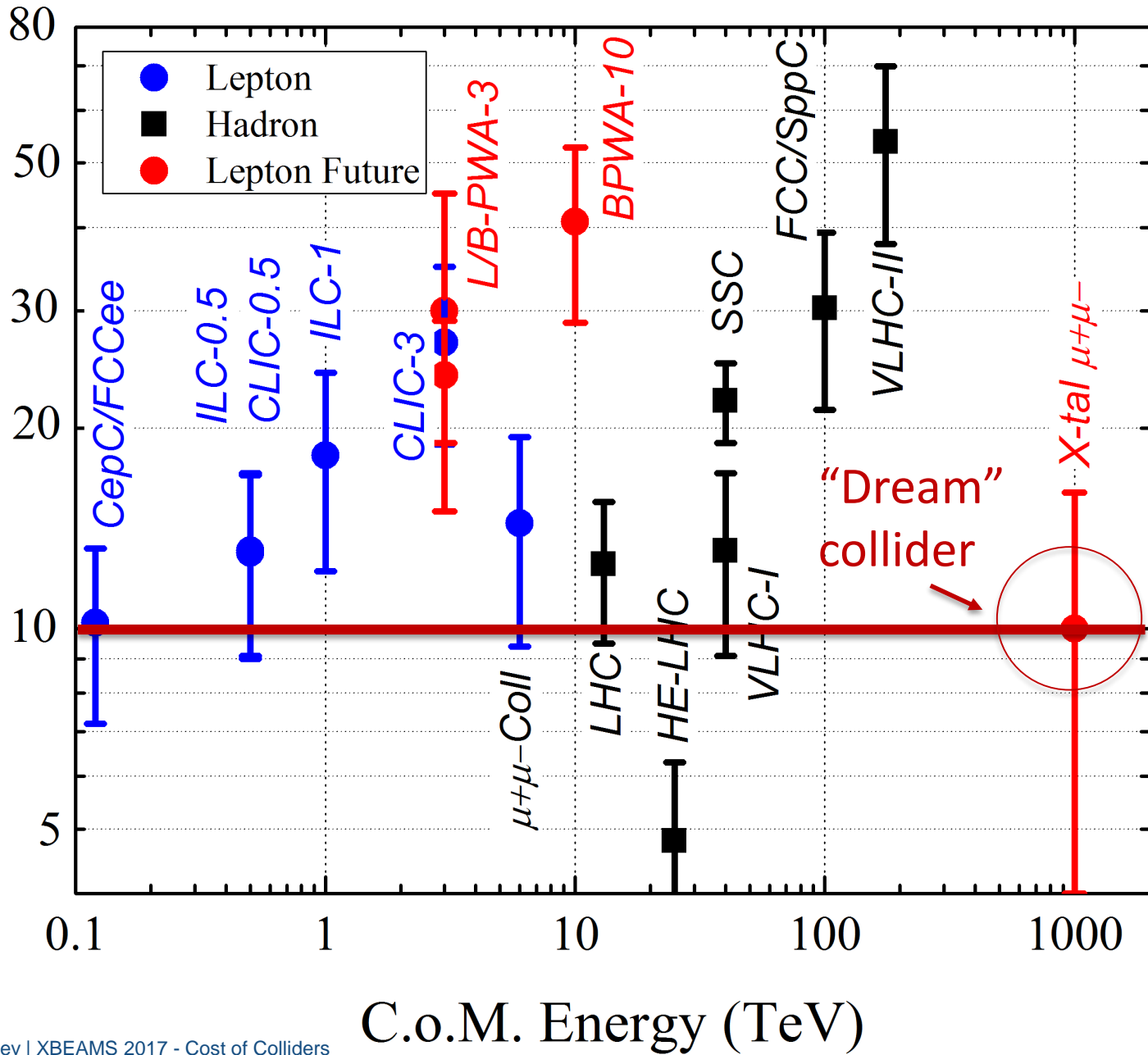
Short intense e-/e+/p bunch  
Few  $10^{16} \text{ cm}^{-3}$ , **6 GV/m** over 0.3m

**Option B:**

Short intense laser pulse  
 $\sim 10^{18} \text{ cm}^{-3}$ , **50 GV/m** over 0.1m

First looks into "Plasma-Collider": **staging kills !  $\langle E \rangle \sim 2 \text{ GV/m}, \varepsilon$**

Cost Estimate (2016 B\$ TPC)



# Option 5: $\mu^+\mu^-$ Collider

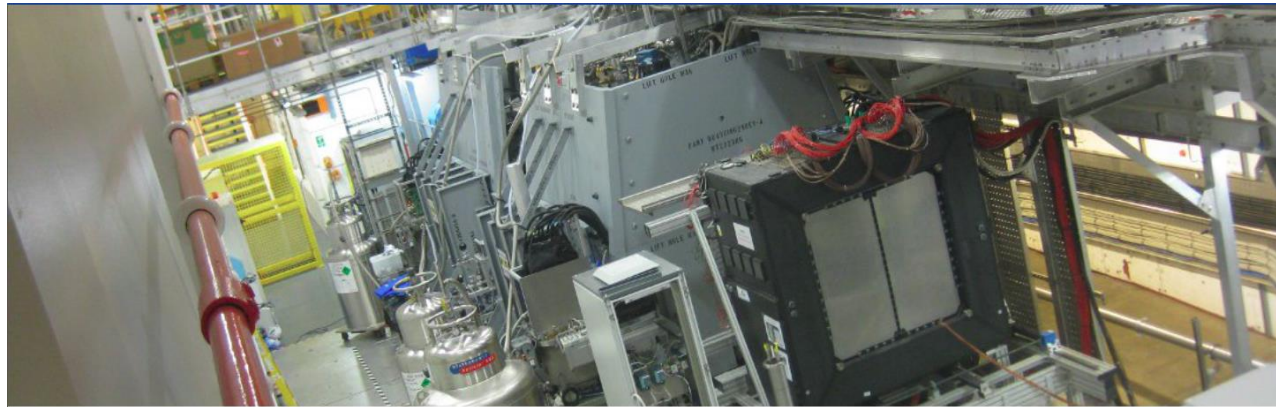
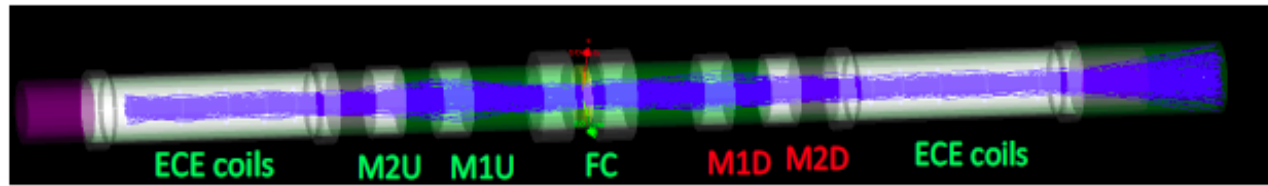
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**x5-10 more  $E_{cm}$  for same  $E_{beam}$**

- **Muons are particles for the far-future anyway**
  - The only option for a 1000 TeV collider
  - As convincingly shown Monday
- **There are opportunities even now:**
  - Even with fully traditional technology MC shows much more economical design options than any e+e-, approaching LHC in terms of Energy/\$\$ and facility power/Energy
  - MICE shows that muon cooling works
  - Great savings for labs having either proton complex or big tunnels
  - Novel approaches, like shown Mon, can offer further gains... need R&D
- **The past tells us that we were much more successful in improving performance than the energy**

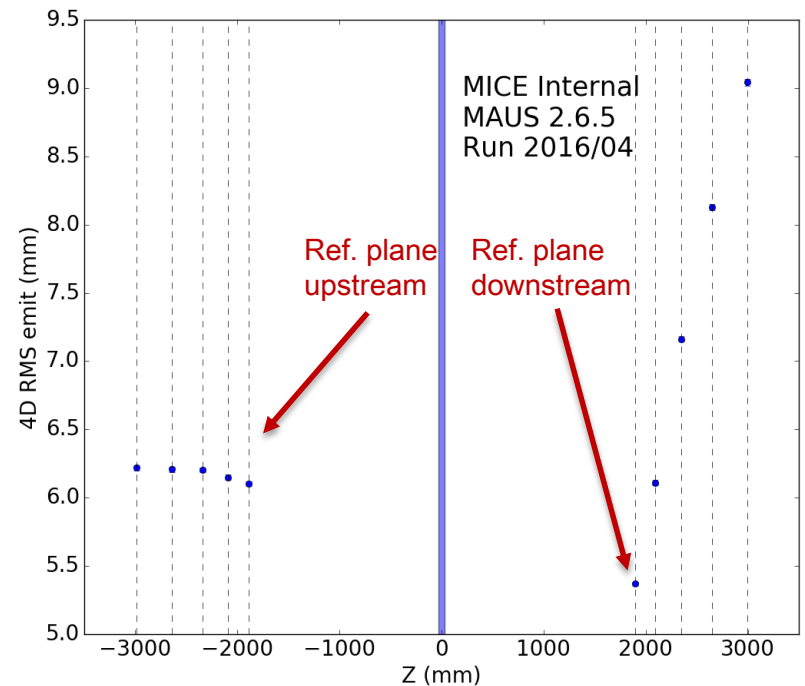
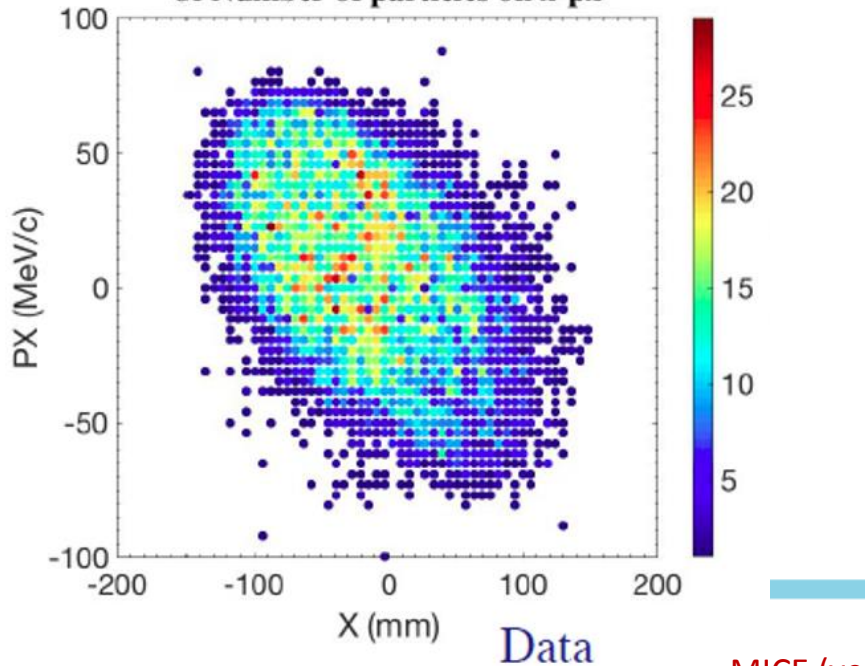


# MICE



MICE Operation and Demonstration of Muon Ionization Cooling

Horizontal Phase Space Distribution Plot for PDGid: -  
of Number of particles on x-px



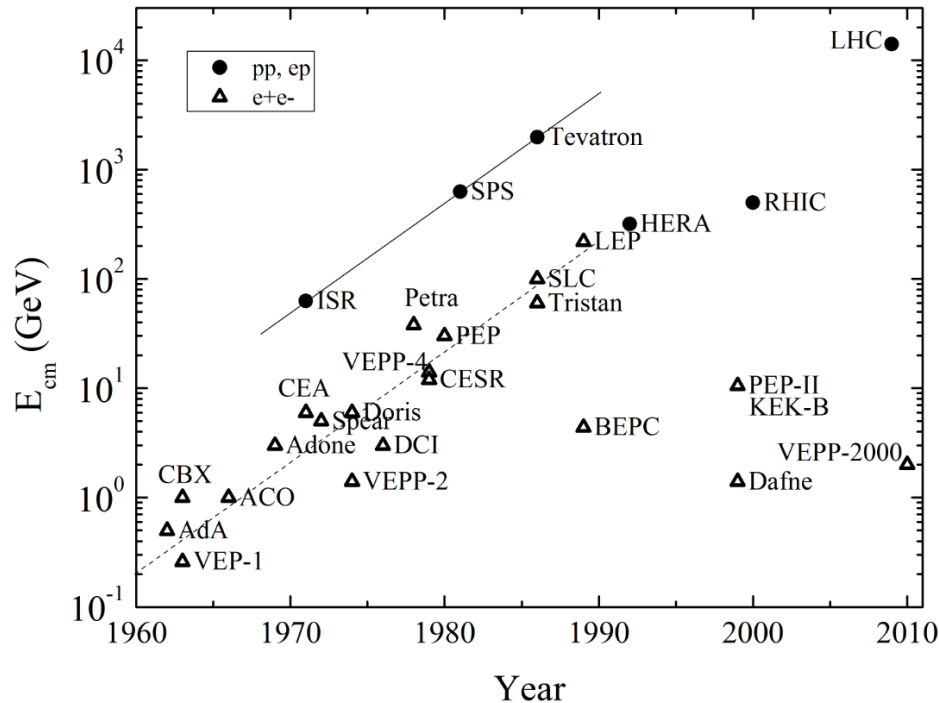
MICE (very) preliminary A.Bross, A.Liu, F.Drielsma

# Race : Energy vs Luminosity

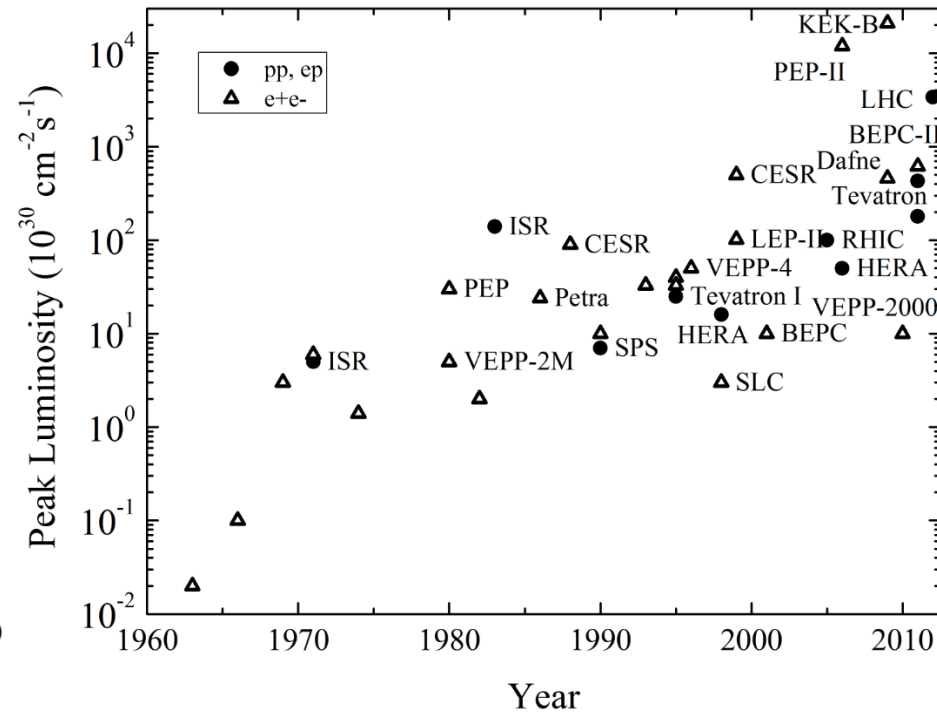
V.Shiltsev, Physics–Uspekhi, 2012, 55:10, 965–976

Over the 5 decades of developments of the particle colliders

~4 orders of magnitude in  $E$



~6 orders of magnitude in  $L$

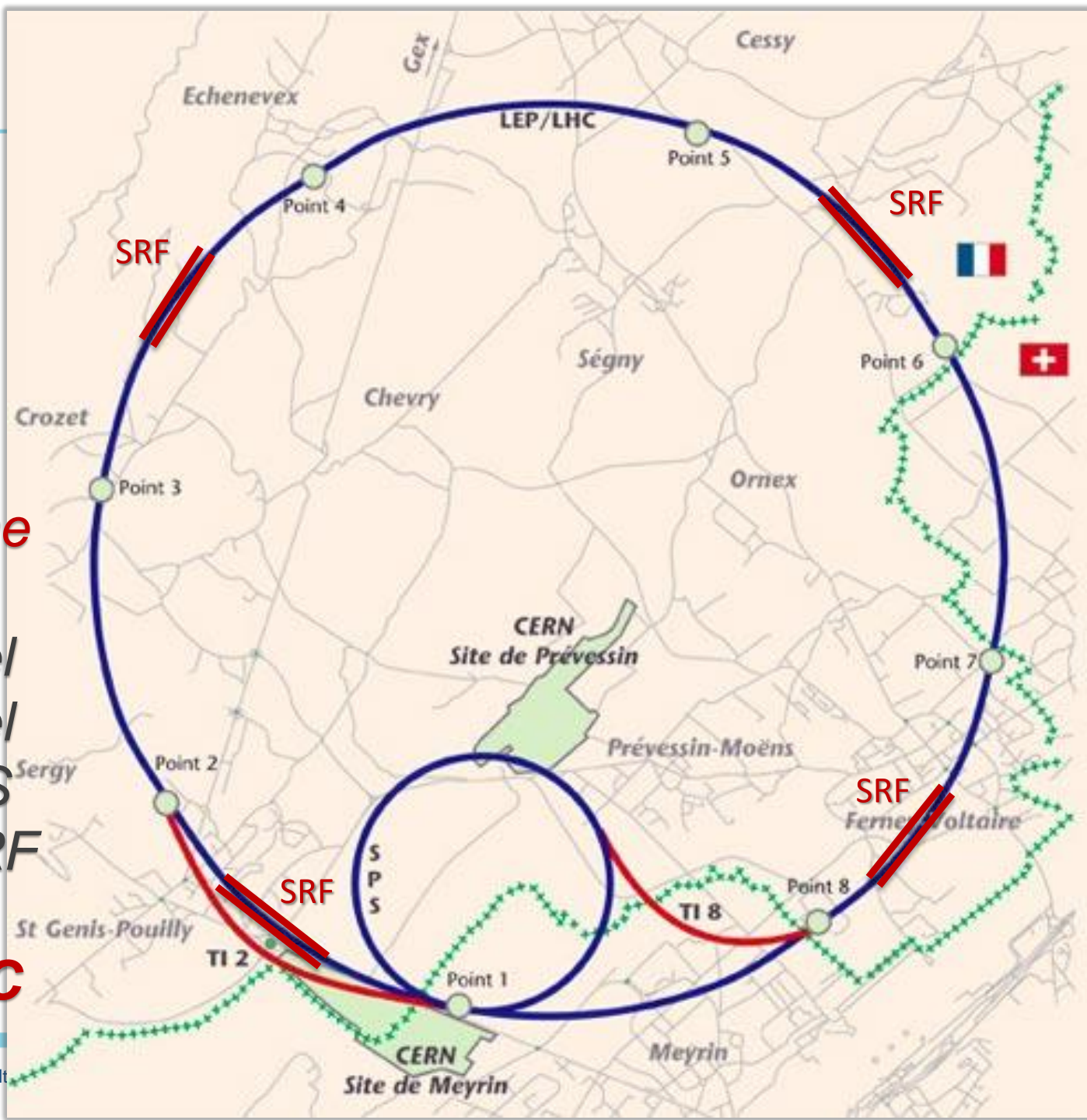


The reason (of faster pace of  $L$ ) is economical – the cost of new technological advances in acceleration is much higher than the cost of advances in performance (focusing, cooling, sources, etc)... and the latter are thus much more numerous

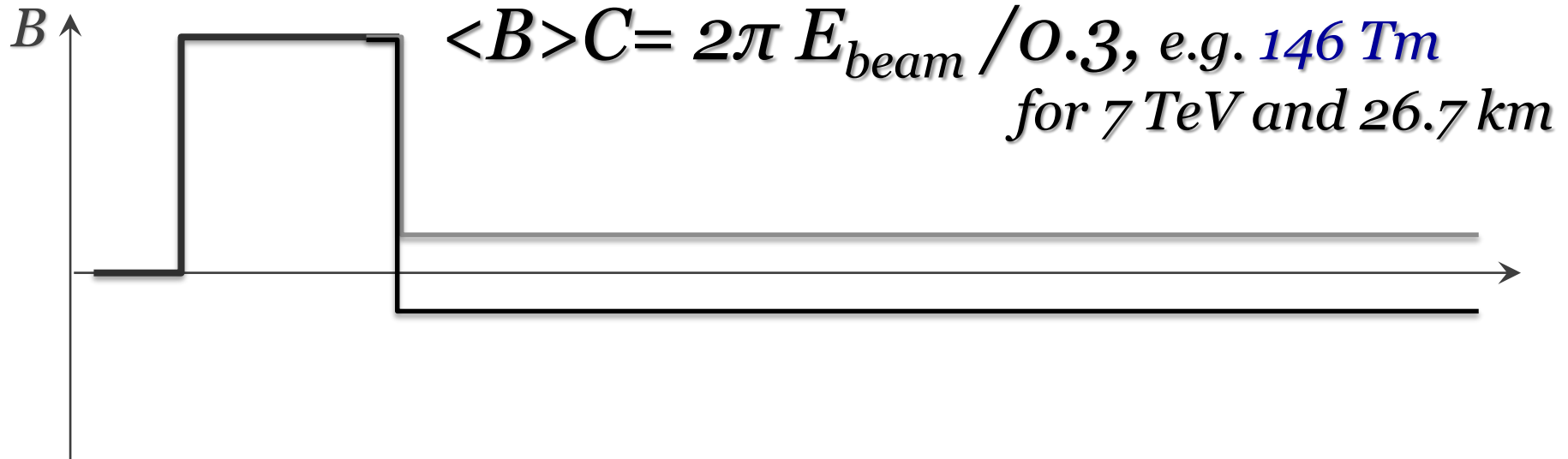
# CMC

## CERN Muon Collider

- *14 TeV cme*
- *LHC tunnel*
- *SPS tunnel*  
*and mb PS*
- *~7GeV SRF*
- *Cost ~LHC*



# Assume RCS Acceleration





# (Simple math)

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- Acceleration range:

$$R = \frac{E_{max}}{E_{min}} = \frac{B_{max}L_{SC} + B_{min}L_{pulsed}}{B_{max}L_{SC} - B_{min}L_{pulsed}}$$

- If the ratio of fields :  $f = \frac{B_{max}}{B_{min}}$  then :  $\frac{L_{pulsed}}{L_{SC}} = f \frac{R - 1}{R + 1}$

- and equation for the required fields reads :

$$\frac{2\pi}{0.3} E_{max} = \langle B \rangle C = B_{max} \Pi C \frac{2R}{R(1+f) + 1 - f}$$



# Example: 7 TeV, 26.7 km tunnel, 16T max

$$\frac{2\pi}{0.3} E_{max} = \langle B \rangle C = B_{max} \Pi C \frac{2R}{R(1+f) + 1 - f}$$

146 T × km

26.7km

16T

0.85

0.4=1/2.5

then :

$$f = \frac{B_{max}}{B_{min}}$$

$$R = \frac{f - 1}{f - 4}$$

$B_{min}$

$E_{inj}$

4.2

16

3.8T

0.45TeV

4.5

7

3.5T

1TeV

5

4

3.2T

4TeV

8

1.75

2.0T

9.1TeV

lab

# Example 2: 1 TeV, 6.9km tunnel, 16T max

$$\frac{2\pi}{0.3} E_{max} = \langle B \rangle C = B_{max} \Pi C \frac{2R}{R(1+f) + 1 - f}$$

$\uparrow$   
20.9 T × km
 $\uparrow$   
6.9km
 $\uparrow$   
16T
 $\uparrow$   
0.9
 $\uparrow$   
0.21=1/5

then :

$f = \frac{B_{max}}{B_{min}}$	$R = \frac{f - 1}{f - 9}$	$B_{min}$	$E_{inj}$
10	9	1.6T	110 GeV
9.5	17	1.7T	60 GeV

# Example 3: 60GeV, 0.7km tunnel, 16T max

$$\frac{2\pi}{0.3} E_{max} = \langle B \rangle C = B_{max} \Pi C \frac{2R}{R(1+f) + 1 - f}$$

1.26 T × km
0.7km
16T
0.9
0.125=1/8

then :

$f = \frac{B_{max}}{B_{min}}$	$R = \frac{f - 1}{f - 15}$	$B_{min}$	$E_{inj}$
16	15	1.0T	5 GeV

# To sum up: 14 TeV CMC

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- **One can build a 14 TeV cme  $\mu+\mu-$  collider at CERN if:**
  - Re-use tunnels 26.7km LHC, 6.9km SPS, 0.7km PS
  - 16 T SC magnets (DC), need ~5 km
  - Pulsed  $\pm 3.5$  T magnets, with ramp ~100ms, need ~20km
  - Pulsed  $\pm 2$  T magnets, with ramp ~10ms, need ~6km
  - Pulsed  $\pm 1$  T magnet, with ramp ~1ms, need ~1km
- **The  $\alpha\beta\gamma$ -model predicts TPC ~12B\$  $\pm 4$** 
  - 5B\$ SC magnets, 3B\$ NC magnets, 2B\$ SRF, 2B\$ 100MW power infrst.
  - ~ cost of LHC; ~6B\$ in European accounting
- **“Free cookie” – if one has 24 T SC magnets**
  - Either 4x luminosity can be achieved with collider in SPC tunnel – that requires 7 km of 24T magnets
  - Or 7 TeV cme in the LHC tunnel with just 3T pulsed magnets

# Summary

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- **Future energy frontier colliders are expensive:**
  - $\alpha\beta\gamma$ -model approx. well NC/SC Magnets and RF
  - Significant fraction is in civil and site power infrastructure
- **Possible options/preemptive measures:**
  1. Re-use existing (injectors, tunnels, etc)
    - Though saves a lot, works only at few places (big existing labs)
  2. Develop traditional technology to lower cost by a factor (SC mag, SRF)
    - Decade(s) of R&D, ongoing... need to be more aggressive
  3. “*Move to China!*” or some other place to save big factor
    - The advantage might disappear in 10-15 years from now
  4. Wait till new acceleration technology matures (plasma) and lower cost
    - Progress over past 2 decades impressive but no sign of cost feasibility yet... R&D
  5. “*Get more with same energy*” =  $\mu+\mu^-$  (e.g., 14 TeV CERN MC)
    - Need to develop challenging pulsed magnets (NC? SC?), other smart ideas
    - But the switch to muons is inevitable in a long run...



*Thank You for Your  
Attention!*

## Back up slides

- Cost  $\sim$  Size<sup>3</sup>
- Power (MVA)  $\sim$  Size<sup>4</sup>
- So, Cost  $\sim$  (Power)<sup>3/4</sup>

From basic theory

*Electrical Transmission  
and Distribution  
Reference Book*

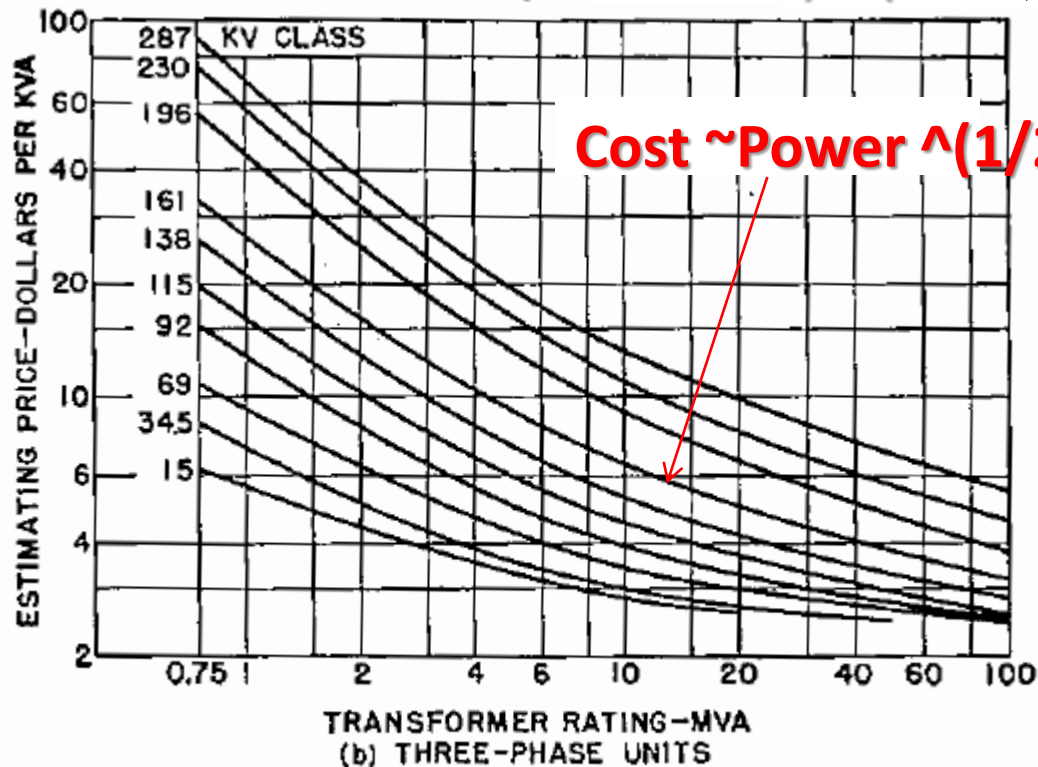
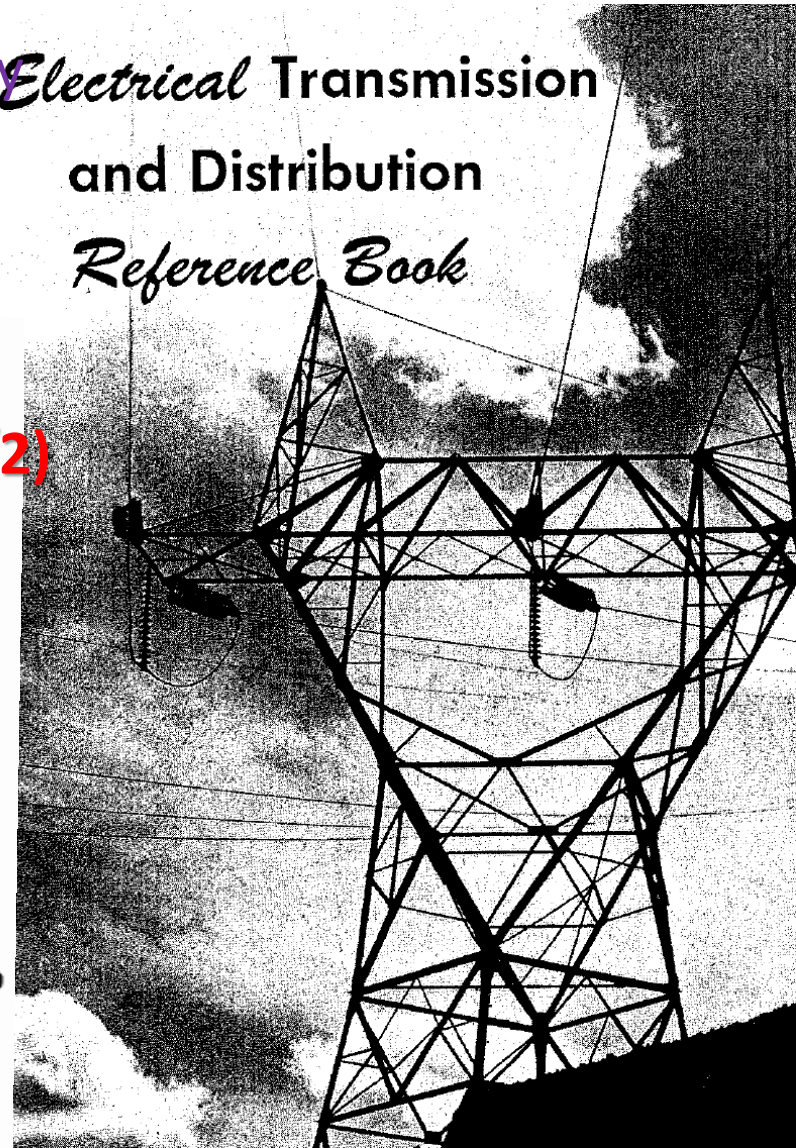
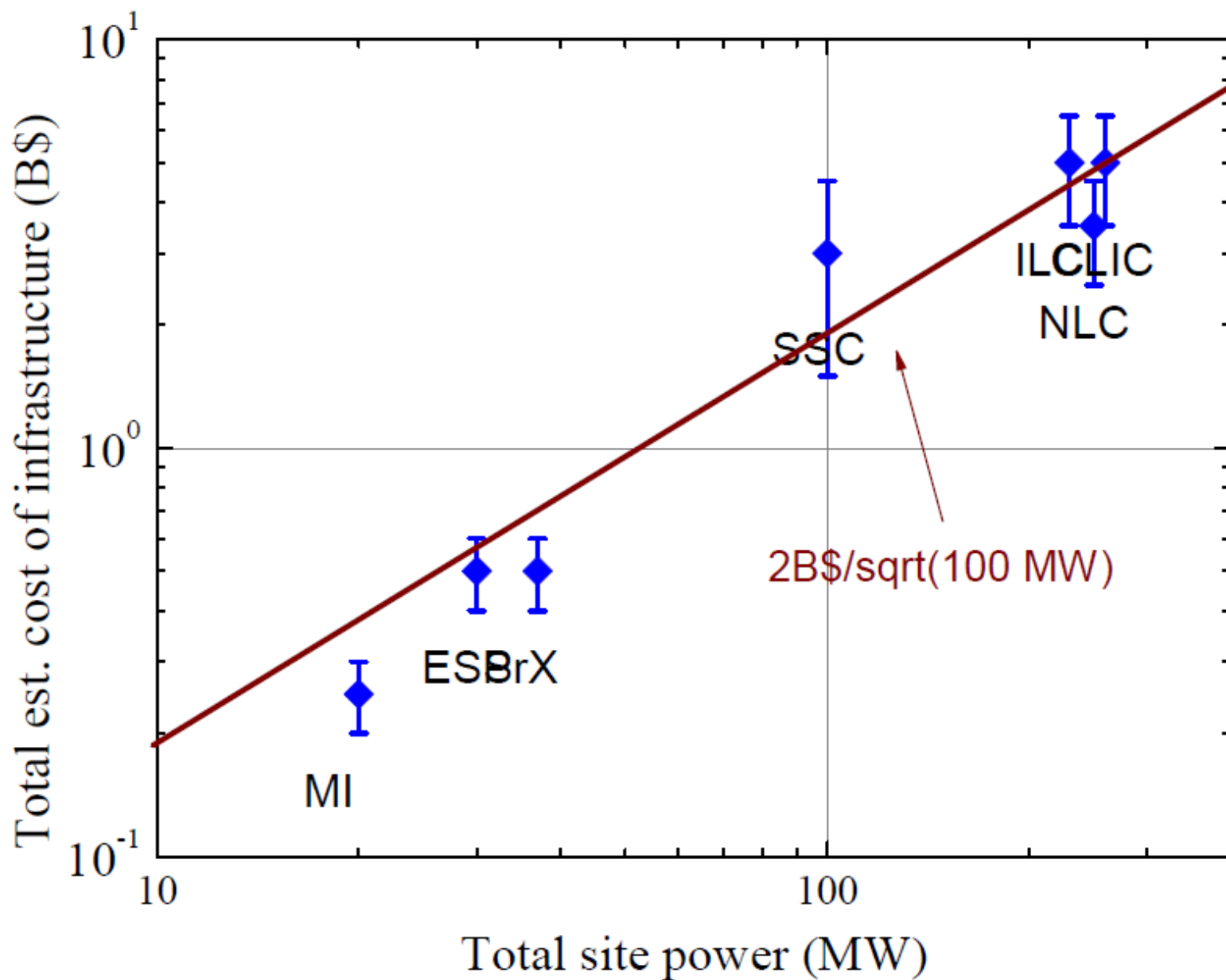
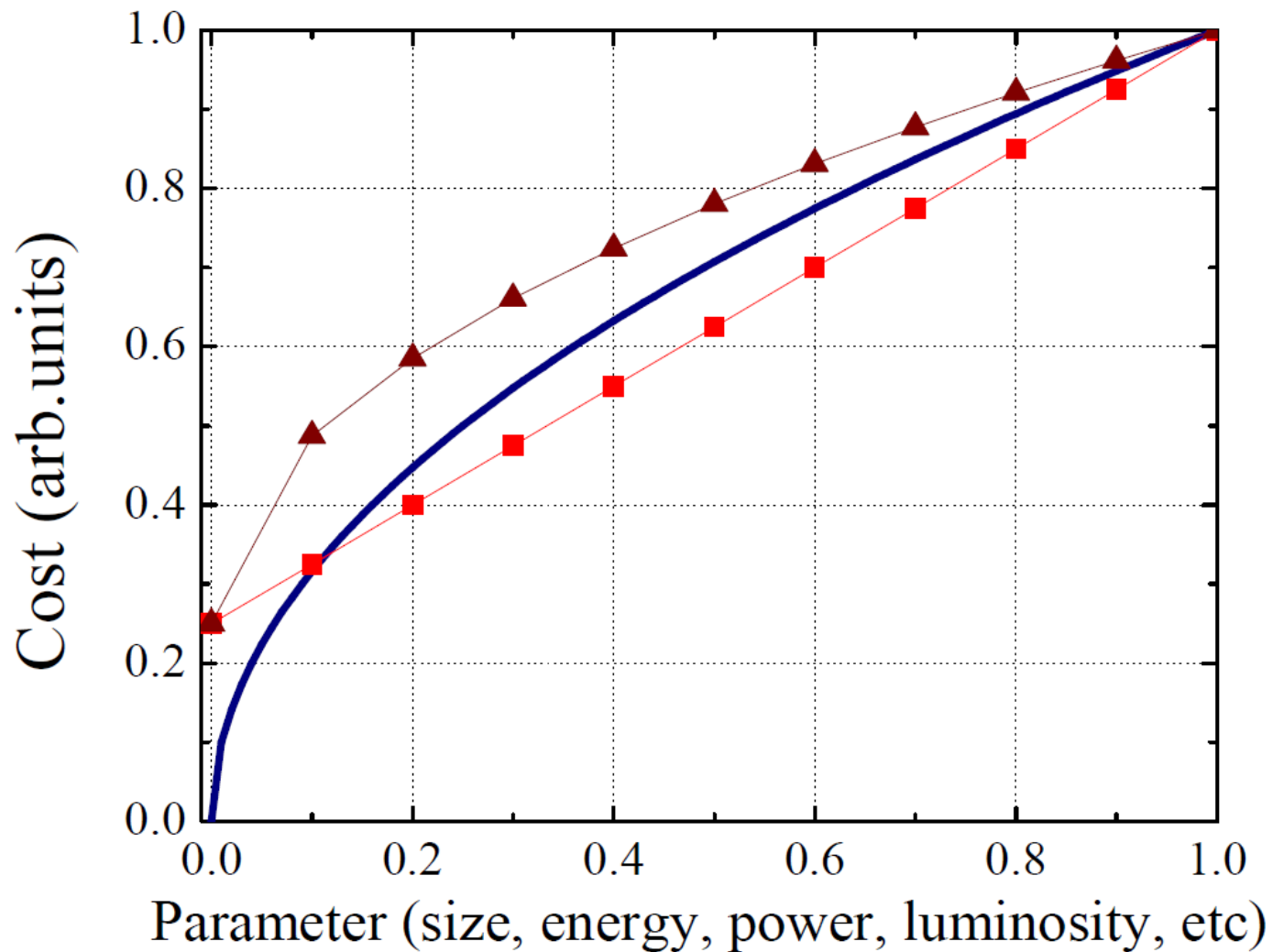


Fig. 48—Curve for estimating prices of oil-immersed, 60-cycle, two-winding, type OA power transformers.





- Recurring theme: “zero-cost” + some growing function can be reasonably well described by  $\sqrt{\text{Parameter}}$



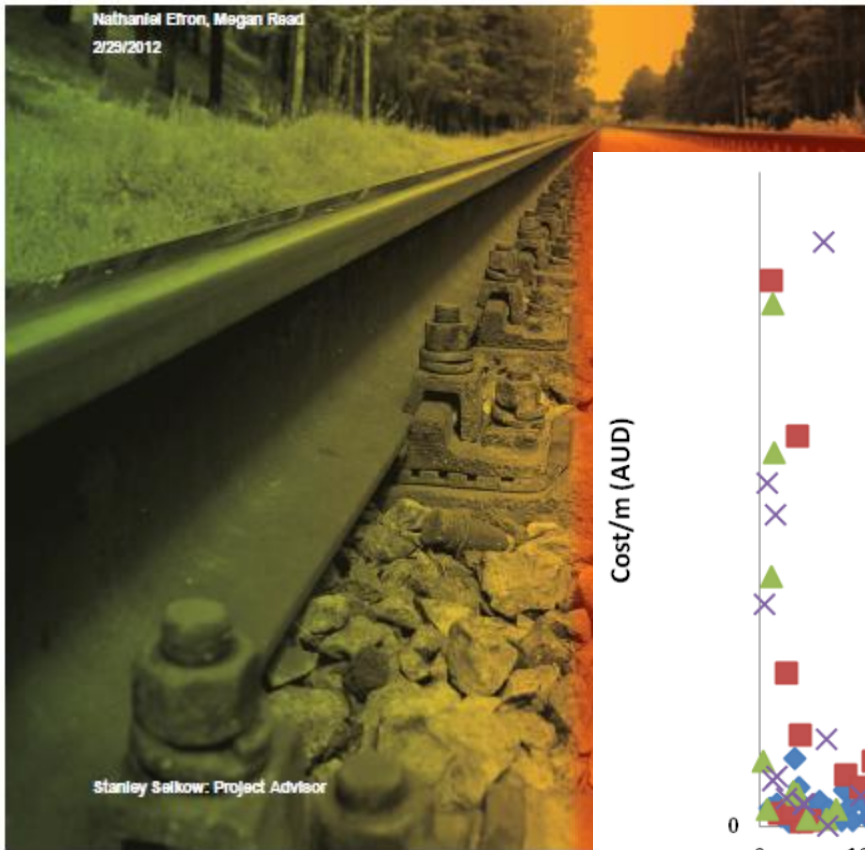


## Cost of Tunnel

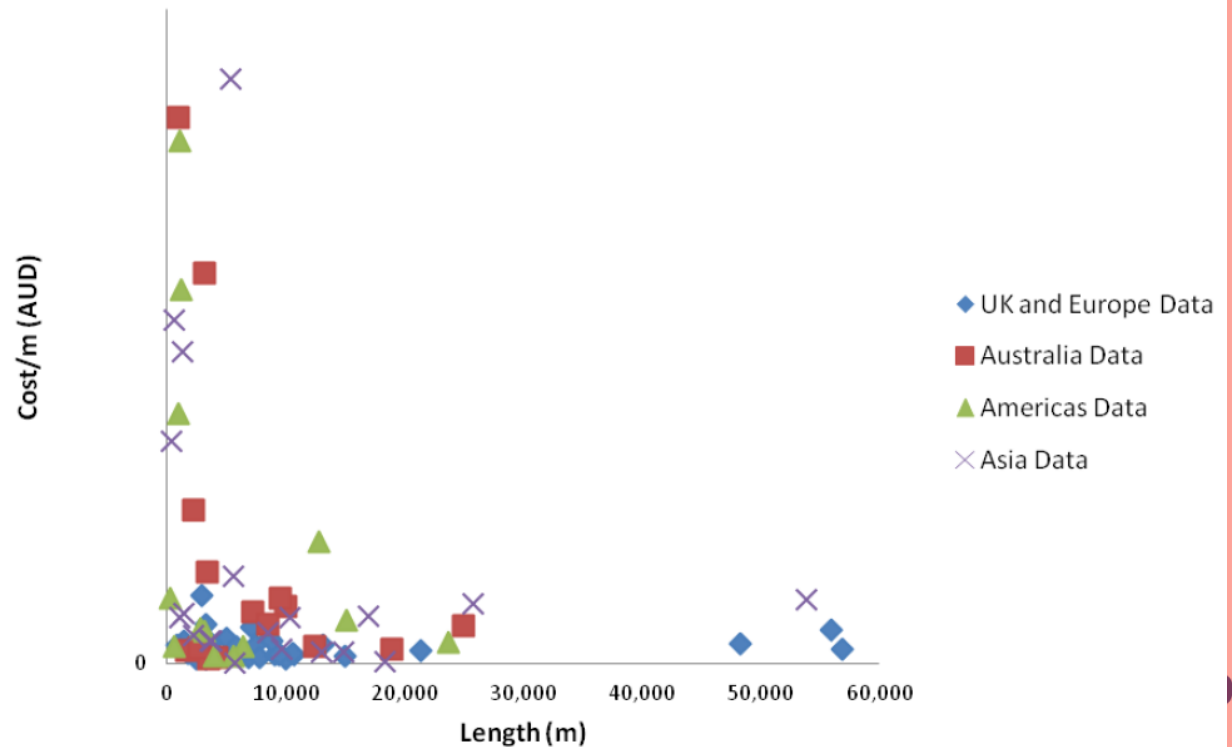
WORCESTER POLYTECHNIC INSTITUTE

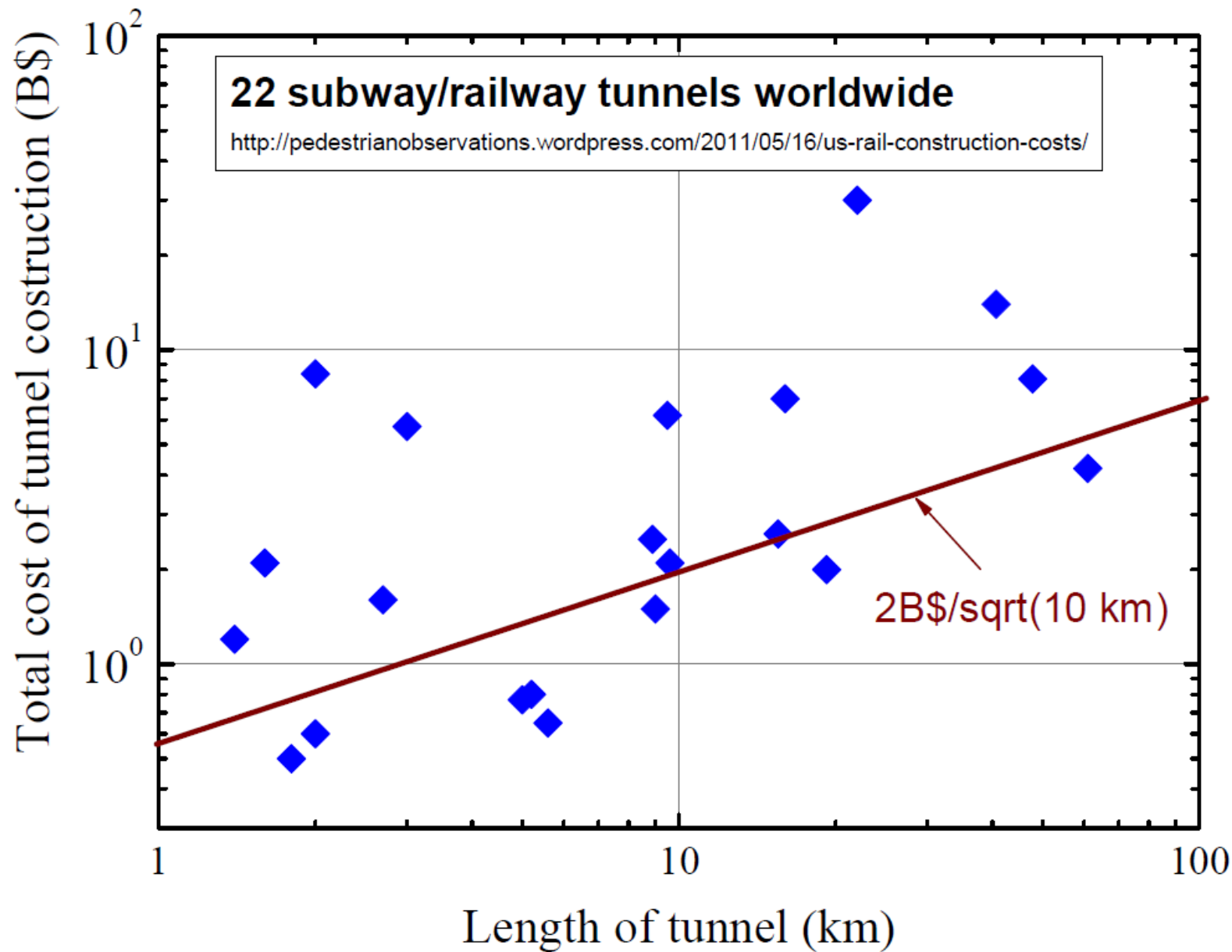
# Analysing International Tunnel Costs

An Interactive Qualifying Project



- Some 100 tunnels world wide





# More on Tunneling cost

- Do not expect  $\text{Cost} \sim (L \times D^2) = \text{meter}^3$  !

Tunnelling and Underground Space Technology 33 (2013) 22–33

*Data on 270 tunnels  
world wide*

Planning level tunnel cost estimation based on statistical analysis of historical data

Jamal Rostami<sup>a</sup>, Mahmoud Sepehrmanesh<sup>b</sup>, Ehsan Alavi Gharahbagh<sup>a,\*</sup>, Navid Mojtabai<sup>c</sup>

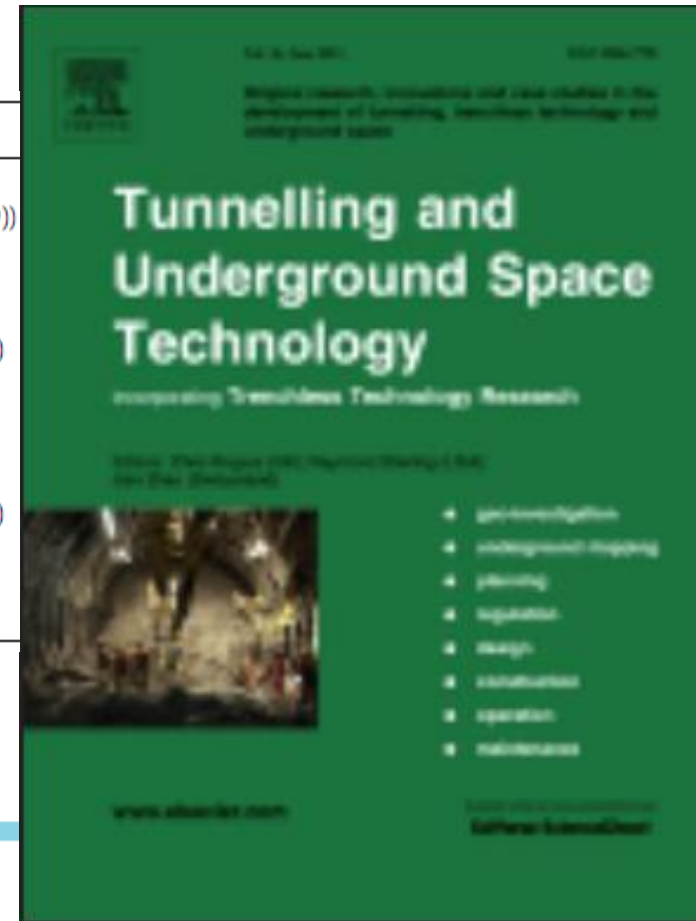
**Table 9**  
Summary of unit cost and multi-variable regression analyses.

Application	Type of excavation	Multi-variable regression equation
Highway	Conventional	$\text{Cost (M\$)} = 10^{(1.51 + 1.02 \log(L) + 0.374 \log(D))}$
Waste water	Conventional	$\text{Cost (M\$)} = 10^{(-0.391 + 1.63 \log(L) + 1.11 \log(D))}$
Waste water	Mixed	$\text{Cost (M\$)} = 10^{(1.03 + 0.761 \log(L) + 0.804 \log(D))}$
Waste water	Hard rock mechanized	$\text{Cost (M\$)} = 10^{(0.319 + 0.901 \log(L) + 1.35 \log(D))}$
Waste water	Soft ground mechanized	$\text{Cost (M\$)} = 10^{(0.377 + 1.02 \log(L) + 1.53 \log(D))}$
Waste water	Micro-tunneling	$\text{Cost (M\$)} = 10^{(0.553 + 0.975 \log(L) + 0.374 \log(D))}$
Subway	Conventional	$\text{Cost (M\$)} = 10^{(1.10 + 0.933 \log(L) + 0.614 \log(D))}$
Subway	Mixed	$\text{Cost (M\$)} = 10^{(1.47 + 0.760 \log(L) + 0.527 \log(D))}$
Subway	Hard rock mechanized	$\text{Cost (M\$)} = -97.2 + 11.7L + 28.3D$
Subway	Soft ground mechanized	$\text{Cost (M\$)} = 10^{(1.23 + 1.05 \log(L) + 0.636 \log(D))}$
Water	Conventional	$\text{Cost (M\$)} = 10^{(0.917 + 0.669 \log(L) + 0.658 \log(D))}$
Water	Mixed	$\text{Cost (M\$)} = 10^{(1.94 + 0.414 \log(L) + 0.053 \log(D))}$
Water	Hard rock mechanized	$\text{Cost (M\$)} = 10^{(0.553 + 0.866 \log(L) + 1.23 \log(D))}$
Water	Soft ground mechanized	$\text{Cost (M\$)} = 10^{(1.07 + 0.725 \log(L) + 1.02 \log(D))}$

L: Length of the tunnel (km).

D: Equivalent diameter (m).

$$\text{Cost} \sim L^{(0.4-1)} D^{(0.6-1.5)}$$



TUPMY001

Proceedings of IPAC2016, Busan, Korea

## VERY LOW EMITTANCE MUON BEAM USING POSITRON BEAM ON TARGET

M. Antonelli, M. Biagini, M. Boscolo, A. Variola INFN/LNF, Frascati, Italy  
 P. Raimondi, ESRF Grenoble, France  
 G. Cavoto INFN Roma, Italy E. Bagli INFN Ferrara, Italy

	positron source	proton source
$\mu$ rate[Hz]	$9 \cdot 10^{10}$	$2 \cdot 10^{13}$
$\mu$ /bunch	$4.5 \cdot 10^7$	$2 \cdot 10^{12}$
normalised $\epsilon$ [ $\mu\text{m-mrad}$ ]	40	25000

The muon collider ring would have bunches of  $\mu^+$  and  $\mu^-$  with energy of 22 GeV with  $4.5 \cdot 10^7$  muon particles, emittance 0.19  $\mu\text{m-mrad}$ , and beam energy spread of 9%, produced with a spacing of 500  $\mu\text{s}$  (2 KHz rate). Bunches

Promising values of luminosities can be obtained with these parameters, being in the range of  $L \approx 10^{34} \text{ cm}^{-2}\text{s}^{-1}$ .

