

Interactions of Particles with Matter













EIROFORUM School of Instrumentation

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The 'Standard Model'




matter particles

	1st gen.	2nd gen.	3rd gen.
Q U A R K	 <i>up</i>	 <i>charm</i>	 <i>top</i>
	 <i>down</i>	 <i>strange</i>	 <i>bottom</i>
L E P T O N	 <i>e neutrino</i>	 <i>μ neutrino</i>	 <i>τ neutrino</i>
	 <i>electron</i>	 <i>muon</i>	 <i>tau</i>

gauge particles

Strong Force  <i>Gluon</i>
Electro-Magnetic Force  <i>photon</i>
Weak Force  <i>W bosons</i> <i>Z boson</i>

scalar particle(s)

 <i>Higgs</i>			• • •
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The 'Standard Model'

$$\begin{aligned}
 L_{GSW} = & L_0 + L_H + \sum_l \left\{ \frac{g}{2} \bar{L}_l \gamma_\mu \bar{\tau} L_l \bar{A}^\mu + g' \left[\bar{R}_l \gamma_\mu R_l + \frac{1}{2} \bar{L}_l \gamma_\mu L_l \right] B^\mu \right\} + \\
 & + \frac{g}{2} \sum_q \bar{L}_q \gamma_\mu \bar{\tau} L_q \bar{A}^\mu + \\
 & + g' \left\{ \frac{1}{6} \sum_q [\bar{L}_q \gamma_\mu L_q + 4 \bar{R}_q \gamma_\mu R_q] + \frac{1}{3} \sum_{q'} \bar{R}_{q'} \gamma_\mu R_{q'} \right\} B^\mu
 \end{aligned}$$

$$\begin{aligned}
 L_H = & \frac{1}{2} (\partial_\mu H)^2 - m_H^2 H^2 - h \lambda H^3 - \frac{h}{4} H^4 + \\
 & + \frac{g^2}{4} (W_\mu^+ W^\mu + \frac{1}{2 \cos^2 \theta_W} Z_\mu Z^\mu) (\lambda^2 + 2 \lambda H + H^2) + \\
 & + \sum_{l,q,q'} (\frac{m_l}{\lambda} \bar{l} l + \frac{m_q}{\lambda} \bar{q} q + \frac{m_{q'}}{\lambda} \bar{q}' q') H
 \end{aligned}$$

Over the last century
this 'Standard Model' of
Fundamental Physics was discovered
by studying

Radioactivity

Cosmic Rays

Particle Collisions (Accelerators)

A large variety of Detectors and
experimental techniques have been
developed during this time.

Scales

$$E = m a^2$$

$$E = m b^2$$

$$E = m c^2 \quad \leftarrow \text{Energy} \hat{=} \text{Mass}$$

⋮

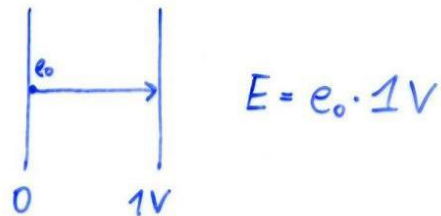
$$m(\text{electron}) = 9.1 \cdot 10^{-31} \text{ kg}$$

$$m_e c^2 = 8.19 \cdot 10^{-14} \text{ J}$$

$$= 510\,999 \text{ Electron Volt (eV)}$$

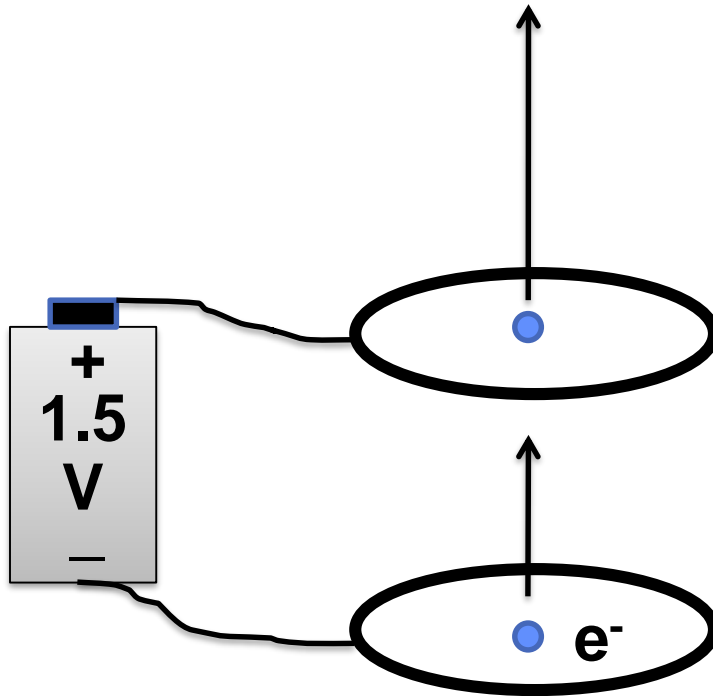
$$= 0.511 \text{ MeV}$$

$$1 \text{ Electron Volt} = e_0 \cdot 1V = 1.603 \cdot 10^{-19} \text{ J}$$



1 Electron Volt - Energy an Electron gains as it traverses a Potential Difference of 1V

Build your own Accelerator



$$E_{\text{kin}} = 1.5\text{eV} =$$

$$2\,615\,596\text{ km/h}$$

Scales

8

Visible Light:

$\lambda = 500 \text{ nm}$, $h\nu \approx 2.5 \text{ eV}$

Excited States in Atoms:

1-100 keV "X-Rays"

Nuclear Physics:

1-50 MeV

Particle Physics:

1-1000 GeV (LHC 14 TeV)

Highest Measured Energy:

10^{20} eV (Cosmic Rays)

Basics

9

Lorentz Boost:

$$\mu^- \rightarrow e^- + \bar{\nu}_e + \nu_\mu \quad \tau = 2.2 \cdot 10^{-6} \text{ s}$$

E.g. Produced by Cosmic Rays (p, He, Li ...)
colliding with air in the upper Atmosphere $\sim 10 \text{ km}$

$$s = \tau \cdot \gamma \sim c \cdot \tau = 660 \text{ m}$$

But we see Muons here on Earth

$$E_\mu \sim 2 \text{ GeV}, m_\mu c^2 = 105 \text{ MeV} \rightarrow \gamma \sim 19$$

$$\text{Relativity: } \bar{\tau} = \tau \cdot \gamma$$

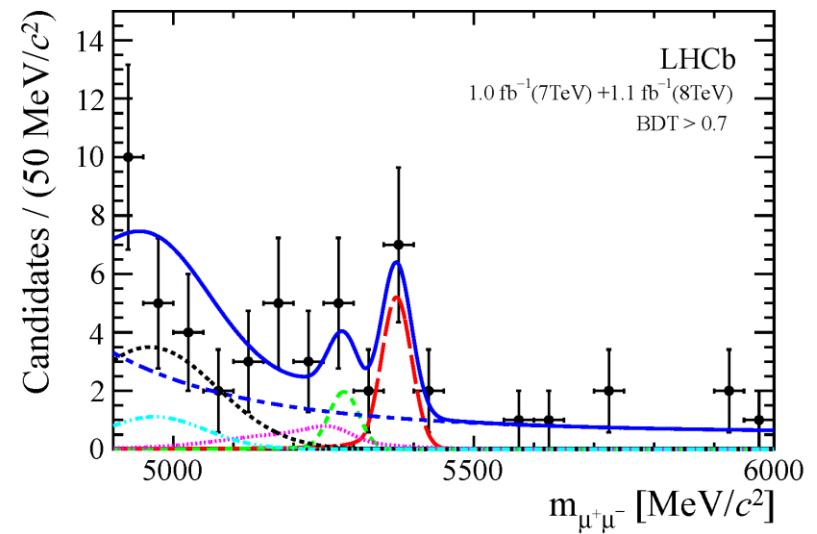
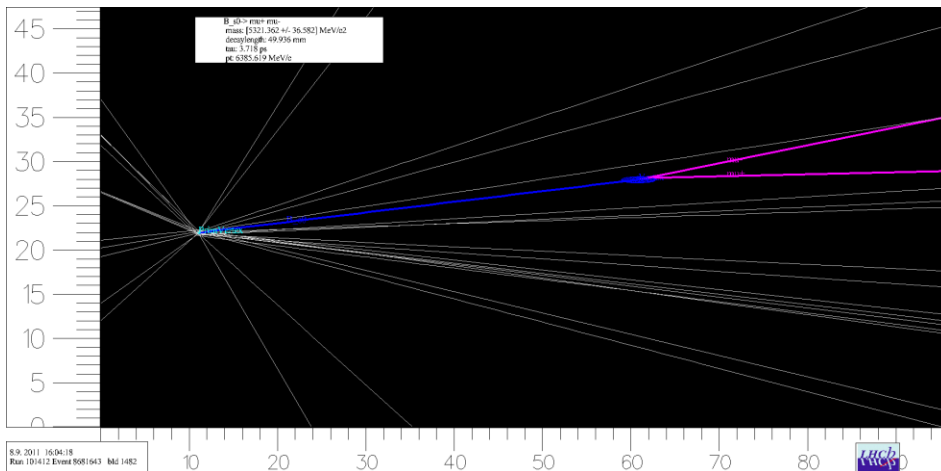
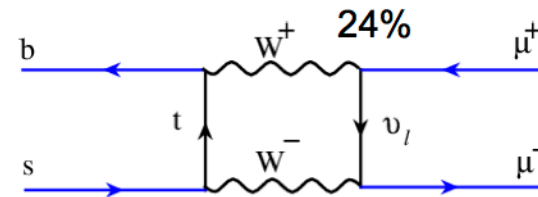
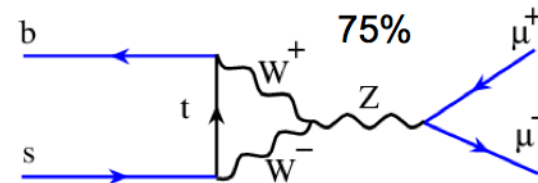
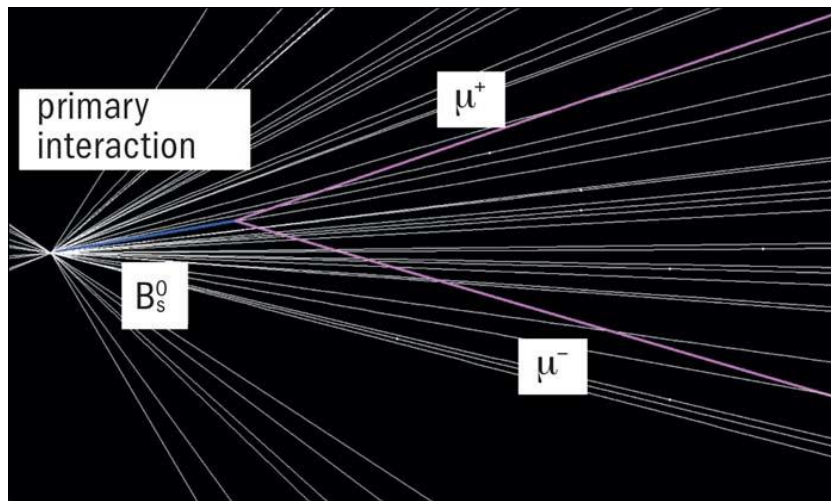
$$s = c \cdot \bar{\tau} = 12.5 \text{ km} \rightarrow \text{Earth}$$

$$\text{Pions: } \pi^+, \pi^- \quad \tau \sim 2.6 \cdot 10^{-8} \text{ s}, m_\pi c^2 = 135 \text{ MeV}$$

$$2 \text{ GeV} \rightarrow s = 115 \text{ m}$$

Pions were discovered in Emulsions exposed
to Cosmic Rays on high Mountains.

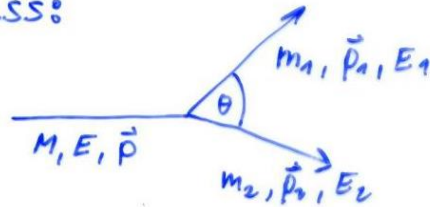
LHCb B decay, displaced Vertex



Basics

Invariant Mass:

LAB:



Relativity: $\tilde{a} = \begin{pmatrix} a_0 \\ \vec{a} \end{pmatrix}$ $\tilde{b} = \begin{pmatrix} b_0 \\ \vec{b} \end{pmatrix}$ $\tilde{a} \tilde{b} = a_0 b_0 - \vec{a} \cdot \vec{b}$

$$E = mc^2 \gamma, \quad \vec{p} = m \vec{v} \gamma$$

$$\tilde{p} = \begin{pmatrix} \frac{E}{c} \\ \vec{p} \end{pmatrix}, \quad \tilde{p}_1 = \begin{pmatrix} \frac{E_1}{c} \\ \vec{p}_1 \end{pmatrix}, \quad \tilde{p}_2 = \begin{pmatrix} \frac{E_2}{c} \\ \vec{p}_2 \end{pmatrix}$$

$$\tilde{p} = \tilde{p}_1 + \tilde{p}_2 \quad \text{Energy + Momentum Conservation}$$

$$\tilde{p}^2 = (\tilde{p}_1 + \tilde{p}_2)^2 \rightarrow \tilde{p} \tilde{p} = \tilde{p}_1 \tilde{p}_1 + \tilde{p}_2 \tilde{p}_2 + 2 \tilde{p}_1 \tilde{p}_2$$

$$\underline{M^2 c^2 = m_1^2 c^2 + m_2^2 c^2 + 2 \left(\frac{E_1 E_2}{c^2} - p_1 p_2 \cos \theta \right)}$$

- Measuring Momenta and Energies OR
- Measuring Momenta and identifying Particles
gives the Mass of the original Particle

$\pi^{\pm}, W^{\pm}, Z^0, q, e, \mu, \tau, \nu_e, \nu_{\mu}, \nu_{\tau}, \pi^{\pm}, \pi^0, \eta, f_0(660), \rho(770),$
 $\omega(782), \eta'(958), f_0(980), a_0(980), \phi(1020), h_1(1170), b_1(1235),$
 $a_1(1260), f_2(1270), f_1(1285), \eta(1295), \pi(1300), a_2(1320),$
 $f_0(1370), f_1(1420), \omega(1420), \eta(1440), a_0(1450), \rho(1450),$
 $f_0(1500), f_2'(1525), \omega(1650), \omega_3(1670), \pi_2(1670), \phi(1680),$
 $\rho_3(1690), \rho(1700), f_0(1710), \pi(1800), \phi_3(1850), f_2(2010),$
 $a_4(2040), f_4(2050), f_2(2300), f_2(2340), K^{\pm}, K^0, K_S^0, K_L^0, K^{*}(892),$
 $K_1(1270), K_1(1400), K^{*}(1410), K_0^{*}(1430), K_2^{*}(1430), K^{*}(1680),$
 $K_2(1770), K_3^{*}(1780), K_2(1820), K_4^{*}(2045), D^{\pm}, D^0, D^{*}(2007)^0,$
 $D^{*}(2010)^{\pm}, D_1(2420)^0, D_2^{*}(2460)^0, D_2^{*}(2460)^{\pm}, D_s^{\pm}, D_s^{*\pm},$
 $D_{s1}(2536)^{\pm}, D_{s1}(2573)^{\pm}, B^{\pm}, B^0, B^{*}, B_S^0, B_c^{\pm}, \eta_c(1S), J/\psi(1S),$
 $\chi_{c0}(1P), \chi_{c1}(1P), \chi_{c2}(1P), \psi(2S), \psi(3770), \psi(4040), \psi(4160),$
 $\psi(4415), \Upsilon(1S), \chi_{b0}(1P), \chi_{b1}(1P), \chi_{b2}(1P), \Upsilon(2S), \chi_{b0}(2P),$
 $\chi_{b2}(2P), T(3S), T(4S), T(10860), T(11020), p, n, N(1440),$
 $N(1520), N(1535), N(1650), N(1675), N(1680), N(1700), N(1710),$
 $N(1720), N(2190), N(2220), N(2250), N(2600), \Delta(1232), \Delta(1600),$
 $\Delta(1620), \Delta(1700), \Delta(1905), \Delta(1910), \Delta(1920), \Delta(1930), \Delta(1950),$
 $\Delta(2420), \Lambda, \Lambda(1405), \Lambda(1520), \Lambda(1600), \Lambda(1670), \Lambda(1690),$
 $\Lambda(1800), \Lambda(1810), \Lambda(1820), \Lambda(1830), \Lambda(1890), \Lambda(2100),$
 $\Lambda(2110), \Lambda(2350), \Sigma^{+}, \Sigma^0, \Sigma^{-}, \Sigma(1385), \Sigma(1660), \Sigma(1670),$
 $\Sigma(1750), \Sigma(1775), \Sigma(1915), \Sigma(1940), \Sigma(2030), \Sigma(2250), \Xi^0, \Xi^{-},$
 $\Xi(1530), \Xi(1690), \Xi(1820), \Xi(1950), \Xi(2030), \Omega^{-}, \Omega(2250)^{-},$
 $\Lambda_c^{+}, \Lambda_c^{+}, \Sigma_c(2455), \Sigma_c(2520), \Xi_c^{+}, \Xi_c^0, \Xi_c^{*+}, \Xi_c^{*0}, \Xi_c(2645),$
 $\Xi_c(2780), \Xi_c(2815), \Omega_c^0, \Lambda_b^0, \Xi_b^0, \Xi_b^{-}, t, \bar{t}$

There are many more

Particle	Mass (MeV)	Life time τ (s)	$c\tau$
γ	0	∞	∞
$\pi^\pm (u\bar{d}, d\bar{u})$	140	$2.6 \cdot 10^{-8}$	7.8 m
$K^\pm (u\bar{s}, \bar{u}s)$	494	$1.2 \cdot 10^{-8}$	3.7 m
$K^0 (d\bar{s}, \bar{d}s)$	497	$5.1 \cdot 10^{-8}$ $8.9 \cdot 10^{-11}$	15.5 m 2.7 cm
$D^\pm (c\bar{d}, \bar{c}d)$	1869	$1.0 \cdot 10^{-12}$	315 μm
$D^0 (c\bar{u}, \bar{c}u)$	1864	$4.1 \cdot 10^{-13}$	123 μm
$D_s^\pm (c\bar{s}, \bar{c}s)$	1969	$4.9 \cdot 10^{-13}$	147 μm
$B^\pm (u\bar{b}, \bar{u}b)$	5279	$1.7 \cdot 10^{-12}$	502 μm
$B^0 (b\bar{d}, \bar{b}d)$	5279	$1.5 \cdot 10^{-12}$	462 μm
$B_s^0 (s\bar{b}, \bar{s}b)$	5370	$1.5 \cdot 10^{-12}$	438 μm
$B_c^\pm (c\bar{b}, \bar{c}b)$	~ 6400	$\sim 5 \cdot 10^{-13}$	150 μm
$p (uud)$	938.3	$> 10^{33} \text{ y}$	∞
$n (udd)$	939.6	885.7 s	$2.655 \cdot 10^8 \text{ km}$
$\Lambda^0 (uds)$	1115.7	$2.6 \cdot 10^{-10}$	7.89 cm
$\Sigma^+ (uus)$	1189.4	$8.0 \cdot 10^{-11}$	2.404 cm
$\Sigma^- (dds)$	1197.4	$1.5 \cdot 10^{-10}$	4.434 cm
$\Xi^0 (uss)$	1315	$2.9 \cdot 10^{-10}$	8.71 cm
$\Xi^- (dss)$	1321	$1.6 \cdot 10^{-10}$	4.91 cm
$\Omega^- (sss)$	1672	$8.2 \cdot 10^{-11}$	2.461 cm
$\Lambda_c^+ (udc)$	2285	$\sim 2 \cdot 10^{-13}$	60 μm
$\Xi_c^+ (usc)$	2466	$4.4 \cdot 10^{-13}$	132 μm
$\Xi_c^0 (dcs)$	2472	$\sim 1 \cdot 10^{-13}$	29 μm
$\Omega_c^0 (ssc)$	2698	$6.0 \cdot 10^{-14}$	19 μm
$\Lambda_b (udb)$	5620	$1.2 \cdot 10^{-12}$	368 μm

"Secondary
Vertices"

From the 'hundreds' of Particles listed by the PDG there are only ~ 27 with a life time $c\tau > \sim 1\mu\text{m}$ i.e. they can be seen as 'tracks' in a Detector.

~ 13 of the 27 have $c\tau < 500\mu\text{m}$ i.e. only $\sim\text{mm}$ range at GeV Energies.
→ 'short' tracks measured with Emulsions or Vertex Detectors.

From the ~ 14 remaining particles

$$e^{\pm}, \mu^{\pm}, \gamma, \pi^{\pm}, K^{\pm}, K^0, p^{\pm}, n$$

are by far the most frequent ones

A particle Detector must be able to identify and measure Energy and Momenta of these 8 particles.

$$\begin{array}{l}
 e^{\pm} \quad m_e = 0.511 \text{ MeV} \\
 \mu^{\pm} \quad m_{\mu} = 105.7 \text{ MeV} \sim 200 m_e \\
 \gamma \quad m_{\gamma} = 0, \quad Q = 0
 \end{array}
 \left. \vphantom{\begin{array}{l} e^{\pm} \\ \mu^{\pm} \\ \gamma \end{array}} \right\} \text{EM}$$

$$\begin{array}{l}
 \pi^{\pm} \quad m_{\pi} = 139.6 \text{ MeV} \sim 270 m_e \\
 K^{\pm} \quad m_K = 493.7 \text{ MeV} \sim 1000 m_e \\
 p^{\pm} \quad m_p = 938.3 \text{ MeV} \sim 2000 m_e
 \end{array}
 \left. \vphantom{\begin{array}{l} \pi^{\pm} \\ K^{\pm} \\ p^{\pm} \end{array}} \right\} \begin{array}{l} \text{EM, Strong} \\ \sim 3.5 m_{\pi} \end{array}$$

$$\begin{array}{l}
 K^0 \quad m_{K^0} = 497.7 \text{ MeV} \quad Q = 0 \\
 n \quad m_n = 939.6 \text{ MeV} \quad Q = 0
 \end{array}
 \left. \vphantom{\begin{array}{l} K^0 \\ n \end{array}} \right\} \text{Strong}$$

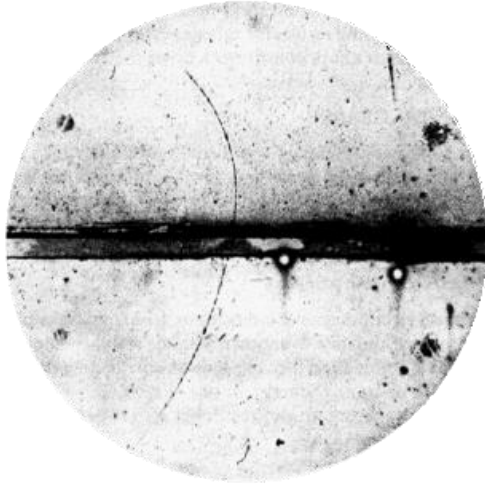
The Difference in Mass, Charge,

Mass, Charge, Interaction

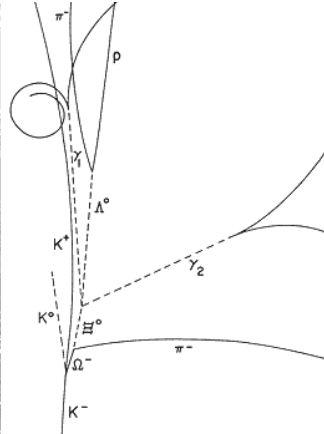
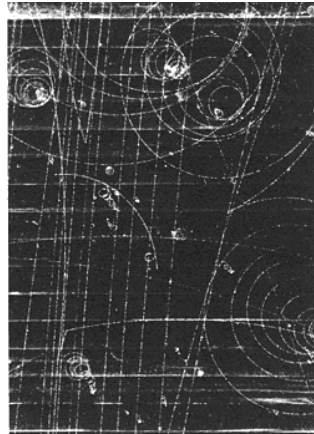
is the key to the Identification

Interactions of Particles with Matter

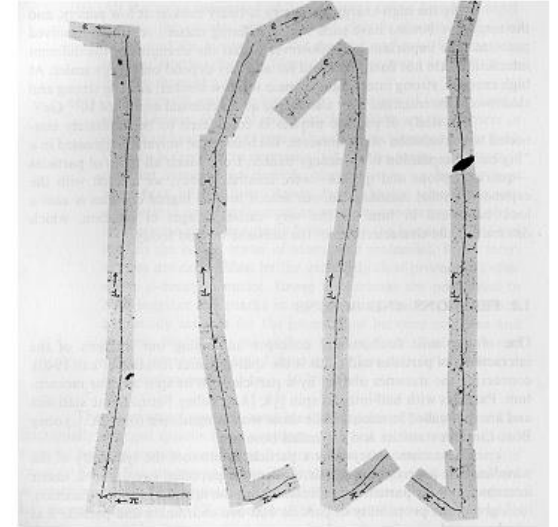
Cloud chambers
1911-1950ies



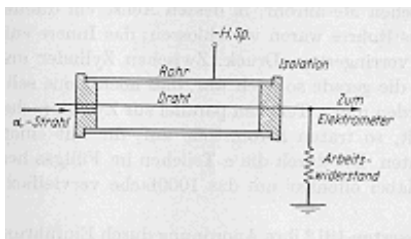
Bubble chambers
1950ies-1980ies



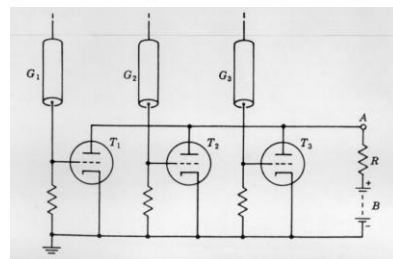
Photographic Emulsions
1930ies to present



Geiger Counter
since 1906

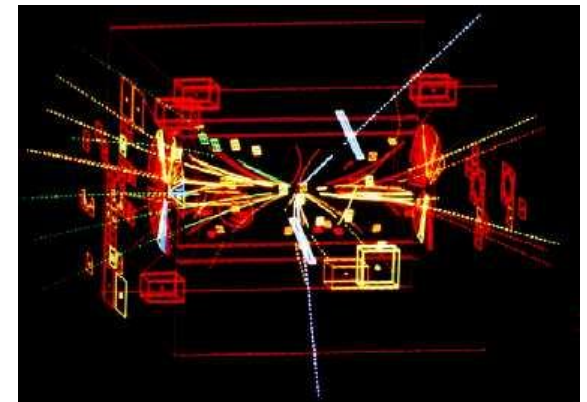


Geiger Counter
Electronics 1930ies

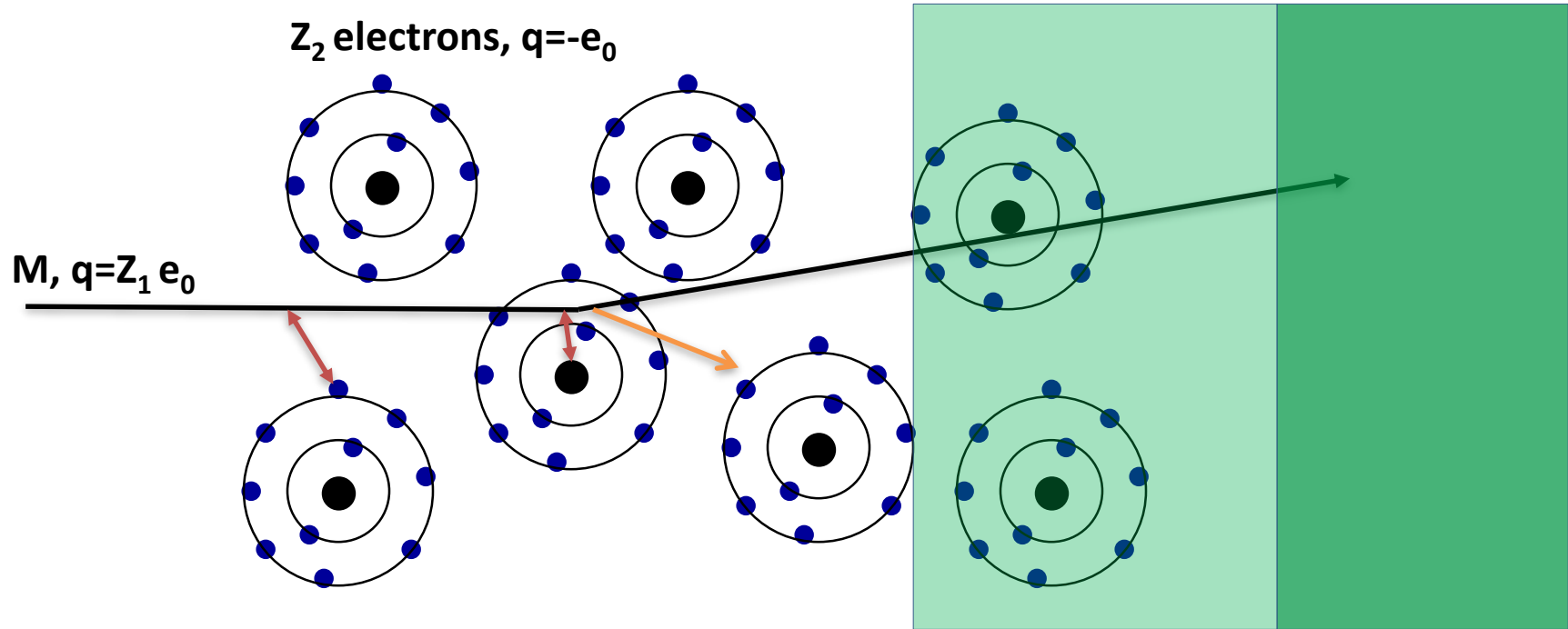


....

Today: Large variety of
electronic detectors



Electromagnetic Interaction of Particles with Matter

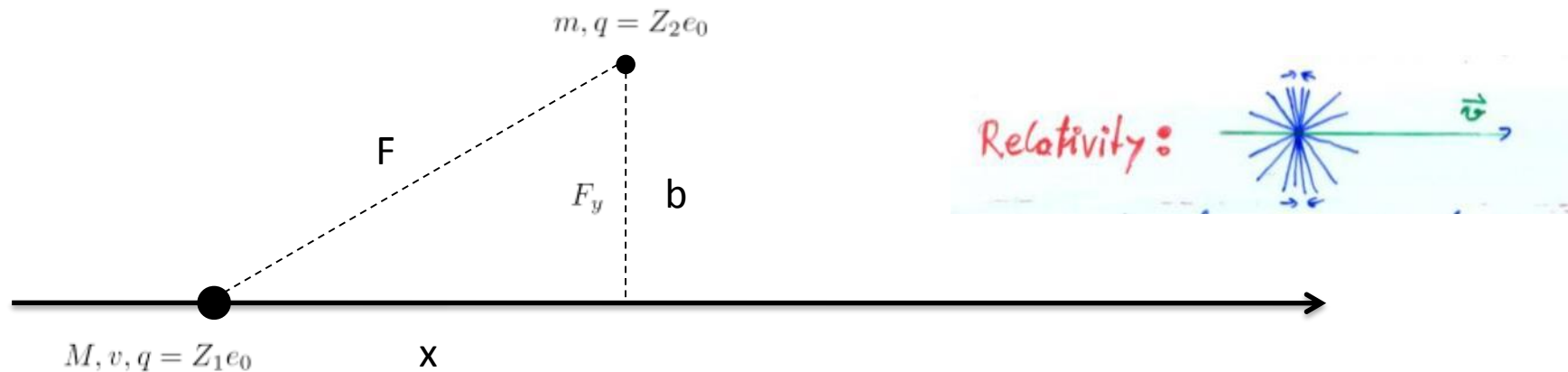


Interaction with the atomic electrons. The incoming particle loses energy and the atoms are excited or ionized.

Interaction with the atomic nucleus. The particle is deflected (scattered) causing multiple scattering of the particle in the material. During this scattering a Bremsstrahlung photon can be emitted.

In case the particle's velocity is larger than the velocity of light in the medium, the resulting EM shockwave manifests itself as Cherenkov Radiation. When the particle crosses the boundary between two media, there is a probability of the order of 1% to produce and X ray photon, called Transition radiation.

Ionization and Excitation



While the charged particle is passing another charged particle, the Coulomb Force is acting, resulting in momentum transfer

$$F_y = \frac{Z_1 Z_2 e_0^2}{4\pi\epsilon_0(b^2 + v^2 t^2)} \frac{b}{\sqrt{b^2 + v^2 t^2}} \quad \Delta p = \int_{-\infty}^{\infty} F_y(t) dt = \frac{2Z_1 Z_2 e_0^2}{4\pi\epsilon_0 v b}$$

The relativistic form of the transverse electric field doesn't change the momentum transfer. The transverse field is stronger, but the time of action is shorter

$$F_y = \frac{\gamma Z_1 Z_2 e_0^2 b}{4\pi\epsilon_0(b^2 + \gamma^2 v^2 t^2)^{3/2}} \quad \Delta p = \int_{-\infty}^{\infty} F_y(t) dt = \frac{2Z_1 Z_2 e_0^2}{4\pi\epsilon_0 v b}$$

The transferred energy is then

$$\Delta E = \frac{(\Delta p)^2}{2m} = \frac{Z_2^2}{m} \frac{2Z_1^2 e_0^4}{(4\pi\epsilon_0)^2 v^2 b^2}$$

$$\Delta E(\text{electrons}) = Z_2 \frac{1}{m_e} \frac{2Z_1^2 e_0^4}{(4\pi\epsilon_0)^2 v^2 b^2} \quad \Delta E(\text{nucleus}) = \frac{Z_2^2}{2Z_2 m_p} \frac{2Z_1^2 e_0^4}{(4\pi\epsilon_0)^2 v^2 b^2} \quad \frac{\Delta E(\text{electrons})}{\Delta E(\text{nucleus})} = \frac{2m_p}{m_e} \approx 4000$$

→ The incoming particle transfer energy only (mostly) to the atomic electrons !

Ionization and Excitation

Target material: mass A, Z_2 , density ρ [g/cm³], Avogadro number N_A

A gramm $\rightarrow N_A$ Atoms:

Number of atoms/cm³

Number of electrons/cm³

$n_a = N_A \rho / A$ [1/cm³]

$n_e = N_A \rho Z_2 / A$ [1/cm³]

$$\Delta E(\text{electrons}) = \frac{2Z_2 Z_1^2 m_e c^2}{\beta^2 b^2} \frac{e_0^4}{(4\pi \epsilon_0 m_e c^2)^2} = \frac{2Z_2 Z_1^2 m_e c^2}{\beta^2 b^2} r_e^2$$



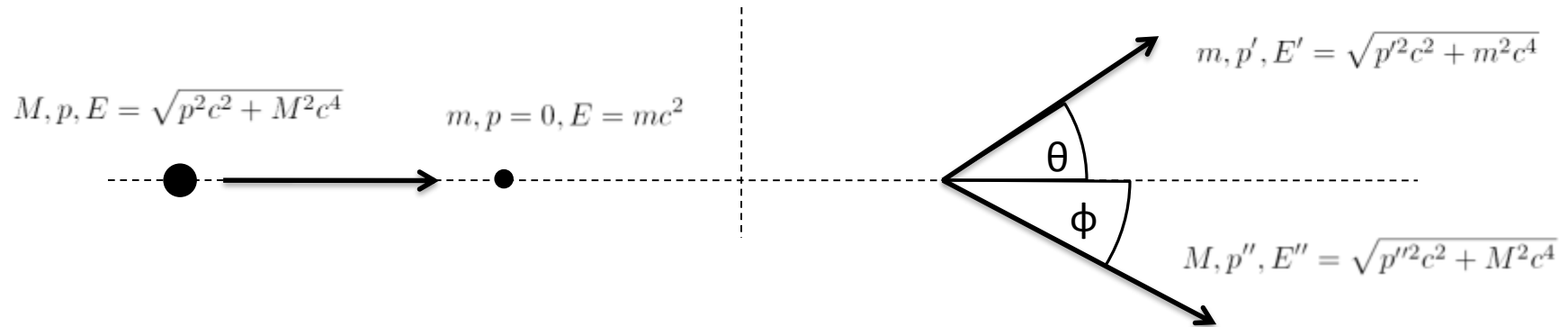
$$dE = - \int_{b_{min}}^{b_{max}} n_e \Delta E dx 2\pi b db = - \frac{4\pi Z_2 Z_1^2 m_e c^2 r_e^2}{\beta^2} \frac{N_A \rho}{A} \int_{b_{min}}^{b_{max}} \frac{db}{b}$$

With $\Delta E(b) \rightarrow db/b = -1/2 dE/E \rightarrow E_{max} = \Delta E(b_{min}) \quad E_{min} = \Delta E(b_{max})$

$$\frac{dE}{dx} = -2\pi r_e^2 m_e^2 c^2 \frac{Z_1^2}{\beta^2} \frac{N_A Z_2 \rho}{A} \int_{E_{min}}^{E_{max}} \frac{dE}{E} = -2\pi r_e^2 m_e^2 c^2 \frac{Z_1^2}{\beta^2} \frac{N_A Z_2 \rho}{A} \ln \frac{E_{max}}{E_{min}}$$

$E_{min} \approx I$ (Ionization Energy)

Relativistic Collision Kinematics, E_{\max}



$$1) \quad \sqrt{p^2 c^2 + M^2 c^4} + mc^2 = \sqrt{p'^2 c^2 + m^2 c^4} + \sqrt{p''^2 c^2 + M^2 c^4}$$

$$2) \quad \begin{aligned} p &= p' \cos \theta + p'' \cos \phi \\ 0 &= p' \sin \theta + p'' \sin \phi \end{aligned} \quad p''^2 = p'^2 + p^2 - 2pp' \cos \theta$$

$$1+2) \quad E^{k'} = \sqrt{p'^2 c^2 + m^2 c^4} - mc^2 = \frac{2mc^2 p^2 c^2 \cos^2 \theta}{\left[mc^2 + \sqrt{p^2 c^2 + M^2 c^4} \right]^2 - p^2 c^2 \cos^2 \theta}$$

$$E_{\max}^{k'} = \frac{2mc^2 p^2 c^2}{(m^2 + M^2)c^4 + 2m\sqrt{p^2 c^2 + M^2 c^4}} = 2mc^2 \beta^2 \gamma^2 F \quad F = \left(1 + \frac{2m}{M} \sqrt{1 + \beta^2 \gamma^2} + \frac{m^2}{M^2} \right)^{-1}$$

Classical Scattering on Free Electrons

$$\frac{1}{\rho} \frac{dE}{dx} = -2\pi r_e^2 m_e c^2 \frac{Z_1^2}{\beta^2} N_A \frac{Z}{A} \ln \frac{2m_e c^2 \beta^2 \gamma^2 F}{I}$$

This formula is up to a factor 2 and the density effect identical to the precise QM derivation →

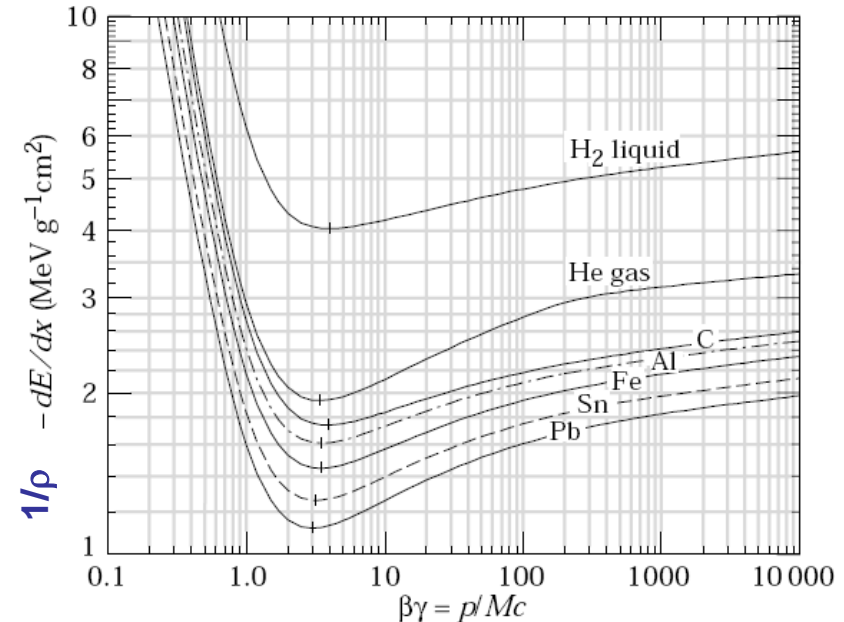
Bethe Bloch Formula

$$\frac{1}{\rho} \frac{dE}{dx} = \underbrace{-4\pi r_e^2 m_e c^2 \frac{Z_1^2}{\beta^2} N_A \frac{Z}{A}}_{\text{Electron Spin}} \left[\ln \frac{2m_e c^2 \beta^2 \gamma^2 F}{I} - \beta^2 - \underbrace{\frac{\delta(\beta\gamma)}{2}}_{\text{Density effect}} \right]$$

Electron Spin

$$\delta(\beta\gamma) = \ln h\omega_p/I + \ln \beta\gamma - \frac{1}{2}$$

Density effect. Medium is polarized
Which reduces the log. rise.



Bethe Bloch Formula

$$\frac{1}{\rho} \frac{dE}{dx} = -4\pi r_e^2 m_e c^2 \frac{Z_1^2}{\beta^2} N_A \frac{Z}{A} \left[\ln \frac{2m_e c^2 \beta^2 \gamma^2 F}{I} - \beta^2 - \frac{\delta(\beta\gamma)}{2} \right]$$

Für $Z>1$, $I \approx 16Z^{0.9} \text{ eV}$

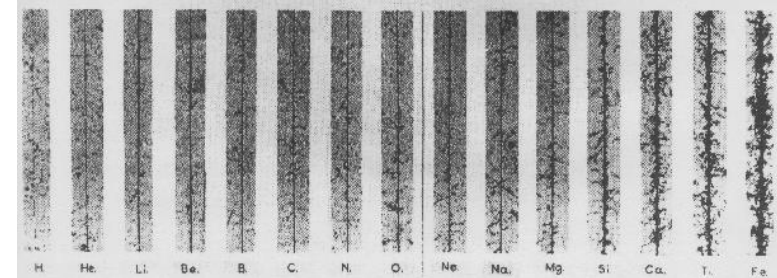
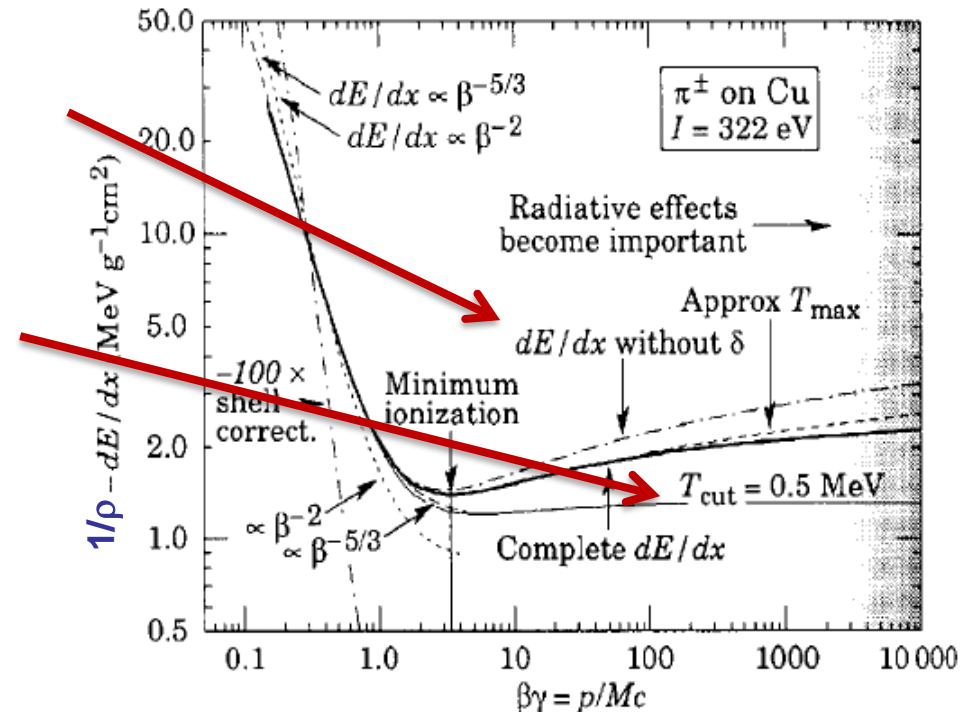
For Large $\beta\gamma$ the medium is being polarized by the strong transverse fields, which reduces the rise of the energy loss \rightarrow density effect

At large Energy Transfers (delta electrons) the liberated electrons can leave the material. In reality, E_{max} must be replaced by E_{cut} and the energy loss reaches a plateau (Fermi plateau).

Characteristics of the energy loss as a function of the particle velocity ($\beta\gamma$)

The specific Energy Loss $1/\rho \, dE/dx$

- first decreases as $1/\beta^2$
- increases with $\ln \gamma$ for $\beta = 1$
- is \approx independent of M ($M \gg m_e$)
- is proportional to Z_1^2 of the incoming particle.
- is \approx independent of the material ($Z/A \approx \text{const}$)
- shows a plateau at large $\beta\gamma$ (> 100)
- $dE/dx \approx 1-2 \times \rho \text{ [g/cm}^3\text{]} \text{ MeV/cm}$



Bethe Bloch Formula

Bethe Bloch Formula, a few Numbers:

For $Z \approx 0.5$ A

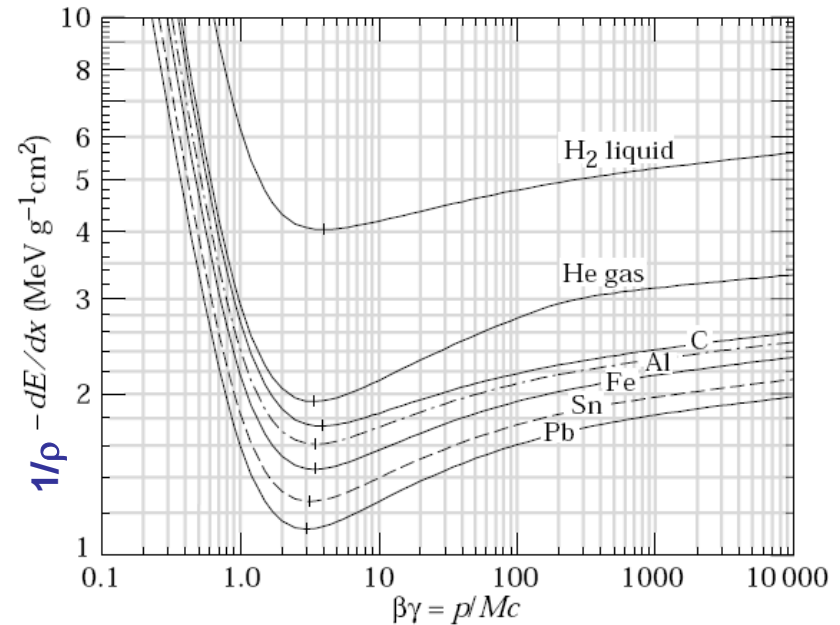
$1/\rho \, dE/dx \approx 1.4 \text{ MeV cm}^2/\text{g}$ for $\beta\gamma \approx 3$

Example :

Iron: Thickness = 100 cm; $\rho = 7.87 \text{ g/cm}^3$

$dE \approx 1.4 * 100 * 7.87 = 1102 \text{ MeV}$

→ A 1 GeV Muon can traverse 1m of Iron



This number must be multiplied with ρ [g/cm^3] of the Material → dE/dx [MeV/cm]

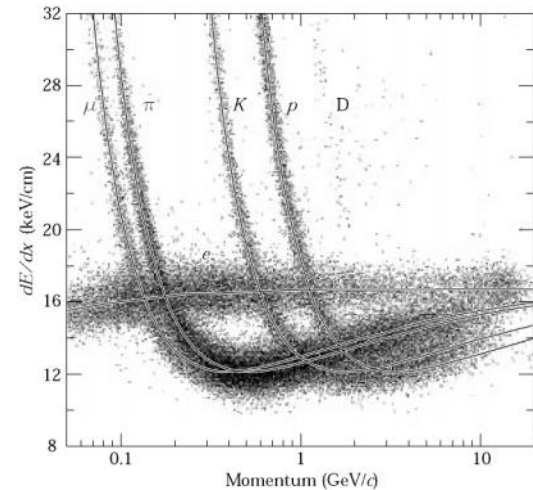
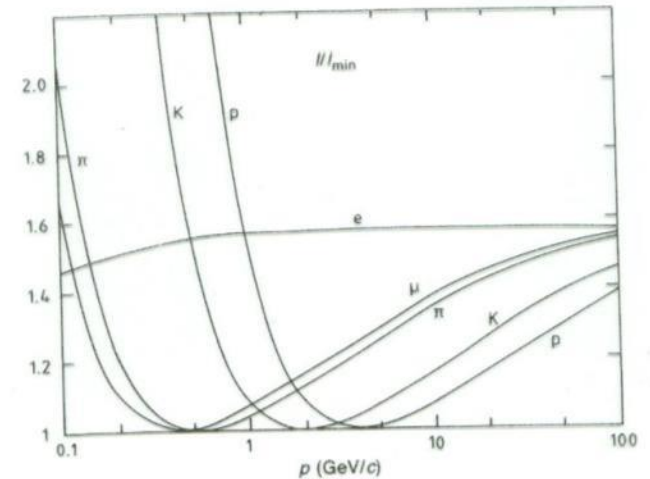
Energy Loss as a Function of the Momentum

Energy loss depends on the particle velocity and is \approx independent of the particle's mass M .

The energy loss as a function of particle Momentum $P = Mc\beta\gamma$ IS however depending on the particle's mass

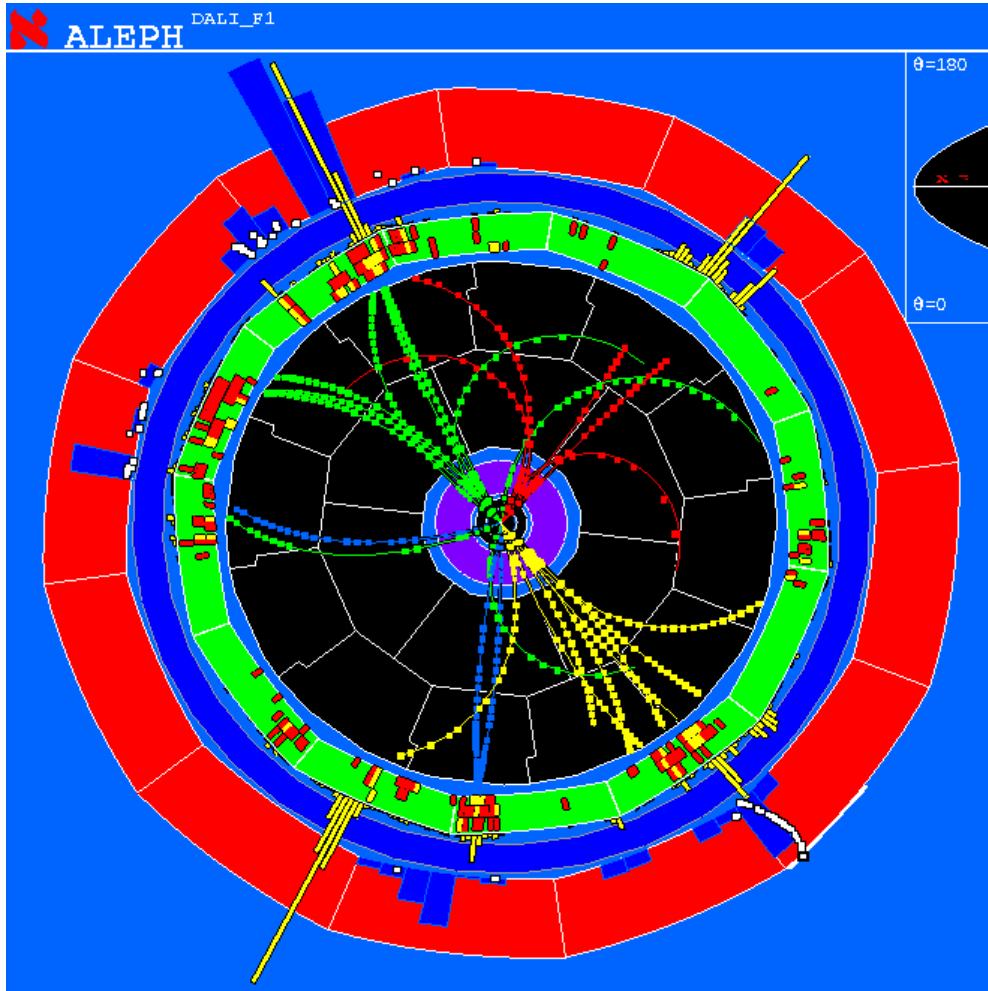
By measuring the particle momentum (deflection in the magnetic field) and measurement of the energy loss one can measure the particle mass

→ Particle Identification !



$$\frac{1}{\rho} \frac{dE}{dx} = -4\pi r_e^2 m_e c^2 Z_1^2 \frac{p^2 + M^2 c^2}{p^2} N_A \frac{Z}{A} \left[\ln \frac{2m_e c^2 F}{I} \frac{p^2}{M^2 c^2} - \frac{p^2}{p^2 + M^2 c^2} \right]$$

Energy Loss as a Function of the Momentum



Measure momentum by curvature of the particle track.

Find dE/dx by measuring the deposited charge along the track.

→ Particle ID

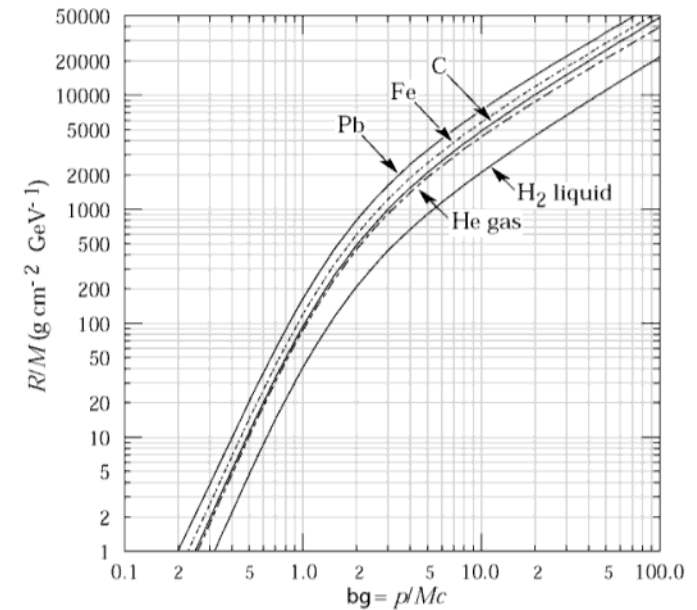
Range of Particles in Matter

Particle of mass M and kinetic Energy E_0 enters matter and loses energy until it comes to rest at distance R .

$$R(E_0) = \int_{E_0}^0 \frac{-1}{dE/dx} dE$$

$$R(\beta_0 \gamma_0) = \frac{Mc^2}{\rho} \frac{1}{Z_1^2} \frac{A}{Z} f(\beta_0 \gamma_0)$$

$$\frac{\rho}{Mc^2} R(\beta_0 \gamma_0) = \frac{1}{Z_1^2} \frac{A}{Z} f(\beta_0 \gamma_0) \approx \text{Independent of the material}$$

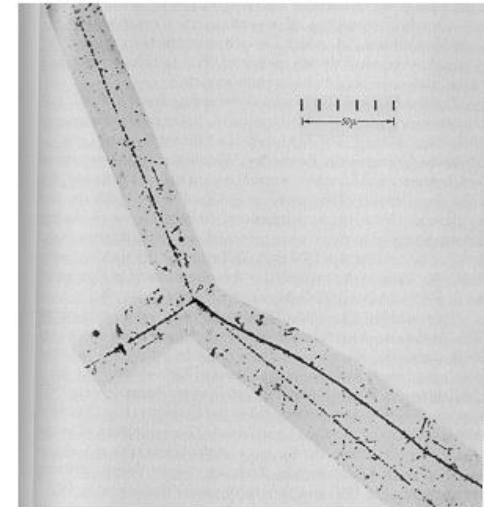
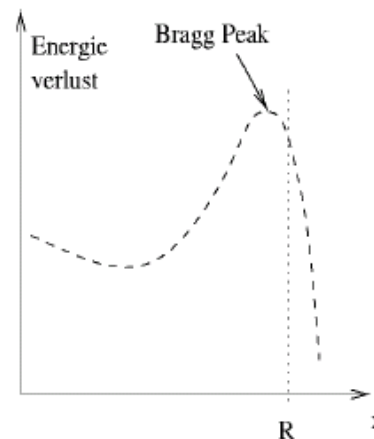


Bragg Peak:

For $\beta\gamma > 3$ the energy loss is \approx constant (Fermi Plateau)

If the energy of the particle falls below $\beta\gamma=3$ the energy loss rises as $1/\beta^2$

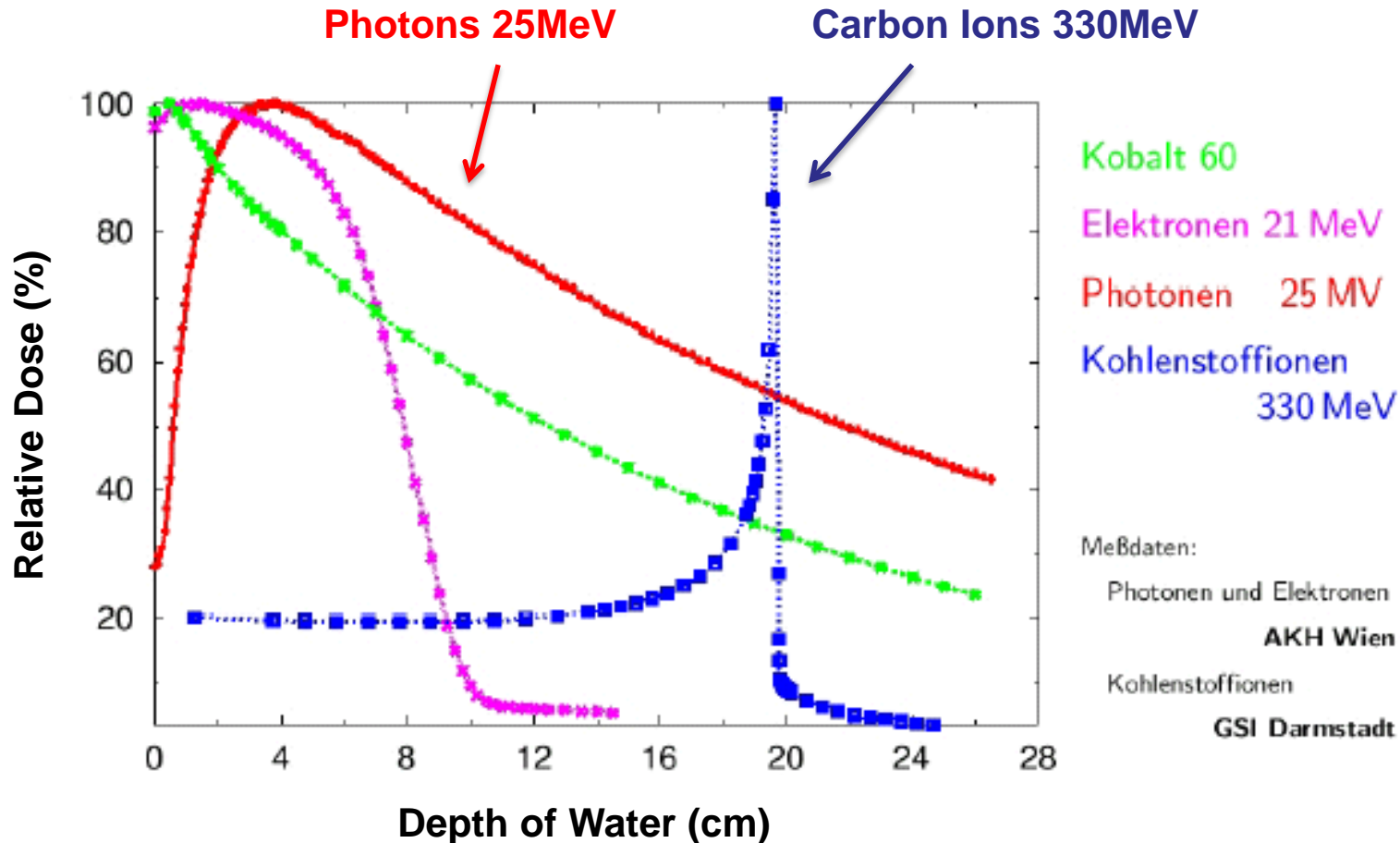
Towards the end of the track the energy loss is largest \rightarrow Cancer Therapy.



Range of Particles in Matter

Average Range:

Towards the end of the track the energy loss is largest → Bragg Peak → Cancer Therapy



Fluctuation of the energy Loss: Landau Distribution

Landau Distribution

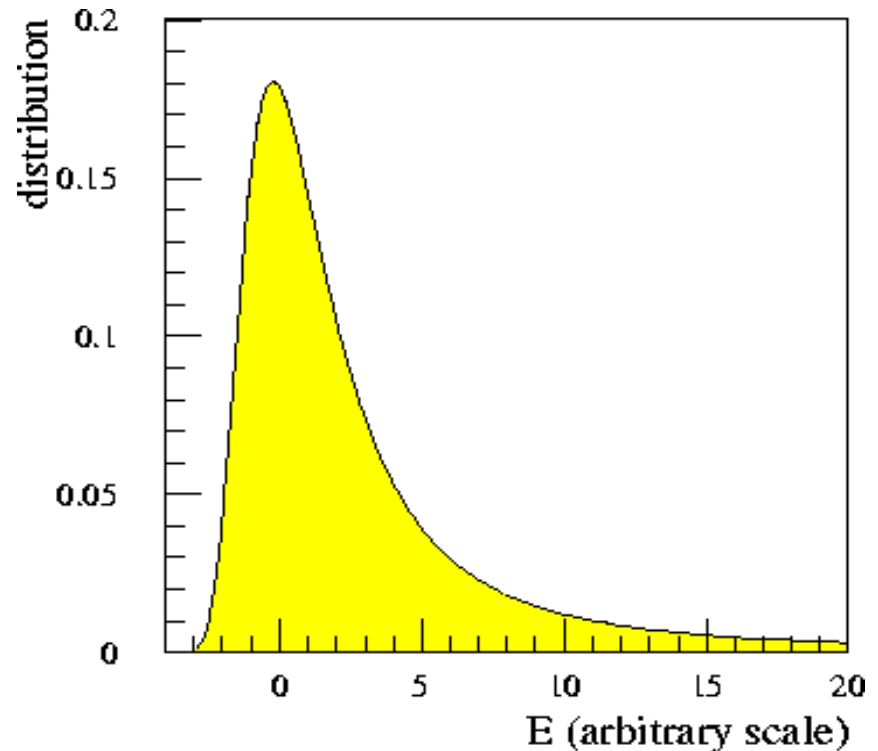
$P(\Delta)$: Probability for energy loss Δ
in matter of thickness D .

Landau distribution is very
asymmetric.

Average and most probable
energy loss must be
distinguished !

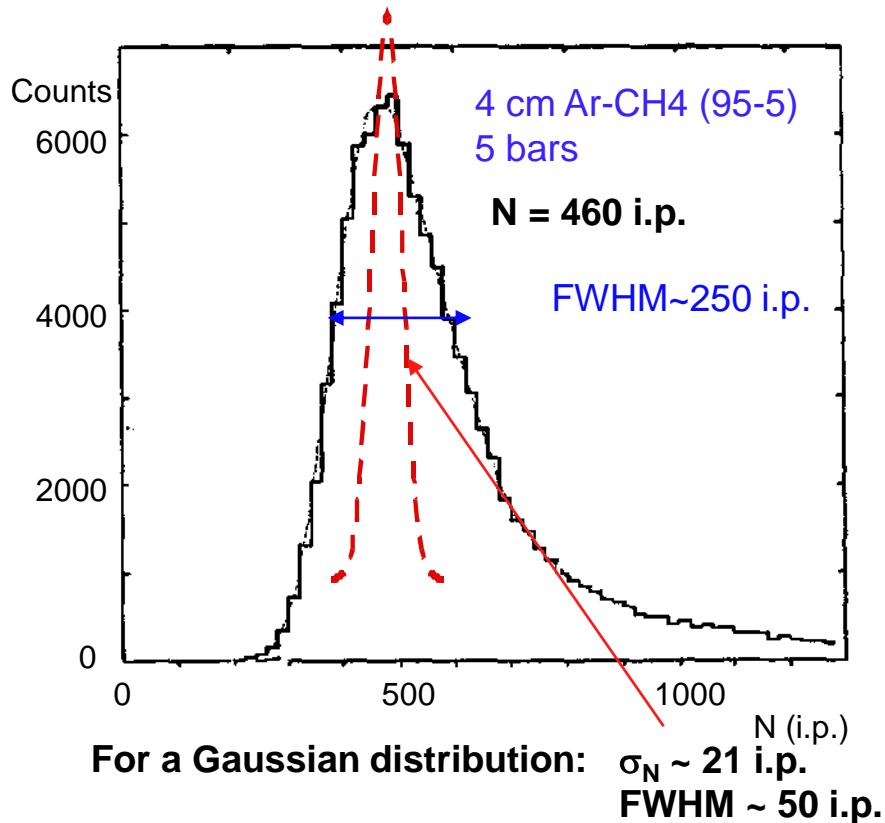
Measured Energy Loss is usually
smaller than the real energy loss:

3 GeV Pion: $E'_{\max} = 450\text{MeV} \rightarrow$ A
450 MeV Electron usually leaves
the detector.



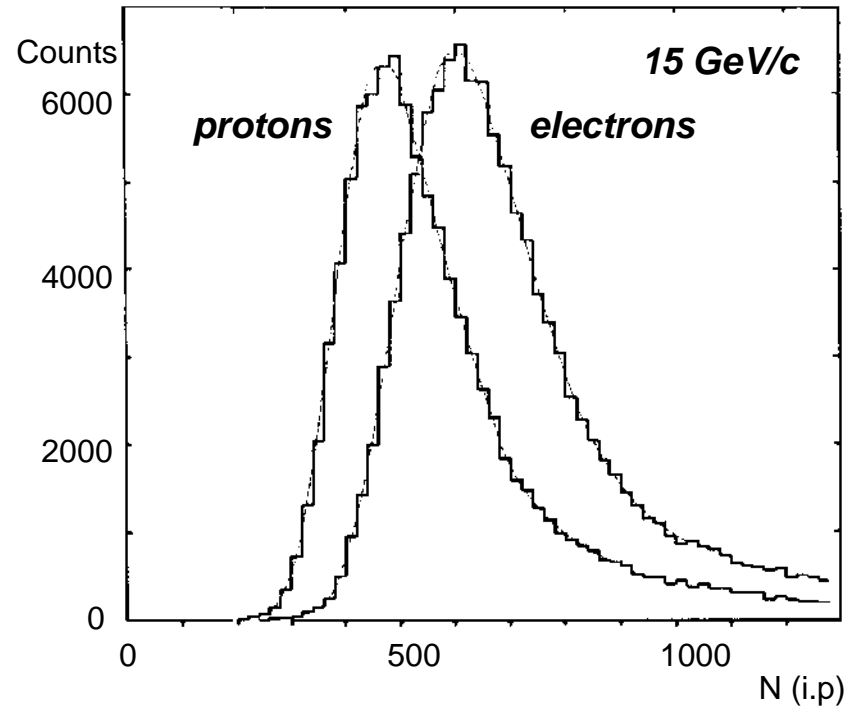
Landau Distribution

LANDAU DISTRIBUTION OF ENERGY LOSS:



PARTICLE IDENTIFICATION

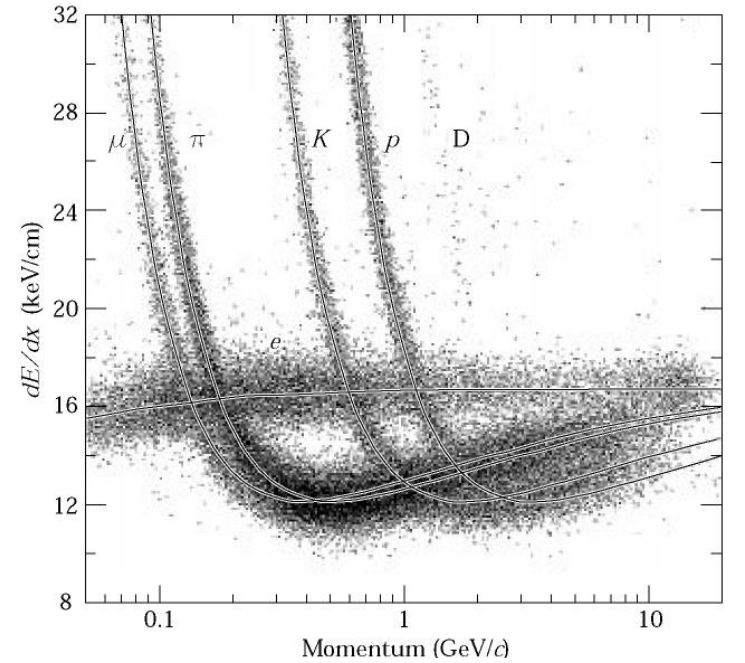
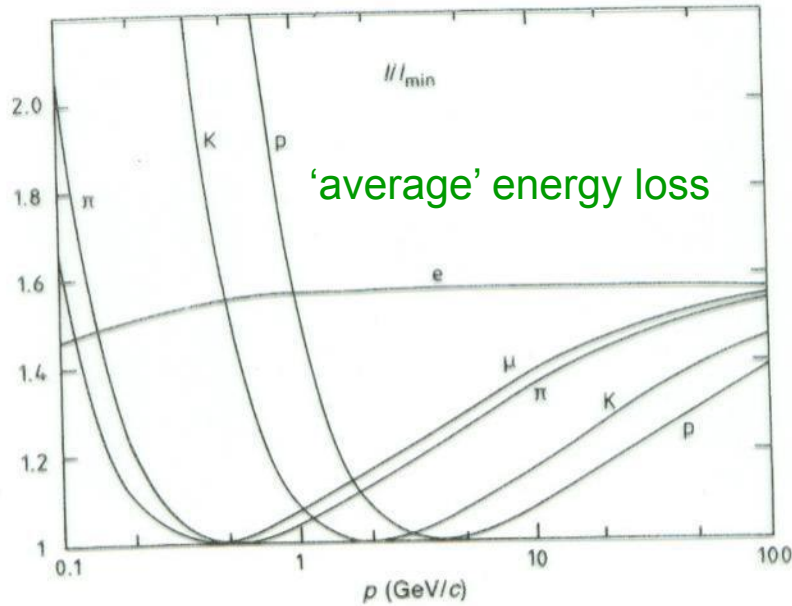
Requires statistical analysis of hundreds of samples



I. Lehraus et al, Phys. Scripta 23(1981)727

Particle Identification

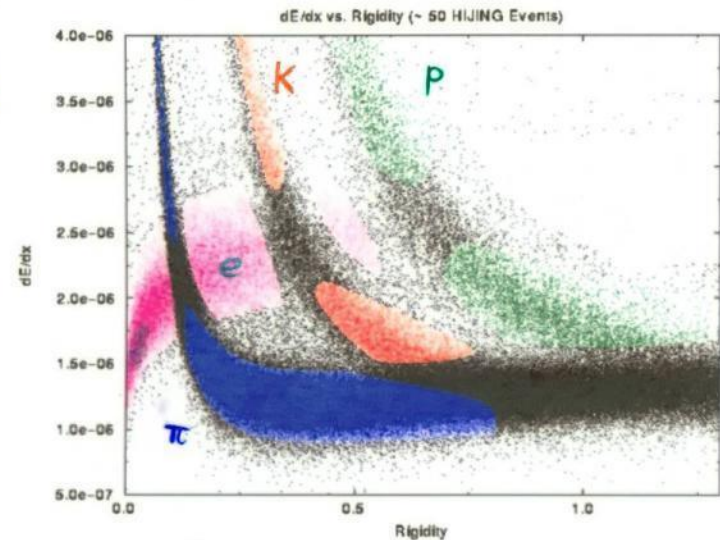
Measured energy loss



BLUE \Rightarrow PIONS RED \Rightarrow KAONS GREEN \Rightarrow PROTONS MAGENTA \Rightarrow ELECTRONS BLACK \Rightarrow NO ID POSSIBLE

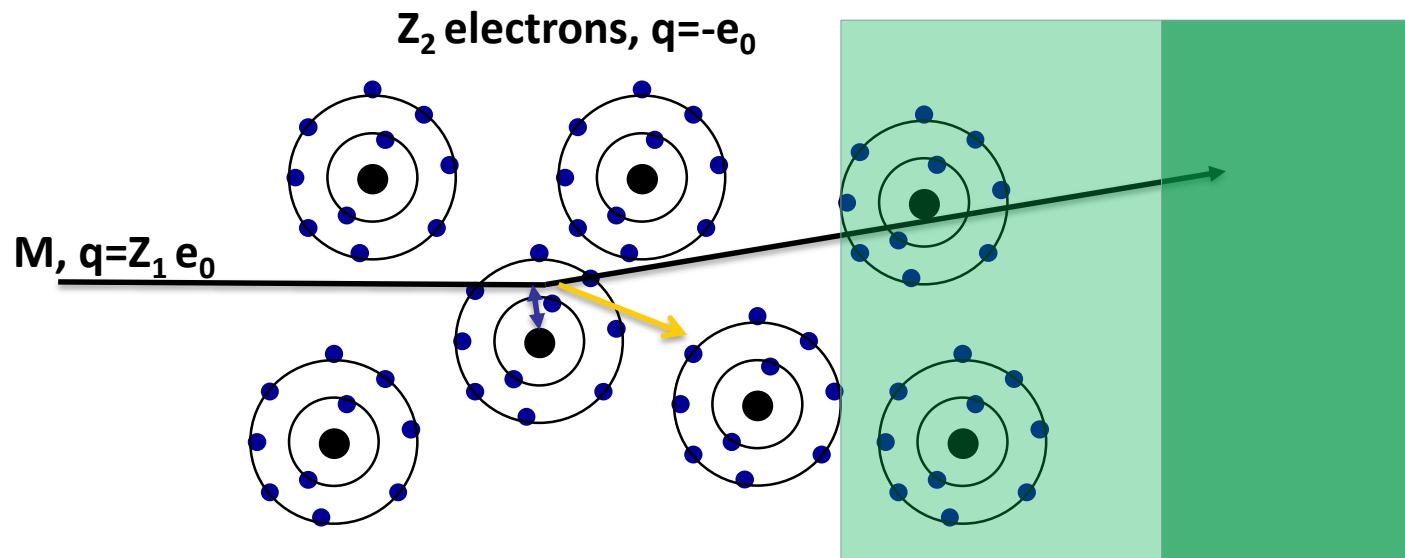
In certain momentum ranges, particles can be identified by measuring the energy loss.

STAR
TPC



Bremsstrahlung

A charged particle of mass M and charge $q=Z_1e$ is deflected by a nucleus of charge Ze which is partially 'shielded' by the electrons. During this deflection the charge is 'accelerated' and it therefore radiated \rightarrow Bremsstrahlung.



7/5/2017

Bremsstrahlung, Classical



$$\frac{d\sigma}{d\Omega} = \left(\frac{2Z_1Z_2e^2}{4\pi\epsilon_0 p \cdot v} \right)^2 \frac{1}{(2\sin \frac{\theta}{2})^4} \quad p = Mv\gamma$$

"Rutherford Scattering"

Written in Terms of Momentum Transfer $Q^2 = 2p^2(1 - \cos\theta)$

$$\frac{d\sigma}{dQ} = 8\pi \left(\frac{Z_1Z_2e^2}{4\pi\epsilon_0 \beta c} \right)^2 \cdot \frac{1}{Q^3}$$



$$Q = |\vec{p} - \vec{p}'|$$

$$\lim_{\omega \rightarrow 0} \frac{dI}{d\omega} \sim \frac{2}{3\pi} \frac{Z_1^2 e^2}{M^2 c^3} \frac{1}{4\pi\epsilon_0} Q^2 \quad \text{Radiated Energy between } \omega, \omega + d\omega$$

→ From Maxwell's Eq (Jackson)

$$\frac{dE}{dx} = \frac{N_A g}{A} \cdot \int_0^{Q_{max}} dQ \int_{Q_{min}}^{Q_{max}} \frac{dI}{d\omega} \cdot \frac{d\sigma}{dQ} \quad , \quad Q_{max} = \frac{E}{\hbar}$$

$$\frac{dE}{dx} = \frac{N_A g}{A} \cdot \frac{16}{3} d \cdot Z^2 \cdot \left(\frac{Z_1^2 e^2}{4\pi\epsilon_0 M c^2} \right)^2 \cdot E \cdot \ln \frac{Q_{max}}{Q_{min}}$$

$$d = \frac{e^2}{4\pi\epsilon_0 \hbar c} \sim \frac{1}{137}$$

A charged particle of mass M and charge $q=Z_1e$ is deflected by a nucleus of Charge Ze .

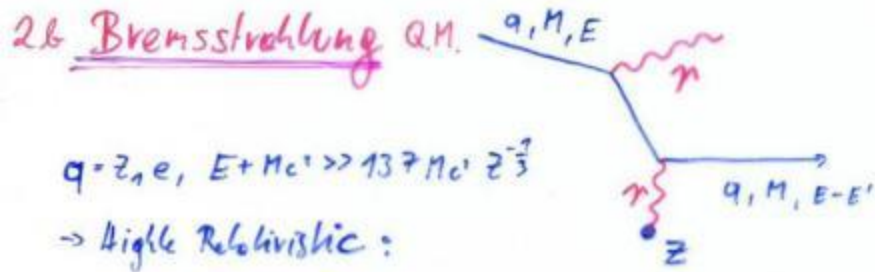
Because of the acceleration the particle radiated EM waves → energy loss.

Coulomb-Scattering (Rutherford Scattering) describes the deflection of the particle.

Maxwell's Equations describe the radiated energy for a given momentum transfer.

→ dE/dx

Bremsstrahlung, QM



$$\frac{d\sigma(E, E')}{dE'} = 4\alpha Z^2 Z_1^4 \left(\frac{1}{4\pi\epsilon_0} \frac{e^2}{mc^2} \right)^2 \left(\frac{1}{E'} \right) F(E, E')$$

$$F(E, E') = \left[1 + \left(1 - \frac{E'}{E + mc^2} \right)^2 - \frac{2}{3} \left(1 - \frac{E'}{E + mc^2} \right) \right] \ln 183 Z^{-\frac{2}{3}} + \frac{1}{9} \left(1 - \frac{E'}{E + mc^2} \right)$$

$$\frac{dE}{dx} = - \frac{N_A g}{A} \int_0^E E' \frac{d\sigma}{dE'} dE' \approx 4\alpha Z^2 Z_1^4 \left(\frac{1}{4\pi\epsilon_0} \frac{e^2}{mc^2} \right)^2 E \left[\ln 183 Z^{-\frac{2}{3}} + \frac{1}{18} \right]$$

$$\underline{\underline{\frac{dE}{dx} = - \frac{N_A g}{A} 4\alpha Z^2 Z_1^4 \left(\frac{1}{4\pi\epsilon_0} \frac{e^2}{mc^2} \right)^2 E \ln(183 Z^{-\frac{2}{3}})}}$$

$$E(x) = E_0 e^{-\frac{x}{X_0}} \quad X_0 = \frac{A}{4\alpha N_A g Z^2 \left(\frac{1}{4\pi\epsilon_0} \frac{e^2}{mc^2} \right)^2 \ln 183 Z^{-\frac{2}{3}}}$$

X_0 ... Radiation length

Proportional to Z^2/A of the Material.

Proportional to Z_1^4 of the incoming particle.

Proportional to ρ of the material.

Proportional $1/M^2$ of the incoming particle.

Proportional to the Energy of the Incoming particle \rightarrow

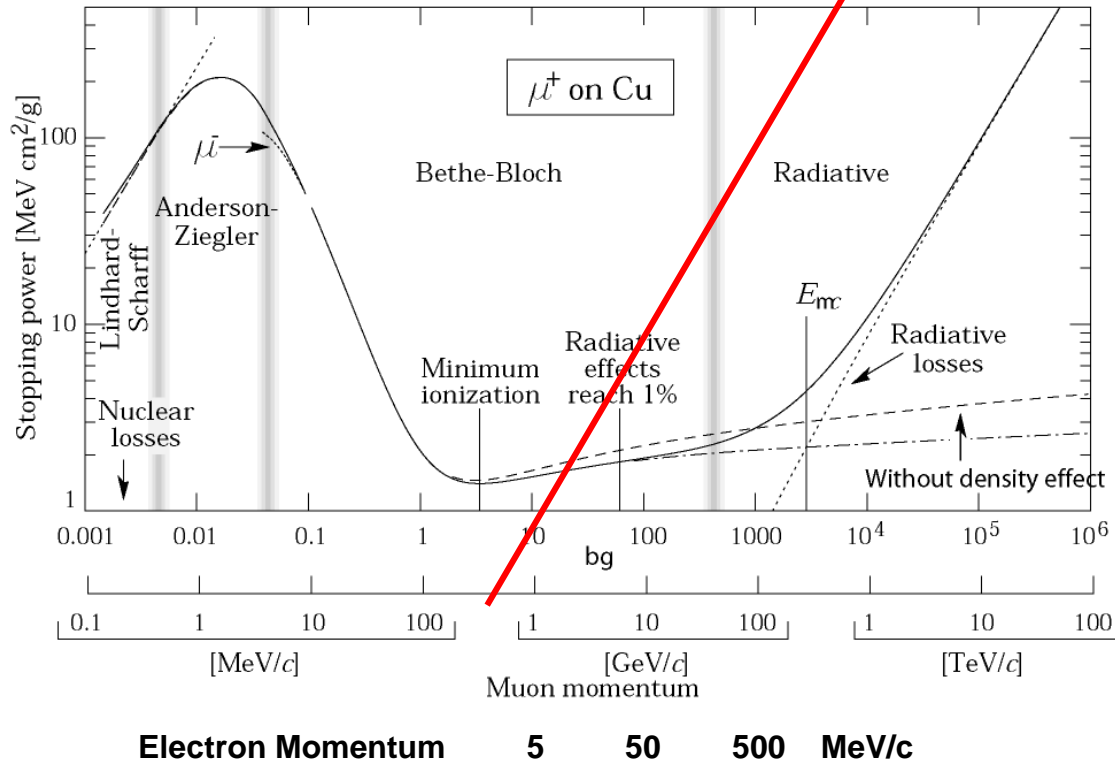
$E(x) = \text{Exp}(-x/X_0)$ – 'Radiation Length'

$$X_0 \propto M^2 A / (\rho Z_1^4 Z^2)$$

X_0 : Distance where the Energy E_0 of the incoming particle decreases $E_0 \text{Exp}(-1) = 0.37 E_0$.

Critical Energy

such as copper to about 1% accuracy for energies between about 6 MeV and 6 GeV



For the muon, the second lightest particle after the electron, the critical energy is at 400GeV.

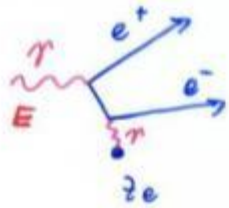
The EM Bremsstrahlung is therefore only relevant for electrons at energies of past and present detectors.

Critical Energy: If dE/dx (Ionization) = dE/dx (Bremsstrahlung)

Myon in Copper: $p \approx 400\text{GeV}$

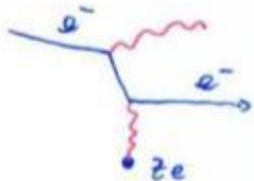
Electron in Copper: $p \approx 20\text{MeV}$

Pair Production, QM



$$\gamma + \text{Nucleon} \rightarrow e^+ + e^- + \text{Nucleon}$$

The Diagram is very similar to Bremsstrahlung



$$e^- + \text{Nucleon} \rightarrow \gamma + e^- + \text{Nucleon}$$

Crossing Symmetry: bring particle to the other side and make it the anti-particle → same correction ...

$$\frac{d\sigma(E, E')}{dE'} = 4\alpha Z^2 v_0^2 \frac{1}{E} G(E, E') \quad E \gg 137 m_e c^2 Z^{-1/3}$$

$$G(E, E') = \left[\left(\frac{E' + m_e c^2}{E} \right)^2 \left(1 - \frac{E' + m_e c^2}{E} \right)^2 + \frac{2}{3} \frac{E' + m_e c^2}{E} \left(1 - \frac{E' + m_e c^2}{E} \right) \ln \frac{E}{E' + m_e c^2} - \frac{1}{3} \frac{E' + m_e c^2}{E} \left(1 - \frac{E' + m_e c^2}{E} \right) \right]$$

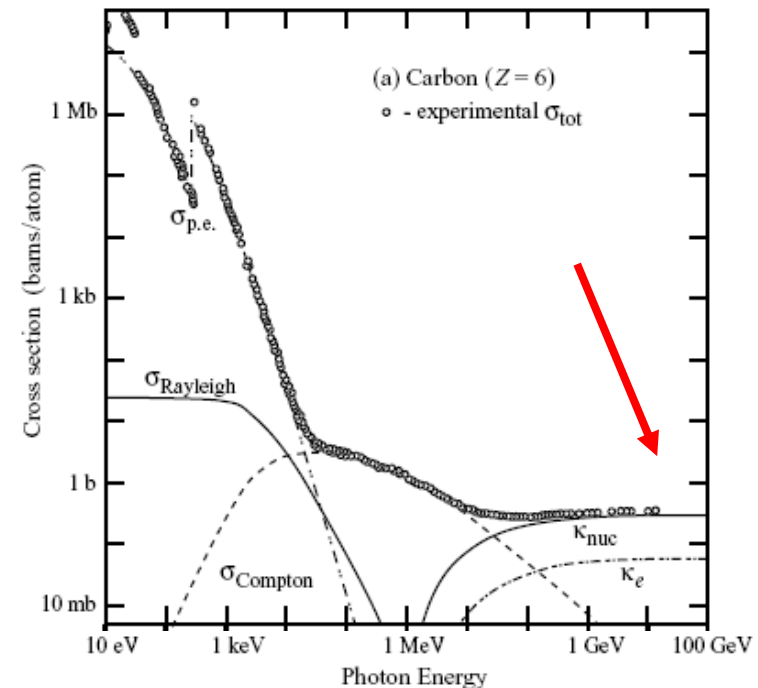
$$\sigma = \int_0^{E-2m_e c^2} \frac{d\sigma}{dE'} dE' = 4\alpha Z^2 v_0^2 \cdot \frac{7}{9} \ln 183 Z^{-1/3}$$

$$P(x) = \frac{1}{\lambda} e^{-\frac{x}{\lambda}} \quad \lambda = \frac{A}{9 N_A \sigma} = \frac{9}{7} X_0$$

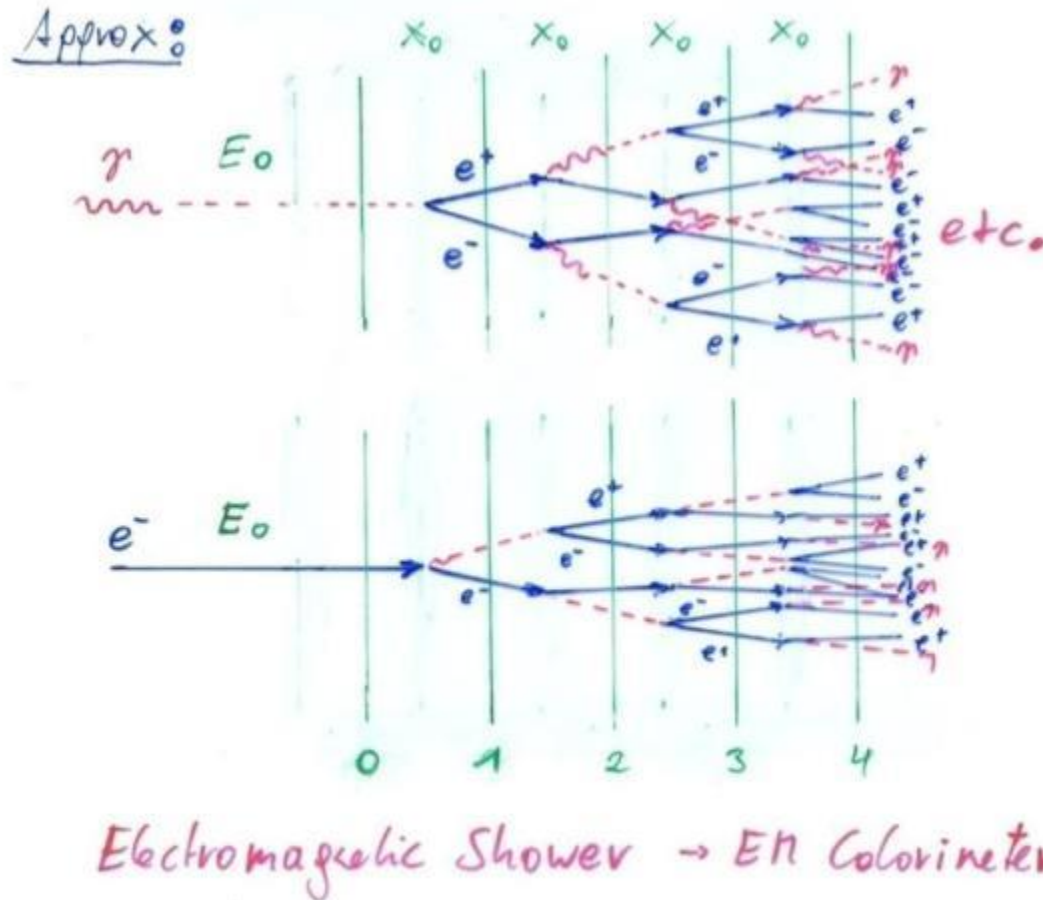
↳ Probability that Photon converts to $e^+ e^-$ after a distance x .

$$\text{For } E_\gamma \gg m_e c^2 = 0.5 \text{ MeV} : \lambda = 9/7 X_0$$

Average distance a high energy photon has to travel before it converts into an $e^+ e^-$ pair is equal to 9/7 of the distance that a high energy electron has to travel before reducing its energy from E_0 to $E_0 \cdot \text{Exp}(-1)$ by photon radiation.



Bremsstrahlung + Pair Production \rightarrow EM Shower



Tracking:

Momentum by bending in the B-field

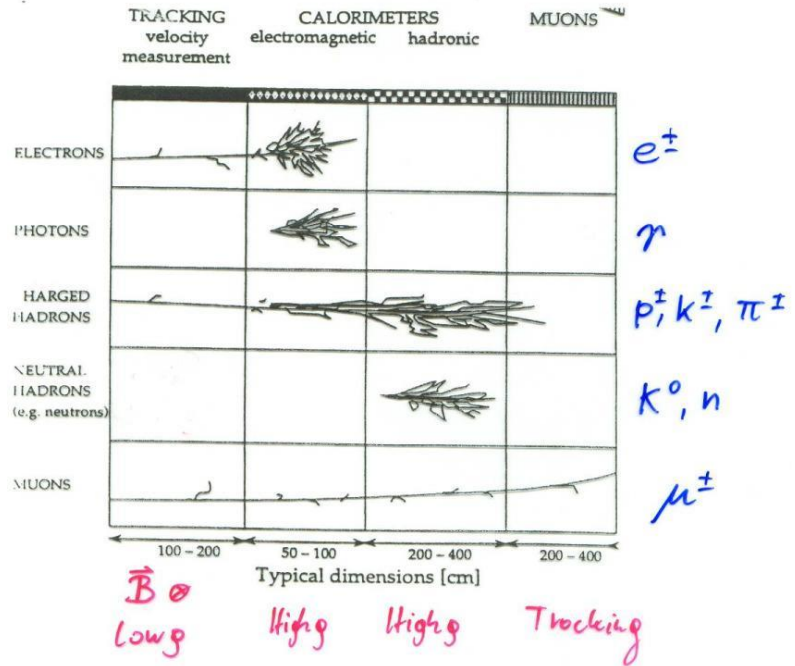
Secondary vertices

Calorimeter:

Energy by absorption

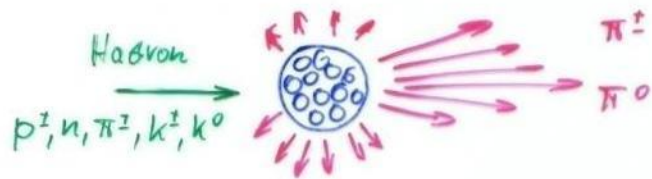
Muons:

Only particles passing through calorimeters



- Electrons ionize and show Bremsstrahlung due to the small mass
- Photons don't ionize but show Pair Production in high Z Material. From then on equal to e^\pm
- Charged Hadrons ionize and show Hadron Shower in dense Material.
- Neutral Hadrons don't ionize and show Hadron Shower in dense Material
- Muons ionize and don't shower

Hadronic Calorimetry

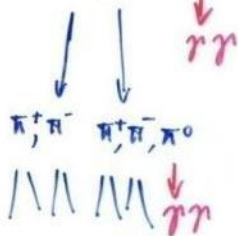


Strong Interaction

Approximate Energy Distribution

~50%

π^+, π^-, π^0



Hadron cascade

~20%

Nuclear Excitation

5-30 MeV

p, n, γ

~30%

Slow

Nucleons

$\pi^0 \rightarrow \gamma\gamma \rightarrow$ Electromagnetic Component

In Hadronic Cascades the longitudinal Shower is given by the Absorption Length λ_a $I \sim e^{-\frac{x}{\lambda_a}}$

In typical Detector Materials λ_a is much larger than X_0

$$\lambda \sim \frac{1}{9} \cdot 35 A^{\frac{1}{3}}$$

	λ	X_0	λ
Fe	7.87	1.76 cm	~17 cm
Pb	11.35	0.56 cm	~17 cm

Energy Resolution:

- A large Fraction of the Energy 'disappears' into
 - Binding Energy of emitted Nucleons
 - $\pi \rightarrow \mu + \nu$ which are not absorbed
- π^0 's Decaying into $\gamma\gamma$ start an EM Cascade ($\tau \sim 10^{-14}s$)
- Energy Resolution is worse than for EM Calorimeters

Multiple Scattering

Statistical (quite complex) analysis of multiple collisions gives:

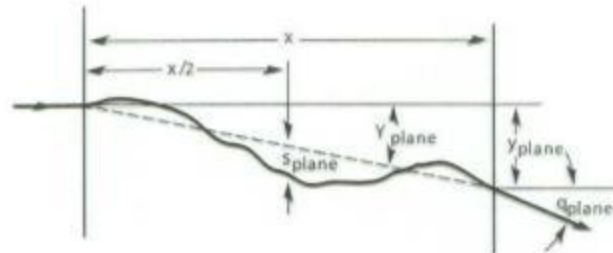
Probability that a particle is deflected by an angle θ after travelling a distance x in the material is given by a Gaussian distribution with sigma of:

$$\Theta_0 = \frac{0.0136}{\beta c p [\text{GeV}/c]} Z_1 \sqrt{\frac{x}{X_0}}$$

X_0 ... Radiation length of the material

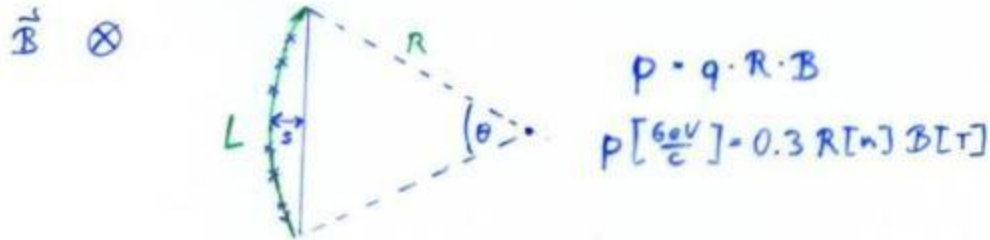
Z_1 ... Charge of the particle

p ... Momentum of the particle



Momentum Measurement

Magnetic Spectrometer: A charged particle describes a circle in a magnetic field:



$$L = R \cdot \theta$$

$$S = R(1 - \cos \frac{\theta}{2}) \sim R \frac{\theta^2}{8} = \frac{L^2}{8R} \rightarrow R = \frac{L^2}{8S}$$

$$\Delta p = 0.3 B \Delta R = 0.3 B \frac{L^2}{8S^2} \Delta S$$

$$\Delta S = \frac{\sigma_x}{\sqrt{N}} \quad \sigma_x \dots \text{point resolution, } N \dots \text{Measured Points}$$

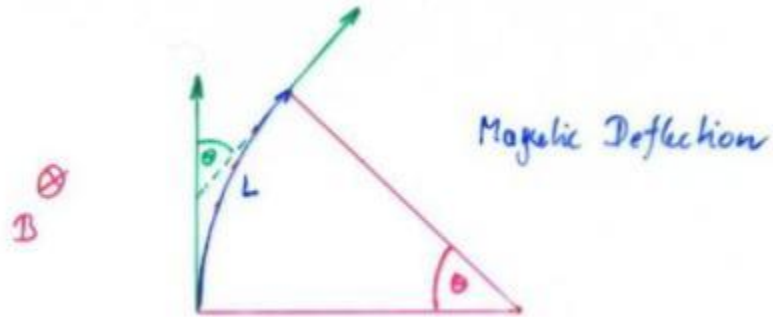
$$\frac{\Delta p}{p} = \frac{\Delta S}{S} = \frac{\sigma_x [\text{m}]}{\sqrt{N}} \cdot \frac{3.3 \cdot 8 p [\frac{\text{GeV}}{c}]}{B[\text{T}] \cdot L^2 [\text{m}^2]}$$

$$\text{E.g: } p = 10 \frac{\text{GeV}}{c}, B = 1\text{T}, L = 1\text{m}, \sigma = 200\mu\text{m}, N = 25$$

$$\frac{\Delta p}{p} = 0.01 \rightarrow 1\%$$

Limit \rightarrow Multiple Scattering

Multiple Scattering



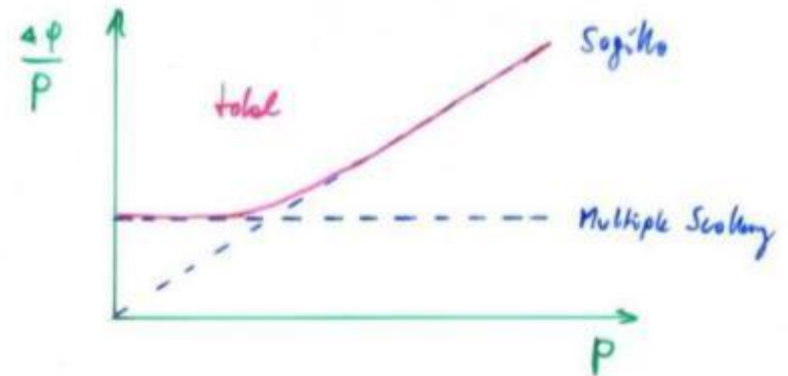
$$p \left[\frac{\text{GeV}}{c} \right] = 0.3 R [\text{m}] B [\text{T}]$$

$$\theta = \frac{L}{R} = \frac{L}{p} \cdot 0.3 B$$

$$\frac{\Delta p}{p} = \frac{\Delta \theta}{\theta} = \frac{\theta_0}{\theta} \sim \frac{0.05}{3 B [\text{T}] L [\text{m}]} \sqrt{\frac{L}{x_0}}$$

→ Independent of p

$$\frac{\Delta p}{p} \Big|_{\text{tot}} = \sqrt{\left(\frac{\Delta p}{p} \Big|_{\text{Sog}} \right)^2 + \left(\frac{\Delta p}{p} \Big|_{\text{ms}} \right)^2}$$



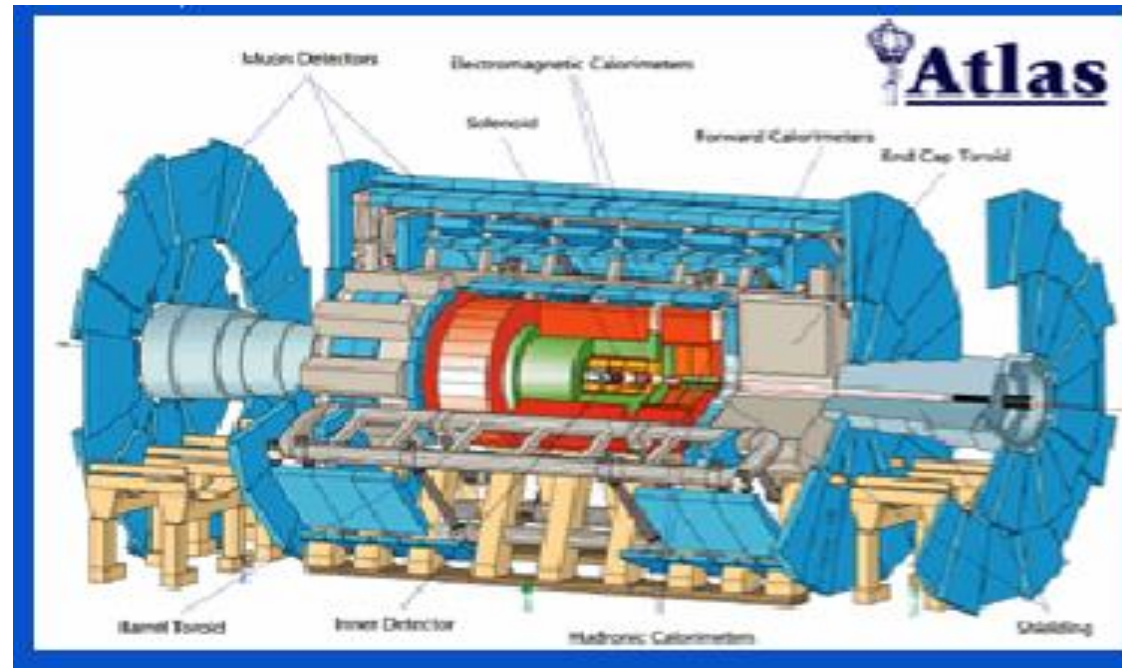
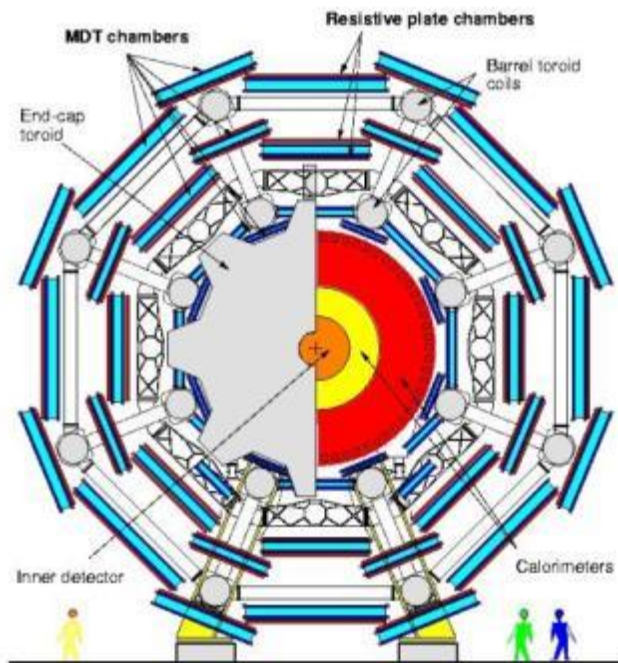
Multiple Scattering

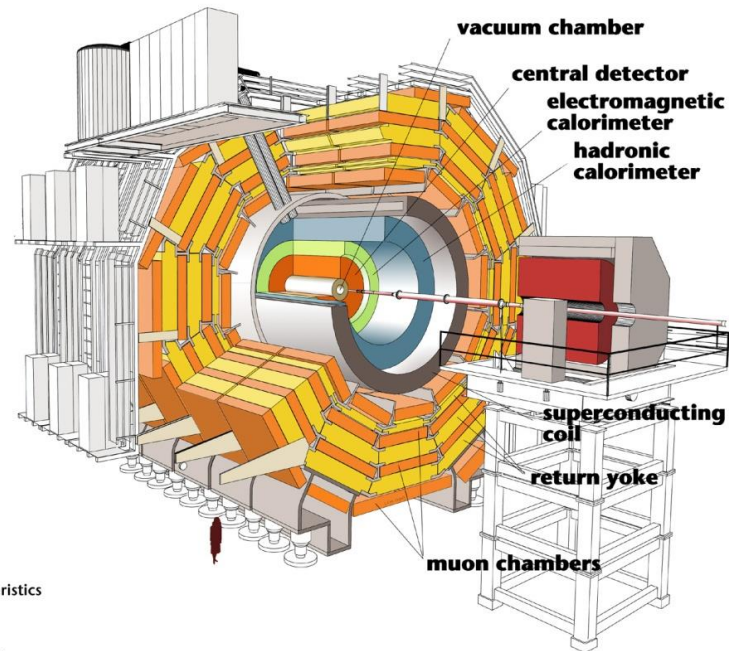
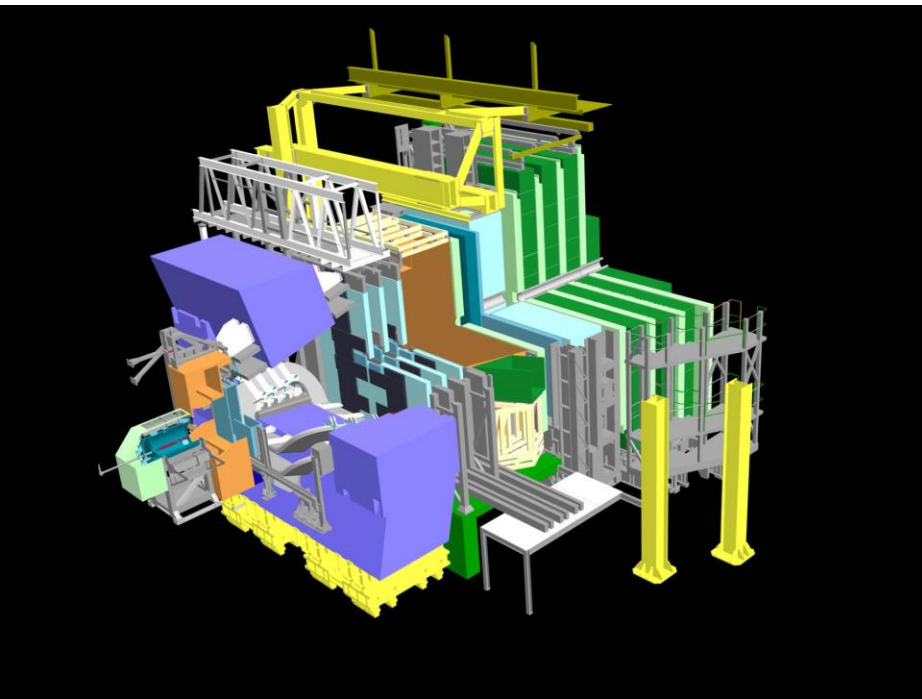
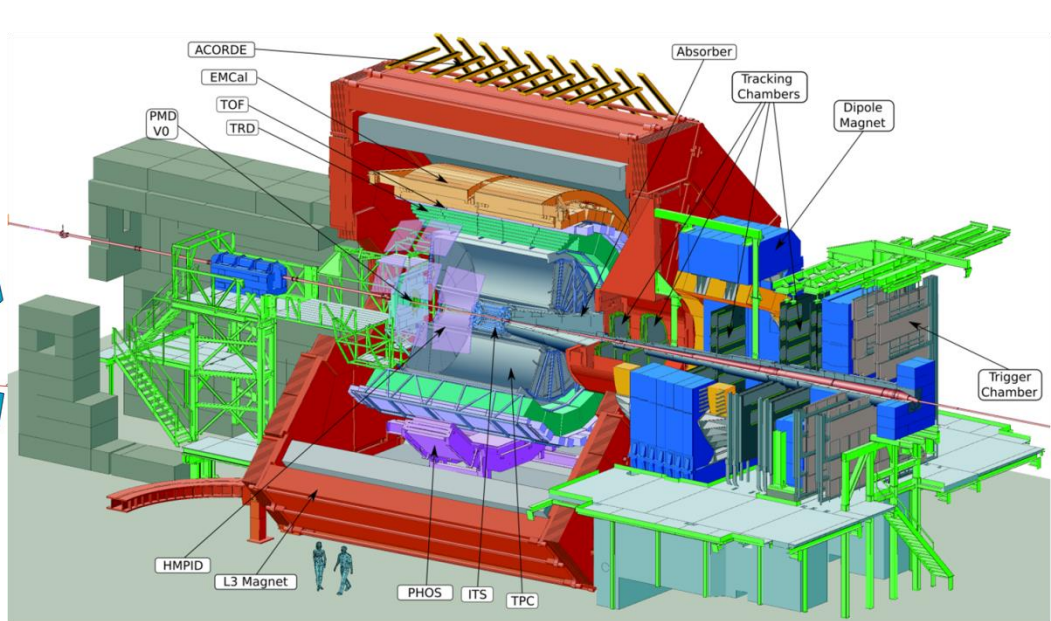
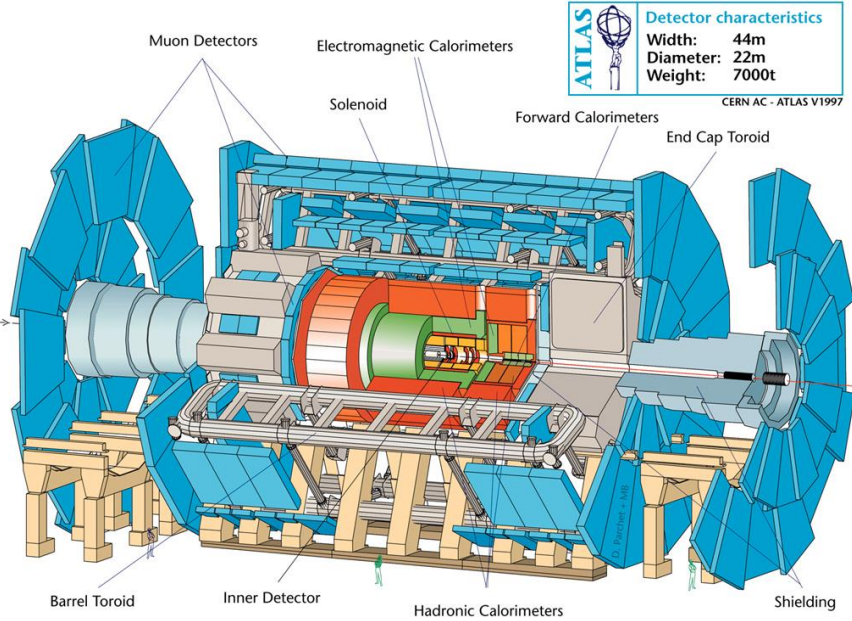
ATLAS Muon Spectrometer:

$N=3$, $\sigma=50\mu\text{m}$, $P=1\text{TeV}$,

$L=5\text{m}$, $B=0.4\text{T}$

$\Delta p/p \sim 8\%$ for the most energetic muons at LHC

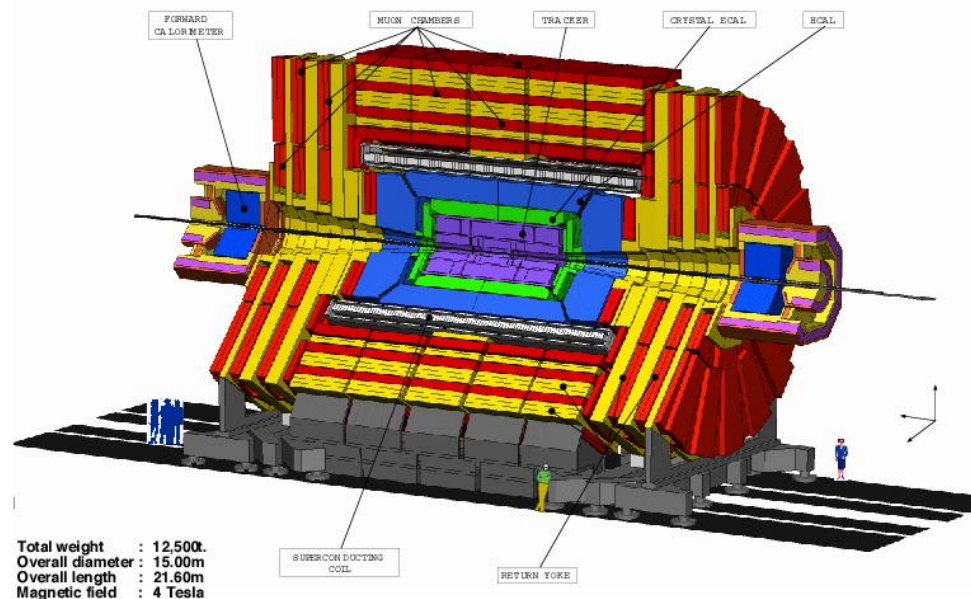




Detector characteristics

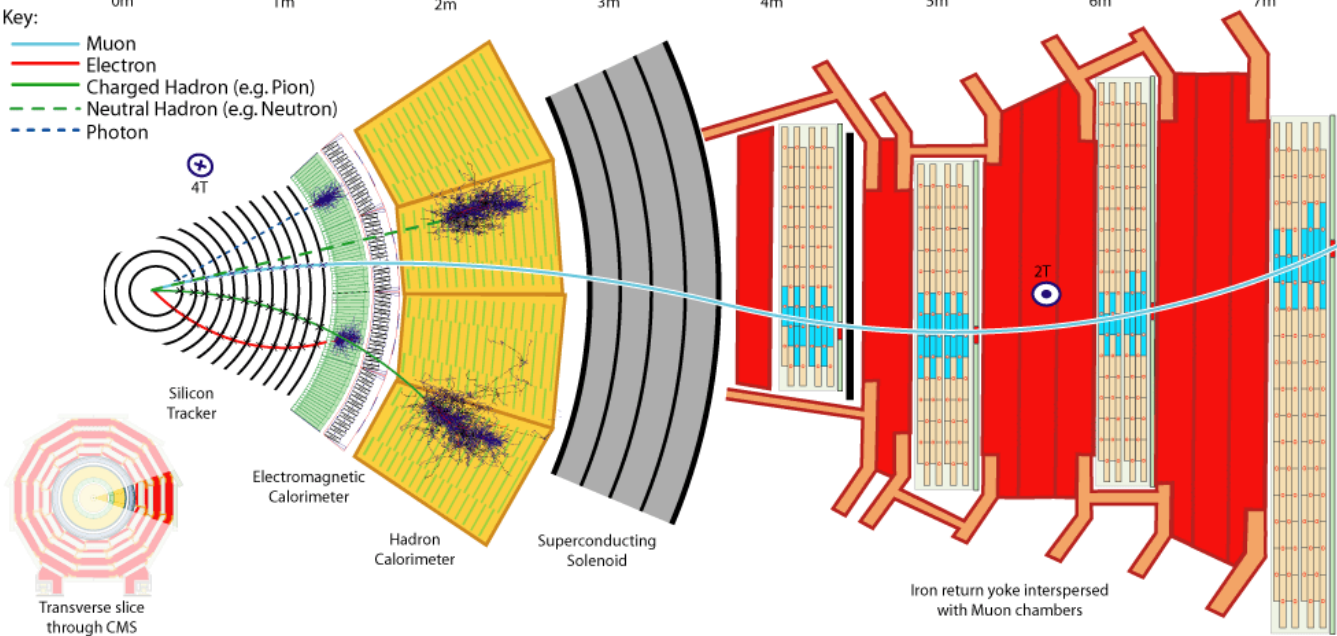
Width: 22m
 Diameter: 15m
 Weight: 14'500t

CMS A Compact Solenoidal Detector for LHC



Key:

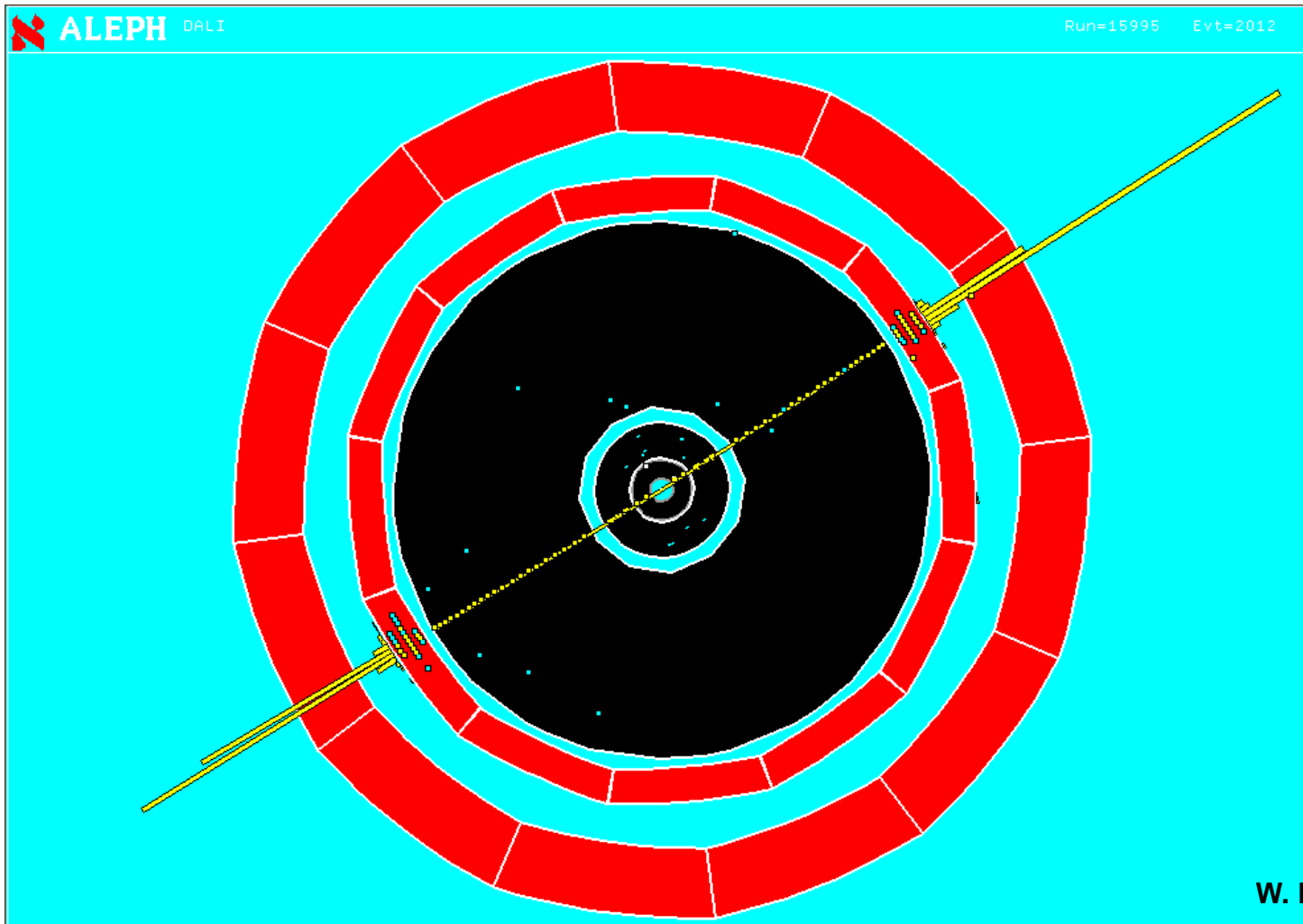
- Muon
- Electron
- Charged Hadron (e.g. Pion)
- - - Neutral Hadron (e.g. Neutron)
- - - Photon



D. Barney, CERN, February 2004

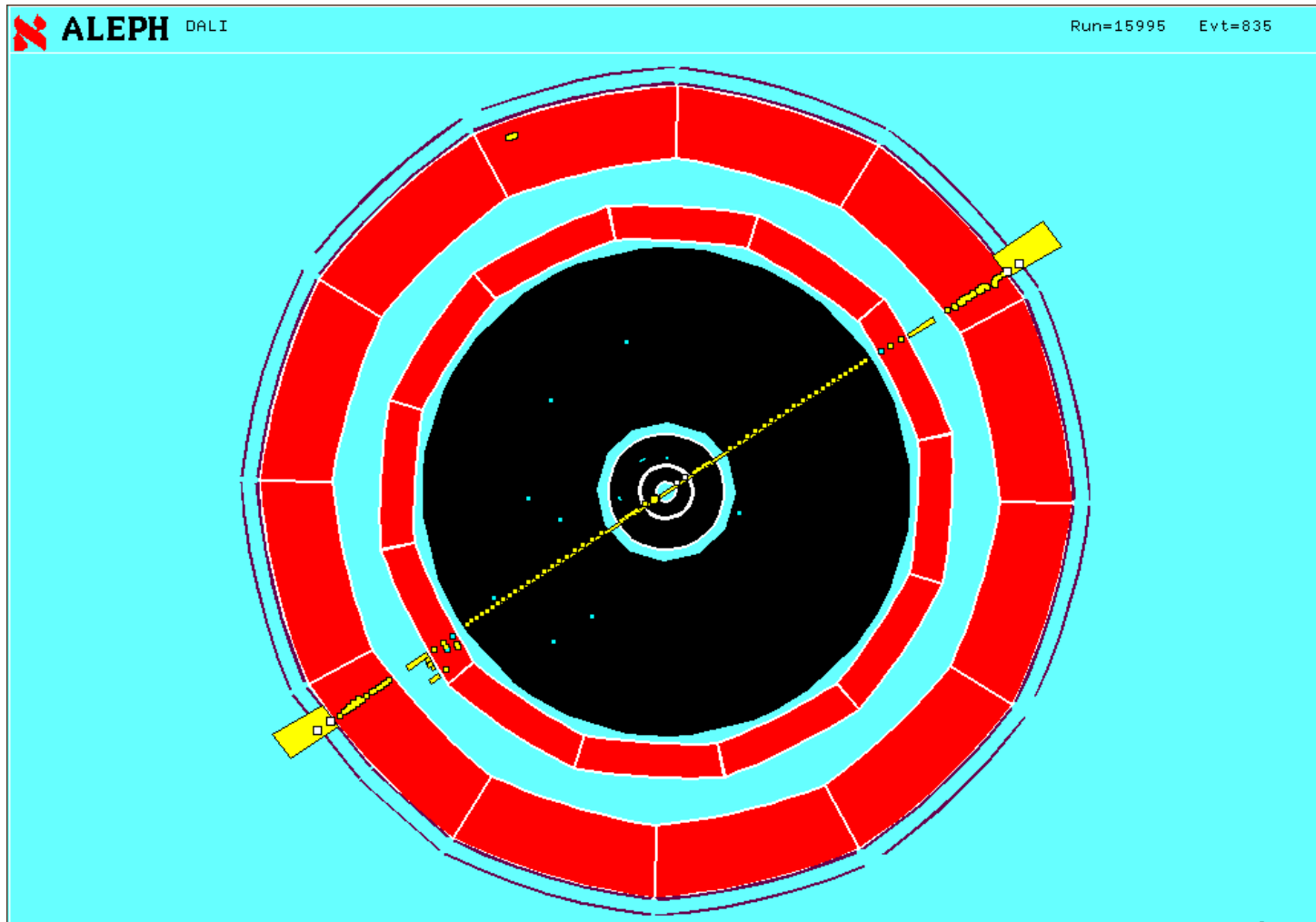
$$Z \rightarrow e^+ e^-$$

Two high momentum charged particles depositing energy in the Electro Magnetic Calorimeter



$$Z \rightarrow \mu^+ \mu^-$$

Two high momentum charged particles traversing all calorimeters and leaving a signal in the muon chambers.



Interaction of Particles with Matter

Any device that is to detect a particle must interact with it in some way → almost ...

In many experiments neutrinos are measured by missing transverse momentum.

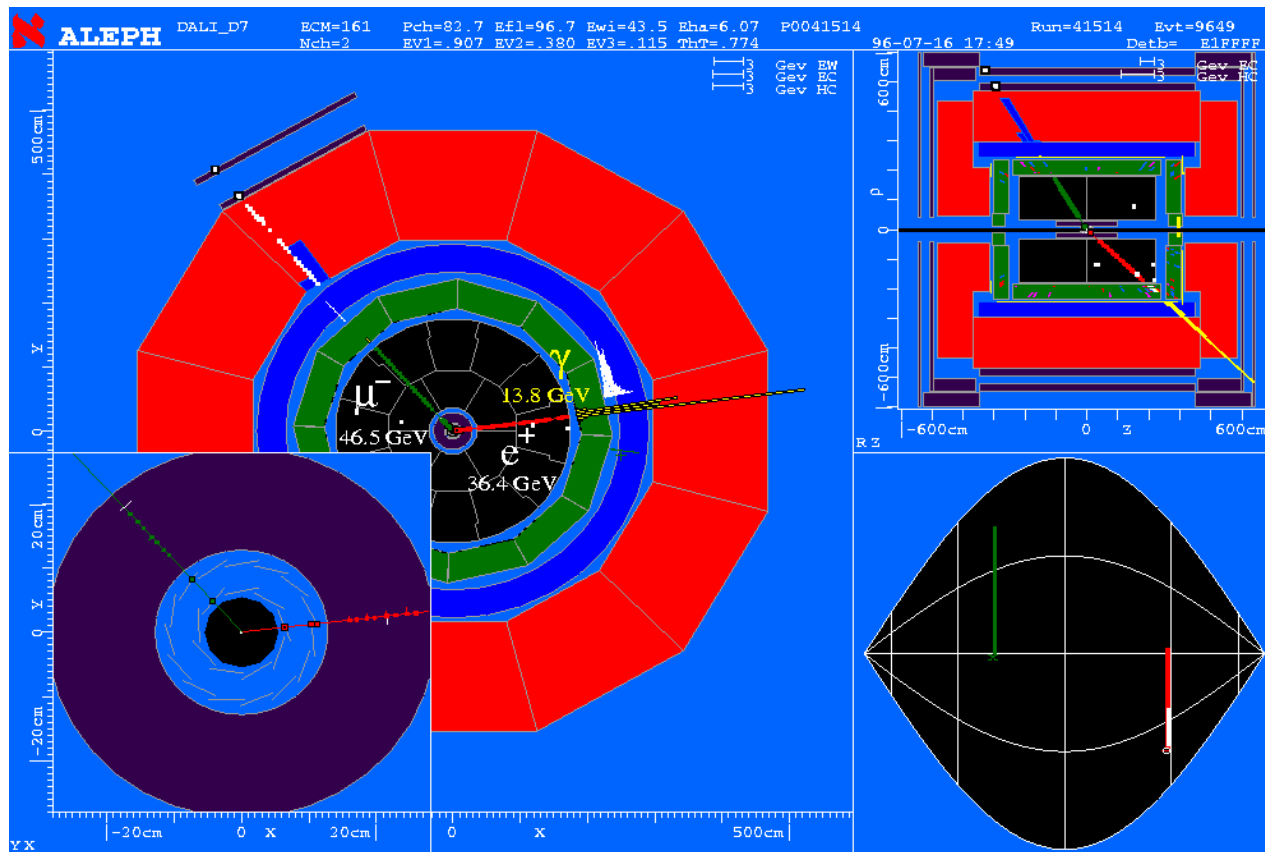
E.g. e^+e^- collider. $P_{\text{tot}}=0$,

If the Σp_i of all collision products is $\neq 0$ → neutrino escaped.



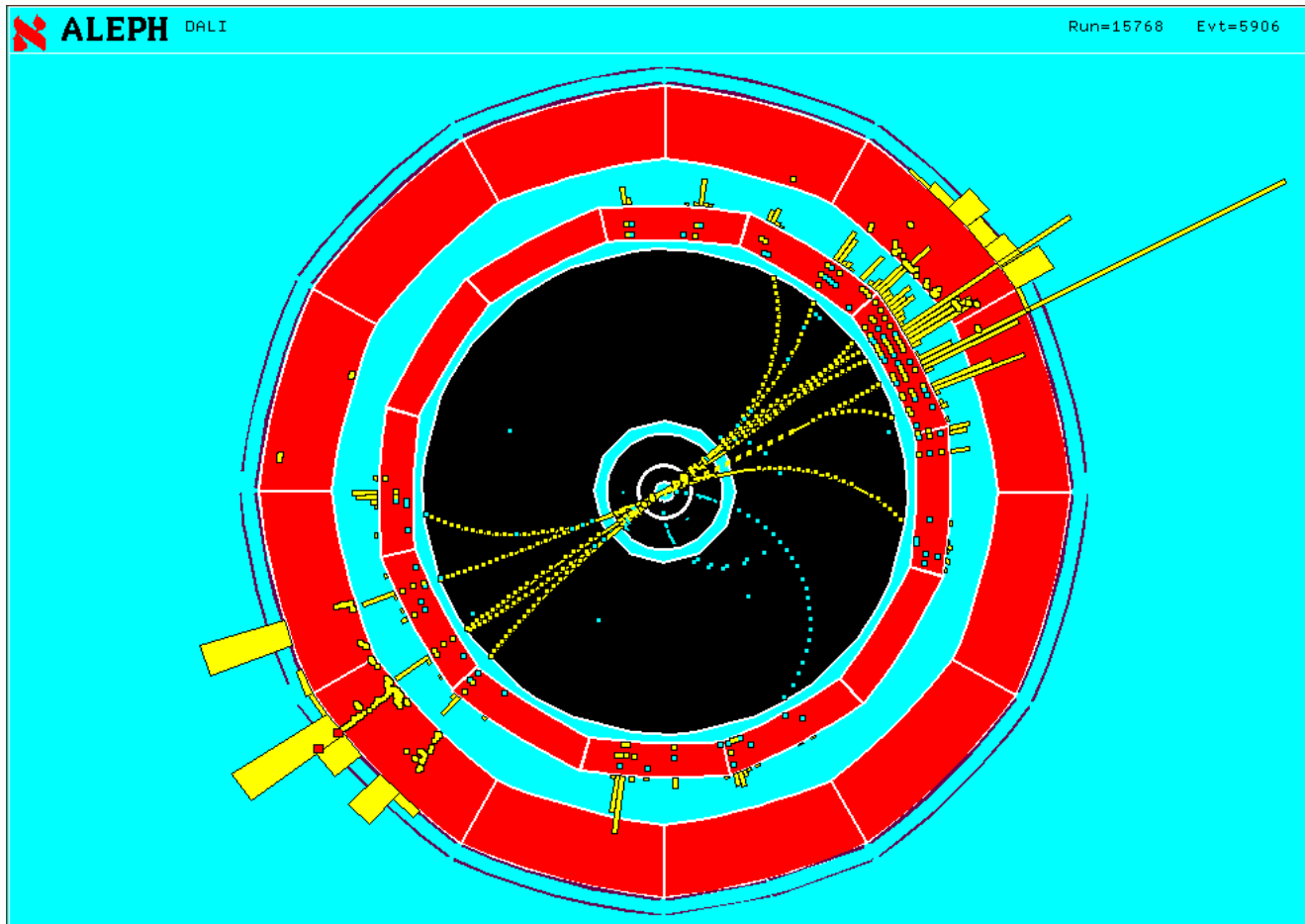
$$W^+W^- \rightarrow e + \mu_e + \mu + \mu$$

Single electron, single Muon, Missing Momentum



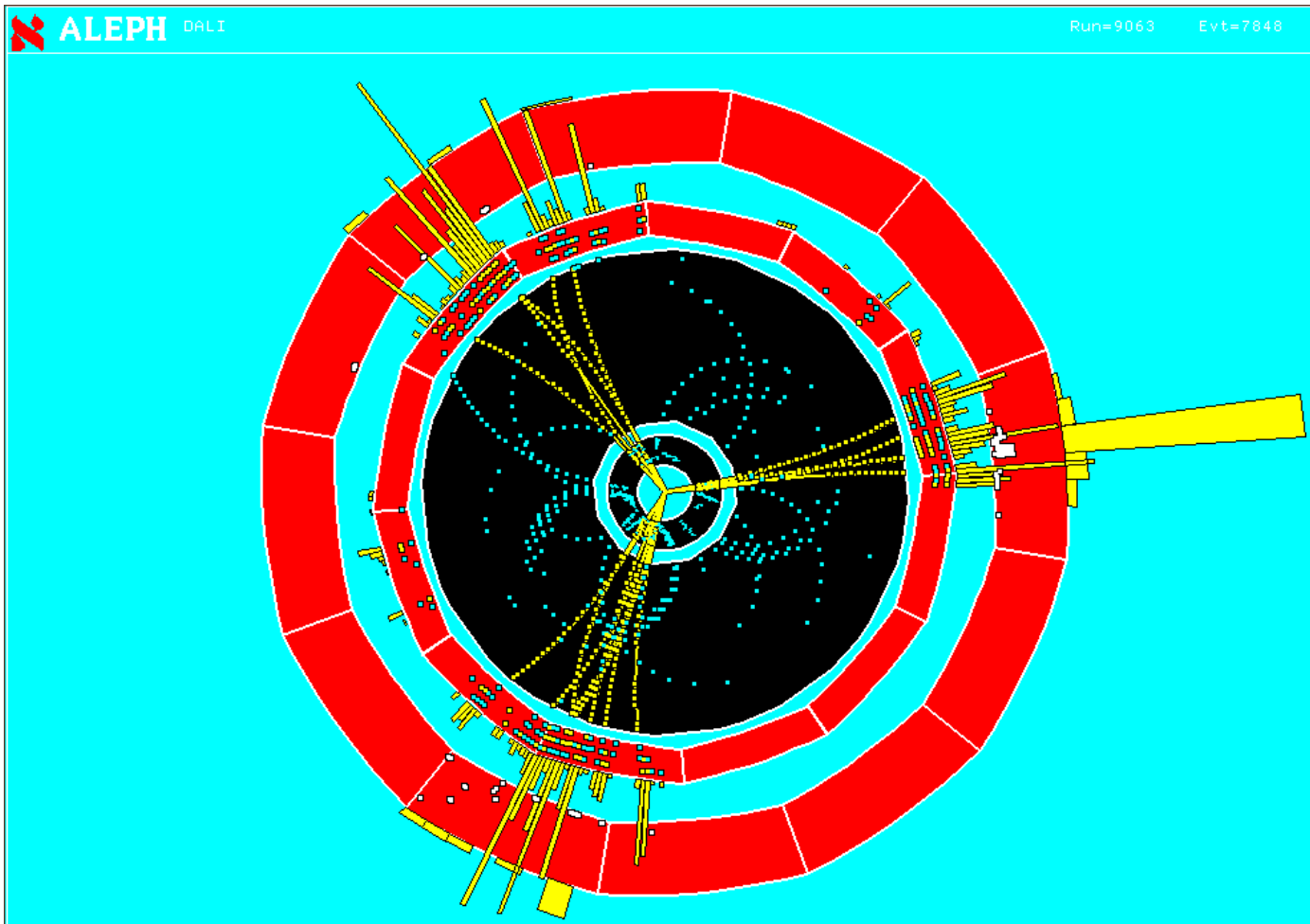
$$Z \rightarrow q \bar{q}$$

Two jets of particles



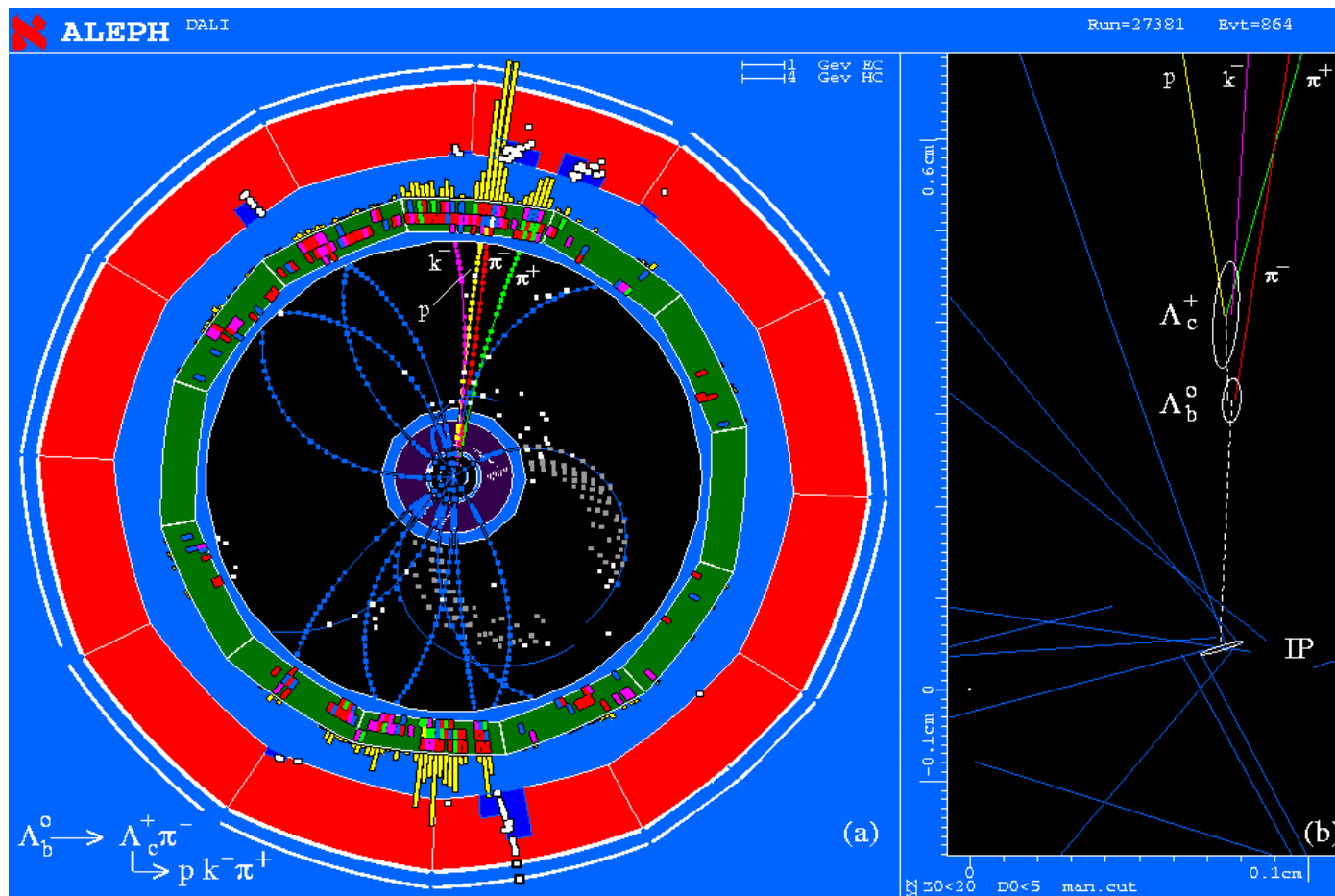
$$Z \rightarrow q \bar{q} g$$

Three jets of particles

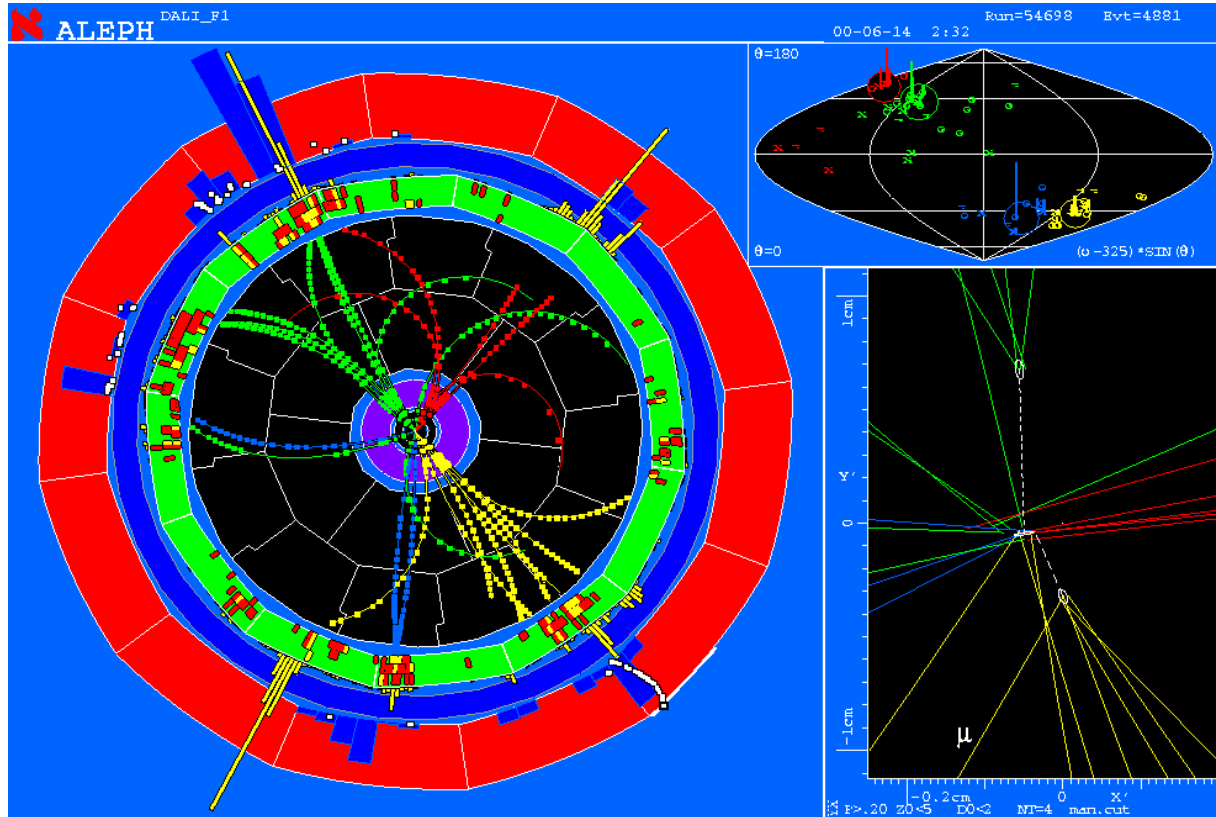
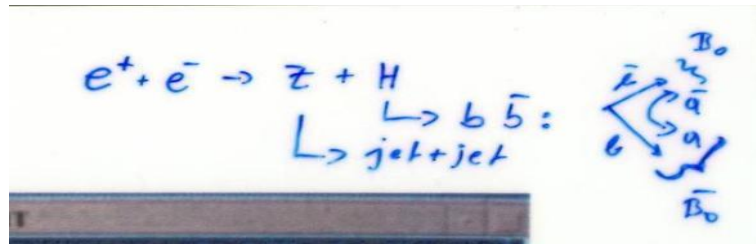


Two secondary vertices with characteristic decay particles giving invariant masses of known particles.

Bubble chamber like – a single event tells what is happening. Negligible background.

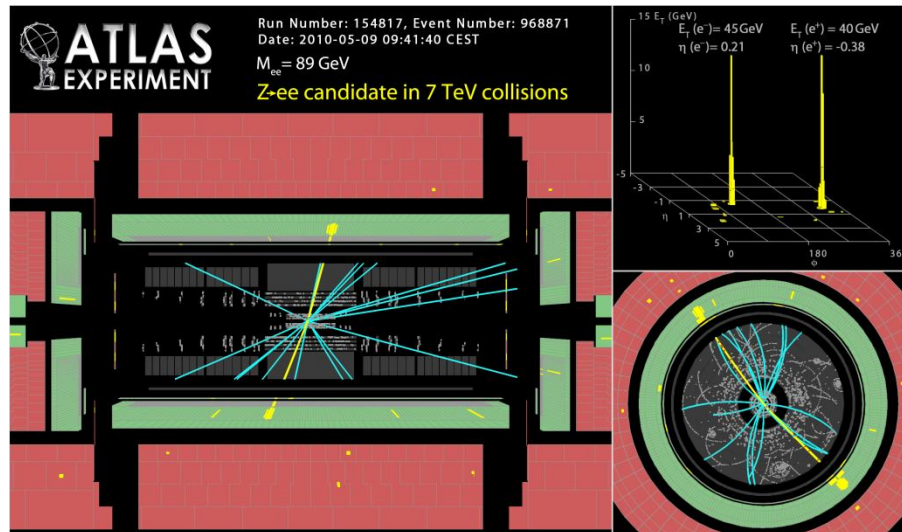
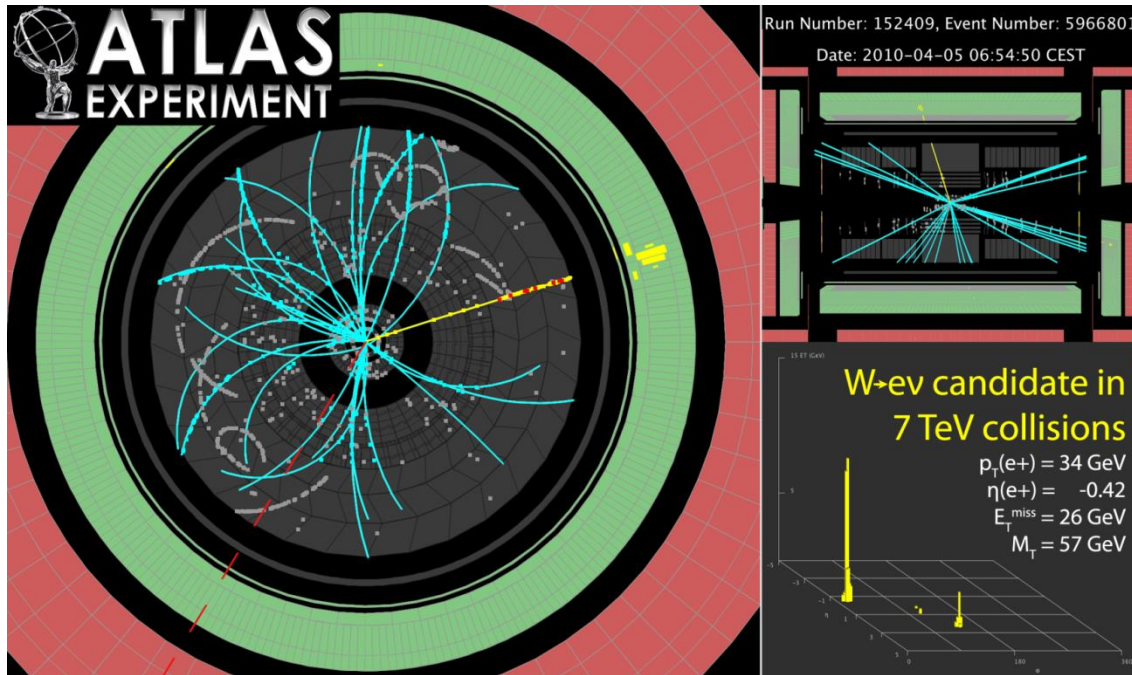


ALEPH Higgs Candidate

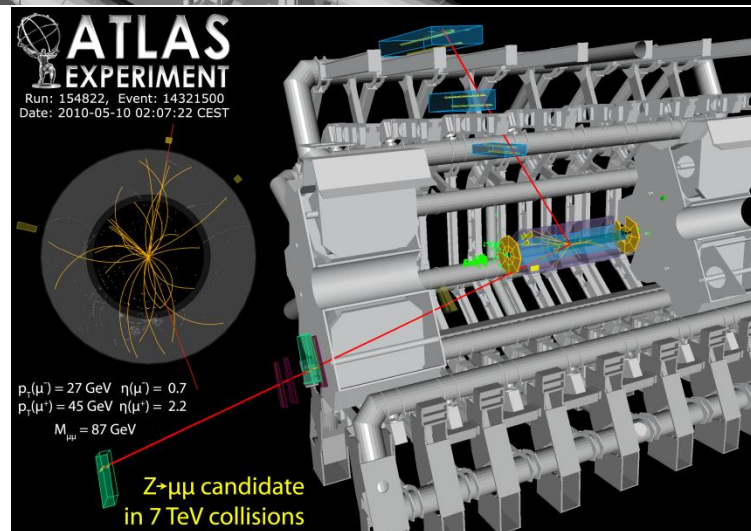
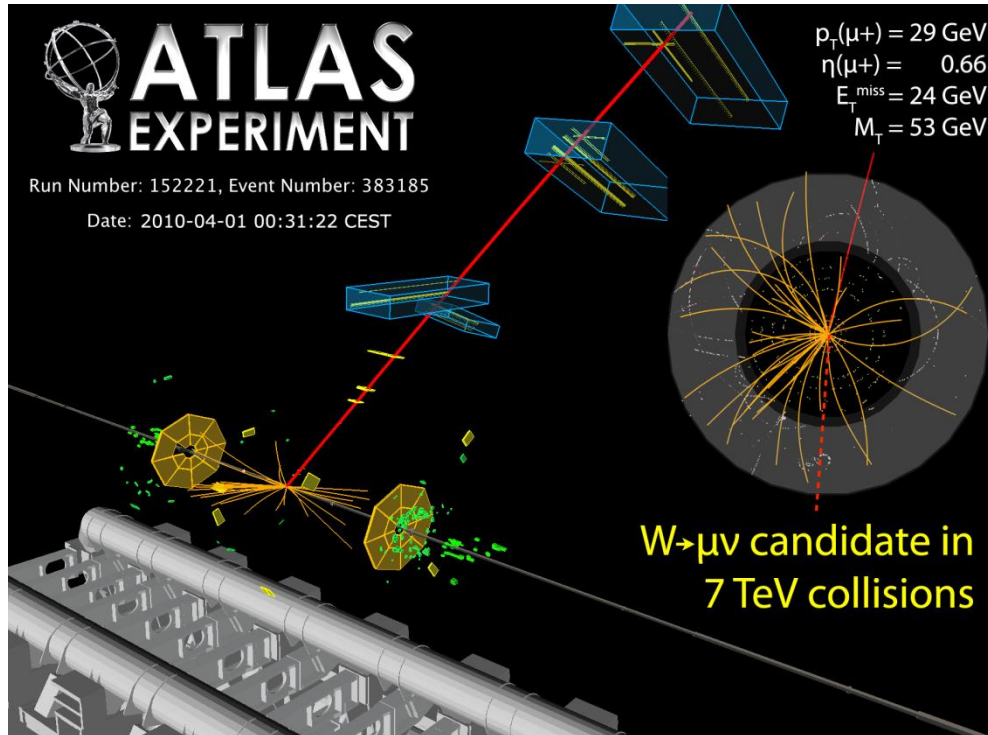


Undistinguishable background exists. Only statistical excess gives signature.

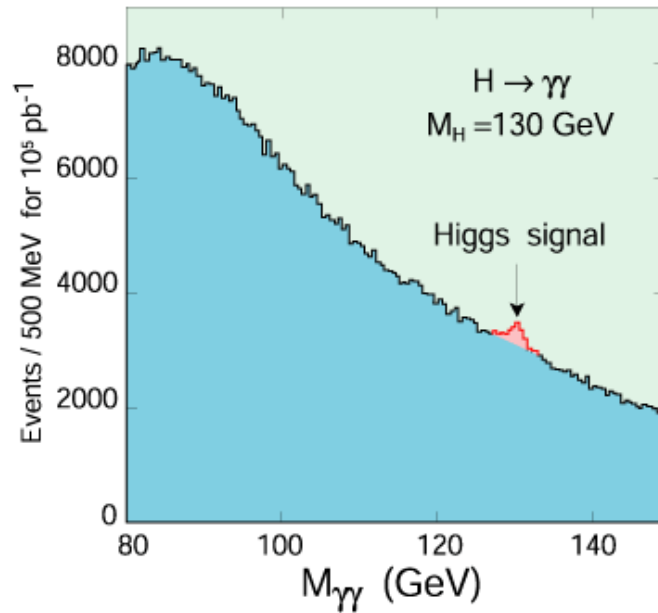
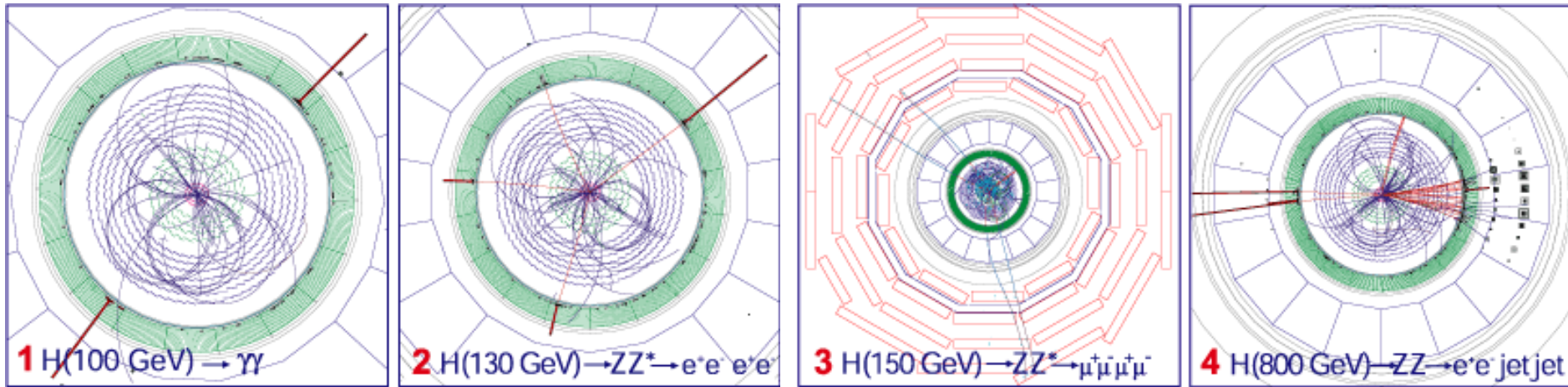
2010 ATLAS W, Z candidates



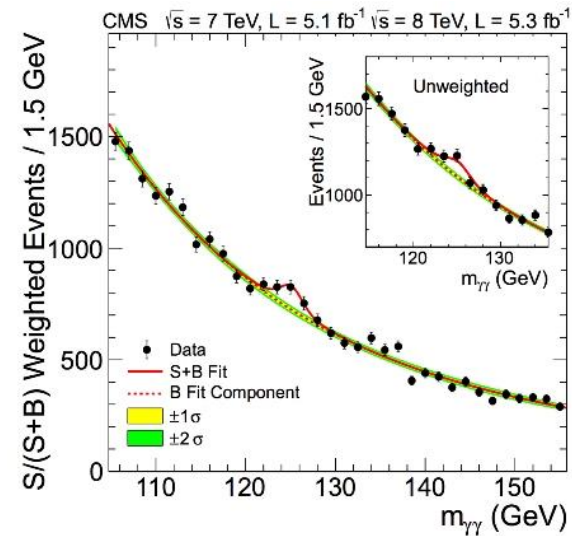
2010 ATLAS W, Z candidates



Simulated Higgs Boson at CMS



Particle seen as an excess of two photon events above the irreducible background.



Principles:

Only a few of the numerous known particles have lifetimes that are long enough to leave tracks in a detector.

Most of the particles are measured through the decay products and their kinematic relations (invariant mass). Most particles are only seen as an excess over an irreducible background.

Some short lived particles (b,c –particles) reach lifetimes in the laboratory system that are sufficient to leave short tracks before decaying → identification by measurement of short tracks.

In addition to this, detectors are built to measure the 8 particles

$$e^{\pm}, \mu^{\pm}, \gamma, \pi^{\pm}, K^{\pm}, K^0, p^{\pm}, n$$

Their difference in mass, charge and interaction is the key to their identification.

Backup

Cherenkov Radiation

If we describe the passage of a charged particle through material of dielectric permittivity ϵ_1 (using Maxwell's equations) the differential energy cross section is >0 if the velocity of the particle is larger than the velocity of light in the medium is

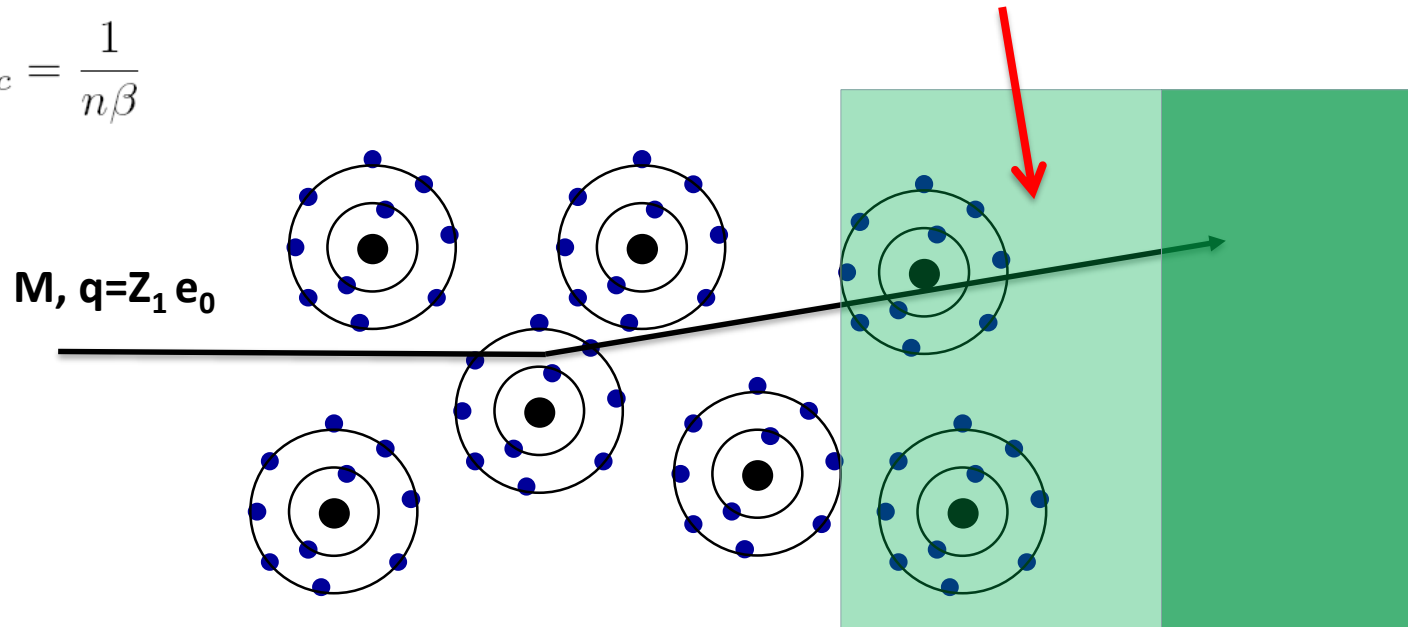
$$\frac{d\sigma}{dE} = \frac{\alpha}{\beta^2 \pi} \frac{A}{N_A \rho Z_2 \hbar c} \left(\beta^2 - \frac{1}{\epsilon_1} \right) \rightarrow \frac{N_A \rho Z_2}{A} \frac{d\sigma}{d\omega} \frac{d\omega}{dE} = \frac{\alpha}{c} \left(1 - \frac{1}{\beta^2 n^2} \right) \quad n = \sqrt{\epsilon_1} \quad E = \hbar \omega$$

$$\frac{dE}{dx d\omega} \frac{1}{\hbar} = \frac{\alpha}{c} \left(1 - \frac{1}{\beta^2 n^2} \right) \rightarrow \frac{dN}{dx d\lambda} = \frac{2\pi\alpha}{\lambda^2} \left(1 - \frac{1}{\beta^2 n^2} \right) \quad \omega = \frac{2\pi c}{\lambda}$$

N is the number of Cherenkov Photons emitted per cm of material. The expression is in addition proportional to Z_1^2 of the incoming particle.

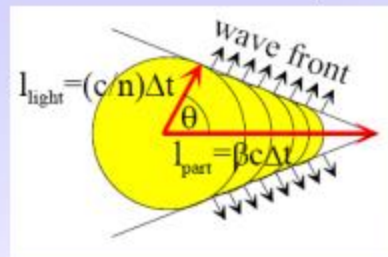
The radiation is emitted at the characteristic angle Θ_c , that is related to the refractive index n and the particle velocity by

$$\cos \Theta_c = \frac{1}{n\beta}$$



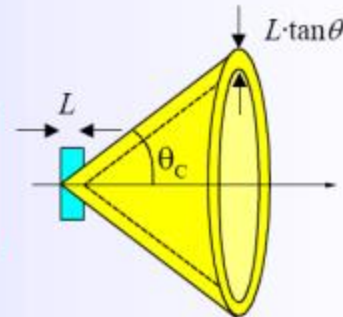
Cherenkov Radiation

with velocity $\beta \geq \beta_{thr} = \frac{1}{n}$ n : refractive index



$$\cos \theta_c = \frac{1}{n\beta}$$

with $n = n(\lambda) \geq 1$



■ $\beta_{thr} = \frac{1}{n} \rightarrow \theta_c \approx 0$ Cherenkov threshold

■ $\theta_{max} = \arccos \frac{1}{n}$ 'saturated' angle ($\beta=1$)

If the velocity of a charged particle is larger than the velocity of light in the medium $v > \frac{c}{n}$ (n ... Refractive Index of Material) it emits 'Cherenkov' radiation at a characteristic angle of $\cos \theta_c = \frac{1}{n\beta}$ ($\beta = \frac{v}{c}$)

$$\frac{dN}{dx} \sim 2\pi\alpha z_1^2 \left(1 - \frac{1}{\beta^2 n^2}\right) \frac{\lambda_2 - \lambda_1}{\lambda_2 \cdot \lambda_1}$$

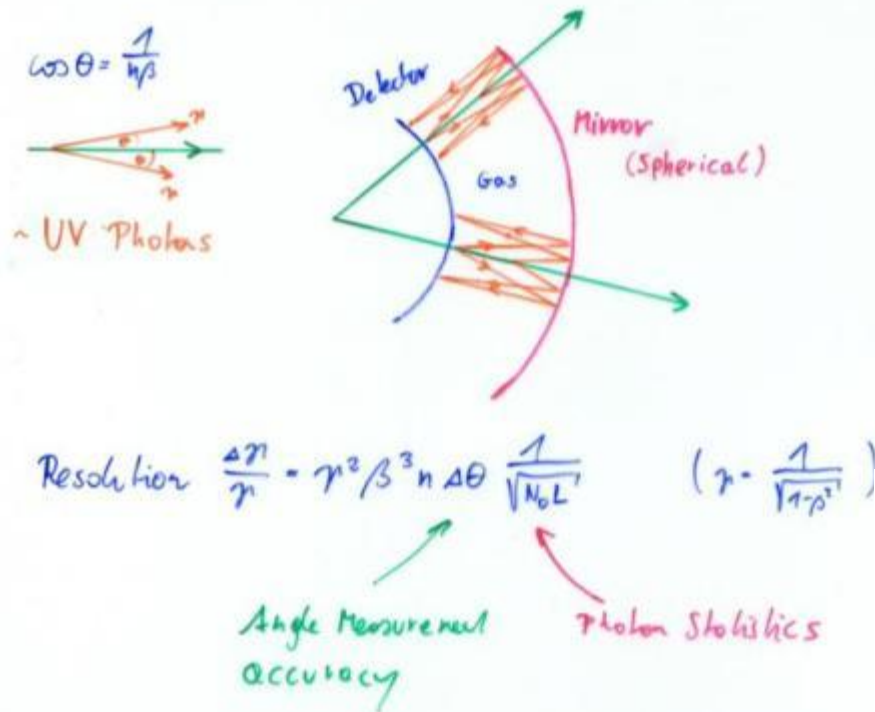
= Number of emitted Photons/length with λ between λ_1 and λ_2

With $\lambda_1 = 400\text{nm}$ $\lambda_2 = 700\text{nm}$

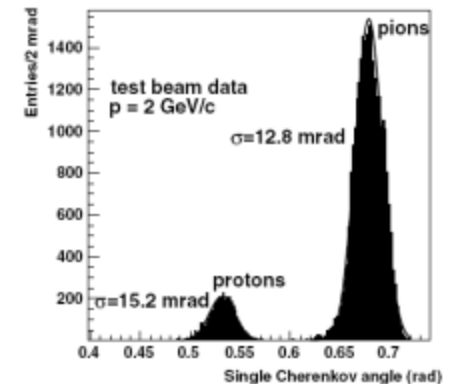
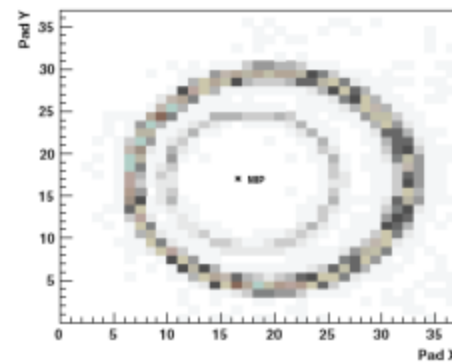
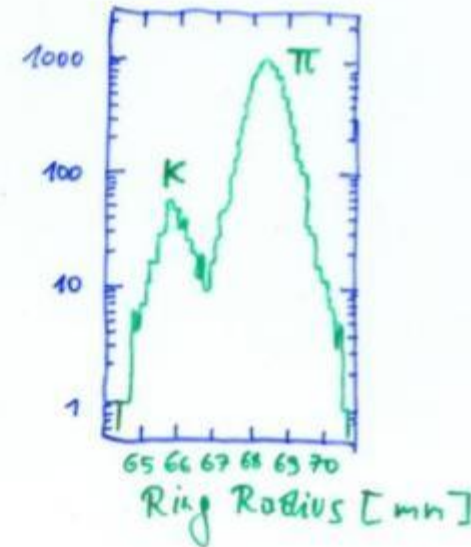
$$\frac{dN}{dx} = 490 \left(1 - \frac{1}{\beta^2 n^2}\right) \left[\frac{1}{\text{cm}}\right]$$

Material	$n-1$	β threshold	n threshold
solid Sodium	3.22	0.24	1.029
lead glass	0.67	0.60	1.25
water	0.33	0.75	1.52
Silica aerogel	0.025-0.075	0.93-0.976	2.7 - 4.6
air	$2.93 \cdot 10^{-4}$	0.9997	41.2
He	$3.3 \cdot 10^{-5}$	0.99997	123

Ring Imaging Cherenkov Detector (RICH)



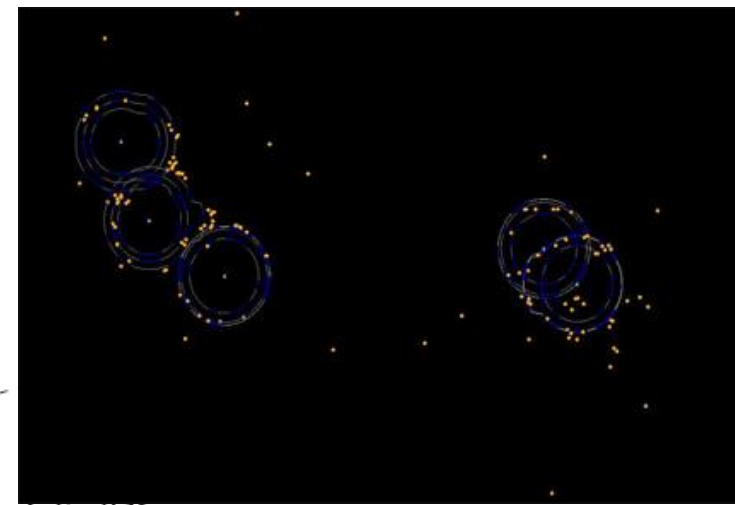
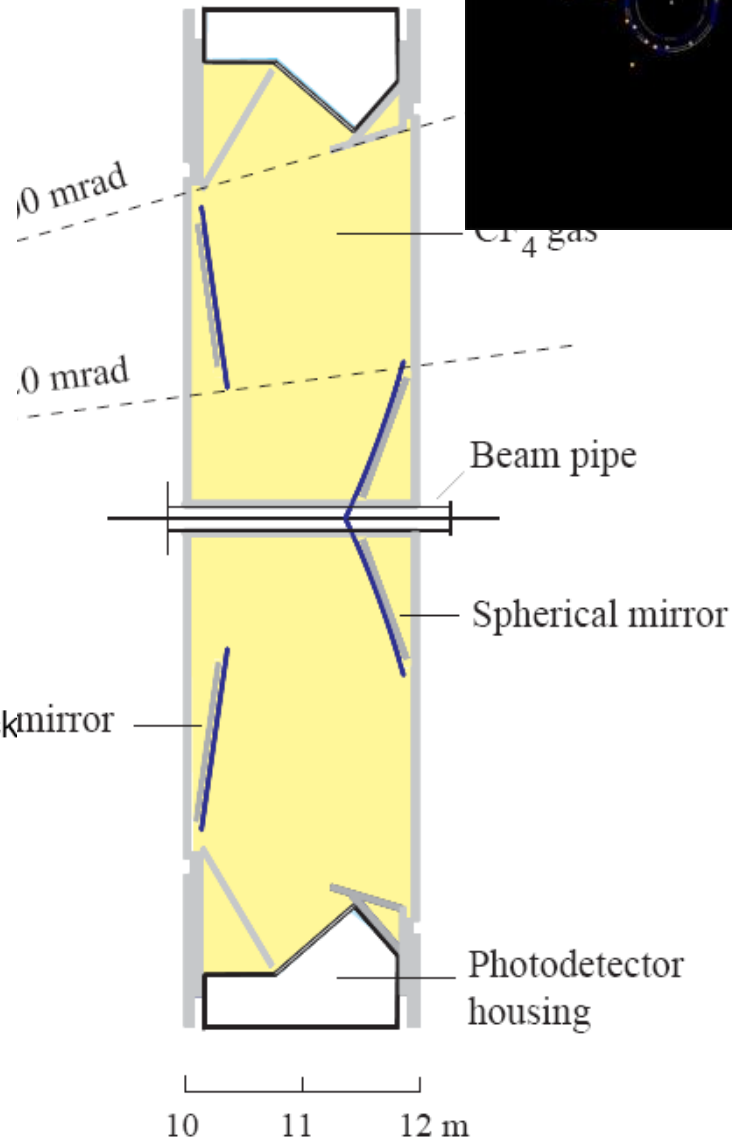
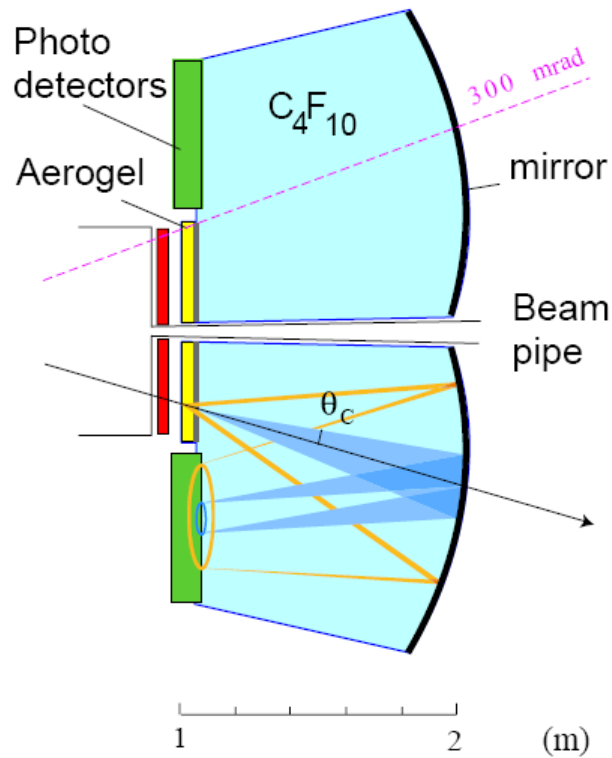
200 GeV/c K, π



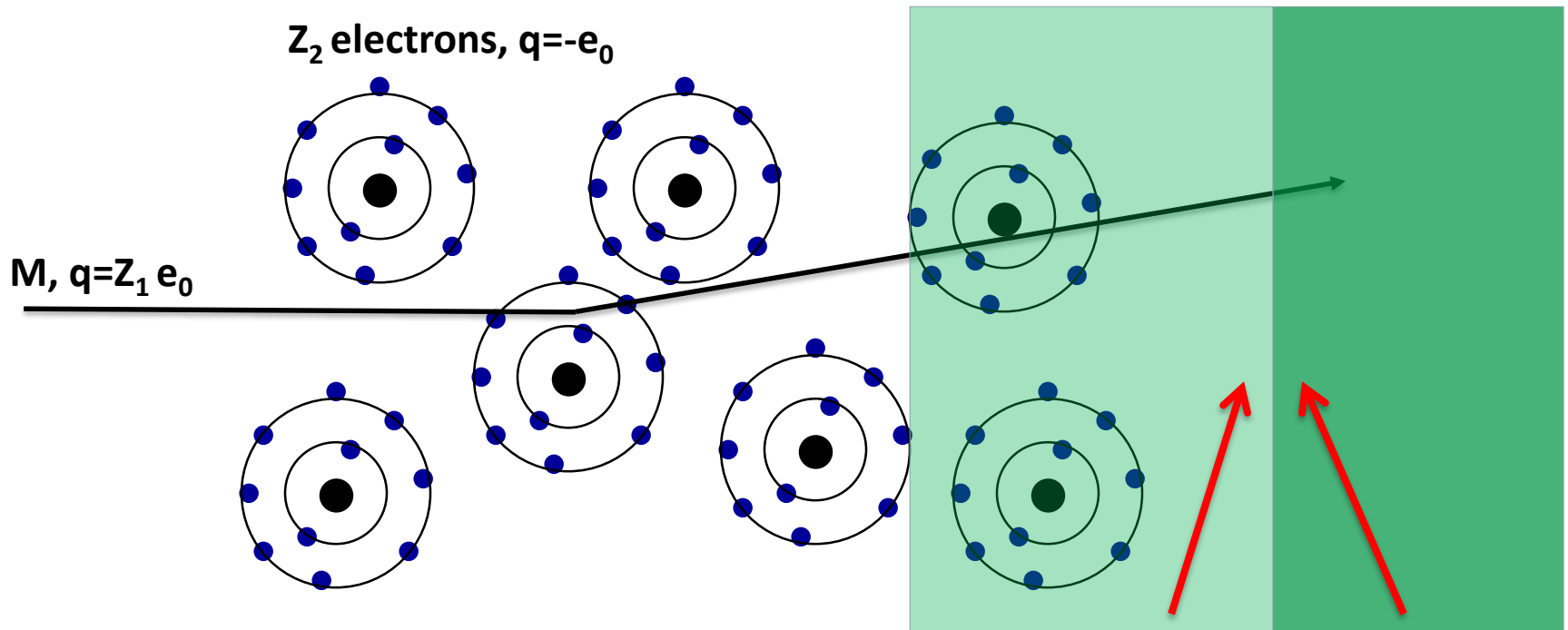
There are only 'a few' photons per event \rightarrow one needs highly sensitive photon detectors to measure the rings !

medium	n	θ_{\max} (deg.)	N_{ph} (eV ⁻¹ cm ⁻¹)
air*	1.000283	1.36	0.208
isobutane*	1.00127	2.89	0.941
water	1.33	41.2	160.8
quartz	1.46	46.7	196.4

LHCb RICH



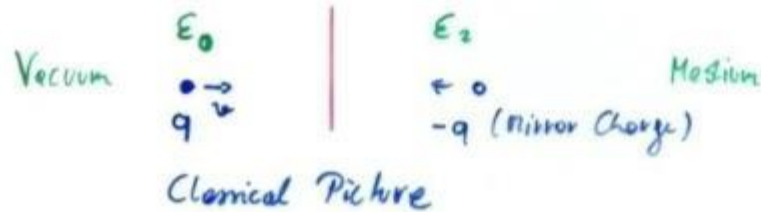
Transition Radiation



When the particle crosses the boundary between two media, there is a probability of the order of 1% to produced and X ray photon, called Transition radiation.

Transition Radiation

Radiation ($\sim \text{keV}$) emitted by
ultra-relativistic Particles when they
traverse the boarder of 2 Materials
of different Dielectric Permittivity (ϵ_1, ϵ_2)



$$q = Z_1 e$$

$$I = \frac{1}{3} d Z_1^2 (\hbar \omega_p) \gamma \dots \text{Radiated Energy per Transition}$$

$\hbar \omega_p \dots$ plasma Frequency of the Medium
 $\dots \sim 20 \text{ eV}$ for Styrene

About half the Energy is radiated between

$$0.1 \hbar \omega_p \gamma < \hbar \omega < \hbar \omega_p \gamma$$

E.g. $\gamma = 1000$ 2-20 keV X-Rays

$$N_\gamma \sim \frac{2}{3} d Z_1^2 \sim 5 \cdot 10^{-3} \cdot Z_1^2$$

γ - Dependence from hardening rather than N_γ

$$\text{Emission Angle} \sim \frac{1}{\gamma}$$

The Number of Photons can be increased by
placing many foils of Material.

