

Theory perspectives on $t\bar{t} + X$ ($X = H, W, Z, b\bar{b}, \dots$)

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$t\bar{t} + X$: a powerful physics case

- $t\bar{t} + X$ processes ($X = V, H, b\bar{b}, \dots$) crucial role in Run II physics
 - ▷ $t\bar{t}H/W/Z/\gamma$: measure top-quark properties
 - ▷ $t\bar{t} + b\bar{b}, W/Z$: backgrounds to Higgs ($t\bar{t}H$) and new-physics searches
- Distinctive yet challenging signatures
 - ▷ $t\bar{t} + H, W, Z$: rare modes, achievable at Run 2
 - ▷ $t\bar{t} + b\bar{b}, t\bar{t} + \text{jets}$: large, complex multiparticle QCD backgrounds
 - ▷ soon to be limited by theoretical systematic uncertainty
 - ▷ vast theoretical effort to provide state-of-the-art predictions
 - ↪ **NLO QCD and EW corrections**
 - ↪ **interface with NLO parton-shower Monte Carlo generators**
- All $t\bar{t} + X$ channels play a role in the measurement of $t\bar{t} + H$
 - ↪ main focus of $t\bar{t}H/tH$ subgroup of HXSWG → YR4
 - ↪ excerpt of results and ideas presented in this talk:
thanks to my co-conveners [S. Guindon, C. Neu, S. Pozzorini],
and all working-group participants!

Theory progress $t\bar{t} + X$

- $t\bar{t}H$

- ▷ **NLO QCD corrections**

Beenakker et al., hep-ph/0107081, hep-ph/0211352
Dawson et al., hep-ph/0211438, hep-ph/030508

- ▷ **NLO QCD+EW corrections**

Frixione et al., arXiv:1407.0823, arXiv:1504.03446
Zhang et al., arXiv:1407.1110

- ▷ **$b\bar{b}l^+l^-\nu\bar{\nu}H$, NLO QCD corrections**

Denner et al., arXiv:1506.07448

- ▷ **Beyond NLO QCD, soft-gluon resummation**

Kulesza et al., arXiv:1509.02780
Broggio et al., arXiv:1510.0191

- ▷ **$t\bar{t}H + j$, NLO QCD corrections**

van Deurzen et al., arXiv:1307.8437

Theory progress $t\bar{t} + X$

- $t\bar{t}b\bar{b}$

- ▷ **NLO QCD corrections**

- Bredenstein et al., arXiv:0905.0110, arXiv:1001.4006
 - Bevilacqua et al. arXiv:0907.4723

- $t\bar{t}V$ ($V = W, Z, \gamma$)

- ▷ **NLO QCD corrections**

- Melnikov et al., arXiv:1102.1967 ($t\bar{t}\gamma$)
 - Hirschi et al. arXiv:1103.0621 ($t\bar{t}\gamma, Z, W$)
 - Lazopoulos et al. arXiv:0804.2220 ($t\bar{t}Z$)
 - Kardos et al. arXiv:1111.0610 ($t\bar{t}Z$),
 - Campbell et al. arXiv:1204.5678 ($t\bar{t}W$)

- ▷ **NLO QCD+EW corrections**

- Frixione et al. arXiv:1504.03446 ($t\bar{t}VV$)

- ▷ **Beyond NLO QCD, soft-gluon resummation**

- Broggio et al., arXiv:1702.00800 ($Zb\bar{b}$)

- $t\bar{t}VV$ ($V = W, Z, \gamma$)

- ▷ **NLO QCD corrections**

- Kardos et al., arXiv:1408.0278 ($t\bar{t}\gamma\gamma$)
 - Maltoni et al., arXiv:1507.05640 ($t\bar{t}VV, V = W, Z, \gamma$)
 - van Deurzen et al., arXiv:1509.02077 ($t\bar{t}\gamma\gamma$)

Theory progress, NLO QCD+Parton Shower

- $t\bar{t}H$

MG5_aMC@NLO, Frederix et al., arXiv:1104.5613, [arXiv:1610.07922](#)

PowHel, Garzelli et al., arXiv:1108.0387, [arXiv:1610.07922](#)

POWHEG BOX, Hartanto et al., arXiv:1501.04498, [arXiv:1610.07922](#)

OpenLoops+SHERPA, Cascioli et al., [arXiv:1610.07922](#)

HERWIG7: Reuschle et al., [arXiv:1610.07922](#)

- tH

MG5_aMC@NLO, Demartin et al., arXiv:1504.00611

- $t\bar{t}b\bar{b}$

PowHel, Kardos et al., arXiv:1303.6291, [arXiv:1610.07922](#)

OpenLoops+SHERPA, Cascioli et al., arXiv:1309.5912, [arXiv:1610.07922](#)

MG5_aMC@NLO, Frederix et al., [arXiv:1610.07922](#)

- $t\bar{t}V$ ($V = W, Z$)

PowHel, Garzelli et al. arXiv:1111.1444, arXiv:1208.2665, [arXiv:1610.07922](#)

OpenLoops+SHERPA, Cascioli et al., [arXiv:1610.07922](#)

MG5_aMC@NLO, Frixione et al., [arXiv:1610.07922](#)

[arXiv:1610.07922](#) → LHC Higgs XS Working Group, Yellow Report 4
($t\bar{t}H/tH$ section)

Highlights from TH progress

Through $t\bar{t} + X$ processes following the $t\bar{t}H$ lead:

- $t\bar{t}H$
 - ↪ NLO QCD+EW, parton-level accuracy
 - ↪ NLO QCD+PS, understanding accuracy at PS-level
- $t\bar{t}b\bar{b}$: many layers of complexity
 - ↪ 5F $t\bar{t}$ +jets vs 4F $t\bar{t} + b\bar{b}$ revisited
 - ↪ 4F $t\bar{t} + b\bar{b}$ recommended but need further studies
 - ↪ $t\bar{t}b\bar{b}$: NLO+PS, comparison of MC generators
 - ↪ Off-shell effects: signal (NLO) and signal-background interference (LO)
- $t\bar{t}$ +jets,
 - ↪ NLO QCD+PS, with merging
- $t\bar{t} + V, t\bar{t} + VV$ ($V = W, Z$)
 - ↪ NLO QCD+EW, parton-level accuracy
 - ↪ NLO QCD+PS
- $t\bar{t} + \gamma\gamma$

$t\bar{t}H$, NLO QCD+EW corrections

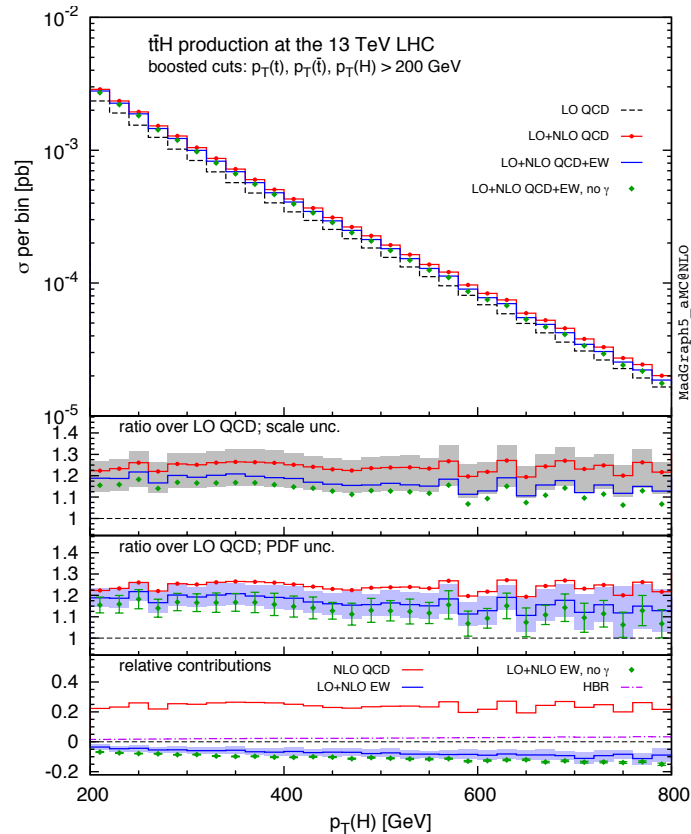
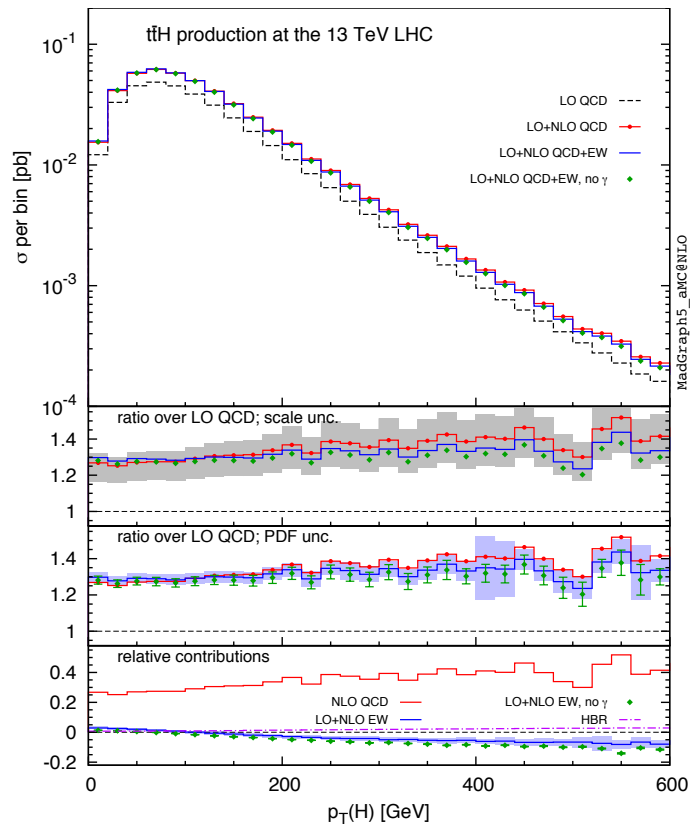
At 13 TeV, for $M_H = 125$ GeV,

$$\sigma_{QCD+EW}^{NLO} [\text{fb}] = 507.1^{+5.7\%}_{-9.2\%} (\text{scale}) \pm 3.6\% (\text{PDF} + \alpha_s)$$

where

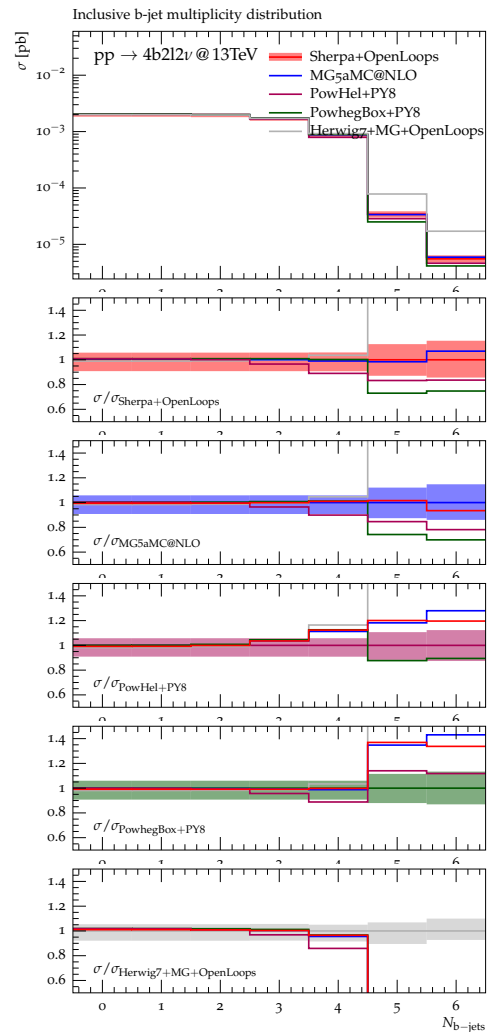
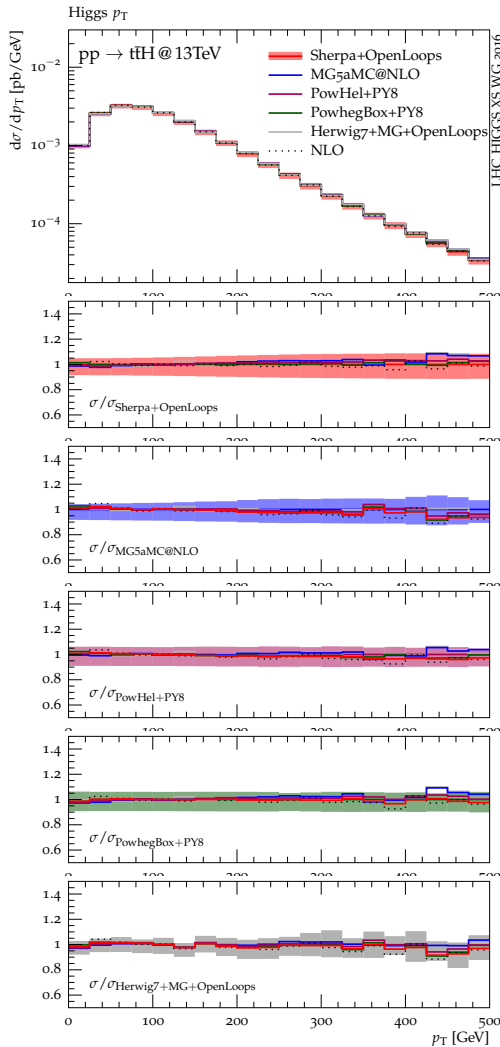
$$\sigma_{QCD+EW}^{NLO} = \sigma_{QCD}^{NLO} + \delta\sigma_{EW} = K\sigma_{QCD}^{LO} + \delta\sigma_{EW}$$

with $K = \sigma_{QCD}^{NLO}/\sigma_{QCD}^{LO} = 1.25$ and $\delta_{EW} = \delta\sigma_{EW}/\sigma_{QCD}^{NLO} = 1.7\%$.



$t\bar{t}H(H \rightarrow b\bar{b})$, validation of NLO QCD+PS

5 different NLO PS-MC compared!



Comparison with and w/o top decays,

$$t \rightarrow be^+ \nu_e$$

$$\bar{t} \rightarrow \bar{b}\mu^- \nu_\mu$$

Proved very good compatibility within scale uncertainty

$$N_{b\text{-jets}} > 4$$

↪ shower effects

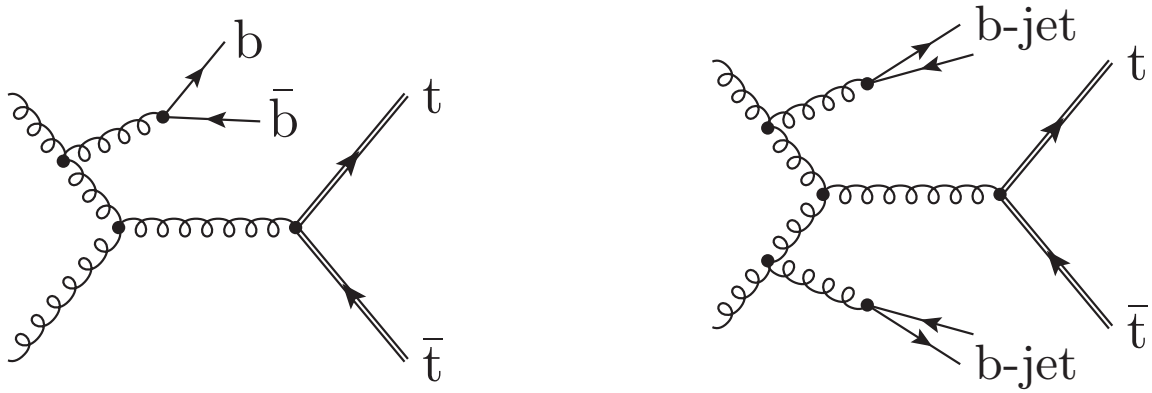
↪ more meaningful to investigate in the context of specific experimental analyses.

see YR4 - $t\bar{t}H/tH$ section, arXiv:1610.07922

$t\bar{t} + b$ jets, NLO QCD

Accuracy of theoretical predictions and reliable estimate of their uncertainty still problematic, but progress is being made.

- NLO QCD calculation reduces uncertainty from $\approx 80\%$ to $\approx 20 - 30\%$
[Bredenstein et al., arXiv:0905.0110, arXiv:1001.4006, Bevilacqua et al., arXiv:0907.4723]
- NLO QCD+PS poses new questions
 - ▷ **5F $t\bar{t}$ +jets** ($m_b = 0$, $N_f = 5$) [PowHel, Kardos et al., arXiv:1303.6291]
 - ↪ NLO matrix elements cannot describe $g \rightarrow b\bar{b}$
 - ↪ $m_{b\bar{b}} > \xi_m 2m_b$ and $p_T^b > \xi_T m_b$ cuts introduced to mimic m_b effects.
 - ▷ **4F $t\bar{t}b\bar{b}$** ($m_b \neq 0$, $N_f = 4$) [OpenLoops+SHERPA, Cascioli et al., arXiv:1309.5912; MG5_aMC@NLO, Frederix et al.]
 - ↪ NLO matrix element describe first $g \rightarrow b\bar{b}$ splitting
 - ↪ NLO accuracy for any $N_b \geq 1$ observable

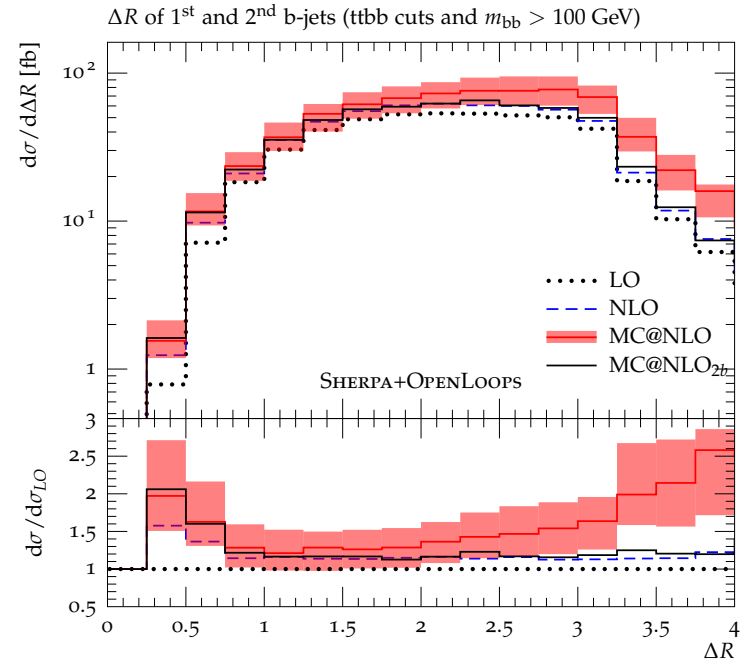
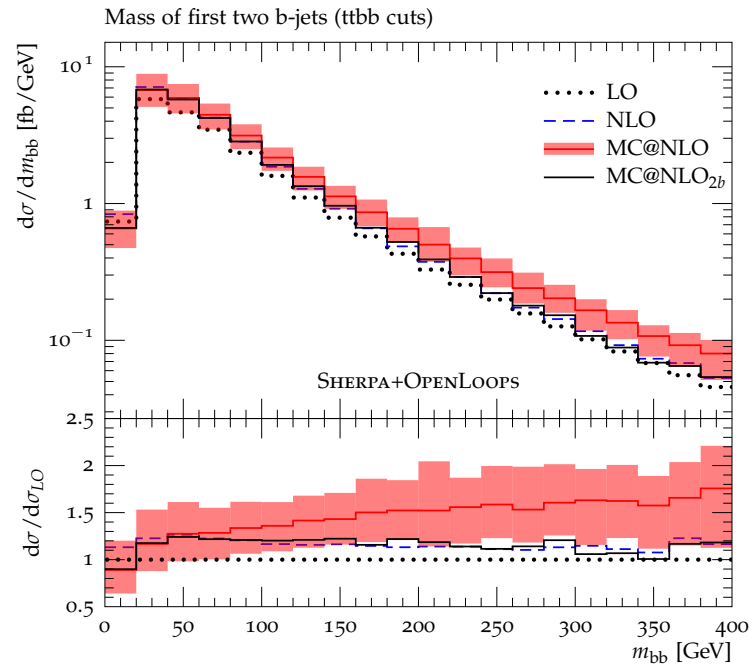


Interesting to notice that:

	ttb	ttbb	ttbb($m_{bb} > 100$)
σ_{LO} [fb]	$2644^{+71\%+14\%}_{-38\%-11\%}$	$463.3^{+66\%+15\%}_{-36\%-12\%}$	$123.4^{+63\%+17\%}_{-35\%-13\%}$
σ_{NLO} [fb]	$3296^{+34\%+5.6\%}_{-25\%-4.2\%}$	$560^{+29\%+5.4\%}_{-24\%-4.8\%}$	$141.8^{+26\%+6.5\%}_{-22\%-4.6\%}$
$\sigma_{\text{NLO}}/\sigma_{\text{LO}}$	1.25	1.21	1.15
σ_{MC} [fb]	$3313^{+32\%+3.9\%}_{-25\%-2.9\%}$	$600^{+24\%+2.0\%}_{-22\%-2.1\%}$	$181.0^{+20\%+8.1\%}_{-20\%-6.0\%}$
$\sigma_{\text{MC}}/\sigma_{\text{NLO}}$	1.01	1.07	1.28
σ_{MC}^{2b} [fb]	3299	552	146
$\sigma_{\text{MC}}^{2b}/\sigma_{\text{NLO}}$	1.00	0.99	1.03

[Cascioli et al., arXiv:1309.5912]

Large enhancement in Higgs-boson region due to $g \rightarrow b\bar{b}$ (from PS).



From the ongoing discussion within $t\bar{t}H/tH$ WG

- In experimental analyses $t\bar{t} + b\bar{b}$ obtained as (\hookrightarrow see Maria's talk):
 - ▷ 5F $t\bar{t} + \text{jets}$ (light/ c/b) ($m_b = 0$)
extracting and reweighing $t\bar{t} + 1b$, $t\bar{t} + 2b$, $t\bar{t} + B$, ... samples with 4F $t\bar{t} + b\bar{b}$
NLO calculation: prone to several correlated systematic errors.
 - ▷ 4F $t\bar{t} + b\bar{b}$ ($m_b \neq 0$): $t\bar{t} + b$, $t\bar{t} + 2b$, etc. well defined.
- WG recommendation: use NLO PS MC to produce 4F $t\bar{t} + b\bar{b}$ samples for $t\bar{t} + b$ jets, and $t\bar{t} + \text{jets}$ for everything else.
- Caveat: this assumes the validity of 4F calculation in all regimes and over the entire phase space. What else?
- **Proper 5F calculation** of $t\bar{t} + b$ should be structured as:
 - ▷ tree level: $bg \rightarrow t\bar{t} + b$
 - ▷ + $O(\alpha_s)$ QCD virtual corrections
 - ▷ + $O(\alpha_s)$ QCD real corrections (including $gg \rightarrow t\bar{t} + b\bar{b}$, $m_b \neq 0$)
 - ▷ initial state $\ln(m_b^2/M^2)$ resummed
 - ▷ not yet consistently implemented in NLO PS MC

$t\bar{t} + b$ jets, comparison of NLO Monte Carlo simulations

[Full details at: <https://twiki.cern.ch/twiki/bin/view/LHCPhysics/ProposalTtbb>]

- Comparing different matchings:

- ▷ SHERPA+OpenLoops [Höche et al.] and [Cascioli et al.] (4F, $m_b > 0$)
- ▷ Madgraph5_aMC@NLO+PYTHIA8.2 [Frederix et al.] (4F, $m_b > 0$)
- ▷ PowHel+PYTHIA8.2 [Garzelli et al.] (5F, $m_b = 0, m_{bb} > 2m_b, p_{T,b} > m_b$)

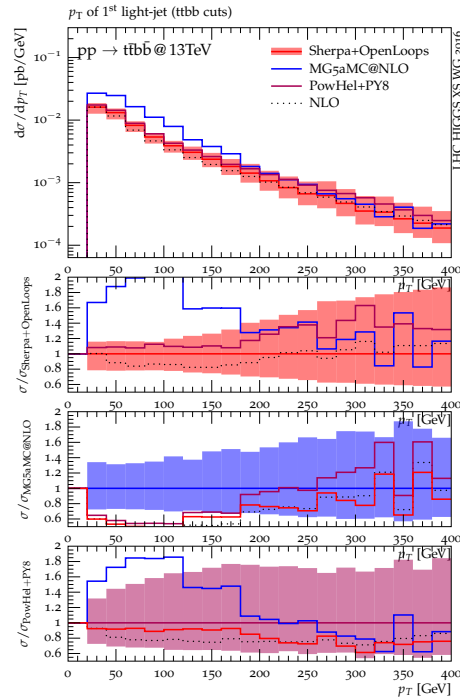
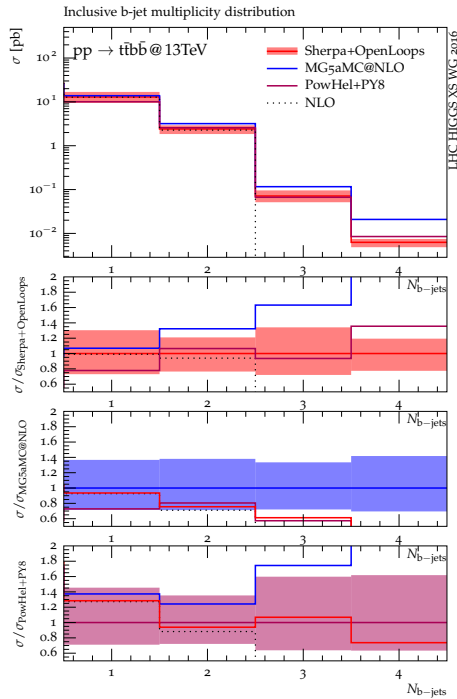
- General setup: not just a choice of parameters

- ▷ consistent HF treatment: $N_f = 4$ vs $N_f = 5 \rightarrow \alpha_s, \text{PDF}$
- ▷ control source of b quarks: matrix element, parton shower, top decays \hookrightarrow
exclude some of these sources (e.g: switch off top decays, ...)
- ▷ consistent b -jet definition
- ▷ ...

- Coherent treatment of theoretical uncertainty

- ▷ $\mu_R = \langle E_T \rangle_{\text{geom}}, \mu_F = \mu_Q = H_T/2$
- ▷ scale, PDF dependence
- ▷ shower scale dependence
($\mu_Q = H_T/2$ vs $\mu_Q = f(\xi)\sqrt{\hat{s}}, 0.1 < f(\xi) < 0.25$ vs $h_{\text{damp}} \approx H_T/2, \dots$)

$t\bar{t} + b$ jets, NLO+PS, from YR4



↪ switch off top decays, hadronization, UE

↪ To better compare the effect of

- different matchings
- different parton showers
- different flavor scheme

[$t\bar{t}H/tH$ working group, YR4, arXiv:1610.07922]

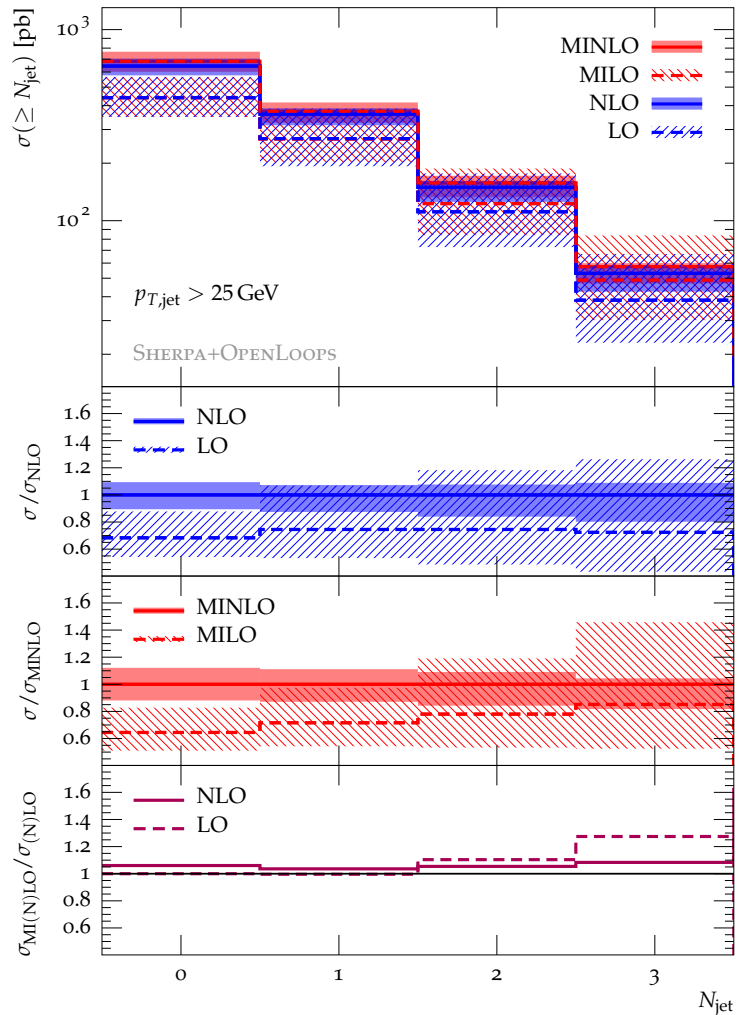
Discrepancies emerge that will have to be understood if we want to resolve the very large systematic uncertainties that affects experimental analyses

↪ **This is becoming a limiting factor** → see ATLAS and CMS talks

Moving forward:

- ▷ Dedicated collaboration on NLO+PS $t\bar{t} + b$ jets in the context of the HXSWG
- ▷ Madgraph5_aMC@NLO 2.5.3 now allows for $\mu_Q = H_T/2$ → ongoing comparison

$t\bar{t}$ +jets at NLO+PS [Höche et al. arXiv:1607.06934]



NLO+PS: Openloops+Sherpa

scale choice and uncertainties:

MINLO method [Hamilton, et al, 12]:
 improved convergence for multi-scale
 processes through NLO+NLL CKKW
 resummation

Large NLO/LO, nice MINLO convergence

↪ can aim for $t\bar{t}$ +multijets at the
 10% precision level

Off-shell signal-background interference, LO

$pp \rightarrow t(bl^+\nu)\bar{t}(\bar{b}jj)H(b\bar{b})$ at LO [Denner, Feger, Scharf, arXiv:1412.5290]

- ▷ include all possible channels with/without top and Higgs resonances
- ▷ include all QCD and EW contributions to matrix elements and interferences

matrix-element order	$O(\alpha_s^3\alpha)$	$O(\alpha_s^2\alpha^2)$	$O(\alpha_s\alpha^3)$	$O(\alpha^4)$
$t\bar{t}H(b\bar{b})$ signal			×	×
$t\bar{t}b\bar{b}$ background		×	×	×
full process ($l^+\nu + 2j + 4b$)	×	×	×	×

▷ Results for 13 TeV LHC:

- negligible $t\bar{t}H$ signal-background interference
- significant **-8% interference between QCD and EW contributions to $t\bar{t}b\bar{b}$ background** (from W exchange in t -channel)
- significant **+11% enhancement in $t\bar{t}b\bar{b}$ background** from diagrams without top resonances

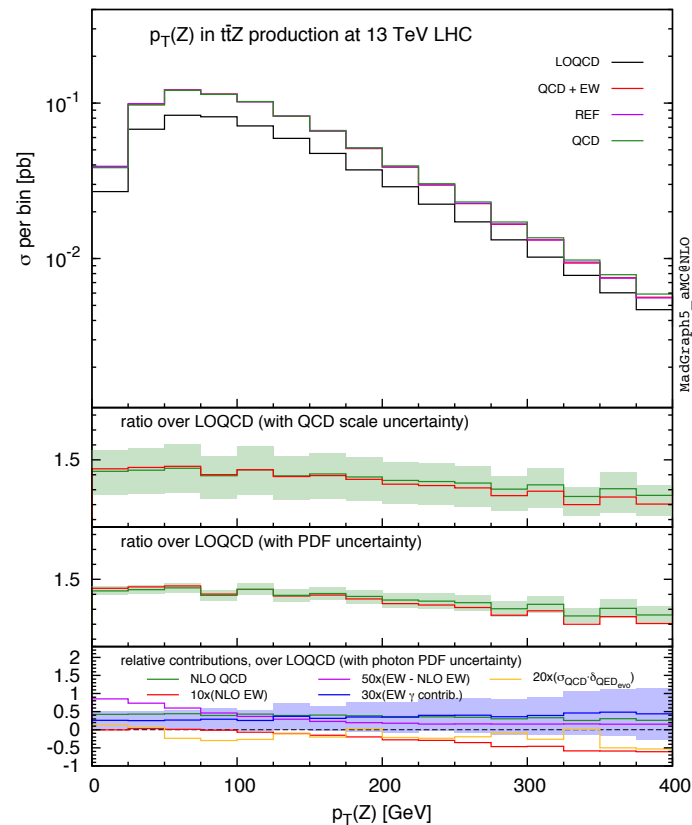
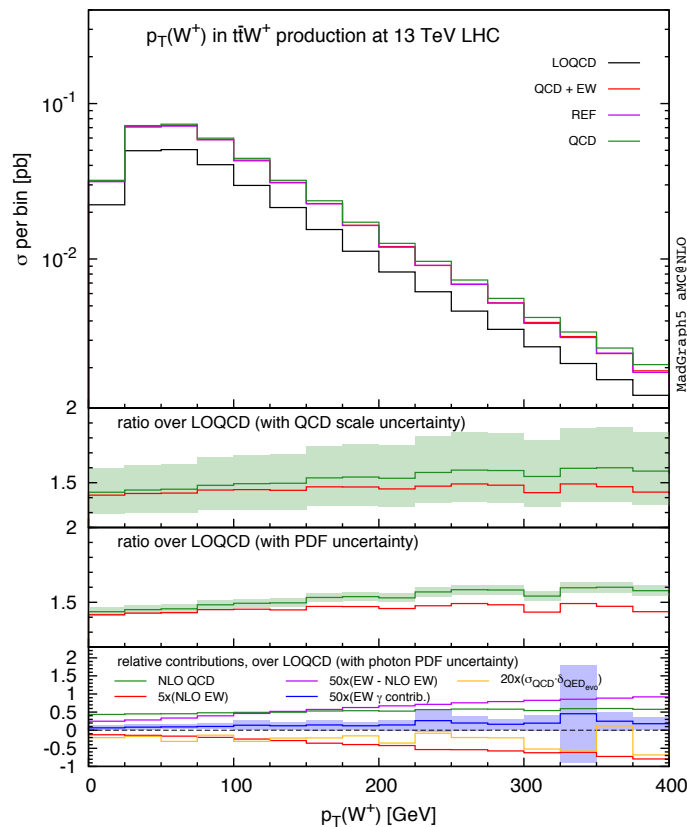
NLO QCD+EW corrections for $t\bar{t} + V$ ($V = W^\pm, Z$) production

[Frixione, Hirschi, Pagani, Shao, Zaro, arXiv:1504.03446]

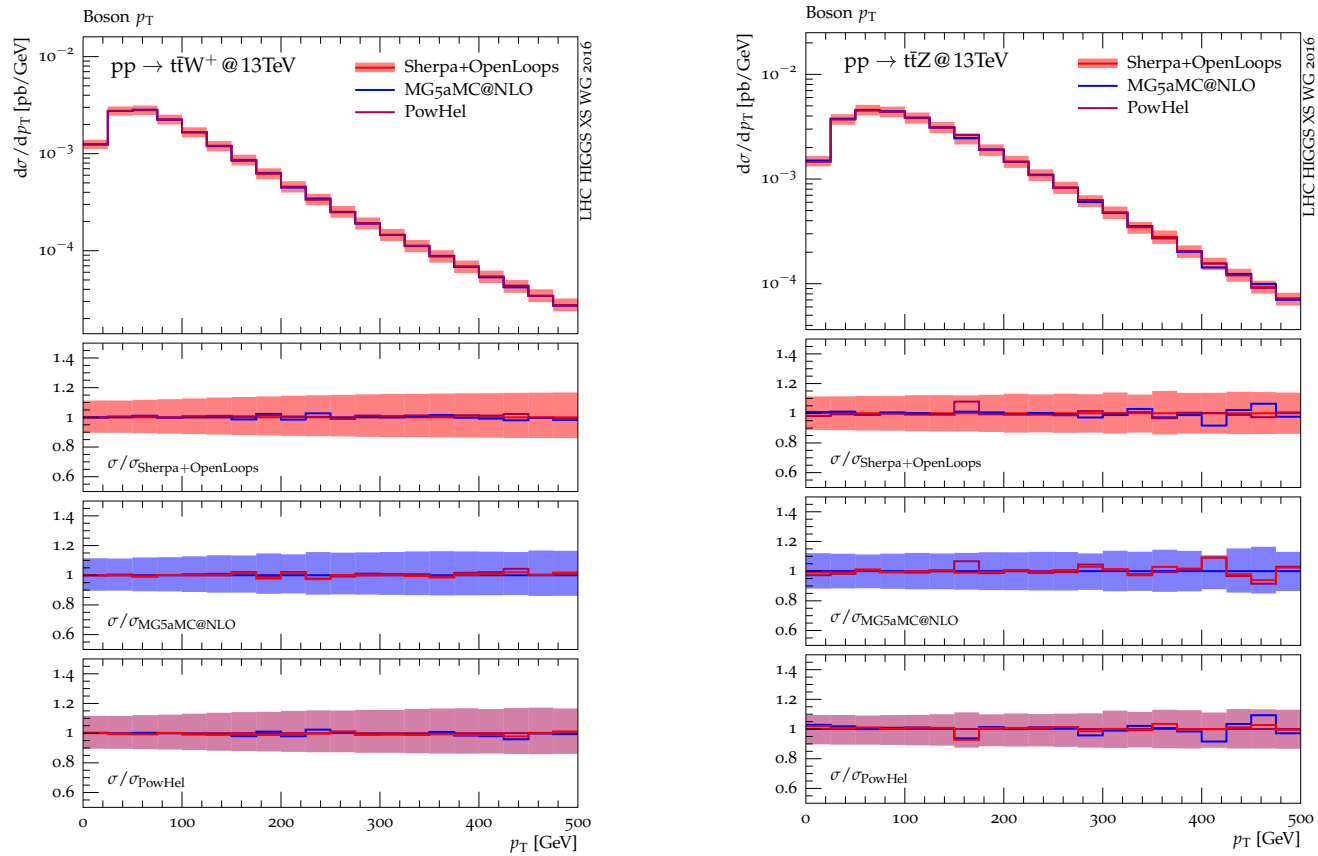
$$\sqrt{s} = 13 \text{ TeV}, K = \sigma_{QCD}^{NLO} / \sigma_{QCD}^{LO}, \delta_{EW} = \delta\sigma_{EW} / \sigma_{QCD}^{NLO}$$

Process	σ_{QCD}^{NLO}	σ_{QCD+EW}^{NLO}	K_{QCD}	$\delta_{EW}[\%]$	Scale[%]		PDF[%]		$\alpha_S[\%]$	
$t\bar{t}Z$	841.3(1.6)	839.3(1.6)	1.39	-0.2	+9.6%	-11.3%	+2.8%	-2.8%	+2.8%	-2.8%
$t\bar{t}W^+$	412.0(0.32)	397.6(0.32)	1.49	-3.5	+12.7%	-11.4%	+2.0%	-2.0%	+2.6%	-2.6%
$t\bar{t}W^-$	208.6(0.16)	203.2(0.16)	1.51	-2.6	+13.3%	-11.7%	+2.1%	-2.1%	+2.9%	-2.9%

▷ inclusive cross section: **NLO EW corrections** \ll **NLO QCD uncertainty**



Comparison of $t\bar{t} + V$ distributions at NLO QCD \rightarrow YR4



\rightarrow consistency among different generators at fixed order

NLO QCD corrections for $t\bar{t} + VV$ ($V = W^\pm, Z, H$) production

[Maltoni, Pagani, Tsinikos, arXiv:1507.05640 and YR4]

Heavy-Boson-Radiation (HBR) for $t\bar{t} + V$ processes

13 TeV σ [ab]	$t\bar{t}W^+Z$	$t\bar{t}W^-Z$	$t\bar{t}ZZ$
NLO QCD	2705(3) ^{+9.9%} ^{+2.7%} _{-10.6%} _{-2.7%}	1179(2) ^{+11.2%} ^{+3.7%} _{-11.2%} _{-3.7%}	1982(2) ^{+5.2%} ^{+2.6%} _{-9.0%} _{-2.6%}
LO	1982(2) ^{+28.4%} ^{+3.3%} _{-20.6%} _{-3.3%}	839.4(6) ^{+28.2%} ^{+4.2%} _{-20.5%} _{-4.2%}	1611(1) ^{+31.4%} ^{+2.7%} _{-22.1%} _{-2.7%}
K -factor	1.36	1.40	1.23
13 TeV σ [ab]	$t\bar{t}W^+H$	$t\bar{t}W^-H$	$t\bar{t}ZH$
NLO QCD	1089(1) ^{+1.8%} ^{+2.6%} _{-5.9%} _{-2.6%}	493.0(5) ^{+2.6%} ^{+3.4%} _{-6.4%} _{-3.4%}	1535(2) ^{+1.9%} ^{+3.0%} _{-6.8%} _{-3.0%}
LO	997.0(9) ^{+26.9%} ^{+3.0%} _{-19.8%} _{-3.0%}	440.0(4) ^{+26.9%} ^{+3.8%} _{-19.8%} _{-3.8%}	1391(1) ^{+32.2%} ^{+2.8%} _{-22.6%} _{-2.8%}
K -factor	1.09	1.12	1.10
13 TeV σ [ab]	$t\bar{t}W^+W^-$	$t\bar{t}W^+W^-$ (4f)	$t\bar{t}HH$
NLO QCD	–	11500(10) ^{+8.1%} ^{+3.0%} _{-10.9%} _{-3.0%}	756.5(7) ^{+1.1%} ^{+3.3%} _{-4.4%} _{-3.3%}
LO	8380(5) ^{+33.2%} ^{+3.0%} _{-23.1%} _{-3.0%}	8357(5) ^{+33.3%} ^{+3.0%} _{-23.1%} _{-3.0%}	765.4(5) ^{+31.8%} ^{+2.9%} _{-22.4%} _{-2.9%}
K -factor	–	1.38	0.99

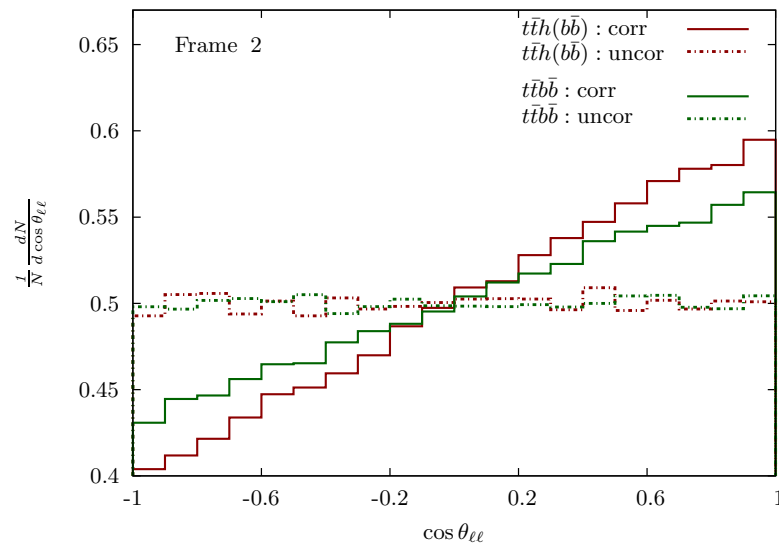
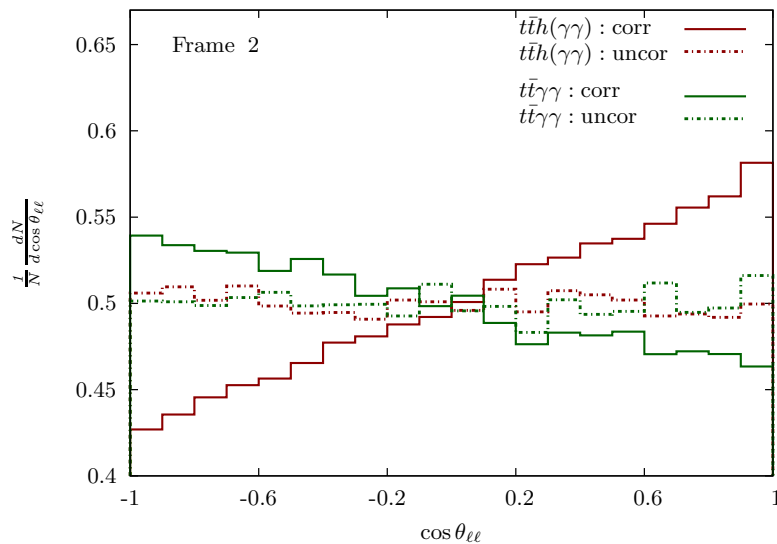
$t\bar{t} + \gamma\gamma$: spin-correlation effects in top decays

Implemented at NLO+PS in MG5_aMC@NLO, POWHEG BOX, and SHERPA

- only (NLO production) \times (LO decay) accuracy
- off-shell and non-resonant effects neglected → need off-shell studies

On top of discriminating SM (scalar) vs BSM (pseudoscalar) Higgs-boson ([Artoisenet et al, arXiv:1212.3460](#)),

can be very important in discriminating signal and background:



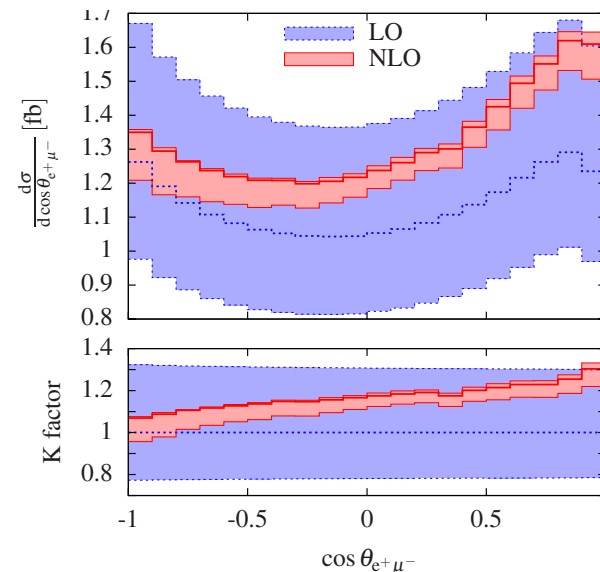
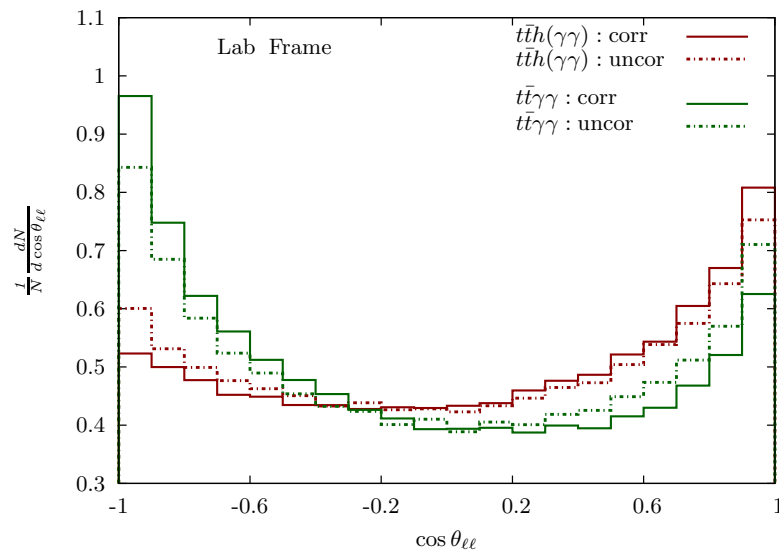
[Biswas et al., arXiv:1403.1790](#)

Idea: $t\bar{t}(\gamma\gamma)$ and $t\bar{t}H$ have different helicity structure in the chiral limit $m_t \rightarrow 0$ or $m_t/m_{t\bar{t}} \rightarrow 0$, and this main character is approximately preserved away from the chiral limit. Not so easily arguable for $t\bar{t}(b\bar{b})$.

Off-shell $t\bar{t}H$ production and decay

$pp \rightarrow t(be^+ \nu_e)\bar{t}(\bar{b}\mu^- \bar{\nu}_\mu)H$ at NLO in QCD [Denner, Feger, arXiv:1506.07448]

- ▷ include all non-resonant effects, off-shell effects, and interferences: NLO production and decay;
- ▷ full $2 \rightarrow 5$ NLO QCD calculation:
RECOLA+COLLIER [Denner, Dittmaier, Hofer, Uccirati]
- ▷ effects of only 1% on NLO total cross section ($\approx \Gamma_t/m_t$);
- ▷ validate LO study of distributions:



Biswas et al., arXiv:1403.1790

Denner et al., arXiv:1506.07448

- ▷ validation with PS study [van Deurzen et al., arXiv:1509.02077]

Outlook

- $t\bar{t} + X$ processes have gained a prominent role in Run II LHC Higgs-physics analyses.
- **Lots of recent theoretical progress:**
 - ▷ $t\bar{t}H$: NLO QCD+EW, NLO QCD+PS
 - ▷ $t\bar{t}b\bar{b}$, NLO QCD+PS
 - ▷ $t\bar{t}$ + light jets, , NLO QCD+PS
 - ▷ Off-shell effects: signal (NLO) and signal-background interference (LO)
 - ▷ $t\bar{t}V$, $t\bar{t}VV$, NLO QCD+EW
 - ▷ Spin-correlation effects in top decays, and more ...
- **They are very challenging modes** to control. Building on existing experience, much needed progress will depend on
 - ▷ **validating state-of-the-art theoretical tools for Monte-Carlo simulations**, signal and **background**
 - ▷ **adopting validated tools** in experimental analyses.