

**Space charge: PART I**

**Analytical solution of the Laplace equ. for  
a coaxial cavity**

**Space charge: PART II**

**Space charge scenarios for the ALICE TPC**

**Space charge: PART III**

**Space point distortions due to space charges  
and more ...**

# **Space charge: PART III**

**Space point  
distortions due to  
space charges  
and more ...**

**Stefan Rossegger**

# Basic concept

Space Charge  
distribution

$$\rho(r, \phi, z)$$

*Laplace  
equation*

1

Field Distortions

$$\Delta E_r, \Delta E_\phi, \Delta E_z$$

Space point  
distortions

$$\Delta r, \Delta \phi, \Delta z$$

*Langevin  
equation*

2

Solved by the ...

... **novel analytical solution**

(see Part I)

So far **numerically** ...

... with either ALIROOT code

... or within GARFIELD

# ... Equation of motion

$$\mathbf{u} = \frac{e}{m} \tau |\mathbf{E}| \frac{1}{1 + \omega^2 \tau^2} (\mathbf{E} + \omega \tau [\mathbf{E} \times \mathbf{B}] + \omega^2 \tau^2 (\mathbf{E} \cdot \mathbf{B}) \mathbf{B})$$

*Included in the numerical algorithm (within **AliRoot**):*

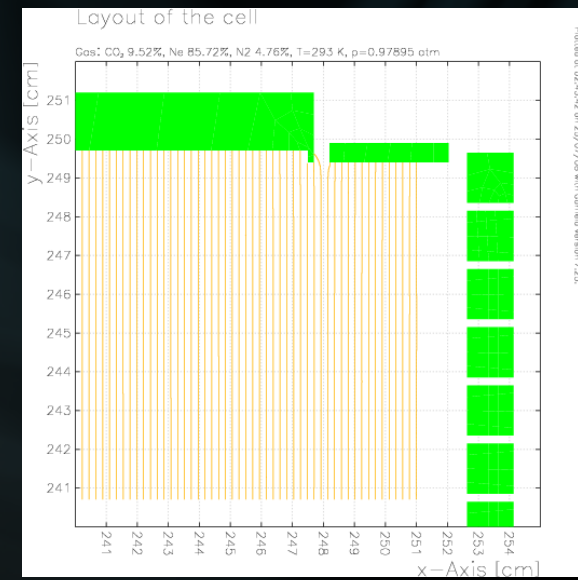
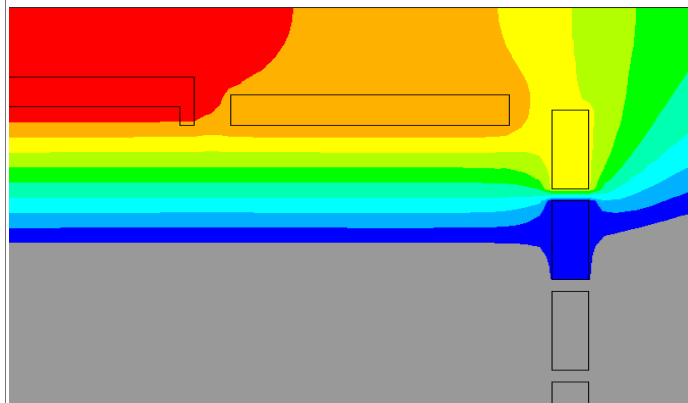
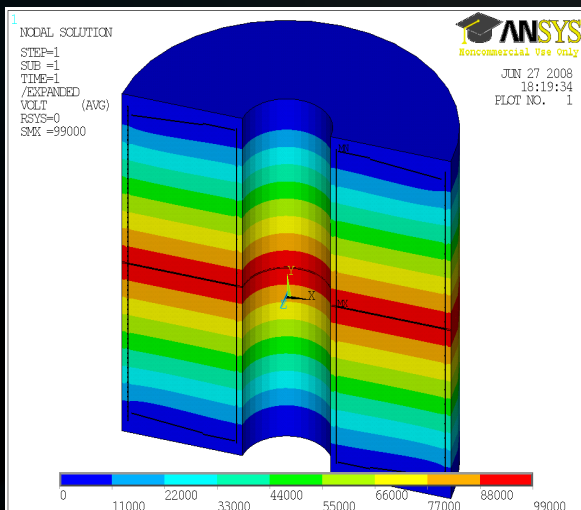
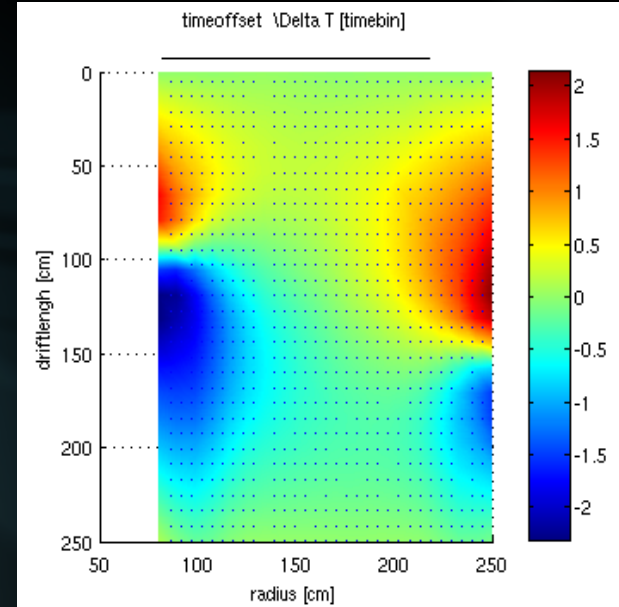
- Inhomogeneous **B-field** (via `AliMagF`)
- Inhomogeneous **E-field** (due to Space Charges)
- **Drift velocity** dependency for changing E field  
(  $\Delta v_{dE} \sim 0.24$  [% cm/V] )

# Further studies within Garfield ....

*Included (besides the above):*

- **E-field deviations** due to Field Cage or Read Out chambers (*Finite-Element map*)
- **Gas density variations** (P,T,gas composition by *Magboltz*)

e.g. broken resistor in the field cage





# Case studies: Space Charges

Case I: Primary Ionization

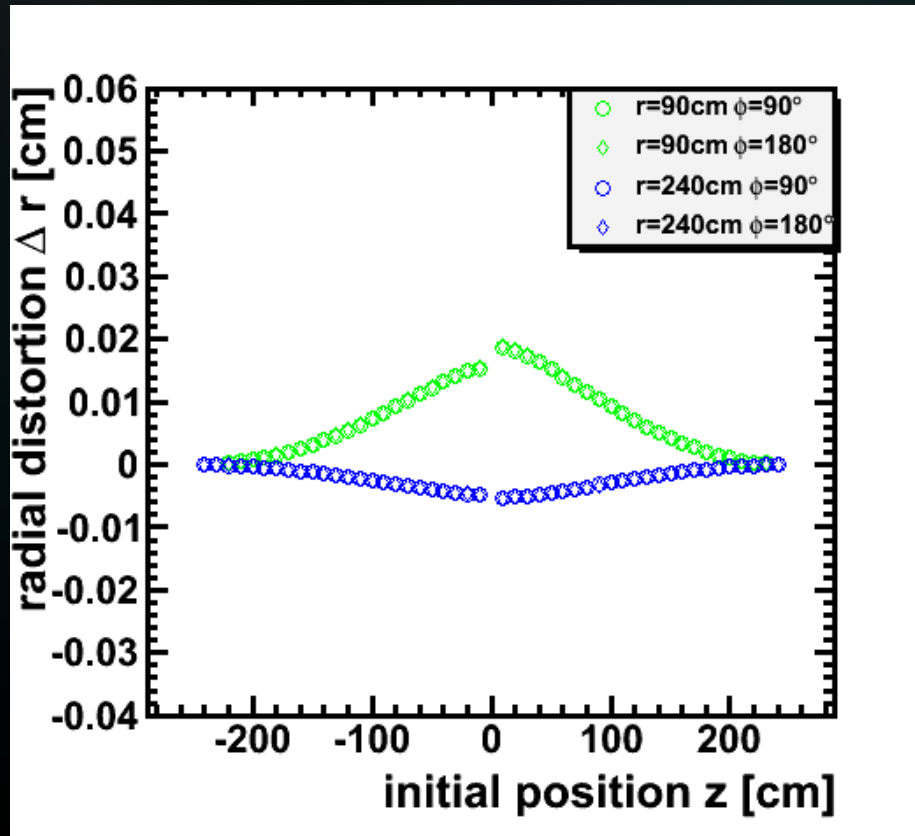
Case II: Primary Ionization + ROC-IFB

Case III: PI + Leaking gate wires

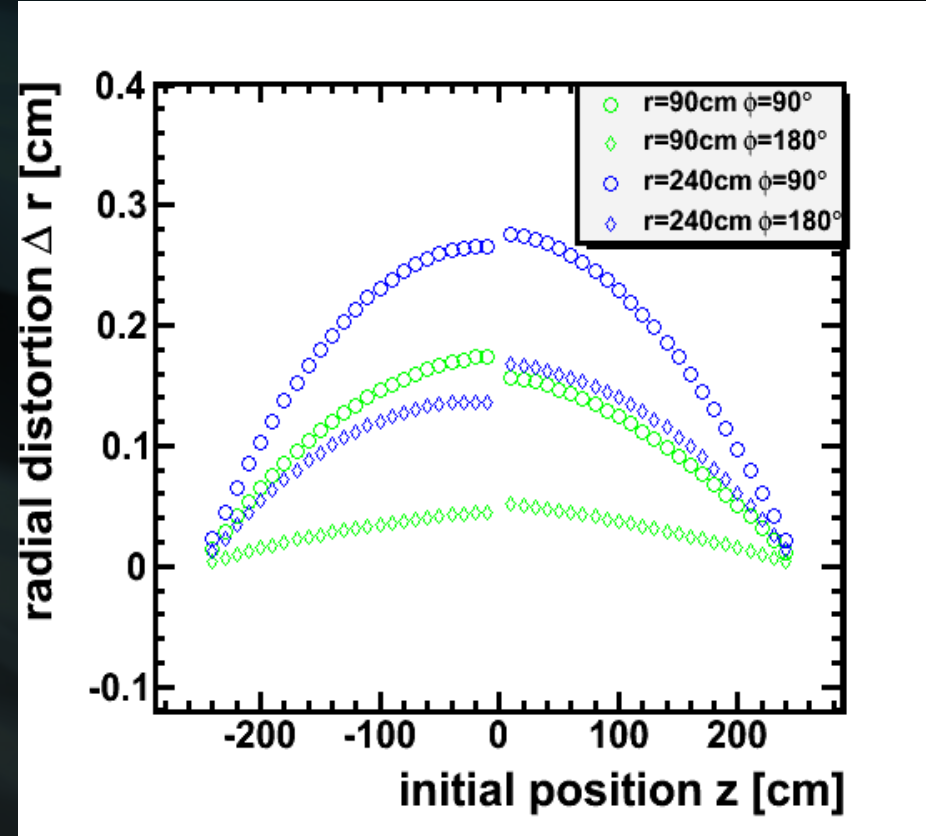
Case IV: Leak between IROC&OROC

# Case I: Primary Ionization – Pile Up

Charge distribution is basically radial symmetric. MAX:  $\sim 2.4e^{-10}C/m^3$



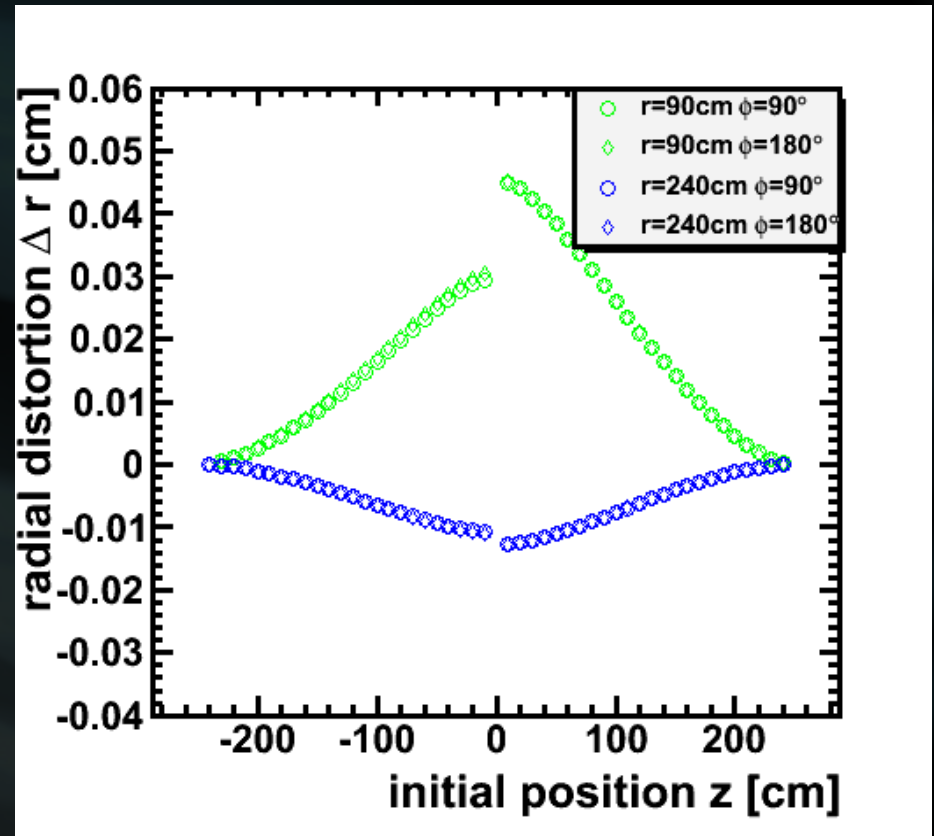
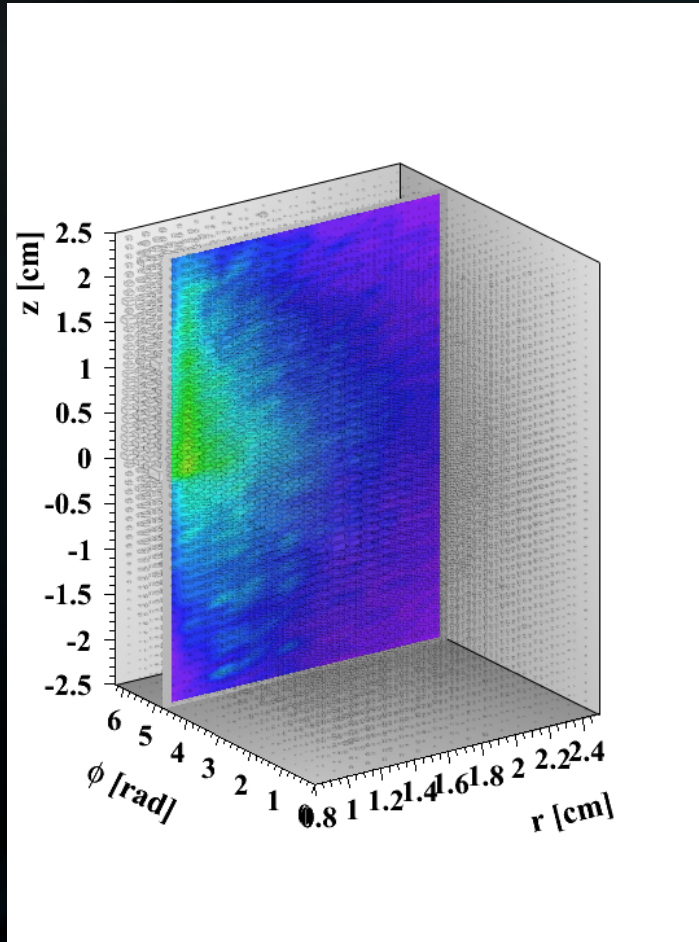
+ uniform B-field ( $B_z=0.5$  T)



+ measured B-field (AliMagF)

# Case II: Primary Ionization + ROC-IFB

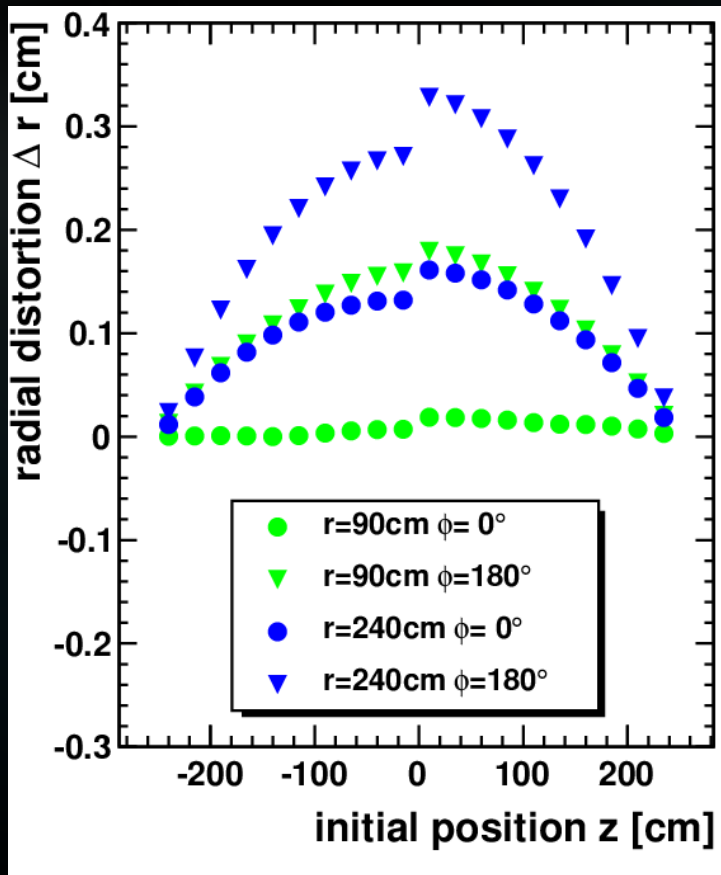
Charge distribution is still radial symmetric (but not z symmetric)



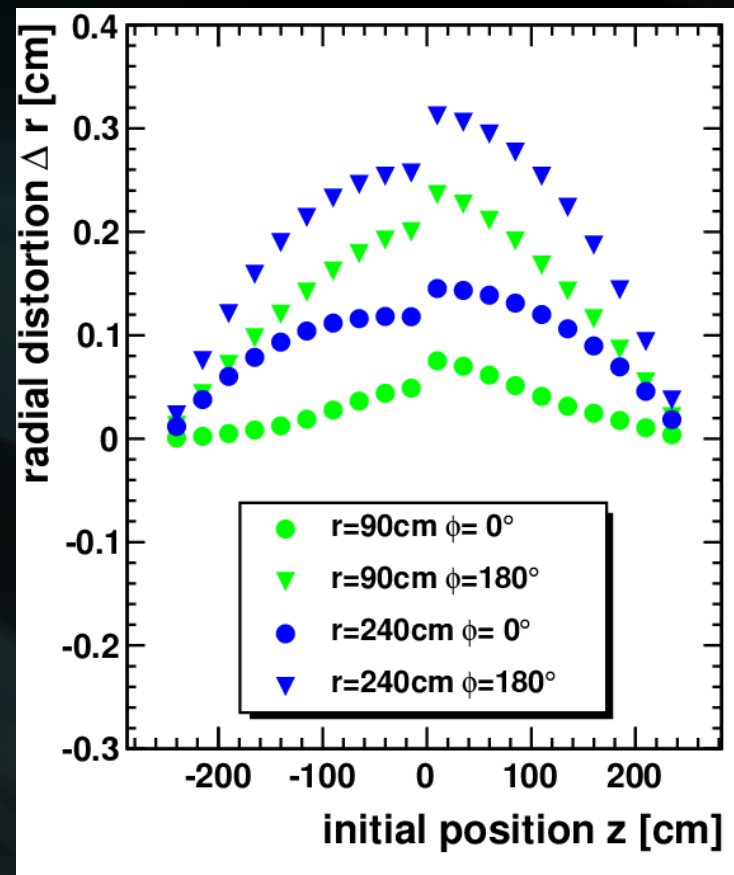
+ uniform B-field ( $B_z=0.5\text{ T}$ )



... combined with the B Field inhom.

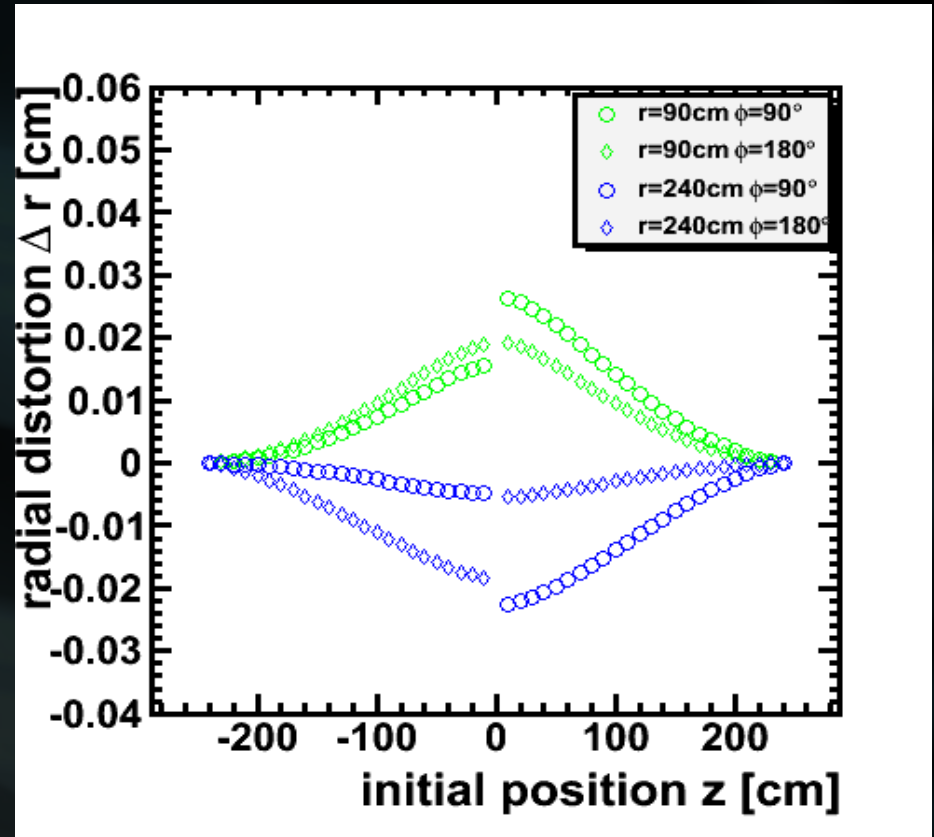
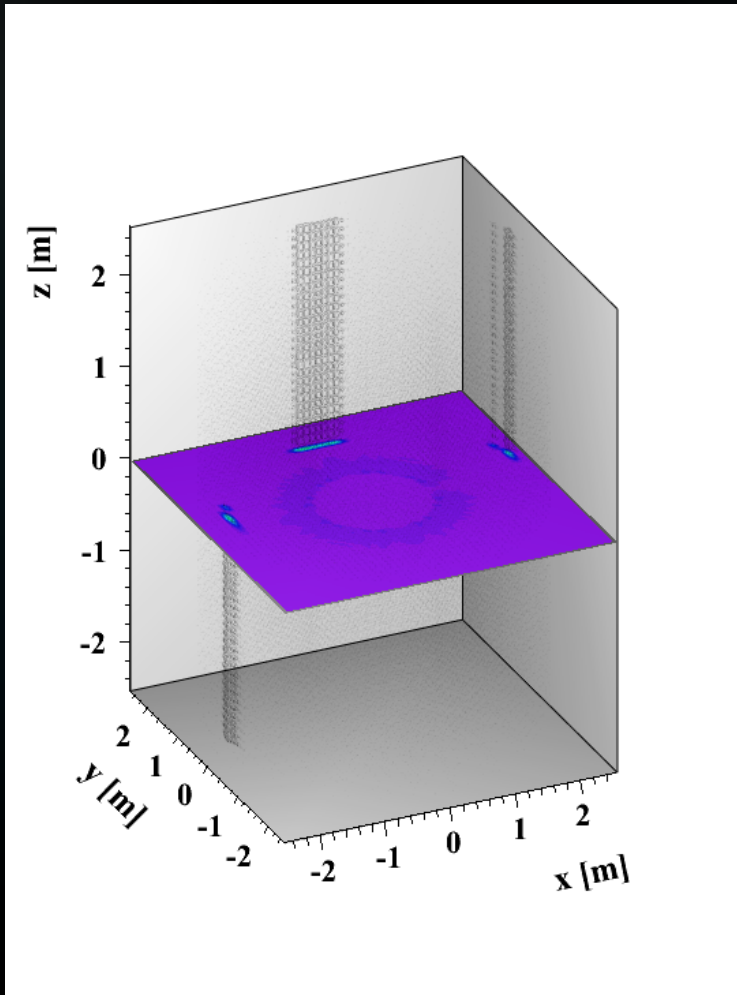


$\Delta r$  due to imperfect B-field  
(  $B_z=0.5$  T)



$\Delta r$  due to imperfect B-field  
plus expected space charges

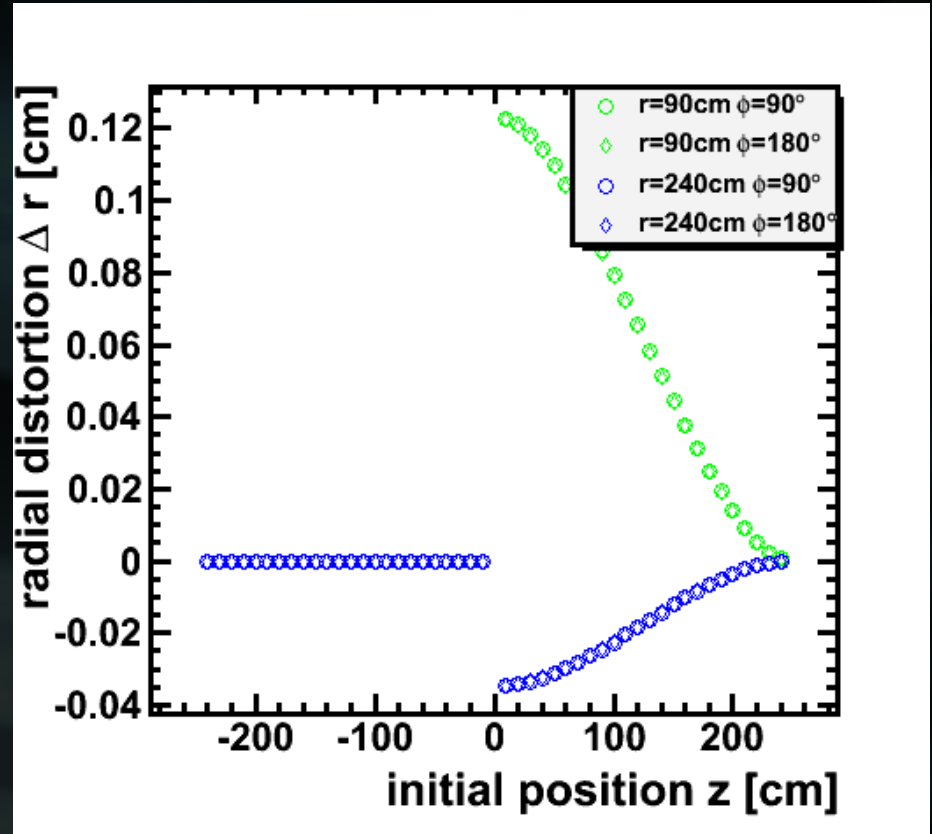
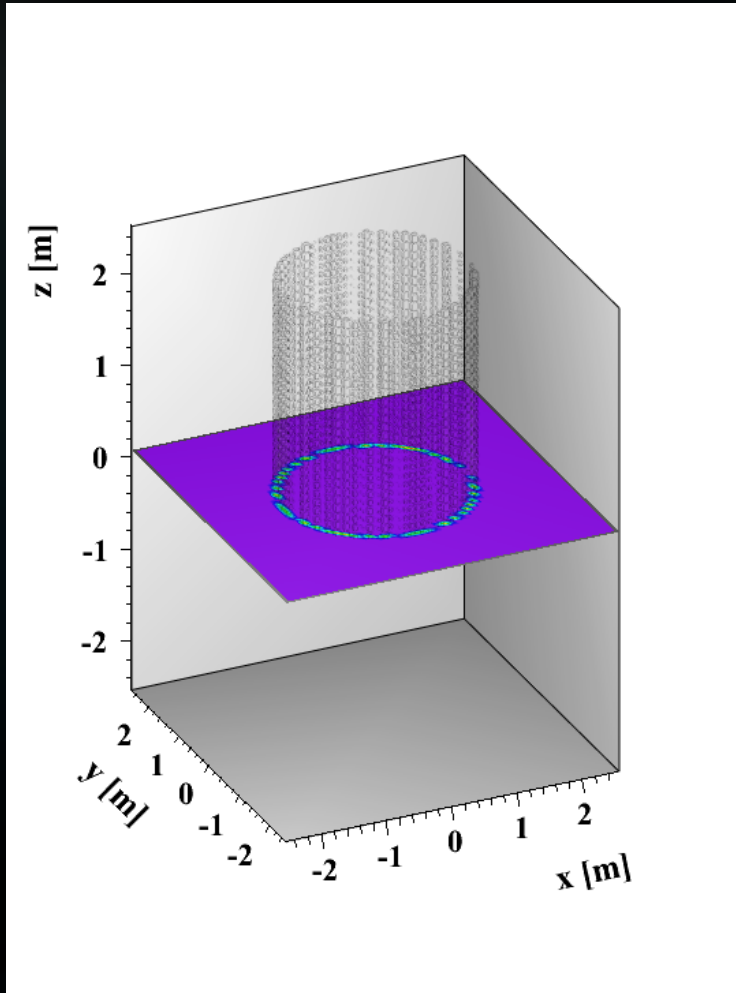
# Case III: PI + Leaking gate wires



+ uniform B-field ( $B_z=0.5$  T)

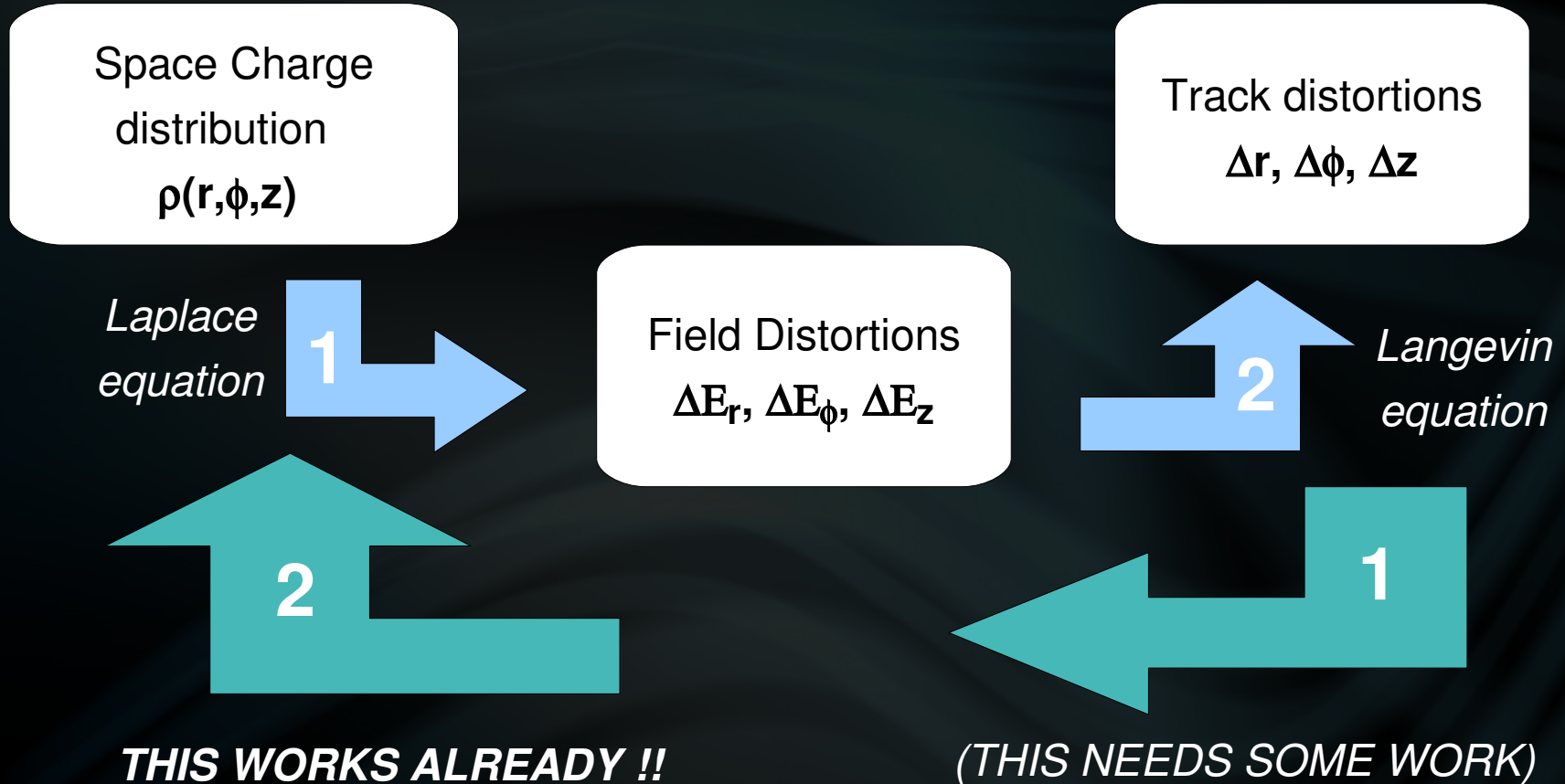
THERE IT BECOMES complicated,  
but it's easy to calculate ;-)

# Case IV: Leak between IROC&OROC



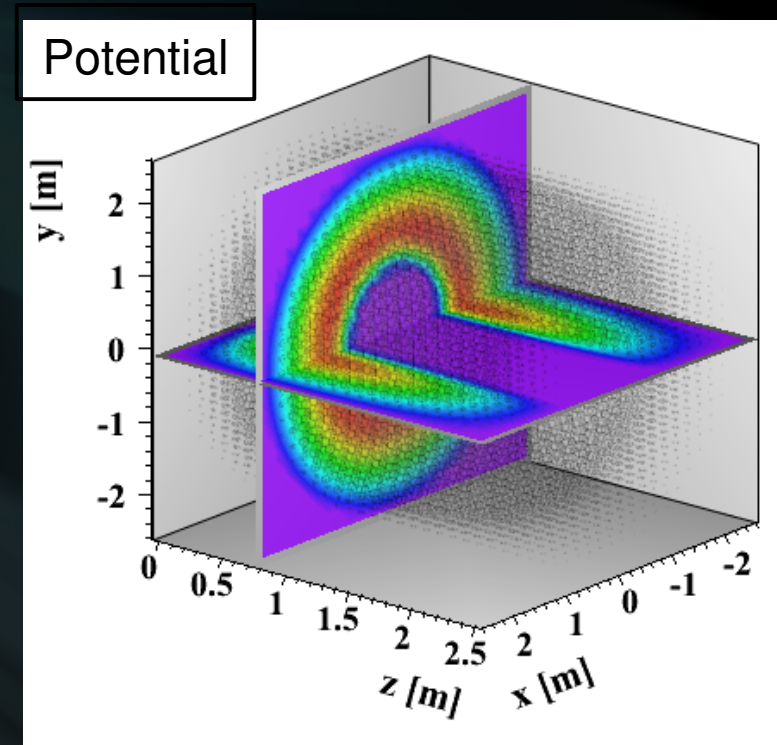
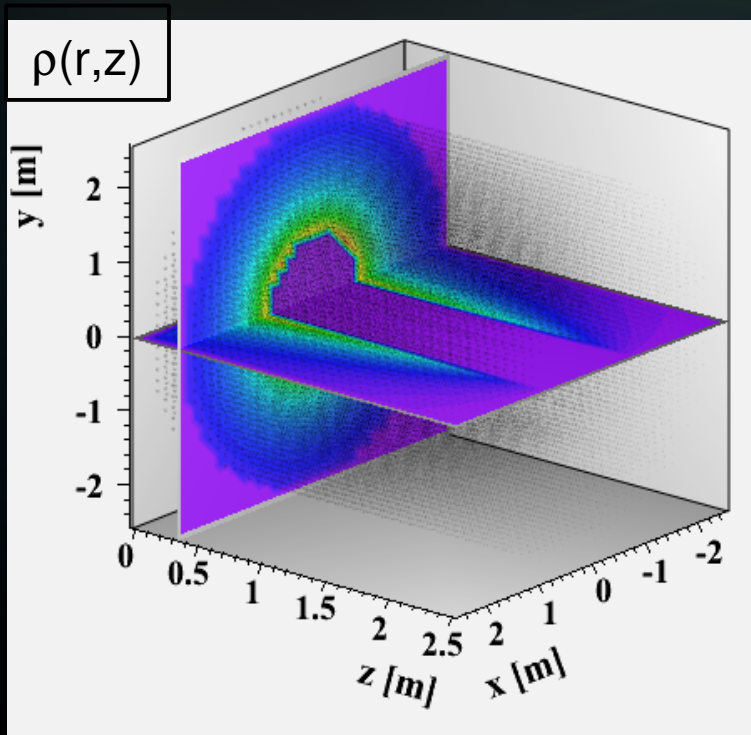
Problem of the STAR TPC ... ?

# The Inverse Model



# Inverse Model: Step 2

Thanks to the analytical solution, this is fast and accurate ...



$$A_1: (2.19 \text{ } ^{-1}_{+0.07})e^{-10}$$
$$A_2: (-0.87 \text{ } ^{-1}_{+0.05})e^{-10}$$

Model:

$$\rho(r,z) = (A_1 + A_2 z) / r^2$$

... due to simulated events



# CONCLUSION

- Forward direction  $|\rho(\mathbf{r}, \phi, \mathbf{z}) - (\Delta E_r, \Delta E_\phi, \Delta \epsilon_z) - (\Delta r, \Delta \phi, \Delta z)|$  works nicely for any Charge distribution one might find!
- Thanks to *Garfield* (Rob Veenhof), we can include nearly any distortion-effect into our calculations (complete TPC simulation)  
**→ Simulations, predictions and crosschecks possible**
- Inverse Model: Would lead to nice '**tomographic picture**' of inhomogeneities (in charge equivalence) within the TPC

**ANY QUESTIONS OR SUGGESTIONS ?**