

QCD CHALLENGES

in Trento on February 27 – March 3

QCD CHALLENGES
in *pp*, *pA* and *AA* collisions

László L. Jenkovszky

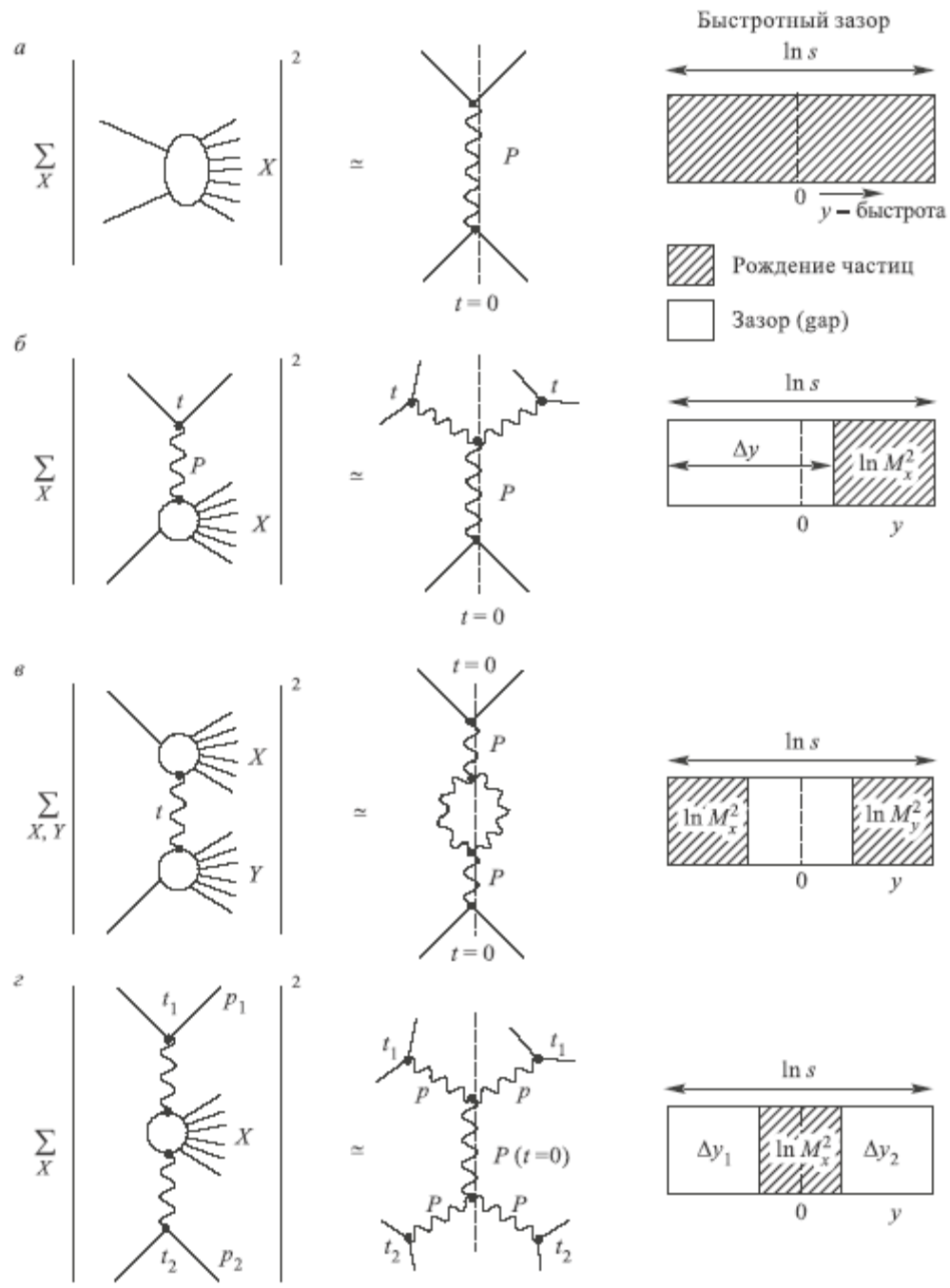
EMMI visiting professor
Heidelberg, February 2017

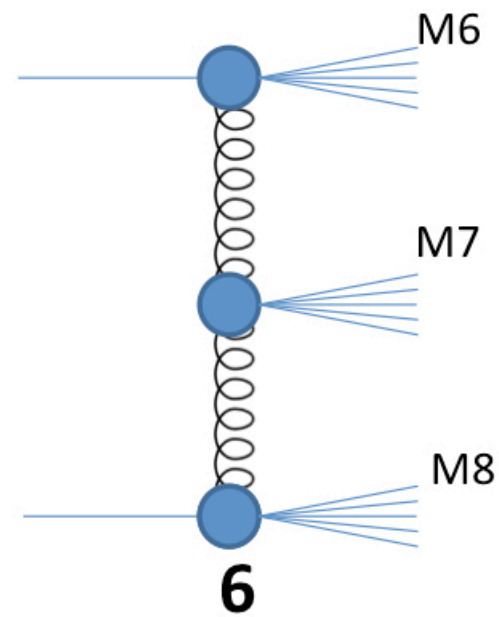
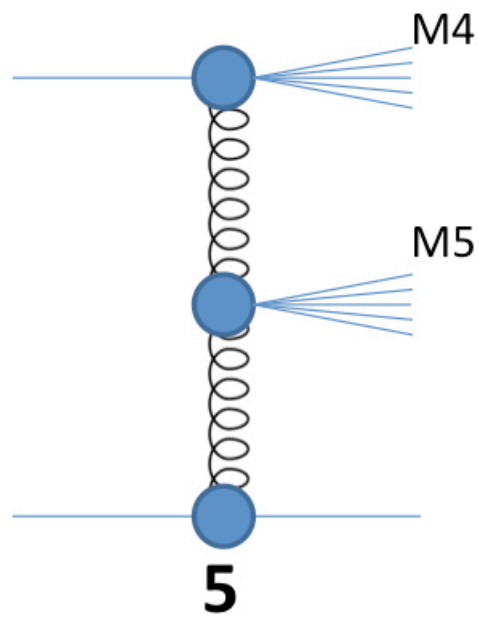
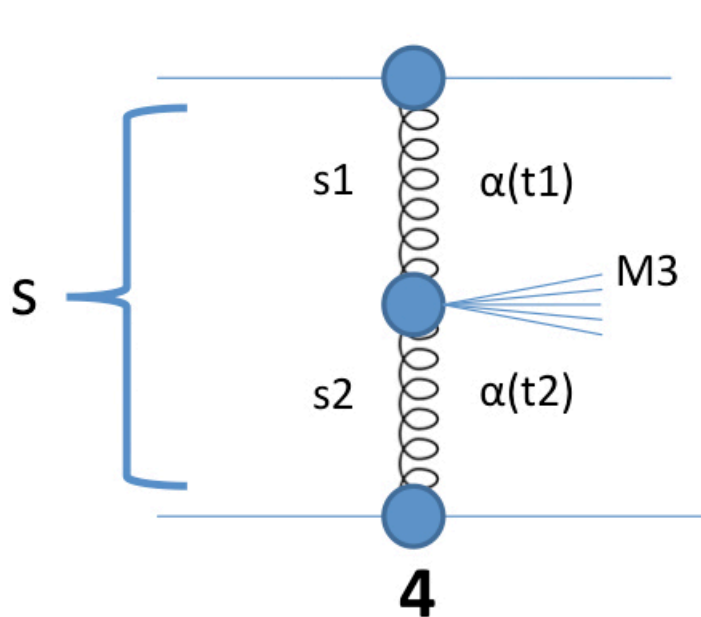
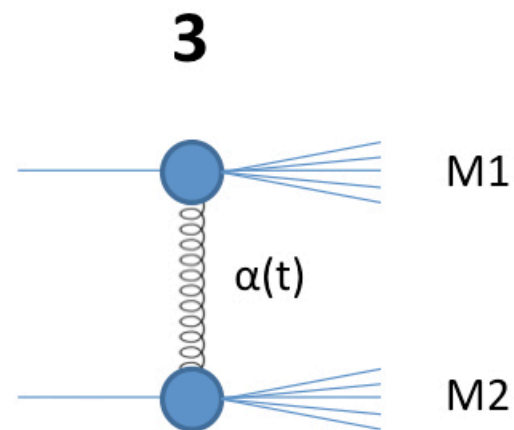
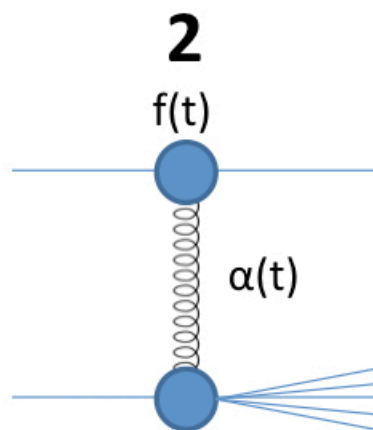
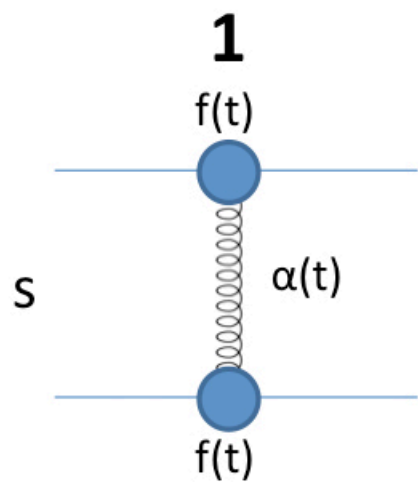
jenk@bitp.kiev.ua

Content of the talk:

evergreen, still confusing issues

- What is the Pomeron and what are the glueballs?
- How many Pomerons (“soft”, “hard”/”QCD”-, etc. Pomerons,...);
- “BFKL (Lipatov) Pomeron”: $s^{\alpha(t)} \rightarrow \text{pQCD} \rightarrow s^{\alpha(t)}$;
- Does (should) the Odderon exist and how to detect it?
- See: Carlo Ewerz, The Odderon: Theoretical Status and Experimental Tests, [arXiv:hep-ph/0511196](https://arxiv.org/abs/hep-ph/0511196);
- *A proposal (let us put it forward!)*: rescale LHC down to ~ 1.8 TeV ?!
- Momentum (t) vs. coordinate (b) picture (F-B transform);
- Beyond “standard QCD”?
- How many resonances, do they terminate on the $\rho(m)$ plot?





Factorization (nearly perfect at the LHC!)

$$(g_1 g_2)^2 = \frac{(g_1 f_1)^2 (f_1 g_2)^2}{(f_1 f_2)^2}.$$

Hence

$$\frac{d^3 \sigma}{dt dM_1^2 dM_2^2} = \frac{d^2 \sigma_1}{dt dM_1^2} \frac{d^2 \sigma_2}{dt dM_2^2} \frac{d\sigma_{el}}{dt}.$$

Assuming exponential cone, t^{bt} and integrating in t , one gets

$$\frac{d^2 \sigma_{DD}}{dM_1^2 dM_2^2} = k \frac{1}{\sigma_{el}} \frac{d\sigma_1}{dM_1^2} \frac{d\sigma_2}{dM_2^2},$$

where $k = r^2 / (2r - 1)$, $r = b_{SD} / b_{el}$.

Further integration in M^2 yields $\sigma_{DD} = k \frac{\sigma_{SD}^2}{\sigma_{el}}$.

$$\sigma_t(s) = \frac{4\pi}{s} \text{Im}A(s, t=0); \quad \frac{d\sigma}{dt} = \frac{\pi}{s^2} |A(s, t)|^2; \quad n(s);$$

$$\sigma_{el} = \int_{t_{min} \approx -s/2 \approx \infty}^{t_{thr.} \approx 0} \frac{d\sigma}{dt}; \quad \sigma_{in} = \sigma_t - \sigma_{el}; \quad B(s, t) = \frac{d}{dt} \ln\left(\frac{d\sigma}{dt}\right);$$

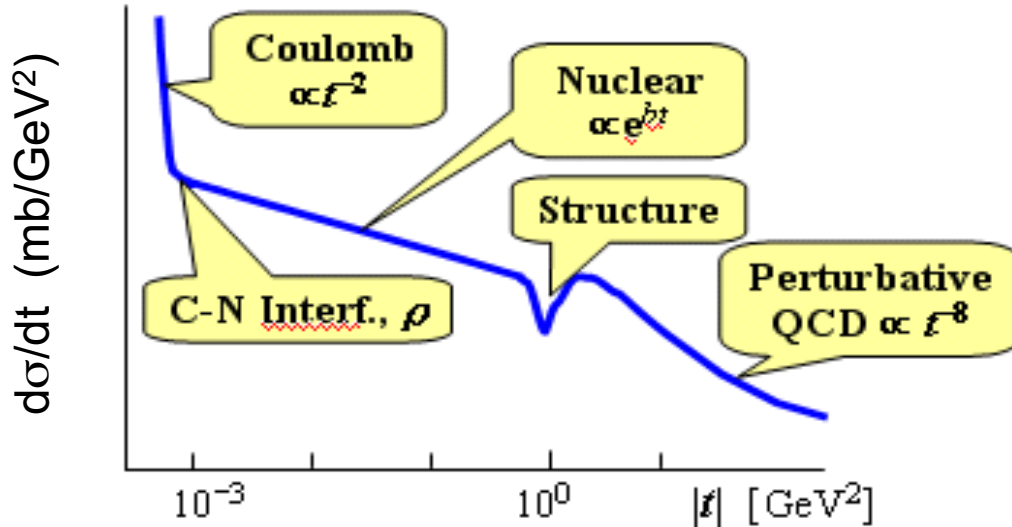
$$A_{pp}^{\bar{p}}(s, t) = P(s, t) \pm O(s, t) + f(s, t) \pm \omega(s, t) \rightarrow_{LHC} \approx P(s, t) \pm O(s, t),$$

where P , O , f , ω are the Pomeron, odderon and non-leading Reggeon contributions.

| $\alpha(0) \setminus C$ | + | - |
|-------------------------|----------|----------------------------|
| 1 | P | O |
| 1/2 | f | ω |

Elastic Scattering

$\sqrt{s} = 14$ TeV prediction of BSW model



momentum transfer $-t \sim (p\theta)^2$
 θ = beam scattering angle
 p = beam momentum

$$\rho = \frac{\text{Re}(f_{el}(t))}{\text{Im}(f_{el}(t))} \Big|_{t \rightarrow 0}$$

$$\left. \frac{dN}{dt} \right|_{t=CNI} = L\pi |f_C + f_N|^2 \approx L\pi \left| -\frac{2\alpha_{EM}}{|t|} + \frac{\sigma_{tot}}{4\pi} (i + \rho) e^{-\frac{b|t|}{2}} \right|^2$$

L , σ_{tot} , b , and ρ
 from FIT in CNI
 region (UA4)

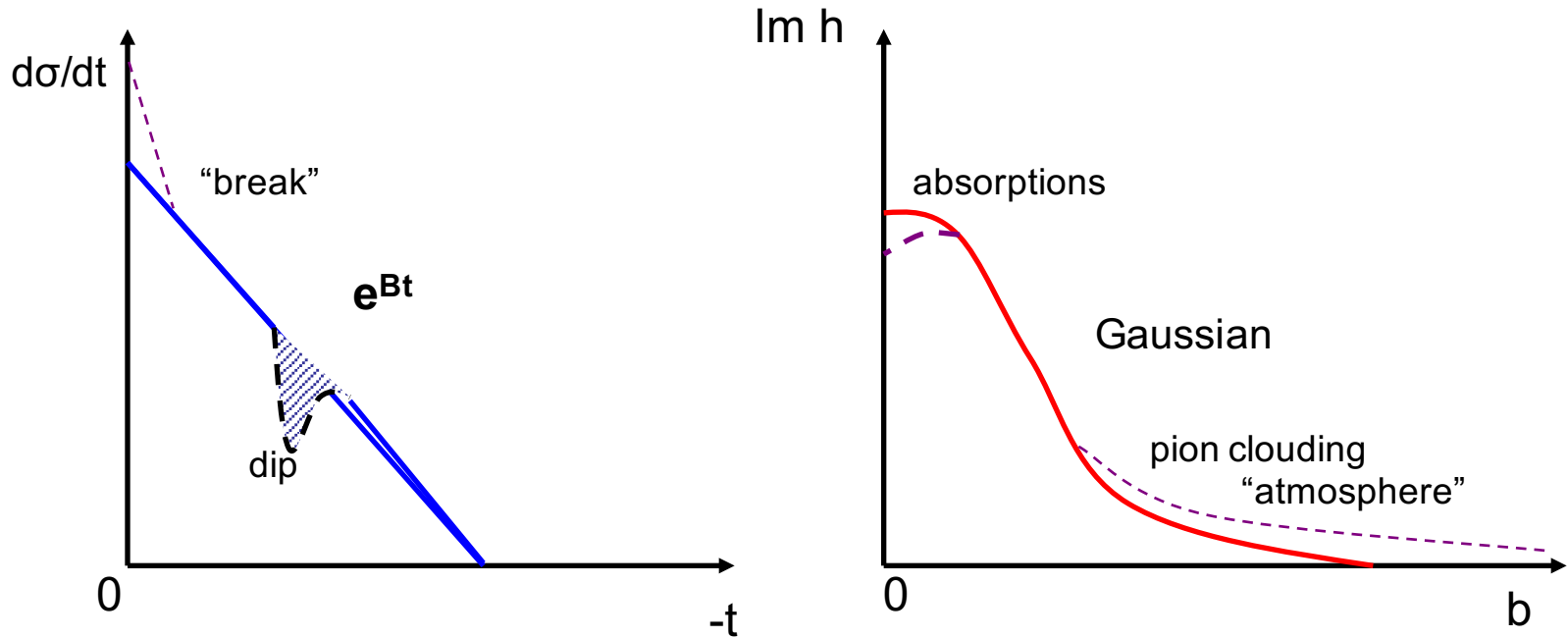
CNI region: $|f_C| \sim |f_N| \rightarrow$ @ LHC: $-t \sim 6.5 \cdot 10^{-4} \text{ GeV}^2$; $\theta_{min} \sim 3.4 \text{ } \mu\text{rad}$

($\theta_{min} \sim 120 \text{ } \mu\text{rad}$ @ SPS)

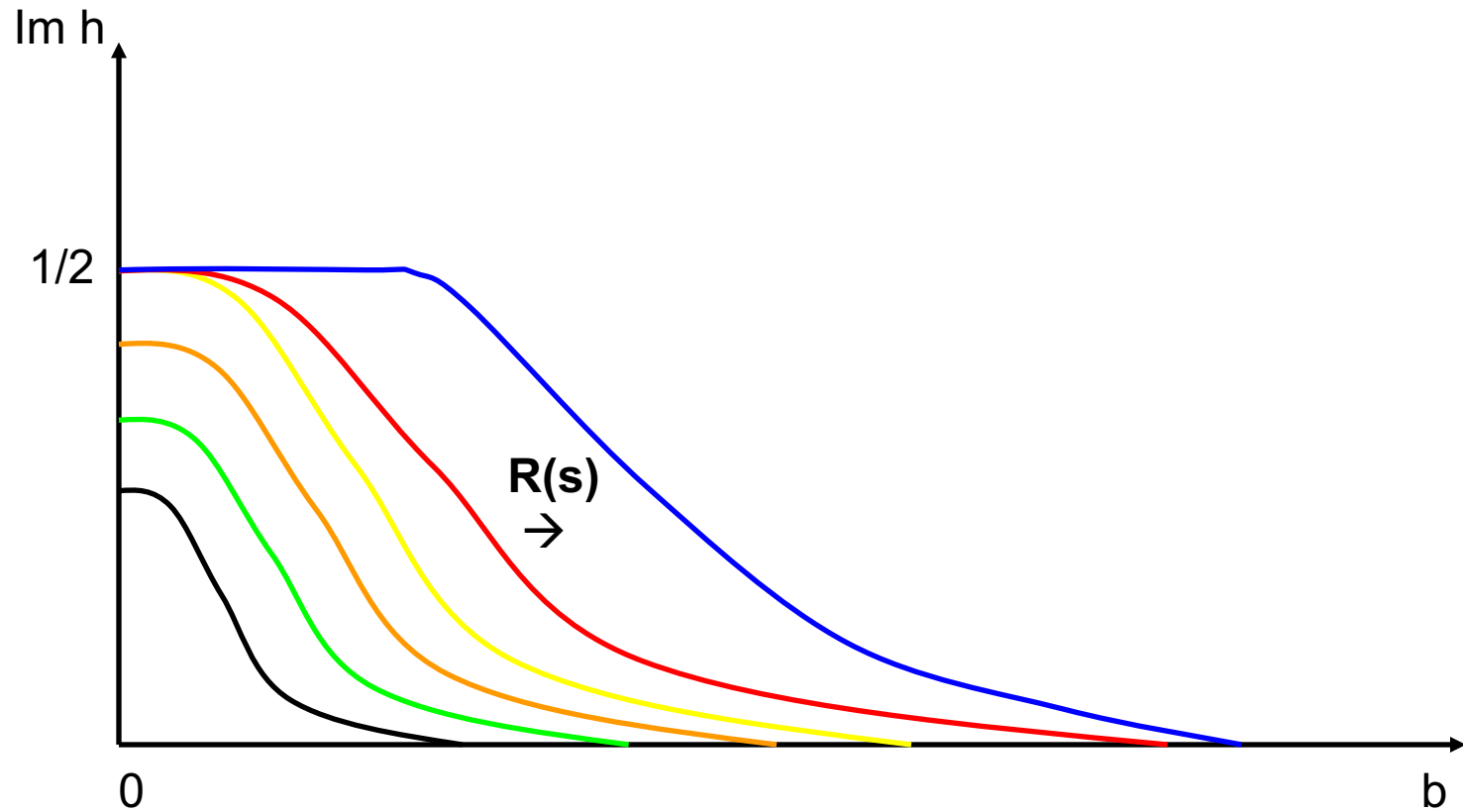
Geometrical scaling (GS), saturation and unitarity

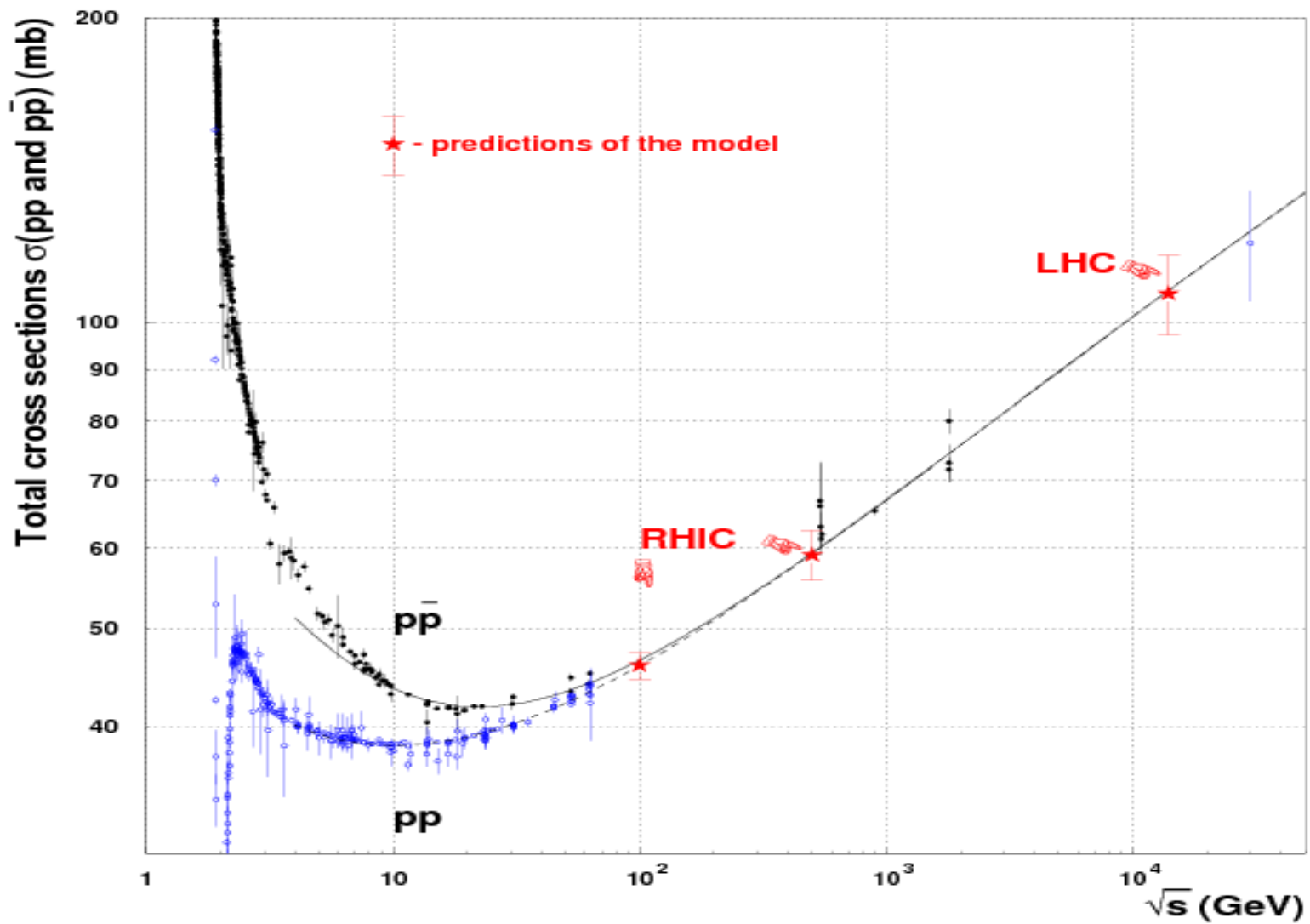
1. On-shell (hadronic) reactions ($s, t, Q^2=m^2$);

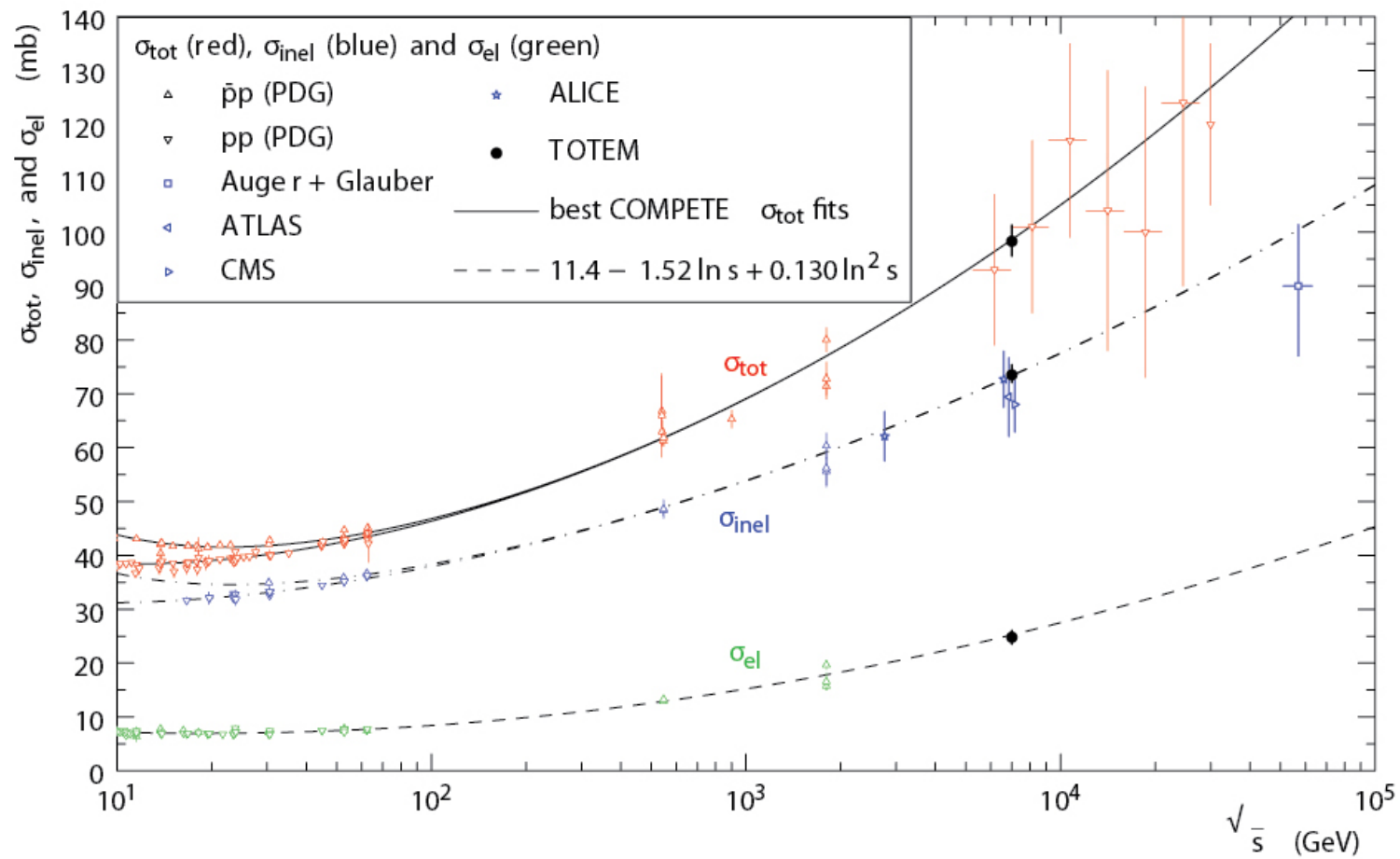
$t \leftrightarrow b$ transformation: $h(s, b) = \int_0^\infty d\sqrt{-t}\sqrt{-t}A(s, t)$
and dictionary:

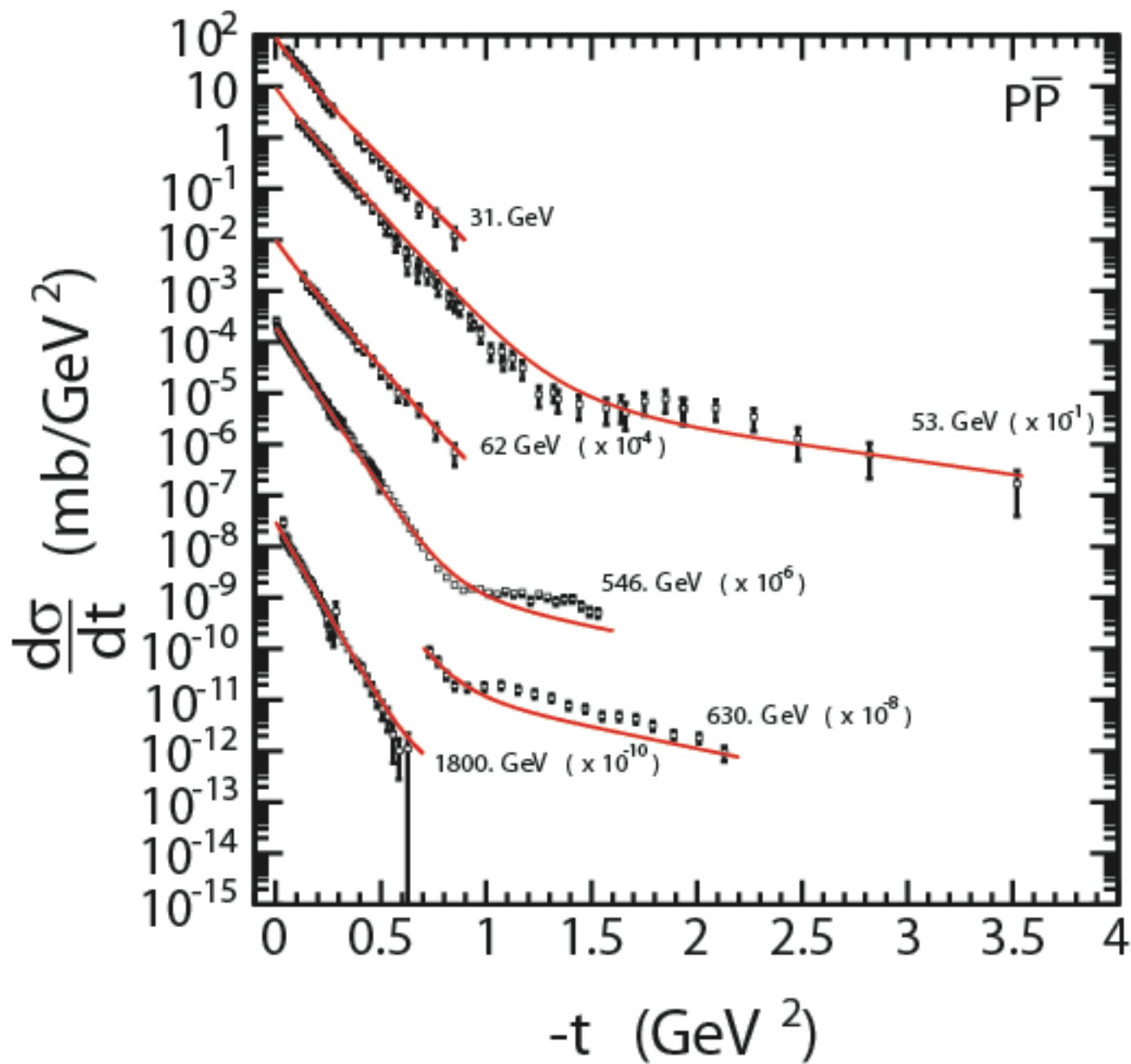


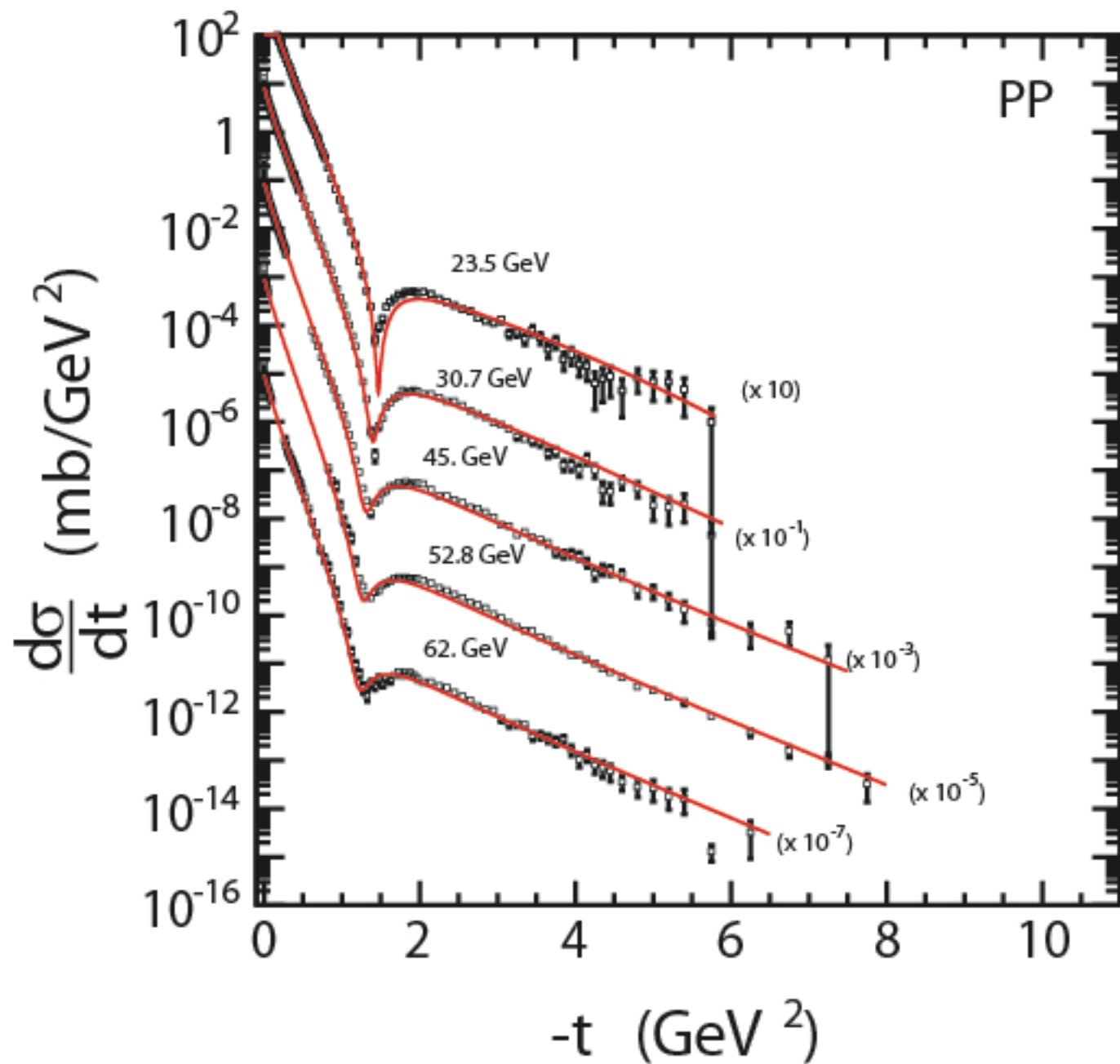
П.Дегрола, Л.Л. енковский, Б.В. Струминский, ЯФ

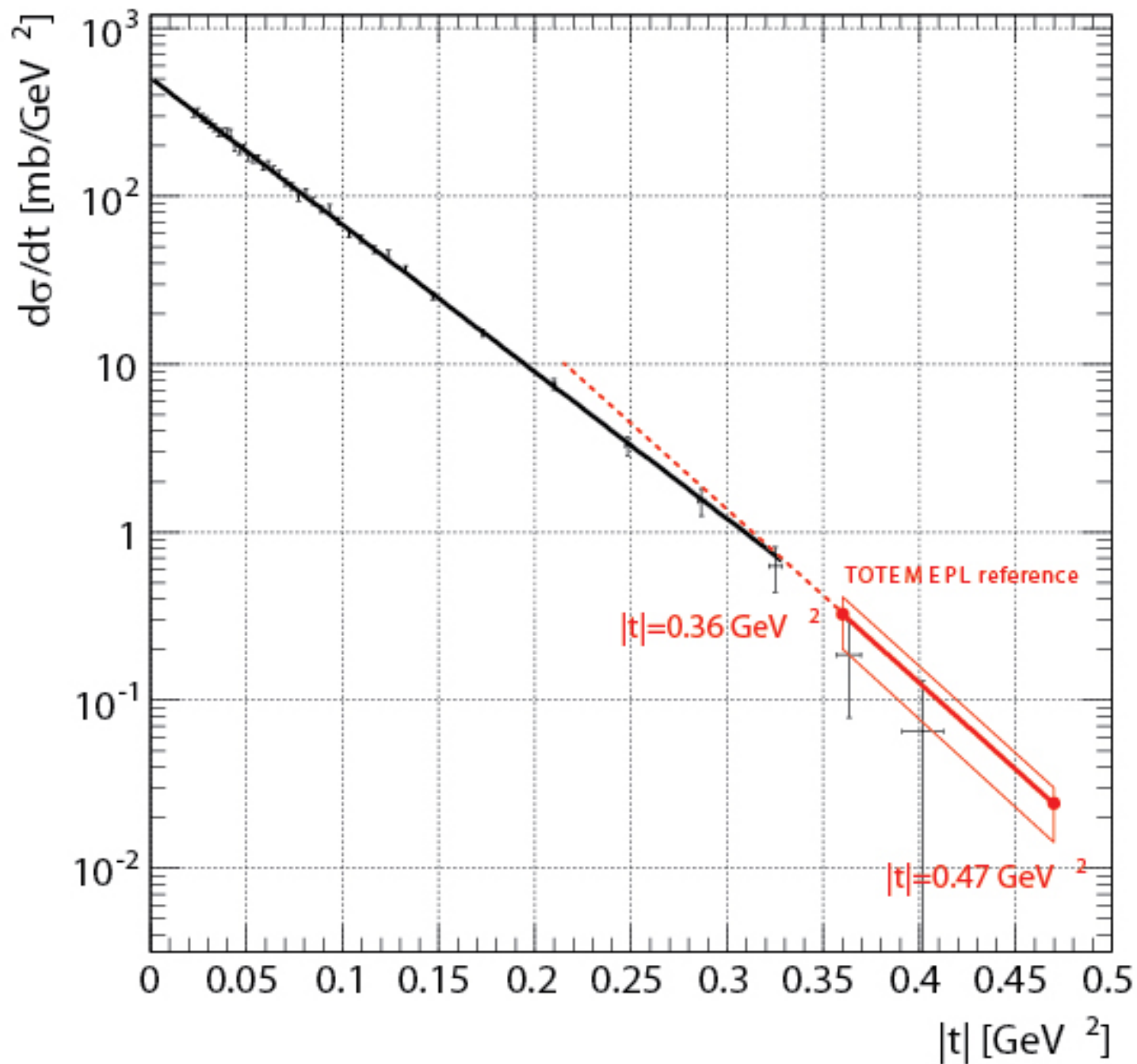




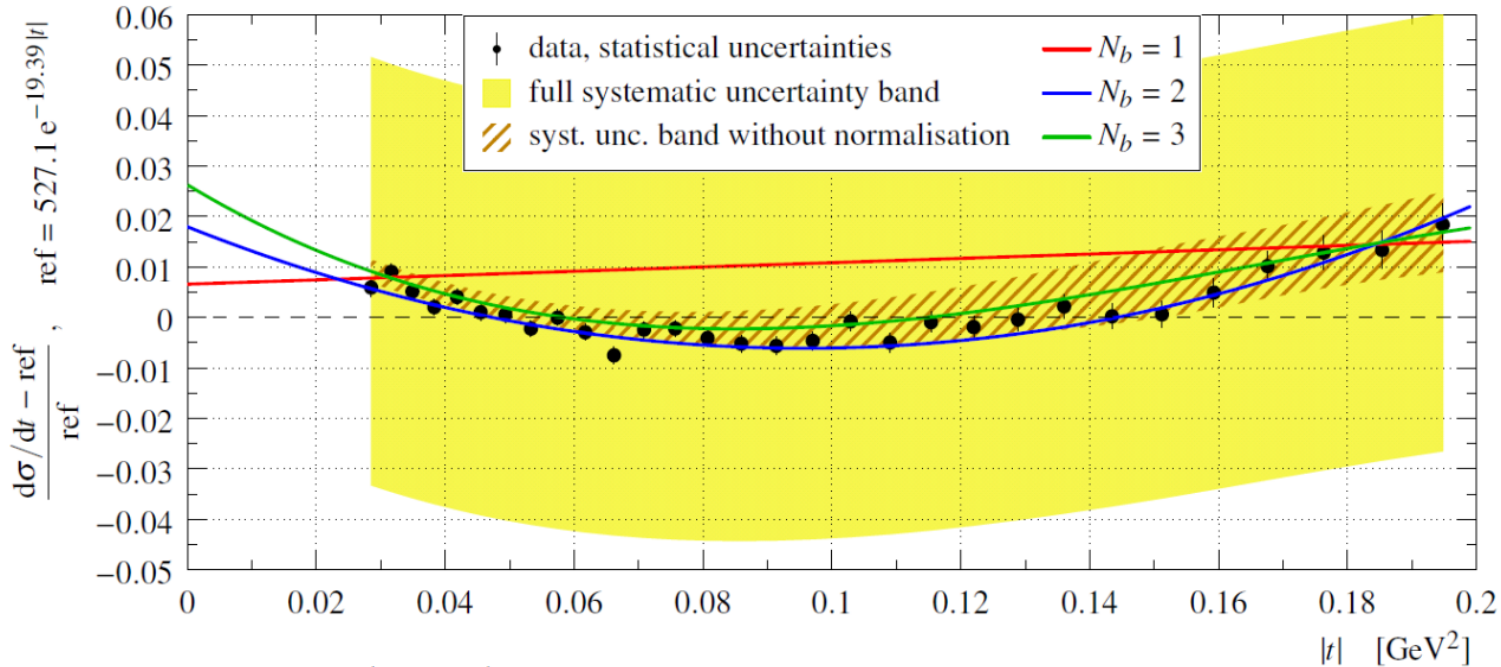








NEW: Elastic scattering: non-exponentiality at low $|t|$



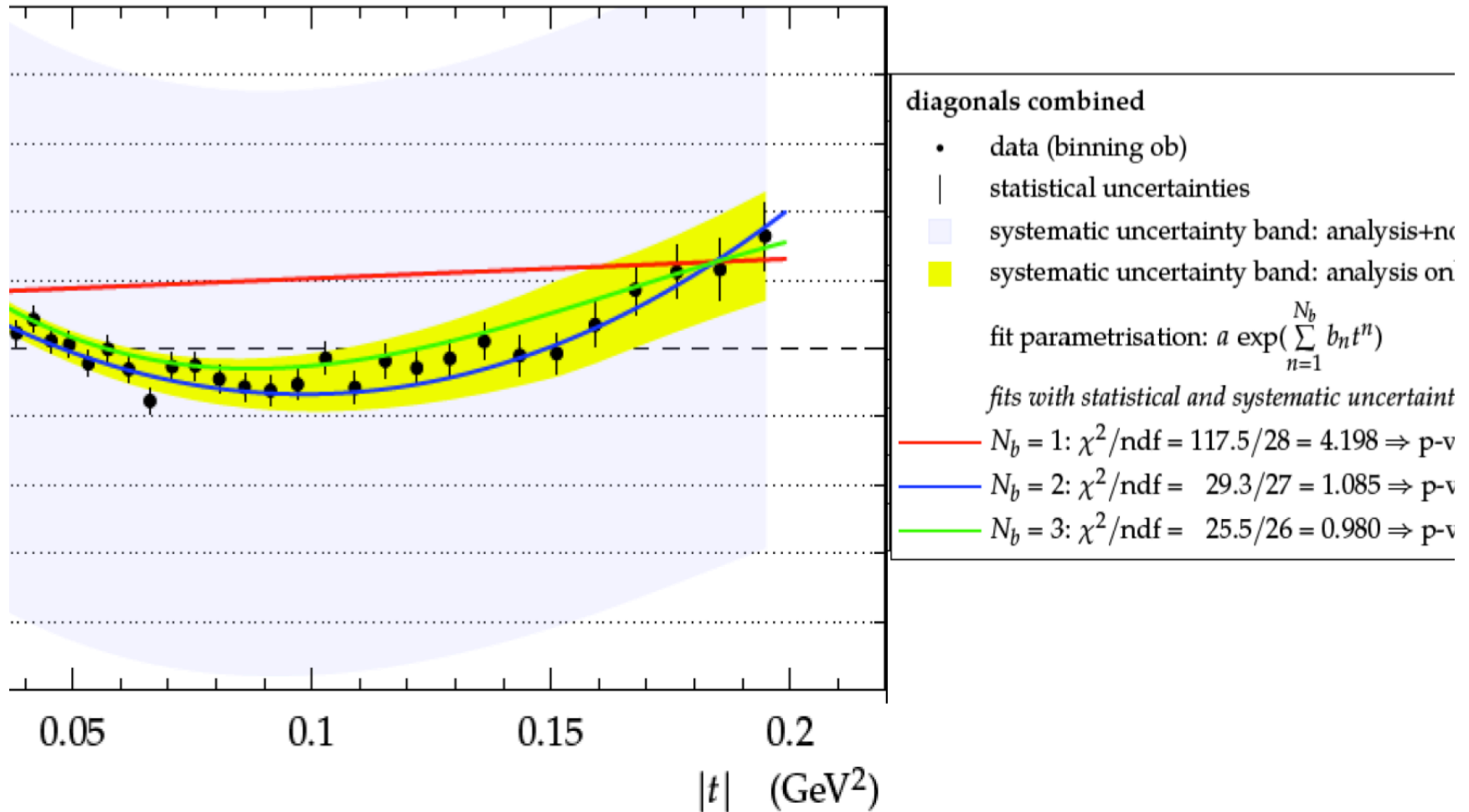
$$\frac{d\sigma}{dt}(t) = \frac{d\sigma}{dt} \Big|_{t=0} \exp \left(\sum_{i=1}^{N_b} b_i t^i \right)$$

$N_b = 1$ excluded with 7σ significance!

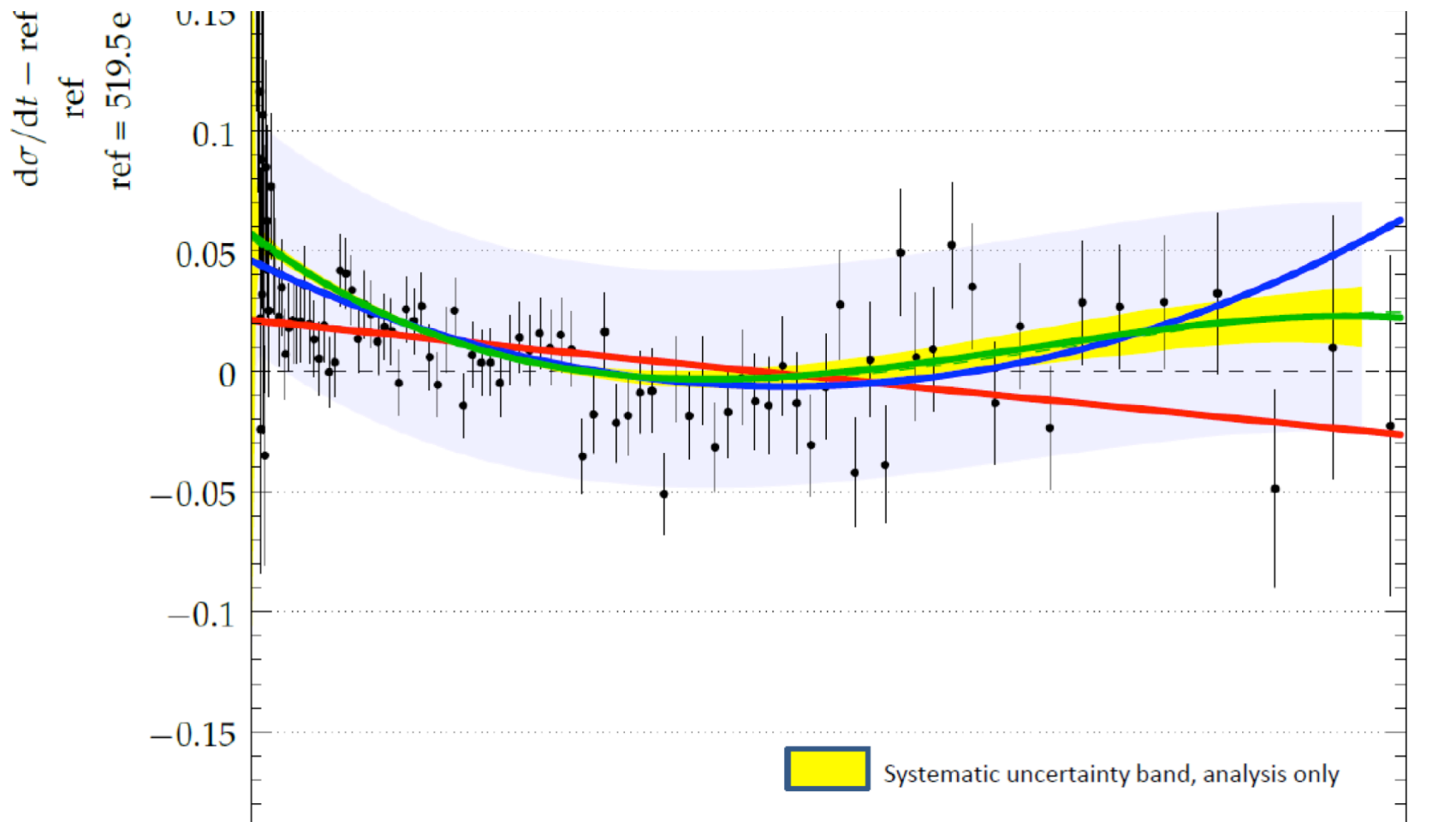
$N_b = 2 : \sigma_{\text{tot}} = (101.5 \pm 2.1) \text{ mb}$

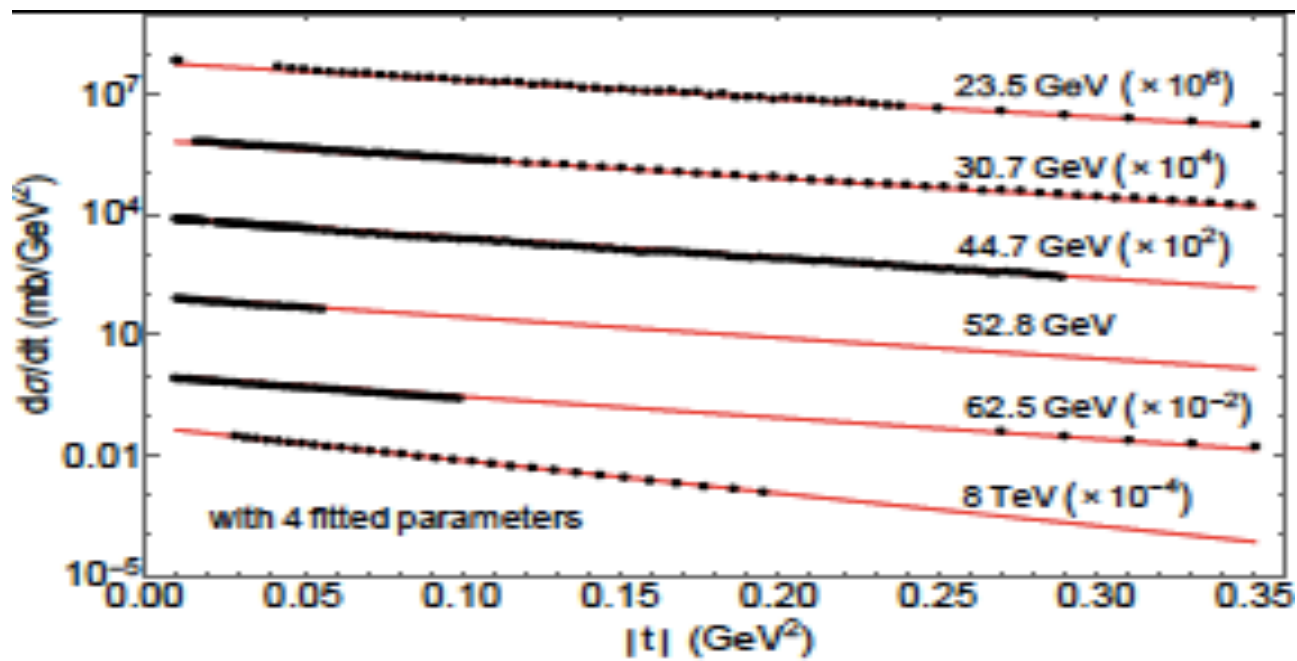
$N_b = 3 : \sigma_{\text{tot}} = (101.9 \pm 2.1) \text{ mb}$

Fine structure of the Pomeron (at the LHC)



Fine structure of the Pomeron (TOTEM)

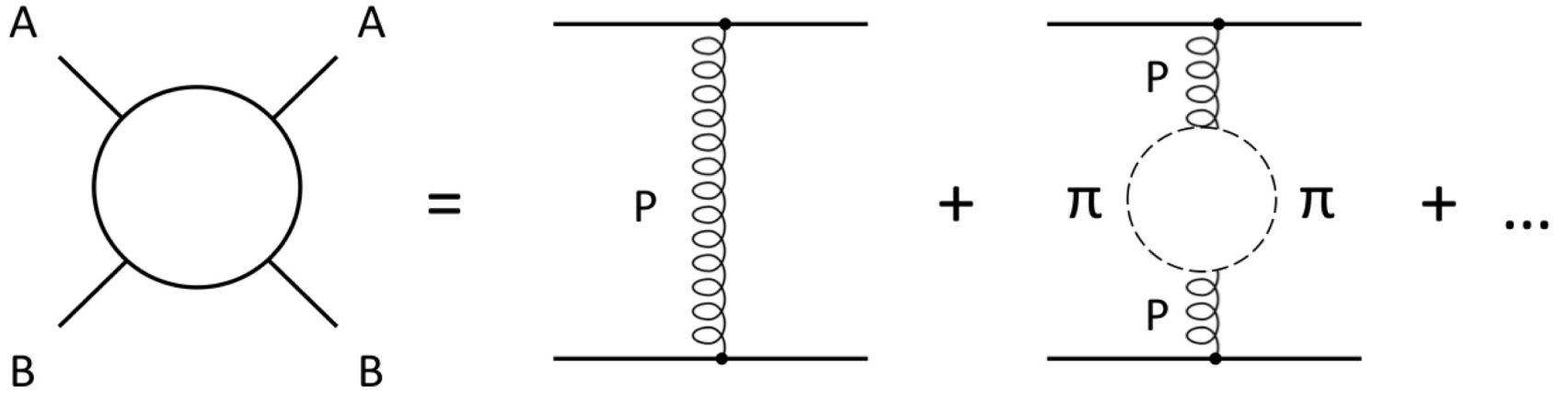




G. Antchev et al. (TOTEM Collaboration), Nucl. Phys. B **899** (2015) 527-546, arXiv:1503.08111; T. Csörgő (for the TOTEM Collaboration), Evidence for Non-Exponential Differential Cross-Section of pp Elastic Scattering at Low $|t|$ and $\sqrt{s} = 8$ TeV by TOTEM, arXiv:1602.00219.

Frigyes Nemes (for the TOTEM Collaboration), LHC optics and elastic scattering measured by the TOTEM experiment, arXiv:1602.06207; Frigyes Nemes (for the TOTEM collaboration), The results of the TOTEM experiment, to be publ. in the Proceedings of the Diffraction 2016 conference, held in Acireale, Sicily, Sept. 2-8, 2016; Nicola Minafra, Latest results of the TOTEM experiment at LHC, Low- x Workshop, Gyöngyös, June 6-11, 2016; G. Antchev et al. (TOTEM Collaboration), *Measurement of Elastic pp Scattering at $\sqrt{s} = 8$ TeV in the Coulomb-Nuclear Interference Region Determination of the ρ -Parameter and the Total Cross-Section*, Eur. Phys. J. C **76** (2016) 661; arXiv:1610.00603.

B. Barbiellini et. al. Phys. Letters **B39** (1972) 663.



Experimentalists usually quantify the departure from the linear exponential by replacing

$$|A^N| = a \exp(Bt) \rightarrow a \exp(b_1 t + b_2 t^2 + b_3 t^3 + \dots) \quad (1)$$

with coefficients b_i fitted to the data.

Two-pion loop contributes in the t channel through Regge trajectories, that are non-linear complex functions,

$$\Im\alpha(t) \sim (t - t_0)^{\Re\alpha(t_0)+1/2}, \quad (2)$$

where t_0 is the lightest threshold, $4m_\pi^2$ in the case of the vacuum quantum numbers (Pomeron or f meson). Since $\Re\alpha(4m_\pi^2)$ is small, a square-root threshold is a reasonable approximation to the above constrain.

$$A(s, t) = A_P(s, t) + A_f(s, t),$$

where

$$A_P(s, t) = -a_P e^{b_P \alpha_P(t)} e^{-i\pi \alpha_P(t)/2} (s/s_0)^{\alpha_P(t)}, \quad A_f(s, t) = -a_f e^{b_f \alpha_f(t)} e^{-i\pi \alpha_f(t)/2} (s/s_0)^{\alpha_f(t)}$$

with the trajectories

$$\alpha_P(t) = \alpha_{0P} + \alpha'_P t - \alpha_{1P} (\sqrt{4m_\pi^2 - t} - 2m_\pi), \quad \alpha_f(t) = \alpha_{0f} + \alpha'_f t - \alpha_{1f} (\sqrt{4m_\pi^2 - t} - 2m_\pi).$$

Norm:

$$\sigma_T(s) = \frac{4\pi}{s} \Im A(s, t=0), \quad \frac{d\sigma}{dt} = \frac{\pi}{s} |A(s, t)|^2.$$

D.A. Fagundes *et. al.* Phys. Rev. **D88** (2013) 094019.

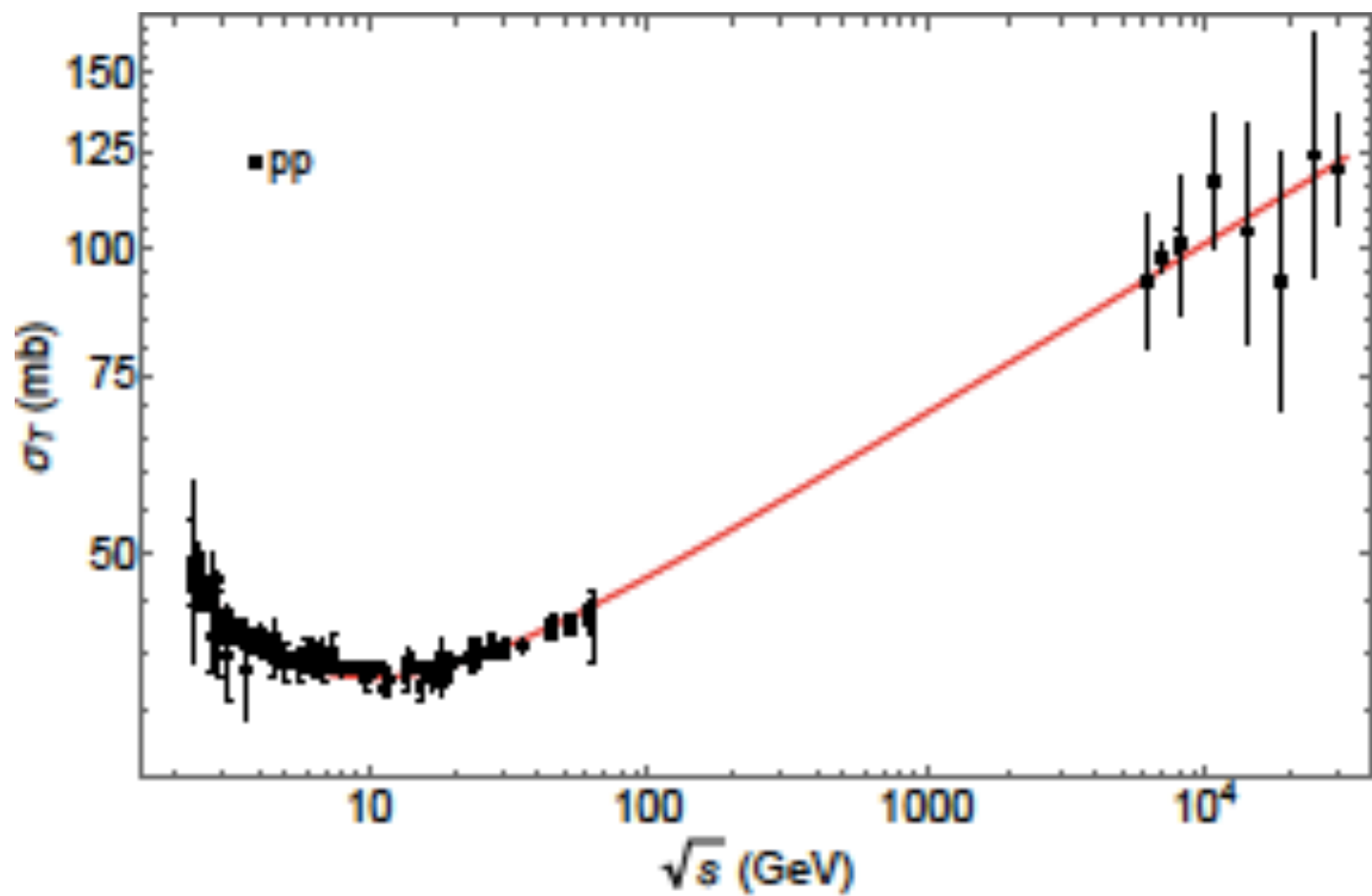
Giulia Pancheri, Yogendra N. Srivastava, *Introduction to the physics of the total cross-section at LHC: A Review of Data and Models*, arXiv:1610.10038; to be published in the European Journal of Physics C.

D.A. Fagundes, L. Jenkovszky, E.Q. Miranda, G. Pancheri, P.V.R.G. Silva, *Fine structure of the diffraction cone: from the ISR to the LHC*, International Journal of Modern Physics A **31**, Nos. 28 & 29 (2016) 1645022, World Scientific Publishing Company DOI: 10.1142/S0217751X16450226 D, arXiv:1509.02197.

R. Fiore, L. Jenkovszky and R. Schicker, EPJ C **76** (2016) 1; hep-ph/1512.04977.

Laszlo Jenkovszky and Alexander Lengyel, Acta Phys. Pol. **B 46**(2015) 863; arXiv:1410.4106.

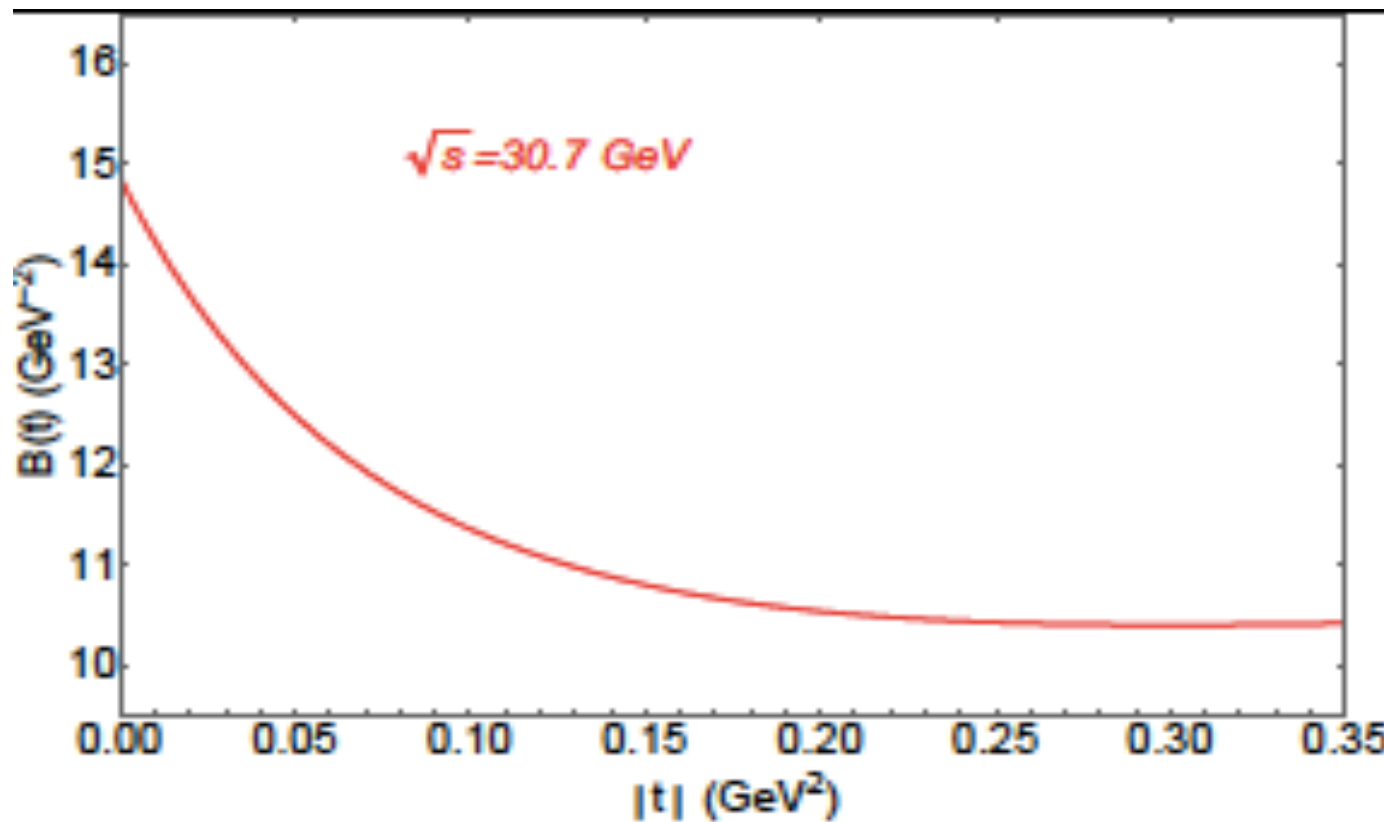
Laszlo Jenkovszky and Istvan Szanyi, arXiv:hep-ph/1701.01269; to be publ. in PEPAN Letters.

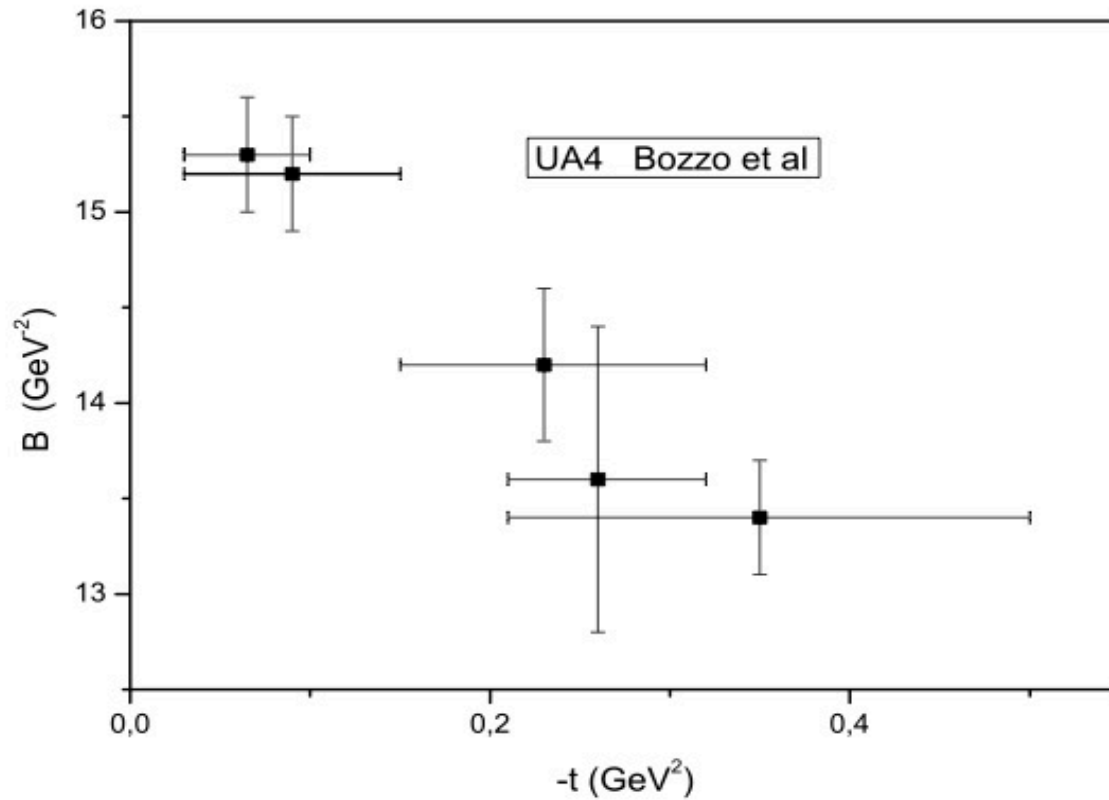


To see the fine structure, one calculates the local slope as $B(s, t) = \frac{d}{dt} \ln \frac{d\sigma}{dt}$ (in t bins!). TOTEM instead uses "normalized" cross sections:

$$R = \frac{\frac{d\sigma}{dt} - ref}{ref}, \quad (7)$$

where $ref = Ae^{B|t|}$.

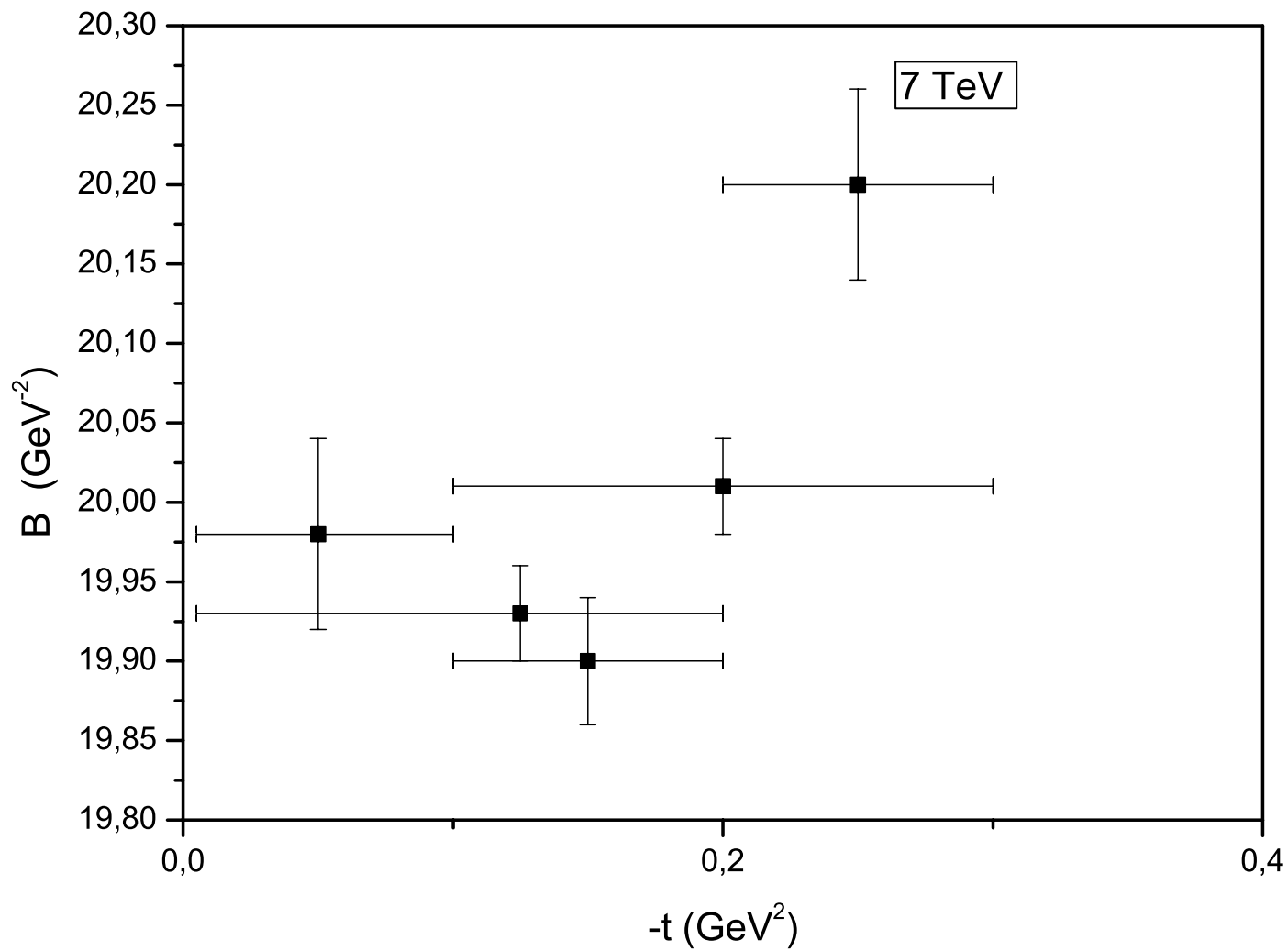


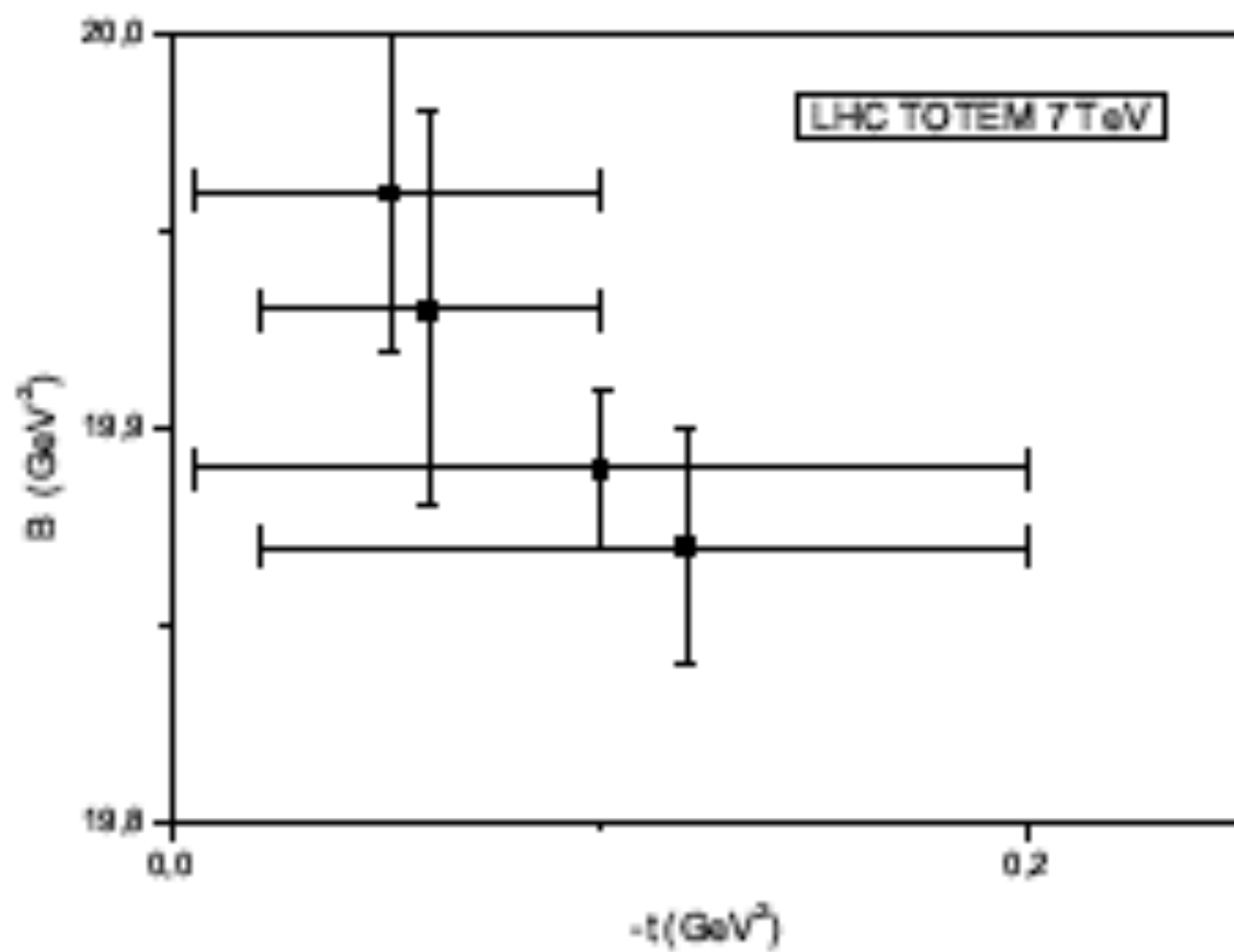


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Hagedorn spectrum:

$$\rho(m) \sim f(m) \exp(m/T), \quad T \approx 160 \text{ MeV}. \quad (8)$$

From statistical bootstrap (duality): $f(m) \sim \alpha'(m)$.

A trajectory obeying the known constraints (unitarity, analyticity, polynomial boundedness) generally can be written as (the signs are fixed uniquely by imposing positivity of the imaginary part (unitarity)).

$$\alpha(s) = \alpha_0 - \sum_i \gamma_i \ln(1 + \beta_i \sqrt{s_i - s}). \quad (9)$$

A simple model satisfying the above conditions, yet fitting the observed spectrum of resonances can be written as a sum, *e.g.*

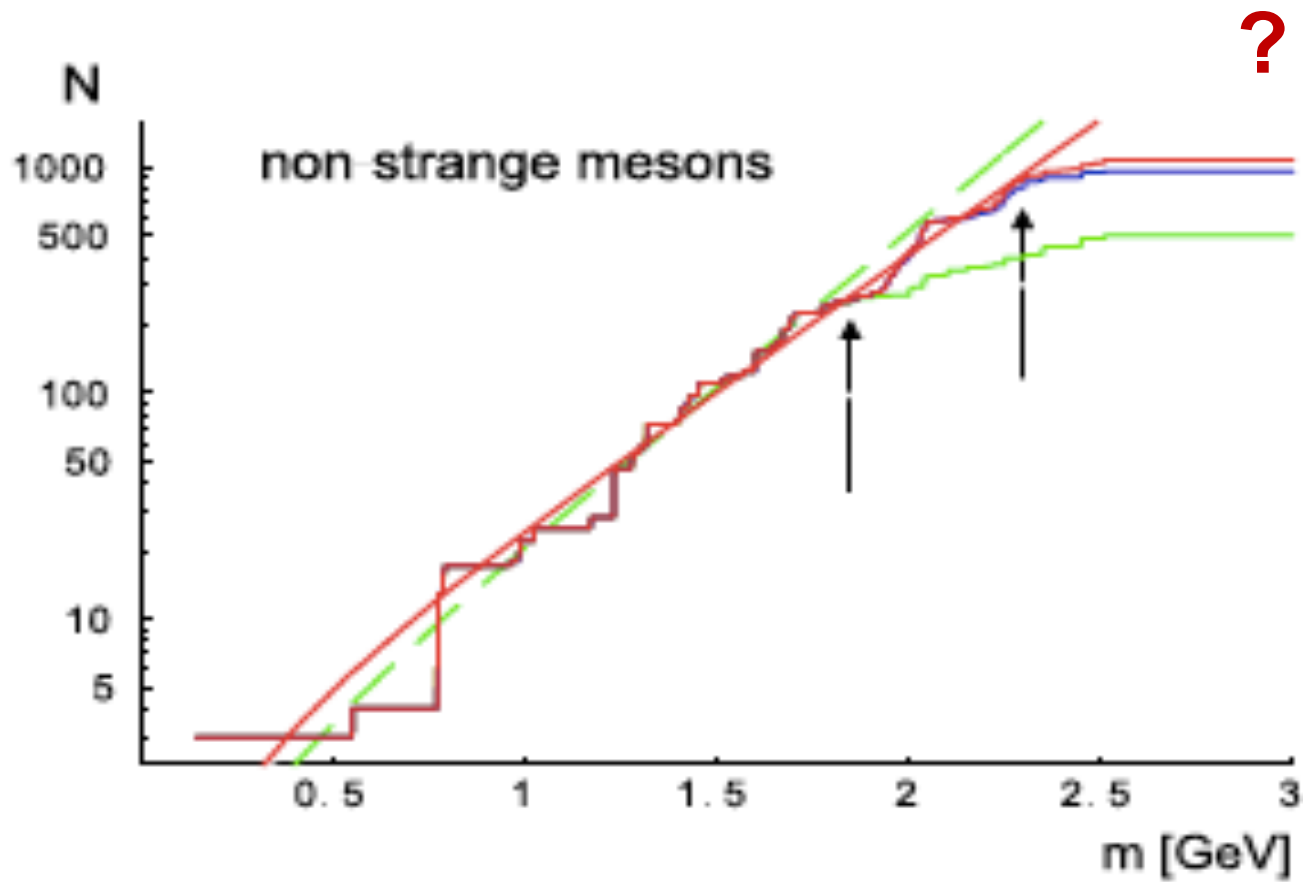
$$\alpha_\rho(m) = 7.64 - 0.127\sqrt{m - 0.28} - 0.093\sqrt{m - 0.988} - 0.761\sqrt{m - 1.88} - (\Lambda\bar{\Sigma}, \Sigma\bar{\Sigma}, \Xi\bar{\Xi}?), \quad (10)$$

with parameters fitted to the masses and widths of known resonances.

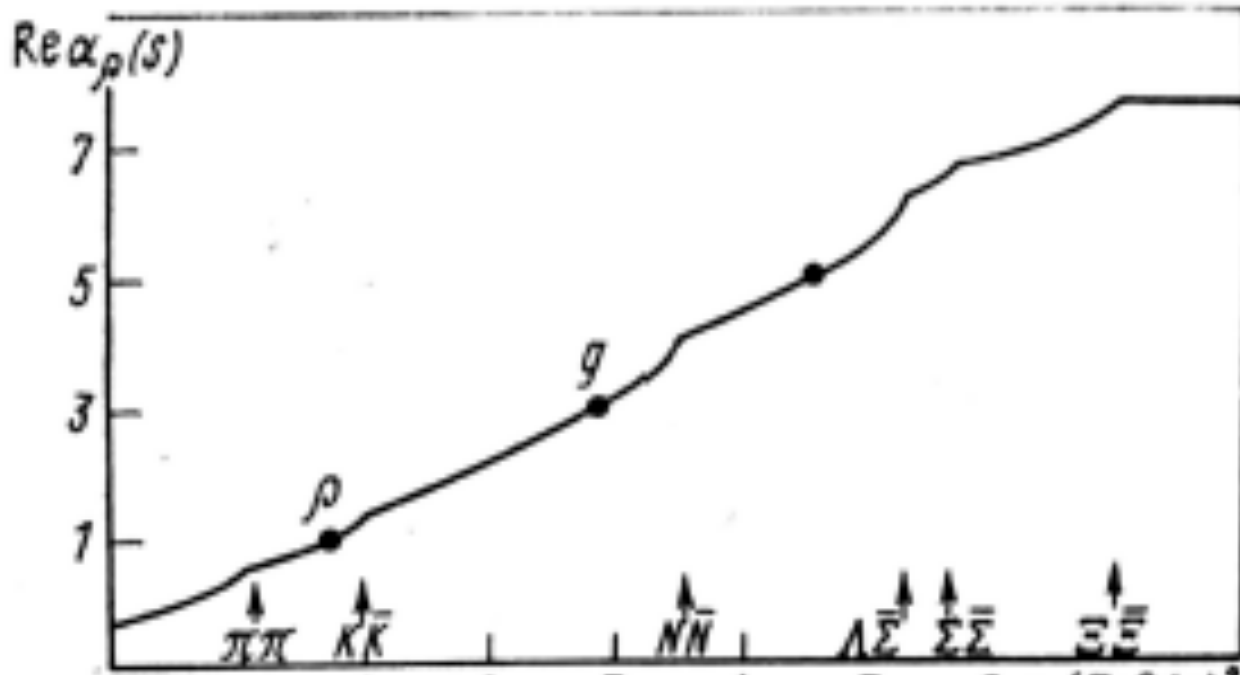
A.O. Barut and D.E. Zwanziger, Phys. Rev. **127 (1962) 974.**

G. Cohen-Tannoudji, V. Ilyin, Jenkovszky *et al.*, Lett. Nuov. Cim. **5 (1972) 957.**

A.I. Bugrij and N.A. Kobylinsky, Annalen der Physik, **32 (1975) 297.**



W.Broniowski, L.J., and R. Schicker, work in progress



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Pomerons (diffraction's) fraction

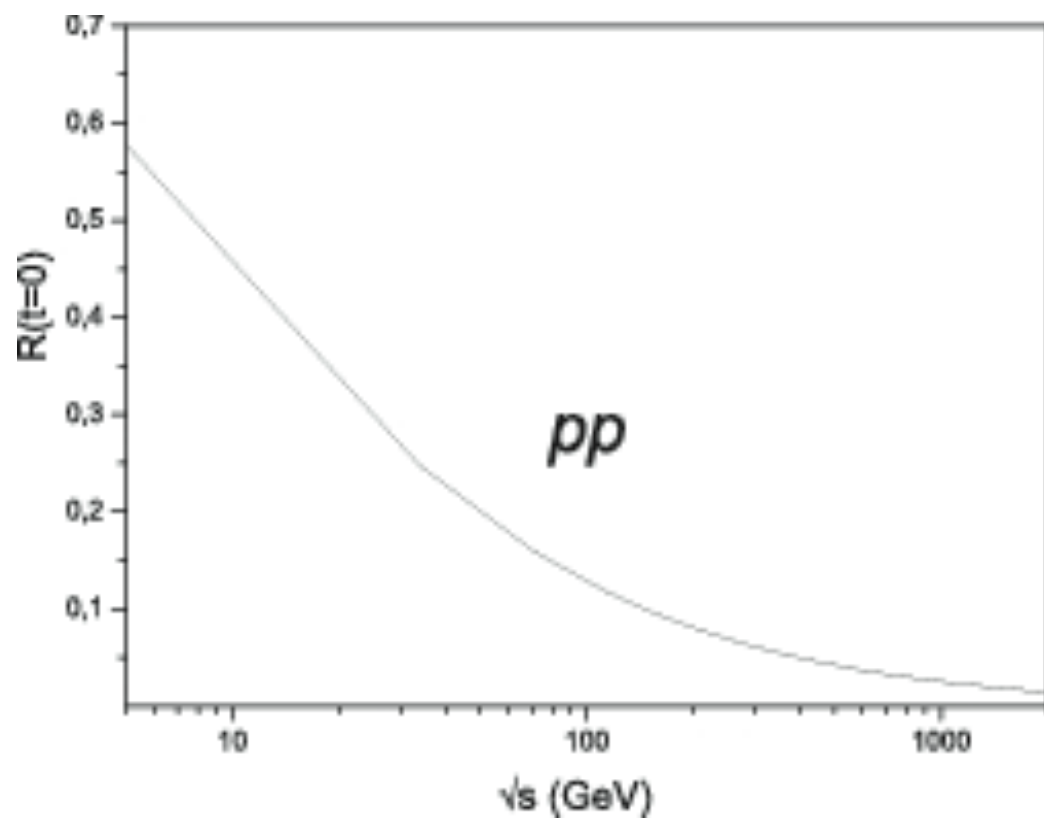
Energy variation of the relative importance of the Pomeron with respect to contributions from the secondary trajectories and the Odderon:

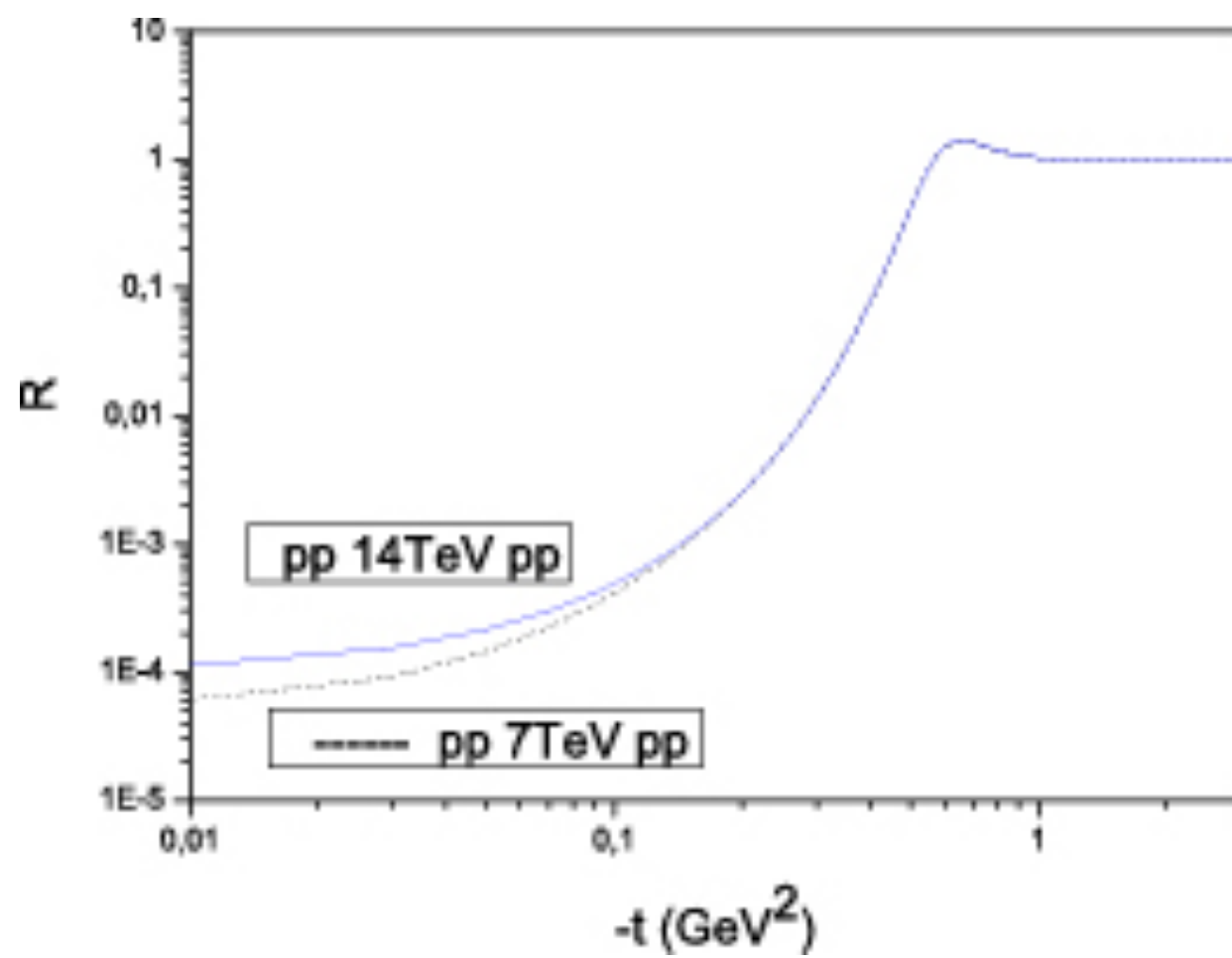
$$R(s, t = 0) = \frac{\Im m(A(s, t) - A_P(s, t))}{\Im A(s, t)}, \quad (1)$$

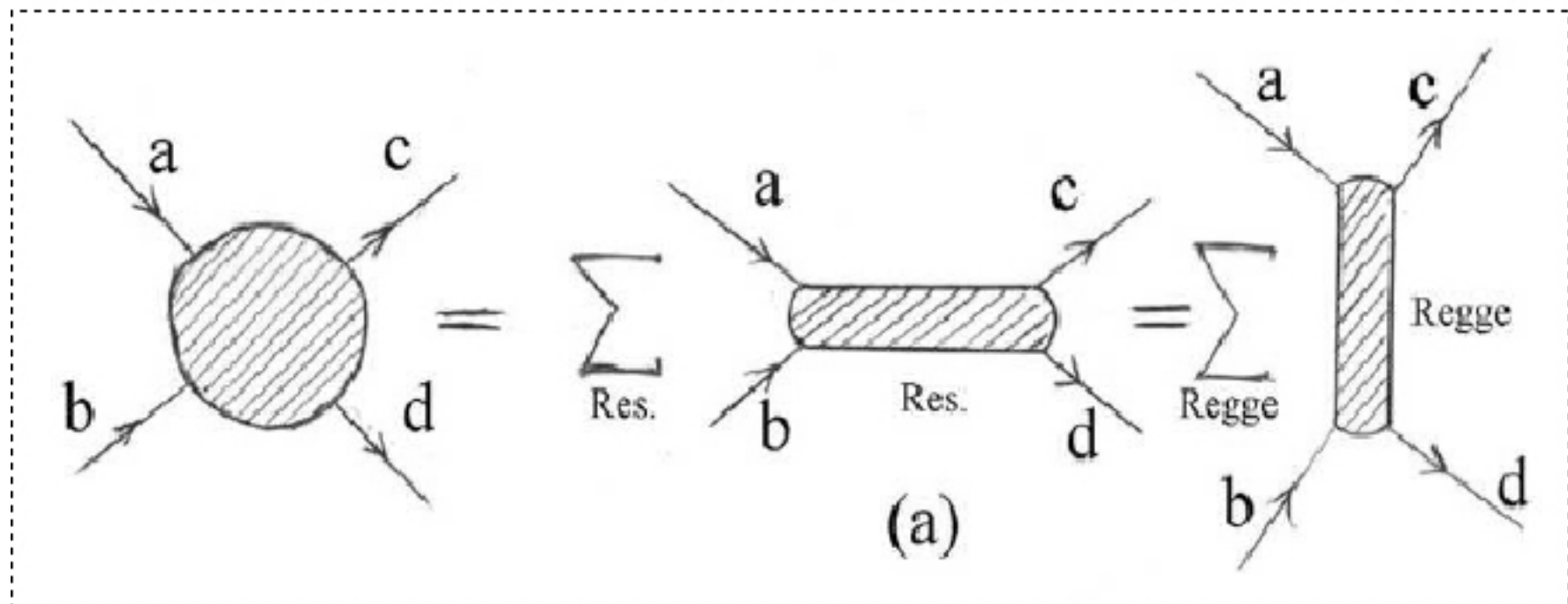
where the total scattering amplitude A includes the Pomeron contribution A_P plus the contribution from the secondary Reggeons and the Odderon.

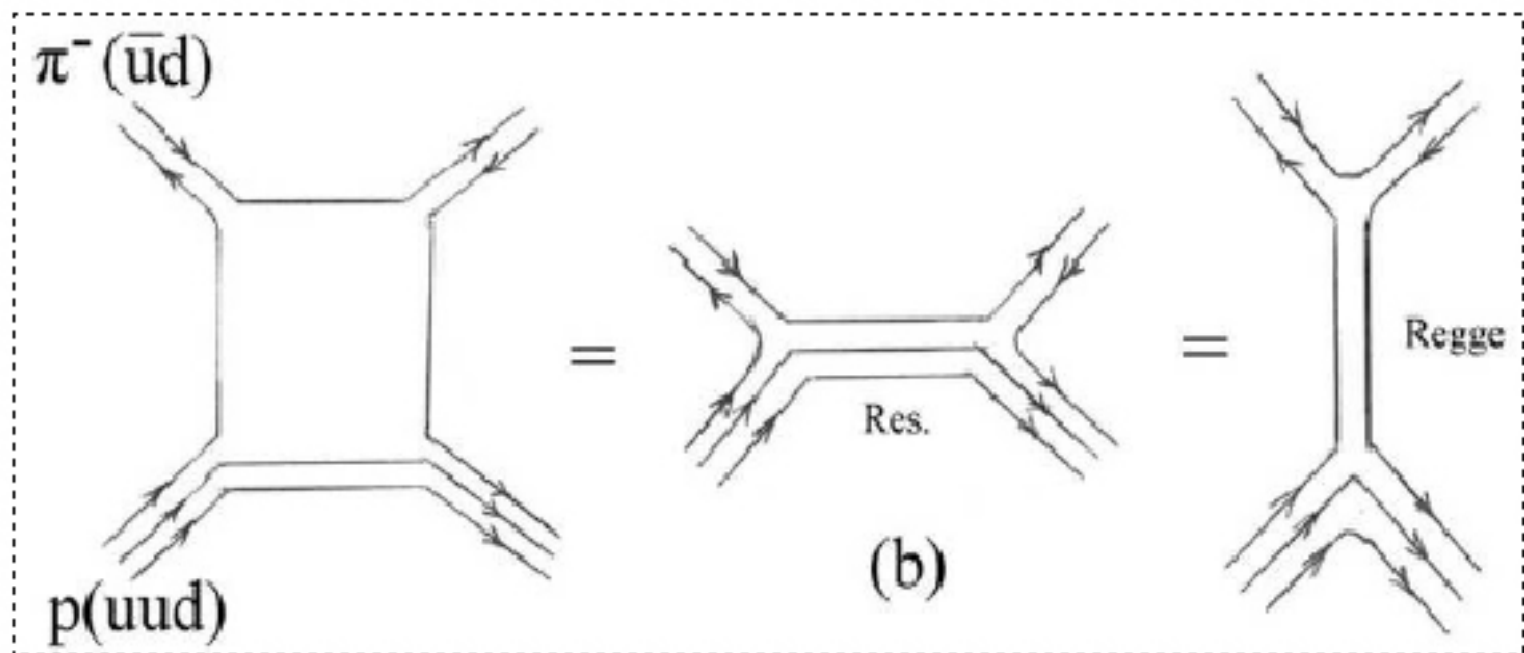
Starting from the Tevatron energy region, the relative contribution of the non-Pomeron terms to the total cross-section becomes smaller than the experimental uncertainty and hence at higher energies they may be completely neglected, irrespective of the model used.

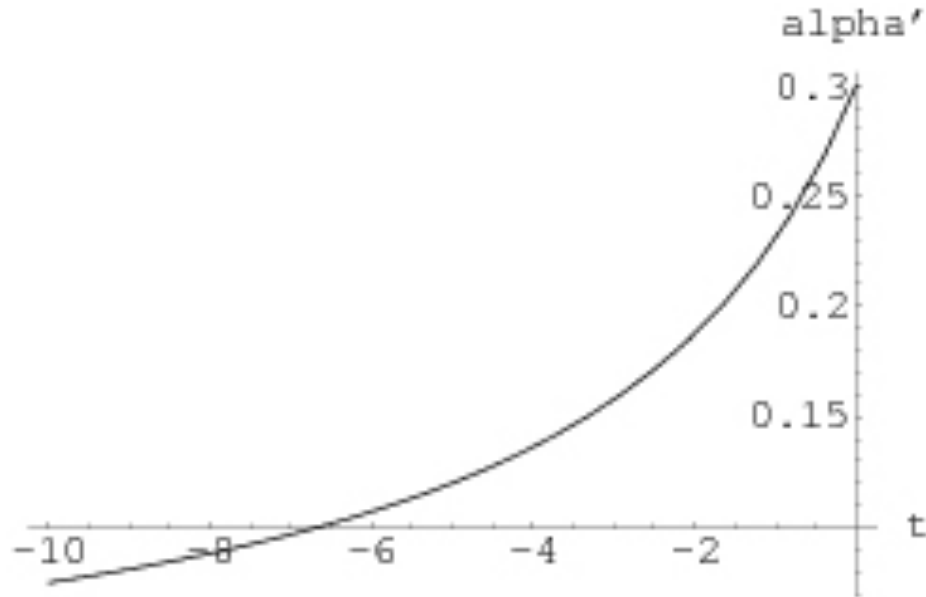
$$R(s, t) = \frac{|(A(s, t) - A_P(s, t))|^2}{|A(s, t)|^2}. \quad (2)$$







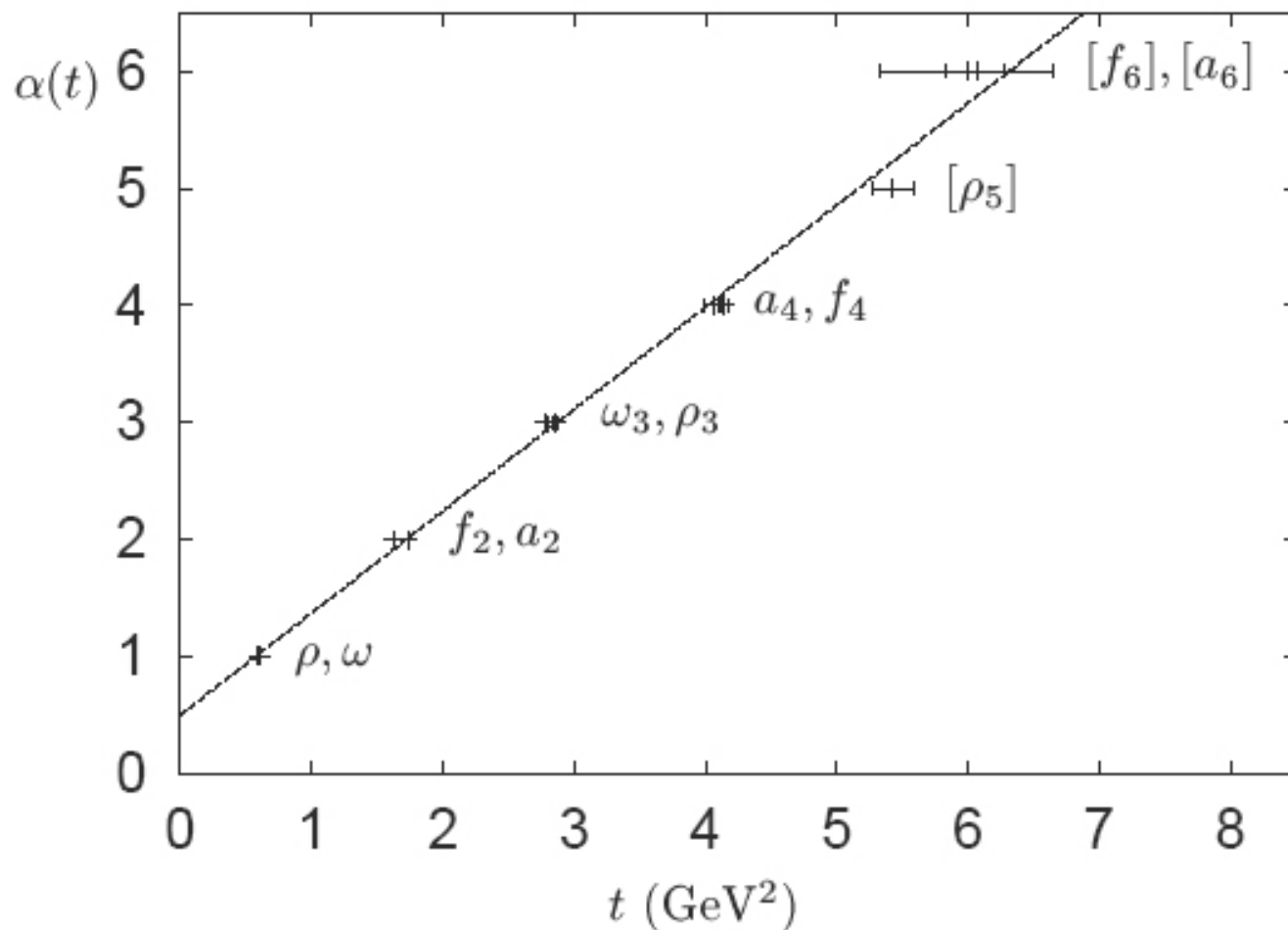




The slope of the cone for a single pole is: $B(s, t) \sim \alpha'(t) \ln s$. The Regge residue $e^{b\alpha(t)}$ with a logarithmic trajectory $\alpha(t) = \alpha(0) - \gamma \ln(1 - \beta t)$, is identical to a form factor (geometrical model).

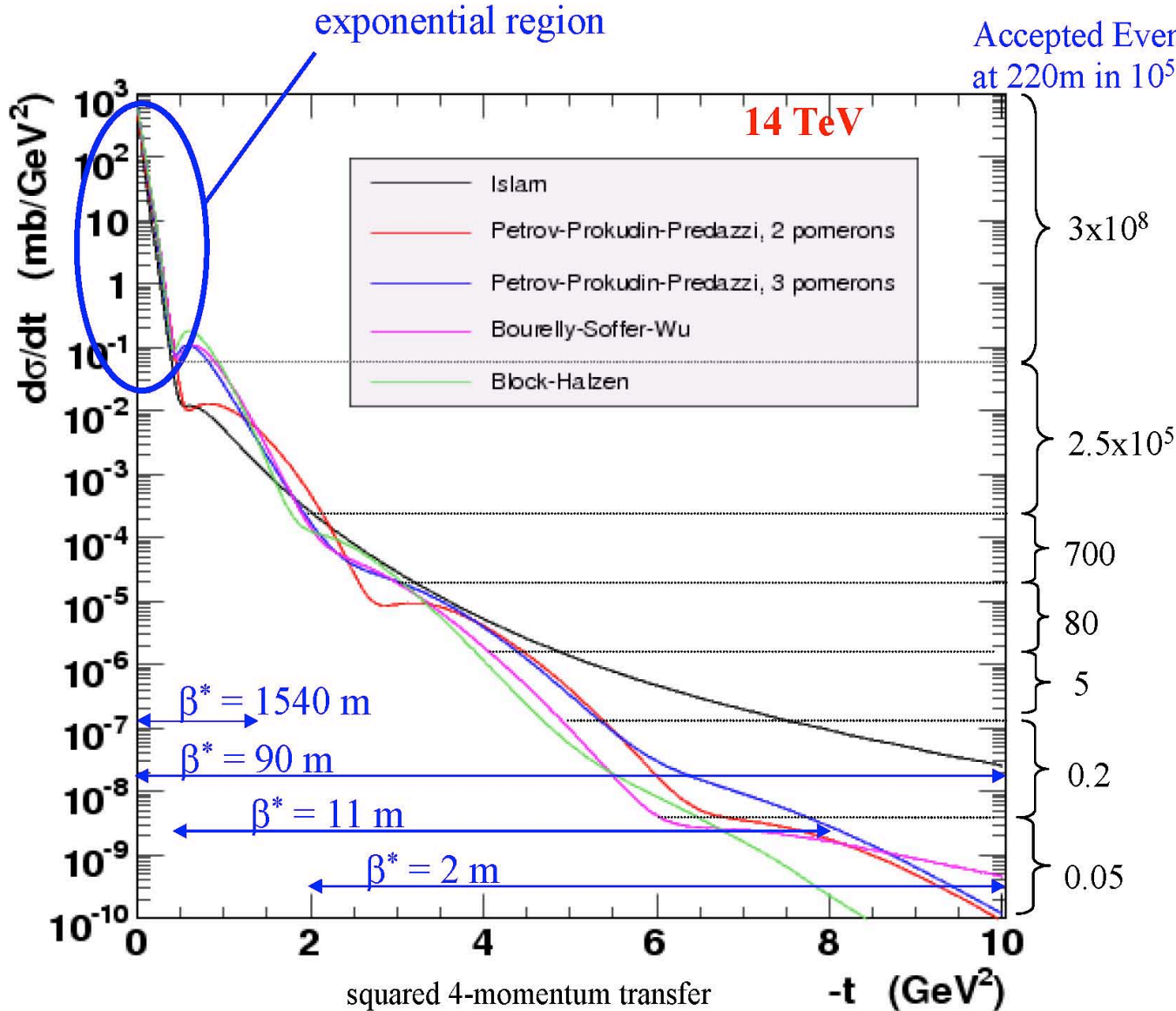
Linear particle trajectories

Plot of spins of families of particles against their squared masses:

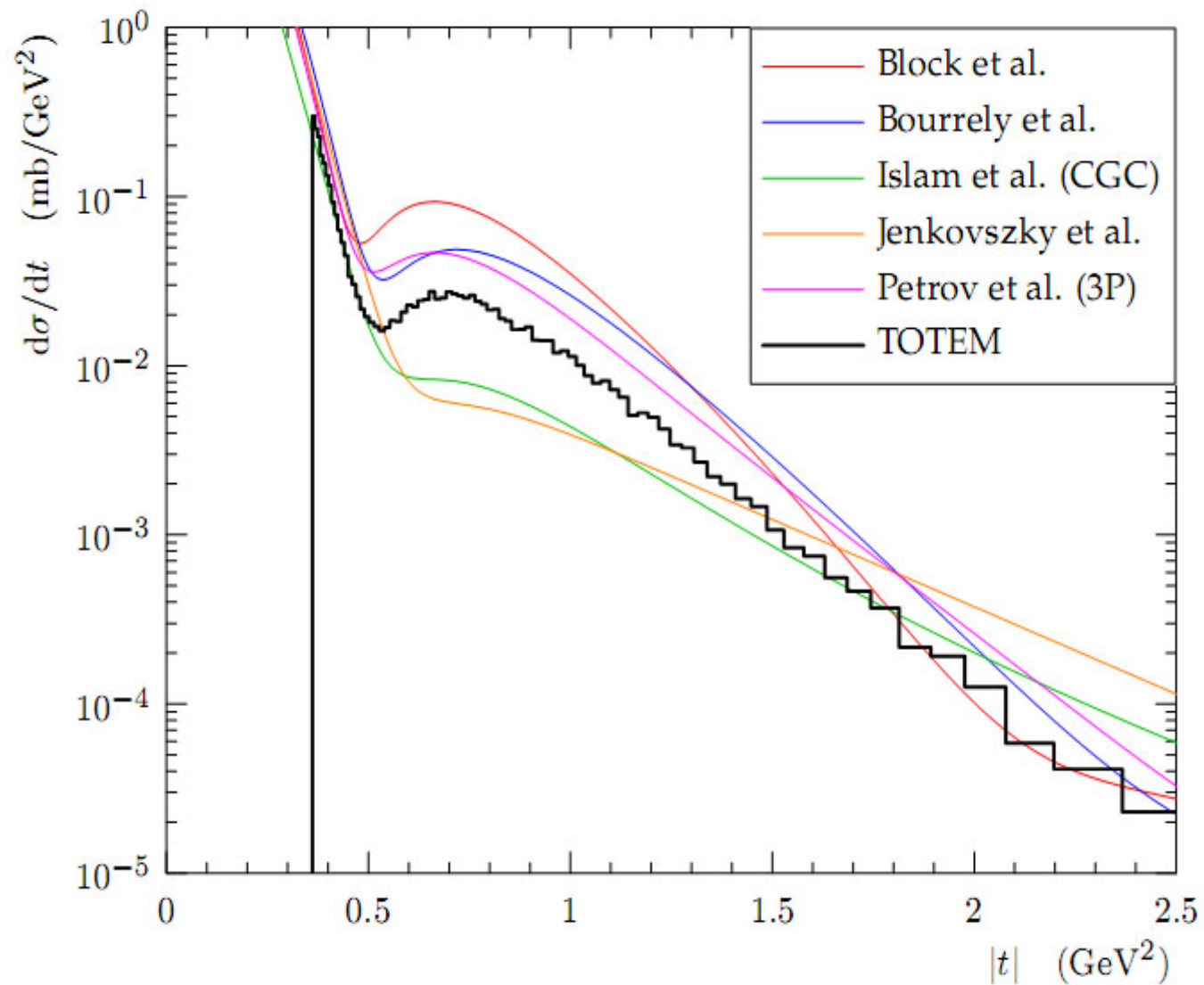


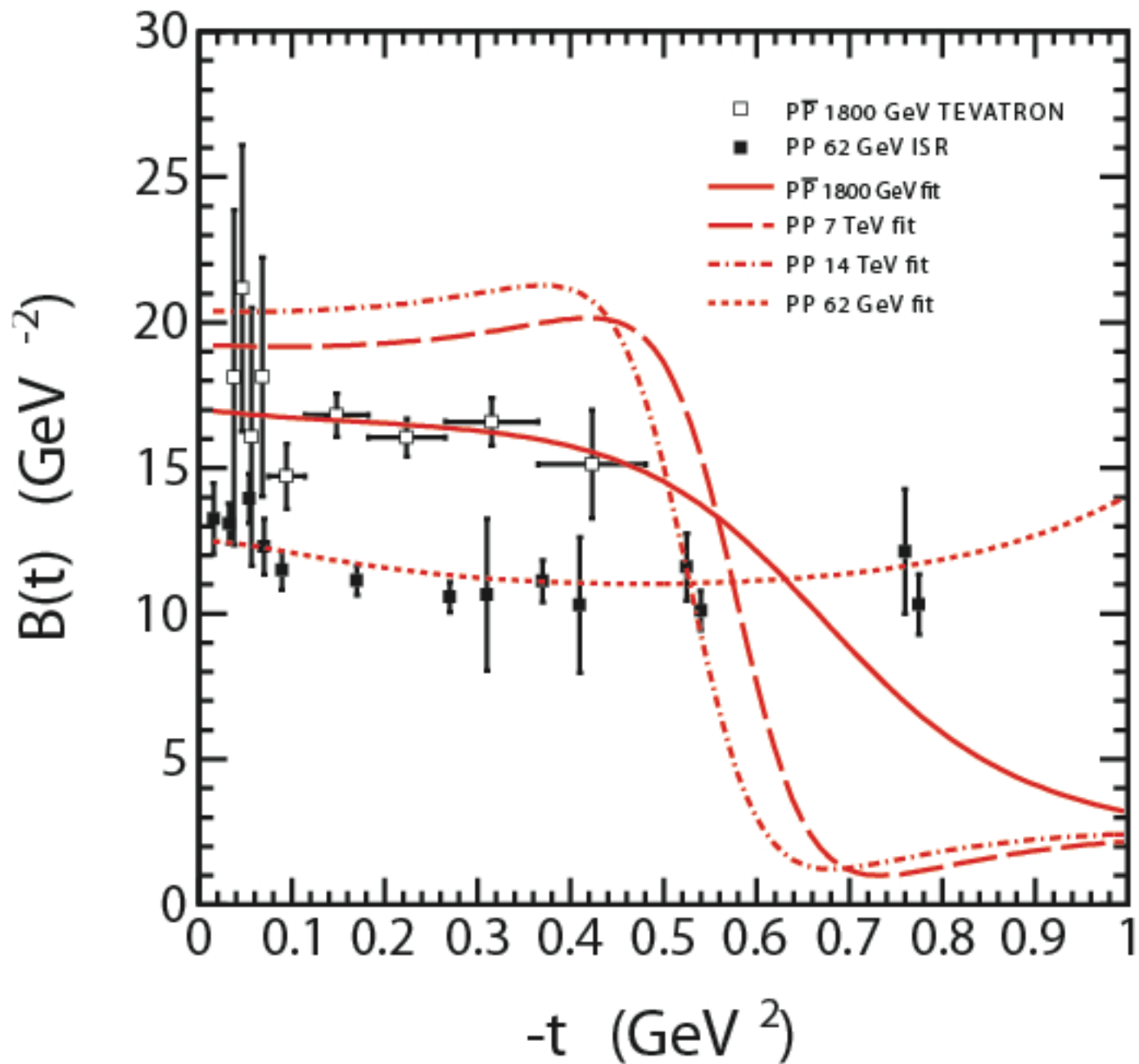


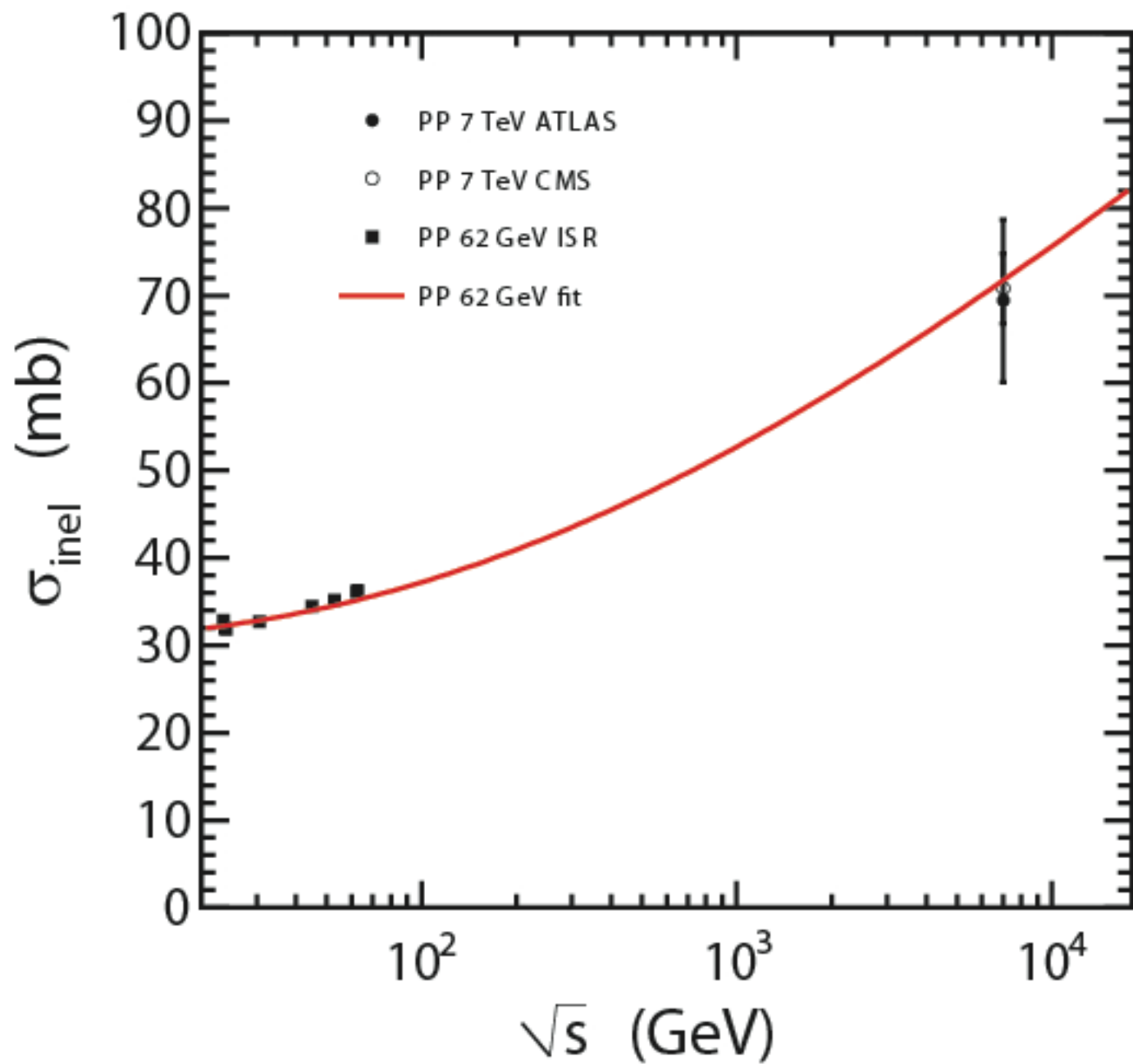
Accepted Events (BSW model)
at 220m in 10^5 s, $\beta^*=90$ m, $\mathcal{L}=5 \times 10^{29}$

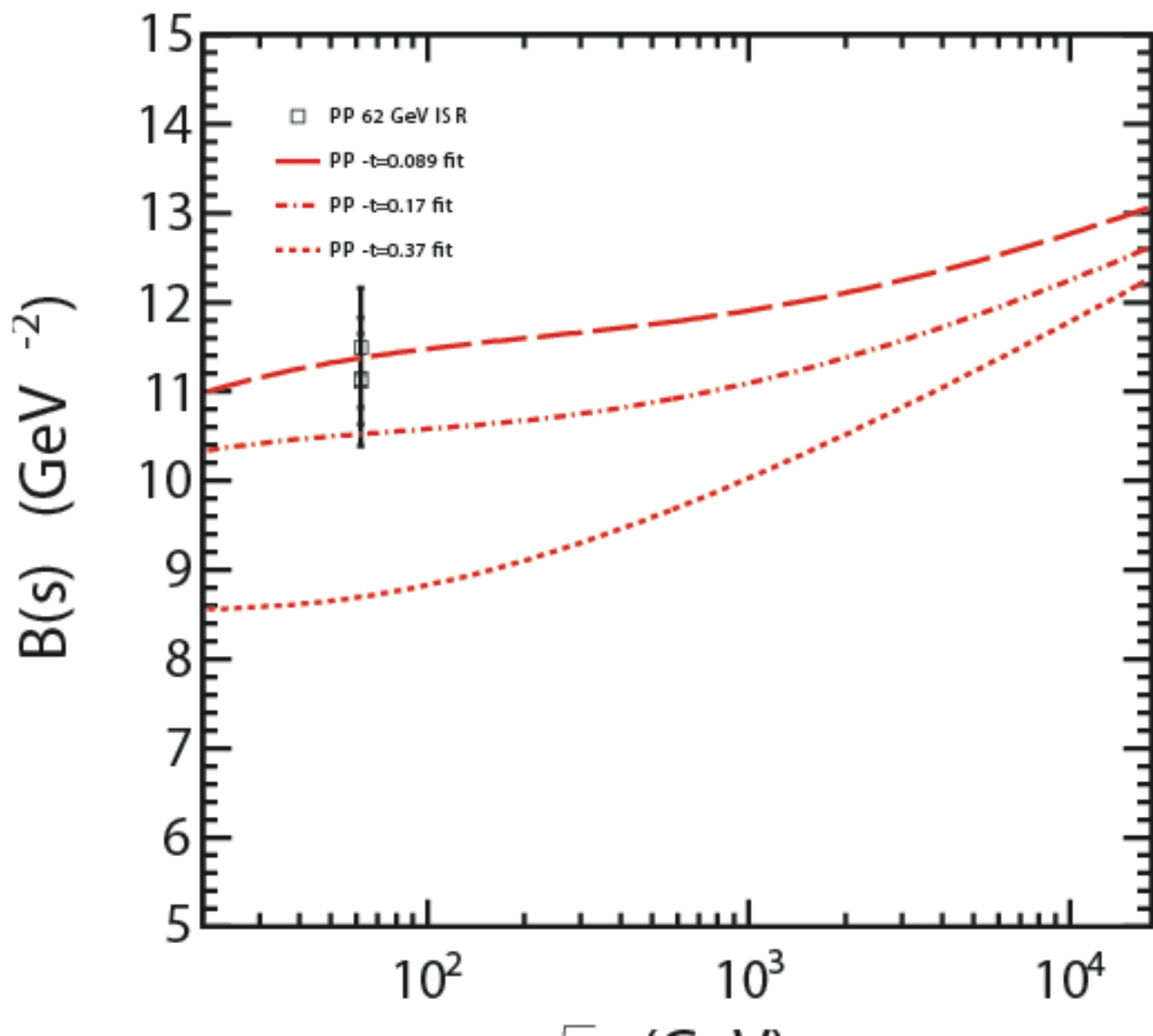


CERN LHC, TOTEM Collab., June 26, 2011:

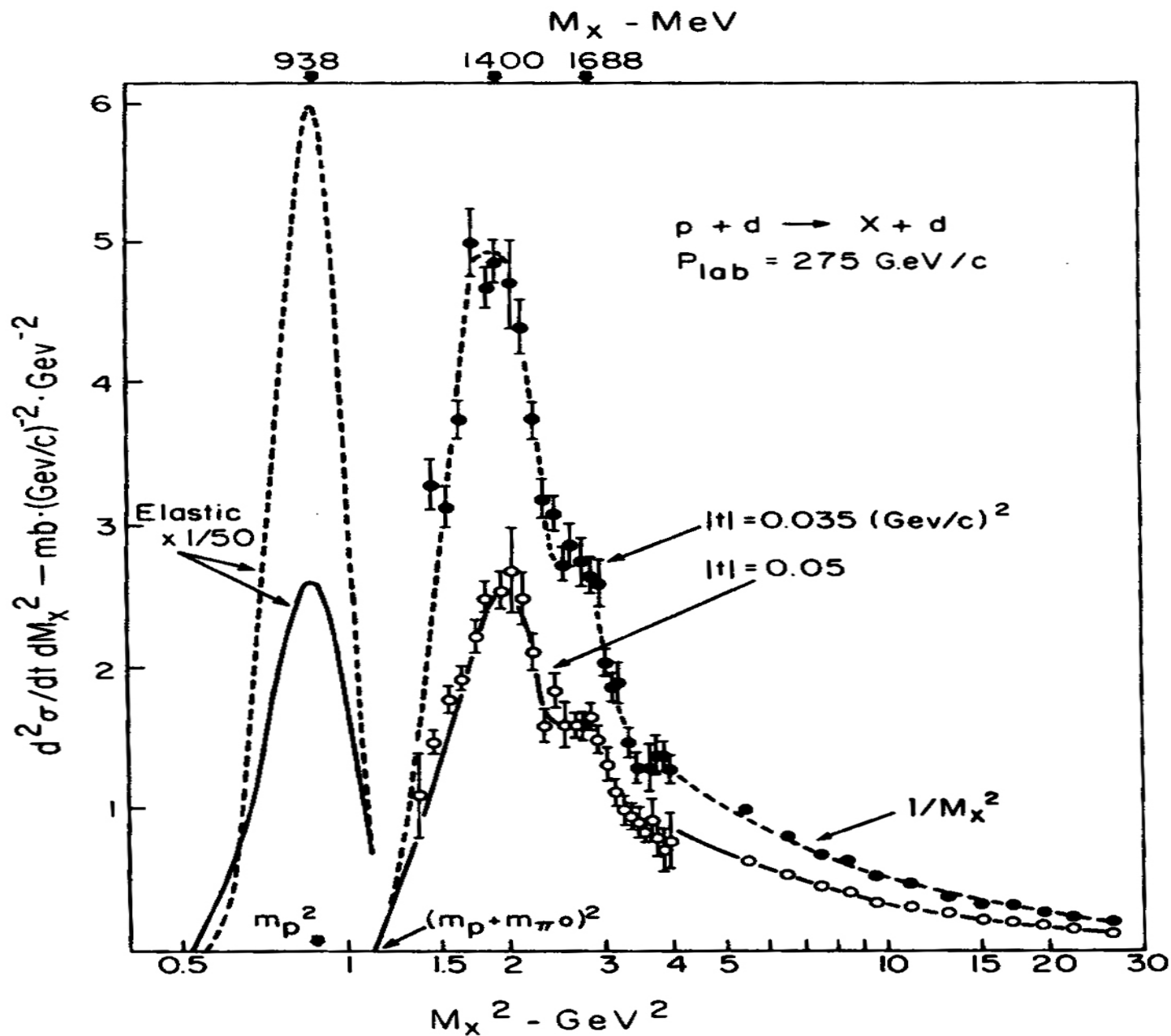


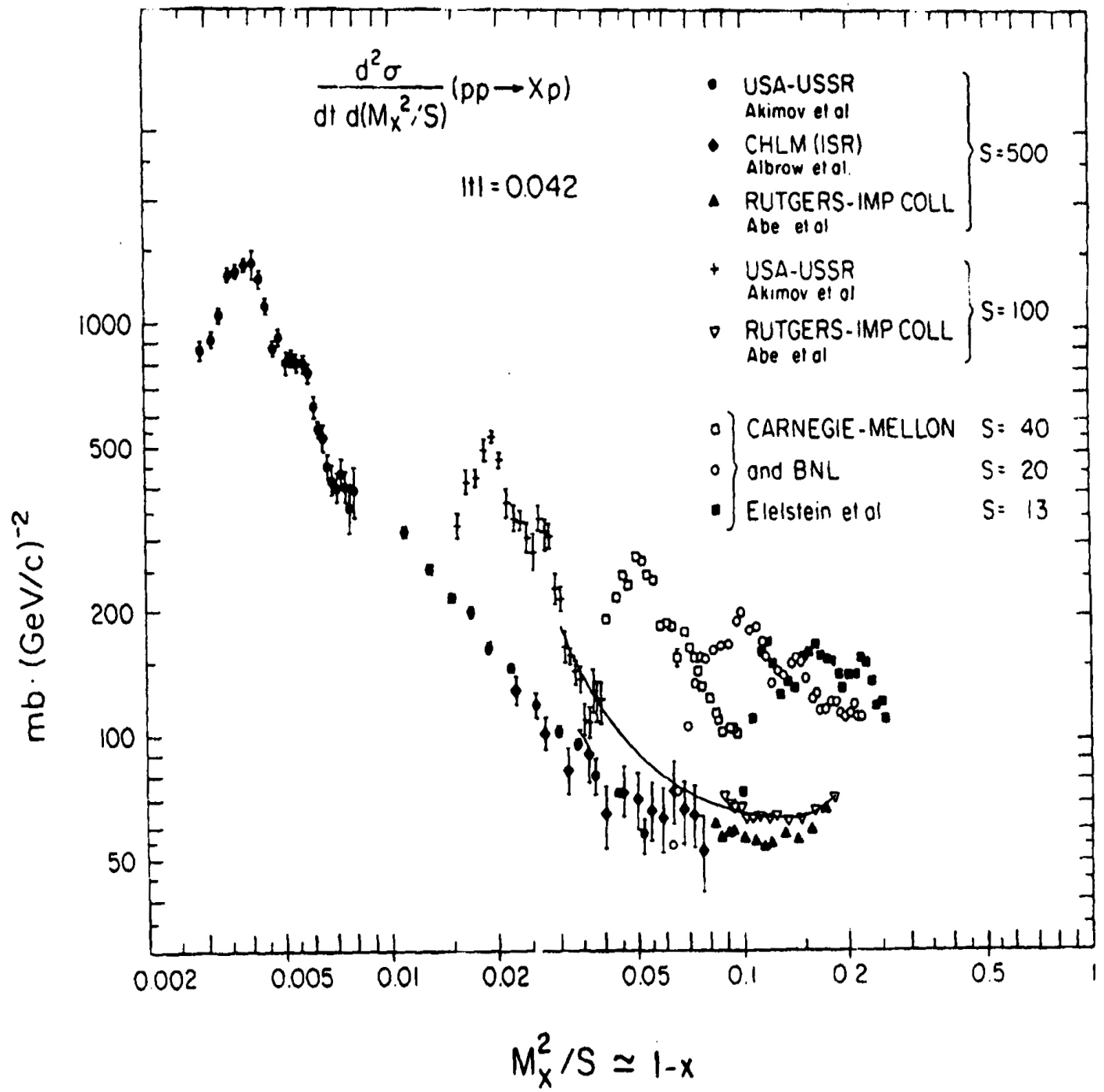


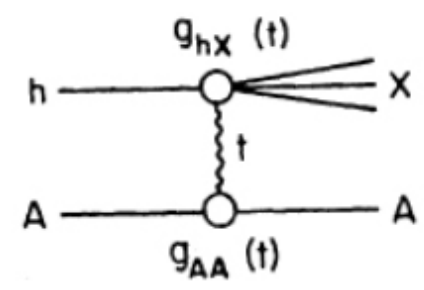
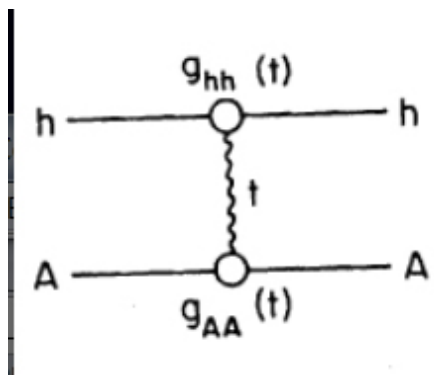




FNAL

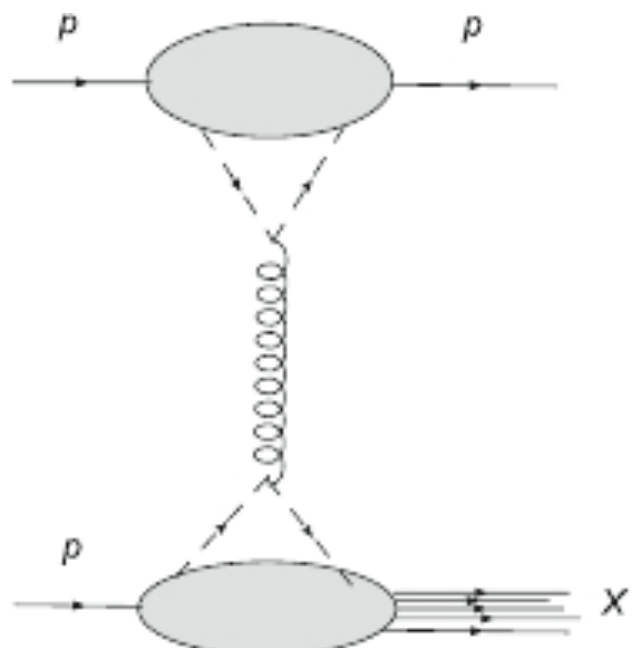
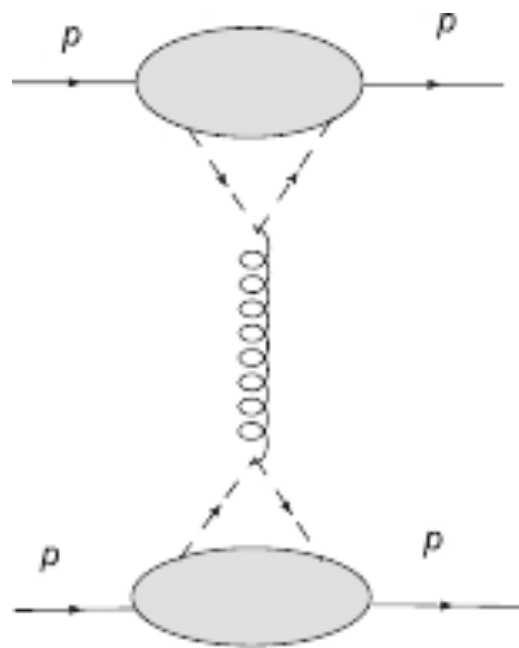






$$\frac{d^2\sigma}{dtdx} = \left| \begin{array}{c} \text{h} \\ \text{p} \end{array} \right|_{\text{X}}^2 = \left| \begin{array}{c} \text{h} \\ \text{p} \end{array} \right|_{t=0}^2 = \left| \begin{array}{c} \text{h} \\ \text{p} \end{array} \right|_{t=0}^2$$

$$\sigma_{\text{tot}} = \left| \begin{array}{c} \text{h} \\ \text{p} \end{array} \right|^2 = \left| \begin{array}{c} \text{h} \\ \text{p} \end{array} \right|^2 = \left| \begin{array}{c} \text{h} \\ \text{p} \end{array} \right|_{t=0}^2$$



The pp scattering amplitude

$$A(s, t)_P = -\beta^2 [f^u(t) + f^d(t)]^2 \left(\frac{s}{s_0} \right)^{\alpha_P(t)-1} \frac{1 + e^{-i\pi\alpha_P(t)}}{\sin \pi\alpha_P(t)}, \quad (1)$$

where $f^u(t)$ and $f^d(t)$ are the amplitudes for the emission of u and d valence quarks by the nucleon, β is the quark-Pomeron coupling, to be determined below; $\alpha_P(t)$ is a vacuum Regge trajectory. It is assumed that the Pomeron couples to the proton via quarks like a scalar photon.

A single-Pomeron exchange is valid at the LHC energies, however at lower energies (e.g. those of the ISR or the SPS) the contribution of non-leading Regge exchanges should be accounted for as well.

Thus, the unpolarized elastic pp differential cross section is

$$\frac{d\sigma}{dt} = \frac{[3\beta F^p(t)]^4}{4\pi \sin^2[\pi\alpha_P(t)/2]} (s/s_0)^{2\alpha_P(t)-2}. \quad (2)$$

Similar to the case of elastic scattering, the double differential cross section for the SDD reaction, by Regge factorization, can be written as

$$\frac{d^2\sigma}{dt dM_X^2} = \frac{9\beta^4 [F^P(t)]^2}{4\pi \sin^2[\pi\alpha_P(t)/2]} (s/M_X^2)^{2\alpha_P(t)-2} \times \left[\frac{W_2}{2m} \left(1 - M_X^2/s\right) - mW_1(t + 2m^2)/s^2 \right], \quad (1)$$

where W_i , $i = 1, 2$ are related to the structure functions of the nucleon and $W_2 \gg W_1$. For high M_X^2 , the $W_{1,2}$ are Regge-behaved, while for small M_X^2 their behavior is dominated by nucleon resonances. The knowledge of the inelastic form factors (or transition amplitudes) is crucial for the calculation of low-mass diffraction dissociation.

In the LHC energy region it simplifies to:

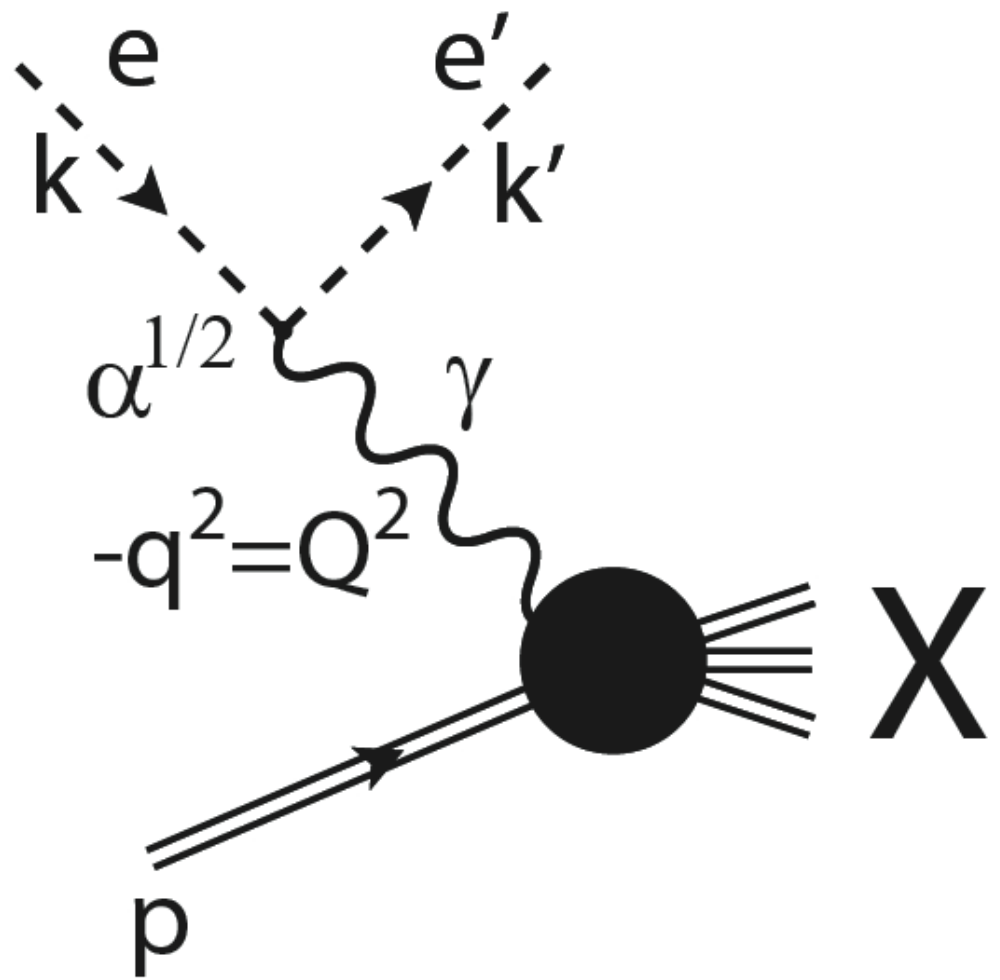
$$\frac{d^2\sigma}{dt dM_X^2} \approx \frac{9\beta^4 [F^p(t)]^2}{4\pi} (s/M_X^2)^{2\alpha_P(t)-2} \frac{W_2}{2m}. \quad (1)$$

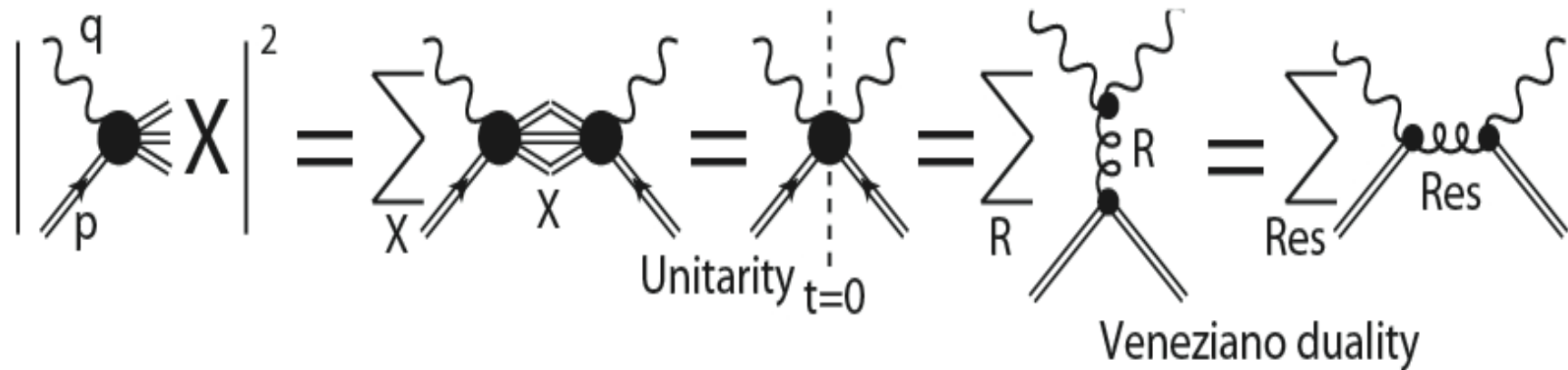
These expressions for SDD do not contain the elastic scattering limit because the inelastic form factor $W_2(M_X, t)$ has no elastic form factor limit $F(t)$ as $M_X \rightarrow m$. This problem is similar to the $x \rightarrow 1$ limit of the deep inelastic structure function $F_2(x, Q^2)$. The elastic contribution to SDD should be added separately.

Low-mass diffraction dissociation at the LHC

L. Jenkovszky, O. Kuprash, J. Lamsa, V. Magas, and R. Orava:
Dual-Regge approach to high-energy, low-mass DD at the LHC,
Phys. Rev. D83(2011)0566014; hep-ph/1-11.0664.

L. Jenkovszky, O. Kuprash, J. Lamsa and R. Orava: hep-ph/11063299,
Mod. Phys. Letters A. **26**(2011) 1-9, August 2011.



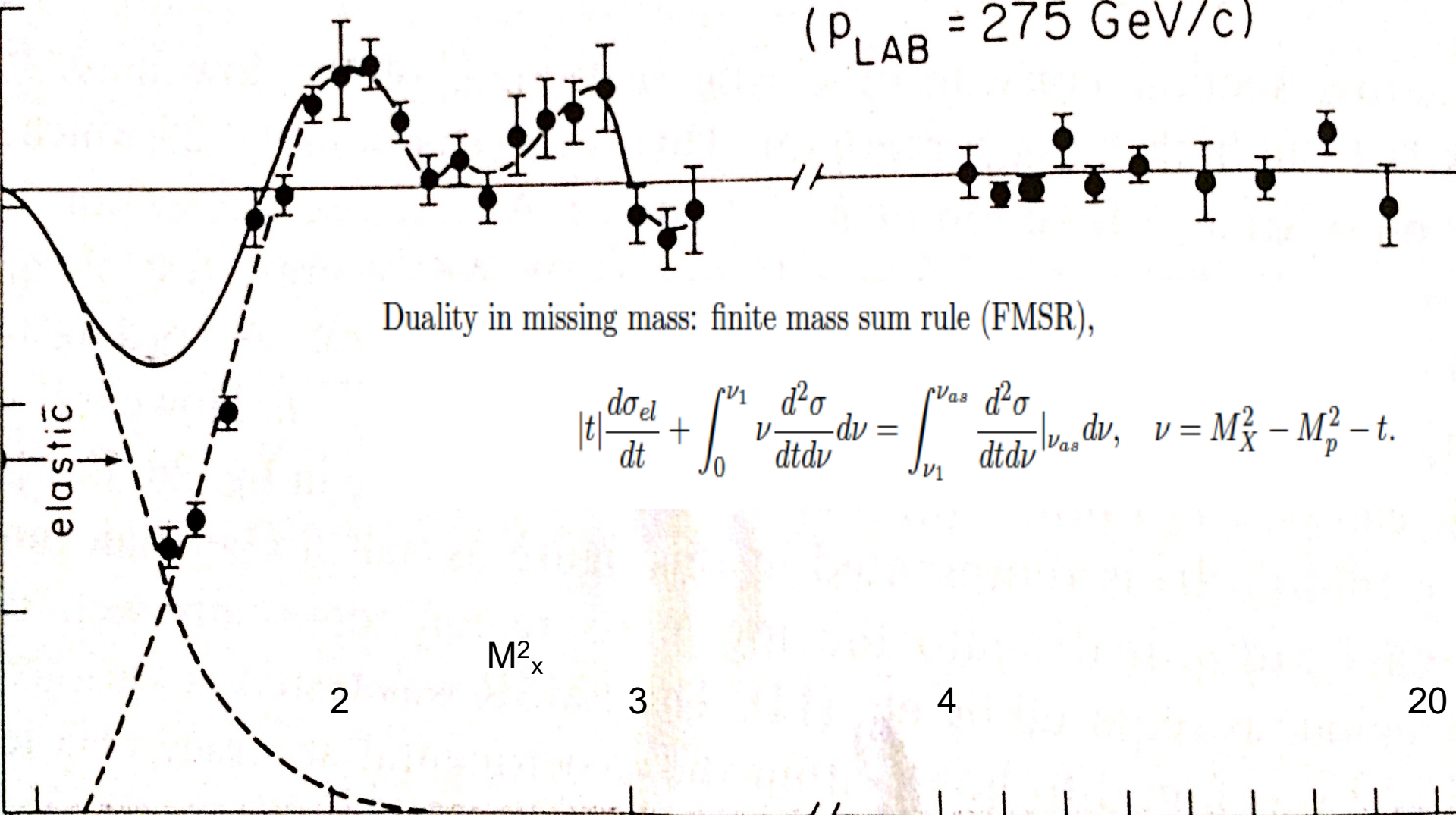


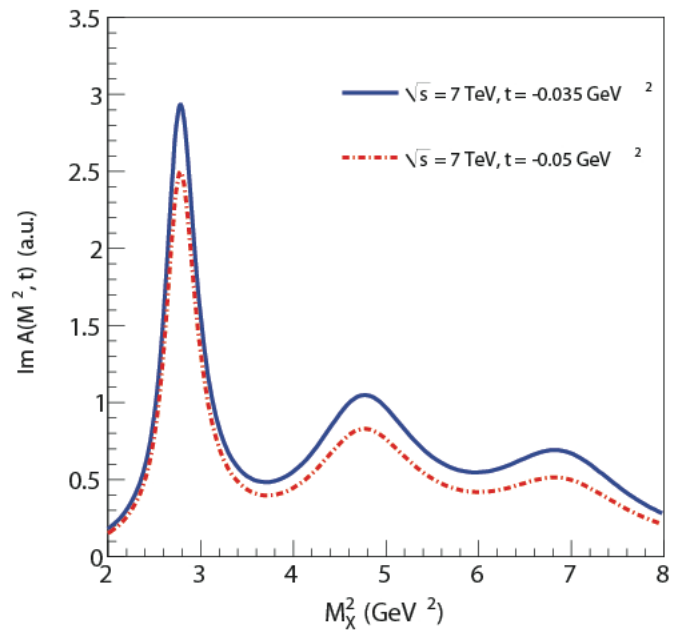
The final expression for the double differential cross section reads:

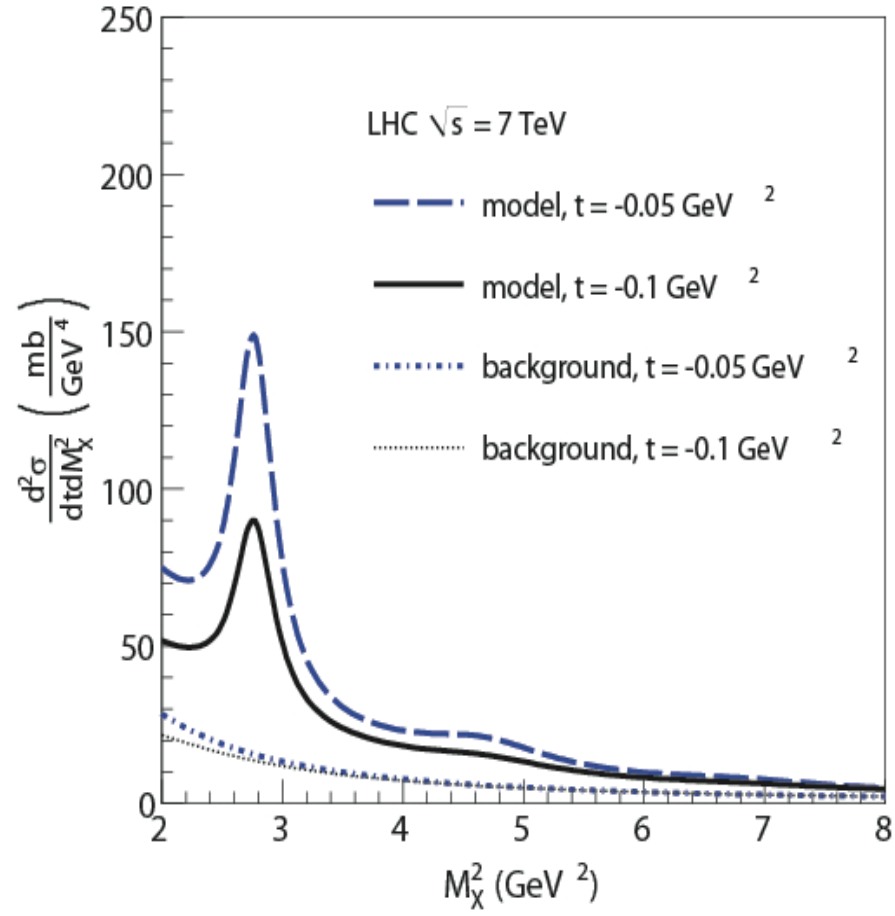
$$\begin{aligned}
 \frac{d^2\sigma}{dt dM_X^2} = & \\
 A_0 \left(\frac{s}{M_X^2} \right)^{2\alpha_P(t)-2} & \frac{x(1-x)^2 [F^p(t)]^2}{(M_x^2 - m^2) \left(1 + \frac{4m^2 x^2}{-t}\right)^{3/2}} \times \\
 \sum_{n=1,3} & \frac{[f(t)]^{2(n+1)} \text{Im } \alpha(M_X^2)}{(2n + 0.5 - \text{Re } \alpha(M_X^2))^2 + (\text{Im } \alpha(M_X^2))^2} .
 \end{aligned} \tag{1}$$

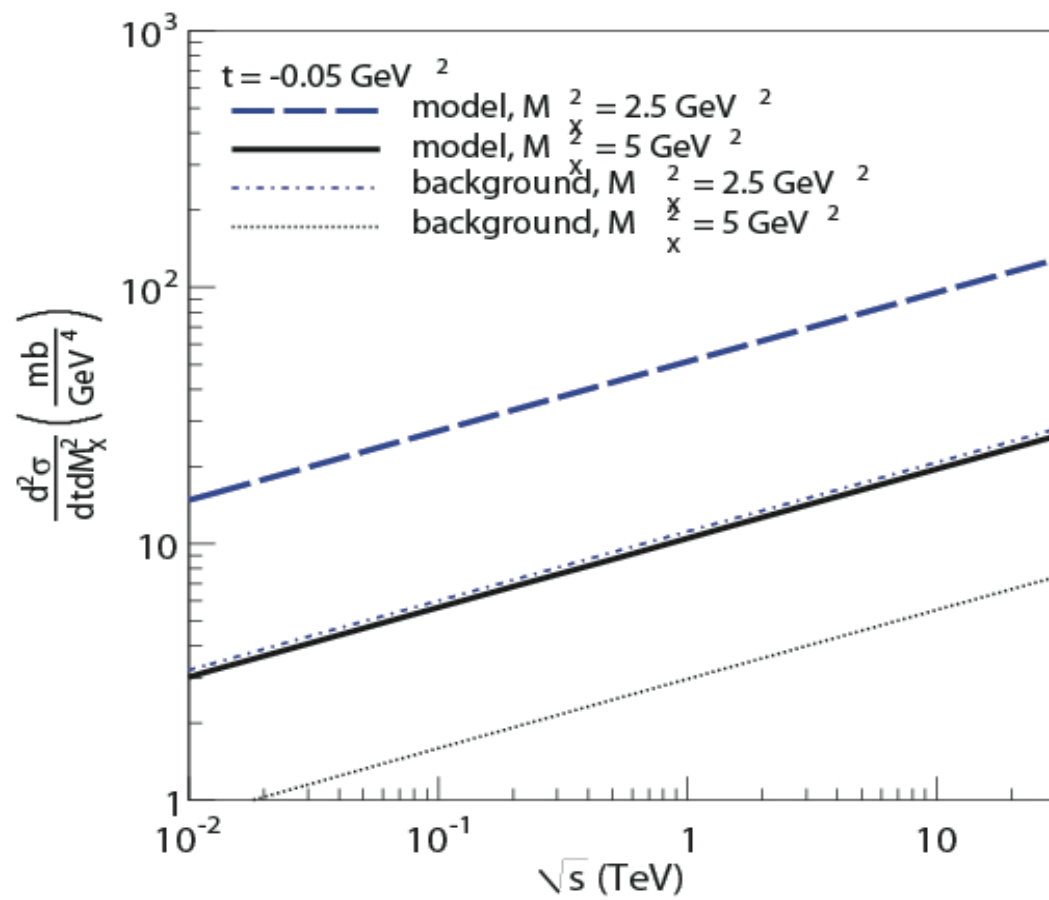
$$\nu \left. \frac{d^2\sigma}{dt dM_X^2} \right|_{|t|=0.035} \quad (p+d \rightarrow X+d) / F_d$$

$(p_{LAB} = 275 \text{ GeV}/c)$

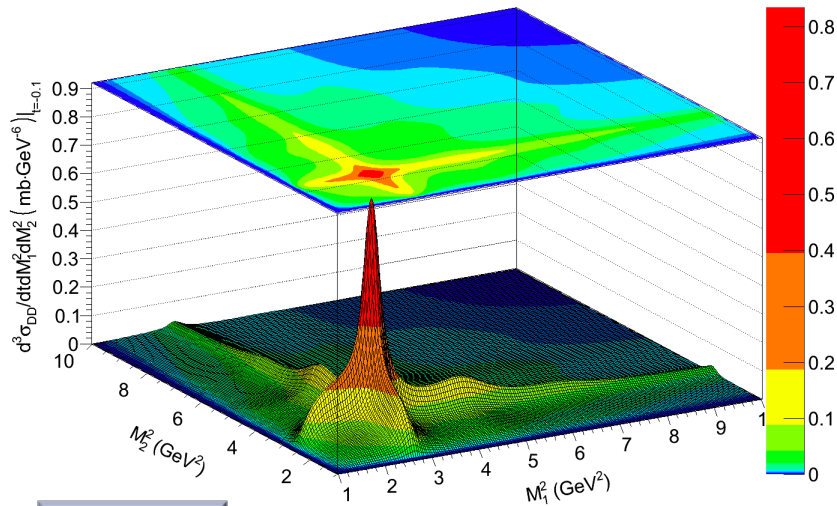




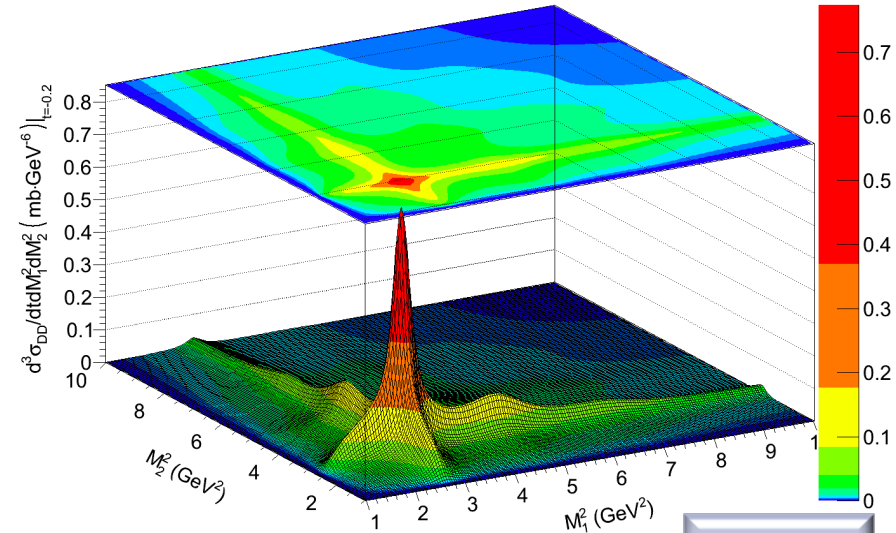




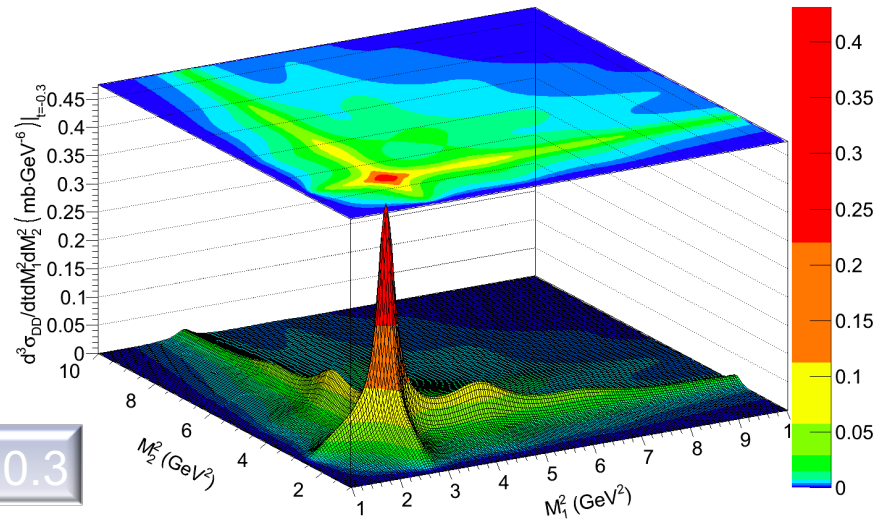
Triple differential DD cross sections



$t = -0.1$



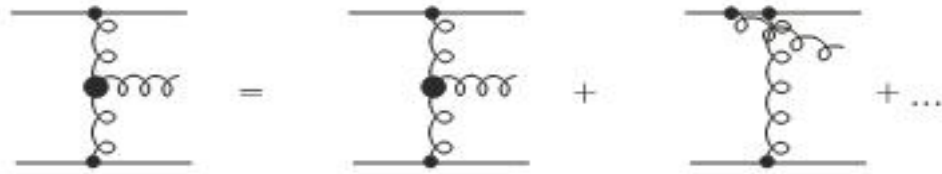
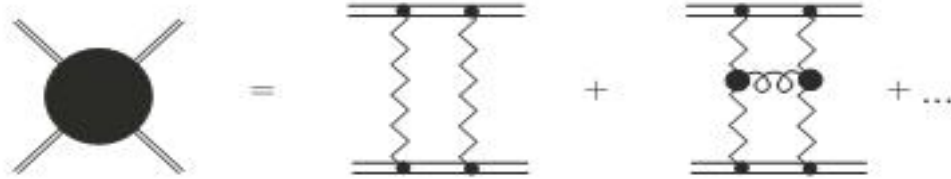
$t = -0.2$



$t = -0.3$

Thank you !

R. Fiore, L.L. Jenkovszky, E.A. Kuraev, A.I. Lengyel, and Z.Z. Tarics,
*Predictions for high-energy pp and $\bar{p}p$ scattering from a finite sum of
gluon ladders*, Phys. Rev. D81, #5 (2010) 056005; arXiv0911.2094/hep-ph



$$\sigma_t^{(P)}(s) = \sum_{i=0}^N f_i \theta(s - s_0^i) \theta(s_0^{i+1} - s) , \quad (1)$$

where

$$f_i = \sum_{j=0}^i a_{ij} L^j , \quad (2)$$