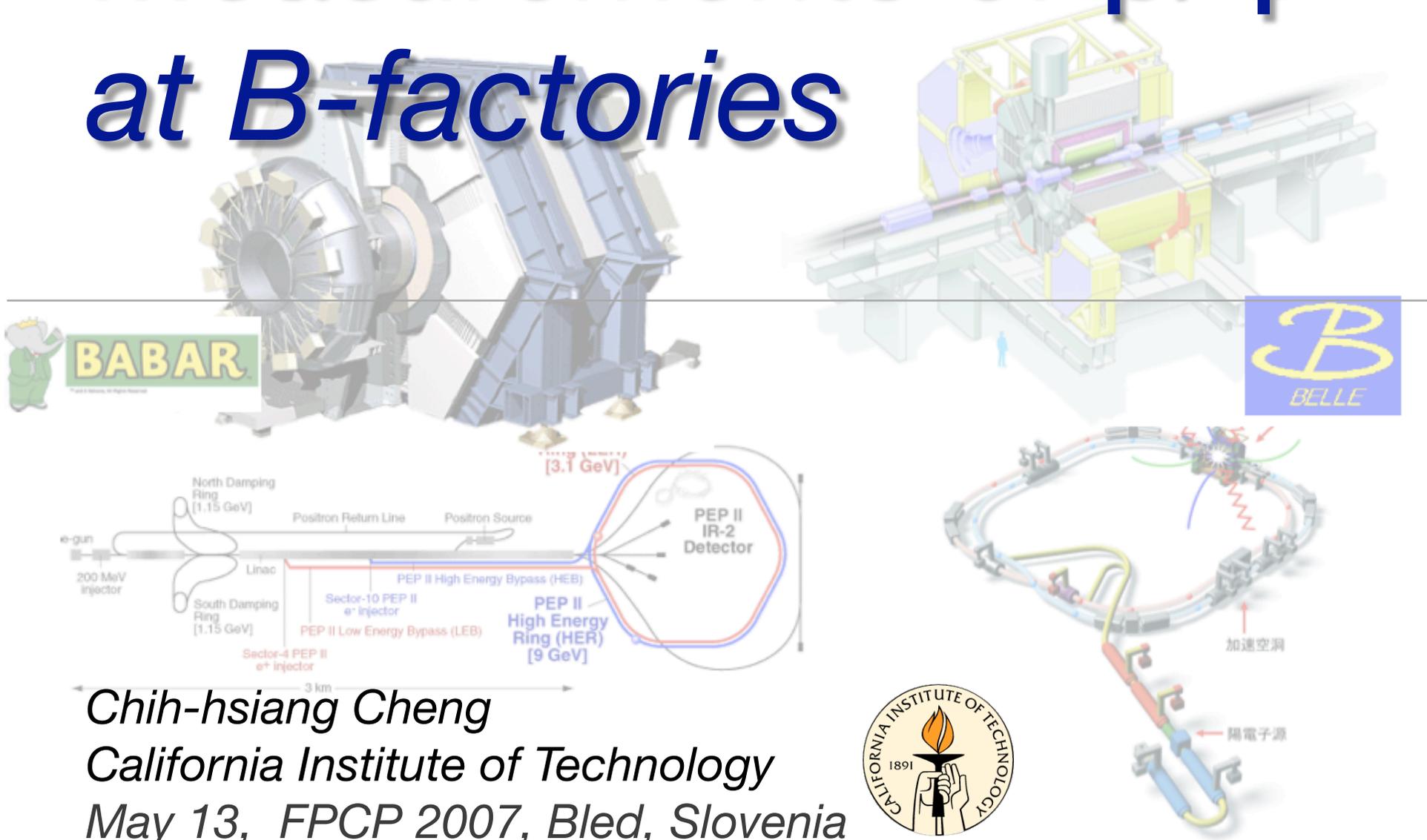


Measurements of β/φ_1 at *B*-factories

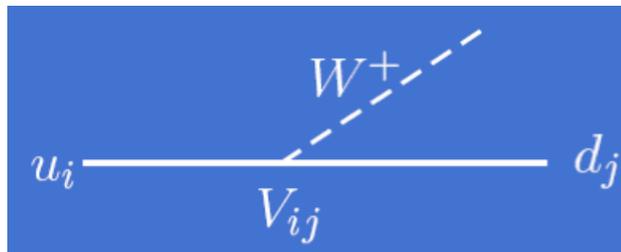


Chih-hsiang Cheng
California Institute of Technology
May 13, FPCP 2007, Bled, Slovenia



Main mission of B-factories: measure and over-constrain the CKM unitarity triangle

- Weak charged current and the CKM matrix.

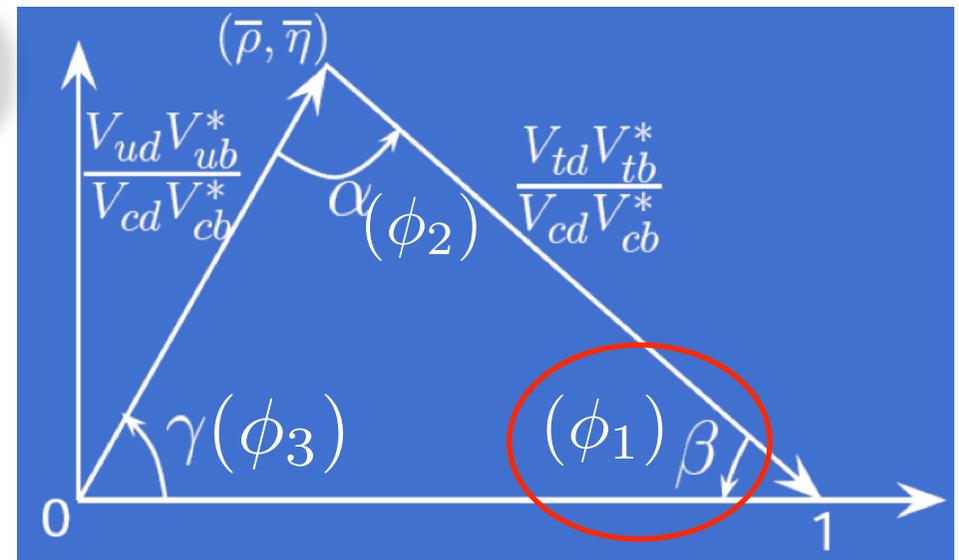


$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

- Unitarity:

$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$

- Measure sides and angles in multiple ways to constrain the CKM matrix and search for possible inconsistency, which might indicate new physics.



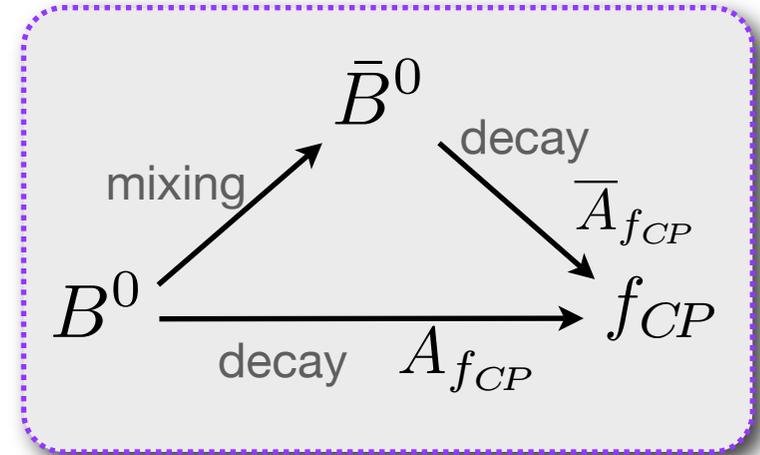
Sin2β (Sin2φ₁) in time-dependent CP asymmetry

- A B⁰ meson can mix with its antiparticle before decay.
- Interference is parameterized by

$$\lambda = \frac{q}{p} \cdot \frac{\bar{A}}{A}$$

phase factor due to mixing

decay amplitude ratio



$$\lambda_{f_{CP}} \neq \pm 1 \Rightarrow \text{Prob}(\bar{B}_{\text{phys}}^0(t) \rightarrow f_{CP}) \neq \text{Prob}(B_{\text{phys}}^0(t) \rightarrow f_{CP})$$

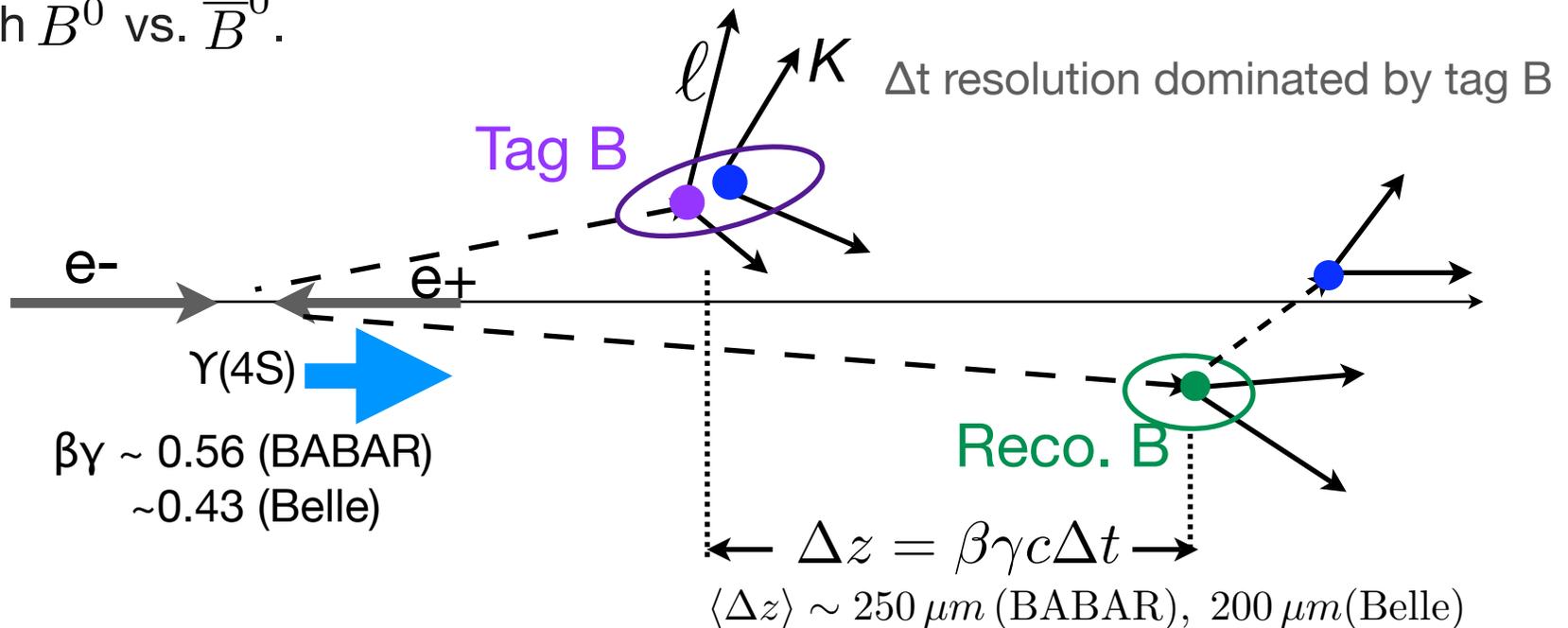
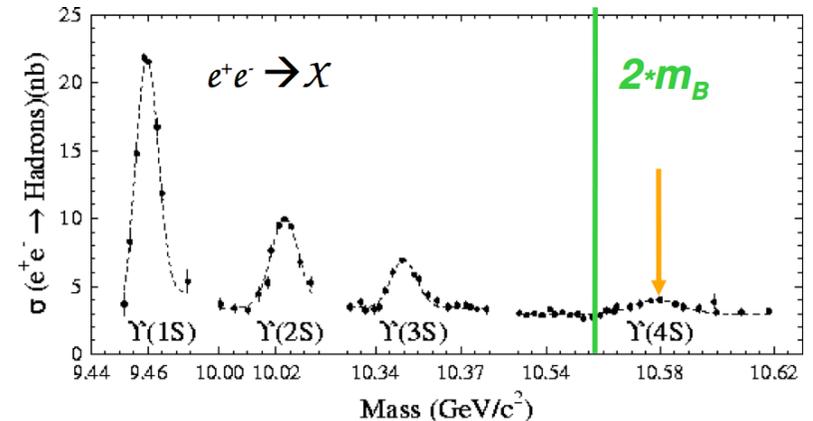
$$A_{CP} = \frac{\Gamma(\bar{B}_{\text{phys}}^0(t) \rightarrow f_{CP}) - \Gamma(B_{\text{phys}}^0(t) \rightarrow f_{CP})}{\Gamma(\bar{B}_{\text{phys}}^0(t) \rightarrow f_{CP}) + \Gamma(B_{\text{phys}}^0(t) \rightarrow f_{CP})} = S \cdot \sin(\Delta m_d t) - C \cdot \cos(\Delta m_d t)$$

$$S = \frac{2 \text{Im } \lambda}{1 + |\lambda|^2} \quad C = \frac{1 - |\lambda|^2}{1 + |\lambda|^2}$$

- For modes in this talk, Standard Model expects S = ±sin2β (sin2φ₁), C=0.

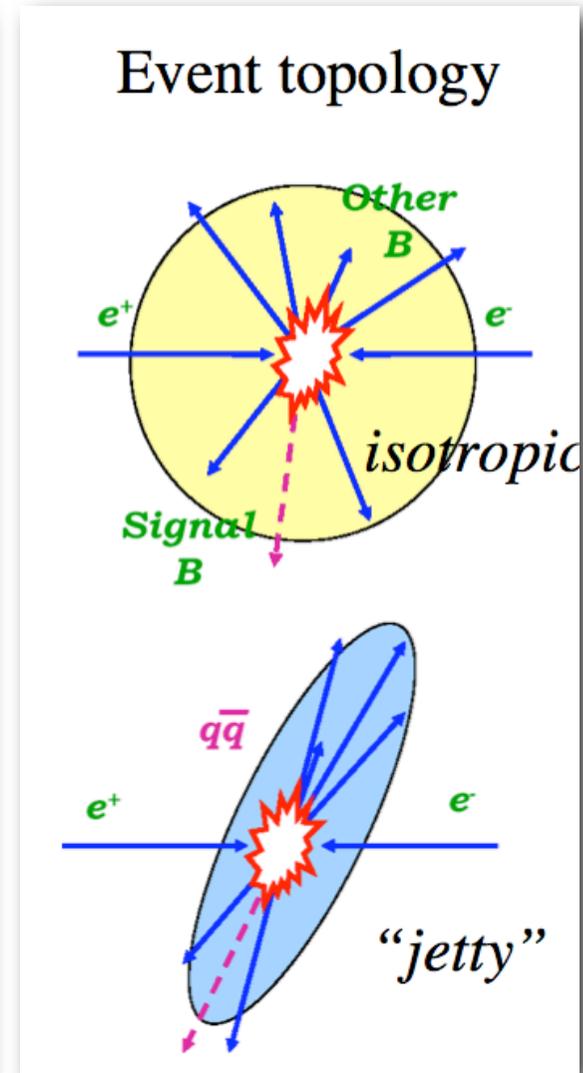
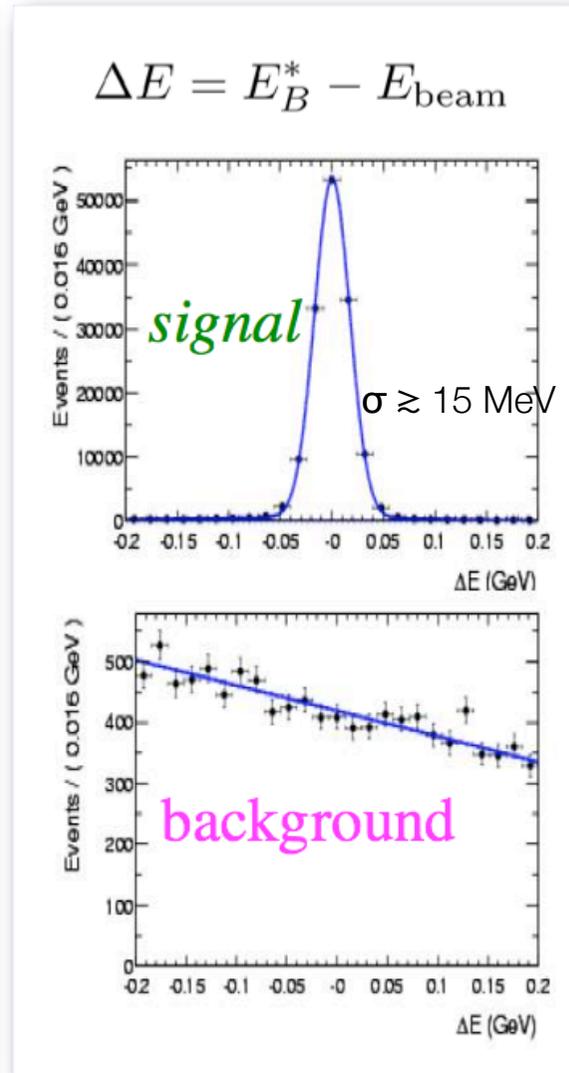
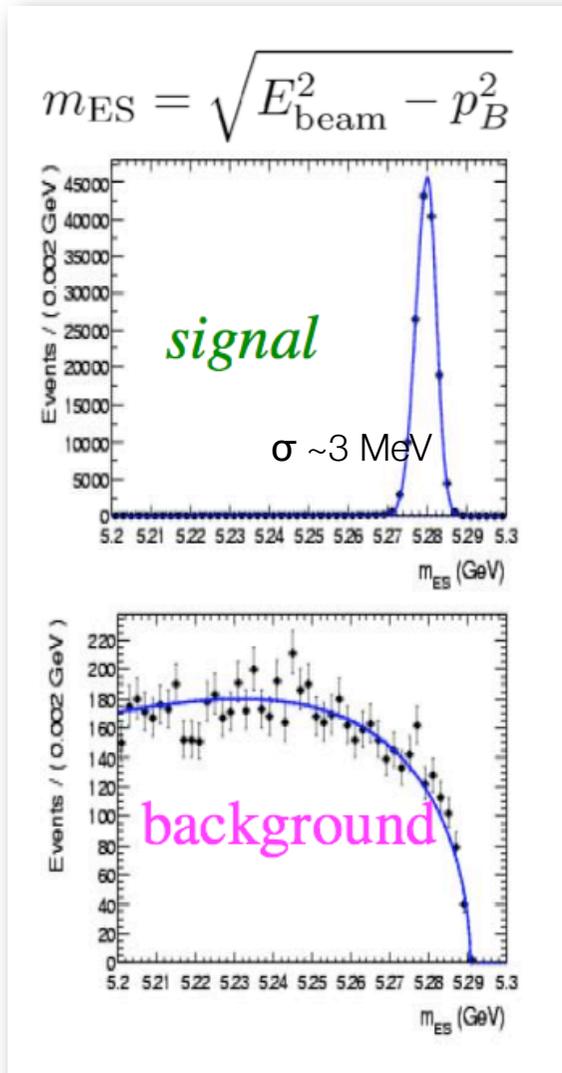
Measure time-dependent \mathcal{CP} at B-factories

- $\Upsilon(4S)$ resonance is just over $B\bar{B}$ threshold and decays to $B\bar{B}$ coherently.
- Center-of-mass is boosted to separate the two B decay vertices.
- One B, decaying to $f_{\mathcal{CP}}$, is fully reconstructed.
- Decay products of the other B allow us to distinguish B^0 vs. \bar{B}^0 .



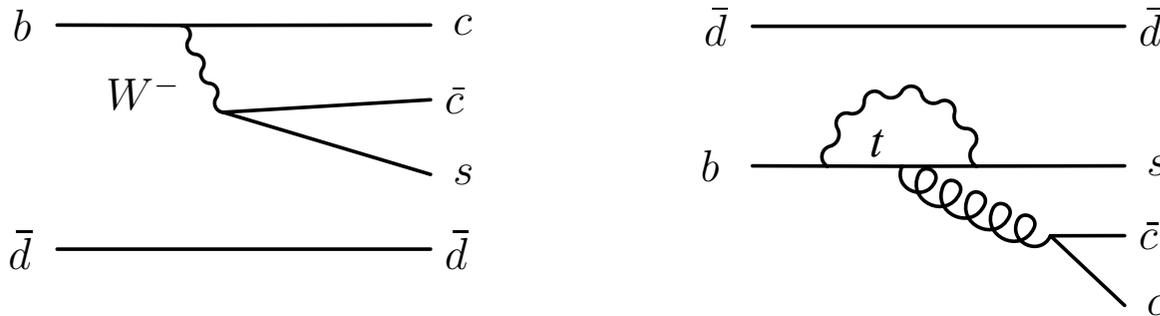
How to find a B meson

- Typical variables used to isolate $\Upsilon(4S) \rightarrow B\bar{B}$ events:



Golden modes: $B^0 \rightarrow (c\bar{c})K_S$

- Tree diagram dominates. Dominant penguin diagram has the same weak phase.



- Small SM theoretical correction/uncertainty on $\sin 2\beta_{\text{eff}}$:

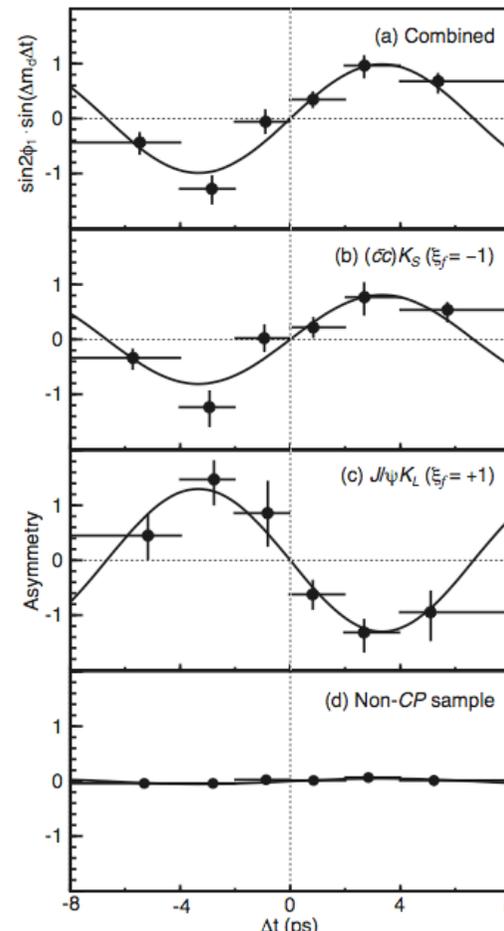
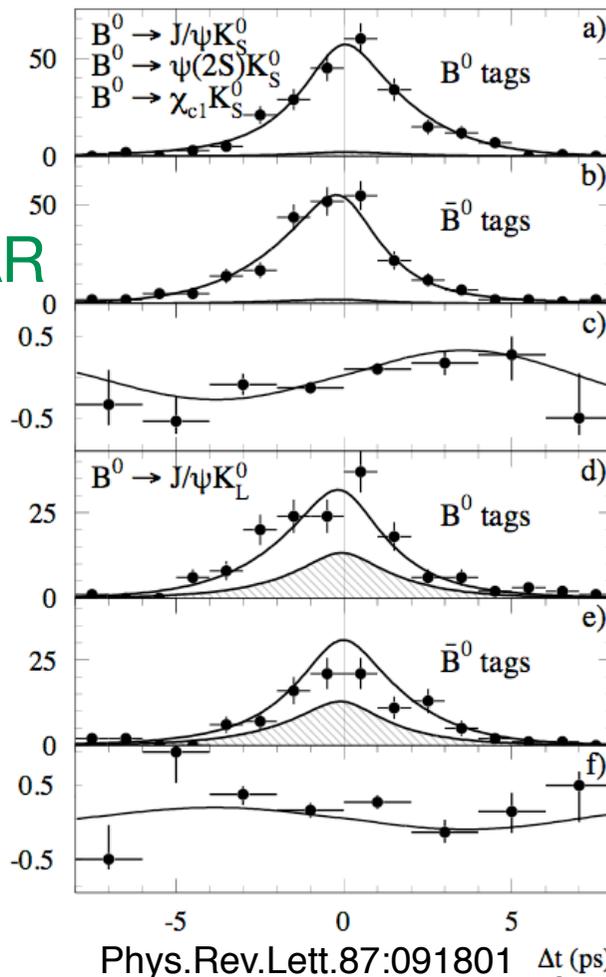
Boos et al, PRD 70, 036006 (2004)	$-(2.2 \pm 2.2) \times 10^{-4}$
Li, Mishima, hep-ph/0610120	$(9.3_{-5}^{+4}) \times 10^{-4}$
Ciuchini et al, PRL 95, 221804 (2005)	0 ± 0.012

- Relatively large branching fraction, $\sim O(10e-4)$.
- Clean final states, e.g., $B^0 \rightarrow J/\psi K_S$, $J/\psi \rightarrow \ell^+ \ell^-$, $K_S \rightarrow \pi^+ \pi^-$

CP in B established at each B factory in 2001 using golden modes

- Each experiment used ~ 32 million $\Upsilon(4S) \rightarrow B\bar{B}$ decays, obtaining ~ 1000 signal events, and established time-dependent CP violation in neutral B meson decays.

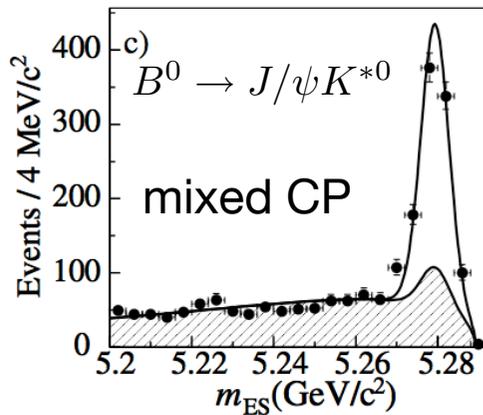
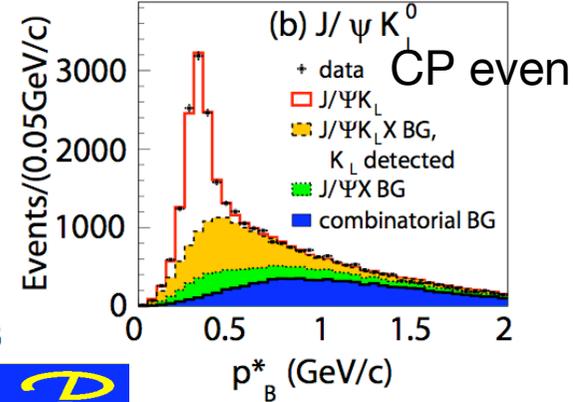
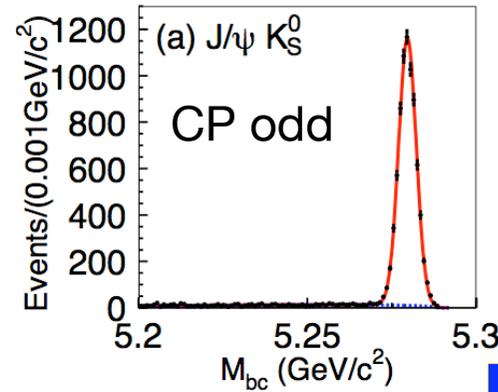
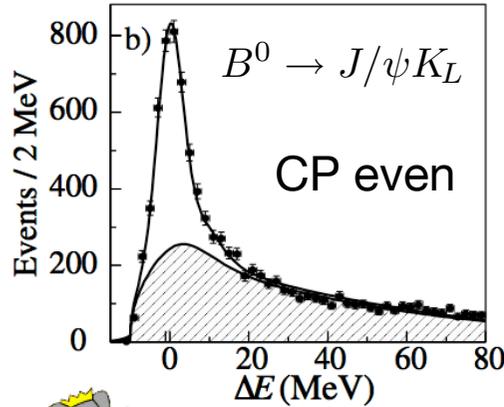
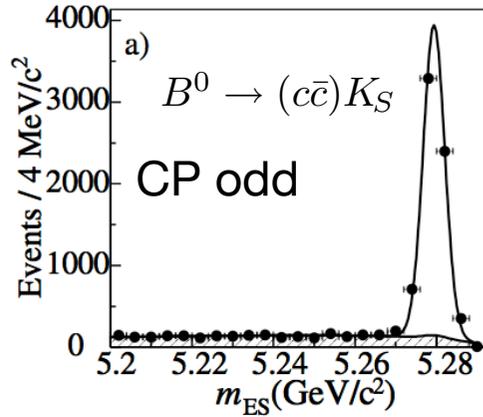
BABAR



Phys.Rev.Lett.87:091802



Today, more than 10 times more data later



$383 \times 10^6 B\bar{B}$



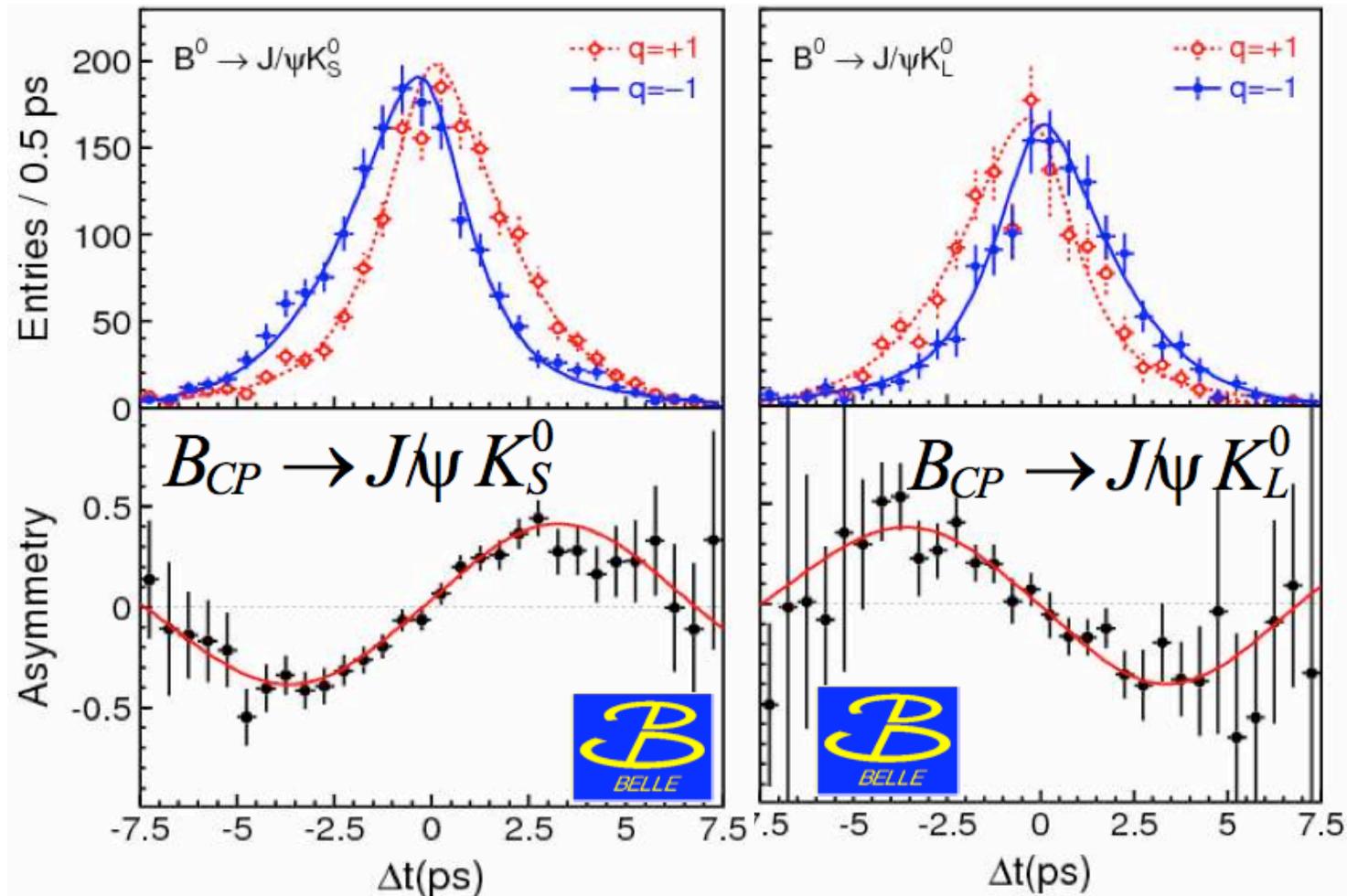
$535 \times 10^6 B\bar{B}$

N signal (purity)	CP Odd	CP even
BABAR	6900 (92%)	3700 (55%)
Belle	7482 (97%)	6512 (59%)

Belle results for $J/\psi K_S$ and $J/\psi K_L$



$535 \times 10^6 B\bar{B}$

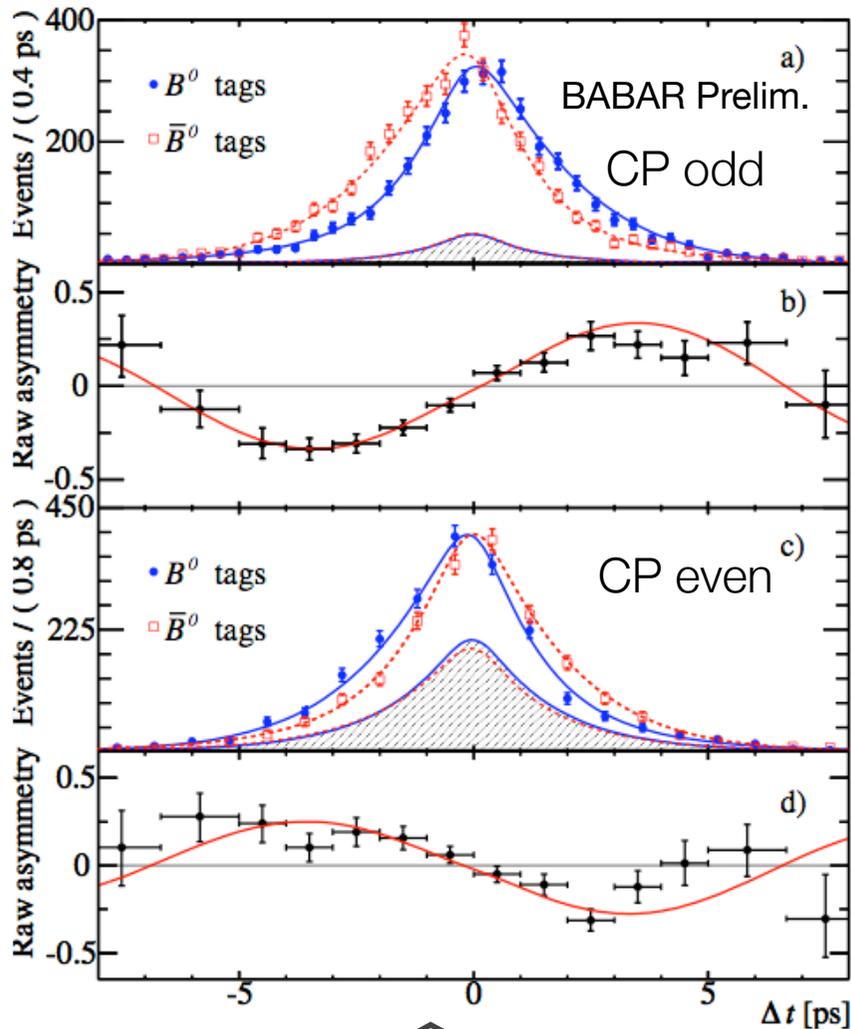


- PRL 98, 031802 (2007) $\sin 2\beta_{\text{eff}} = +0.642 \pm 0.031 \pm 0.017$
 $C = -0.018 \pm 0.021 \pm 0.014$

BABAR results: $\sin 2\beta$ for individual decay modes



$383 \times 10^6 B\bar{B}$



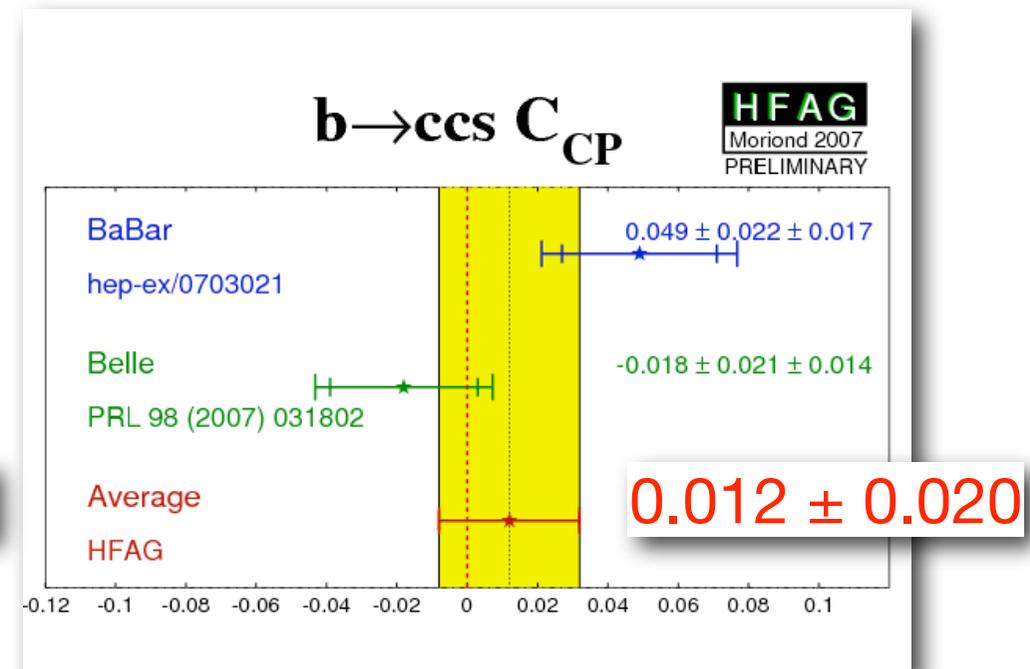
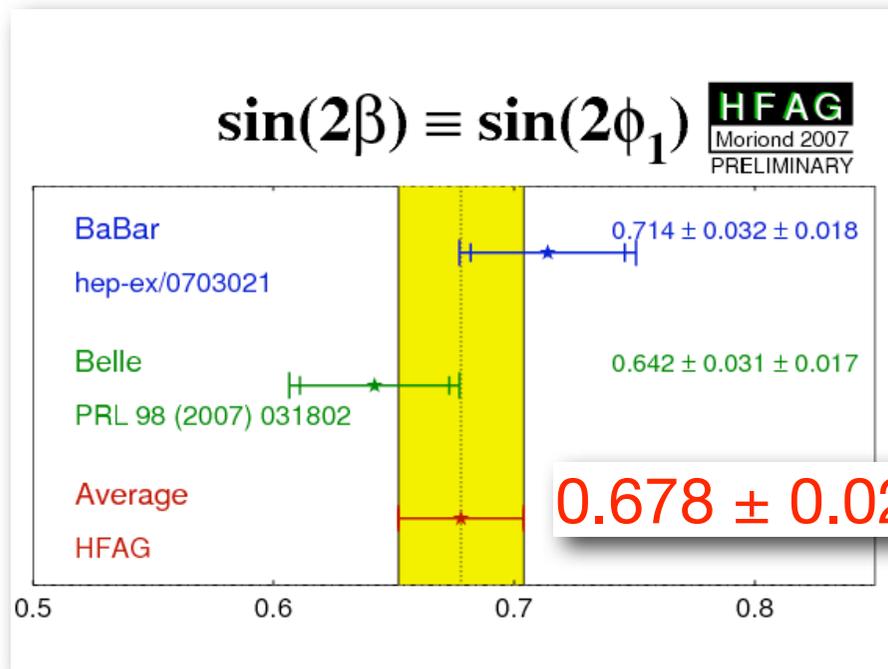
↑
All modes combined

$J/\psi K_S (\pi^+\pi^-)$	$0.702 \pm 0.042 \pm 0.020$
$J/\psi K_S (\pi^0\pi^0)$	$0.617 \pm 0.103 \pm 0.036$
$\psi(2S)K_S$	$0.947 \pm 0.112 \pm 0.062$
$\chi_{c1} K_S$	$0.759 \pm 0.170 \pm 0.037$
$\eta_c K_S$	$0.778 \pm 0.195 \pm 0.093$
$J/\psi K^{*\pm}$	$0.477 \pm 0.271 \pm 0.155$
<hr/>	
$J/\psi K_S$	$0.686 \pm 0.039 \pm 0.015$
$J/\psi K_L$	$0.735 \pm 0.074 \pm 0.067$
$J/\psi K^0$	$0.697 \pm 0.035 \pm 0.016$
All	$0.714 \pm 0.032 \pm 0.018$

↑
systematic

- hep-ex/0703021, submitted to PRL

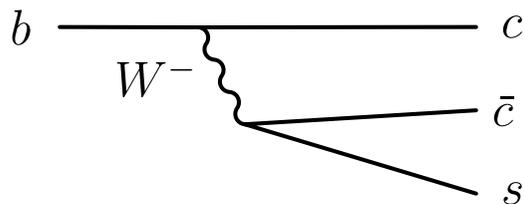
Summary of $\sin 2\beta$ measurements from $(c\bar{c})K^0$



- Two experiments agree very well.
- Experimental uncertainty on $\sin 2\beta \sim 4\%$.
- Small theoretical uncertainty in the Standard Model.

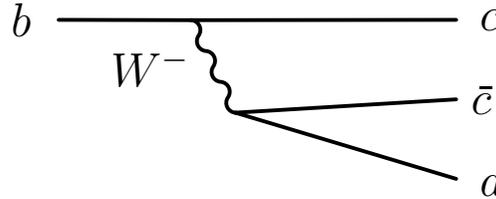
Many ways to measure $\sin 2\beta$

- $b \rightarrow c\bar{c}s$
charmonium



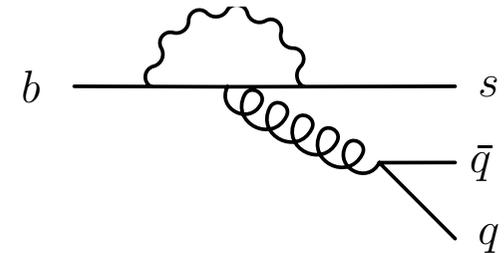
$J/\psi K_S, \psi(2S)K_S, \chi_{c1}K_S$
 $\eta_c K_S, J/\psi K_L$
 $J/\psi K^{*0} (K_S \pi^0)$

- $b \rightarrow c\bar{c}d$
charm or
charmonium

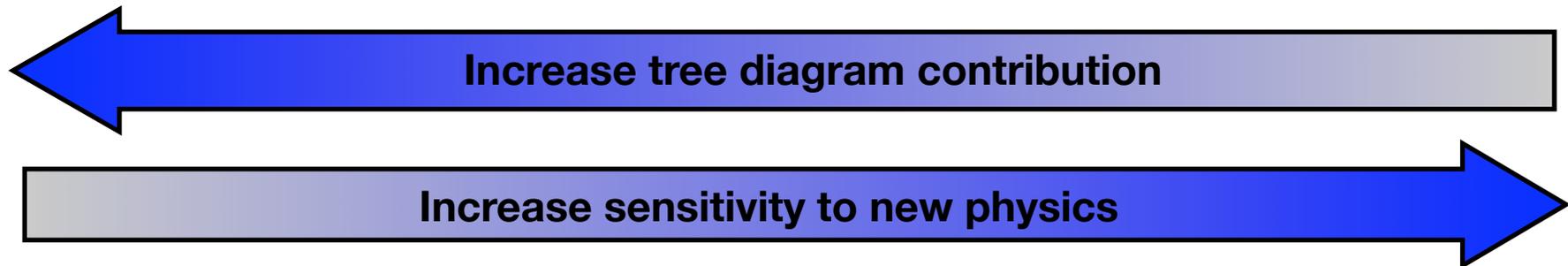


$D^{(*)+} D^{(*)-}, J/\psi \pi^0$

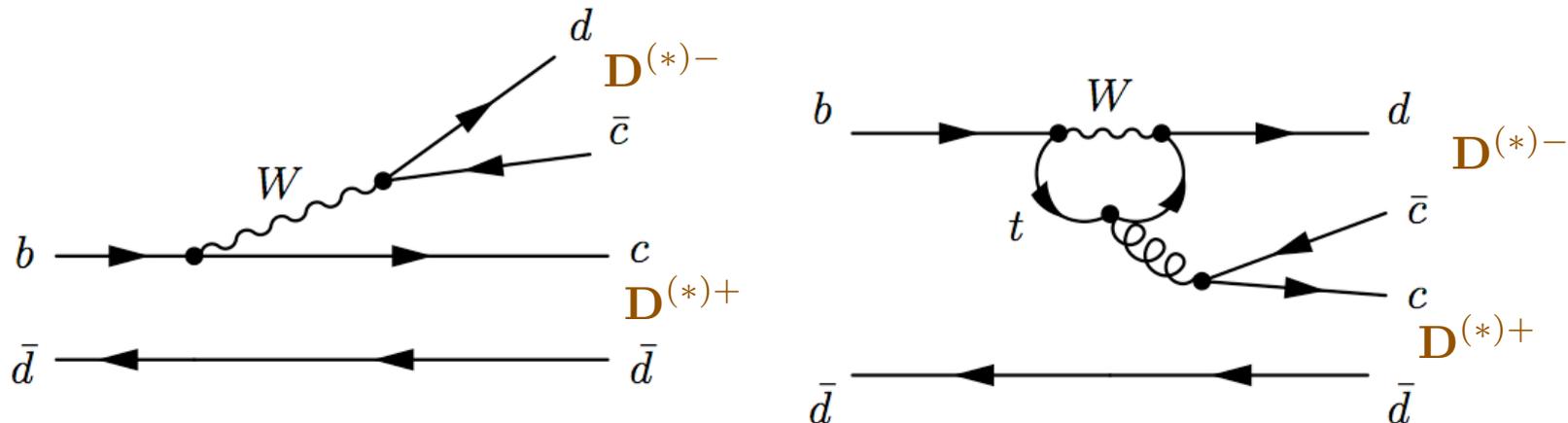
- $b \rightarrow ss\bar{s}, sdd\bar{d}$
penguin-dominated



$\phi K_S, K^+ K^- K^0,$
 $K_S K_S K_S, \eta' K_S, K_S \pi^0,$
 $\omega K_S, f_0 K_S$

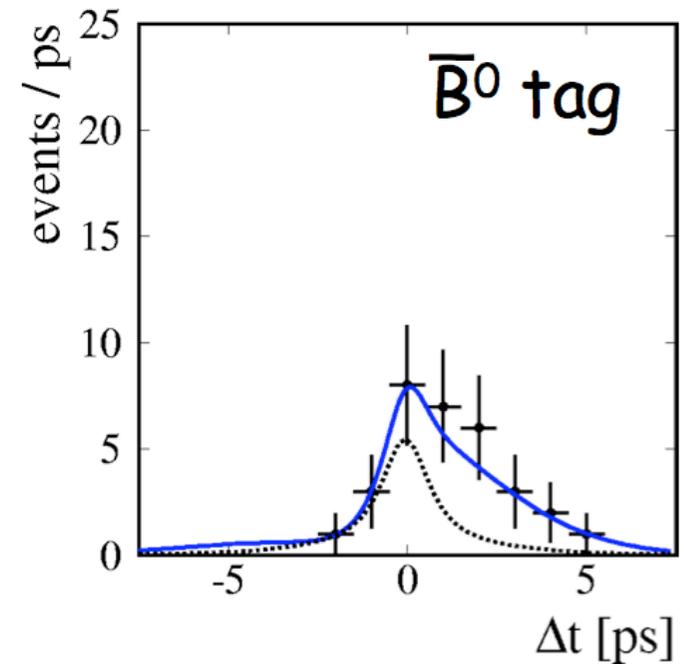
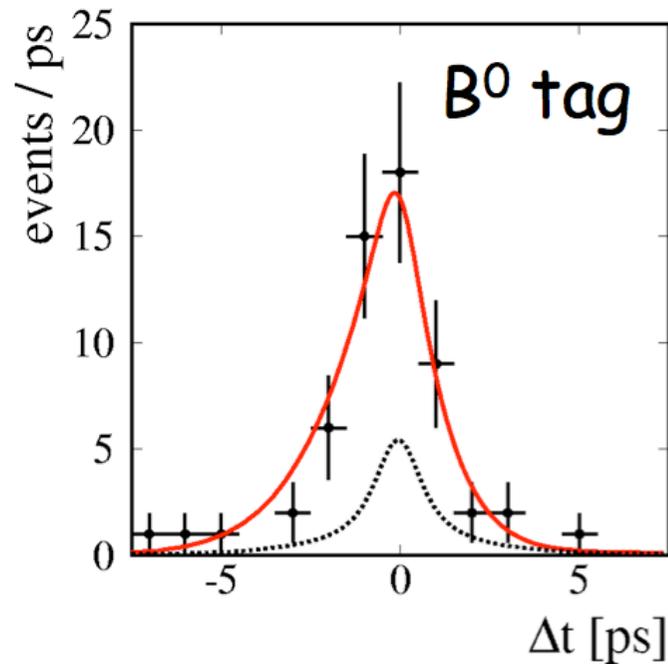
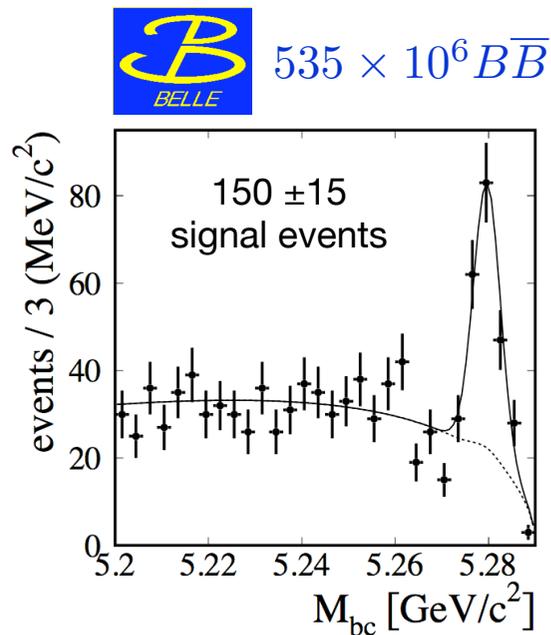


CP in $b \rightarrow c\bar{c}d$ decays: $B^0 \rightarrow D^{(*)} D^{(*)}$



- D^+D^- is a CP eigenstate. $D^{*+}D^{*-}$ is a mixture of CP even and odd state (angular analysis is needed). $D^{*+}D^{\mp}$ are not CP eigenstates. But the S's are closely related to $\sin 2\beta$.
- $C=0$, $S \simeq -\sin 2\beta$ in the Standard Model.
- Penguin contribution is expected to be small
 - ▶ 2--10% correction [Xing PRD 61, 014010 (2000)]
- Sensitive to new physics in the loop.

Belle's evidence of large direct \mathcal{CP} in $B^0 \rightarrow D^+ D^-$



$$\mathcal{S} = -1.13 \pm 0.37 \pm 0.09$$

$$\mathcal{A} = +0.91 \pm 0.23 \pm 0.06 \quad (= -\mathcal{C})$$

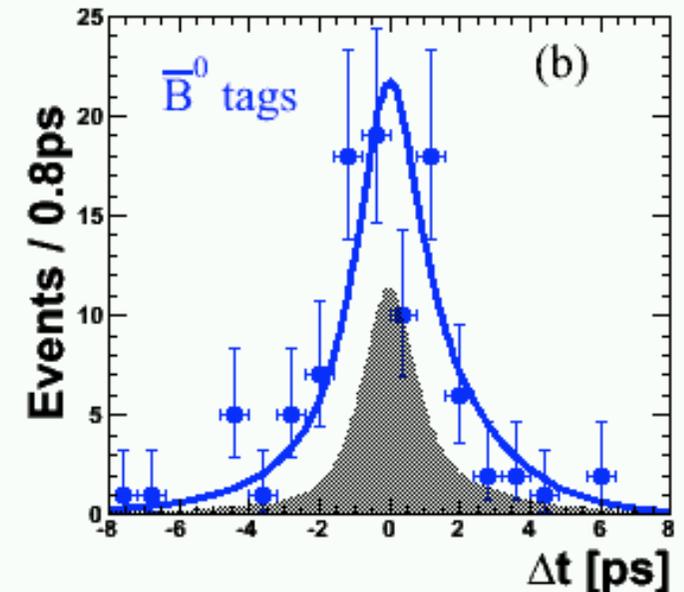
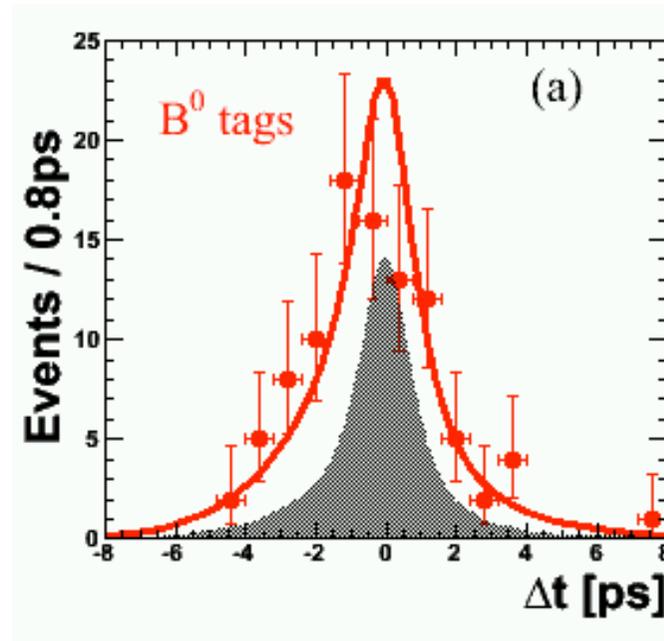
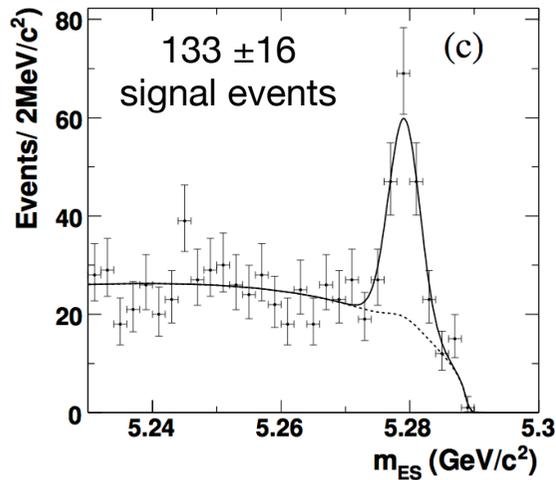
- $\mathcal{S} = \mathcal{A} = 0$ is excluded at 4.1σ level.
- Direct CPV at 3.2σ level.

[hep-ex/0702031, submitted to PRL]

BABAR does *not* confirm the large \mathcal{CP} observed by Belle in $B^0 \rightarrow D^+ D^-$



$383 \times 10^6 B\bar{B}$



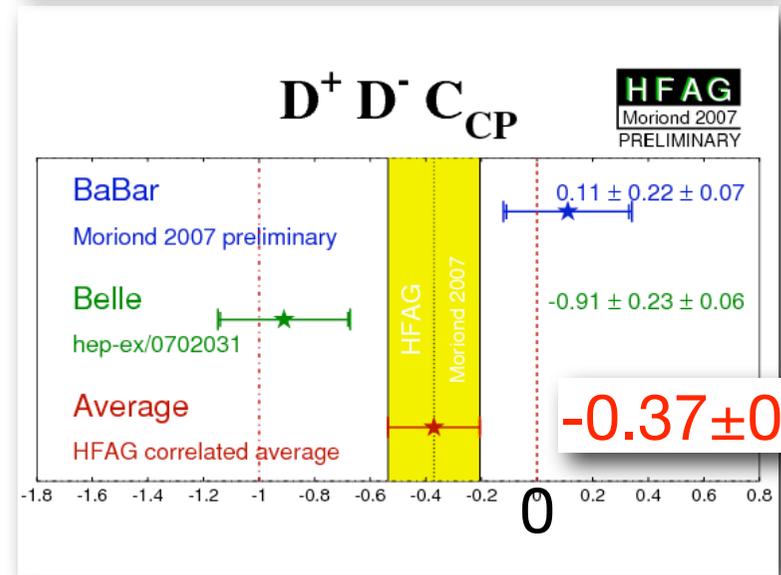
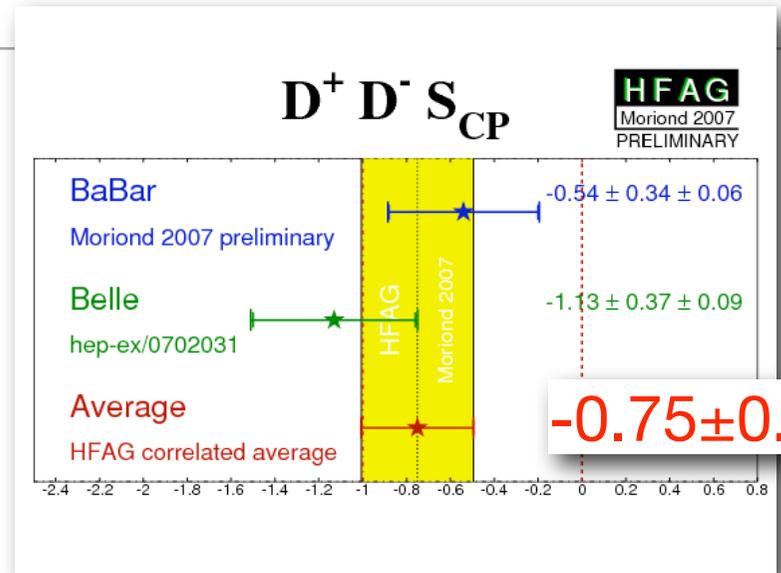
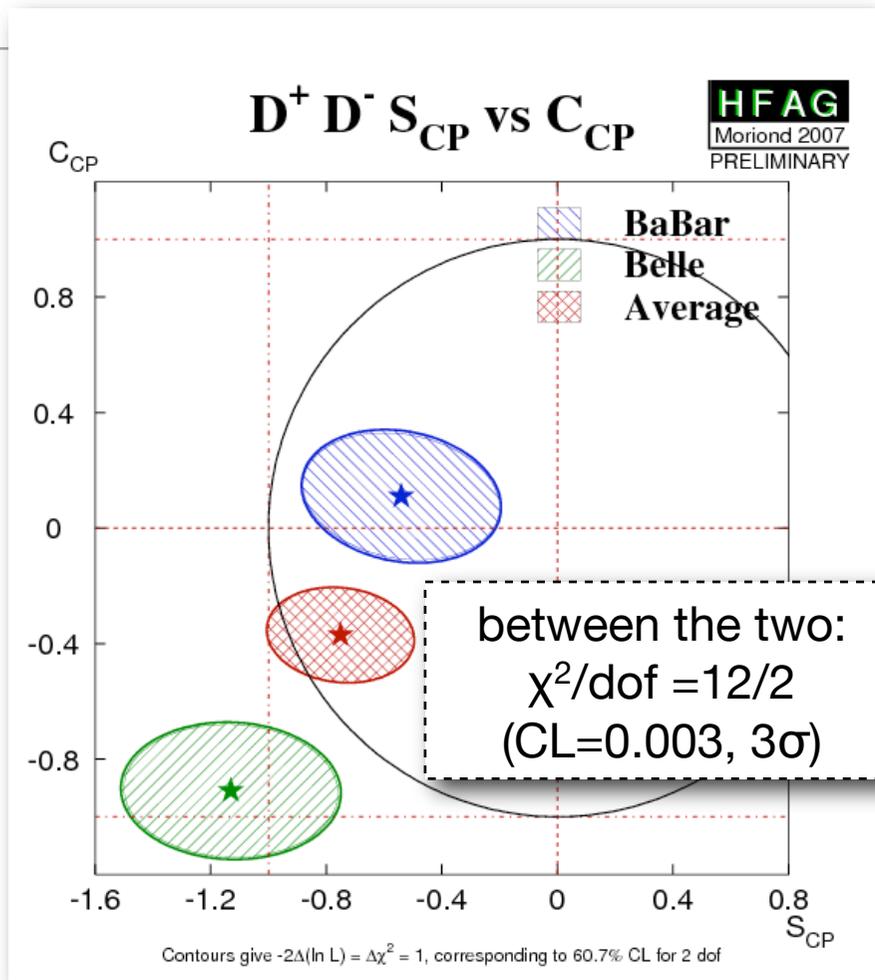
$$S = -0.54 \pm 0.34 \pm 0.06$$

$$C = +0.11 \pm 0.22 \pm 0.07$$

- Consistent with the SM expectation.

[arXiv:0705.1190v1 [hep-ex]
submitted to PRL]

Comparison between *BABAR* and Belle's $B^0 \rightarrow D^+ D^-$ result



- Handle average with care due to possible non-gaussian tails.

Evidence of CPV in $B^0 \rightarrow D^{*\pm} D^{\mp}$



$152 \times 10^6 B\bar{B}$
[PRL 93, 201802 (2004)]



$383 \times 10^6 B\bar{B}$
[hep-ex/0705xxx]

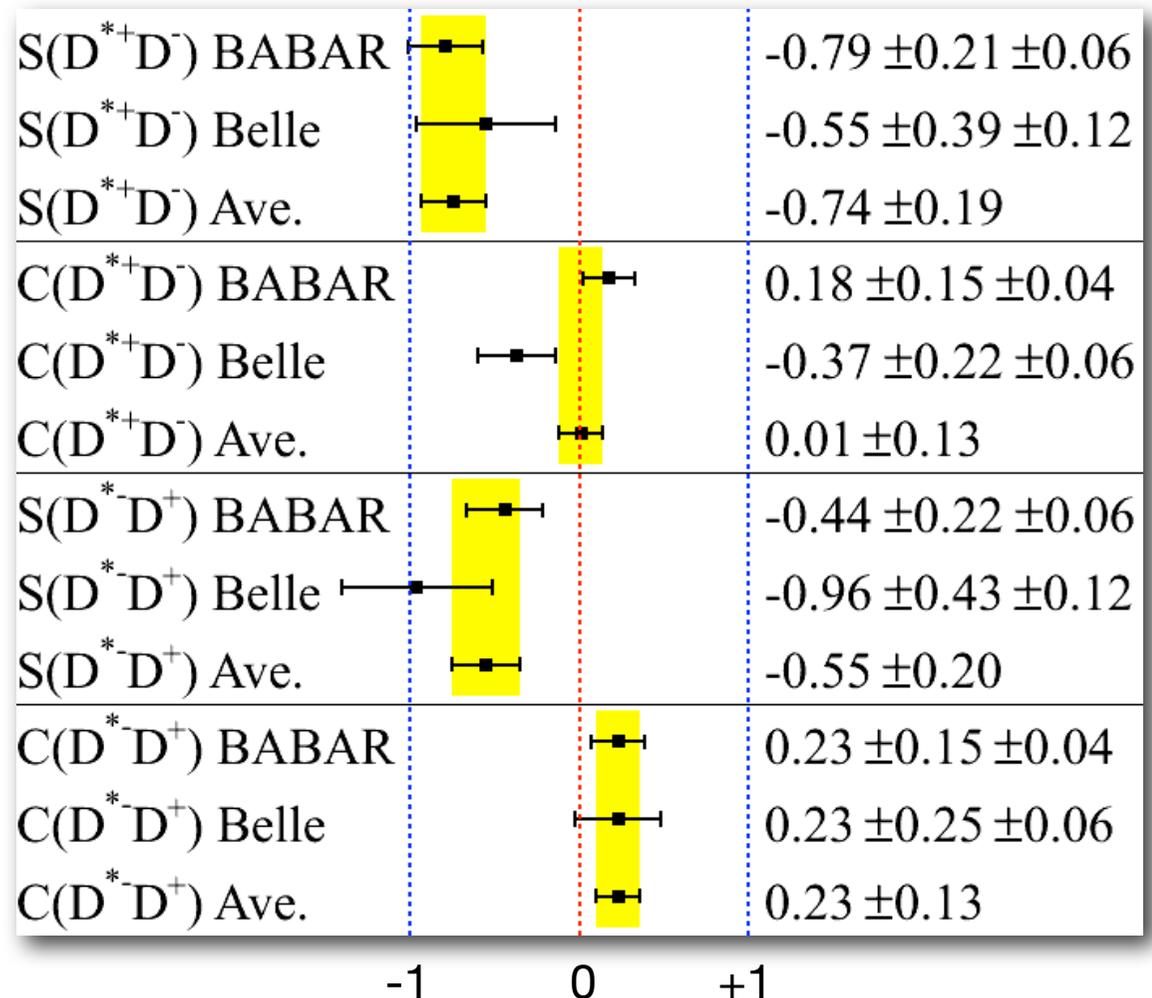
- $D^{*\pm}D^{\mp}$ is not a CP eigenstate.
- Analyze $D^{*+}D^-$ and $D^{*-}D^+$ modes separately.

$$\frac{A(D^{*+}D^-)}{A(D^{*-}D^+)} = Re^{i\delta}$$

$$S_{\pm} = \frac{2R \sin(2\beta \pm \delta)}{1 + R^2}$$

$$(S_+ + S_-)/2 = \frac{2R}{1+R^2} \cos \delta \sin 2\beta$$

- If no CPV (and no penguin),
 $S_+ = -S_-$, $C_+ = -C_-$.
- $\cos \delta \sin 2\beta \neq 0$ at $\sim 4\sigma$ level.



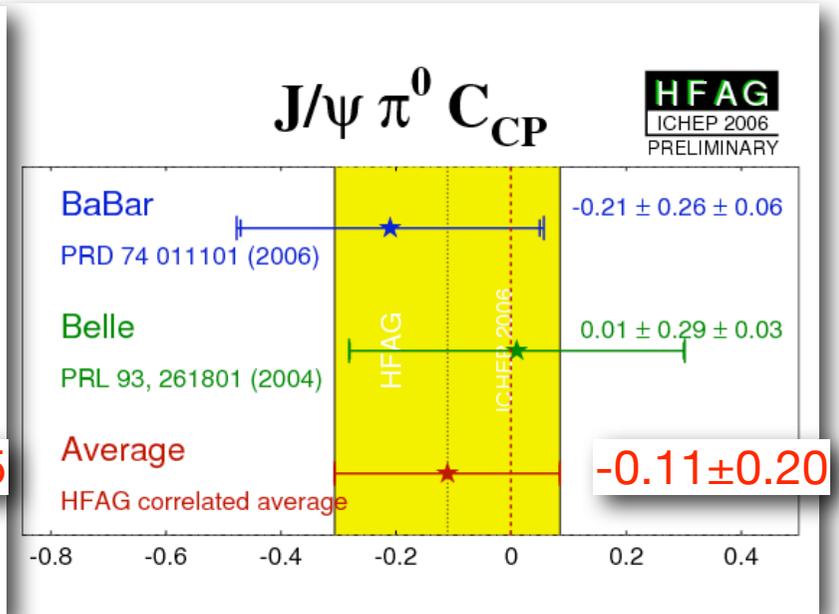
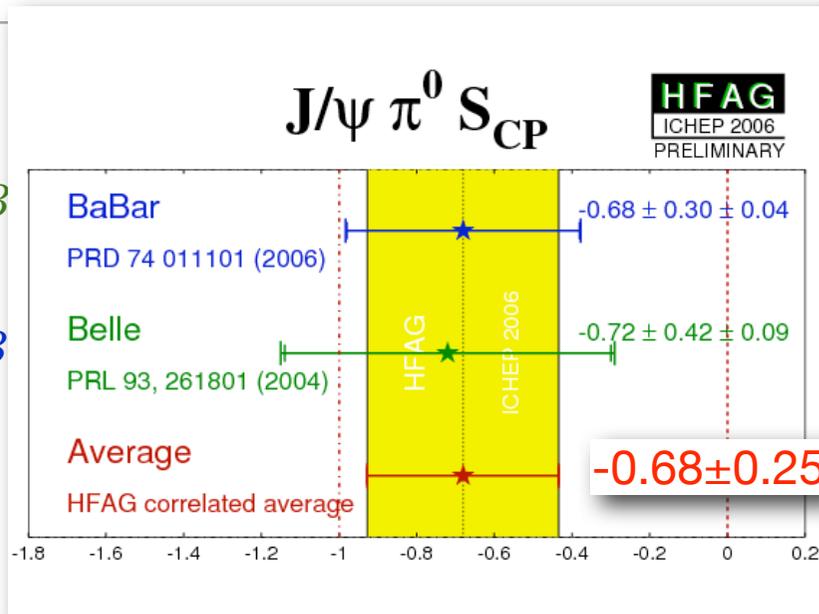
CP in $b \rightarrow c\bar{c}d$ decay: $B^0 \rightarrow J/\psi \pi^0$



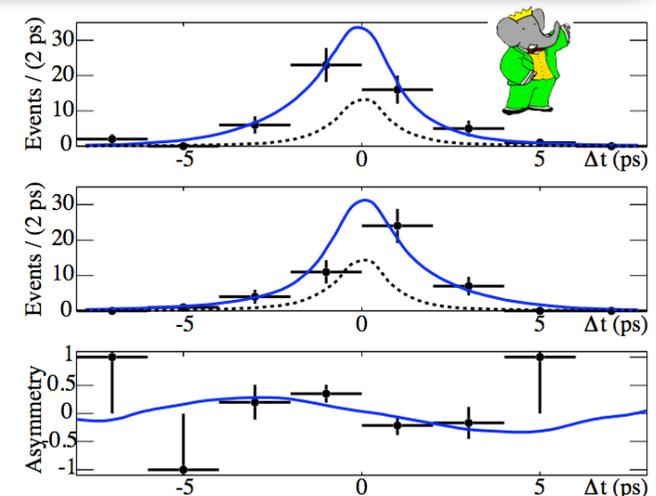
$232 \times 10^6 B$



$152 \times 10^6 B$



- Same tree and penguin diagrams as golden modes except the s quark is replaced by d. But the penguin with a different weak phase can have a more significant contribution than in golden modes.
- Can be used to constrain the penguin pollution in the golden mode in a model-independent way. [Ciuchini et al., PRL 95, 221804 (2005)]

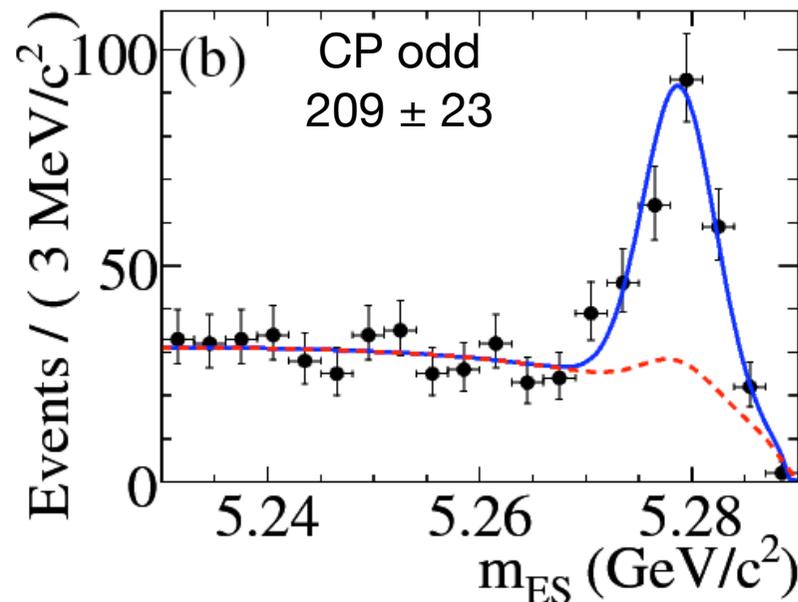
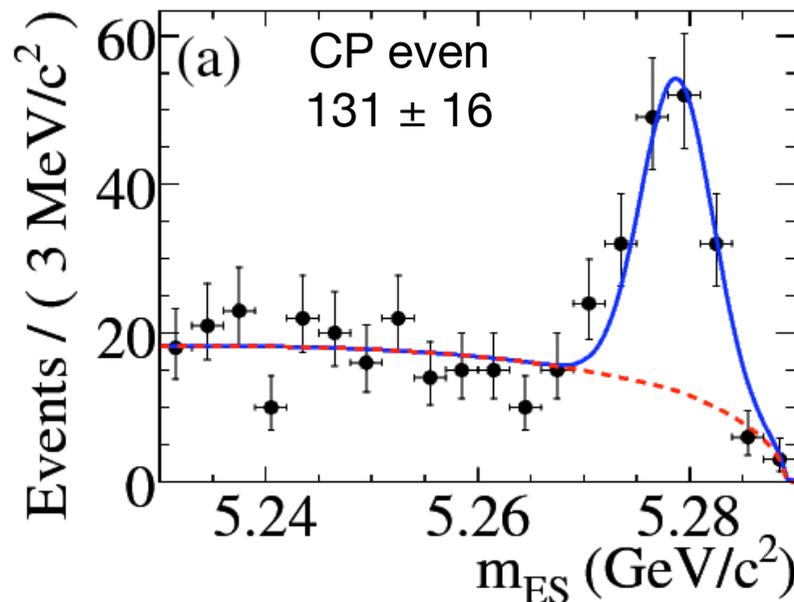
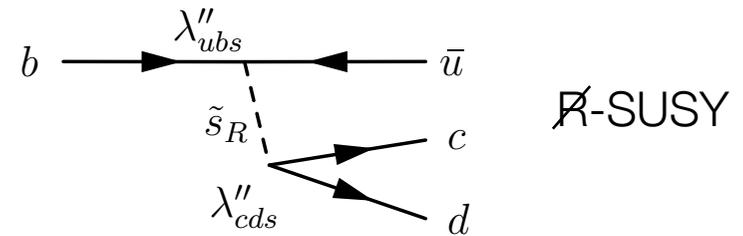
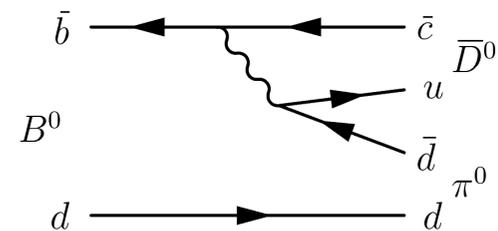


New BABAR result: $B^0 \rightarrow D^{(*)0} h^0$ using $D^0 \rightarrow K^+ K^-, K_S \omega, K_S \pi^0$

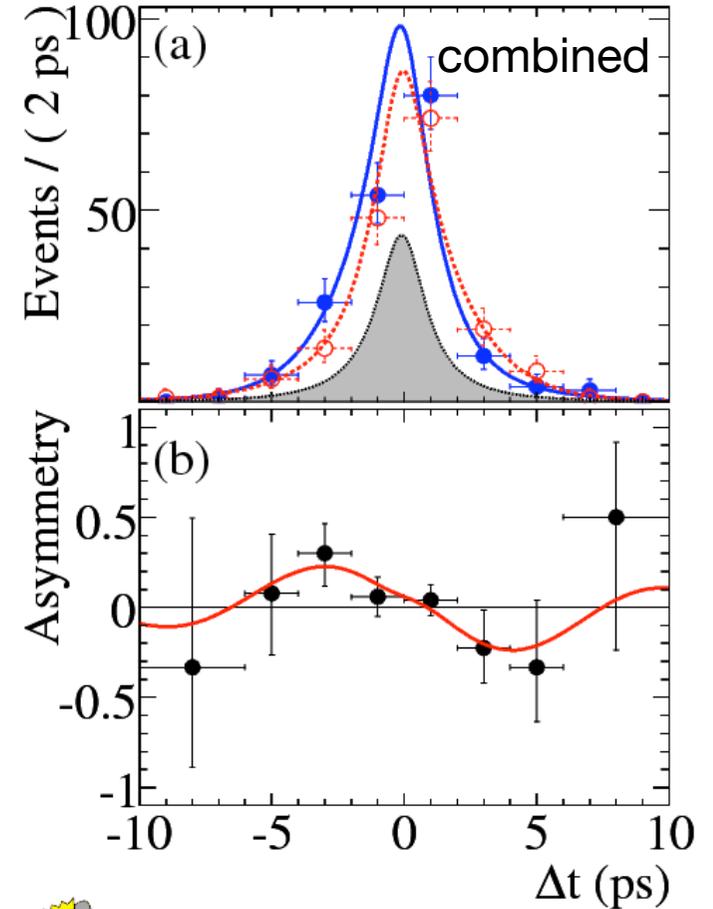
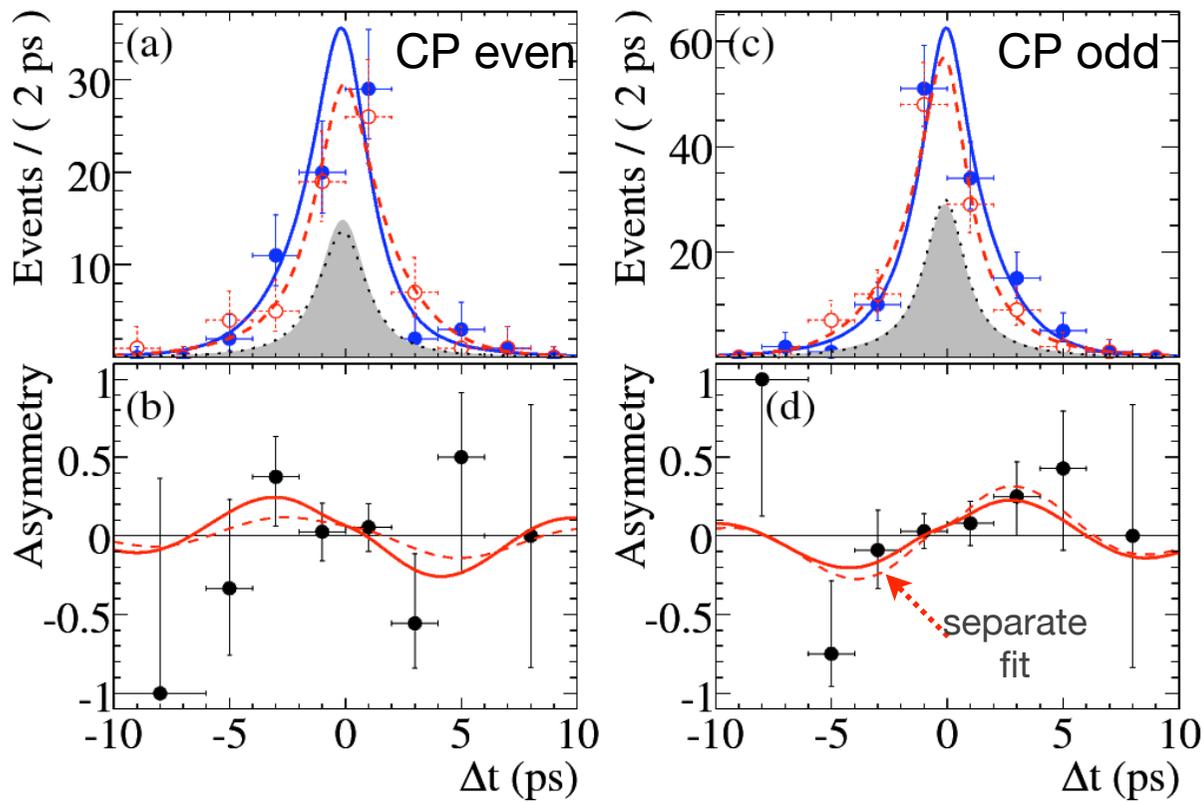


$383 \times 10^6 B\bar{B}$

- Color-suppressed tree diagram.
- Doubly-Cabbibo suppressed (tree) amplitude has small effect: $\Delta S \lesssim 0.05$.
- No penguin diagrams \Rightarrow sensitive to different kind of new physics.



$\sin 2\beta$ in $B^0 \rightarrow D^{(*)0} h^0$



$$\sin 2\beta_{\text{eff}} = +0.56 \pm 0.23 \pm 0.05$$

$$C = -0.23 \pm 0.16 \pm 0.04$$



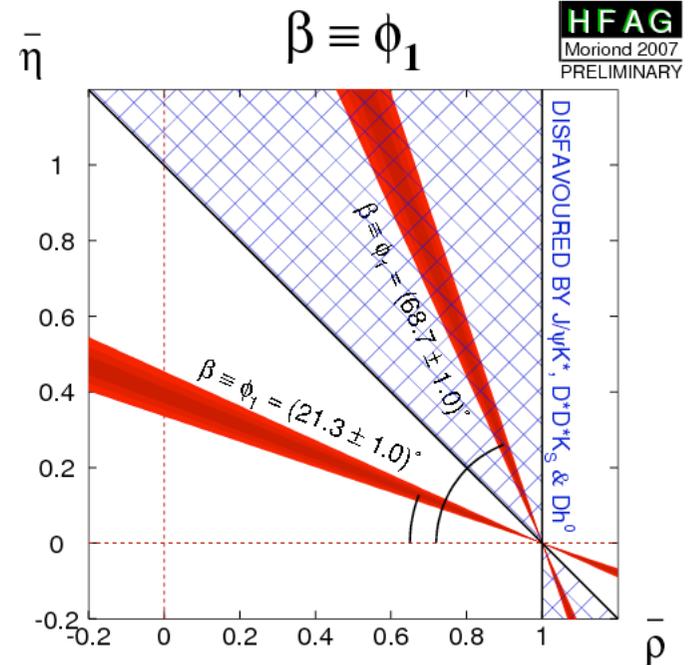
[hep-ex/0703019,
submitted to PRL]

- 2.3σ from CP conservation.

Compared with $S=C=0$: $\sqrt{2\Delta \ln \mathcal{L}} = 2.80$, $\Rightarrow p=0.0198$ for dof=2.
equivalent to 2.3σ for dof=1.

Resolve ambiguity in β

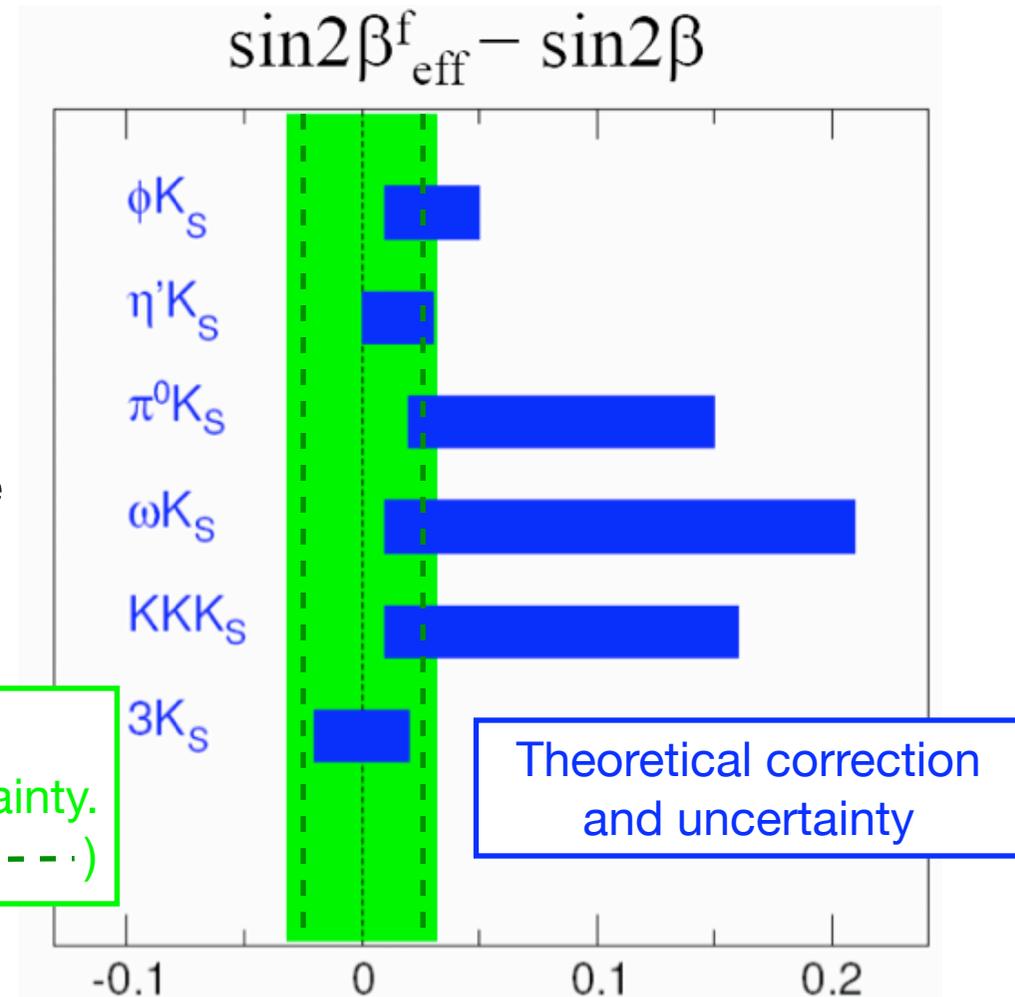
- Measuring $\sin 2\beta$ resulting in 4-fold ambiguity in β .
- Can be reduced to 2-fold by measuring (the sign of) $\cos 2\beta$. Negative $\cos 2\beta$ is ruled out by:
 - ▶ $B^0 \rightarrow J/\psi K\pi$: Interference between CP even and odd; resolve strong phase using $K\pi$ S- and P-wave.
 - ▶ BABAR [PRD 71, 032005 (2005)]
 - ▶ Belle [PRL 95, 091601 (2005)]
 - ▶ $B^0 \rightarrow D^0[K_S\pi^+\pi^-] h^0$: Time-dependent Dalitz analysis
 - ▶ Belle [PRL 97, 081801 (2006)] 98.3% CL
 - ▶ BABAR [hep-ex/0607105] 87% CL.
 - ▶ $B^0 \rightarrow D^*D^*K_S$: Time-dependent Dalitz analysis
 - ▶ BABAR [PRD 74, 091101] 94% CL.
 - ▶ $B^0 \rightarrow K^+K^-K^0$: Time-dependent Dalitz analysis
 - ★ 21° is favored over 69° at 4.6σ level. (detail later)



$\sin 2\beta$ in $b \rightarrow s$ penguin dominated modes

- Different charmless modes have different Standard Model corrections and uncertainties.
 - ▶ Considering, e.g., Cabibbo-suppressed trees, final state interaction long distance effect.
- Significant deviation from golden mode $\sin 2\beta$ would indicate new physics.

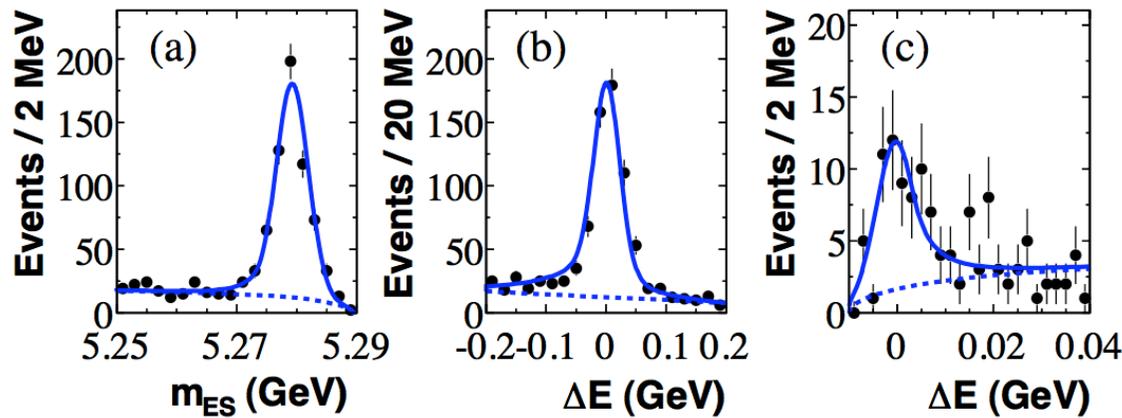
Golden mode
experimental uncertainty.
(Updated range - - - - .)



Beneke, PLB 620, 143 (2005)
Mishima, Sanda, PRD 72, 114005 (2005)
Williamson, Zupan, PRD 74, 014003 (2006)
Cheng, Chua, Soni, PRD, 014006 (2005)

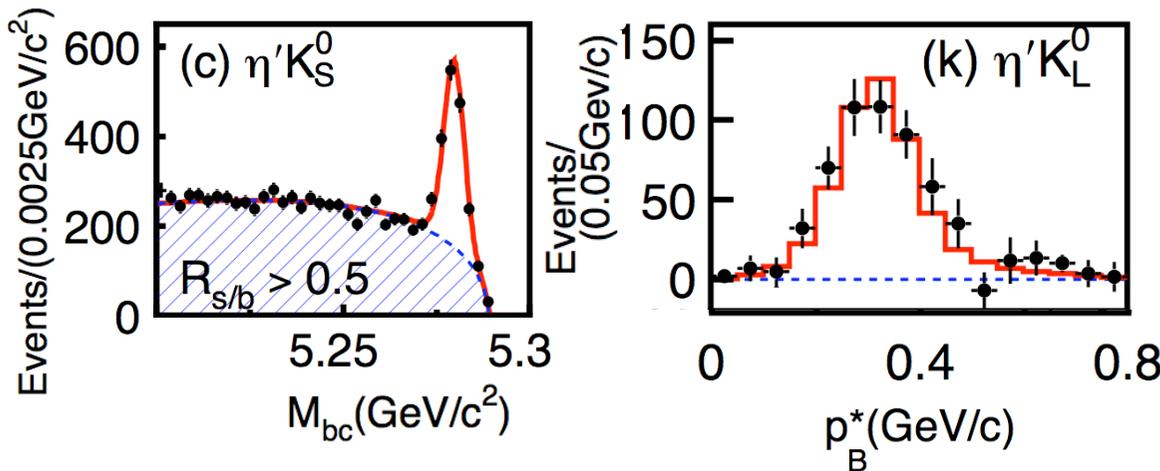
“Golden” charmless mode: $B^0 \rightarrow \eta' K^0$

- Small SM uncertainty, relatively large yield.



$383 \times 10^6 B\bar{B}$

~1050 $\eta' K_S$ events
~250 $\eta' K_L$ events



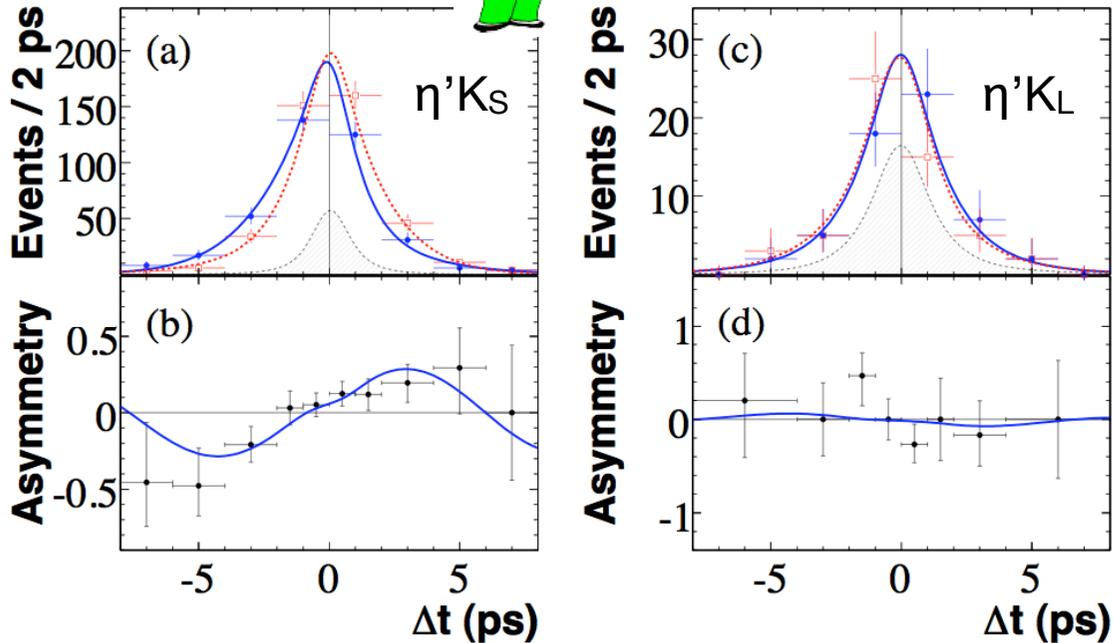
$535 \times 10^6 B\bar{B}$

~1420 $\eta' K_S$ events
~450 $\eta' K_L$ events

~~CP~~ established in charmless mode



$383 \times 10^6 B\bar{B}$



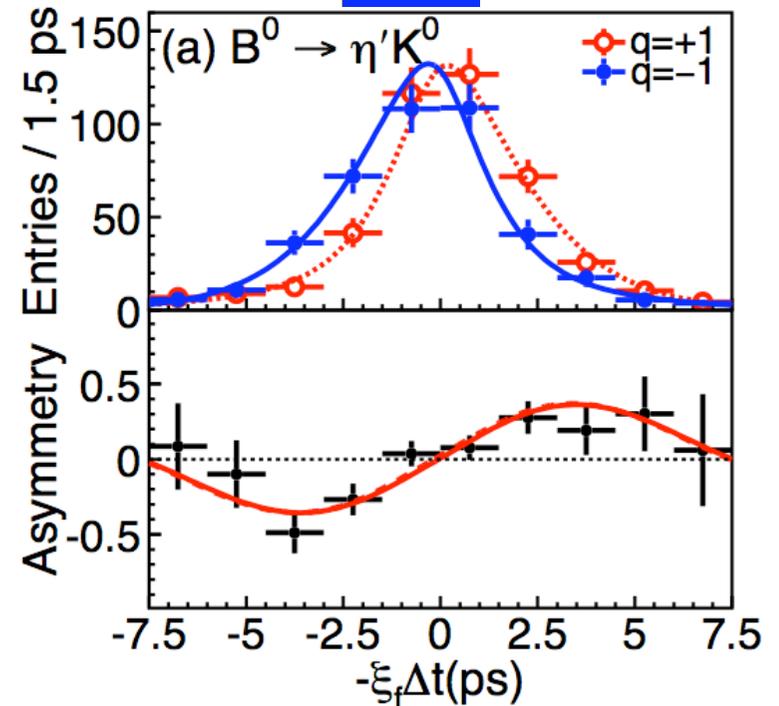
$$\sin 2\beta_{\text{eff}} = +0.58 \pm 0.10 \pm 0.03$$

$$C = -0.16 \pm 0.07 \pm 0.03$$

[PRL98, 031801 (2007)]



$535 \times 10^6 B\bar{B}$



$$\sin 2\beta_{\text{eff}} = +0.64 \pm 0.10 \pm 0.04$$

$$C = +0.01 \pm 0.07 \pm 0.05$$

[PRL98, 031802 (2007)]

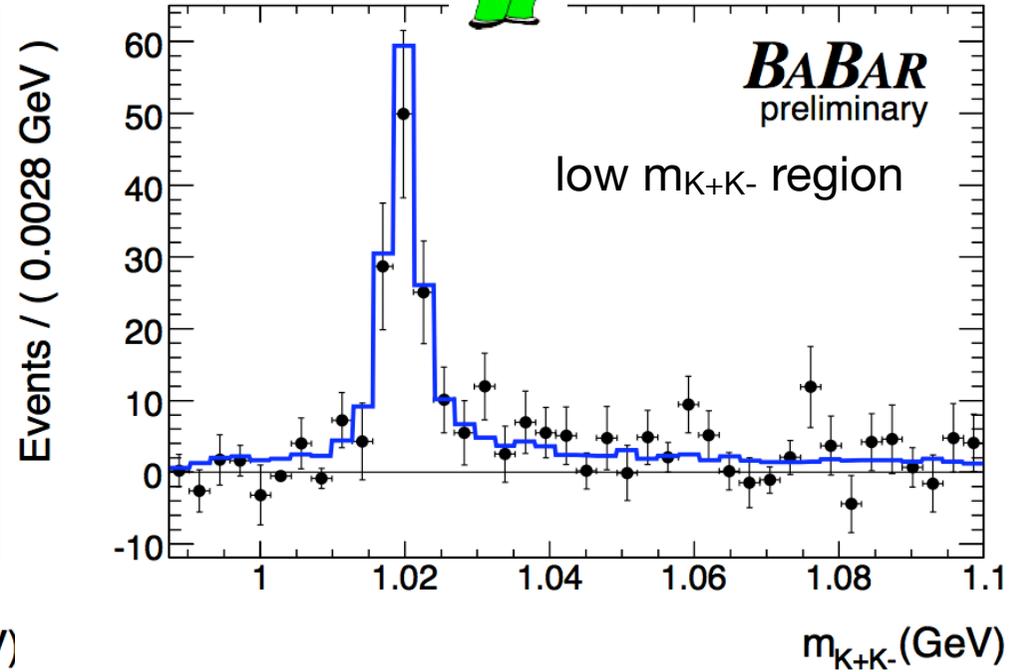
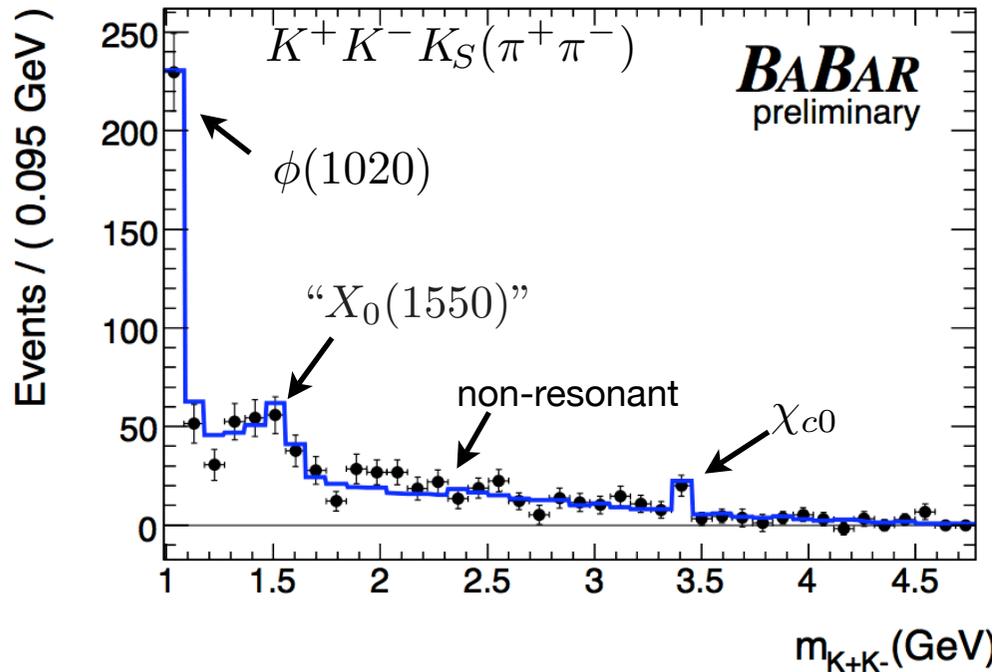
- Both experiments observe more than 5σ CP violation in charmless mode.

BABAR time-dependent Dalitz analysis

$$B^0 \rightarrow K^+ K^- K^0$$



$347 \times 10^6 B\bar{B}$



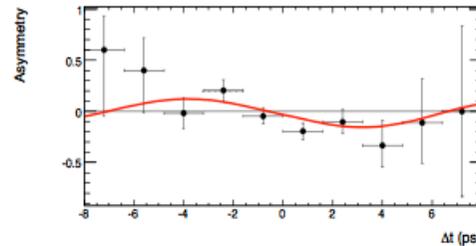
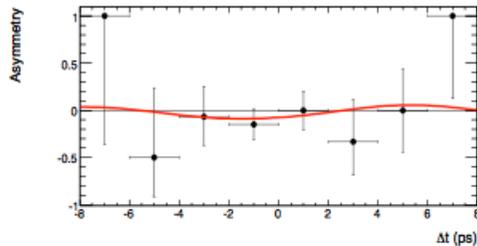
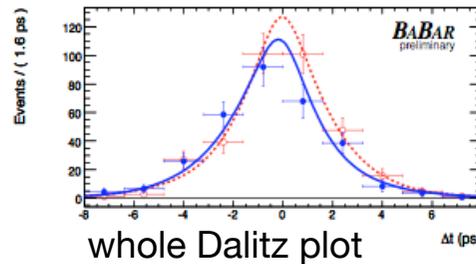
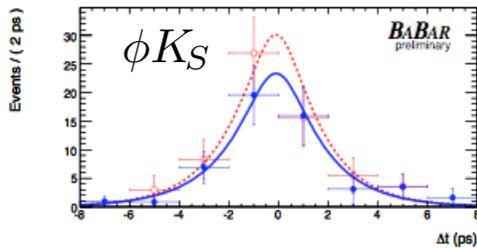
- Final state is a mixture of CP even/odd depending on the resonances.
- Signal events: $\sim 1000 K^+ K^- K_S$, $\sim 500 K^+ K^- K_L$.
- Time-dependent Dalitz analysis to extract Dalitz structures and CP asymmetry.
 - Resonances: $f_0(980)$, $\phi(1020)$, $X_0(1550)$, χ_{c0} , and non-resonant.

Extract β from time-dependent Dalitz analysis of $B^0 \rightarrow K^+ K^- K^0$

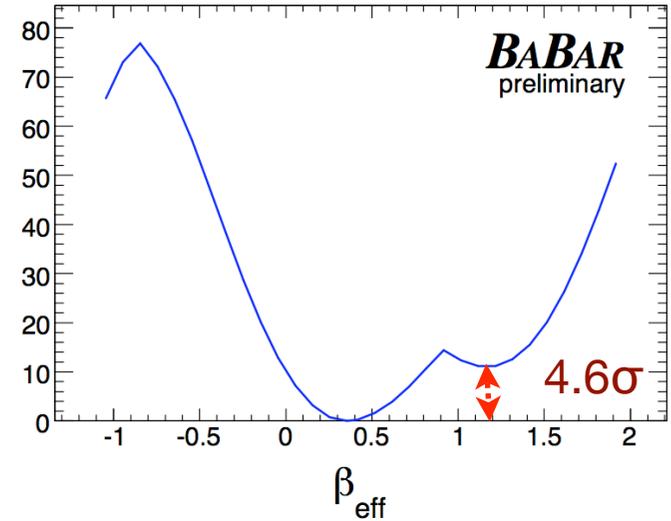
$$\frac{d\Gamma}{d\Delta t} \propto \frac{e^{-|\Delta t|/\tau}}{2\tau} \times \left[|\mathcal{A}|^2 + |\bar{\mathcal{A}}|^2 + q_{\text{tag}} 2\text{Im}(\xi \mathcal{A} \bar{\mathcal{A}}^*) \sin \Delta m_d \Delta t - q_{\text{tag}} (|\mathcal{A}|^2 - |\bar{\mathcal{A}}|^2) \cos \Delta m_d \Delta t \right]$$

$$\xi = \eta_{CP} e^{-2i\beta}$$

sensitive to 2β directly if $\bar{\mathcal{A}}\mathcal{A}^*$ is not real.



$\Delta \log(L)$



- Fit the whole Dalitz plot, and then fit $m_{K^+K^-} < 1.1$ GeV region.

[hep-ex/0607112]

whole

ϕK^0

$f_0 K^0$

$$\beta_{\text{eff}} = 0.361 \pm 0.079 \pm 0.037$$

$$\beta_{\text{eff}} = 0.06 \pm 0.16 \pm 0.05$$

$$\beta_{\text{eff}} = 0.18 \pm 0.19 \pm 0.04$$

$\sim 4.5\sigma$ from CP conservation

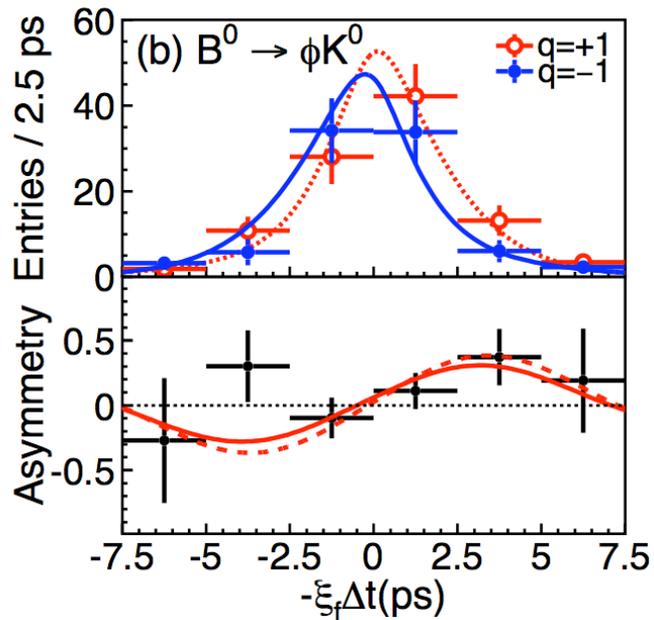
Belle separates ϕK^0 and $K^+K^-K_S$



$535 \times 10^6 B\bar{B}$

$$B^0 \rightarrow \phi K^0$$

Quasi-2body approach
Nsig \sim 420



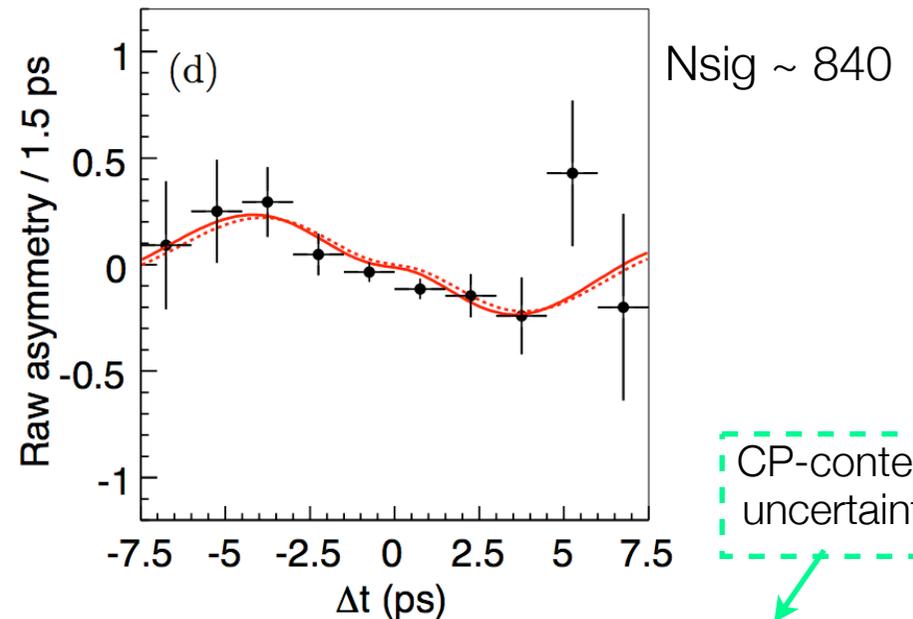
$$\sin 2\beta_{\text{eff}} = +0.50 \pm 0.21 \pm 0.06$$

$$C = -0.07 \pm 0.15 \pm 0.05$$

[PRL98, 031802 (2007)]

$$B^0 \rightarrow K^+ K^- K^0$$

Average CP content is determined
using isospin relations and the BFs of
 $B^+ \rightarrow K^+ K_S K_S$ and $B^0 \rightarrow K^+ K^- K^0$



$$\sin 2\beta_{\text{eff}} = +0.68 \pm 0.15 \pm 0.03_{+0.21}^{-0.13}$$

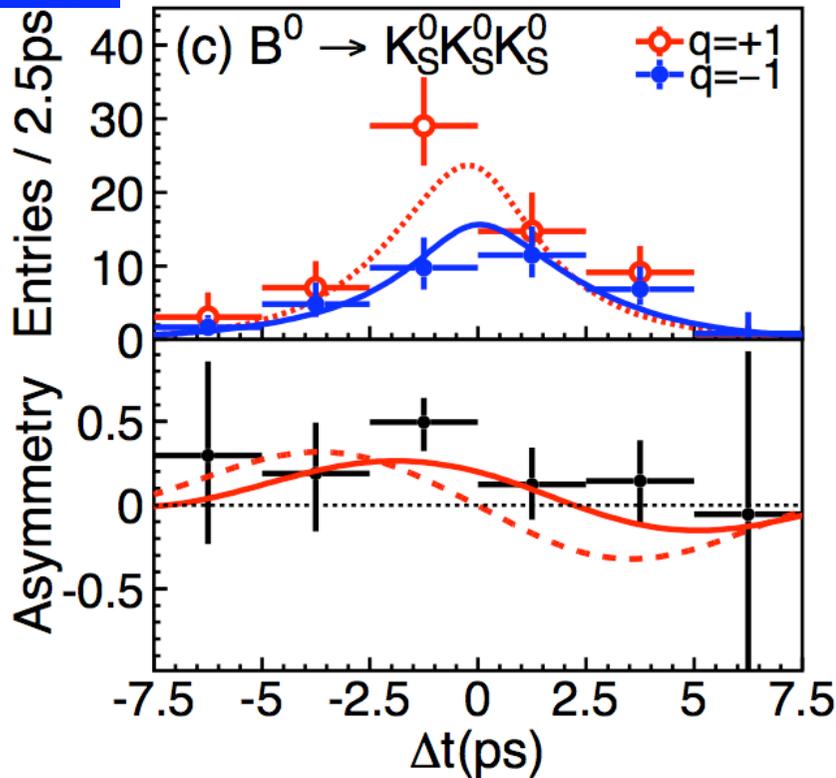
$$C = +0.09 \pm 0.10 \pm 0.05$$

[hep-ex/0609006]

$B^0 \rightarrow K_S K_S K_S$ is a CP eigenstate, no Dalitz analysis is necessary



$535 \times 10^6 B\bar{B}$



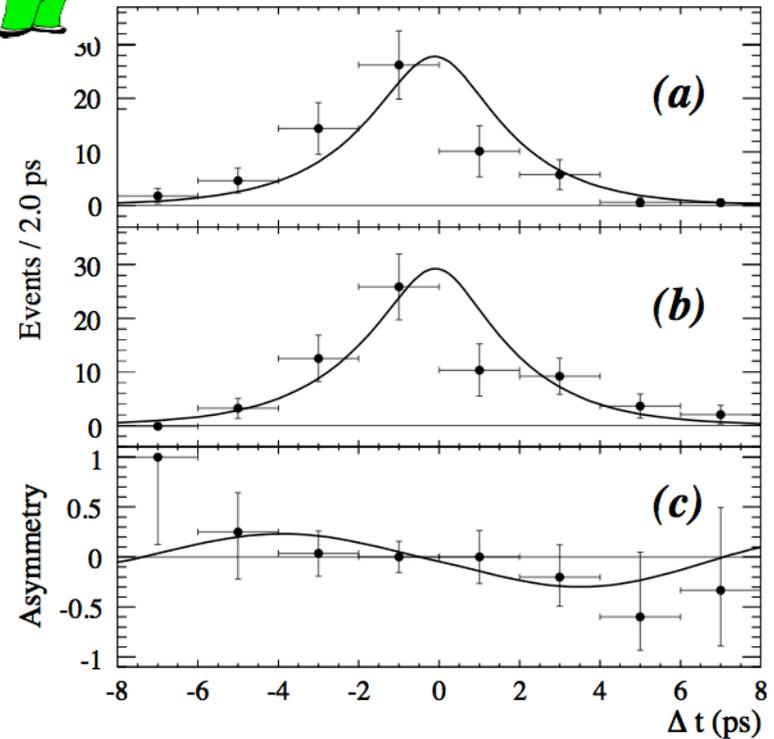
$$\sin 2\beta_{\text{eff}} = +0.30 \pm 0.32 \pm 0.08$$

$$C = -0.31 \pm 0.20 \pm 0.07$$

[PRL98, 031802 (2007)]



$383 \times 10^6 B\bar{B}$

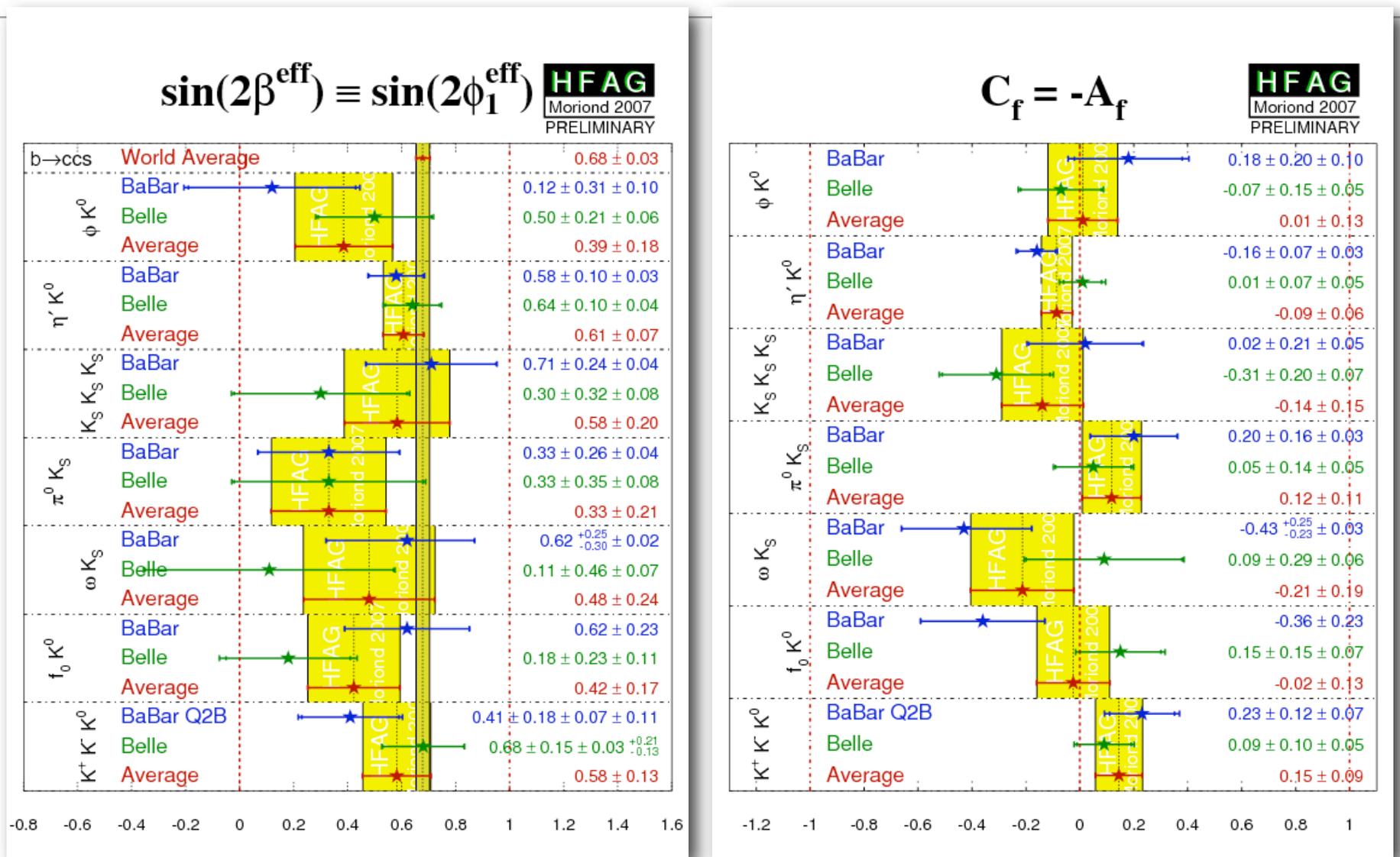


$$\sin 2\beta_{\text{eff}} = +0.71 \pm 0.24 \pm 0.04$$

$$C = +0.02 \pm 0.21 \pm 0.05$$

[hep-ex/0702046 submitted to PRL]

Hint of $\sin 2\beta_{\text{eff}}(\text{charmless}) < \sin 2\beta_{\text{eff}}(\text{golden modes})$



Conclusion

- Measuring the CKM angle β is a rich program at B-factories.
 - ▶ (CPV $>5\sigma$) $B^0 \rightarrow J/\psi K^0$   $B^0 \rightarrow \eta' K^0$  
 - ▶ (CPV $>4\sigma$) $B^0 \rightarrow K^+ K^- K^0$  $B^0 \rightarrow D^+ D^-$?  $B^0 \rightarrow D^{*\pm} D^\mp$ 
- $\sin 2\beta$ has been measured to 4% precision. More than 900 million BB pairs analyzed.
- $B^0 \rightarrow D^+ D^-$ puzzle.
- Ambiguity broken: $\cos 2\beta > 0$, $\beta = (21.3 \pm 1.0)$ degrees.
- Hint of inconsistent $\sin 2\beta_{\text{eff}}$ between penguin modes and golden modes persists.