Review of Neutrino Oscillations – Past, Present, and Future

> FPCP07 Bled, Slovenia May 16, 2007



Science & Technology Facilities Council Dave Wark Imperial/RAL

Imperial College London **FPCP07** The Maki-Nakagawa-Sakata-Pontecorvo Matrix If neutrinos have mass: $|\nu_l\rangle = \sum U_{li} |\nu_i\rangle$

For three neutrinos:

 $U_{1i} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{2} & c_{23} \end{pmatrix} \cdot \begin{pmatrix} c_{13} & 0 & s_{13}e^{i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{-i\delta} & 0 & c_{17} \end{pmatrix} \cdot \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$ where $c_{ij} = \cos \theta_{ij}$, and $s_{ij} = \sin \theta_{ij}$

Three Angles

 $P(v_{\mu} \rightarrow v_{e}) = \sin^{2} 2\theta \sin^{2} (1.27 \frac{\Delta m^{2} L}{E})$

FPCP07 The MNSP Matrix If neutrinos have mass: $|\nu_l\rangle = \sum U_{li} |\nu_i\rangle$

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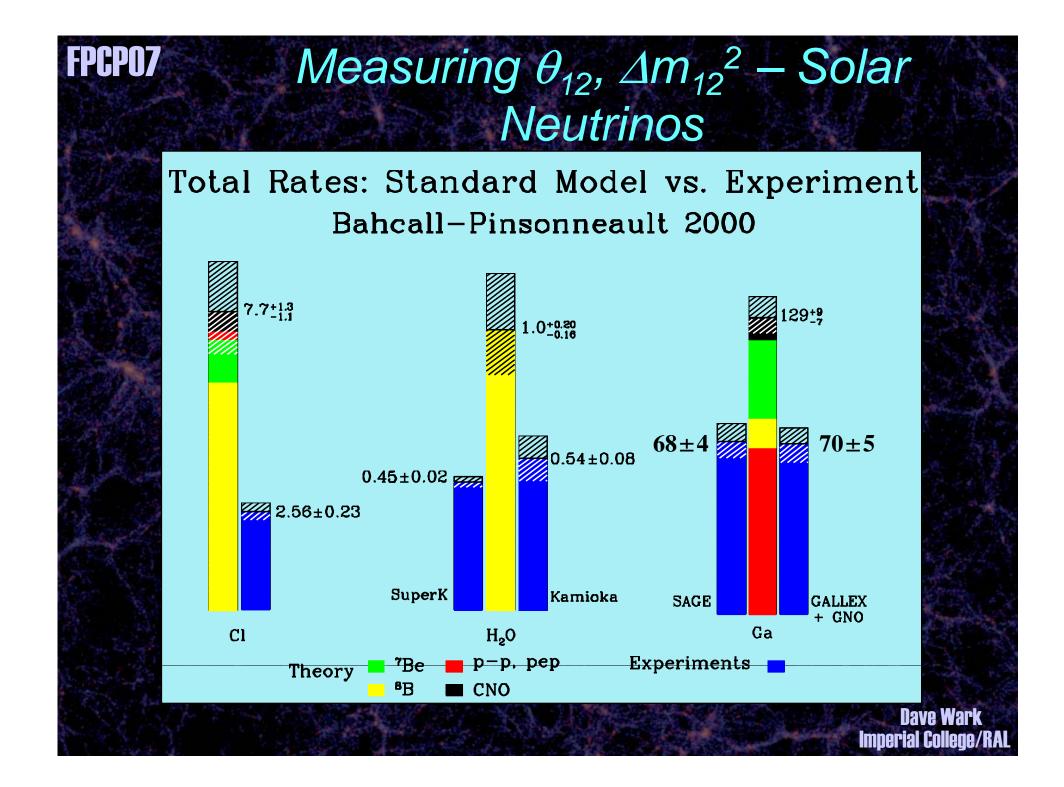
where $c_{ij} = \cos \theta_{ij}$, and $s_{ij} = \sin \theta_{ij}$

Two mass differences - each has a sign

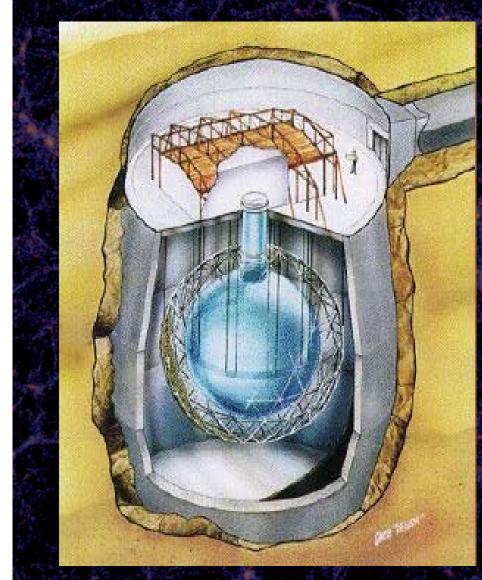
 $P(v_{\mu} \rightarrow v_{e}) = \sin^{2} 2\theta \sin^{2} (1.27 \underbrace{4m^{2}}_{E})$ $\sin^{2} 2\theta_{m} = \frac{\sin^{2} 2\theta}{(\omega - \cos 2\theta)^{2} + \sin^{2} 2\theta}$ $\omega = -2\sqrt{2}G_{F}N_{e}E/\Delta m^{2}$

FPCP07 The MNSP Matrix If neutrinos have mass: $|\nu_l\rangle = \sum U_{li} |\nu_i\rangle$ For three neutrinos: $U_{1i} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \cdot \begin{pmatrix} c_{13} & 0 & s_{2}e^{i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{-i\delta} & 0 & c_{13} \end{pmatrix} \cdot \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$ where $c_{ij} = \cos \theta_{ij}$, and $s_{ij} = \sin \theta_{ij}$ **CP** violating phase δ

 $P(v_{\mu} \rightarrow v_{e}) = \sin^{2} 2\theta \sin^{2} (1.27 \frac{\Delta m^{2} L}{E})$



Measuring θ_{12} , Δm_{12}^2 - SNO



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$$\nu_e + d \rightarrow p + p + e^-$$

Q = 1.445 MeV

- good measurement of v_e energy spectrum - some directional info $\propto (1 - 1/3 \cos \theta)$
- $-v_{e}$ only

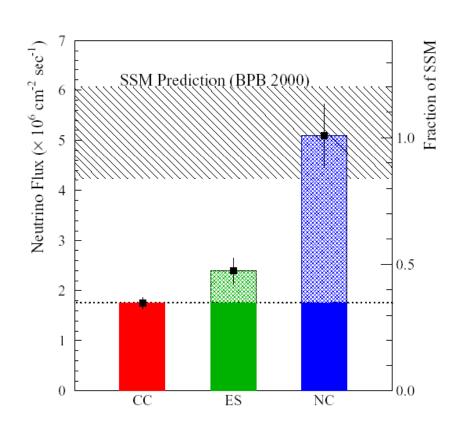
NC $V_x + d \rightarrow p + n + V_x$

Q = 2.22 MeV - measures total ⁸B v flux from the Sun - equal cross section for all v types

$$\underbrace{\mathsf{ES}}_{x} \mathcal{V}_{x} + \mathrm{e}^{-} \to \mathcal{V}_{x} + \mathrm{e}^{-}$$

- low statistics - mainly sensitive to v_e , some v_{μ} and v_{τ} - strong directional sensitivity

Measured SNO Fluxes

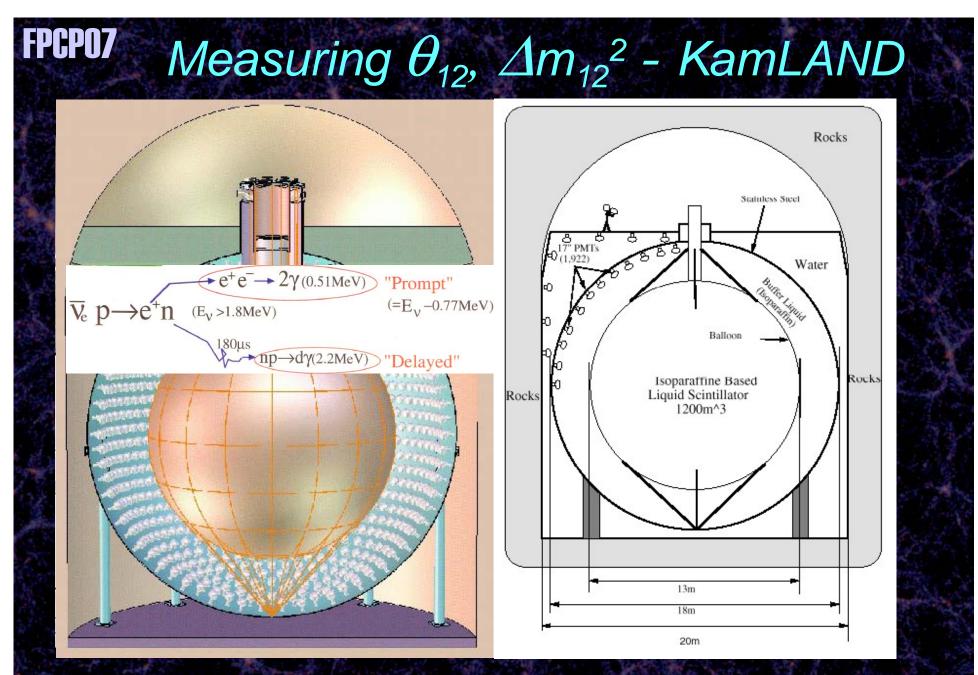


Assuming ⁸B energy spectrum ...

Fluxes (
$$\times 10^6$$
 cm⁻² sec⁻¹)

 $\phi_{CC} = 1.76^{+0.06}_{-0.05} \text{ (stat.)} \pm 0.09 \text{ (sys.)}$ $\phi_{ES} = 2.39^{+0.24}_{-0.23} \text{ (stat.)} \pm 0.12 \text{ (sys.)}$ $\phi_{NC} = 5.09^{+0.44}_{-0.43} \text{ (stat.)}^{+0.46}_{-0.43} \text{ (sys.)}$

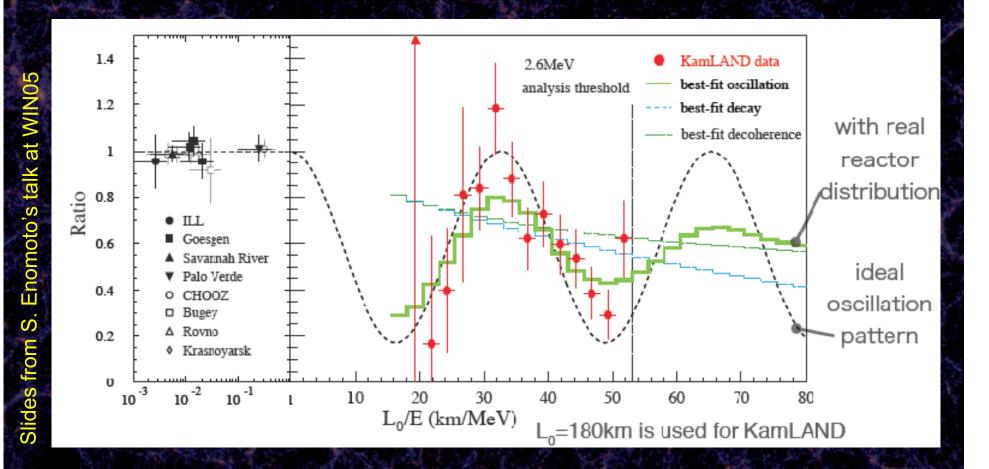
Repeated with NaCl to enhance NC signal, blind analysis \rightarrow All results agreed.



Sum over all Japanese power reactors...

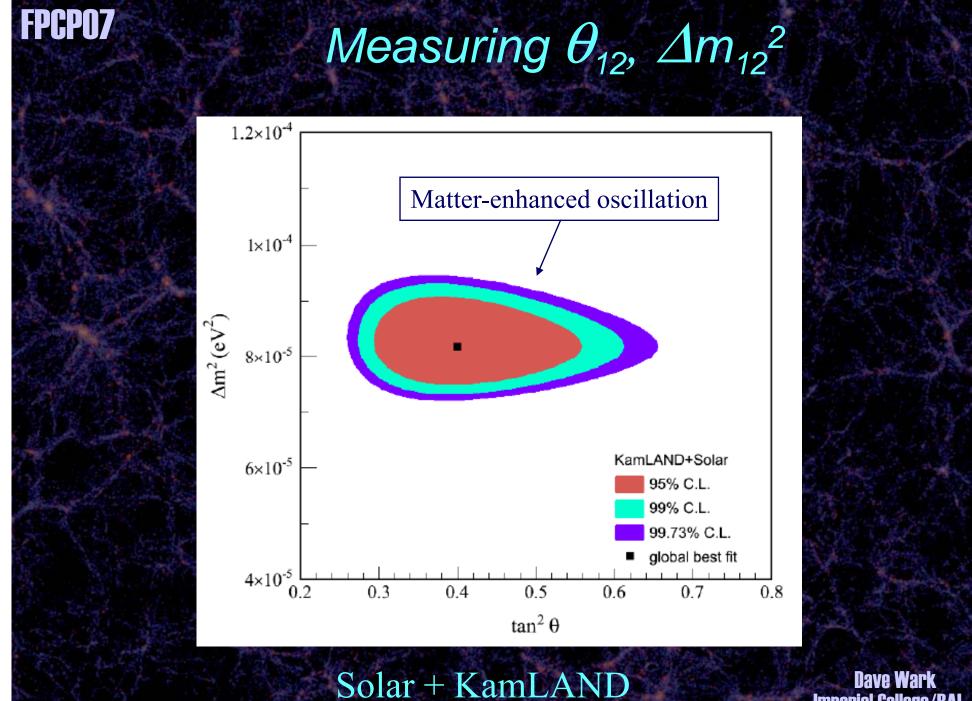
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Measuring θ_{12} , Δm_{12}^2 - KamLAND



Dave Wark Imperial College/RAL

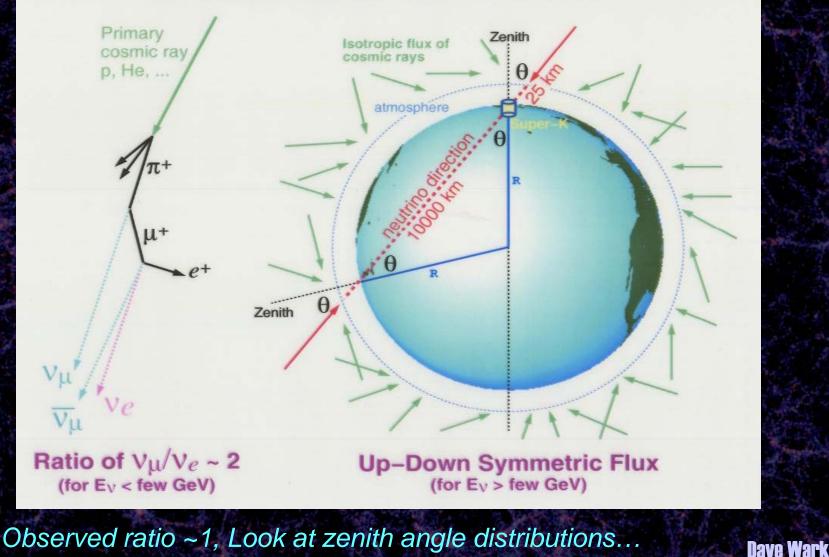
Proved (with other results) that neutrinos oscillate... ...or at least do a damned fine impression.



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FPCP07 1st Smoking Gun – SK Atmospheric

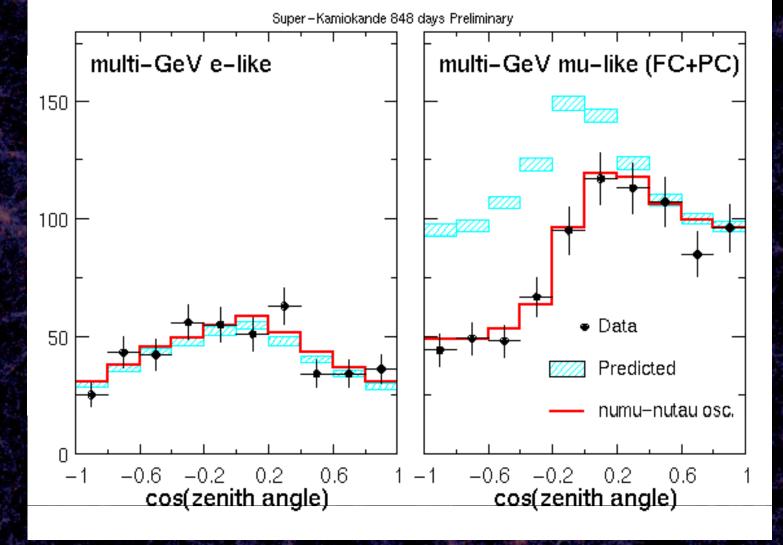
ATMOSPHERIC NEUTRINOS

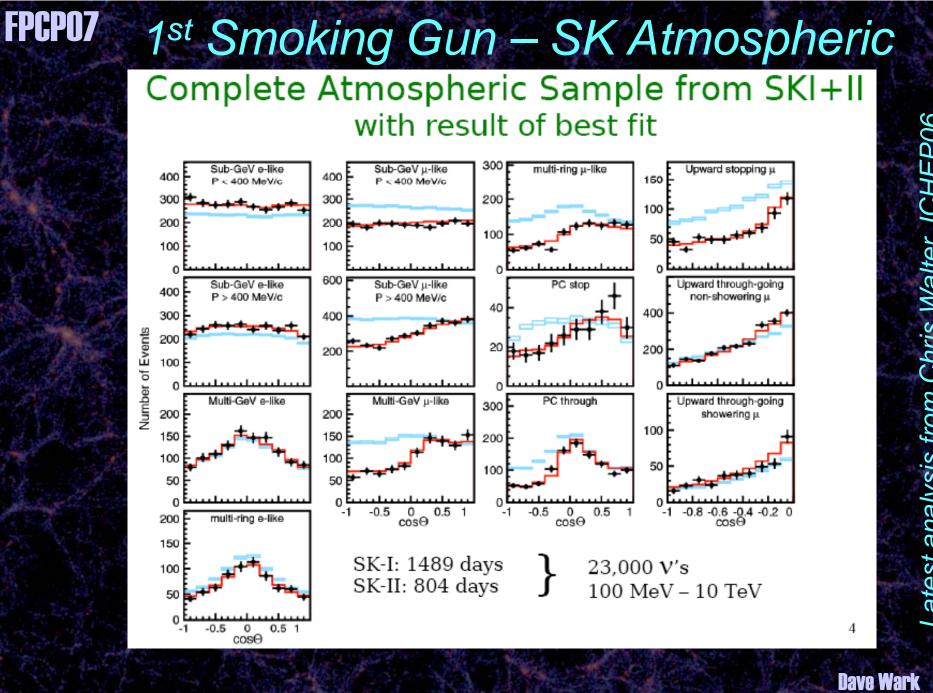


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SK data as a function of zenith angle

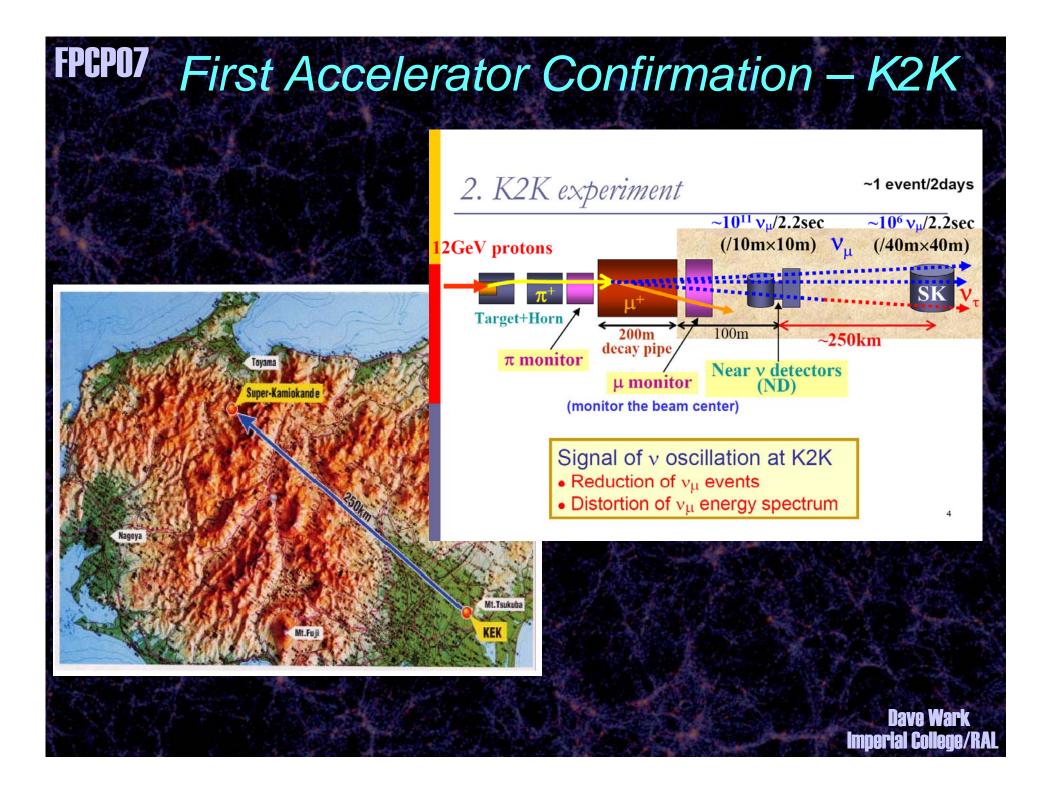
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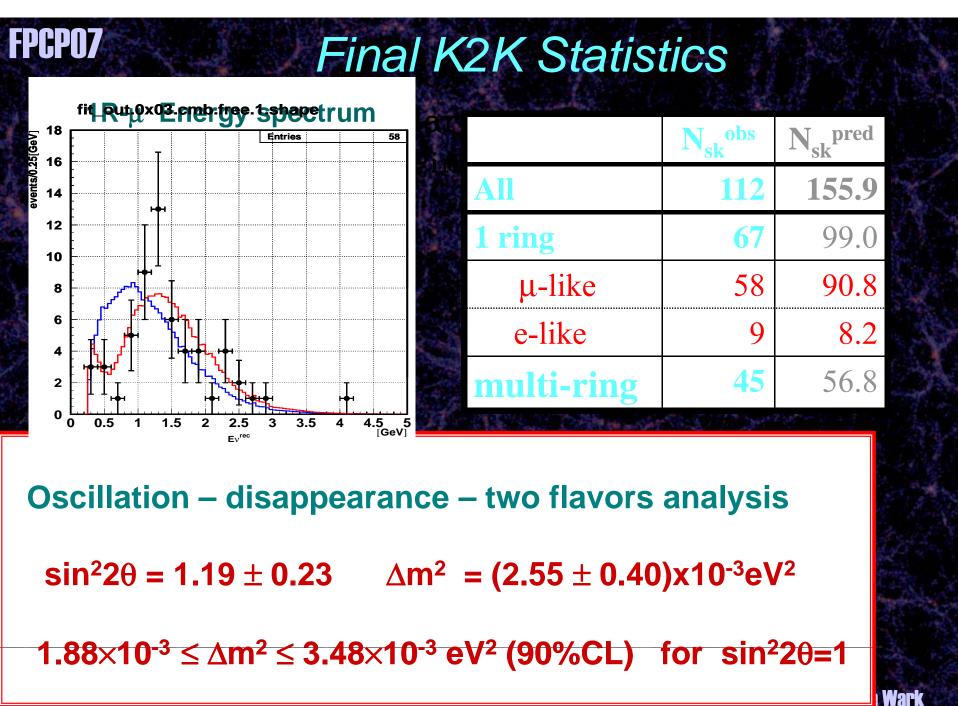




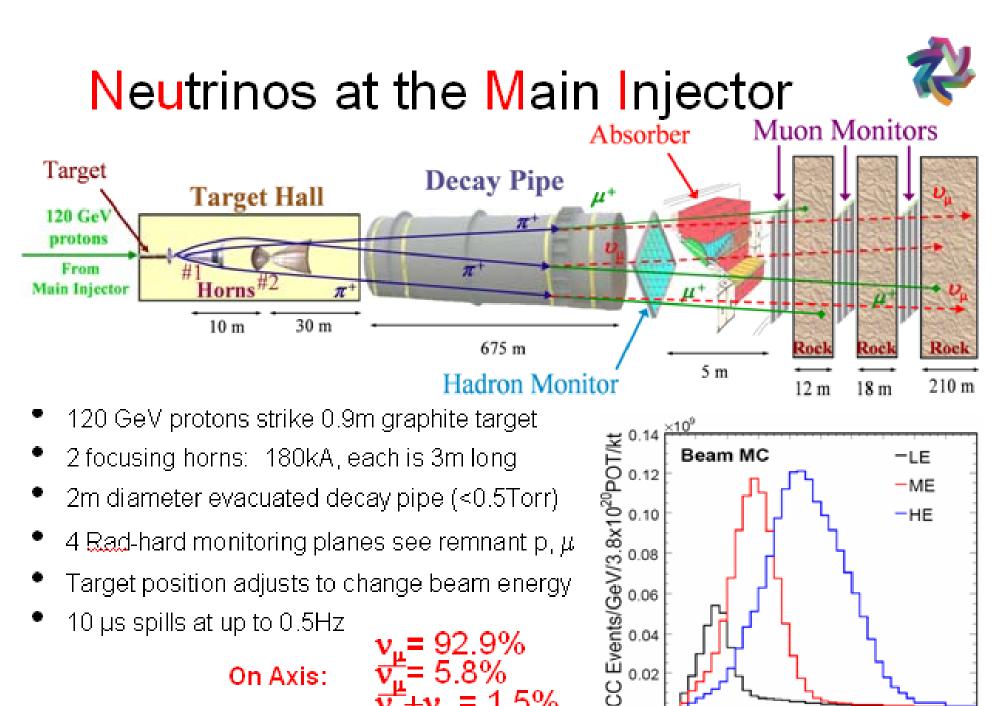
Latest analysis from Chris Walter, ICHEP06.

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Plots from Pier Loverre's talk.



1.5%

Deborah Harris WIN'07

0.00

12

14

16

18

20

10

Energy (GeV)

10 µs spills at up to 0.5Hz

On Axis:

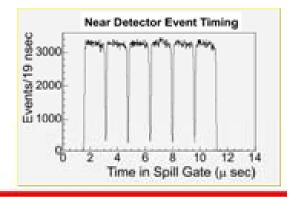
15 January 2007

MINOS Detectors

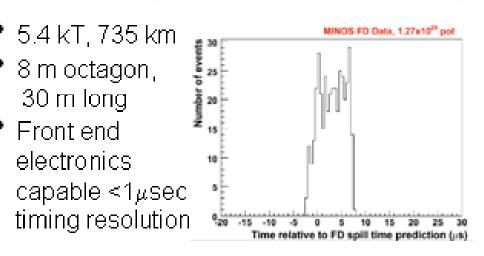


- 980 tons, 1 km from target
- Data used to predict v spectrum at far detector
- 4.8 m x 3.8 m, 15 m long

Front end electronics read out every 19nsec

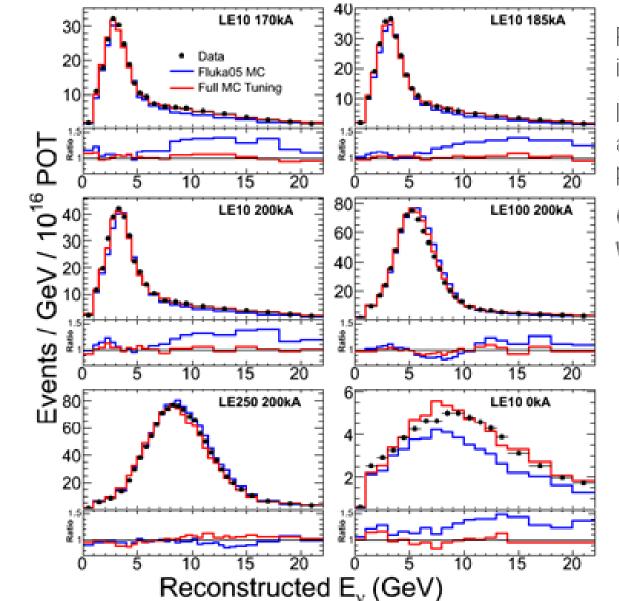






Energy Spectrum Tuning

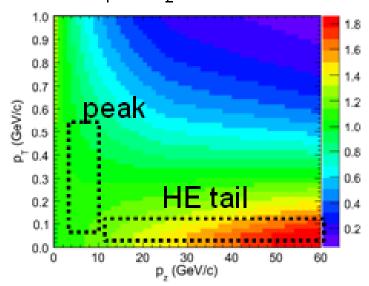


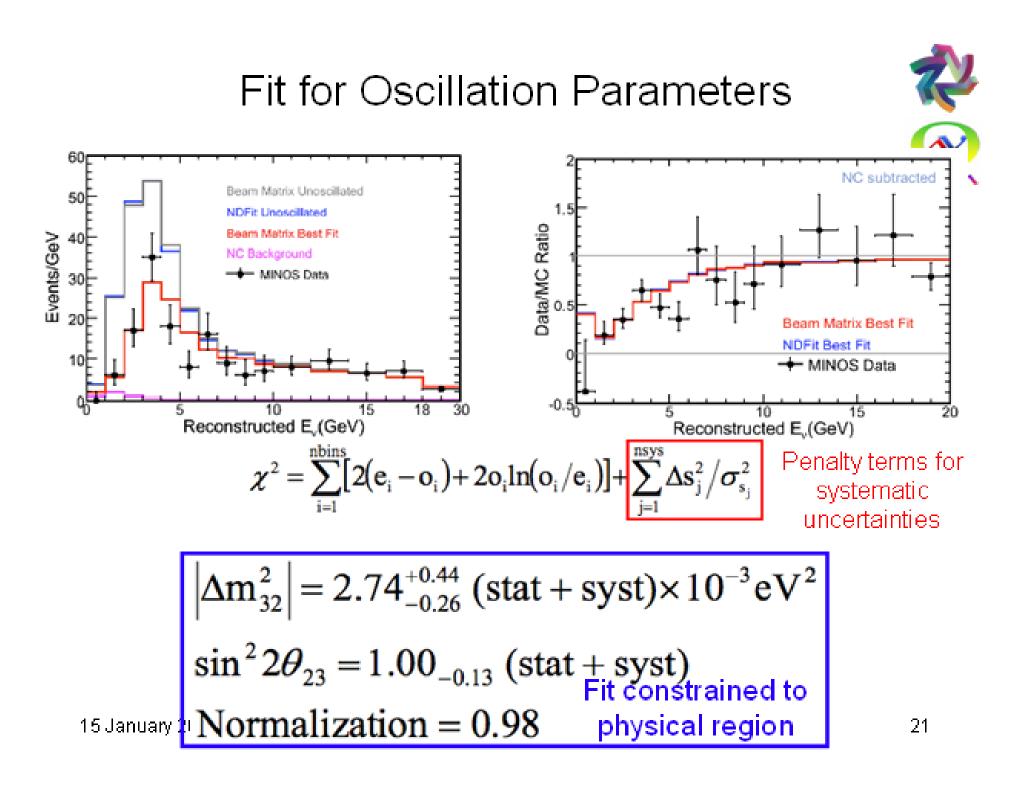


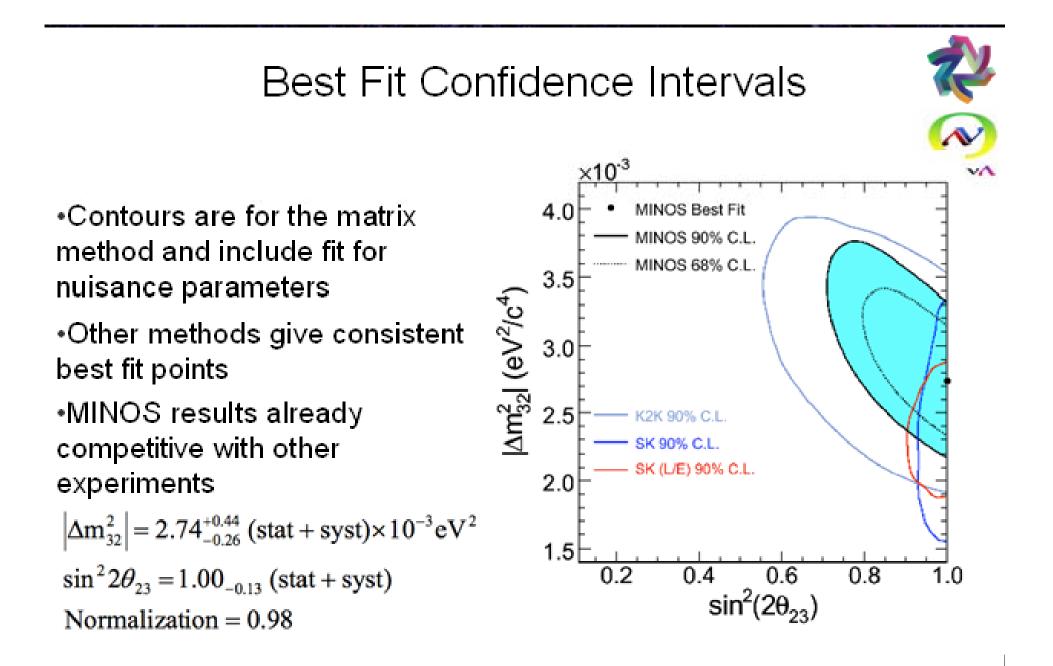
Reweight pion x_F and p_T to ****** improve data/MC agreement

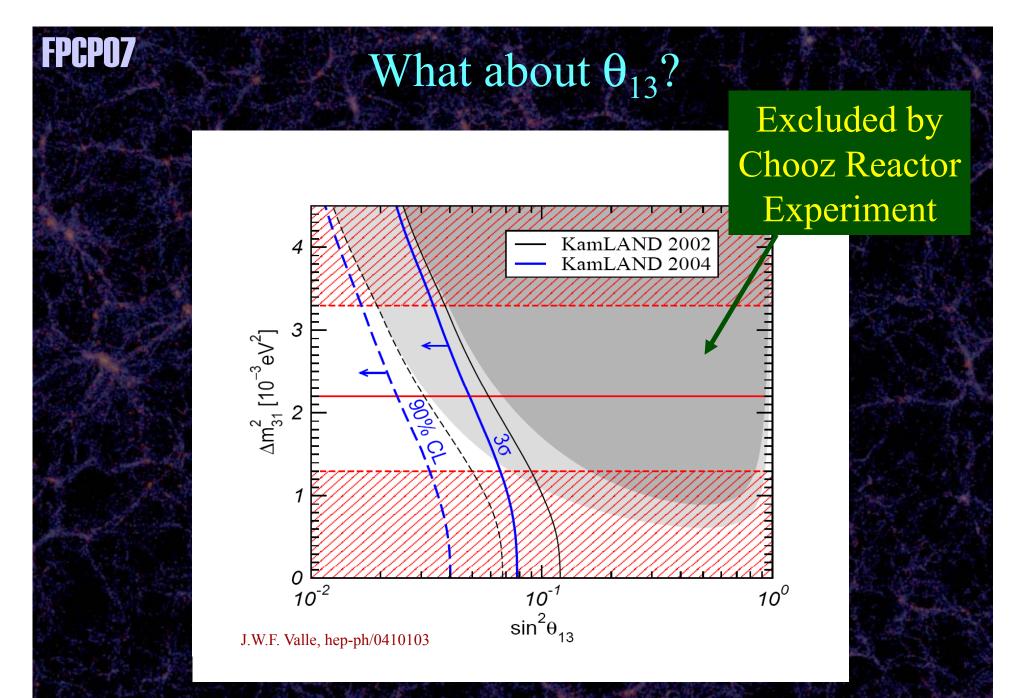
Include horn focusing, NC norm and energy scale as nuisance parameters

Osc. analyses use these weights P_T v P₂ weights









All we have at present are limits, showing θ_{13} is small...

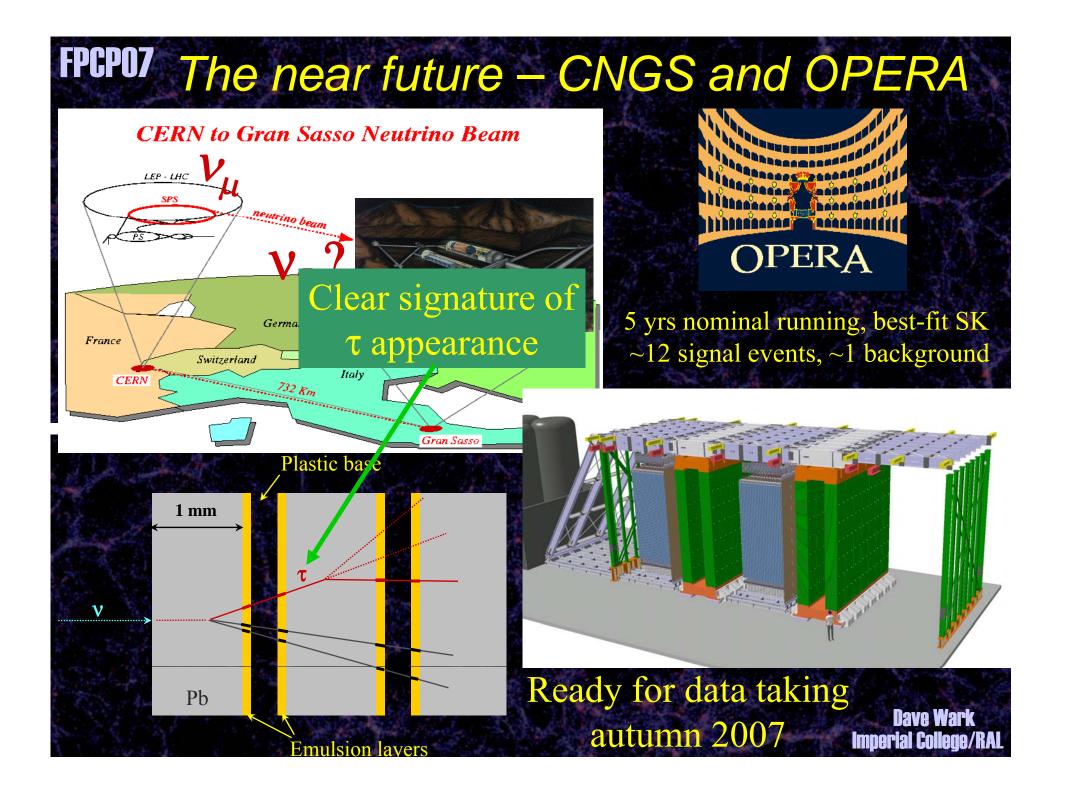
What are the experimental targets for new accelerator experiments?

- More accurate determinations of already measured parameters (better than CKM?) ⇒ is θ₂₃ = 45°?
- Other signatures of oscillations $-v_{\tau}$ appearance.
- θ_{13} look for $\nu_{\mu} \rightarrow \nu_{e}$,

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- The sign of Δm_{23}^2 (or Δm_{31}^2)
- The CP-violating phase δ

• First, however, resolve the LSND anomaly. Has now been done! See talk by H. Tanaka. We don't know what happened to LSND, but it doesn't appear to be oscillations...



FCP07 Three neutrino mixing.
If neutrinos have mass:
$$|V_{l}\rangle = \sum U_{li}|V_{i}\rangle$$

 $U_{ii} = \begin{pmatrix} U_{el} & U_{e2} & U_{e3} \\ U_{\mu} & U_{\mu2} & U_{\mu3} \\ U_{\tau} & U_{\tau2} & U_{\tau3} \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{22} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{i\delta} \\ 0 & 1 & 0 \\ -s_{12}e^{-i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12}e^{-i\delta} & 0 & c_{13} \end{pmatrix}$
 $P_{e\mu} \cong \sin^{2} 2\theta_{13} \sin^{2} 2\theta_{23} \sin^{2} \Delta$
 $\mp \alpha \sin 2\theta_{13} \sin \delta \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{23} \sin^{3} \Delta$
 $-\alpha \sin 2\theta_{13} \cos \delta \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{23} \cos \Delta \sin 2\Delta$
 $+\alpha^{2} \cos^{2} \theta_{23} \sin^{2} 2\theta_{12} \sin^{2} \Delta$
where $\alpha = -0.03$ and $\Delta = -\pi/4$
And $\sin^{2} 2\theta_{13} < -0.14$

Three neutrino mixing.

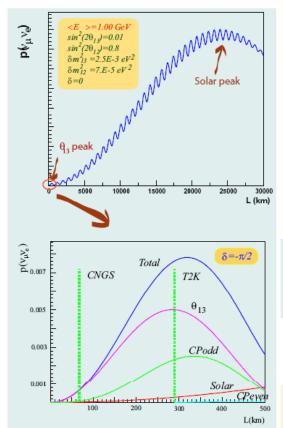
- Until limit is improved by a factor of a few the first term dominates.
- Optimal situation for CP measurement is when all terms are \approx equal, or when $\sin^2 2\theta_{13} \sim 0.01$.

$$P_{e\mu} \cong \sin^2 2\theta_{13} \sin^2 2\theta_{23} \sin^2 \Delta$$

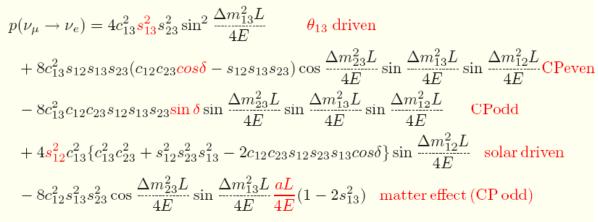
 $\mp \alpha \sin 2\theta_{13} \sin \delta \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{23} \sin^3 \Delta$ $- \alpha \sin 2\theta_{13} \cos \delta \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{23} \cos \Delta \sin 2\Delta$ $+ \alpha^2 \cos^2 \theta_{23} \sin^2 2\theta_{12} \sin^2 \Delta$ $\text{ where } \alpha = -0.03 \quad \text{and } \Delta = -\pi/4$ $\text{ And } \sin^2 2\theta_{13} < -0.14$

Three neutrino mixing.

Sub leading $u_{\mu} -
u_{e}$ oscillations



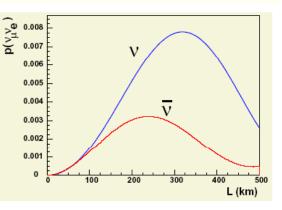
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2

 $heta_{13}$ discovery requires total probability greater than solar driven probability

Leptonic CP discovery requires $A_{CP} = \frac{P(\nu_{\mu} \rightarrow \nu_{e}) - P(\overline{\nu}_{\mu} \rightarrow \overline{\nu}_{e})}{P(\nu_{\mu} \rightarrow \nu_{e}) + P(\overline{\nu}_{\mu} \rightarrow \overline{\nu}_{e})} \neq 0$



M. Mezzetto, Taup 05, Zaragoza, 13 september 2005,

Three neutrino mixing.

- Most experiments make essentially one measurement of $P(v_u \rightarrow v_e)$.
- There are correlations between parameters, including ones that cannot be measured at accelerators.
- There are degenerate solutions from the sign of Δm_{31}^2 and whether θ_{23} is greater or smaller than $\pi/4$.

$$\begin{split} P(\nu_{\mu} \rightarrow \nu_{e}) &= 4C_{13}^{2}S_{13}^{2}S_{23}^{2}\sin^{2}\frac{\Delta m_{31}^{2}L}{4E} \times \left(1 + \frac{2a}{\Delta m_{31}^{2}}\left(1 - 2S_{13}^{2}\right)\right) \\ &+ 8C_{13}^{2}S_{12}S_{13}S_{23}(C_{12}C_{23}\cos\delta - S_{12}S_{13}S_{23})\cos\frac{\Delta m_{32}^{2}L}{4E}\sin\frac{\Delta m_{31}^{2}L}{4E}\sin\frac{\Delta m_{21}^{2}L}{4E} \\ &- 8C_{13}^{2}C_{12}C_{23}S_{12}S_{13}S_{23}\sin\delta\sin\frac{\Delta m_{32}^{2}L}{4E}\sin\frac{\Delta m_{31}^{2}L}{4E}\sin\frac{\Delta m_{21}^{2}L}{4E} \\ &+ 4S_{12}^{2}C_{13}^{2}\left\{C_{12}^{2}C_{23}^{2} + S_{12}^{2}S_{23}^{2}S_{13}^{2} - 2C_{12}C_{23}S_{12}S_{23}S_{13}\cos\delta\right\}\sin^{2}\frac{\Delta m_{21}^{2}L}{4E} \\ &- 8C_{13}^{2}S_{13}^{2}S_{23}^{2}\cos\frac{\Delta m_{32}^{2}L}{4E}\sin\frac{\Delta m_{31}^{2}L}{4E}\frac{aL}{4E}\left(1 - 2S_{13}^{2}\right) \end{split}$$

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FPCP07 Long Baseline $v_{\mu} \Leftrightarrow v_{e}$ Appearance

- Modest improvements (factor~2) available from MINOS and OPERA
- Major improvements in sensitivity will require major new dedicated experiments.
- Superbeams v derived from π decay:
 - T2KI, T2KII
 - NOvA, NOvA + Proton Driver
 - CERN \rightarrow Modanne or LNGS or...
 - BNL \rightarrow Homestake or Henderson
 - FNAL \rightarrow various sites
 - β Beams v_e derived from β -decaying nucleus:
 - CERN
 - FNAL
 - EC beams? produces "monoenergetic" neutrinos
 - Neutrino Factories v_e/v_μ derived from μ decay:
 - CERN
 - RAL

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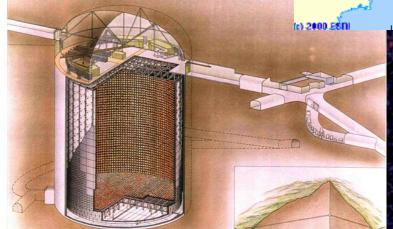
- FNAL
- JPARC



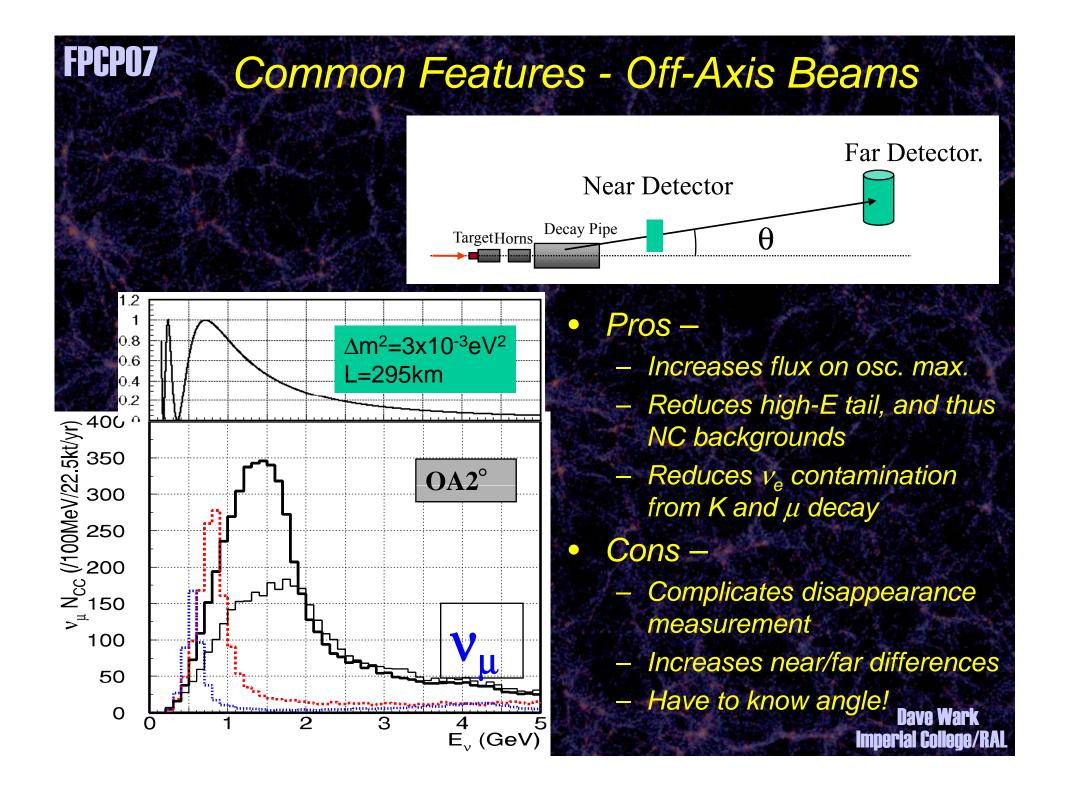
FPCP07 JPARC – SuperK, AKA T2K JPARC Accelerator – Phase I, 0.75 MW @ 50 GeV Phase II, raise power to 4 MW Approved Under const.



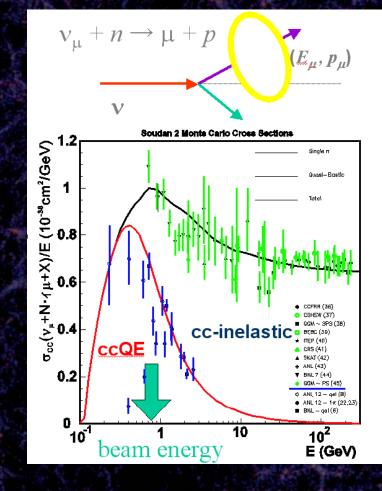


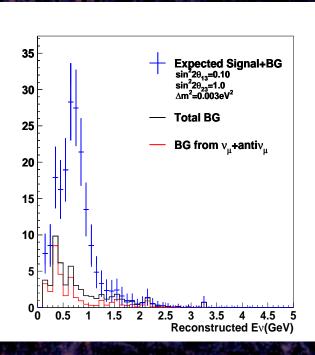


Far Detector – Super Kamiokande Rebuild (completed).



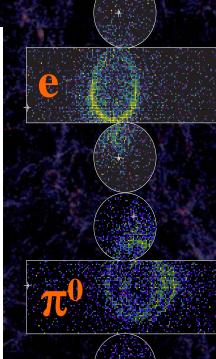
L/E well-tuned to CCQE, Critical for untangling Beam $\otimes \Sigma \sigma \otimes$ detector





T₂K

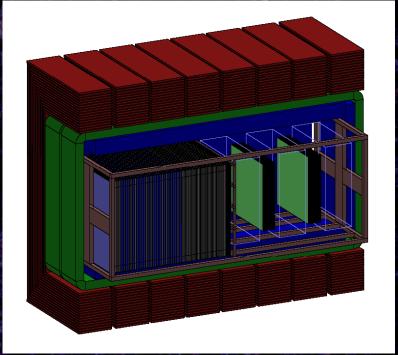
Super Kamiokande well understood, Ideal for separating Electrons, μ , π^0



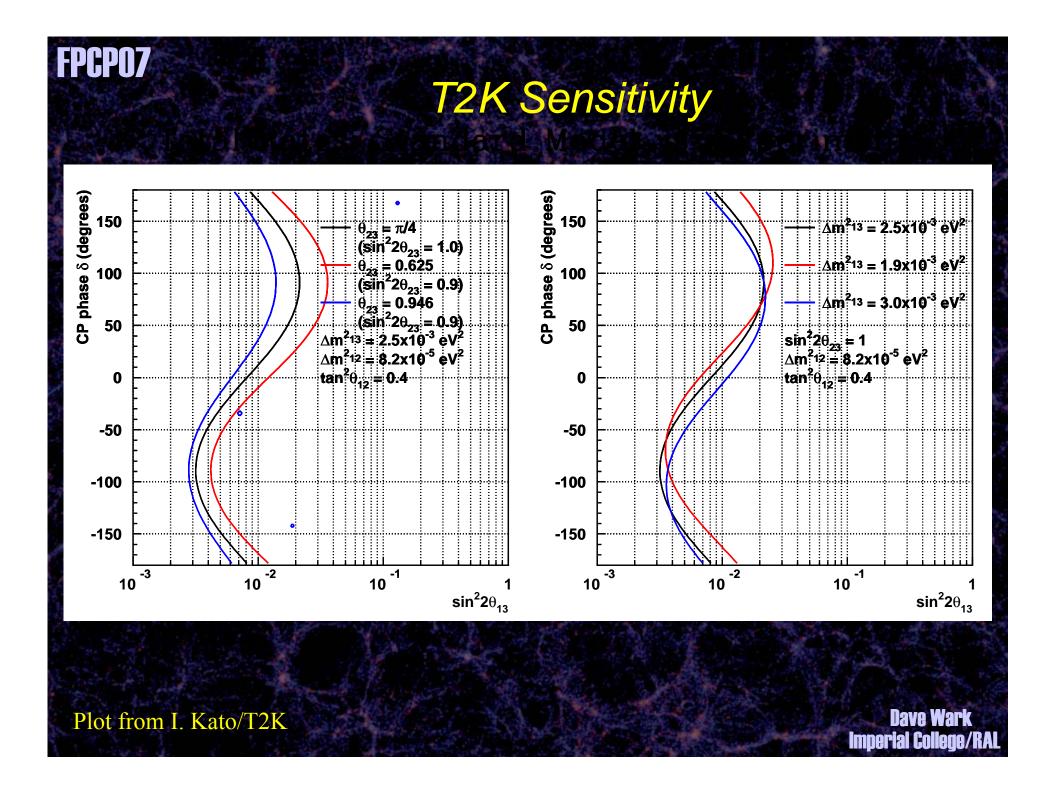
T2K

Near Detector @ 280m - Built inside UA1/NOMAD magnet for p_{μ} measurement - Sandwich calorimeters/trackers and TPCs for precision beam spectrum and composition measurement. - $\chi(v,n)\chi' \rightarrow \chi(n,\pi^0)\chi'?$

Artistic view of LAr integration in 2km underground site

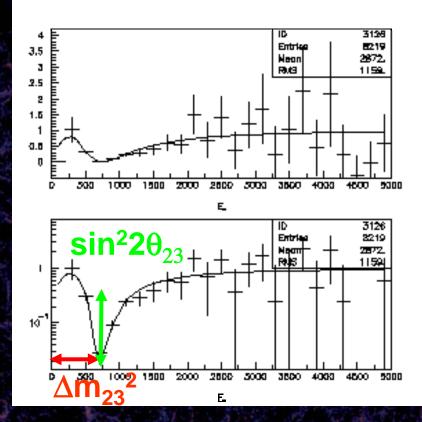


Near Detector @ 2km
Near/far spectral uncertainties negligible
Water Cerenkov, MRD, and LAr



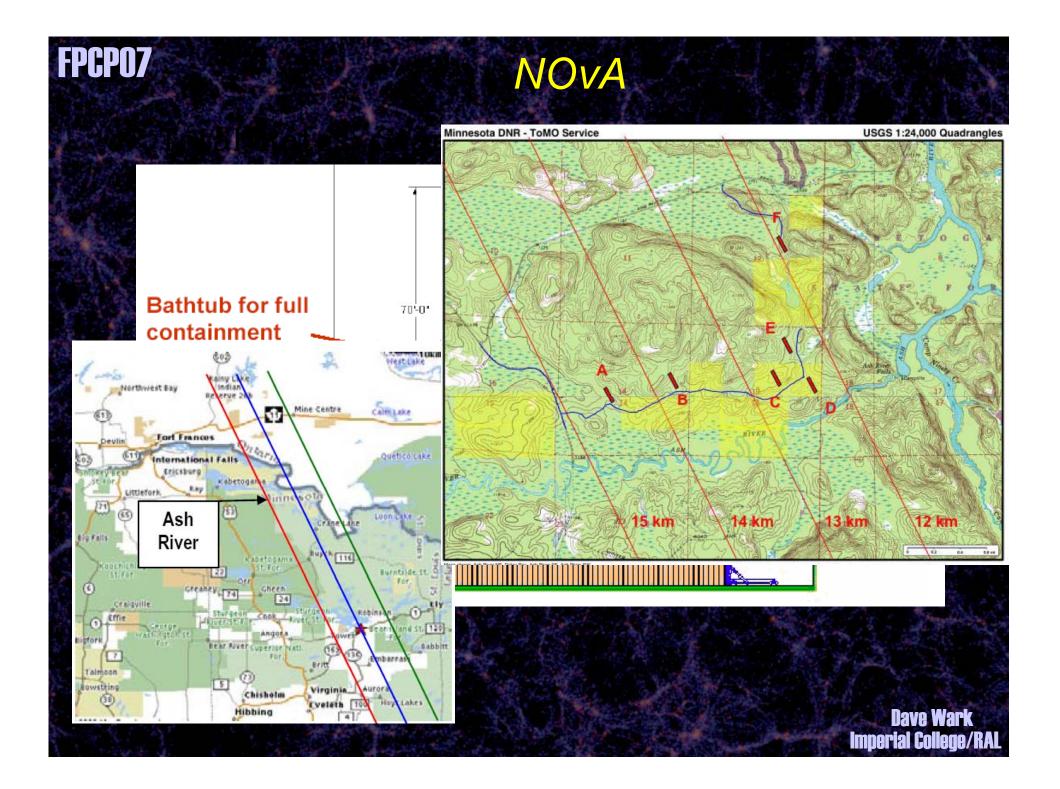
Design sensitivity

v_{μ} disappearance

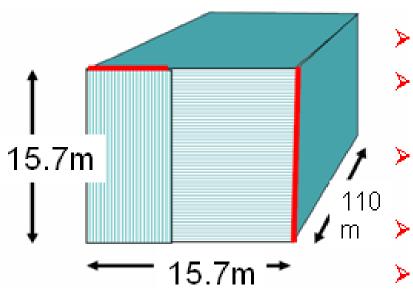


NOvA will also be sensitive to v_u disappearance

δ(sin²2θ) ~0.01 δ(Δm²) <1×10⁻⁴(eV²)



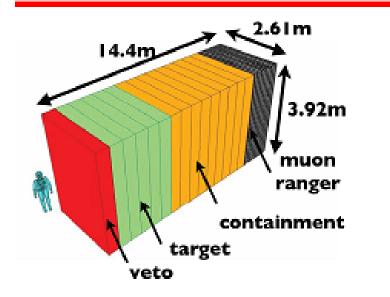
NOvA Detectors





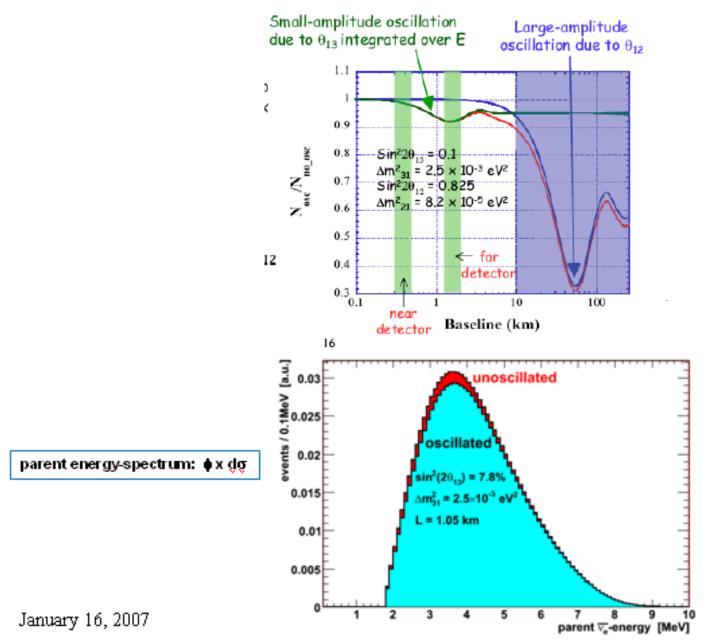
25 <u>ktons</u>

- 1984 liquid scintillator planes, no additional absorber (~80% active)
- Scintillator cells 3.8 x 6.0 x 1570 cm
- Read out from one side per plane with <u>APDs</u>
- Expected minimum signal 20pe

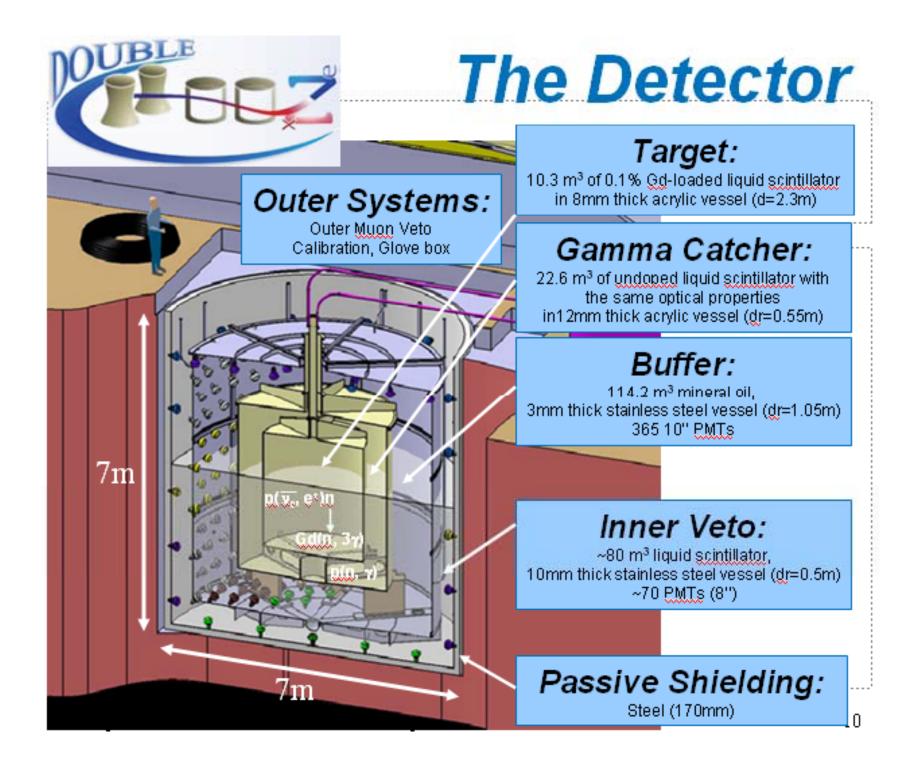


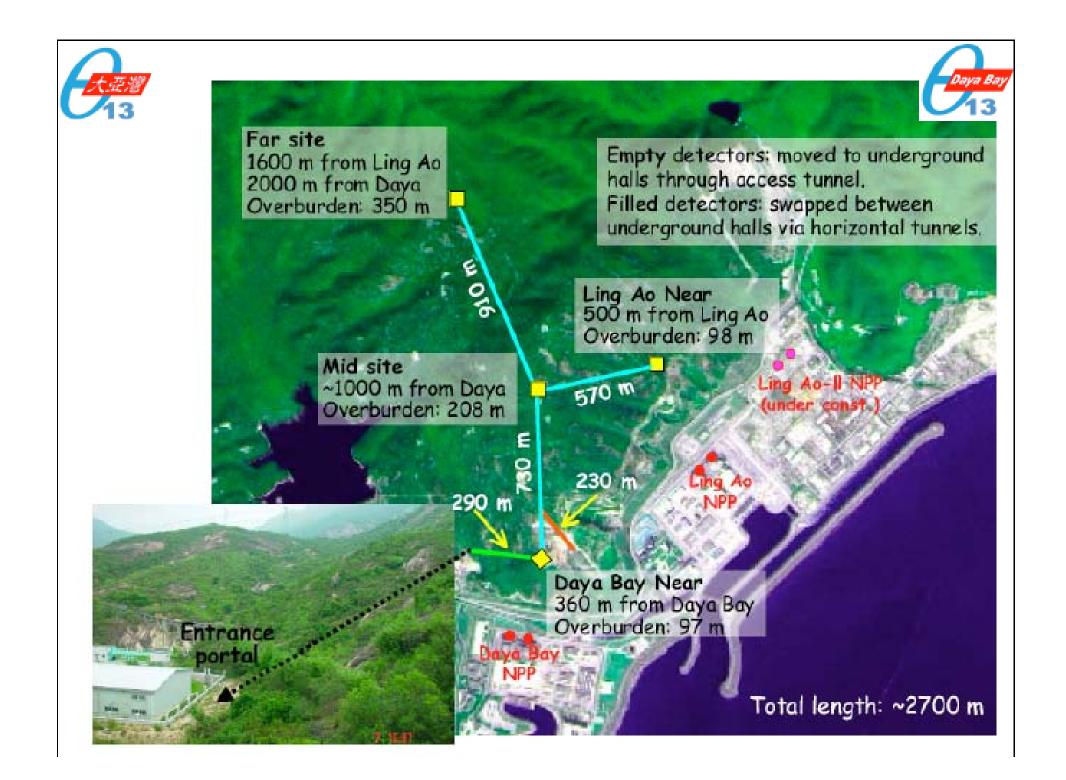
- 126 tons of scintillator, 83 tons of steel
- 23 ton fiducial mass
- 186 liquid scintillator planes in target, 10 in muon ranger, 1m of steel
- Same cell size, same minimum signal
- Read out from one side per plane with APDs plus faster electronics than in far detector

v-Oscillation at Nuclear Reactors



7









Systematic Uncertainties

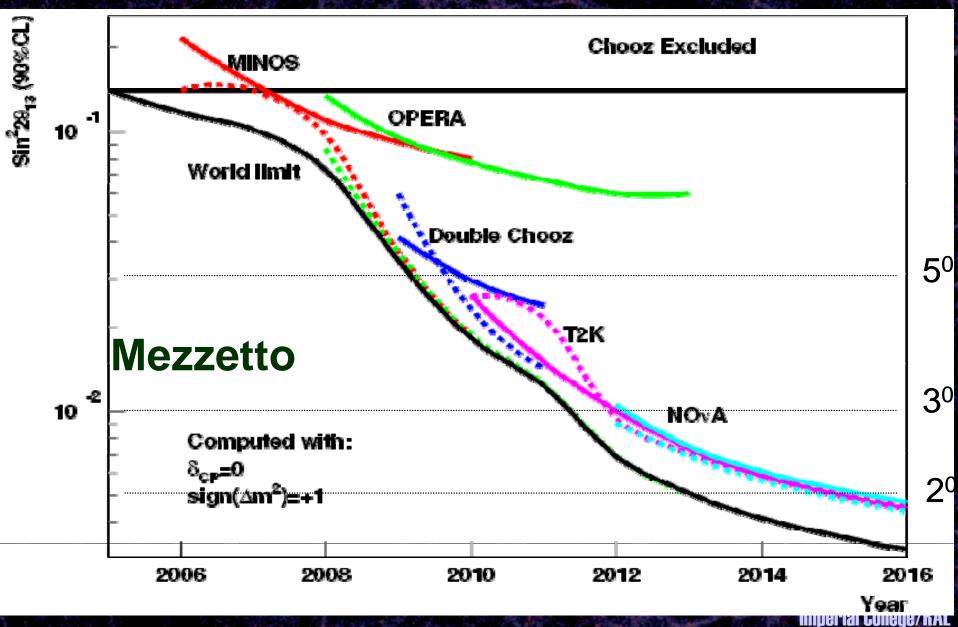
• Reactor-related:

Number of cores	α	σ_{ρ} (power)	$\sigma_{\rho}(\text{location})$	$\sigma_{\rho}(\text{total})$
4	0.338	0.035%	0.08%	0.087%
6	0.392	0.097%	0.08%	0.126%

· Detector-related:

Source of uncertainty		Chooz	Daya Bay (relative)		
		(absolute)	Baseline	Goal	Goal w/Swapping
# protons	H/C ratio	0.8	0.2	0.1	0
	Mass	-	0.2	0.02	0.006
Detector	Energy cuts	0.8	0.2	0.1	0.1
Efficiency	Position cuts	0.32	0.0	0.0	0.0
	Time cuts	0.4	0.1	0.03	0.03
	H/Gd ratio	1.0	0.1	0.1	0.0
	n multiplicity	0.5	0.05	0.05	0.05
	Trigger	0	0.01	0.01	0.01
	Live time	0	< 0.01	< 0.01	< 0.01
Total detector-related uncertainty		1.7%	0.38%	0.18%	0.12%

A possible future...

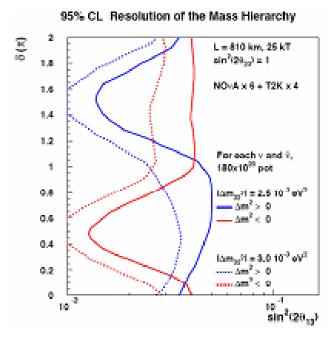


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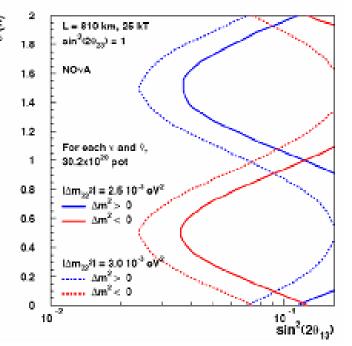


Determining the Mass Hierarchy

 Comparing v and anti-v
 probabilities, there is a region of phase space where NOvA could determine the mass hierarchy



95% CL Resolution of the Mass Hierarchy



 NOvA and T2K upgrades when combined do even better than just upgrading one by itself

Three Ways Forward?

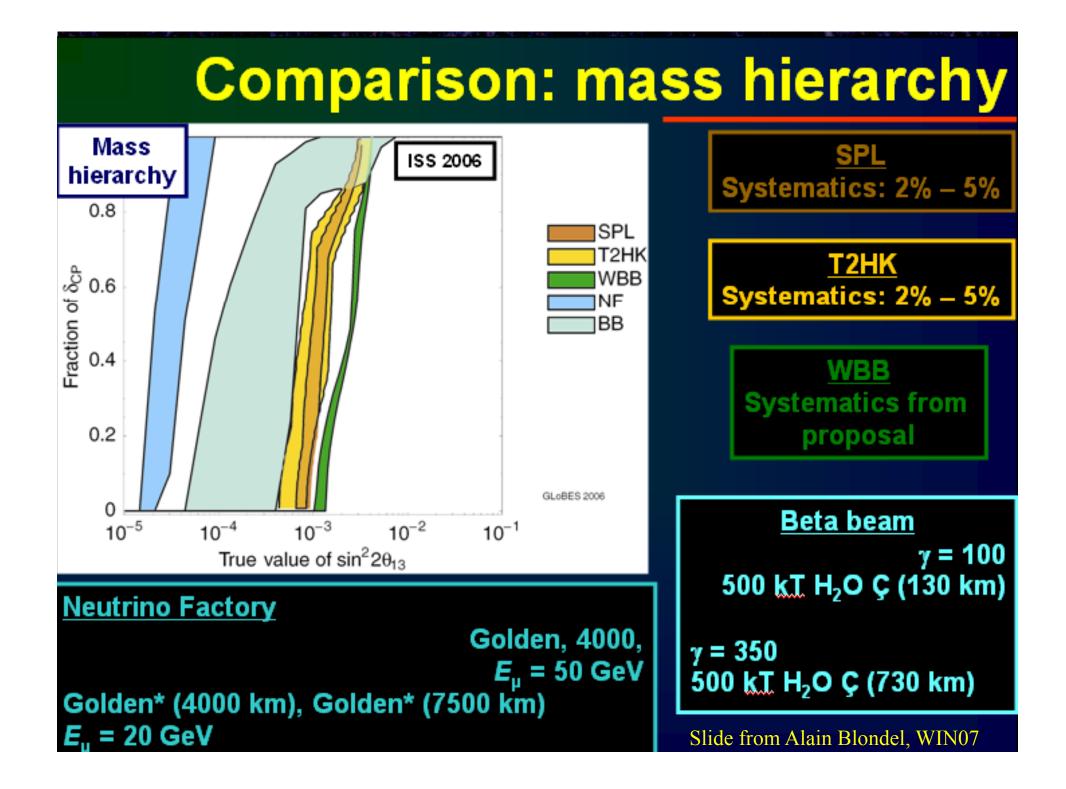
Superbeams:

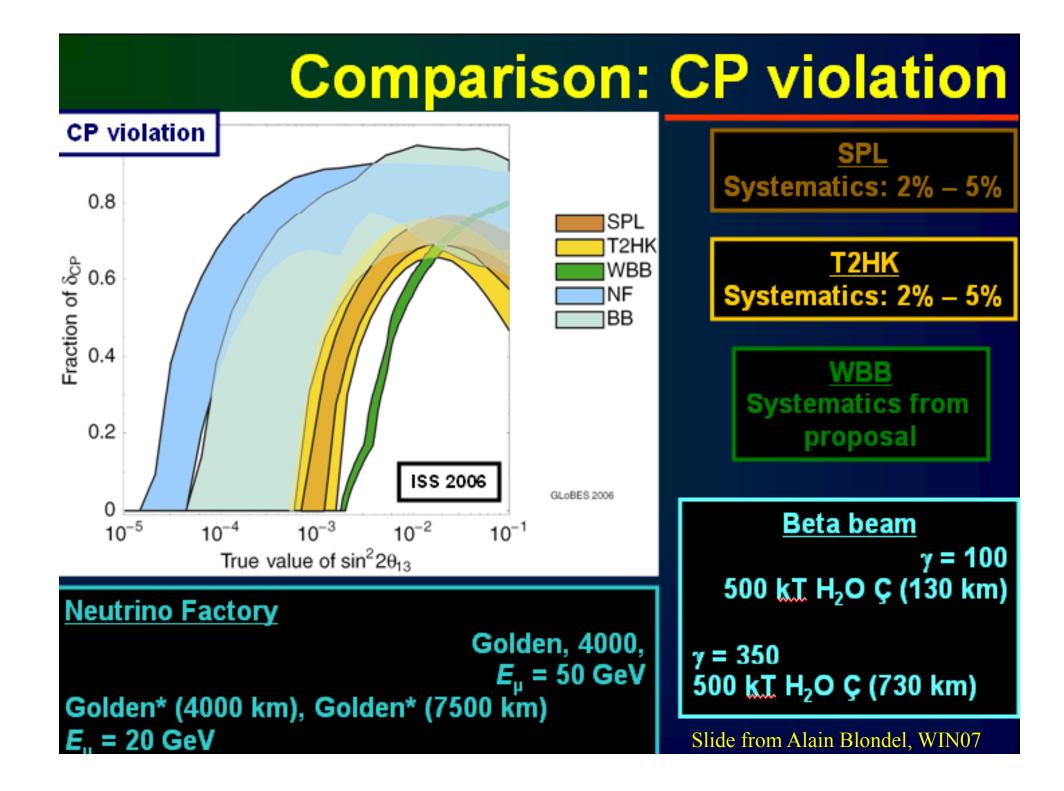
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- \checkmark We know how to build them (except for the targets).
- \checkmark The beams are "cheap" (relative to the others).
- × The beams are not pure, and not well focussed.
- × The detectors have to be huge.
- β Beams:
 - ✓ Produce pure flavour beams.
 - \checkmark Synergies with the nuclear physics programme.
 - \times If low γ , need huge detector, if high γ , expensive.

Neutrino Factory

- ✓ Most intense source.
- \checkmark Gives two beams at the same time.
- Synergies with μ -collider development.
- × \$\$\$...





Conclusions

- Neutrino oscillations are an established property of nature (and the first confirmed physics beyond the Standard Model).
 - The parameters of the MNSP and v mass matrices are windows on higher scales, and understanding them is an essential element in developing BSM particle physics.
 - The pattern emerging from experiments hints at higher symmetry, but needs better measurement!
- There is no access to this physics except through specialized facilities the LHC and ILC will not help.
- This game is just beginning and will provide a rich field of particle physics for years to come.
 - Join us!

FPCP07 Editorial Comment

- It is commonly stated that science only progresses where there are problems.
- Two of the main CP "problems" (the strong and the SUSY) arise from the failure to observe the electric dipole moment of the neutron.
- Particle EDMs (or rather the lack of them) provide some of the strongest constraints on BSM CP violation.
- No mention at this conference...
- Invite someone to Taiwan to give a talk.