

# Analysis of $\pi^-\pi^-\pi^+$ COMPASS data: role of $a_1(1260)$ meson and Deck process.

D. Ryabchikov

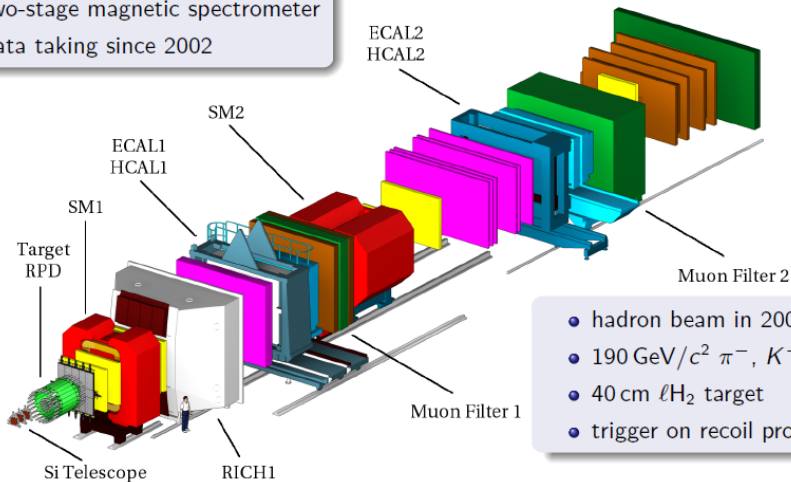
E18 Technische Universität München

The reaction  $\pi^- p \rightarrow \pi^- \pi^- \pi^+ p$  at  $p_{\pi^-} = 190$  GeV

- Mass-independent Partial-Wave Analysis (PWA)
- Mass-dependent analysis
  - brief description of the model
  - results in  $m(3\pi)$  bins
  - $a_1(1260)$  parametrization, fit results for  $M_{a_1(1260)}$ ,  $\Gamma_{a_1(1260)}$
  - results in  $t'$  bins and  $b$ -slopes of  $1^{++}$  components
- Deck process
  - Deck amplitude components
  - decomposition of Deck amplitude to partial waves and comparison with mass-dependent fits of  $3\pi$  data

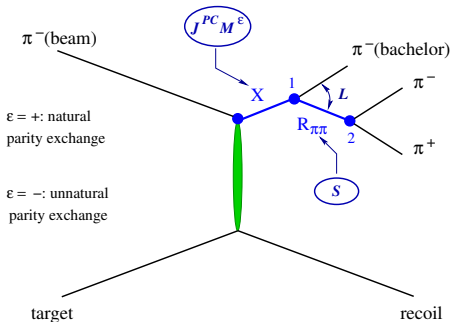
# Apparatus

- fixed target experiment
- located at CERN's SPS
- two-stage magnetic spectrometer
- data taking since 2002



- hadron beam in 2008
- $190 \text{ GeV}/c^2$   $\pi^-$ ,  $K^-$ ,  $\bar{p}$
- $40 \text{ cm } \ell\text{H}_2$  target
- trigger on recoil proton

# The reaction



- Reggeon exchange, naturality  $\eta = P_R(-1)^J$
- Gottfried-Jackson frame: SCM of  $X$ :  $Z_{GJ} \parallel \vec{p}_{beam}^*$ ,  $Y_{GJ} = [\vec{p}_{recoil}^* \times \vec{p}_{beam}^*]$
- Reflectivity basis for system of mesons:  
 $|JM\epsilon\rangle = |JM\rangle - \epsilon P(-1)^{J-M} |J-M\rangle$
- At high beam energies: reflectivity  $\epsilon$  equal to naturality  $\eta$
- unpolarised target:  $\epsilon = \pm 1$  states do not interfere

# Mass-independent vs. mass-dependent

The mass-independent PWA events density:

$$\mathcal{I}(m, t, \tau) = \sum_{\epsilon} \sum_r \left| \sum_i T_{ir}^{\epsilon}(m, t) \bar{\psi}_i^{\epsilon}(\tau, m) \right|^2 \quad (1)$$

Events intensity including production and propagation of  $3\pi$  intermediate states :

$$\mathcal{I}(m, t, \tau) = \sum_{\epsilon} \sum_r \left| \sum_i \sum_l C_{ilr}^{\epsilon} D_{il}(m, t, \zeta) \sqrt{\int |\psi_i^{\epsilon}(\tau', m)|^2 d\Phi_3(\tau')} \bar{\psi}_i^{\epsilon}(\tau, m) \right|^2 \quad (2)$$

The spin-density matrix:

$$\rho_{i,k}^{\epsilon} = \sum_r T_{ir}^{\epsilon} T_{kr}^{\epsilon*}$$

comparing (1) and (2) mass-dependent model for spin-density matrix reads:

$$\rho_{i,k}^{\epsilon}(m, t) =$$

$$\sqrt{\int |\psi_i^{\epsilon}(\tau)|^2 d\Phi_3(\tau)} \sqrt{\int |\psi_k^{\epsilon}(\tau)|^2 d\Phi_3(\tau)} \sum_r \sum_{l,m} C_{ilr}^{\epsilon} C_{kmr}^{\epsilon*} D_{il}(m, t, \zeta) D_{km}^*(m, t, \zeta)$$

# Mass-independent and mass-dependent analysis

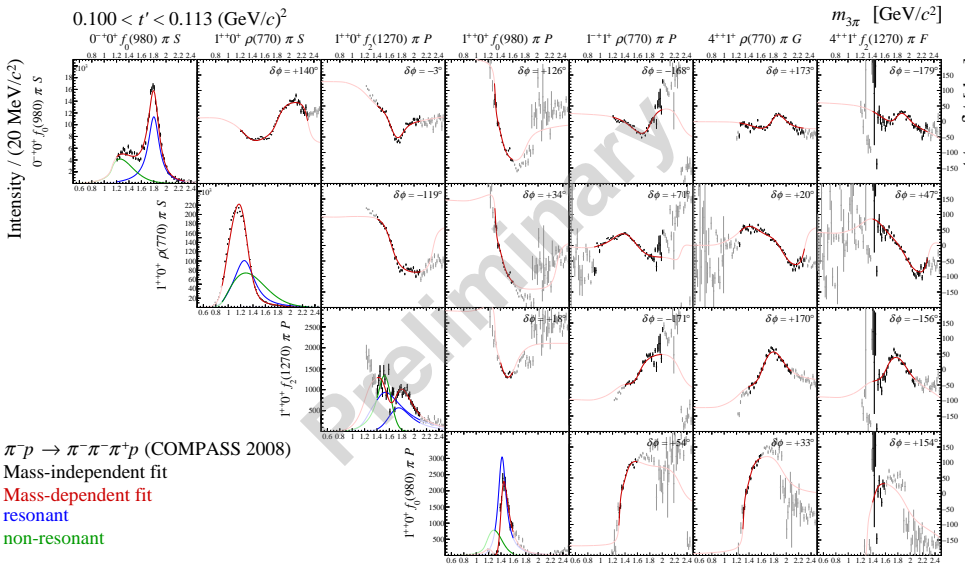
## Mass-independent:

- partial waves are labelled as  $J^{PC} M^{\epsilon} \xi \pi L$
- decay amplitudes for  $\pi^{-}\pi^{-}\pi^{+}$  are constructed in the framework of helicity formalism
- 5 standard  $\pi^{+}\pi^{-}$  isobars:  $\rho(770)$ ,  $f_2(1270)$ ,  $\rho_3(1690)$ ,  $(\pi\pi)_S$  (AMP with  $f_0(980)$  withdrawn) and  $f_0(980)$  (FLATTE)
- **rank=1** used (narrow  $m(3\pi)$  and  $t'$  bins; helicity non-flip nature of Pomeron)
- 80 waves with  $\epsilon = +1$ , 7 waves with  $\epsilon = -1$  and incoherent FLAT wave

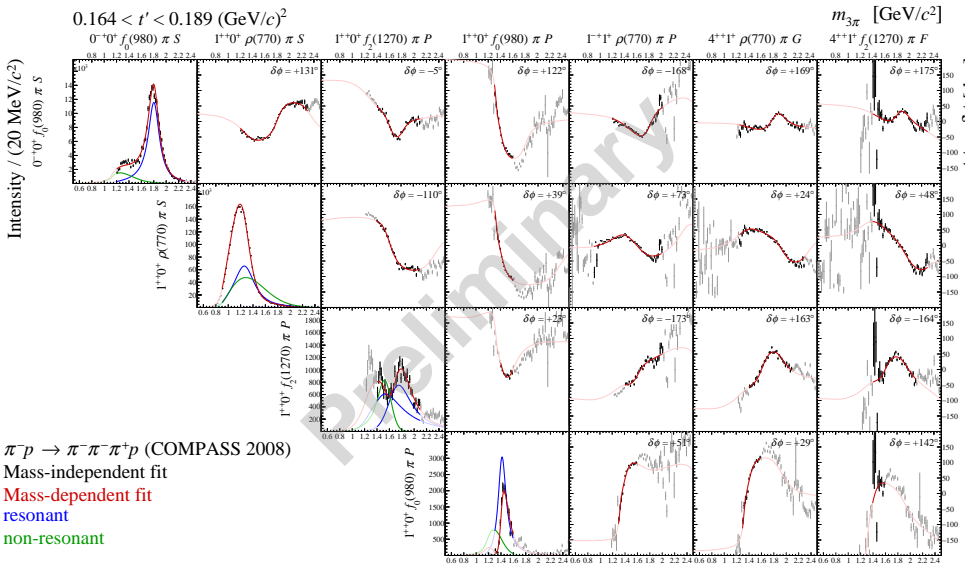
## Mass-dependent:

- **14x14** sub-density matrices measured independently in  $m(3\pi)$ -bins and  $t'$ -bins are described by resonance model
- each partial wave is described by 1-3 resonant terms and background term
- Masses, widths and decay couplings of resonances do not depend on  $t'$ , so fit should be done simultaneously in all  $t'$  intervals

# sub-density matrix in the first $t'$ bin

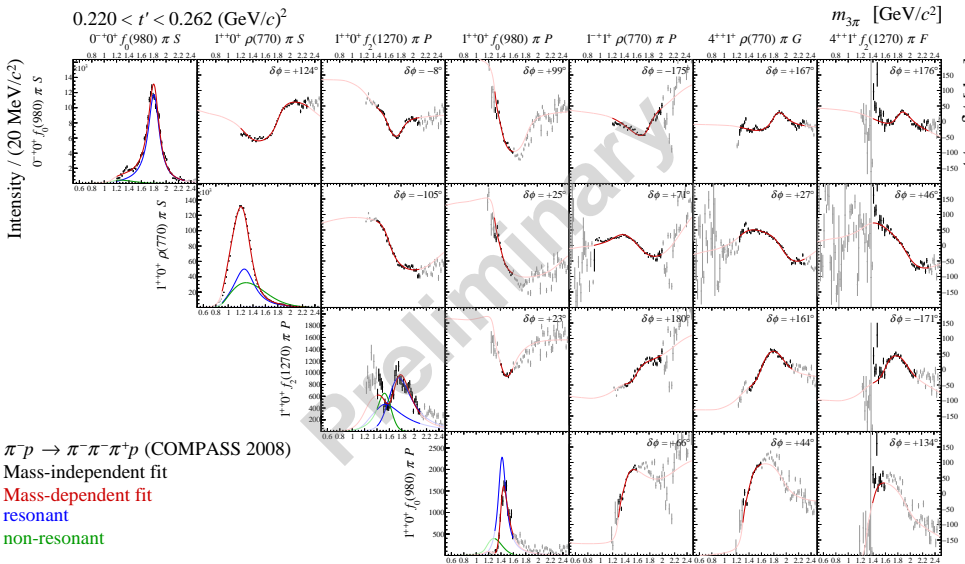


# sub-density matrix in fourth $t'$ bin





# sub-density matrix in seventh $t'$ bin



# Bowler parametrization of $a_1(1260)$ dynamical width

The dominant decay mode is assumed to be  $\rho\pi S$

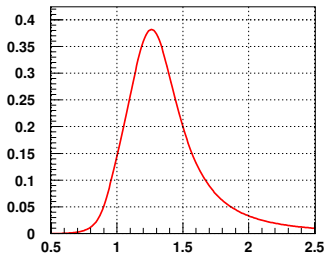
$$\Gamma(m) = \Gamma_0 \frac{m_0}{m} \frac{\int |\psi_{1^{++}\rho\pi S}(\tau, m)|^2 d\Phi_3(\tau)}{\int |\psi_{1^{++}\rho\pi S}(\tau, m_0)|^2 d\Phi_3(\tau)}$$

Intensity:

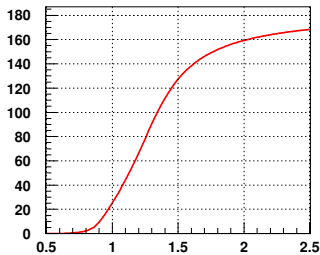
$$\mathcal{I}(m) = \frac{\Gamma(m)}{(m_0^2 - m^2)^2 + m_0^2 \Gamma(m)^2}$$

Phase:

$$\phi(m) = \arg\left(\frac{1}{m_0^2 - m^2 - im_0\Gamma(m)}\right)$$

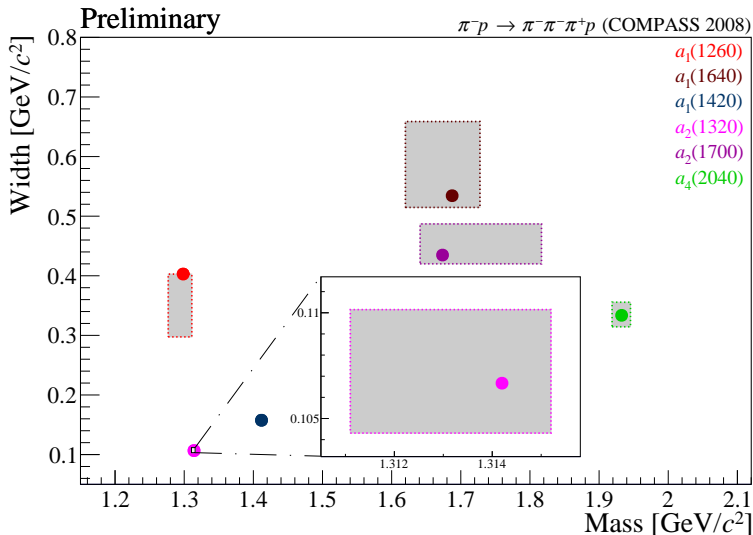


$a_1(1260)$  intens



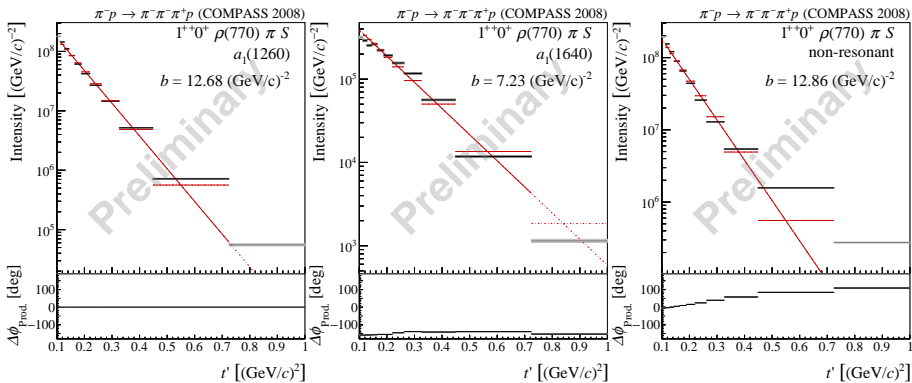
$a_1(1260)$  phase

# Parameters of $a_J$ resonances, incl. systematics



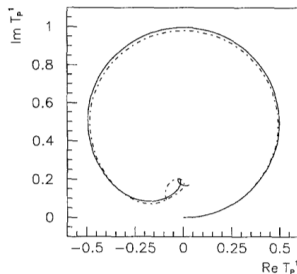
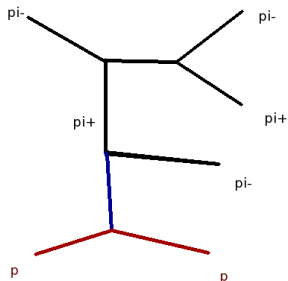
$$M_{a_1(1260)} = 1298^{+13}_{-22} \text{ MeV}, \Gamma_{a_1(1260)} = 400^{+0}_{-100} \text{ MeV}$$

# $t'$ - intensities and phases of $1^{++}0^+ \rho\pi$ components



$$b_{a_1(1260)} = 12.68^{+0.25}_{-5.25}, \quad b_{a_1(1640)} = 7.2^{+1.9}_{-0.4}, \quad b_{NR} = 12.9^{+3.5}_{-2.7}$$

# Deck process



Amplitudes for  $\pi\pi \rightarrow \pi\pi$

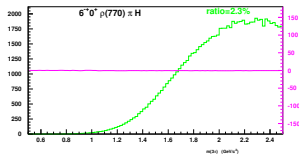
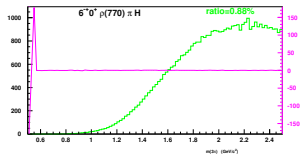
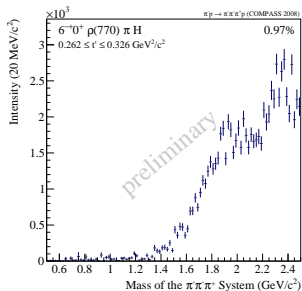
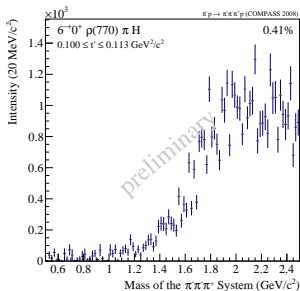
Amplitude of  $\pi^- N$  scattering:  $T_{\pi N}(s_{\pi N}, t') = s_{\pi N} e^{-8t'}$

Pion propagator:  $P(t_\pi) = \frac{m_\pi^2 e^{bt_\pi}}{m_\pi^2 - t_\pi}$  with  $b = 1.7 \text{ GeV}^{-1}$  and  $m_\pi = m_{\pi^c}$

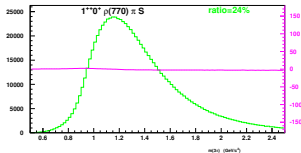
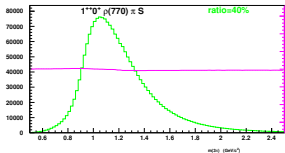
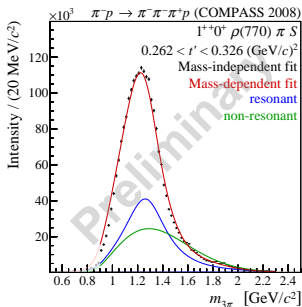
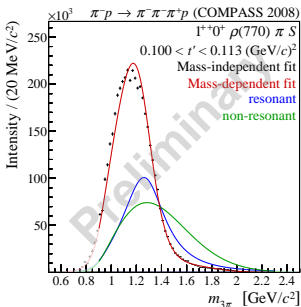
Deck decomposition to partial waves:

$$\Psi_{Deck}(\tau, m, t') \sim \sum C_i(m, t') \Psi_i(\tau, m)$$

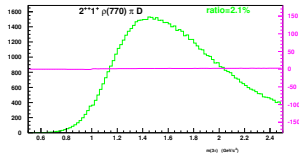
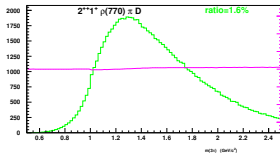
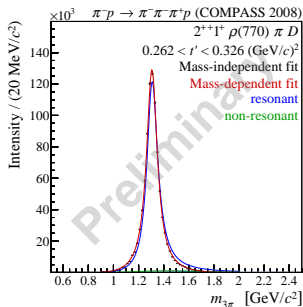
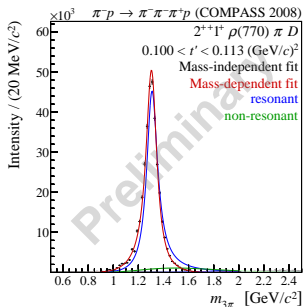
# $6^{-+}0^{+}\rho\pi H$ used to normalize Deck contribution



# $1^{++}0^+$ mass-dep fit of the data vs. Deck decomposition

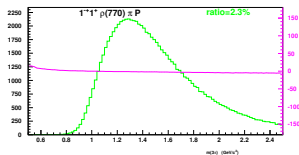
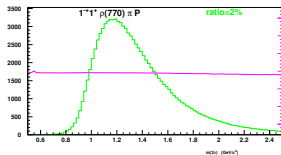
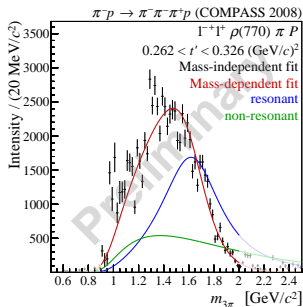
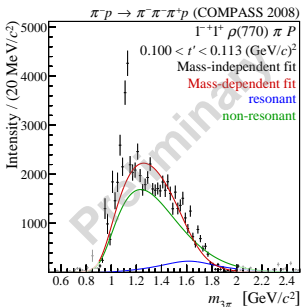


# $2^{++}1^+$ mass-dep fit of the data vs. Deck decomposition





# $1^{-+}1^{+}$ mass-dep fit of the data vs. Deck decomposition



# CONCLUSIONS

- The mass-independent PWA  $\pi^- p \rightarrow \pi^- \pi^- \pi^+ p$  of 46 000 000 events is carried out using set of 88 waves and for  $0.1 < t' < 1.0 \text{ GeV}^2$  divided into 11  $t'$  intervals
- First time the  $t'$ -resolved mass-dependent analysis of  $\pi^- \pi^- \pi^+$  is performed using **14x14** sub-density matrix
  - The extraction of resonance parameters is based on intensity shapes and relative phase motions in  $m(3\pi)$  bins
  - fitting simultaneously in set of  $t'$  intervals leads to improved separation between resonant and background components
- The  $a_1(1260)$  is observed in  $1^{++}0^+ \rho(770)\pi S$ 
  - this intensity is dominant contributing to about 30% of the total intensity
  - substantial amount of non-resonating background in  $1^{++}0^+ \rho(770)\pi S$  leads to large systematic uncertainties of  $a_1(1260)$  parameters
- The Deck mechanism is related to background processes in diffractive production of  $3\pi$ 
  - The partial-wave decomposition of Deck amplitude is performed, showing dominance of  $1^{++}0^+ \rho(770)\pi S$  with increase of its rate at lowest  $t'$
  - Deck model has contributions of high orbital moment states at high  $m(3\pi)$
  - It contributes to  $M = 1$  partial waves, this can explain, in particular, dominance of background  $\pi$  component in exotic  $J^{PC} M^e = 1^{-+}1^+ \rho\pi$  at low  $t'$