

# Revisiting gravitino dark matter in thermal leptogenesis

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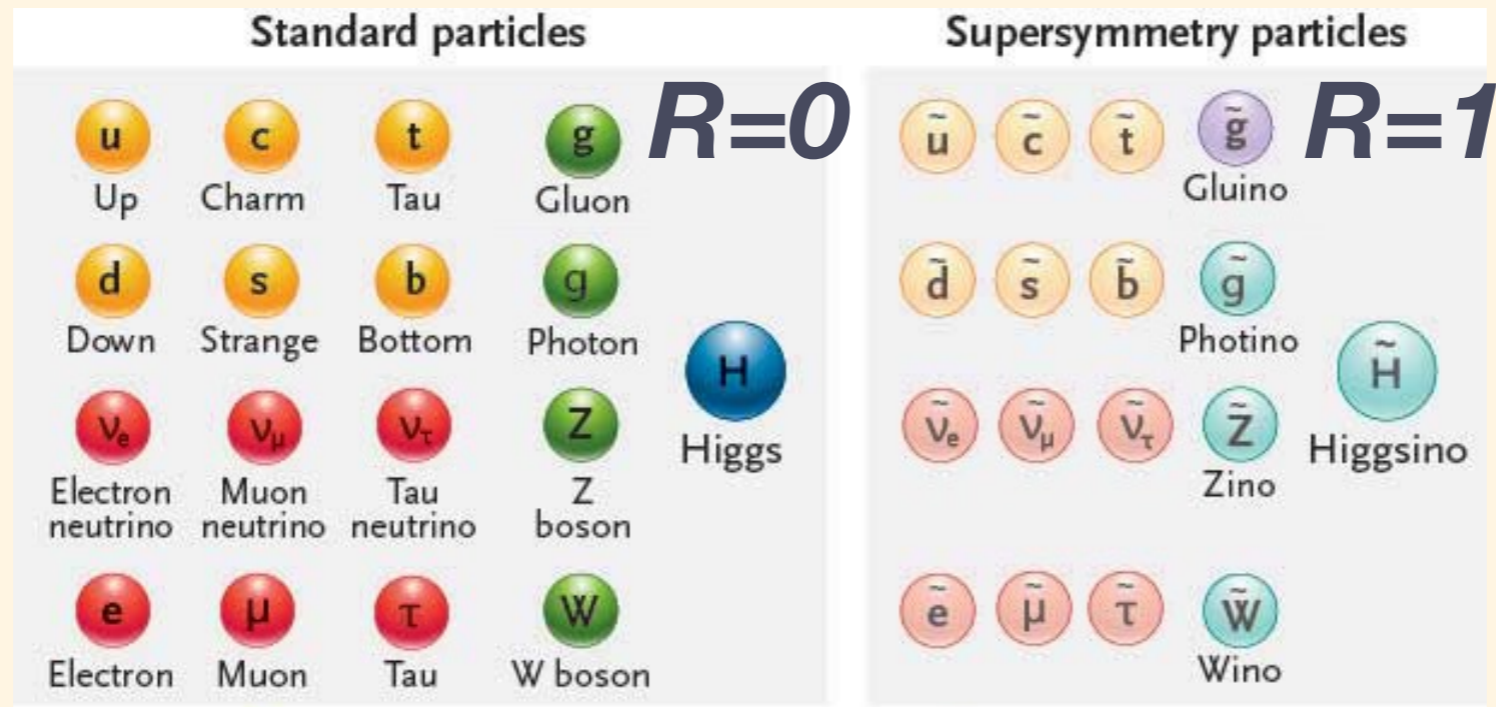
arXiv:1609.06834  
JHEP1702(2017)063

In collaboration with Masahiro Ibe and Tsutomu T. Yanagida

# R-parity

*R-parity* is introduced for *phenomenological consistency* in Minimal Supersymmetric Standard Model (MSSM)

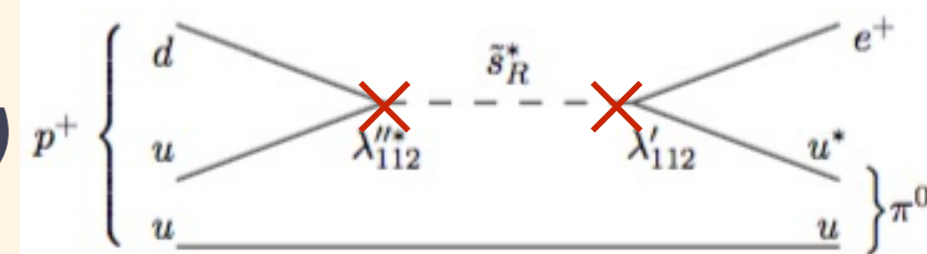
## *R-parity charge assignment*



<http://www7b.biglobe.ne.jp/~kcy05t/supersymmetry.html>

**A. Prohibiting rapid proton decay**

**B. Stable lightest SUSY particle (dark matter)**



<https://arxiv.org/abs/hep-ph/9709356>

*Do we have  
theoretical ground on R-parity?*

# Theoretical ground on R-parity

*Gravity breaks all global symmetry*



**R-parity can be embedded into gauge symmetry**

e.g. **U(1)<sub>B-L</sub>** gauge symmetry (adding NR)

**B-L parity**  $(-1)^{B-L}$  accidentally introduce **R-parity**

$$SO(10) \supset U(1)_{B-L} \supset \text{R-parity } (-1)^{B-L}$$

**R-parity is acceptable!!**

***However...***

# Theoretical ground on R-parity

*However...*

this framework has *tension* with “**perturbative  $SO(10)$  GUT**”

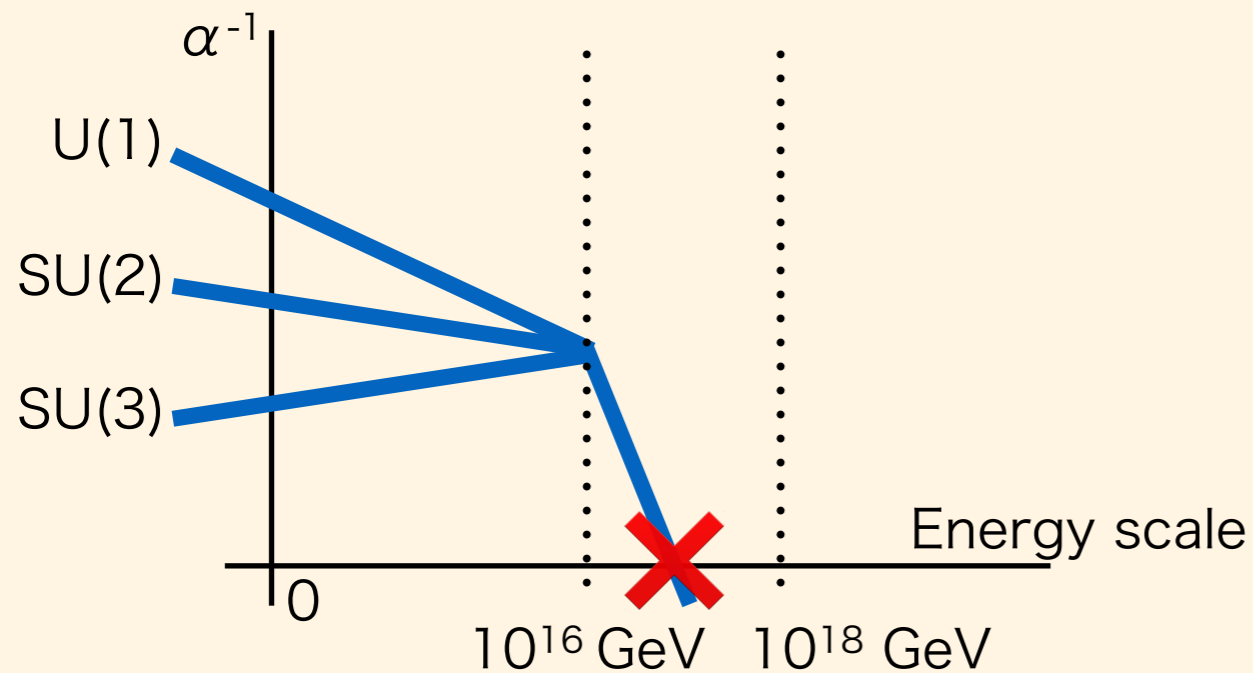
There are *two possibilities* in R-parity breaking (and neutrino mass)

## A. Unbroken R-parity

e.g. VEV of fields in 126 representation

$$\text{NR mass : } \overline{126}_H \cdot 16_M \cdot 16_M$$

$$\text{B-L : } -2 \quad +1 \quad +1$$



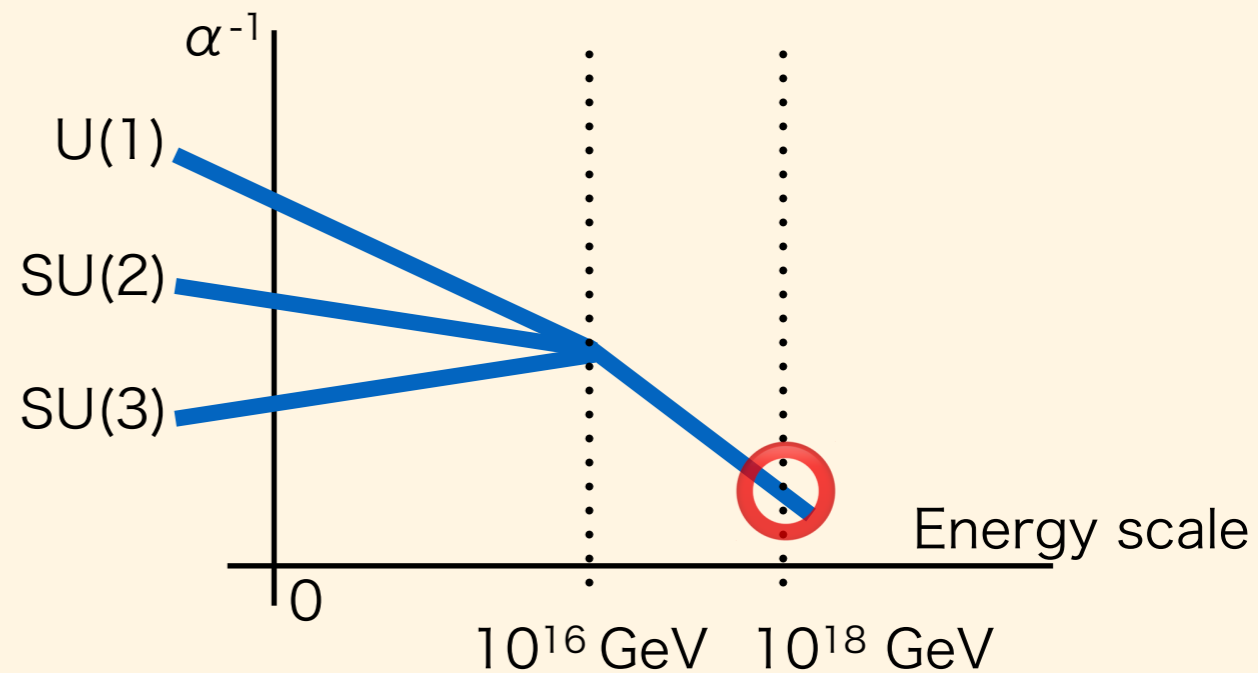
**Non-perturbative**

## B. Broken R-parity

e.g. VEV of fields in 16 representation

$$\text{NR mass : } (\overline{16}_H \cdot 16_M) (\overline{16}_H \cdot 16_M)$$

$$\text{B-L : } -1 \quad +1 \quad -1 \quad +1$$



**R-parity is broken  
in perturbative  $SO(10)$  GUT!!**

# Theoretical ground on R-parity

*However...*

this framework has *tension* with “**perturbative SO(10) GUT**”

There are *two possibilities* in R-parity breaking (and neutrino mass)

## A. Unbroken R-parity

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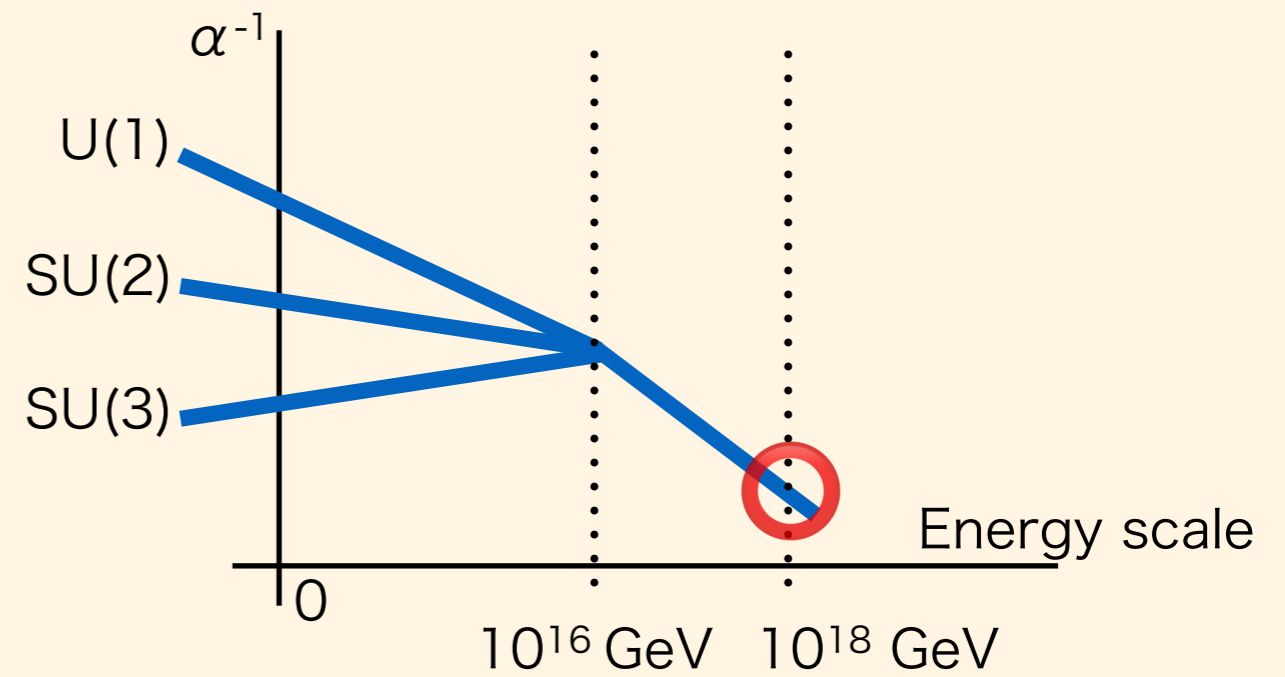
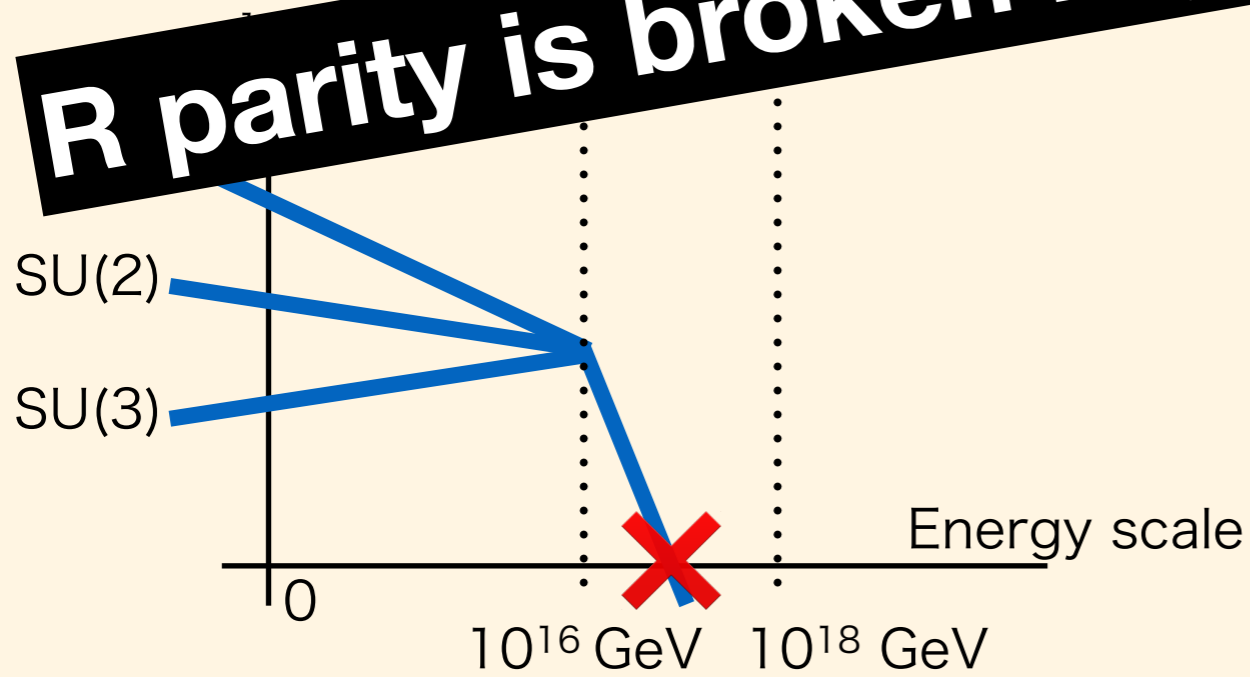
## B. Broken R-parity

e.g. VEV of fields in 10 representation

$$\overline{10}_H \cdot 16_M \cdot 16_M$$

$$\text{B-L : } -1 \quad +1 \quad -1 \quad +1$$

**R parity is broken in perturbative SO(10) GUT!!**



**R-parity is broken  
in perturbative SO(10) GUT!!**

# What is dark matter candidate in R-parity violation?

In the following,

consider **bilinear R-parity dominated case**  $W_{\mathcal{R}} = \mu'_i L_i H_u$

- **Neutralino LSP cannot be dark matter**

Neutralino lifetime  $\ll$  the age of universe ( e.g. for  $\frac{\mu'}{\mu} \sim 10^{-7}$  )

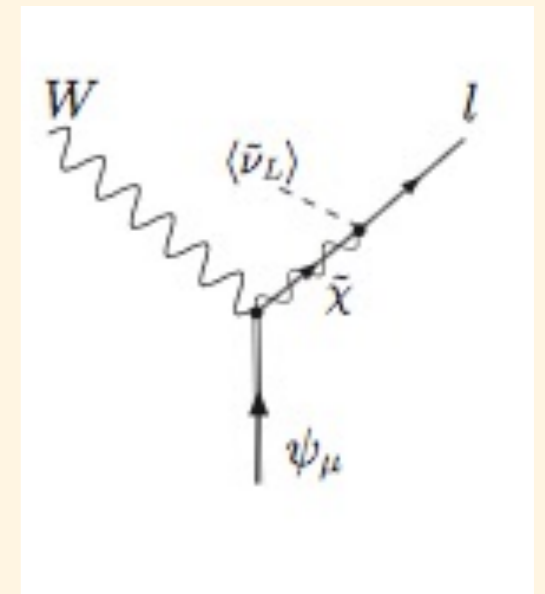
- **Gravitino LSP can be dark matter**

$$\Gamma[\psi_{3/2} \rightarrow Z\nu, h\nu, Wl] \sim \frac{m_{3/2}^3}{192\pi M_{\text{PL}}^2} \left(\frac{\mu'}{\mu}\right)^2$$

K. Ishiwata, S. Matsumoto, and T. Moroi (2008)

**Long Lifetime**

$$\begin{aligned} \tau_{3/2} &\simeq 10^{20} \text{sec} \times \left(\frac{1\text{TeV}}{m_{3/2}}\right)^3 \left(\frac{10^{-7}\mu}{\mu'}\right)^2 \\ &\gg \mathcal{O}(10^{17} \text{sec}) \end{aligned}$$



**Gravitino dark matter !!**



# Consistency

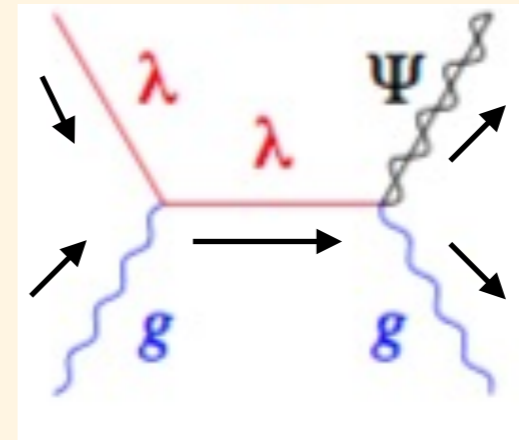
## between gravitino dark matter and baryon asymmetry

- *dark matter abundance*

$$\Omega_{3/2} h^2(m_{3/2}, m_{\tilde{g}}, T_R) \sim 0.12$$

Planck (2015)

e.g.  $T_R \sim 10^9 \text{ GeV}$ ,  $m_{3/2} \sim m_{\tilde{g}} \sim 1 \text{ TeV}$



g: gluon  
λ: gluino  
Ψ: gravitino

<https://arxiv.org/pdf/hep-ph/>

e.g. **gluon** and **gluino** collisions produce **gravitino** dark matter

- *Successful thermal leptogenesis occurs in following reheating temperature range*

$$10^9 \text{ GeV} \lesssim T_R \lesssim 10^{10} \text{ GeV}$$

W. Buchmuller *et al.* (2003)

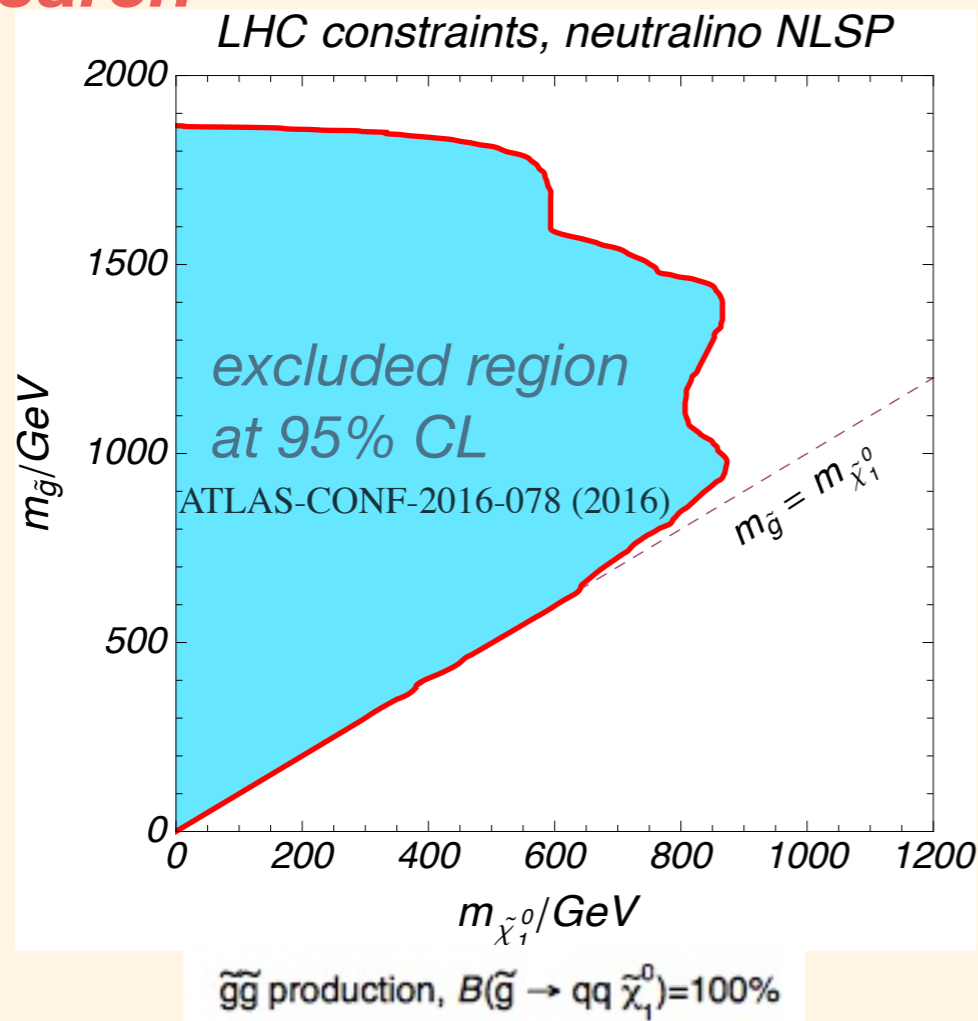
K. Kohri *et al.* (1999)

- ✓ **Dark matter abundance**
- ✓ **Baryon asymmetry**

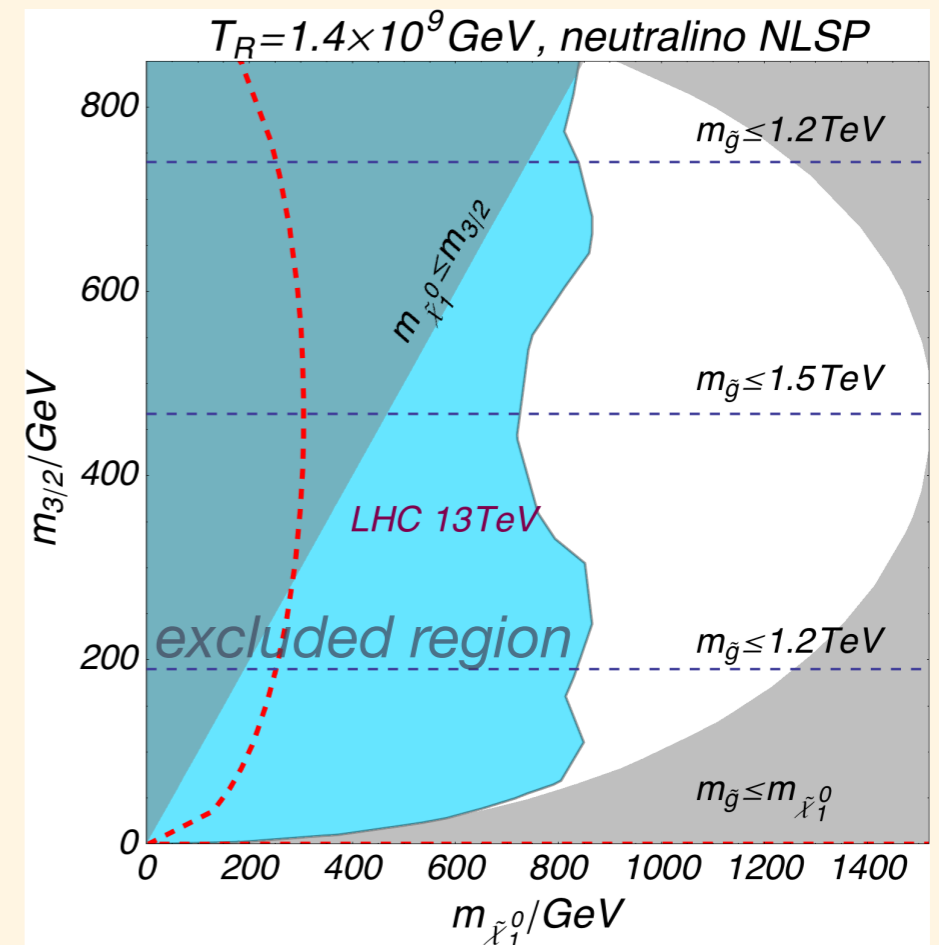
***Constraining  
gravitino dark matter  
in thermal leptogenesis***

# Collider constraints in neutralino NLSP

Neutralino NLSP stable in detector : *multi-jet with missing momentum search*



$$m_{\tilde{g}} \longrightarrow m_{3/2}$$



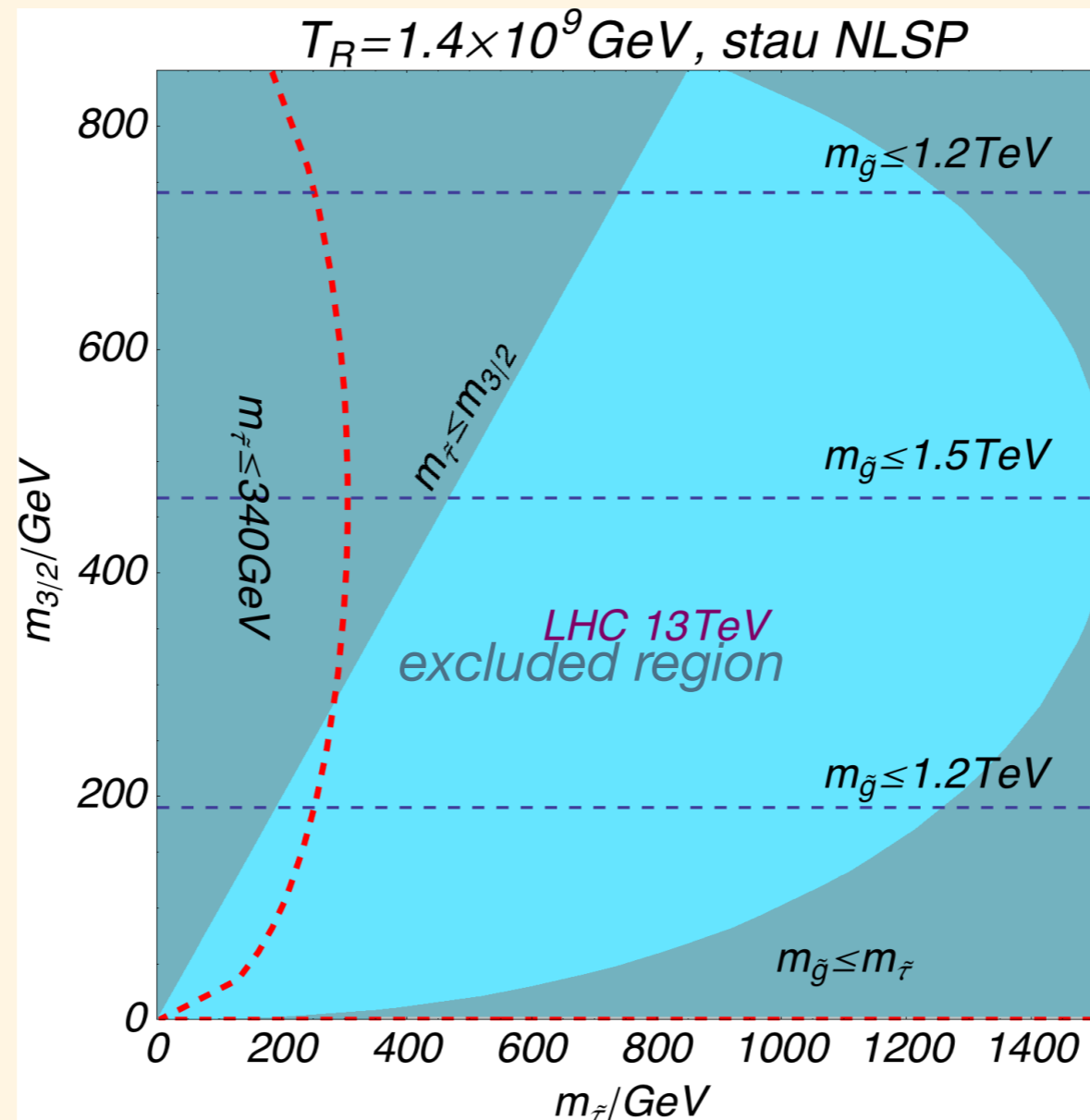
$\Omega_{3/2} h^2(m_{3/2}, m_{\tilde{g}}, T_R) |_{\text{fixed } T_R} \sim 0.12$   
 neutralino-gluino  $\rightarrow$  mass relation  $\rightarrow$  neutralino-gravitino

*neutralino mass < 700 GeV is excluded !!*

*Future LHC experiment may be able to search entire region !!*

# Collider constraints in stau NLSP

*Stau NLSP stable in detector : long-lived charged particle searches*

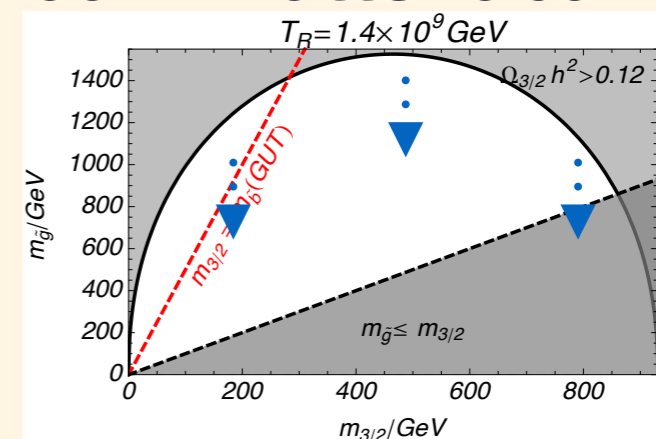


***Current LHC experiment exclude entire region !!***

# Conclusions

- R-parity can be embedded into B-L gauge symmetry
- However, R-parity can be broken in perturbative SO(10) GUT
- In R-parity violation model, gravitino is dark matter candidate
- Furthermore, gravitino dark matter consistent with thermal leptogenesis
- Future LHC may settle down this scenario; gravitino dark matter with leptogenesis
- ***If R-parity is conserved, constraints get more severe because NLSP always contributes gravitino dark matter abundance***

$$\Omega_{3/2}^{\text{tot}} h^2 = \Omega_{3/2} h^2 + Br_{3/2} \times \frac{m_{3/2}}{m_{\text{NLSP}}} \Omega_{\text{NLSP}} h^2 = 1$$



**Back Up**

# Gravitino and gluino mass relation

- **Theoretically predicted gravitino dark matter abundance**

$$\Omega_{3/2} h^2 \simeq 0.09 \left( \frac{m_{3/2}}{100 \text{ GeV}} \right) \left( \frac{T_R}{10^{10} \text{ GeV}} \right) \left( \left( 1 + 0.558 \frac{r_{\tilde{g}}^{-2} m_{\tilde{g}}^2}{m_{3/2}^2} \right) - 0.011 \left( 1 + 3.062 \frac{r_{\tilde{g}}^{-2} m_{\tilde{g}}^2}{m_{3/2}^2} \right) \log \left[ \frac{T_R}{10^{10} \text{ GeV}} \right] \right)$$

$$m_{\tilde{g}} = r_{\tilde{g}} m_{1/2}$$

$$r_{\tilde{g}} \sim 2.5$$

- **Gravitino and gluino mass relation from dark matter abundance**

$$\Omega_{3/2} h^2 |_{T_R} \sim 0.12$$

$$m_{3/2} \leftrightarrow m_{\tilde{g}}$$

# B-L parity breaking and R-parity breaking

*Broken B-L parity*

$$\langle 16_H \rangle = v_{B-L}$$

*Broken B-L parity induce Broken R parity*

$$\begin{aligned} \text{e.g. } W &\sim \epsilon 16_H 16_M 10_H \\ &\sim \epsilon v_{B-L} 16_M 10_H \\ &\sim \epsilon v_{B-L} L H_u \end{aligned}$$

$10_H$  : SM higgs

$16_M$  : SM matter

$16_H$  : B-L breaking higgs

$\epsilon$  : (small) coupling

**Bilinear R-parity breaking!!**

***B-L parity breaking*  $\longleftrightarrow$  *Bilinear R-parity breaking***

**R parity is broken in perturbative SO(10) GUT!!**



# R-parity violation and its constraints

## *R-parity violating superpotential*

$$W_{\cancel{R}} = \lambda_{ijk} \cancel{D}_i^c Q_j L_k + \frac{1}{2} \lambda'_{ijk} L_i \cancel{E}_j^c L_k^c + \frac{1}{2} \lambda''_{ijk} \cancel{D}_i^c U_j^c \cancel{D}_k^c$$

~~B-L~~ → ~~L~~ ~~B~~

$$+ \mu'_i L_i H_u \quad i, j, k : \text{generation indices}$$

~~L~~

## Constraints

- **Erase of baryon asymmetry** K. Hamaguchi *et al.* (2010)

$$\lambda, \lambda', \lambda'', \mu' / \mu < \mathcal{O}(10^{-(6-7)})$$

- **Rapid proton decay**

$$|\lambda' \lambda''| < 10^{-25} \left( \frac{m_{\text{SUSY}}}{1 \text{ TeV}} \right)^2 \quad (\tau_{p^+ \rightarrow e^+ \pi^0} \gtrsim 10^{34} \text{ year})$$

K. Abe *et al.* (2011)

***R-parity violation must be small***

# What is dark matter candidate in R-parity violation?

In the following,

consider **bilinear R-parity dominated case**

- **Neutralino LSP cannot be dark matter**

**Neutralino lifetime  $\ll$  the age of universe ( e.g. for  $\frac{\mu'}{\mu} \sim 10^{-7}$  )**

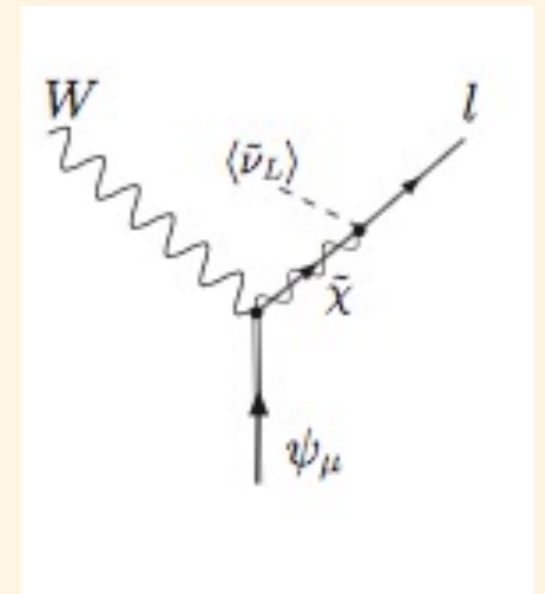
- **Gravitino LSP can be dark matter**

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K. Ishiwata, S. Matsumoto, and T. Moroi (2008)

**Long Lifetime**

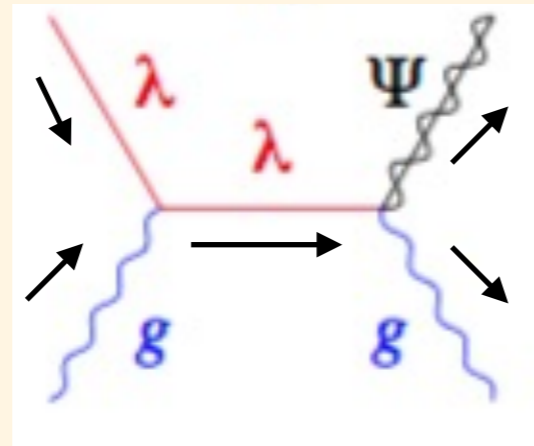
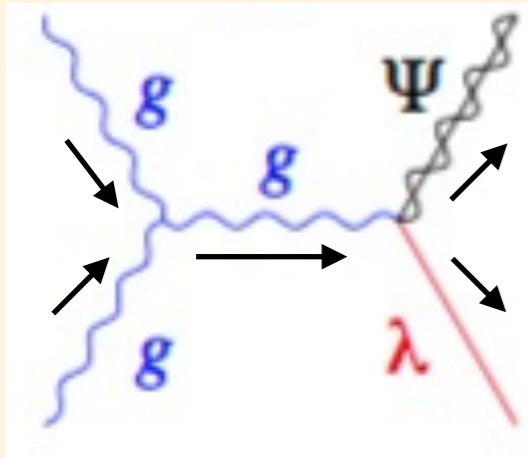
$$\begin{aligned} \tau_{3/2} &\simeq 10^{20} \text{sec} \times \left(\frac{1\text{TeV}}{m_{3/2}}\right)^3 \left(\frac{10^{-7}\mu}{\mu'}\right)^2 \\ &\gg \mathcal{O}(10^{17} \text{sec}) \end{aligned}$$



**Gravitino dark matter !!**

# Gravitino dark matter abundance

e.g. **gluon** and **gluino** collisions produce **gravitino** dark matter



g: gluon  
λ: gluino  
Ψ: gravitino

<https://arxiv.org/pdf/hep-ph/0701104.pdf>

## Thermally produced gravitino dark matter abundance

J. Ellis *et al.* (2016)

$$\Omega_{3/2} h^2 \simeq 0.09 \left( \frac{m_{3/2}}{100 \text{ GeV}} \right) \left( \frac{T_R}{10^{10} \text{ GeV}} \right) \left( \left( 1 + 0.558 \frac{r_{\tilde{g}}^{-2} m_{\tilde{g}}^2}{m_{3/2}^2} \right) - 0.011 \left( 1 + 3.062 \frac{r_{\tilde{g}}^{-2} m_{\tilde{g}}^2}{m_{3/2}^2} \right) \log \left[ \frac{T_R}{10^{10} \text{ GeV}} \right] \right)$$

$$m_{\tilde{g}} = r_{\tilde{g}} m_{1/2}$$

# Assumption

## A. Bilinear R-parity violation

$$\frac{\mu'}{\mu} < 10^{-11} \times \left( \frac{1\text{TeV}}{m_{3/2}} \right)^{3/2}$$

E, Carquin *et.al.* (2016)  
S. Ando and K. Ishiwata(2016)

## B. gravitino dark matter in thermal leptogenesis

## C. $m_{3/2} < 1 \text{ TeV}, \quad 10^9 \text{ GeV} < T_R < 10^{10} \text{ GeV}$

Searching this scenario

# **Gluino mass upper bound**

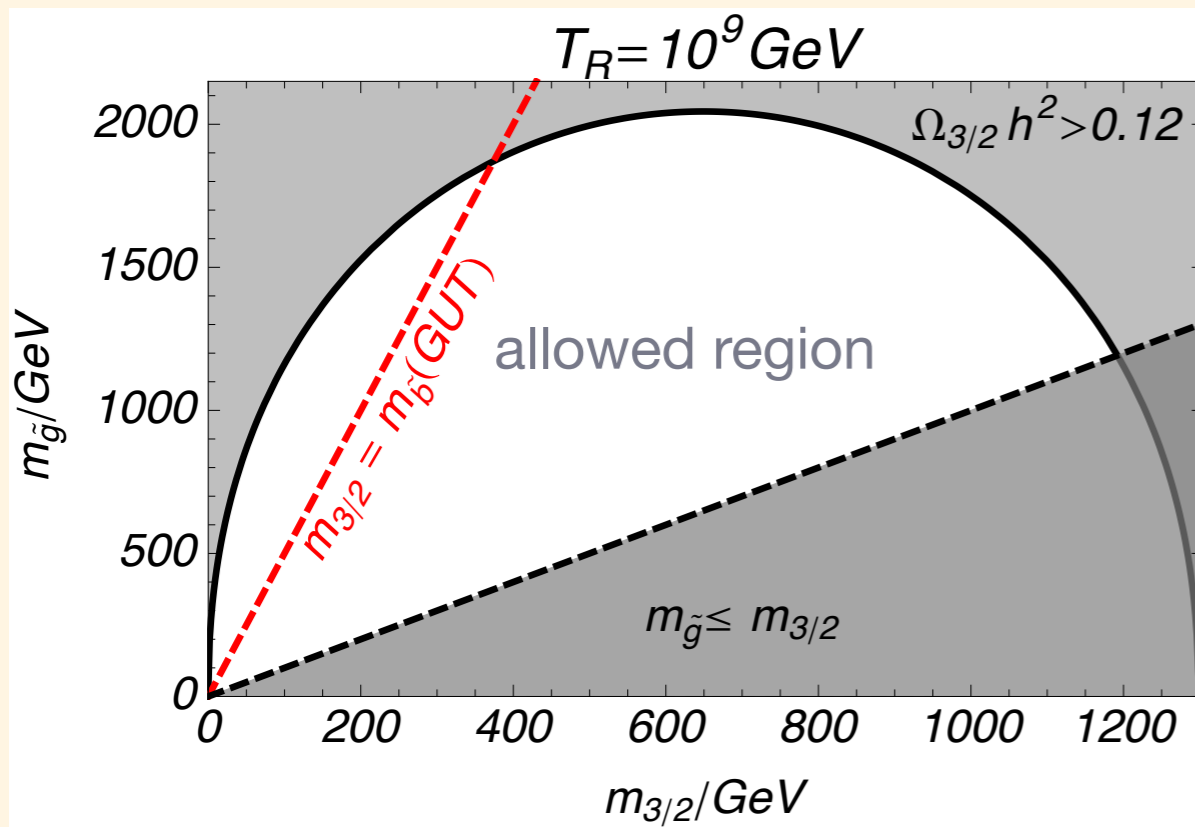
# Glino mass upper bound

$$\Omega_{3/2} h^2 |_{T_R} \sim 0.12$$

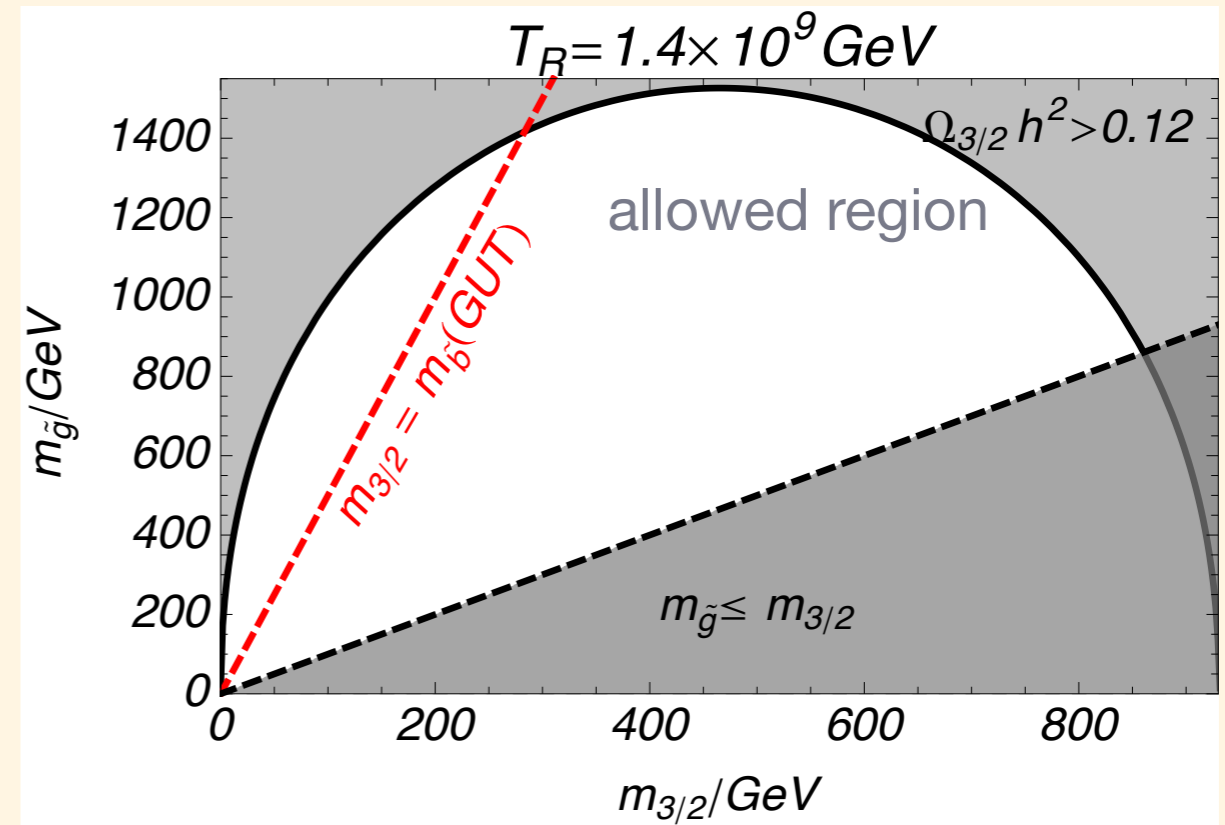
## Latest reheating temperature upper bound in thermal leptogenesis

$$T_R \lesssim 1.4 \times 10^9 \text{ GeV}$$

S. Antusch and A. M. Teixeira (2006)



$$m_{\tilde{g}} < 2 \text{ TeV}$$



$$m_{\tilde{g}} < 1.6 \text{ TeV}$$

# LHC constraints

# NLSP contribution into dark matter abundance

Gravitino dark matter abundance from NLSP decay

$$\Omega_{3/2}^{\text{tot}} h^2 = \Omega_{3/2} h^2 + Br_{3/2} \times \frac{m_{3/2}}{m_{\text{NLSP}}} \Omega_{\text{NLSP}} h^2 .$$

- R-parity conserving decay into gravitino

$$\tau_{\text{NLSP}}^R \simeq 5 \times 10^3 \text{sec} \left( \frac{m_{3/2}}{100 \text{GeV}} \right)^2 \left( \frac{1 \text{TeV}}{m_{\text{NLSP}}} \right)^5 .$$

- R-parity violating decay into the other SM particles

$$\tau_{\text{NLSP}}^{\cancel{R}} \simeq 10^{-12} \text{sec} \left( \frac{10^{-7} \mu}{\mu'} \right)^2 \left( \frac{1 \text{TeV}}{m_{\text{NLSP}}} \right)$$

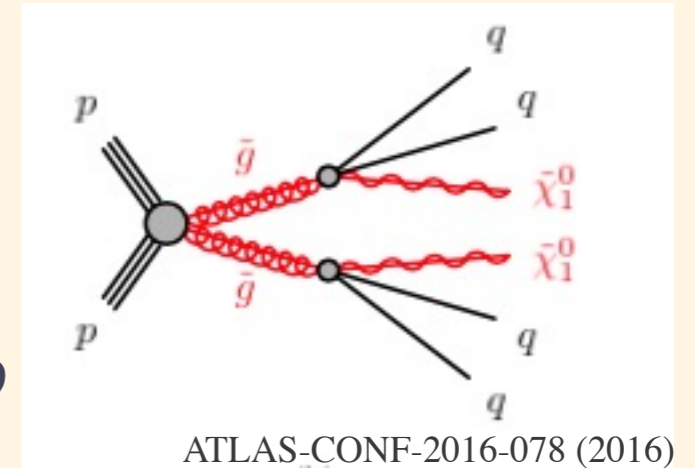
$$\tau_{\text{NLSP}}^{\cancel{R}} \ll \tau_{\text{NLSP}}^R$$

**NLSP contribution is negligible for dark matter abundance**



# Neutralino NLSP

- **Neutralino production by gluino decay**
  - **all squark decoupled limit**
  - **no mass degeneracy**
  - **gluino decaying into two squarks and a neutralino**



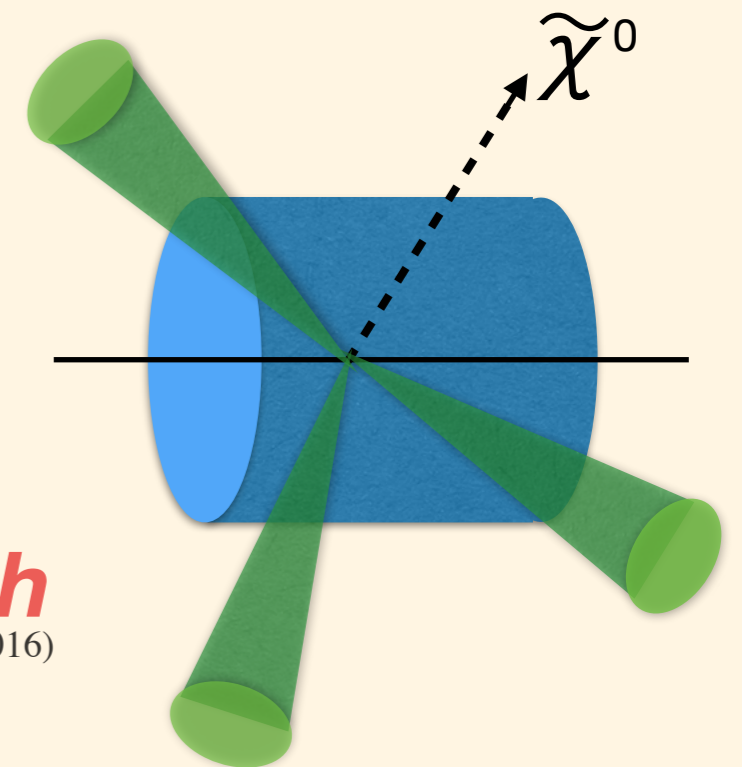
- **Neutralino stable in detector**

$$c\tau_{\tilde{\chi}_1^0} \gtrsim 10^6 \text{ m} \times \left( \frac{1\text{TeV}}{m_{\tilde{\chi}_1^0}} \right)^3 \left( \frac{10^{-11}\mu}{\mu'} \right)^2 \left( \frac{10}{\tan\beta} \right)^2 .$$

K. Hamaguchi *et al.* (2007)

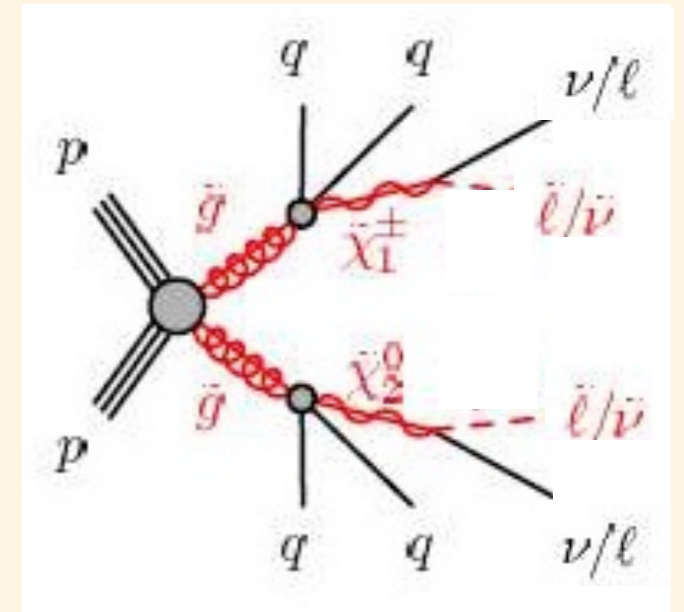
→ **multi-jet with missing momentum search**

ATLAS-CONF-2016-078 (2016)



# Stau NLSP

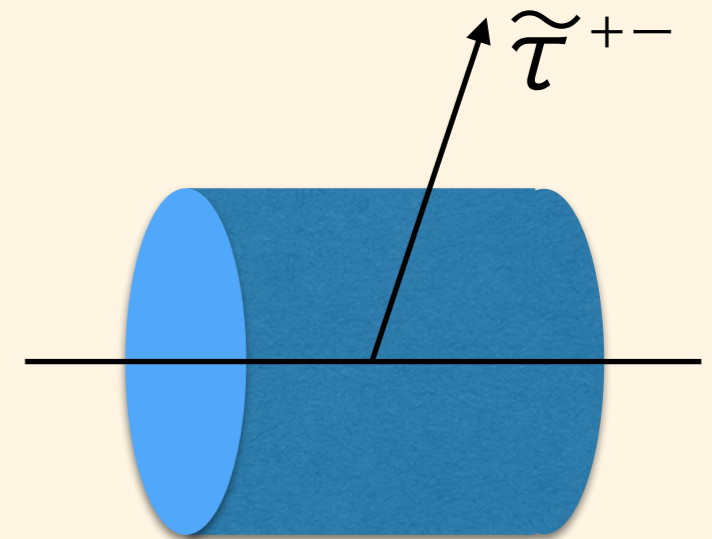
- **Stau production**
  - *all squark decoupled limit*
  - *no mass degeneracy*
  - *stau cross section* ← *gluino cross section*
  - *direct Drell-Yan stau pair production*



- **Stau stable in detector**

$$c\tau_{\tilde{\tau}} \gtrsim 10^7 \text{ m} \times \left( \frac{1\text{TeV}}{m_{\tilde{\tau}}} \right) \left( \frac{10^{-11}\mu}{\mu'} \right)^2 \left( \frac{10}{\tan\beta} \right)^2 .$$

K. Hamaguchi *et al.* (2007)

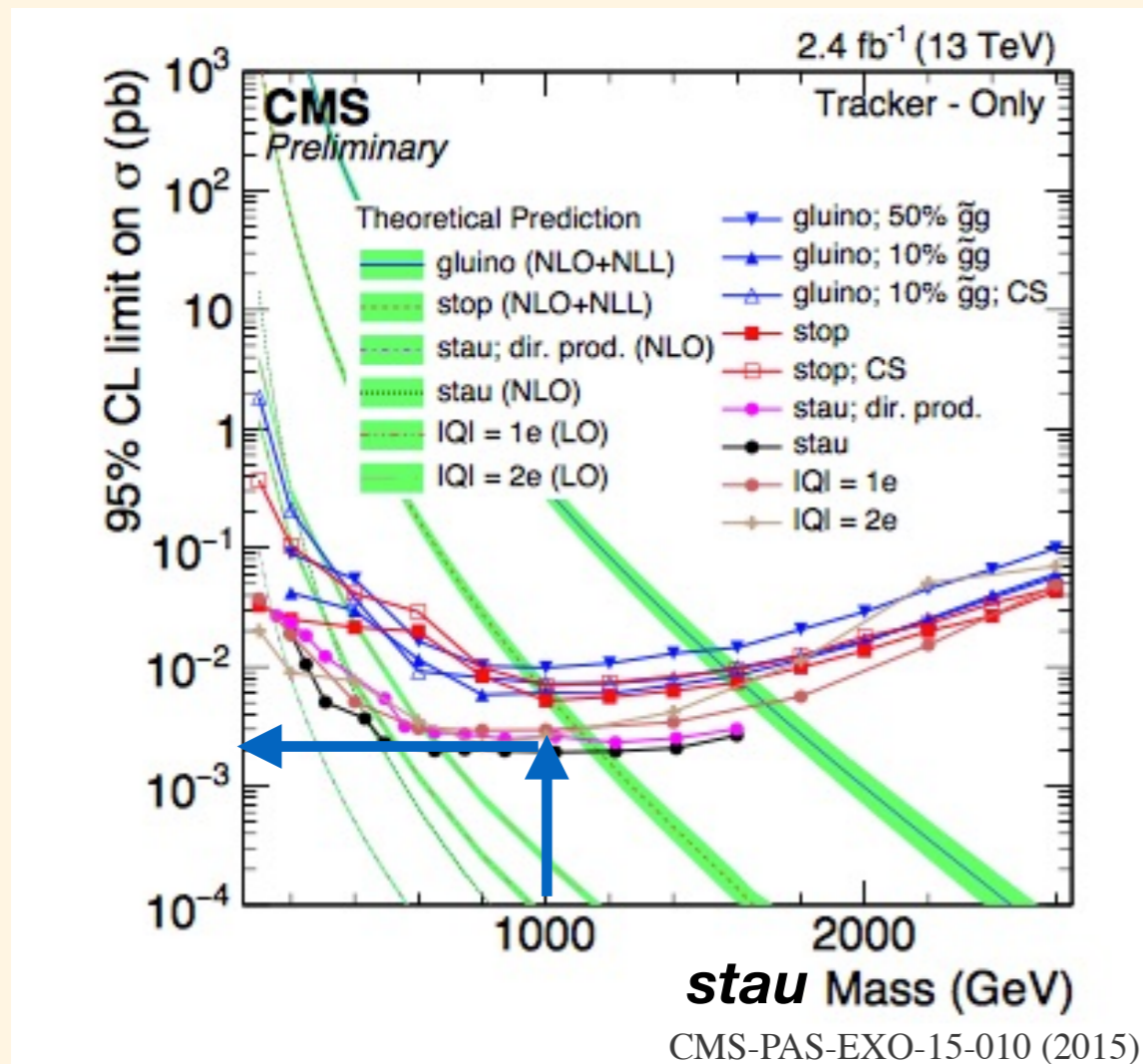


→ **long-lived charged particle searches**

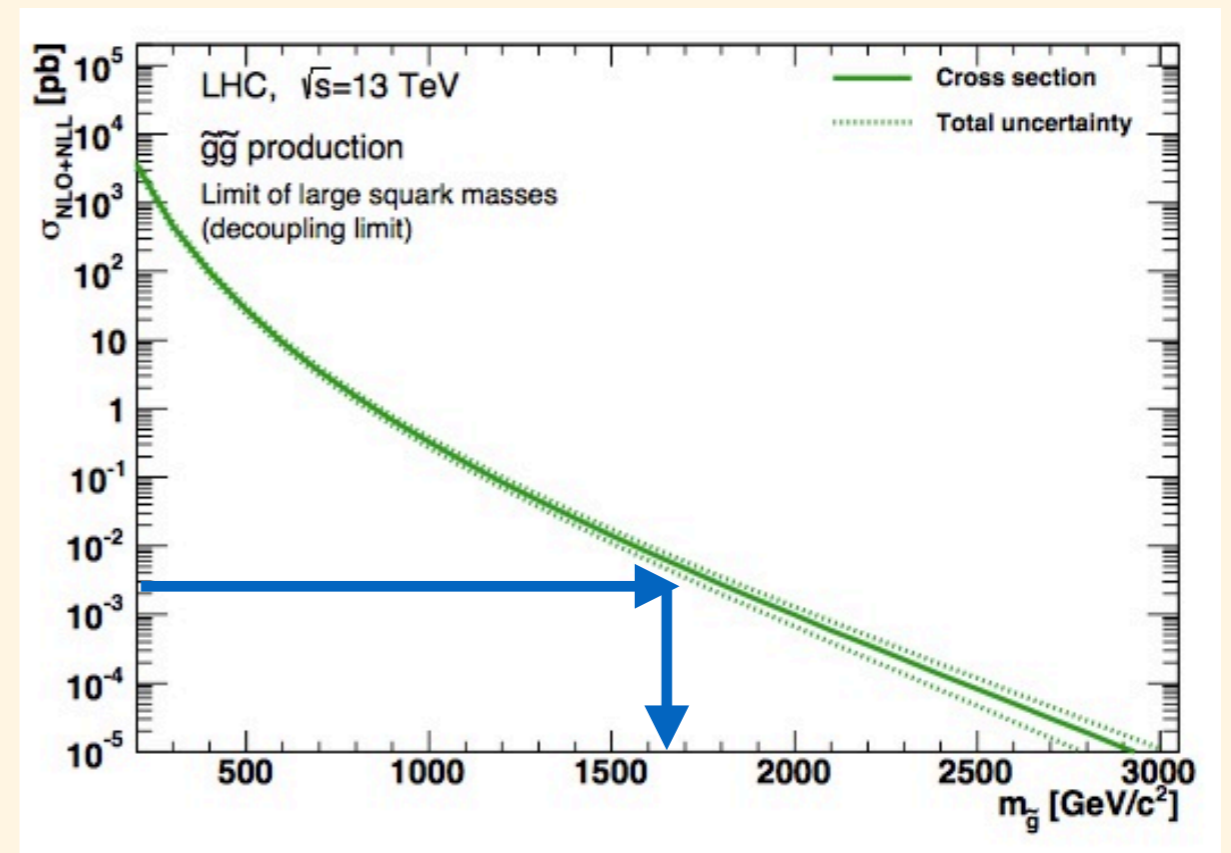
CMS-PAS-EXO-15-010 (2015)

# Stau and gluino constraint

## Stau cross section upper limit



## Gluino production cross section

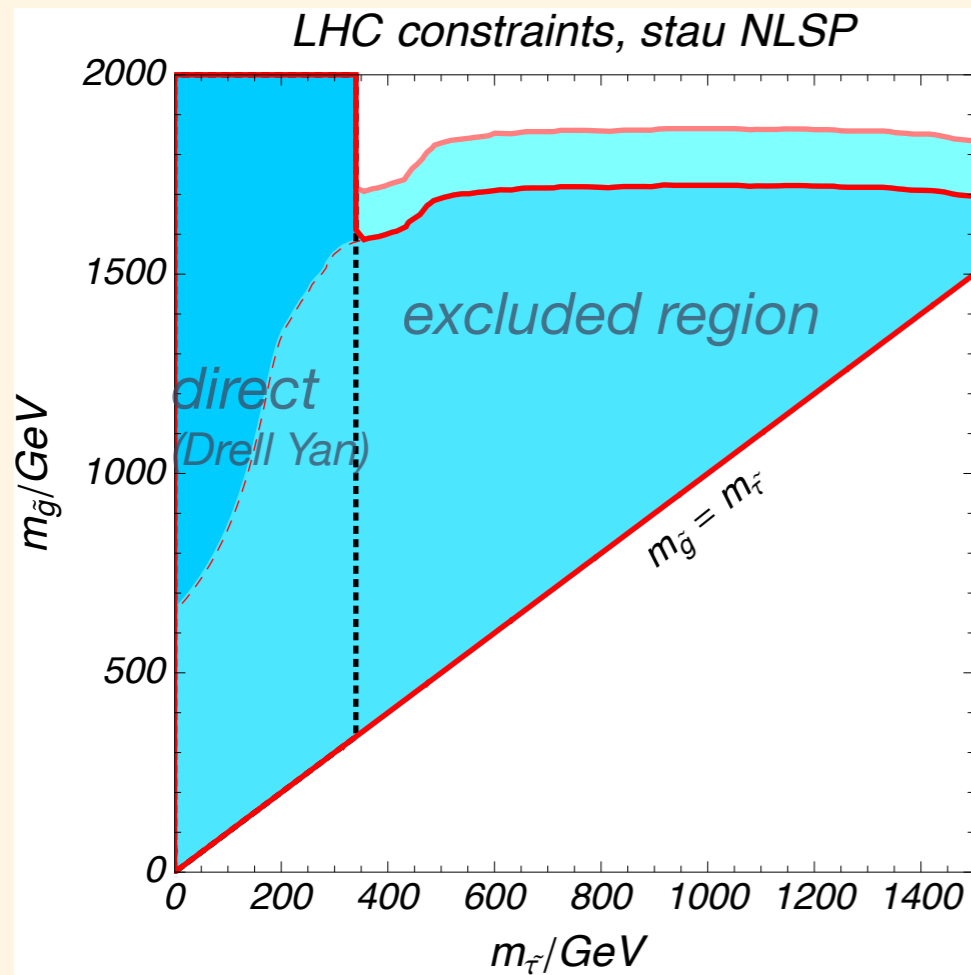


C. Borschensly *et al.* (2014)

**Gluino and stau mass constraint by**  
**Stau cross section upper bound > Gluino production cross section**

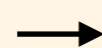
# Collider constraints in stau NLSP

## Gluino and stau mass constraint

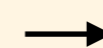


direct + gluino decay

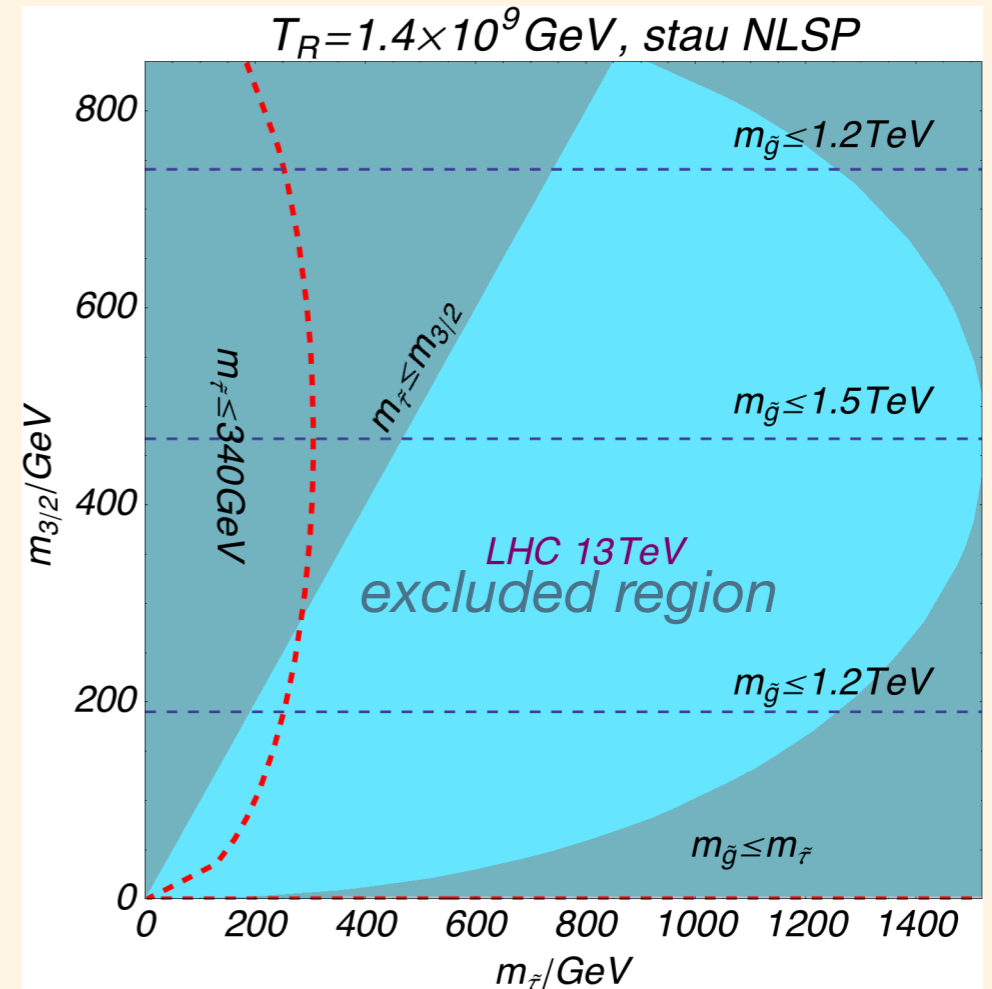
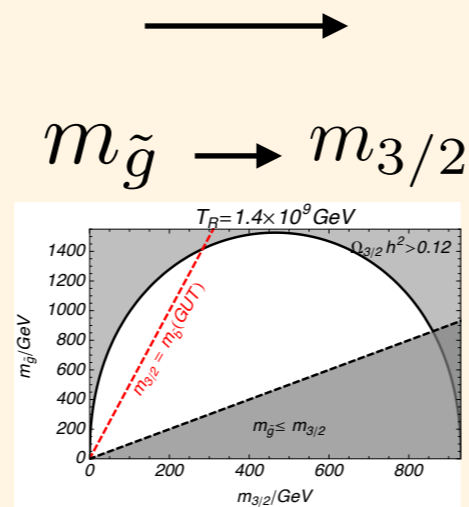
stau-gluino



mass relation

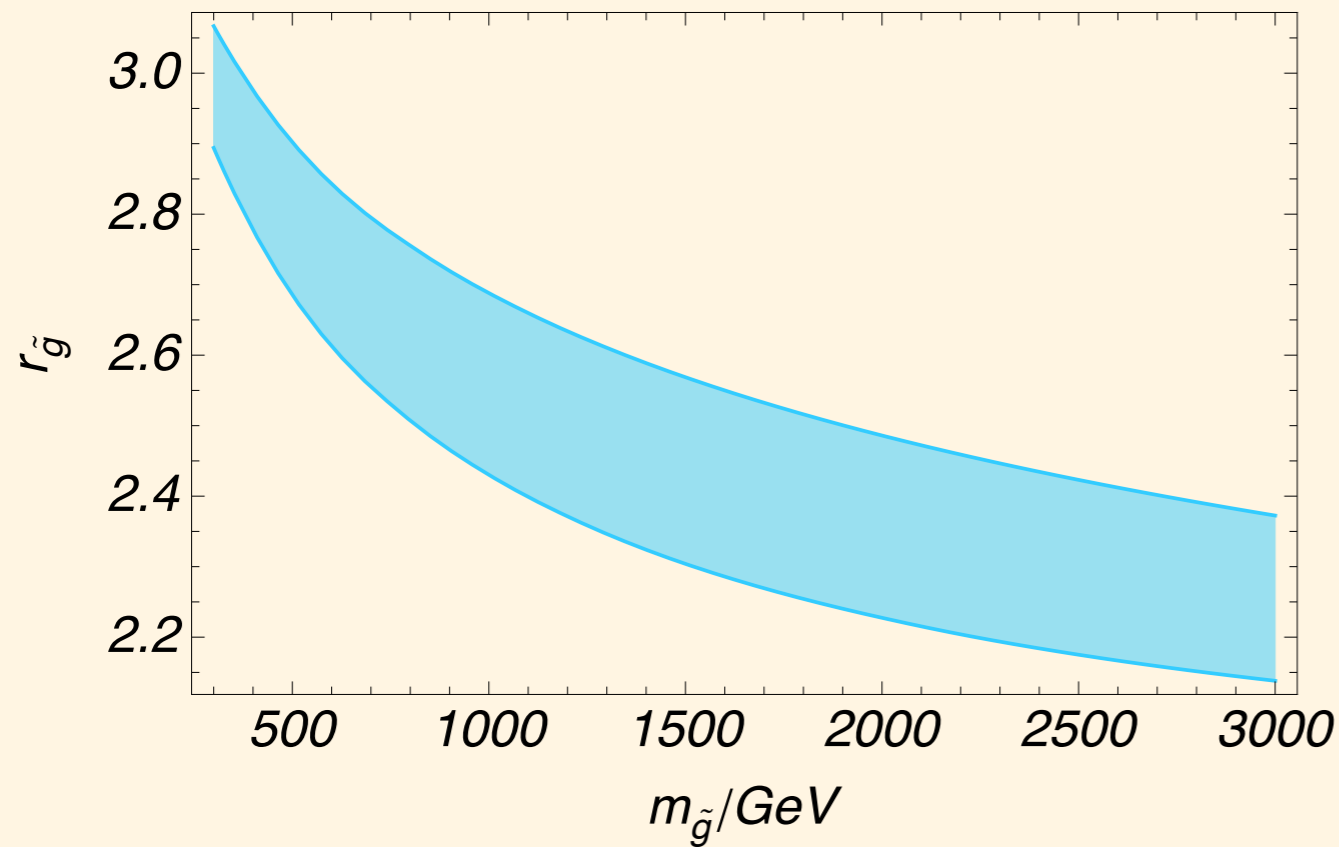


stau-gravitino



**Current LHC experiment exclude entire region !!**

# Physical gluino mass and gaugino mass at GUT scale



$$m_{\tilde{g}} = r_{\tilde{g}} m_{1/2}$$

$$\Omega_{3/2} h^2 \simeq 0.09 \left( \frac{m_{3/2}}{100 \text{ GeV}} \right) \left( \frac{T_R}{10^{10} \text{ GeV}} \right) \left( \left( 1 + 0.558 \frac{r_{\tilde{g}}^{-2} m_{\tilde{g}}^2}{m_{3/2}^2} \right) - 0.011 \left( 1 + 3.062 \frac{r_{\tilde{g}}^{-2} m_{\tilde{g}}^2}{m_{3/2}^2} \right) \log \left[ \frac{T_R}{10^{10} \text{ GeV}} \right] \right)$$

# R-parity violation model in SO(10)

	$\mathbf{16}_M$	$\mathbf{10}_H$	$\mathbf{16}_H$	$\overline{\mathbf{16}}_H$	$v_{B-L}$	$X$	$m_{3/2}$
$R$	1	0	$-1/2$	0	$-1/4$	$5/2$	2

Table 1:  $R$ -charges of matter fields, Higgs fields and  $SO(10)$  singlets.

## A. Superpotential

$$W = \underbrace{\mathbf{10}_H \mathbf{16}_M \mathbf{16}_M}_{\text{Yukawa term}} + \underbrace{\overline{\mathbf{16}}_H \overline{\mathbf{16}}_H \mathbf{16}_M \mathbf{16}_M}_{\substack{\text{vR mass term} \\ \text{Bilinear R-parity breaking term}}} + X \underbrace{(\mathbf{16}_H \overline{\mathbf{16}}_H - v_{B-L}^2)}_{\text{B-L breaking}}$$

## B. Bilinear R-parity violation by right-handed sneutrino VEV

$$K = v_{B-L}^4 \mathbf{16}_M \overline{\mathbf{16}}_H$$

$$\rightarrow W \sim m_{3/2} v_{B-L}^5 N_R \rightarrow \langle \tilde{N}_R \rangle \simeq v_{B-L}^3 \times m_{3/2} \rightarrow \mu' = v_{B-L}^3 m_{3/2}$$

## C. mu-term

$$W \sim m_{3/2} \mathbf{10}_H \mathbf{10}_H$$

Finally,

$$\frac{\mu'}{\mu} \sim v_{B-L}^3$$

# R-parity violation model in SO(10)

	$\mathbf{16}_M$	$\mathbf{10}_H$	$\mathbf{16}_H$	$\overline{\mathbf{16}}_H$	$v_{B-L}$	$X$	$m_{3/2}$
$R$	1	0	$-1/2$	0	$-1/4$	$5/2$	2

Table 1:  $R$ -charges of matter fields, Higgs fields and  $SO(10)$  singlets.

- **Bilinear  $R$ -parity violation**

$$W \sim \mathbf{16}_M \overline{\mathbf{16}}_H$$

- **Trilinear  $R$ -parity violation**

$$W \sim \mathbf{16}_H \mathbf{16}_M \mathbf{16}_M \mathbf{16}_M$$

**Small  $R$ -parity violation!!**

$$\frac{\mu'}{\mu}, \lambda, \lambda', \lambda'' \sim v_{B-L}^3 \quad (v_{B-L} \sim 10^{-3 \sim -4})$$