

3ν masses, mixings and phases, circa 2017

Invisibles 2017 Workshop, Zurich, 12-16 June



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Mainly based on:

F. Capozzi, E. Di Valentino, E. Lisi, A. Marrone, A. Melchiorri, A. Palazzo,
“Global constraints on absolute neutrino masses and their ordering”

arXiv:1703.04471 [PRD 95, 096014 (2017)]

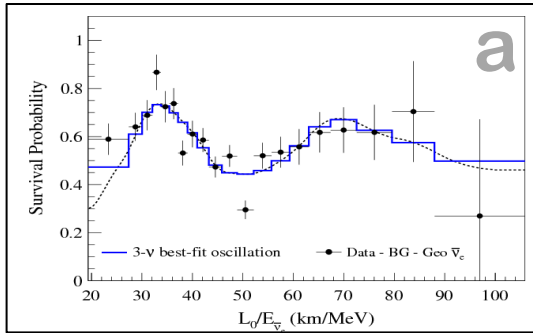
[For an independent analysis of recent oscillation data, see I. Esteban *et al.*, 1611.01514]

OUTLINE:

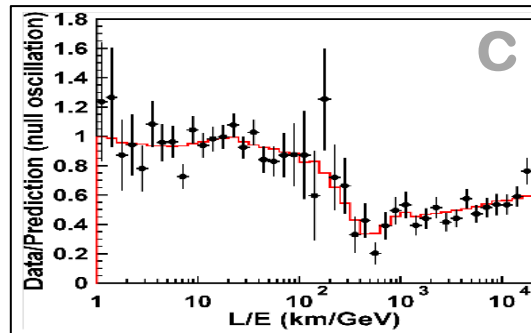
- Knowns and unknowns from 3ν oscillations
- Nonoscillation constraints from $0\nu\beta\beta$ & Cosmology
- Global analysis of oscillation + nonoscillation data
- Summary and prospects

Last two decades: oscillations → “standard” 3ν framework

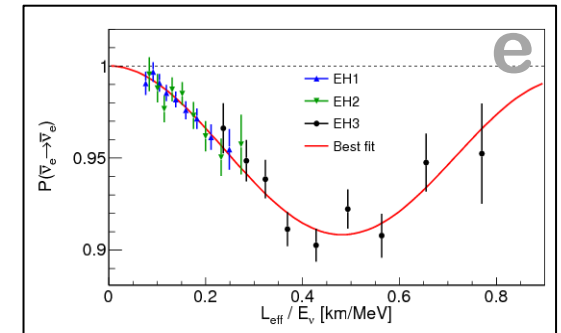
$e \rightarrow e$ (δm^2 , θ_{12})



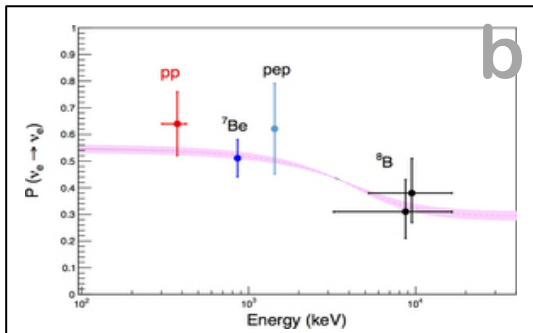
$\mu \rightarrow \mu$ (Δm^2 , θ_{23})



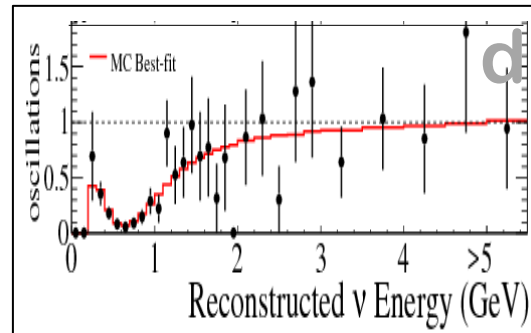
$e \rightarrow e$ (Δm^2 , θ_{13})



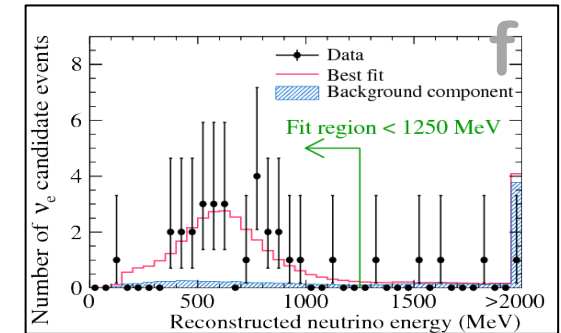
$e \rightarrow e$ (δm^2 , θ_{12})



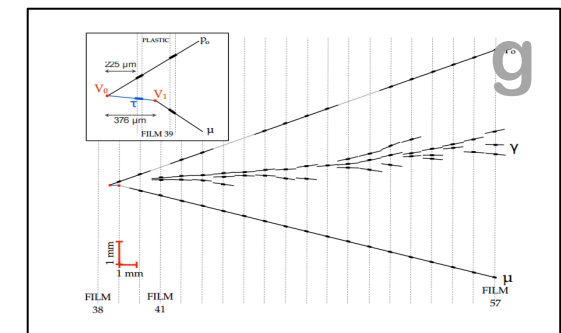
$\mu \rightarrow \mu$ (Δm^2 , θ_{23})



$\mu \rightarrow e$ (Δm^2 , θ_{13} , θ_{23})



$\mu \rightarrow \tau$ (Δm^2 , θ_{23})



Data from various types of neutrino experiments: (a) solar, (b) long-baseline reactor, (c) atmospheric, (d) long-baseline accelerator, (e) short-baseline reactor, (f,g) long baseline accelerator (and, in part, atmospheric).

(a) KamLAND [plot]; (b) Borexino [plot], Homestake, Super-K, SAGE, GALLEX/GNO, SNO; (c) Super-K atmosph. [plot], DeepCore, MACRO, MINOS etc.; (d) T2K (plot), MINOS, K2K; (e) Daya Bay [plot], RENO, Double Chooz; (f) T2K [plot], MINOS, NOvA; (g) OPERA [plot], Super-K atmospheric.

“Broad-brush” picture (with 1-digit accuracy)

Knowns:

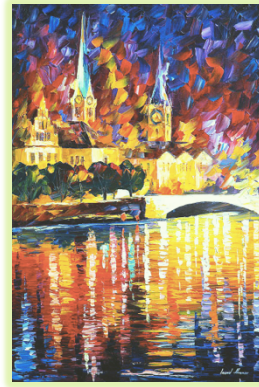
$$\delta m^2 \sim 7 \times 10^{-5} \text{ eV}^2$$

$$\Delta m^2 \sim 2 \times 10^{-3} \text{ eV}^2$$

$$\sin^2 \theta_{12} \sim 0.3$$

$$\sin^2 \theta_{23} \sim 0.5$$

$$\sin^2 \theta_{13} \sim 0.02$$



Unknowns:

$\delta(\text{CP})$

$\text{sign}(\Delta m^2) = \text{ordering}$

octant(θ_{23})

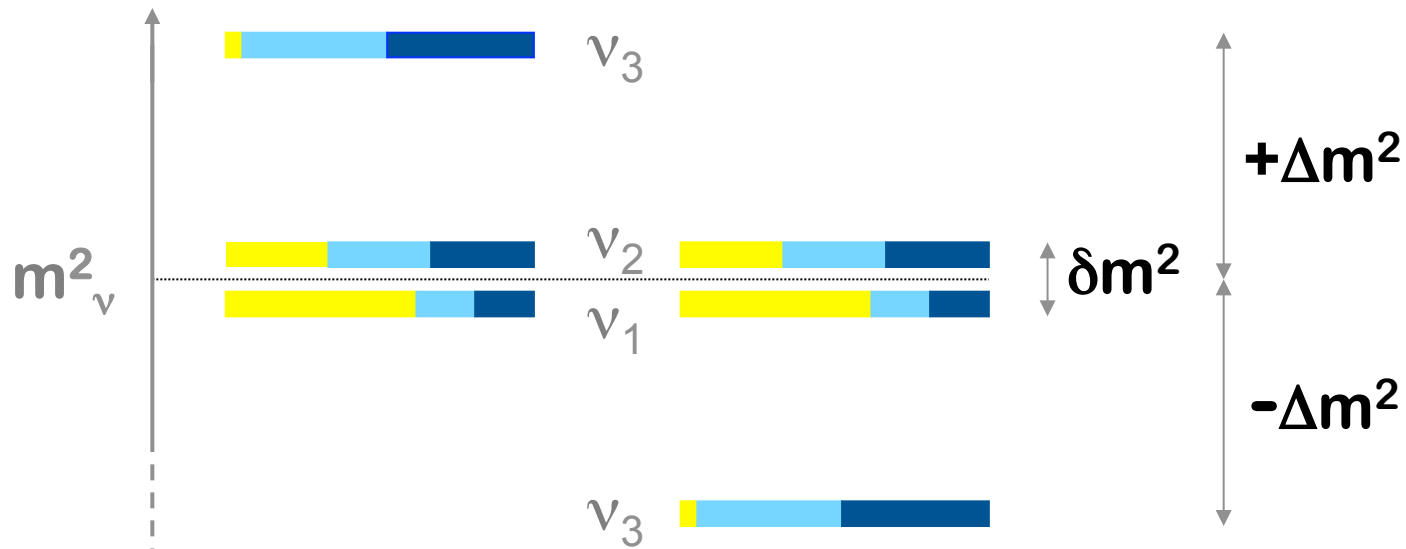
absolute mass scale

Dirac/Majorana nature

Normal Ordering (NO)

e **μ** **τ**

Inverted Ordering (IO)



Hi-res and broader picture → Global analysis of ν oscill. data



Analysis includes increasingly rich oscillation data sets:

LBL Acc + Solar + KL

LBL Acc + Solar + KL + SBL Reactor

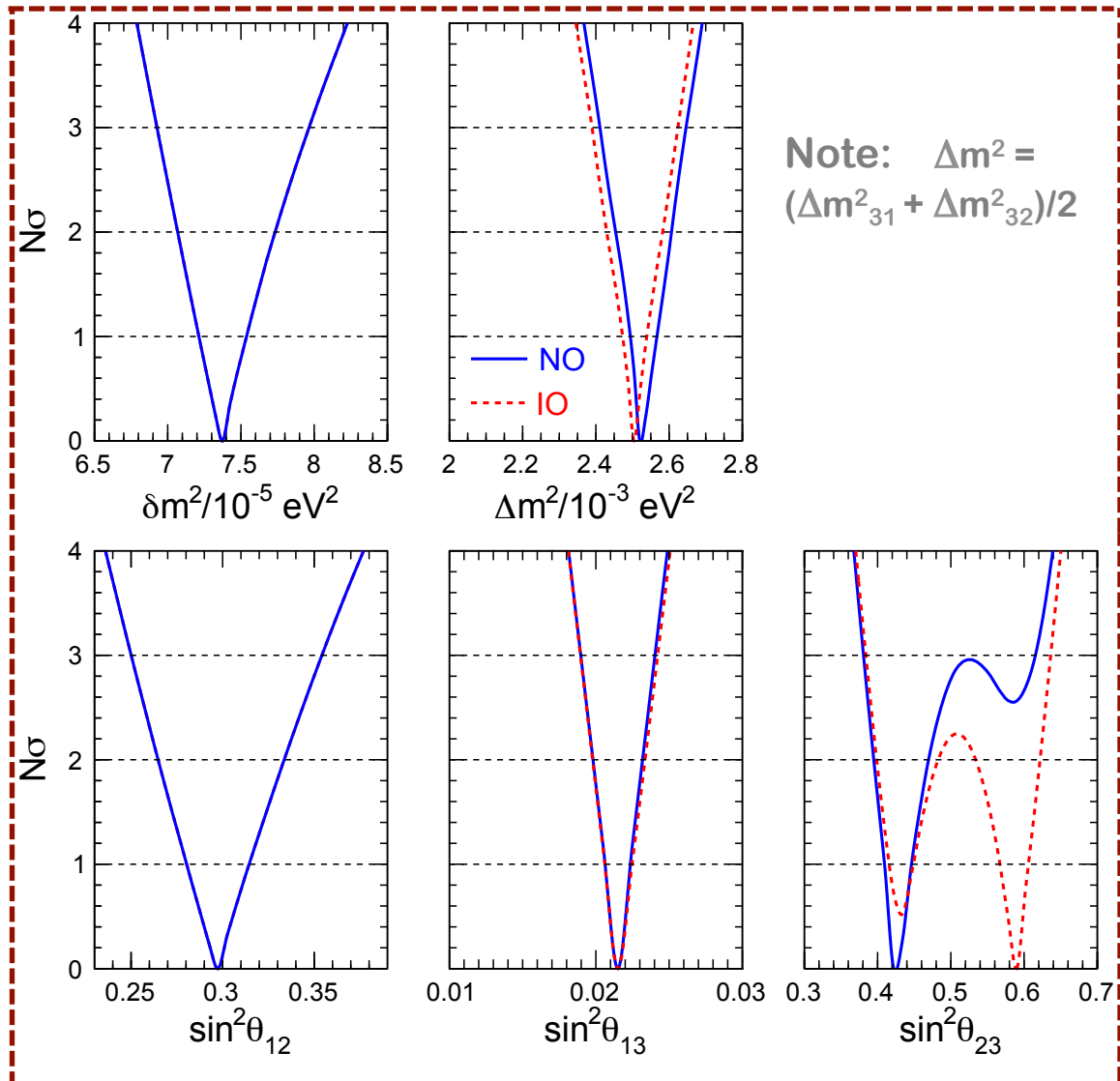
LBL Acc + Solar + KL + SBL Reactor + Atmosph.

χ^2 metric adopted. Parameters not shown are marginalized away:

C.L.'s refer to $N\sigma = \sqrt{\Delta\chi^2} = 1, 2, 3, \dots$

Five known oscillation parameters:

LBL Acc + Solar + KamLAND + SBL Reactors + Atmos



Current 1σ errors
(1/6 of $\pm 3\sigma$ range):

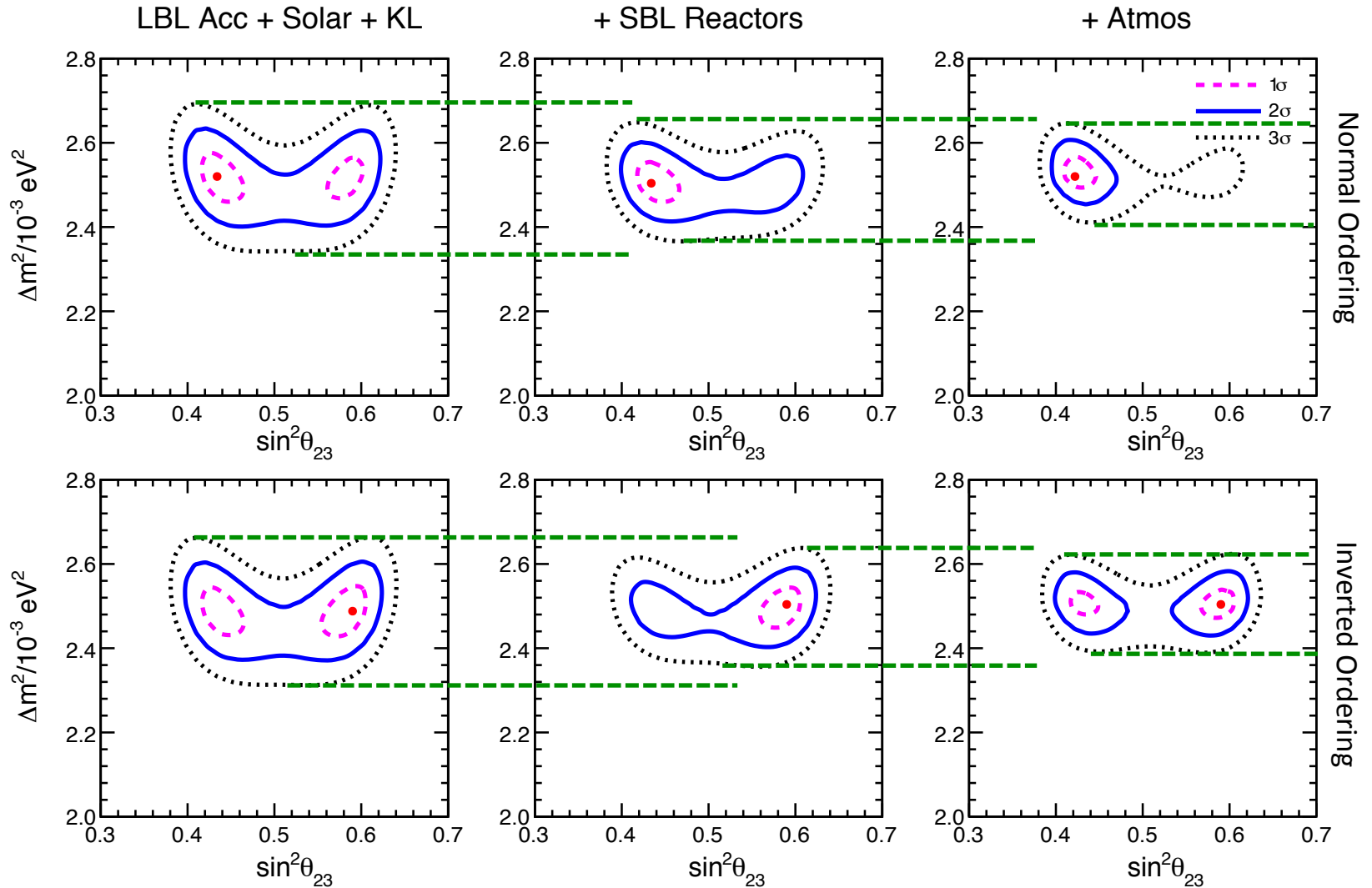
| | |
|---------------------|------------|
| δm^2 | 2.3 % |
| Δm^2 | 1.6 % |
| $\sin^2\theta_{12}$ | 5.8 % |
| $\sin^2\theta_{13}$ | 4.0 % |
| $\sin^2\theta_{23}$ | ~ 9 % |

all < 10%...

Precision Era!

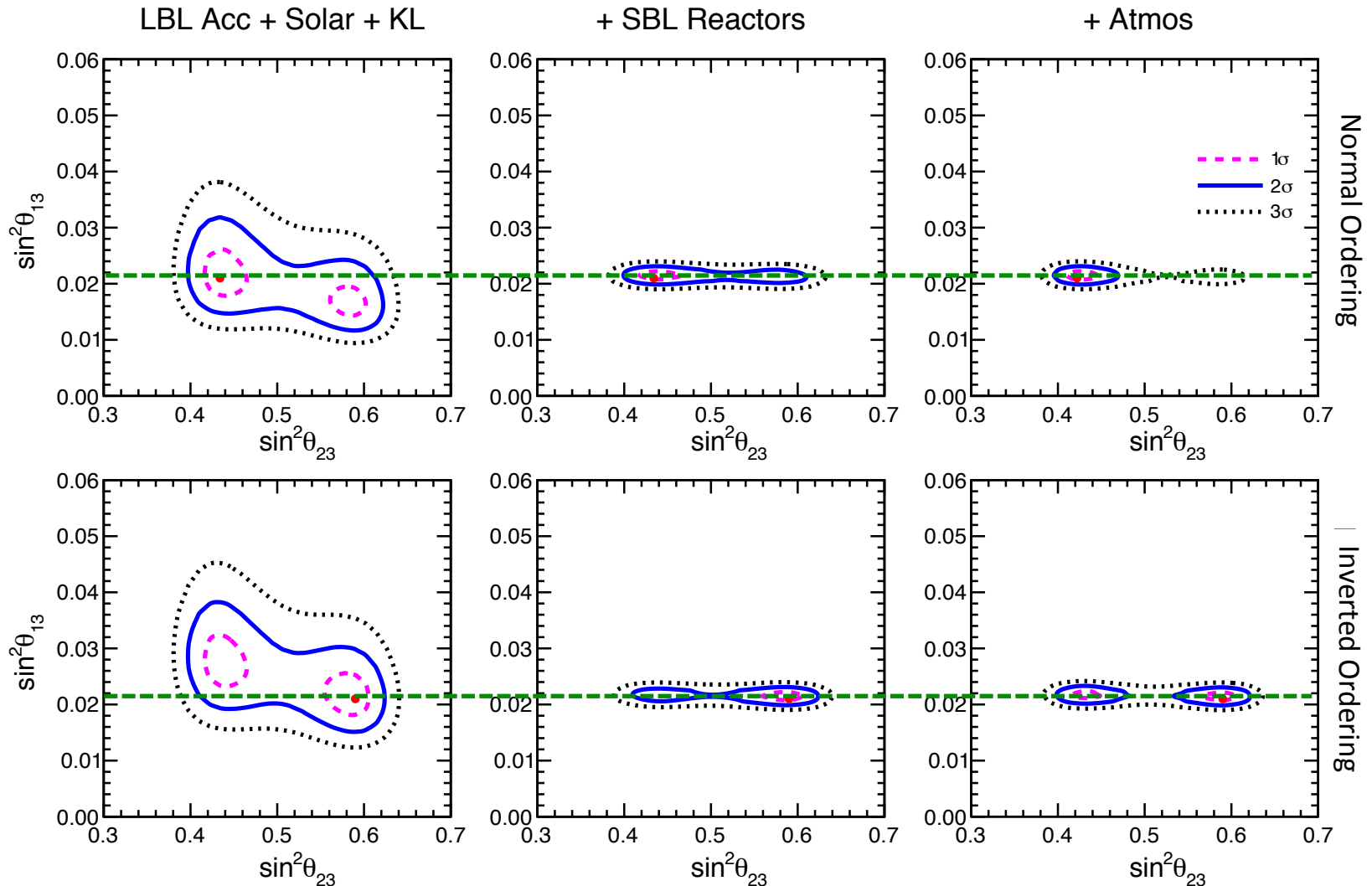
[but PMNS still
very far from
CKM accuracy]

More on known oscillation parameters: synergy on Δm^2



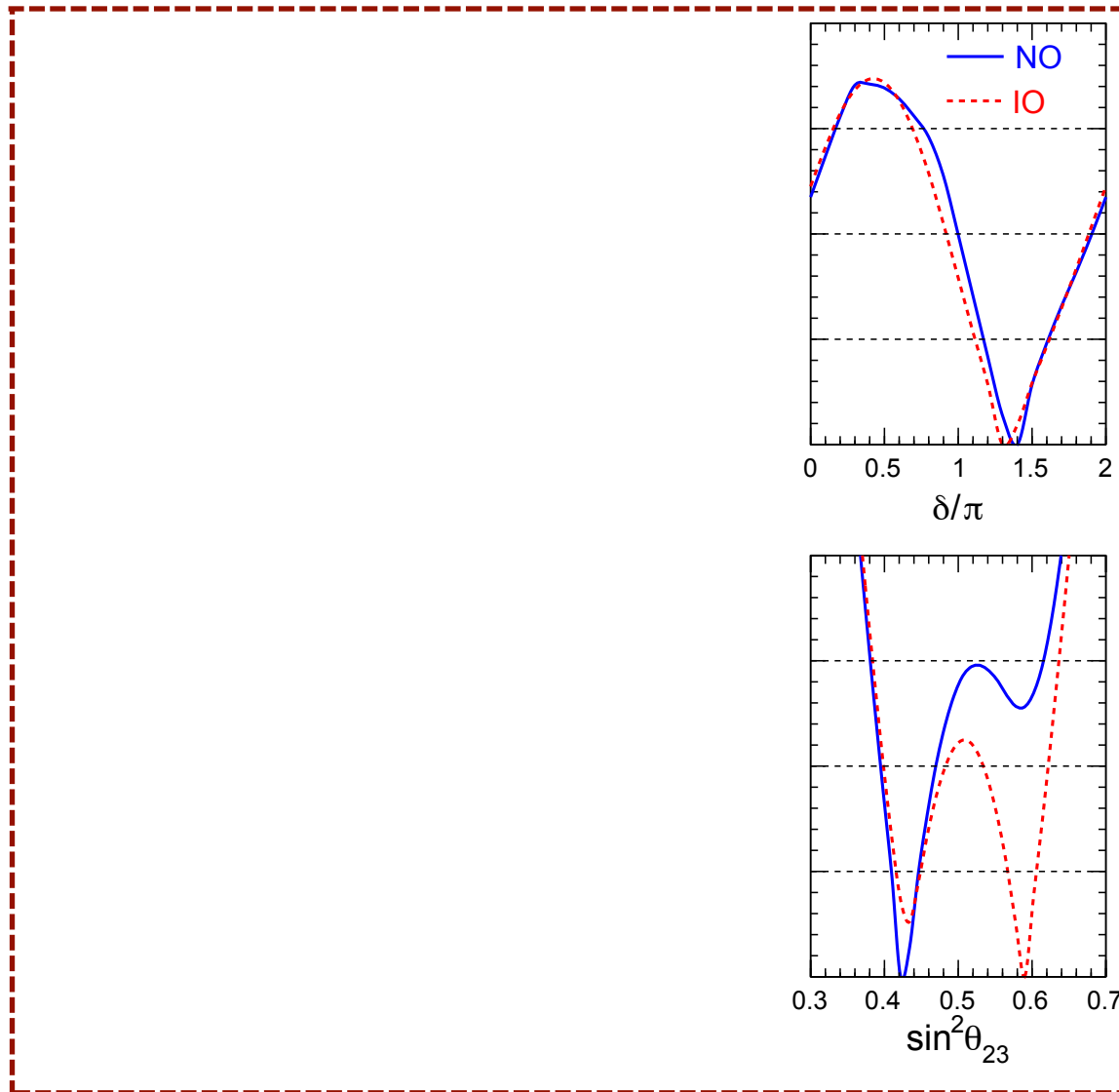
All data sets contribute to Δm^2

More on known oscillation parameters: synergy on θ_{13}



LBL + solar + KL prefer the same θ_{13} as reactors (within large uncertainties)

Three unknown oscillation parameters

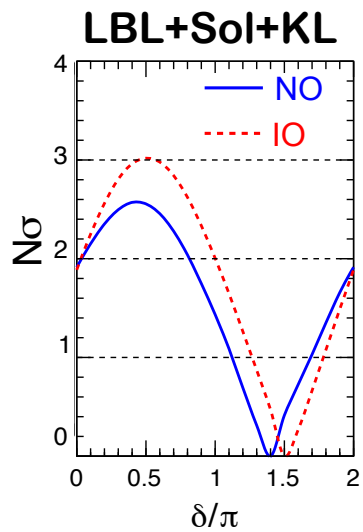
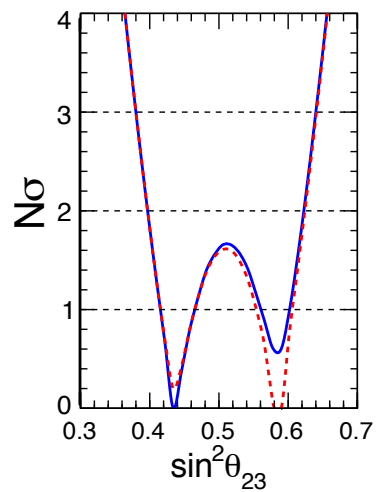


δ_{CP}

θ_{23} octant

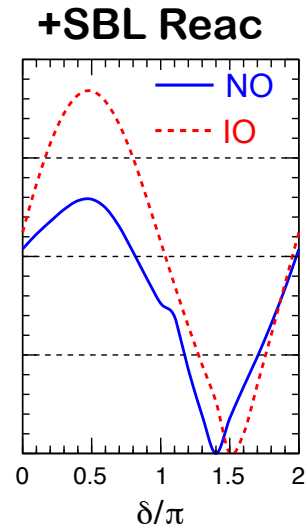
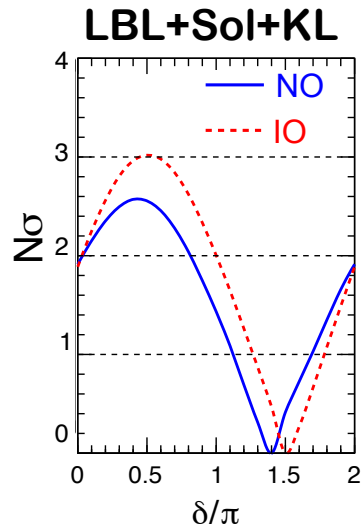
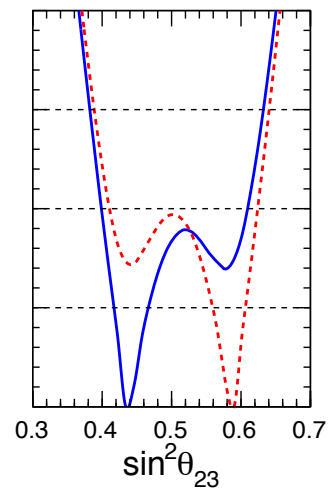
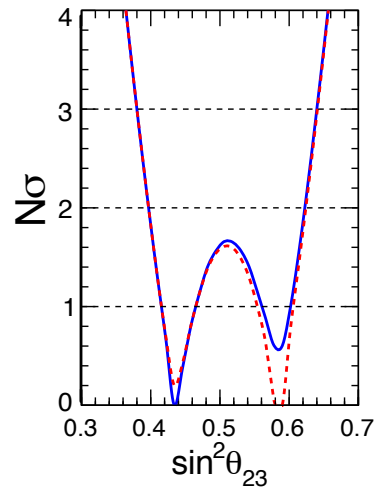
NO or IO

More on unknown oscillation parameters:

 δ_{CP}

 θ_{23}
octant

 $\Delta\chi^2$
(IO-NO)

+1.1

More on unknown oscillation parameters:

 δ_{CP}

 θ_{23}
octant

 $\Delta\chi^2$
(IO-NO)

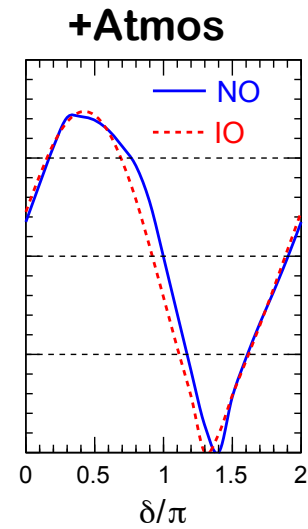
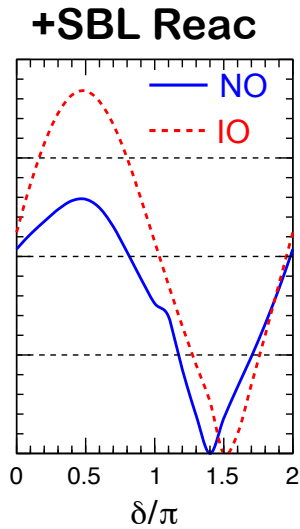
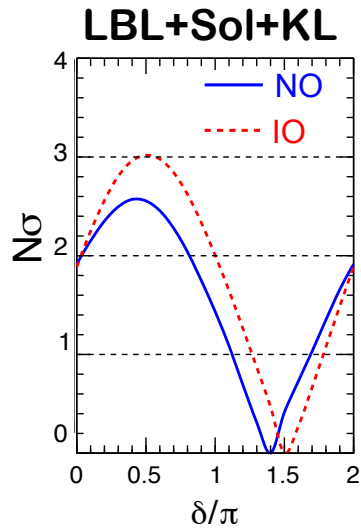
+1.1



+1.1

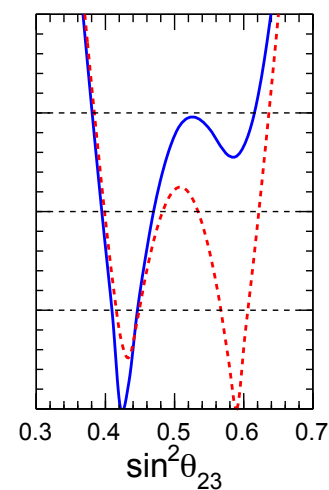
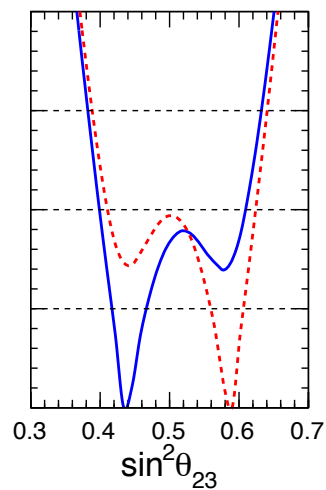
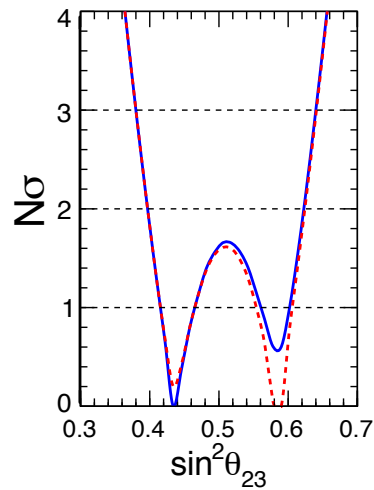
More on unknown oscillation parameters:

δ_{CP}



**$\sin \delta \sim -1$
(or $\sin \delta < 0$)
favored;
 $\sin \delta \sim +1$
excluded**

θ_{23}
octant



**Max-mixing
disfavored;
octant flips
with NO/IO**

$\Delta\chi^2$
(IO-NO)

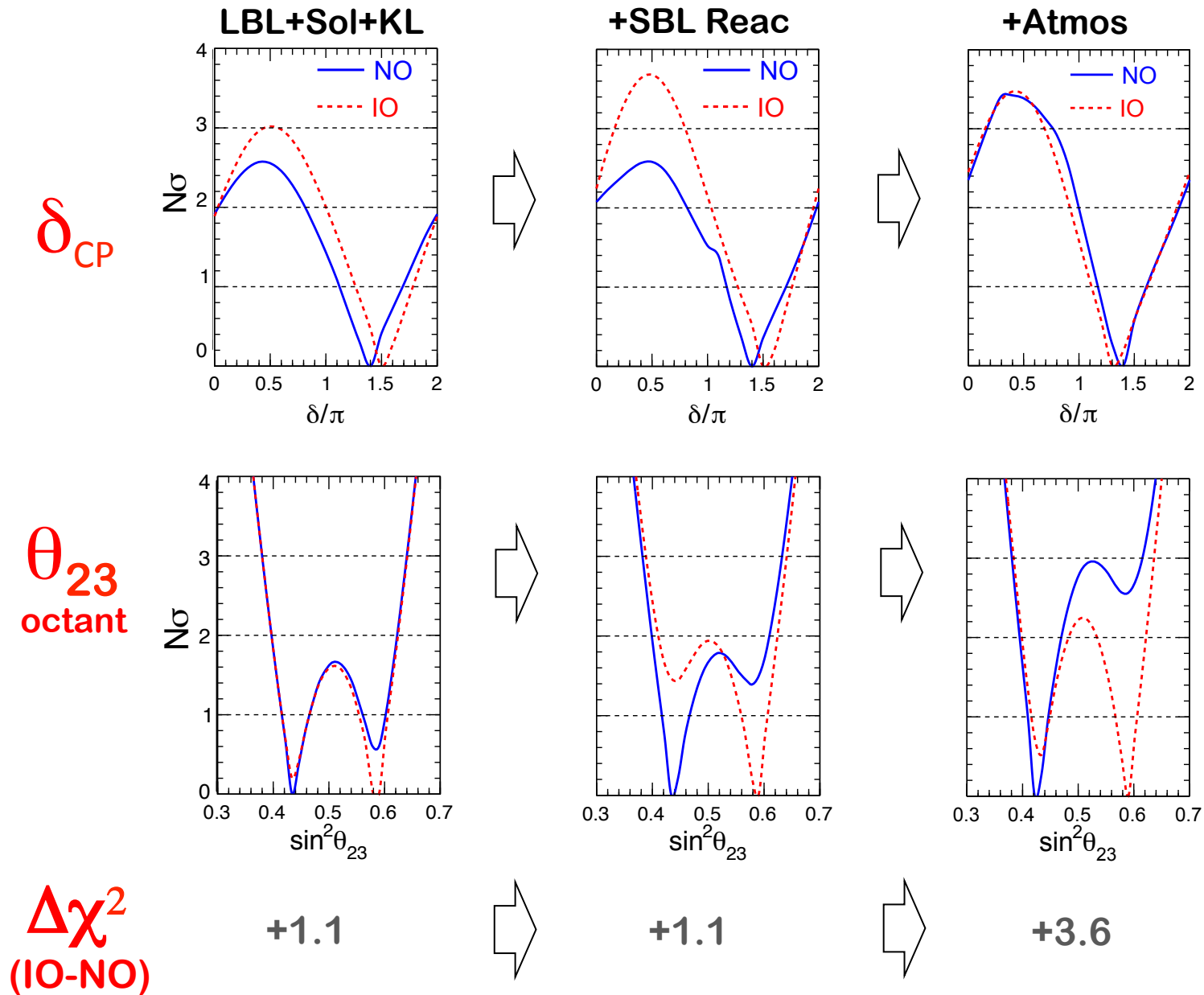
+1.1

+1.1

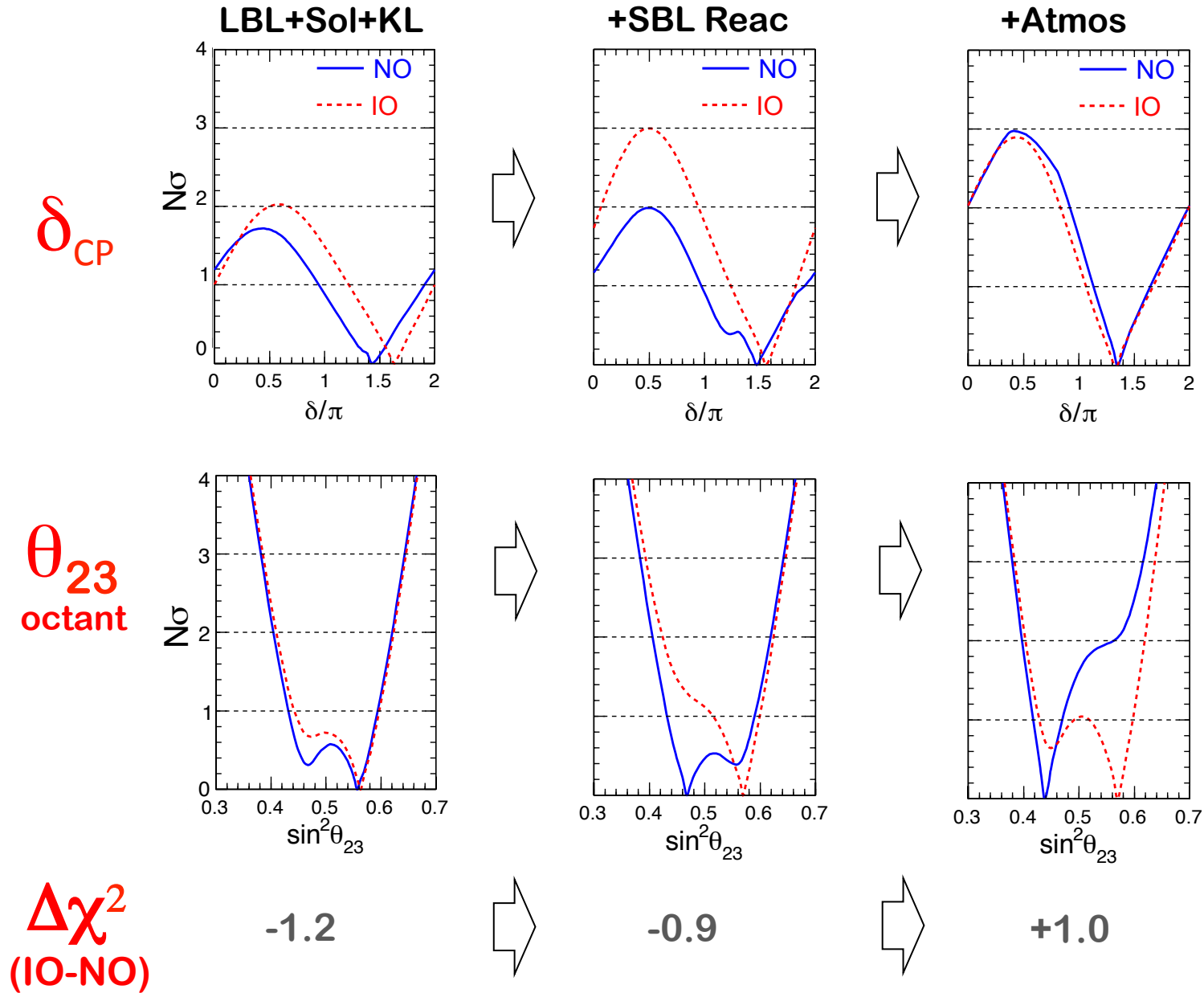
+3.6

**Intriguing!
NO favored**

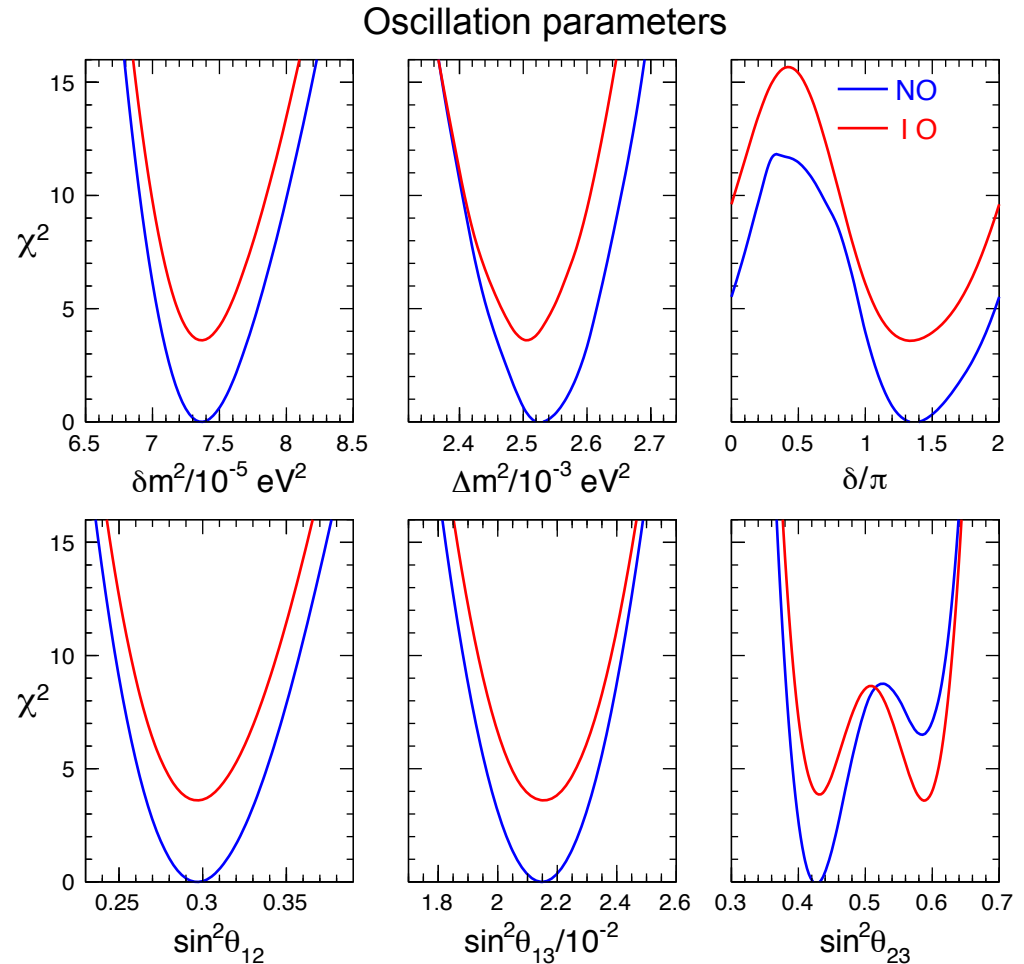
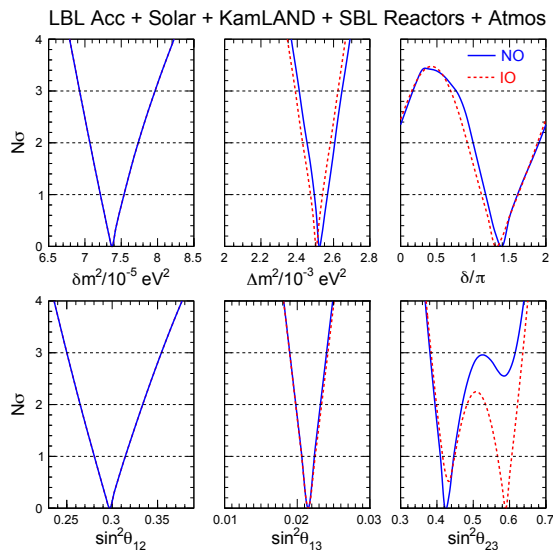
Compare the current results (circa 2017) with...



... 1yr ago, 2016: trends were somewhat weaker

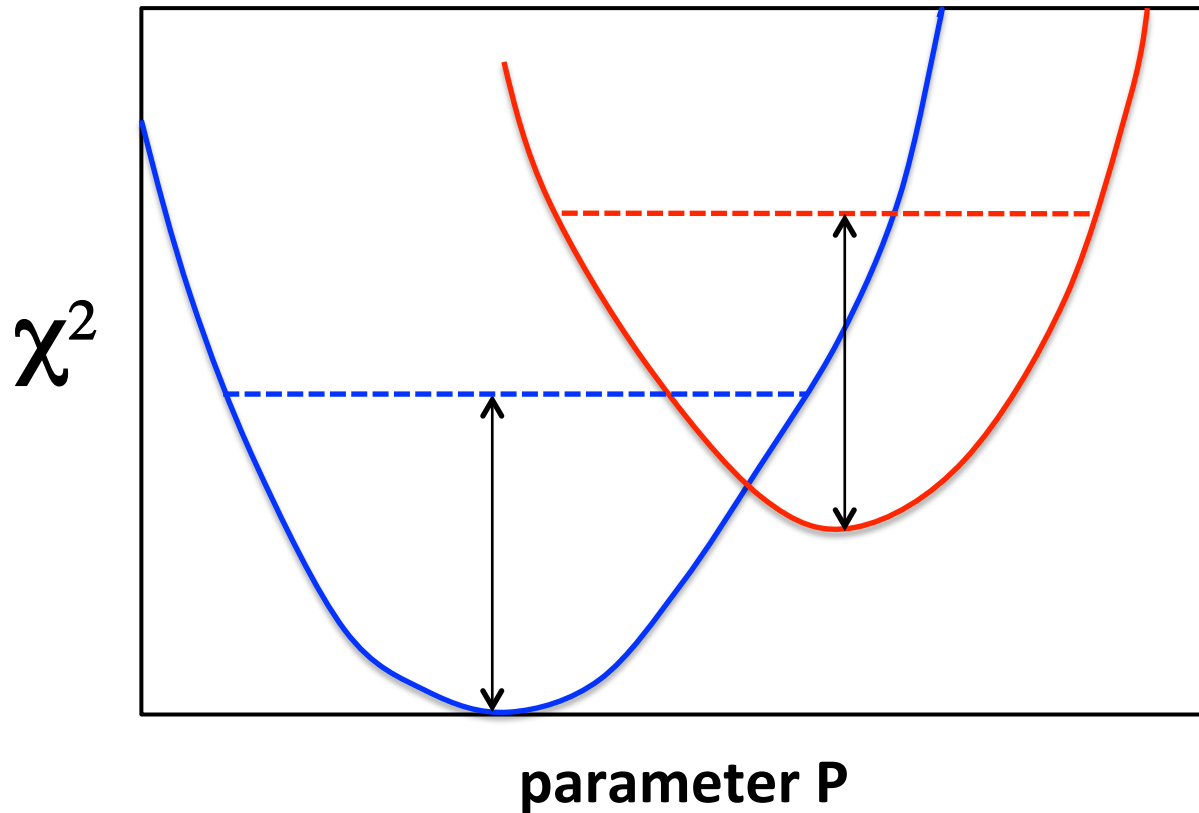


Current indication $\Delta\chi^2_{\text{IO-NO}} = 3.6$ from oscill. data starts to be interesting.
Useful to see the effect of excluding/including this offset in the analysis:



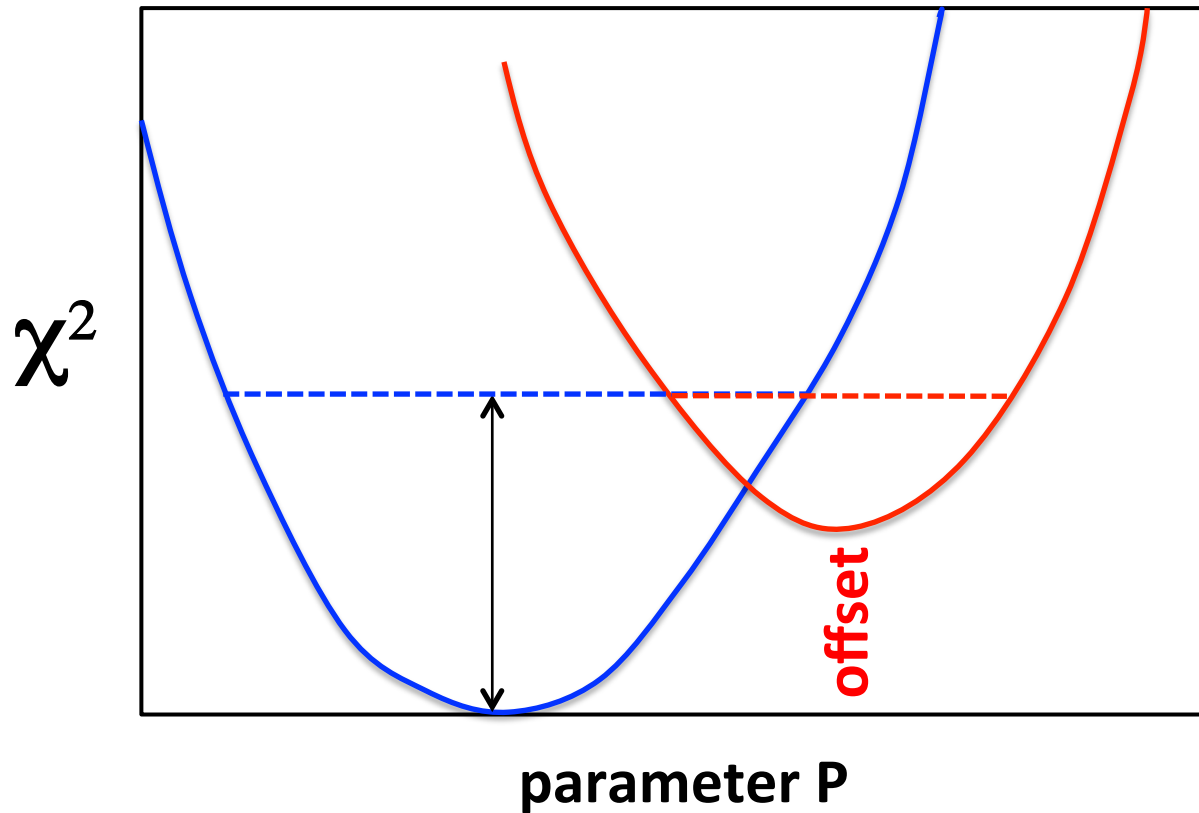
Two different ways of marginalizing over mass ordering(s) →

Apply a " $\Delta\chi^2$ cut" to **SEPARATE** minima in **NO**, **IO**....

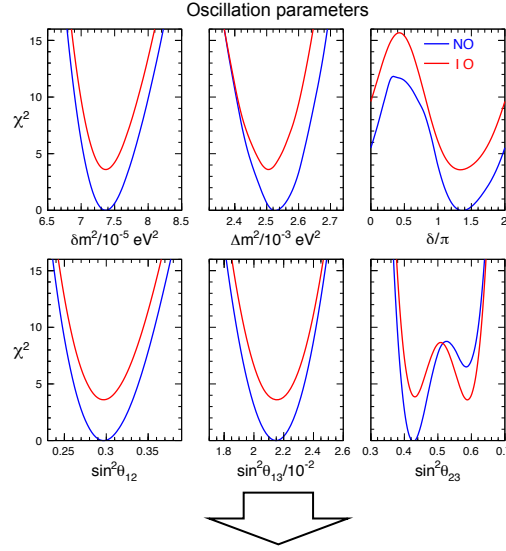


(does **not** include **IO-NO offset** information)

...or minimize and expand over **ANY ORDERING**



(includes **IO-NO offset** information)



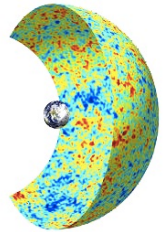
Oscillation parameter ranges

TABLE I: Results of the global 3ν oscillation analysis, in terms of best-fit values for the mass-mixing parameters and associated $n\sigma$ ranges ($n = 1, 2, 3$), defined by $\chi^2 - \chi^2_{\min} = n^2$ with respect to the separate minima in each mass ordering (NO, IO) and to the absolute minimum in any ordering. (Note that the fit to the δm^2 and $\sin^2 \theta_{12}$ parameters is basically insensitive to the mass ordering.) We recall that Δm^2 is defined herein as $m_3^2 - (m_1^2 + m_2^2)/2$, and that δ is taken in the (cyclic) interval $\delta/\pi \in [0, 2]$.

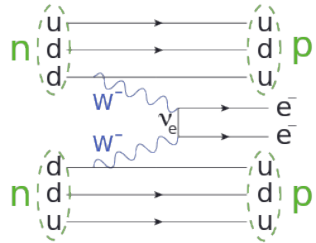
| Parameter | Ordering | Best fit | 1σ range | 2σ range | 3σ range |
|-------------------------------------|-------------|----------|----------------------------------|----------------------------------|----------------------------|
| $\delta m^2/10^{-5} \text{ eV}^2$ | NO, IO, Any | 7.37 | 7.21 – 7.54 | 7.07 – 7.73 | 6.93 – 7.96 |
| $\sin^2 \theta_{12}/10^{-1}$ | NO, IO, Any | 2.97 | 2.81 – 3.14 | 2.65 – 3.34 | 2.50 – 3.54 |
| $ \Delta m^2 /10^{-3} \text{ eV}^2$ | NO | 2.525 | 2.495 – 2.567 | 2.454 – 2.606 | 2.411 – 2.646 |
| | IO | 2.505 | 2.473 – 2.539 | 2.430 – 2.582 | 2.390 – 2.624 |
| | Any | 2.525 | 2.495 – 2.567 | 2.454 – 2.606 | 2.411 – 2.646 |
| $\sin^2 \theta_{13}/10^{-2}$ | NO | 2.15 | 2.08 – 2.22 | 1.99 – 2.31 | 1.90 – 2.40 |
| | IO | 2.16 | 2.07 – 2.24 | 1.98 – 2.33 | 1.90 – 2.42 |
| | Any | 2.15 | 2.08 – 2.22 | 1.99 – 2.31 | 1.90 – 2.40 |
| $\sin^2 \theta_{23}/10^{-1}$ | NO | 4.25 | 4.10 – 4.46 | 3.95 – 4.70 | 3.81 – 6.15 |
| | IO | 5.89 | 4.17 – 4.48 \oplus 5.67 – 6.05 | 3.99 – 4.83 \oplus 5.33 – 6.21 | 3.84 – 6.36 |
| | Any | 4.25 | 4.10 – 4.46 | 3.95 – 4.70 \oplus 5.75 – 6.00 | 3.81 – 6.26 |
| δ/π | NO | 1.38 | 1.18 – 1.61 | 1.00 – 1.90 | 0 – 0.17 \oplus 0.76 – 2 |
| | IO | 1.31 | 1.12 – 1.62 | 0.92 – 1.88 | 0 – 0.15 \oplus 0.69 – 2 |
| | Any | 1.38 | 1.18 – 1.61 | 1.00 – 1.90 | 0 – 0.17 \oplus 0.76 – 2 |

Absolute neutrino mass observables

Cosmo

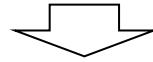


$0\nu\beta\beta$



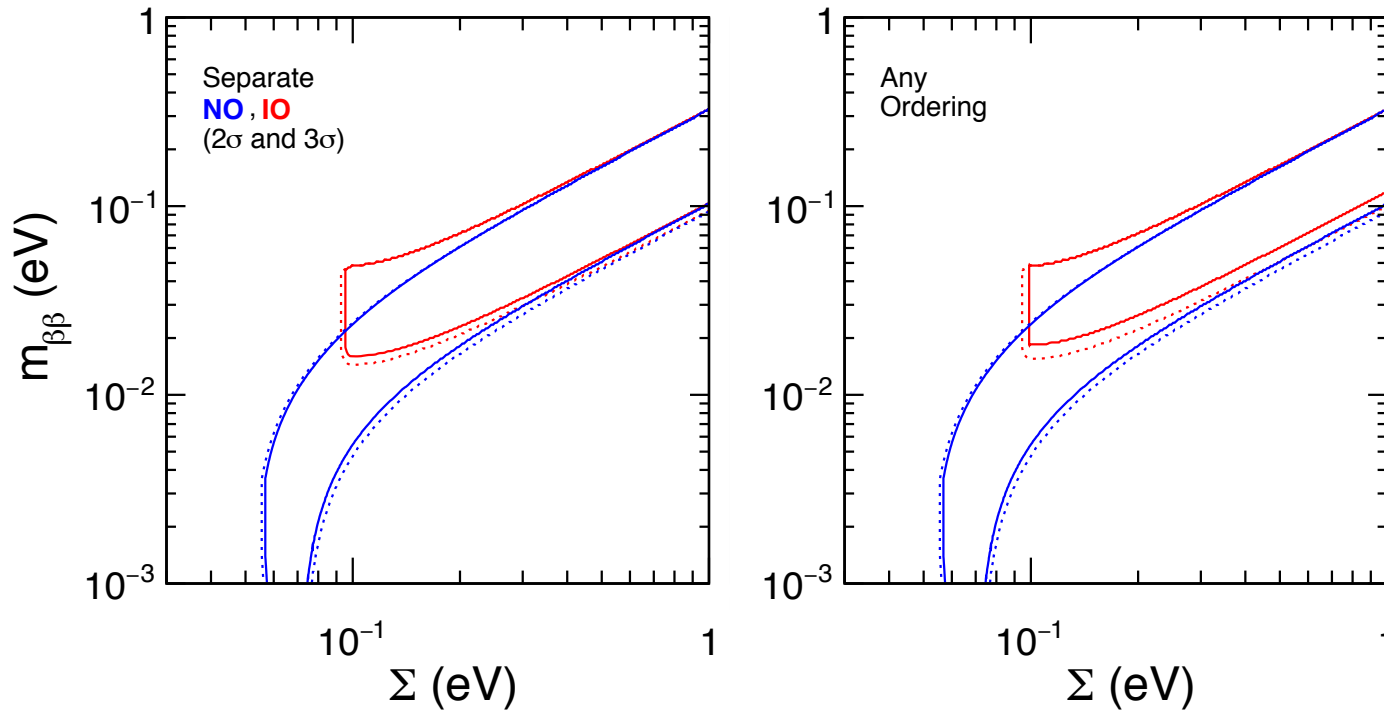
$$m_{\beta\beta} = |c_{13}^2 c_{12}^2 m_1 + c_{13}^2 s_{12}^2 m_2 e^{i\phi_2} + s_{13}^2 m_3 e^{i\phi_3}|$$

$$\Sigma = m_1 + m_2 + m_3$$



Oscillations

Effective Majorana Mass (DBD)

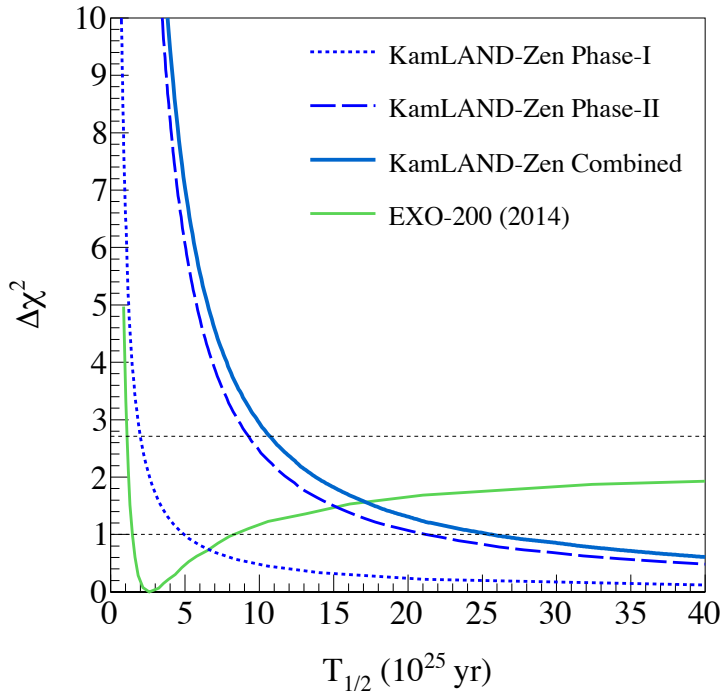


↑↓ spread from
Majorana
CPV phases

Sum of neutrino masses (Cosmology)

Current leading $0\nu\beta\beta$ constraints

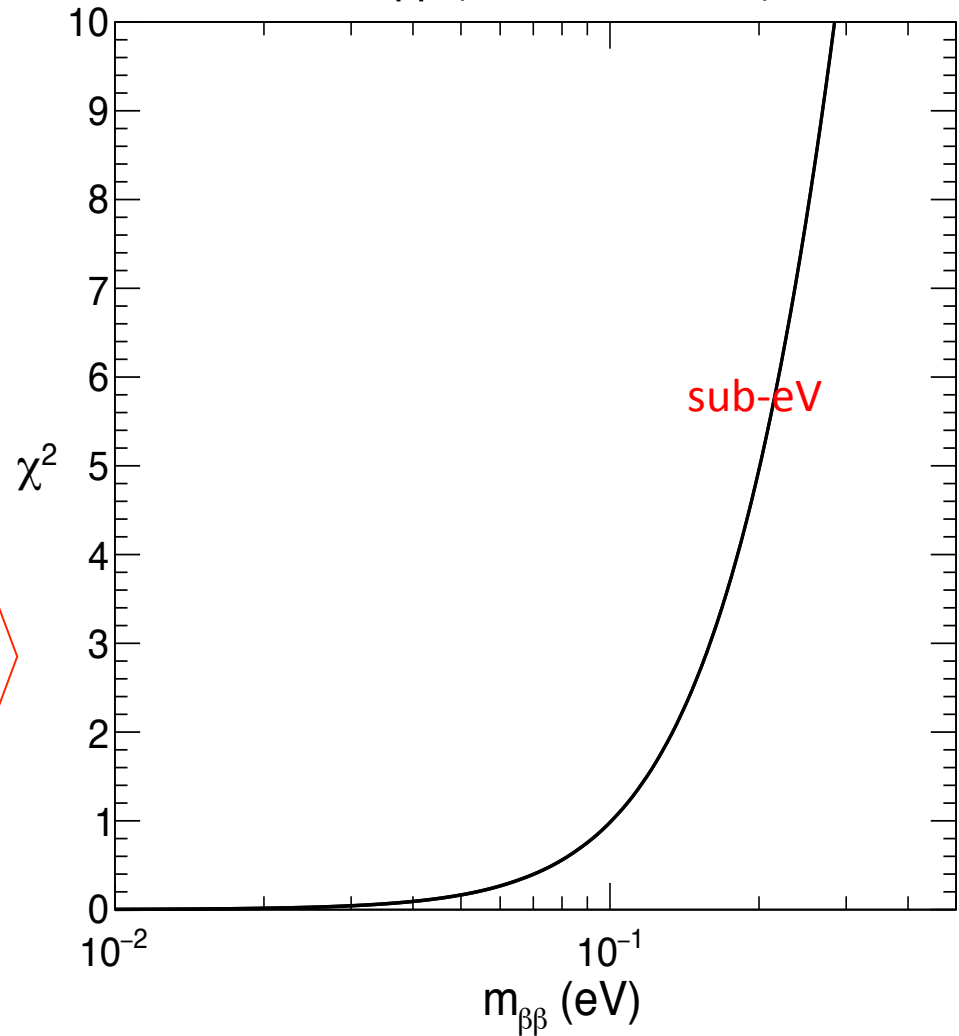
KamLAND-Zen half-life limits

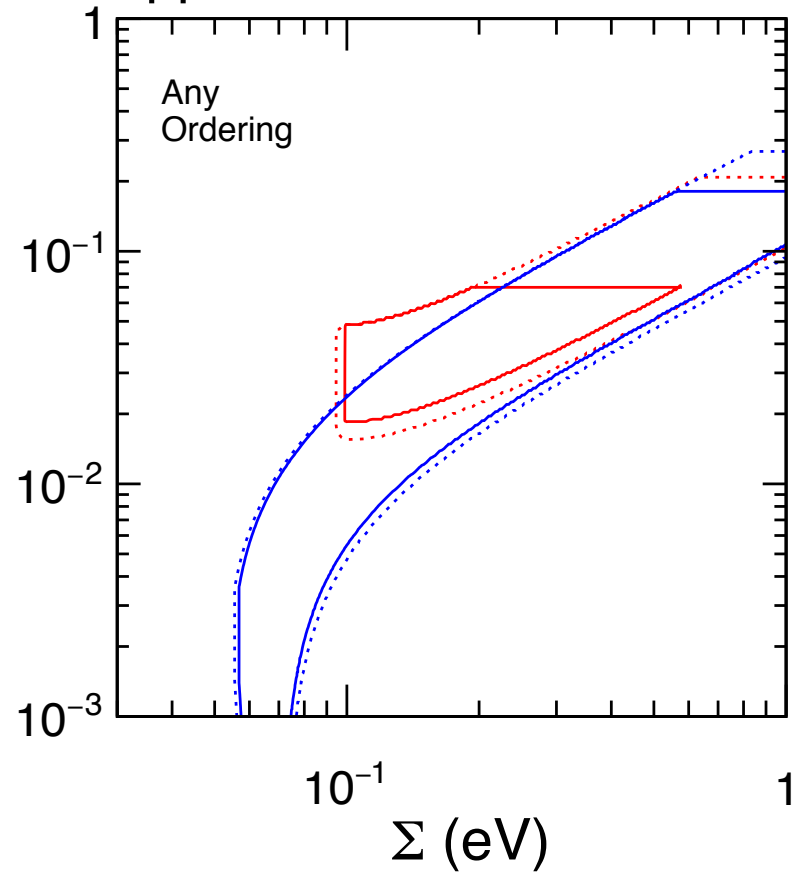
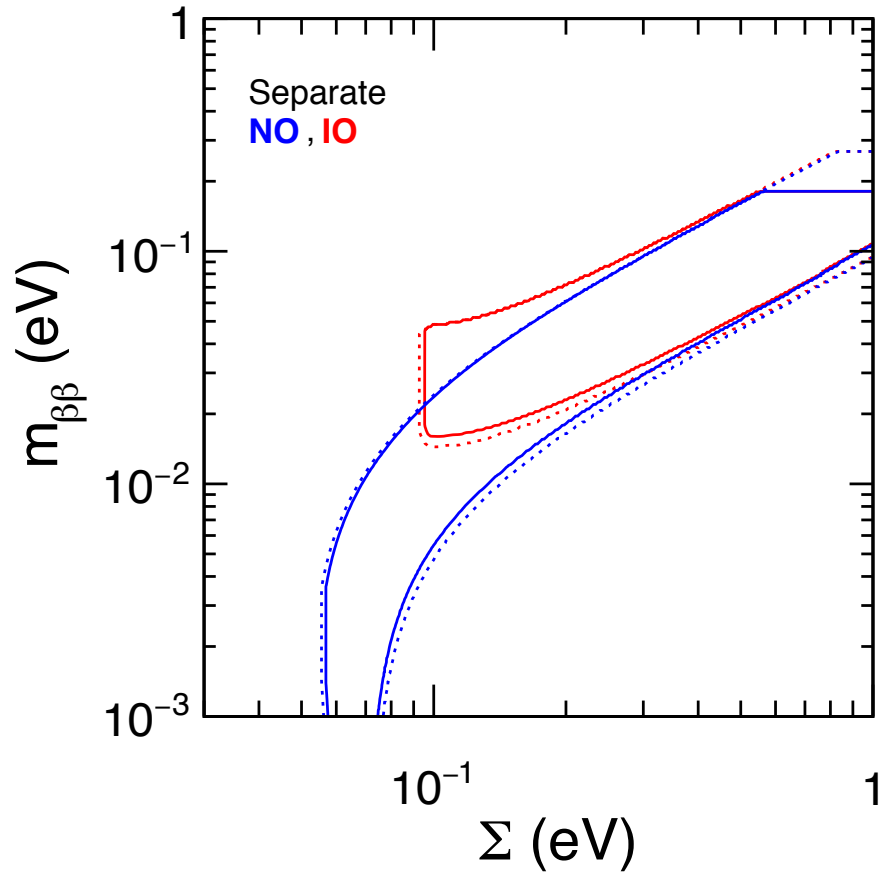


+NME Likelihood based on:
 E.L., A. Rotunno, F. Simkovic,
 arXiv:1506.04058



$0\nu\beta\beta$ (KamLAND-Zen)



Oscill. + $0\nu\beta\beta$ 

Cosmological constraints (circa 2017)

Analysis of various **datasets** within standard (6-param.) Λ **CDM model** augmented with Σ (plus one possible 1 extra parameter \mathbf{A}_{lens} , to account for syst's or nonstandard effects)

Code: **CosmoMC with NO / IO options explicitly included in Σ** , via the two mass² differences

→ unphysical spectra of neutrino masses (e.g., $\Sigma = 0$) not allowed by construction.

→ expect small NO-IO differences at low Σ , but vanishing at high Σ (degenerate spectrum)

Cosmological constraints (circa 2017)

Analysis of various **datasets** within standard (6-param.) Λ CDM **model** augmented with Σ (plus one possible 1 extra parameter A_{lens} , to account for syst's or nonstandard effects)

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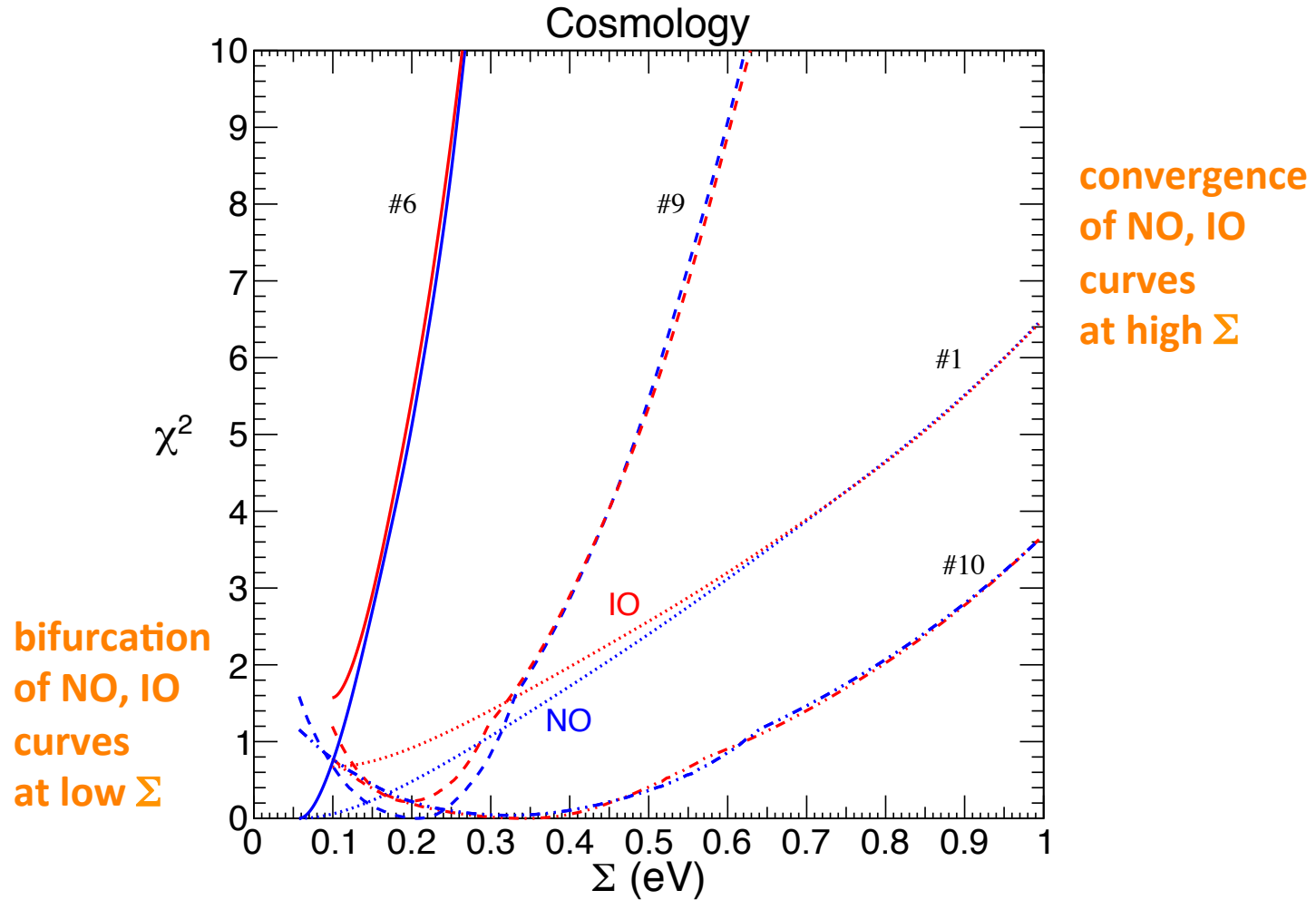
→ expect small NO-IO differences at low Σ , but vanishing at high Σ (degenerate spectrum)

Results on Σ (upper bounds) and on $\Delta\chi^2_{\text{IO-NO}}$

TABLE II: Results of the global 3ν analysis of cosmological data within the standard Λ CDM + Σ and extended Λ CDM + Σ + A_{lens} models. The datasets refer to various combinations of the Planck power angular CMB temperature power spectrum (TT) plus polarization power spectra (TE, EE), reionization optical depth τ_{HFI} , lensing potential power spectrum (lensing), and BAO measurements. For each of the 12 cases we report the 2σ upper bounds on $\Sigma = m_1 + m_2 + m_3$ for NO and IO, together with the $\Delta\chi^2$ difference between the two mass orderings (with one digit after decimal point). For any Σ , the masses m_i are taken to obey the δm^2 and Δm^2 constraints coming from oscillation data. See the text for more details.

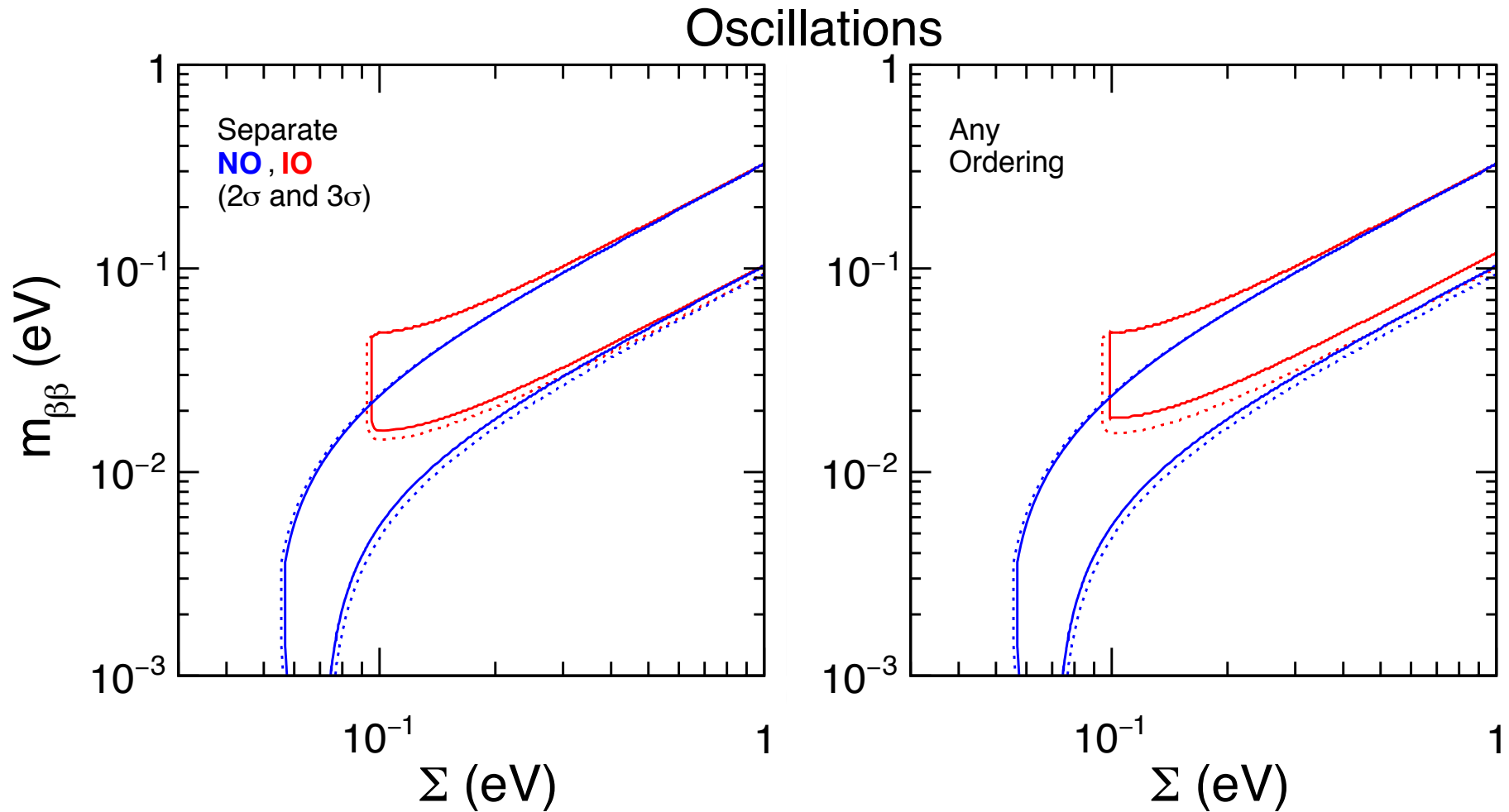
| # | Model | Cosmological data set | Σ/eV (2σ), NO | Σ/eV (2σ), IO | $\Delta\chi^2_{\text{IO-NO}}$ |
|----|--|---|--------------------------------------|--------------------------------------|-------------------------------|
| 1 | Λ CDM + Σ | Planck TT + τ_{HFI} | < 0.72 | < 0.80 | 0.7 |
| 2 | Λ CDM + Σ | Planck TT + τ_{HFI} + lensing | < 0.64 | < 0.63 | 0.2 |
| 3 | Λ CDM + Σ | Planck TT + τ_{HFI} + BAO | < 0.21 | < 0.23 | 1.2 |
| 4 | Λ CDM + Σ | Planck TT, TE, EE + τ_{HFI} | < 0.44 | < 0.48 | 0.6 |
| 5 | Λ CDM + Σ | Planck TT, TE, EE + τ_{HFI} + lensing | < 0.45 | < 0.47 | 0.3 |
| 6 | Λ CDM + Σ | Planck TT, TE, EE + τ_{HFI} + BAO | < 0.18 | < 0.20 | 1.6 |
| 7 | Λ CDM + Σ + A_{lens} | Planck TT + τ_{HFI} | < 1.08 | < 1.08 | -0.1 |
| 8 | Λ CDM + Σ + A_{lens} | Planck TT + τ_{HFI} + lensing | < 0.91 | < 0.93 | 0.0 |
| 9 | Λ CDM + Σ + A_{lens} | Planck TT + τ_{HFI} + BAO | < 0.45 | < 0.46 | 0.2 |
| 10 | Λ CDM + Σ + A_{lens} | Planck TT, TE, EE + τ_{HFI} | < 1.04 | < 1.03 | 0.0 |
| 11 | Λ CDM + Σ + A_{lens} | Planck TT, TE, EE + τ_{HFI} + lensing | < 0.89 | < 0.89 | 0.1 |
| 12 | Λ CDM + Σ + A_{lens} | Planck TT, TE, EE + τ_{HFI} + BAO | < 0.31 | < 0.32 | 0.3 |

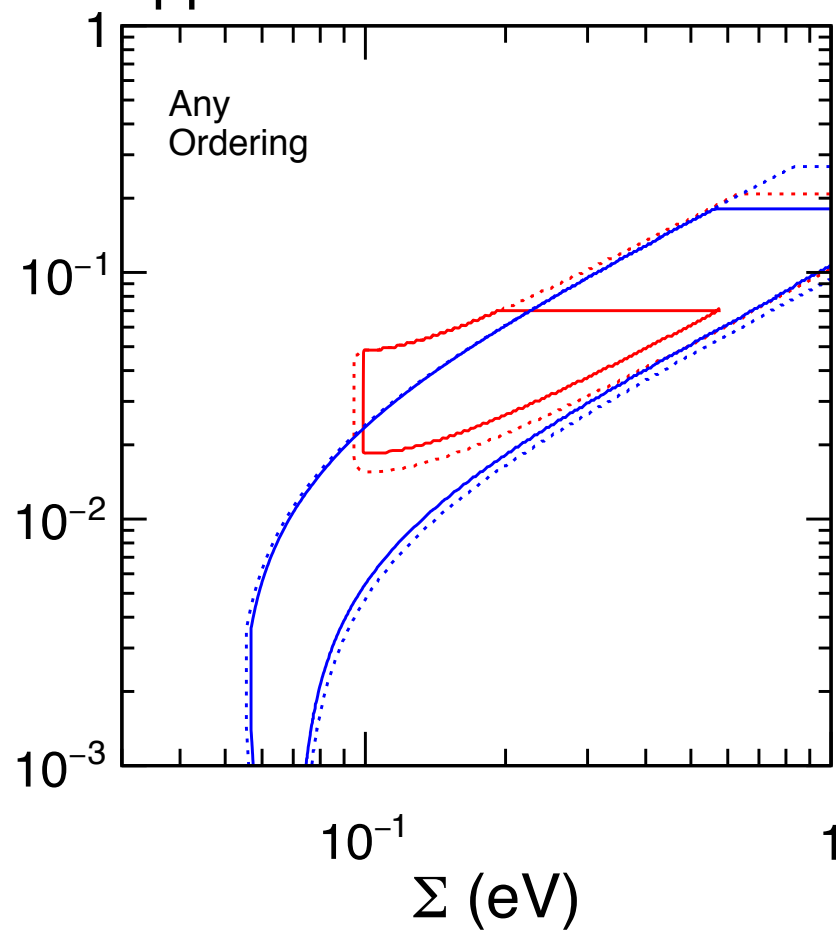
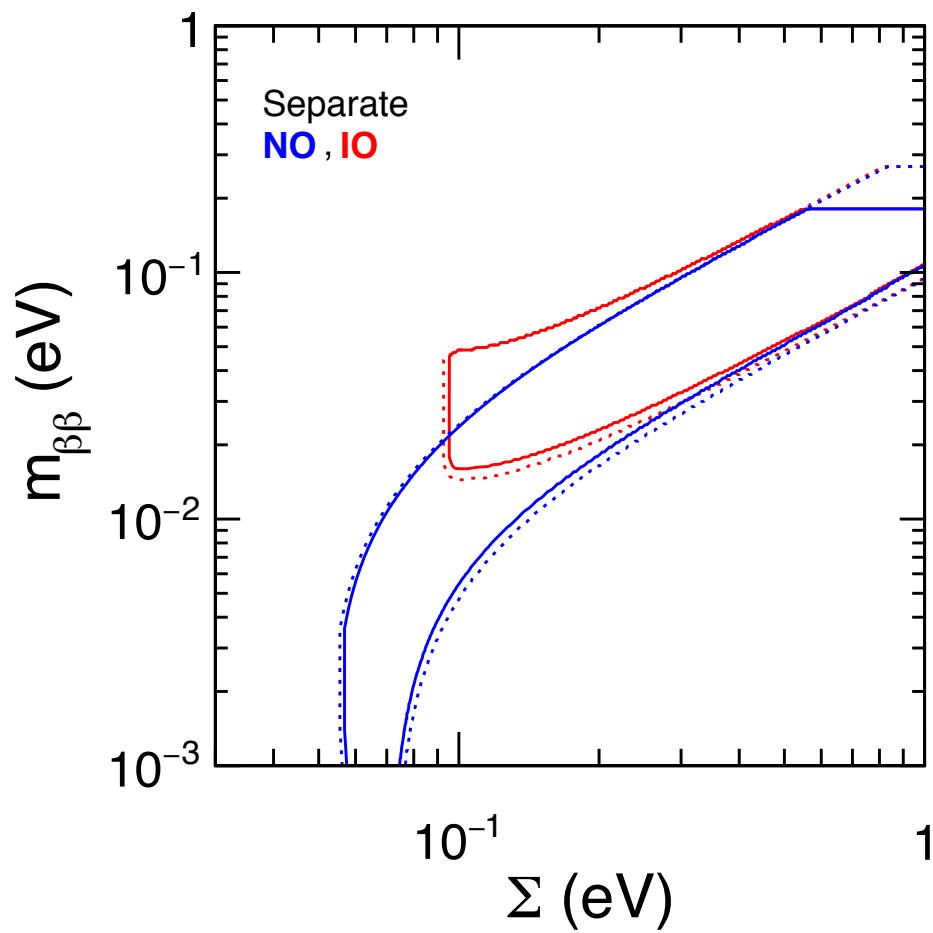
χ^2 profile for NO, IO in representative cases

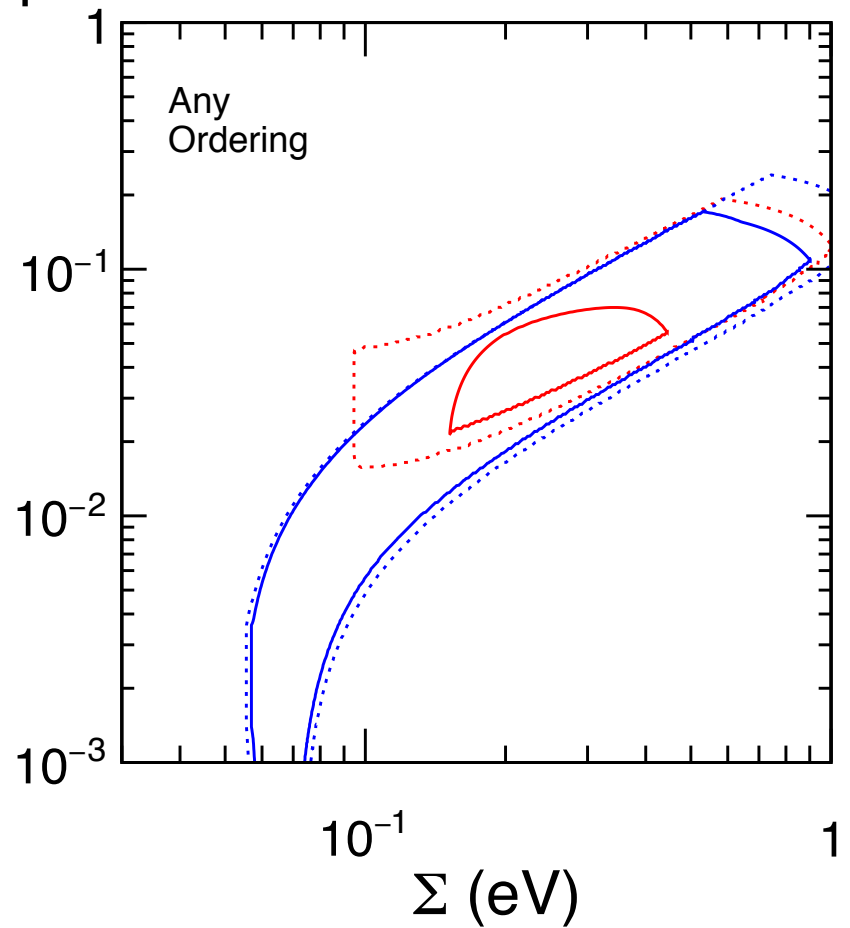
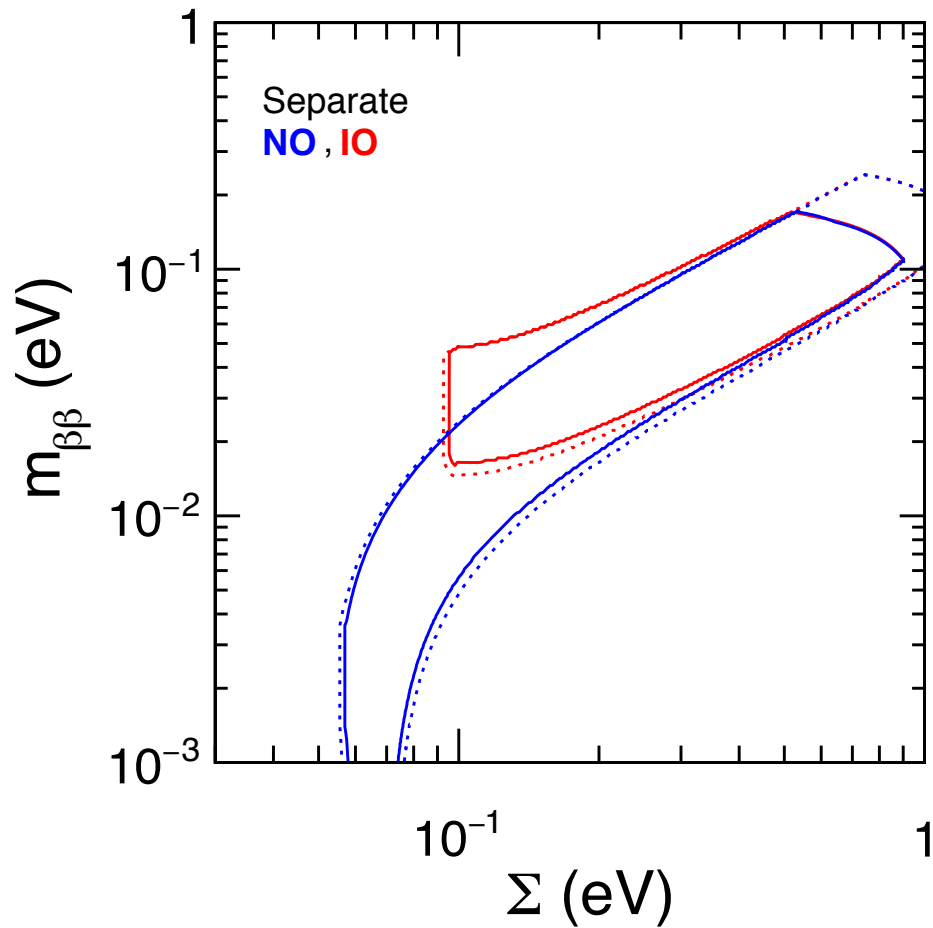


Note: $\Sigma > 0.06$ eV (NO)
 $\Sigma > 0.10$ eV (IO)
 $\Sigma = 0$: not allowed

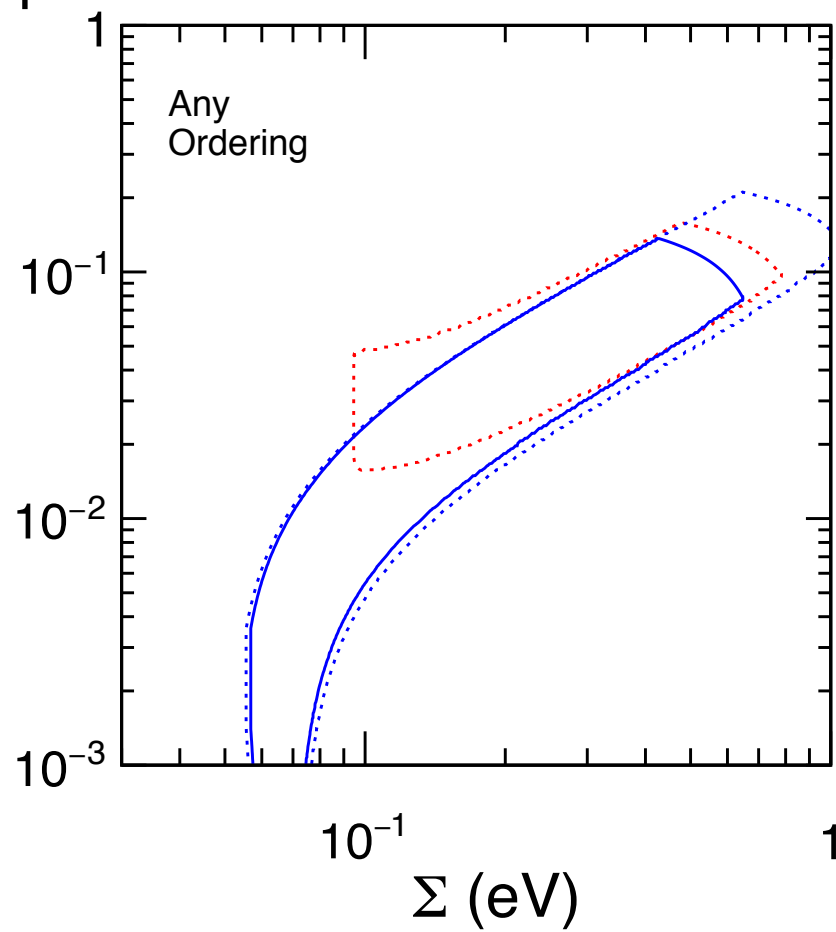
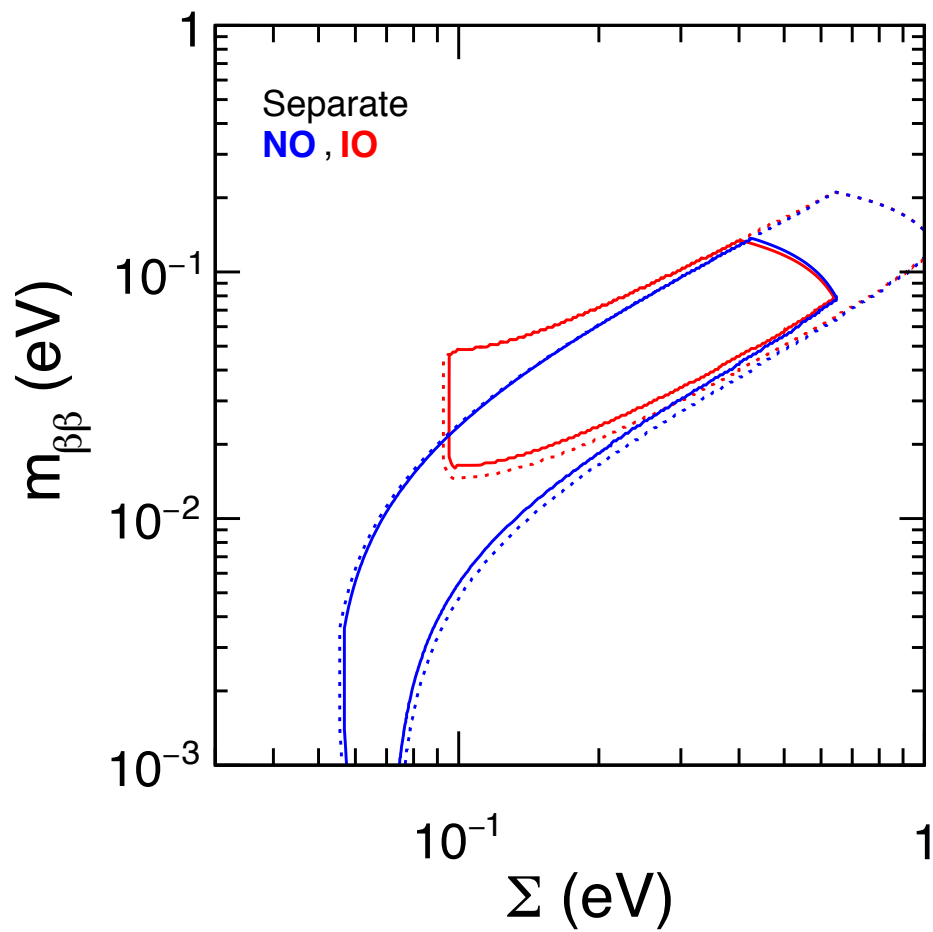
Grand total: combination of oscillation + nonoscillation data (with increasingly strong cosmological constraints)

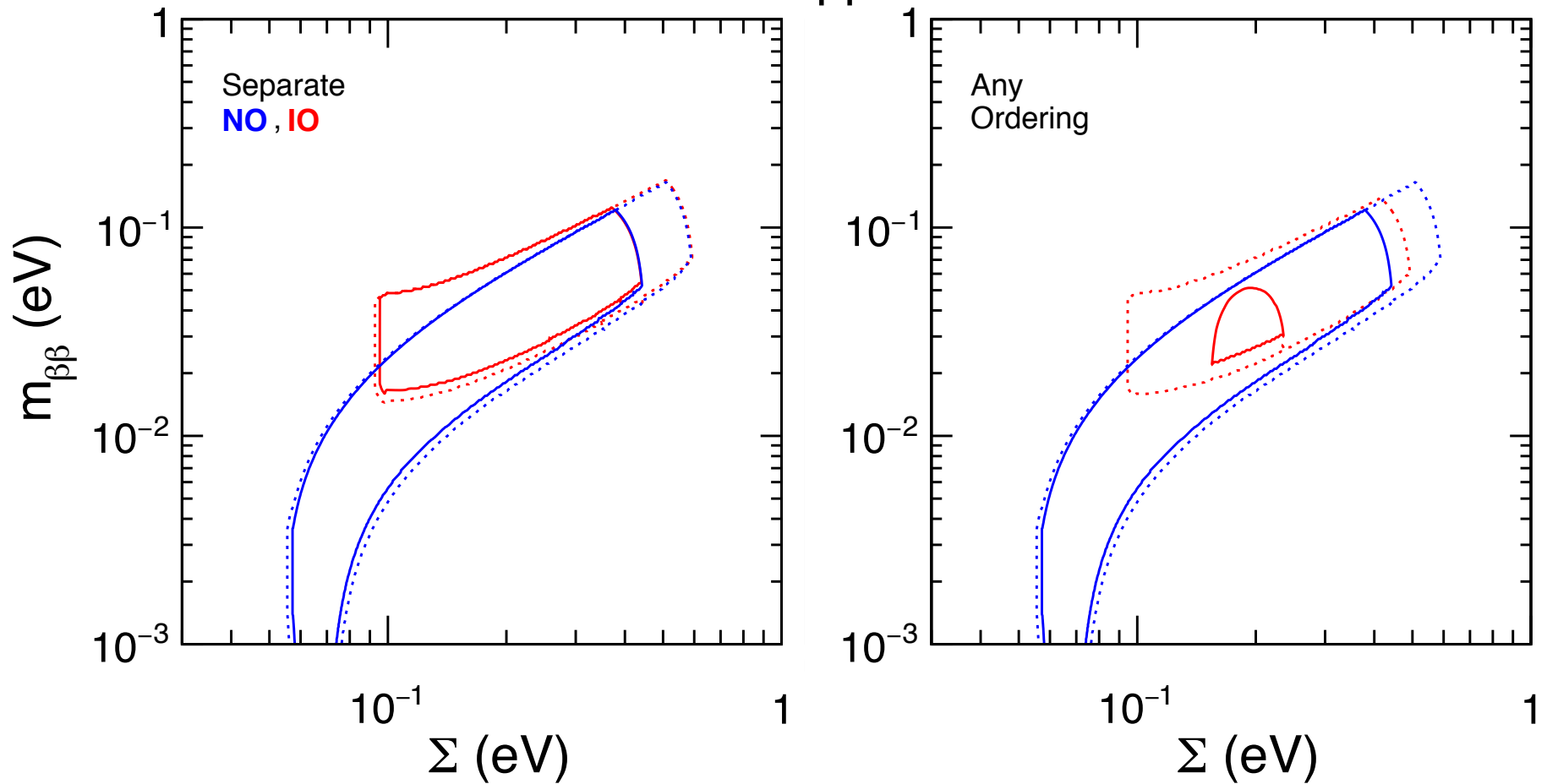


Oscill. + $0\nu\beta\beta$ 

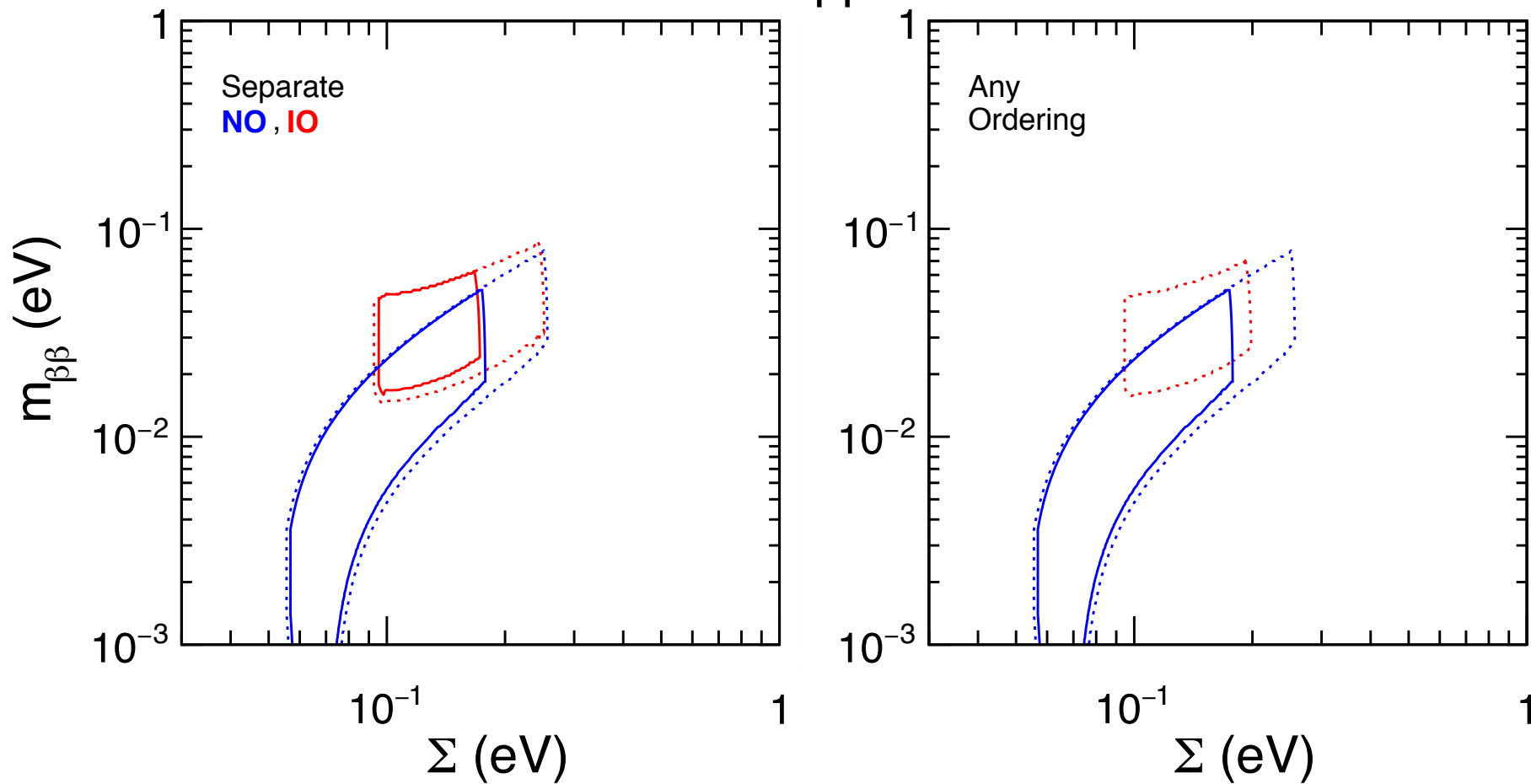
Oscill. + $0\nu\beta\beta$ + Cosmo #10

[Case with “conservative” bounds from cosmology]

Oscill. + $0\nu\beta\beta$ + Cosmo #1

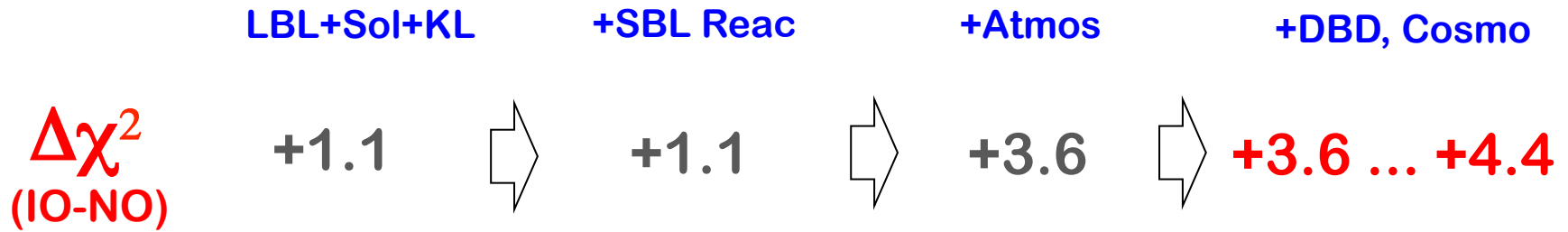
Oscill. + $0\nu\beta\beta$ + Cosmo #9

[RHS plot (inner red curve) shows how a cosmological “claim” of $\Sigma > 0$ could look like]

Oscill. + $0\nu\beta\beta$ + Cosmo #6

[Case with “aggressive” bounds from cosmology]

Grand total of IO-NO differences:



Small but coherent steps: **N.O. favored**... Overall preference at **$1.9\sigma - 2.1\sigma$**

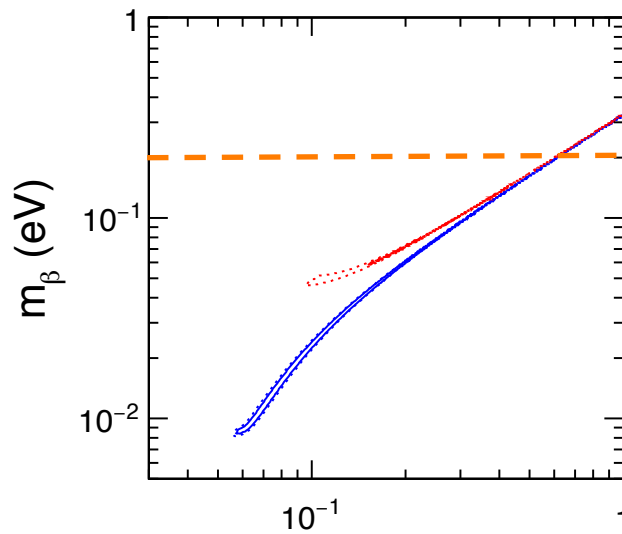
TABLE III: Values of $\Delta\chi_{\text{IO-NO}}^2$ from the global analysis of oscillation and non oscillation data (numbered according to the adopted cosmological datasets as in Table II), to be compared with the value 3.6 from oscillation data only [Eq. (9)]. An overall preference emerges for NO, at the level of $1.9-2.1\sigma$.

| # | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
|-------------------------------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| $\Delta\chi_{\text{IO-NO}}^2$ | 4.3 | 3.8 | 4.4 | 4.2 | 3.9 | 4.4 | 3.6 | 3.7 | 3.8 | 3.7 | 3.8 | 3.9 |

The statistical significance of possible hints about ordering is currently debated. If they are not fluctuations, expect (fractional) improvements in upcoming years
Dedicated projects are planned with reactor, atmospheric, accelerator neutrinos

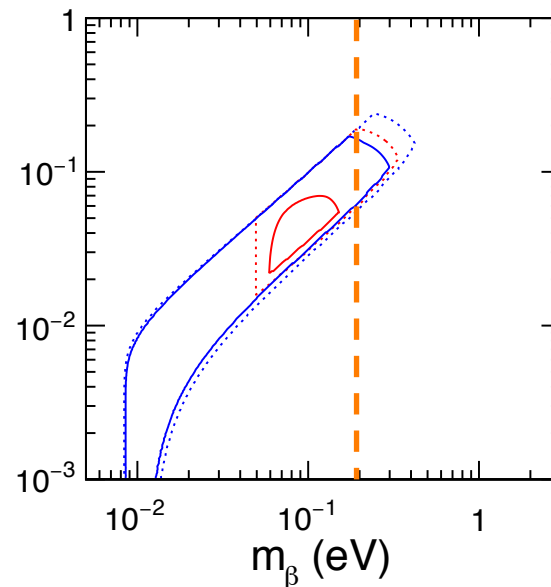
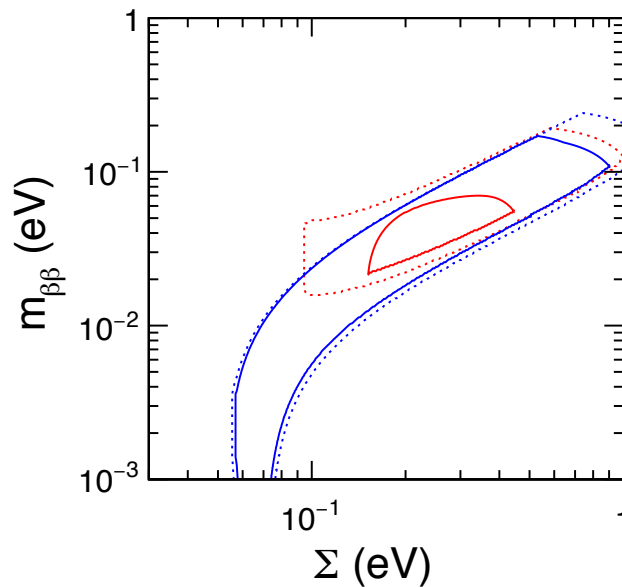
Implications for β -decay (weak cosmo bounds)

$$m_\beta = [c_{13}^2 c_{12}^2 m_1^2 + c_{13}^2 s_{12}^2 m_2^2 + s_{13}^2 m_3^2]^{\frac{1}{2}}$$



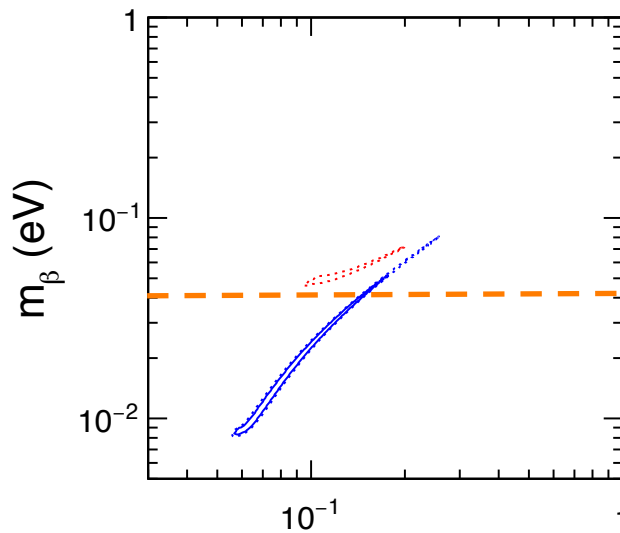
Oscill. + $0\nu\beta\beta$ + Cosmo #10
Any Ordering

--- KATRIN sensit.



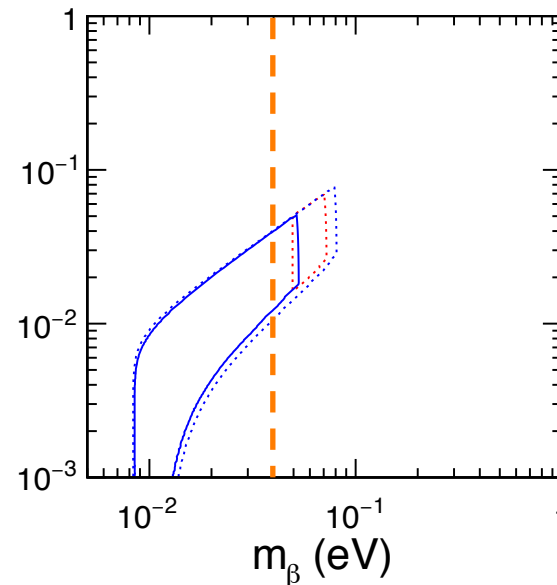
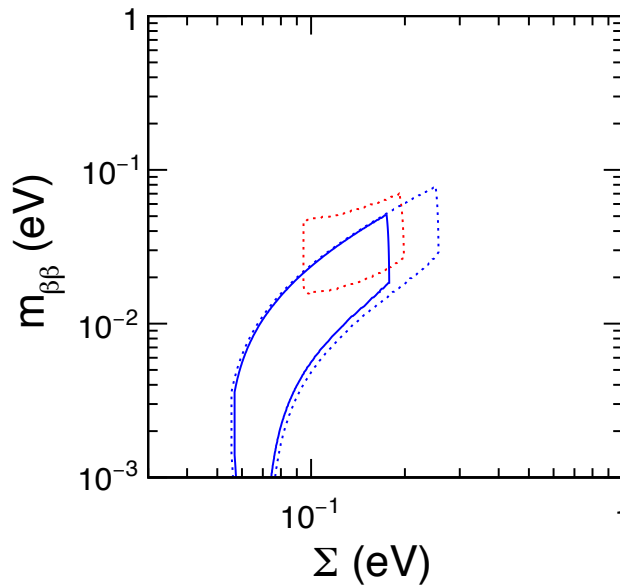
Implications for β -decay (strong cosmo bounds)

$$m_\beta = [c_{13}^2 c_{12}^2 m_1^2 + c_{13}^2 s_{12}^2 m_2^2 + s_{13}^2 m_3^2]^{\frac{1}{2}}$$



Oscill. + $0\nu\beta\beta$ + Cosmo #6
Any Ordering

--- e.g., Project-8 goal



SUMMARY

- **Status of known 3ν oscillation parameters:**
Precision era (but PMNS accuracy far from CKM)
- **Trends of unknown oscillation parameters:**
Favoring **CPV** with $\sin\delta < 0$, nonmax θ_{23} , and **NO**
- **Status of constraints from $0\nu\beta\beta$ & Cosmology:**
Sub-eV sensitivity; Cosmo analysis with **NO vs IO**
- **Oscillation + nonoscillation global analysis:**
Corroborates NO with respect to IO at $\sim 2\sigma$ level

PROSPECTS - oscillations

- **Known 3ν oscillation parameters:**

Higher accuracy with LBL acceler., JUNO react. + others

- **CPV:**

If $\sin\delta \sim -1$, then T2K+NOvA may probe CPV at $\sim 3\sigma$

Higher C.L. requires future LBL acc. (DUNE, Hyper-K)

- **Hierarchy:**

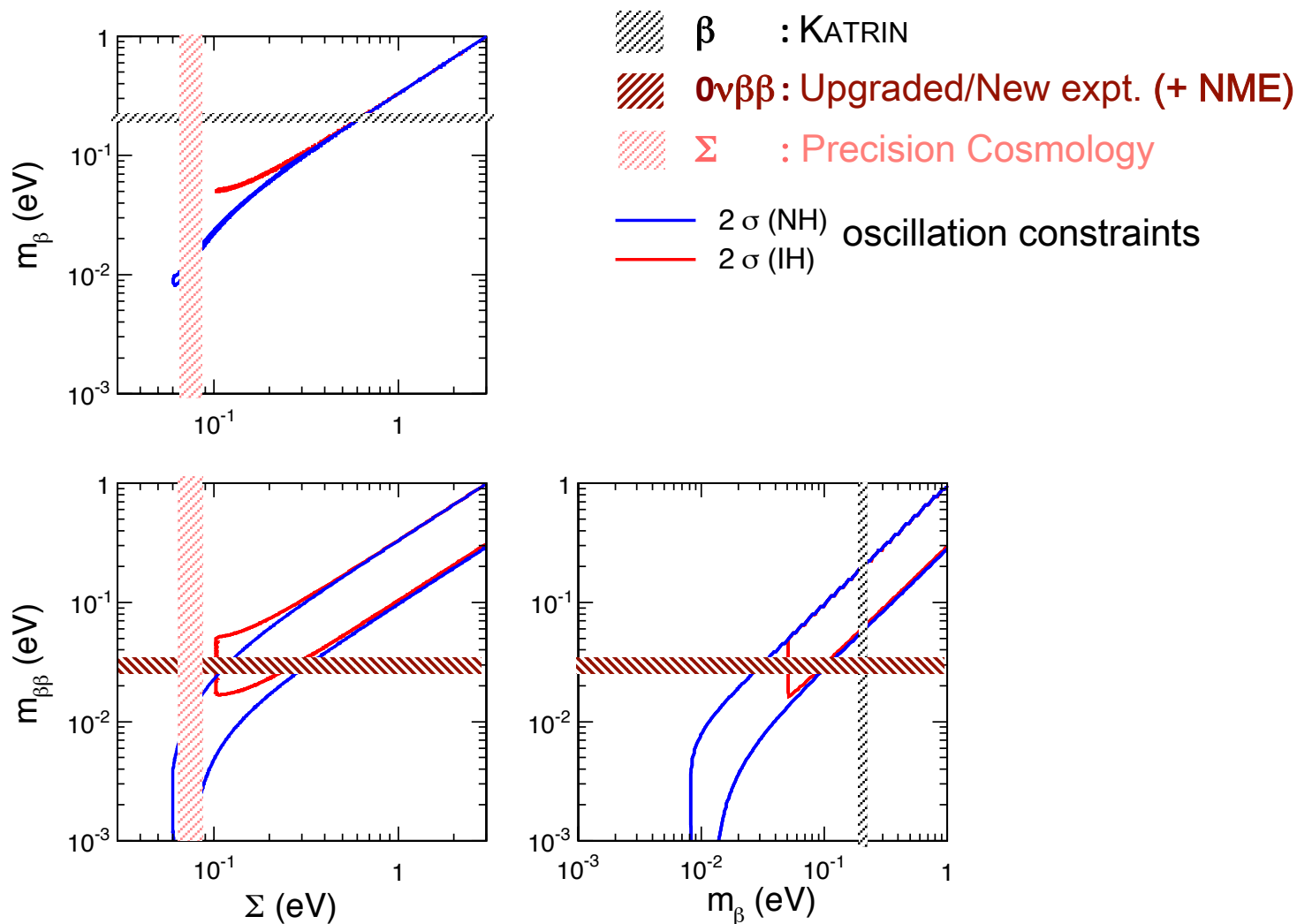
Expect progress from T2K+NOvA and future expts:

JUNO reactor, LBL acceler., Large-volume atmospheric

- **Octant of θ_{23} :**

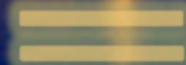
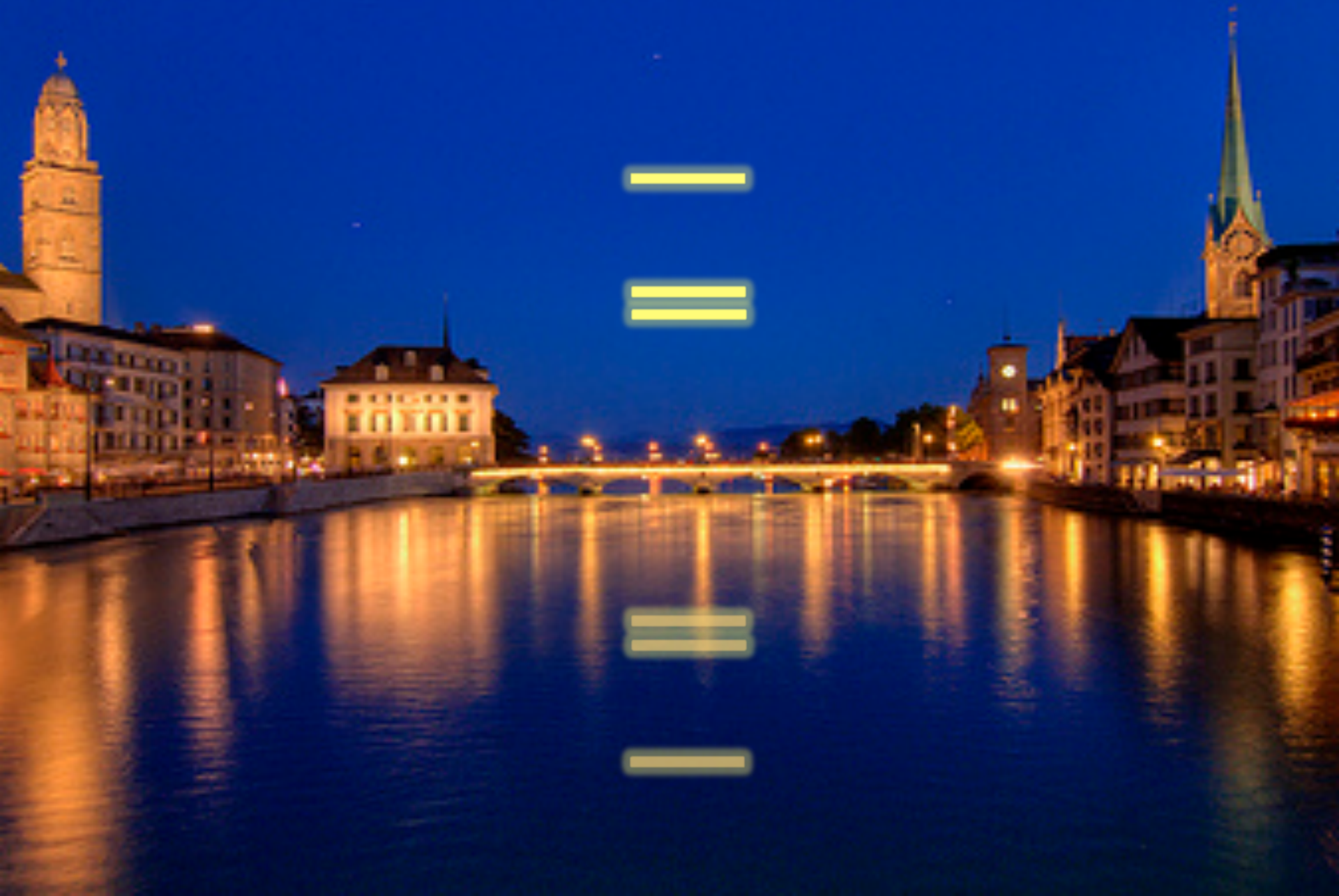
Lifting degeneracy **possible, but not easy** at high CL

Non-oscillations: Upper limits on m_β , $m_{\beta\beta}$, Σ in ~ 10 years ?



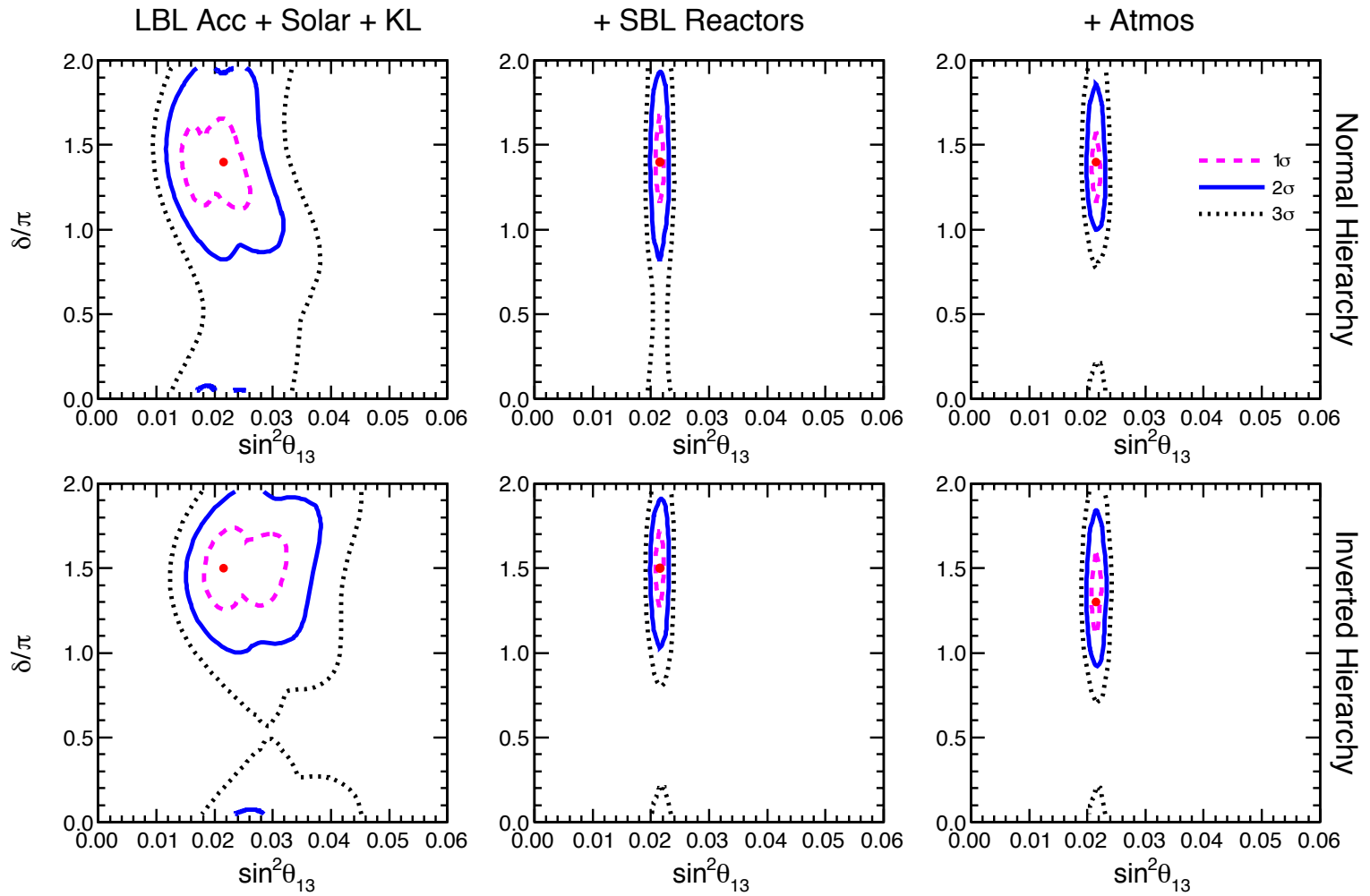
Large phase space for **discoveries... and surprises** (beyond 3ν ?)

Thank you for your attention

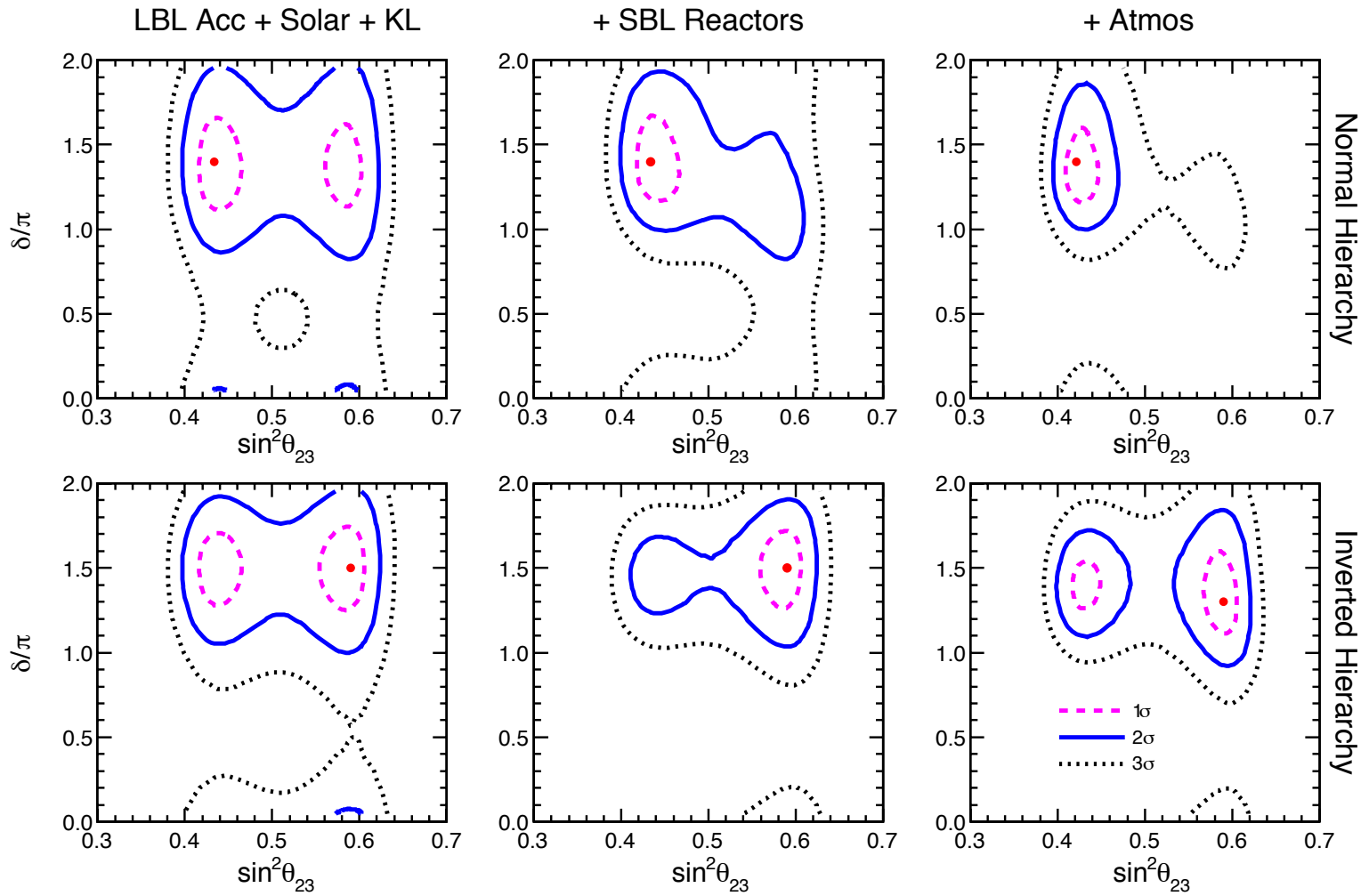


Extra slides

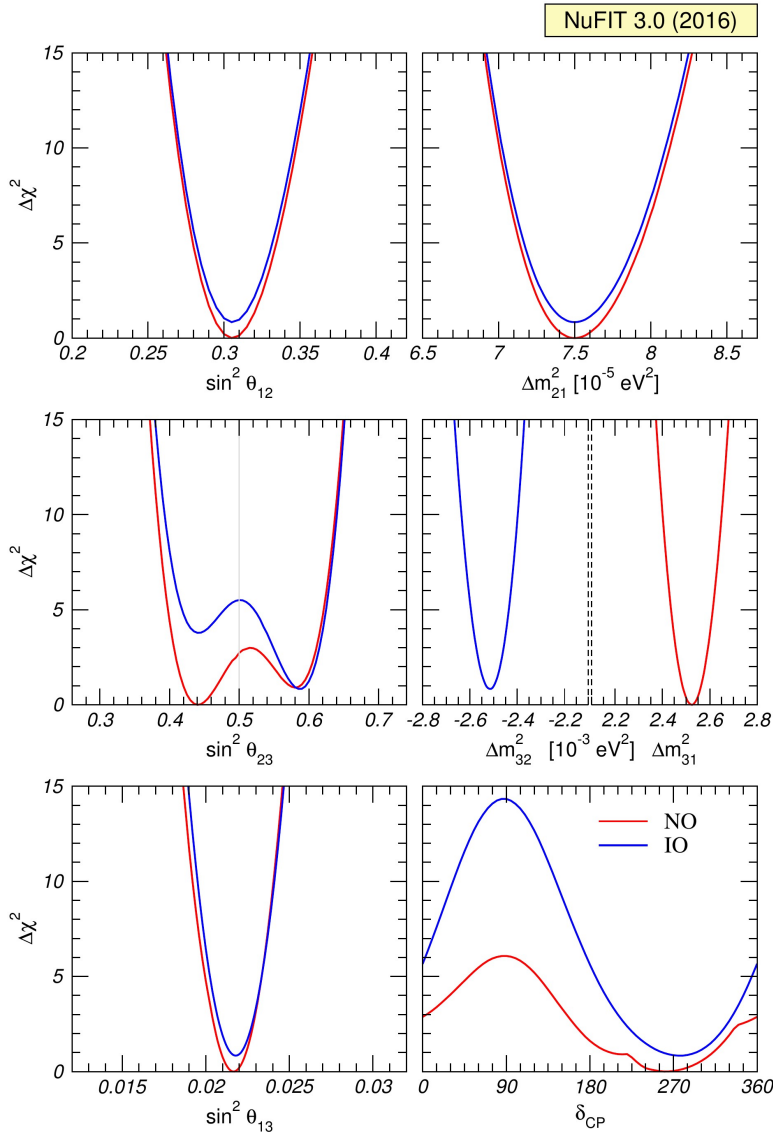
Supplementary to arXiv:1703.04471



Supplementary to arXiv:1703.04471

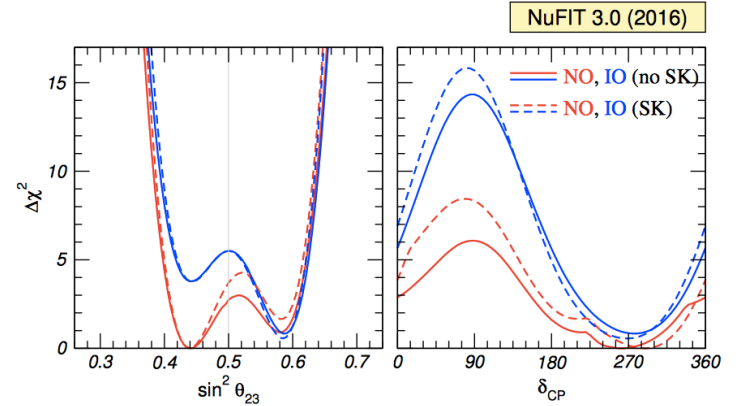


NuFIT: I. Esteban, M.C. Gonzalez-Garcia, M. Maltoni, I. Martinez-Soler, T. Schwetz



← All - SK atmospheric

All + SK atmospheric



arXiv:1611.01514

Bayesian...

Strong Bayesian Evidence for the Normal Neutrino Hierarchy

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Abstract. The configuration of the three neutrino masses can take two forms, known as the normal and inverted hierarchies. We compute the Bayesian evidence associated with these two hierarchies. Previous studies found a mild preference for the normal hierarchy, and this was driven by the asymmetric manner in which cosmological data has confined the available parameter space. Here we identify the presence of a second asymmetry, which is imposed by data from neutrino oscillations. By combining constraints on the squared-mass splittings [1] with the limit on the sum of neutrino masses of $\Sigma m_\nu < 0.13$ eV [2], and using a minimally informative prior on the masses, we infer odds of 42:1 in favour of the normal hierarchy, which is classified as “strong” in the Jeffreys’ scale. We explore how these odds may evolve in light of higher precision cosmological data, and discuss the implications of this finding with regards to the nature of neutrinos. Finally the individual masses are inferred to be $m_1 = 3.80_{-3.73}^{+26.2}$ meV; $m_2 = 8.8_{-1.2}^{+18}$ meV; $m_3 = 50.4_{-1.2}^{+5.8}$ meV (95% credible intervals).

Frequentist...

Cosmological constraints on the neutrino mass including systematic uncertainties

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April 3, 2017

Abstract

When combining cosmological and oscillations results to constrain the neutrino sector, the question of the propagation of systematic uncertainties is often raised. We address it in the context of the derivation of an upper bound on the sum of the neutrino masses (Σm_ν) with recent cosmological data. This work is performed within the Λ CDM model extended to Σm_ν , for which we advocate the use of three mass-degenerate neutrinos. We focus on the study of systematic uncertainties linked to the foregrounds modelling in CMB data analysis, and on the impact of the present knowledge of the reionisation optical depth. This is done through the use of different likelihoods, built from PLANCK data. Limits on Σm_ν are derived with various combinations of data, including latest BAO and SNIa results. We also discuss the impact of the preference of current CMB data for amplitudes of the gravitational lensing distortions higher than expected within the Λ CDM model, and add the PLANCK CMB lensing. We then derive a robust upper limit: $\Sigma m_\nu < 0.17$ eV at 95% CL, including 0.01 eV of foreground systematics. We also discuss the neutrino mass repartition and show that today’s data do not allow to disentangle normal from inverted hierarchy. The impact on the other cosmological parameters is also reported, for different assumptions on the neutrino mass repartition, and different high and low multipoles CMB likelihoods.

Bayesian...

Comment on “Strong Evidence for the Normal Neutrino Hierarchy”

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^dMcWilliams Center for Cosmology, Department of Physics, Carnegie Mellon University, Pittsburgh, PA 15213, USA; Lawrence Berkeley National Laboratory (LBNL), Physics Division, Berkeley, CA 94720-8153, USA; Berkeley Center for Cosmological Physics, University of California, Berkeley, CA 94720, USA

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Abstract. In the preprint arxiv:1703.03425 “strong evidence” for the normal neutrino mass ordering is claimed. The authors obtain Bayesian odds of 42:1 in favour of the normal ordering. Their conclusion is based on adopting a flat logarithmic prior for the three neutrino masses. Such an assumption favours a hierarchical spectrum for the masses, which is much easier to accommodate for the normal mass ordering, and hence their prior assumption makes the inverted ordering much less likely *a priori*. We argue that the claimed “evidence” for normal ordering is almost entirely driven by the adopted prior and not due to the data itself.

... and more ...

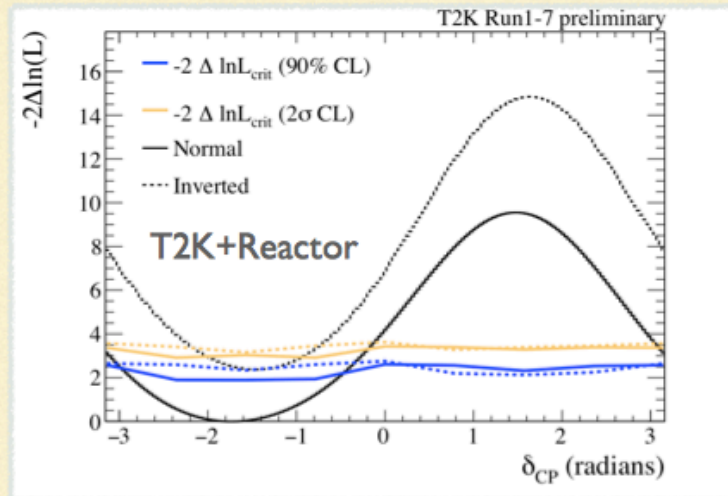
... debated topic
in cosmology!

arXiv:1703.03425v2 [astro-ph.CO] 4 Jun 2017

arXiv:1703.04585v1 [astro-ph.CO] 14 Mar 2017

arXiv:1703.10829v1 [astro-ph.CO]

ANALYSIS RESULTS: θ_{13} AND δ_{CP}



| | $\nu_{e\text{-like}}$ | | $\bar{\nu}_{e\text{-like}}$ | |
|------------------------|-----------------------|----------|-----------------------------|----------|
| Mass hierarchy | Normal | Inverted | Normal | Inverted |
| $\delta_{CP} = -\pi/2$ | 28.8 | 25.5 | 6.0 | 6.5 |
| $\delta_{CP} = 0$ | 24.2 | 21.2 | 6.9 | 7.4 |
| $\delta_{CP} = \pi/2$ | 19.7 | 17.2 | 7.7 | 8.4 |
| $\delta_{CP} = \pi$ | 24.2 | 21.6 | 6.8 | 7.4 |
| Data | 32 | | 4 | |

- Exclude $\sin(\delta_{CP})=0$ at 90% C.L.
- Observed events favour large CPV ($\delta_{CP} \approx -\pi/2$) and normal mass hierarchy
- Data implies more CPV → stronger limits than expected
 - “Statistical fluctuation”? → need further data

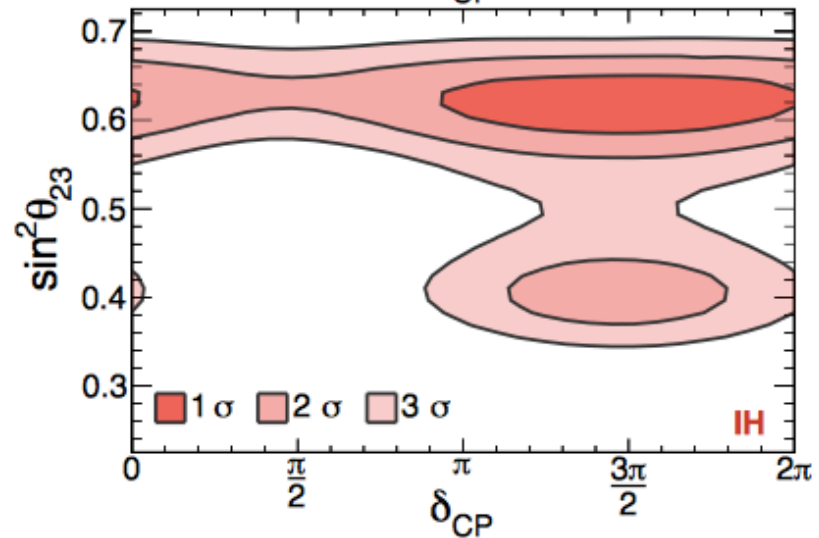
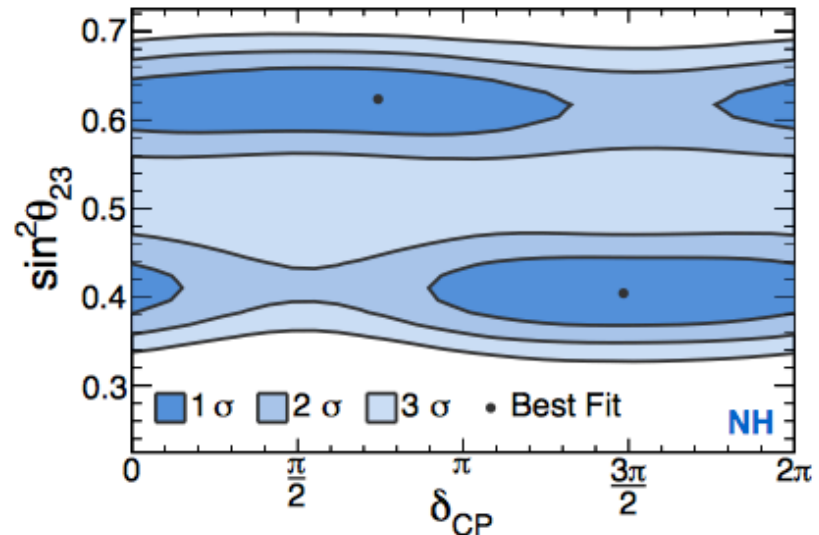
$\nu_\mu \rightarrow \nu_e$ Oscillation Results

- Fit for hierarchy, δ_{CP} , $\sin^2 \theta_{23}$
- Constrain $\sin^2 2\theta_{13} = 0.085 \pm 0.005$ from reactor experiments
- Simultaneous fit NOvA disappearance data
- Global best fit, two degenerate points in Normal Hierarchy

$$\delta_{cp} = 1.48\pi, \sin^2(\theta_{23}) = 0.404$$

$$\delta_{cp} = 0.74\pi, \sin^2(\theta_{23}) = 0.623$$

- best fit IH-NH, $\Delta\chi^2=0.47$
- Lower octant, IH is disfavoured at greater than 93% C.L for all values of δ_{CP}

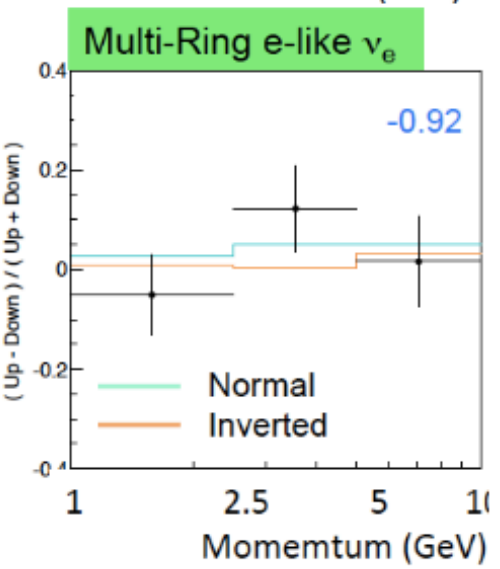
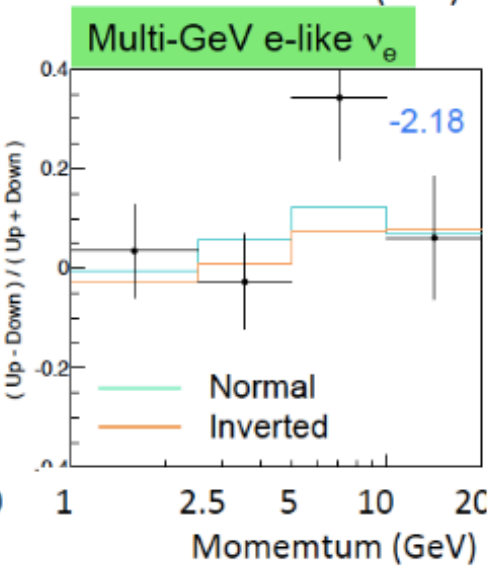
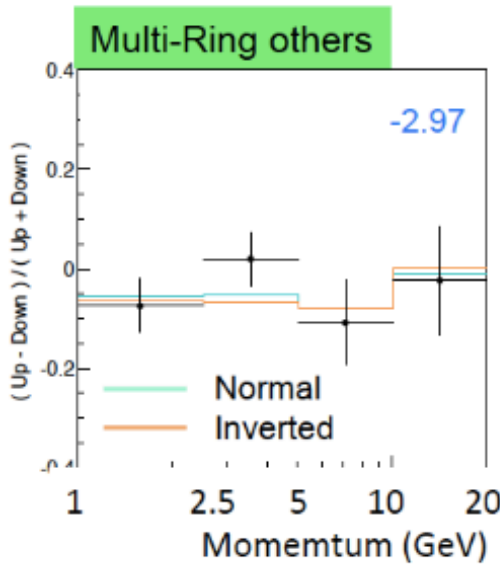
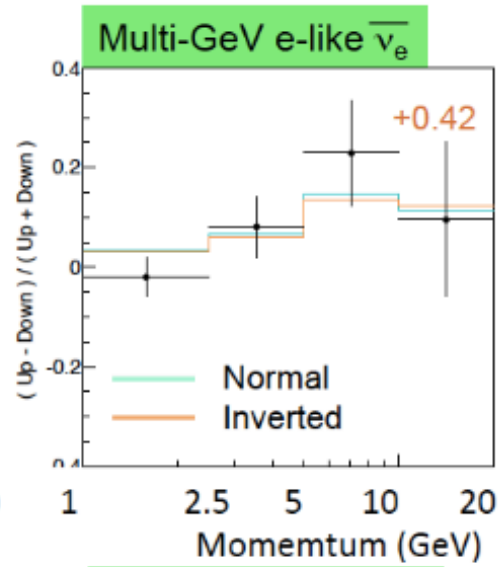
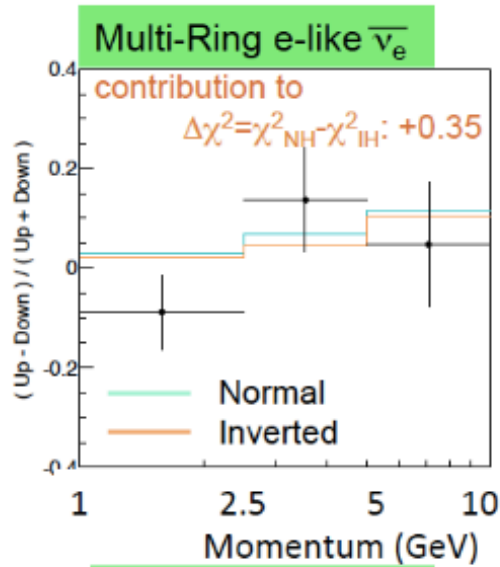


Super-Kamiokande atmospheric: E. Kearns at APS 2017 April Meeting

Hierarchy Sensitive Samples

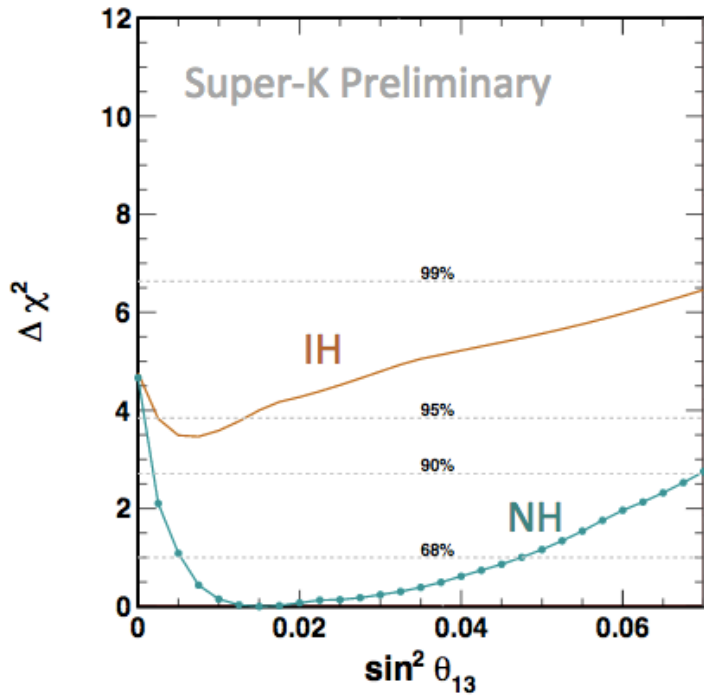
$$\frac{\text{UP-DOWN}}{\text{UP+DOWN}}$$

as a func. of p



Super-Kamiokande atmospheric: E. Kearns at APS 2017 April Meeting

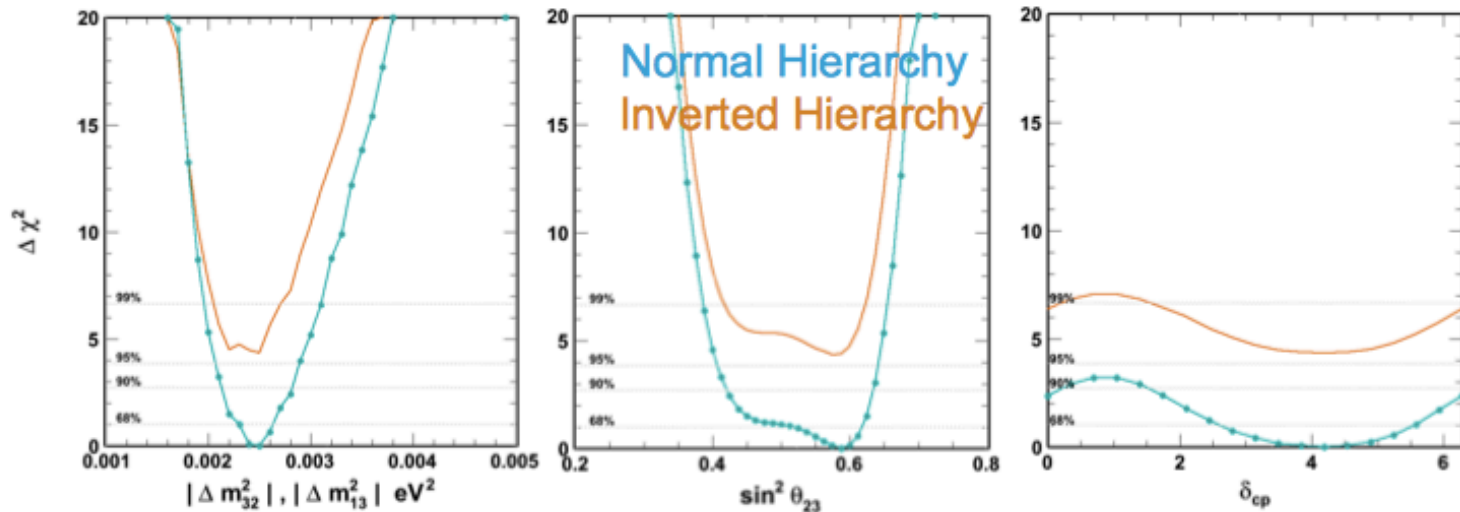
θ_{13} Free – Atm. ν only



Graph by Steve Parke

| Experiment | $\sin^2 2\theta_{13}$ | Value |
|---------------|-----------------------|---------------------------|
| Daya Bay | | 0.0841 ± 0.0033 |
| RENO | | 0.082 ± 0.010 |
| D-CHOOZ | | 0.111 ± 0.018 |
| T2K | | $0.140^{+0.038}_{-0.032}$ |
| | | $0.170^{+0.045}_{-0.037}$ |
| MINOS | | $0.051^{+0.038}_{-0.030}$ |
| | | $0.093^{+0.054}_{-0.049}$ |
| SK Atm. ν | | NH |
| | | IH |

Atmv data fit w/ fixed θ_{13}



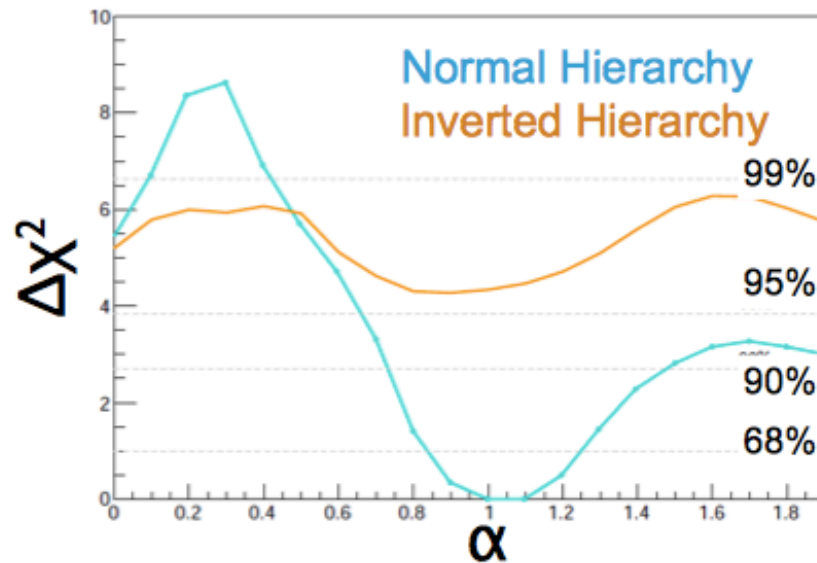
| Fit (517 dof) | χ^2 | $\sin^2\theta_{13}$ | δ_{CP} | $\sin^2\theta_{23}$ | $ \Delta m^2_{32} eV^2$ |
|---------------|----------|---------------------|---------------|---------------------|-------------------------|
| SK (IH) | 576.08 | 0.0219 (fix) | 4.189 | 0.575 | 2.5×10^{-3} |
| SK (NH) | 571.74 | 0.0219 (fix) | 4.189 | 0.587 | 2.5×10^{-3} |

- Mass hierarchy: $\Delta\chi^2 = \chi^2_{NH} - \chi^2_{IH} = -4.3$ (-3.1 expected)
- Under IH hypothesis, the probability to obtain -4.3 or less is 3.1% ($\sin^2\theta_{23}=0.6$) and 0.7% ($\sin^2\theta_{23}=0.4$).
- Under NH hypothesis, it is as large as 45% ($\sin^2\theta_{23}=0.6$)

Matter effect fit

$$H_{\text{matter}} = \begin{pmatrix} \frac{m_1^2}{2E} & 0 & 0 \\ 0 & \frac{m_2^2}{2E} & 0 \\ 0 & 0 & \frac{m_3^2}{2E} \end{pmatrix} + U^\dagger \begin{pmatrix} \alpha a & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} U$$

α : scale factor
 $a = \sqrt{2} G_f N_e$



- Best fit $\alpha=1$ for NH, consistent w/ standard matter effect
- $\Delta\chi^2=5.2$ for $\alpha=0$, Data disfavors zero matter-effect by $>2\sigma$

MSW amplitude in solar+reactor data: G.L. Fogli and E. Lisi, New J.Phys. 6 (2004) 139

