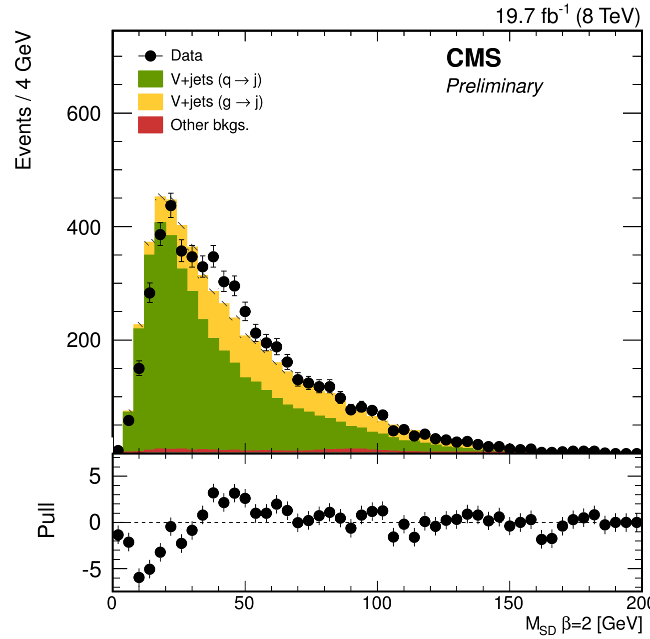
Theory Advances in Jet Substructure

Andrew Larkoski
Reed College

Digging Deeper at LHC Run II, February 24, 2017

Motivation for Precision Jet Substructure

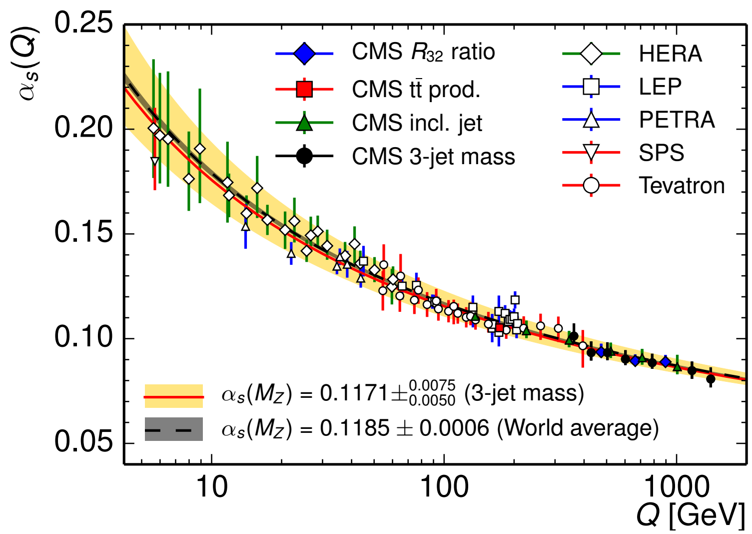
Ever increasing set of experimental measurements



CMS-PAS-JME-14-002

Probing orthogonal regime of QCD

New α_s extractions using resummation-sensitive observables



Eur. Phys. J. C 75 (2015) 186

Quark and gluon jet definitions important for new physics and pdf constraints

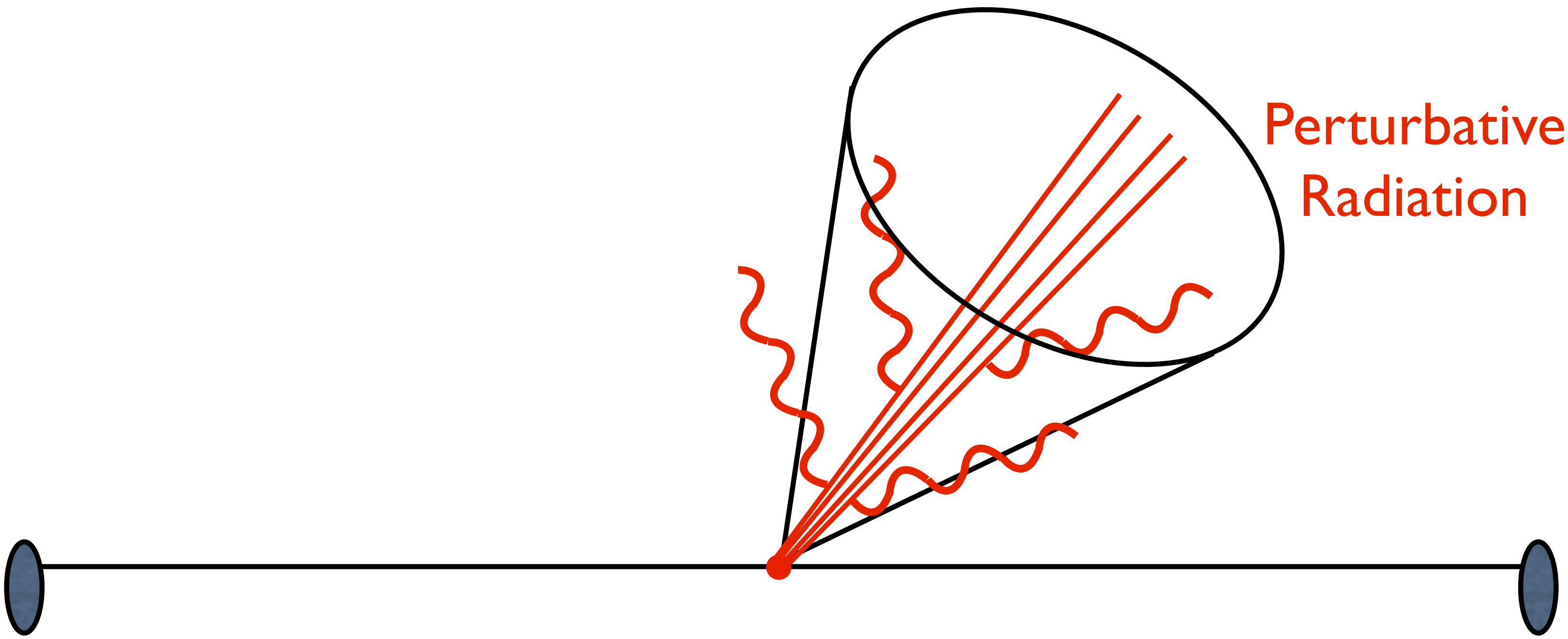
How to get to Precision Jet Substructure

Measure m_J^2 on the jet in pp → Z + j events

How to get to Precision Jet Substructure

Measure m_J^2 on the jet in pp→Z + j events

Experimental Challenge:
Contamination captured in the jet



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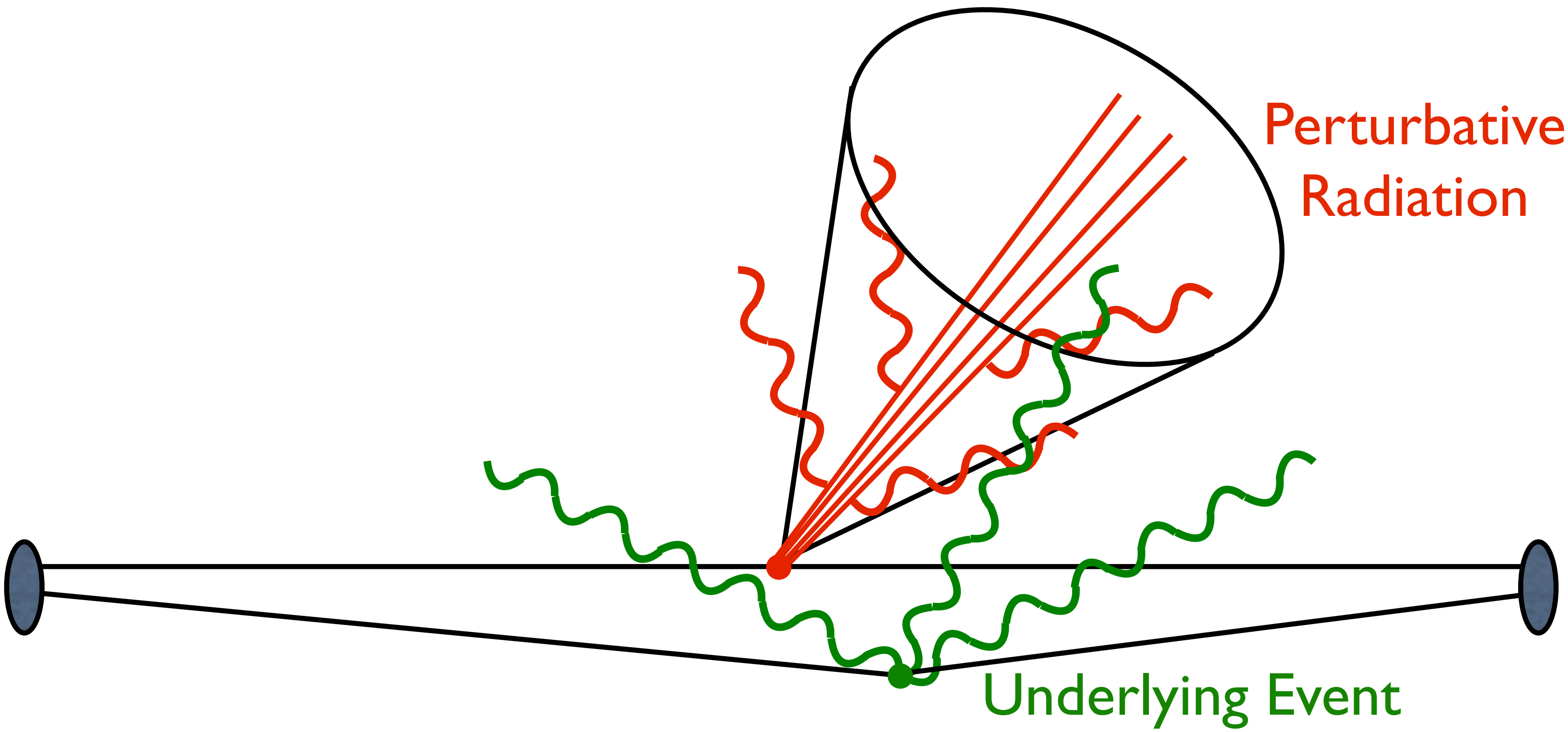

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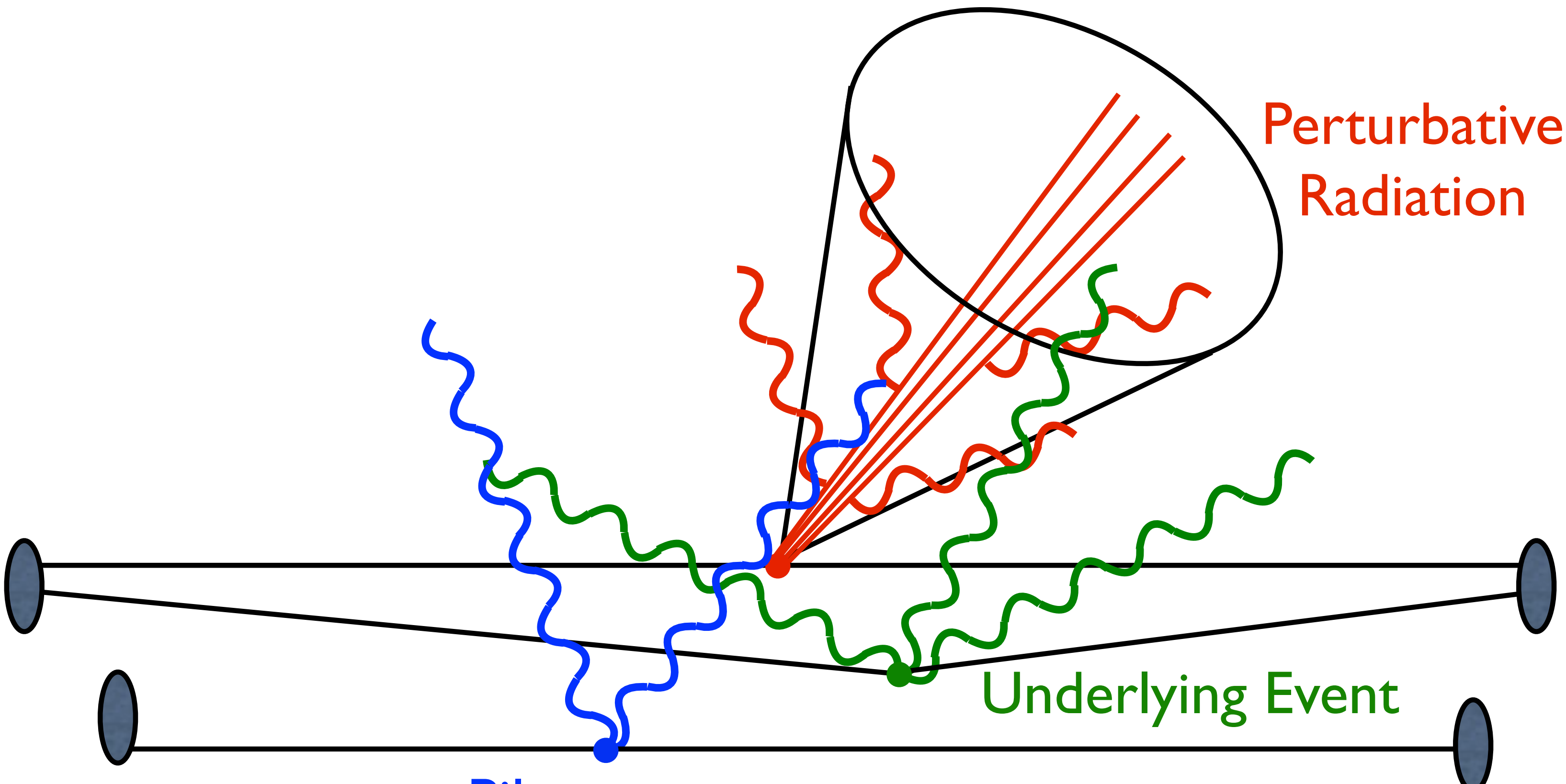
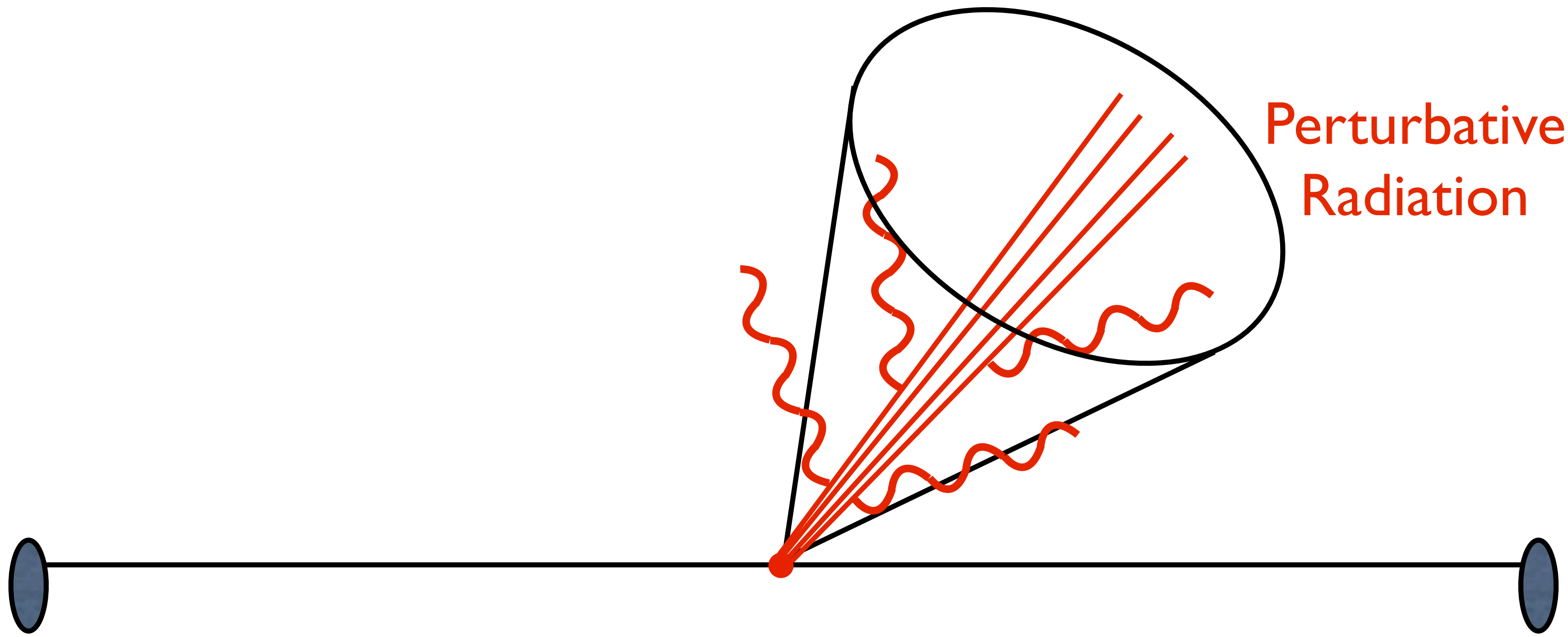


How to get to Precision Jet Substructure

Measure m_J^2 on the jet in pp → Z + j events

Theoretical Challenge:
Non-Global Logarithms

Dasgupta, Salam 2001



How to get to Precision Jet Substructure

Measure m_J^2 on the jet in pp → Z + j events

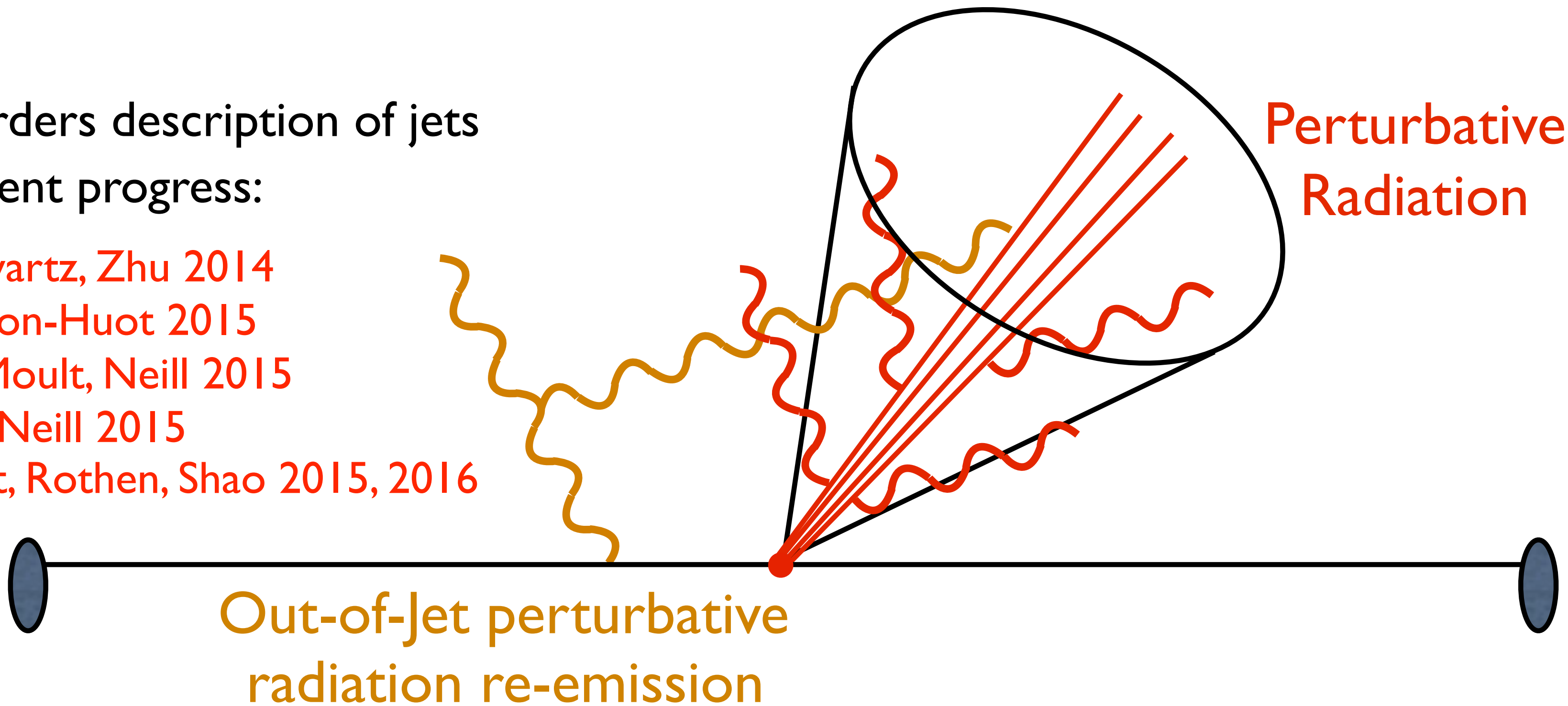
Theoretical Challenge:
Non-Global Logarithms

Dasgupta, Salam 2001

Prohibits all-orders description of jets

Recent progress:

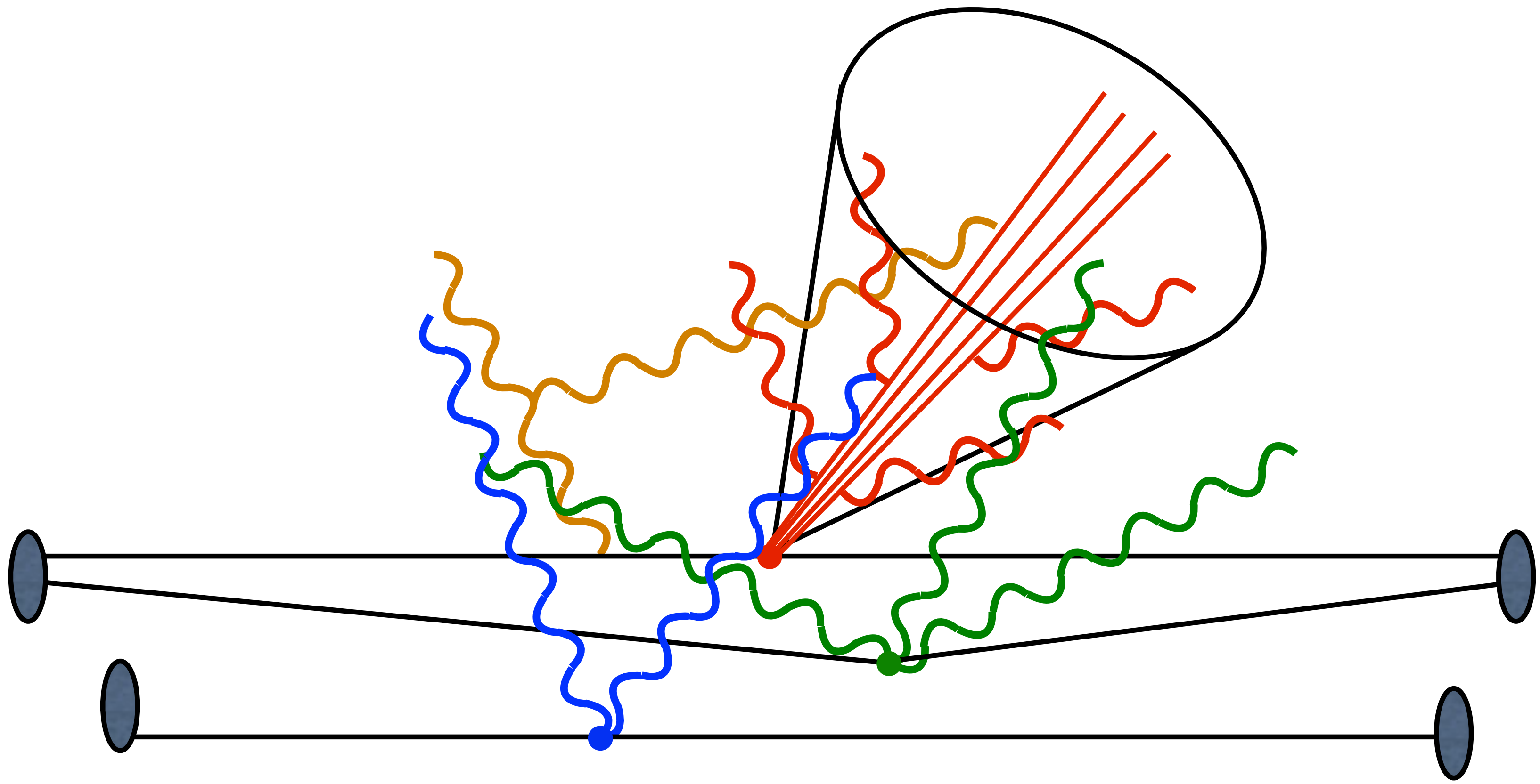
Schwartz, Zhu 2014
Caron-Huot 2015
AJL, Moult, Neill 2015
Neill 2015
Becher, Neubert, Rothen, Shao 2015, 2016



How to get to Precision Jet Substructure

Measure m_J^2 on the jet in pp → Z + j events

Can eliminate these problems by grooming the jet!

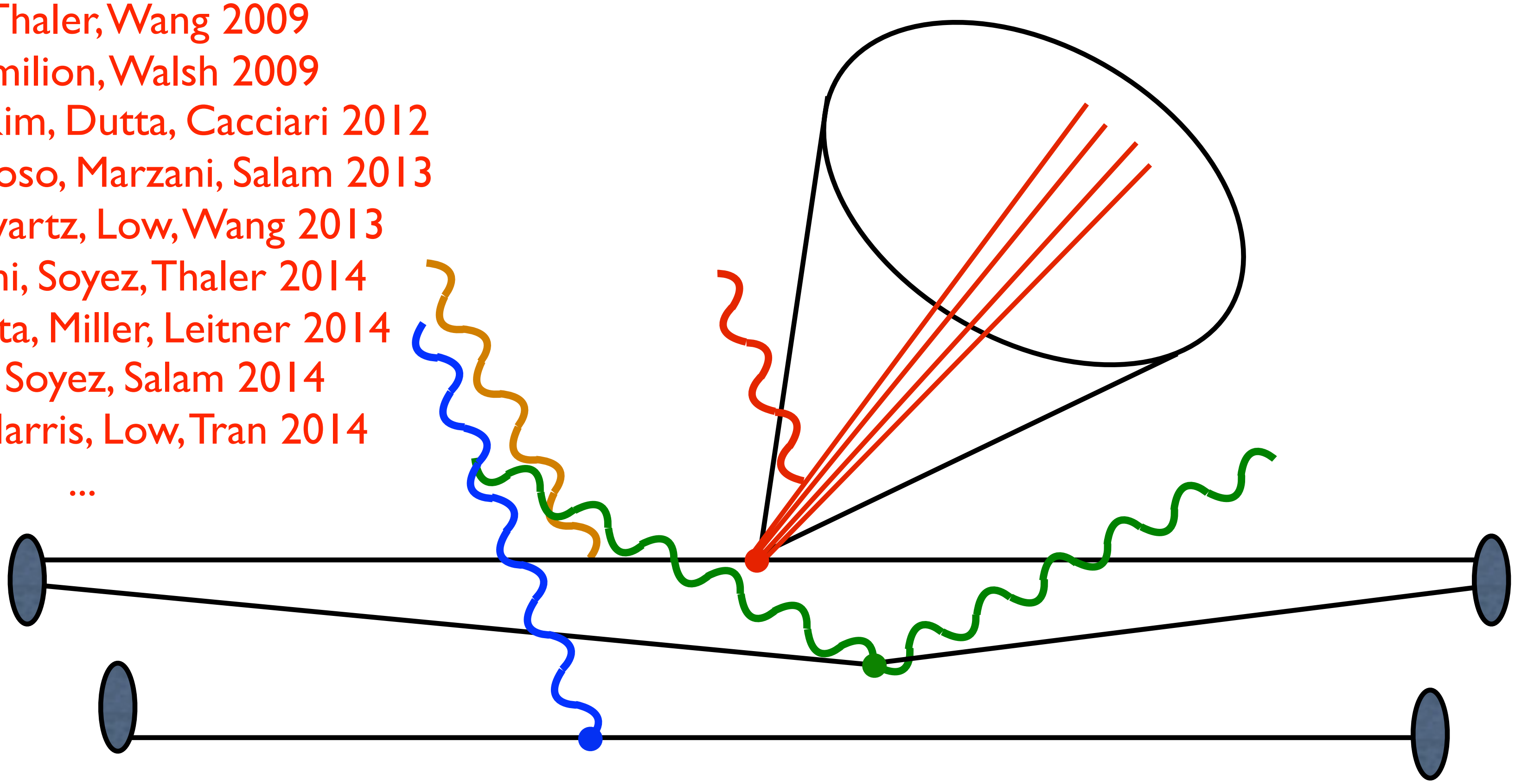


How to get to Precision Jet Substructure

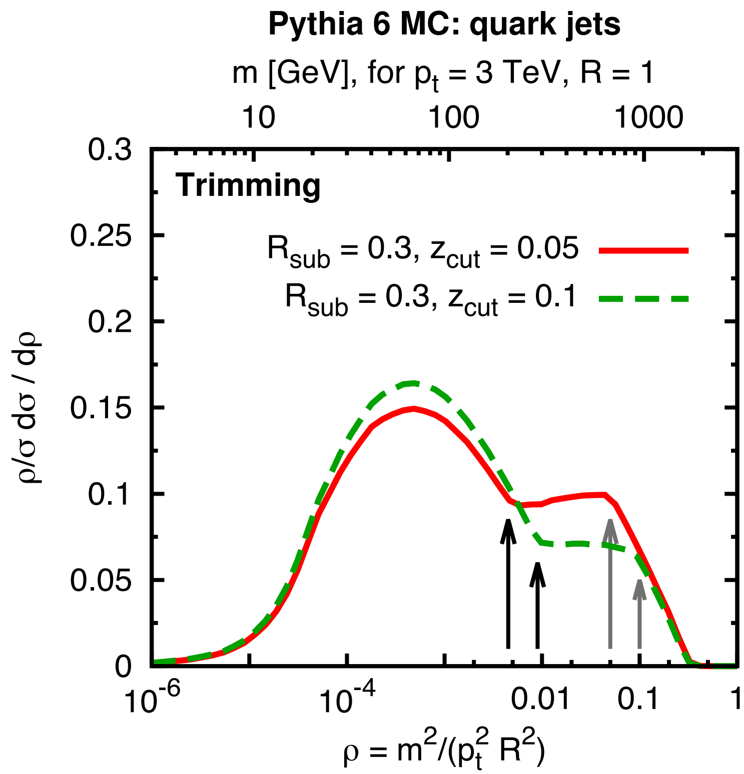
Measure m_J^2 on the jet in pp → Z + j events

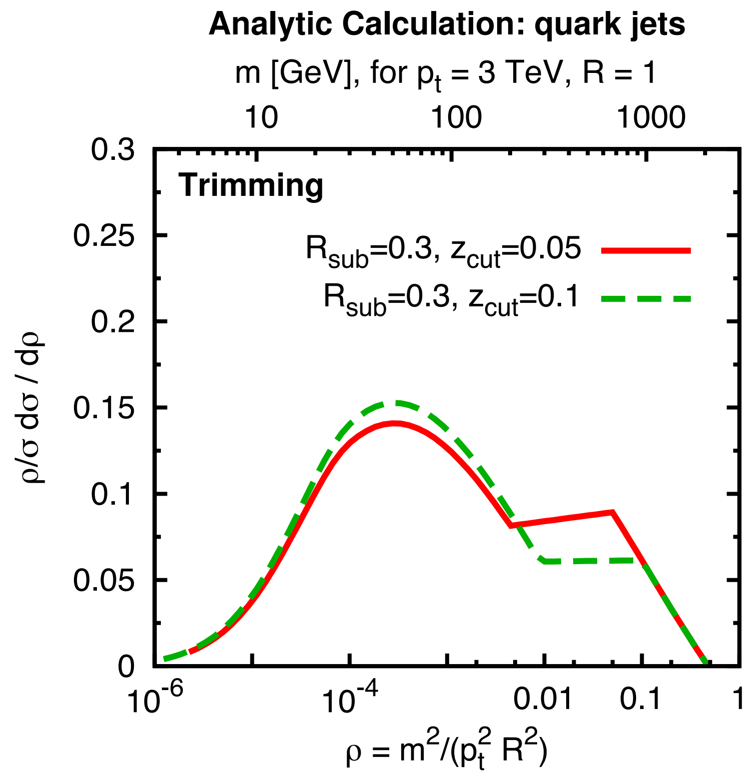
Can eliminate these problems by grooming the jet!

Butterworth, Davison, Rubin, Salam 2008
Cacciari, Salam, Soyez 2008
Krohn, Thaler, Wang 2009
Ellis, Vermilion, Walsh 2009
Soyez, Salam, Kim, Dutta, Cacciari 2012
Dasgupta, Fregoso, Marzani, Salam 2013
Krohn, Schwartz, Low, Wang 2013
AJL, Marzani, Soyez, Thaler 2014
Berta, Spousta, Miller, Leitner 2014
Cacciari, Soyez, Salam 2014
Bertolini, Harris, Low, Tran 2014
...



What has been done: NLL resummation

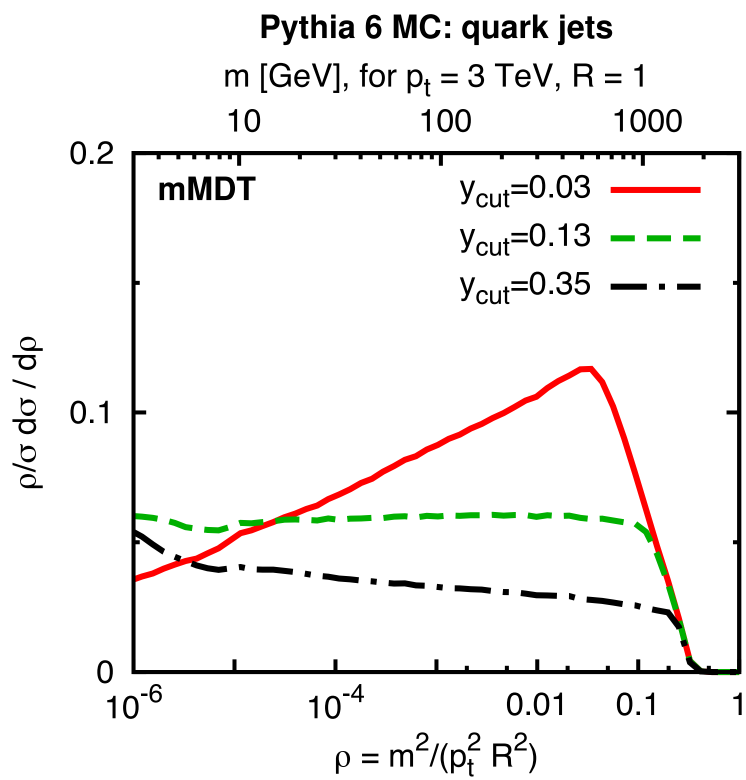


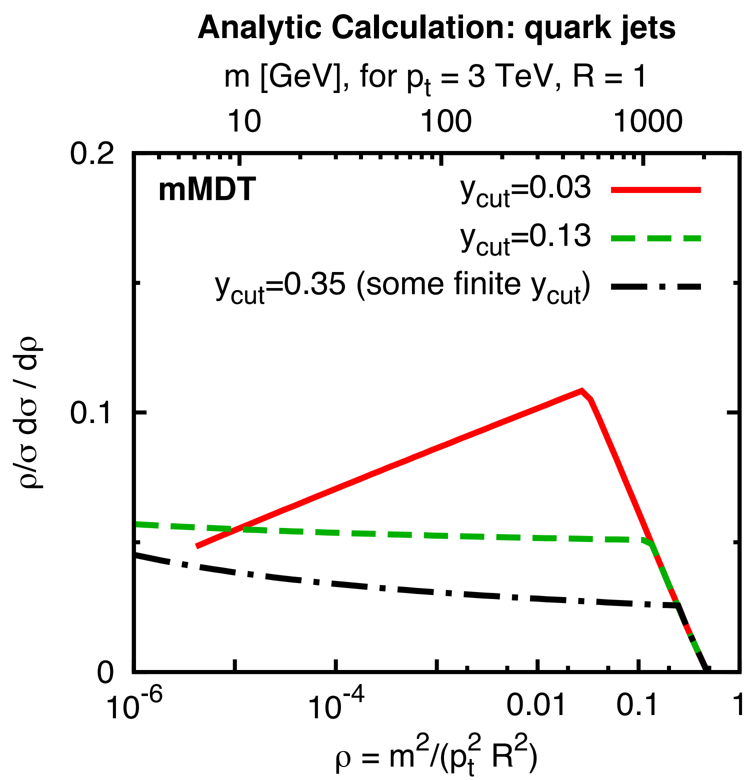


Dasgupta, Fregoso, Marzani, Salam 2013

Trimming:
Krohn, Thaler, Wang 2009

What has been done: NLL resummation



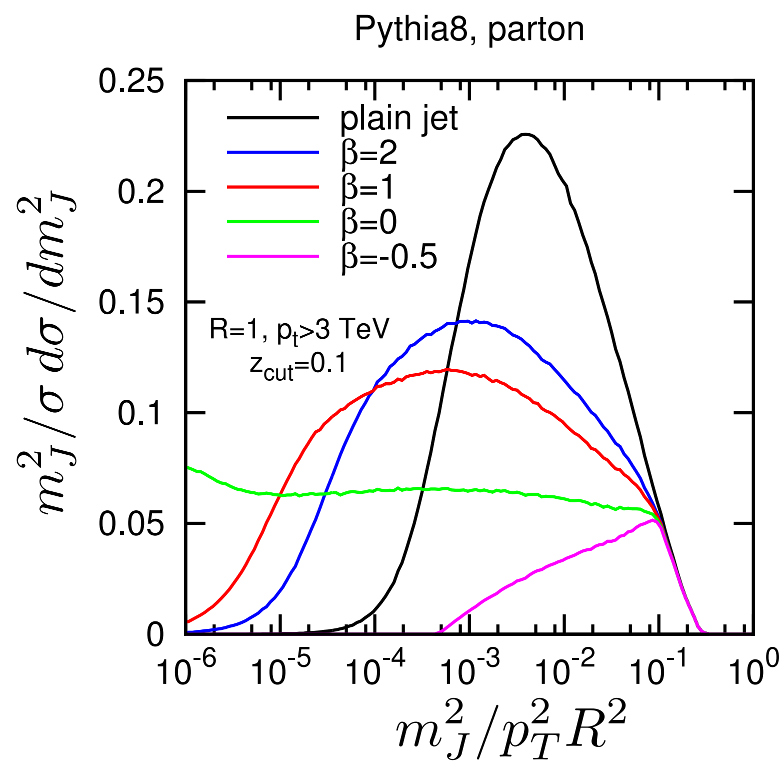


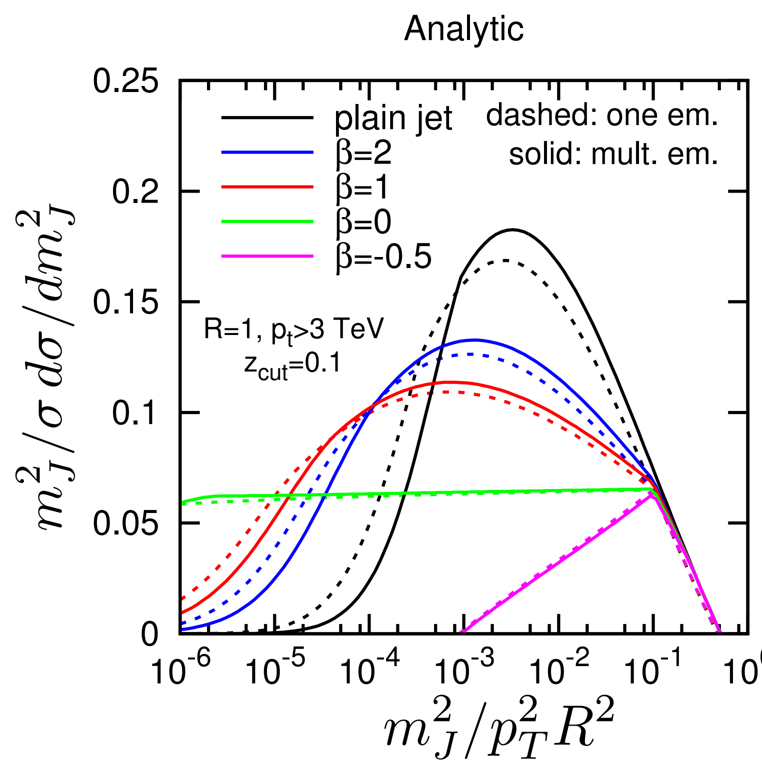
Dasgupta, Fregoso, Marzani, Salam 2013

	highest logs	transition(s)	Sudakov peak	NGLs	NP: $m^2 \lesssim$
plain mass	$\alpha_s^n L^{2n}$	—	$L \simeq 1/\sqrt{\bar{\alpha}_s}$	yes	$\mu_{\rm NP}\, p_t\, R$
trimming	$\alpha_s^n L^{2n}$	$z_{\rm cut},\ r^2 z_{\rm cut}$	$L \simeq 1/\sqrt{\bar{\alpha}_s} - 2\ln r$	yes	$\mu_{\rm NP}\, p_t\, R_{\rm sub}$
pruning	$\alpha_s^n L^{2n}$	$z_{\rm cut},\ z_{\rm cut}^2$	$L \simeq 2.3/\sqrt{\bar{\alpha}_s}$	yes	$\mu_{\rm NP}\, p_t\, R$
MDT	$\alpha_s^n L^{2n-1}$	$y_{\rm cut},\ \frac{1}{4}y_{\rm cut}^2,\ y_{\rm cut}^3$	—	yes	$\mu_{\rm NP}\, p_t\, R$
Y-pruning	$\alpha_s^n L^{2n-1}$	$z_{\rm cut}$	(Sudakov tail)	yes	$\mu_{\rm NP}\, p_t\, R$
mMDT	$\alpha_s^n L^{n}$	$y_{\rm cut}$	—	no	$\mu_{\rm NP}^2/y_{\rm cut}$

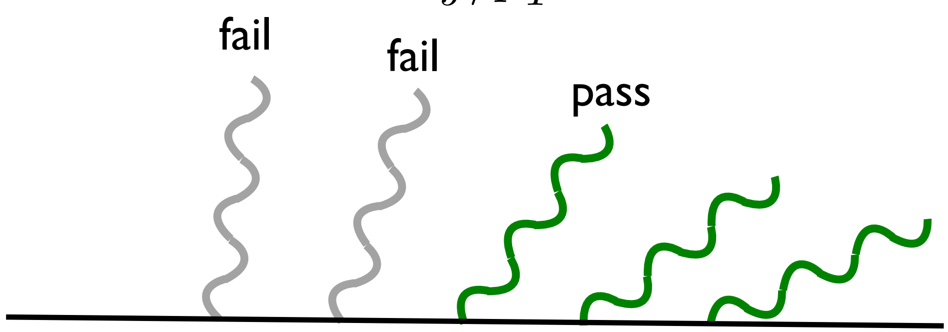
Explicit calculations suggest better techniques!

What has been done: NLL resummation





AJL, Marzani, Soyez, Thaler 2014



Only mMDT/Soft Drop groomers eliminate NGLs!

Soft Drop: $$\frac{\min[p_{Ti}, p_{Tj}]}{p_{Ti}+p_{Tj}} > z_{\rm cut}\left(\frac{R_{ij}}{R}\right)^\beta$$

β = 0: mMDT

Procedure to get NNLL Resummation

Soft Drop the hardest jet in pp→Z + j events

$$\frac{\min[p_{Ti}, p_{Tj}]}{p_{Ti}+p_{Tj}} > z_{\rm cut}\left(\frac{R_{ij}}{R}\right)^{\beta}$$

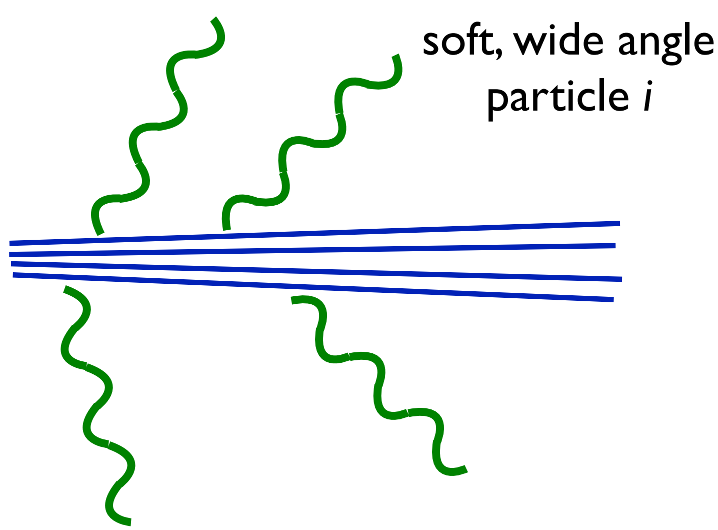
Measure m_J^2 of the soft dropped jet:

$$m_J^2 \simeq \sum_{i<j\in J} p_{Ti}p_{Tj}R_{ij}^2$$

Focus on the regime where:

$$m_J^2 \ll z_{\rm cut}p_{TJ}^2 \ll p_{TJ}^2$$

All remaining particles in the jet must be collinear!



1) $\frac{p_{Ti}}{p_{TJ}} \sim z_{\rm cut} \longrightarrow m_J^2 \sim z_{\rm cut}p_{TJ}^2$

2) $\frac{p_{Ti}}{p_{TJ}} \sim \frac{m_J^2}{p_{TJ}^2} \longrightarrow$ groomed away

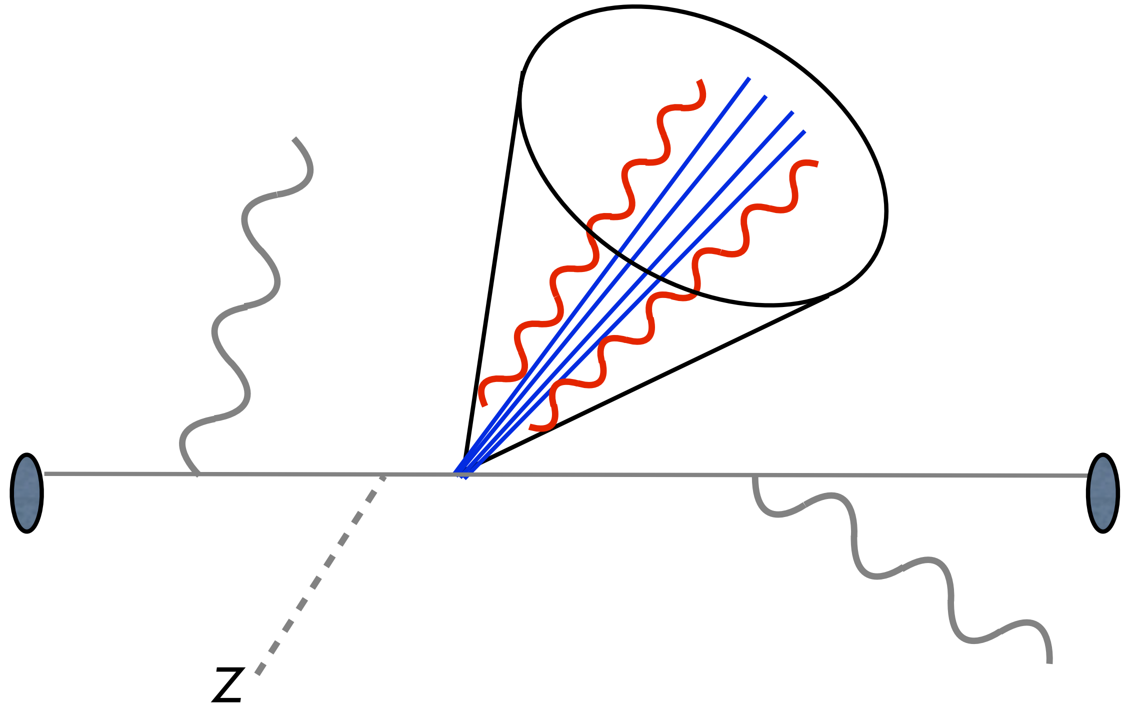
Factorization for NNLL Resummation

Effective theory for soft drop groomed jets

Frye, AJL, Schwartz, Yan 2016

Coefficient D_k can be extracted from fixed-order

Only assumes collinear factorization of high p_T jets in pp collisions



$$m_J^2 \ll z_{\text{cut}} p_{TJ}^2 \ll p_{TJ}^2$$

$$\frac{d\sigma^{\text{resum}}}{dm_J^2} = \sum_{k=q,\bar{q},g} D_k(p_T, z_{\text{cut}}, R) S_{C,k}(z_{\text{cut}} m_J^2) \otimes J_k(m_J^2)$$

sum over jet flavor

includes pdfs, emissions that were groomed away, out-of-jet radiation,...

collinear-soft radiation

hard collinear radiation

Matching NNLL to α_s^2

$$\frac{d\sigma^{\mathrm{NNLL}+\alpha_s^2}}{dm_J^2} \equiv \frac{d\sigma^{\mathrm{NNLL}}}{dm_J^2} + \frac{d\sigma^{\alpha_s^2}}{dm_J^2} - \frac{d\sigma^{\mathrm{NNLL},\alpha_s^2}}{dm_J^2}$$

Use MCFM to generate relative α_s^2 cross section

Campbell, Ellis 2002

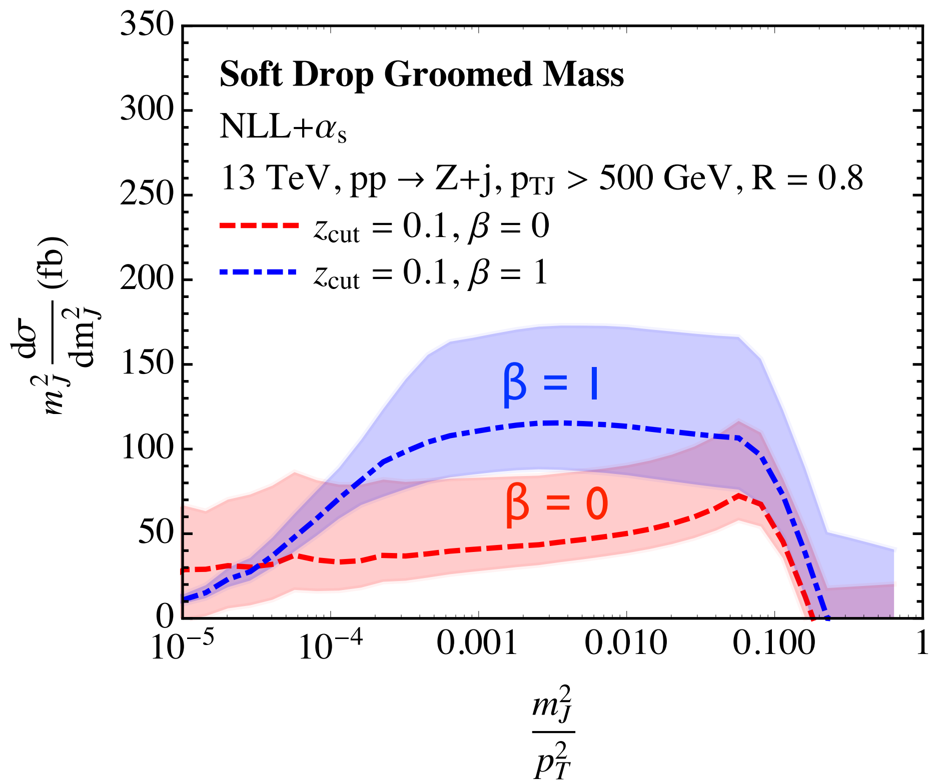
Campbell, Ellis, Rainwater 2003

pp → Z + j at NNLO with $m_J^2 > 0$ = pp → Z + 2j at NLO

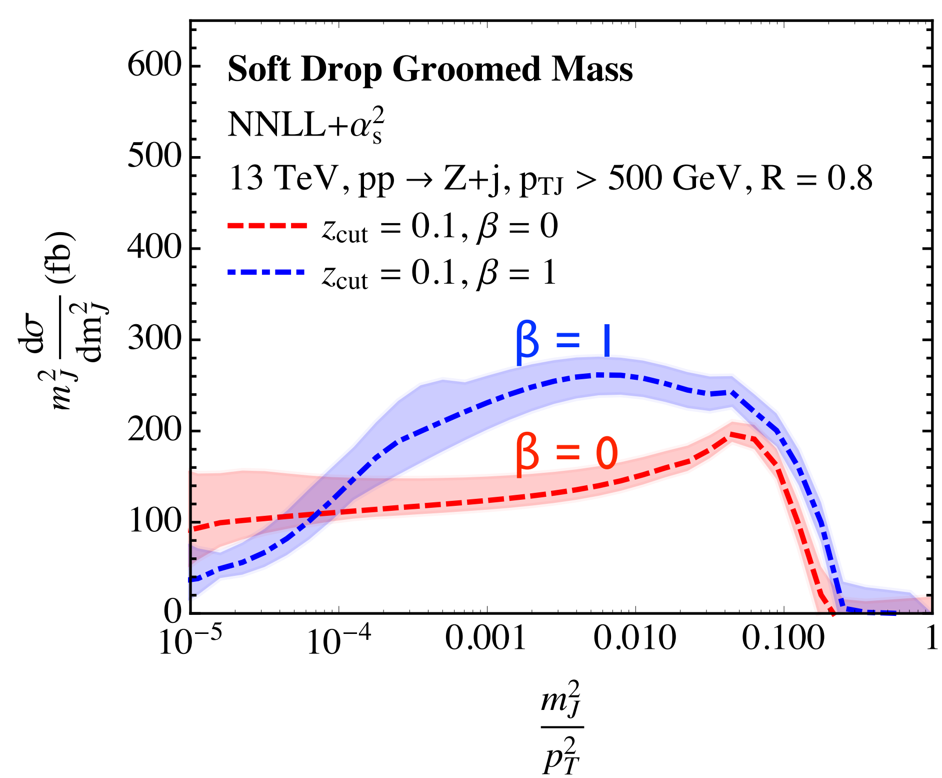
Required extreme computing power:
To make the following plots required centuries of CPU time

The very first jet substructure calculation at high precision!

Results: NNLL+α_s^2 Jet Substructure



NLL+α_s



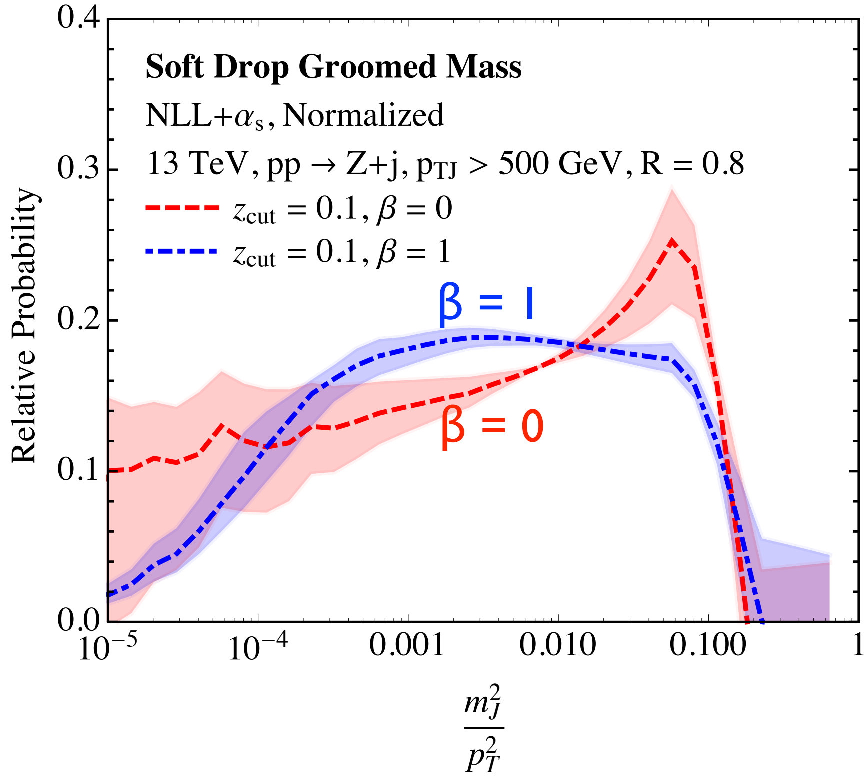
NNLL+α_s^2

Soft Drop: $$\frac{\min[p_{Ti}, p_{Tj}]}{p_{Ti} + p_{Tj}} > z_{\text{cut}} \left(\frac{R_{ij}}{R}\right)^{\beta}$$

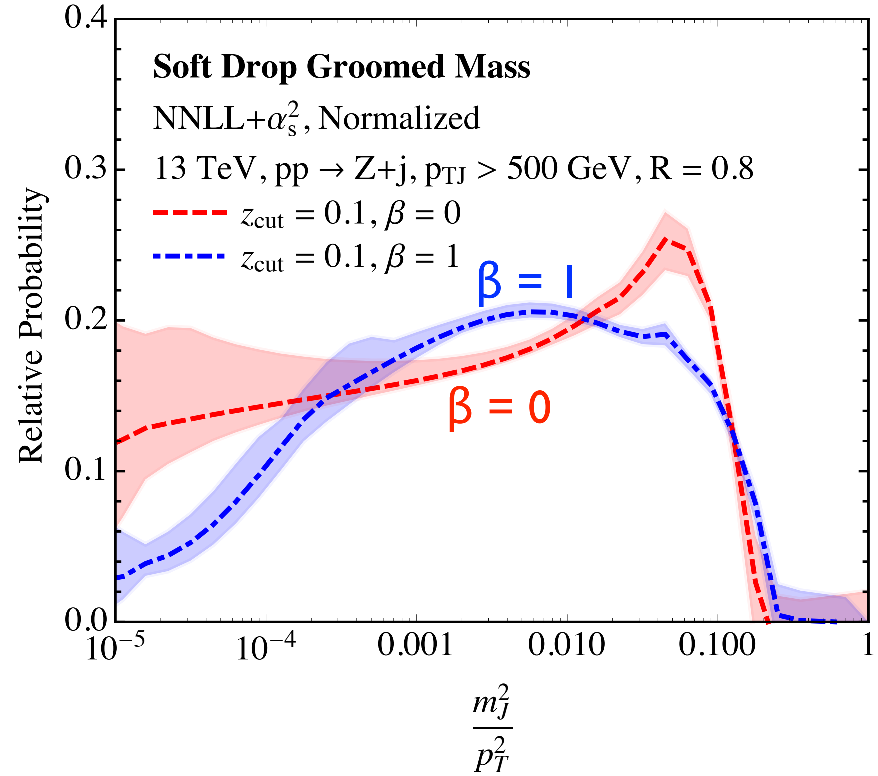
Significant decrease in residual scale uncertainty at NNLL+α_s^2!

Frye, AJL, Schwartz, Yan 2016

Results: NNLL+α_s^2 Jet Substructure



NLL+α_s



NNLL+α_s^2

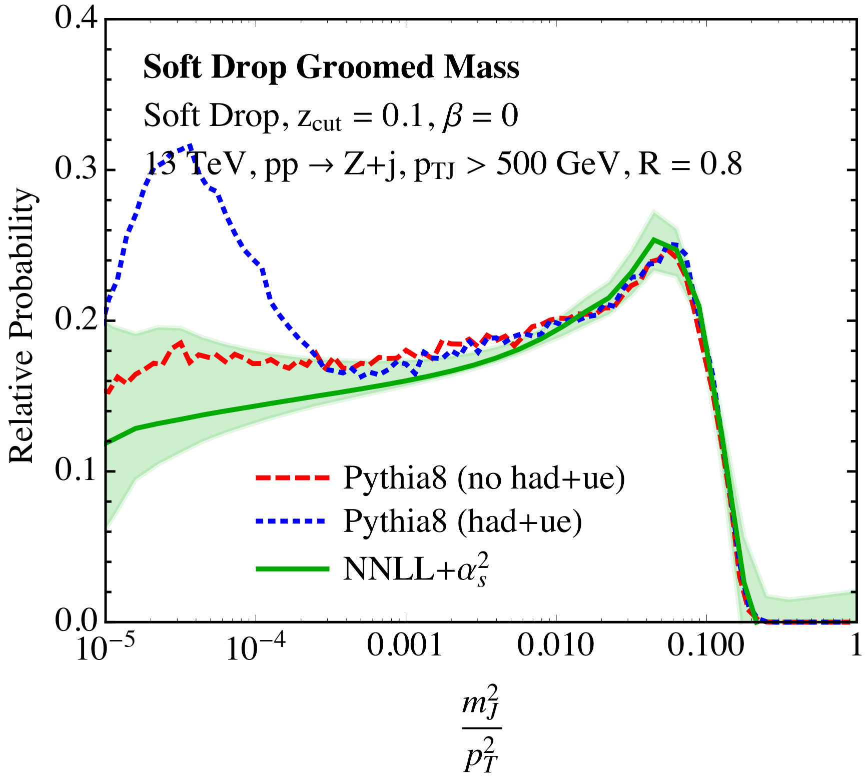
Shape of distribution only depends on collinear physics

$$\frac{d\sigma^{\text{resum}}}{dm_J^2} = \sum_{k=q,\bar{q},g} D_k(p_T, z_{\text{cut}}, R) S_{C,k}(z_{\text{cut}} m_J^2) \otimes J_k(m_J^2)$$

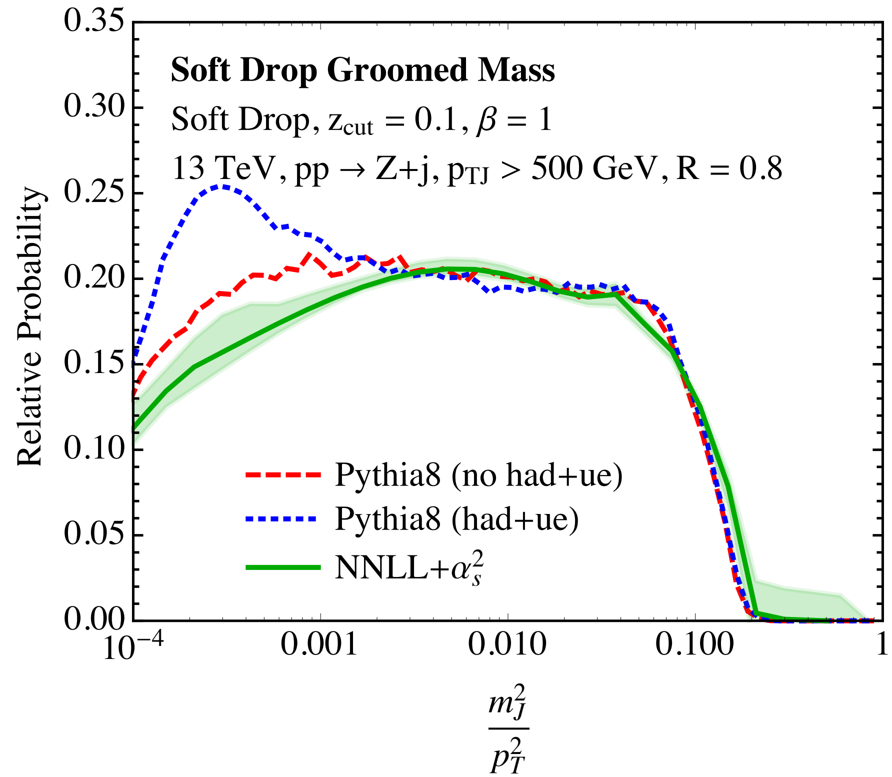
<10%-level residual scale uncertainties in normalized distributions!

Frye, AJL, Schwartz, Yan 2016

Results: NNLL+α_s^2 Jet Substructure



NNLL+α_s^2, β = 0



NNLL+α_s^2, β = 1

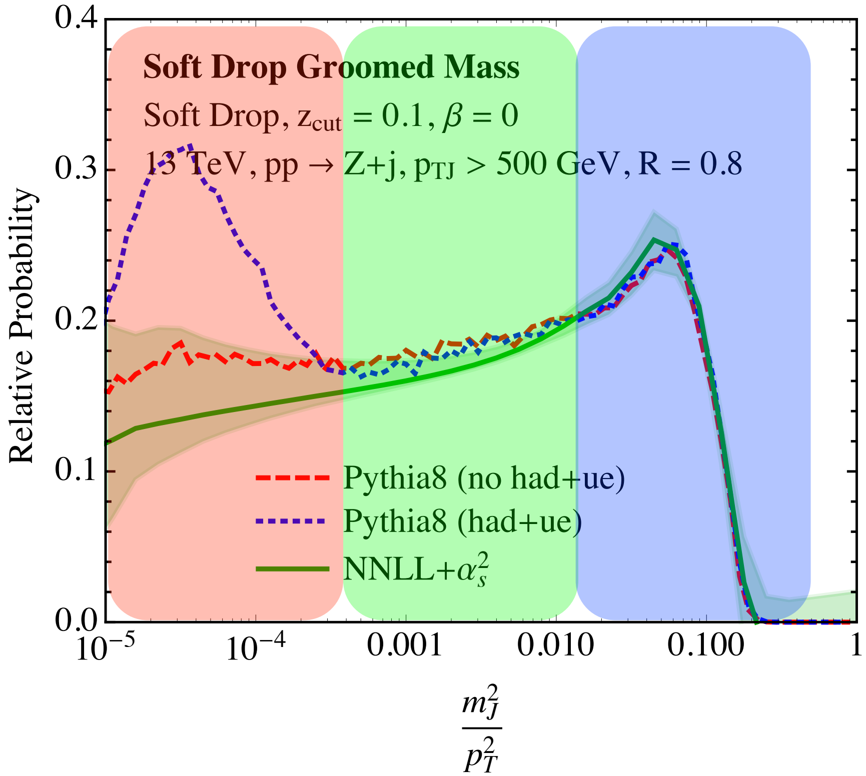
Comparison with Pythia8 Monte Carlo

Hadronization and underlying event only dominate for $m_J^2/p_T^2 \lesssim 10^{-3}$

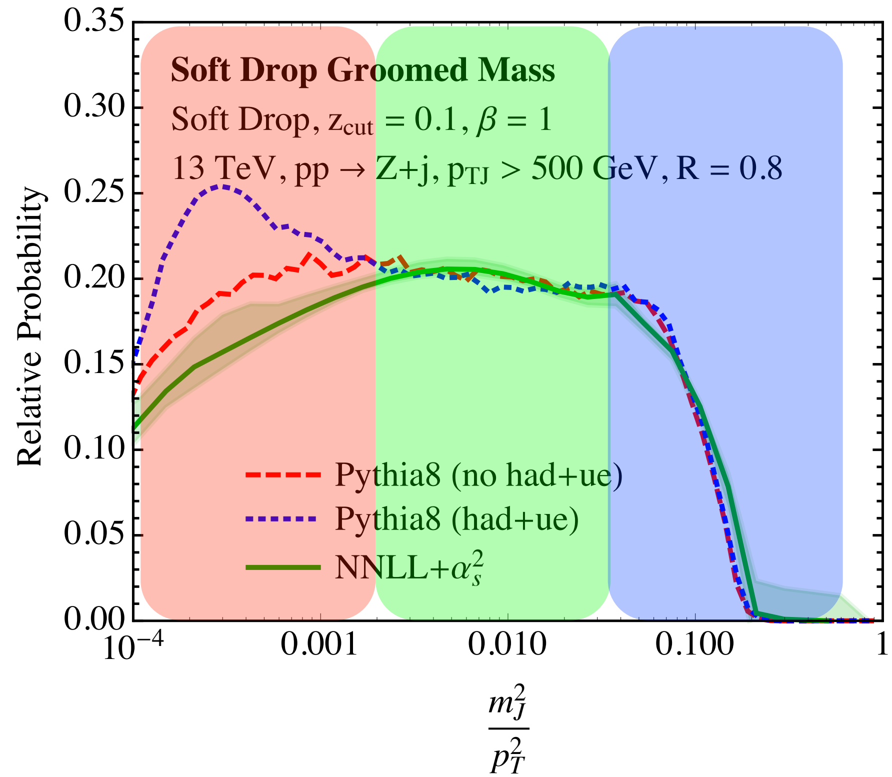
Almost three decades of perturbative control in a single jet distribution!

Frye, AJL, Schwartz, Yan 2016

Results: NNLL+α_s^2 Jet Substructure



NNLL+α_s^2, β = 0



NNLL+α_s^2, β = 1

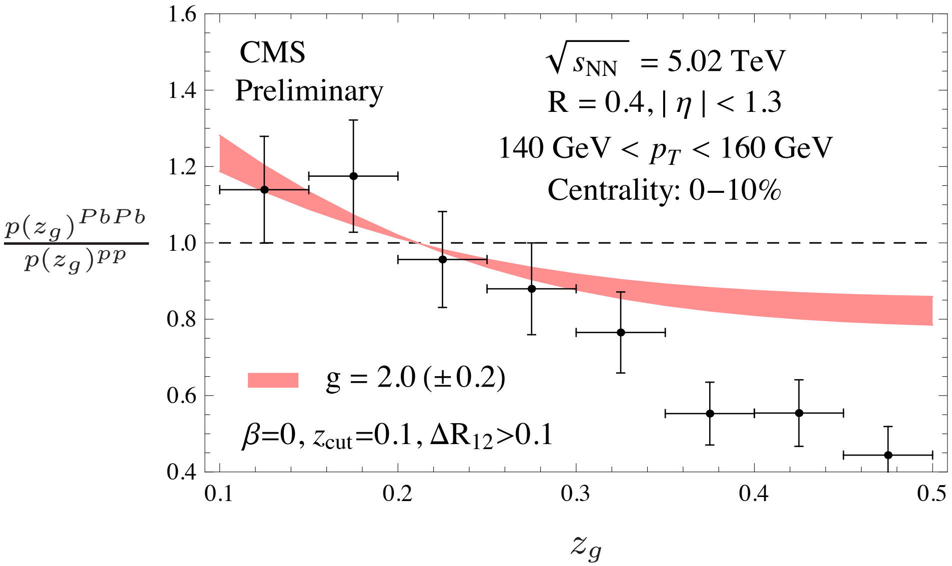
Hadronization Regime

Resummation Regime
Fixed-Order Regime } Perturbative Regime

Almost three decades of perturbative control in a single jet distribution!

Frye, AJL, Schwartz, Yan 2016

Other Applications of Soft Drop



Chien, Vitev 2016

Insights into jet quenching in heavy ion collisions

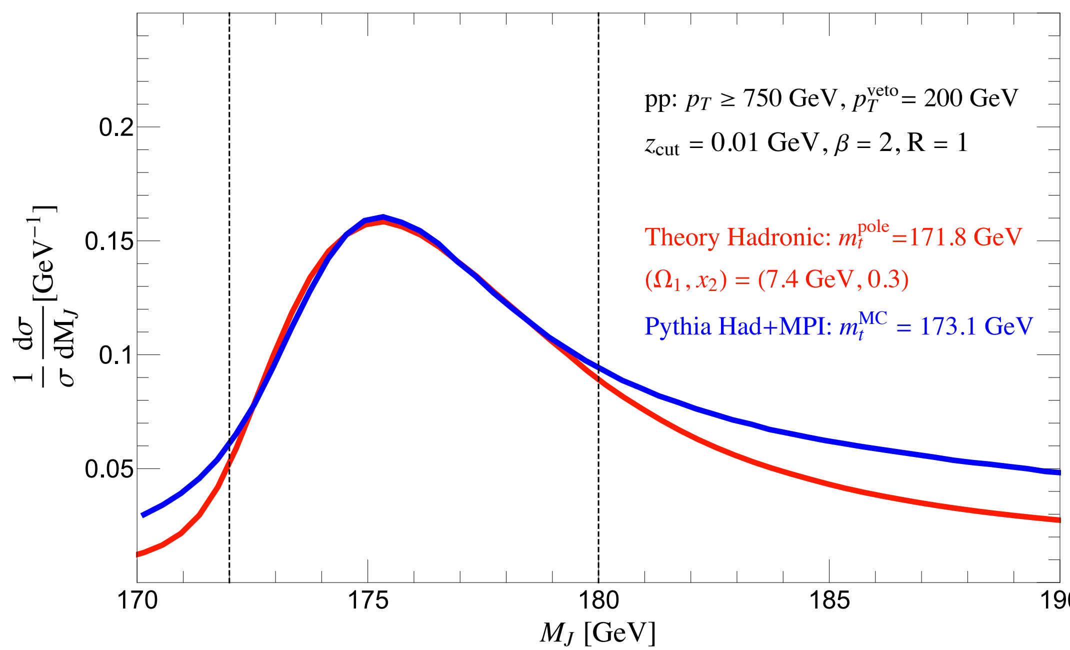
Direct measurement of the QCD splitting function!

Larkoski, Marzani, Thaler 2015

CMS-PAS-HIN-16-006

Enables precision top quark mass measurements at LHC!

Effectively eliminates UE/MPI contamination



Hoang, Mantry, Pathak, Stewart 17xx.sooon

Summary

Precision calculations for jet substructure requires jet grooming

Only mMDT/soft drop remove contamination and eliminate NGLs

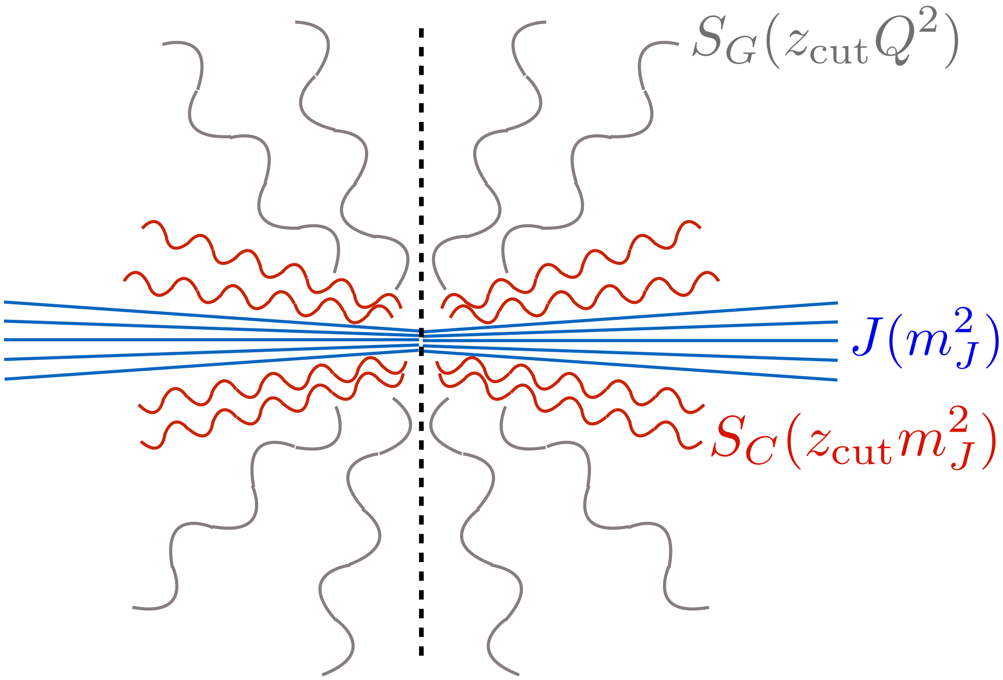
All radiation that remains in the jet is collinear

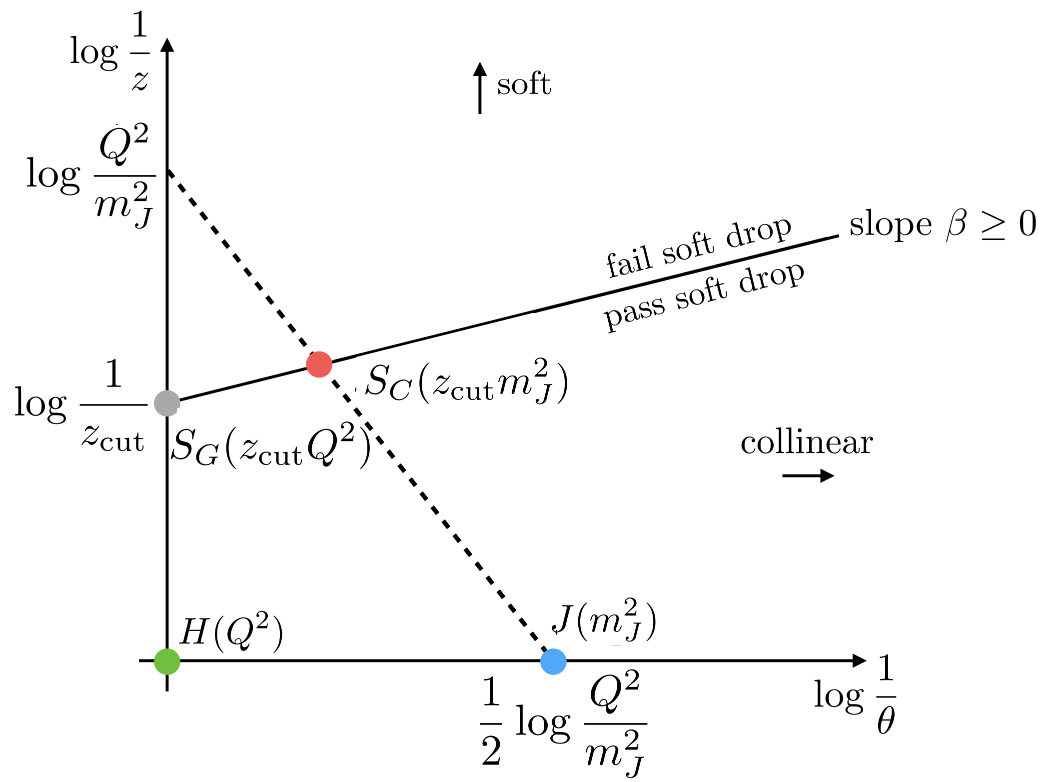
NNLL resummation of groomed jet mass is accomplished

Bonus Slides

Aside: Getting Collinear-Soft Function to NNLL

Factorization theorem in e^+e^- collisions:





$$m_J^2 \ll z_{\rm cut}Q^2 \ll Q^2$$

$$\frac{d^2\sigma}{dm_{J,L}^2\,dm_{J,R}^2} = H(Q^2)S_G(z_{\rm cut}Q^2)\left[S_C(z_{\rm cut}m_{J,L}^2)J(m_{J,L}^2)\right]\left[S_C(z_{\rm cut}m_{J,R}^2)J(m_{J,R}^2)\right]$$

Aside: Getting Collinear-Soft Function to NNLL

Factorization theorem in e^+e^- collisions:

$$\frac{d^2\sigma}{dm_{J,L}^2\, dm_{J,R}^2} = H(Q^2) S_G(z_{\rm cut} Q^2) \left[S_C(z_{\rm cut} m_{J,L}^2) J(m_{J,L}^2)\right] \left[S_C(z_{\rm cut} m_{J,R}^2) J(m_{J,R}^2)\right]$$

$H(Q^2)$: Hard function for $e^+e^- \to qq$. Known beyond two-loops.

van Neerven 1986
Matsuura, van der Marck, van Neerven 1989

$J(m_J^2)$: Jet function. Known at two-loops for quarks and gluons.

Bauer, Manohar 2003
Becher, Neubert 2006

$S_G(z_{\rm cut} Q^2)$: Global soft function. Related to two-loop soft function with energy veto (up to calculable clustering effects).

von Manteuffel, Schabinger, Zhu 2013
Chien, Hornig, Lee 2015

$S_C(z_{\rm cut} m_J^2)$: Collinear-soft function. New, no two-loop calculation exists.

Can get everything from literature and by exploiting RG invariance!

$$0 = \gamma_H + \gamma_{S_G} + 2\gamma_J + 2\gamma_{S_C}$$