

# Off-shell and Interference Theory Update

Stefan Höche (SLAC), Nikolas Kauer (RHUL), Jérémie Quevillon (KCL)

Thanks to Stefan Liebler and Zhen Liu for contributing slides.

13th General Meeting of the LHC Higgs Cross Section Working Group

CERN

July 14, 2017

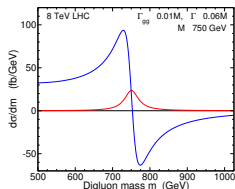
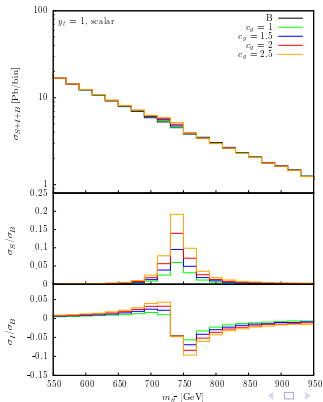
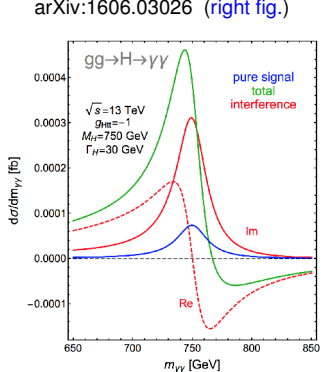
# Overview

- $H \rightarrow ZZ, WW$  in ggF & VBF @ LHC:  $\mathcal{O}(10\%)$  off-shell high-mass Higgs signal contribution with large Higgs(-Higgs)-continuum interference: now taken into account (rather than cut away), provides complementary physics information (similar at high-energy linear collider)
- $gg \rightarrow H \rightarrow ZZ, WW \rightarrow 4$  leptons: signal-background interference studied in detail, mature MC tools available at LO; complete NLO calculations available (2-loop multi-scale!, still some approx.), PS matching demonstrated
- First analysis of interference (& Higgs width bounds) for  $pp \rightarrow H \rightarrow ZZ + \text{jet}$
- Studies of heavy Higgs-light Higgs-background interference effects in  $gg \rightarrow H \rightarrow VV$ , complementary studies for VBF and linear collider
- Direct Higgs width measurement at LHC limited by mass resolution:  $\Gamma_H < 600 \Gamma_H^{SM}$
- high-mass Higgs tail not Higgs width dependent  $\rightarrow$  provides complementary constraints on Higgs couplings and Higgs width  $\Gamma_H$  (when combined with on-peak data)
- Assuming no  $E$ -dependence of relevant Higgs couplings, a bound on  $\Gamma_H$  can be obtained; optimise bound with fully differential discriminant (Matrix Element Method)
- LHC Run 1: CMS:  $\Gamma_H < 5.4 \Gamma_H^{SM}$ , ATLAS:  $\Gamma_H < [4.5, 7.5] \Gamma_H^{SM}$  (95% CL)
- $H \rightarrow \gamma\gamma$ : interference-facilitated bound  $\Gamma_H < 15 \Gamma_H^{SM}$  (14 TeV,  $3 \text{ ab}^{-1}$ , 95% CL)
- LHC Run 2: improved bounds (ggF & VBF), high-mass  $H \rightarrow VV$  EFT and BSM benchmark studies

# Heavy scalar ( $\Phi$ ) interference studies (2016)

## Heavy Higgs – background – light Higgs: non-trivial interference patterns

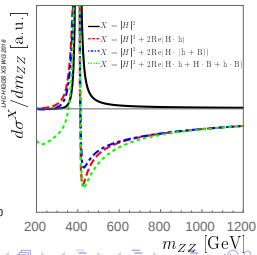
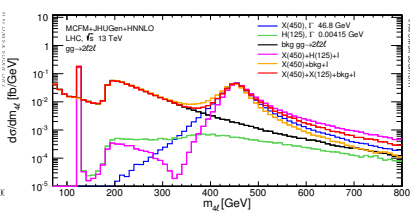
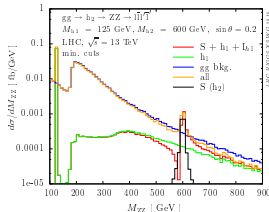
- Signal-background interference in  $gg (\rightarrow \Phi) \rightarrow \gamma\gamma$  (“750 GeV state”) and  $gg (\rightarrow \Phi) \rightarrow t\bar{t}$  [A. Djouadi, J. Ellis, J. Quevillon arXiv:1605.00542](#) (left fig.)
- Signal-background interference in  $gg (\rightarrow \Phi) \rightarrow t\bar{t}$  with higher order QCD effects (simplified model and 2HDM) [B. Hespel, F. Maltoni, E. Vryonidou arXiv:1606.04149](#) (center fig.)
- Higgs-Singlet Model interference effects with EFT operators ( $\Phi$ -SM gauge bosons) [S. Dawson, I.M. Lewis arXiv:1605.04944](#)
- Signal-background interference for a singlet spin-zero digluon resonance [S.P. Martin arXiv:1606.03026](#) (right fig.)



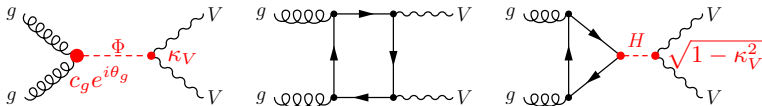
# Heavy scalar interference studies (2015/16)

## Heavy Higgs – background – light Higgs: non-trivial interference patterns

- Higgs Singlet Extension (ggF) NK, C. O'Brien arXiv:1502.04113 and YR4 (left fig.)
- Higgs Portal Scenario (ggF) C. Englert, I. Low, M. Spannowski arXiv:1502.04678
- Higgs Singlet Extension (VBF) A. Ballestrero, E. Maina arXiv:1506.02257 and YR4
- Higgs Singlet Extension (VBF) F. Campanario, M. Rauch YR4
- Generic couplings (tensor structure of  $HVV$ ) Grisan, Sarica, Schulze, Xiao YR4 (center fig.)
- 2HDM:  $gg(\rightarrow \{H, h\}) \rightarrow ZZ, WW$  interference effects N. Greiner, S. Liebler, G. Weiglein arXiv:1512.07232 (right fig.)
- 2HDM:  $pp(\rightarrow \Phi) \rightarrow t\bar{t}$  @ NLO QCD W. Bernreuther, P. Galler, C. Mellein, Z.G. Si, P. Uwer arXiv:1511.05584
- Multiple heavy Higgs and BSM virtual contributions in  $gg(\rightarrow \Phi) \rightarrow t\bar{t}$  M. Carena, Z. Liu arXiv:1608.07282



Idea: Classify relevance of interferences in the  $VV$  and  $HH$  final states:  
Interferences among

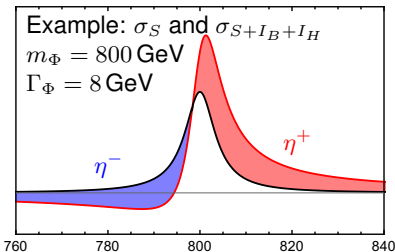


Simplified approach with 5 parameters:  $c_g e^{i\theta_g}$ ,  $m_\Phi$ ,  $\Gamma_\Phi$ ,  $\kappa_V$

Similar for  $HH$  with  $\lambda_{\Phi hh}$  and  $\lambda_{hhh}$  instead of  $\kappa_V$

Quantify interference in terms of:

$$\eta = \sigma_{I_B+I_H} / \sigma_S \quad \text{with} \quad \sigma_X = \int_{m_\Phi - 5\Gamma_\Phi}^{m_\Phi + 5\Gamma_\Phi} dm_{VV} \frac{d\sigma^X}{dm_{VV}}$$



E.g. provide relative corrections:

$$\eta^\mp = \begin{pmatrix} \eta^- \\ \eta^+ \\ \eta \end{pmatrix} = \begin{pmatrix} -165\% \\ +160\% \\ +38\% \end{pmatrix}$$

Make tables, figures as a function of free parameters. Provide guidance.

Check quantity  $\Gamma_\Phi / m_\Phi \cdot \sigma_S / \sigma_B$ .

# Higgs interferometry in $gg \rightarrow \gamma\gamma$

- ▶ Using interference effects in  $gg \rightarrow \gamma\gamma$ , LHC may bound Higgs width much better than in direct measurement [Dixon,Li] arXiv:1305.3854
- ▶ Interference has **symmetric** and **asymmetric** part around  $m_H$   
Asymmetric part generates apparent mass shift that becomes appreciable when convoluted with detector resolution [Martin] arXiv:1208.1533, arXiv:1303.3342 [deFlorian et al.] arXiv:1303.1397

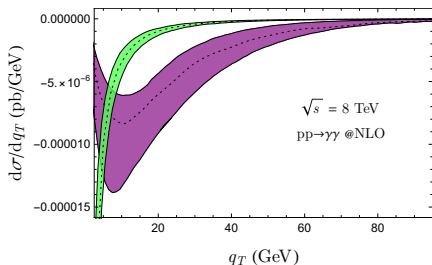
$$\begin{aligned} \delta\hat{\sigma}_{gg \rightarrow H \rightarrow \gamma\gamma} &= -2(\hat{s} - m_H^2) \frac{\text{Re}(\mathcal{A}_{gg \rightarrow H} \mathcal{A}_{H \rightarrow \gamma\gamma} \mathcal{A}_{\text{cont}}^*)}{(\hat{s} - m_H^2)^2 + m_H^2 \Gamma_H^2} \\ &\quad - 2m_H \Gamma_H \frac{\text{Im}(\mathcal{A}_{gg \rightarrow H} \mathcal{A}_{H \rightarrow \gamma\gamma} \mathcal{A}_{\text{cont}}^*)}{(\hat{s} - m_H^2)^2 + m_H^2 \Gamma_H^2} \\ &= \left[ \begin{array}{c} g \\ t, b \\ g \end{array} \right] \text{---} H \text{---} \left[ \begin{array}{c} W, t \\ b, c, \tau \\ \gamma \end{array} \right] + \left[ \begin{array}{c} \gamma \\ \gamma \\ \gamma \end{array} \right] \text{---} H \text{---} \left[ \begin{array}{c} \gamma \\ \gamma \\ \gamma \end{array} \right] + \dots \\ &\quad \times \left[ \begin{array}{c} \gamma \\ b, c, \dots \\ \gamma \end{array} \right] + \left[ \begin{array}{c} \gamma \\ u, c, d, s, b \\ \gamma \end{array} \right] + \dots \end{aligned}$$

- ▶  $gg \rightarrow \gamma\gamma$  more direct than  $gg \rightarrow ZZ/WW$ , as it operates in neighborhood of resonance, also  $gg \rightarrow ZZ/WW$  method could be invalidated by e.g. form factors [Englert,Spannowsky] arXiv:1405.0285

# NLL $q_T$ -resummation for $gg \rightarrow \gamma\gamma$ interference

[Cieri,Coradeschi,de Florian,Fidanza] arXiv:1706.07331

- ▶ NLO+NLL  $q_T$  resummation formalism, based on  
[Bozzi,Catani,de Florian,Grazzini] hep-ph/0508068  
[Catani,Cieri,de Florian,Ferrera,Grazzini] arXiv:1311.1654
- ▶ Uncertainty bands from varying  $\mu_{R/F}$  and resummation scale as  
 $\mu_R = 2m_H, \mu_F = m_H/2, \mu_{\text{res}} \in [m_H/2, 2m_H]$   
 $\mu_R = m_H/2, \mu_F = 2m_H, \mu_{\text{res}} \in [m_H/2, 2m_H]$
- ▶ Setup:  $\sqrt{s} = 8\text{TeV}$ , MSTW 2008 [MSTW] arXiv:0901.0002  
Cuts:  $q_{T,\gamma 1} \geq 40\text{GeV}$ ,  $q_{T,\gamma 2} \geq 30\text{GeV}$   
Smooth cone [Frixione] hep-ph/9801442  $n = 1$ ,  $E_{\text{max}} = 3\text{GeV}$ ,  $R = 0.4$
- ▶ Resummation distributes events from  $q_T = 0$  to finite  $q_T \rightarrow$  negative interference contribution shifted towards larger  $q_T$
- ▶ Uncertainty more realistic due to same effect

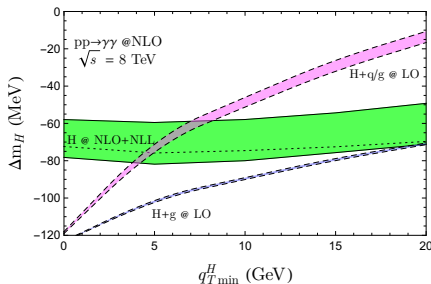
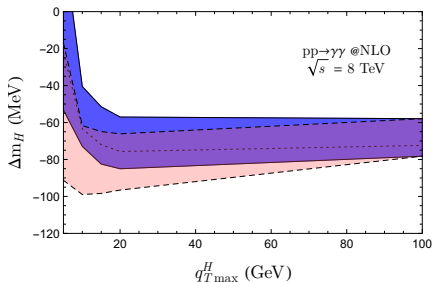


# NLL $q_T$ -resummation for $gg \rightarrow \gamma\gamma$ interference

[Cieri,Coradeschi,de Florian,Fidanza] arXiv:1706.07331

- ▶ Resummed prediction of  $q_T$ -vetoed cross section stabilises at smaller  $q_T$  than fixed-order result
- ▶ Points towards viability of measurement of mass shift in  $gg \rightarrow \gamma\gamma$  alone

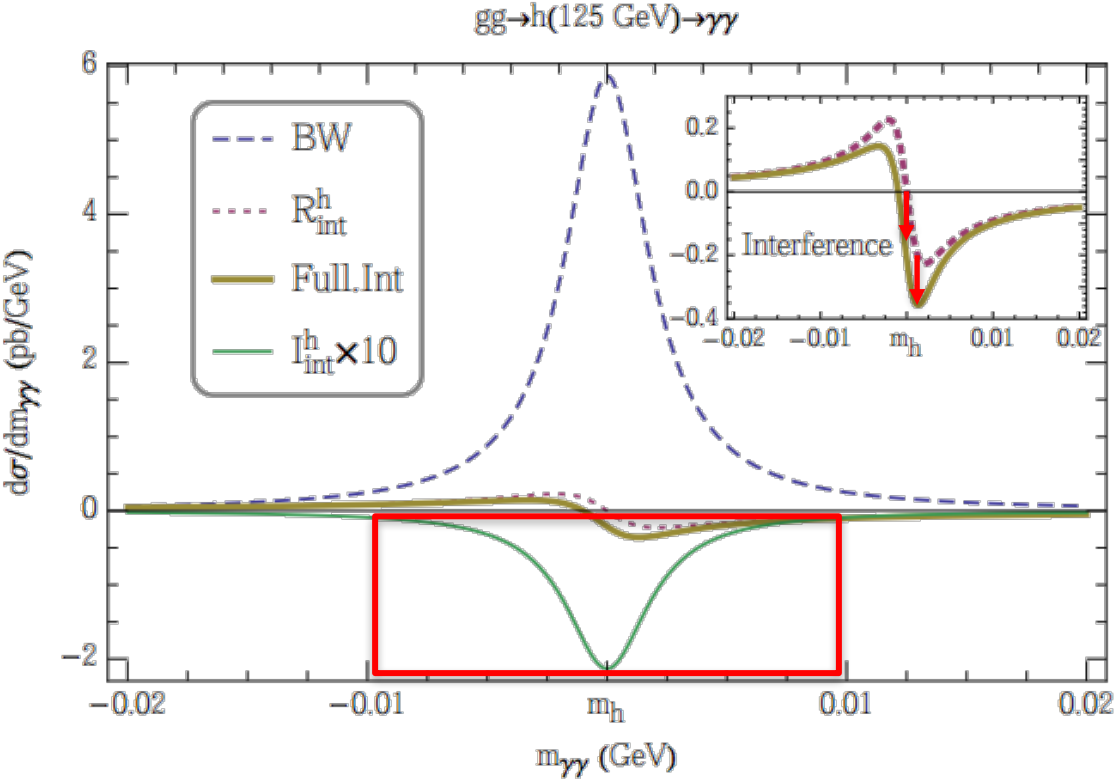
[Dixon,Li] arXiv:1305.3854



- ▶ Resummed prediction of  $q_T$ -region above veto stable at small  $q_T$
- ▶ Again brought about by redistribution of events from  $q_T = 0$  to finite  $q_T$



Diphoton SM Higgs decay: Strong phase J. Campbell, M. Carena, R. Harnik, Z. Liu (arXiv:1704.08259)

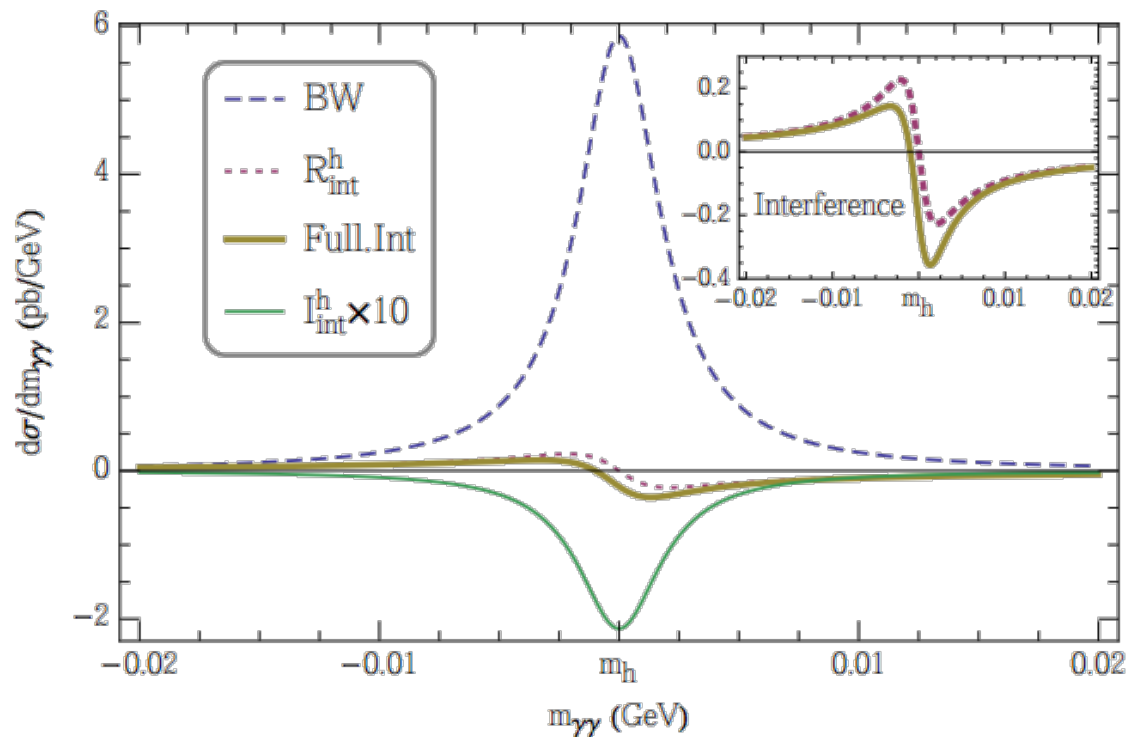


Averaging over helicity amplitudes and polar angles, one can calculate this new interference piece between signal and background:

$$\begin{aligned}
 & \text{Im}[c_{sig}c_{bkg}^*] \\
 & = |c_{sig}||c_{bkg}^*| \sin(\delta_{sig} - \delta_{bkg})
 \end{aligned}$$

The interference term from the strong phase does change the SM rate prediction by  $\sim -2. \%$

gg→h(125 GeV)→γγ



Averaging over helicity amplitudes and polar angles, one can calculate this new interference piece between signal and background:

$$\begin{aligned} & \text{Im}[c_{sig}c_{bkg}^*] \\ &= |c_{sig}| |c_{bkg}^*| \sin(\delta_{sig} - \delta_{bkg}) \end{aligned}$$

The interference term from the strong phase does change the SM rate prediction by  $\sim -2.0\%$

Production	Resolved scaling factor
$\sigma(ggF)$	$1.06 \cdot \kappa_t^2 + 0.01 \cdot \kappa_b^2 - 0.07 \cdot \kappa_t \kappa_b$
$\sigma(\text{VBF})$	$0.74 \cdot \kappa_W^2 + 0.26 \cdot \kappa_Z^2$
$\sigma(WH)$	$\kappa_W^2$ ATLAS and CMS legacy combination paper, JHEP

- The size of this effect is relevant
- This effect cannot be factorized into production times decay branching fractions, the framework fails to capture this;

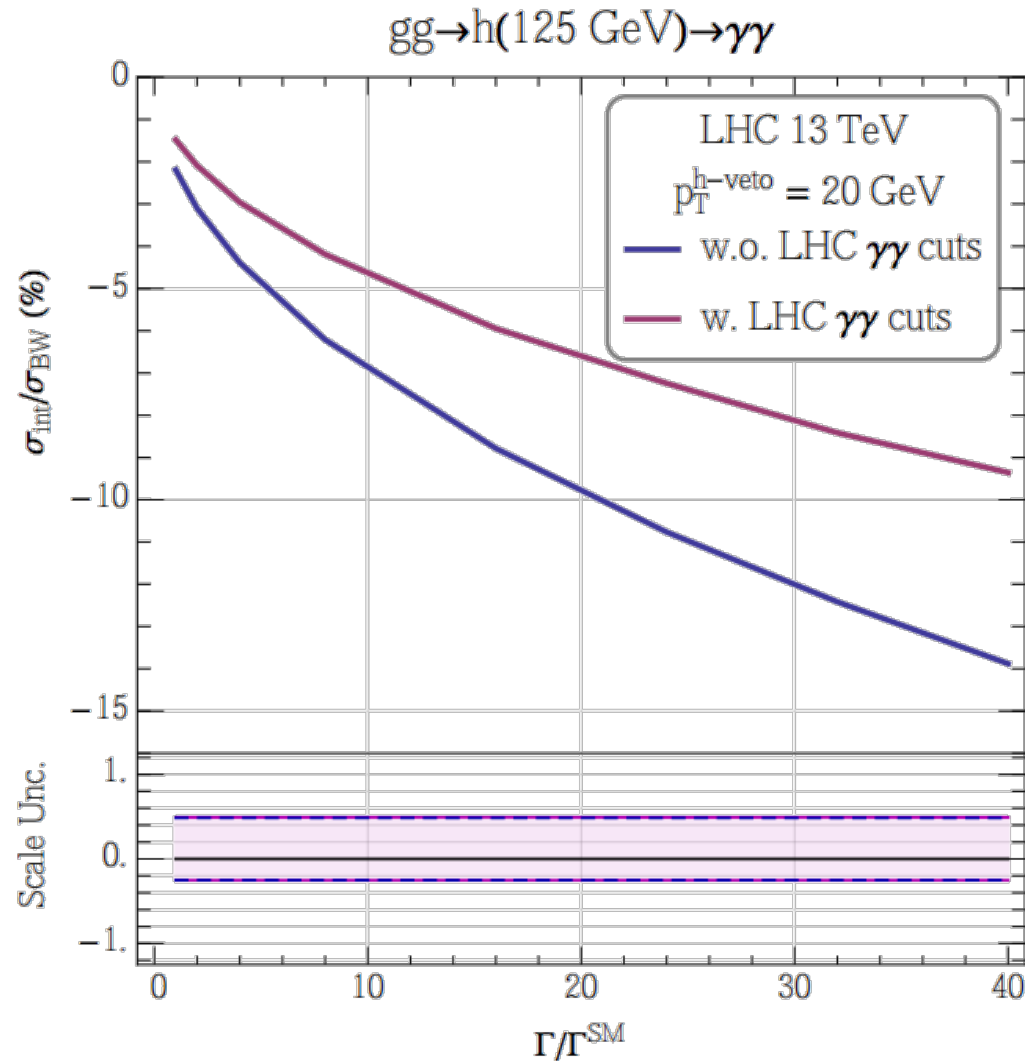
# Strong phase and Higgs $gg \rightarrow h \rightarrow \gamma\gamma$ (BSM)

This rate change as a new probe of Higgs total width

$$\sigma(gg \rightarrow h \rightarrow \gamma\gamma)$$

$$\propto \frac{g_{ggh}^2 g_{\gamma\gamma h}^2}{\Gamma_{tot}} - (\sim 2. \%) g_{ggh} g_{\gamma\gamma h}$$

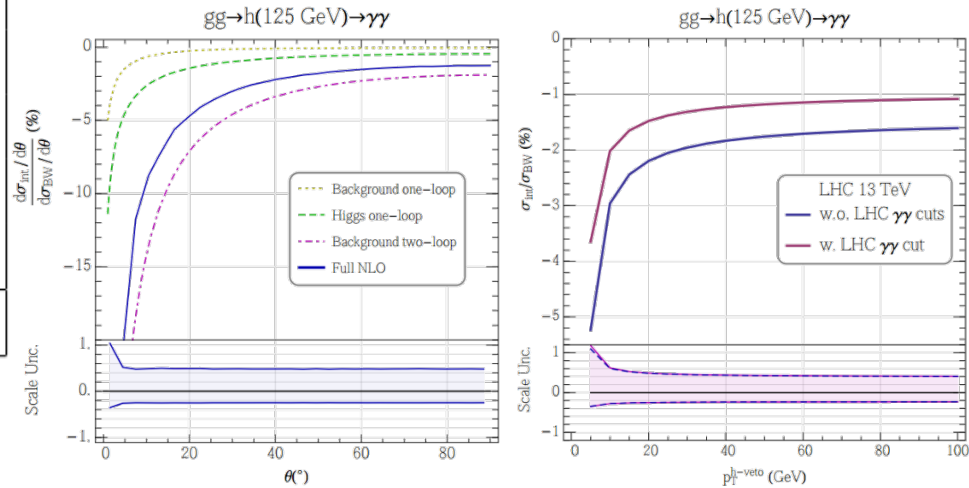
- Unique piece that does not depend on total width;
- Similar to off-shell ZZ/WW measurement;
- Negligible dependence on coupling at different scales.



# Kinematic features of the interference effect

cos θ	$-\sigma_{\text{int}}/\sigma_{\text{BW}}$ (%)		
	no cuts	$p_T^h$ veto	$\gamma\gamma$ cuts+veto
0.0–0.2	$0.87^{+0.34}_{-0.20}$	$1.28^{+0.62}_{-0.32}$	$1.34^{+0.68}_{-0.34}$
0.2–0.4	$0.91^{+0.36}_{-0.21}$	$1.35^{+0.65}_{-0.34}$	$1.41^{+0.72}_{-0.36}$
0.4–0.6	$1.04^{+0.41}_{-0.24}$	$1.53^{+0.74}_{-0.38}$	$1.62^{+0.83}_{-0.42}$
0.6–0.8	$1.37^{+0.53}_{-0.31}$	$1.99^{+0.96}_{-0.50}$	$1.65^{+0.75}_{-0.40}$
0.8–1.0	$3.55^{+1.45}_{-0.82}$	$4.85^{+2.37}_{-1.23}$	—
0.0–1.0	$1.52^{+0.60}_{-0.35}$	$2.20^{+1.06}_{-0.55}$	$1.48^{+0.73}_{-0.38}$

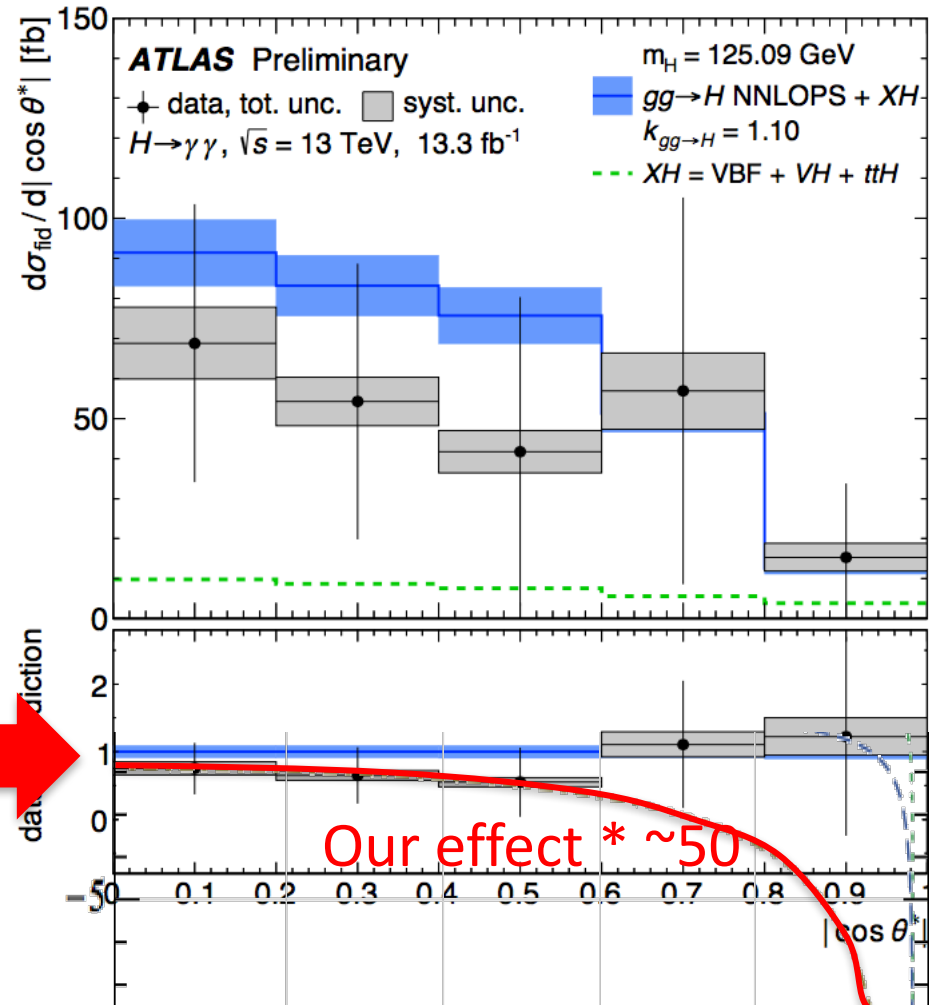
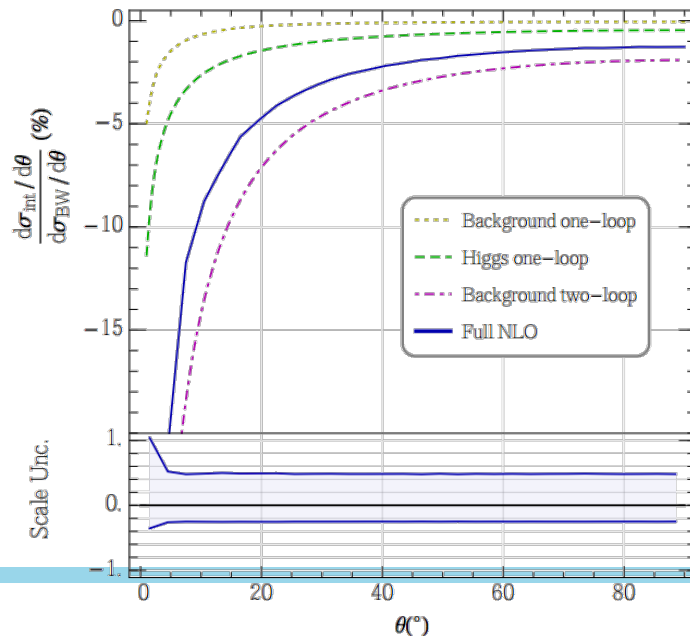
Differential distributions help map out the interference effect, and further the width information!



# Kinematic features of the interference effect

cos θ	$-\sigma_{\text{int}}/\sigma_{\text{BW}}$ (%)		
	no cuts	$p_T^h$ veto	$\gamma\gamma$ cuts+veto
0.0–0.2	$0.87^{+0.34}_{-0.20}$	$1.28^{+0.62}_{-0.32}$	$1.34^{+0.68}_{-0.34}$
0.2–0.4	$0.91^{+0.36}_{-0.21}$	$1.35^{+0.65}_{-0.34}$	$1.41^{+0.72}_{-0.36}$
0.4–0.6	$1.04^{+0.41}_{-0.24}$	$1.53^{+0.74}_{-0.38}$	$1.62^{+0.83}_{-0.42}$
0.6–0.8	$1.37^{+0.53}_{-0.31}$	$1.99^{+0.96}_{-0.50}$	$1.65^{+0.75}_{-0.40}$
0.8–1.0	$3.55^{+1.45}_{-0.82}$	$4.85^{+2.37}_{-1.23}$	—
0.0–1.0	$1.52^{+0.60}_{-0.35}$	$2.20^{+1.06}_{-0.55}$	$1.48^{+0.73}_{-0.38}$

$gg \rightarrow h(125 \text{ GeV}) \rightarrow \gamma\gamma$



We have this info and can extract new physics information from it!

# Summary and outlook $gg \rightarrow h \rightarrow \gamma\gamma$

We uniquely explore the physics consequences of the strong phase in Higgs physics.

We choose the  $gg \rightarrow h \rightarrow \gamma\gamma$  as one example and found the inclusion of this strong phase reduce the signal rate by  $\sim 2\%$  (at NLO, need higher order calculation); an important ingredient should be included in **all** LHC Higgs precision programs (global fit, etc.).

This effect could be used as probes to BSM physics, providing information on

- Higgs light quark Yukawas
- **Higgs total width**
- CPV effect

There are interesting kinematical distributions for the process can be utilized to map out the interference effect.

# Matrix element–parton shower matching/merging

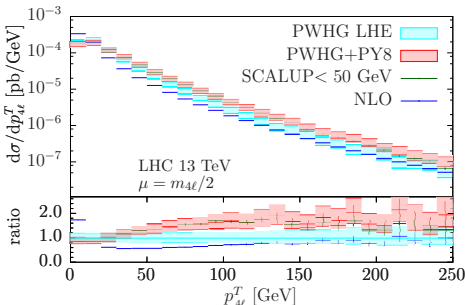
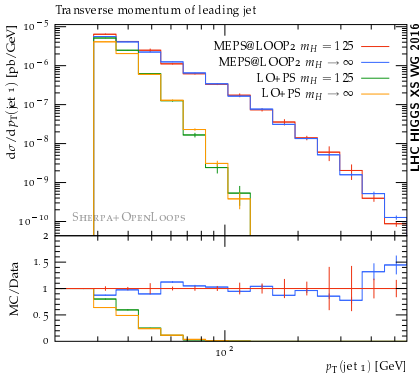
[LO(+partons)]+PS versus LO+PS

SHERPA+OPENLOOPS:  $gg (\rightarrow H) \rightarrow Y$  vs. in addition  $gg \rightarrow Yg$  and  $qg \rightarrow Yq$  ( $Y \equiv \ell\bar{\nu}_\ell\ell'\nu_{\ell'}$ , quark-loop amplitudes) merged with PS; harder  $p_T$  spectrum, overall: 10% effect from multi-jet merging [Höche, Krauss, Pozzorini, Siebert arXiv:1309.0500](#) and YR4 (left fig.)

NLO+PS versus NLO

$gg \rightarrow ZZ \rightarrow 2\ell 2\ell'$  (without Higgs), PS effects for trans. mom. obs. ( $p_{T,4\ell}, p_{T,j_1}$ ), but not for incl. obs. ( $M_{4\ell}, \Delta\phi_{\ell\ell}$ ) [S. Alioli, F. Caola, G. Luisoni, R. Röntsch arXiv:1609.09719](#) (right fig.)

$gg (\rightarrow H) \rightarrow \gamma\gamma$  including interference available in SHERPA: fixed order and matched to PS (MC@NLO) [S. Höche et al., ATLAS studies C. Becot, L. Fayard, et al. ATL-PHYS-PUB-2016-009](#)



# Implementing loop-induced @ NLO in MC tools

## Automated loop-induced @ LO

- ▶ MG5\_AMC (OLP MADLOOP): [Hirschi, Mattelaer](#) arXiv:1507.00020
- ▶ similar capability in SHERPA+OPENLOOPS (e.g. arXiv:1309.0500) and GOSAM (e.g. arXiv:1512.07232, arXiv:1602.05141)
- ▶ ...

## Implementing loop-induced @ NLO in MC tools

- ▶ POWHEG: [Alioli, Caola, Luisoni, Röntsch](#) arXiv:1609.09719
- ▶ MG5\_AMC: in progress  
[Hirschi, Mattelaer, Vryonidou, NK, Shivaji, Mandal, ...](#)  
Method 1: reweighting (arXiv:1607.00763)  
Method 2: direct integration in MADFKS  
Feasibility study for  $gg \rightarrow (\gamma \rightarrow e^+e^-)(\gamma \rightarrow \mu^+\mu^-)$  completed
- ▶ SHERPA: in progress [Kuttimalai, ...](#) (Catani-Seymour)
- ▶ HERWIG7+GOSAM: in progress
- ▶ ...

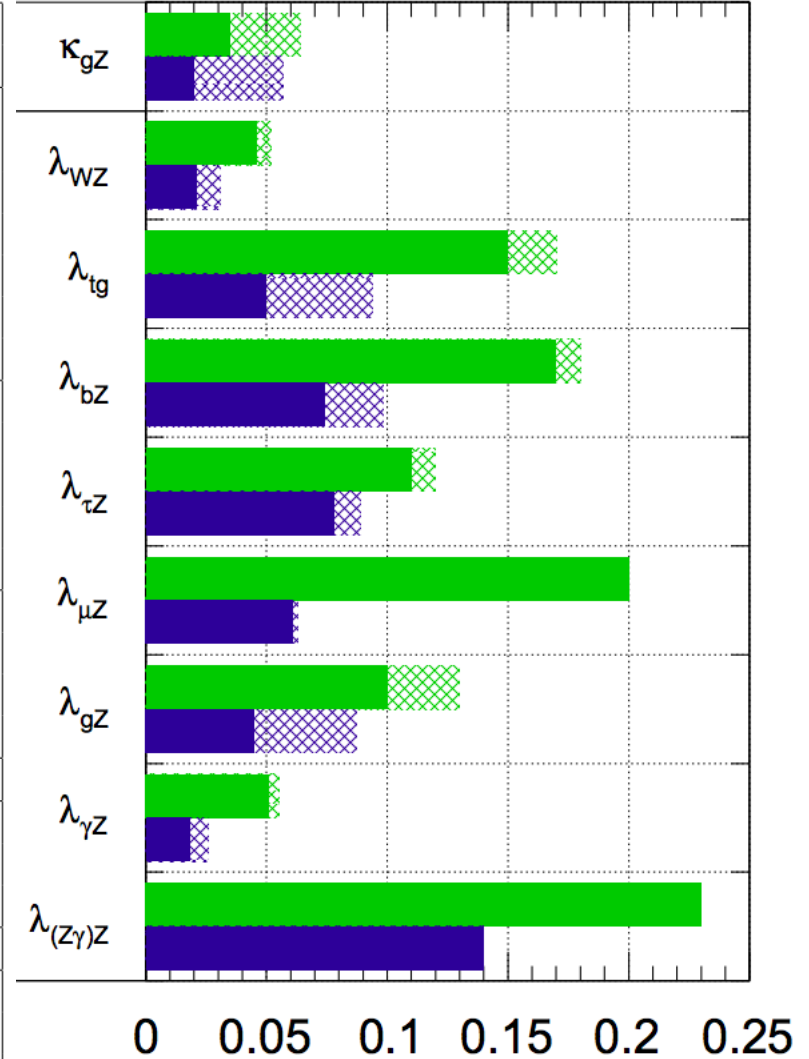


# Future directions and discussion points

- Tools: high-mass NLO  $gg \rightarrow VV$  (exact?) matched/merged with PS  
→ public event generators for experimental studies  
(HERWIG7, MG5\_AMC, POWHEG, SHERPA, ...)
- Comparing NLO+PS with (merged) LO+PS predictions
- $qg$  effects at NLO (overlap with  $pp \rightarrow VV @ N^3LO$ )
- finite top mass corrections
- EW corrections
- Improved precision in  $H \rightarrow \gamma\gamma$  interference studies
- BSM/EFT constraints and interference studies

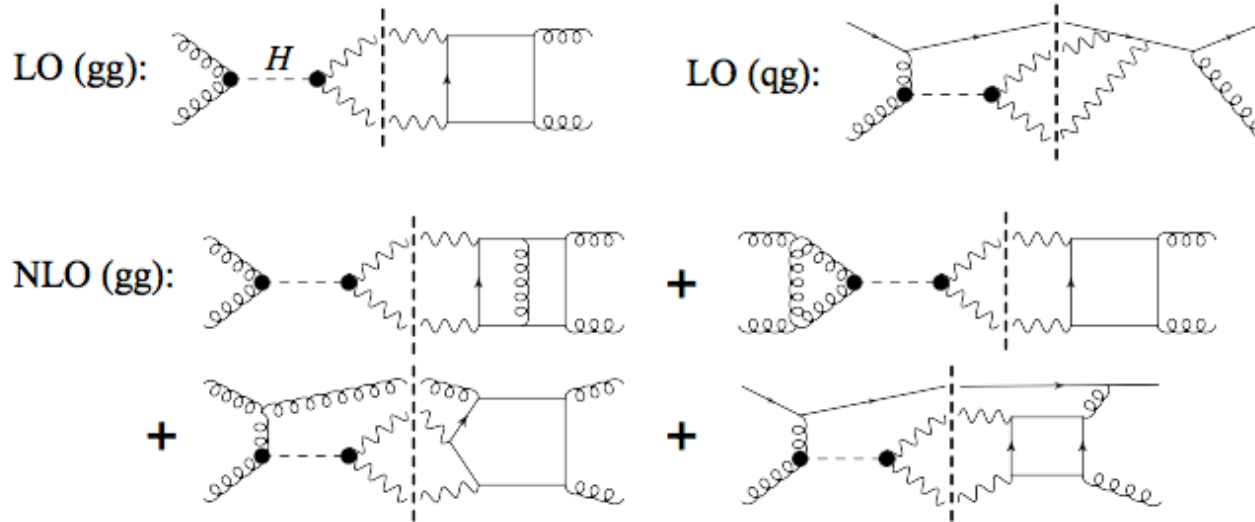
# Backup Slides

$\Delta\mu/\mu$	$300 \text{ fb}^{-1}$		$3000 \text{ fb}^{-1}$	
	All unc.	No theory unc.	All unc.	No theory unc.
$H \rightarrow \gamma\gamma$ (comb.)	0.13	0.09	0.09	0.04
(0j)	0.19	0.12	0.16	0.05
(1j)	0.27	0.14	0.23	0.05
(VBF-like)	0.47	0.43	0.22	0.15
(WH-like)	0.48	0.48	0.19	0.17
(ZH-like)	0.85	0.85	0.28	0.27
( $ttH$ -like)	0.38	0.36	0.17	0.12
$H \rightarrow ZZ$ (comb.)	0.11	0.07	0.09	0.04
(VH-like)	0.35	0.34	0.13	0.12
( $ttH$ -like)	0.49	0.48	0.20	0.16
(VBF-like)	0.36	0.33	0.21	0.16
(ggF-like)	0.12	0.07	0.11	0.04
$H \rightarrow WW$ (comb.)	0.13	0.08	0.11	0.05
(0j)	0.18	0.09	0.16	0.05
(1j)	0.30	0.18	0.26	0.10
(VBF-like)	0.21	0.20	0.15	0.09
$H \rightarrow Z\gamma$ (incl.)	0.46	0.44	0.30	0.27
$H \rightarrow b\bar{b}$ (comb.)	0.26	0.26	0.14	0.12
(WH-like)	0.57	0.56	0.37	0.36
(ZH-like)	0.29	0.29	0.14	0.13
$H \rightarrow \tau\tau$ (VBF-like)	0.21	0.18	0.19	0.15
$H \rightarrow \mu\mu$ (comb.)	0.39	0.38	0.16	0.12
(incl.)	0.47	0.45	0.18	0.14
( $ttH$ -like)	0.74	0.72	0.27	0.23

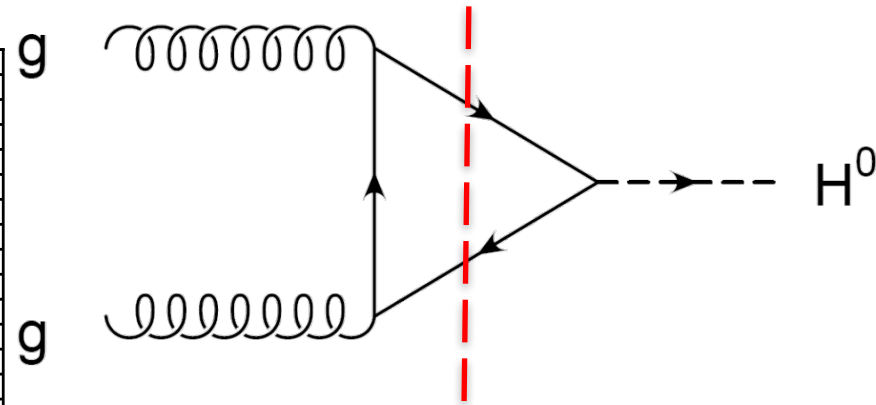
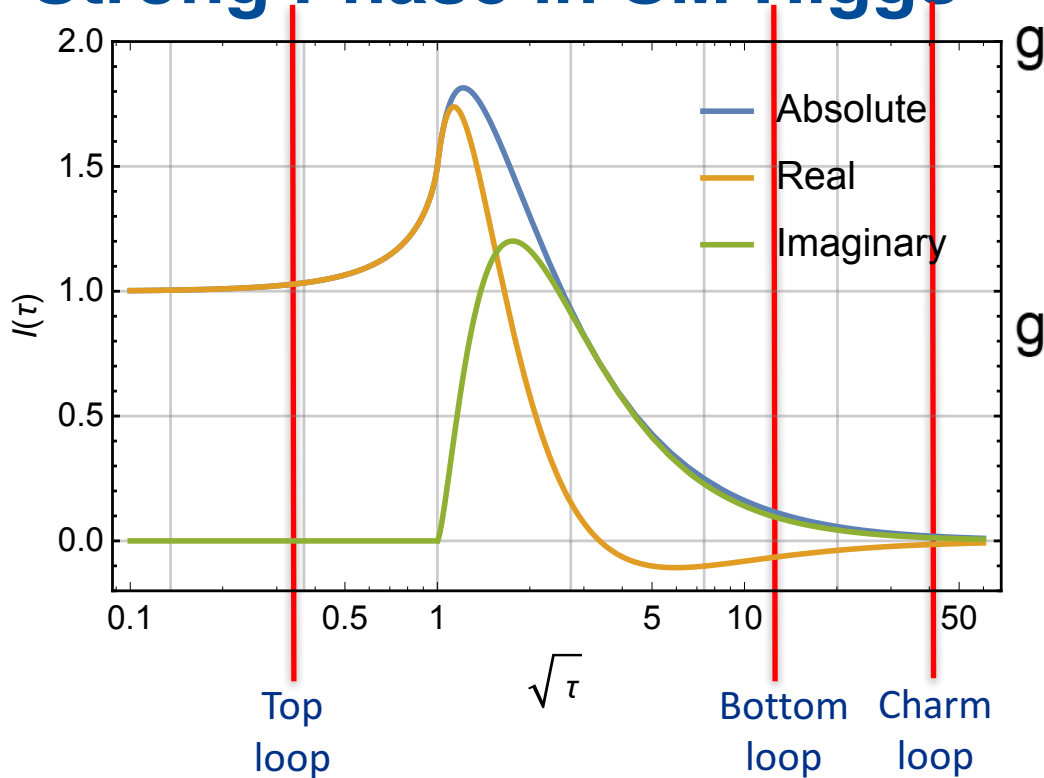


$$\Delta\lambda_{XY} = \Delta\left(\frac{\kappa_X}{\kappa_Y}\right)$$

Dots represent point-like interaction, where the phase is ignored at NLO.



# Strong Phase in SM Higgs



- All quark contributions normalized the same way, the plot represents the relative contributions
- Numerically:
  - t-loop +1.034
  - b-loop  $-0.035 + 0.039i$
  - c-loop  $-0.004 + 0.002i$

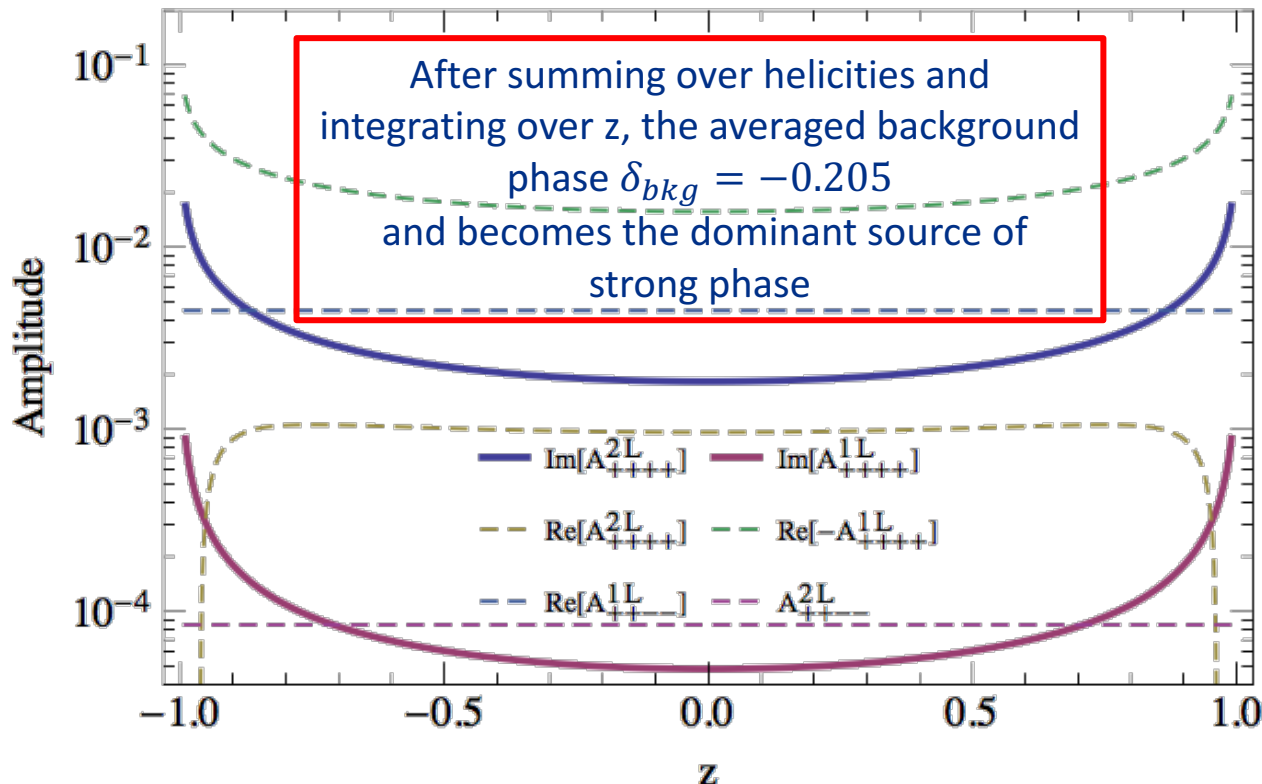
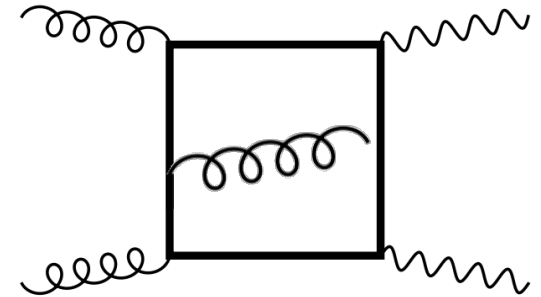
A strong phase in the gluon-gluon fusion production at hadron colliders (imaginary part)

Phase in gluon-gluon-fusion **0.042**

# Phase from interfering background

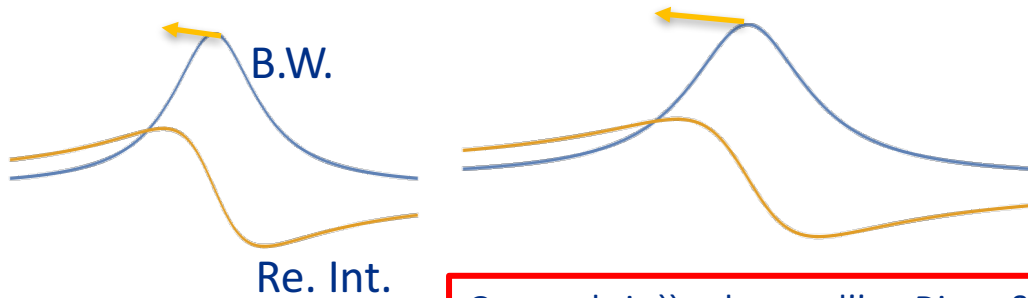
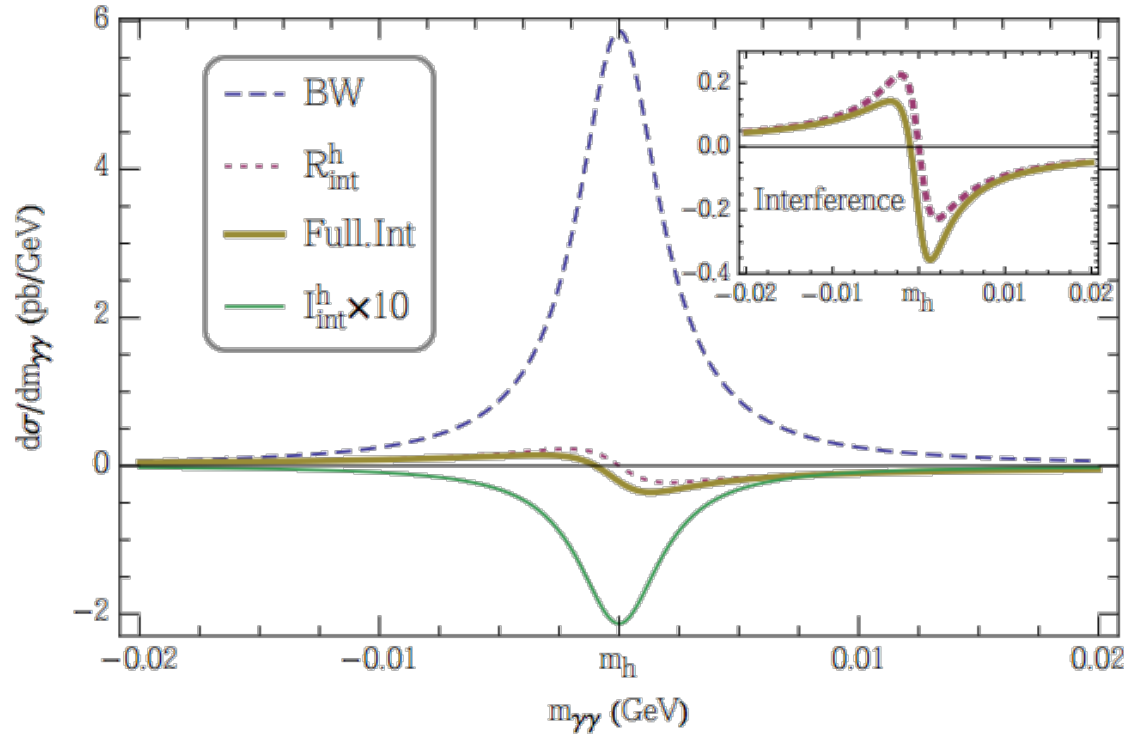
Interfering background are from SM box diagram of  $gg \rightarrow \gamma\gamma$

There is also a strong phase in the background:



- Angular dependence
- a smaller but negative phase w.r.t to the signal
- At 1-loop, the imaginary part is mainly from  $A_{++++} = A_{+---}$  with bottom and charm contributions
- Imaginary part dominated by the 2-loop MHV amplitude.

$gg \rightarrow h(125 \text{ GeV}) \rightarrow \gamma\gamma$

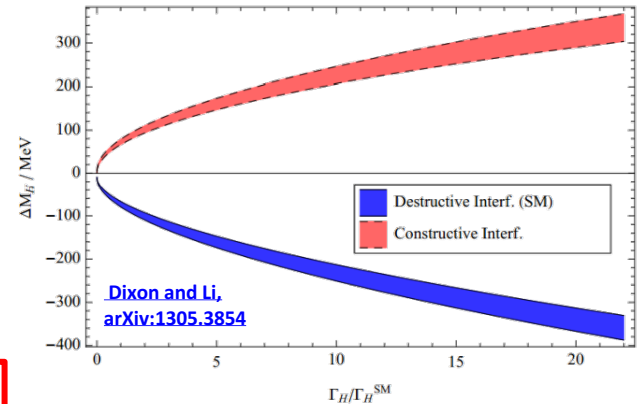


Our study is "orthogonal" to Dixon & Li 13', S. Martin 12, 13'

Averaging over helicity amplitudes and polar angles, one can calculate this new interference piece between signal and background:

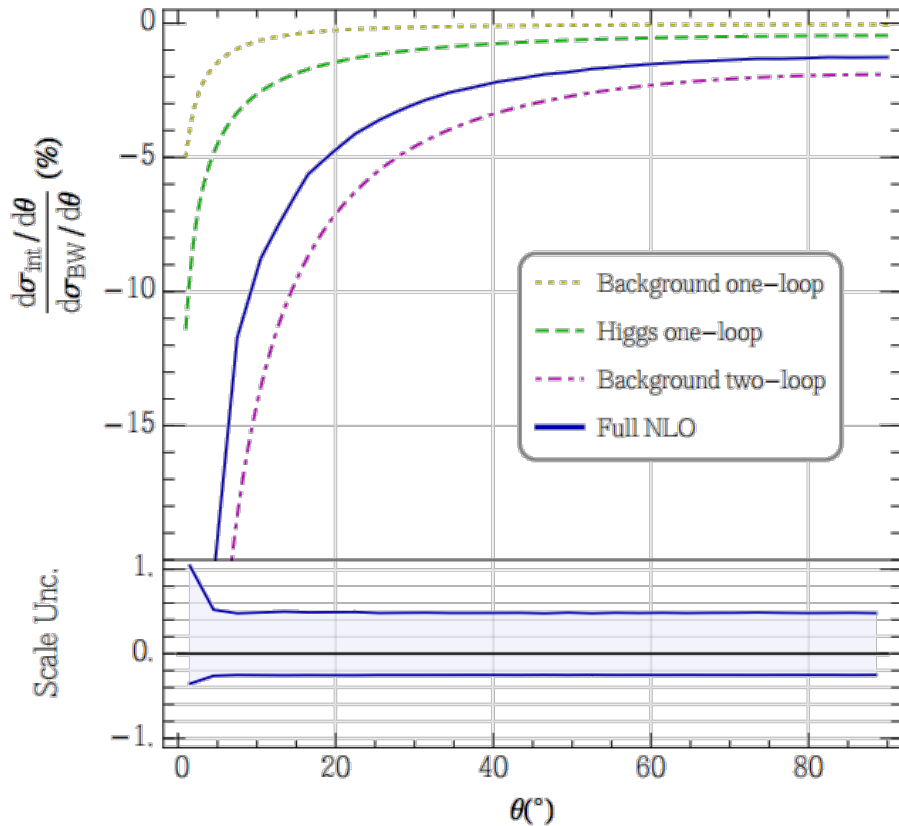
$$\begin{aligned} & \text{Im}[c_{sig}c_{bkg}^*] \\ &= |c_{sig}| |c_{bkg}^*| \sin(\delta_{sig} - \delta_{bkg}) \end{aligned}$$

The interference term from the strong phase does change the SM rate prediction by  $\sim -2.0\%$



# Kinematic features of the interference effect

$gg \rightarrow h(125 \text{ GeV}) \rightarrow \gamma\gamma$



## Angular distribution:

- Interference effects larger in the forward direction, driven by background amplitude kinematics;
- Interference effects  $\sim 0.5\%$  at LO
- Interference effects increases to  $\sim 2\%$  at NLO, driven by the 2-loop MHV amplitude's large imaginary part
- Fully inclusive cross section has larger B.W. cross section while the interference effect does not increase much, resulting in a smaller relative correction.