

## Measurement of the CKM angle $\gamma / \phi_{3}$

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## Quarks mixing and CKM matrix

- The electroweak coupling strength of $W^{ \pm}$to quarks is described by the CKM matrix

$$
-\mathcal{L}_{W^{ \pm}}=\frac{g}{\sqrt{2}} \overline{u_{L i}} \gamma^{\mu}\left(V_{\mathrm{CKM}}\right)_{i j} d_{L j} W_{\mu}^{+}+\text {h.c. } \quad-\frac{W^{+}}{-}-\underline{\underline{V_{i j}}} \begin{aligned}
& u_{i}=u, c, t \\
& \bar{d}_{j}=\bar{d}, \bar{s}, \bar{b}
\end{aligned}
$$

- $3 \times 3$ unitary matrix $\Rightarrow 4$ parameters (after ad hoc choice of quark field phases): 3 real and I CP violating phase

$$
V=\left(\begin{array}{ccc}
V_{u d} & V_{u s} & V_{u b} \\
V_{c d} & V_{c s} & V_{c b} \\
V_{t d} & V_{t s} & V_{t b}
\end{array}\right)=\left(\begin{array}{ccc}
1-\frac{\lambda^{2}}{2} & \lambda & A \lambda^{3}(\rho-i \eta) \\
-\lambda & 1-\frac{\lambda^{2}}{2} & A \lambda^{2} \\
A \lambda^{3}(1-\rho-i \eta) & -A \lambda^{2} & 1
\end{array}\right)+\mathcal{O}\left(\lambda^{4}\right)
$$

( V is unitary: $\mathrm{VV}^{+}=1$
$V_{u d} V_{u b}^{*}+V_{c d} V_{c b}^{*}+V_{t d} V_{t b}^{*}=0$


## Why measure $\gamma$

- Importance of over-constraining the CKM matrix
b precise measurement of Standard Model parameters
b search for evidence of New Physics in discrepancies of redundant measurements

- CP violating parameter $\gamma$ can be measured in tree decays
- assuming that New Physics does not change tree-level processes, its determination is not affected by New Physics
v together with the measurement of $\left|\mathrm{V}_{\mathrm{ub}} / \mathrm{V}_{\mathrm{cb}}\right|$ it gives a constraint in the rho-eta plane that must be met by any New Physics model


## How to measure a phase

- Phases are measured in the interference of two amplitudes

$$
\begin{aligned}
& \left|A_{\text {tot }}\right|^{2}=\left|A_{1}+A_{2} e^{i \phi}\right|^{2}=A_{1}^{2}+A_{2}^{2}+2 A_{1} A_{2} \cos \phi \\
& \left.\mathrm{~B}^{+} \underset{\left(V_{u b}\right)}{V_{c b} \rightarrow r_{b} e^{-i v i}} \boldsymbol{D ^ { 0 }} \mathrm{D}^{0} K^{+} \xrightarrow\left[{A\left(D^{0} \rightarrow[f]\right.}\right)\right]{A\left(\bar{D}^{0} \rightarrow[f]\right)} \\
& \text { interference } \\
& \phi=\gamma+\delta \\
& \delta=\begin{array}{l}
\text { strong phase } \\
\text { from B and } \mathrm{D} \text { decays }
\end{array} \\
& r_{b} \equiv\left|\frac{A\left(B^{+} \rightarrow D^{0} K^{+}\right)}{A\left(B^{+} \rightarrow \bar{D}^{0} K^{+}\right)}\right| \sim 0.1
\end{aligned}
$$

- The unknowns are: $\gamma, \mathrm{r}_{\mathrm{b}}$ and $\delta$
- Same principle applies to several other processes: $\mathrm{B}^{0} \rightarrow \mathrm{D}^{(*)} \pi^{+}$, $\mathrm{B}^{0} \rightarrow \mathrm{D}^{0} \mathrm{~K}\left({ }^{*}\right)^{0}, \mathrm{~B}_{\mathrm{s}} \rightarrow \mathrm{D}_{\mathrm{s}} \mathrm{K}, \ldots$


## Current experiments

- asymmetric e+e- colliders PEP-II (US) and KEK (Japan) at Y(4S) CM energy - $\mathrm{Y}(4 \mathrm{~S}) \rightarrow \mathrm{B} \overline{\mathrm{B}}$ decays detected by general purpose BaBar and Belle detectors

I 300 M $B \bar{B}$ decays overall



## Methods using $\mathrm{B} \rightarrow \mathrm{DK}$ decays

, GLW:

- $\mathrm{D}^{0}$ mesons reconstructed into two-body CP eigenstates $\mathrm{K}^{+} \mathrm{K}^{-}, \pi^{+} \pi^{-}$(even), $\mathrm{K}_{\mathrm{s}} \pi^{0}, \mathrm{~K}_{\mathrm{s}} \omega$ (odd)
- ADS:
- $\mathrm{D}^{0}$ mesons reconstructed into doubly Cabibbo suppressed decays $\mathrm{K}^{+} \pi^{-}, \mathrm{K}^{+} \pi^{-} \pi^{0}, \ldots$
- Dalitz (GGSZ):
- $\mathrm{D}^{0}$ mesons reconstructed into 3-body decays $\mathrm{K}_{\mathrm{s}} \pi^{+} \pi^{-}, \mathrm{K}_{\mathrm{s}} \mathrm{K}^{+} \mathrm{K}^{-}$,

nowadays
- Different $B$ decays $D^{0} K^{ \pm}, D^{* 0} K^{ \pm}, D^{0} K^{* \pm}$ and flavour-tagged $\mathrm{D}^{0} \mathrm{~K}^{* 0}$. They depend on different hadronic factors $\left(\mathrm{r}_{\mathrm{b}}, \delta_{\mathrm{b}}\right)$
- Strategy: combine as many channels as possible to improve the overall sensitivity to $\gamma$


## Dalitz method

D. Atwood et al., PRL78, 3257 (I997);A. Giri et al., PRD68, 0540 I8 (2003)

- The interference varies as function of the position in the $\mathrm{D}^{0}$ Dalitz plot


$A_{+}\left(m_{-}^{2}, m_{+}^{2}\right)=\left|A\left(B^{+} \rightarrow \bar{D}^{0} K^{+}\right)\right|\left[\begin{array}{l}{\left[A_{D}\left(m_{+}^{2}, m_{-}^{2}\right)\right.} \\ A_{B}\end{array} e^{i \delta_{B}} e^{+i \gamma A_{D}\left(m_{-}^{2}, m_{+}^{2}\right)}\right]$

$$
m_{ \pm}^{2} \equiv m^{2}\left(K_{S}^{0} \pi^{ \pm}\right)^{2}
$$

- $A_{D}\left(m_{-}^{2}, m_{+}{ }^{2}\right)$ is measured with a Dalitz plot analysis of high statistics samples of flavour-tagged $\mathrm{D}^{0}$ and $\overline{\mathrm{D}}^{0}$
- The $\mathrm{B}^{+}$and $\mathrm{B}^{-}$yields are measured as a function of the position in the $\mathrm{D}^{0}$ Dalitz plot (ML fit)
, Unknowns: $\gamma$, rb and $\delta_{\mathrm{b}}$



## Dalitz: reconstructed modes

| Decays | DOK | D*0[D0 $\left.0^{0}\right]$ K | D*0[Dor]K | D0K*[Kst] |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{D}^{0} \rightarrow \mathrm{~K} s \pi \pi$ | $\begin{aligned} & 383 M \\ & 657 M \end{aligned}$ | $\begin{aligned} & 383 M \\ & 357 M \end{aligned}$ | 383M | $\begin{aligned} & 383 \mathrm{M} \\ & 386 \mathrm{M} \end{aligned}$ |
| $\mathrm{D}^{0} \rightarrow$ K SKK | 383M | 383M | 383M | --- |



## Dalitz: results

- Extract the cartesian coordinates instead of $\gamma, \mathrm{r}_{\mathrm{b}}, \delta_{\mathrm{b}}$ (likelihood unbiased and Gaussian-shaped with $\mathrm{x}, \mathrm{y}$ )

$$
\begin{aligned}
& x_{\mp}=r_{B} \cos \left(\delta_{B} \mp \gamma\right) \\
& y_{\mp}=r_{B} \sin \left(\delta_{B} \mp \gamma\right)
\end{aligned}
$$

$$
\left\{\begin{array}{l}
\Gamma\left(B^{+}\right) \propto\left|f_{+}\right|^{2}+\left(x_{+}^{2}+y_{+}^{2}\right)\left|f_{-}\right|^{2}+2 x_{+} \operatorname{Re}\left(f_{+} f_{-}^{*}\right)+2 y_{+} \operatorname{Im}\left(f_{+} f_{-}^{*}\right) \\
\Gamma\left(B^{-}\right) \propto\left|f_{-}\right|^{2}+\left(x_{-}^{2}+y_{-}^{2}\right)\left|f_{+}\right|^{2}+2 x_{-} \operatorname{Re}\left(f_{-} f_{+}^{*}\right)+2 y_{-} \operatorname{Im}\left(f_{-} f_{+}^{*}\right)
\end{array}\right.
$$

$\left(x_{ \pm}, y_{ \pm}\right) 4$ variables, 3 indep. $x_{+}{ }^{2}+y_{+}{ }^{2}=x_{-}{ }^{2}+y_{-}{ }^{2}$

$$
f_{\mp} \equiv A_{D}\left(m_{\mp}^{2}, m_{ \pm}^{2}\right)
$$





## Dalitz: from $\mathrm{x}, \mathrm{y}$ to $\gamma\left(\phi_{3}\right)$

- $\left\{\gamma, \mathrm{r}_{\mathrm{b}}, \delta_{\mathrm{b}}\right.$ ) extracted from $\left\{\mathrm{x}_{ \pm}, \mathrm{y}_{ \pm}\right\}$
- frequentist stat. procedure to evaluate the error


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PRD73, II 2009 (2006)
```


$3.5 \sigma$ stat significance of CPV


$$
\begin{array}{ll}
\gamma(D K)=\left(80.8_{-14.8}^{+13.1} \pm 5.0 \pm 8.7\right)^{\circ} & \text { DK only } \\
\gamma\left(D^{*} K\right)=\left(63.8_{-22.9}^{+20.8} \pm 4.7 \pm 8.7\right)^{\circ} & D^{*} K \text { only }
\end{array}
$$

$$
\delta_{b}(D K)=\left(137.4_{-15.7}^{+13.0} \pm 4.0 \pm 22.9\right)^{\circ}
$$

$$
\delta_{b}\left(D^{*} K\right)=\left(342_{-22.9}^{+21.4} \pm 3.7 \pm 22.9\right)^{\circ}
$$

$$
r_{b}(D K)=0.161_{-0.038}^{+0.040} \pm 0.011 \pm 0.049
$$

$$
r_{b}^{*}\left(D^{*} K\right)=0.208_{-0.083}^{+0.085} \pm 0.015 \pm 0.049
$$

$$
\gamma\left(\bmod 180^{\circ}\right)=\left(76_{-13}^{+12} \pm 4 \pm 9\right)^{\circ}
$$

## Dalitz: from x,y to $\gamma\left(\phi_{3}\right)$

- Use frequentist method to obtain the physical parameter $\gamma, \mathrm{r}_{\mathrm{b}}, \delta_{\mathrm{b}}$ from $(\mathrm{x}, \mathrm{y})$

PRD78, 034023 (2008)

$3.0 \sigma$ stat significance of CPV



$$
\begin{aligned}
& r_{b}(D K)=0.086 \pm 0.035 \\
& r_{b}^{*}\left(D^{*} K\right)=0.135 \pm 0.051 \\
& \kappa r_{s}\left(D K^{*}\right)=0.163_{-0.105}^{+0.088}
\end{aligned}
$$

$$
\gamma\left(\bmod 180^{\circ}\right)=(76 \pm \underset{\text { stat }}{22} \pm \underset{\text { syst }}{5} \pm 5)^{\circ}
$$

## Dependence on $r_{b}$ of $\sigma(\gamma)$

- The error on $\gamma$ scales roughly as $\mathrm{I} / \mathrm{r}_{\mathrm{b}}$
- This is the origin of the large difference in the statistical errors of BaBar and Belle

| Parameter | $B^{+} \rightarrow D K^{+}$ |  | $B^{+} \rightarrow D^{*} K^{+}$ |
| :--- | :--- | :---: | :---: |
| $x_{-}$ | $+0.105 \pm 0.047$ | $\pm 0.011$ | $+0.024 \pm 0.140 \pm 0.018$ |
| $y_{-}$ | $+0.177 \pm 0.060 \mid \pm 0.018$ | $-0.243 \pm 0.137 \pm 0.022$ |  |
| $x_{+}$ | $-0.107 \pm 0.043$ | $\pm 0.011$ | $+0.133 \pm 0.083 \pm 0.018$ |
| $y_{+}$ | $-0.067 \pm 0.059$ | $\pm 0.018$ | $+0.130 \pm 0.120 \pm 0.022$ |




| Parameters | $B^{-} \rightarrow \tilde{D}^{0} K^{-}$ |  |
| :--- | ---: | ---: |
| $x_{-}, x_{-}^{*}, x_{s-}$ | $0.090 \pm 0.043 \pm 0.015 \pm 0.011$ |  |
| $y_{-}, y_{-}^{*}, y_{s-}$ | $0.053 \pm 0.056 \pm 0.007 \pm 0.015$ | errors on x,y |
| $x_{+}, x_{+}^{*}, x_{s+}$ | $-0.067 \pm 0.043$ | $\pm 0.014 \pm 0.011$ |
| $y_{+}, y_{+}^{*}, y_{s+}$ | $-0.015 \pm 0.055 \pm 0.006 \pm 0.008$ |  |

$$
\begin{aligned}
& r_{b}(D K)=0.161_{-0.038}^{+0.040} \pm 0.011 \pm 0.049 \\
& r_{b}^{*}\left(D^{*} K\right)=0.208_{-0.083}^{+0.055} \pm 0.015 \pm 0.049 \\
& \gamma\left(\bmod 180^{\circ}\right)=\left(766_{-13}^{+12} \pm 4 \pm 9\right)^{\circ}
\end{aligned}
$$

$$
\begin{aligned}
& r_{b}(D K)=0.086 \pm 0.035 \\
& r_{b}^{*}\left(D^{*} K\right)=0.135 \pm 0.051 \\
& \gamma\left(\bmod 180^{\circ}\right)=(76 \pm 22 \pm 5 \pm 5)^{\circ}
\end{aligned}
$$

central values of $r_{b}$ are significantly

- The " $I / r_{b}$ " effect should reduce as more data are analyzed $\left(\sigma\left(r_{b}\right) / r_{b}\right.$ decreases)


## GLW method

M. Gronau, D. London, D.Wyler, PLB253,483 (I99I); PLB 265, I72 (I99I)

- $\mathrm{D}^{0}$ to $\mathrm{K}^{+} \mathrm{K}^{-}, \pi^{+} \pi^{-}(\mathrm{CP}+)$ and $\mathrm{K} s \pi^{0}$, $\mathrm{K} s \omega$, $\mathrm{K} s \phi$ (CP-)
- measure $\mathrm{B}^{+}$and $\mathrm{B}^{-}$yields to determine the GLW observables:

$$
R_{C P \pm} \equiv \frac{\Gamma\left(B^{-} \rightarrow D_{C P \pm}^{0} K^{-}\right)+\Gamma\left(B^{+} \rightarrow D_{C P \pm}^{0} K^{+}\right)}{2 \Gamma\left(B^{-} \rightarrow D^{0} K^{-}\right)}=1 \pm 2 r_{b} \cos \gamma \cos \delta_{b}+r_{b}^{2}
$$

$$
A_{C P \pm} \equiv \frac{\Gamma\left(B^{-} \rightarrow D_{C P}^{0} K^{-}\right)-\Gamma\left(B^{+} \rightarrow D_{C P \pm}^{0} K^{+}\right)}{\Gamma\left(B^{-} \rightarrow D_{C P \pm}^{0} K^{-}\right)+\Gamma\left(B^{+} \rightarrow D_{C P \pm}^{0} K^{+}\right)}= \pm 2 r_{b} \sin \gamma \sin \delta_{b} / R_{C P \pm}
$$

4 observables
(3 independent), 3 unknowns:
$r_{b}, \delta_{b}, \gamma$
, GLW-Dalitz relation:


## GLW results



HFAG: http://www.slac.stanford.edu/xorg/hfag/
$D^{0} \mathrm{~K}$ GLW results can be translated into $x_{+}=-0.082 \pm 0.045, \quad x_{-}=0.103 \pm 0.045, \quad r_{b}{ }^{2}=0.08 \pm 0.07{ }^{*}$
Exercise:

* Gershon@CKM08

Combining GLW \& Dalitz gives $x_{+}=-0.085 \pm 0.026, x_{-}=0.103 \pm 0.027$

$$
x_{-}-x_{+}=0.189 \pm 0.037 \quad 5.1 \sigma \text { from zero* }
$$

GLW + Dalitz w/o model error

## ADS method

D. Atwood, I. Dunietz, A. Soni, PRL 78, 3357 (I997)

- $\mathrm{D}^{0}$ to $\mathrm{K}^{+} \pi^{-}, \mathrm{K}^{+} \pi^{-} \pi^{0}$ or $\mathrm{K}^{+} \pi^{+} \pi^{+} \pi^{-}$(doubly-suppressed)
suppressed
$B^{+} \rightarrow D^{(*) 0} K^{(*)+}+D^{0} \rightarrow f$ favored
$B^{+} \rightarrow \bar{D}^{(*) 0} K^{(*)+}+\bar{D}^{0} \rightarrow f$
same final state
Large interference $\sim \mathrm{O}(1)$
- measure $\mathrm{B}^{+}$and $\mathrm{B}^{-}$yields to determine the ADS observables:

$$
R_{A D S} \equiv \frac{\Gamma\left(B^{-} \rightarrow D[\rightarrow f] K^{-}\right)+\Gamma\left(B^{+} \rightarrow D[\rightarrow \bar{f}] K^{+}\right)}{\Gamma\left(B^{-} \rightarrow D[\rightarrow \bar{f}] K^{-}\right)+\Gamma\left(B^{+} \rightarrow D[\rightarrow f] K^{+}\right)}=r_{b}^{2}+r_{D}^{2}+2 r_{b} r_{D} \cos \left(\delta_{b}+\delta_{D}\right) \cos \gamma
$$

$$
A_{A D S} \equiv \frac{\Gamma\left(B^{-} \rightarrow D[\rightarrow f] K^{-}\right)-\Gamma\left(B^{+} \rightarrow D[\rightarrow \bar{f}] K^{+}\right)}{\Gamma\left(B^{-} \rightarrow D[\rightarrow f] K^{-}\right)+\Gamma\left(B^{+} \rightarrow D[\rightarrow \bar{f}] K^{+}\right)}=2 r_{b} r_{D} \sin \left(\delta_{b}+\delta_{D}\right) \sin \gamma / R_{A D S}
$$

$$
\begin{aligned}
& r_{D}=\left|\frac{A\left(\bar{D}^{0} \rightarrow f\right)}{A\left(D^{0} \rightarrow f\right)}\right| \\
& \left(\mathrm{r}_{\mathrm{D}}\left(\mathrm{~K}^{+} \pi^{-}\right)=0.06\right) \\
& \delta_{D}=\arg \left[\frac{A\left(\bar{D}^{0} \rightarrow f\right)}{A\left(D^{0} \rightarrow f\right)}\right]
\end{aligned}
$$

- ADS method useful at present to constrain $\mathrm{r}_{\mathrm{b}}$


## ADS results

- Limits on $r_{b}$ derived from $R_{\text {ADS }}$ Measurement of Belle below


$$
R_{A D S}\left(D^{0} K\right)<0.1910^{-3} @ 90 \% C L
$$

$R_{A D S}=r_{b}^{2}+r_{D}^{2}+2 r_{b} r_{D} \cos \left(\delta_{b}+\delta_{D}\right) \cos \gamma$
assuming $\cos \left(\delta_{b}+\delta_{\mathrm{d}}\right)=-1$ and $+2 \sigma$ shift in $\mathrm{r}_{\mathrm{d}}$

$$
\mathrm{r}_{\mathrm{b}}<0.19 @ 90 \% \mathrm{CL}
$$

$\mathbf{R}_{\text {ADS }}$ Averages CRELIMINARY


- No evidence of signal observed in any modes. Upper limits on $\mathrm{R}_{\text {ADS }}$ translated to upper limits on $r_{b}$


## $\mathrm{B}^{ \pm} \rightarrow \mathrm{DK}$ altogether



## Dalitz method with $\mathrm{B}^{0} \rightarrow \mathrm{D}^{0} \mathrm{~K}^{* 0}$

- Same concept as the charged $B$ analysis, with the flavour of $\mathrm{K}^{* 0} \rightarrow \mathrm{~K}^{+} \pi^{-}$ tagging the $\mathrm{B}^{0}$ flavour
- Main features
, w.r.t. charged $B$ mode: much lower signal yield but expected larger $r_{b}(\sim 0.3)$
- $\mathrm{D}^{0} \rightarrow K_{s} \pi^{+} \pi^{-}$with same Dalitz model used for the charged $B$ measurement
> likelihood fit ( $\mathrm{m}_{\mathrm{ES}}$ and event shape variables) to separate signal from background
b fit to the $\mathrm{D}^{0} \rightarrow \mathrm{~K}_{\mathrm{s}} \pi^{+} \pi^{-}$Dalitz plot to constrain $\gamma, \delta_{\mathrm{b}}$ and $\mathrm{r}_{\mathrm{s}}$
, data sample: $371 \mathrm{M} B \bar{B}$


PRD79, 072003 (2009) arXiv:0805.200 Iv2

promising for next B-factories

$$
68 \% \mathrm{CL} \left\lvert\, \begin{aligned}
\gamma & =(162 \pm 56)^{\circ} \text { or }(342 \pm 56)^{\circ} \\
\delta_{S} & =(62 \pm 57)^{\circ} \text { or }(242 \pm 57)^{\circ} \\
r_{S} & <0.30
\end{aligned}\right.
$$

$$
\rightarrow \text { using } r_{\text {s }} \text { likelihood in }
$$

PRD74,03IIOI (2006)

## ADS with $\mathrm{B}^{0} \rightarrow \mathrm{D}^{0} \mathrm{~K}^{* 0}$

arXiv:0904.2||2v| sub. to PRD (RC)

- Selection of $\mathrm{B}^{0} \rightarrow \mathrm{D}^{0} \mathrm{~K}^{*}\left[\mathrm{~K}^{+} \pi^{-}\right], \mathrm{D}^{0} \rightarrow \mathrm{~K}^{+} \pi^{-}, \mathrm{K}^{+} \pi^{-} \pi^{0}$ and
$\mathrm{K}^{+} \pi^{+} \pi^{+} \pi^{-}$
- No evidence of signal on data set of $465 \mathrm{M} B \bar{B}$

$$
\mathrm{N}_{\text {sig }}(\mathrm{tot})=24_{-11}^{+14} \quad(2.2 \sigma \text { stat only })
$$

- Set limits on $R_{\text {ADS }}$ ( $95 \% C L$ )

$\mathrm{R}_{\mathrm{ADS}}(\mathrm{K} \pi \pi \pi)<0.39$ I


- Combining all modes and using external inputs:

$$
\begin{aligned}
& r_{b} \text { in }[0.18,0.34] @ 68 \% ~ C L \\
& r_{b} \text { in }[0.07,0.4 \mathrm{I}] @ 95 \% \mathrm{CL}
\end{aligned}
$$

$r_{D}$ from PDG, $\delta_{D}(\mathrm{~K} \pi) \delta_{D}\left(K \pi \pi^{0}\right) \delta_{D}(K \pi \pi \pi)$ from CLEO-c


## $\sin (2 \beta+\gamma)$ with $\mathrm{B}^{0} \rightarrow \mathrm{D}^{(*)} \pi^{ \pm} / \rho^{ \pm}$


$P\left(B^{0} \rightarrow D^{(*) \mp} h^{ \pm}, \Delta t\right) \propto 1 \pm C \cos \left(\Delta m_{d} \Delta t\right)+S^{\mp} \sin \left(\Delta m_{d} \Delta t\right)$ $P\left(\bar{B}^{0} \rightarrow D^{(*) \mp} h^{ \pm}, \Delta t\right) \propto 1 \mp C \cos \left(\Delta m_{d} \Delta t\right)-S^{ \pm} \sin \left(\Delta m_{d} \Delta t\right)$

$$
\begin{aligned}
& S^{ \pm}=\frac{2 r}{1+r^{2}} \sin (2 \beta+\gamma \pm \delta) \\
& C=\frac{1-r^{2}}{1+r^{2}} \cong 1 \\
& r=\left|\frac{A\left(\overline{B^{0}} \rightarrow D^{(0)}-h^{+}\right)}{A\left(B^{0} \rightarrow D^{(0)}-h^{+}\right)}\right| \sim 0.02
\end{aligned}
$$

- $\mathrm{S}^{ \pm}$and C measured from time-dependent rates
- $r$ too small to be extracted from $C \rightarrow r$ fixed using external input $+\operatorname{SU}(3)$
- Effect of $b \rightarrow u$ vs. $b \rightarrow c$ interference in Btag must be taken into account.

$$
\frac{S^{ \pm} \rightarrow a \mp c \mp \eta b}{\left(\eta= \pm 1 \text { for } D^{(*) \mp} h^{ \pm}\right)}
$$



## $\sin (2 \beta+\gamma)$ with $\mathrm{B}^{0} \rightarrow \mathrm{D}^{(*)} \pi^{ \pm} / \rho^{ \pm}$



## Future experiments and perspectives

- B-factories have collected about $\mathrm{I} 300 \overline{\mathrm{M}} \mathrm{BB}$, allowing CKM test at $\sim 10 \%$ level precision
- Next generation B-factories are needed to go down to the I\% level b LHCb expected to start operations this year - $\mathrm{e}^{+} \mathrm{e}^{-}$SuperB factories proposed in Italy and Japan
- Will $\gamma$ measurements be systematic-limited? In general, no.
- Dalitz model uncertainties seem hard to reduce below $\sim 5^{\circ}$, but a model independent ānalysis is possible. It benefits from $\psi(3770) \rightarrow$ DD data of CLEOc and BESIII
- Effects of charm mixing and CPV are small and under control PRD72,03150(2005)
- Decays that at present have a weak constraining power or are not reconstructed at all (e.g., $\mathrm{B}_{\mathrm{s}} \rightarrow \mathrm{D}_{\mathrm{s}} \mathrm{K}$ ) might give significant contributions at next machines
- An uncertainty of about $2-3^{\circ}$ is expected at LHCb on $\mathrm{IOfb}{ }^{-1}$, and $\mathrm{I}-2^{\circ}$ at $\mathrm{e}^{+} \mathrm{e}^{-}$SuperB factories on $75 \mathrm{ab}^{-1}$


## Summary

- Many measurements have been performed to improve the overall precision on $\gamma / \phi_{3}$
- There is evidence of $C P$ violation in charged $B \rightarrow D K$
- Charged $B \rightarrow$ DK 'Dalitz' is currently the most sensitive method - $\sigma(\gamma) \sim 10 \div 20^{\circ}$
- Fluctuations in $\sigma(\gamma)$ due to the " $I / r_{b}$ " effect should decrease as more data are analyzed and $\sigma\left(r_{b}\right) / r_{b}$ decreases
- On larger datasets a model-independent approach can possibly be used to eliminate the Dalitz model systematics
- New measurements are expected this year. Stay tuned.


## backup slides

## Sensitivity to $\gamma$ over the Dalitz plot

- Sensitivity varies strongly over the Dalitz plane
b $2^{\text {nd }}$ derivative of the $\log (\mathrm{L})$ event-by-event weighs the event


$$
\begin{aligned}
& \sigma^{2}(\gamma) \sim \frac{1}{\frac{d^{2} \ln (L)}{d \gamma^{2}}} \\
& \text { weight }=\frac{d^{2} \ln (L)}{d \gamma^{2}} \\
& \text { events: points (weight }=1 \text { ) }
\end{aligned}
$$

Interference of $B^{-} \rightarrow D^{0}\left[\rightarrow K_{S}^{0} \rho^{0}\right] K^{-}$ with $B^{-} \rightarrow \bar{D}^{0}\left[\rightarrow K_{S}^{0} \rho^{0}\right] K^{-}$
$\equiv$ GLW like

Interference of $B^{-} \rightarrow D^{0}\left[\rightarrow K^{*+} \pi^{-}\right] K^{-}$ (suppressed) with $B^{-} \rightarrow \bar{D}^{0}\left[\rightarrow K^{*+} \pi^{-}\right] K^{-}$ $\equiv$ ADS like

## $\mathrm{x}, \mathrm{y}$ results of $\mathrm{B} \rightarrow \mathrm{D}^{(*) 0} \mathrm{~K}^{(*)}, \mathrm{D}^{0} \rightarrow \mathrm{~K}_{\mathrm{s}} \pi \pi / \mathrm{K}_{\mathrm{s}} \mathrm{KK}$

| 657M B |  |  |
| :--- | :---: | :---: |
| Bar |  |  |
| Parameter | $B^{+} \rightarrow D K^{+}$ | $B^{+} \rightarrow D^{*} K^{+}$ |
| $x_{-}$ | $+0.105 \pm 0.047 \pm 0.011$ | $+0.024 \pm 0.140 \pm 0.018$ |
| $y_{-}$ | $+0.177 \pm 0.060 \pm 0.018$ | $-0.243 \pm 0.137 \pm 0.022$ |
| $x_{+}$ | $-0.107 \pm 0.043 \pm 0.011$ | $+0.133 \pm 0.083 \pm 0.018$ |
| $y_{+}$ | $-0.067 \pm 0.059 \pm 0.018$ | $+0.130 \pm 0.120 \pm 0.022$ |



| Parameter | $B^{+} \rightarrow D K^{+}$mode | $B^{+} \rightarrow D^{*} K^{+}$mode |
| :--- | :---: | :---: |
| $\phi_{3}$ | $80.8^{\circ}{ }_{-14.8^{\circ}}^{+13.8^{\circ}} \pm 5.0^{\circ} \pm 8.7^{\circ}$ | $63.8^{\circ}{ }_{-22.90^{\circ}}^{+20.8^{\circ}} \pm 4.7^{\circ} \pm 8.7^{\circ}$ |
| $r$ | $0.161_{-0.038}^{+0.040} \pm 0.011 \pm 0.049$ | $0.208_{-0.083}^{+0.085} \pm 0.015 \pm 0.049$ |
| $\delta$ | $137.4^{\circ}{ }_{-15.7^{\circ}}^{+13.0^{\circ}} \pm 4.0^{\circ} \pm 22.9^{\circ}$ | $342.0^{\circ}{ }_{-22.9^{\circ}}^{+21.4} \pm 3.7^{\circ} \pm 22.9^{\circ}$ |


|  | Parameters | $B^{-} \rightarrow \tilde{D}^{0} K^{-}$ | $B^{-} \rightarrow \tilde{D}^{* 0} K^{-}$ | $B^{-} \rightarrow \tilde{D}^{0} K^{*-}$ |
| :---: | :---: | :---: | :---: | :---: |
| ${ }_{\text {Bup }}$ | $x_{-}, x_{-}^{*}, x_{s-}$ | $0.090 \pm 0.043 \pm 0.015 \pm 0.011$ | $-0.111 \pm 0.069 \pm 0.014 \pm 0.004$ | $0.115 \pm 0.138 \pm 0.039 \pm 0.014$ |
|  | $y_{-}, y_{*}^{*}, y_{s_{-}}$ | $0.053 \pm 0.056 \pm 0.007 \pm 0.015$ | $-0.051 \pm 0.080 \pm 0.009 \pm 0.010$ | $0.226 \pm 0.142 \pm 0.058 \pm 0.011$ |
| bABAR | $x_{+}, x_{+}^{*}, x_{s+}$ | $-0.067 \pm 0.043 \pm 0.014 \pm 0.011$ | $0.137 \pm 0.068 \pm 0.014 \pm 0.005$ | $-0.113 \pm 0.107 \pm 0.028 \pm 0.018$ |
|  | $y_{+}, y_{+}^{*}, y_{s+}$ | $-0.015 \pm 0.055 \pm 0.006 \pm 0.008$ | $0.080 \pm 0.102 \pm 0.010 \pm 0.012$ | $0.125 \pm 0.139 \pm 0.051 \pm 0.010$ |


|  | Source | $x_{-}$ | $y_{-}$ | $x_{+}$ | $y_{+}$ | $x_{-}^{*}$ | $y_{-}^{*}$ | $x_{+}^{*}$ | $y_{+}^{*}$ | $x_{s-}$ | $y_{s-}$ | $x_{s+}$ | $y_{s+}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $m_{\mathrm{ES}}, \Delta E, \mathcal{F}$ shapes | 0.001 | 0.001 | 0.001 | 0.002 | 0.002 | 0.004 | 0.004 | 0.005 | 0.003 | 0.002 | 0.001 | 0.00 |
|  | Real $D^{0}$ fractions | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 | 0.004 | 0.001 | 0.002 | 0.004 | 0.001 | 0.00 |
|  | Charge-flavor correlation | 0.002 | 0.002 | 0.001 | 0.001 | 0.002 | 0.00 | 0.002 | 0.001 | 0.001 | 0.00 | 0.00 | 00 |
|  | Efficiency in the Dalitz plot | 0.002 | 0.002 | 0.002 | 0.002 | 0.001 | 0.001 | 0.001 | 0.001 | 0.00 | 0.00 | 0.00 | 0.00 |
|  | Background Dalitz plot shape | 0.012 | 0.007 | 0.013 | 0.003 | 0.010 | 0.00 | 0.007 | 0.007 | 0.014 | 0.00 | 0.012 | 0.00 |
|  | $B^{-} \rightarrow D^{+0} K^{-}$cross feed | . |  | ... |  | 0.003 | 0.002 | 0.007 | 0.001 |  |  |  |  |
|  | $C P$ violation in $D \pi$ and $B \bar{B}$ bkg | 0.001 | 0.001 | 0.001 | 0.001 | 0.005 | 0.001 | 0.001 | 0.004 | 0.006 | 0.002 | 0.003 | 0.00 |
|  | Non- $K^{+} B^{-} \rightarrow \tilde{D}^{0} K_{S}^{0} \pi^{-}$decays |  |  |  |  |  |  |  |  | 0.0 | 0.0 | 0.025 | 0.04 |
|  | Total experimental | 0.015 | 0.007 | 0.014 | 0.006 | 0.014 | 0.009 | 0.014 | 0.010 | 0.039 | 0.058 | 0.028 | 0.0 |

