

# ***Bs mixing & interperatation***

Amarjit Soni

HET, BNL

**FPCP09**

**Lake Placid, NY**

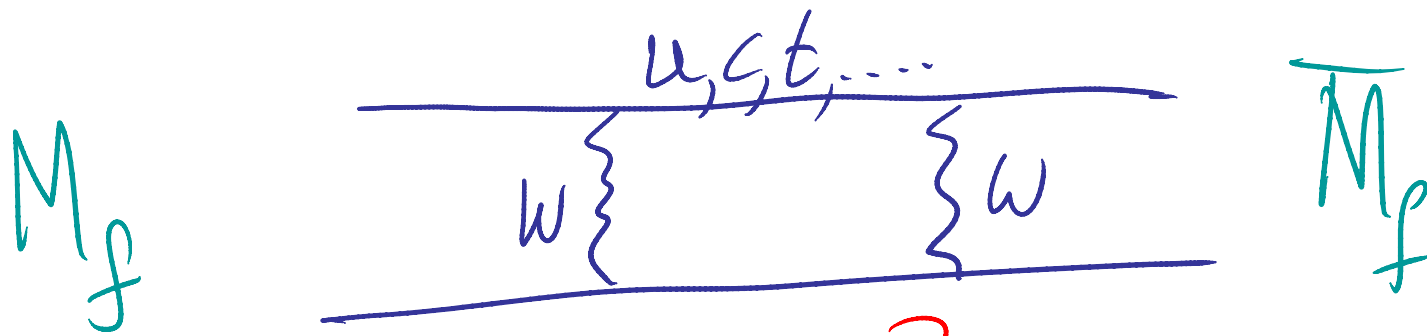
# *Outline*

- **Introduction, Motivation, Basics**
- **Theoretical underpinnings of SM predictions**
- **Possible Hints: Bs & relation with others**
- **Sample BSM scenarios**
- **Summary & Outlook**

# *$\Delta Flavor=2$ processes extremely powerful test*

- **2<sup>nd</sup> order  $\rightarrow$  severe suppression  $\rightarrow$  FLAVOR PUZZLE  $\rightarrow$  extraordinary opportunity to further our understanding of basic physics at short distances & test alignment  $\rightarrow$  FLAVOR PROBLEM for many if not most BSMs**
- **Kaon Mixing  $\rightarrow$  GIM, CHARM, CPV**
- **Bd Mixing  $\rightarrow$  Large  $m_t$ ,  $O(1)$  CP asy, precision test of UT & CKM paradigm, possible anomalies.....**
- **Bs MIXING STUDIES EXPECTED TO BE EXTREMELY RICH  $\rightarrow$  POSSIBILITY OF NEW DISCOVERIES IS A SUPERB BET!**

# A UNIQUE GIFT: EVASION of the decoupling theorem



MIXING Amp  $\propto m^2$  virtual fermion  
HIGHLY counter intuitive!

# ***Importance of being Bs: NULL TESTS GALORE!***

- Because of limitations of theory viability of CP-conserving observables is limited
- Much more precious are CP violating observables:
- CKM predicts:  $\sim 0$  phase in  $b \rightarrow s$  (penguin)
- (related)  $\sim 0$  phase in  $B_s$  box  $\rightarrow$  zilch time-dependent/mixing-induced CP Asyms  $\sim 0.02$
- Semi-leptonic asy ..TINY  $\sim 10^{-5}$

# Bs mixing preliminaries

- Time evolution:

$$i \frac{d}{dt} \begin{pmatrix} |B_s^0(t)\rangle \\ |\bar{B}_s^0(t)\rangle \end{pmatrix} = \left( M - \frac{i}{2} \Gamma \right) \begin{pmatrix} |B_s^0(t)\rangle \\ |\bar{B}_s^0(t)\rangle \end{pmatrix}$$

MASS Eigenstates  $B_L^S (m_L^S)$ ,  $B_H^S (m_H^S)$

OBSERVABLES

Mean mass  $m_S = (m_L^S + m_H^S) / 2$

|| lifetime  $\tau_S = \frac{1}{\Gamma_S} = 2 / (\Gamma_H^S + \Gamma_L^S)$

CPV phase  $\phi_S \equiv \arg(-M_{12} / \Gamma_{12})$

I.  $\Delta m_S \equiv 2 |M_{12}|$ ; II.  $\Delta \Gamma_S = 2 |\Gamma_{12}| \cos \phi_S$

III.  $a_{fs} = \ln(\Gamma_{12} / |M_{12}|) = (\Delta \Gamma_S / \Delta m_S) \tan \phi_S$

$$\Delta M_{B_q} = 2 |M_{12}^q| = \frac{|\langle \bar{B}_q^0 | \mathcal{H}_{\text{eff}} | B_q^0 \rangle|}{m_{B_q}} = \frac{G_F^2}{12\pi^2} m_W^2 m_{B_q} f_{B_q}^2 \hat{B}_{B_q} \eta_B S_0(x_t) |V_{tb} V_{tq}^*|^2$$

CDF + Dφ ... WA

$$\Delta m_s = 17.78 \pm 1.12 / \text{ps}$$

0(.7%)

THEORY CONSISTENT  
BUT LAGS SIGNIFICANTLY

$$\langle B_s | [\bar{t} \gamma_n (1 - \gamma_5) s]^2 | B_s \rangle \sim 0 (30\%)$$

$$\frac{\Delta M_{B_s}}{\Delta M_{B_d}} = \xi^2 \frac{m_{B_s}}{m_{B_d}} \left| \frac{V_{ts}}{V_{td}} \right|^2$$

Non perturbative  
SU(3) breaking  
ratio

$$\Rightarrow \left| \frac{V_{td}}{V_{ts}} \right| = 0.206 \pm 0.01 \pm 0.008$$

PROVIDES STRINGENT  
TEST OF UTφ CKM  
(c later)

~ 1.21 ± 0.05  
MORE PROGRESS  
underway: RUTH  
VDW

# Width Diff

Buchalla, Beneke, Lenz,  
& Nierste '98

$$\Gamma_{21} = \frac{1}{2M_{B_s}} \langle \bar{B}_s | \mathcal{T} | B_s \rangle$$

$$\mathcal{T} = \text{Im } i \int d^4x T \mathcal{H}_{eff}(x) \mathcal{H}_{eff}(0)$$

$$\left( \frac{\Delta\Gamma}{\Gamma} \right)_{B_s} = \left( \frac{f_{B_s}}{210 \text{ MeV}} \right)^2 [0.006 B(m_b) + 0.150 B_S(m_b) - 0.063]$$

$\rightarrow [6\delta_m(1-\delta_S)S]^2$   
 $\rightarrow [6(1+\delta_S)S]^2$

Lenz&Nierste'07

$$\Delta\Gamma_s^{\text{SM}} = \left( \frac{f_{B_s}}{240 \text{ MeV}} \right)^2 \left[ (0.105 \pm 0.016)B + (0.024 \pm 0.004)\tilde{B}'_S \right]$$

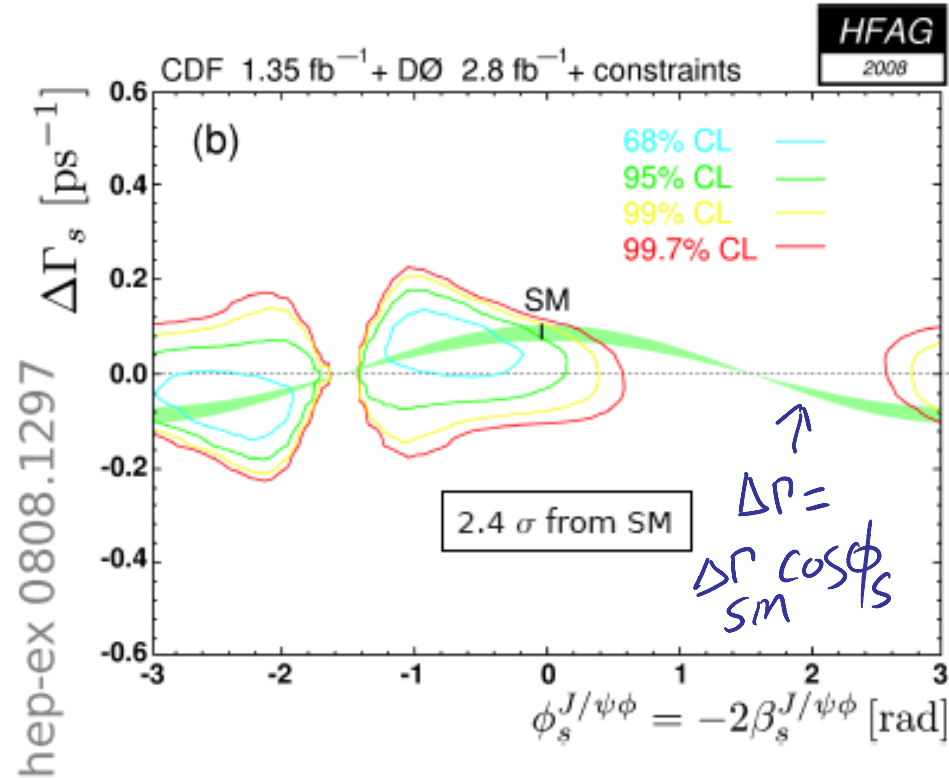
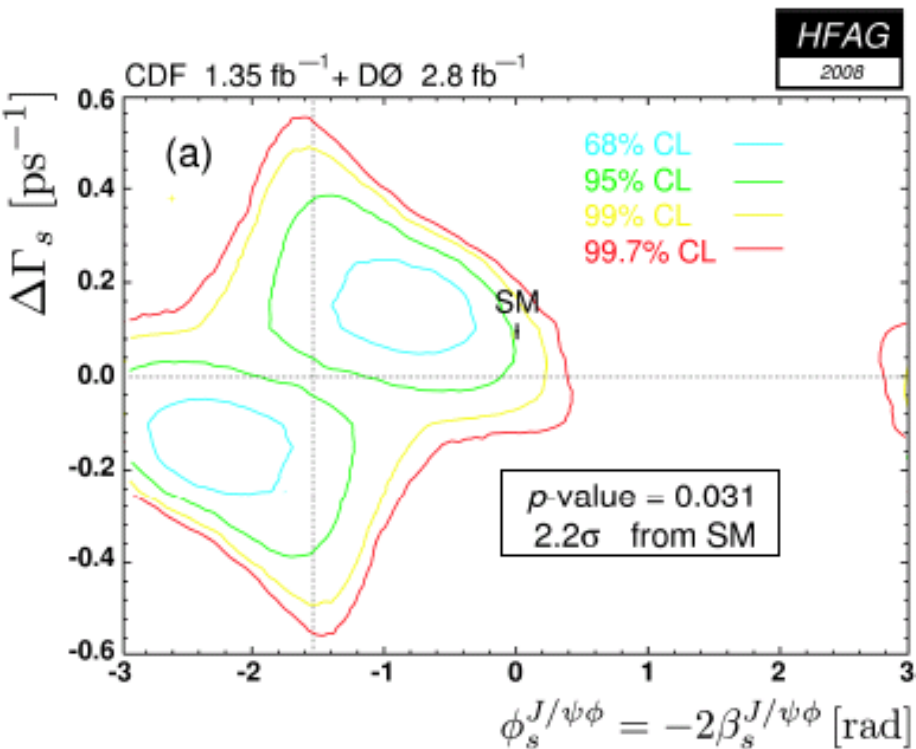
$\tilde{b}_2(1+\delta_S)S_p \tilde{b}_p(1+\delta_S)S_2$

- - - - -

$$\frac{\Delta\Gamma_s}{\Gamma_s} \approx 0.15 \pm 0.07$$



# Combination



- Old CDF result
- No constraint on strong phases

- Constraints on  $B_s$  lifetime and  $a_{\text{SL}}^s$

→ Hint for new physics?

# Summary of B-CP Anomalies

- CDF+D0 HINTS of New Physics in  $B_s \rightarrow \psi \phi$  esp. intriguing as nicely fits with indications from B-Factories
- Dir CP in  $K^+ \pi^-$  vs  $K^+ \pi^0$
- Fitted (“SM-predicted”) value of  $\sin 2\beta$  vs directly measured a) via tree decays
- $LUNGHIA + AS$   
108 b) via loop decays



6  $\mu$ ys

6  $\mu$ ys

EACH  $\sim 2$  to  $\sim 3.56$



# Lunghi+AS, arXiv.0707.0212

( $\sin 2\beta = 0.78 \pm 0.04$ )

Directly measured via  
(gold-plated)  
 $B \rightarrow \psi K_S$ ,  
 $\sin 2\beta = 0.68 \pm 0.026$

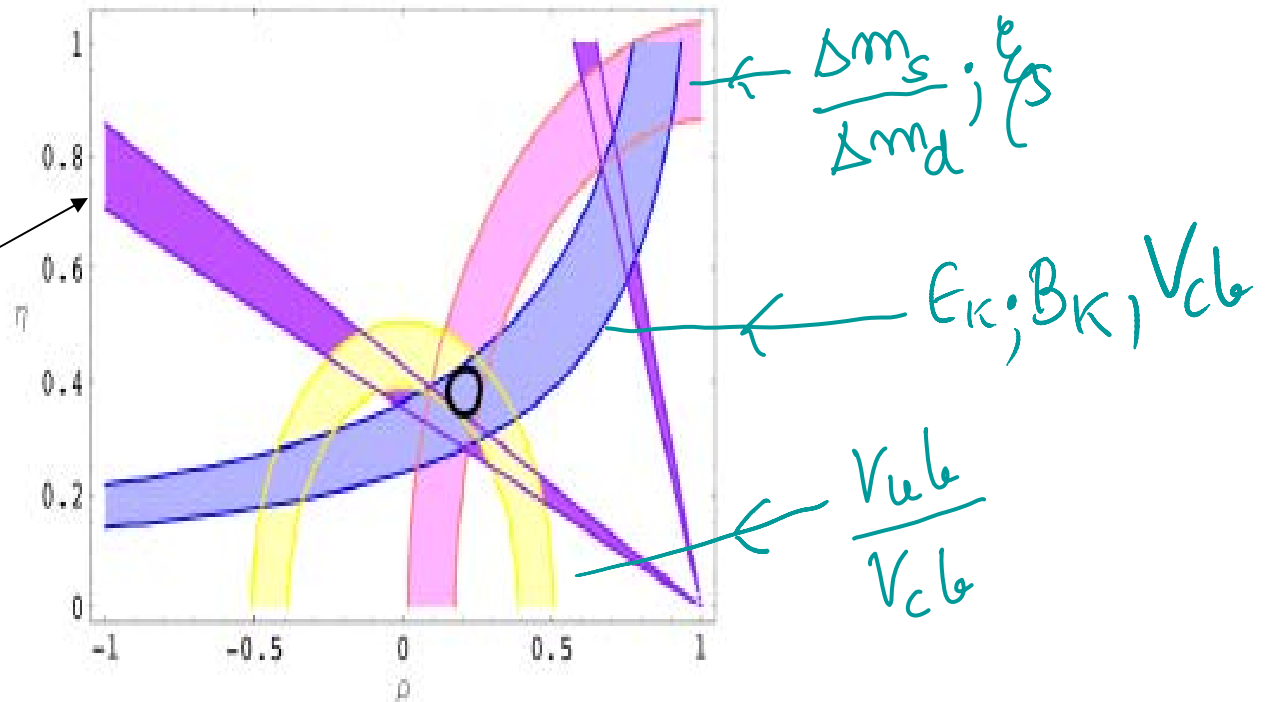


Figure 1: Unitarity triangle fit in the SM. The constraints from  $|V_{ub}/V_{cb}|$ ,  $\epsilon_K$ ,  $\Delta M_{B_s}/\Delta M_{B_d}$  are included in the fit; the region allowed by  $a_{\psi K}$  is superimposed.

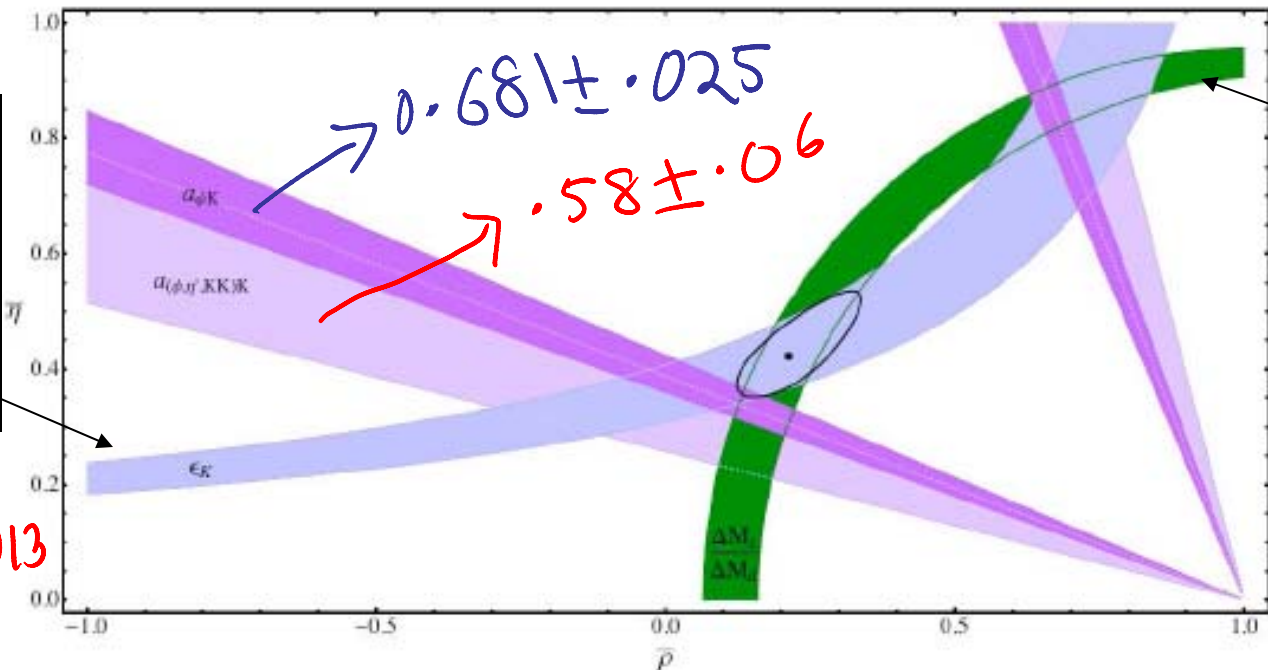
Important to Examine only  $\Delta F=2$  observables: Leave out  $V_{ub}$

$$\sin 2\beta = 0.87 \pm 0.09 \{ \text{Lunghi+AS, hep-ph/08034340} \}$$

( became possible only due significantly reduced error in  $B_K$  )

Antonio et al  
(RBC-UKQCD)  
0702042

Gamiz et al;  
Becirevic;  
Tantalo



$B_K = 0.720 \pm 0.013 \pm 0.037$

$|V_{cb}| = 40.8 \pm 0.6 \times 10^{-2}$

$\xi = 1.20 \pm 0.06$

FIG. 1: Unitarity triangle fit in the SM. All constraints are imposed at the 68% C.L.. The solid contour is obtained using the constraints from  $\epsilon_K$  and  $\Delta M_{B_s}/\Delta M_{B_d}$ . The regions allowed by  $a_{\psi K}$  and  $a_{(\phi+\eta'+2K_s)K_s}$  are superimposed.

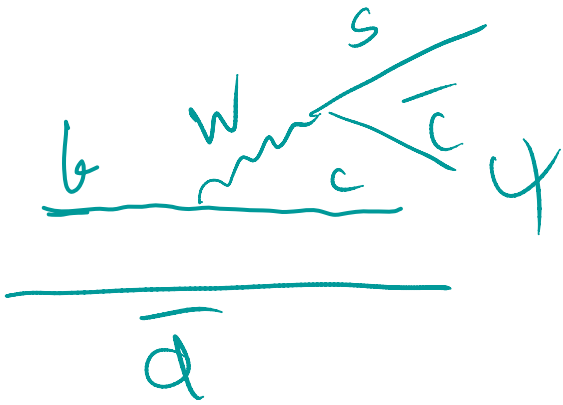
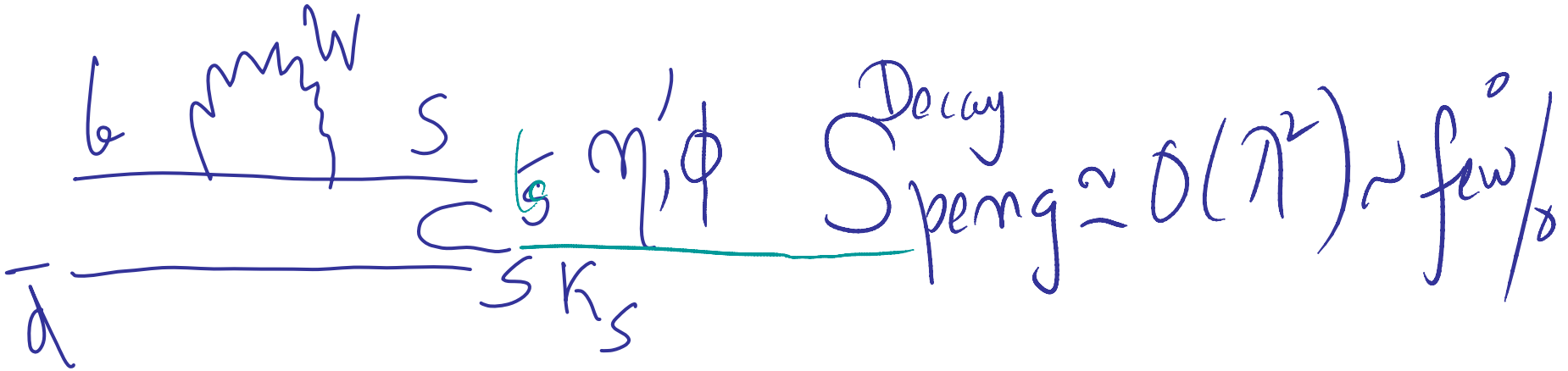
2.1-2.7  $\sigma$ - deviation from the directly measured values of  $\sin 2\beta$  requires careful follow-up

# Anomalies in $B(B_s)$ -CP asymmetries

## MORE RECENTLY

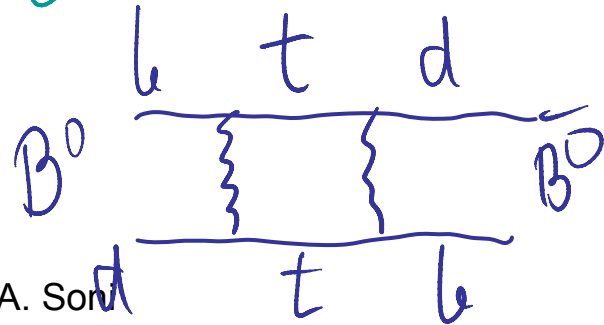
- Increased accuracy in  $B_K$  from the lattice(+ important correction from Buras & Guadagnoli), along with  $\xi_s$  from the lattice suffices now {w/o use of  $V_{ub}$ } to determine  $\sin 2\beta$  to be around  $0.87 \pm 0.09^*$  (Lunghi+AS, 0803.4340)[thanx to lattice remove  $|V_{ub}|$  CONCERN] but heightens discrepancy for SM
  - > If true suggests problem in  $\Delta b=2$  &/or  $\Delta s=2$  (ASSUMING  $V_{cb}$  is not too far off)
- {See L&S above; \*Buras & Guadagnoli 0805.3887}

$$\Delta S \equiv S_{\text{penguin}} - S_{\psi K_S} = O(\lambda^2)$$



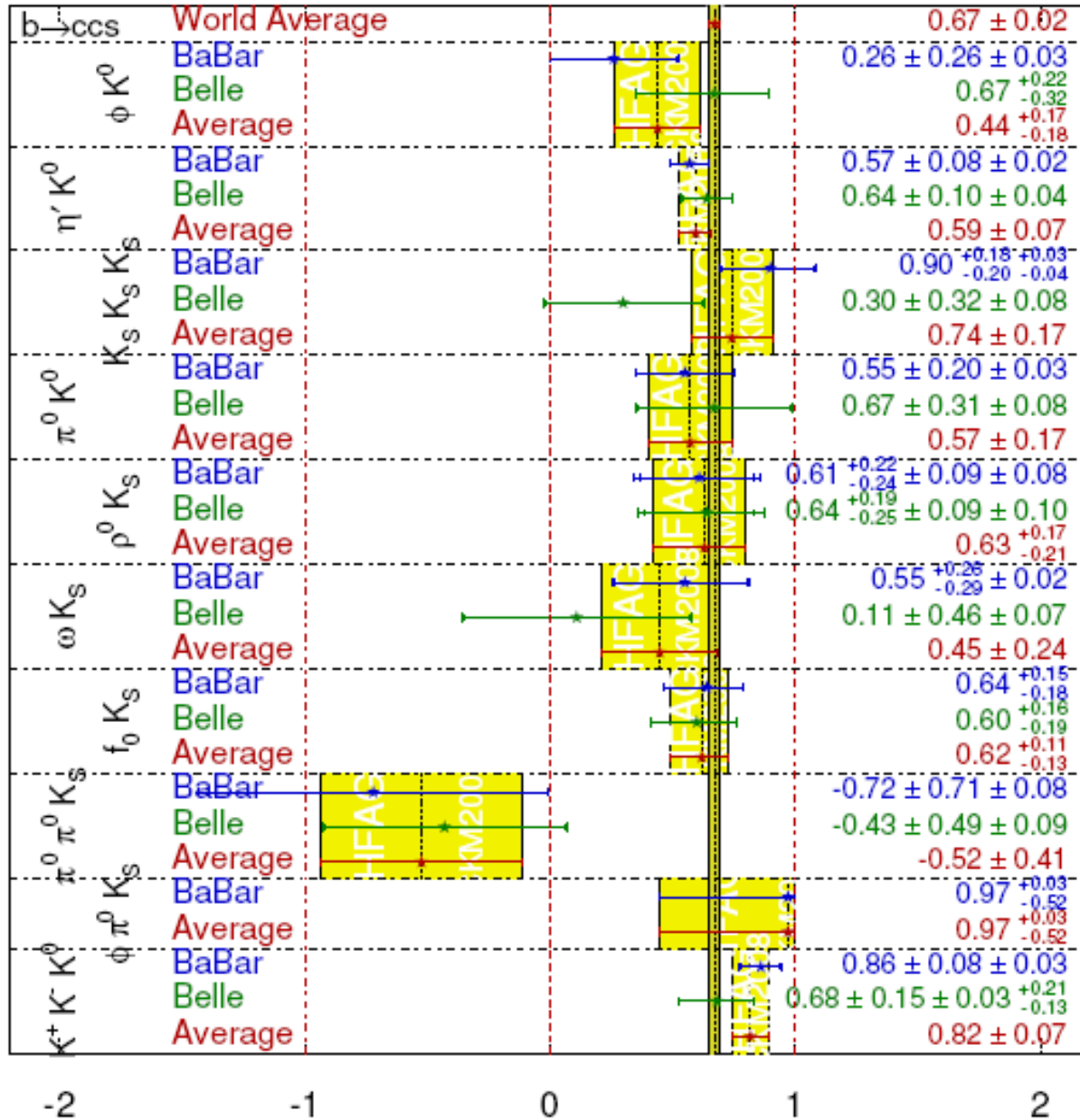
Decay  $S_{\psi K_S} = 0$

OSC is COMMON



$$\sin(2\beta^{\text{eff}}) \equiv \sin(2\phi_1^{\text{eff}})$$

**HFAG**  
CKM2008  
PRELIMINARY



Intriguing:  
Practically all  
have  
 $\sin 2\beta < (\sin 2\beta)_{SM}$   
Most have  
 $\sin 2\beta < (\sin 2\beta)_{4k5}$



Cheng, (hua, AS 105 PRD)

M. Beneke  
PLB 105

WILLIAMSON + Zupam  
Buchalla, Hiller, PRD 06  
NIR + TRAZ  
JHEP 05

TABLE I: Some expectations for  $\Delta S$  in the cleanest modes.

Mode	QCDF+FSI [20, 21]	QCDF [23]	QCDF [24]	SCET [25]
$\eta' K^0$	$0.00^{+0.00}_{-0.04}$	$0.01 \pm 0.01$	$0.01 \pm 0.02$	$-0.019 \pm 0.009$ $-0.010 \pm 0.001$
$\phi K^0$	$0.03^{+0.01}_{-0.04}$	$0.02 \pm 0.01$	$0.02 \pm 0.01$	
$K_S K_S K^0$	$0.02^{+0.00}_{-0.04}$			

# CLEANEST MODES

Courtesy: Tom Browder

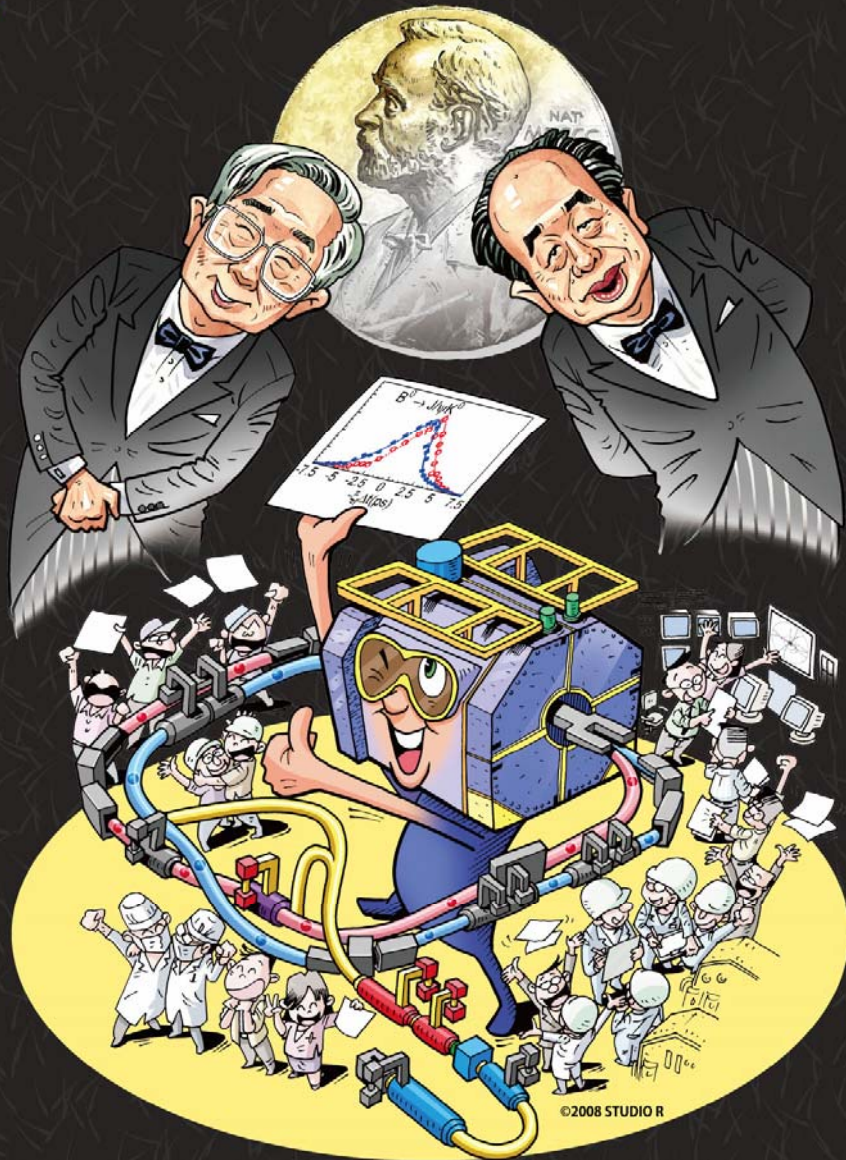
Critical Role of the B factories in the verification of the KM hypothesis was recognized and cited by the Nobel Foundation

A single irreducible phase in the weak interaction matrix accounts for most of the CPV observed in kaons and B's.



CP violating effects in the B sector are  $O(1)$  rather than  $O(10^{-3})$  as in the kaon system<sup>18</sup>

# 小林益川理論が正解だった！ Bファクトリーが放った決定打



©2008 STUDIO R

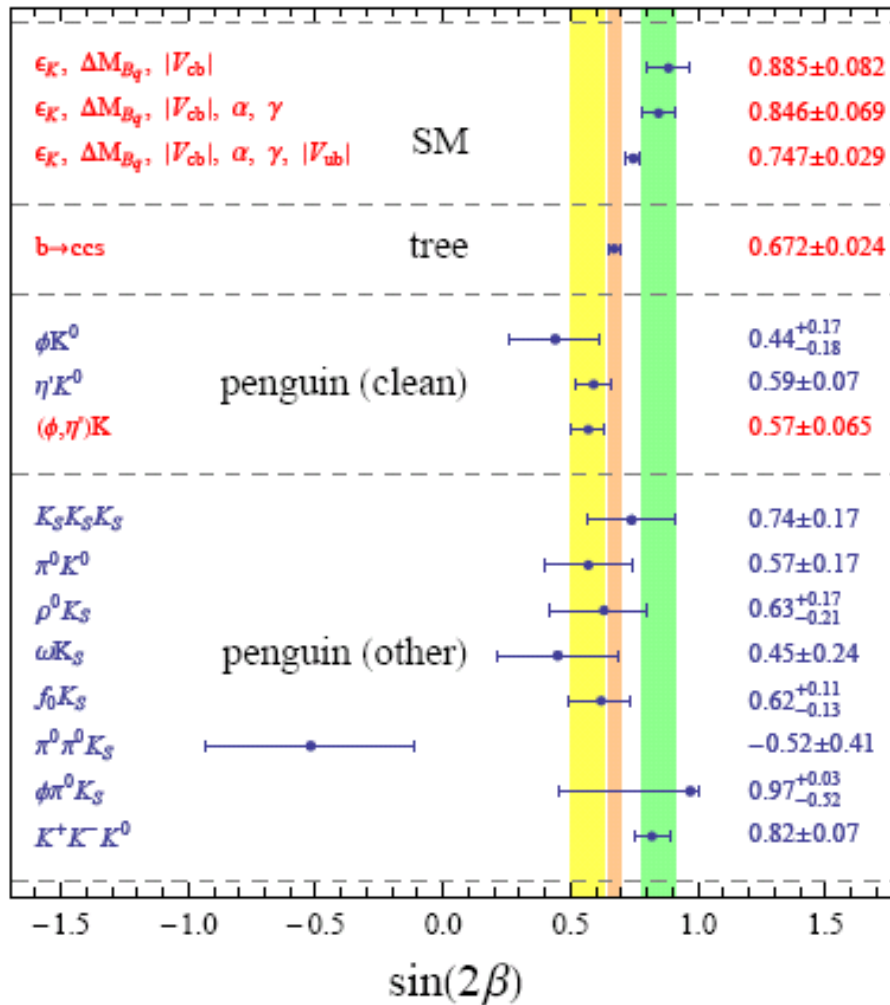
## Bファクトリー実験に参加している研究教育機関

ブドカー研究所 チェンナイ数理解析研 千葉大学  
チョンナム大学 シンシナチ大学 イーファ女子大学  
キーセン大学 キョンサン大学 ハワイ大学  
広島工業大学 北京 高師研  
モスクワ 高エネルギー研 ミスクワ 理論実験物理研  
カルスルーエ大学 神奈川大学 コリア大学  
クラコワ原子核研 京都大学 キョンボック大学  
ローザンメ大学 マックスプランク研究所  
日ゼフステファン研究所 メルボルン大学

名古屋大学 奈良女子大学 台湾 中央大学  
台湾 逢合大学 台湾人学 日本歯科大学 新潟大学  
ノバゴリカ 科学技術学校 大阪大学 大阪府立大学  
バンジャブ大学 北京大学 ビンツバーク大学  
Belle グループ <http://belle.kek.jp>  
KEKB グループ <http://www.kek.jp>  
KEKB <http://kekb.jp>

プリンストン大学 理化学研究所 佐賀大学  
中国科学技術大学 ソウル大学 信州大学  
サンケンカン大学 シドニー大学 華北大学東京  
タタ研究所 東邦大学 東北大学 東北学院大学  
東京大学 東京工業大学 東京農工大学  
トリノ 核物院研 富山高師高専専門学校  
ワエイン大学 ウィーン高エネルギー研  
ハーシニア工科大学 延世大学  
高エネルギー加速器研究機構

Poster Designed by T. Iijima, Y. Iwasaki, S. Kataoka, N. Katayama, K. Miyabayashi



mode	w/out $V_{ub}$	with $V_{ub}$
$S_{\psi K_S}$	$2.4 \sigma$	$2.0 \sigma$
$S_{\phi K_S}$	$2.2 \sigma$	$1.8 \sigma$
$S_{\eta' K_S}$	$2.6 \sigma$	$2.1 \sigma$
$S_{(\phi+\eta') K_S}$	$2.9 \sigma$	$2.5 \sigma$

**YET ANOTHER!**

Adapted from Browder

*A lesson from history (I)*

---

"A special search at Dubna was carried out by E. Okonov and his group. They did not find a single  $K_L \rightarrow \pi^+ \pi^-$  event among **600 decays** into charged particles [12] (Anikira et al., JETP 1962). At that stage the search was terminated by the administration of the Lab. The group was unlucky."

**-Lev Okun, "The Vacuum as Seen from Moscow"**

---

1964:  $BF = 2 \times 10^{-3}$

A failure of imagination ? Lack of patience ?

**Model independent determination of scale of new physics with a non-standard CP phase  
needed to fix B-CP anomalies      {Lunghi + AS '09}**

Scenario	Operator	$\Lambda$ (TeV)	$\varphi$ ( $^\circ$ )
$B_d$ mixing	$O_1^{(d)}$	$\begin{cases} 1.1 \div 2.1 & \text{no } V_{ub} \\ 1.4 \div 2.3 & \text{with } V_{ub} \end{cases}$	$\begin{cases} 15 \div 92 & \text{no } V_{ub} \\ 6 \div 60 & \text{with } V_{ub} \end{cases}$
$B_d = B_s$ mixing	$O_1^{(d)}$ & $O_1^{(s)}$	$\begin{cases} 1.0 \div 1.4 & \text{no } V_{ub} \\ 1.1 \div 2.0 & \text{with } V_{ub} \end{cases}$	$\begin{cases} 25 \div 73 & \text{no } V_{ub} \\ 9 \div 60 & \text{with } V_{ub} \end{cases}$
$K$ mixing	$O_1^{(K)}$ $O_4^{(K)}$ LR	$< 1.9$ $< 24$	$130 \div 320$
$A_{b \rightarrow s}$	$O_4^{b \rightarrow s}$ $O_{3Q}^{b \rightarrow s}$	$.25 \div .43$ $.09 \div .2$	$0 \div 70$ $0 \div 30$

GREAT NEWS for LHC & for SBF!

***WHODUNIT?***

# *Honest answer &*

- **Don't really know (too many possibilities...)**
- **But theoretically the most interesting possibility is that we may be witnessing  
Dawning of the age of**

***“Warped Quantum Flavordynamics”***

# *Many other possibilities*

- Susy<sup>1</sup>...
- Extra Higgs, Extra Z,...
- Extra gen.....
- In past few years have studied few possibilities: WEXD, T2HDM & 4<sup>th</sup> gen
- *What's the simplest solution that "can do the job"*

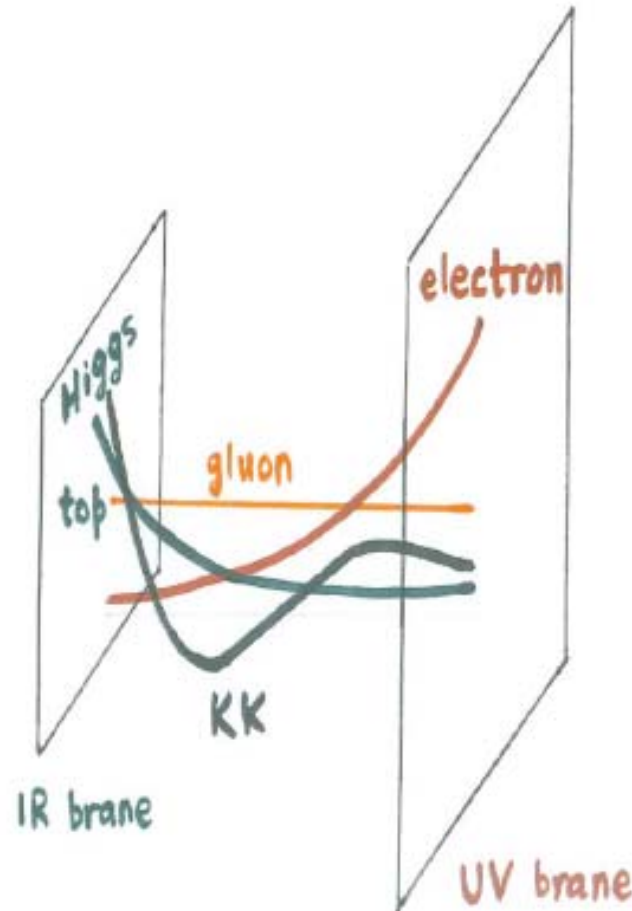
---

<sup>1</sup>"Can do everything except make coffee" —  Physics Book



# SM in bulk

(Davoudiasl, Hewett, Rizzo; Pomarol; Grossman, Neubert; Chang, Hisano, Nakano, Okada, Yamaguchi; Gherghetta, Pomarol)



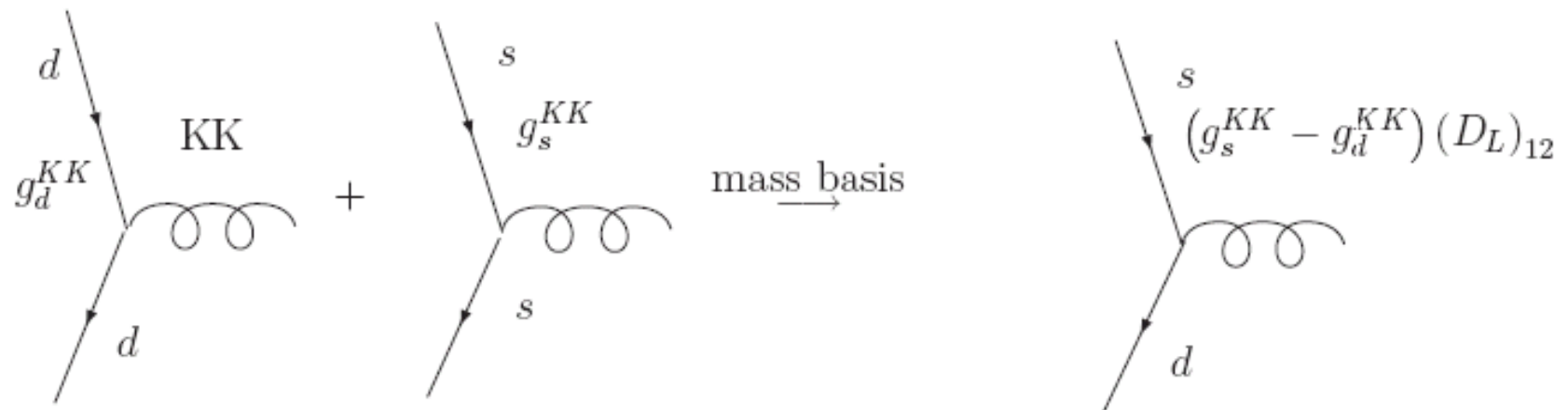
Agashe@Pheno09

# Flavor **hierarchy** from profiles $\rightarrow$

## flavor **violation** from KK's

- Non-universal, but diagonal coupling to gauge KK's in gauge/weak basis...

$$(\bar{d}_{L \text{ weak}} \quad \bar{s}_{L \text{ weak}}) \begin{pmatrix} g_d^{KK} & 0 \\ 0 & g_s^{KK} \end{pmatrix} \gamma^\mu A_\mu^{(n)} \begin{pmatrix} d_{L \text{ weak}} \\ s_{L \text{ weak}} \end{pmatrix}$$



- off-diagonal in mass basis (in general):

$$\dots D_L^\dagger \text{diag} (g_d^{KK}, g_s^{KK}) D_L \dots \rightarrow (g_s^{KK} - g_d^{KK}) (D_L)_{12} \times \bar{d}_{L \text{ mass}} \gamma^\mu A_\mu^{(n)} s_{L \text{ mass}}$$

# Contrasting B-Factory Signals from WED with those from SM

Agashe, Perez & AS, PRL '04  
 (Assumed Bd-mixing is SM)  
 O(1) uncertainties stressed

[ALSO D Mixing, D-CP  
 a medm]

	$\Delta m_{B_s}$	$S_{B_s \rightarrow \psi\phi}$	$S_{B_d \rightarrow \phi K_s}$	$Br[b \rightarrow sl^+l^-]$	$S_{B_{d,s} \rightarrow K^*, \phi\gamma}$	$S_{B_{d,s} \rightarrow \rho, K^*\gamma}$
RS1	$\Delta m_{B_s}^{SM}[1 + O(1)]$	$O(1)$	$\sin 2\beta \pm O(.2)$	$Br^{SM}[1 + O(1)]$	$O(1)$	$O(1)$
SM	$\Delta m_{B_s}^{SM}$	$\lambda_c^2$	$\sin 2\beta$	$Br^{SM}$	$\frac{m_s}{m_b} (\sin 2\beta, \lambda_c^2)$	$\frac{m_d}{m_b} (\lambda_c^2, \sin 2\beta)$

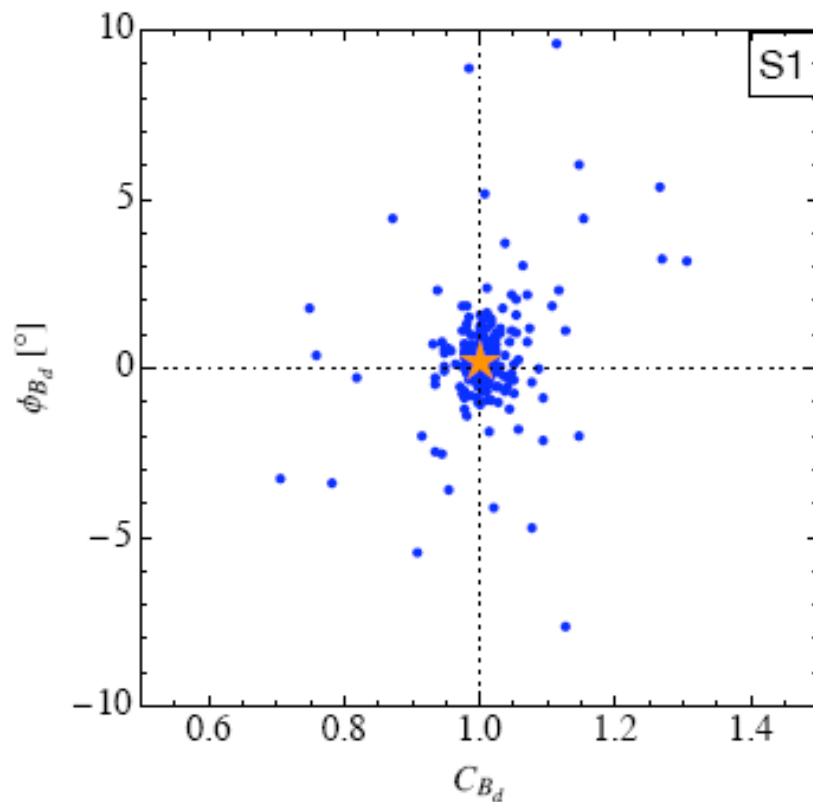
m/KK  
 73 TeV  
 ~

Recently many very nice extensions (Buras, Falkowski, Perez, Weiler, Neubert) et al

# Meson mixing: Neutral $B_d$ mesons\*

HAI SCH  
e BF 108

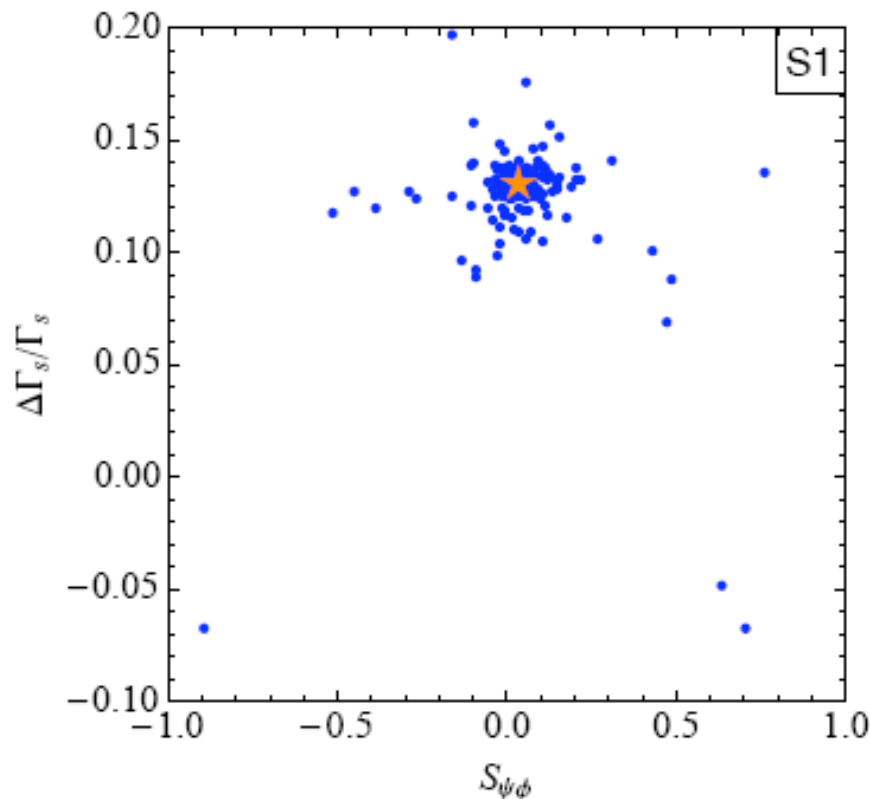
- Even after imposing  $|\varepsilon_K|$  constraint, sizable effects in magnitude and phase of  $B_d$  meson mixing amplitude possible



$$C_{B_d} e^{2i\phi_{B_d}} = \frac{\langle B_d | \mathcal{H}_{\text{eff,full}}^{\Delta B=2} | \bar{B}_d \rangle}{\langle B_d | \mathcal{H}_{\text{eff,SM}}^{\Delta B=2} | \bar{B}_d \rangle}$$

- ★ SM:  $C_{B_d} = 1$ ,  $\phi_{B_d} = 0^\circ$
- consistent with quark masses, CKM parameters, and 95% CL limit  $|\varepsilon_K| \in [1.3, 3.3] \cdot 10^{-3}$

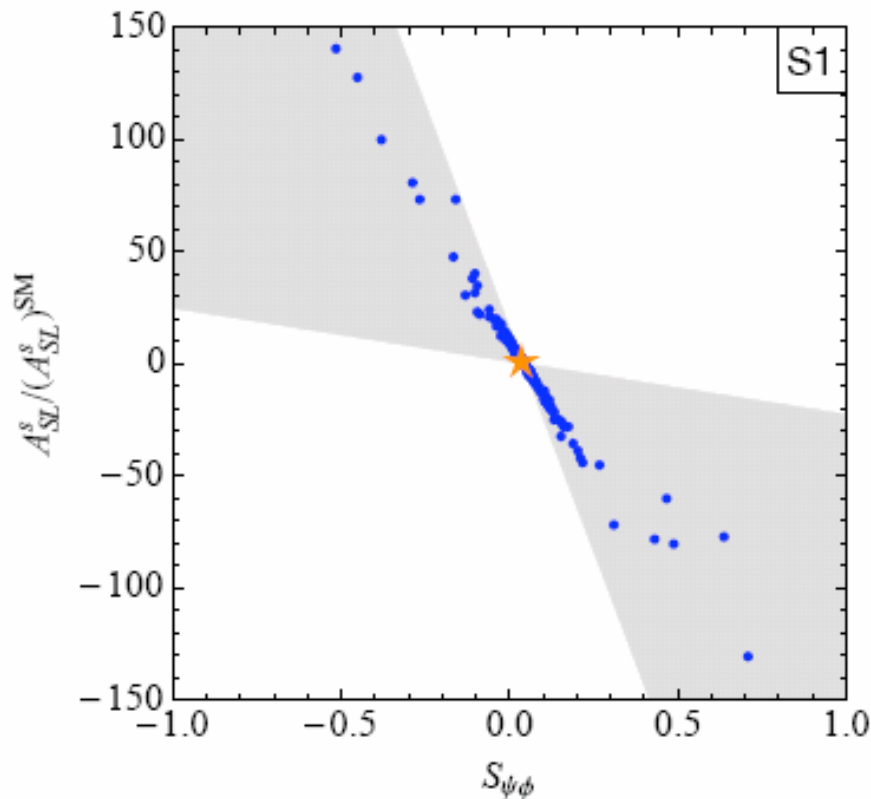
- Constraint from  $|\varepsilon_K|$  does not exclude O(1) effects in width difference  $\Delta\Gamma_s/\Gamma_s$  of  $B_s$  system



$$\begin{aligned}\Delta\Gamma_s &= \Gamma_L^s - \Gamma_S^s \\ &= 2 |\Gamma_{12}^s| \cos(2|\beta_s| - 2\phi_{B_s})\end{aligned}$$

- ★ SM:  $\Delta\Gamma_s/\Gamma_s \approx 0.13$ ,  $S_{\psi\phi} \approx 0.04$
- consistent with quark masses, GKM parameters, and 95% CL limit  $|\varepsilon_K| \in [1.3, 3.3] \cdot 10^{-3}$

- In RS model significant corrections to semileptonic CP asymmetry  $A_{SL}^s$  and  $S_{\psi\phi} = \sin(2|\beta_s| - 2\phi_{B_s})$ , consistent with  $|\varepsilon_K|$ , can arise



$$A_{SL}^s = \frac{\Gamma(\bar{B}_s \rightarrow l^+ X) - \Gamma(B_s \rightarrow l^- X)}{\Gamma(\bar{B}_s \rightarrow l^+ X) + \Gamma(B_s \rightarrow l^- X)}$$

$$= \text{Im} \left( \frac{\Gamma_{12}^s}{M_{12}^s} \right)$$

★ SM:  $A_{SL}^s \approx 2 \cdot 10^{-5}$ ,  $S_{\psi\phi} \approx 0.04$

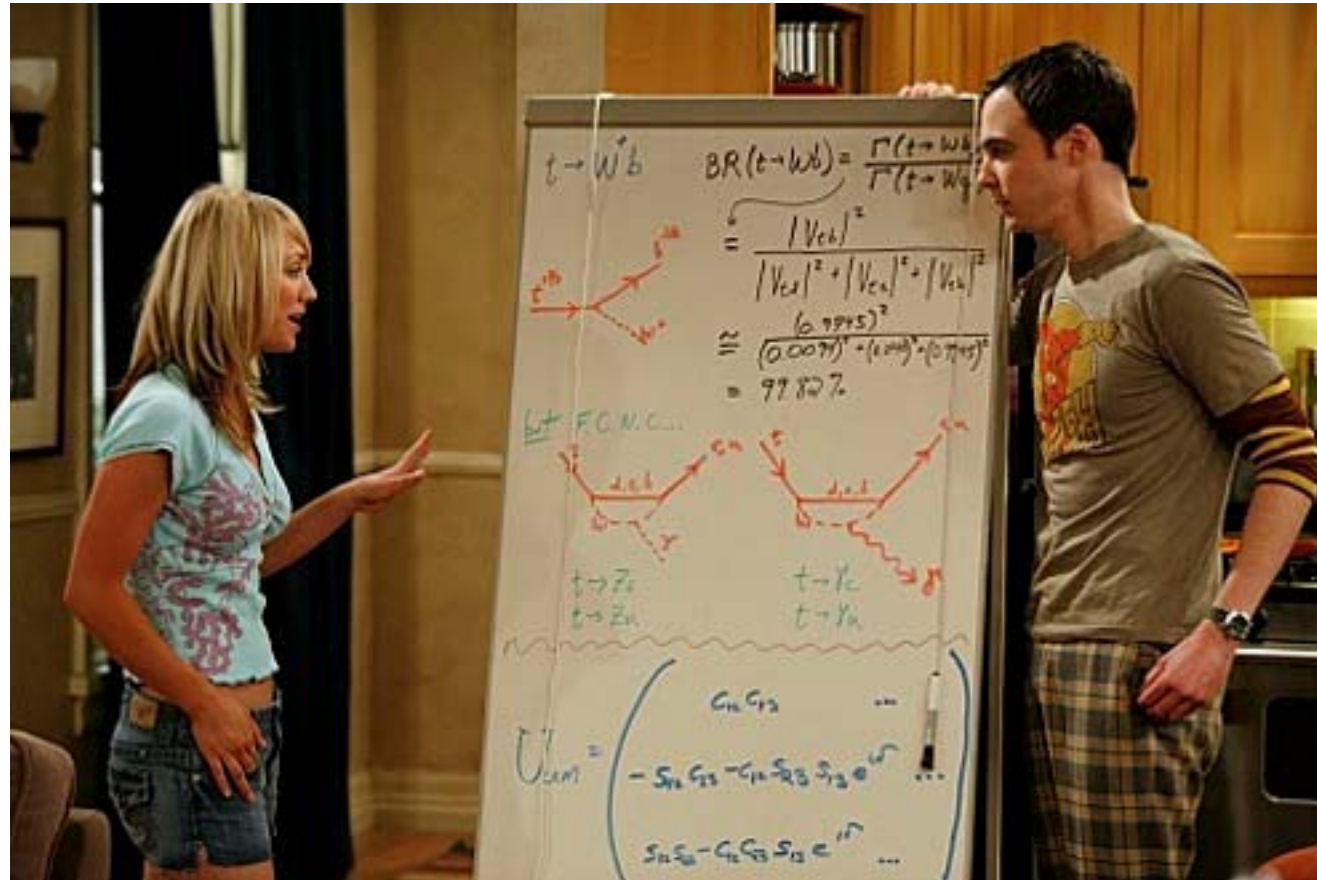
■ model-independent prediction

● consistent with quark masses, CKM parameters, and 95% CL limit  $|\varepsilon_K| \in [1.3, 3.3] \cdot 10^{-3}$

***TWO important subtleties:  
I. The flavor puzzle***

# LHC/Super B factory synergy discussion on US TV comedy

D. Saltzberg,  
Science  
Advisor



CBS, “Big Bang Theory” averages 9 million viewers per episode.

Courtesy Tom Browder



## **II. EXTREMELY INTERESTING SUBTELTY of warped models**

- Maldacena conjecture
- **“Warped Quantum Flavordynamics” is DUAL to strong dynamics->**

**Focus for now on the SIMPLEST 4d**

**Explanation (s):** I T2HDM '07  
II SM4 → Now

**Thus by process of elimination one arrives at**

***More explicitly How does 4<sup>th</sup>  
family fit in?***

For details see AS+ Alok, Giri, Mohanta & Soumitra in WHEPPX (see published Proceedings Jan, '08) & arXiv:0807.1971 & in progress

# HINTS

- I. CP observables are crucial; CP conserving processes seem to see hardly any effect.
- II. EWP seems to have a NP component to it:  
Reminiscent of the non-decoupling effects in SBGT's
- III. NP seems to depend on  $b \rightarrow d$  versus  $b \rightarrow s$  ( $s \rightarrow d$  is also a possibility)
  - > This is suggestive of a “4<sup>th</sup> family”...PERHAPS THE SIMPLEST SOLUTION
  - > 2 entirely new phases..THEREFORE NOT A PERTURBATION for CPV..NULL TESTS of SM-CKM MAY FAIL A LOT... $B_s \rightarrow \psi\phi$  ,  $B_d \rightarrow \phi$   $K_s$  are null tests whereas  $B_r$ s show little effect.
  - > 3 new mixing angles, 2 new masses: total of 7 parameters...

-> 4th family with rather heavy  $t'(b')$ , masses  $\sim 400-600$  GeV provides perhaps the simplest explanation (AS et al, 0807.1971)

{suggestion of 4th family also made by Hou et al JHEP'06;PRL'05;PRL'07.... though their discussions seem confined to lighter  $m_{t'}$ }

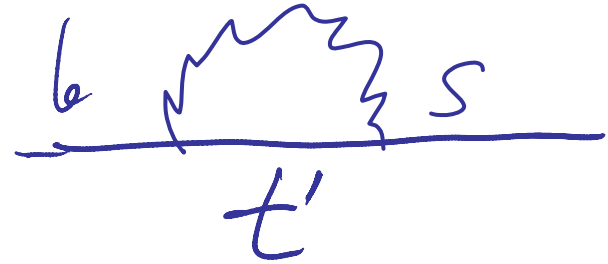
-> IN OUR WORK  $m_{t'} 400-600\text{GeV}$  -> If true then it likely plays an impt. ROLE IN DYNAMICAL EWSB thereby providing a possible resolution to EW-Planck hierarchy{ see, e.g. He, Hill & Tait, hep-ph/0108041}

INPUTS  
 &  
 Constraints

$B_K = 0.72 \pm 0.05$	
$f_{b_s} \sqrt{B_{b_s}} = 0.281 \pm 0.021 \text{ GeV}$	
$\Delta M_s = (17.77 \pm 0.12) ps^{-1}$	
$\Delta M_d = (0.507 \pm 0.005) ps^{-1}$	
$\xi_s = 1.2 \pm 0.06$	
$\gamma = (75.0 \pm 22.0)^\circ$	
$ \epsilon_k  \times 10^3 = 2.32 \pm 0.007$	
$\sin 2\beta_{\psi K_s} = 0.672 \pm 0.024$	←
$\mathcal{BR}(K^+ \rightarrow \pi^+ \nu \nu) = (0.147_{-0.089}^{+0.130}) \times 10^{-9}$	
$\mathcal{BR}(B \rightarrow X_c \ell \nu) = (10.61 \pm 0.17) \times 10^{-2}$	
$\mathcal{BR}(B \rightarrow X_s \gamma) = (3.55 \pm 0.25) \times 10^{-4}$	
$\mathcal{BR}(B \rightarrow X_s \ell^+ \ell^-) = (0.44 \pm 0.12) \times 10^{-6}$	←
( High $q^2$ region )	
$R_{bb} = 0.216 \pm 0.001$	←
$ V_{ub}  = (37.2 \pm 2.7) \times 10^{-4}$	
$ V_{cb}  = (40.8 \pm 0.6) \times 10^{-3}$	
$\eta_c = 1.51 \pm 0.24$ [21]	
$\eta_t = 0.5765 \pm 0.0065$ [22]	
$\eta_{ct} = 0.47 \pm 0.04$ [23]	
$m_t = 172.5 \text{ GeV}$	

TABLE I: Inputs that we use in order to constrain the SM4 parameter space, we have considered the  $2\sigma$  range for  $V_{ub}$ .

$$\lambda_{t'}^s = |V_{t's}^* V_{t'l}|$$



$m_{t'}$	400	500	600	700
$\lambda_{t'}^s$	(0.08 - 1.4)	(0.06 - 0.9)	(0.05 - 0.7)	(0.04 - 0.55)
$\phi'_s$	-80 $\rightarrow$ 80	-80 $\rightarrow$ 80	-80 $\rightarrow$ 80	-80 $\rightarrow$ 80

NOTE

TABLE II: Allowed ranges for the parameters,  $\lambda_{t'}^s$  ( $\times 10^{-2}$ ) and phase  $\phi'_s$  (in degree) for different masses  $m_{t'}$  (GeV), that has been obtained from the fitting with the inputs in Table I.

New CP phase of  $V_{t's}$  responsible for  $\phi_{K_s}, \eta'_{K_s}$

Recall  $\lambda_{t'}^s = 0.04$   
 $\arg V_{t's} \sim 0$

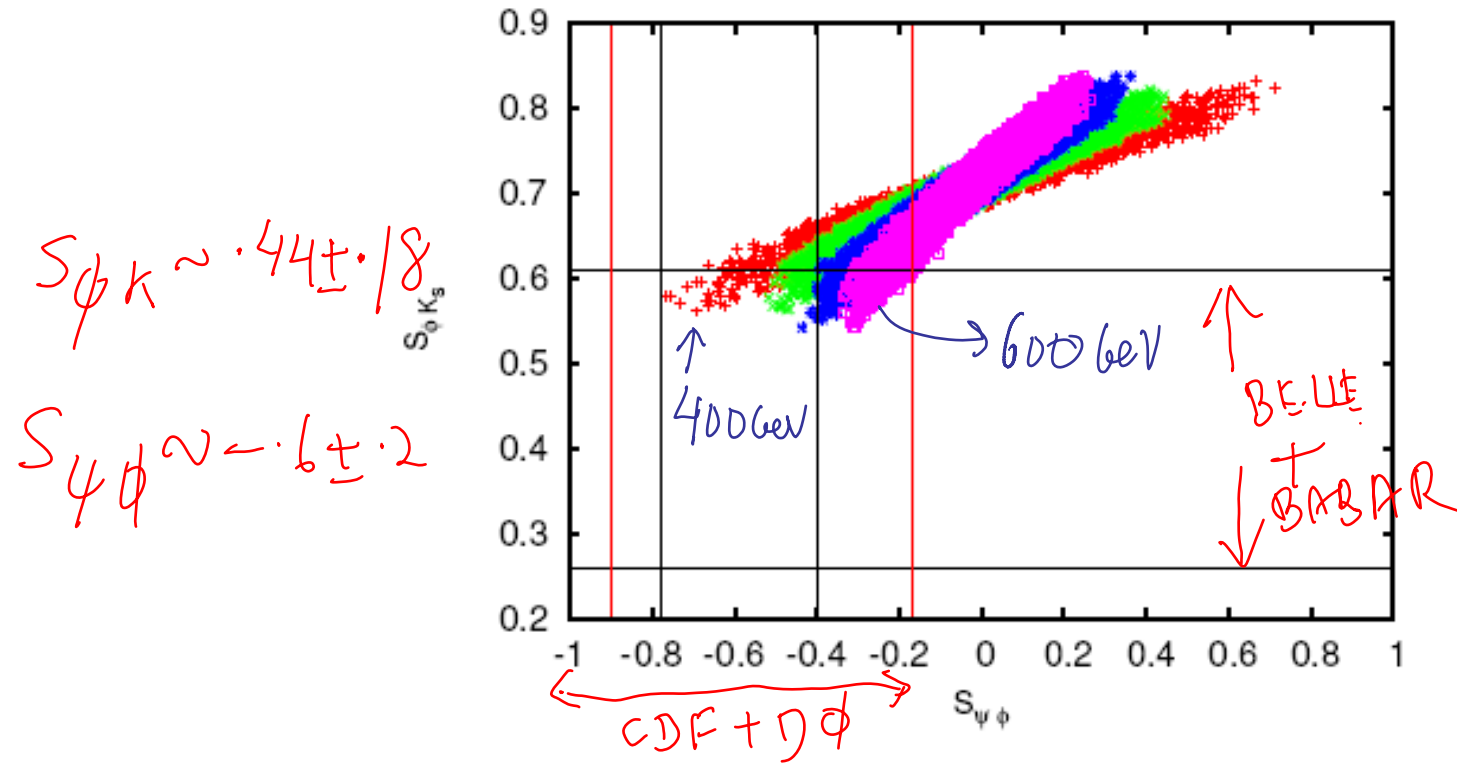


FIG. 3: Correlation between  $S_{\phi K_s}$  and  $S_{\psi\phi}$  for  $m_{t'} = 400$  (red), 600 (green), 800 (magenta) and 1000 (blue) GeV respectively. The horizontal lines represent the experimental  $1\sigma$  range for  $S_{\phi K_s}$  whereas the vertical lines (Black  $1\sigma$  and red  $2\sigma$ ) represent that for  $S_{\psi\phi}$ .

CURRENT  
 DATA MILDLY  
 FAVORS  
 $m_{t'} \approx 4-500$

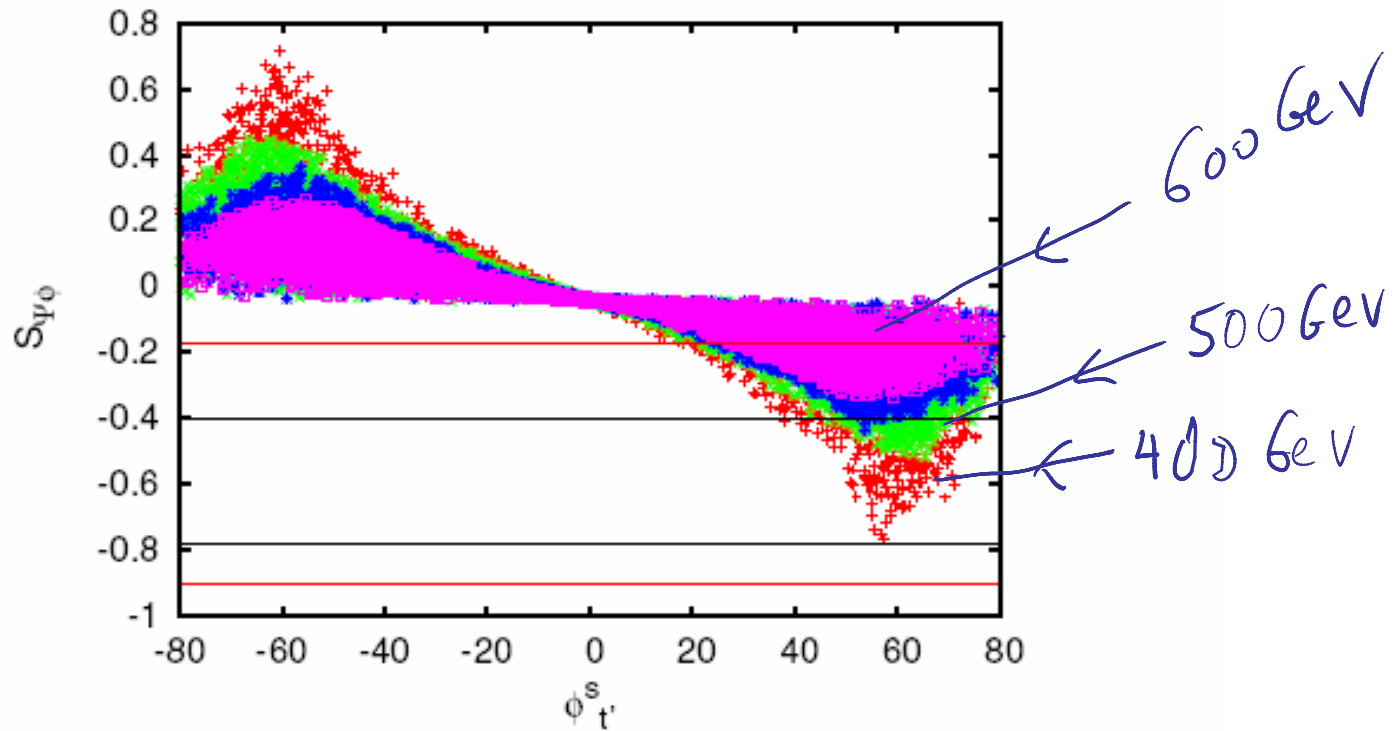


FIG. 2: The allowed range for  $S_{\psi\phi}$  in the  $(S_{\psi\phi} - \phi_{t'}^s)$  plane for  $m_{t'} = 400$  (red), 500 (green), 600 (magenta) and 700 (blue) GeV respectively. Black and red horizontal lines in the figure indicate  $1-\sigma$  and  $2-\sigma$  experimental ranges for  $S_{\psi\phi}$  respectively.



$L \rightarrow t' \rightarrow S$   
 $Z \rightarrow \dots \rightarrow \pi^0$   
 $A_{\text{adm}}^2$   
**NONDECOUP.**  
 Color Allowed  
 EWP  
 (See also HWS '87)

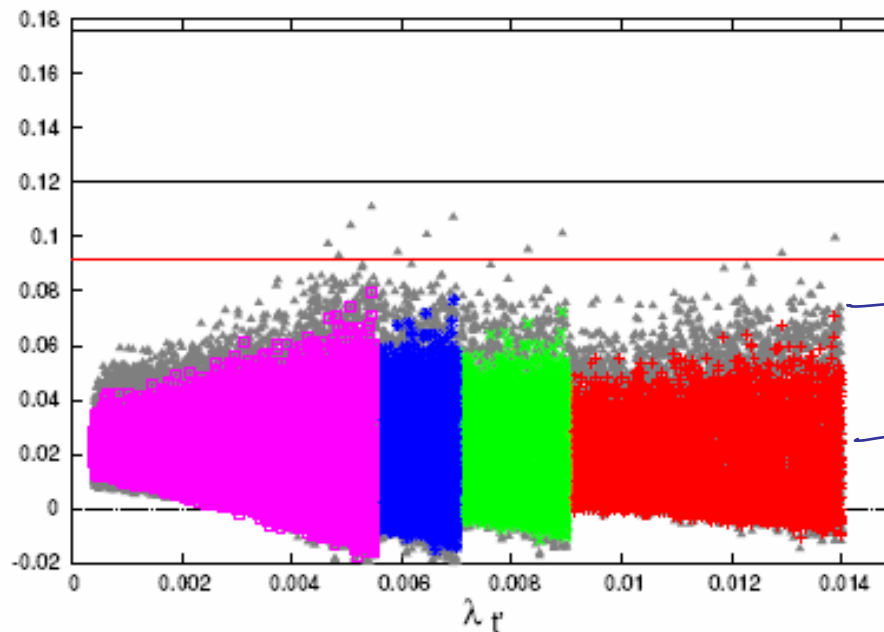


FIG. 1: The allowed range of the CP asymmetry difference ( $\Delta A_{CP}$ ) in the ( $\Delta A_{CP} - \lambda_{t'}^s$ ) plane, where the red, green, magenta and blue regions correspond to  $m_{t'} = 400, 500, 600$  and  $700$  GeV. The 30 % error bars due to hadronic uncertainties [5] are shown by grey bands. The black and red horizontal lines correspond to the experimentally allowed 1 and 2- $\sigma$  range respectively.

***Possible relevance of SM4:  
This is a revisit***

## ***Early (~87-88) studies on 4<sup>th</sup> gen.***

- **Hou, Willey and AS, PRL (88)..b->s | l...**
- **Hou, AS, Steger, PRL 87.....b-> s g**
- **Hou, AS, Steger, PLB 87**  
**4X4 mixing matrix and b -> s gamma**

**Importance of B-decays for studying 4<sup>th</sup> gen. due to non-decoupling  
emphasized long ago**

Annals of The New York Academy of Sciences Volume 578

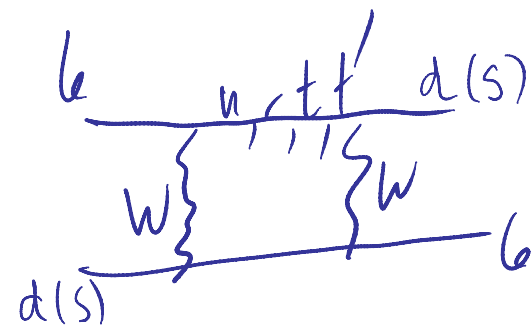
# The Fourth Family of Quarks and Leptons

## Second International Symposium

Editors

DAVID B. CLINE • AMARJIT SONI





# THUS

by construction

- The CKM-paradigm of CP violation accounts for the observed CP patterns to an accuracy of about 15%!
- SM3-CKM predicted value of  $\sin 2\beta$  tends to be high compared to direct ( $\psi K$ ) measurements by about 15-20%...t is dominant
- Hierarchical structure of SM4 mixing matrix **NATURALLY** lets  $t'$  be subdominant here but due to its large mass (and decoupling theorem) not negligible *leads to small  $\sim 15\%$  deviations*
- Dynamics of EW gauge interactions (evasion of decoupling theorem) by EWpenguins and the large  $mt'$  plays an important role in the large "isospin" violating  $\Delta A_{CP}(K\pi)$
- SM3 says  $B_s$  mixing has negligible CP-odd phase therein  $t'$  plays a dominant role (& t is subdominant)

due to t

# ***BORING REPETITION?***

- If the  $m_{t'}$  is heavy  $\sim(400-600)$  GeV, then for sure it will have a very serious role to play in EWSB .(NOTE CDF+D0 latest bound  $m_{t'} > 350$  GeV).
- It will clearly have significant impact on CP violation phenomena, given that now we will have 2 additional CP-odd phases
- It may play an interesting role in baryogenesis (W.-S. Hou, 0803.1234; Fok & Kribs, 0803.4207)
- CANNOT BE A CONVENTIONAL 4<sup>th</sup> Gen.. $m_{t'} > m_Z/2$
- Possible DMC (if no mixing with lighter 3  $\nu$ 's)..see e.g. Volovik
- An important CAVEAT...such heavy mass of  $t'$  means Yukawa couplings are somewhat large so perturbation theory calculations used in here are likely to have non-negligible corrections

# ***SUMMARY & OUTLOOK***

- Bs mixing is an **EXTREMELY VALUABLE TREASURE...most likely** will enrichen our understanding significantly.
- **SEVERAL ANOMALIES** involving Bs,Bd mixings & decays should be scrutinized with the highest priority...Underlying cause may well be NP in a sub-TeV range...**“4<sup>th</sup> Gen”** seems to offer a simple solution
- These indications imply lots of accessible manifestations at LHC but also, for sure, means that LHC(b), SBF & (S)LHCb will have a very important role to play

# Backup slides



It is perhaps of some use to extract the values of  $\hat{B}_K$ ,  $\xi_s$  and  $V_{cb}$  that are required to reduce to the 1- $\sigma$  level the discrepancy between the prediction given in Eq. (5) and  $a_{(\psi+\phi+\eta'+K_S K_S)K_S} = 0.66 \pm 0.024$ . We find that one has to choose either  $\hat{B}_K^{\text{new}} = 0.96 \pm 0.04$ ,  $\xi_s^{\text{new}} = 1.37 \pm 0.06$  or  $V_{cb} = (44.3 \pm 0.6) \times 10^{-3}$ .

[USED  $\hat{B}_K = 0.72 \pm 0.04$ ;  $\xi_s = 1.20 \pm 0.06$ ;  
 $V_{cb} = (40.8 \pm 0.6) \times 10^{-3}$ ]

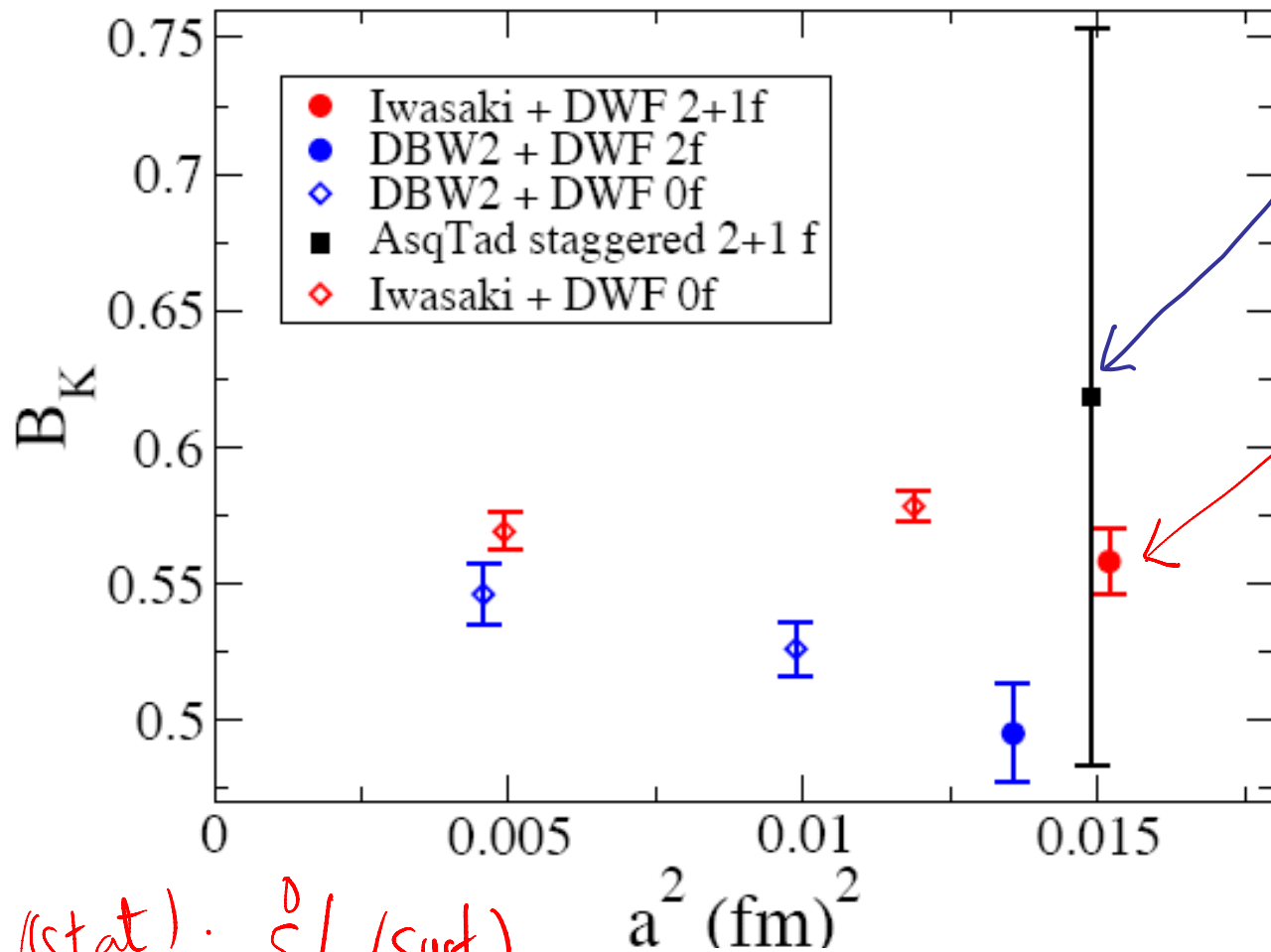
# Continuing saga of Vub

- For past 2 years or so exclusive & inclusive  
~small discrepancy:
- Exc  $\sim (3.7 \pm .2 \pm .5) \times 10^{-3}$
- Inc  $\sim (4.3 \pm .2 \pm .3) \times 10^{-3}$

-> ***Let's try NOT use Vub***

$$B_K^{\overline{\text{MS}}}(2 \text{ GeV}) = 0.524(10)(28)$$

PRL Jan25,08



$\sim 2\%$  (stat);  $5\%$  (syst)

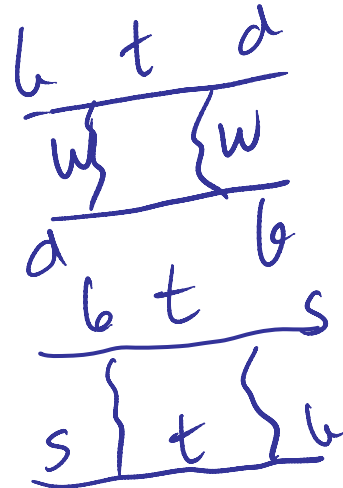
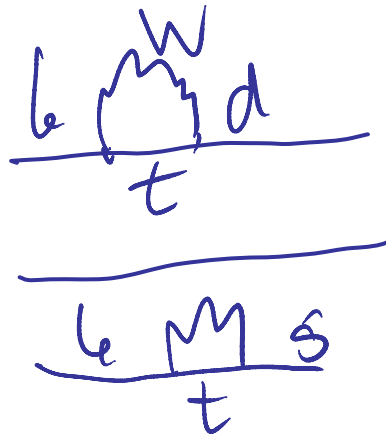
Stagg2+1  
(HPQCD)  
RBC+UKQCD  
IMPORTANCE  
OF SYMMETRIES  
OF CONTINUUM  
THEORY

# **Cons: “Cancellations”**

- **Extra contributions to EWP observables due  $m_{t'}$ ,  $m_{b'}$  need to be cancelled by the heavier “higgs”**
- **Similarly,  $|m_{t'} - m_{b'}| < \sim 60 \text{ GeV}$  for  $m_{t'} \sim O(500 \text{ GeV})$**
- **So how much of a concern should one give to these cons?**
- **Let's just remember  $\Delta(m_n - m_p) < O(0.1\%)$**   
**We understand this now as due ISOSPIN**

# *t & t' Role Reversals in Bd & Bs mixing*

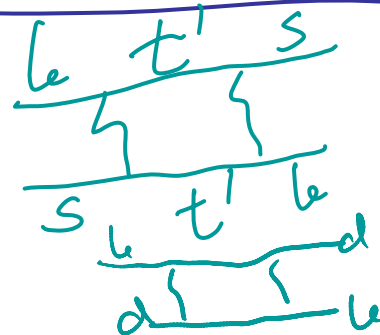
SM3



$V_{td}$  has  
Dominant CP-  
odd phase

Negligible

SM4



**DOMINANT**

small

108

# \*Buras & Guadagnoli correction

They stressed that due increased demands on precision,  $O(5\%)$  (below) should not be ignored anymore

$$|\epsilon_K| = \frac{G_F^2 m_W^2 f_K^2 m_K}{12\sqrt{2}\pi^2 \Delta m_K^{\text{exp}}} \hat{B}_K \kappa_\epsilon \text{Im} \left( \eta_1 S_0(x_c) (V_{cs} V_{cd}^*)^2 + 2\eta_3 S_0(x_c, x_t) V_{cs} V_{cd}^* V_{ts} V_{td}^* + \eta_2 S_0(x_t) (V_{ts} V_{td}^*)^2 \right). \quad (2.3)$$

LMNGHI+AS 108

$$\epsilon_K = \frac{\exp(i\pi/4)}{\sqrt{2}\Delta M_K} \left( \text{Im}(M_{12}^K) + 2\xi \text{Re}(M_{12}^K) \right),$$

$$\xi = \frac{\text{Im}A_0}{\text{Re}A_0}, \quad (9)$$

Increased discrepancy with SM

Knibs, Plehn,  
Spannowsky  
& Tait,  
PRD 107

LEP EW  
Constraints on  
 $m_t$ ,  
 $m_{b'}$ ,  $m_H$

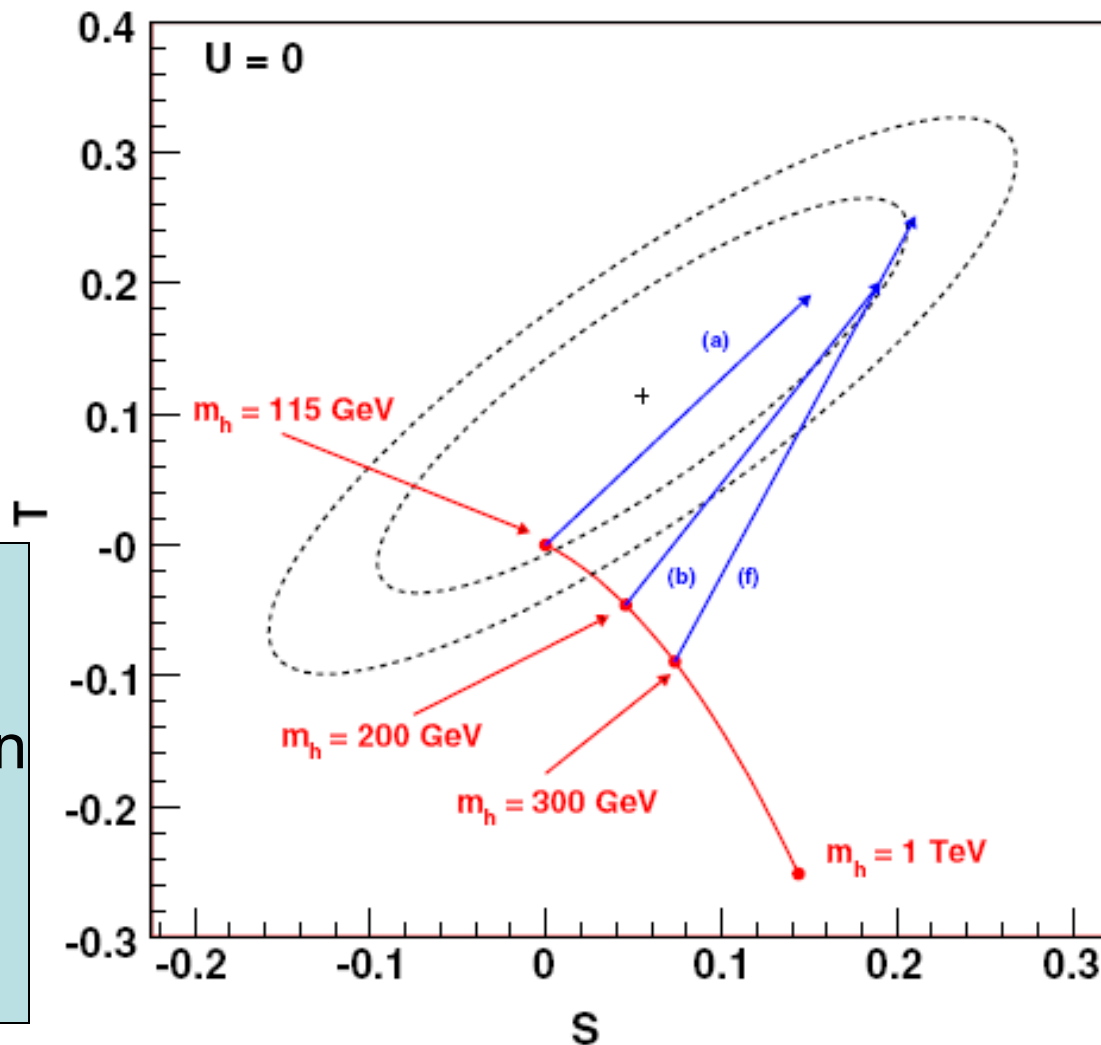


FIG. 2 (color online). The 68% and 95% C.L. constraints on the  $(S, T)$  parameters obtained by the LEP Electroweak Working Group [34,35]. The shift in  $(S, T)$  resulting from increasing the Higgs mass is shown in red (solid line). The shifts in  $\Delta S$  and  $\Delta T$  from a fourth generation with several of the parameter sets given in Table I are shown in blue (arrow lines).

TABLE I. Examples of the total contributions to  $\Delta S$  and  $\Delta T$  from a fourth generation. The lepton masses are fixed to  $m_{\nu_4} = 100$  GeV and  $m_{\ell_4} = 155$  GeV, giving  $\Delta S_{\nu\ell} = 0.00$  and  $\Delta T_{\nu\ell} = 0.05$ . The best fit to data is  $(S, T) = (0.06, 0.11)$  [35]. The standard model is normalized to  $(0, 0)$  for  $m_t = 170.9$  GeV and  $m_H = 115$  GeV. All points are within the 68% C.L. contour defined by the LEP EWWG [35].

Parameter set	$m_{u_4}$	$m_{d_4}$	$m_H$	$\Delta S_{\text{tot}}$	$\Delta T_{\text{tot}}$
(a)	310	260	115	0.15	0.19
(b)	320	260	200	0.19	0.20
(c)	330	260	300	0.21	0.22
(d)	400	350	115	0.15	0.19
(e)	400	340	200	0.19	0.20
(f)	400	325	300	0.21	0.25



# Improved prospects for baryogenesis in SM4

WMAP Data :  $\frac{n_B}{n_\gamma} = \left( 5.1^{+0.3}_{-0.2} \right) 10^{-10}$

But  $\frac{n_{\bar{B}}}{n_\gamma} \sim 0$

$$A_{BAU} \approx \frac{n_B - n_{\bar{B}}}{n_B + n_{\bar{B}}} \approx 100\%$$

$$J_3 = \frac{(m_t^2 - m_c^2)(m_c^2 - m_u^2)(m_t^2 - m_u^2)(m_b^2 - m_s^2)(m_s^2 - m_d^2)(m_b^2 - m_d^2)}{m_W^2} A$$

with  $A \sim 6 \times 10^5$

WITH 4 generations, there are 3 sets of 3 generations. One of them (w/o the 1st gen) has a huge enhancement over  $J_3$ .

$$J^{2,3,4} = (m_{t'}^2 - m_t^2)(m_{t'}^2 - m_c^2)(m_t^2 - m_c^2)(m_b^2 - m_s^2)(m_b^2 - m_s^2) * (m_b^2 - m_s^2) A^{2,3,4}$$

$$\frac{J^{2,3,4}}{J_3} = \frac{m_{t'}^2}{m_c^2} \left( \frac{m_{t'}^2}{m_t^2} - 1 \right) \frac{m_b^4}{m_b^2 m_s^2} \frac{A^{2,3,4}}{A} \sim 10^{14} \frac{A^{2,3,4}}{A} !!!$$