

Hadronic Charm Decays

Jonas Rademacker on behalf of CLEO-c

28 May 2009, FCPC Lake Placid

Outline

- Decay rates
- Dalitz analyses
- Charm for Beauty: Quantum correlations at CLEO-c and their impact on measuring γ .

BR of $D, D_{(s)} \rightarrow PP$

CLEO-c preliminary, full data set

818/pb at $\psi(3770)$

$3 \cdot 10^6$ $D^0 D^0$

$2.4 \cdot 10^6$ $D^+ D^-$

586/pb at $\psi(4170)$

$5.4 \cdot 10^5$ $D_s^+ D_s^-$

TABLE II: Ratios of branching fractions to the corresponding normalization modes $D^0 \rightarrow K^- \pi^+$, $D^+ \rightarrow K^- \pi^+ \pi^+$, and $D_s^+ \rightarrow K_S^0 K^+$, branching fractions results from this analysis, and charge asymmetries \mathcal{A}_{CP} . Uncertainties are statistical error systematic error, and the error from the input branching fractions of normalization modes.

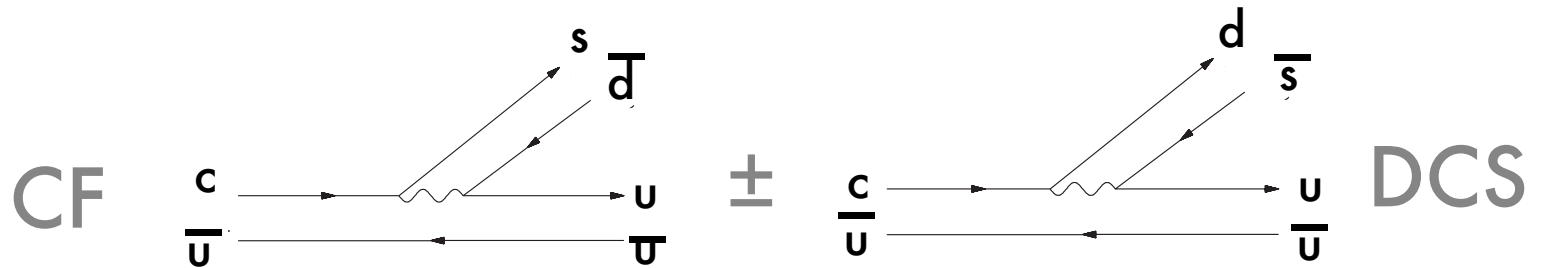
Mode	$\mathcal{B}_{\text{mode}}/\mathcal{B}_{\text{Normalization}}$ (%)	This result \mathcal{B} (%)	\mathcal{A}_{CP} (%)
$D^0 \rightarrow K^+ K^-$	$10.4138 \pm 0.1064 \pm 0.1128$	$0.4052 \pm 0.0041 \pm 0.0044 \pm 0.0080$	
$D^0 \rightarrow K_S^0 K_S^0$	$0.4095 \pm 0.0432 \pm 0.0214$	$0.0159 \pm 0.0017 \pm 0.0008 \pm 0.0003$	
$D^0 \rightarrow \pi^+ \pi^-$	$3.7023 \pm 0.0561 \pm 0.0893$	$0.1441 \pm 0.0022 \pm 0.0035 \pm 0.0029$	
$D^0 \rightarrow \pi^0 \pi^0$	$2.1491 \pm 0.0740 \pm 0.0758$	$0.0836 \pm 0.0029 \pm 0.0030 \pm 0.0017$	
$D^0 \rightarrow K^- \pi^+$	100	3.8910 external input [2]	$0.5 \pm 0.4 \pm 0.9$
$D^0 \rightarrow K_S^0 \pi^0$	$31.0495 \pm 0.2964 \pm 0.7467$	$1.2081 \pm 0.0115 \pm 0.0291 \pm 0.0239$	
$D^0 \rightarrow K_S^0 \eta$	$12.2575 \pm 0.2872 \pm 0.6677$	$0.4769 \pm 0.0112 \pm 0.0260 \pm 0.0094$	
$D^0 \rightarrow \pi^0 \eta$	$1.7714 \pm 0.1481 \pm 0.1047$	$0.0689 \pm 0.0058 \pm 0.0041 \pm 0.0014$	
$D^0 \rightarrow K_S^0 \eta'$	$24.7307 \pm 0.8154 \pm 1.1433$	$0.9623 \pm 0.0317 \pm 0.0445 \pm 0.0190$	
$D^0 \rightarrow \pi^0 \eta'$	$2.4084 \pm 0.2874 \pm 0.1519$	$0.0937 \pm 0.0112 \pm 0.0059 \pm 0.0019$	
$D^0 \rightarrow \eta \eta$	$4.2495 \pm 0.2838 \pm 0.3522$	$0.1653 \pm 0.0110 \pm 0.0137 \pm 0.0033$	
$D^0 \rightarrow \eta \eta'$	$2.7318 \pm 0.6235 \pm 0.2500$	$0.1063 \pm 0.0243 \pm 0.0097 \pm 0.0021$	
$D^+ \rightarrow K^- \pi^+ \pi^+$	100	9.1400 external input [2]	$-0.1 \pm 0.4 \pm 0.9$
$D^+ \rightarrow K_S^0 K^+$	$3.3502 \pm 0.0573 \pm 0.0720$	$0.3062 \pm 0.0052 \pm 0.0066 \pm 0.0066$	$-0.2 \pm 1.5 \pm 0.9$
$D^+ \rightarrow \pi^+ \pi^0$	$1.3208 \pm 0.0382 \pm 0.0443$	$0.1207 \pm 0.0035 \pm 0.0041 \pm 0.0026$	$2.9 \pm 2.9 \pm 0.3$
$D^+ \rightarrow K_S^0 \pi^+$	$16.8160 \pm 0.1239 \pm 0.3679$	$1.5370 \pm 0.0113 \pm 0.0336 \pm 0.0331$	$-1.3 \pm 0.7 \pm 0.3$
$D^+ \rightarrow K^+ \pi^0$	$0.1923 \pm 0.0206 \pm 0.0063$	$0.0176 \pm 0.0019 \pm 0.0006 \pm 0.0004$	$-3.5 \pm 10.7 \pm 0.9$
$D^+ \rightarrow K^+ \eta$	< 0.1442 (90% C.L.)	< 0.0132 (90% C.L.)	
$D^+ \rightarrow \pi^+ \eta$	$3.8538 \pm 0.0895 \pm 0.1916$	$0.3522 \pm 0.0082 \pm 0.0175 \pm 0.0076$	$-2.0 \pm 2.3 \pm 0.3$
$D^+ \rightarrow K^+ \eta'$	< 0.2032 (90% C.L.)	< 0.0187 (90% C.L.)	
$D^+ \rightarrow \pi^+ \eta'$	$5.2061 \pm 0.1762 \pm 0.2565$	$0.4758 \pm 0.0161 \pm 0.0234 \pm 0.0103$	$-4.0 \pm 3.4 \pm 0.6$
$D_s^+ \rightarrow K_S^0 K^+$	100	1.4900 external input [3]	$4.7 \pm 1.8 \pm 0.9$
$D_s^+ \rightarrow \pi^+ \pi^0$	< 2.3492 (90% C.L.)	< 0.0376 (90% C.L.)	
$D_s^+ \rightarrow K_S^0 \pi^+$	$8.4766 \pm 0.7147 \pm 0.1778$	$0.1263 \pm 0.0106 \pm 0.0026 \pm 0.0073$	$16.3 \pm 7.3 \pm 0.3$
$D_s^+ \rightarrow K^+ \pi^0$	$4.2383 \pm 1.4756 \pm 0.2304$	$0.0632 \pm 0.0220 \pm 0.0034 \pm 0.0036$	$-26.6 \pm 23.8 \pm 0.9$
$D_s^+ \rightarrow K^+ \eta$	$11.7933 \pm 2.1753 \pm 0.5888$	$0.1757 \pm 0.0324 \pm 0.0088 \pm 0.0101$	$9.3 \pm 15.2 \pm 0.9$
$D_s^+ \rightarrow \pi^+ \eta$	$123.1123 \pm 4.2907 \pm 6.2133$	$1.8344 \pm 0.0639 \pm 0.0926 \pm 0.1059$	$-4.6 \pm 2.9 \pm 0.3$
$D_s^+ \rightarrow K^+ \eta'$	$11.9866 \pm 3.6840 \pm 0.6158$	$0.1786 \pm 0.0549 \pm 0.0092 \pm 0.0103$	$6.0 \pm 18.9 \pm 0.9$
$D_s^+ \rightarrow \pi^+ \eta'$	$269.8080 \pm 8.9375 \pm 14.0957$	$4.0201 \pm 0.1332 \pm 0.2100 \pm 0.2320$	$-6.1 \pm 3.0 \pm 0.6$

U-spin and $D^0 \rightarrow K_{S,L}\pi^0$

I. Bigi and H. Yamamoto, Physics Letters 349 (1995) 363-366

- $\Gamma(D^0 \rightarrow K_S \pi^0) \neq \Gamma(D^0 \rightarrow K_L \pi^0)$

- $A(D^0 \rightarrow K_{S,L}\pi^0) = A(D \rightarrow \bar{K}^0 \pi^0) \pm A(D \rightarrow K^0 \pi^0)$



U-spin* prediction

- *U-spin: swap $d \leftrightarrow s$ quarks, important e.g. for extracting γ from $B_s \rightarrow KK$, $B_d \rightarrow \pi\pi$

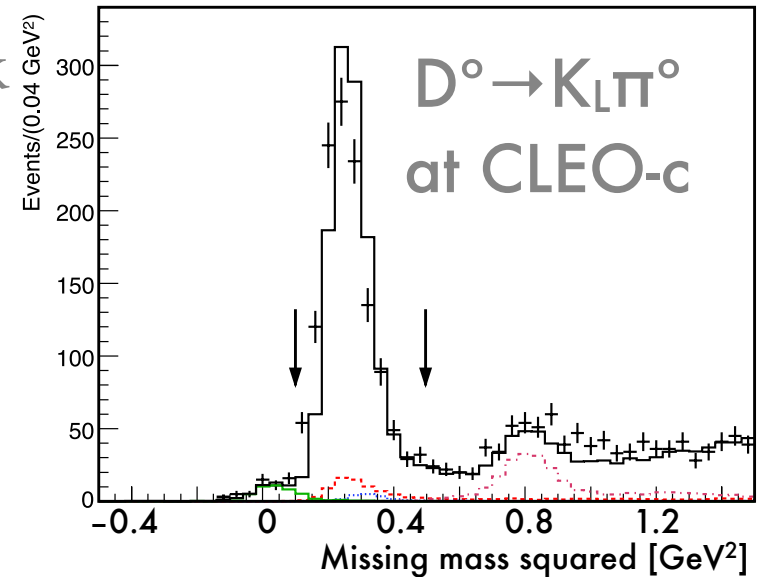
- $$\frac{\Gamma(D^0 \rightarrow K_S \pi^0) - \Gamma(D^0 \rightarrow K_L \pi^0)}{\Gamma(D^0 \rightarrow K_S \pi^0) + \Gamma(D^0 \rightarrow K_L \pi^0)} = -2 \frac{A_{DCS}}{A_{CF}} = 2 \tan^2 \theta_C = 0.109$$

- Challenging in practice - K_L invisible. Can be done at CLEO-c from beam constraints.

$D^0 \rightarrow K_{L,S}\pi^0$, at CLEO-c

4110907-001

- Clean missing mass-squared peak at $m^2_{K^0} = 0.28\text{GeV}^2$
- Lines: MC simulation. Crosses: Data.
- Result



$$\frac{\Gamma(D^0 \rightarrow K_S \pi^0) - \Gamma(D^0 \rightarrow K_L \pi^0)}{\Gamma(D^0 \rightarrow K_S \pi^0) + \Gamma(D^0 \rightarrow K_L \pi^0)} = 0.108 \pm 0.025 \pm 0.024$$

- In good agreement with U-spin prediction of $2\tan^2\theta=0.109$

281/pb at CLEO: PRL **100**, 091801 (2008)

$D^+ \rightarrow K_{L,S}\pi^+$ at CLEO-c

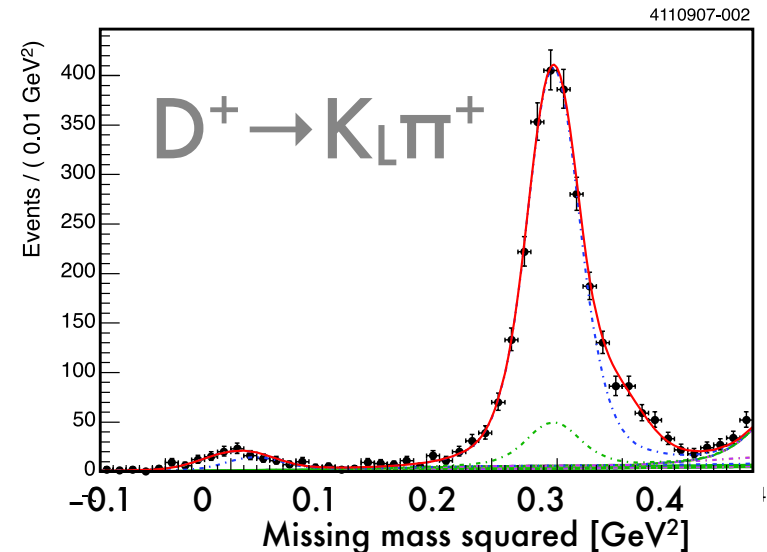
- Similar logic as for D^0 , but no U-spin symmetry.
- Still, possible to estimate effect, expect

$$\frac{\Gamma(D^+ \rightarrow K_S\pi^+) - \Gamma(D^+ \rightarrow K_L\pi^+)}{\Gamma(D^+ \rightarrow K_S\pi^+) + \Gamma(D^+ \rightarrow K_L\pi^+)} \approx 0.04$$

D.-N. Gao, Phys. Lett. B **645**, 59 (2007)

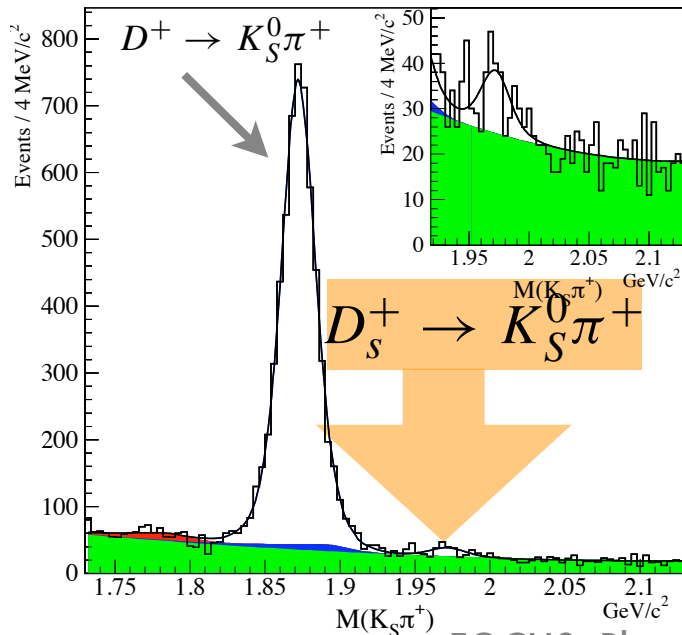
- Result:

$$\frac{\Gamma(D^+ \rightarrow K_S\pi^+) - \Gamma(D^+ \rightarrow K_L\pi^+)}{\Gamma(D^+ \rightarrow K_S\pi^+) + \Gamma(D^+ \rightarrow K_L\pi^+)} = 0.022 \pm 0.016 \pm 0.018$$



281/pb at CLEO: PRL **100**, 091801 (2008)

$D_S^+ \rightarrow K_S \pi^+ (\pi^- \pi^+)$



FOCUS: [Phys.Lett.B660:147-153,2008](#)

Recently discovered by FOCUS

$$\frac{\Gamma(D_S^+ \rightarrow K_S^0 \pi^+)}{\Gamma(D_S^+ \rightarrow K_S^0 K^+)} = 0.104 \pm 0.024 \pm 0.013$$

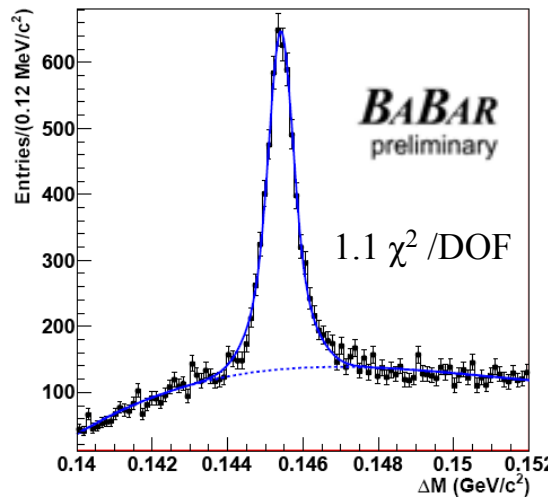
$$\frac{\Gamma(D_S^+ \rightarrow K_S^0 \pi^+ \pi^- \pi^+)}{\Gamma(D_S^+ \rightarrow K_S^0 K^+ \pi^- \pi^+)} = 0.18 \pm 0.04 \pm 0.05$$

$D_S^+ \rightarrow K_S \pi^+$ now confirmed by CLEO: *CLEO-c preliminary, full data set*
 $\Gamma(D_S^+ \rightarrow K_S^0 \pi^+) = (0.1263 \pm 0.0106 \pm 0.0026 \pm 0.0073) \%$

$D^0 \rightarrow V\eta$

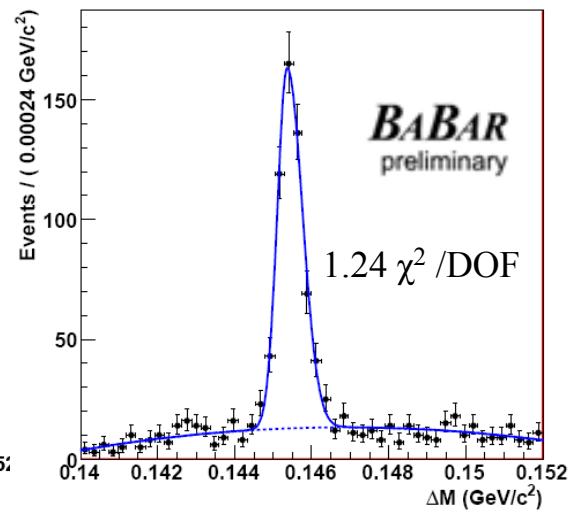
- BaBar analysed 467 fb^{-1} data (on and off resonance)
- About 1 billion D mesons in sample
- Preliminary result shown in April 2009 APS Meeting*:

$D^0 \rightarrow \omega\eta$ **new mode**



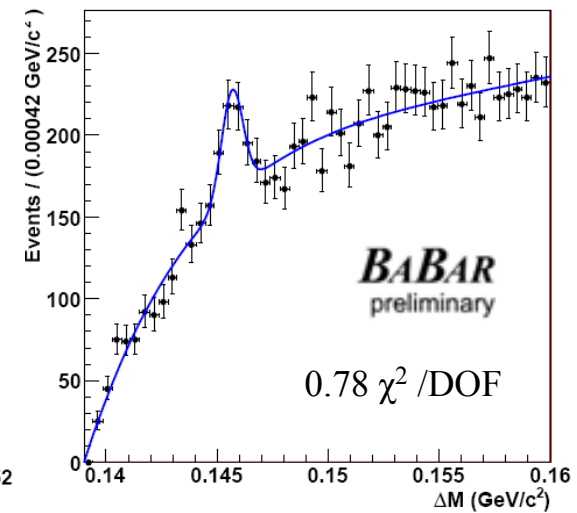
$$N = 4450 \pm 103$$

$D^0 \rightarrow \phi\eta$



$$N = 513 \pm 26$$

$D^0 \rightarrow K^{*0}\eta$ **new mode**



$$N = 117 \pm 37$$

*) Caitlin Malone on behalf of the BaBar Collaboration at APS April Meeting 2009

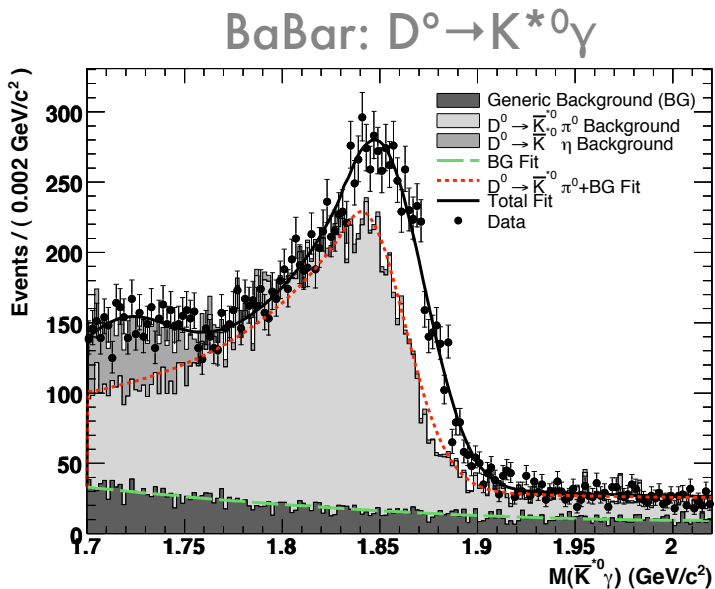
$D^0 \rightarrow V\eta$

Mode	Theory B.F. / 10^{-3} B. Bhattacharya, J. L. Rosner, arXiv: 0812.3167v1 [hep-ph] (2008)		Experiment previously ^[1]	BaBar Results (preliminary) April 08 ^[2]	
	Sol A	Sol B		BF	yield
$D^0 \rightarrow \phi\eta$	0.93 ± 0.09	1.4 ± 0.1	0.14 ± 0.04	$0.21 \pm 0.01 \pm 0.02$	513 ± 26
$D^0 \rightarrow \omega\eta$	1.4 ± 0.09	1.27 ± 0.09		$2.21 \pm 0.08 \pm 0.22$	4450 ± 103
$D^0 \rightarrow K^{*0}\eta$	0.038 ± 0.004	0.037 ± 0.004		$0.048 \pm 0.010 \pm 0.004$	117 ± 37

[1] BELLE: Phys.Rev.Lett.92:101803,2004

[2] Caitlin Malone on behalf of the BaBar Collaboration at APS April Meeting 2009

$D^0 \rightarrow K^{*0} \gamma$ and $D^0 \rightarrow \phi \gamma$



- New CLEO-c study confirms BaBar result.

BaBar:

$$\mathcal{B}(D^0 \rightarrow \bar{K}^{*0} \gamma) = (3.22 \pm 0.20 \pm 0.27) \times 10^{-4}$$

$$\mathcal{B}(D^0 \rightarrow \phi \gamma) = (2.73 \pm 0.30 \pm 0.26) \times 10^{-5}$$

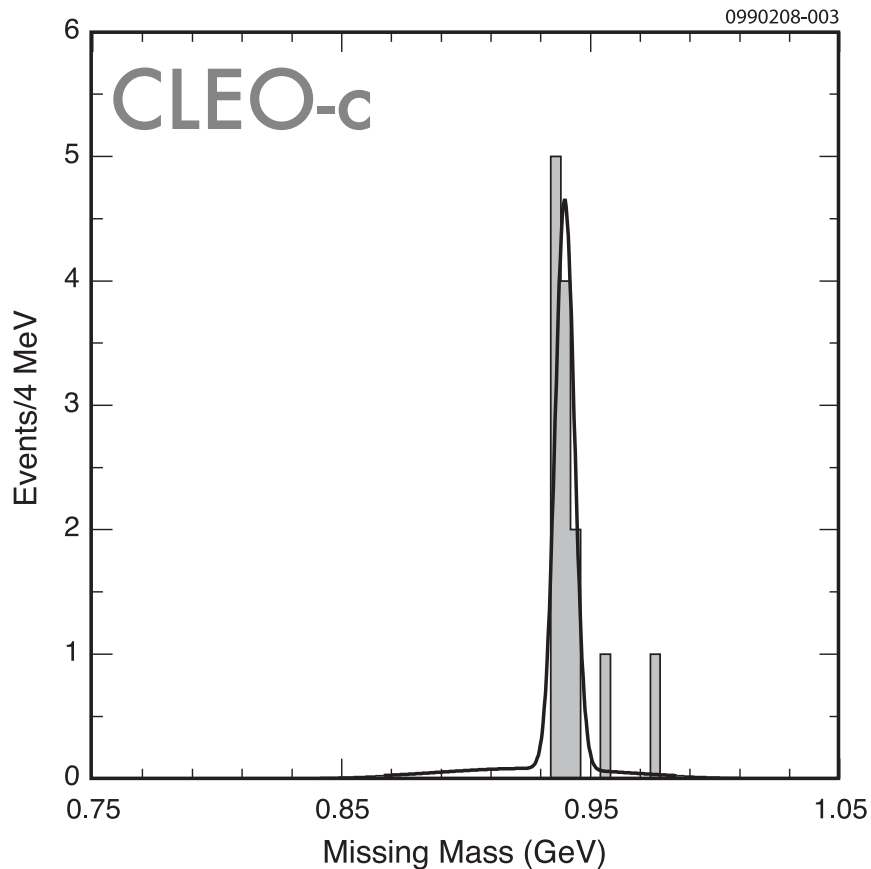
First Observation of $D^0 \rightarrow K^{*0} \gamma$

BaBar, Phys. Rev. D 78, 071101 (2008)

CLEO-c preliminary

Channel	\mathcal{B}
$D^0 \rightarrow \bar{K}^{*0} \gamma$	$(4.37 \pm 0.37 \pm 0.52) \cdot 10^{-4}$
$D^0 \rightarrow \phi \gamma$	$(2.21 \pm 0.95 \pm 0.28) \cdot 10^{-5}$
$D^0 \rightarrow \gamma \gamma$	$< 8.93 \cdot 10^{-6} (90\% CL)$
$D^0 \rightarrow \rho \gamma$	$< 3.63 \cdot 10^{-5} (90\% CL)$
$D^0 \rightarrow \omega \gamma$	$< 3.00 \cdot 10^{-5} (90\% CL)$

First Observation of $D_s^+ \rightarrow p\bar{n}$



CLEO-c: [Phys. Rev. Lett. 100, 181802 \(2008\)](#)

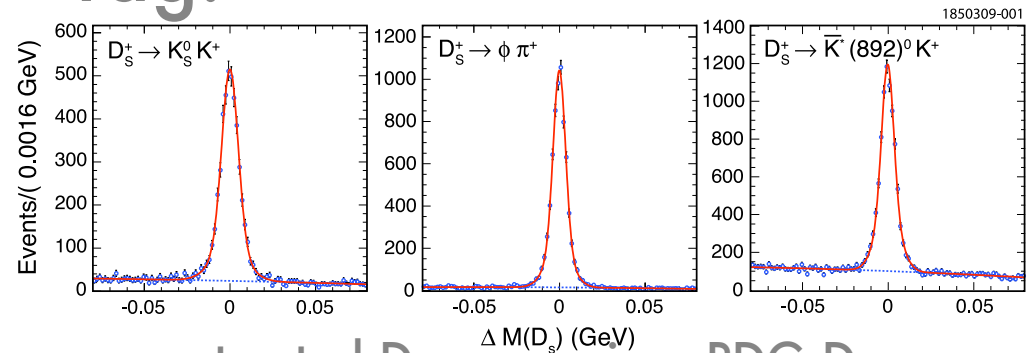
- Only baryonic state kinematically accessible to $D^0 D^+ D_s^+$
- Virtually background-free reconstruction at CLEO-c
- First observation of meson \rightarrow 2 baryons plus nothing else.

$$\mathcal{B}(D_s^+ \rightarrow p\bar{n}) = (1.30 \pm 0.36_{-0.16}^{+0.12}) \times 10^{-3}$$

Inclusive D_s BF

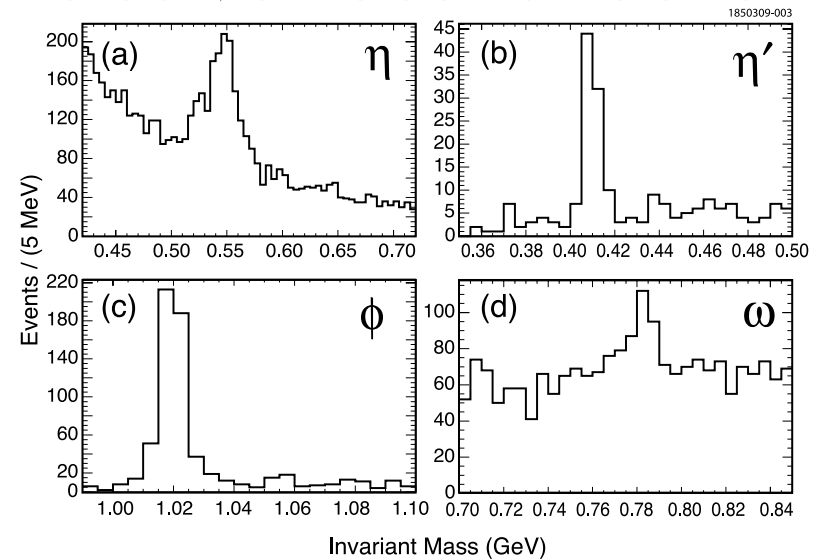
- $e^+e^- \rightarrow \psi(4170) \rightarrow D_s^{+*} D_s^-$
- Fully reconstruct one D_s as tag
- Reconstruction of desired decay product on other side gives absolute, inclusive BF.

Tag:



reconstructed D_s mass minus PDG D_s mass

Inclusive reconstruction:



CLEO: [arXiv:0904.2417 \[hep-ex\]](https://arxiv.org/abs/0904.2417), submitted to PRD

Inclusive D_s BF Results

Mode	Yield(%)	K_L^0 Mode	Yield(%)	$\mathcal{B}(\text{PDG})(\%)$
$D_s^+ \rightarrow \pi^+ X$	$119.3 \pm 1.2 \pm 0.7$			
$D_s^+ \rightarrow \pi^- X$	$43.2 \pm 0.9 \pm 0.3$			
$D_s^+ \rightarrow \pi^0 X$	$123.4 \pm 3.8 \pm 5.3$			
$D_s^+ \rightarrow K^+ X$	$28.9 \pm 0.6 \pm 0.3$			20^{+18}_{-14}
$D_s^+ \rightarrow K^- X$	$18.7 \pm 0.5 \pm 0.2$			13^{+14}_{-12}
$D_s^+ \rightarrow \eta X$	$29.9 \pm 2.2 \pm 1.7$			
$D_s^+ \rightarrow \eta' X$	$11.7 \pm 1.7 \pm 0.7$			
$D_s^+ \rightarrow \phi X$	$15.7 \pm 0.8 \pm 0.6$			
$D_s^+ \rightarrow \omega X$	$6.1 \pm 1.4 \pm 0.3$			
$D_s^+ \rightarrow f_0(980)X, f_0(980) \rightarrow \pi^+\pi^-$	$< 1.3\% (90\% \text{ CL})$			
$D_s^+ \rightarrow K_S^0 X$	$19.0 \pm 1.0 \pm 0.4$	$D_s^+ \rightarrow K_L^0 X$	15.6 ± 2.0	20 ± 14
$D_s^+ \rightarrow K_S^0 K_S^0 X$	$1.7 \pm 0.3 \pm 0.1$	$D_s^+ \rightarrow K_L^0 K_S^0 X$	5.0 ± 1.0	
$D_s^+ \rightarrow K_S^0 K^+ X$	$5.8 \pm 0.5 \pm 0.1$	$D_s^+ \rightarrow K_L^0 K^+ X$	5.2 ± 0.7	
$D_s^+ \rightarrow K_S^0 K^- X$	$1.9 \pm 0.4 \pm 0.1$	$D_s^+ \rightarrow K_L^0 K^- X$	1.9 ± 0.3	
$D_s^+ \rightarrow K^+ K^- X$	$15.8 \pm 0.6 \pm 0.3$			
$D_s^+ \rightarrow K^+ K^+ X$	$< 0.26\% (90\% \text{ CL})$			
$D_s^+ \rightarrow K^- K^- X$	$< 0.06\% (90\% \text{ CL})$			

CLEO result: [arXiv:0904.2417 \[hep-ex\]](https://arxiv.org/abs/0904.2417), submitted to PRD

Exclusive vs inclusive $D_S \rightarrow \omega X$

- Most incl. rates^[1] accounted for by known excl. ones^[2], except, at first: $\sum_i \Gamma_{\text{excl}}(D_S \rightarrow \omega X_i) \sim 0.13 \times \Gamma_{\text{incl}}(D_S \rightarrow \omega X)$
- A closer look at exclusive $D_S \rightarrow \omega X$ BR:

Mode	$\mathcal{B}_{\text{mode}}(\%)$
$D_s^+ \rightarrow \pi^+ \omega$	$0.21 \pm 0.09 \pm 0.01$
$D_s^+ \rightarrow \pi^+ \pi^0 \omega$	$2.78 \pm 0.65 \pm 0.25$
$D_s^+ \rightarrow \pi^+ \pi^+ \pi^- \omega$	$1.58 \pm 0.45 \pm 0.09$
$D_s^+ \rightarrow \pi^+ \eta \omega$	$0.85 \pm 0.54 \pm 0.06$
	< 2.13 (90% CL)
$D_s^+ \rightarrow K^+ \omega$	< 0.24 (90% CL)
$D_s^+ \rightarrow K^+ \pi^0 \omega$	< 0.82 (90% CL)
$D_s^+ \rightarrow K^+ \pi^+ \pi^- \omega$	< 0.54 (90% CL)
$D_s^+ \rightarrow K^+ \eta \omega$	< 0.79 (90% CL)

CLEO Preliminary

[1] CLEO result: [arXiv:0904.2417 \[hep-ex\]](https://arxiv.org/abs/0904.2417), submitted to PRD

[2] Gronau, Rosner, [arXiv:0903.2287](https://arxiv.org/abs/0903.2287), Mar 2009, Submitted to Phys.Rev.D

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$D_s^+ \rightarrow K^+ \pi \omega$	< 0.82 (90% CL)
$D_s^+ \rightarrow K^+ \pi^+ \pi^- \omega$	< 0.54 (90% CL)
$D_s^+ \rightarrow K^+ \eta \omega$	< 0.79 (90% CL)

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The two $D_s \rightarrow \omega X$ decay modes with the largest B.R. were previously unknown

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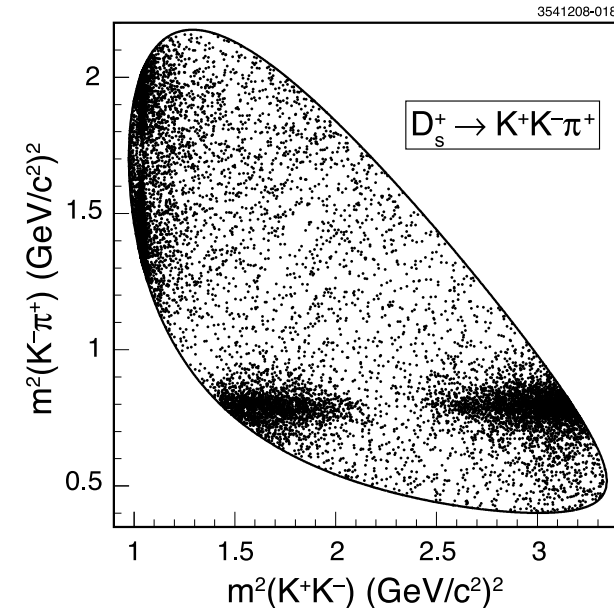
- Now, sum of known $D_s \rightarrow \omega X$ modes = $(5.4 \pm 1.0)\%$, accounts for most of inclusive $\text{BR}(D_s \rightarrow \omega X) = (6.1 \pm 1.4)\%$

[1] CLEO result: [arXiv:0904.2417 \[hep-ex\]](https://arxiv.org/abs/0904.2417), submitted to PRD

[2] Gronau, Rosner, [arXiv:0903.2287](https://arxiv.org/abs/0903.2287), Mar 2009, Submitted to Phys.Rev.D

Dalitz Analyses

- Kinematics of 3-body decay
 $D \rightarrow A, B, C$ fully described by
 $m_{AB}^2 \equiv (p_A + p_B)^2$
 $m_{BC}^2 \equiv (p_B + p_C)^2$.
- Phase-space is flat in m_{AB}^2, m_{BC}^2



- Decay rates:

$$\frac{d^2\Gamma}{dm_{ab}^2 dm_{bc}^2} = \left| a_1 e^{i\delta_1} + a_2 e^{i\delta_2} + a_3 e^{i\delta_3} + \dots \right|^2 \frac{d^2\Phi}{dm_{ab}^2 dm_{bc}^2}$$

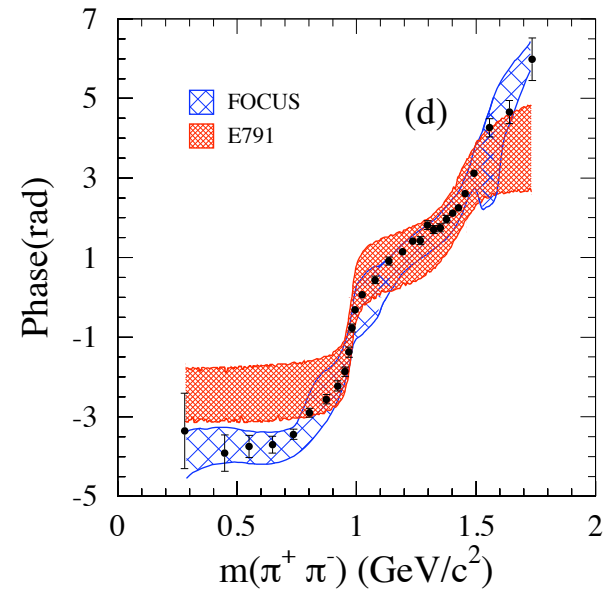
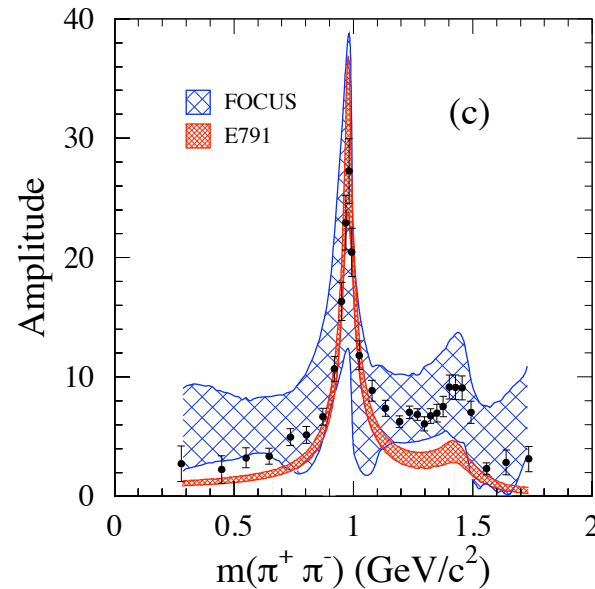
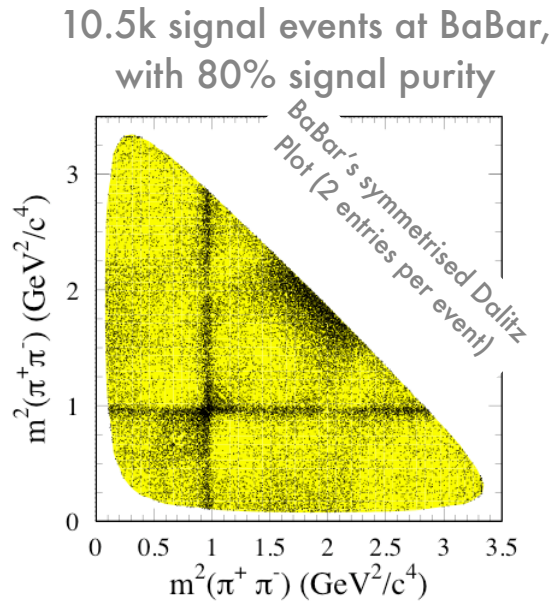
- Strength: Access to **magnitudes**
AND phases of amplitudes.

“Isobar” Model

- Each resonance = Breit Wigner lineshape (or similar) times factors accounting for spin.
- Popular amongst experimentalists, less so amongst theorists: violates unitarity. OK as long as resonances are reasonably narrow, don't overlap too much.
- Alternatives exist, e.g. K-matrix formalism, which respects unitarity.
- General consensus: Isobar OK for P, D wave, but problematic for (usually very broad) S-wave.

$D_s^+ \rightarrow \pi^- \pi^+ \pi^+$

BaBar: arXiv:0808.0971v3 [hep-ex], submitted to PRD



All plots and dots by BaBar:
arXiv:0808.0971v3 [hep-ex]
Red and blue bands based on
FOCUS [2] and E791 [3]

- Dominated by S-wave (fit fraction 83%).
- BaBar: model-independent analysis^[1] of S-wave component. Result compatible with FOCUS (K-matrix)^[2] and E791 (isobar)^[3] analyses.
- Many more results in paper.

[1] Method pioneered by E791: Phys. Rev. D 73, 032004 (2006).

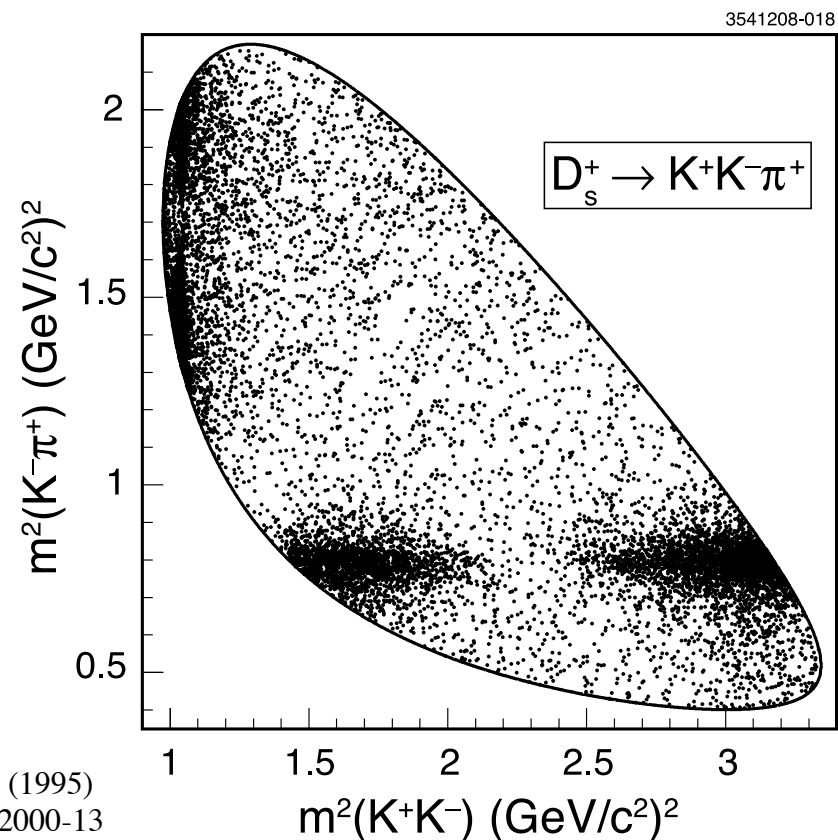
[2] E791: Phys. Rev. Lett. 86, 765 (2001)

[3] FOCUS: Phys. Lett. B 585, 200 (2004)

$D_s^+ \rightarrow K^- K^+ \pi^+$

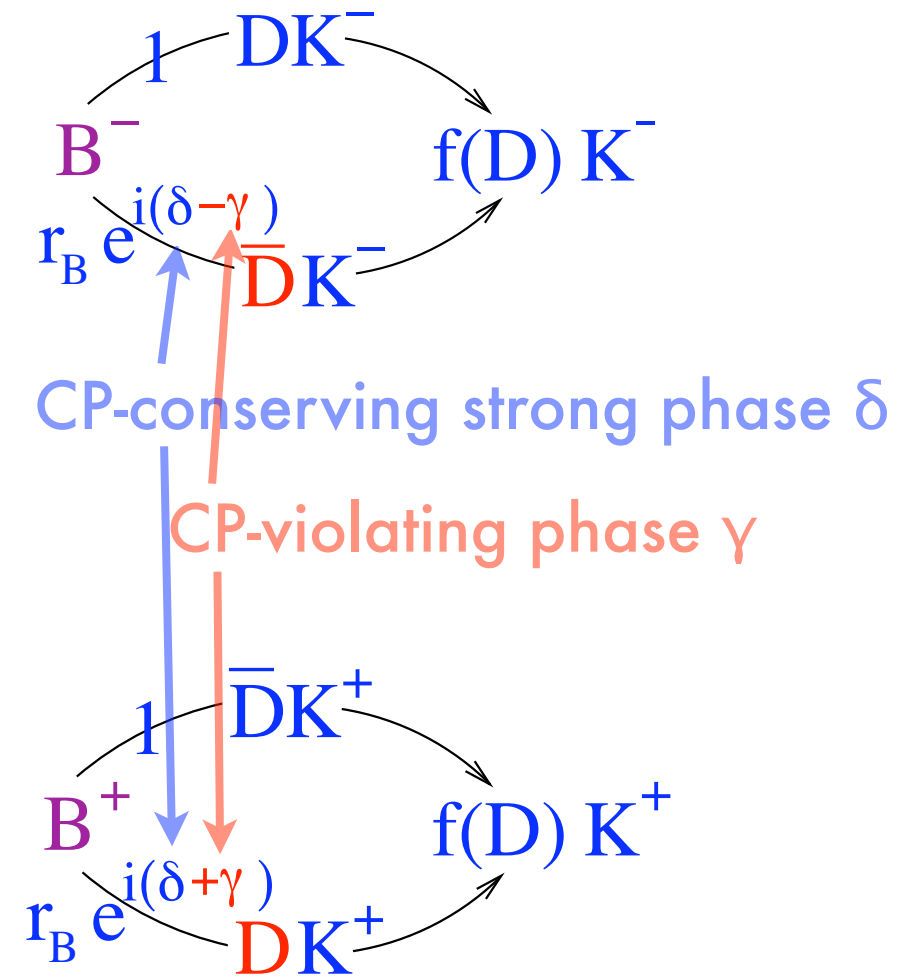
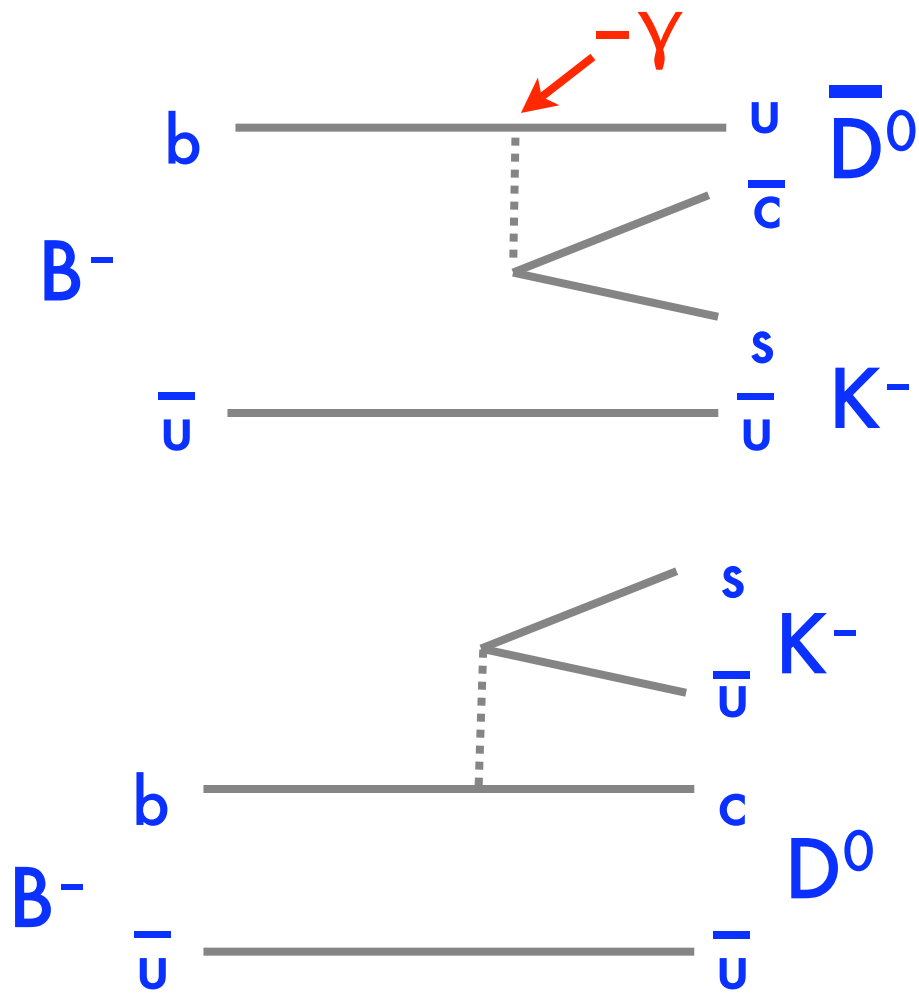
- Isobar fit. Good agreement with previous E687 (701 event) fit^[1].
- Get much-improved fit to CLEO-c data with additional KK S-wave contribution.
- Best results by adding an $f_0(1370)$ resonance.

12k $D_s^+ \rightarrow K^- K^+ \pi^+$ events at CLEO-c
CLEO: PRD 79, 072008 (2009), arXiv:0903.1301



[1] E687: P.L. Frabetti et al. (E687 Collaboration), Phys. Lett., B351, 591 (1995)
see also unpublished FOCUS result: A.M. Rahimi, FERMILAB-THESIS-2000-13
and S. Malvezzi, AIP Conf. Proc. 549, 569 (2002)

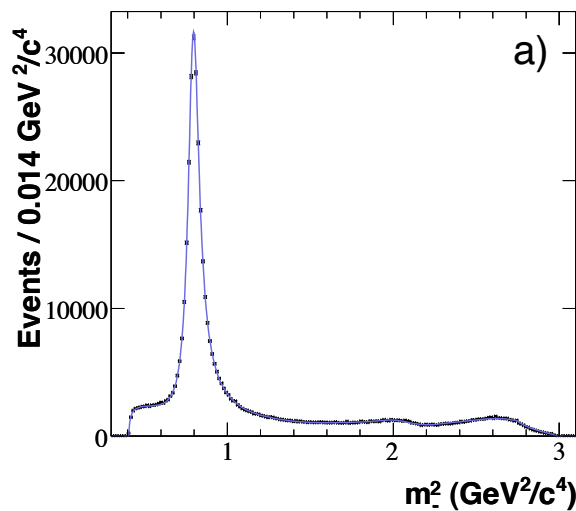
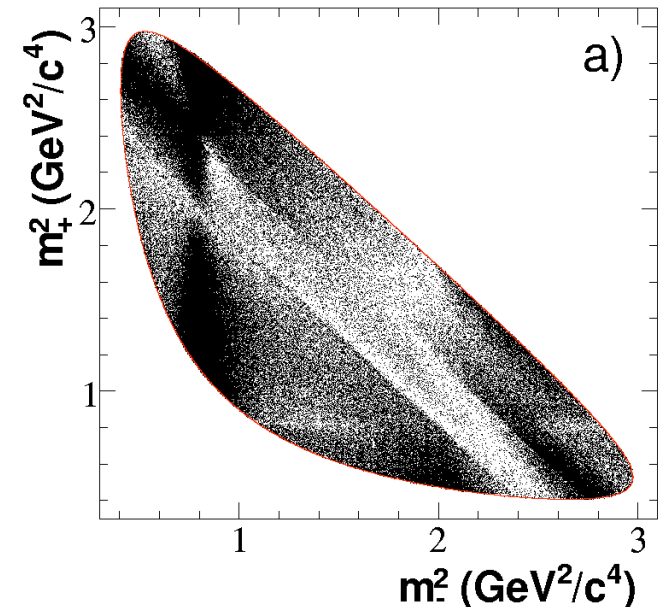
Charm for Bottom: $B^\pm \rightarrow DK^\pm$



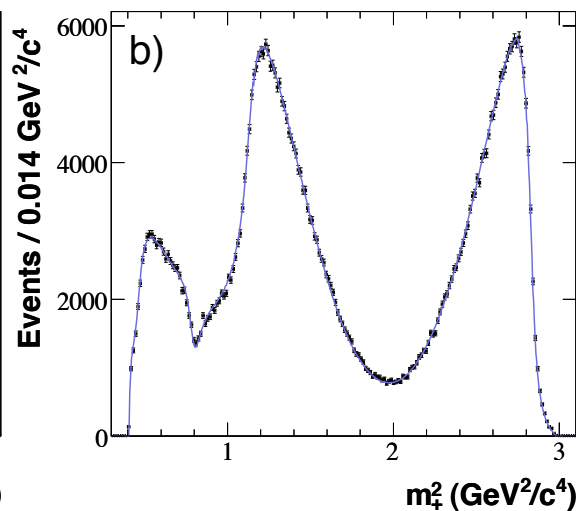
Gronau, Wyler Phys.Lett.B265:172-176,1991, (GLW), Gronau, London Phys.Lett.B253:483-488,1991 (GLW) Atwood, Dunietz and Soni Phys.Rev.Lett. 78 (1997) 3257-3260 (ADS) Giri, Grossman, Sofer and Zupan Phys.Rev. D68 (2003) 054018 Belle Collaboration Phys.Rev. D70 (2004) 072003

BaBar fit to $D^0 \rightarrow K_S \pi \pi$

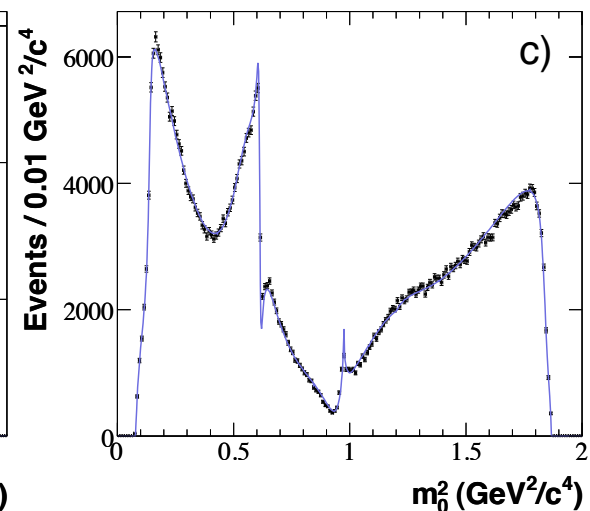
- Fit to 0.5M $D^0 \rightarrow K_S \pi \pi$ events
- K-matrix for $\pi\pi$ S-wave contribution, LASS for $K\pi$ S-wave.
- $\chi^2/\text{ndof} = 1.11$



Jonas Rademacker for CLEO-c

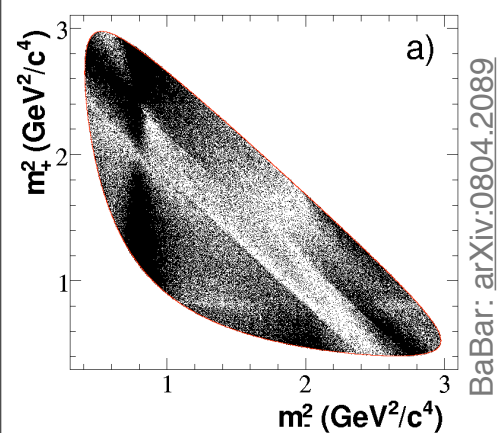


Hadronic Charm

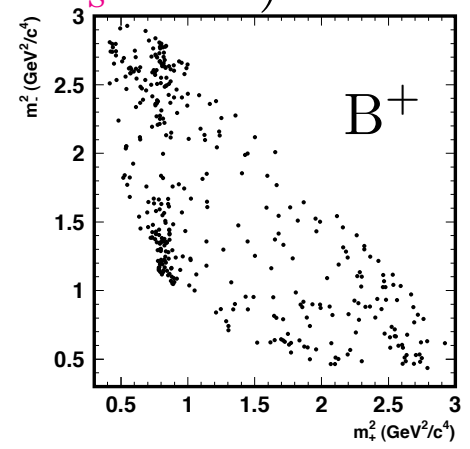
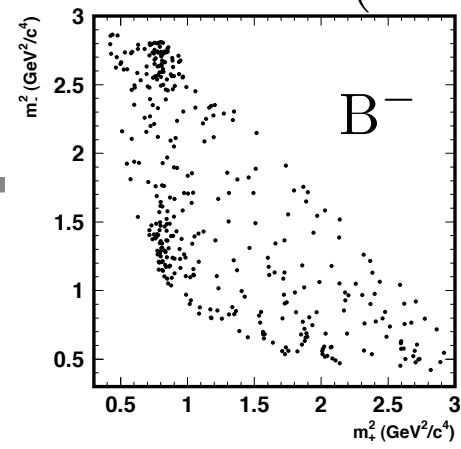


31 May 2009, FPCP 2009 20

Dalitz Plots for γ at Belle&BaBar



D_{flavour}
+ amplitude
model



Combined result (CKM-fitter, summer 08): $\gamma = 70^\circ_{-29^\circ}^{+27^\circ}$

Model required to interpret measured D-Dalitz plot in terms of complex amplitudes (magnitudes *and* phases)

Source of largest systematic uncertainty: Model dependence, ca 7° – 9° .

Would limit LHCb's precision soon.

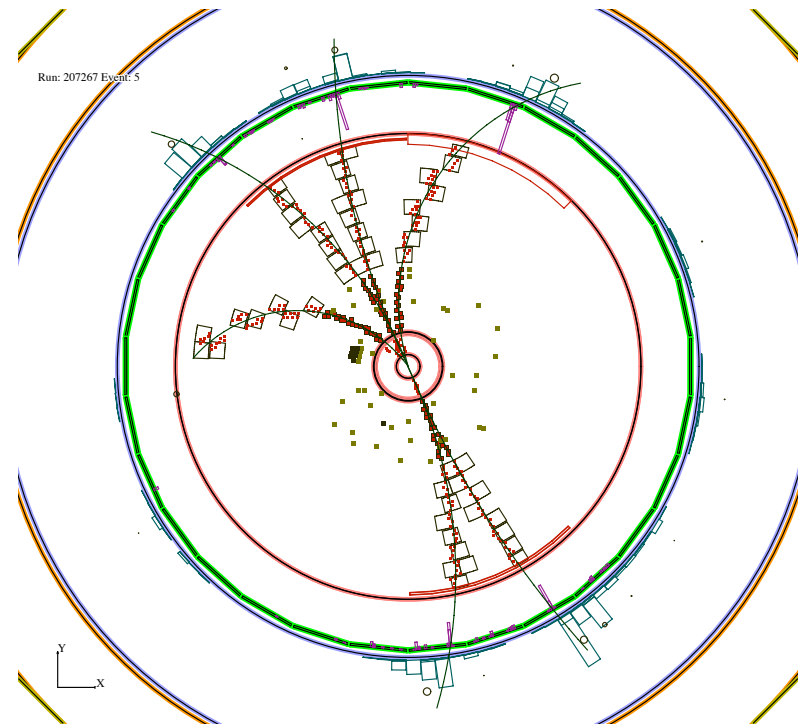
BaBar: Phys.Rev.D78:034023,2008, BELLE: arXiv:0803.3375v1 [hep-ex]
CKMfitter: Eur. Phys. J. C41, 1-131 (2005) [hep-ph/0406184], <http://ckmfitter.in2p3.fr>

CLEO-c

$$e^+e^- \rightarrow \psi(3770) \rightarrow D\bar{D}$$

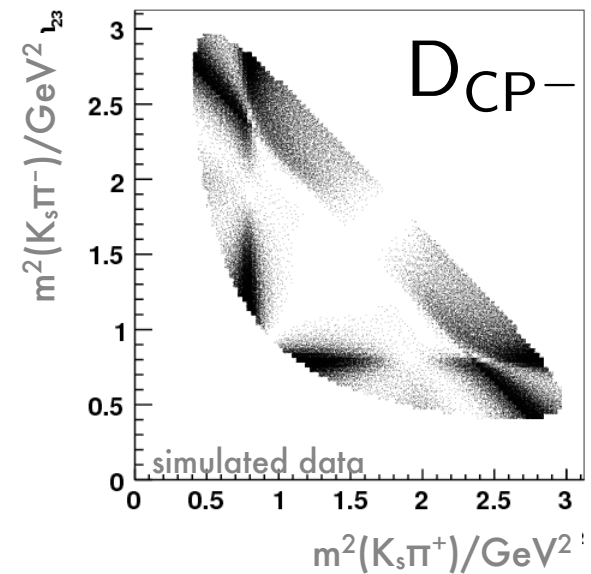
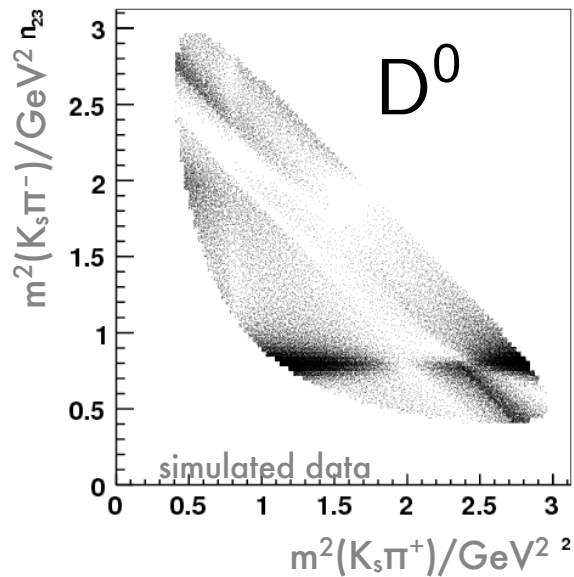
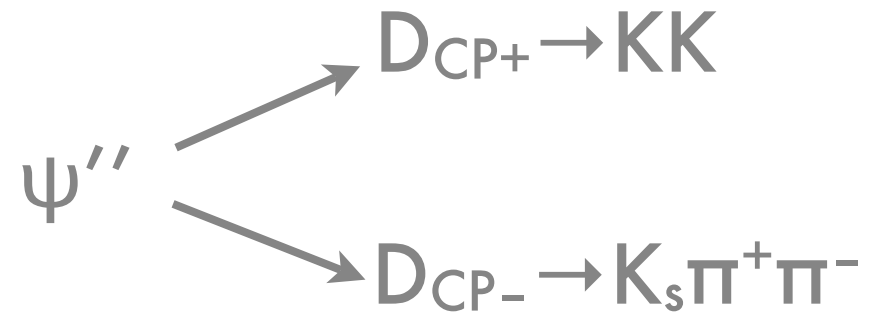
- Threshold production of correlated $D\bar{D}$.
- Final state must be CP-odd,
- ...and flavour-neutral.
- That gives us access to both amplitude and phase across the Dalitz plot.

CLEAN-c

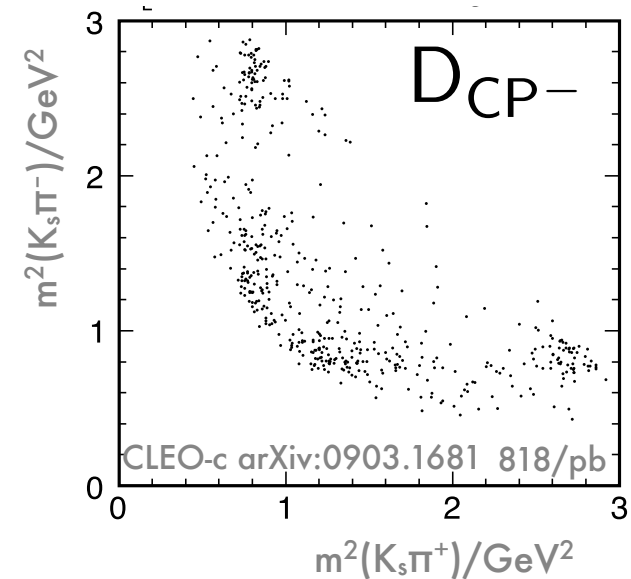
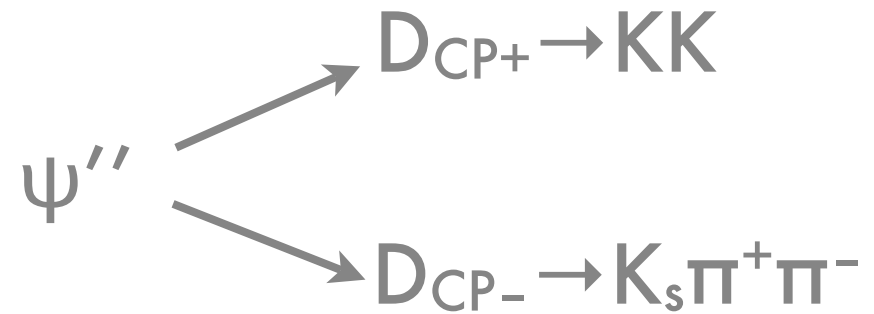
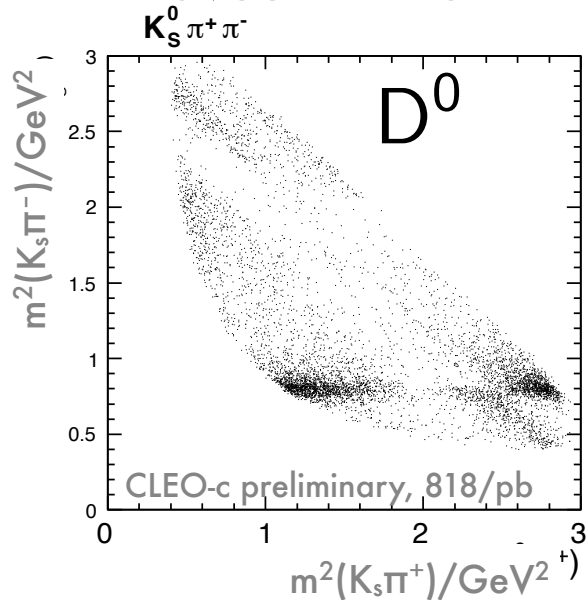
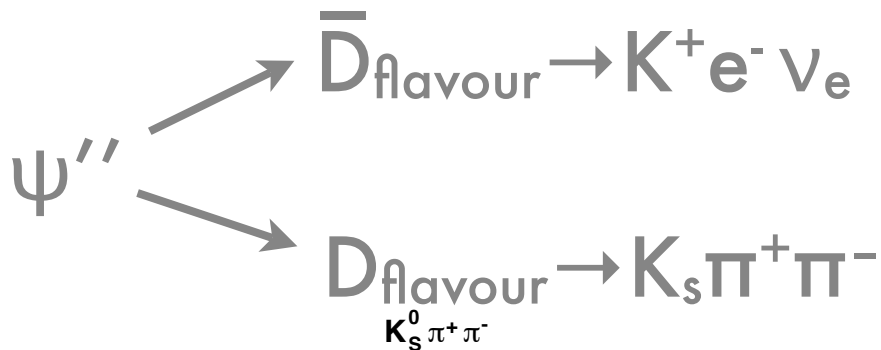


$$\psi(3770) \rightarrow D^0(K_S\pi^+\pi^-)\bar{D}^0(K^+\pi^-)$$

CP and flavour tagged D^0



CP and flavour tagged D^0 at CLEO



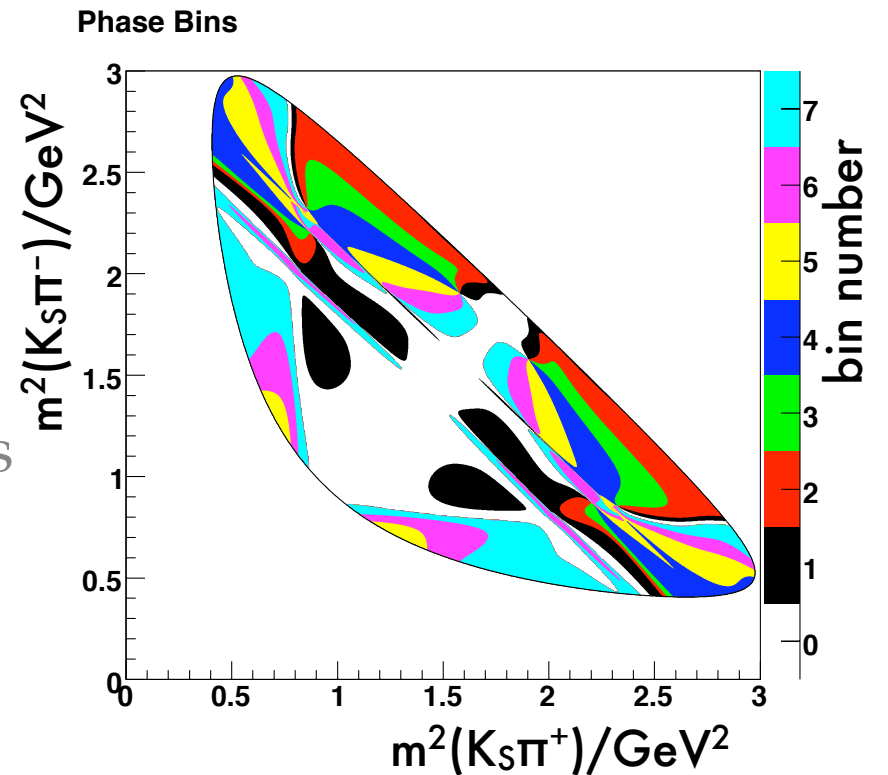
CLEO-c's input to γ

- CLEO-c's input is concerned with δ_D , the phase difference between $A(D^0 \rightarrow K_S \pi^+ \pi^-)$ and $A(\bar{D}^0 \rightarrow K_S \pi^+ \pi^-)$ at a point on the Dalitz plot.
- Measure the cosine and sine of this phase, averaged over bins:

$$c_i = \langle \cos(\delta_D) \rangle_i, \quad s_i = \langle \sin(\delta_D) \rangle_i$$
- This input allows model-independent γ measurement.

Giri, Grossmann, Soffer, Zupan, Phys Rev D 68, 054018 (2003).

Binning used at CLEO-c*



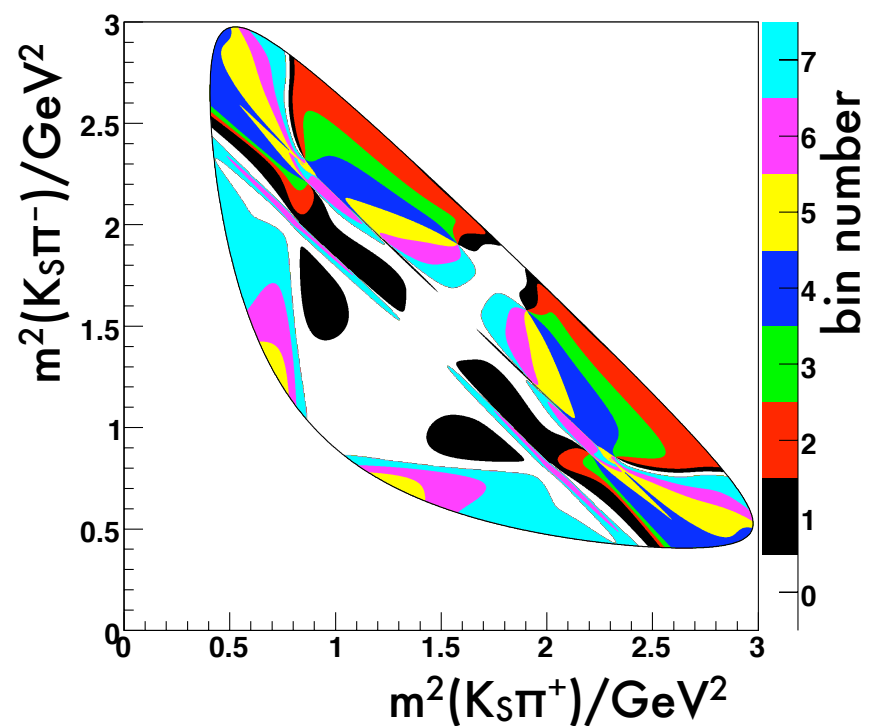
*bin width uniform in δ_D based on BaBar model PRL 95 (2005) 121802
 31 May 2009, FPCP 2009 25

Optimal binning

- Best γ sensitivity if phase difference δ_D is as constant as possible over each bin^[1].
- Plot shows CLEO-c's 8 bins, uniform in δ_D , (based on BaBar isobar model*).
- Choice of model will not bias result. (At worst a bad model would reduce the statistical precision of the result.)

[1] Bondar, Poluektov hep-ph/0703267v1 (2007)

Binning at CLEO-c based on BaBar model*

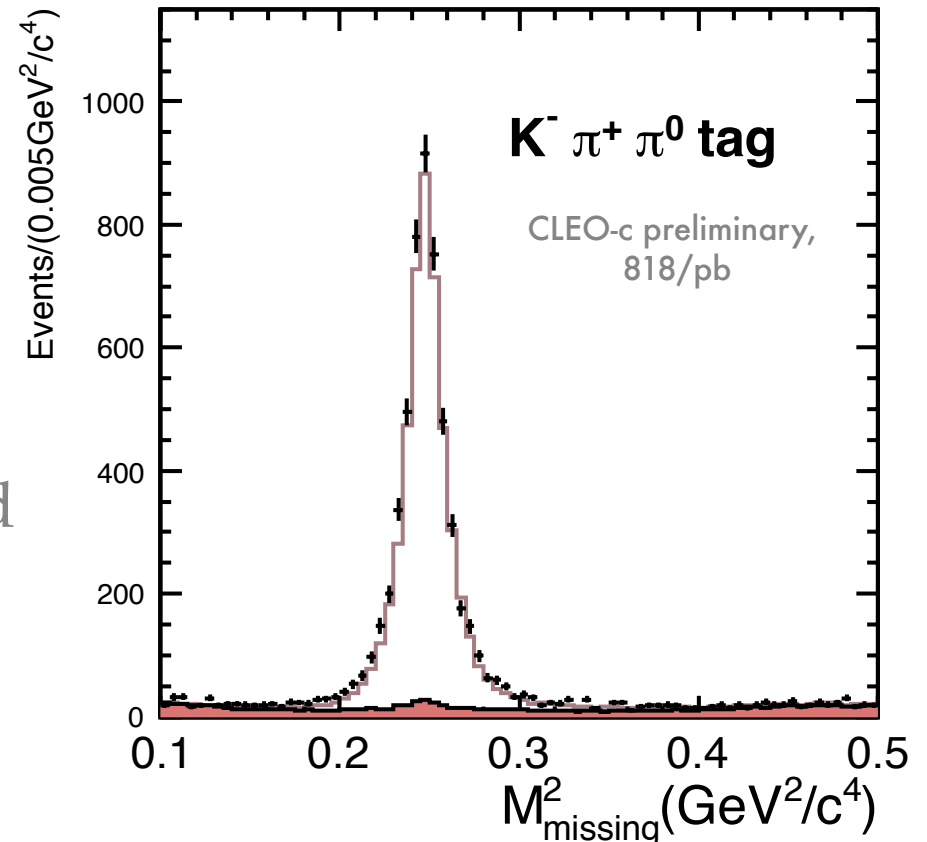


*model = BaBar PRL 95 (2005) 121802

CP-even $K_L\pi\pi \approx$ CP-odd $K_S\pi\pi$

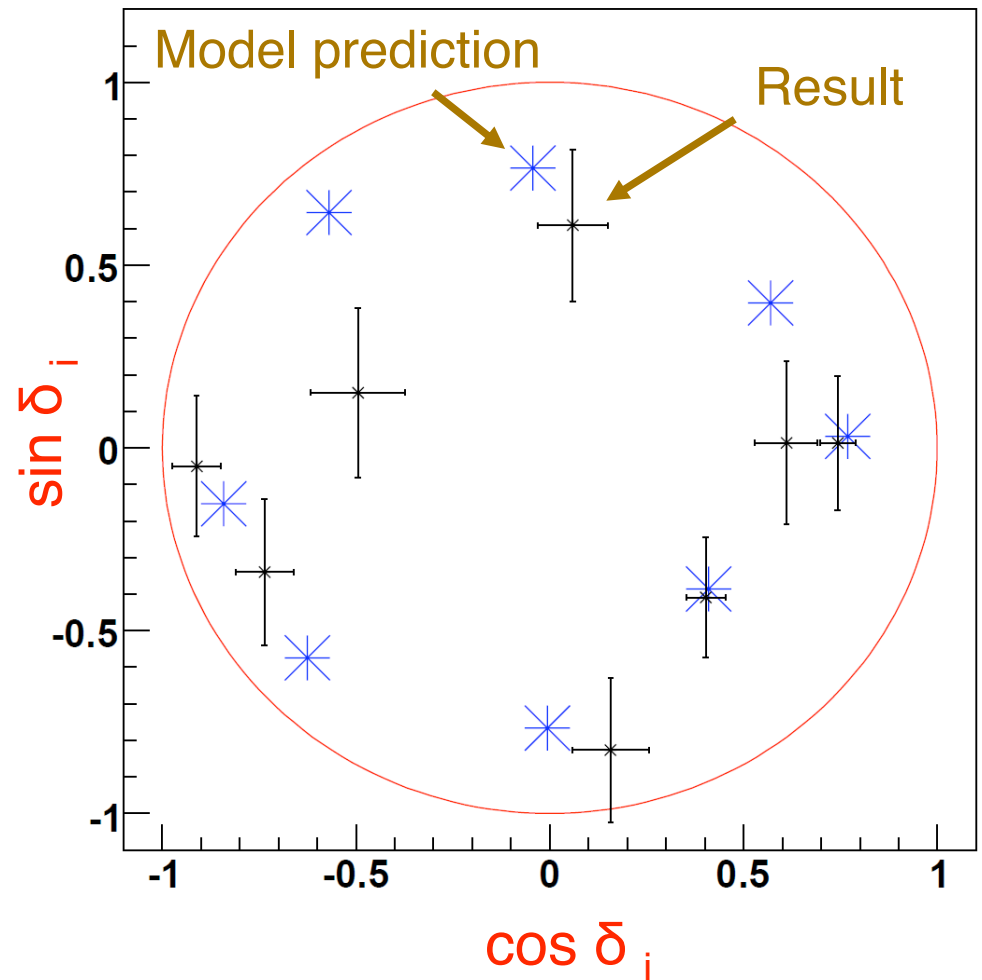
- CLEO-c's clean environment allows the reconstruction of K_L from kinematic constraints.
- Significantly increases statistics.
- There is price to pay: A $\mathcal{O}(\tan^2\theta_C)$ model-dependent correction. Carefully evaluated (small) systematic uncertainty.

Overlaying Data (black) and MC (red) for missing M^2 in K_L reconstruction in $K_L\pi^+\pi^-$ vs $K^-\pi^+\pi^0$



CLEO-c results

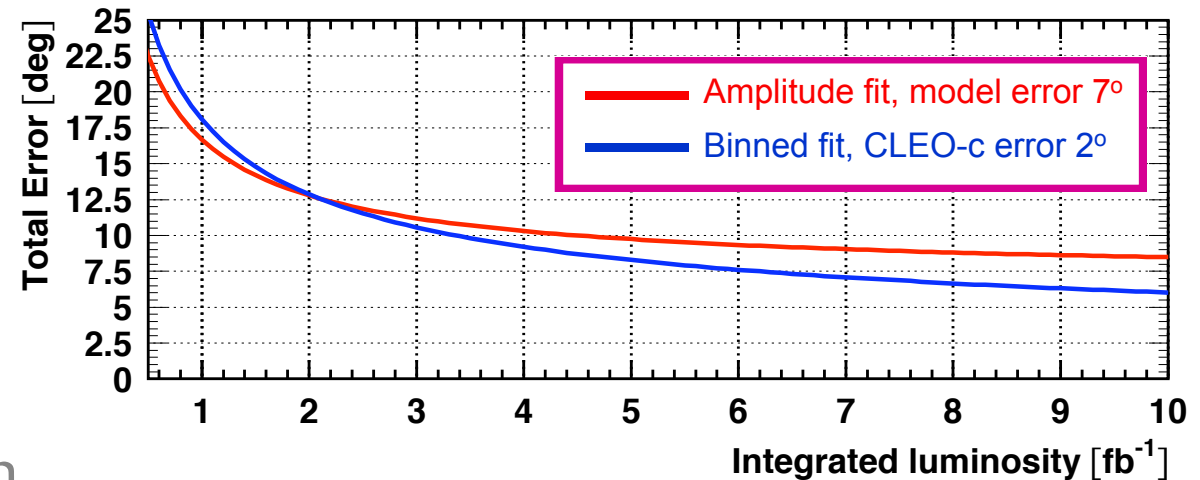
- 818 / fb at CLEO-c
- 20k flavour tagged events (for magnitude of $A(D^0 \rightarrow K_S \pi^+ \pi^-)$)
- 1.6 k CP-tagged events (for c_i extraction)
- 1.3k $K_{L,S} \pi \pi$ vs $K_S \pi \pi$ (for c_i and s_i extraction)
- S/B between 10 and 100, depending on tag mode.



Result = CLEO-c arXiv:0903.1681v1 [hep-ex], submitted to PRD
model = BaBar PRL 95 (2005) 121802

Impact on γ from $B^\pm \rightarrow D(K_S \pi \pi) K^\pm$

- Replace 7° model systematic on γ from $B^\pm \rightarrow D(K_S \pi \pi) K^\pm$ with $\sigma_{\text{CLEO-input}}(\gamma) \sim 1.7^\circ$
- Significant reduction in BaBar/BELLE's systematic.
- Especially important for future flavour experiments, which will be systematics limited.



Error at the end of baseline LHCb (10 fb⁻¹) for γ from $B^\pm \rightarrow D(K_S \pi \pi) K^\pm$:

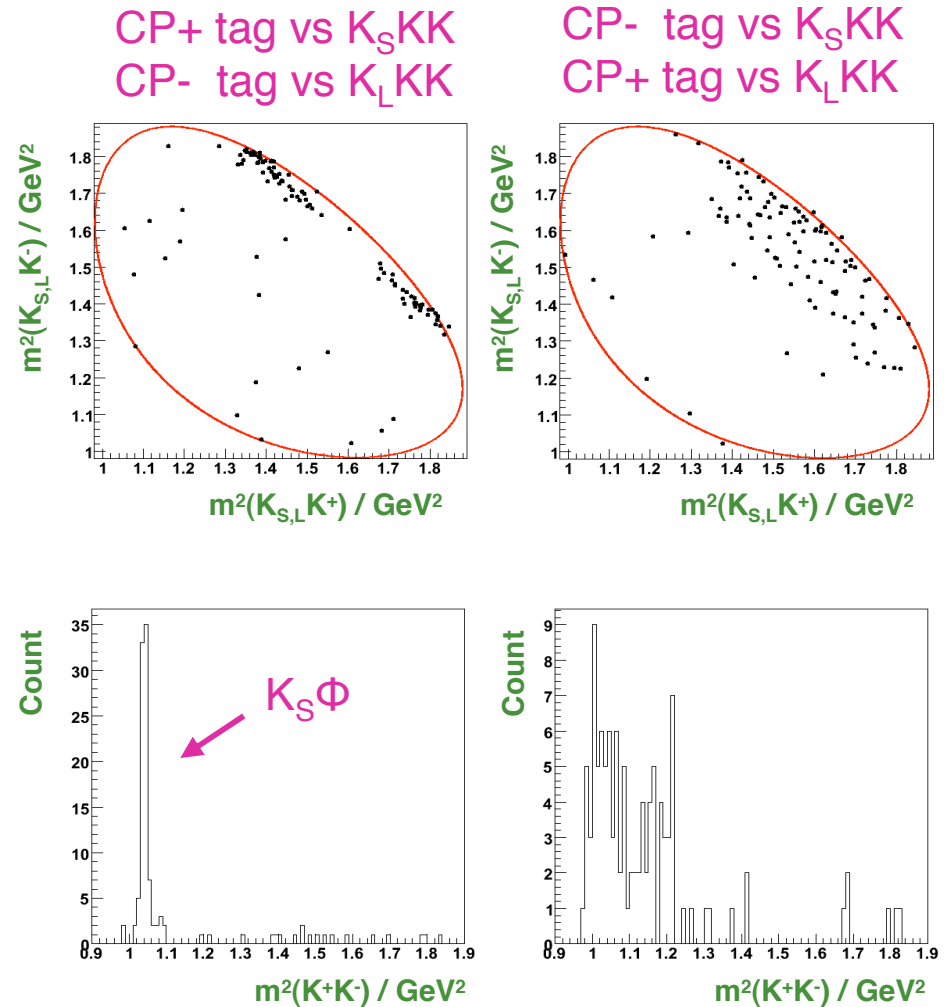
8.5°(amplitude model);

6°(binned, with CLEO-c input)

(numbers for $r_B=0.1$)

Extend to $B^+ \rightarrow (D^0 \rightarrow K_S K K) K^+$

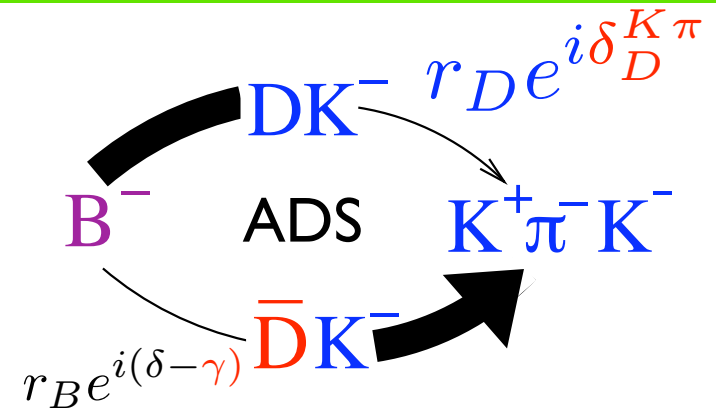
- Pioneered at BaBar: PRD78:034023 (2008)
- CLEO-c input: ca 550 quantum-correlated events.
- Results from CLEO-c soon...



CLEO-c preliminary

γ from 2-body decays, ADS

- Extract γ from 2-body decays^[1]
- Particularly powerful: “ADS” modes with **large interference terms** (when $r_D \sim r_B$).



$$\Gamma(B^- \rightarrow (K^+ \pi^-)_D K^-) \propto r_B^2 + (r_D^{K\pi})^2 + 2r_B r_D^{K\pi} \cdot \cos(\delta_B + \delta_D^{K\pi} - \gamma)$$

$$\Gamma(B^+ \rightarrow (K^- \pi^+)_D K^+) \propto r_B^2 + (r_D^{K\pi})^2 + 2r_B r_D^{K\pi} \cdot \cos(\delta_B + \delta_D^{K\pi} + \gamma)$$

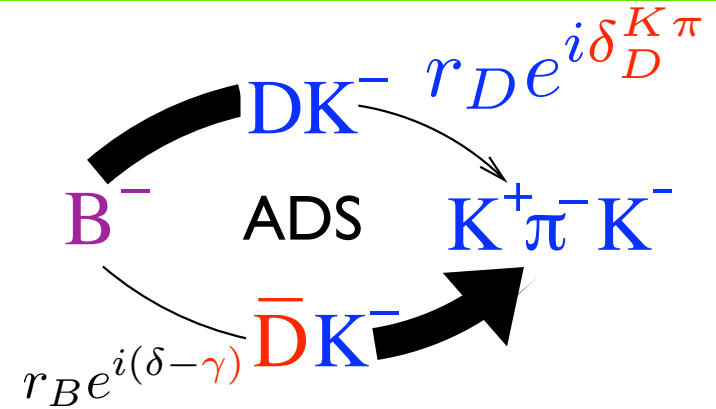
- CLEO-c's provides as input: $\delta_D^{K\pi} = 22^\circ + 11^\circ + 9^\circ$ PRL 100, 221801 (2008), $-12^\circ - 11^\circ$ PRD 78, 012001 (2008)
- Also important input for D-mixing! *

* Result shown includes external input on γ, γ' from mixing measurements. Without external inputs: $\cos \delta = 1.03_{-0.17}^{+0.31} \pm 0.06$

Gronau, Wyler Phys.Lett.B265:172-176,1991, (GLW), Gronau, London Phys.Lett.B253:483-488,1991 (GLW) Atwood, Dunietz and Soni Phys.Rev.Lett. 78 (1997) 3257-3260 (ADS) Giri, Grossman, Soffer and Zupan Phys.Rev. D68 (2003) 054018 Belle Collaboration Phys.Rev. D70 (2004) 072003

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CLEO-c $\delta_D^{K\pi}$ result based on 1/3 of data set update with full 818/fb and more tag modes, soon.

CLEO-c provides as input: $\delta_D^{K\pi} = 22^{+11}_{-12} + 9^{+11}_{-11}$ PRL 100, 221801 (2008), PRD 78, 012001 (2008)

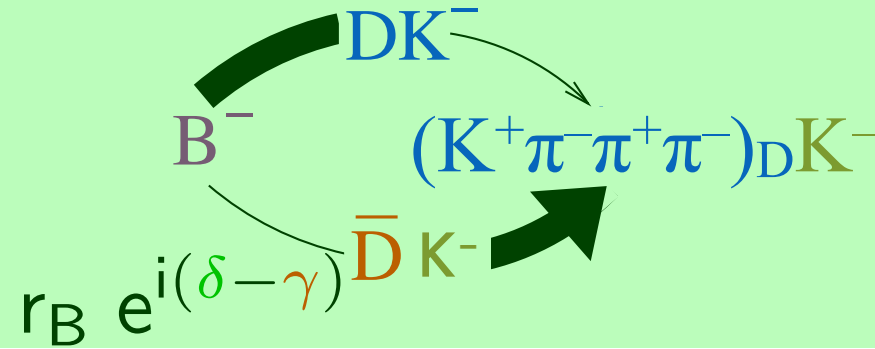
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Coherence Factor Analysis of:

Atwood, Soni: Phys.Rev. D68 (2003) 033003



- Treat $K3\pi$ like two-body decay with single effective strong phase δ_D .
- New parameter: Coherence factor $R < 1$.

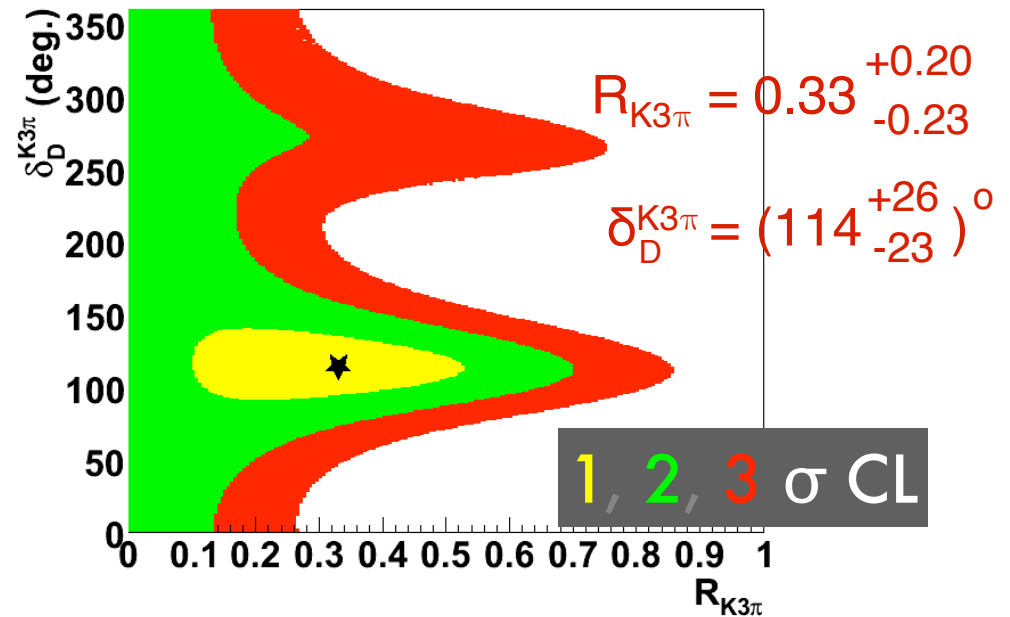
$$\Gamma(B^- \rightarrow (K^+ 3\pi)_D K^-) \propto r_B^2 + (r_D^{K3\pi})^2 + 2R_{K3\pi} r_B r_D^{K3\pi} \cdot \cos(\delta_B + \delta_D^{K3\pi} - \gamma)$$

- CLEO-c's coherent $\psi(3770) \rightarrow DD$ events allow measurement of R , δ_D - important input for LHCb

Double Tag Rate	Sensitive To
$K^\pm \pi^\mp \pi^+ \pi^-$ vs. $K^\pm \pi^\mp \pi^+ \pi^-$	$(R_{K3\pi})^2$
$K^\pm \pi^\mp \pi^+ \pi^-$ vs. CP	$R_{K3\pi} \cos(\delta^{K3\pi})$
$K^\pm \pi^\mp \pi^+ \pi^-$ vs. $K^\pm \pi^\mp$	$R_{K3\pi} \cos(\delta^{K\pi} - \delta^{K3\pi})$

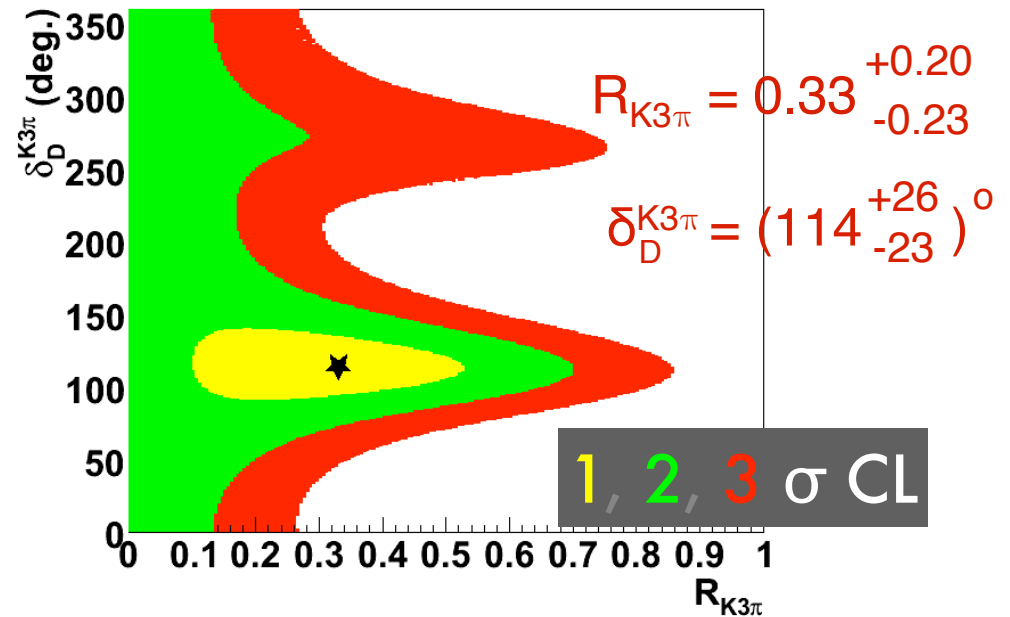
$K\pi\pi\pi$ coherence factor

- Low value preferred. This channel **on its own would** not be very sensitive to γ .
- For a **combined analysis** of $B^\pm \rightarrow DK^\pm$ modes, this provides powerful constraints.



$K\pi\pi\pi$ coherence factor

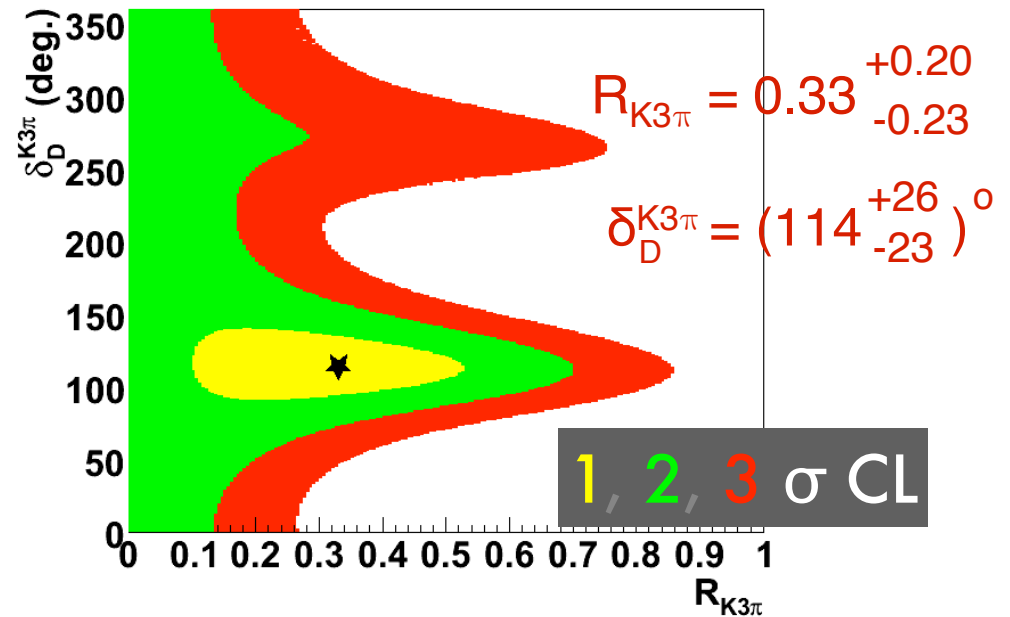
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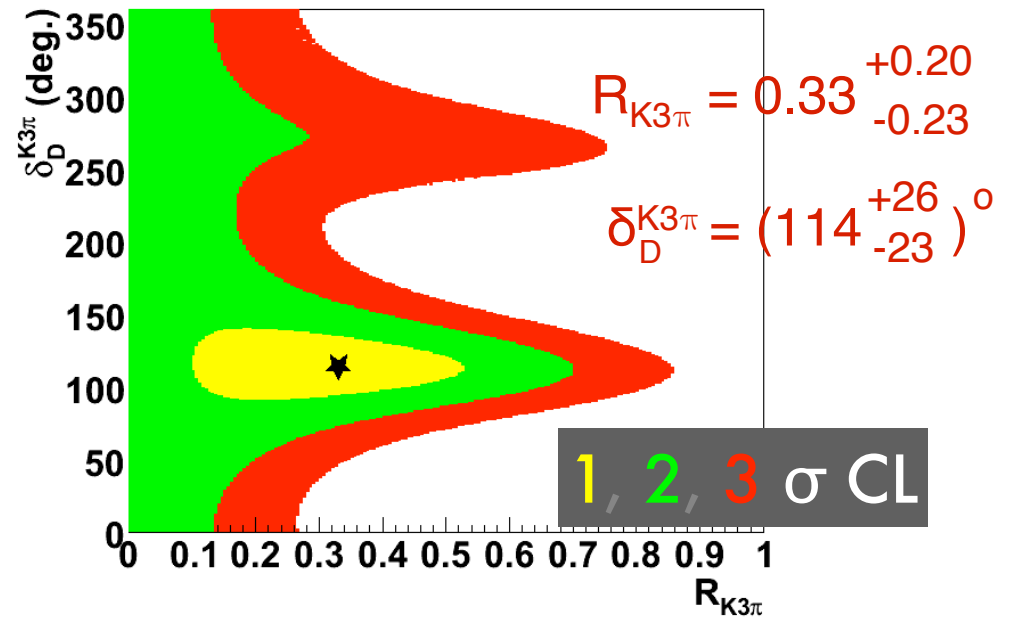
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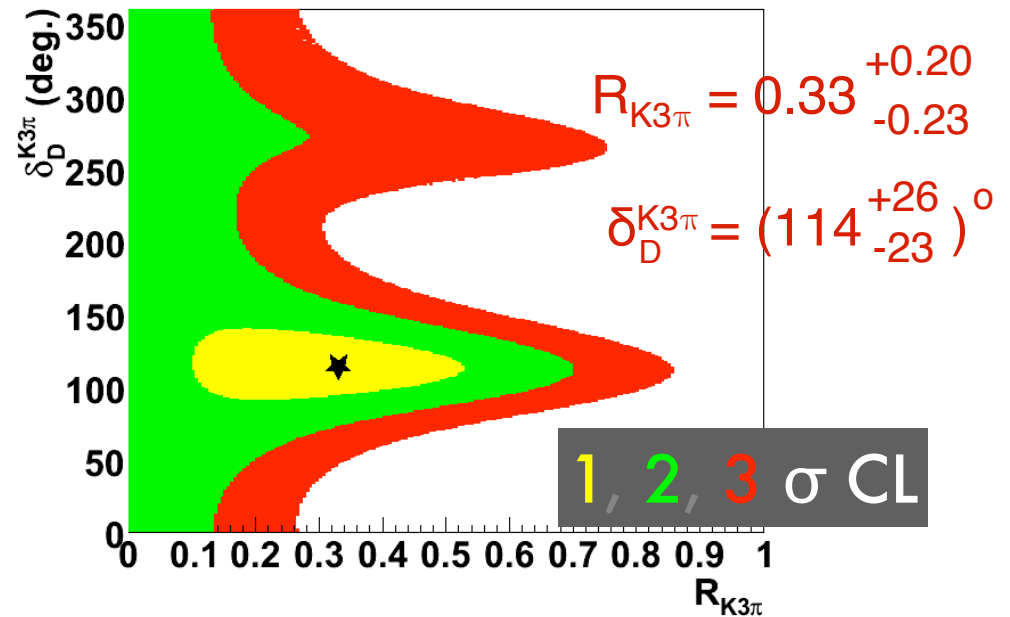
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$$\Gamma(B^- \rightarrow (K^+ 3\pi)_D K^-) \propto \underbrace{r_B^2}_{\text{badly known}} + (r_D^{K3\pi})^2 + \cancel{2R_{K3\pi} r_B r_D^{K3\pi} \cdot \cos(\delta_B + \delta_D^{K3\pi} - \gamma)}$$

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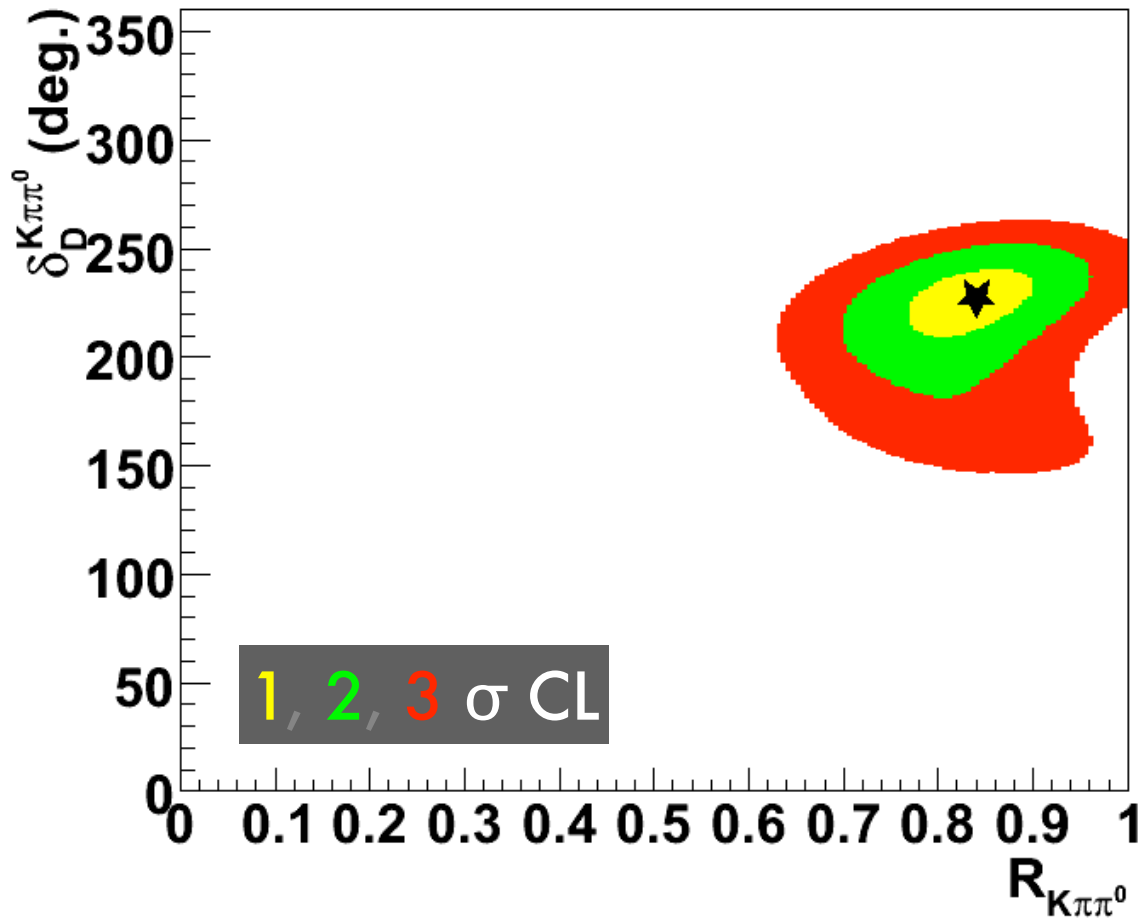


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- At LHCb, using $B^\pm \rightarrow D(hh)K^\pm$, $B^\pm \rightarrow D(K\pi\pi\pi)K^\pm$, for 2/fb (average year): This input improves $\sigma(\gamma)$ from 9.5° to 7.9° .

(typical values used - exact size of improvement depends on input parameters and can be larger).

$K\pi\pi^0$ Coherence Factor



$$R_{K\pi\pi^0} = 0.84 \pm 0.07$$

$$\delta_{K\pi\pi^0}^D = (227^{+14}_{-17})^\circ$$

Very coherent!

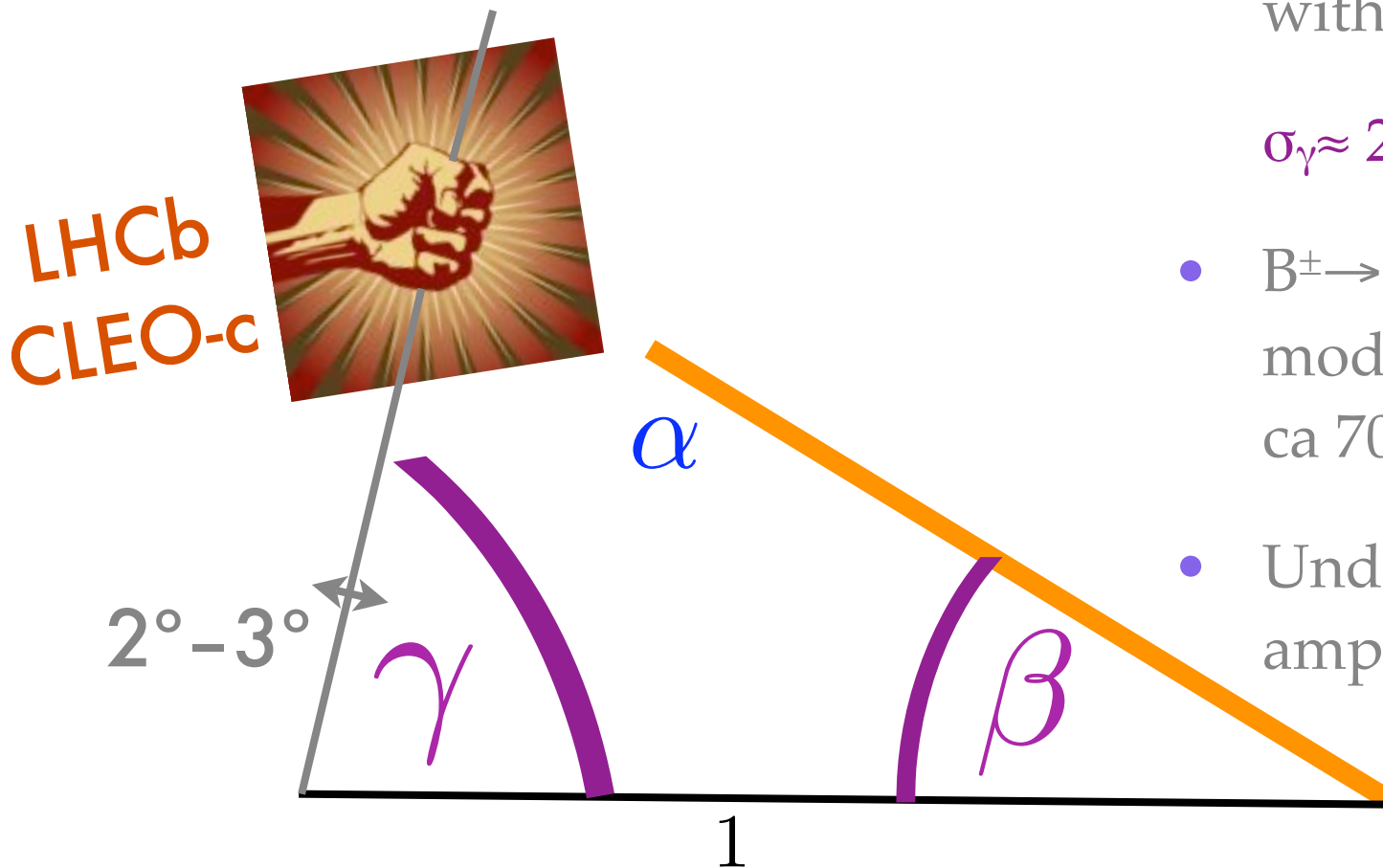
Expect significant further improvement (not evaluated at LHCb, yet)

CLEO-c & γ

- Combining tree-level γ modes, LHCb expects with 10/fb (5 years):

$$\sigma_{\gamma} \approx 2^{\circ} - 3^{\circ}$$

- $B^{\pm} \rightarrow DK^{\pm}$ and $B^0 \rightarrow DK^{*0}$ modes have a weight of ca 70% in that result.
- Understanding D amplitudes crucial!



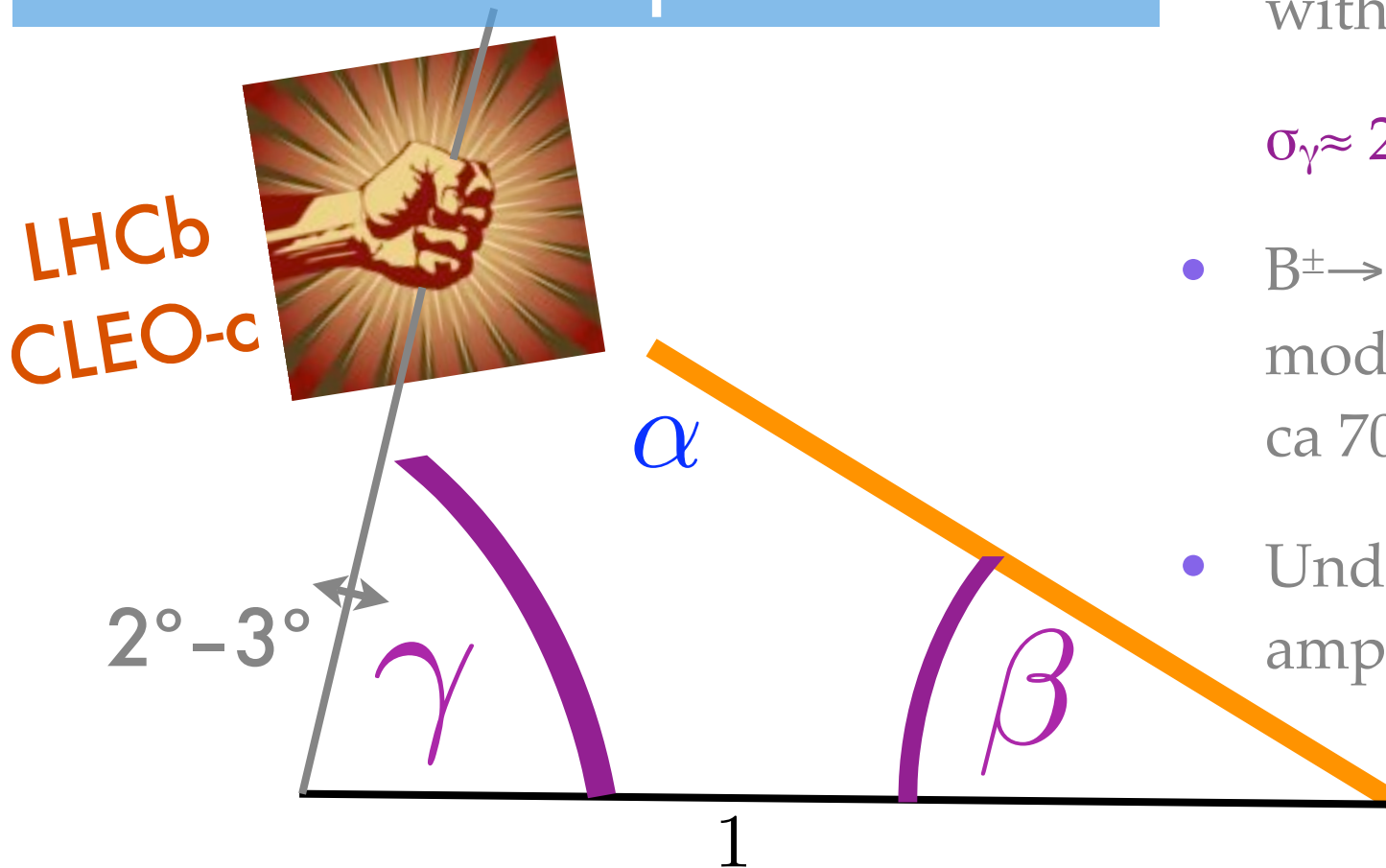
CLEO-c & γ

See also Sean Brisbane's excellent poster

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Summary & Outlook

- Huge statistics, very clean data samples and renewed interest in charm \Rightarrow lots of new, important results, only a few shown here.
- Comprehensive set of charm BF's, several new modes • First Meson \rightarrow 2baryon decay • U-spin test in $D^0 \rightarrow K^0 \pi^0$. • A lot of new D_S results • Dalitz analyses to study light resonances: nature and composition of S-wave remains intriguing.
- Quantum-correlated charm provides crucial input to γ from $B^\pm \rightarrow DK^\pm$ and $B^0 \rightarrow DK^{*0}$ • Dalitz analyses essential • Other powerful techniques benefit from quantum-correlated input, too
- Updates with more data and additional channels from CLEO-c, soon • BESIII will be able to extend these measurements with significantly increased statistics, once starting to run at $\psi(3770)$.

Backup

CLEO-c $D^0 \rightarrow K_S \pi \pi$

Format: result $\pm \sigma(\text{stat}) \pm \sigma(\text{sys}) \pm \sigma(K_S \leftrightarrow K_L \text{ residual model dependence})$

bin

i	c_i	s_i
0	$0.743 \pm 0.037 \pm 0.022 \pm 0.013$	$0.014 \pm 0.160 \pm 0.077 \pm 0.045$
1	$0.611 \pm 0.071 \pm 0.037 \pm 0.009$	$0.014 \pm 0.215 \pm 0.055 \pm 0.017$
2	$0.059 \pm 0.063 \pm 0.031 \pm 0.057$	$0.609 \pm 0.190 \pm 0.076 \pm 0.037$
3	$-0.495 \pm 0.101 \pm 0.052 \pm 0.045$	$0.151 \pm 0.217 \pm 0.069 \pm 0.048$
4	$-0.911 \pm 0.049 \pm 0.032 \pm 0.021$	$-0.050 \pm 0.183 \pm 0.045 \pm 0.036$
5	$-0.736 \pm 0.066 \pm 0.030 \pm 0.018$	$-0.340 \pm 0.187 \pm 0.052 \pm 0.047$
6	$0.157 \pm 0.074 \pm 0.042 \pm 0.051$	$-0.827 \pm 0.185 \pm 0.060 \pm 0.036$
7	$0.403 \pm 0.046 \pm 0.021 \pm 0.002$	$-0.409 \pm 0.158 \pm 0.050 \pm 0.002$

Dalitz Plot

R.H. Dalitz, *Philos. Mag.* 44, 1068 (1953)

Tags

Flavour (semi-leptonic)
 (14k tagged $K_S \pi \pi$
 evts, $B/(S+B)=0.6\%$)

$$K^- e^+ \nu$$

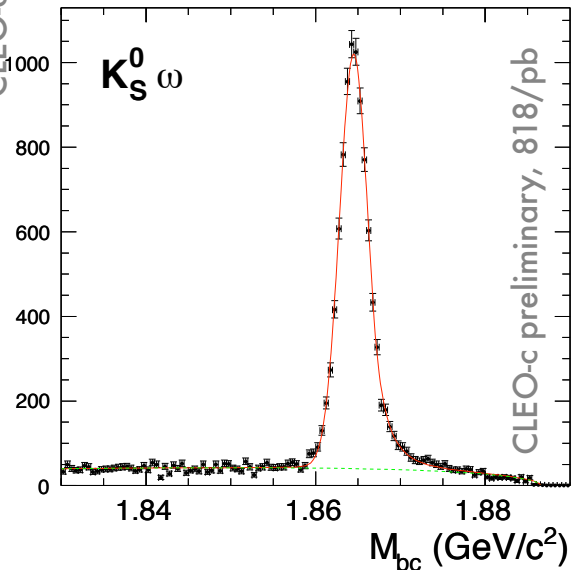
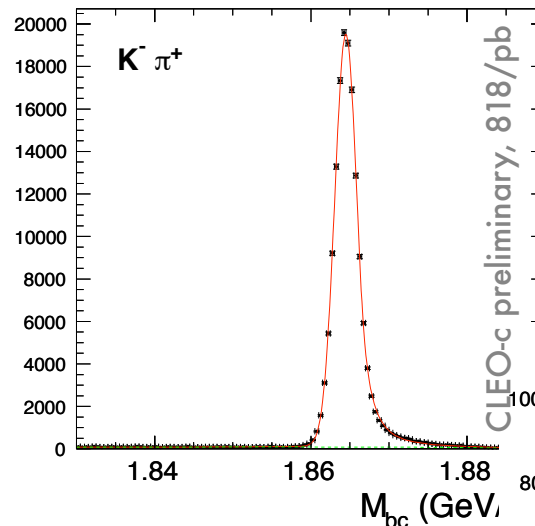
Flavour (hadronic)
 4.4k tagged $K_S \pi \pi$
 evts, $B/(S+B)=3\%$

$$\frac{K^- \pi^+}{K^- \pi^+ \pi^0} \frac{K^- \pi^+ \pi^+}{\pi^+ \pi^-} \frac{K^+ K^-}{K_S^0 \pi^0 \pi^0} \frac{K_S^0 \pi^0}{K_L^0 \pi^0} \frac{K_S^0 \pi^0}{K_S^0 \eta} \frac{K_S^0 \omega}{K_S^0 \omega}$$

CP-even,
 470 tagged $K_S \pi \pi$
 evts, $B/(S+B)=6\%$

CP-odd,
 310 tagged $K_S \pi \pi$
 evts, $B/(S+B)=4\%$

Reconstructed, beam-constrained D mass
 in CLEO-c tag-side data
 (2 example plots, before requiring $K_S \pi \pi$ on other side)

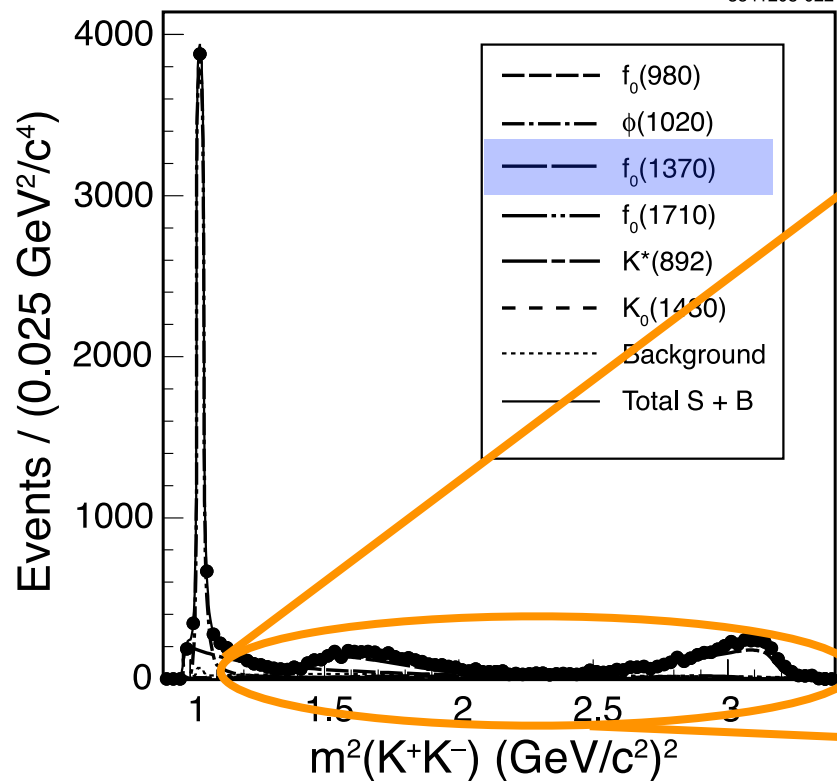


$D_s^+ \rightarrow K^- K^+ \pi^+$

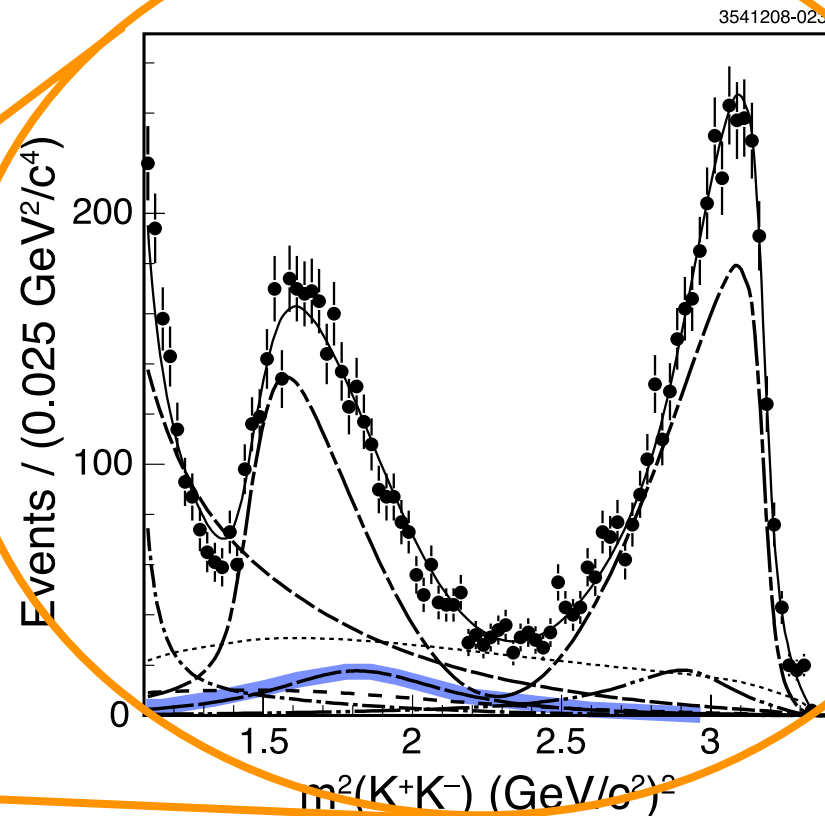
Parameter	E687 Model	$f_2(1270)$	$a_2(1320)$	$f_0(1370)$	$f_0(1500)$	$f_2(1525)$	$a_0(1450)$	$\phi(1680)$
$m_{K^*(892)}$	895.8 ± 0.5	-0.4	-0.1	-0.9	-0.5	0.0	-0.8	0.1
$\Gamma_{K^*(892)}$	44.2 ± 1.0	2.3	2.4	1.5	0.6	0.6	1.0	1.2
$a_{K_0^*(1430)}$ (a.u.)	1.76 ± 0.12	0.11	0.08	-0.25	-0.03	-0.16	-0.22	-0.18
$\phi_{K_0^*(1430)}$ ($^\circ$)	145 ± 8	-32	-28	1.0	-15	1.7	-15	18
$a_{f_0(980)}$ (a.u.)	3.67 ± 0.13	0.29	0.26	1.05	0.52	0.03	1.09	0.20
$\phi_{f_0(980)}$ ($^\circ$)	156 ± 3	-2	-1.6	1.3	2.3	0.22	3.8	10.5
$a_{\phi(1020)}$ (a.u.)	1.15 ± 0.02	-0.03	-0.04	-0.02	-0.003	-0.02	-0.007	-0.012
$\phi_{\phi(1020)}$ ($^\circ$)	-15 ± 4	-7	-6.3	7.2	-0.6	1.5	4.3	13.2
$a_{f_0(1710)}$ (a.u.)	1.27 ± 0.07	0.08	0.07	-0.16	0.17	-0.04	0.03	-0.018
$\phi_{f_0(1710)}$ ($^\circ$)	102 ± 4	7	4.7	-13	-4.1	-3.8	-17	5.3
a_{add} (a.u.)		0.64 ± 0.09	0.45 ± 0.06	1.15 ± 0.09	0.50 ± 0.05	0.50 ± 0.07	1.32 ± 0.10	1.04 ± 0.17
ϕ_{add} ($^\circ$)		17 ± 9	40 ± 8	53 ± 5	132 ± 7	173 ± 10	103 ± 5	-4 ± 11
χ^2/ν	$278/119$	$237/117$	$237/117$	$178/117$	$229/117$	$249/117$	$192/117$	$256/117$

$D_S^+ \rightarrow K^- K^+ \pi^+$

$M^2(KK)$ fit projection
with $f_0(1370)$ S-wave
contribution



$D_S^+ \rightarrow K^- K^+ \pi^+$ $M^2(KK)$ projections
CLEO: arXiv:0903.1301v1 [hep-ex] (March 2009)



[1] P.L. Frabetti et al. (E687 Collaboration), Phys. Lett., B351, 591 (1995)

See also FOCUS: A.M. Rahimi, FERMILAB-THESIS-2000-13 and S. Malvezzi, AIP Conf. Proc. 549, 569 (2002)

Model independent γ fit

Giri, Grossmann, Soffer, Zupan, Phys Rev D 68, 054018 (2003).

- Binned decay rate:

$$\Gamma(B^\pm \rightarrow D(K_s \pi^+ \pi^-)K^\pm)_i =$$

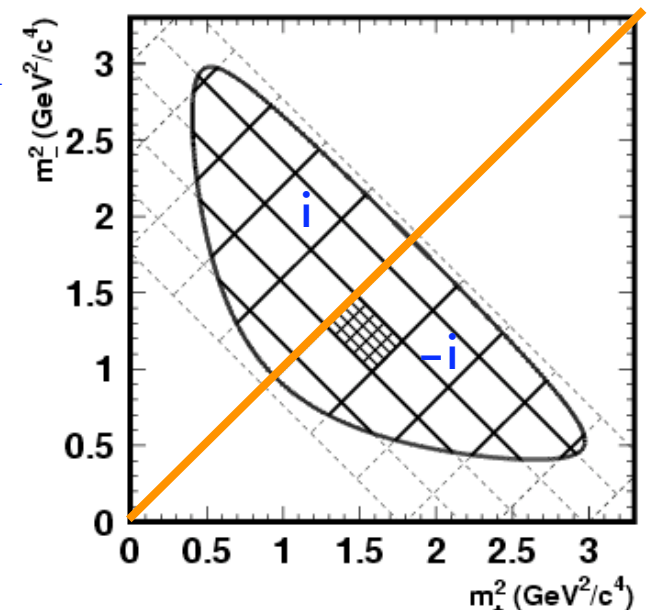
\mathcal{T}_i known from flavour-specific D decays (e.g. D^*)

$\delta_D \equiv$ phase of $A(D \rightarrow K_s \pi \pi)$

$$\mathcal{T}_i + r_B^2 \mathcal{T}_{-i} + 2r_B \sqrt{\mathcal{T}_i \mathcal{T}_{-i}} \{c_i \cos(\delta \pm \gamma) + s_i \sin(\delta \pm \gamma)\}$$

(weighted) average of $\cos(\delta_D(s_{12}, s_{23}) - \delta_D(s_{23}, s_{12}))$ and $\sin(\delta_D(s_{12}, s_{23}) - \delta_D(s_{23}, s_{12}))$ over bin i

- Binning such that such that $c_i = c_{-i}$, $s_i = -s_{-i}$
- Distribution sensitive to c_i , s_i , r_B , δ and γ .
- To extract γ from realistic numbers of B events need external input from CLEO's quantum-correlated $DD\bar{b}b$ pairs.



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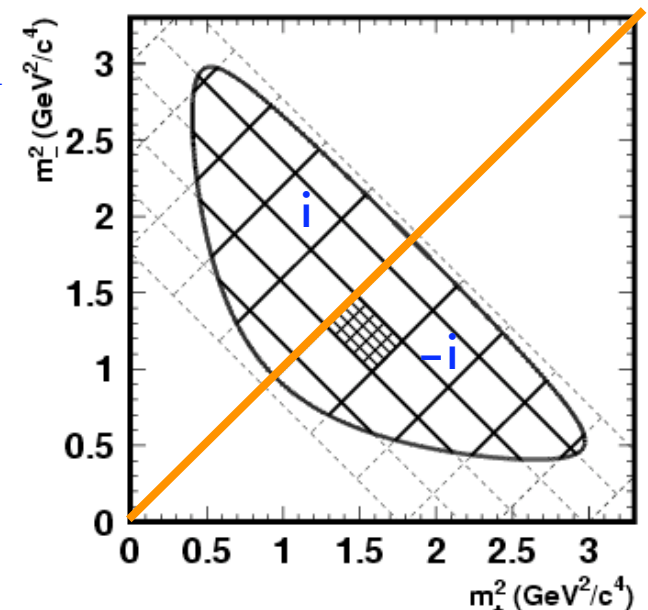
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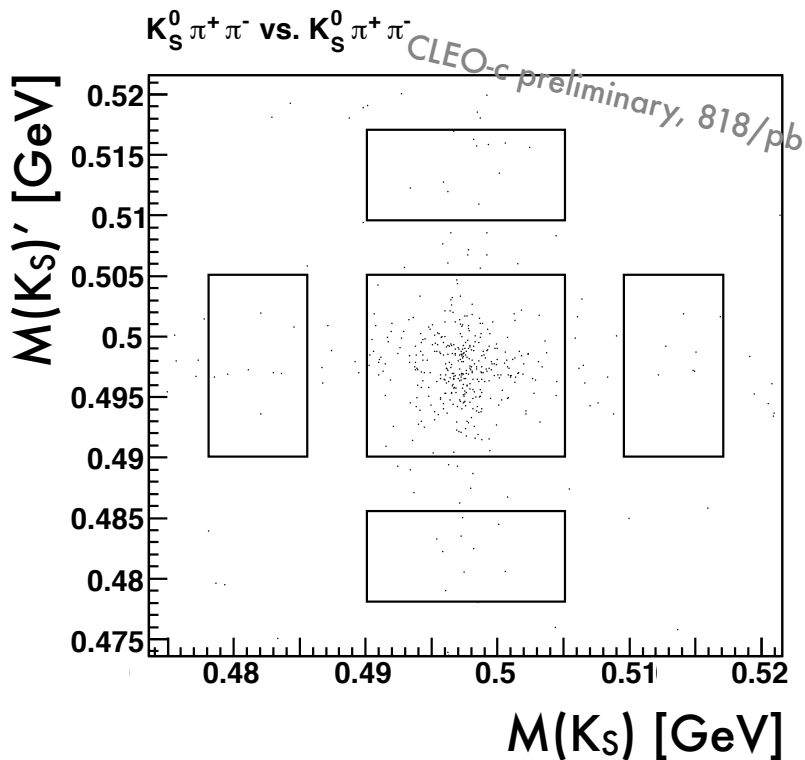
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s_i, c_i from $K_S\pi\pi\pi$ vs $K_S\pi\pi\pi$

- CP-tagged binned Dalitz Plots sensitive to c_i only.
- Simultaneous, binned analysis of quantum-correlated $D_a \rightarrow K_S\pi\pi, D_b \rightarrow K_S\pi\pi$ pairs gives access to both c_i and s_i :



- 420 fully reconstructed events, $S/(B+S) = 90\%$
- 50 partially reconstructed events (ignore one π in reconstruction), $S/(B+S) = 85\%$

CP-even $K_L\pi\pi \approx$ CP-odd $K_S\pi\pi$

↑ unfortunately only "≈", not quite "="

$$K_S^0 = (K^0 + \bar{K}^0)/\sqrt{2}$$

$$K_L^0 = (K^0 - \bar{K}^0)/\sqrt{2}.$$

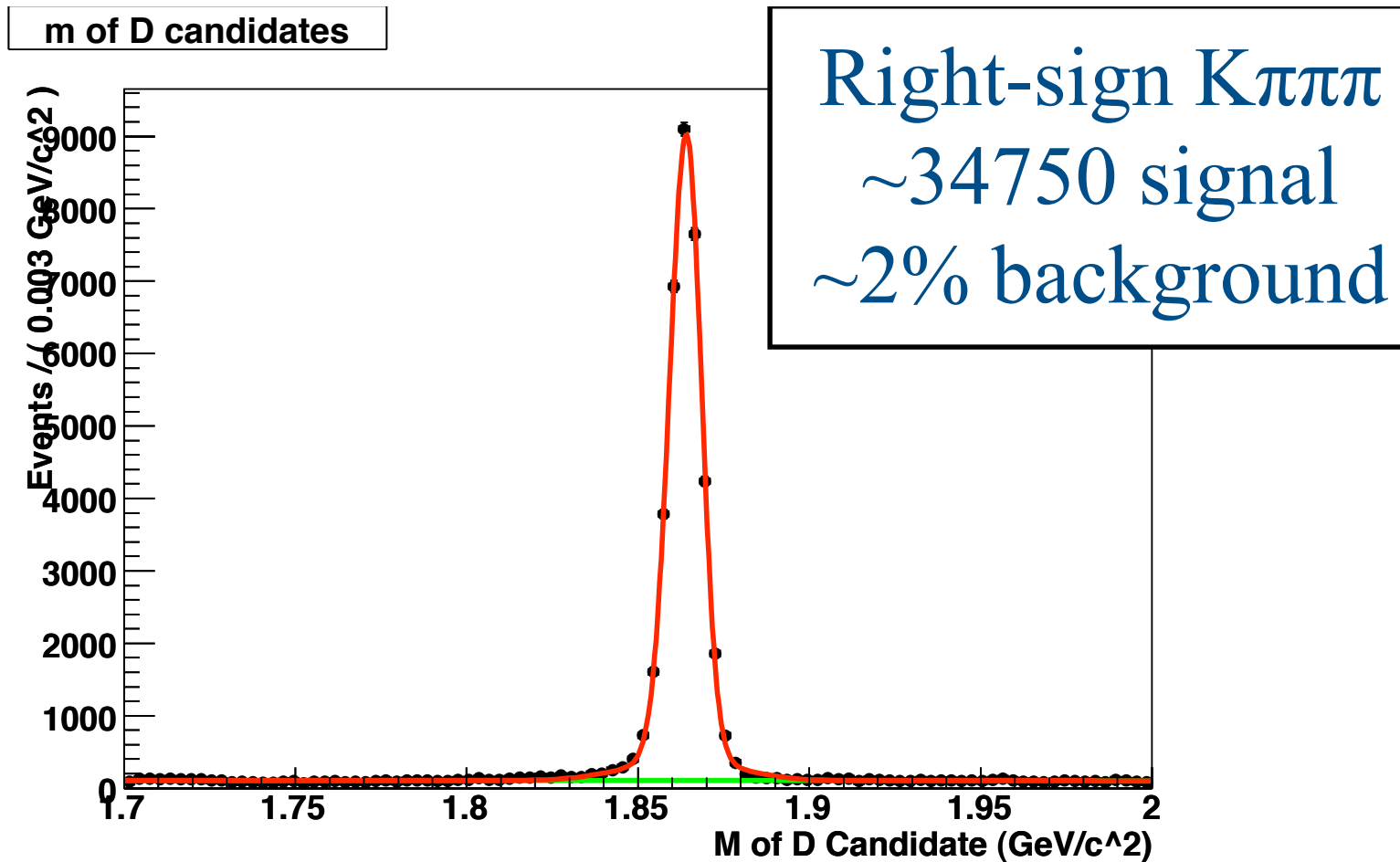
$$-A(D^0 \rightarrow K_L^0 \pi^+ \pi^-) = A(D^0 \rightarrow K_S^0 \pi^+ \pi^-) - \sqrt{2}A(D^0 \rightarrow K_{\text{flavour}}^0 \pi^+ \pi^-)$$

CF+DCS DCS

- Using $K_L\pi\pi$ significantly enhances statistics.
- However, need a **correction** of $\mathcal{O}(\tan^2\theta_C)$. Residual model dependence enters as an uncertainty on a small correction. Detailed systematics study shows effect is small.
- Notation: c_i, s_i from $K_S\pi\pi$. c_i', s_i' from $K_L\pi\pi$.

$$\Delta c_i \equiv c_i - c_i', \quad \Delta s_i \equiv s_i - s_i'$$

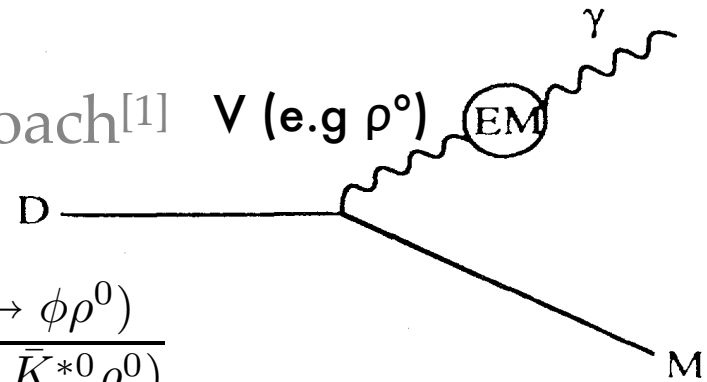
D → K3π events at CLEO



VMD, $D^0 \rightarrow V\gamma$ and $D^0 \rightarrow V\rho^0$

- Dominated by long-distance effects. Difficult to calculate.

- Vector-Meson-Dominance approach^[1]



- Predicts

$$\frac{\mathcal{B}(D^0 \rightarrow \phi\gamma)}{\mathcal{B}(D^0 \rightarrow \bar{K}^{*0}\gamma)} = \frac{\mathcal{B}(D^0 \rightarrow \phi\rho^0)}{\mathcal{B}(D^0 \rightarrow \bar{K}^{*0}\rho^0)}$$

- Find $\frac{\mathcal{B}(D^0 \rightarrow \phi\gamma)}{\mathcal{B}(D^0 \rightarrow \bar{K}^{*0}\gamma)} = (6.27 \pm 0.71 \pm 0.79) \times 10^{-2}$ BaBar 08

$$\frac{\mathcal{B}(D^0 \rightarrow \phi\rho^0)}{\mathcal{B}(D^0 \rightarrow \bar{K}^{*0}\rho^0)} = (6.7 \pm 1.6) \times 10^{-2} \quad \text{PDG 07}$$

[1] G. Burdman, E. Golowich, J. L. Hewett, and S. Pakvasa, Phys. Rev. , 6383 (1995)

Direct CP Violation

- Main focus there: time-dependent studies
- But direct CPV in time-integrated

$$A_{CP} = \frac{\Gamma(D \rightarrow f) - \Gamma(\bar{D} \rightarrow \bar{f})}{\Gamma(D \rightarrow f) + \Gamma(\bar{D} \rightarrow \bar{f})}$$

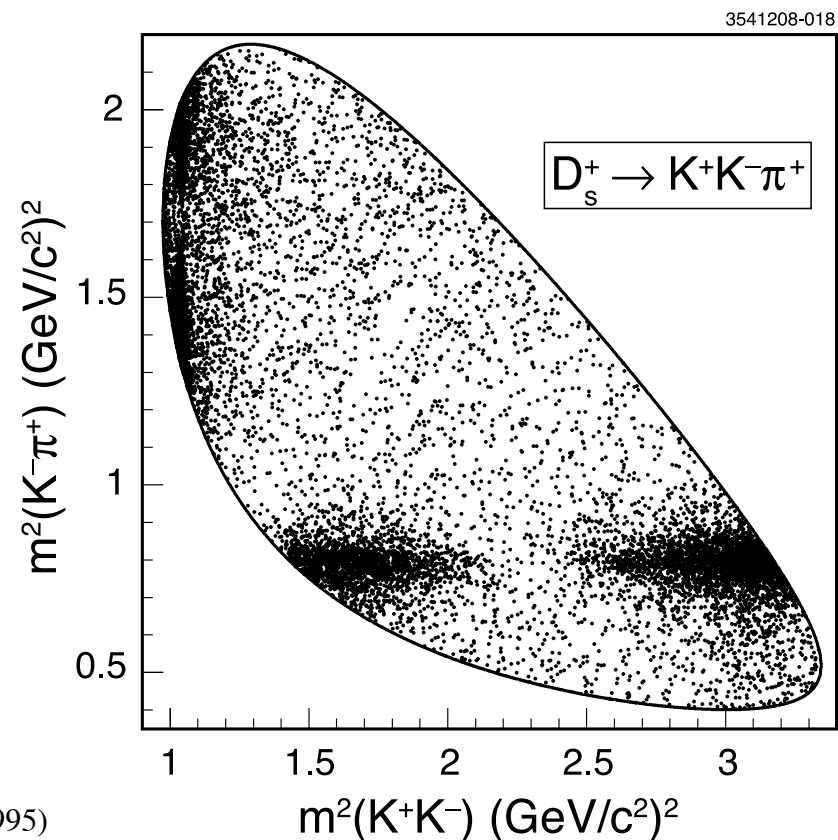
decays also interesting!

$D_s^+ \rightarrow K^- K^+ \pi^+$

- Follows CLEO-c's $D_s^+ \rightarrow K^- K^+ \pi^+$ absolute B.R. measurement.
- Isobar fit.
- Previously done at E687 with 701 events.

12k $D_s^+ \rightarrow K^- K^+ \pi^+$ events at CLEO-c

CLEO: arXiv:0903.1301v1 [hep-ex] (March 2009)



Previous measurements:

E687: P.L. Frabetti et al. (E687 Collaboration), Phys. Lett., B351, 591 (1995)

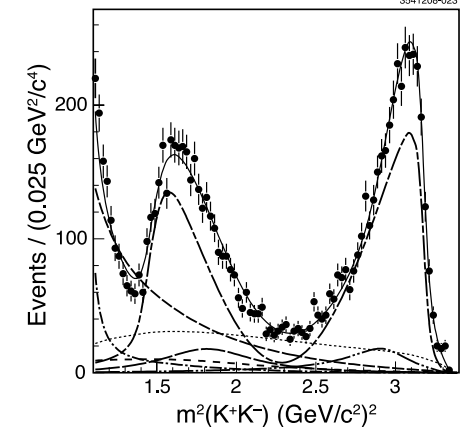
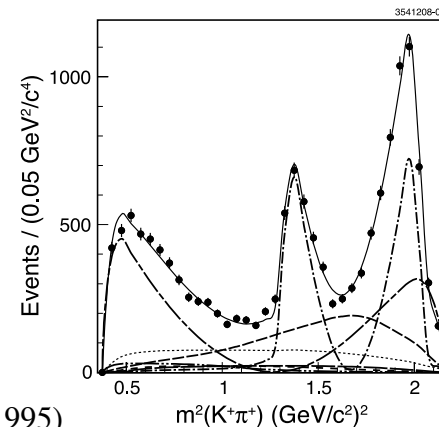
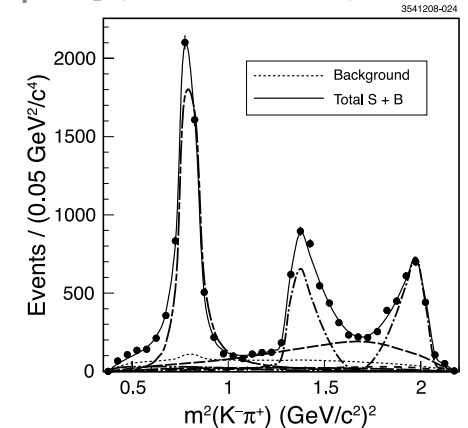
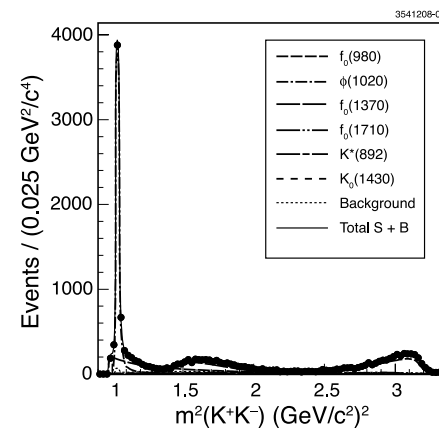
FOCUS: A.M. Rahimi, FERMILAB-THESIS-2000-13, S. Malvezzi, AIP Conf. Proc. 549, 569 (2002)

$D_s^+ \rightarrow K^- K^+ \pi^+$

- Find good agreement with E687 model parameters.
- Get much-improved fit to our data with additional KK S-wave contribution.
- Tried many options. Best results with $f_0(1370)$

12k $D_s^+ \rightarrow K^- K^+ \pi^+$ fit projections

CLEO: arXiv:0903.1301v1 [hep-ex] (March 2009)



[1] P.L. Frabetti et al. (E687 Collaboration), Phys. Lett., B351, 591 (1995)

[2] [4] A.M. Rahimi, FERMILAB-THESIS-2000-13

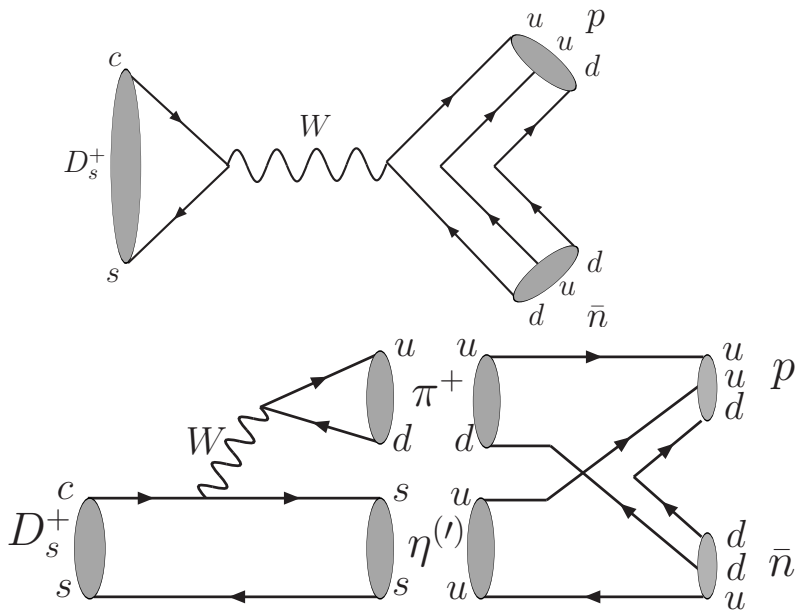
[3] S. Malvezzi, AIP Conf. Proc. 549, 569 (2002)

Binned Dalitz Result

Format: bin, result $\pm \sigma_{\text{stat}} \pm \sigma_{\text{sys}} \pm \sigma_{(\text{KL} \leftrightarrow \text{KS})}$

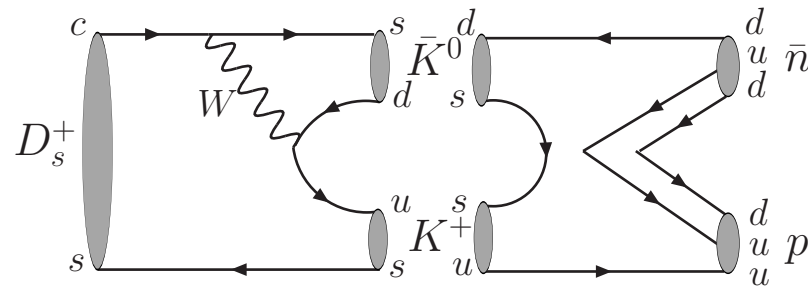
i	C_i	S_i
0	$0.743 \pm 0.037 \pm 0.022 \pm 0.013$	$0.014 \pm 0.160 \pm 0.077 \pm 0.045$
1	$0.611 \pm 0.071 \pm 0.037 \pm 0.009$	$0.014 \pm 0.215 \pm 0.055 \pm 0.017$
2	$0.059 \pm 0.063 \pm 0.031 \pm 0.057$	$0.609 \pm 0.190 \pm 0.076 \pm 0.037$
3	$-0.495 \pm 0.101 \pm 0.052 \pm 0.045$	$0.151 \pm 0.217 \pm 0.069 \pm 0.048$
4	$-0.911 \pm 0.049 \pm 0.032 \pm 0.021$	$-0.050 \pm 0.183 \pm 0.045 \pm 0.036$
5	$-0.736 \pm 0.066 \pm 0.030 \pm 0.018$	$-0.340 \pm 0.187 \pm 0.052 \pm 0.047$
6	$0.157 \pm 0.074 \pm 0.042 \pm 0.051$	$-0.827 \pm 0.185 \pm 0.060 \pm 0.036$
7	$0.403 \pm 0.046 \pm 0.021 \pm 0.002$	$-0.409 \pm 0.158 \pm 0.050 \pm 0.002$

Theory of $D_s^+ \rightarrow p\bar{n}$



- Short Distance:

$$\mathcal{B}(D_s^+ \rightarrow p\bar{n})_{\text{SD}} = (0.4_{-0.3}^{+1.1}) \times 10^{-6}$$



- Long Distance $\mathcal{B}(D_s^+ \rightarrow p\bar{n}) \approx (0.8_{-0.6}^{+2.4}) \times 10^{-3}$
- Measured $\mathcal{B}(D_s^+ \rightarrow p\bar{n}) = (1.30 \pm 0.36_{-0.16}^{+0.12}) \times 10^{-3}$

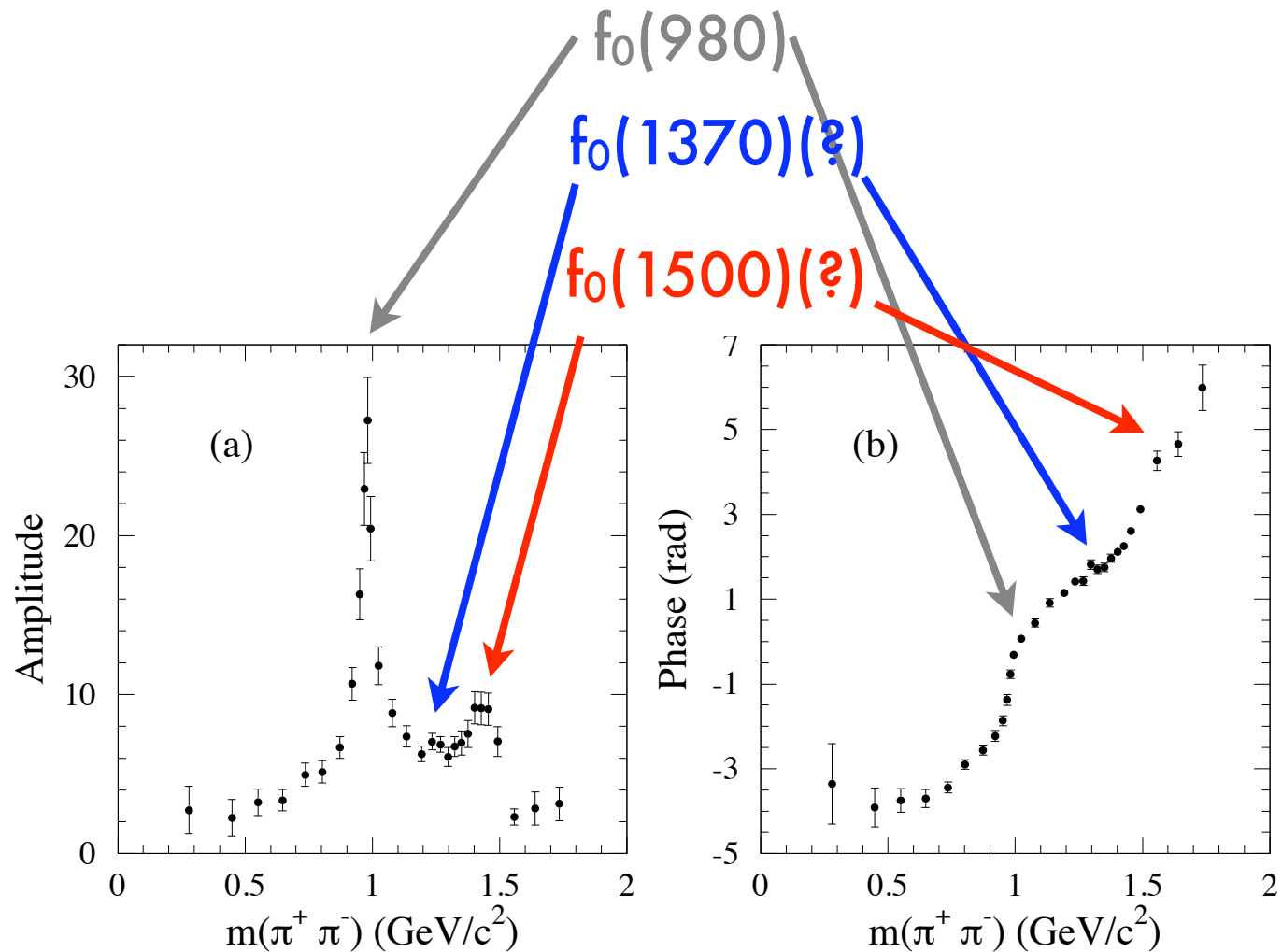
Chen, Cheng, Hsiao: [Phys.Lett.B663:326-329,2008](#)

Absolute BF

- Important normalising modes: $D^0 \rightarrow K^- \pi^+$
 $D^+ \rightarrow K^- \pi^+ \pi^+$
 $D_s^+ \rightarrow K^- K^+ \pi^+$
(historically “ $\phi\pi^+$ ”)
- Methods - need to know there is a D before reconstructing it
- BaBar: partial reconstruction of $D^* \rightarrow D\pi$, using only the π (and the rest of the event, but not the D)
- BELLE: $e^+e^- \rightarrow D_s^{*+} D_{s1}^- (\rightarrow \bar{D}^{*0} K^-)$
- CLEO-c: $e^+e^- \rightarrow \psi \rightarrow \bar{D} D$

$D_s^+ \rightarrow \pi^- \pi^+ \pi^+$

Model independent S-wave parameterisation



BaBar: arXiv:0808.0971v3 [hep-ex], submitted to PRD



- $D_S^+ \rightarrow (\pi^+ \pi^-)_{S\text{-wave}} \pi^+$ dominates.
- Model-independent S-wave fit compatible with $f_0(980)$ resonance.
- Also with FOCUS's K-matrix and E791's isobar fit
- Signs of something going on near $f_0(1370)$, $f_0(1500)$.
- Large D-wave component with $f_2(1270)$

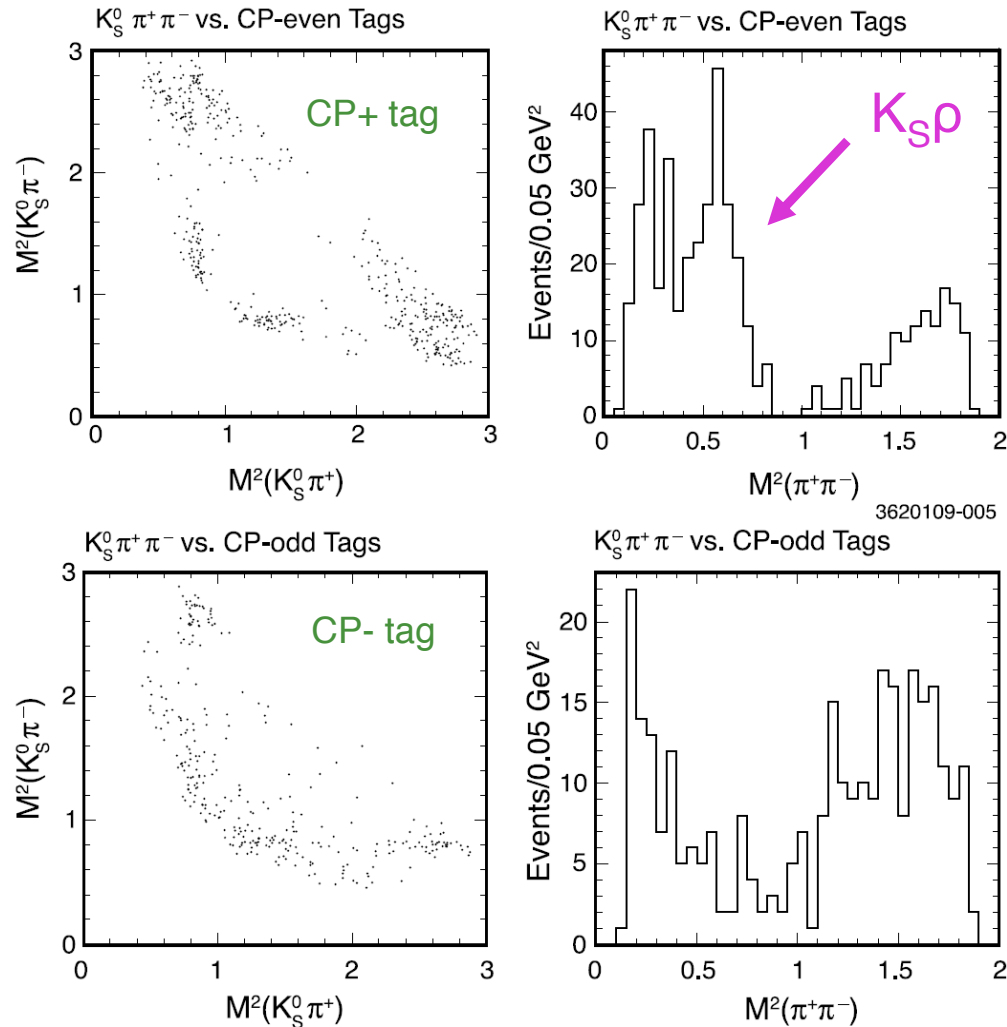
Fit Fractions

Decay Mode	Decay fraction(%)
$f_2(1270)\pi^+$	$10.1 \pm 1.5 \pm 1.1$
$\rho(770)\pi^+$	$1.8 \pm 0.5 \pm 1.0$
$\rho(1450)\pi^+$	$2.3 \pm 0.8 \pm 1.7$
S-wave	$83.0 \pm 0.9 \pm 1.9$
Total	$97.2 \pm 3.7 \pm 3.8$
χ^2 / NDF	$\frac{437}{422-64} = 1.2$

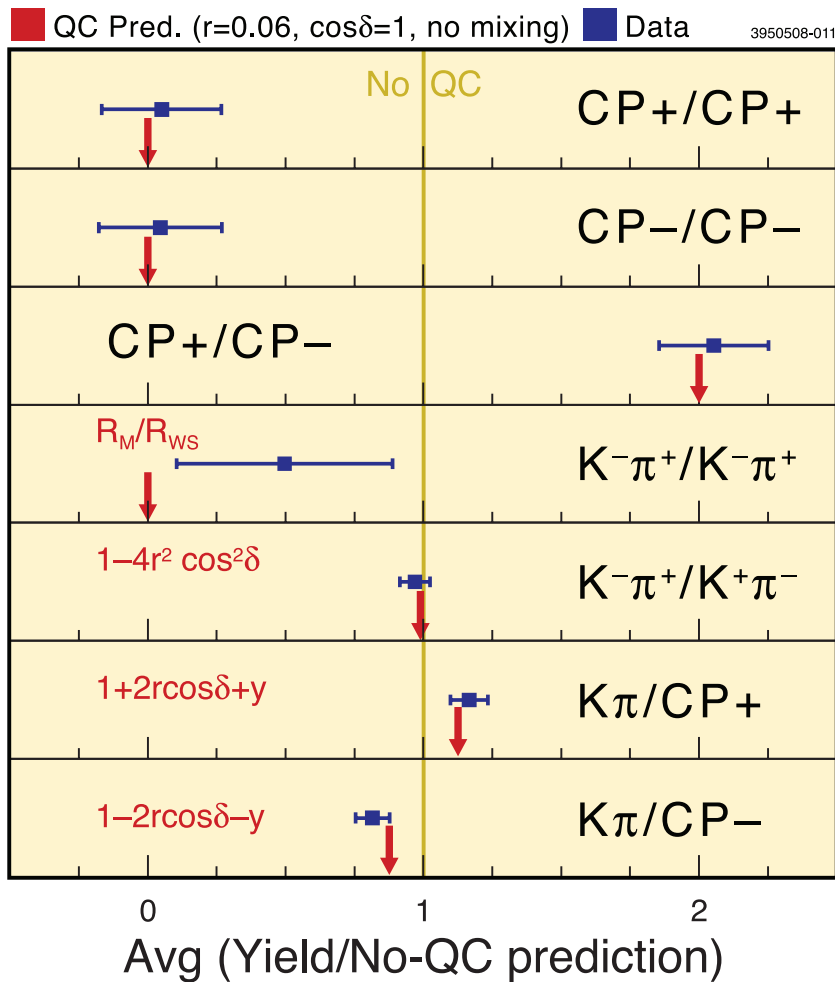
BaBar: arXiv:0808.0971v3 [hep-ex], submitted to PRD

CP+ and CP- $D^0 \rightarrow K_S \pi \pi$ at CLEO-c

CLEO-c arXiv:0903.1681v1 [hep-ex], submitted to PRD



Exploiting Quantum Correlations at CLEO-c



- CP-tagged rates

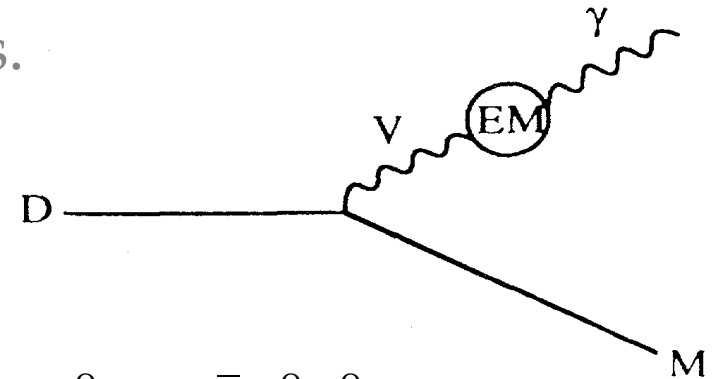
$$\propto (1 \pm 2 r_D^{K\pi} \cos \delta_D^{K\pi} \pm y)$$
- Combined analysis in many modes sensitive to $\delta_D^{K\pi}$ w/o ambiguity.
- Crucial input to charm mixing measurements, as well as helping measure γ
- Result:
$$\delta_D^{K\pi} = 22^\circ_{-12^\circ}^{+11^\circ} + 9^\circ_{-11^\circ}$$

Analysis based on 1/3 of data set -
update with full 818/fb soon.

PRL 100, 221801 (2008), PRD 78, 012001 (2008)

VMD, $D^0 \rightarrow V\gamma$ and $D^0 \rightarrow V\rho^0$

- Dominated by long-distance effects.
- Vector meson dominance (VMD):
 $A(D^0 \rightarrow M\gamma) \approx (e/f_\rho) A(D \rightarrow M\rho^0)$ [1]



$$\mathcal{B}(D^0 \rightarrow \bar{K}^{*0}\gamma) = \underline{(0.021 \pm 0.005)} \mathcal{B}(D^0 \rightarrow \bar{K}^{*0}\rho^0)$$

$$\mathcal{B}(D^0 \rightarrow \phi\gamma) = \underline{(0.020 \pm 0.003)} \mathcal{B}(D^0 \rightarrow \phi\rho^0)$$

- Using $(e/f_\rho) = 0.06$ [2], expect:

$$\mathcal{B}(D^0 \rightarrow V\gamma) \approx \underline{0.0036} \cdot \mathcal{B}(D^0 \rightarrow V\rho^0)$$

- While proportionality predicted by VMD is seen, measured proportionality factor is a bit large.

[1] G. Burdman, E. Golowich, J. L. Hewett, and S. Pakvasa, Phys. Rev. , 6383 (1995) [2] E. Golowich and S. Pakvasa, Phys. Rev. D 51, 1215 - 1223 (1995)

Branching Fractions

- Absolute BF: Progress in key reference modes.

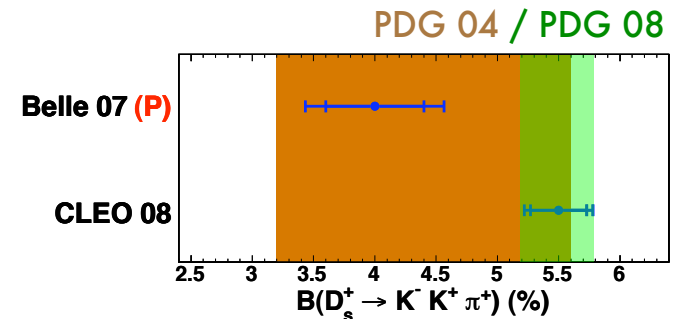
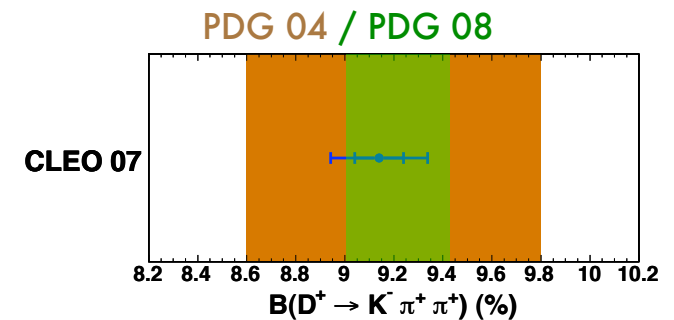
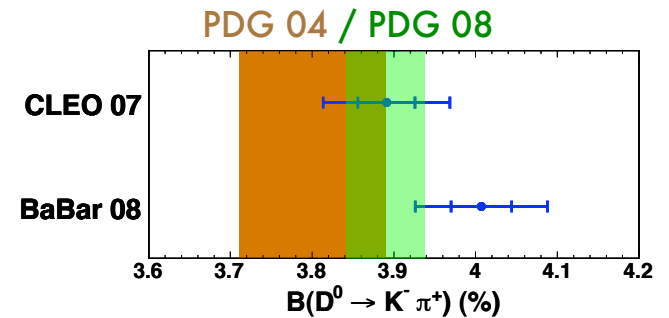
- Comprehensive set of BF:

$D_{(S)} \rightarrow PP$ with $P=K^\pm, K_S, K_L, \pi^\pm, \pi^0, \eta, \eta'$

$D_{(S)} \rightarrow V\gamma, V\eta, V\phi$

$D_{(S)} \rightarrow$ baryons

- Recent addition: CLEO-c's new $D_s^* D_s$ data sample.



Belle 07: hep-ex/0701053 (Prel.) [552 fb⁻¹]

CLEO 07: PRD 76, 112001 [281 pb⁻¹]

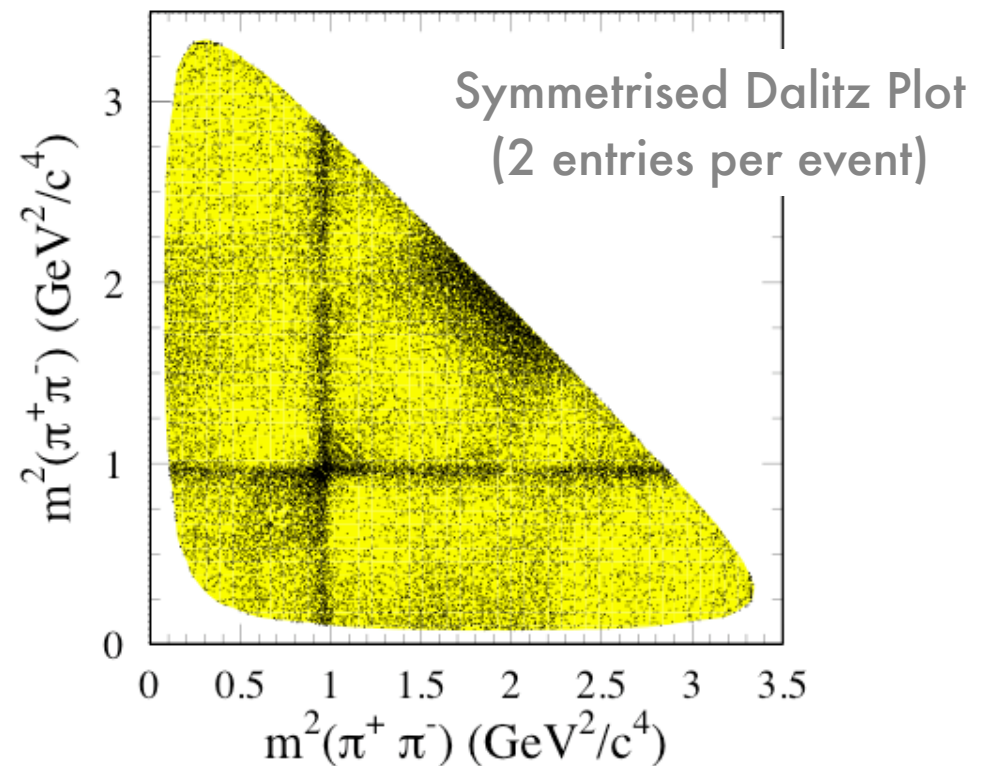
BaBar 08: PRL 100, 051802 [210 fb⁻¹]

CLEO 08: PRL 100, 161804 [298 pb⁻¹]



- Dominated by S-wave (fit-fraction 83%).
- BaBar perform model-independent analysis of S-wave component [1], method pioneered by E791[2].

10.5k signal events at BaBar,
with 80% signal purity



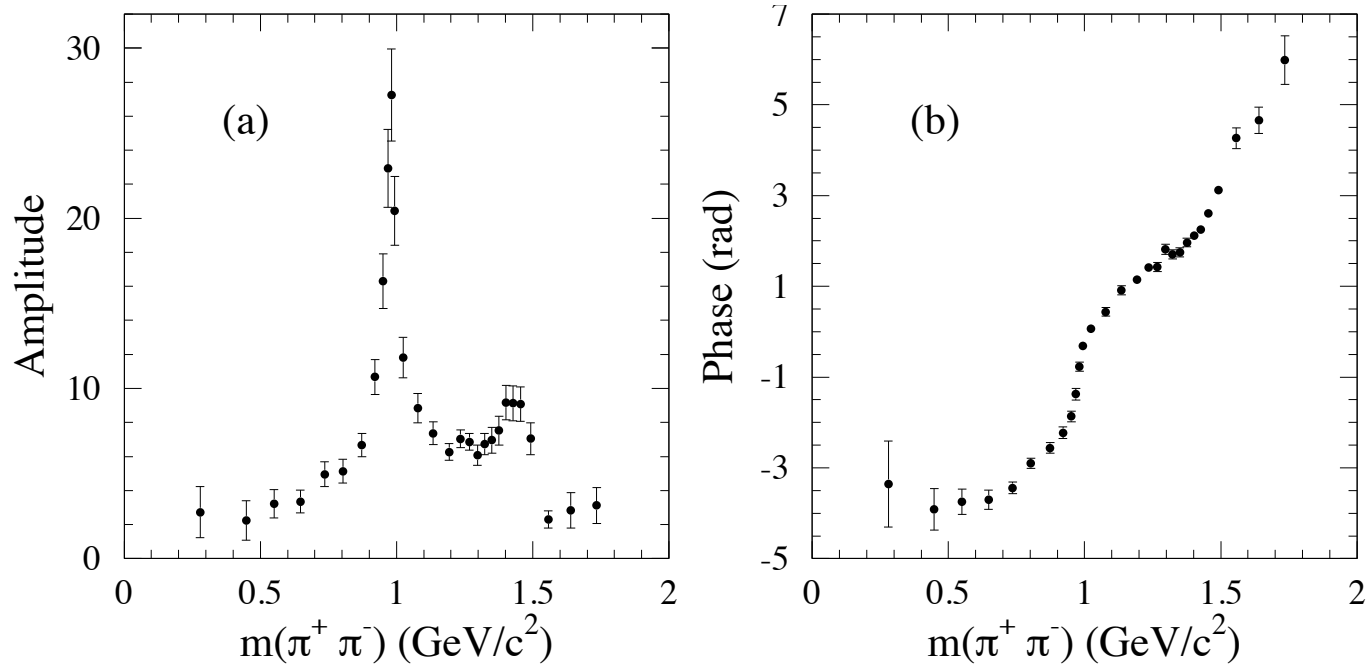
[1] BaBar: arXiv:0808.0971v3 [hep-ex], submitted to PRD

[2] E791: Phys. Rev. D 73, 032004 (2006).

$D_s^+ \rightarrow \pi^- \pi^+ \pi^+$

Model independent S-wave parameterisation

- Define 30 points in $m(\pi^+ \pi^-)$.
- 2 fit parameters (magnitude & phase) for each point
- Interpolate between points*

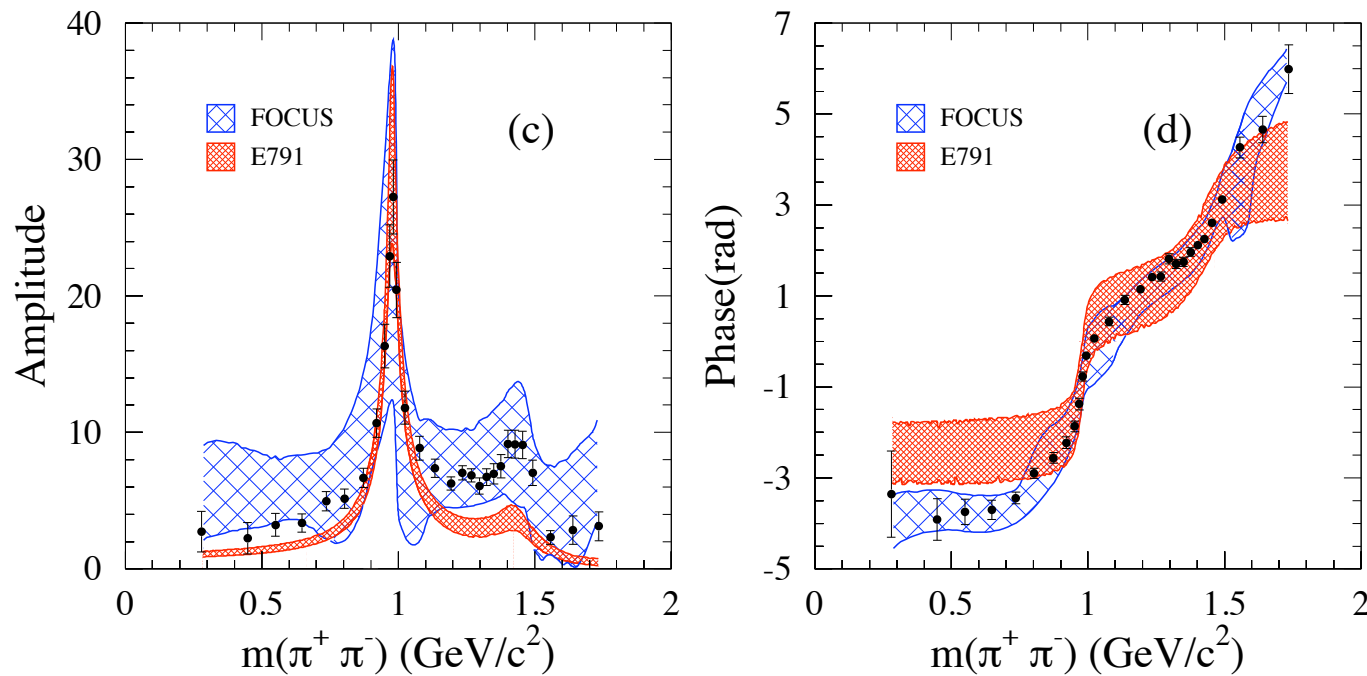


BaBar: arXiv:0808.0971v3 [hep-ex], submitted to PRD

*)Relaxed Cubic Spline: K. S. Kölbig and H. Lipps, Cubic Splines and Their Integrals, CERN Program Library, E211.

$D_s^+ \rightarrow \pi^- \pi^+ \pi^+$

- Model-independent S-wave compatible with FOCUS (K-matrix) and E791 (isobar).



- Clear $f_0(980)$, signs of $f_0(1370)$, $f_0(1500)$
- Also: large D-wave contribution $f_2(1220)$

E791: Phys. Rev. Lett. 86, 765 (2001)
FOCUS: Phys. Lett. B 585, 200 (2004)
Dots and plots by:
BaBar: arXiv:0808.0971v3 [hep-ex], submitted to PRD

Direct CPV in D^0 , D^+

- Plenty of results from BaBar, BELLE, CDF, CLEO, E791, FOCUS, averaged by HFAG
- Table shows averages for those results that received updates in 2007 or 2008.
- Plenty more modes
- Reaching per-mil precision.

	Mode	$A_{CP}(\%)$ Charm09	$A_{CP}(\%)$ Charm07
D^0	K^+K^-	-0.16 ± 0.23	1.36 ± 1.2
	$\pi^+\pi^-$	0.22 ± 0.37	1.27 ± 1.25
	$\pi^+\pi^-\pi^0$	-0.23 ± 0.42	1.0 ± 9.0
	$K^-\pi^+\pi^0$	0.16 ± 0.89	3.1 ± 8.6
	$K^-K^+\pi^0$	0.16 ± 0.89	-
D^+	$K^-K^+\pi^+$	0.39 ± 0.61	0.7 ± 0.8
	$K_S\pi^+$	-0.86 ± 0.90	-1.6 ± 1.7
	$K_S\pi^+\pi^0$	$0.3 \pm 0.9 \pm 0.3$	-
	$K^-\pi^+\pi^+\pi^0$	$1.0 \pm 0.9 \pm 0.9$	-

Direct CPV in Ds

- CLEO-c's Ds data allowed for the first time a precise test of direct CP in the Ds system
- Plenty of modes, all results new since Charm 2007
- Many results at the few % level.

Mode	A _{CP} (%)
$\pi^+\eta$	$-8.2 \pm 5.2 \pm 0.8$
$\pi^+\eta'$	$-5.5 \pm 3.7 \pm 1.2$
$K_S\pi^+$	27 ± 11
$K_S\pi^0$	2 ± 29
$K^+\eta$	-20 ± 18
$K^+\eta'$	-17 ± 37
K^+K_S	$4.9 \pm 2.1 \pm 0.9$
$\pi^+\pi^-\pi^+$	$2.0 \pm 4.6 \pm 0.7$
$K^+\pi^+\pi^-$	$11.2 \pm 7.0 \pm 0.9$
$K_S K^-\pi^+\pi^+$	$-0.7 \pm 3.6 \pm 1.1$
$K^+K^-\pi^+\pi^0$	$-5.9 \pm 4.2 \pm 1.2$

Prospects for direct CPV

- Example: $D^0 \rightarrow K^+ \bar{K}^-$
 - BaBar 2008: $+0.0000 \pm 0.0034 \pm 0.0013$
 - BELLE 2008: $-0.0043 \pm 0.0030 \pm 0.0011$
 - World average (HFAG): $+0.0022 \pm 0.0037$
- CDF has obtained its result of $+0.020 \pm 0.012 \pm 0.006$ with only 2% of its current data set. CDF could beat world stat precision now.
- LHCb, due to start this year, expects stat precision of 0.004% in 10/fb (ca 5 years, using charm from B decays, including prompt charm will improve this further).

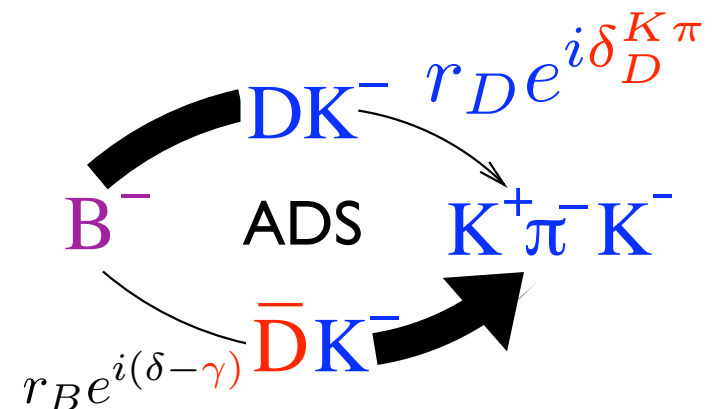
γ from 2-body decays, ADS

- CLEO uses quantum coherence to measure $\delta_D^{K\pi}$ in decays such as

$$\Gamma(D_{CP+} \rightarrow K^+ \pi^-) = \frac{1}{2} |A(D \rightarrow K^+ \pi^-) + A(\bar{D} \rightarrow K^+ \pi^-)|^2$$

$$\propto (1 + 2r_D^{K\pi} \cos \delta_D^{K\pi}) + \text{mixing terms}$$

- Result: $\delta_D^{K\pi} = 22^\circ + 11^\circ + 9^\circ$
 $-12^\circ - 11^\circ$
- Also important input for D-mixing! *



PRL 100, 221801 (2008), PRD 78, 012001 (2008)

Analysis based on 1/3 of data set -
 update with full 818/fb and more tag
 modes, soon.

* Result shown includes external input on y, y' from mixing measurements. Without external inputs: $\cos \delta = 1.03_{-0.17}^{+0.31} \pm 0.06$