

Leptonic D Decays

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FPCP09 Lake Placid
29 May 2009



Outline

Introduction

CLEO-c $D^+ \rightarrow \mu\nu$

Belle $D_s \rightarrow \mu\nu$

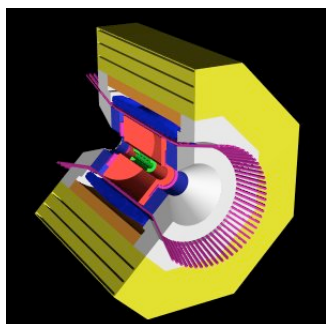
CLEO-c $D_s \rightarrow \mu\nu, \tau\nu$

[$\tau \rightarrow \pi\nu$]

CLEO-c $D_s \rightarrow \tau\nu$

[$\tau \rightarrow e\nu\nu$]

The Future...



@ charm
threshold

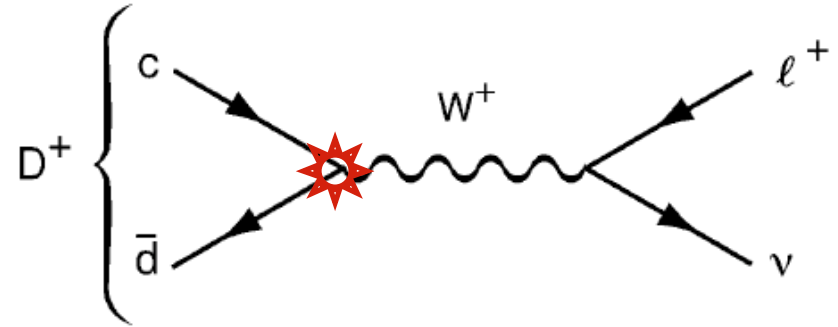
10 GeV
continuum
charm



Theory-on-a-Page

**Decay
Constant
Our Prey**

**Phase
Space
inhibits tau,
esp. for D^+**



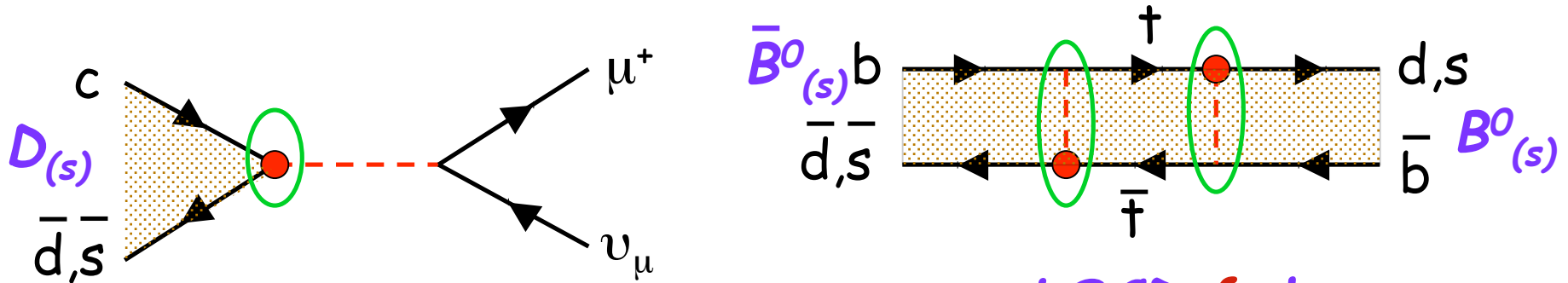
$$\Gamma(D^+ \rightarrow \ell^+ \nu) = \frac{G_F^2}{8\pi} f_{D^+}^2 m_\ell^2 M_{D^+} \left(1 - \frac{m_\ell^2}{M_{D^+}^2}\right)^2 |V_{cd}|^2$$

**Helicity
Suppression
favors τ, μ over e**

**CKM
larger Γ & BR
for D_s**

B Physics Connection

B mixing experimental results are not fully utilized due to f_B uncertainty
(accurate f_B directly from B leptonic is tough !!!)



f_D LQCD = experiment ?

use LQCD f_B here

Get V_{td} , V_{ts}

Leptonic Decays $D_{(s)} \rightarrow l\nu$ to extract decay constants

Key issue:

Precision tests of (unquenched) Lattice QCD

Helicity & Phase Space

$$B(D^+ \Rightarrow \mu\nu) = 3.8 \times 10^{-4} \quad \times 2.1 \text{ "lifetime favored"}$$

$$B(D_s^+ \Rightarrow \mu\nu) = \sim 5.6 \times 10^{-3} \quad \left\{ \begin{array}{l} \times 19 \text{ Cabibbo favored} \\ \times 1.5 \text{ decay const} \\ \times 1.05 \text{ phase space} \end{array} \right.$$

$$D^+ \text{ SM ratios } e\nu : \mu\nu : \tau\nu \Leftrightarrow 2.3 \times 10^{-5} : 1 : 2.65$$

$$D_s^+ \text{ SM ratios } e\nu : \mu\nu : \tau\nu \Leftrightarrow 2.3 \times 10^{-5} : 1 : 9.76$$

Tau modes can be relevant with key one-prong tau decays:

18% $e\nu\nu$ 11% $\pi\nu$

for D^+ : dominated by muons; small smeared-out tau rate

for D_s^+ : can measure BOTH muon and tau channels

(more details later)

Electron channel: only limits, hard to approach Standard Model

CLEO f_D Technique

CLEO-c uses Tagging:

$e^+e^- \rightarrow \psi(3770) \rightarrow D^0D^0, D^+D^-$
creates ONLY D pairs

Fully reconstruct one D

- Can then infer neutrinos (constrained kinematics)
- or get absolute hadronic BFs

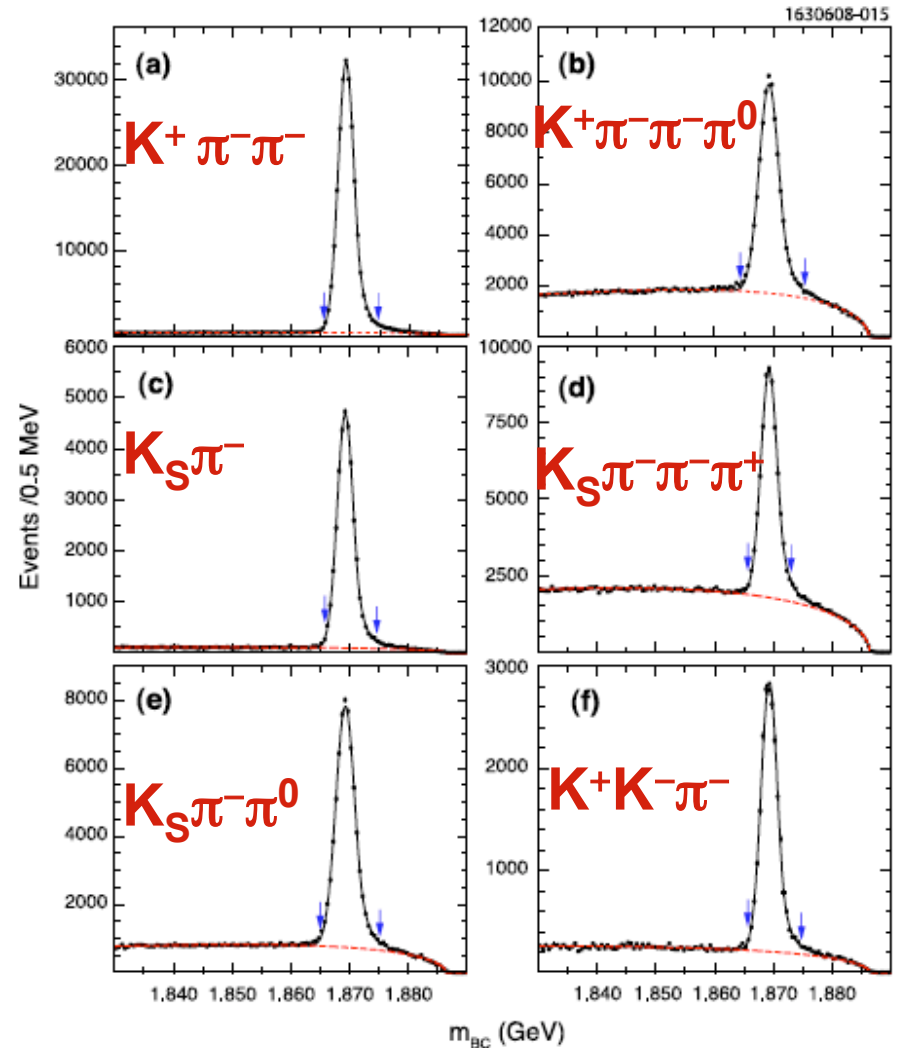
Typical tag rate per D:
15% / 10% / 5%
 D^0 / D^+ / D_s

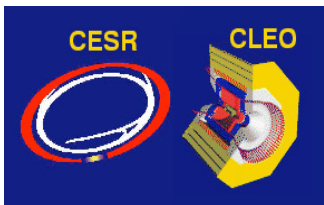
Belle (for D_s only):

Has used a similar technique,
with exclusive final states
from continuum at 10 GeV

CLEO-c D^- Tags

= fully-recon. hadronic decay





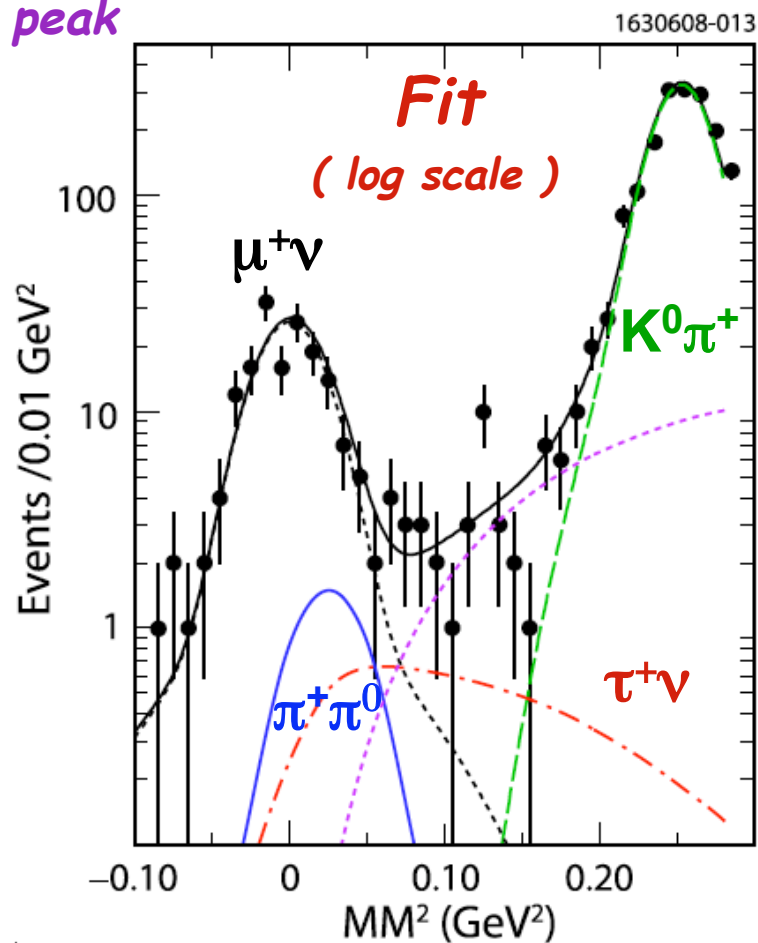
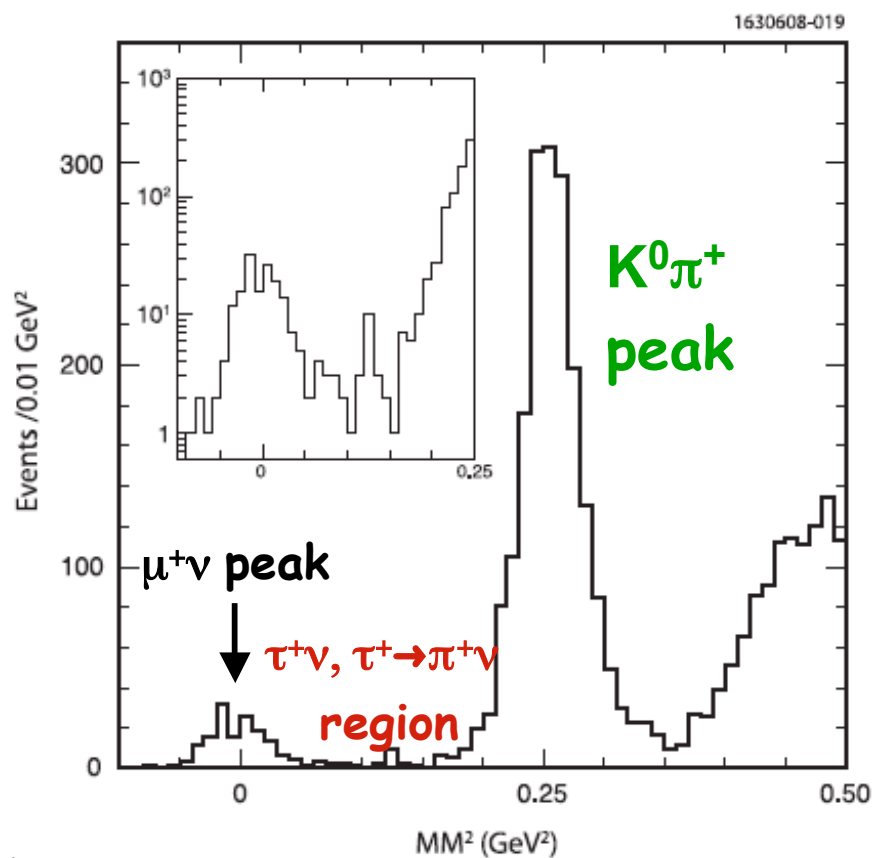
PRD 78, 052003
2008 818 pb⁻¹

Neutrino from 4-momentum balance
can plot (missing mass)²: MM^2

Signal side is one track + unobserved neutrino

Veto on extra unmatched showers > 250 MeV

>>> D-tagging gives a clean, isolated signal peak



Systematics: Backgrounds

PRD 78, 052003
2008 818 pb⁻¹

Previous page, signal plot:

"muon": <300 MeV in CsI calorimeter

This page, background check:

"muon": >300 MeV in CsI calorimeter

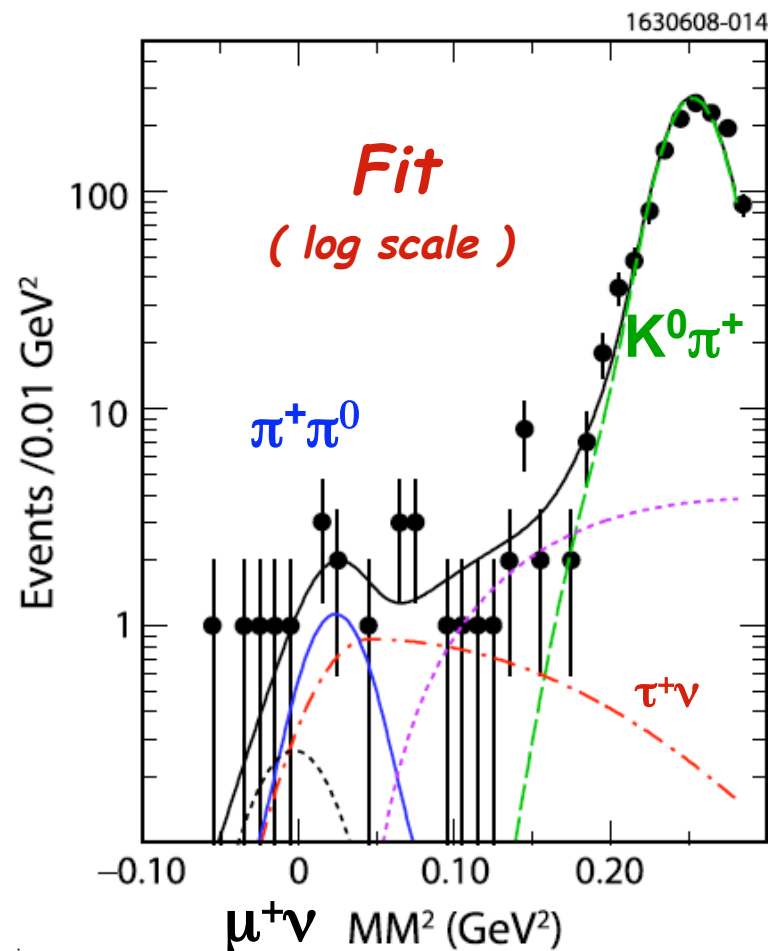
$\tau^+\nu$, $\tau^+ \rightarrow \pi^+\nu$ shows up in both

$\pi^+\pi^0$ background would be problematic,
but is small and well-simulated

$\tau^+\nu$ has known kinematics,
rate related to signal in SM

Tails of the $K^0\pi^+$ peak will be
shown to be well-understood next...

Other backgrounds are small,
and peak away from signal region



Systematics: Resolution

PRD 78, 052003
2008 818 pb⁻¹

Missing-mass is intrinsically powerful,
*But one needs to understand resolution,
including mis-reconstruction.*

In data, tag one D:

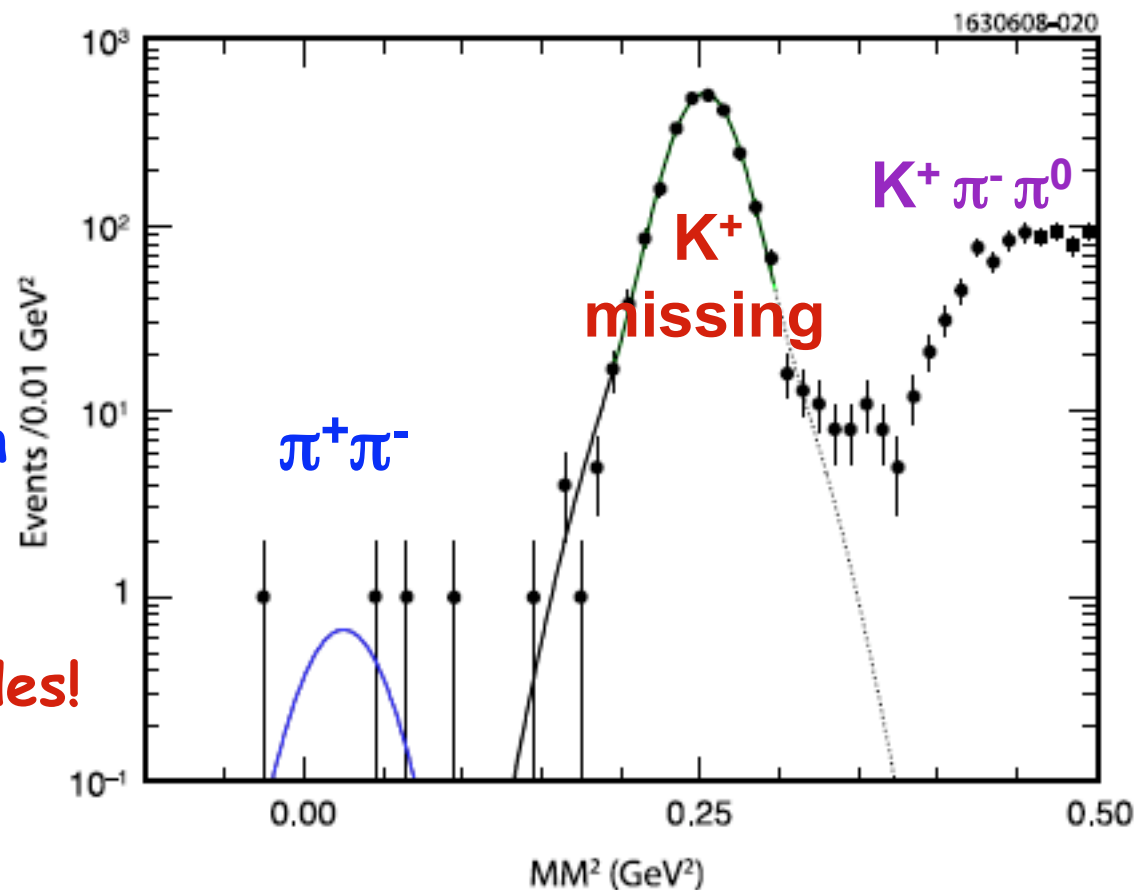


Study other D:



ignore a well-ID'd Kaon

Nice double-Gaussian
resolution over 3 decades!



Systematic Error Summary

PRD 78, 052003
2008 818 pb⁻¹

Error on f_D is 1/2 of this

Already only
1.1% on f_D !

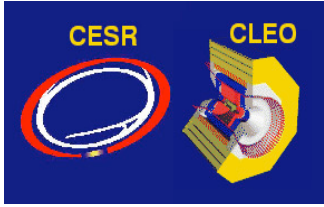
No one dominant
Source of error.

May be hard
to improve ???

TABLE III. Systematic errors on the $D^+ \rightarrow \mu^+ \nu$ branching ratio.

	Systematic errors (%)
Track finding	0.7
PID cut	1.0
MM ² width	0.2
Minimum ionization cut	1.0
Number of tags	0.6
Extra showers cut	0.4
Radiative corrections	1.0
Background	0.7
Total	2.2

But... most of systematics are based on data.



$D^+ \rightarrow \mu^+ \nu$ Results

PRD 78, 052003
2008 818 pb⁻¹

Fix $\tau\nu/\mu\nu$ at SM ratio of 2.65 :

$$\mathcal{B}(D^+ \rightarrow \mu^+ \nu) = (3.82 \pm 0.32 \pm 0.09) \times 10^{-4}$$

$$f_{D^+} = (205.8 \pm 8.5 \pm 2.5) \text{ MeV} \quad [\pm 4.1\% \pm 1.2\%]$$

Best number in context of SM

Float $\tau\nu/\mu\nu$:

$$\mathcal{B}(D^+ \rightarrow \mu^+ \nu) = (3.93 \pm 0.35 \pm 0.10) \times 10^{-4}$$

$$f_{D^+} = (207.6 \pm 9.3 \pm 2.5) \text{ MeV} \quad \text{consistent}$$

Best number for use with Non-SM models

(Only small loss of precision)

Note: numbers are radiatively corrected; -1% on BR



Belle: $D_s \rightarrow \mu^+ \nu$

PRL 100, 241801
(2008) 548 fb⁻¹

Use "Continuum tagging":

$$e^+e^- \rightarrow D^{\pm,0} K^{\pm,0} X D_s^*,$$

"X" = $n\pi$ -or- $n\pi \gamma$ (fragmentation)

about 25% of D BF used

Use recoil mass:

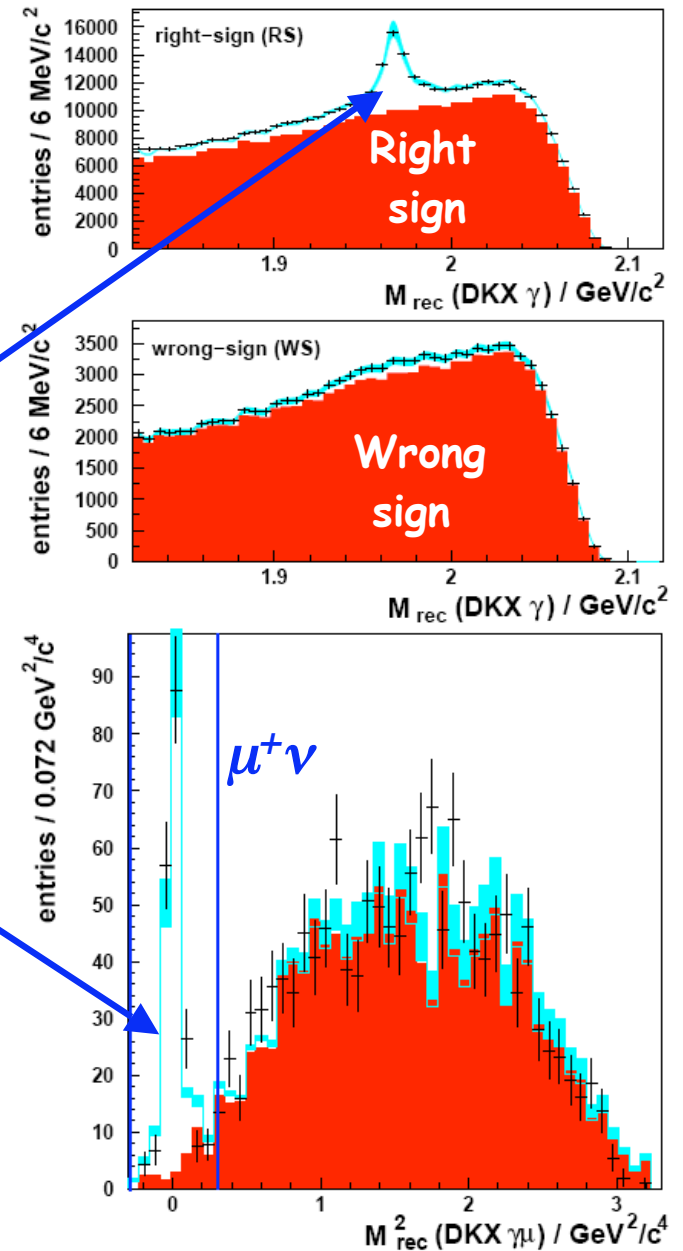
against $DKX\gamma$ counts total D_s

against $DKX\gamma\mu$ counts $D_s \rightarrow \mu^+ \nu$

$$\mathcal{B}(D_s^+ \rightarrow \mu^+ \nu) = (0.644 \pm 0.076 \pm 0.057)\%$$

$$f_{D_s} = 274 \pm 16 \pm 12 \text{ MeV}^* \\ [\pm 5.8\% \pm 4.4\%]$$

* including radiative correction of -1% in BR





Belle: $D_s \rightarrow \mu^+ \nu$

PRL 100, 241801
(2008) 548 fb⁻¹

Systematic error totals 4.4% on f_D

3.2% MC statistics

2.2% background

1.5% Tag simulation

1.4% Muon ID

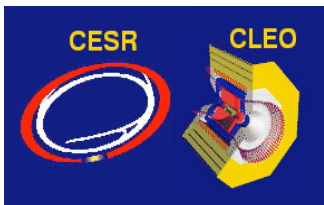
Many checks with careful attention paid to tags:
simulation accuracy, stability of result, ...

Super B Factory: 3.2 ab⁻¹ = final CLEO-c stat error

Need to control systematics 3x better to match CLEO-c

That may not be crazy, but may be hard to push far beyond ?

Still would be a nice independent cross-check



$$D_s \rightarrow \mu^+ \nu \text{ \& \ } \tau^+ \nu$$

$$(\tau^+ \rightarrow \pi^+ \nu)$$

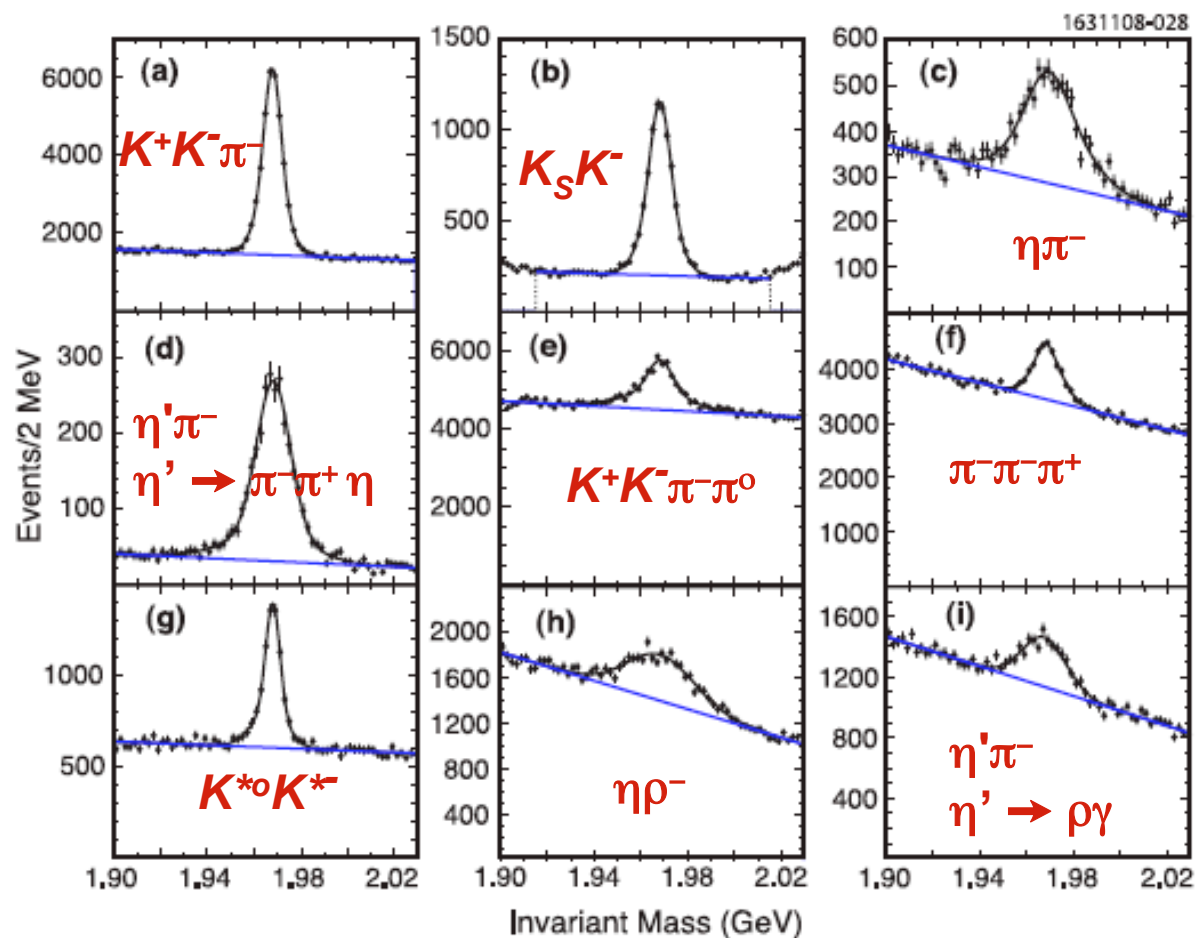
PRD 79, 052001
(2009) 600 pb⁻¹

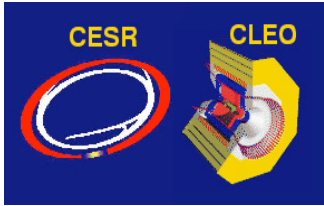
D_s : Larger leptonic BF, but tougher for tagging

Use data from 4170 MeV: $D_s^{*+} D_s^- + c.c$ events

On top of uds +*plus* other charm continuum

Invariant mass
of 9 tag modes





$$D_s \rightarrow \mu^+ \nu \text{ \& \ } \tau^+ \nu$$

$$(\tau^+ \rightarrow \pi \nu)$$

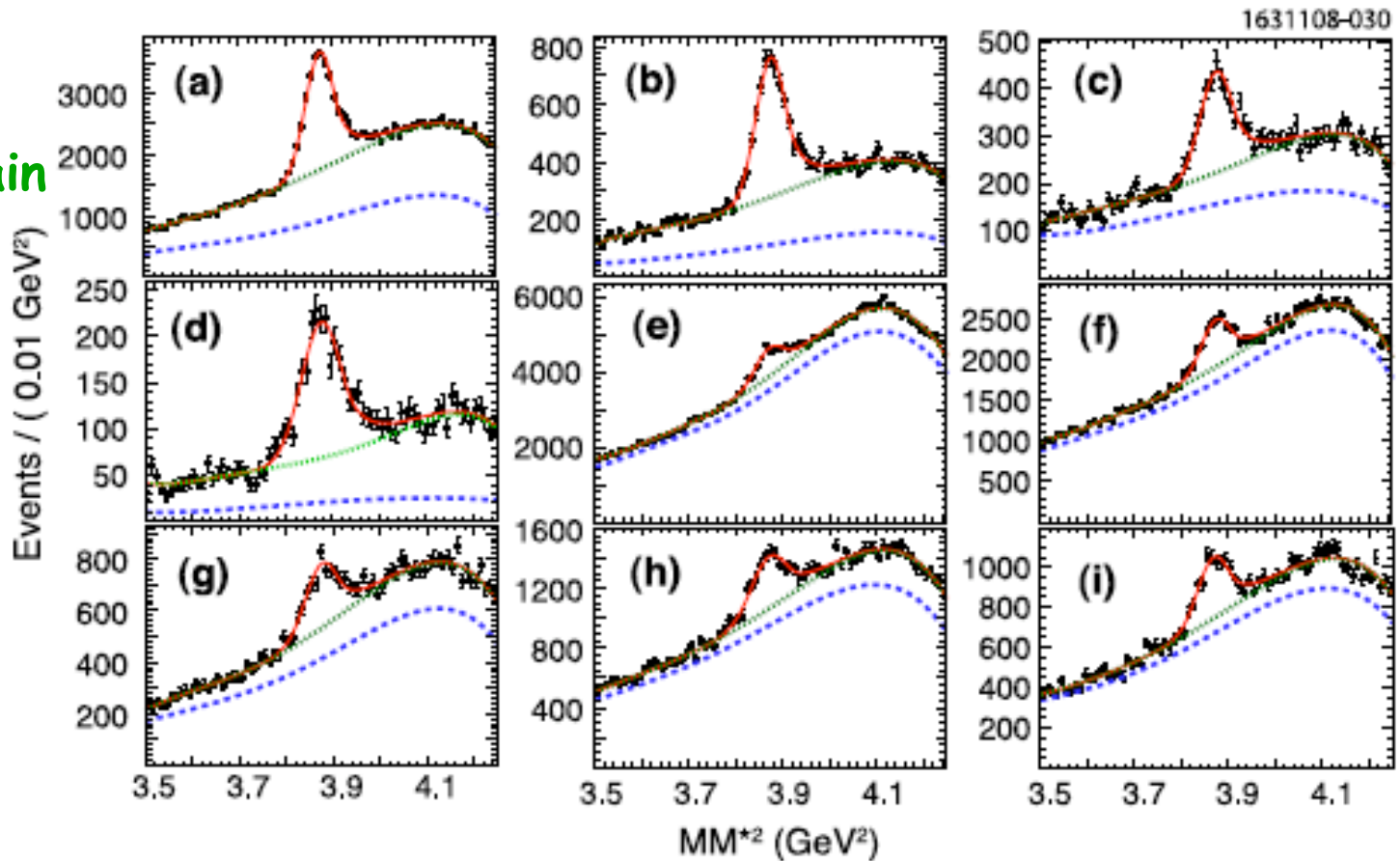
PRD 79, 052001
(2009) 600 pb⁻¹

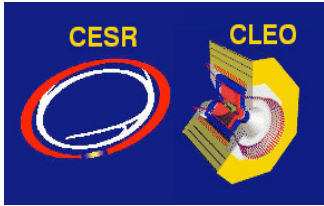
Look at missing mass after adding photon

(from $D_s^* \rightarrow D_s \gamma$)

Plot missing-mass² against $D_s \gamma$ system

Need photon
to fully constrain
the other D_s ...





More on the Method...

PRD 79, 052001
(2009) 600 pb⁻¹

As with D⁺ analysis, separate two cases:

Case (i): signal track deposits <300 MeV in CsI calorimeter

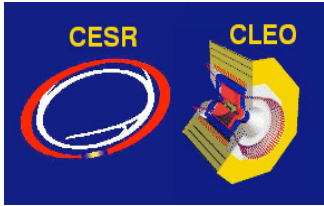
dominantly $\mu^+\nu$ (but $\sim 1/2$ of $\tau^+\nu$, $\tau^+\rightarrow\pi^+\nu$ is also here)

Case (ii): signal track deposits >300 MeV in CsI calorimeter

dominantly $\tau^+\nu$ ($\sim 1/2$ of $\tau^+\nu$, $\tau^+\rightarrow\pi^+\nu$; very little $\mu^+\nu$)

Similar to D⁺ case: Veto on extra unmatched showers > 300 MeV

First, I will show combined data, then separated...



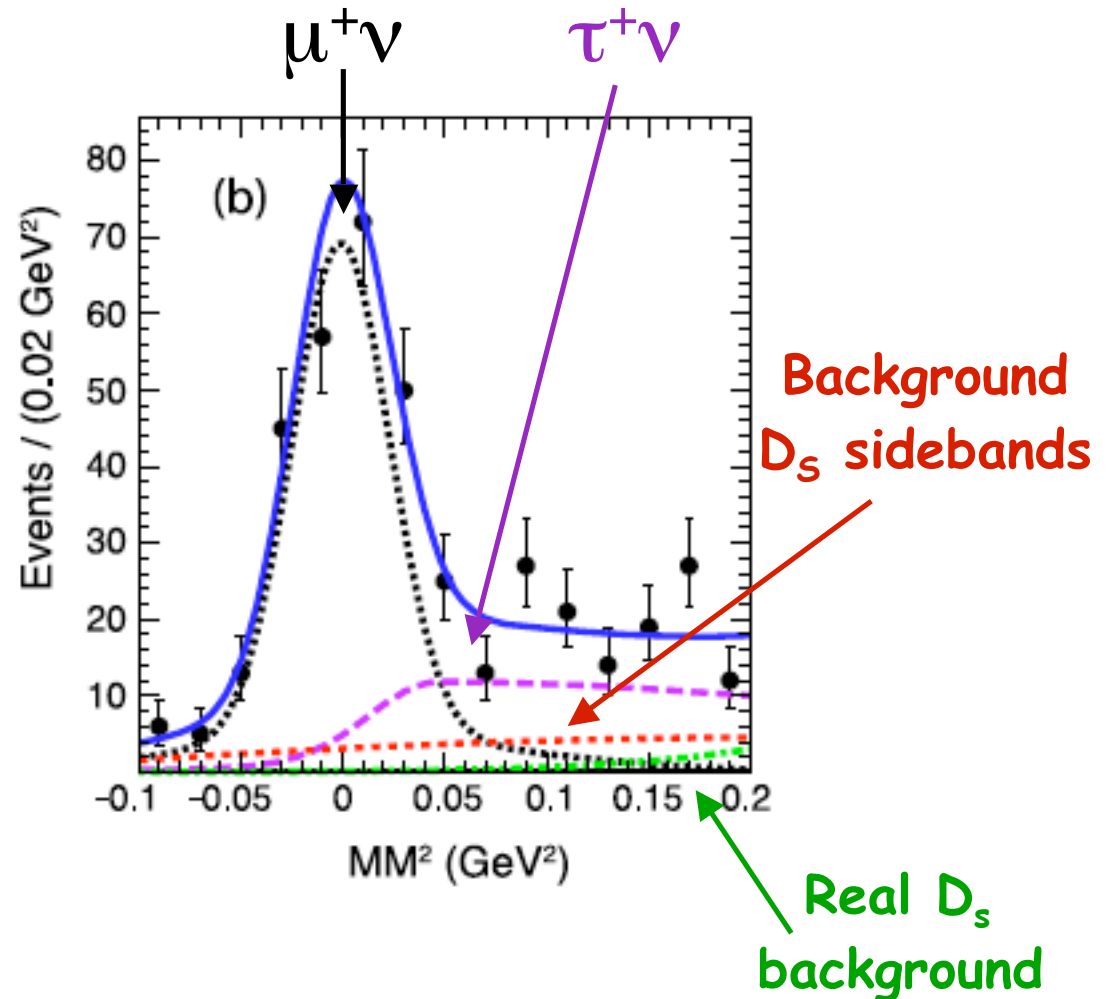
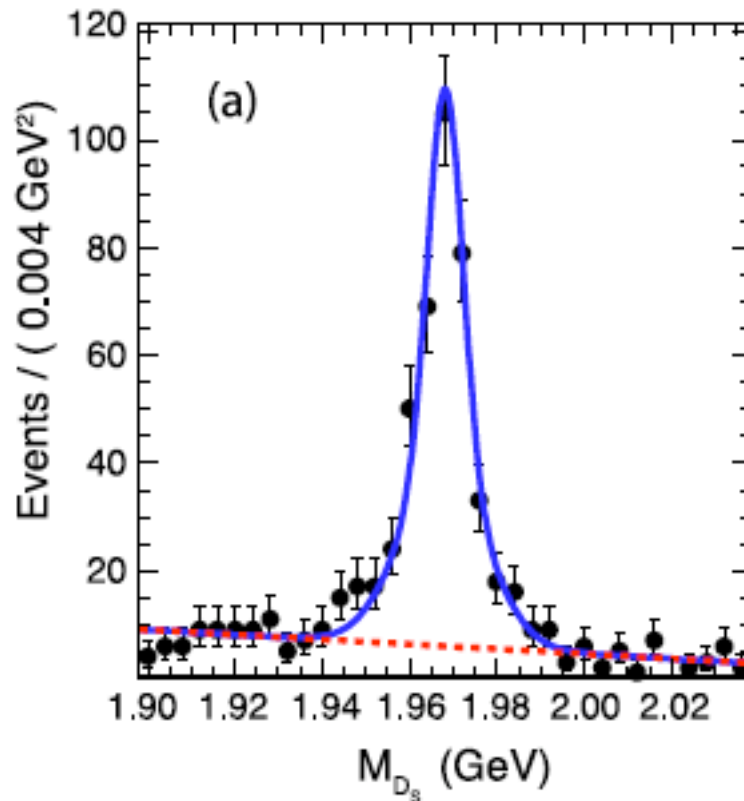
$$D_s \rightarrow \mu^+ \nu \text{ \& \ } \tau^+ \nu$$

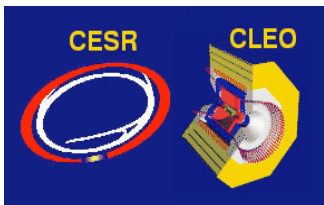
$$(\tau^+ \rightarrow \pi \nu)$$

PRD 79, 052001
(2009) 600 pb⁻¹

2-dimensional fit
to D_s Tag mass and
missing-mass-squared

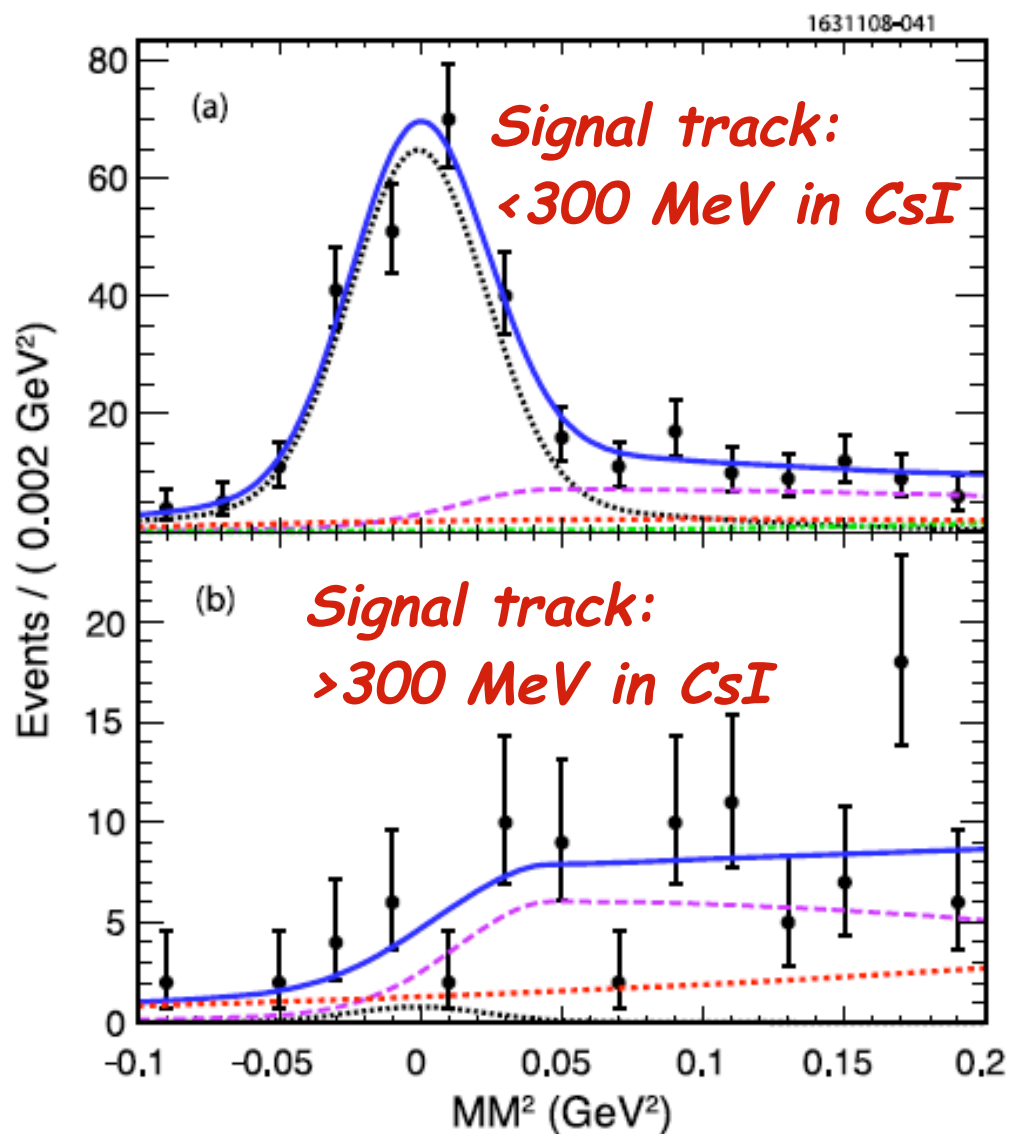
Two signal modes





Separated Data

PRD 79, 052001
(2009) 600 pb⁻¹



Color-code:

$\mu^+\nu$

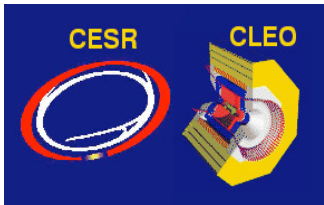
$\tau^+\nu$

Background

D_s sidebands

Real D_s

background



Backgrounds

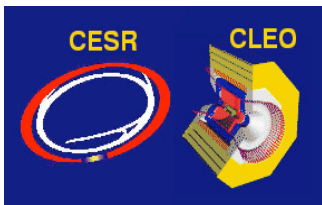
PRD 79, 052001
(2009) 600 pb⁻¹

TABLE II. Background estimates for the data in the signal region $-0.1 < MM^2 < 0.2 \text{ GeV}^2$. (We assume $\mathcal{B}(D_s^+ \rightarrow \tau^+ \nu) = 6.2 \pm 0.7\%$.)

Final State	\mathcal{B} (%)	# of events case(i)	# of events case (ii)
$\tau^+ \rightarrow \pi^+ \pi^0 \bar{\nu}$	1.6 ± 0.2	2.06 ± 0.34	1.43 ± 0.36
$\tau^+ \rightarrow \mu^+ \nu \bar{\nu}$	1.1 ± 0.1	1.60 ± 0.24	0
$D_s^+ \rightarrow \pi^+ \pi^0 \pi^0$	1.1 (estimate)	0.12	0.12
$D_s^+ \rightarrow K^0 \pi^+$	0.24 ± 0.03	1.3 ± 0.3	1.1 ± 0.3
$D_s^+ \rightarrow \eta \pi^+$	1.5 ± 0.2	1.1 ± 0.3	0.9 ± 0.3
Sum		6.2 ± 0.7	3.5 ± 0.6

Rates are for
full range of
signal plots
I've shown...

For reference, $\mu^+ \nu$ signal is 235.5 ± 13.8 events



Systematic Errors

PRD 79, 052001
(2009) 600 pb⁻¹

Error on f_{D_s} is 1/2 on this

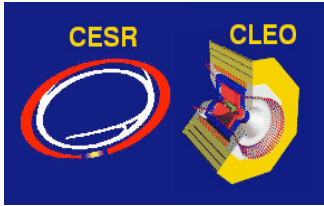
TABLE III. Systematic errors on determination of the $D_s^+ \rightarrow \mu^+ \nu$ branching fraction.

Error Source	Size (%)
Track finding	0.7
Particle identification of μ^+	1.0
MM ² width	0.2
Photon veto	0.4
Background	1.0
Number of tags	2.0
Tag bias	1.0
Radiative Correction	1.0
Total	3.0

Largest single error
is # tags:
might be better at
4030 MeV, with no D_s^*
(but only 30%
of cross-section!)

$$f_{D_s} = (263.3 \pm 8.2 \pm 3.9) \text{ MeV} \quad [\pm 3.1\% \pm 1.5\%]$$

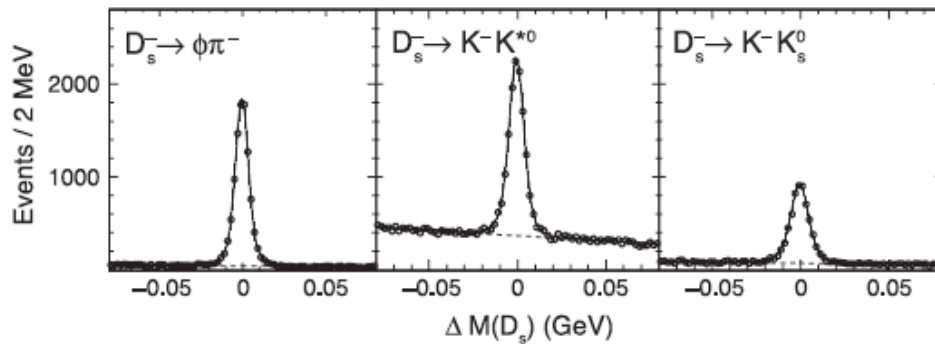
$$\Gamma(D^+ \rightarrow \tau^+ \nu) / \Gamma(D^+ \rightarrow \mu^+ \nu) = 11.74 \pm 1.7 \pm 0.2 \quad [SM = 9.76]$$



$$D_s \rightarrow \tau^+ \nu \quad (\tau^+ \rightarrow e^+ \nu \nu)$$

PRD 79, 052002
(2009) 602 pb⁻¹

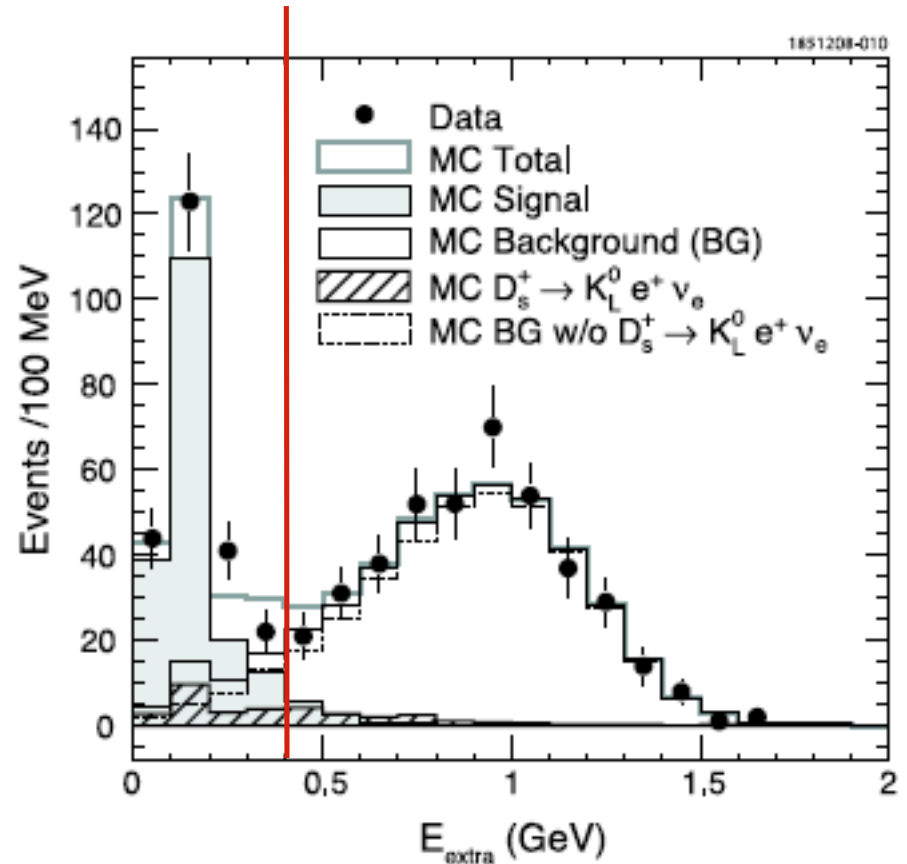
Uses only cleanest tags:



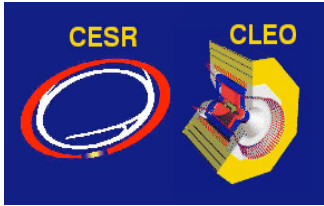
Always have >1 neutrino!
Abandon use of MM²
 Semileptonic events tend to
 have hadronic Energy in CsI
 (but careful re: K_L !)

Plot E_{extra} in Calorimeter
(Extra: not tag or e)

Signal region:
<400 MeV



Peaks away from zero:
E_{extra} can include γ from D_s^{} decay*



Systematic Errors

PRD 79, 052002
(2009) 602 pb⁻¹

Error on f_{D_s} is 1/2 of this

Source	Effect on \mathcal{B} (%)
Background (nonpeaking)	0.7
$D_s^+ \rightarrow K_L^0 e^+ \nu_e$ (peaking)	3.2
Extra shower	1.1
Extra track	1.1
$Q_{\text{net}} = 0$	1.1
Non electron	0.1
Secondary electron	0.3
Number of tag	0.4
Tag bias	0.2
Tracking	0.3
Electron identification	1.0
FSR	1.0
Total	4.1

Errors on f_{D_s} :

1.6% from $K_L e \nu$
(BR + energy deposit)

1.3% all others
combined

$$f_{D_s} = (252.5 \pm 11.1 \pm 5.2) \text{ MeV} \quad [\pm 4.4\% \pm 2.1\%]$$

Note: rad. corr. is small, since tau has only 9 MeV kin. E

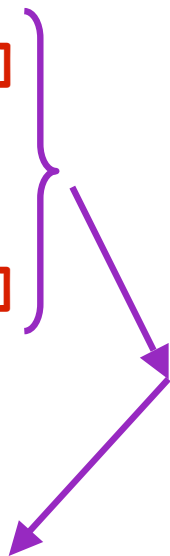
Combining CLEO-c

$$D_s \rightarrow \tau^+ \nu \quad (\tau^+ \rightarrow e^+ \nu \nu)$$

$$f_{D_s} = (252.5 \pm 11.1 \pm 5.2) \text{ MeV} \quad [\pm 4.4\% \pm 2.1\%]$$

$$D_s \rightarrow \mu^+ \nu, \tau^+ \nu \quad (\tau^+ \rightarrow \pi^+ \nu)$$

$$f_{D_s} = (263.3 \pm 8.2 \pm 3.9) \text{ MeV} \quad [\pm 3.1\% \pm 1.5\%]$$



Combine two CLEO-c D_s results; recall D result

$$f_{D_s} = (259.5 \pm 6.6 \pm 3.1) \text{ MeV} \quad [\pm 2.5\% \pm 1.2\%]$$

$$f_D = (205.8 \pm 8.5 \pm 2.5) \text{ MeV} \quad [\pm 4.1\% \pm 1.2\%]$$

D_s / D Ratio:

$$f_{D_s} / f_D = 1.26 \pm 0.06 \pm 0.02$$

Khodjamirian obtains bounds: $f_D < 230 \text{ MeV}$ $f_{D_s} < 270 \text{ MeV}$

(from 2-pt. Correlation functions; arXiv:0812:3747v1)

Experiment vs. Theory

Final CLEO f_{D^+} result:	$f_D = 205.8 \pm 8.9 \text{ MeV}$
2+1 unquenched lattice QCD*	$208 \pm 4 \text{ MeV}$
2+1 unquenched lattice QCD**	$207 \pm 11 \text{ MeV}$

Excellent Agreement, to ~5% (7%) accuracy

Final CLEO $f_{D_s^+}$ result:	$f_{D_s} = 259.5 \pm 7.3 \text{ MeV}$
2+1 unquenched lattice QCD obtains*	$241 \pm 3 \text{ MeV}$
2+1 unquenched lattice QCD obtains**	$249 \pm 11 \text{ MeV}$

*2.3 σ high ? **Or need more accuracy?

CLEO-c ratio of $f_{D_s^+} / f_{D^+}$	$f_{D_s} / f_D = 1.26 \pm 0.06$
2+1 unquenched lattice QCD obtains*	1.162 ± 0.009
2+1 unquenched lattice QCD obtains**	1.20 ± 0.024

*1.6 σ high ? **Or need more accuracy?

* Follana et al. (HPQCD/UKQCD), PRL 100, 062002 (2008)

** Bernard et al. (FNAL/MILC), arXiv:0904.1895

Other predictions are in backup slides.

If D_s Discrepancy is Real...

Models need to raise f_{D_s} without much effect on f_D

Dobrescu & Kronfeld argue that possible New Physics could be either a charged Higgs (their own model) or leptoquarks
[PRL 100, 241802 (2008)]

Kundu & Nandi suggest R-parity violating SUSY to explain large f_{D_s} and B_s mixing phase [PRD 78, 015009 (2008)]

Hewett, and Akeroyd & Chen, also discussed 2 Higgs doublet model
[H: arXiv:hep-ph/9505246
A: PrThPh 111, 295 (2004); A&C: PRD 75 075004 (2007)]

Note that mass-dependent Higgs couplings exactly mimic the V-A helicity suppression, preserving the $e:\mu:\tau$ ratio

Electron Mode Limits

CLEO-c

$$B(D^+ \rightarrow e^+\nu) < 8.8 \times 10^{-6} \quad [960 \times \text{SM expectation}]$$

No events in signal area

$$B(D_s^+ \rightarrow e^+\nu) < 1.2 \times 10^{-4} \quad [890 \times \text{SM expectation}]$$

One event in signal area

CP-Asymmetries

CLEO-c

$$[\Gamma(D^+ \rightarrow \mu^+\nu) - \Gamma(D^- \rightarrow \mu^-\nu)] / (\text{SUM}) = (8 \pm 8) \%$$

$$[\Gamma(D_s^+ \rightarrow \mu^+\nu) - \Gamma(D_s^- \rightarrow \mu^-\nu)] / (\text{SUM}) = (4.8 \pm 6.1) \%$$

The Future

CLEO-c @ Charm Threshold: Largely Done

- Both f_D , f_{D_s} together (and two D_s methods)
- Also best semileptonic results:
can ratio out CKM $|V_{cq}|$ for pure LQCD test, etc.

BESIII @ Charm Threshold:

- Now at $3 \times 10^{32} \text{ cm}^{-2}\text{s}^{-1}$ [$\sim 4x$ CLEO-c; goal is 10×10^{32}]
- 12x (4x) CLEO data for D (D_s) would lower statistical errors
to equal the CLEO-c systematics

Super B Factories

- Updated f_{D_s} ? (f_D not feasible)
- Need to maintain detector understanding at very high rates
- Likely syst. limitations, BUT the only cross-check on the horizon

Conclusions

Experiment:

- The future is luminosity *plus* systematic error control

Lattice QCD

- More methods reaching high-precision
- Continuing CPU, technical advances

Phenomenology:

- Models that can accommodate possible deviations

BACKUP SLIDES

f_{D_s} Results Summary

TABLE V. Our results for $\mathcal{B}(D_s^+ \rightarrow \mu^+ \nu)$, $\mathcal{B}(D_s^+ \rightarrow \tau^+ \nu)$, and $f_{D_s^+}$ compared with previous measurements. Results have been updated for the new value of the D_s lifetime of 0.5 ps [12]. ALEPH combines both measurements to derive a value for the decay constant. (This table adopted from Table I of ref. [7].)

Exp.	Mode	\mathcal{B}	$\mathcal{B}_{\phi\pi}$ (%)	$f_{D_s^+}$ (MeV)
CLEO-c	$\mu^+ \nu$	$(5.65 \pm 0.45 \pm 0.17) \times 10^{-3}$		$257.3 \pm 10.3 \pm 3.9$
CLEO-c	$\tau^+ \nu$	$(6.42 \pm 0.81 \pm 0.18) \times 10^{-2}$		$278.7 \pm 17.1 \pm 3.8$
CLEO-c		combined above 2 results using SM		$263.3 \pm 8.2 \pm 3.9$
CLEO-c [2]	$\tau^+ \nu$	$(5.30 \pm 0.47 \pm 0.22) \times 10^{-2}$		$252.5 \pm 11.1 \pm 5.2$
CLEO-c		combined all CLEO-c results		$259.5 \pm 6.6 \pm 3.1$
Belle ^a [21]	$\mu^+ \nu$	$(6.38 \pm 0.76 \pm 0.52) \times 10^{-3}$		$274 \pm 16 \pm 12$
Average of CLEO and Belle results above, radiatively corrected				261.2 ± 6.9
CLEO [14]	$\mu^+ \nu$	$(6.2 \pm 0.8 \pm 1.3 \pm 1.6) \times 10^{-3}$	3.6 ± 0.9	$273 \pm 19 \pm 27 \pm 33$
BEATRICE [15]	$\mu^+ \nu$	$(8.3 \pm 2.3 \pm 0.6 \pm 2.1) \times 10^{-3}$	3.6 ± 0.9	$312 \pm 43 \pm 12 \pm 39$
ALEPH [16]	$\mu^+ \nu$	$(6.8 \pm 1.1 \pm 1.8) \times 10^{-3}$	3.6 ± 0.9	$282 \pm 19 \pm 40$
ALEPH [16]	$\tau^+ \nu$	$(5.8 \pm 0.8 \pm 1.8) \times 10^{-2}$		
L3 [17]	$\tau^+ \nu$	$(7.4 \pm 2.8 \pm 1.6 \pm 1.8) \times 10^{-2}$		$299 \pm 57 \pm 32 \pm 37$
OPAL [18]	$\tau^+ \nu$	$(7.0 \pm 2.1 \pm 2.0) \times 10^{-2}$		$283 \pm 44 \pm 41$
BABAR [19]	$\mu^+ \nu$	$(6.74 \pm 0.83 \pm 0.26 \pm 0.66) \times 10^{-3}$	4.71 ± 0.46	$283 \pm 17 \pm 7 \pm 14$

^aThis result has been radiatively corrected by multiplying the measured branching ratio by 99%.

Table from CLEO-c f_{D_s} paper

f_{D^*}, f_{D_s} Prediction Summary

TABLE VI. Theoretical predictions of $f_{D_s^*}$, f_{D^*} , and $f_{D_s^*}/f_{D^*}$. QL indicates quenched lattice calculations. (This table adopted from Table II of ref. [7].)

Model	$f_{D_s^*}$ (MeV)	f_{D^*} (MeV)	$f_{D_s^*}/f_{D^*}$
Lattice (HPQCD+UKQCD) [6]	241 ± 3	208 ± 4	1.162 ± 0.009
Lattice (FNAL+MILC+HPQCD) [5]	$249 \pm 3 \pm 16$	$201 \pm 3 \pm 17$	$1.24 \pm 0.01 \pm 0.07$
QL (QCDSF) [36]	$220 \pm 6 \pm 5 \pm 11$	$206 \pm 6 \pm 3 \pm 22$	$1.07 \pm 0.02 \pm 0.02$
QL (Taiwan) [37]	$266 \pm 10 \pm 18$	$235 \pm 8 \pm 14$	$1.13 \pm 0.03 \pm 0.05$
QL (UKQCD) [38]	$236 \pm 8^{+17}_{-14}$	$210 \pm 10^{+17}_{-16}$	$1.13 \pm 0.02^{+0.04}_{-0.02}$
QL [39]	$231 \pm 12^{+6}_{-1}$	$211 \pm 14^{+2}_{-12}$	1.10 ± 0.02
QCD Sum Rules [40]	205 ± 22	177 ± 21	$1.16 \pm 0.01 \pm 0.03$
QCD Sum Rules [41]	235 ± 24	203 ± 20	1.15 ± 0.04
Field Correlators [42]	210 ± 10	260 ± 10	1.24 ± 0.03
Quark Model [43]	268	234	1.15
Quark Model [44]	248 ± 27	230 ± 25	1.08 ± 0.01
LFQM (Linear) [45]	211	248	1.18
LFQM (HO) [45]	194	233	1.20
LF-QCD [46]	253	241	1.05
Potential Model [47]	241	238	1.01
Isospin Splittings [48]		262 ± 29	

Table from CLEO-c f_{D_s} paper

(FNAL/MILC arXiv:0904.1895 appeared later)

BaBar f_{D_s} Result

BaBar (2007) 230 fb⁻¹
PRL 98, 141801

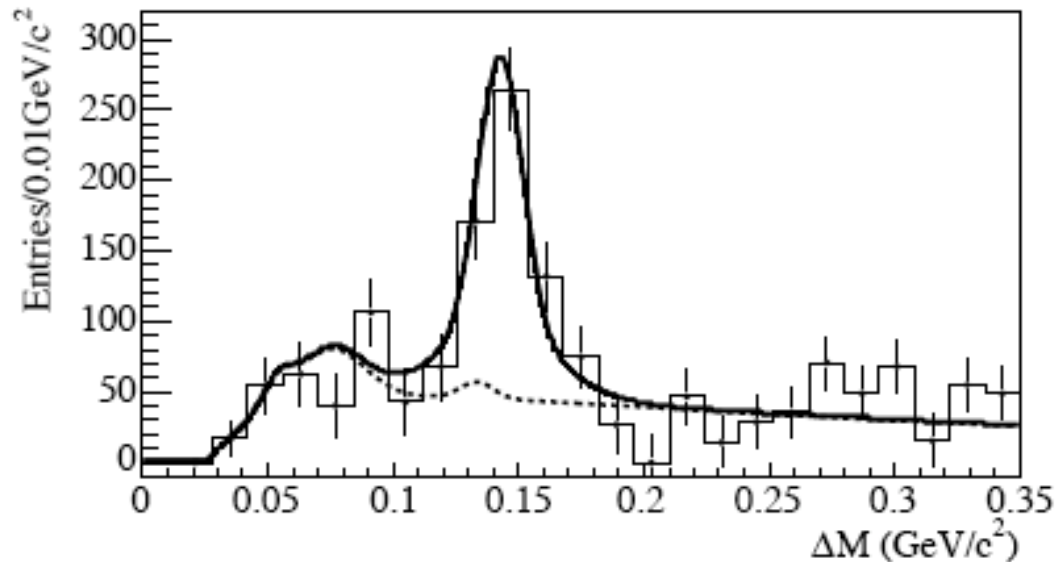


FIG. 3: ΔM distribution after the tag sidebands and the electron sample are subtracted. The solid line is the fitted signal and background distribution ($N_{\text{sig}}f_{\text{sig}} + N_{\text{Bkgd}}f_{\text{Bkgd}}$), the dashed line is the background distribution ($N_{\text{Bkgd}}f_{\text{Bkgd}}$) alone.

$$f_D = 283 \pm 17 \pm 7 \pm 14 \text{ MeV}$$

[last error from $B(\phi\pi)$]