

# **MaGiC - Matter and Gravitation in relativistic Collisions of Neutron Stars and Heavy Ions -probing the EoS of dense matter by Gravitational Waves**

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# Matter and Gravity

1679 I. Newton published his theory of gravitation. According to Newton, gravity manifests itself as an instantaneous force between masses proportional to their masses and inversely proportional distance squared. With this theory he could explain all of the astronomical observations of this time.

1915 A. Einstein published his General Relativity, GR:

Gravity governs the motion of massive bodies mass/energy by curving spacetime.

1915 Karl Schwarzschild, born 1873 in Frankfurt am Main, published the static solution of GR - just after Einsteins article - and died soon after. Consequences of his vision: black and white holes, neutron stars !

Add Einstein's gravitational waves - You see a **whole new Universe**





# Einstein equations first solved by Karl Schwarzschild

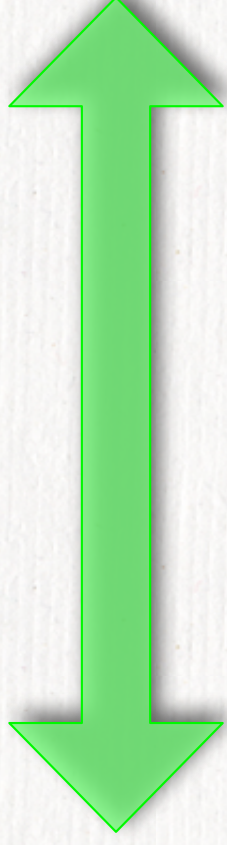
Einstein tensor

stress-energy tensor

$$G_{\mu\nu} = 8\pi T_{\mu\nu}$$

spacetime  
curvature

mass and energy  
in the spacetime

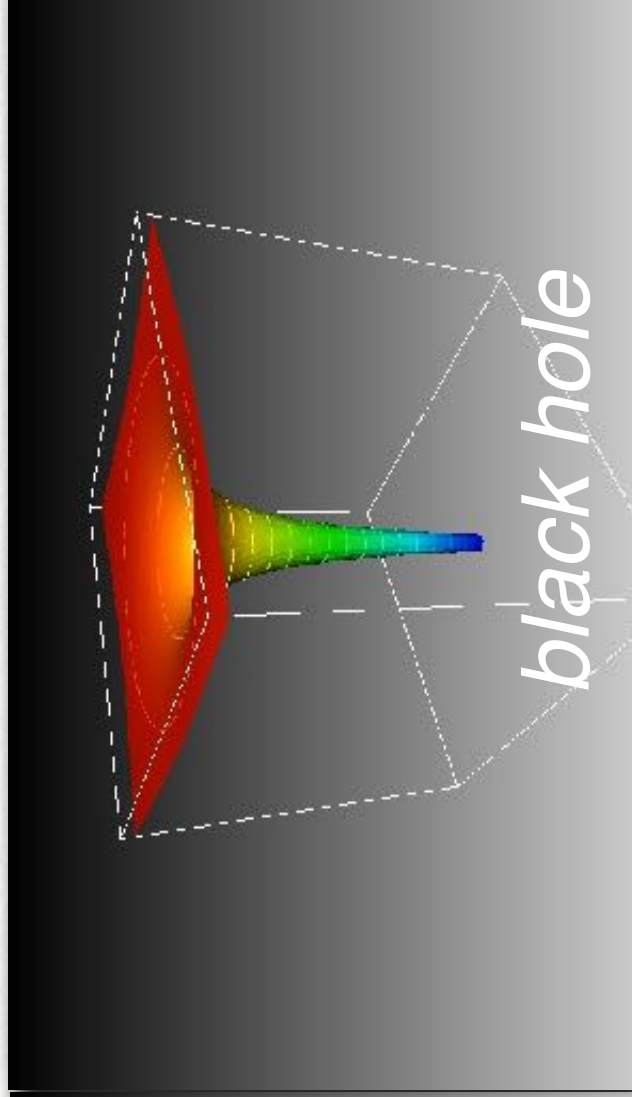
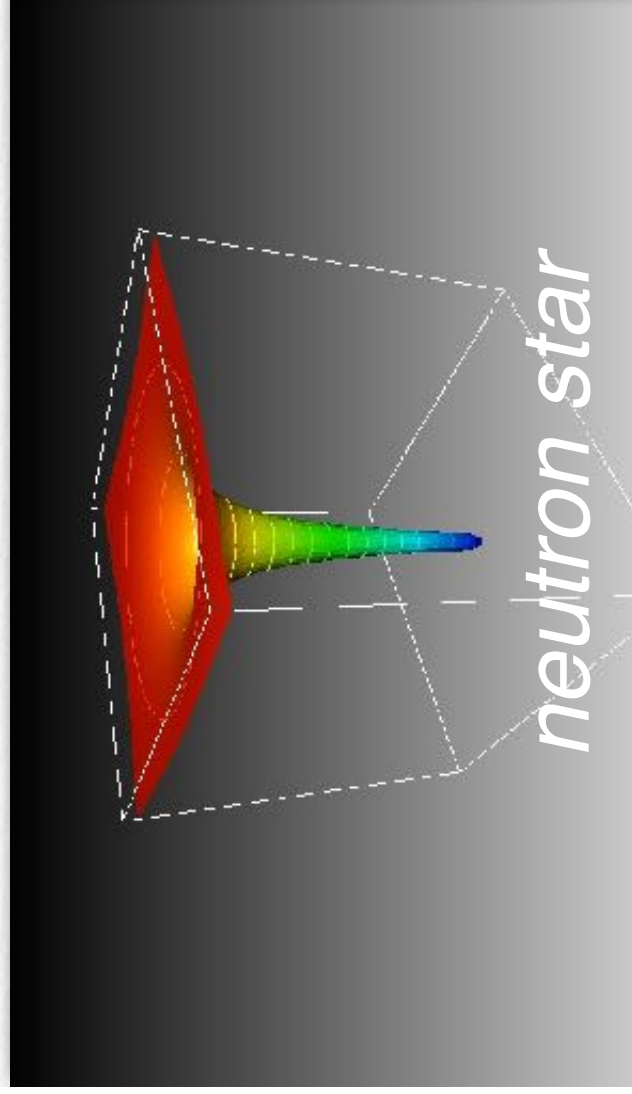


The importance of Einstein equations lies in setting a relation between the **curvature** and the **mass/energy**:

**gravity becomes the manifestation of spacetime curvature**

# Neutron Star or Schwarzschild Black Hole ?

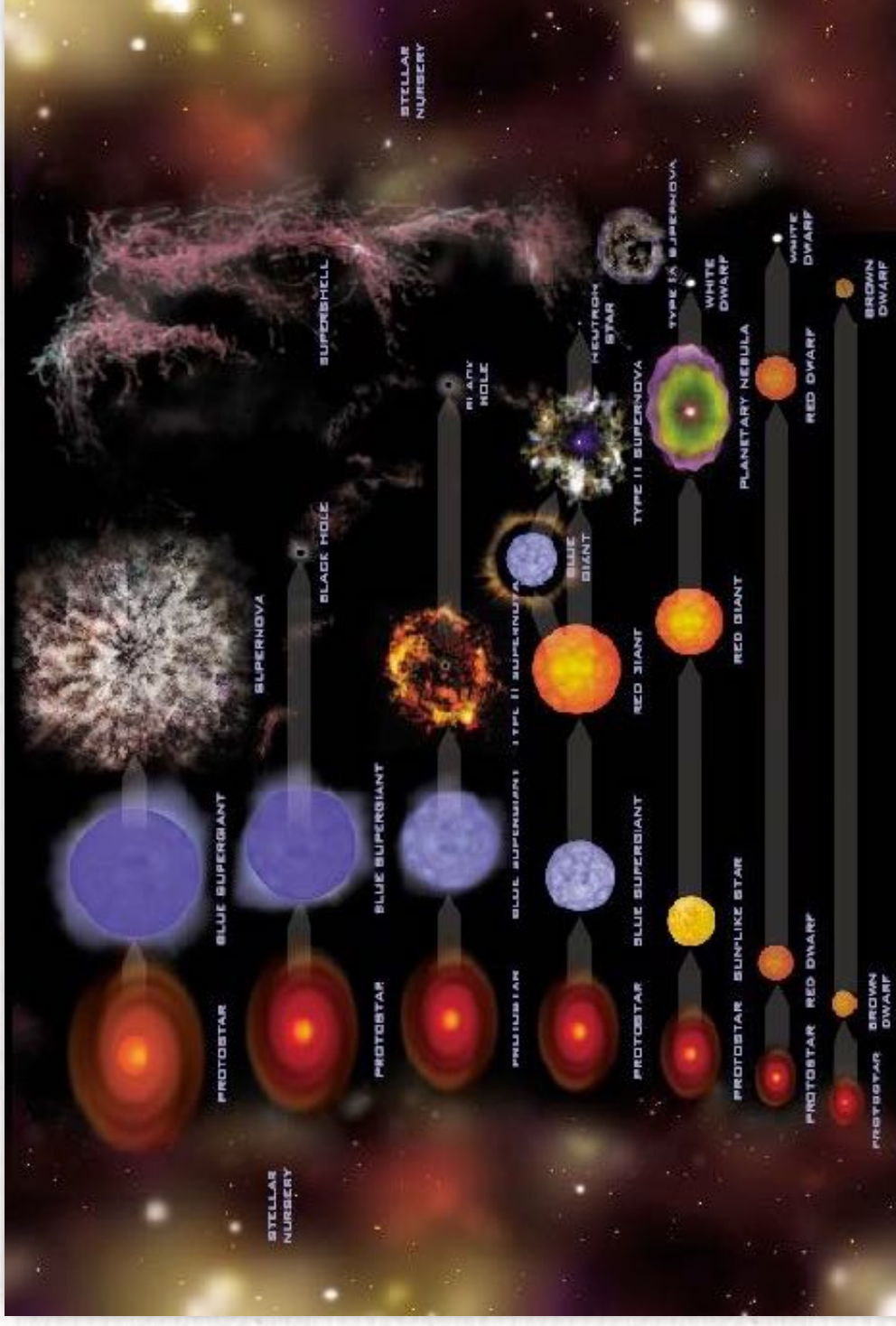
Narrow transition from a very compact star to a black hole  
- many of the spacetime properties are similar.



Two aspects differ: Neutron Stars have a **hard surface**,  
the curvature is large - but **finite** ;  
Black Hole: **No Surface** - curvature is **infinite** at the centre  
- but the SINGULARITY : NEVER divide by zero !



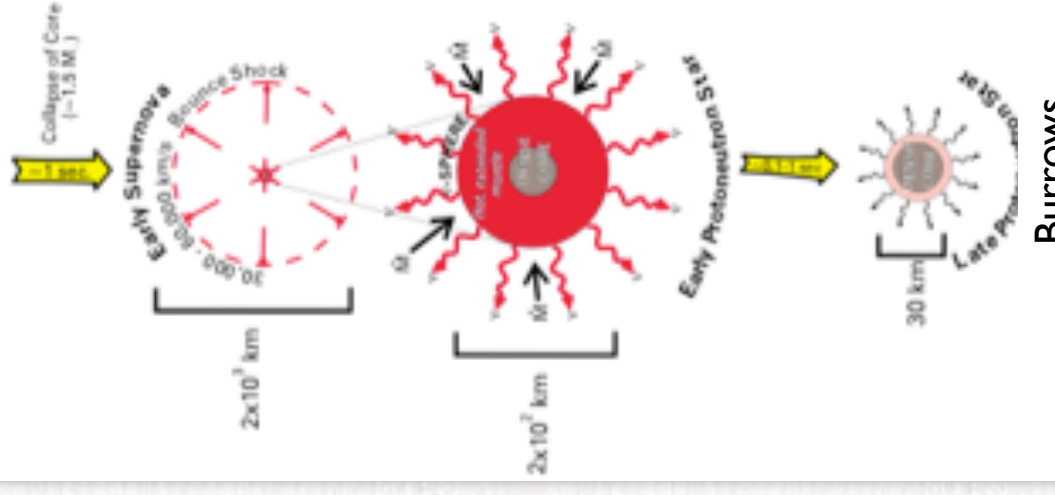
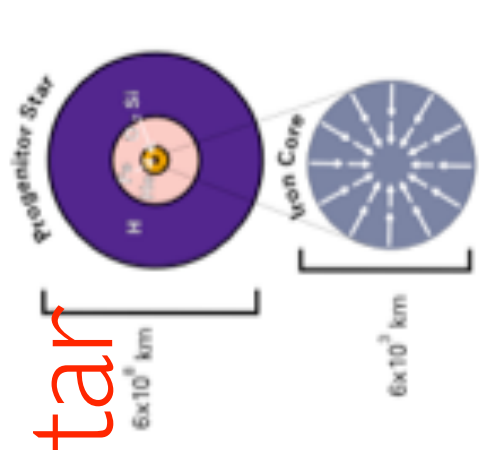
# Birth of neutron star - death of star



Neutron stars are most commonly born in the violent death of massive stars, i.e. stars with

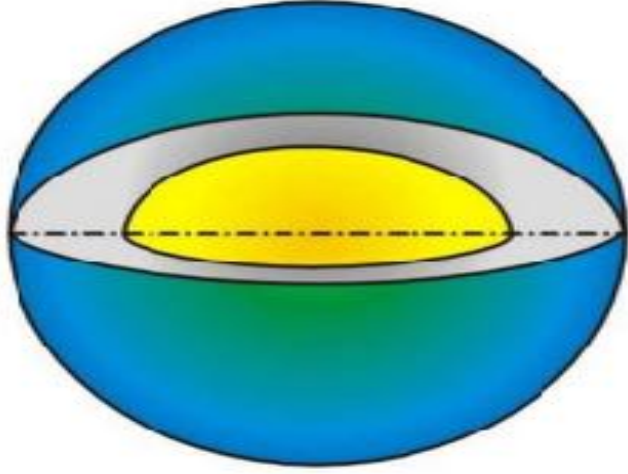
$$10M_{\odot} \lesssim M \lesssim 100M_{\odot}$$

ending their evolution as **supernovae collapse**



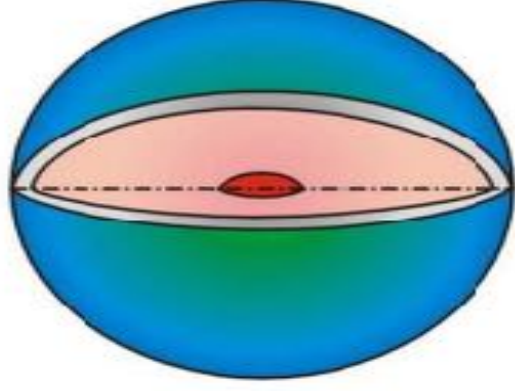
# Neutronstars, Quarkstars, Black holes

Neutron Stars



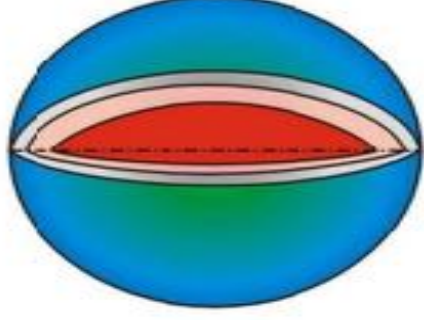
$\rho_c = \rho_0$

Hybrid Stars



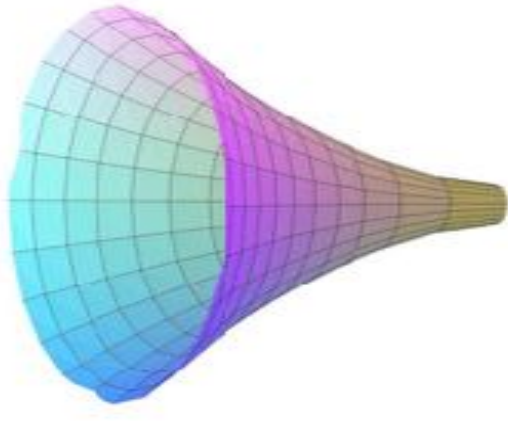
$\approx 2 \rho_0$

Quark Stars



$\approx 5 \rho_0$

Black Holes



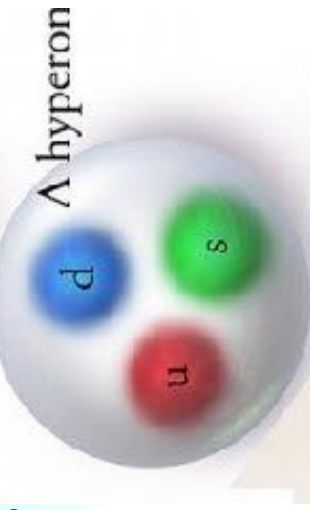
$\dots \infty$

Central density  $\rho_c$  in the star

( $\rho_0 := 0.15/\text{fm}^3$ )

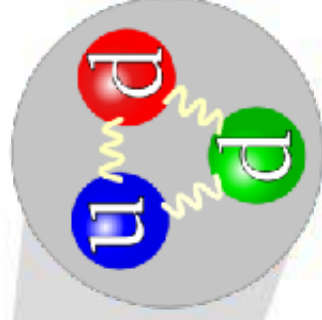
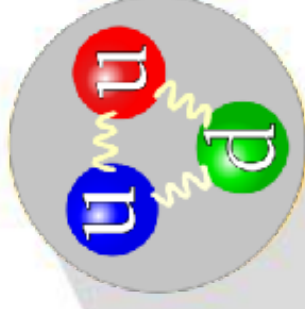


# Nuclear Matter, Hypermatter, Quark Matter



**Proton**

(2 Up-Quarks +  
1 Down-Quark)

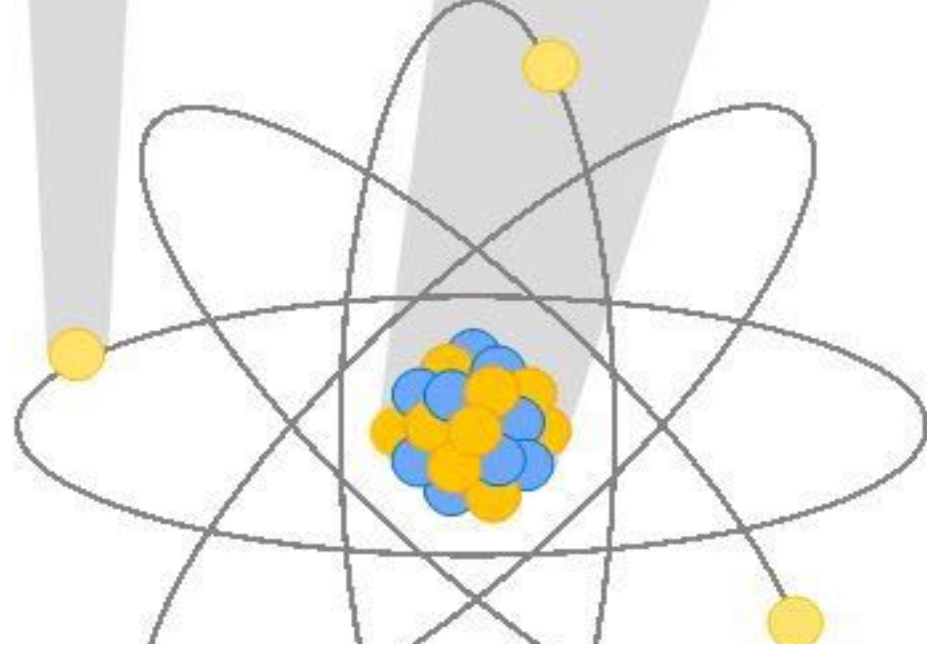


**Neutron**

(1 Up-Quark +  
2 Down-Quarks)

7

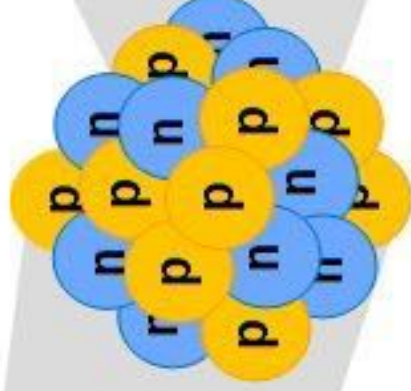
**Elektron**



**Atom**

(Atomkern +  
Elektronenhülle)

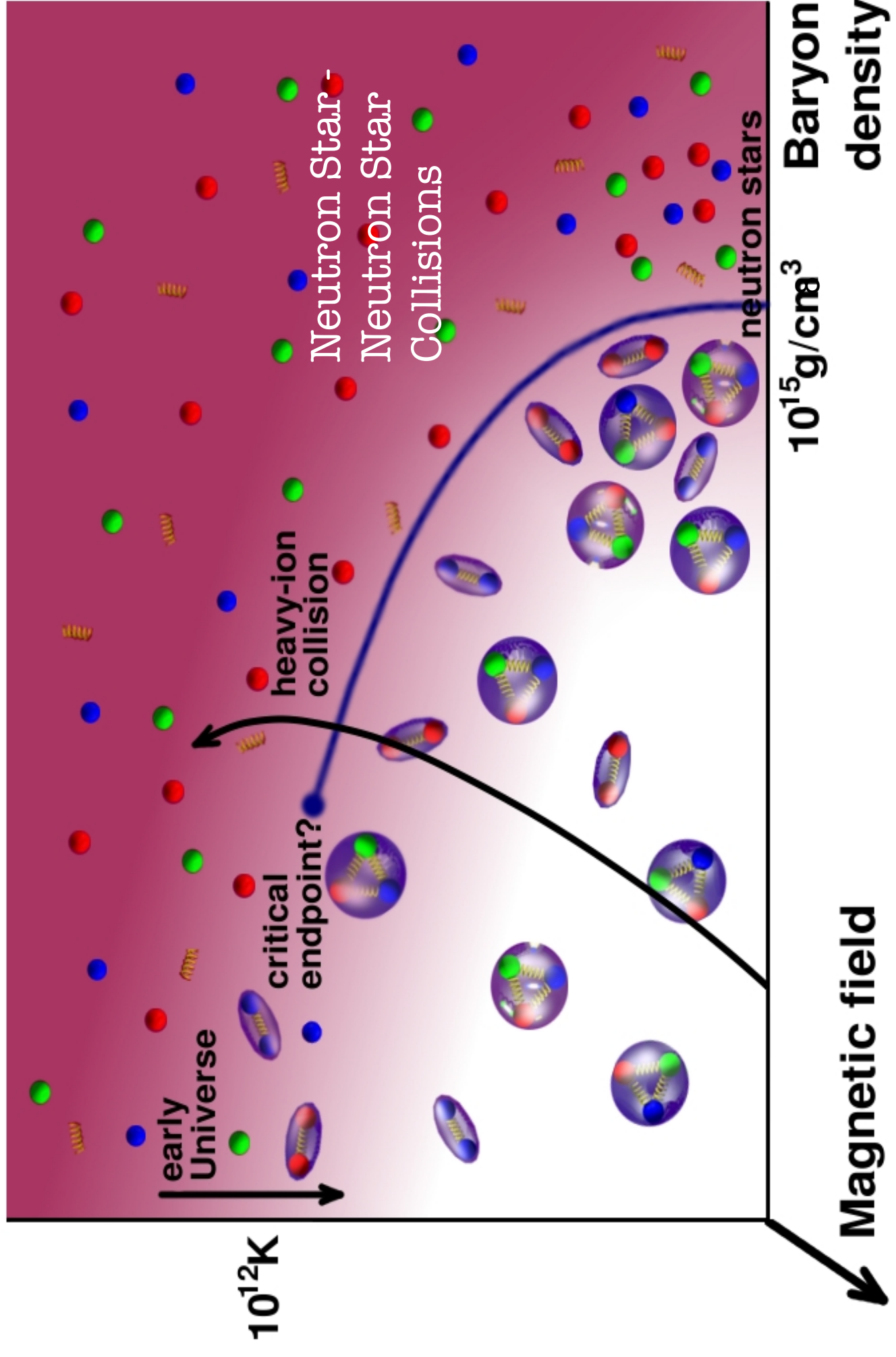
**Atomkern**



# FAIR: Dense Matter, Strange Matter, Quark Matter, Quark Stars?

## Temperature

### Relativistic collisions of NS-NS vs. Heavy Ions



Baryon density

$10^{15}\text{g/cm}^3$

Magnetic field





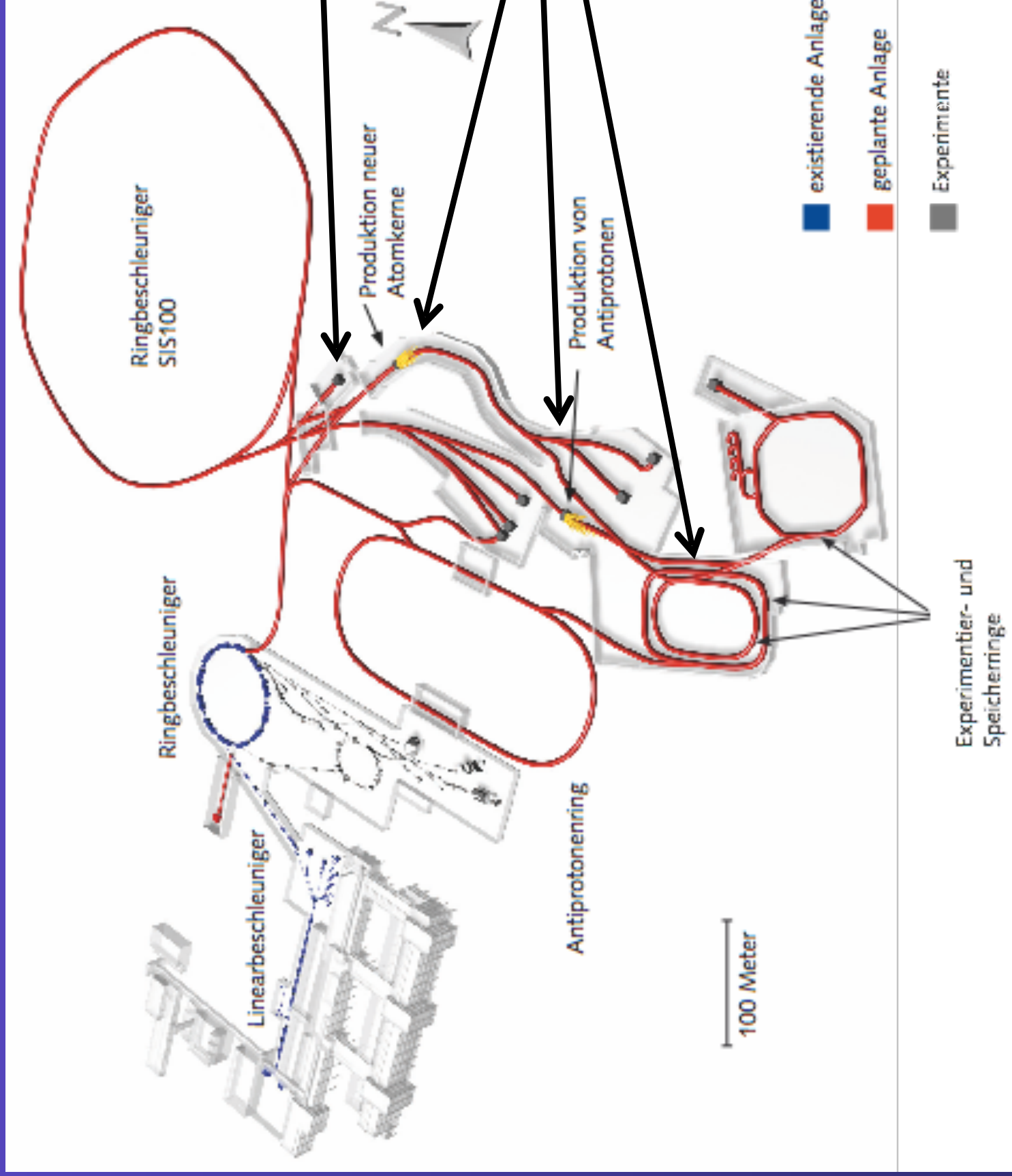
# **FAIR - the death star machine!**

**(The Times of India)**

**FAIR is ideally equipped for precision studies,  
FAIR is ideal to compare relativistic collisions of  
neutron stars and heavy ions**



**Understanding the high density QCD equation of state**







# Neutronstar merger vs. heavy ion collisions

## *Differences in chemical composition*

Quark-Hadron Chiral Parity Doublet Model ( $Q_{\chi P}$ ):

**Only model which is able to consistently describe a chiral crossover and a transition from hadrons to quarks and gluons**

A. Mukherjee, J. Steinheimer and S. Schramm, arXiv:1611.10144 [nucl-th].

Calculate:

- The EOS for heavy ion collisions: with conserved strangeness and no beta-equilibrium
- The EOS for compact stars: in beta-equilibrium



## Neutronstar merger vs. heavy ion collisions Differences in dynamical description.

- ❑ System Size: Kilometers vs. Femtometers
- ❑ Evolution time: Milliseconds vs. fm/c
- ❑ Equilibrium: Chemical + Phase-Equilibrium vs. Non-Equilibrium
- ❑ Gravity is relevant - or not ?
- ❑ Yet : hydrodynamics seems to work for both!

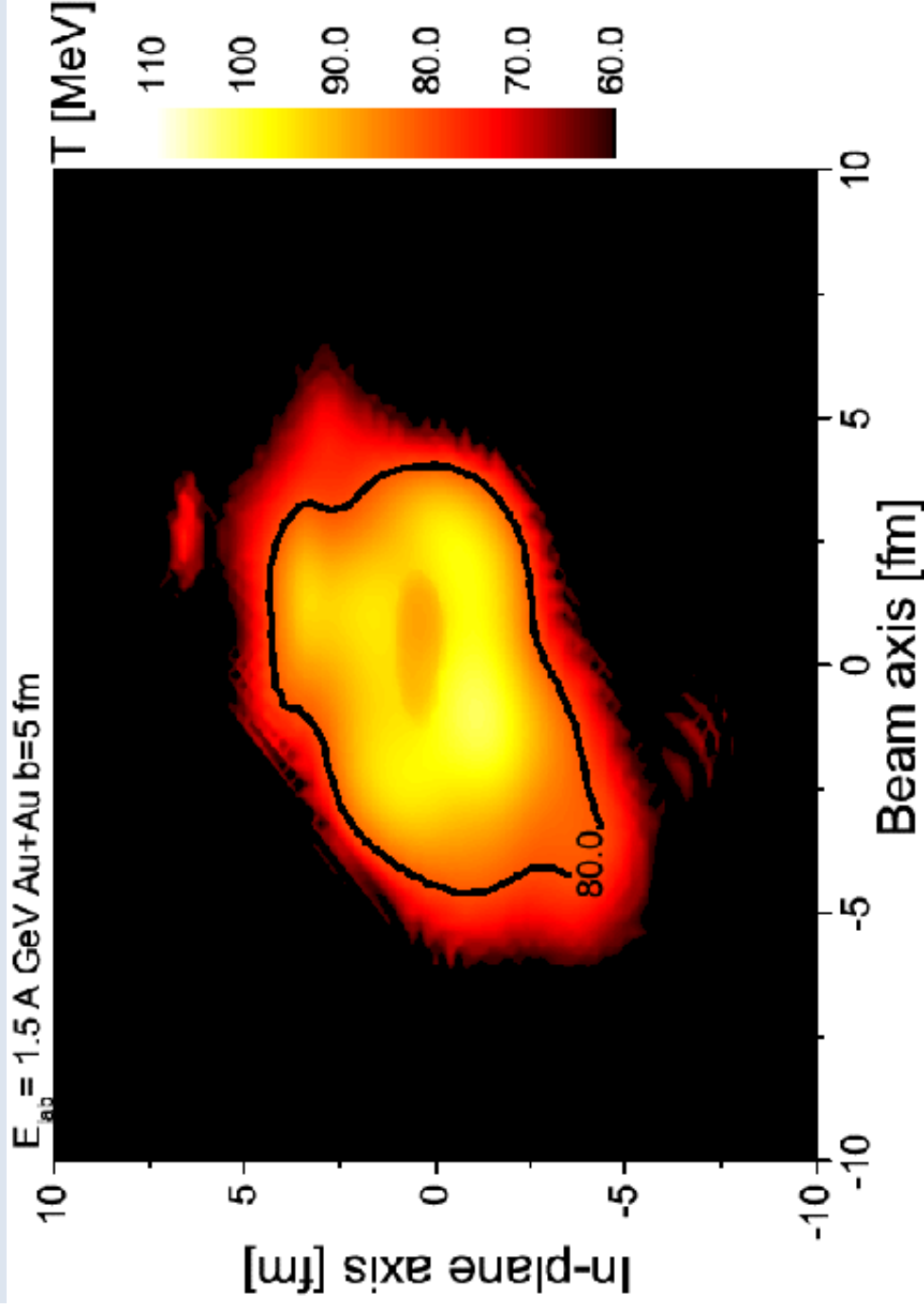
➤ **Importance of the equation of state as input for hydrodynamics**



# Neutronstar merger vs. heavy ion collisions

## *What temperatures can we expect?*

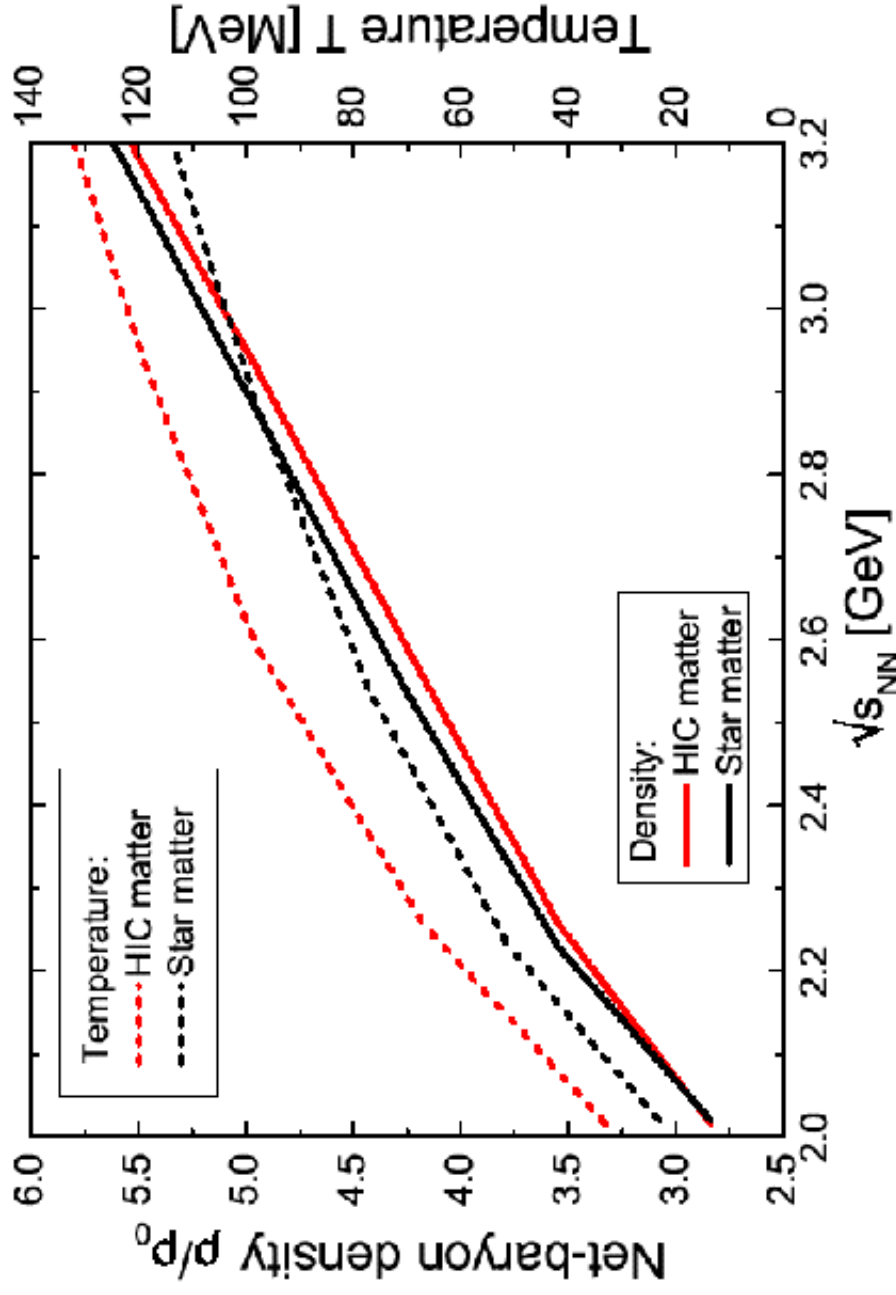
Coarse grained UrQMD simulation input for hydrodynamical evolution



- Beam energy corresponds to GSI-SIS18.
- Temperatures up to  $T=100 \text{ MeV}$  reached.
- Large inhomogeneity.
- Short lifetime  $\sim 20 \text{ fm}/c$
- Small system size  $\sim 10 \text{ fm}$

# Neutronstar merger vs. heavy ion collisions: Which densities and Temperatures can we expect?

Estimate using the relativistic Rankine Hugoniot Taub Adiabate and the *QxP* EoS



Compare central heavy ion collisions  
with head-on neutron star collisions

Rankine Hugoniot Taub Adiabate:

conserved baryon number and energy  
momentum current densities across  
shock front yields 1-Dim, stationary  
hydrodynamical equation

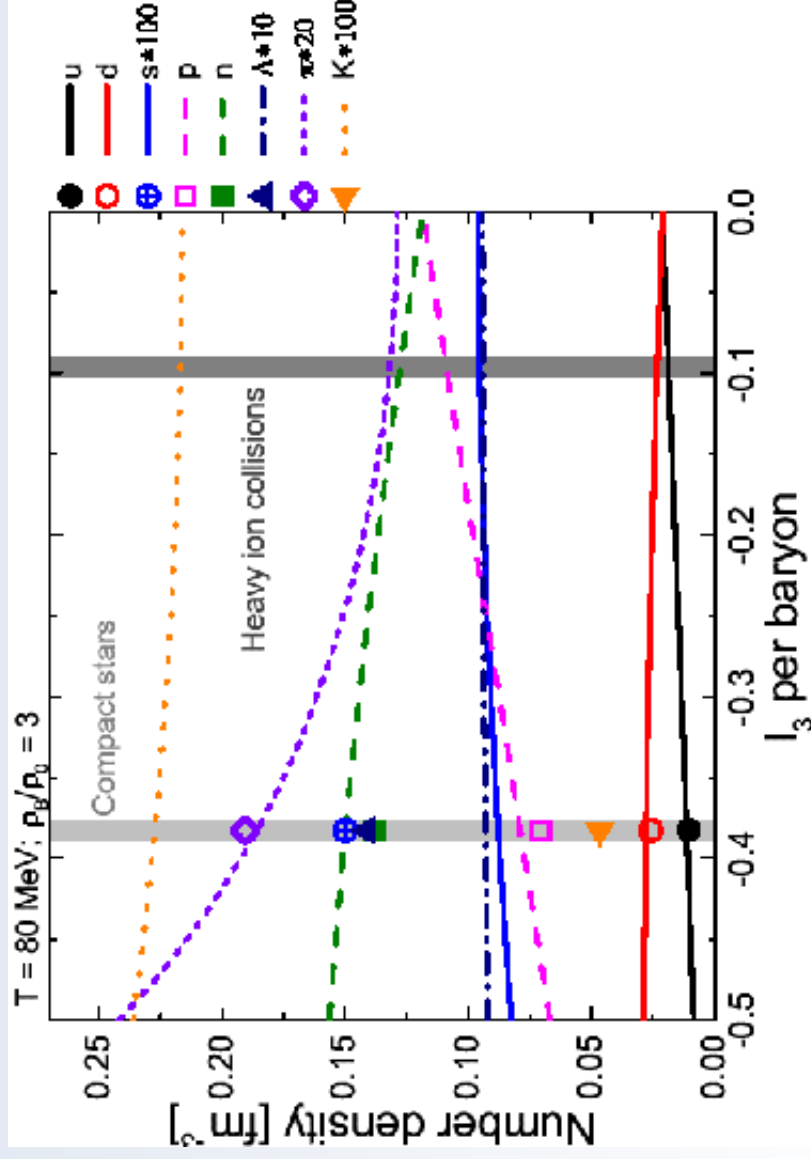
$$E^2 - E_0^2 = (p - p_0)(E/n - E_0/n_0)$$



# Neutronstar merger vs. heavy ion collisions

## Differences in chemical composition

- The EOS for heavy ion collisions: conserved strangeness and no beta-equilibrium
- The EOS for compact stars: in beta-equilibrium



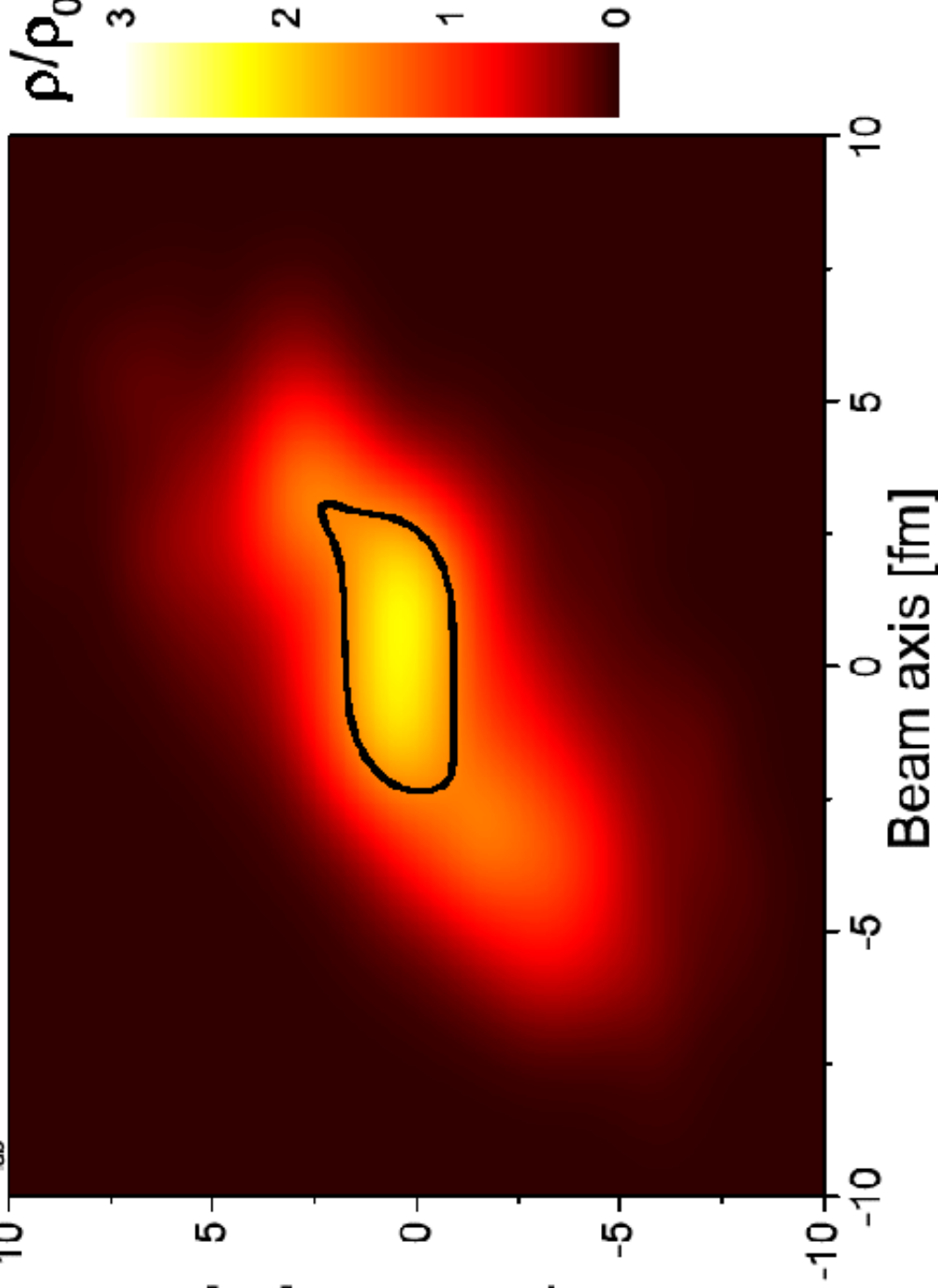
- T = 80 MeV
- 3 times nuclear ground state density
- Large difference in strangeness content and iso-spin

# Neutronstar merger vs. heavy ion collisions

## *What densities can we expect?*

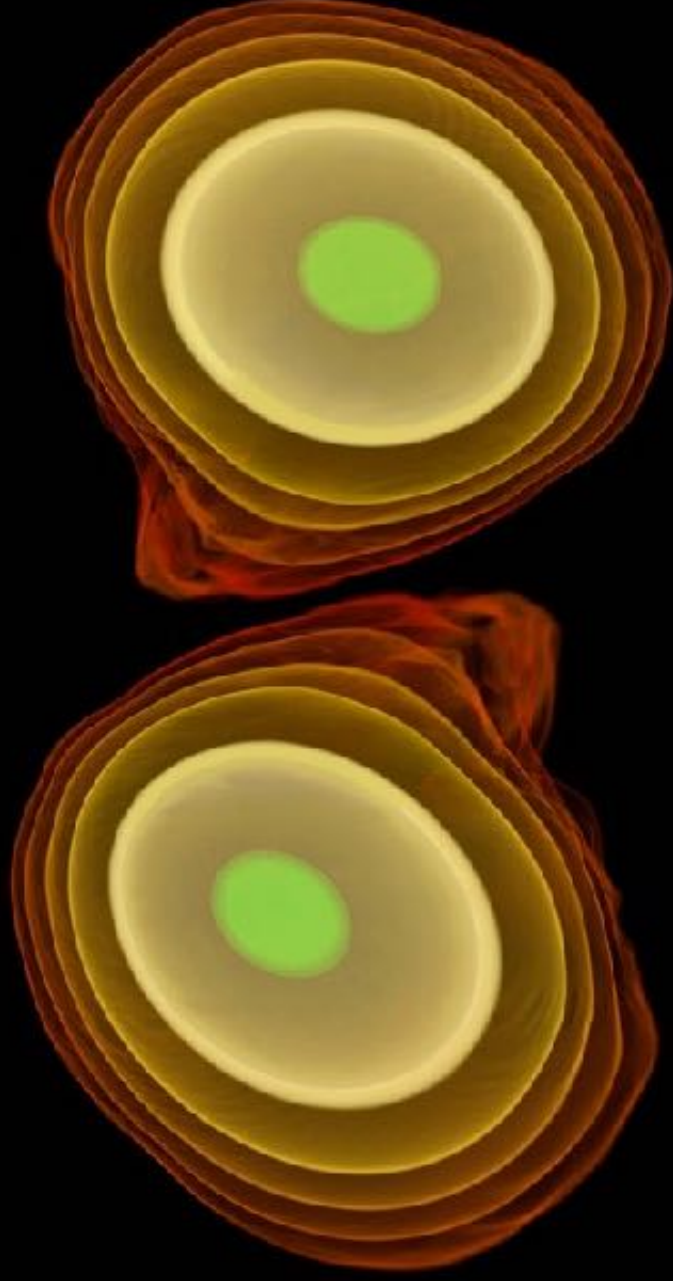
Coarse grained UrQMD simulation input for hydrodynamical evolution; Jan Steinheimer et al

$E_{lab} = 1.5 \text{ A GeV Au+Au } b=5 \text{ fm}$



- Beam energy corresponds to GSI-SIS18.
- 3-5 times nuclear ground state density reached.
- Large inhomogeneity.
- Short lifetime  $\sim 20 \text{ fm/c}$
- Small system size  $\sim 10 \text{ fm}$

# Relativistic Collisions of Binary Neutron Stars





# The two-body problem in GR

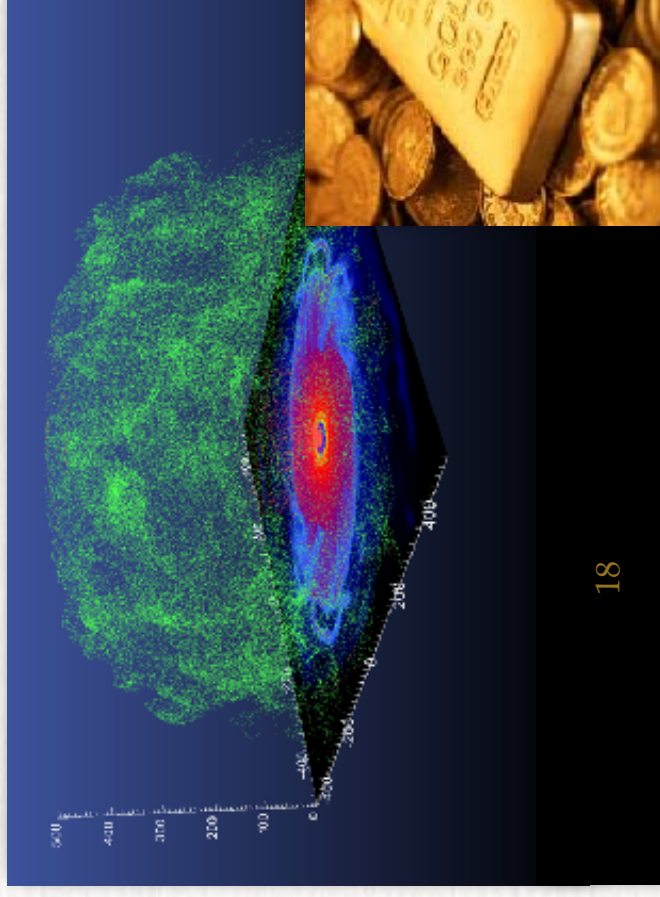
- For BHs we know what to **expect**:



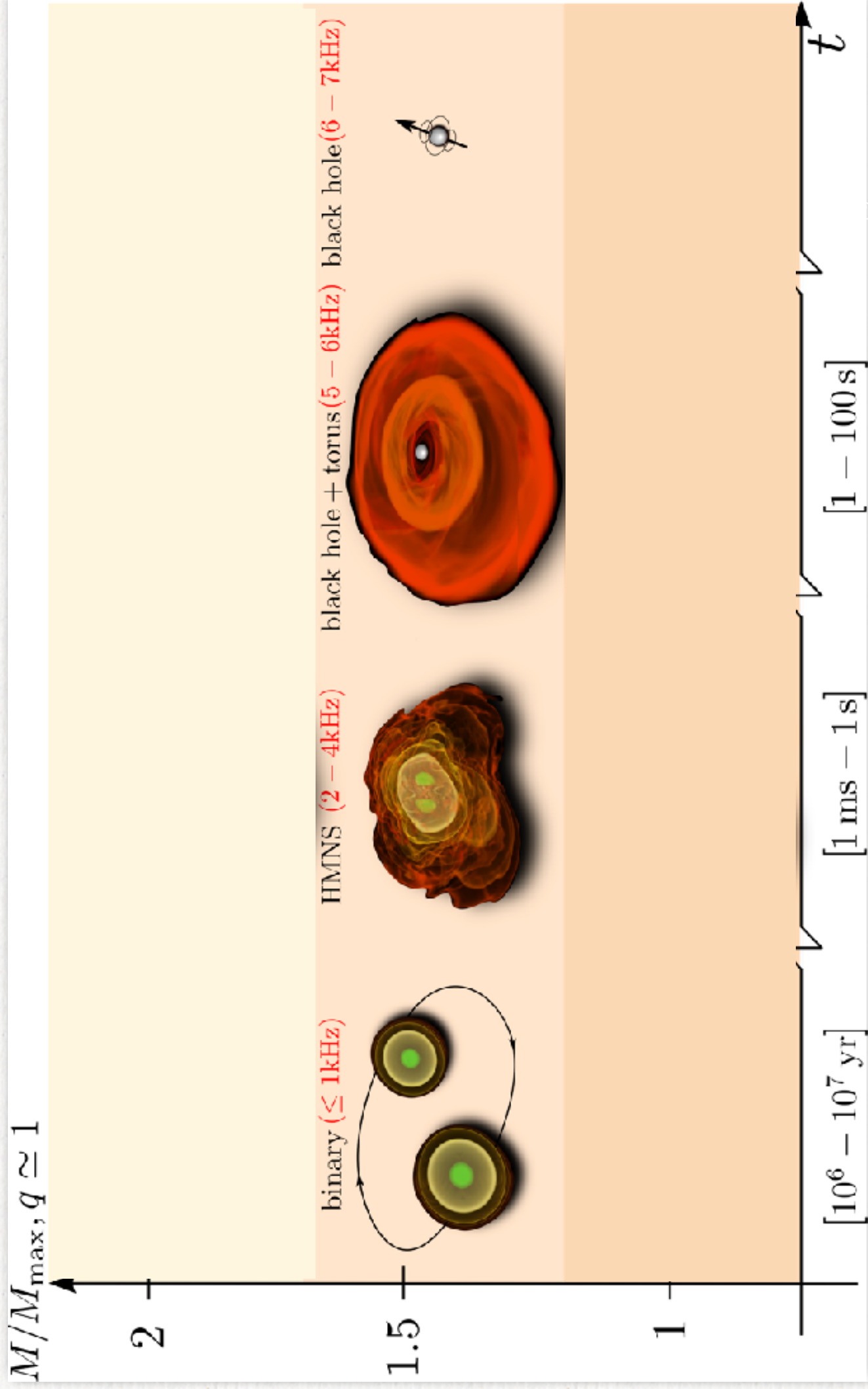
- For NSs the question is more **subtle**: the merger leads to an hyper-massive neutron star (HMNS), ie a metastable equilibrium:



- **ejected matter**  
undergoes  
nucleosynthesis of  
heavy elements



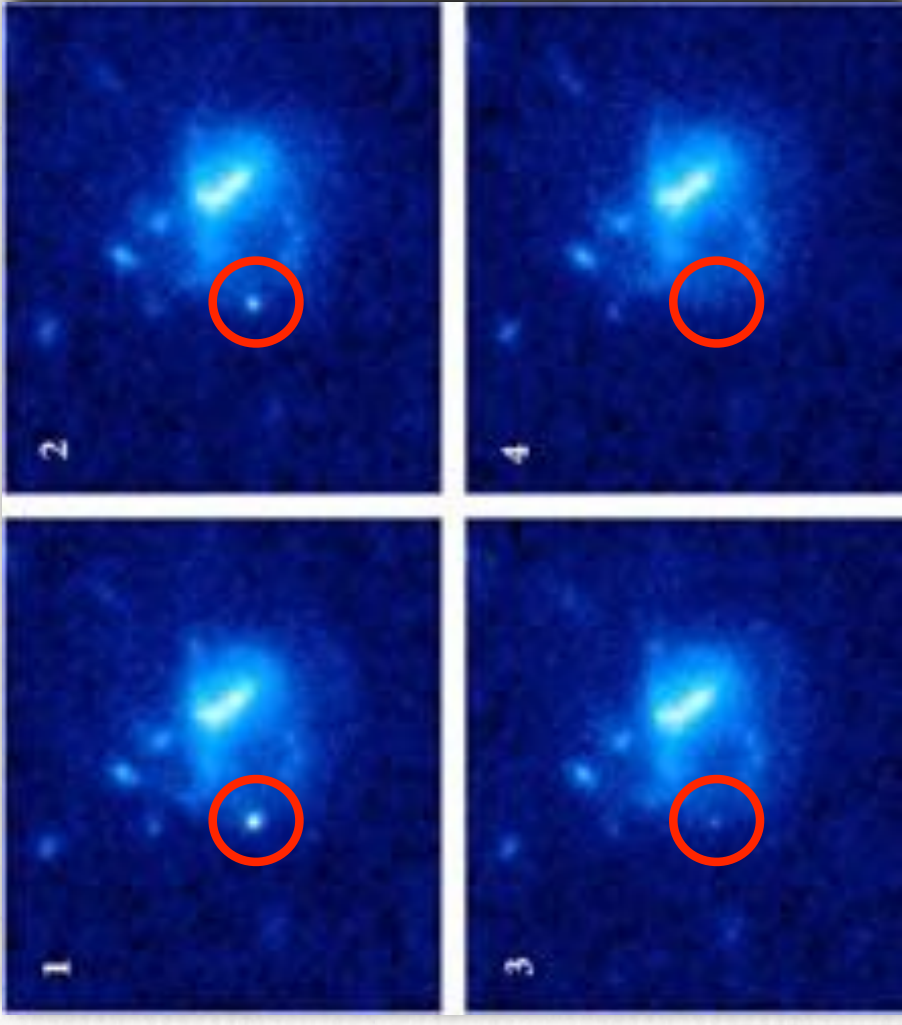
# Broadbrush picture





# Probe the EoS in collisions of binary neutron stars

- We know they exist - among the strongest sources of GWs
- We expect them related to SGRBs:
- energies released are huge:  $10^{48-50}$  erg.
- Equivalent to what is released by the whole Galaxy over  $\sim 1$  year !



short GRB,  
artist impression  
(NASA) <sup>20</sup>

- Despite decades of observations no self-consistent model has yet been produced to explain SGRBs.



“merger” → HMNS → BH + torus”

Quantitative differences are produced by:

- differences induced by the **gravitational MASS**:

a binary with smaller mass will produce a HMNS further away from the stability threshold and will collapse at a later time

- differences induced by the **EOS (“cold” or “hot”)**:

a binary with an EOS with large thermal capacity (ie hotter after merger) will have more pressure support and collapse later

- differences induced by **MASS ASYMMETRIES**:

tidal disruption before merger; may lead to prompt BH

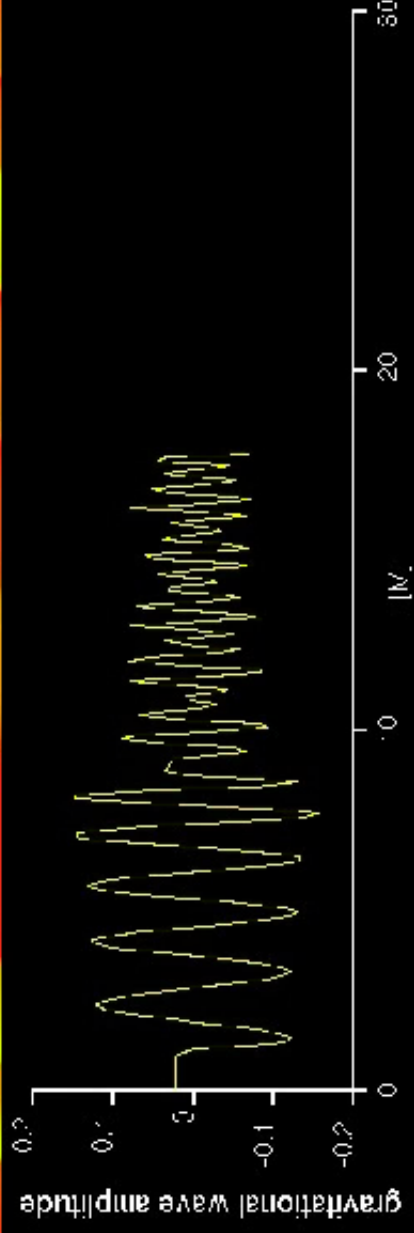
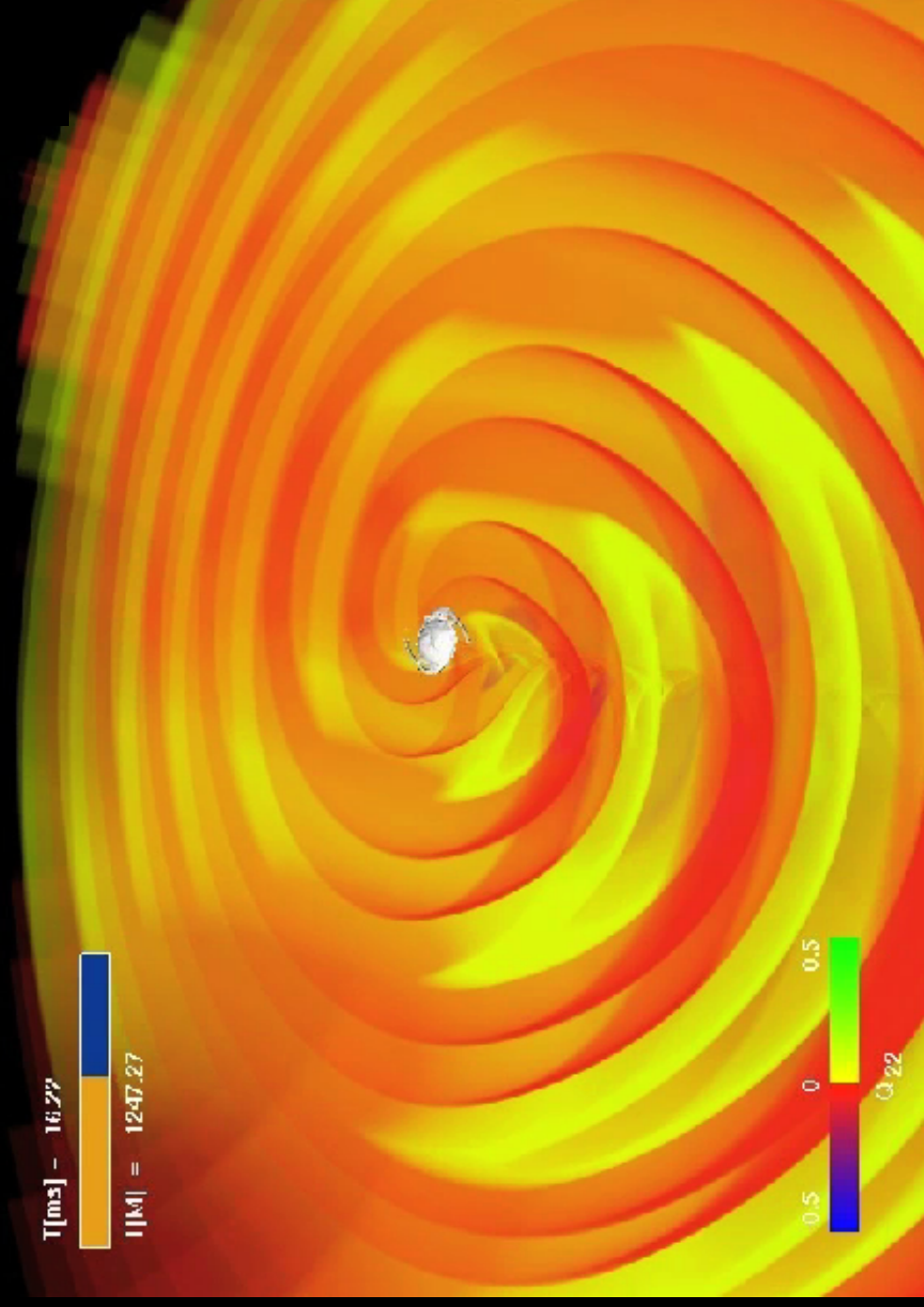
- differences induced by **MAGNETIC FIELDS**:

the angular momentum redistribution via magnetic braking or MRI can increase/decrease time to collapse

- differences induced by **RADIATIVE PROCESSES**:

radiative losses will alter the equilibrium of the HMNS

# Gravitational waves: Einstein's last prediction



# Über Gravitationswellen.

Von A. EINSTEIN.

(Vorgelegt am 31. Januar 1918 [s. oben S. 79].)

Die wichtige Frage, wie die Ausbreitung der Gravitationsfelder erfolgt, ist schon vor anderthalb Jahren in einer Akademiearbeit von mir behandelt worden<sup>1</sup>. Da aber meine damalige Darstellung des Gegenstandes nicht genügend durchsichtig und außerdem durch einen bedauerlichen Rechenfehler verunstaltet ist, muß ich hier nochmals auf die Angelegenheit zurückkommen.

Sitzungsberichte der Königlich-Preußischen Akademie der Wissenschaften<sup>23</sup>

Einstein's First work on Gravitational Waves, Juni 1916, was ... **wrong**....





 Selected for a Viewpoint in *Physics*

PHYSICAL REVIEW LETTERS

week ending  
12 FEBRUARY 2016

PRL 116, 061102 (2016)



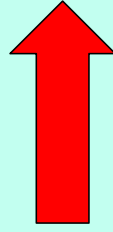
## Observation of Gravitational Waves from a Binary Black Hole Merger

B. P. Abbott *et al.*\*

(LIGO Scientific Collaboration and Virgo Collaboration)

(Received 21 January 2016; published 11 February 2016)

On September 14, 2015 at 09:50:45 UTC the two detectors of the Laser Interferometer Gravitational-Wave Observatory simultaneously observed a transient gravitational-wave signal. The signal sweeps upwards in frequency from 35 to 250 Hz with a peak gravitational-wave strain of  $1.0 \times 10^{-21}$ . It matches the waveform predicted by general relativity for the inspiral and merger of a pair of black holes and the ringdown of the resulting single black hole. The signal was observed with a matched-filter signal-to-noise ratio of 24 and a false alarm rate estimated to be less than 1 event per 203 000 years, equivalent to a significance greater than  $5.1\sigma$ . The source lies at a luminosity distance of  $410^{+150}_{-180}$  Mpc corresponding to a redshift  $z = 0.09^{+0.03}_{-0.04}$ . In the source frame, the initial black hole masses are  $36^{+5}_{-4} M_{\odot}$  and  $29^{+4}_{-4} M_{\odot}$ , and the final black hole mass is  $62^{+4}_{-4} M_{\odot}$ , with  $3.0^{+0.5}_{-0.3} M_{\odot} c^2$  radiated in gravitational waves. All uncertainties define 90% credible intervals. These observations demonstrate the existence of binary stellar-mass black hole systems. This is the first direct detection of gravitational waves and the first observation of a binary black hole merger.



First Direct Discovery of Gravitational Waves

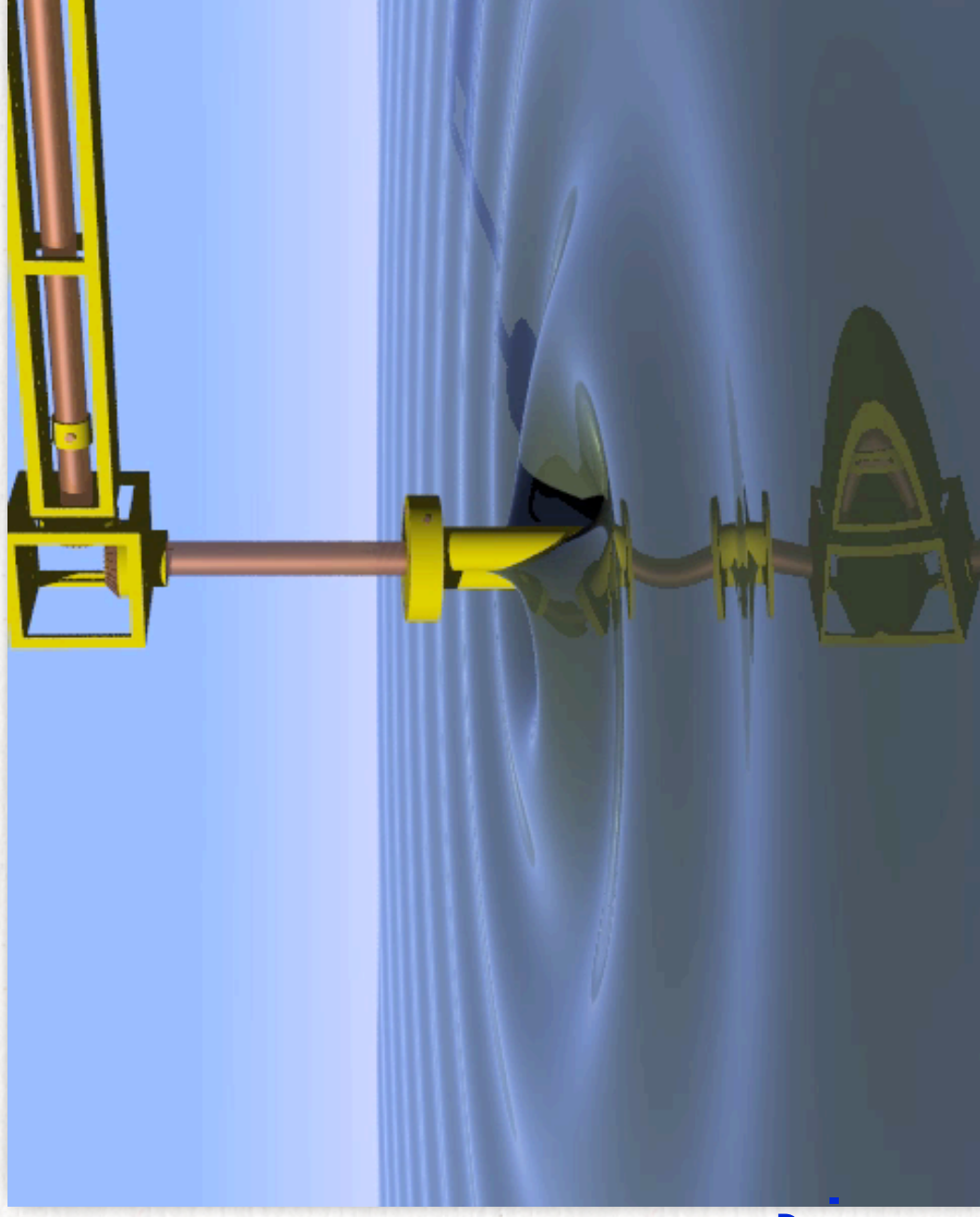
Signalform: melting of two Black Holes

# Gravitational waves: ripples in spacetime

We have seen that compact objects like black holes and neutron stars curve the spacetime near them.

- What happens to the curvature when they move?
- What happens if they orbit around the same center of mass?

A mechanical  
“Gedankenexperiment”.



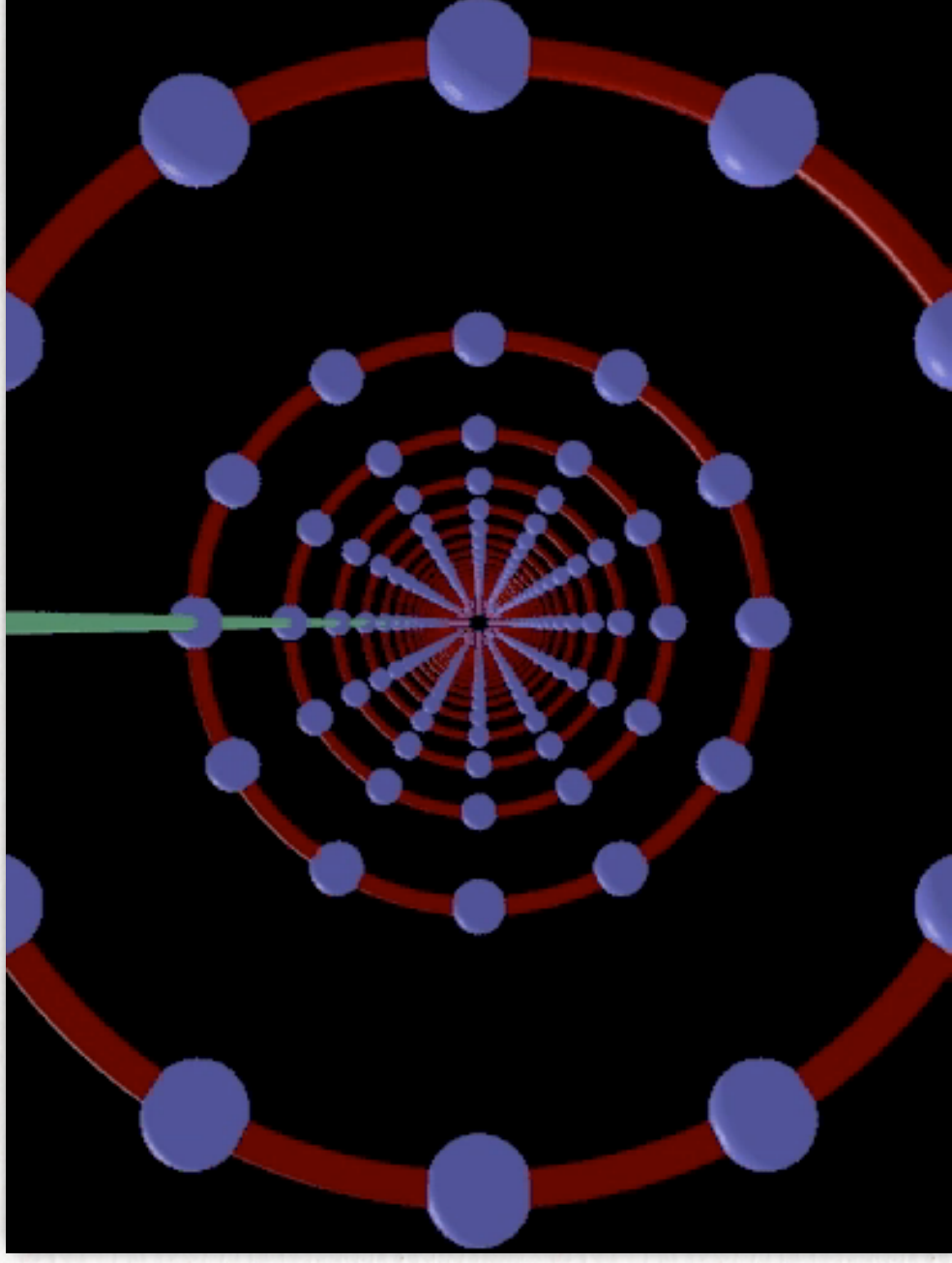


# Gravitational waves: ripples in spacetime

The mechanical analogy is very close: general relativity predicts that if masses are accelerated, they produce **gravitational waves (GWs)**

- GWs are **transverse** waves moving at the speed of light, i.e. they produce changes in the direction orthogonal to the propagation one

- GWs effect is distorting space and time, producing **quadrupole distortions**: **squeeze** in one direction and **stretch** in the orthogonal one





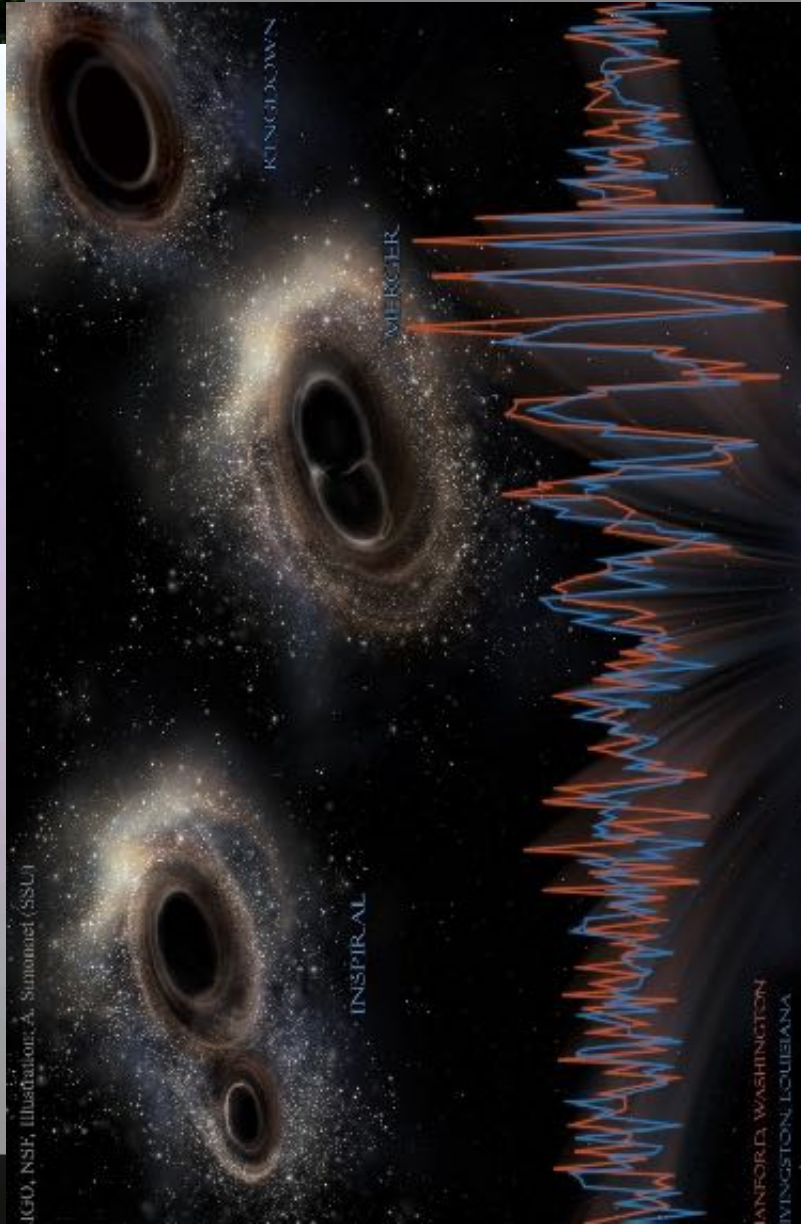
# Gravitational Waves discovered ???!!!

## Collision of 2 BHs GW150914

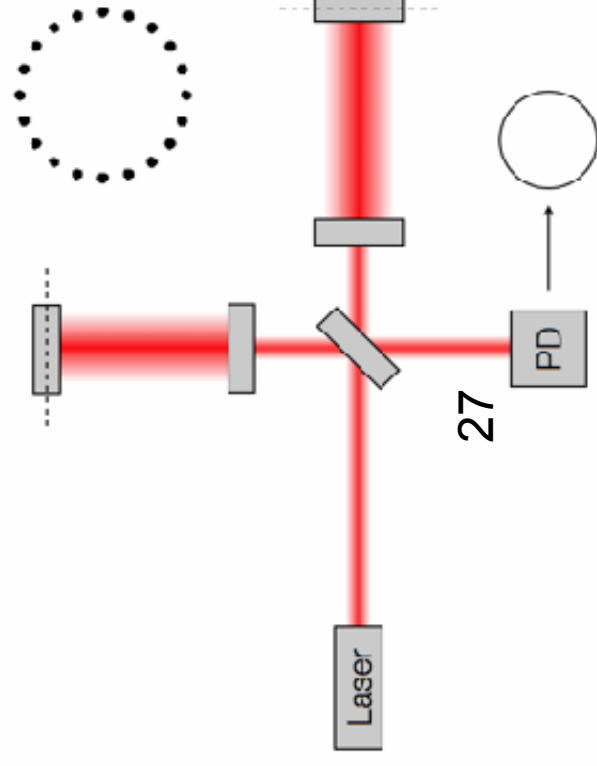
**Masses of BHs: 36 & 29 Solar Masses**

**Distance to Earth 410 Mpc  
(1340 Million Lightyears)**

**Length Difference  $10^{-21}$  m**



IGO, NSF, Illustration: A. Simonnet (SSU)



Credit: Les Wade from Kenyon College.

# Gen. relativ. Hydro for Neutronstar-Neutronstar Collisions

## Density of Neutronstar Matter Temperature of Neutronstar Matter

8.5

14



$\lg(\rho)$  [g/cm<sup>3</sup>]

0

50



T [MeV]

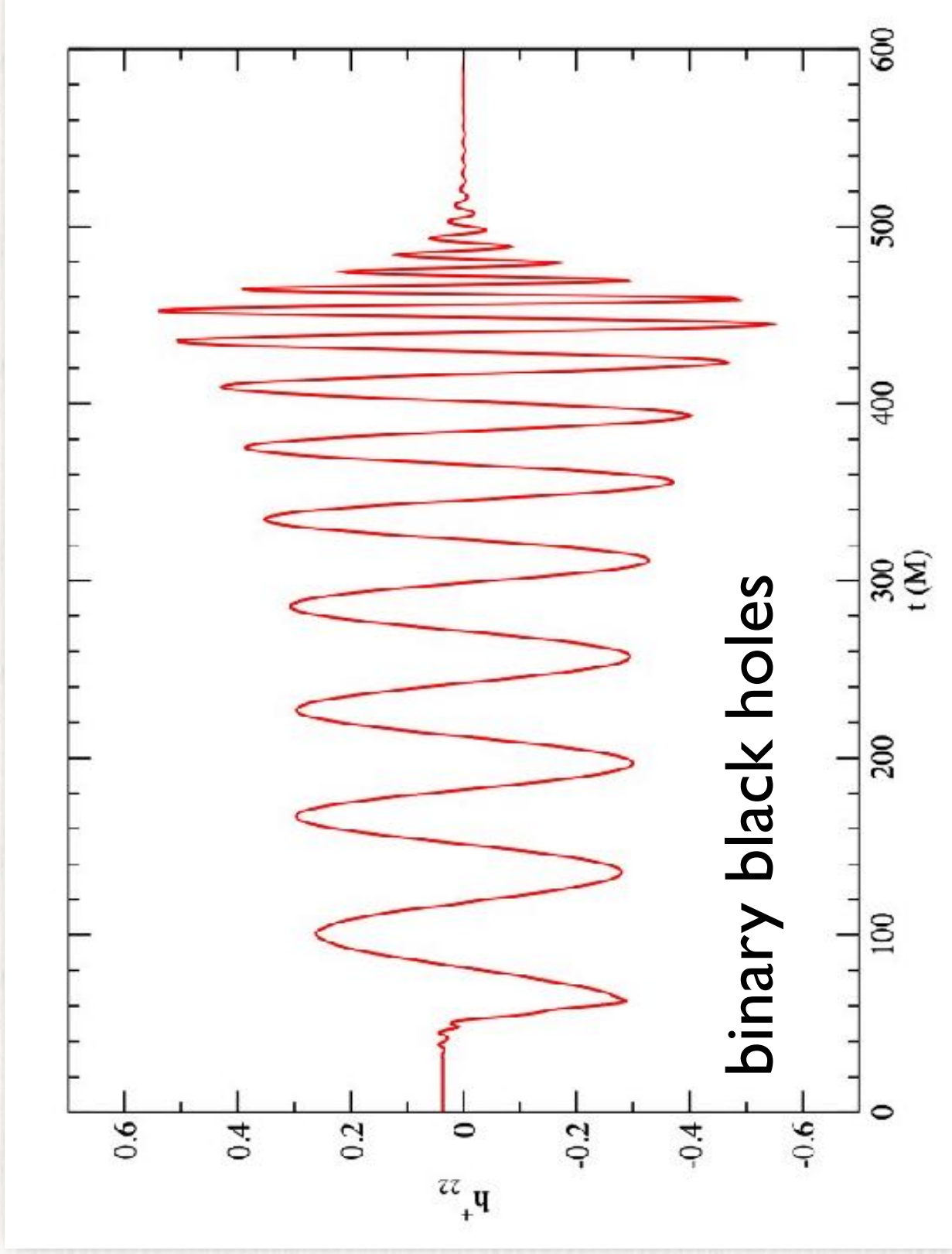
Credits: Cosima Breu, David Radice und Luciano Rezzolla



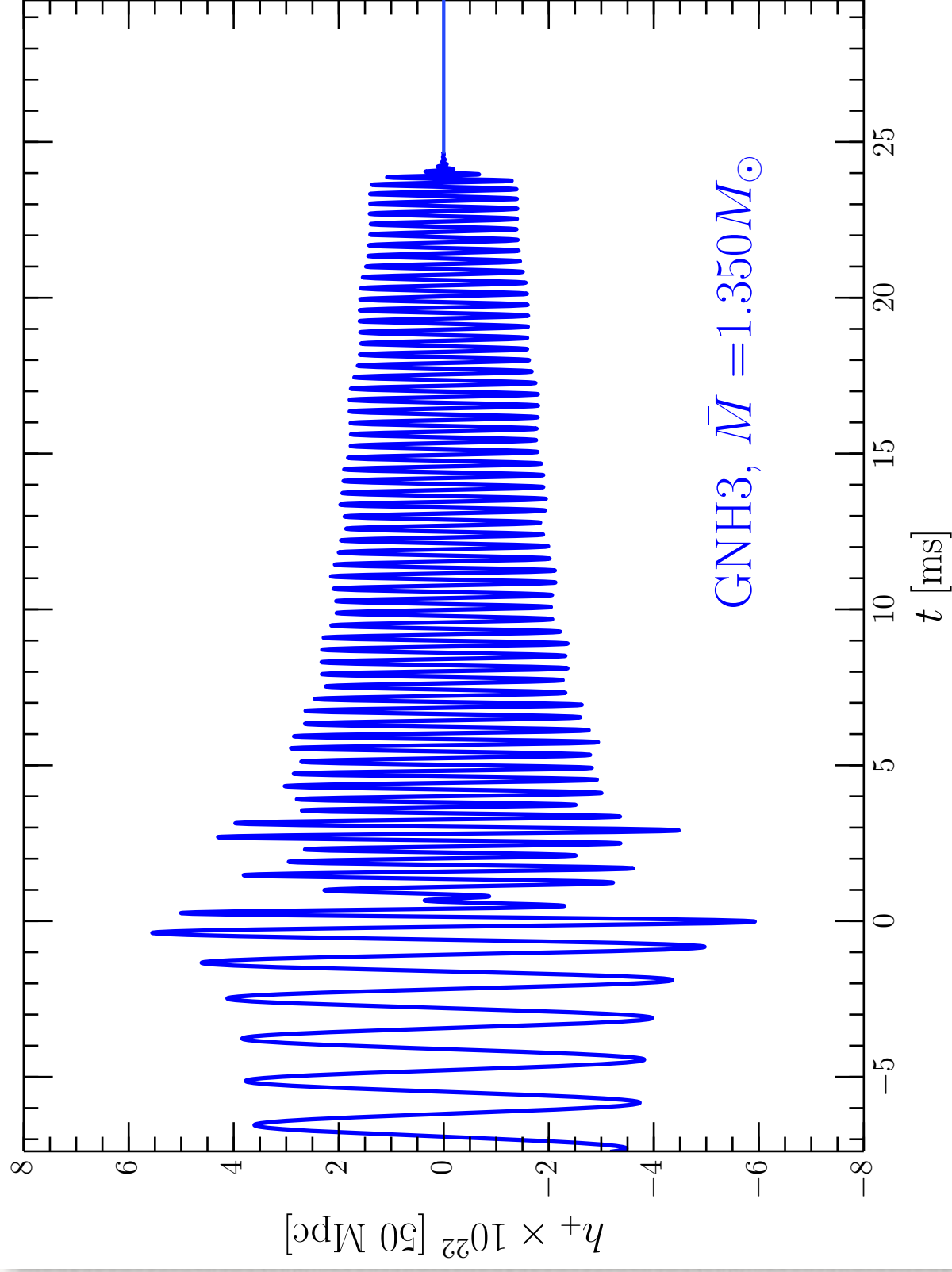
How to constrain the  
EOS  
of superdense  
neutronstar matter  
by relativistic binary  
neutron star- and  
heavy ion<sup>29</sup> collisions



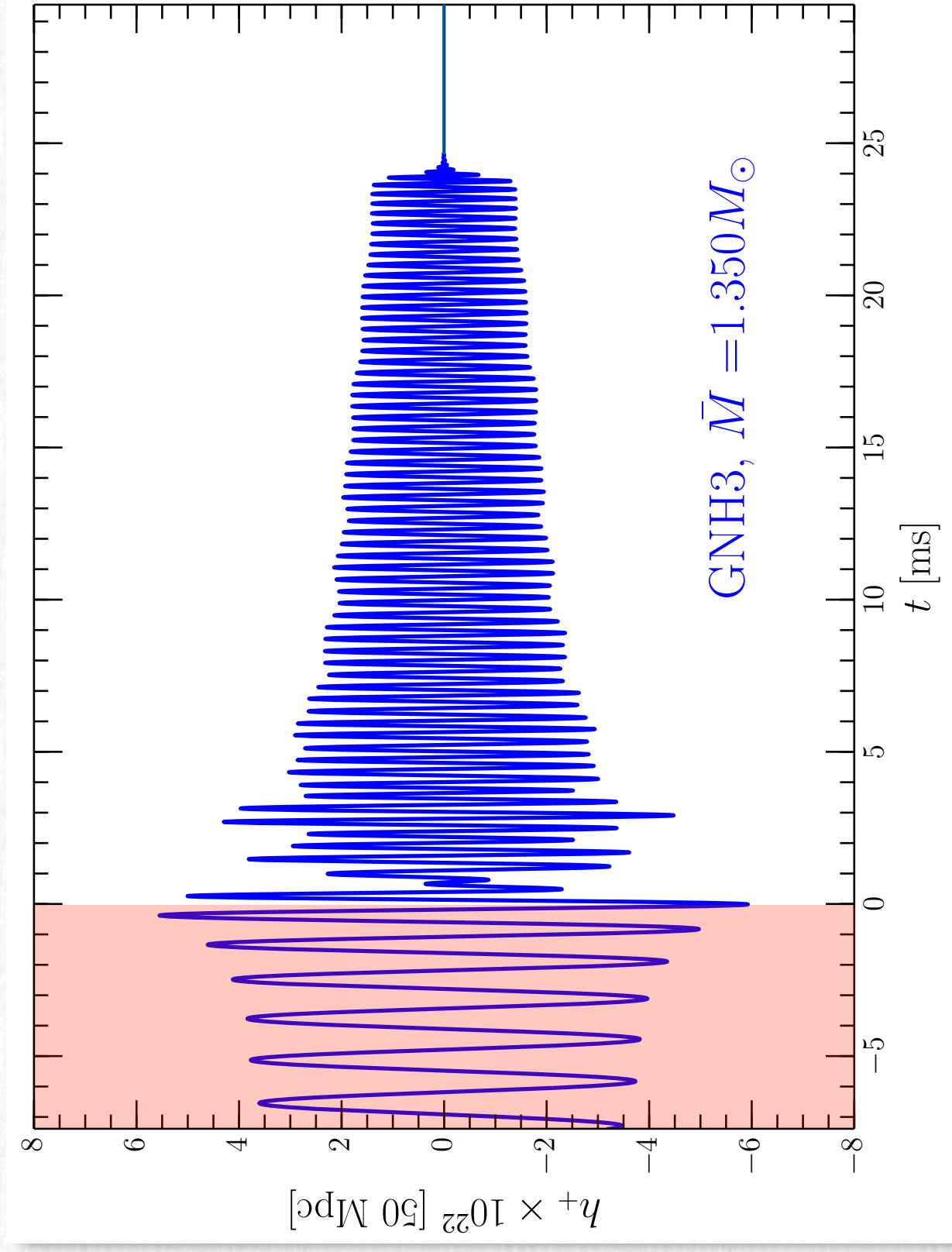
# Anatomy of the GW signal



# Anatomy of the GW signal



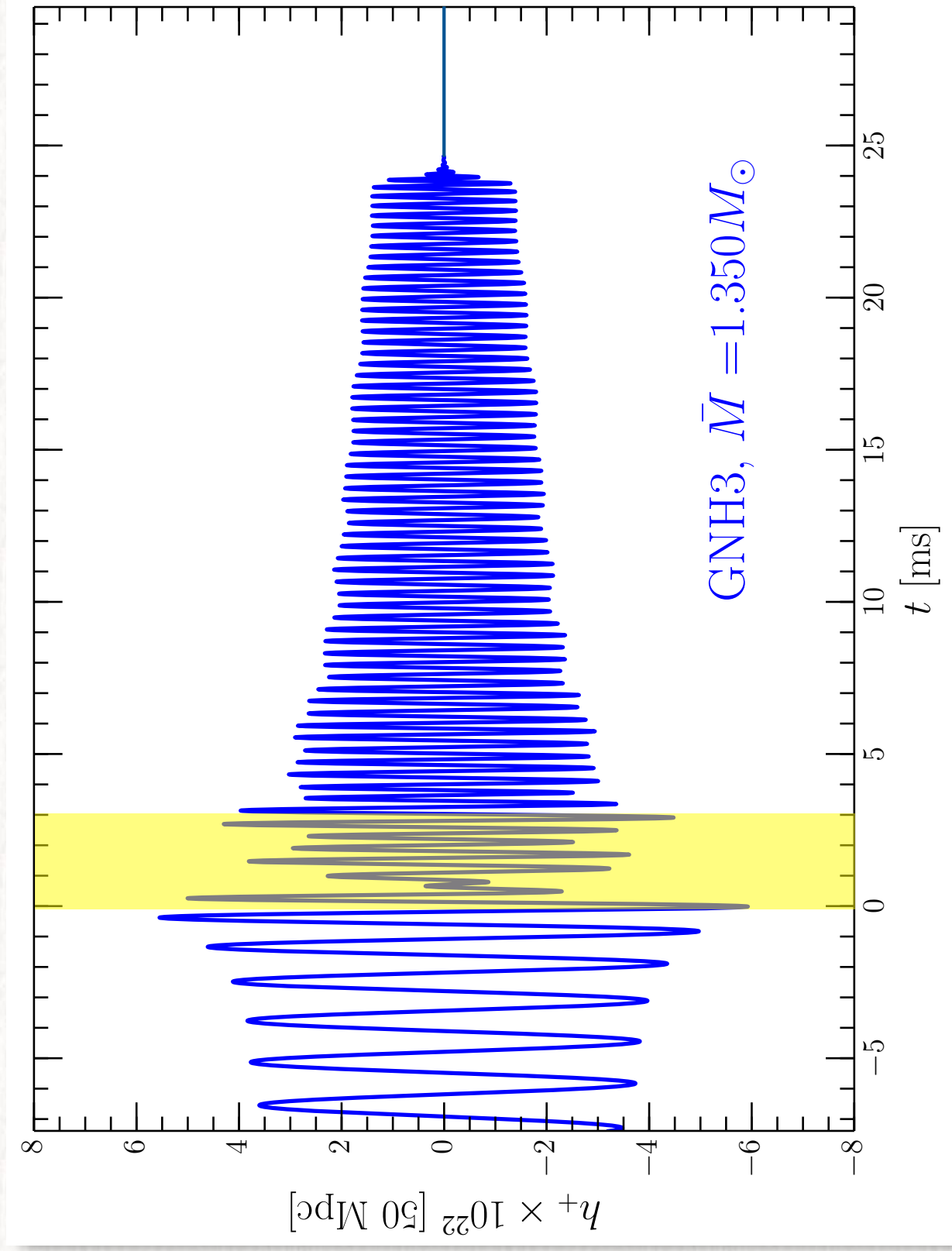
# Anatomy of the GW signal



**Inspiral:** well approximated by  $\text{PN}_{32}$ /EOB; tidal effects important

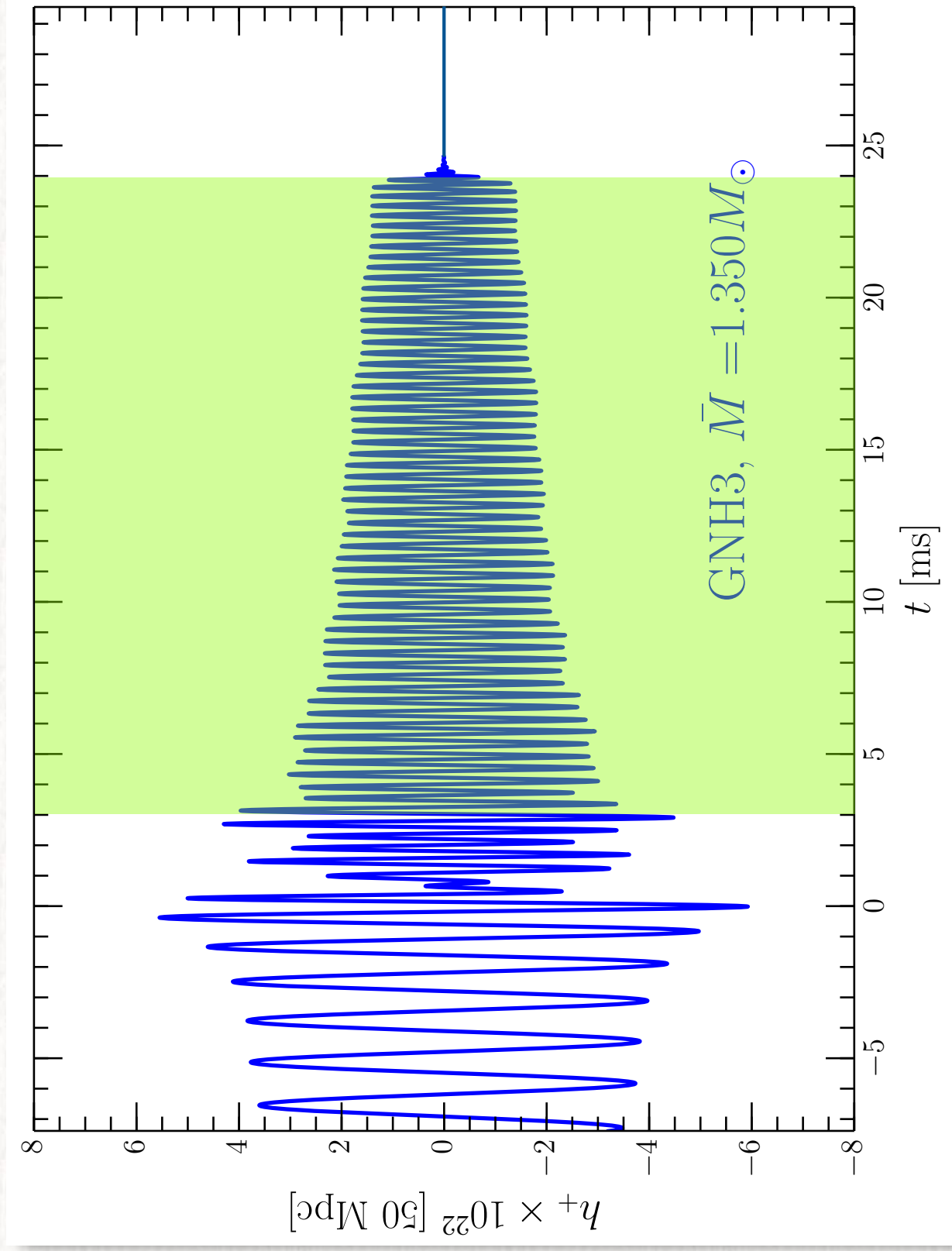


# Anatomy of the GW signal



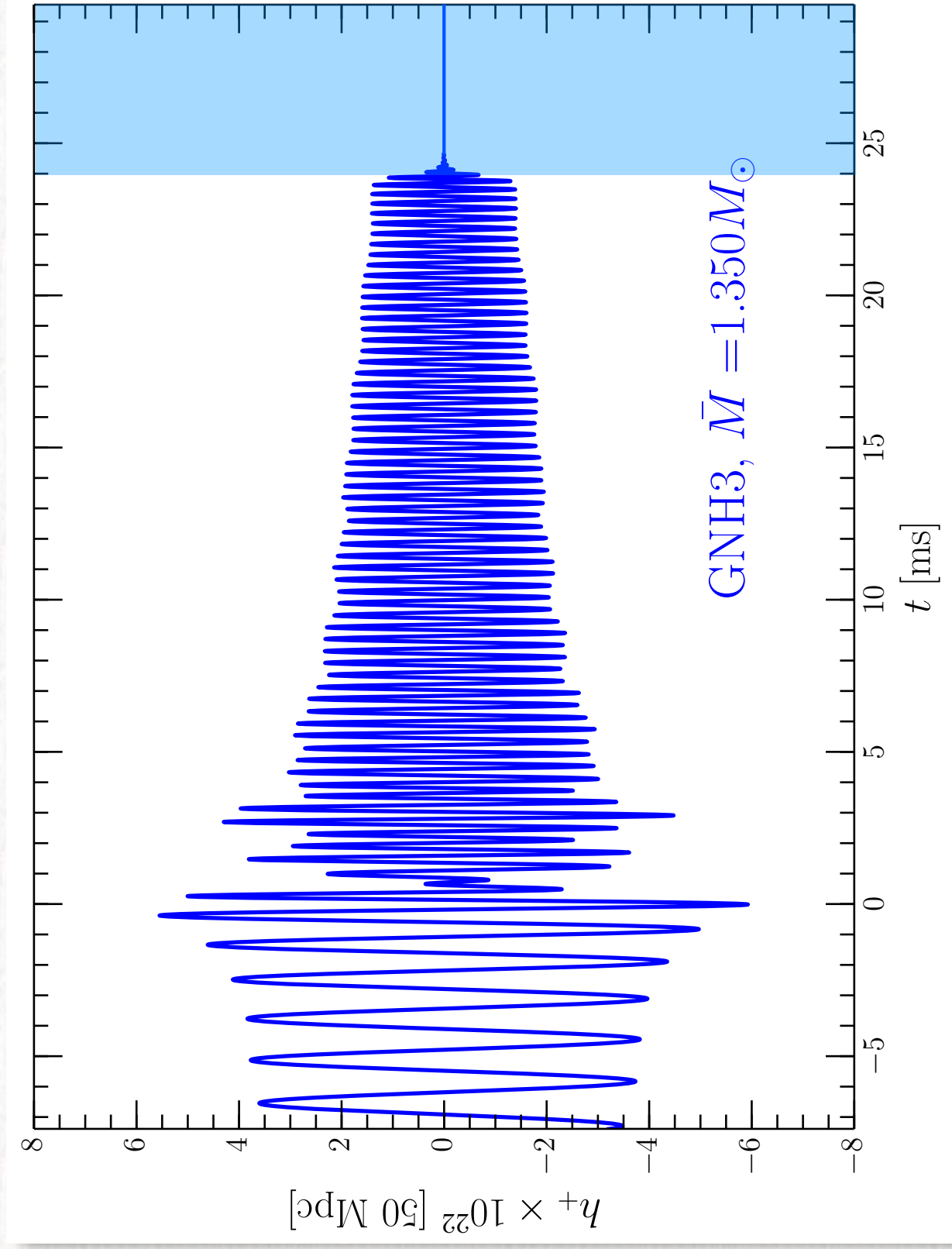
**Merger:** highly nonlinear but <sup>33</sup>analytic description possible

# Anatomy of the GW signal



**post-merger:** quasi-periodic emission of bar-deformed HMNS<sup>34</sup>

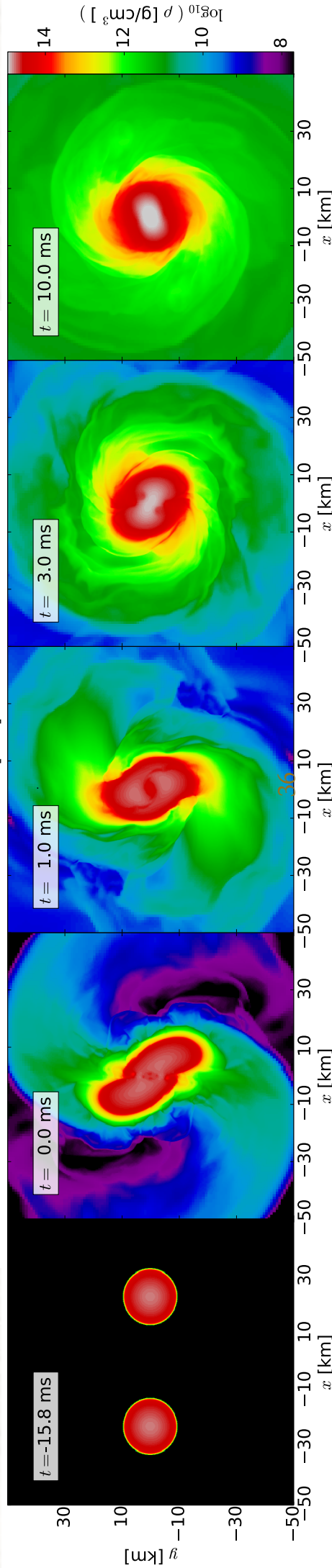
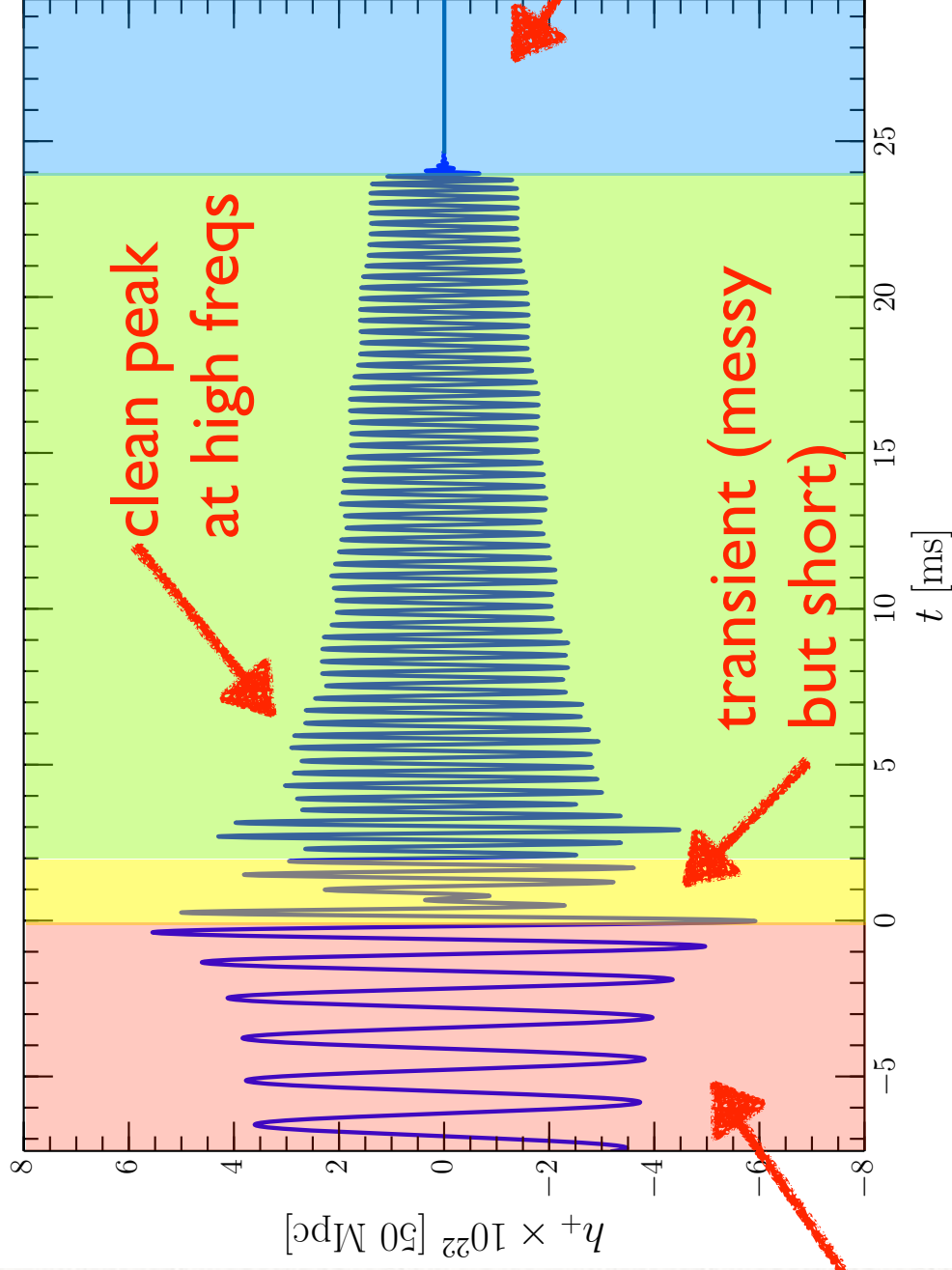
# Anatomy of the GW signal



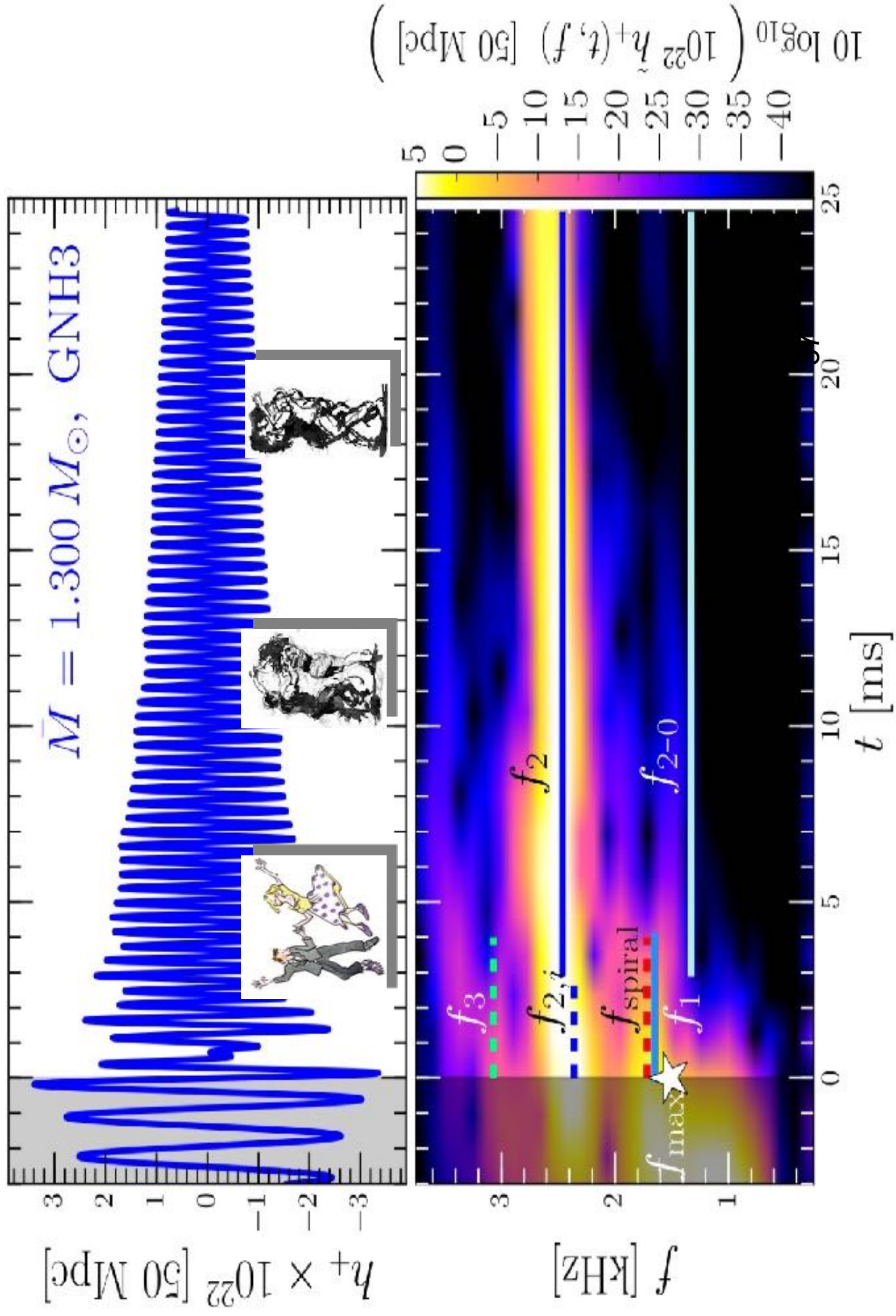
**Collapse-ringdown:** signal essentially shuts off.



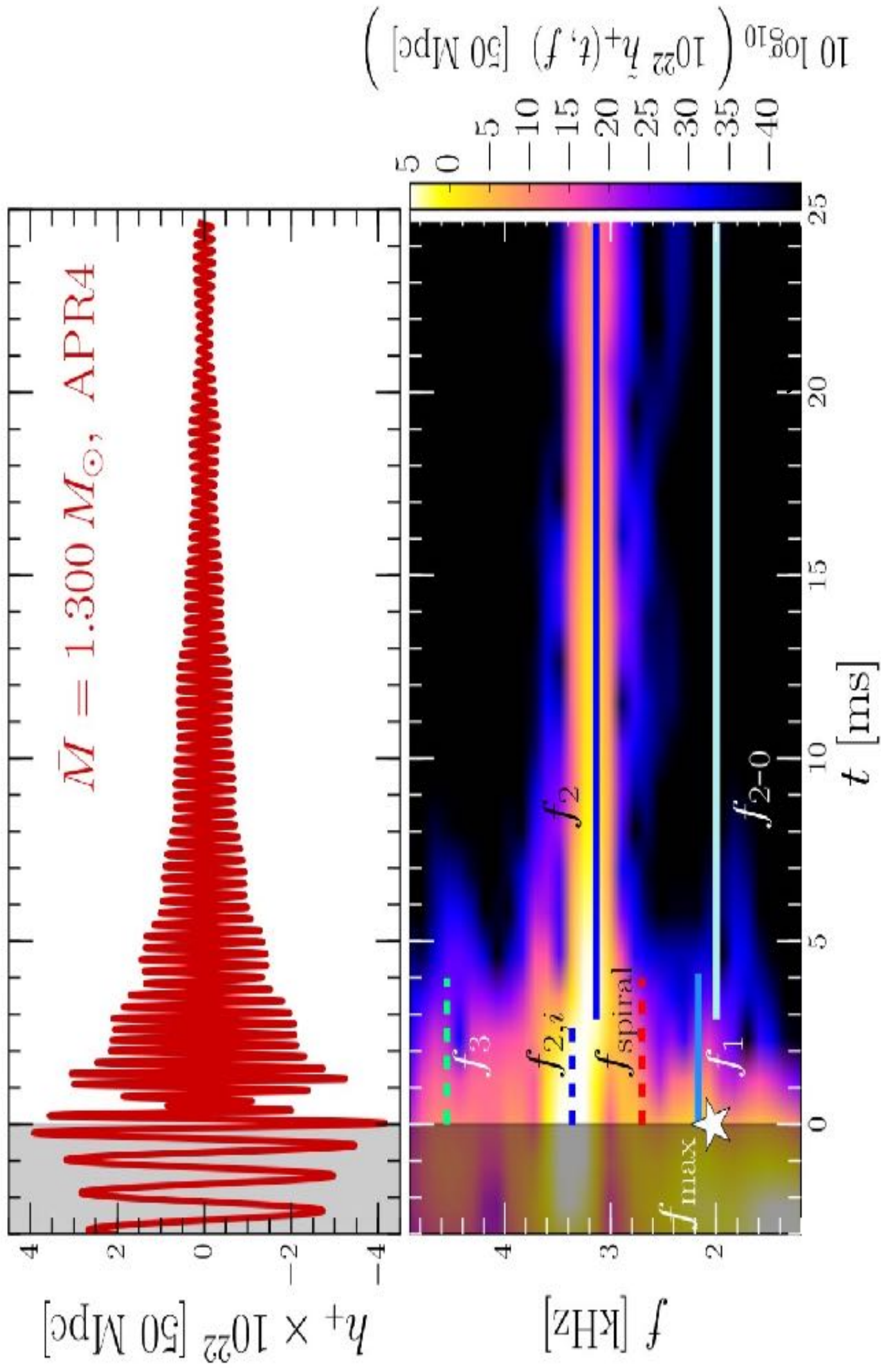
# Anatomy of the GW signal



# The Gravitational Wave Spectrum for a HARD nuclear EoS

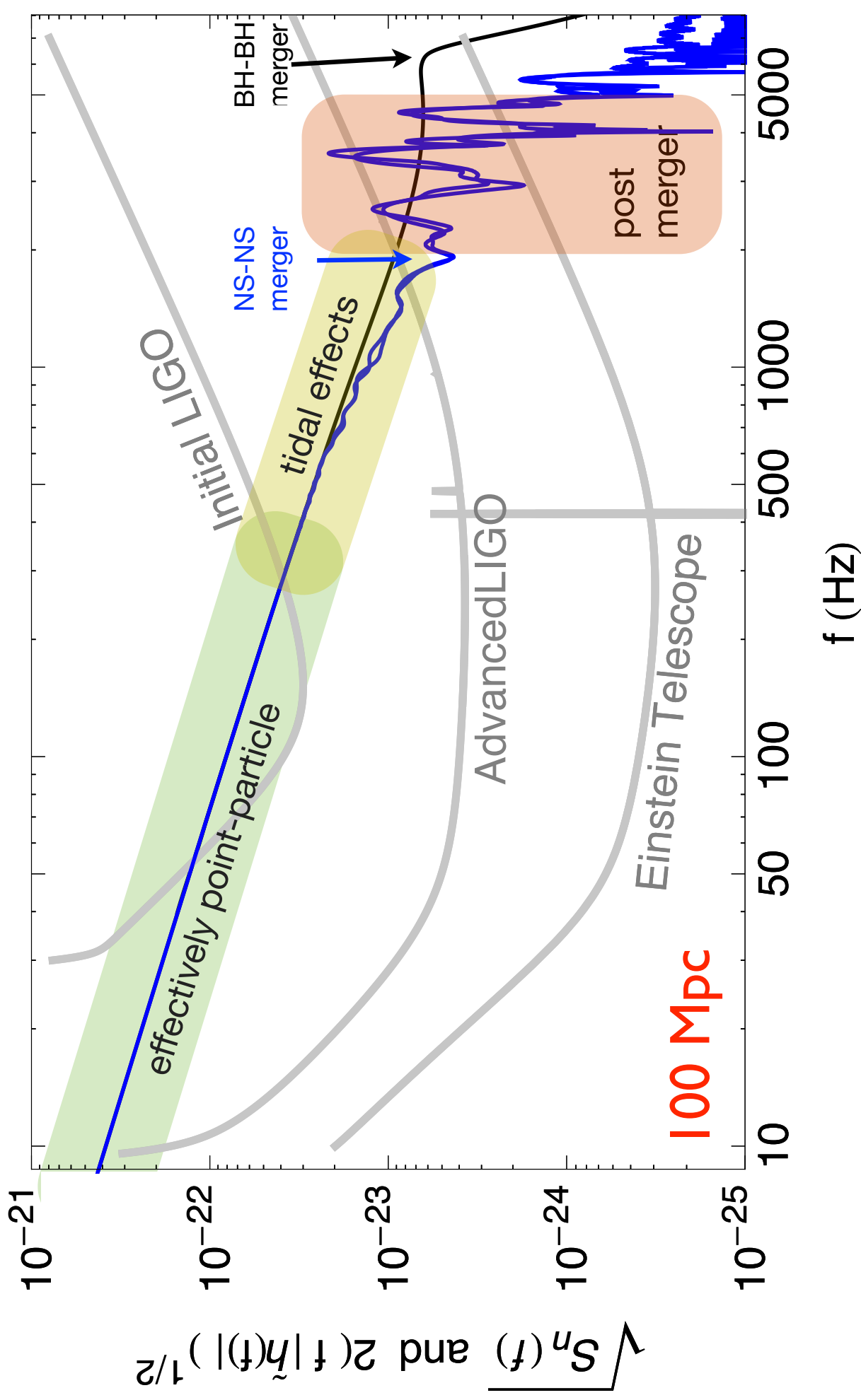


# Gravitational Wave Frequency Spectrum: **soft** nuclear matter EoS



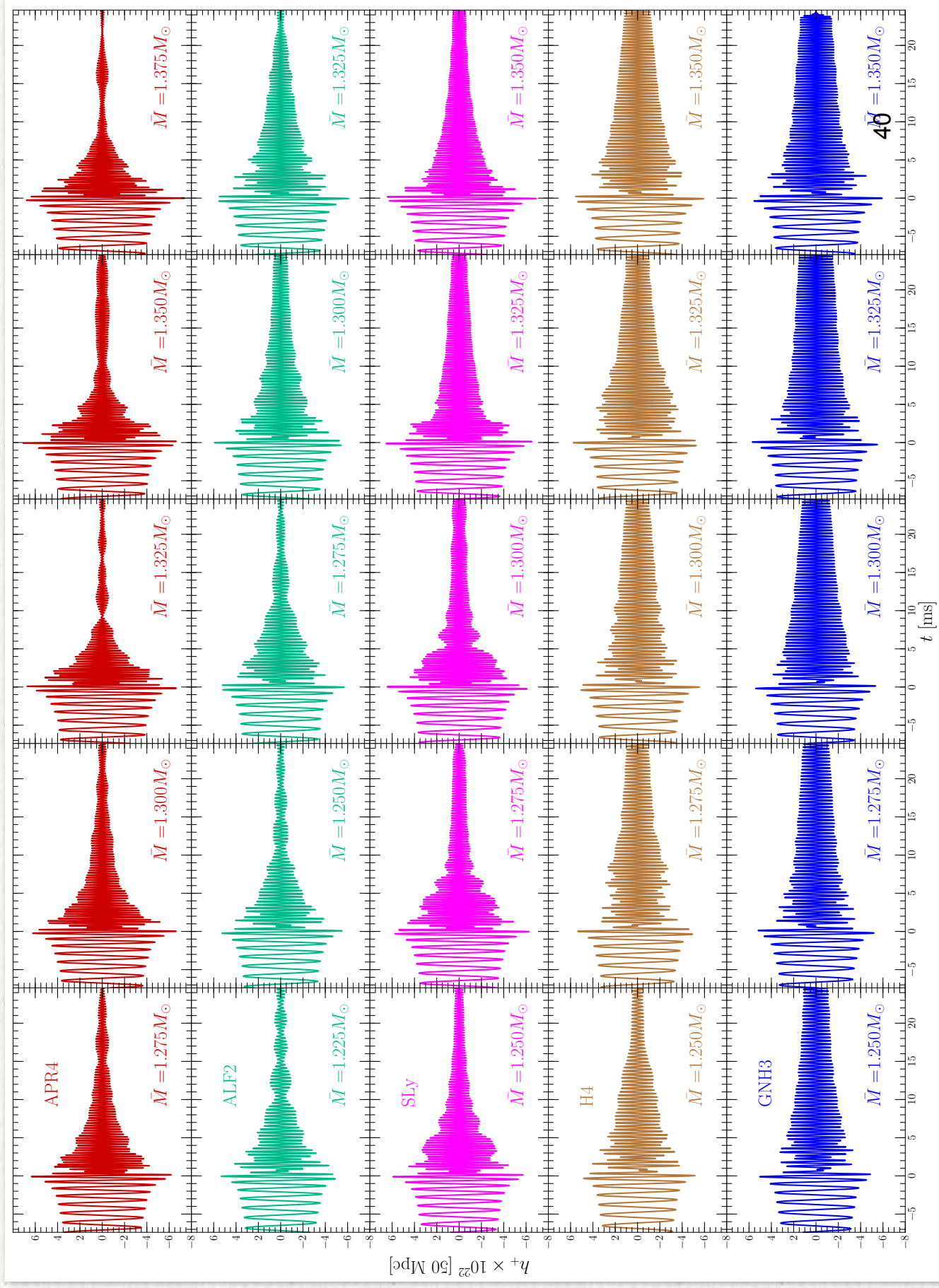


# In frequency space



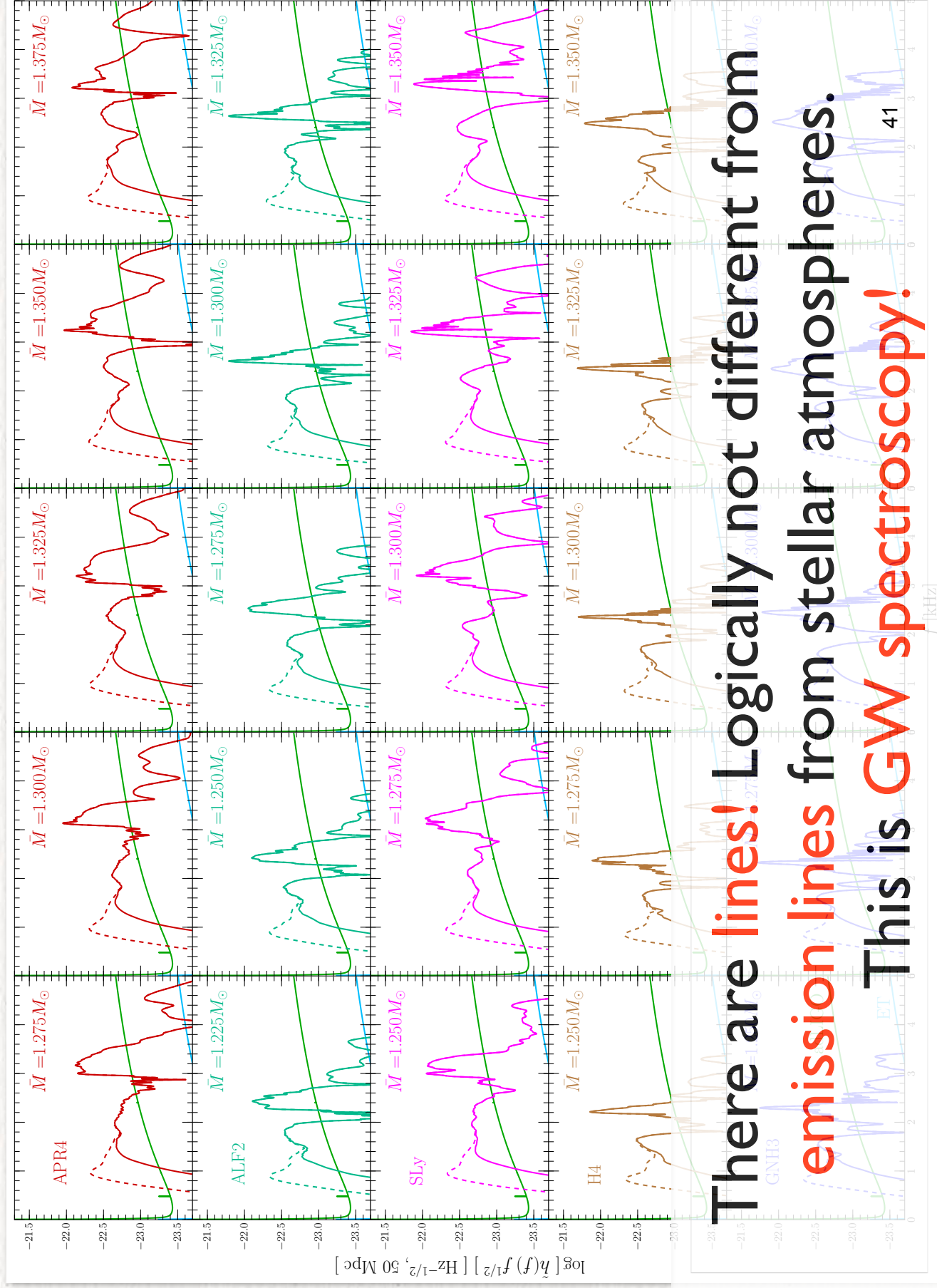
# What we can do nowadays

Takami, L.Rezzolla, Baiotti (2014, 2015), LR+ (2016)



# Extracting information from the EOS

Takami, LR, Baiotti (2014, 2015), LR+ (2016)

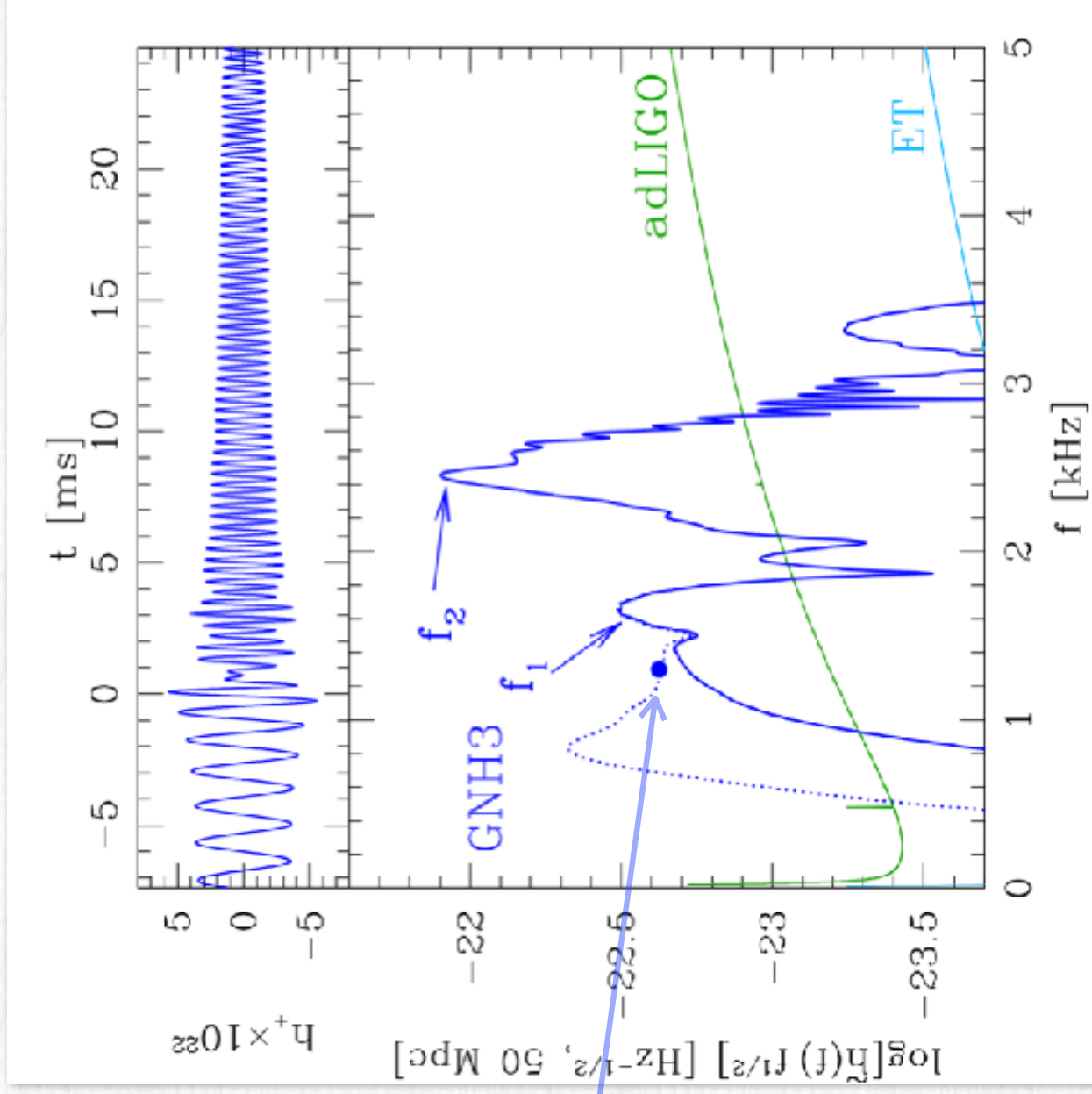


**There are lines!** Logically not different from emission lines from stellar atmospheres. This is **GW spectroscopy!**



# A new approach to constrain the EOS

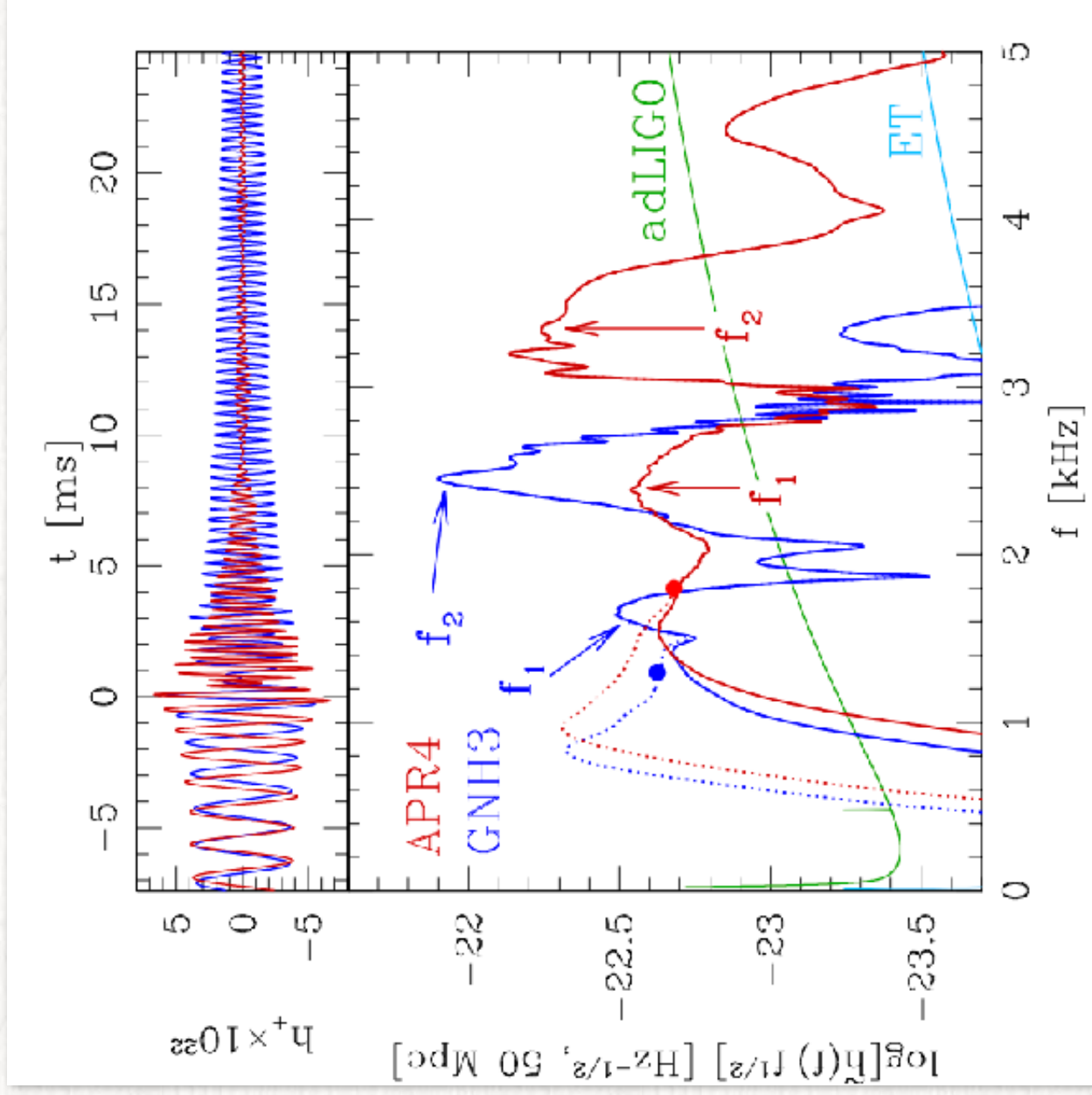
Oechslin+2007, Baiotti+2008, Bauswein+ 2011, 2012, Stergioulas+ 2011, Hotokezaka+ 2013, Takami 2014, 2015, Bernuzzi 2014, 2015, Bauswein+ 2015, LR+2016...



merger  
frequency

# A new approach to constrain the EOS

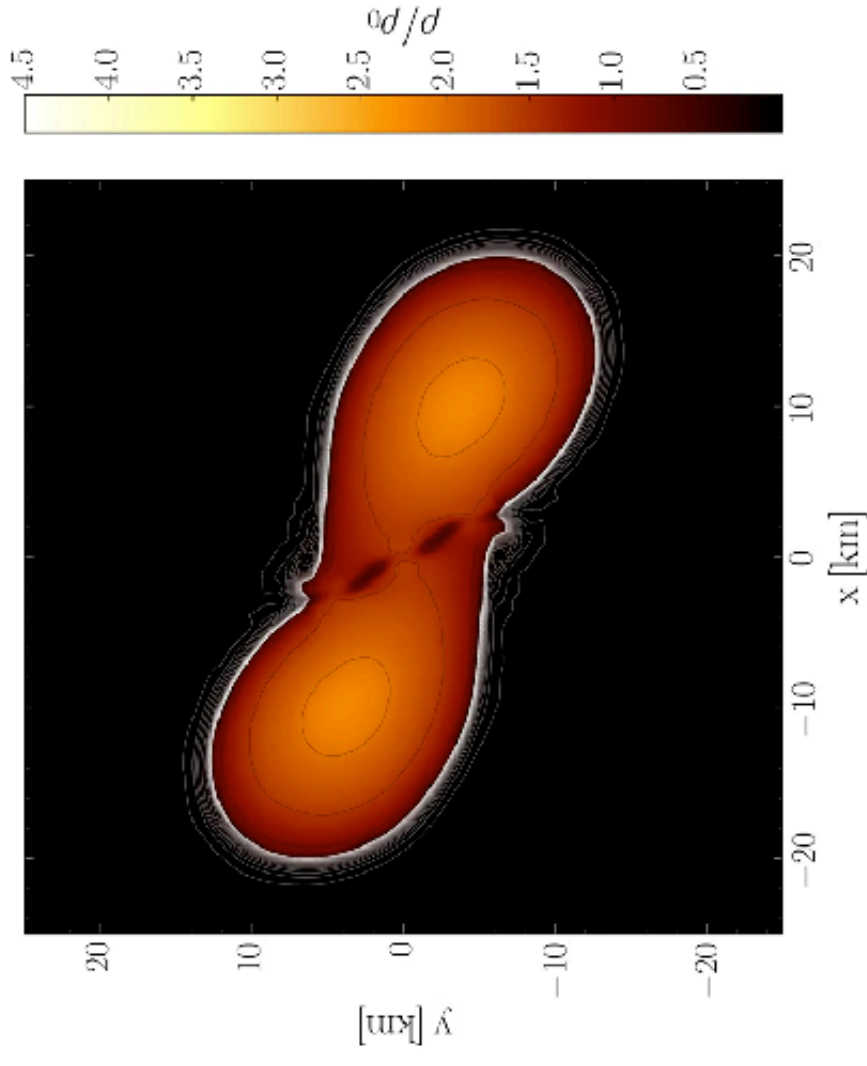
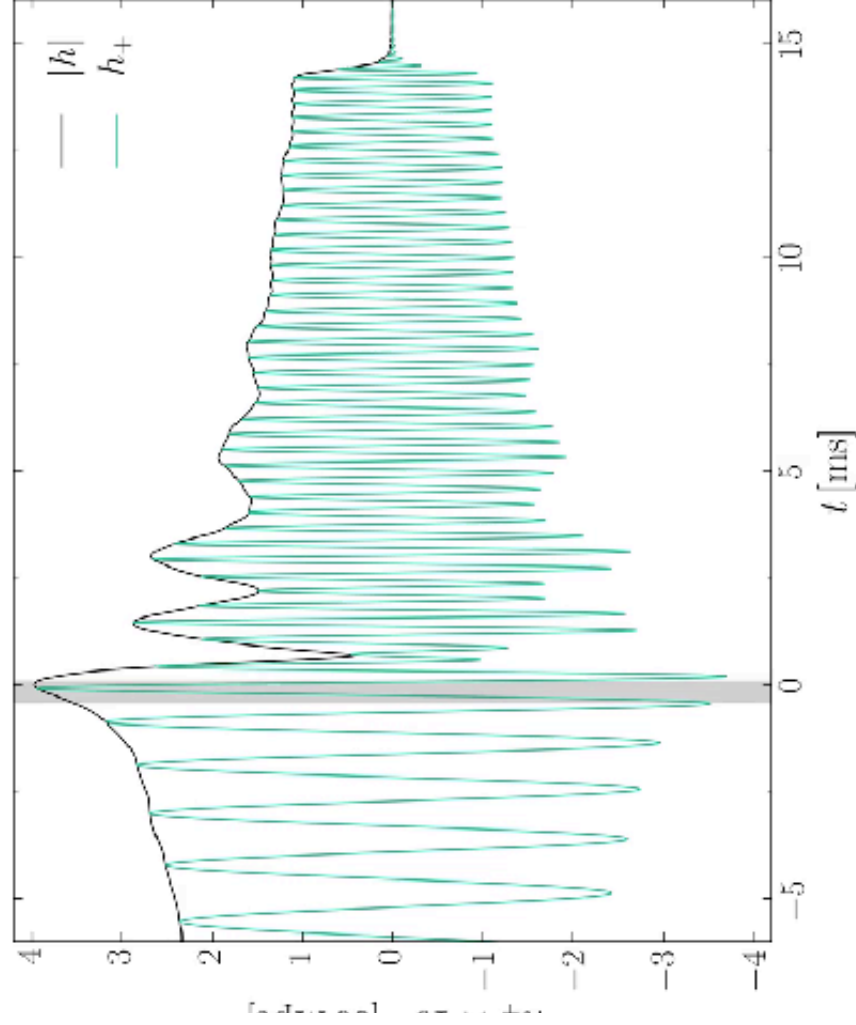
Oechslin+2007, Baiotti+2008, Bauswein+ 2011, 2012, Stergioulas+ 2011, Hotokezaka+ 2013, Takami 2014, 2015, Bernuzzi 2014, 2015, Bauswein+ 2015, LR+2016...



# Hypermassive Neutronstar GR Hydro Simulation

EoS Contains Neutrons, Protons, Electrons, Hyperons, Muons

At high net baryon density ( $3\rho_0$ ) **Quarkmatter!** Each NS:  $M = 1.35$  Solar Mass



Amplitude der emittierten Gravitationswelle  
im Abstand von 50 Mpc

Die Teilchendichte  $\rho(x,y)$   
in der äquatorialen Ebene in Einheiten der  
normalen nuklearen Dichte  $\rho_0$



# Extending the work to MHD

Neutron stars have large magnetic fields:  $10^8$ - $10^{12}$  G and it is the strong magnetic field that makes them observable as radio and pulsars.

As mentioned above, magnetic fields can play an important role and to study this it is necessary to solve the equations or relativistic magnetohydrodynamics (MHD)

We work within the ideal-MHD limit (i.e. infinite electrical conductivity) and this is an excellent approximation during the inspiral.

For simplicity, the magnetic fields are buried under the surface, to avoid magnetospheric problems

Typical evolution for a magnetized binary  
(hot EOS)  $M = 1.5 M_{\odot}$ ,  $B_0 = 10^{12}$  G

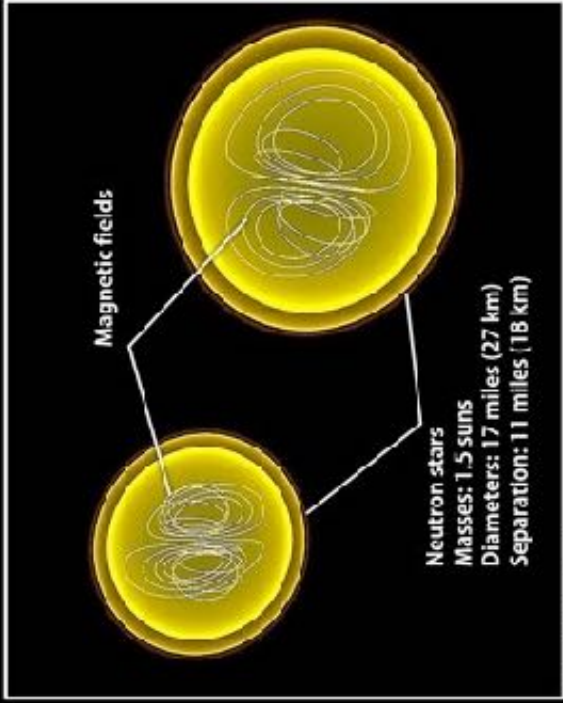


A magnetic jet is produced as a result  
of MHD instabilities and ultra-strong  
magnetic fields

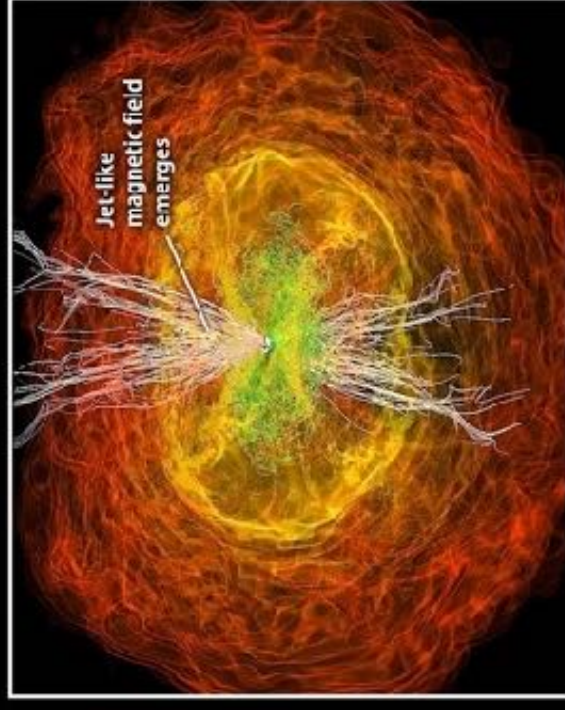
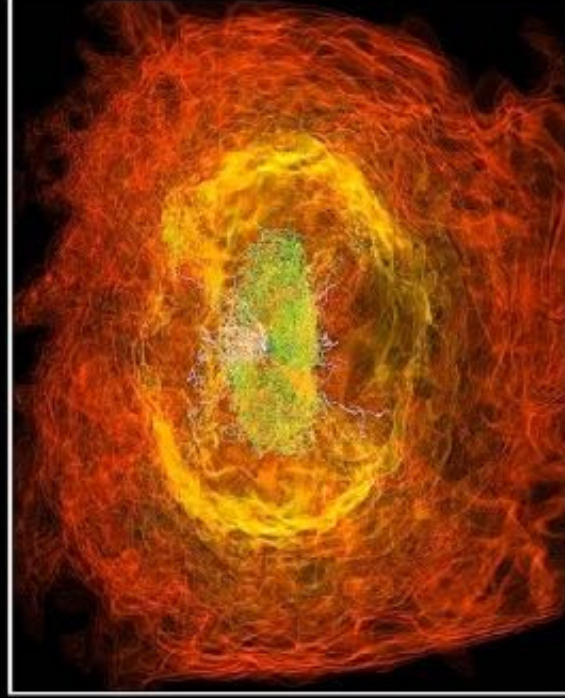
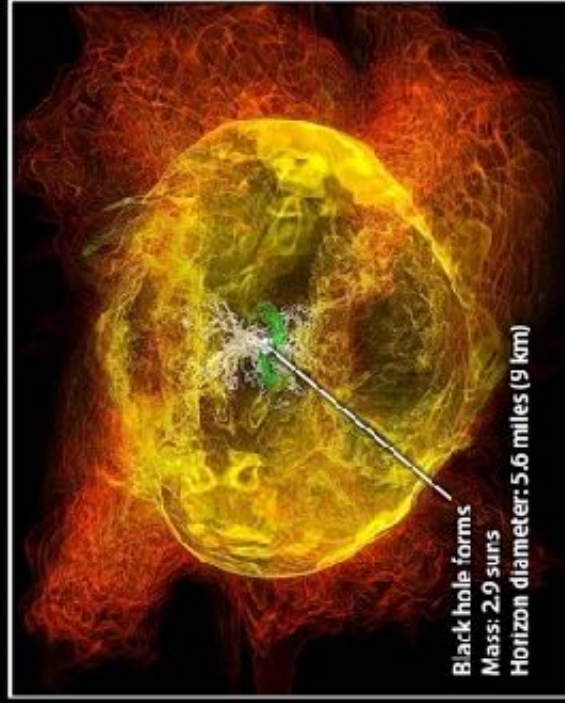
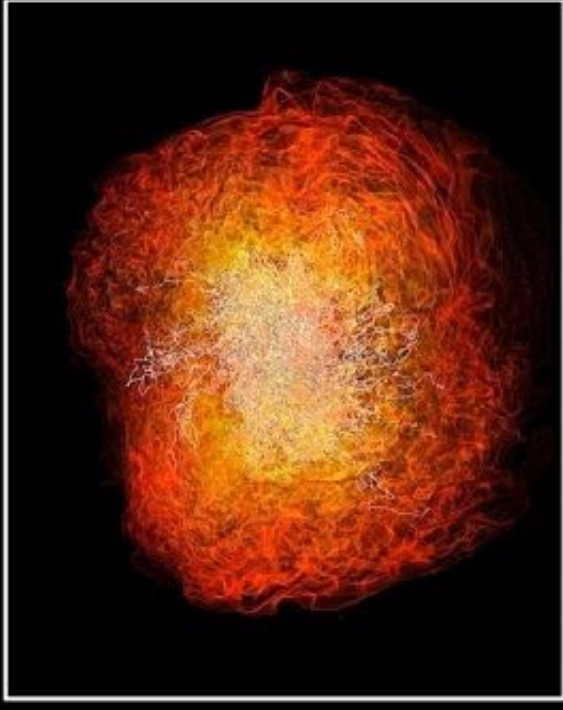
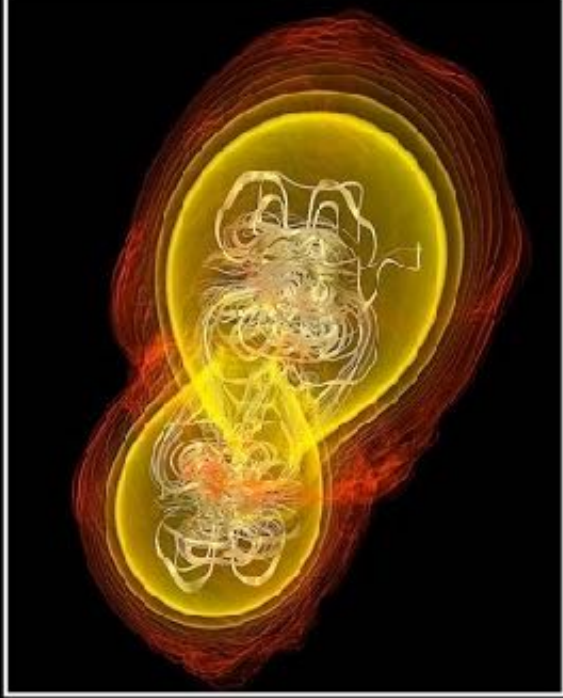




# Crashing neutron stars can make gamma-ray burst jets



Simulation begins



$$J/M^2 = 0.83$$

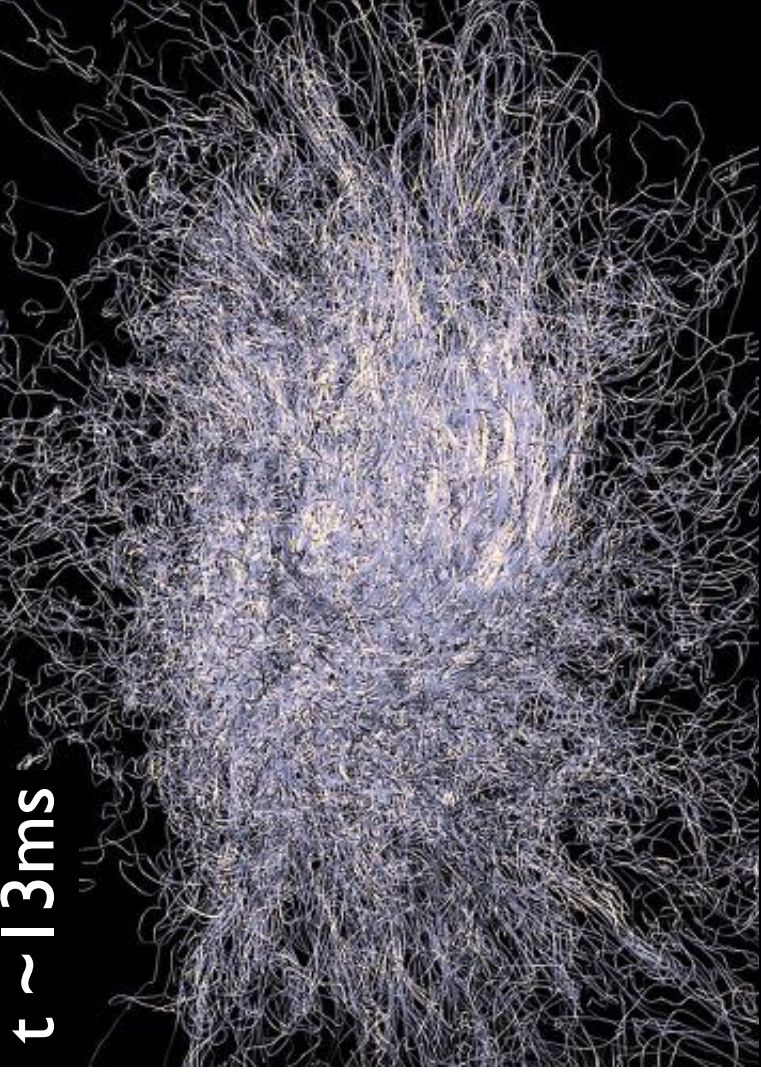
$$M_{\text{tor}} = 0.063 M_{\odot}$$

$$t_{\text{accr}} \simeq M_{\text{tor}} / \dot{M} \simeq 0.3 \text{ s}$$

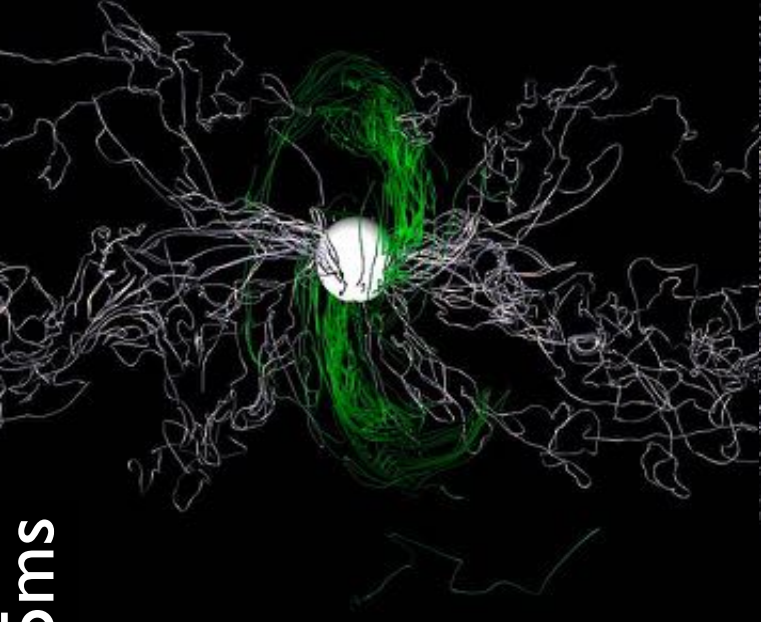
Credit: NASA/AEIZI/M. Koppitz and L. Rezzolla



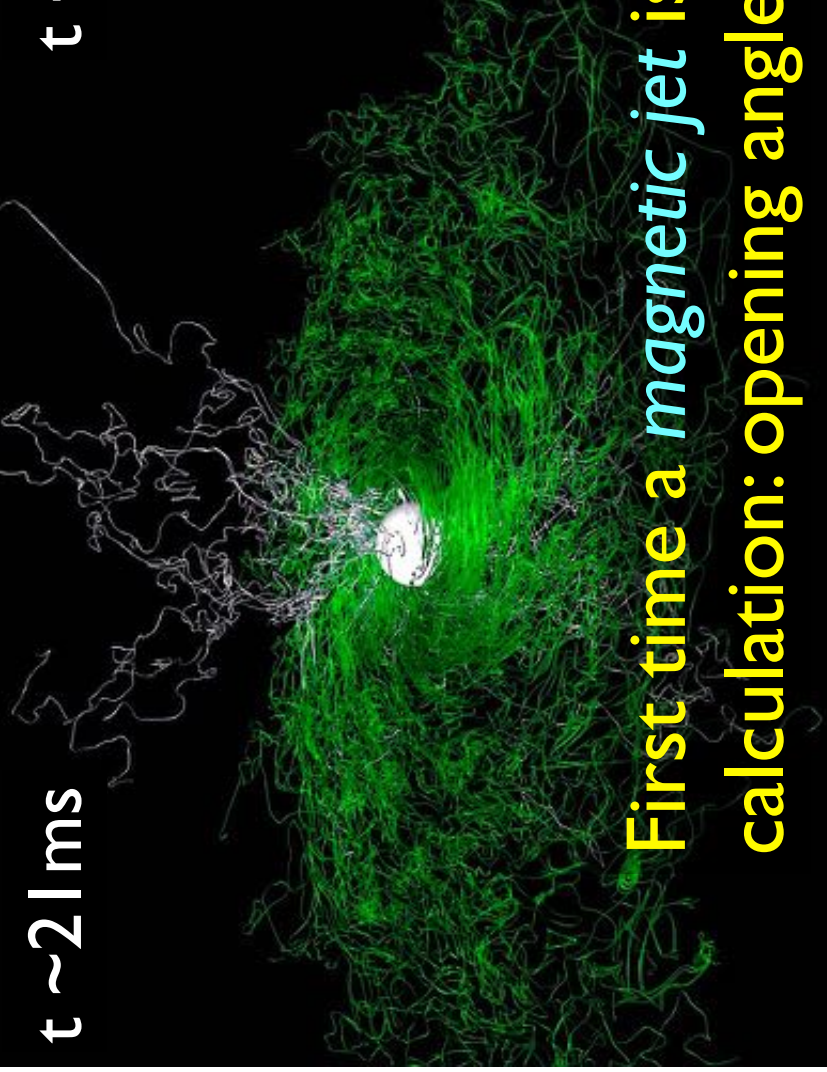
$t \sim 13\text{ms}$



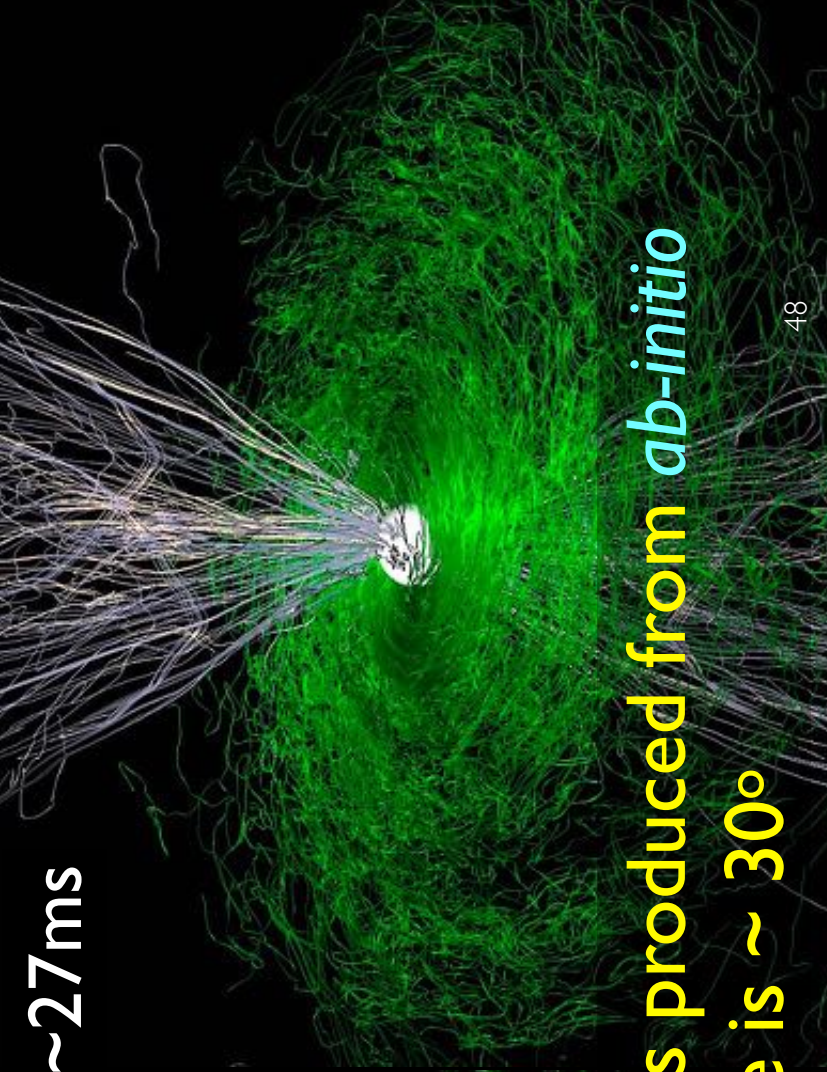
$t \sim 15\text{ms}$



$t \sim 21\text{ms}$



$t \sim 27\text{ms}$

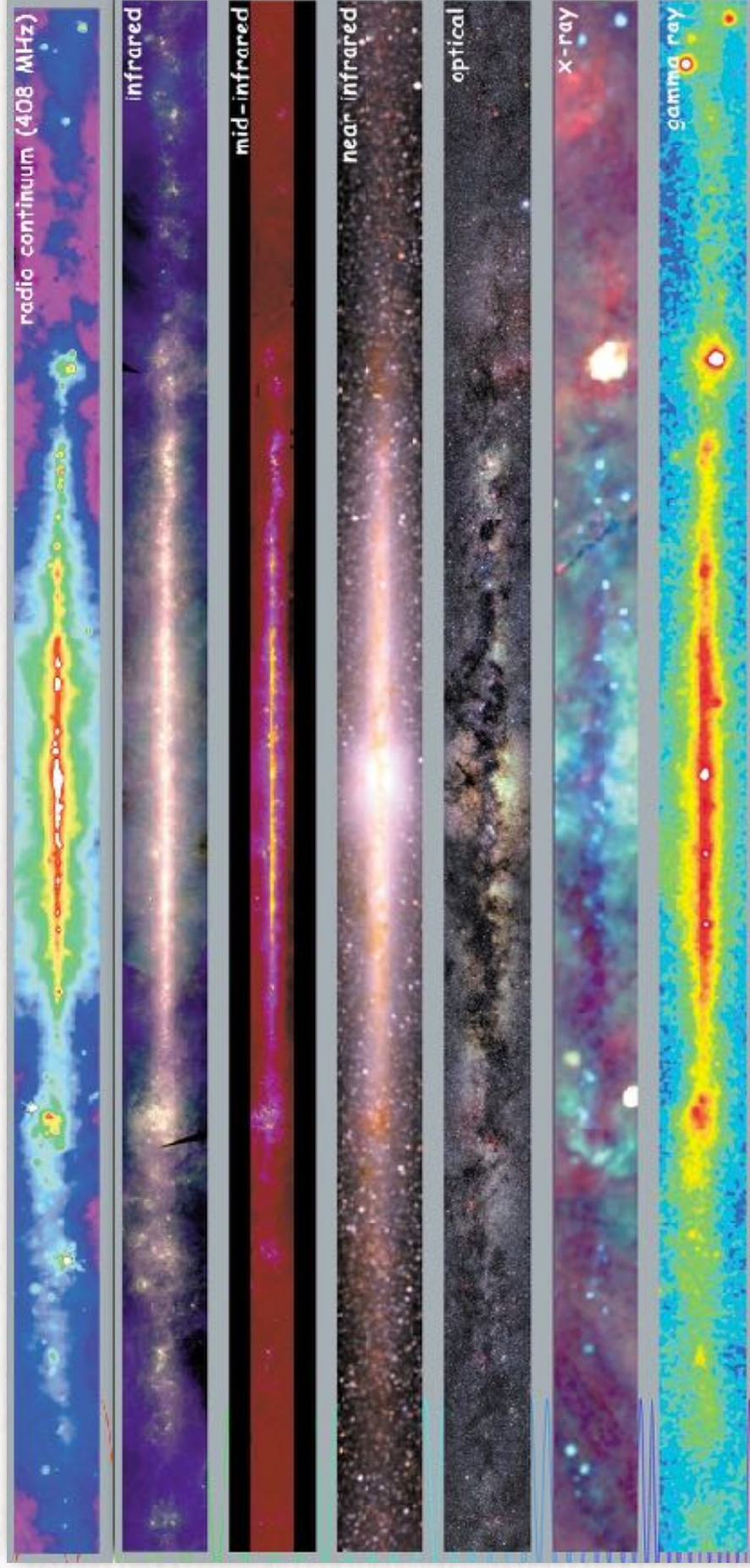


First time a magnetic jet is produced from *ab-initio* calculation: opening angle is  $\sim 30^\circ$



# Conclusions

GSFC/NASA



radio

far-IR

mid-IR

near-IR

optical

X-ray

gamma-ray

GWs

???

It has happened over and over in the history of astronomy: as a new “window” has been opened, a “new”, universe has been revealed.

GWs will reveal Einstein’s universe<sup>49</sup> of black holes and neutron stars