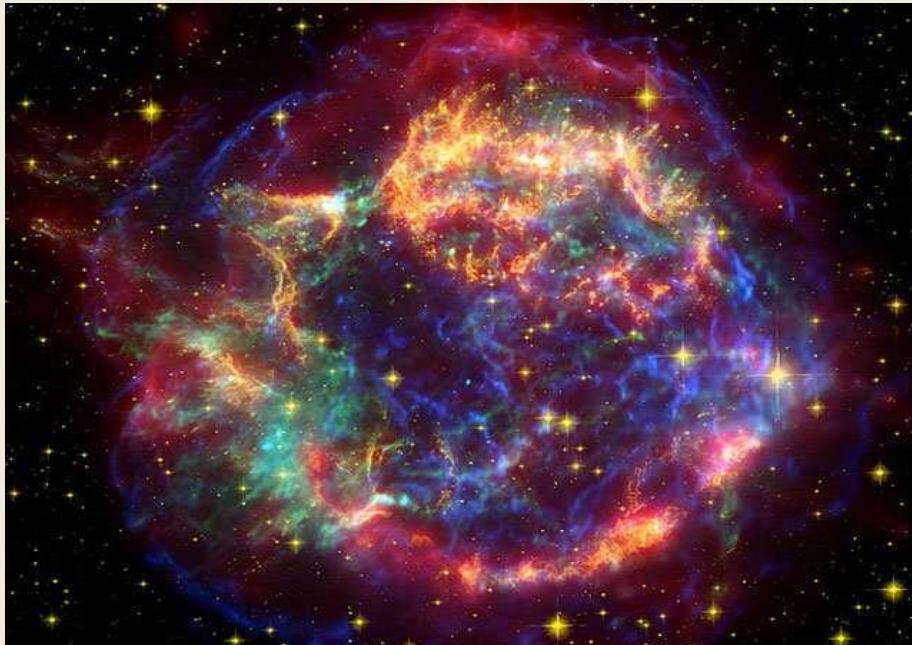


# Cooling of massive neutron stars



Hovik Grigorian:

*JINR – Dubna  
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***MPCS&RG - 2017  
Yerevan - 21  
September***

my co-authors: D.Blaschke, D.Voskresensky,  
N-U. Bastian, S. Typel, E. Kolomeitsev, K. Maslov

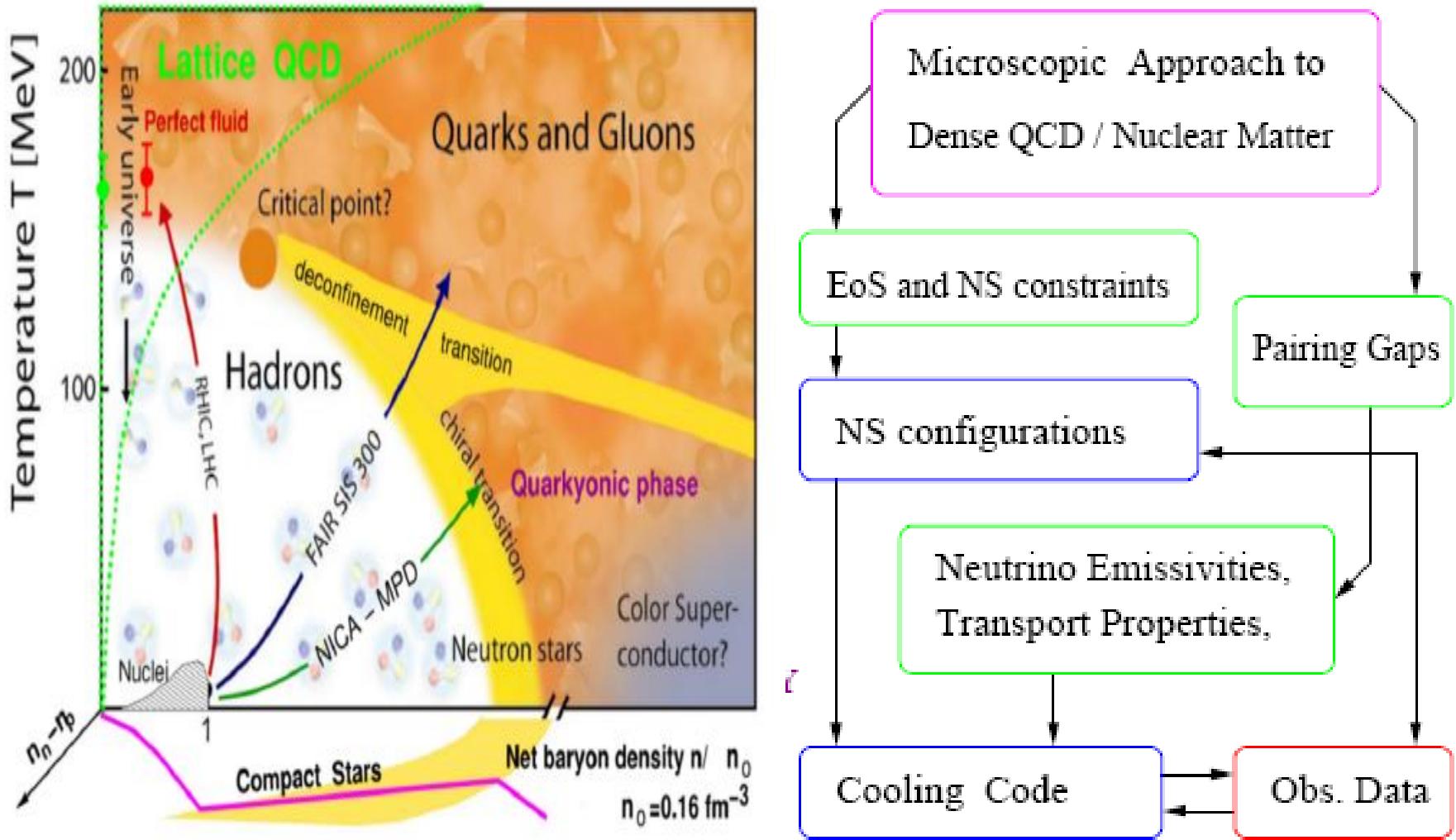
The research was carried out under financial support of the Russian Science Foundation (project #17-12-01427)

# Cooling Of Neutron Stars

- Introduction to Cooling Simulation
- Cooling regulators
- Time Evolution of Temperature
- *Superconductivity & in-medium effects*
- *Results for NS cooling*

H. Grigorian, D. N. Voskresensky and D. Blaschke  
Eur. Phys. J. A **52**: 67 (2016).

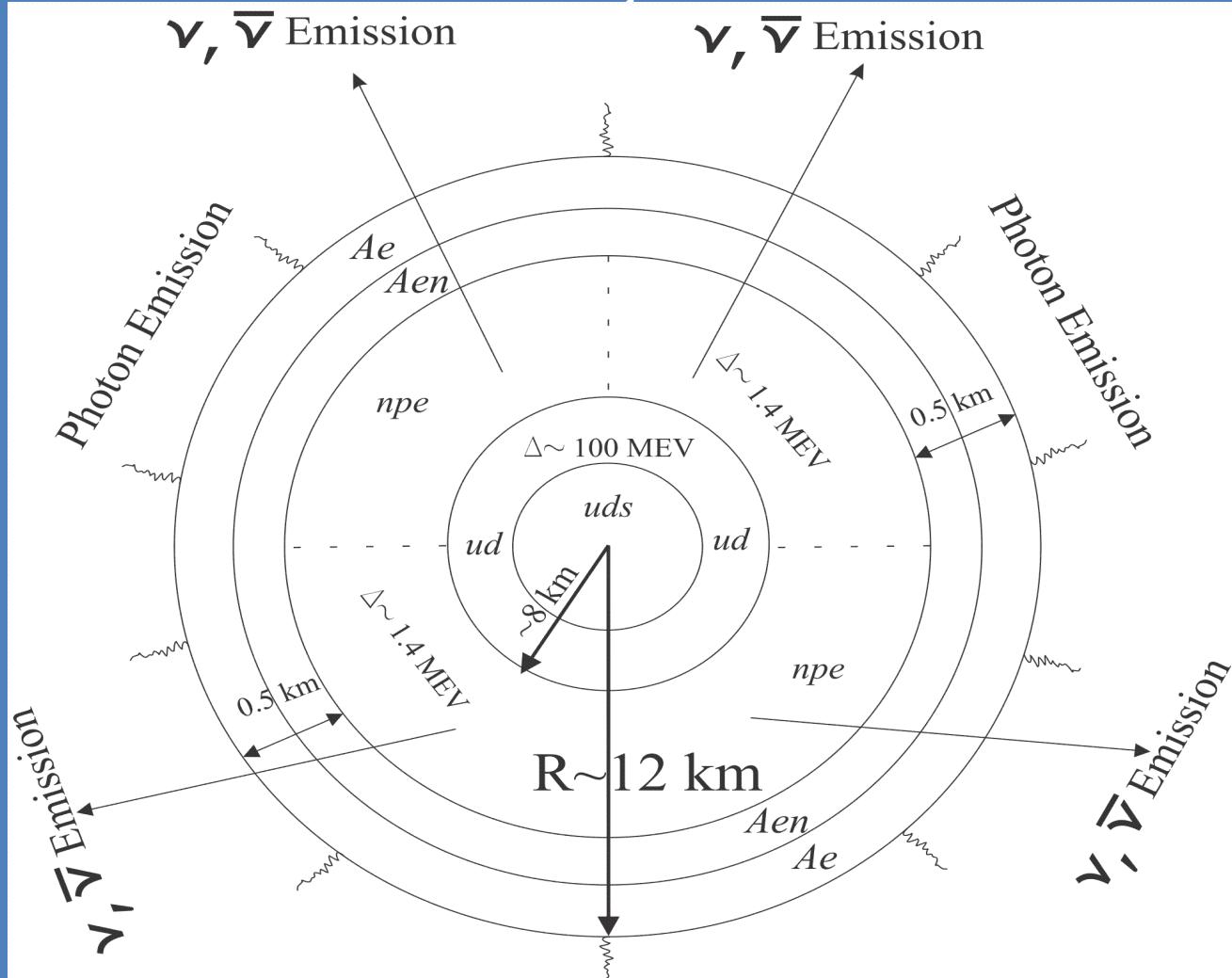
# Phase Diagramm & Cooling Simulation



# Phase Diagramm & Cooling Simulation

- ✓ Description of the stellar matter - local properties (EoS of super-dense matter)
- ✓ Modeling of the gravitationally self bound compact star - including the density profiles
- ✓ Extrapolations of the energy loss mechanisms to higher densities and temperatures
- ✓ Consistency of the approaches
- ✓ Comparison with observational data

# Structure Of Hybrid Star



## Static neutron star mass and radius

The structure and global properties of compact stars are obtained by solving the Tolman-Oppenheimer-Volkoff (TOV) equations<sup>1,2</sup>:

$$\left\{ \begin{array}{l} \frac{dP(r)}{dr} = -\frac{GM(r)\varepsilon(r)}{r^2} \frac{\left(1 + \frac{P(r)}{\varepsilon(r)}\right) \left(1 + \frac{4\pi r^3 P(r)}{M(r)}\right)}{\left(1 - \frac{2GM(r)}{r}\right)}; \\ \frac{dM(r)}{dr} = 4\pi r^2 \varepsilon(r); \\ \frac{dN_B(r)}{dr} = 4\pi r^2 \left(1 - \frac{2GM(r)}{r}\right)^{-1/2} n(r). \end{array} \right.$$

<sup>1</sup>R. C. Tolman, Phys. Rev. **55**, 364 (1939).

<sup>2</sup>J. R. Oppenheimer and G. M. Volkoff, Phys. Rev. **55**, 374 (1939).

# Modification of HHJ (HDD) parameterization of EoS

As mentioned, we adopted the HHJ ( $\delta = 0.2$ ) EoS for the description of the nucleon contribution. The energy density of nucleons is parameterized as follows:

$$E_N = un_0 \left[ m_N + e_B u \frac{2 + \delta - u}{1 + \delta u} + a_{\text{sym}} u^{0.6} (1 - 2x_p)^2 \right], \quad (5)$$

where  $u = n/n_0$ ,  $e_B \simeq -15.8$  MeV is the nuclear binding energy per nucleon,  $a_{\text{sym}} \simeq 32$  MeV is the symmetry energy coefficient and we chose  $\delta = 0.2$ . With these values of parameters one gets the best fit of APR (A18 +  $\delta v$  + UIX\*)

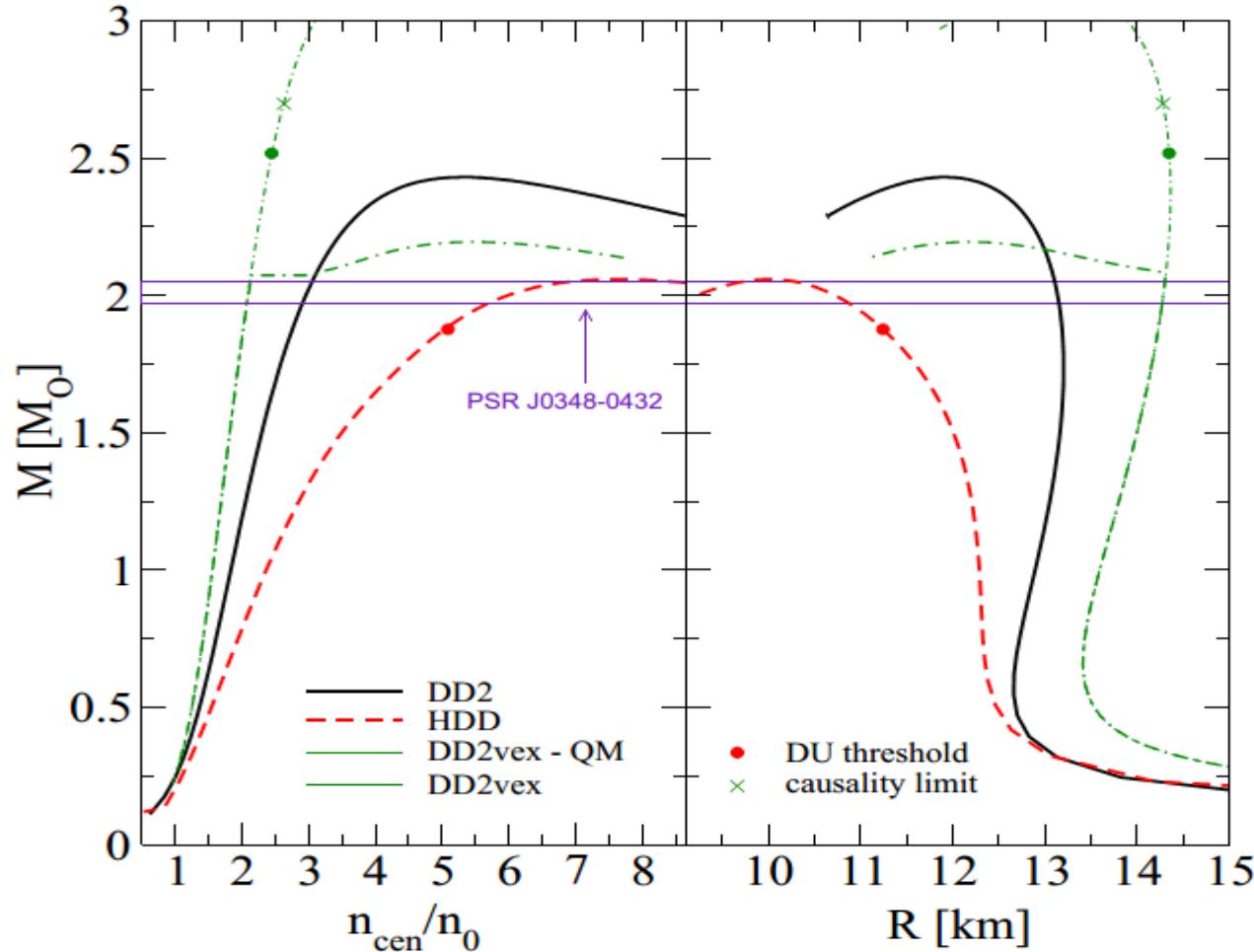
Introduction of the excluded volume

H. Heiselberg and M. Hjorth-Jensen, [Astrophys. J. 525, L45 \(1999\)](#).

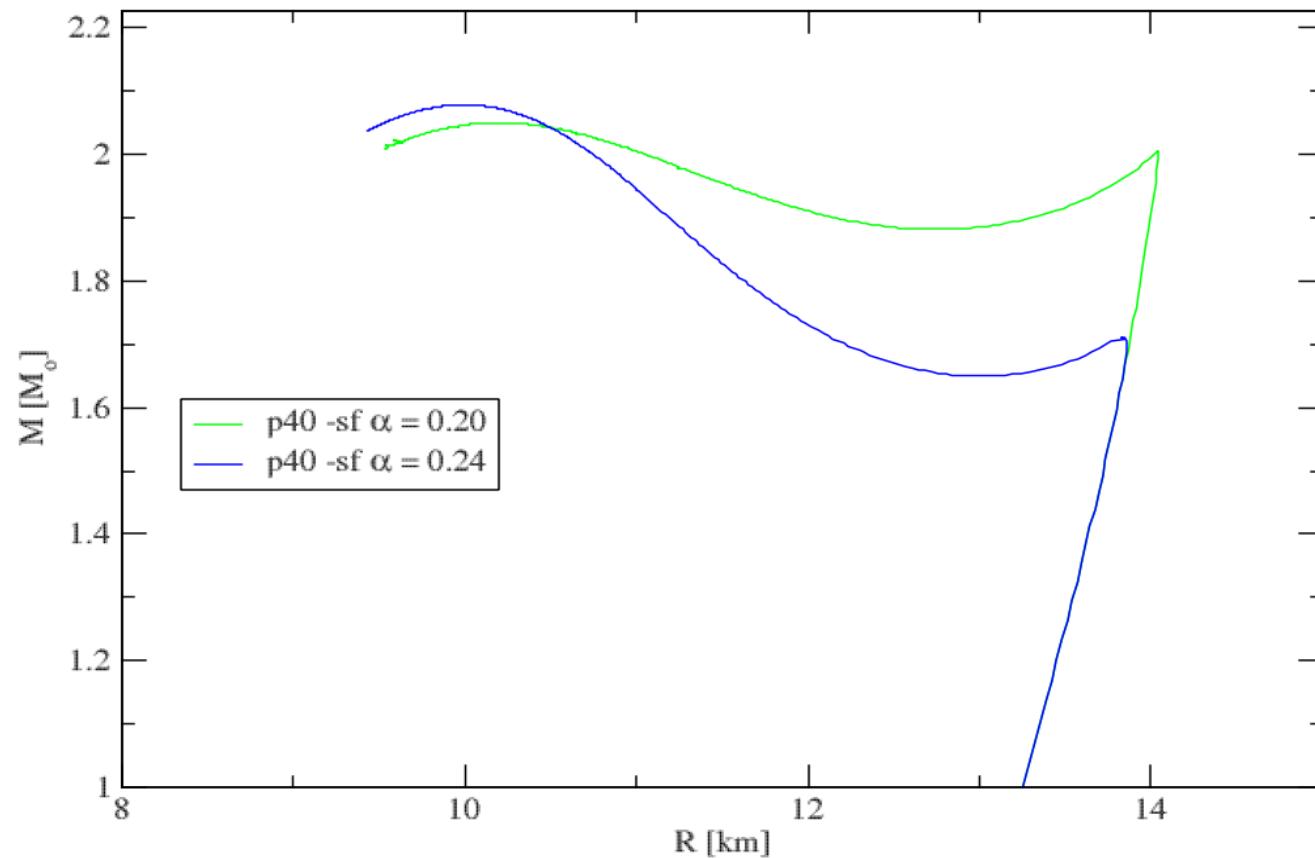
$$u \rightarrow \frac{u}{1 - \alpha u e^{-(\beta/u)^\alpha}}$$

# Stability of stars

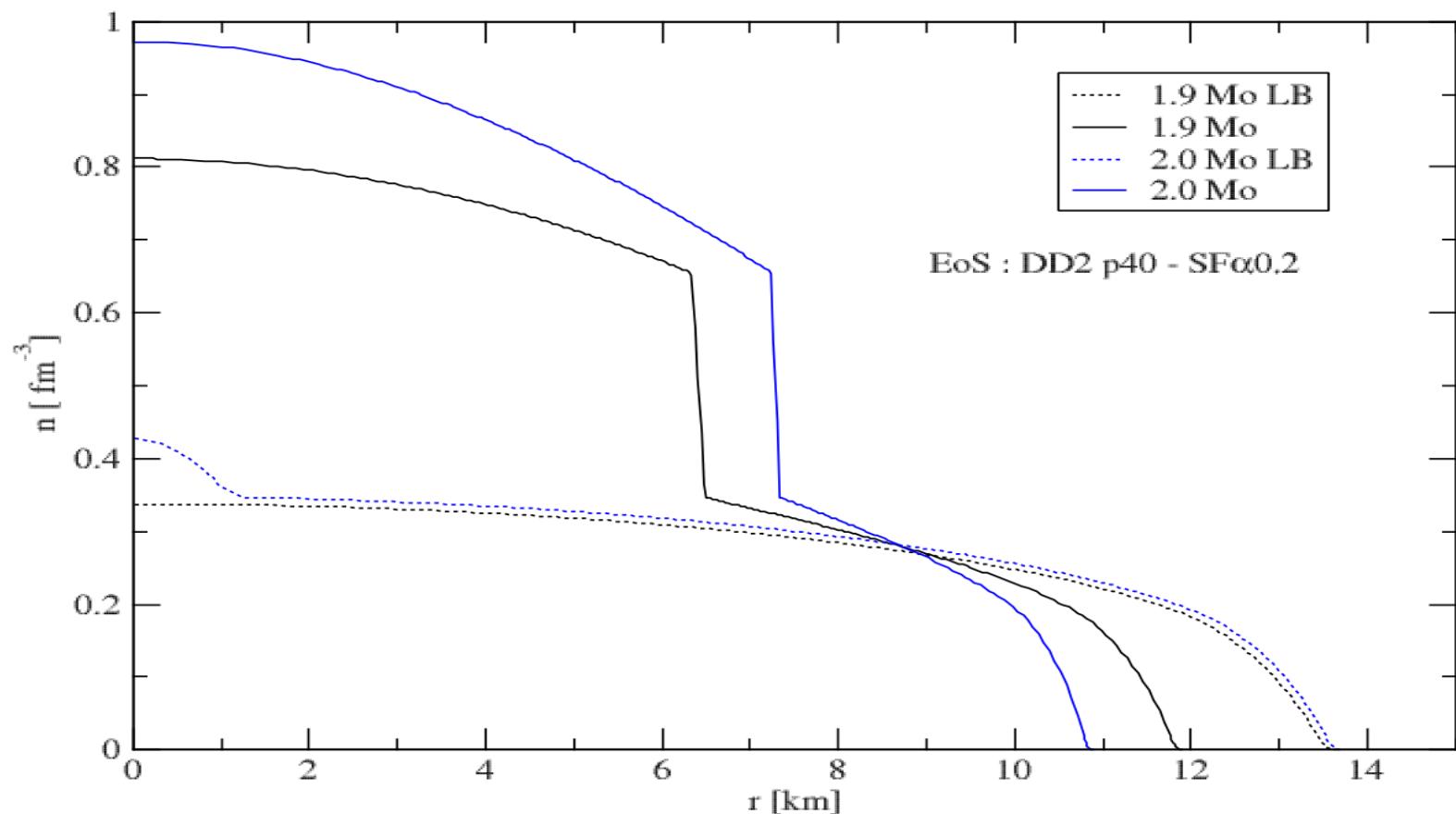
## HDD, DD2 & DDvex-NJL EoS model



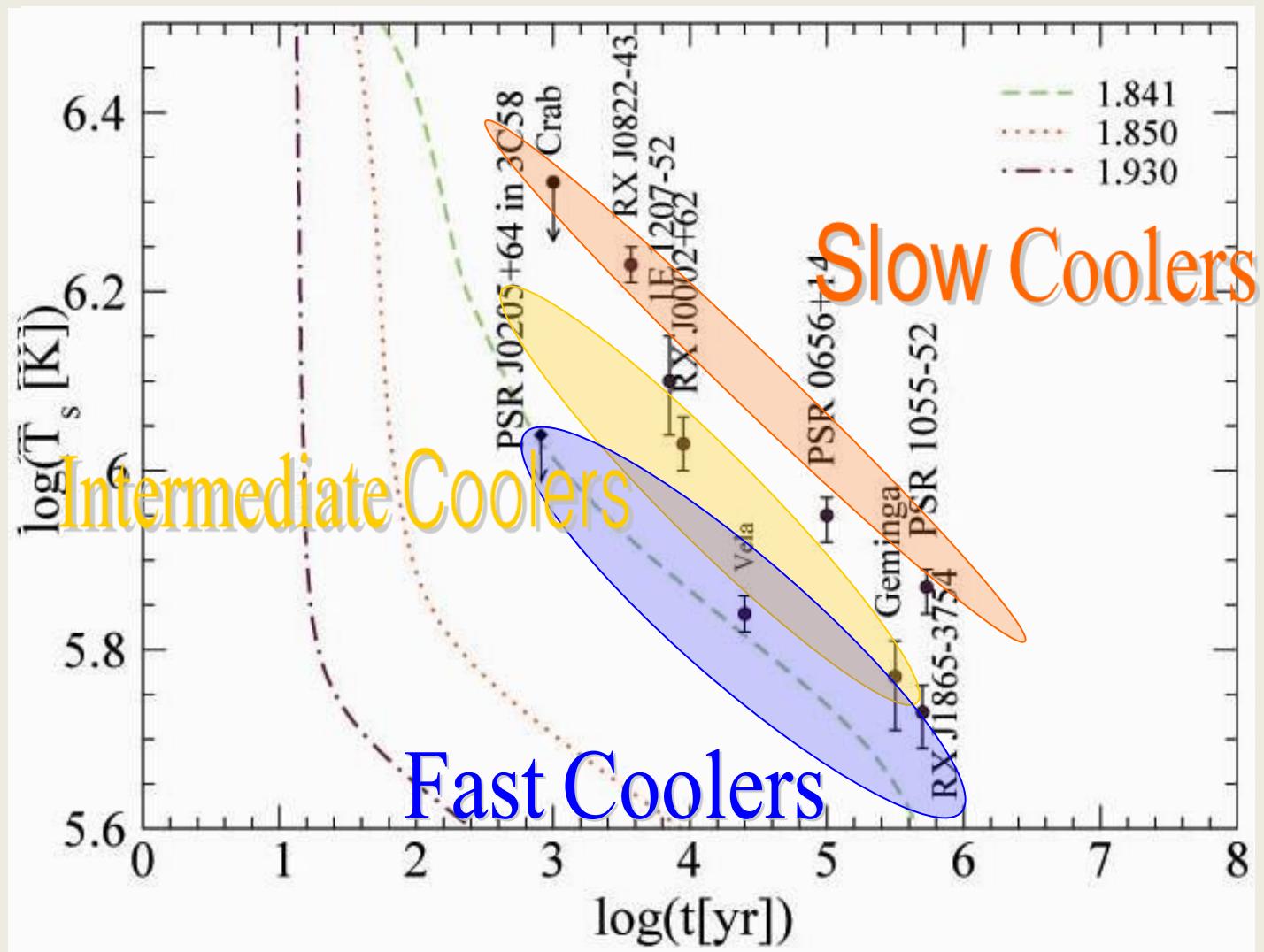
# High Mass Twin CS



# Different Configurations with the same NS mass



# Surface Temperature & Age Data



# Cooling Mechanism

$$\frac{dU}{dt} = \sum_i C_i \frac{dT}{dt} = -\varepsilon_\gamma - \sum_j \varepsilon_\nu^j$$

## Cooling Processes

- ➡ Direct Urca:  $n \rightarrow p + e + \bar{\nu}_e$
- ➡ Modified Urca:  $n + n \rightarrow n + p + e + \bar{\nu}_e$
- ➡ Photons:  $\rightarrow \gamma$
- ➡ Bremsstrahlung:  $n + n \rightarrow n + n + \nu + \bar{\nu}$

# Cooling Evolution

The energy flux per unit time  $I(r)$  through a spherical slice at distance  $r$  from the center is:

$$I(r) = -4\pi r^2 k(r) \frac{\partial(T e^\Phi)}{\partial r} e^{-\Phi} \sqrt{1 - \frac{2M}{r}}.$$

The equations for energy balance and thermal energy transport are:

$$\frac{\partial}{\partial N_B}(l e^{2\Phi}) = -\frac{1}{n}(\epsilon_\nu e^{2\Phi} + c_V \frac{\partial}{\partial t}(T e^\Phi))$$

$$\frac{\partial}{\partial N_B}(T e^\Phi) = -\frac{1}{k} \frac{l e^\Phi}{16\pi^2 r^4 n}$$

where  $n = n(r)$  is the baryon number density,  $N_B = N_B(r)$  is the total baryon number in the sphere with radius  $r$

$$\frac{\partial N_B}{\partial r} = 4\pi r^2 n \left(1 - \frac{2M}{r}\right)^{-1/2}$$

F.Weber: Pulsars as Astro. Labs ... (1999);

D. Blaschke Grigorian, Voskresensky, A&A 368 (2001) 561.

# Neutrino emissivities in hadronic matter:

- Direct Urca (DU) the most efficient processes

$$\epsilon_{DU} = M_{DU} * (m_p^*)(m_n^*) * \Gamma_{wN}^2 * (n_e)^{1/3} (T_9)^6 * R_D;$$

$$M_{DU} = 4 \times 10^{27} \text{ erg/s/cm}^3$$

- Modified Urca (MU) and Bremsstrahlung

$$\epsilon_{MUp} = F_M * M_p * (m_p)^3 (m_n^*)(T_9)^8 (n_e)^{1/3} * R_{MUp}(v_n, v_p);$$

$$\epsilon_{nnBS} = P_{nnBS} * R_{BS}^{nn}(v_n) * \Gamma_w^2 \Gamma_s^4 (n_b)^{4/3} (T_9)^8 (m_n^*)^4 / (\omega)^3;$$

- Suppression due to the pairing

$$v_N = \Delta_N(T)/T = \sqrt{1 - \tau_N} \left( 1.456 - \frac{0.157}{\sqrt{\tau_N}} + \frac{1.766}{\tau_N} \right)$$

- Enhanced cooling due to the pairing

$$\epsilon_\nu^{\text{NPBF}} = 6.6 \times 10^{28} (m_n^*/m_n) (\Delta_n(T)/\text{MeV})^7 u^{1/3} \\ \times \xi I(\Delta_n(T)/T) \text{ erg cm}^{-3} \text{s}^{-1},$$

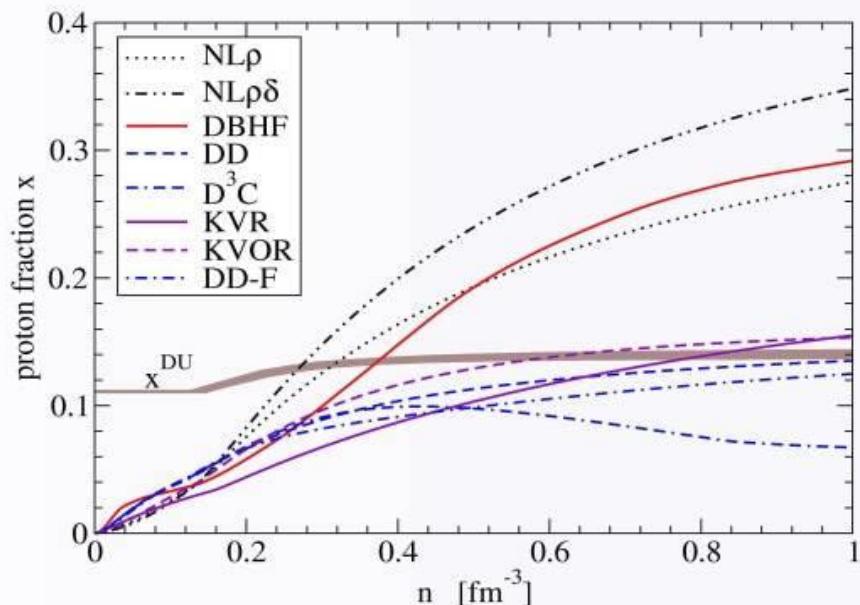
$$\epsilon_\nu^{\text{PPBF}} = 0.8 \times 10^{28} (m_p^*/m_p) (\Delta_p(T)/\text{MeV})^7 u^{2/3} \\ \times I(\Delta_p(T)/T) \text{ erg cm}^{-3} \text{s}^{-1},$$

# DU constraint

$n \rightarrow p + e + \bar{\nu}_e$  implies  $p_n \leq p_p + p_e$ , charge neutrality results in

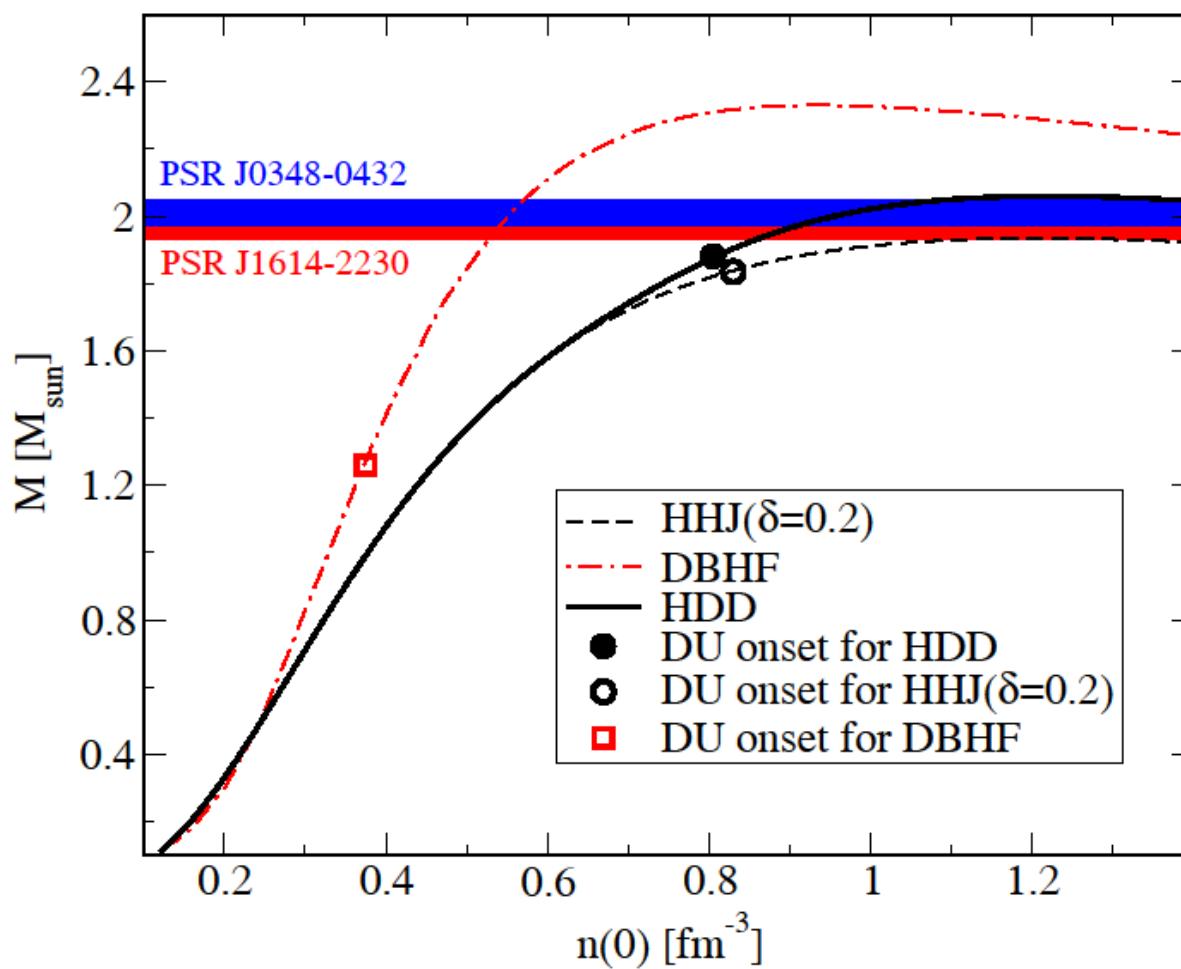
$$x_{DU}(x_e) \geq \frac{1}{1 + (1 + x_e^{1/3})^3} \quad x_e = n_e/(n_e + n_\mu)$$

- » no muons:  $x_{DU} = 11.1\%$
- » relativistic limit ( $n_e = n_\mu$ ):  $x_{DU} = 14.8\%$



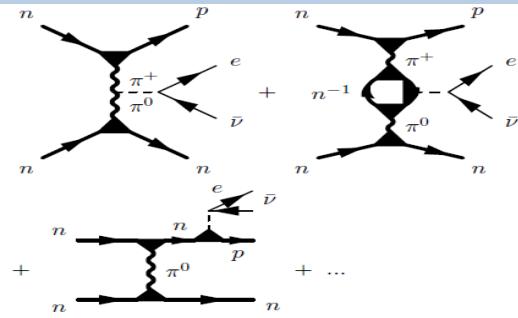
$\text{NL}\rho, \text{NL}\rho\delta, \text{DBHF}$ :  
DU occurs below  $2.5n_0$

# The Mass constraint and DU - onsets



# Medium Effects In Cooling Of Neutron Stars

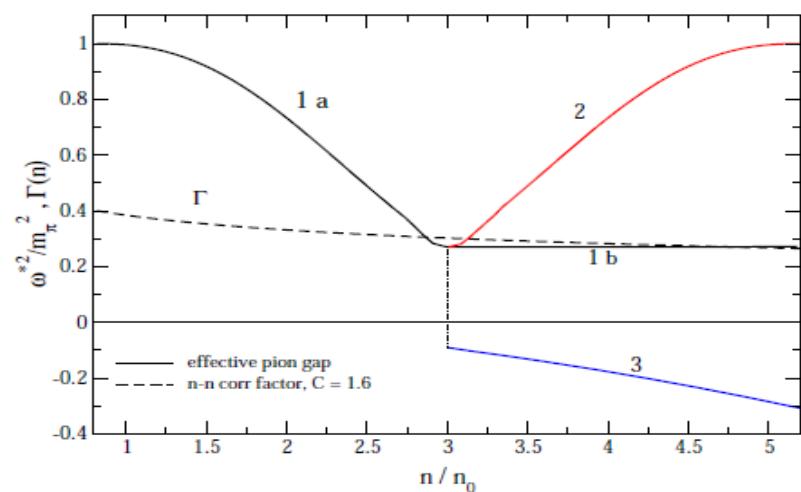
- Based on Fermi liquid theory ( Landau (1956), Migdal (1967), Migdal et al. (1990))
- MMU – instead of MU



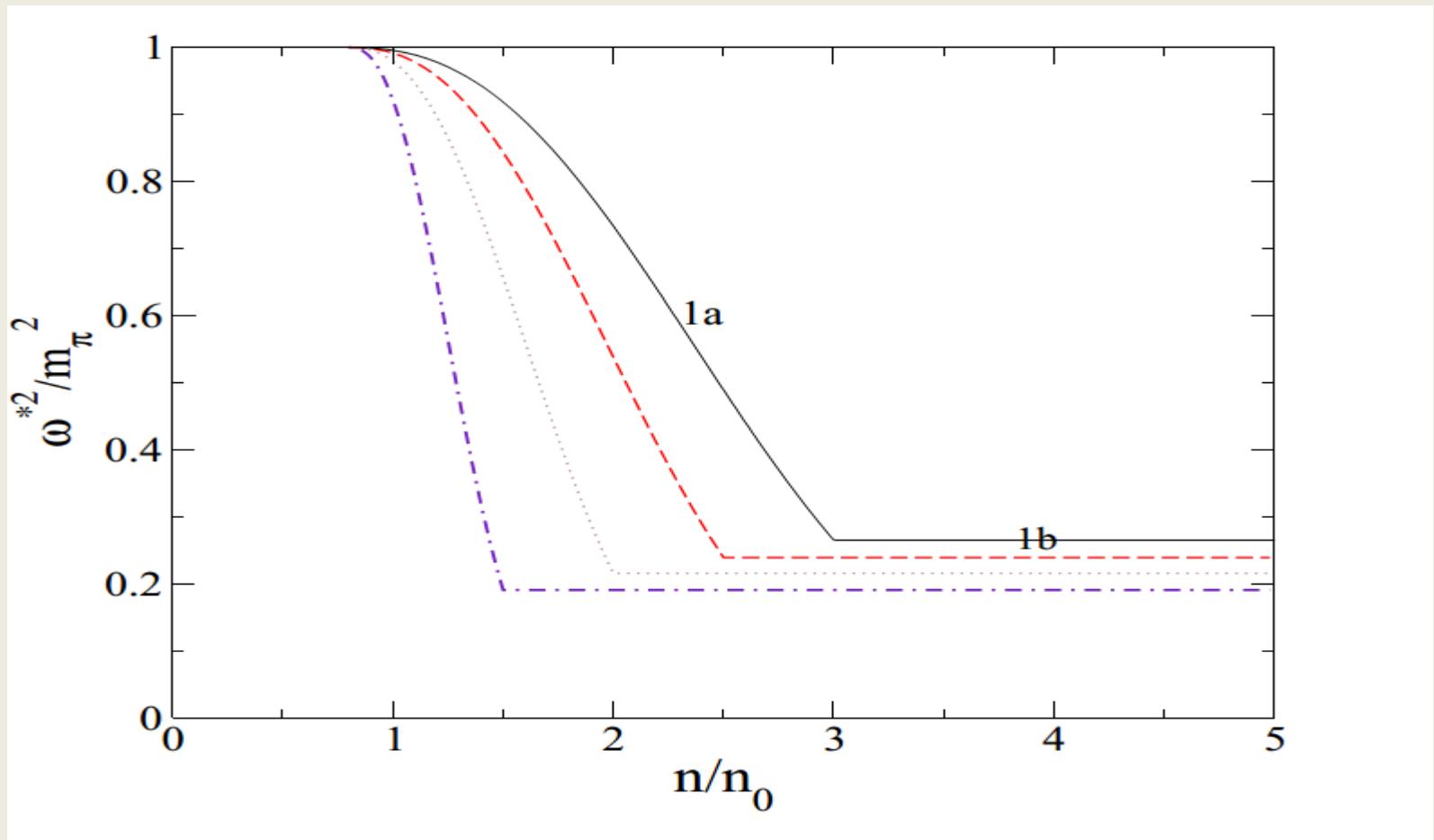
$$\frac{\varepsilon_\nu[\text{MMU}]}{\varepsilon_\nu[\text{MU}]} \sim 10^3 (n/n_0)^{10/3} \frac{\Gamma^6(n)}{[\omega^*(n)/m_\pi]^8},$$

- Main regulator in Minimal Cooling

$$\begin{aligned} \varepsilon_\nu[\text{MpPBF}] &\sim 10^{29} \frac{m_N^*}{m_N} \left[ \frac{p_{Fp}}{p_{Fn}(n_0)} \right] \left[ \frac{\Delta_{pp}}{\text{MeV}} \right]^7 \\ &\times \left[ \frac{T}{\Delta_{pp}} \right]^{1/2} \xi_{pp}^2 \frac{\text{erg}}{\text{cm}^3 \text{ sec}}, \quad T < T_{cp}. \end{aligned}$$



# Medium Effects In Cooling Of Neutron Stars



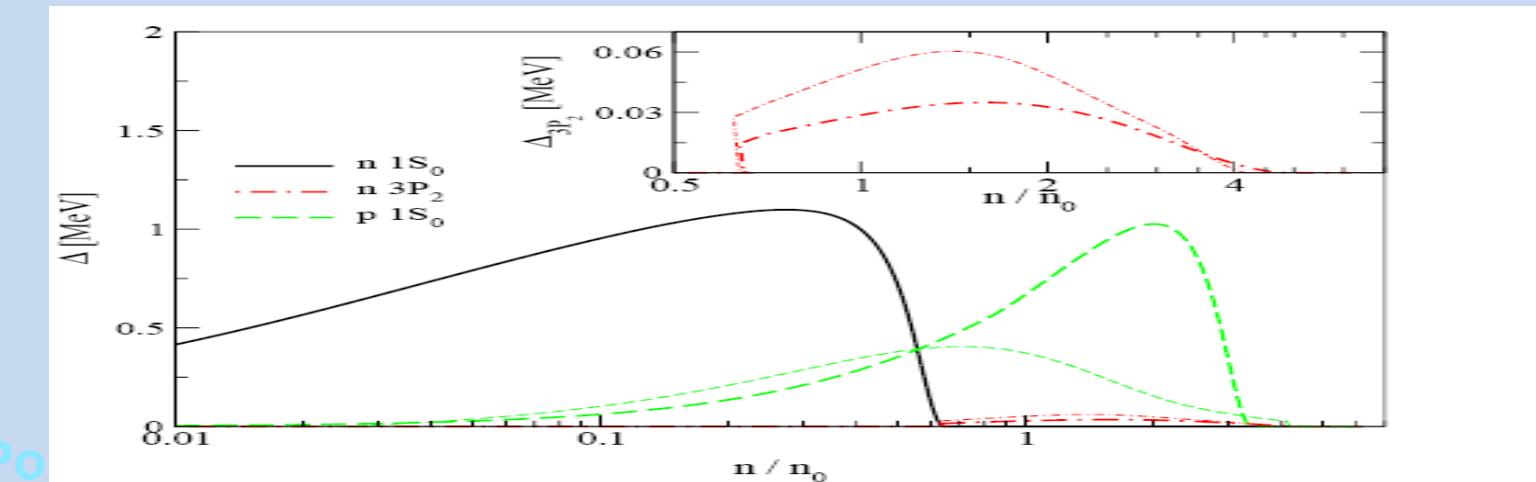
# SC Pairing Gaps

- 2SC phase: 1 color (blue) is unpaired (mixed superconductivity)
- Ansatz    2SC + X phase:

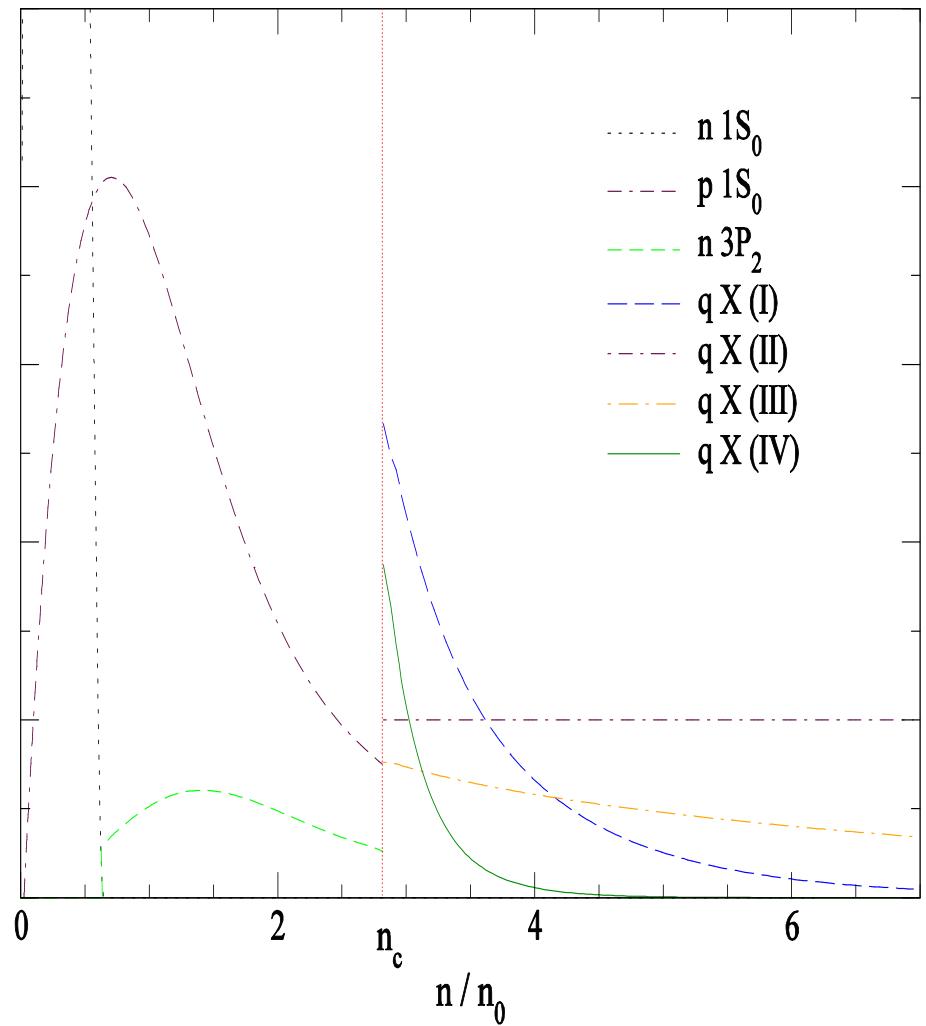
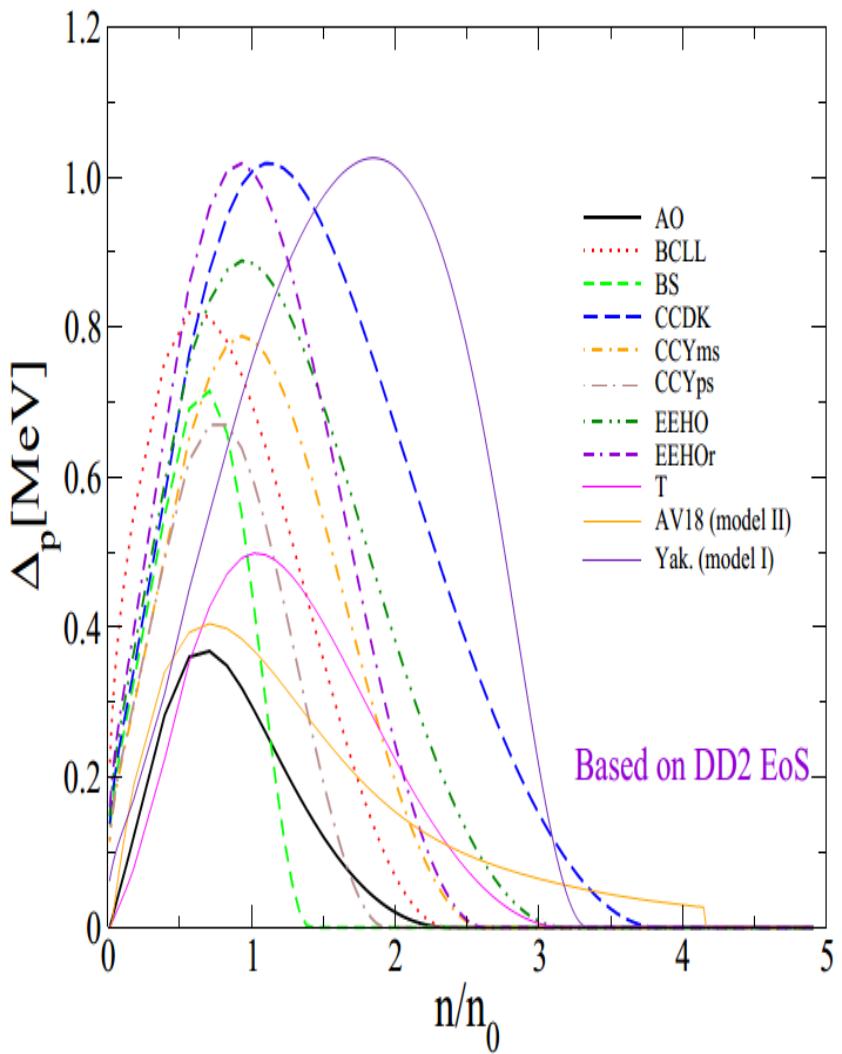
$$\Delta_0^X = \Delta_0 \exp -\alpha \left( \frac{\mu - \mu_c}{\mu_c} \right)$$

Model	$\Delta_0$ [MeV]	$\alpha$
I	1	10
II	0.1	0
III	0.1	2
IV	5	25

Pairing gaps for hadronic phase  
**(AV18 - Takatsuka et al. (2004))**



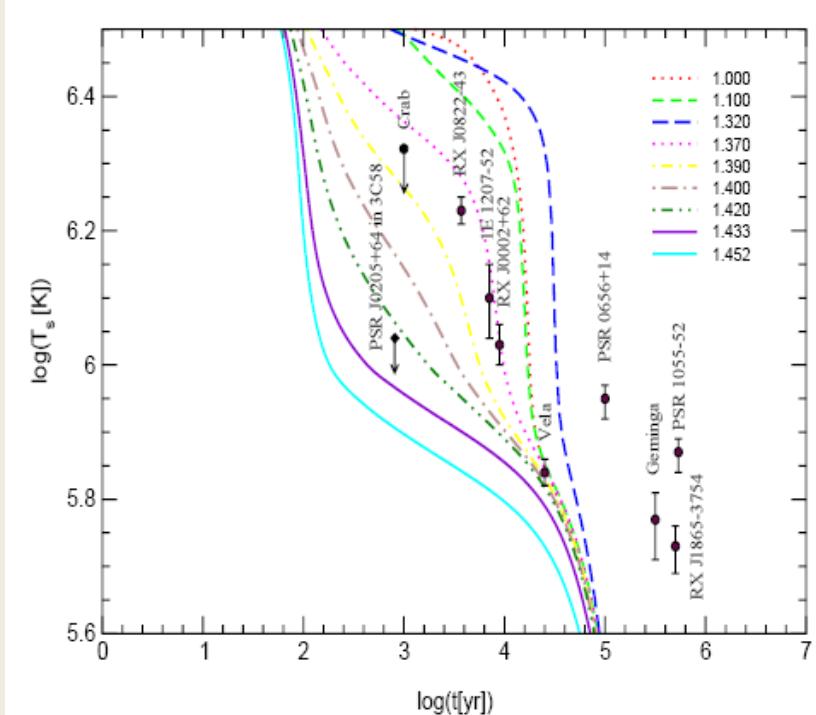
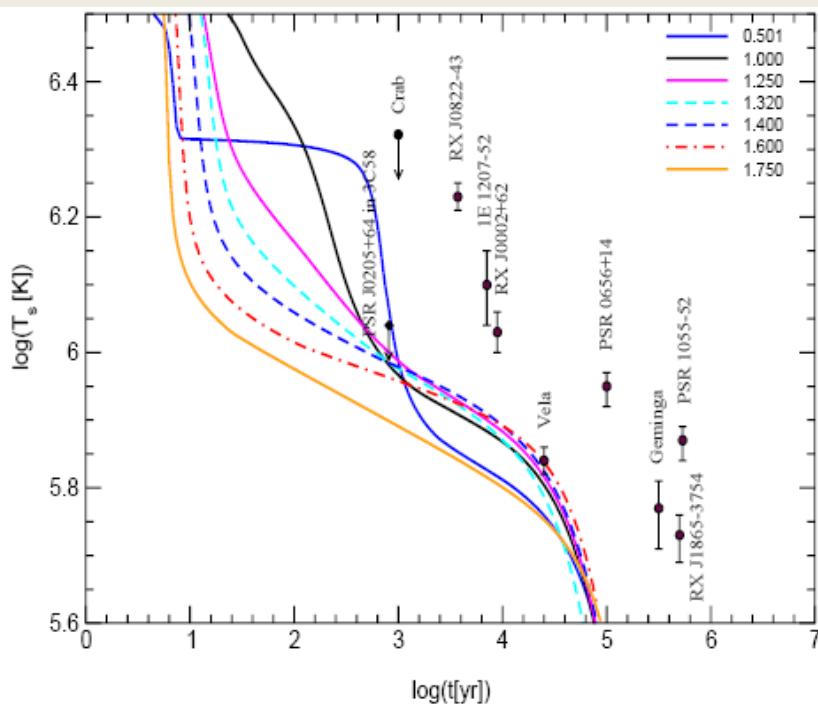
# SC Pairing Gaps



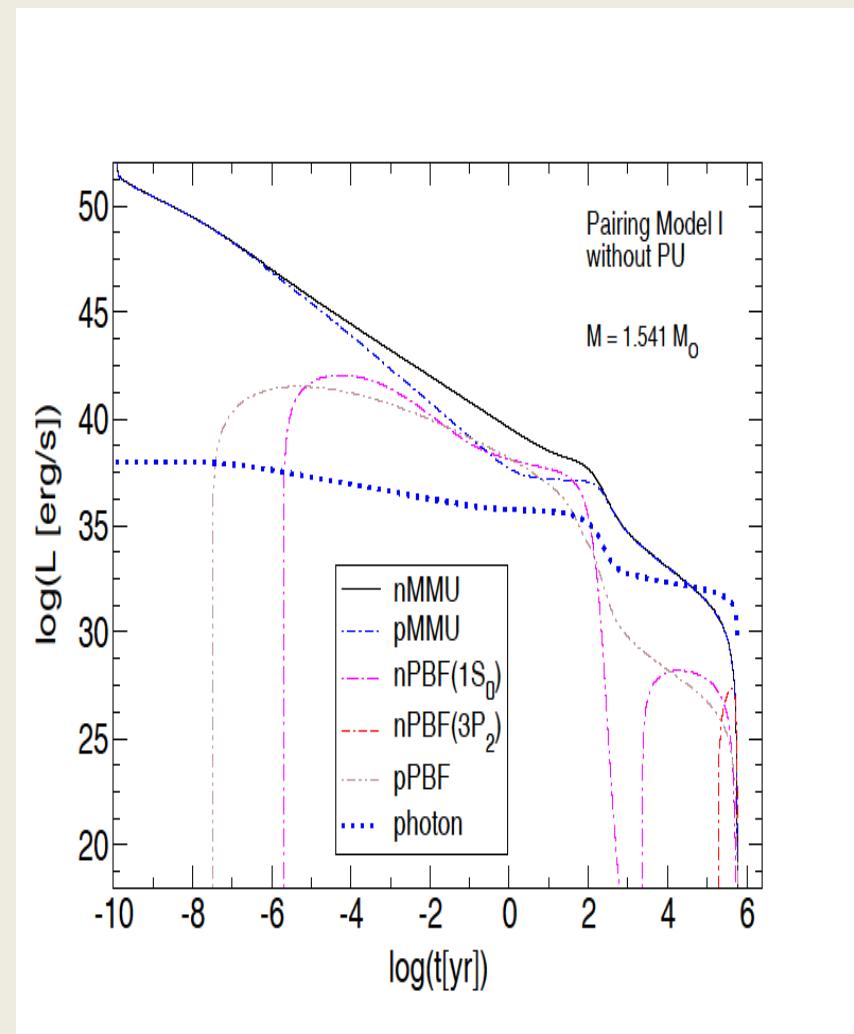
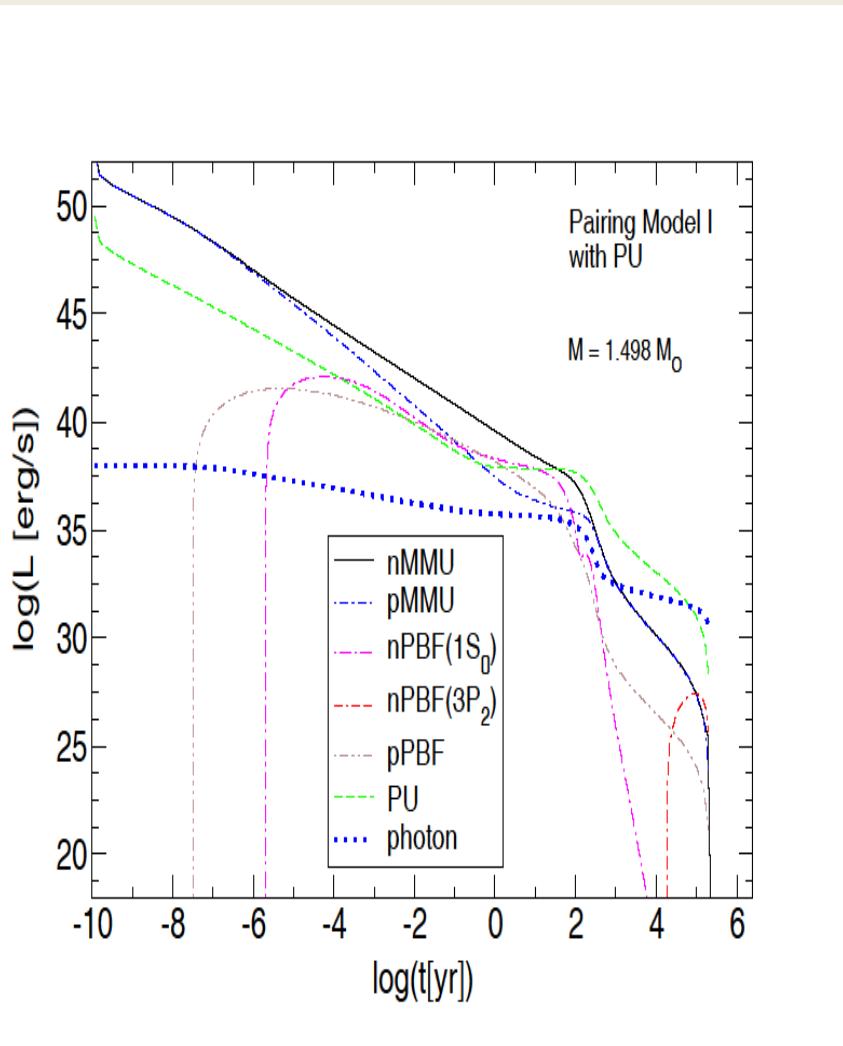
# Anomalies Because Of PBF Process

AV18 gaps, pi-condensate, without suppression of  $\beta$ P2 neutron pairing - Enhanced PBF process

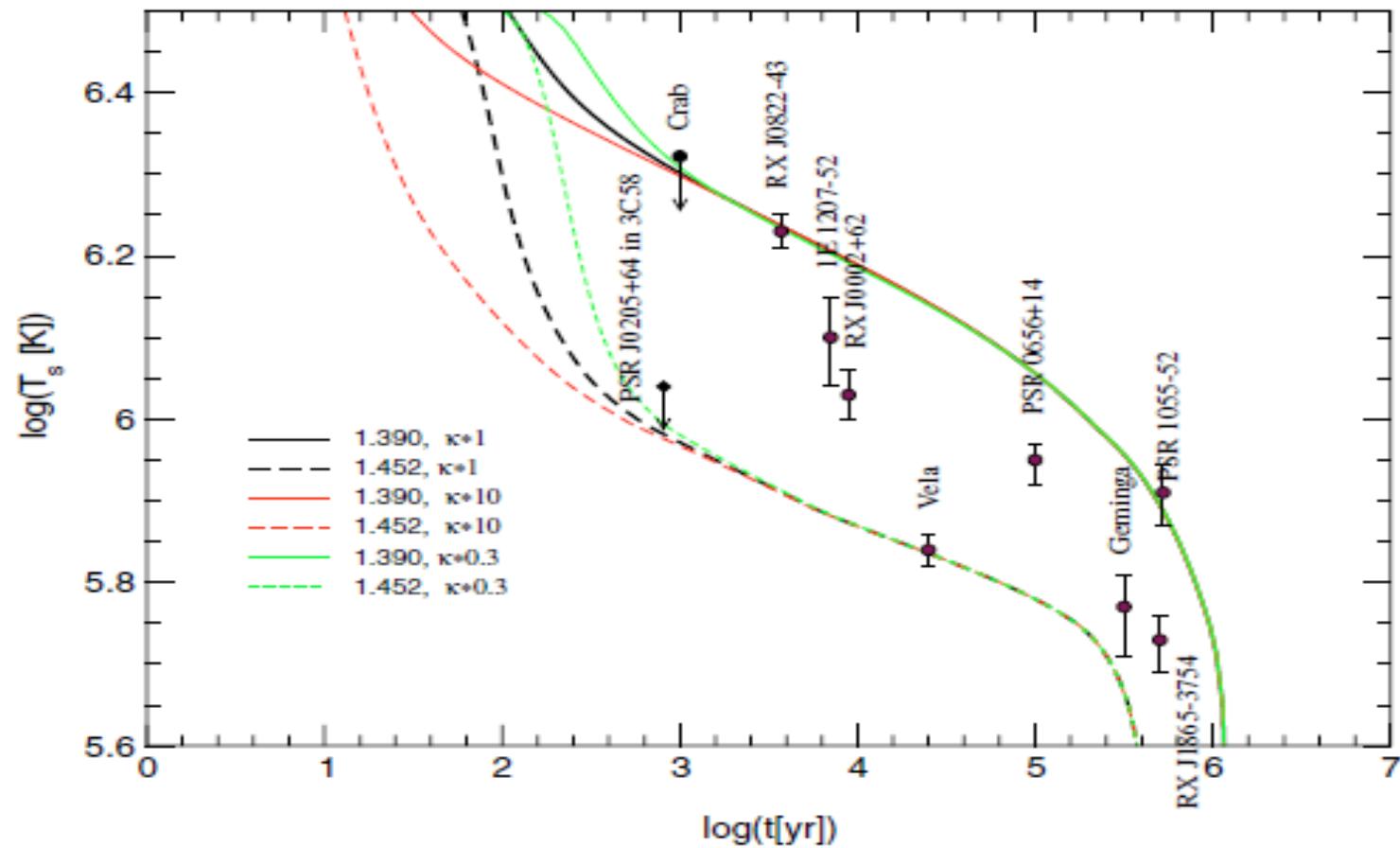
The gaps from Yakovlev et al. (2003)



# Contributions To Luminosities



# The Influence of A Change Of The Heat Conductivity On The Scenario



Blaschke, Grigorian, Voskresensky, A& A 424, 979 (2004)

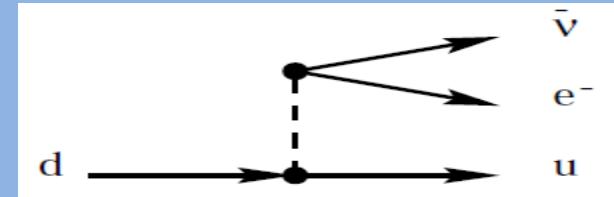
# Neutrino emissivities in quark matter:

- Quark direct Urca (QDU) the most efficient processes

$$d \rightarrow u + e + \bar{\nu} \text{ and } u + e \rightarrow d + \nu$$

$$\epsilon_{\nu}^{\text{QDU}} \simeq 9.4 \times 10^{26} \alpha_s u Y_e^{1/3} \zeta_{\text{QDU}} T_9^6 \text{ erg cm}^{-3} \text{ s}^{-1},$$

Compression n/no  $\simeq 2$ , strong coupling  $\alpha_s \approx 1$



- Quark Modified Urca (QMU) and Quark Bremsstrahlung

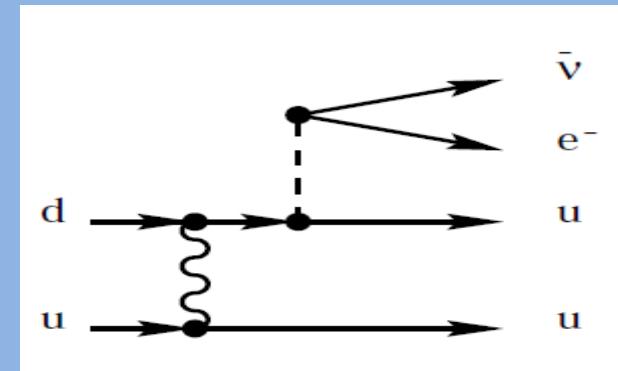
$$d + q \rightarrow u + q + e + \bar{\nu} \text{ and } q_1 + q_2 \rightarrow q_1 + q_2 + \nu + \bar{\nu}$$

$$\epsilon_{\nu}^{\text{QMU}} \sim \epsilon_{\nu}^{\text{QB}} \simeq 9.0 \times 10^{19} \zeta_{\text{QMU}} T_9^8 \text{ erg cm}^{-3} \text{ s}^{-1}.$$

- Suppression due to the pairing

**QDU**:  $\zeta_{\text{QDU}} \sim \exp(-\Delta_q/T)$

**QMU and QB**:  $\zeta_{\text{QMU}} \sim \exp(-2\Delta_q/T)$  for  $T < T_{\text{crit},q} \simeq 0.57 \Delta_q$



- Enhanced cooling due to the pairing

- $e + e \rightarrow e + e + \nu + \bar{\nu}$  (becomes important for  $\Delta_q/T \gg 1$ )

$$\epsilon_{\nu}^{ee} = 2.8 \times 10^{12} Y_e^{1/3} u^{1/3} T_9^8 \text{ erg cm}^{-3} \text{ s}^{-1},$$

Quark PBF

# Crust Model

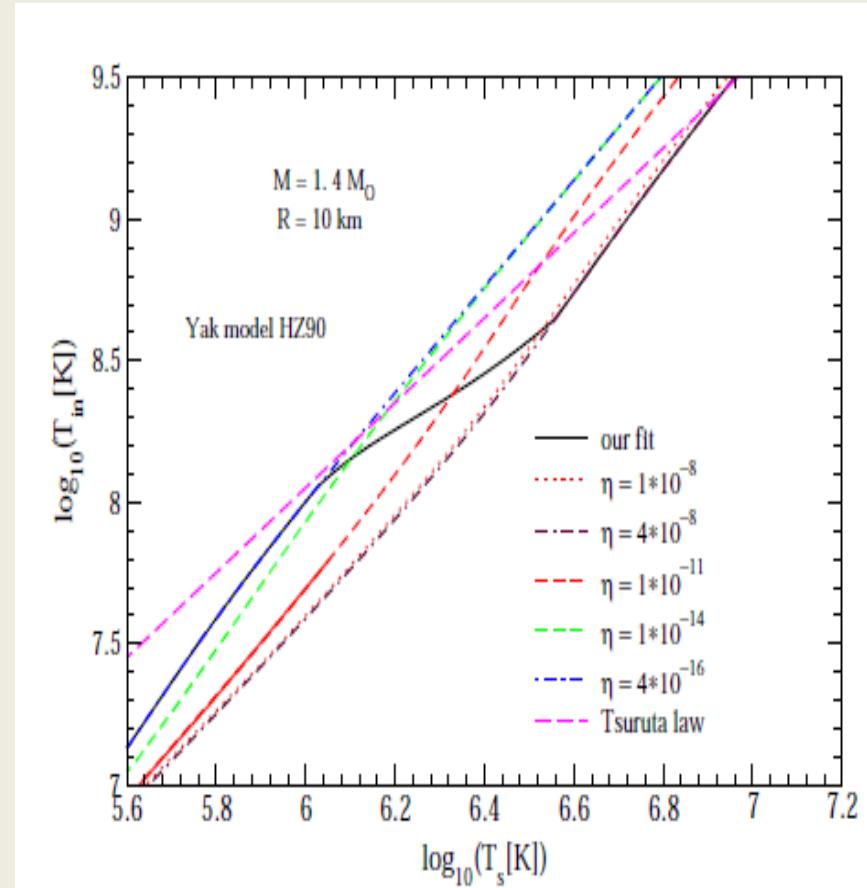
Time dependence of the light element contents in the crust

$$\Delta M_L(t) = e^{-t/\tau} \Delta M_L(0)$$

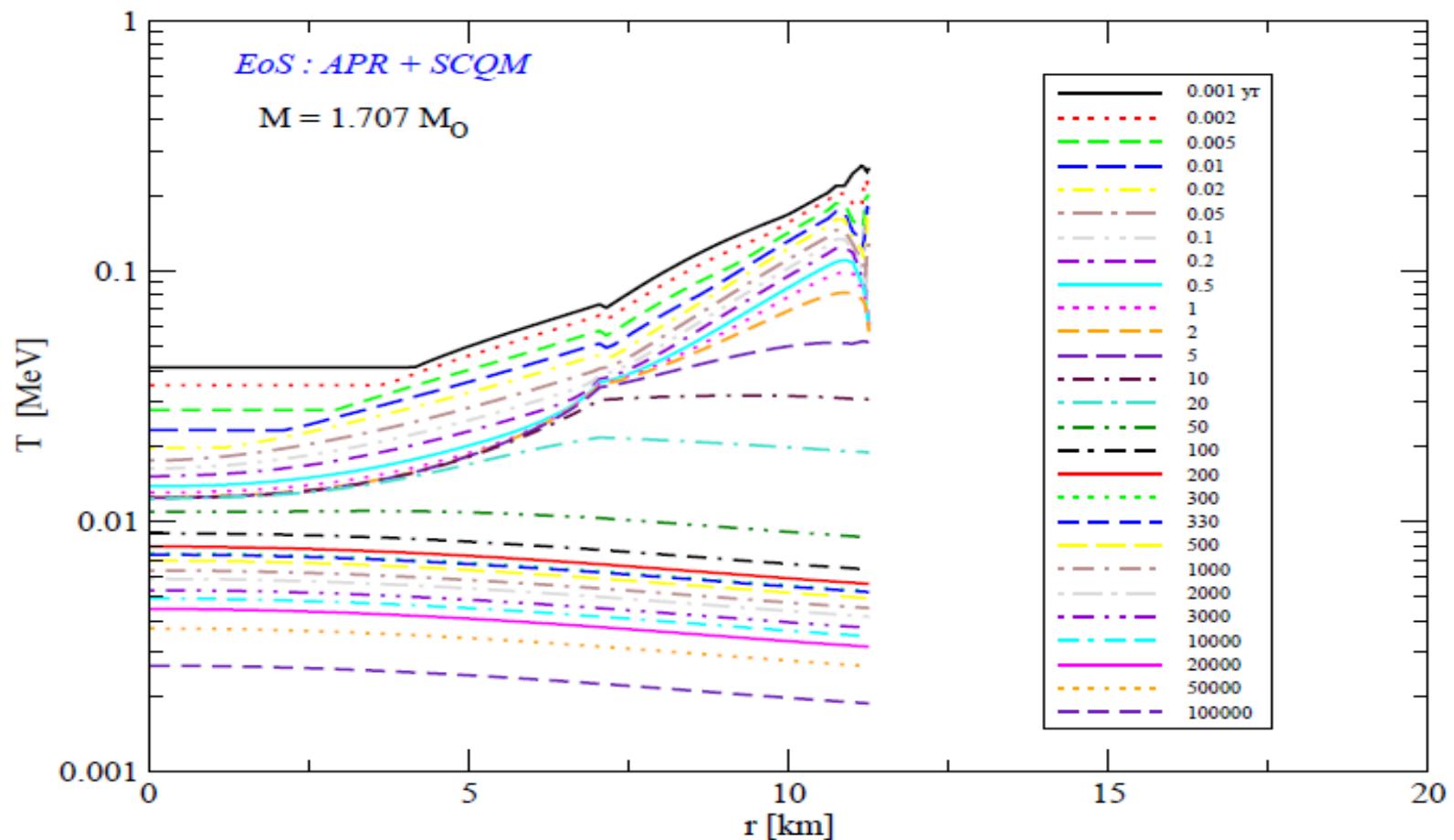
Blaschke, Grigorian, Voskresensky,  
A&A 368 (2001) 561.

Page, Lattimer, Prakash & Steiner,  
Astrophys.J. 155, 623 (2004)

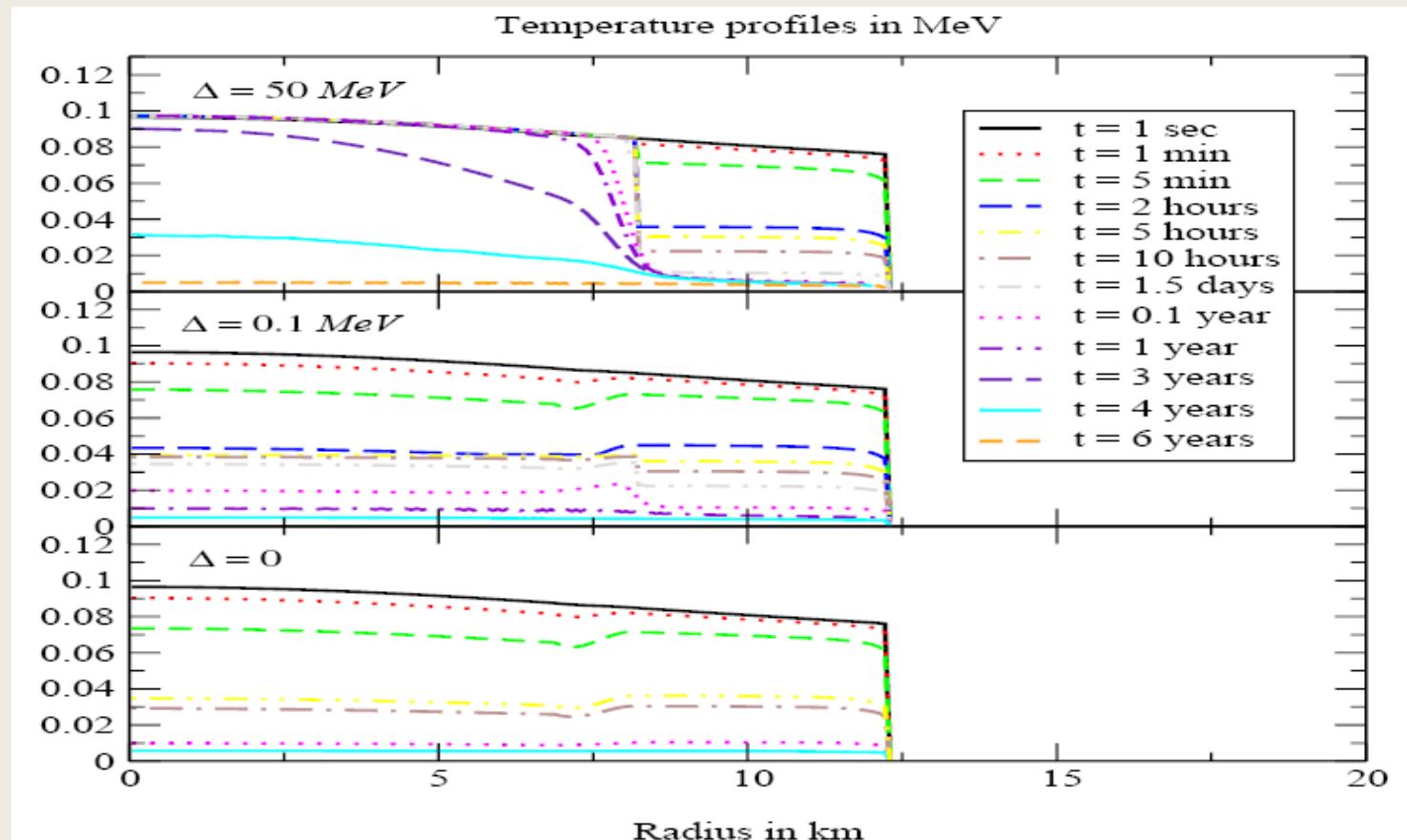
Yakovlev, Levenfish, Potekhin,  
Gnedin & Chabrier, Astron. Astrophys  
, 417, 169 (2004)



# Temperature In The Hybrid Star Interior

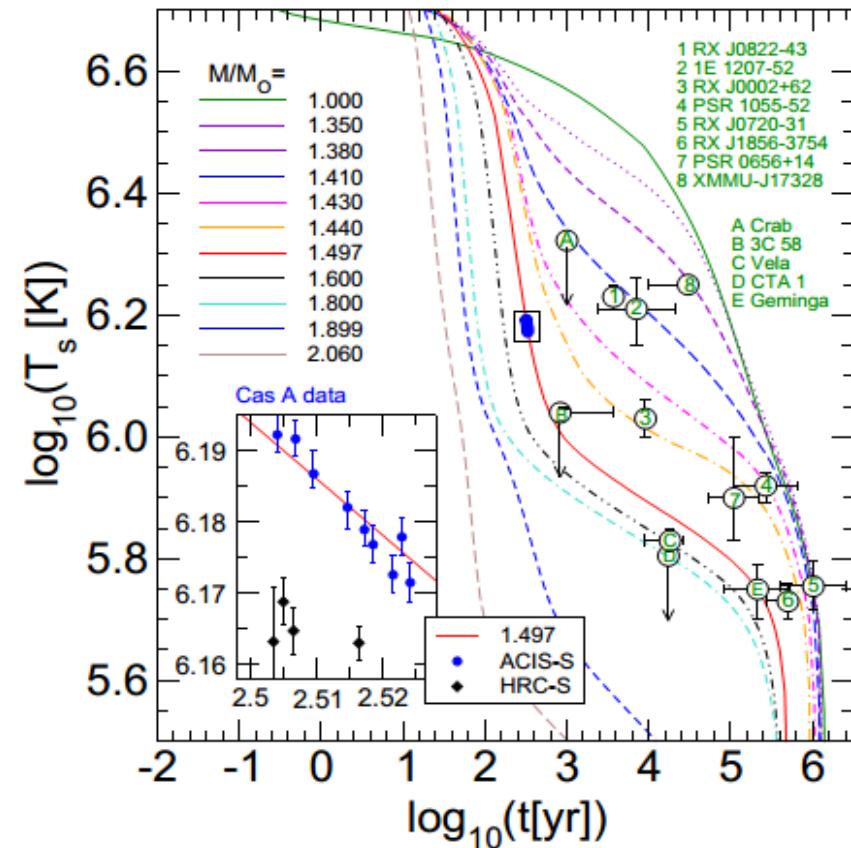
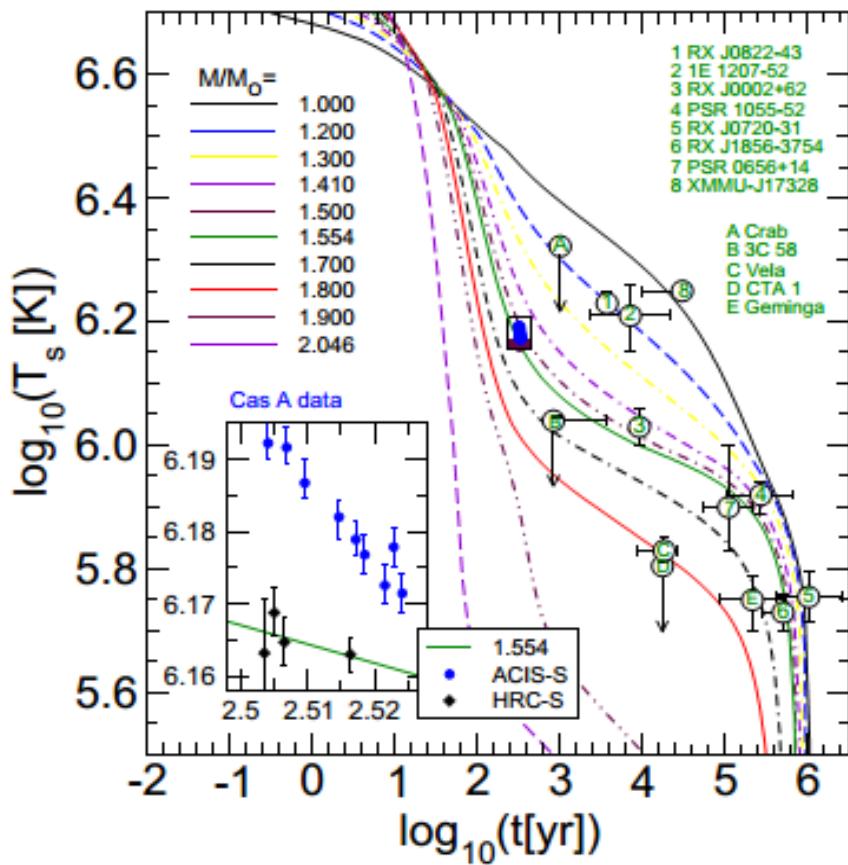


# Temperature In The Hybrid Star Interior



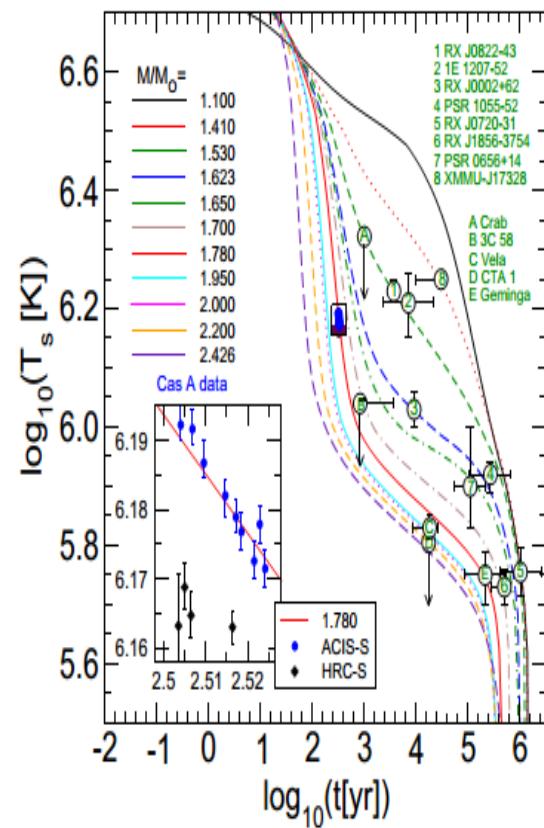
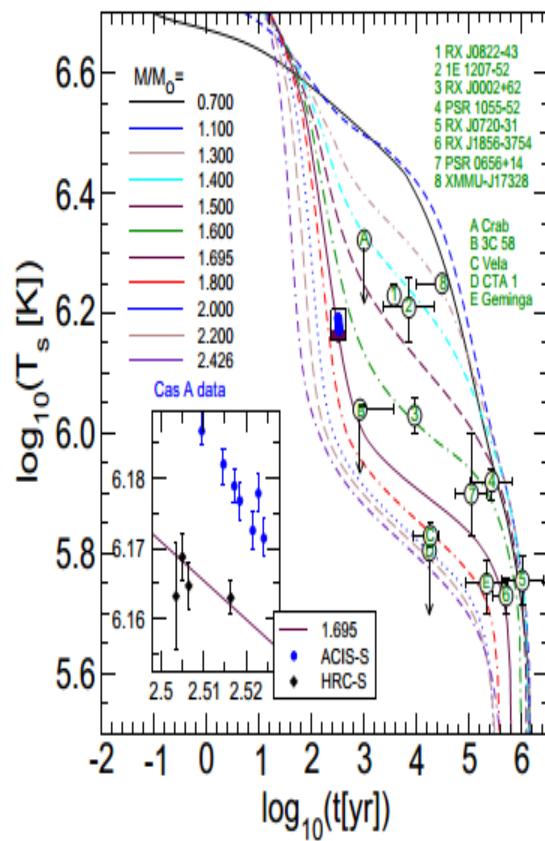
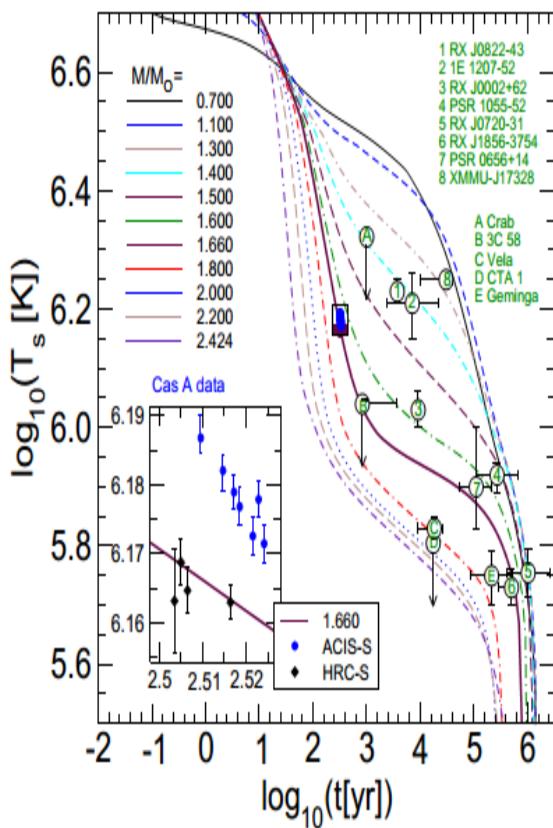
# HDD - AV18 , Yak.

## ME nc = 3 n0

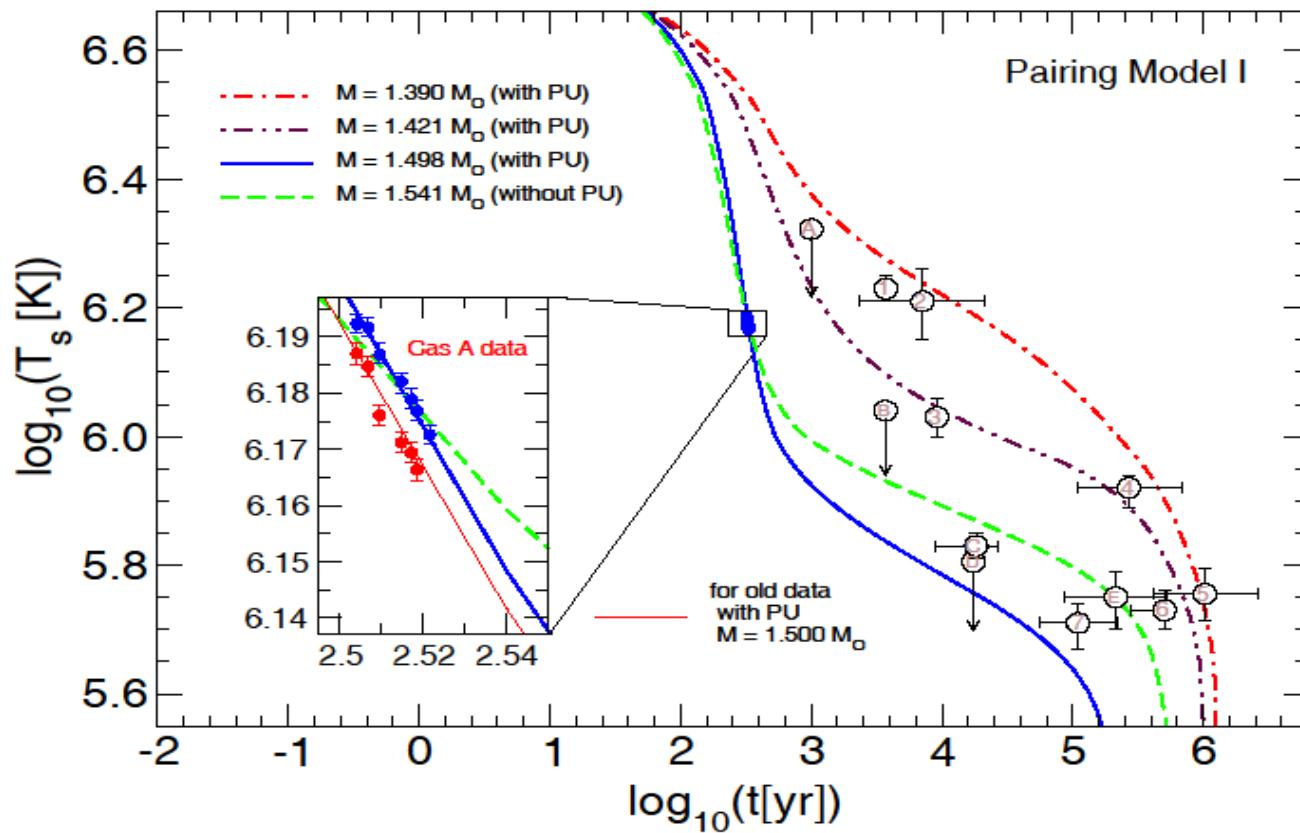


# DD2 - EEHOr

## ME-nc=1.5, 2.0, 2.5n0

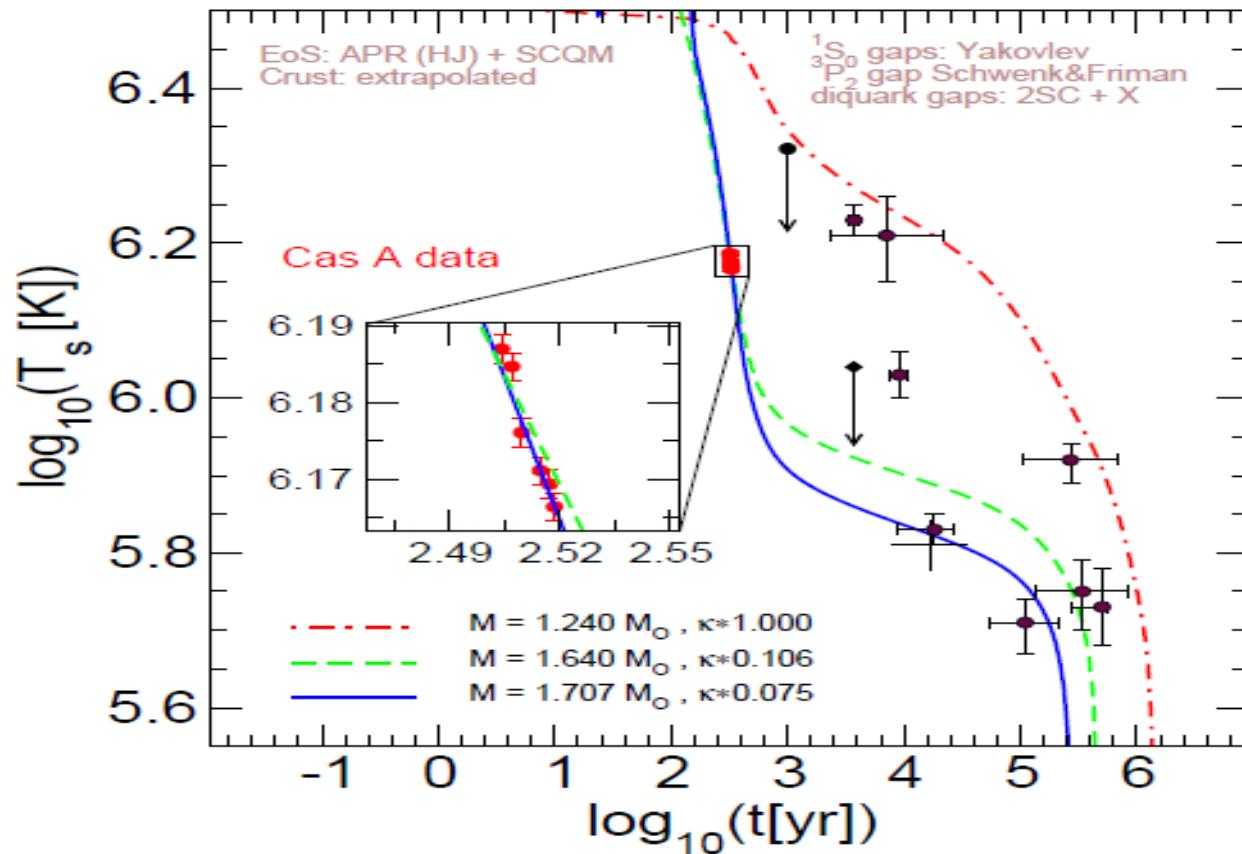


# Cas A as an Hadronic Star

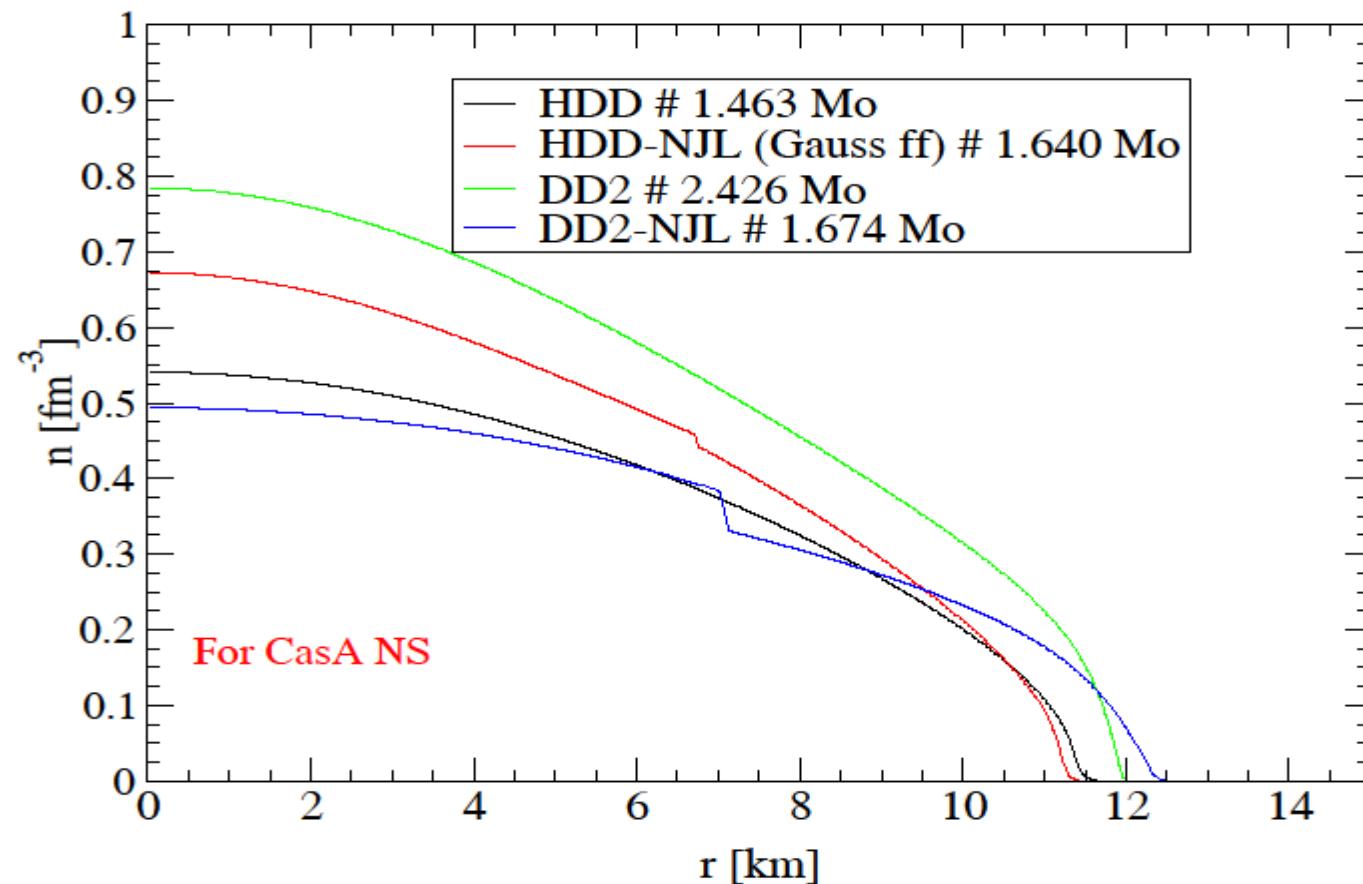


# Cas A As An Hybrid Star

H. Grigorian, D. Blaschke, D.N. Voskresensky, Phys. Rev. C 71, 045801 (2005)



# Possible internal structure of CasA



# MKVOR – EoS model

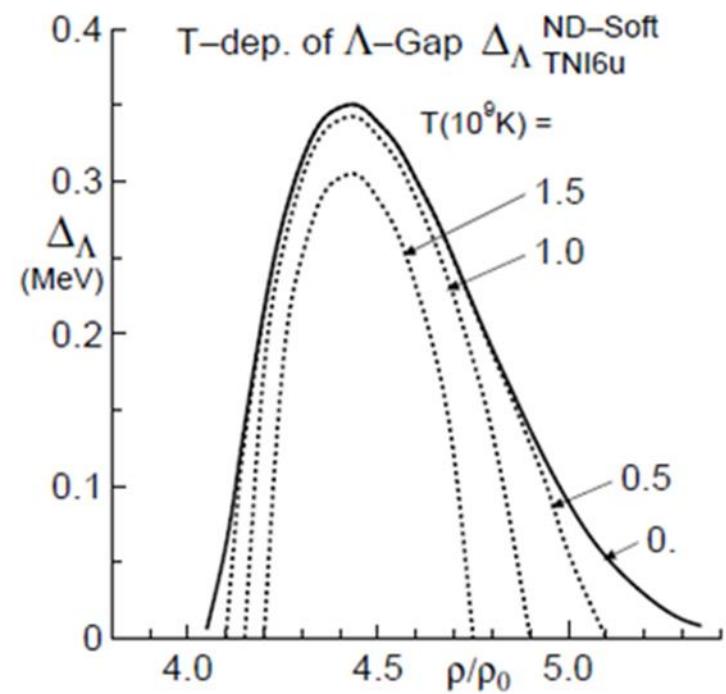
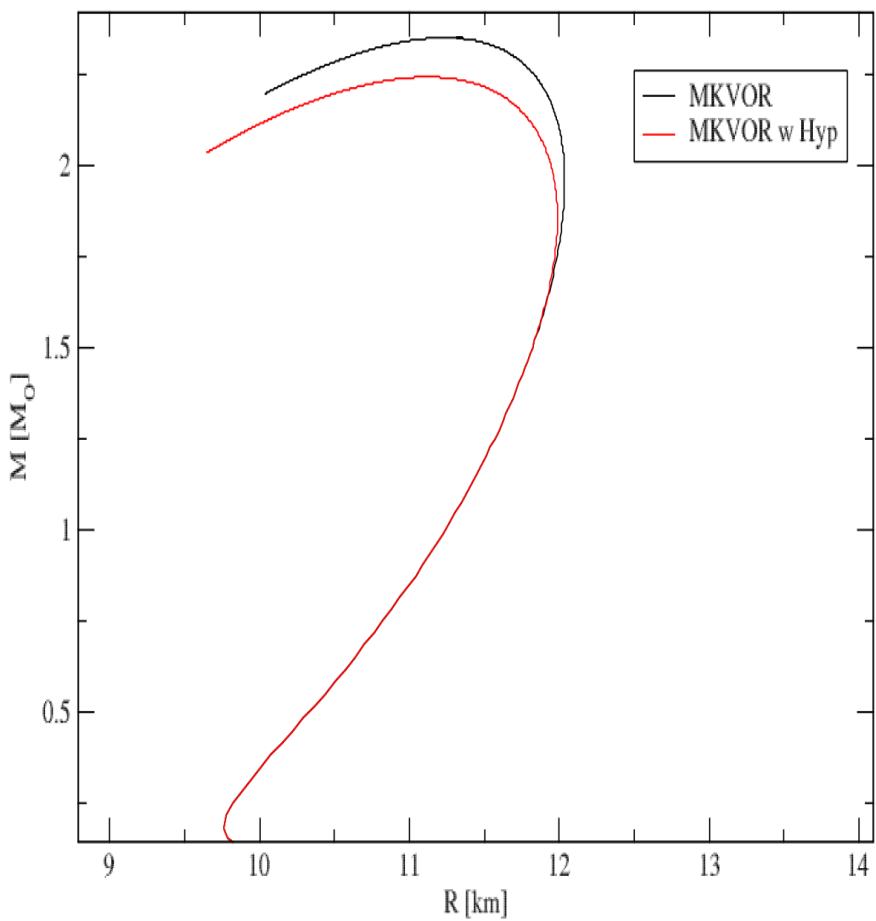
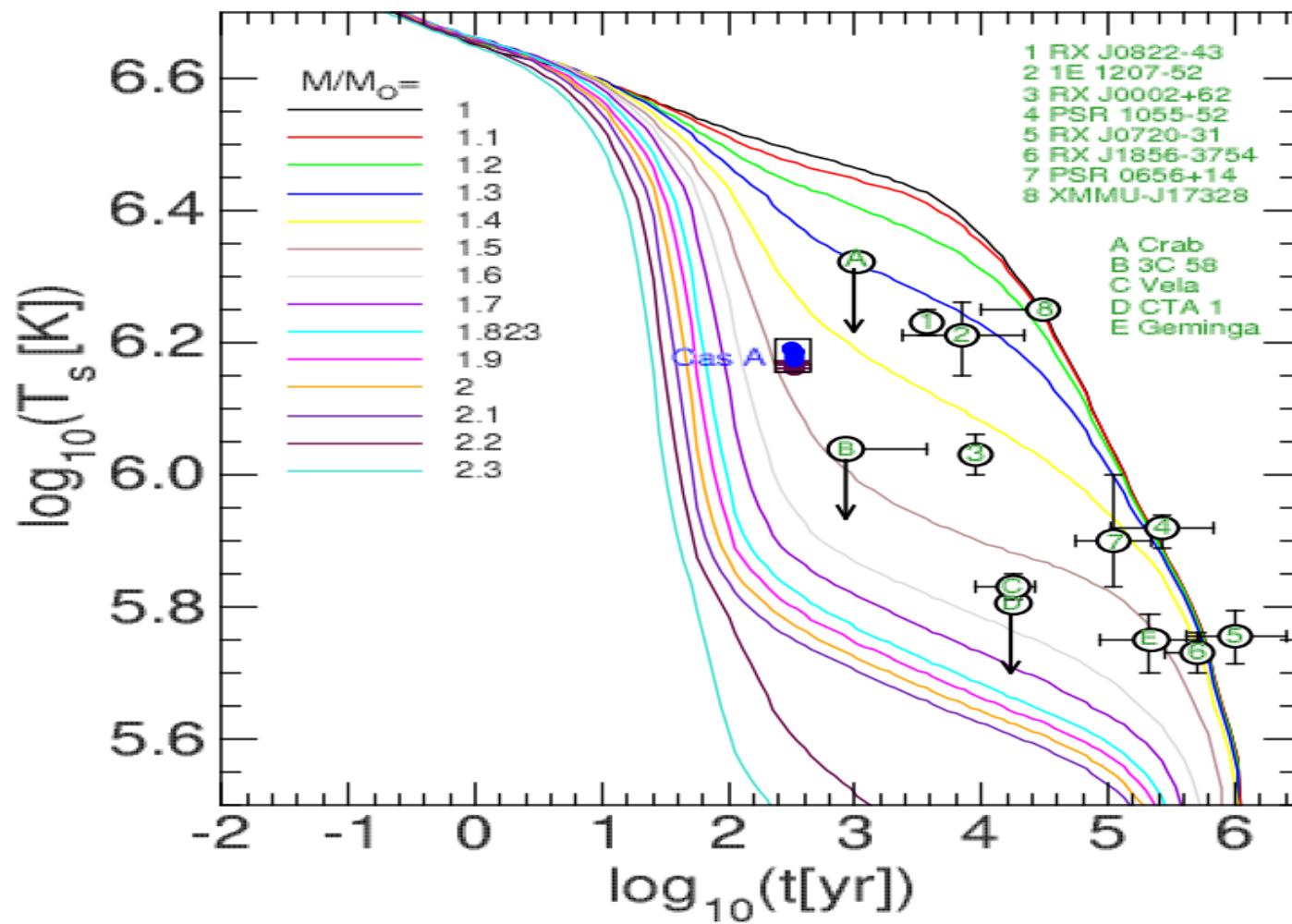


Fig. 8. Temperature( $T$ ) dependence of  $\Lambda$  energy gap ( $\Delta_\Lambda$ ) for the case of TNI6u EOS and ND-Soft potential, as an example.

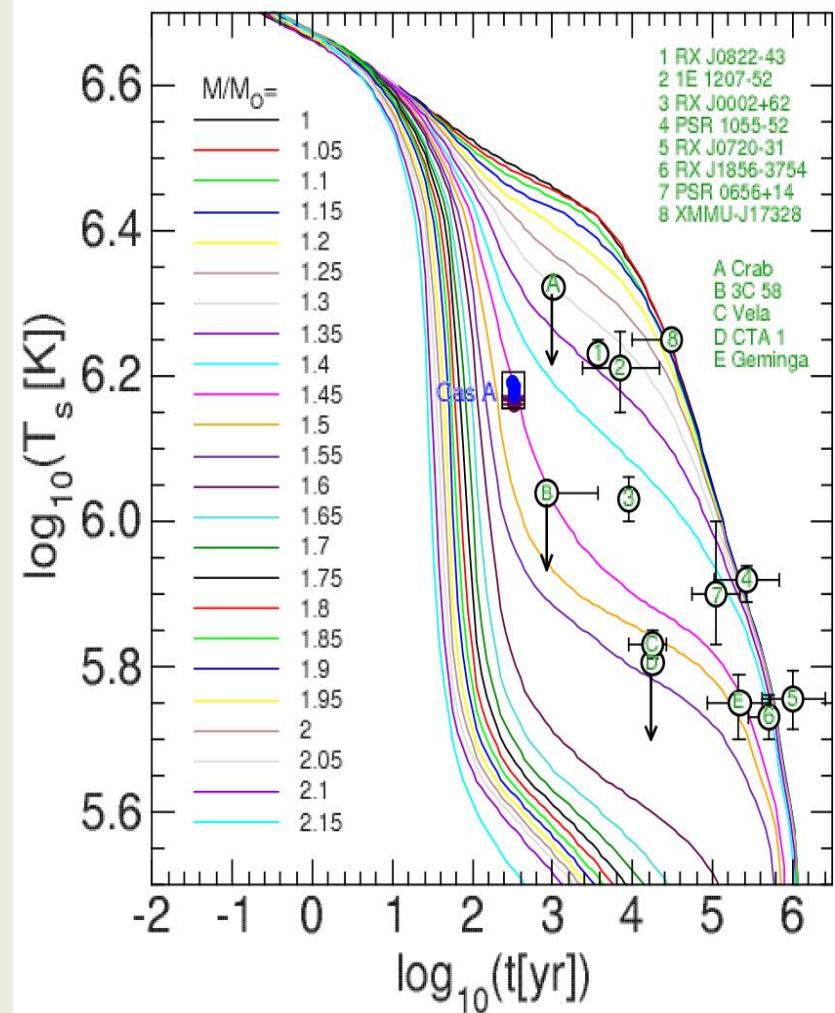
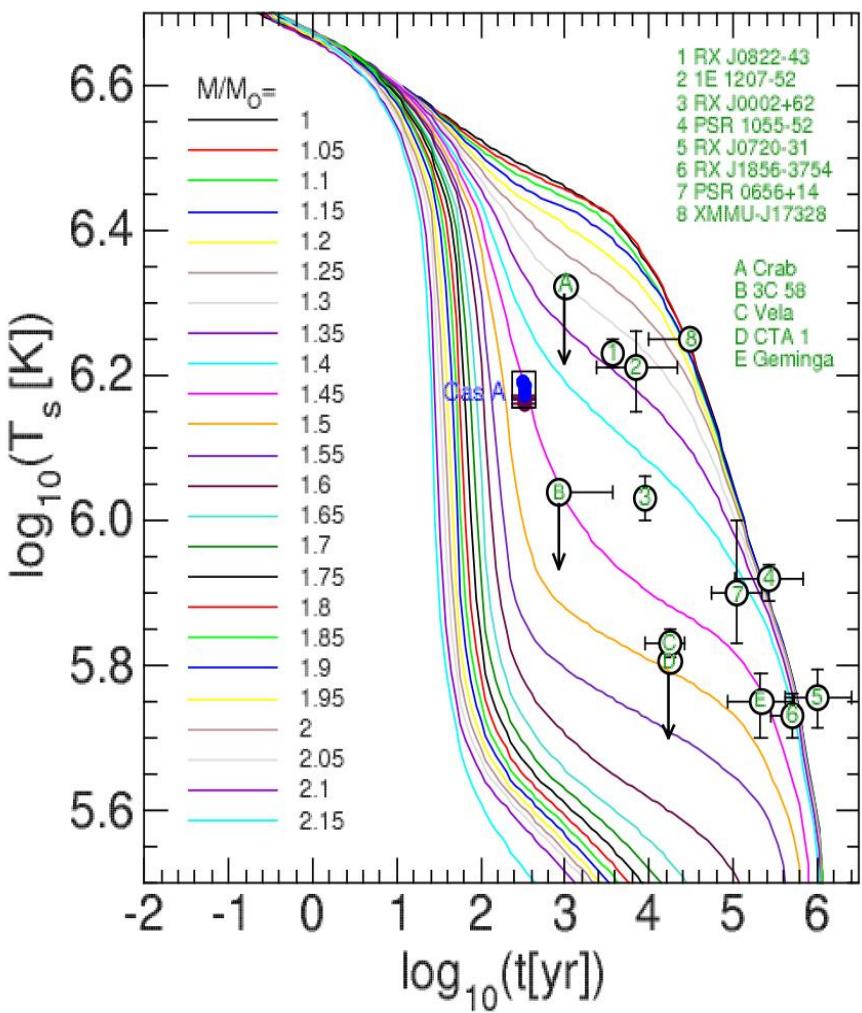
# MKVOR - EEHOr

ME-nc=3.0n0

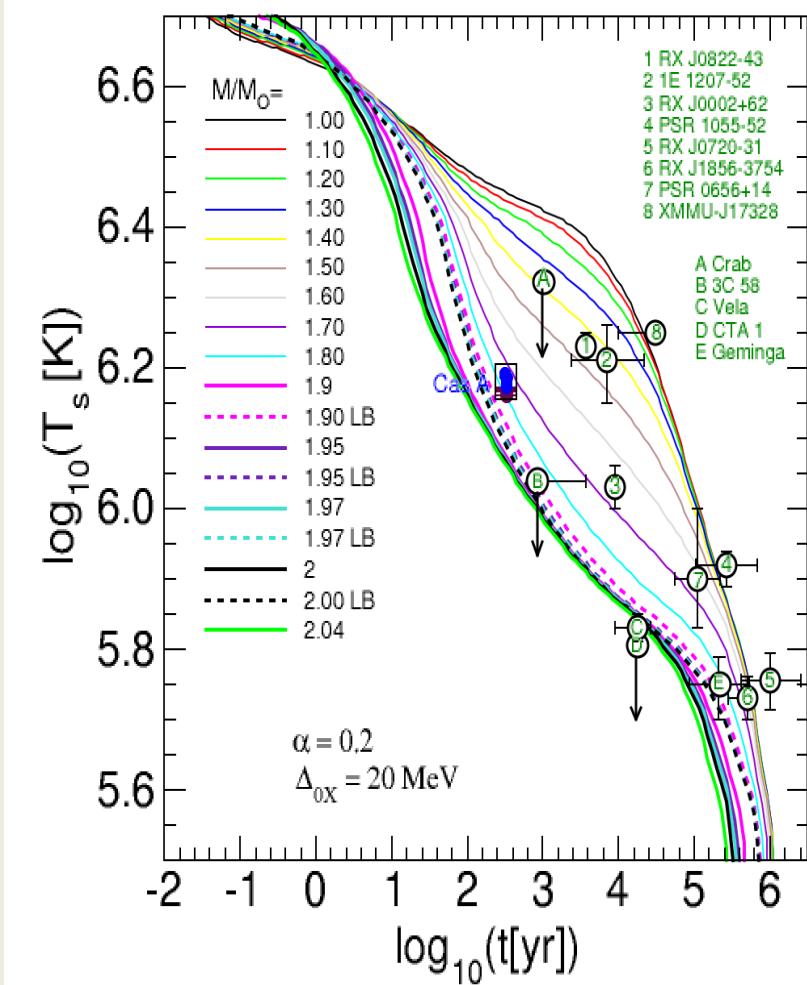
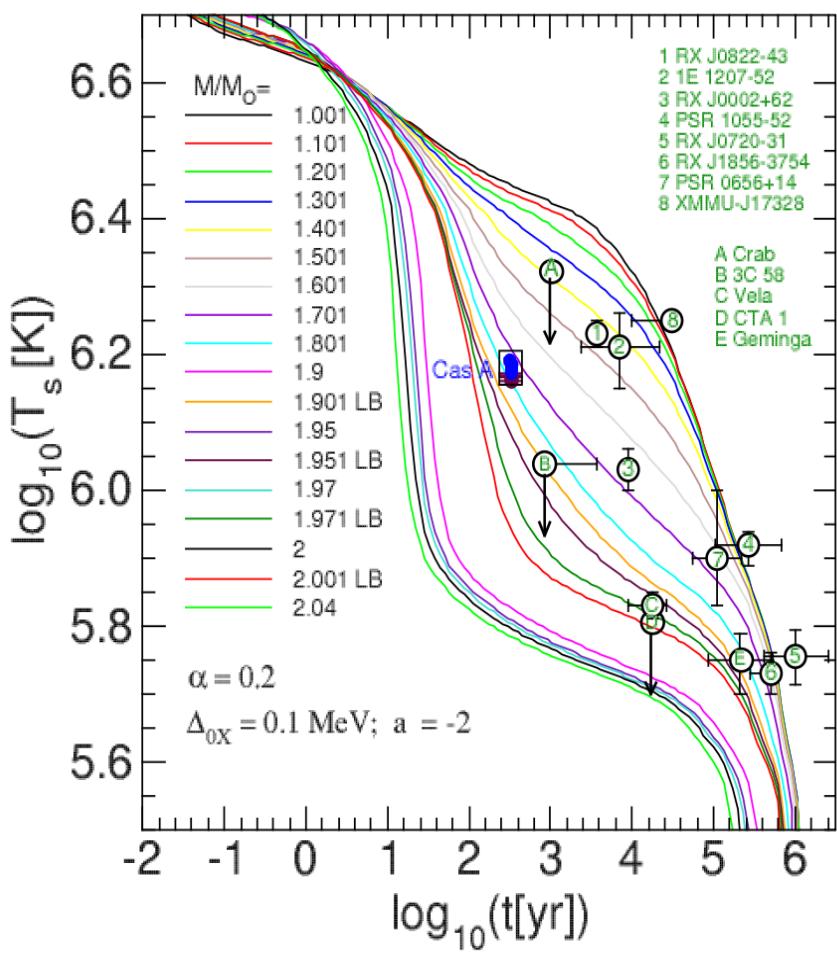


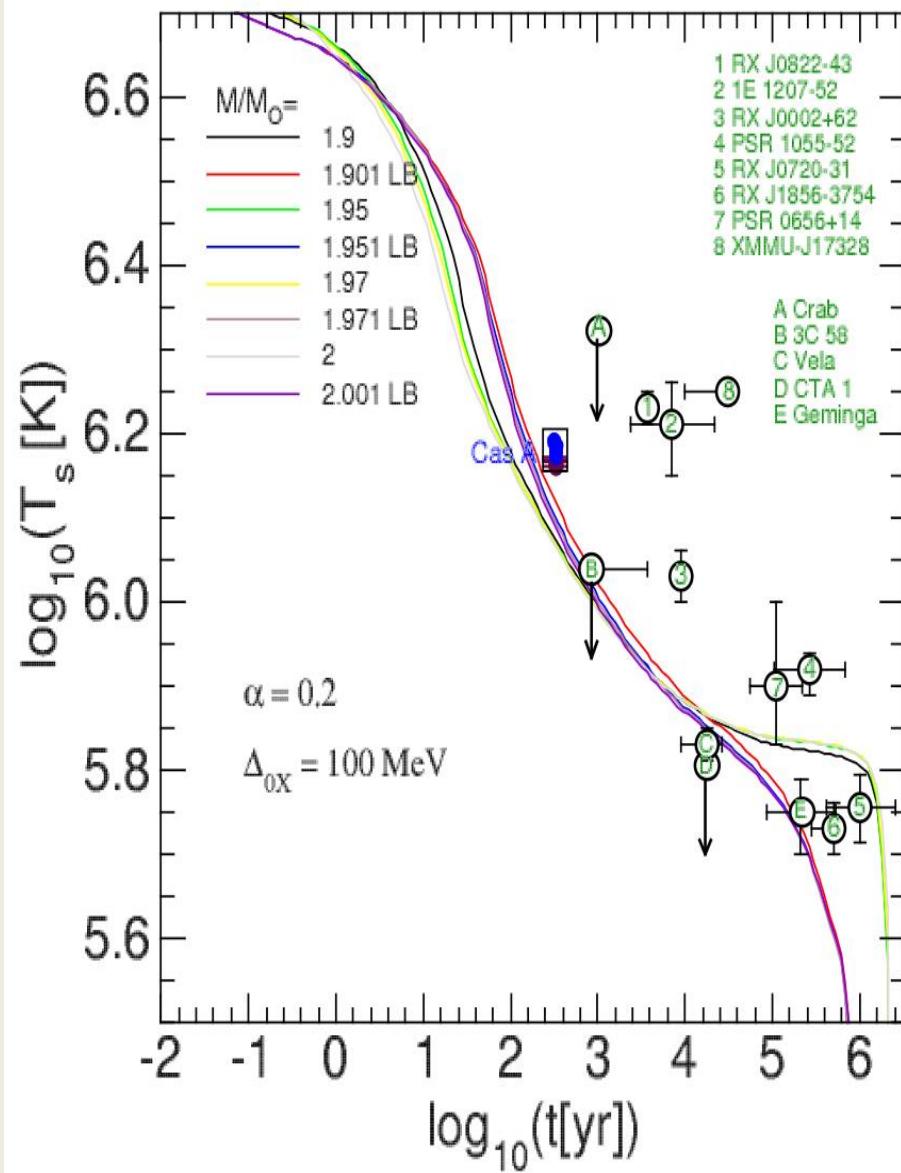
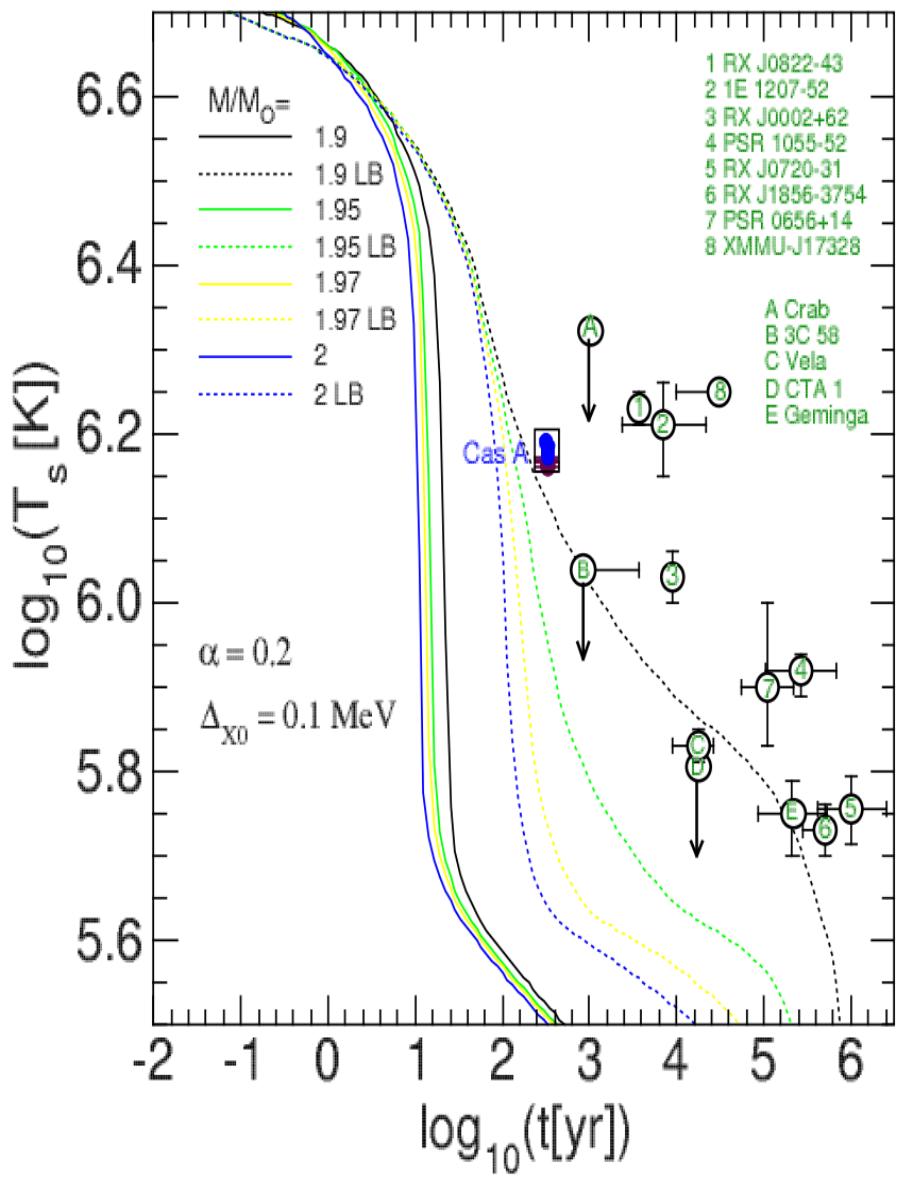
# MKVOR Hyp - EEHOr

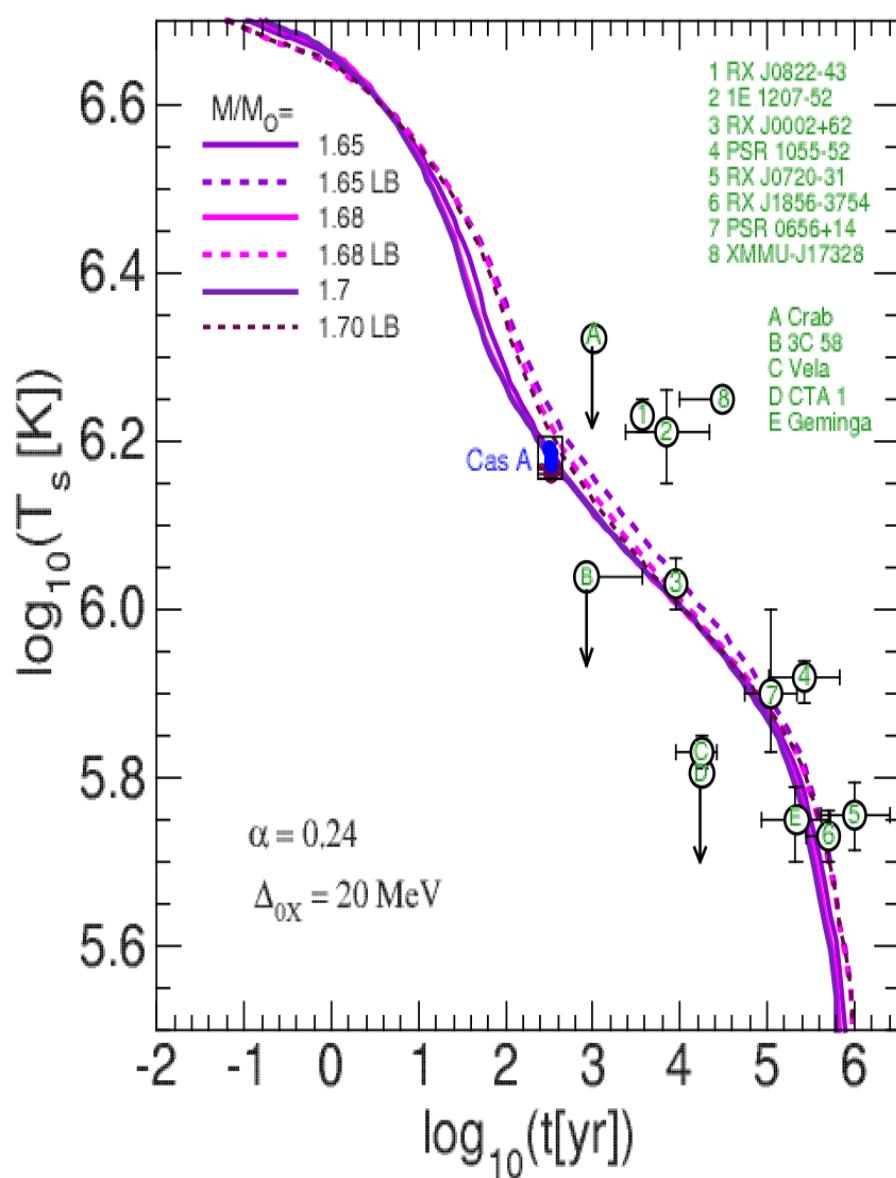
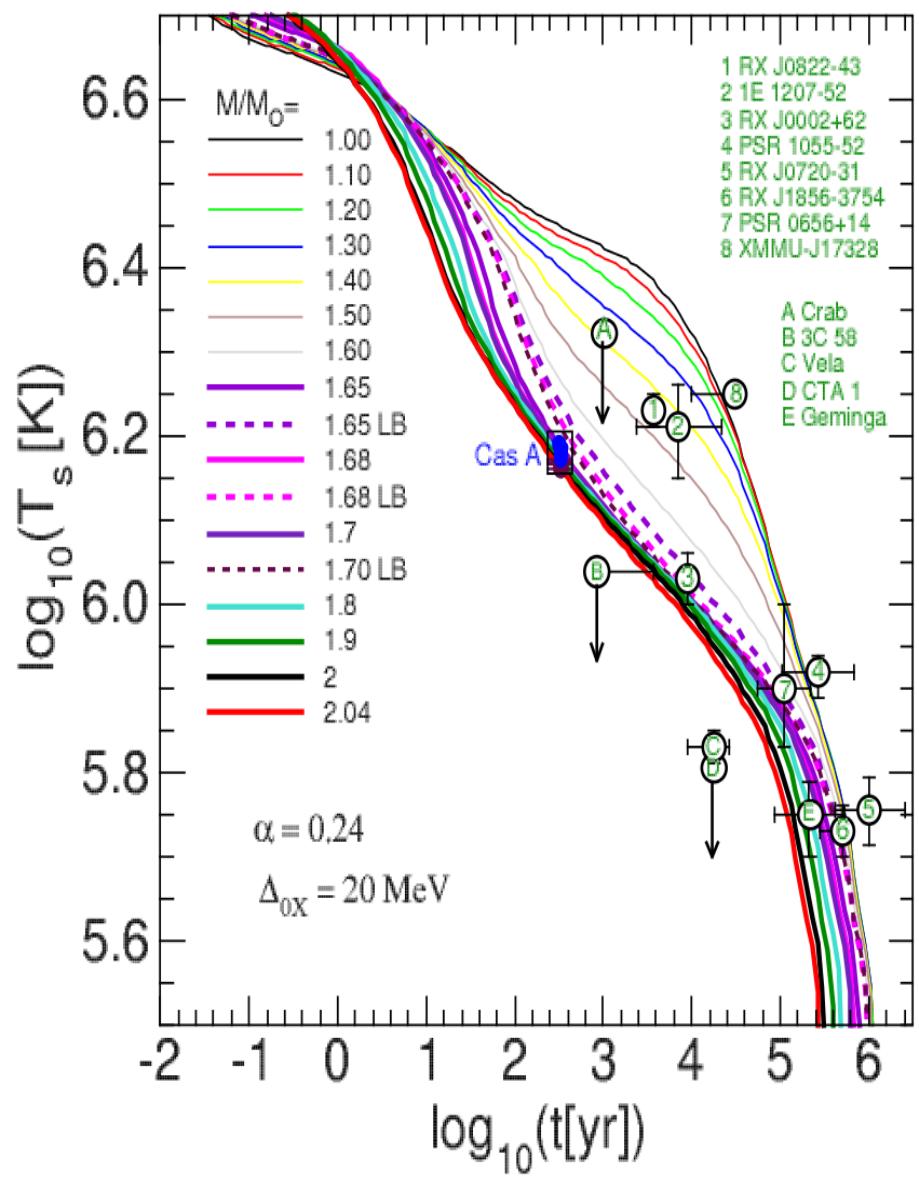
## ME-nc=3.0n0

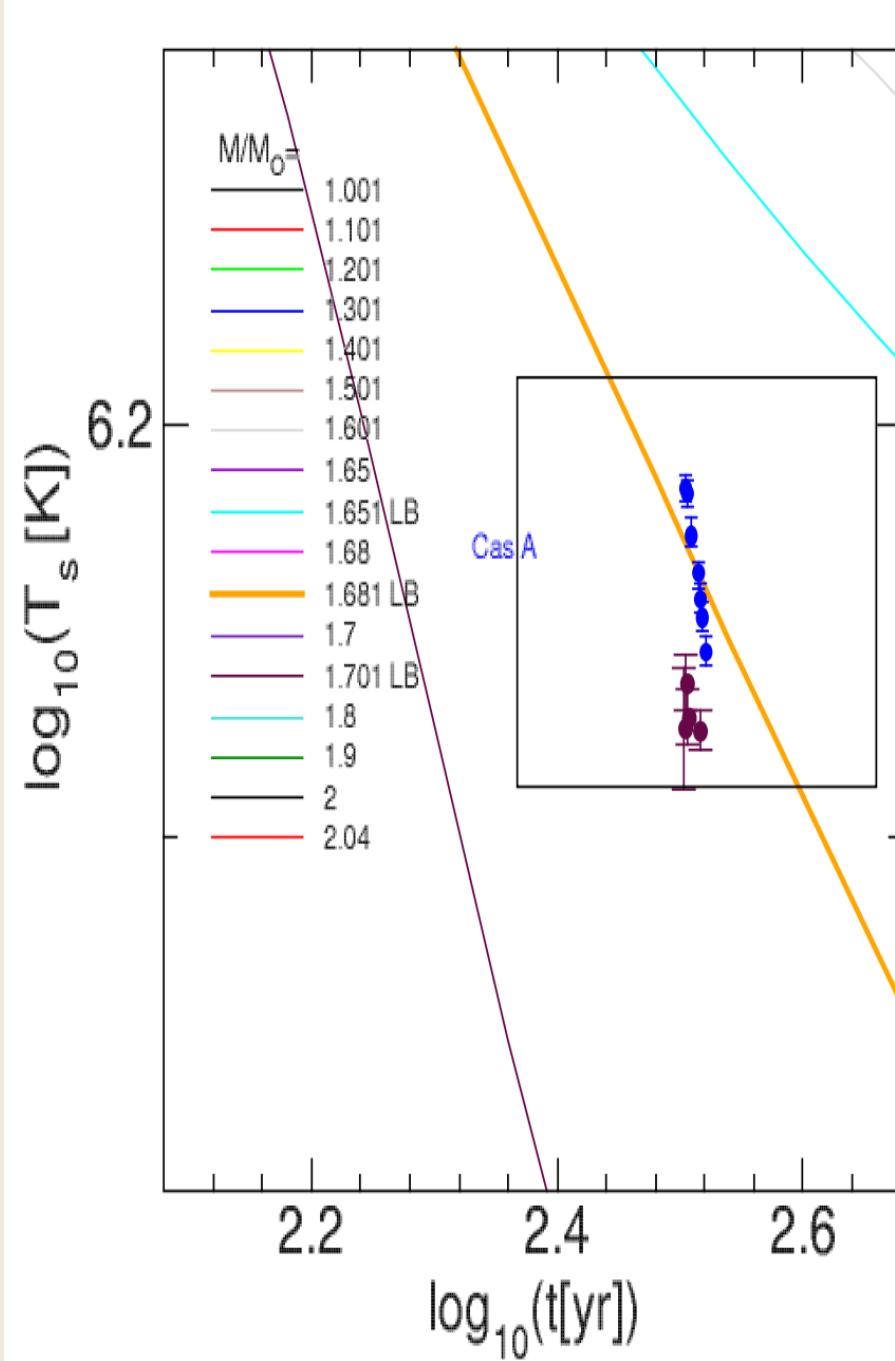
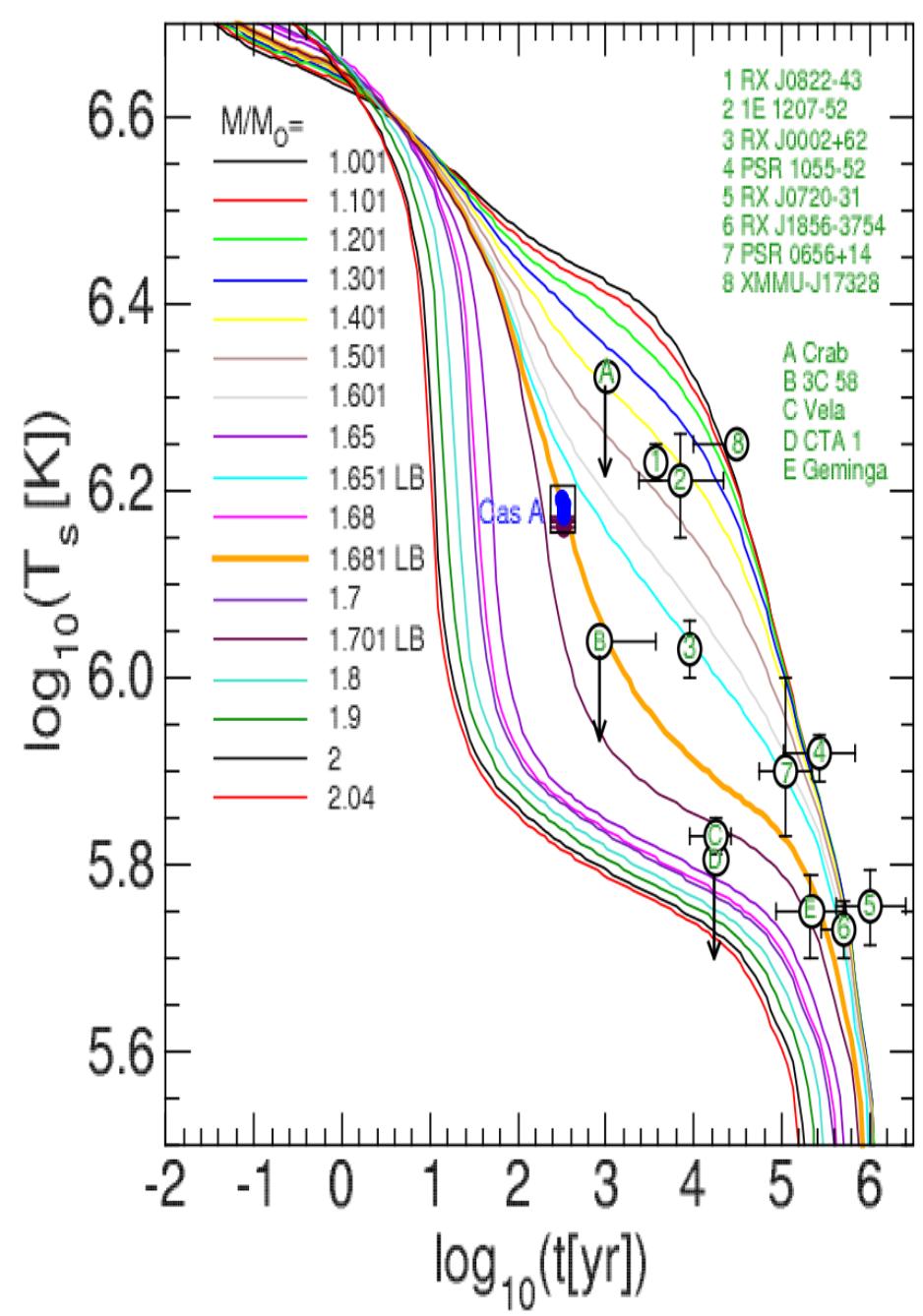


# Cooling of Twin CS







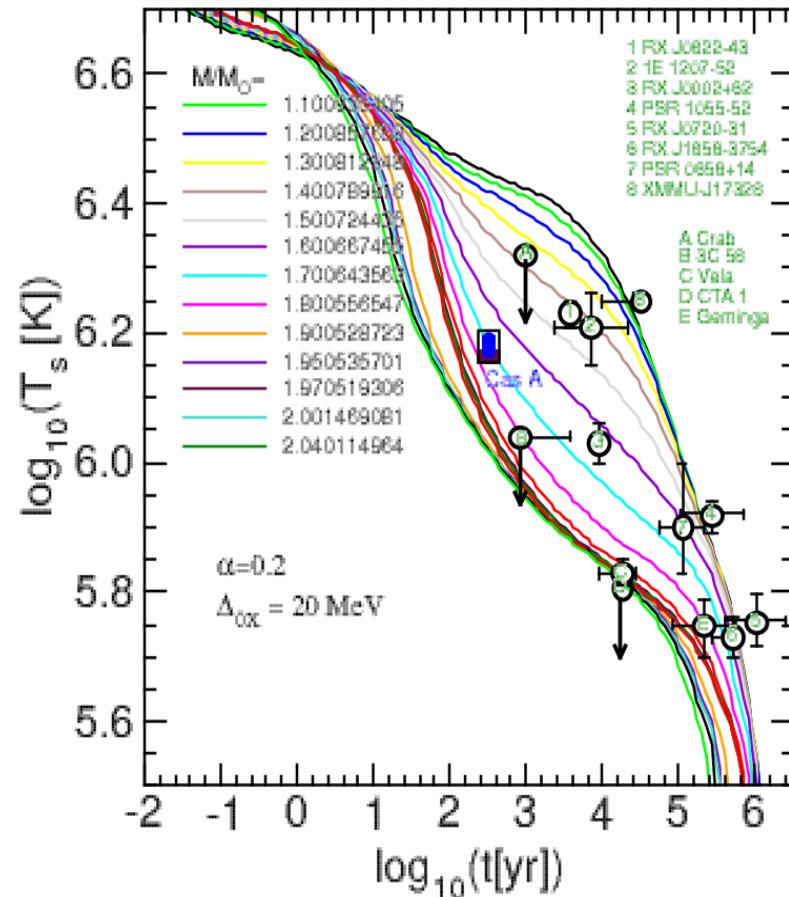
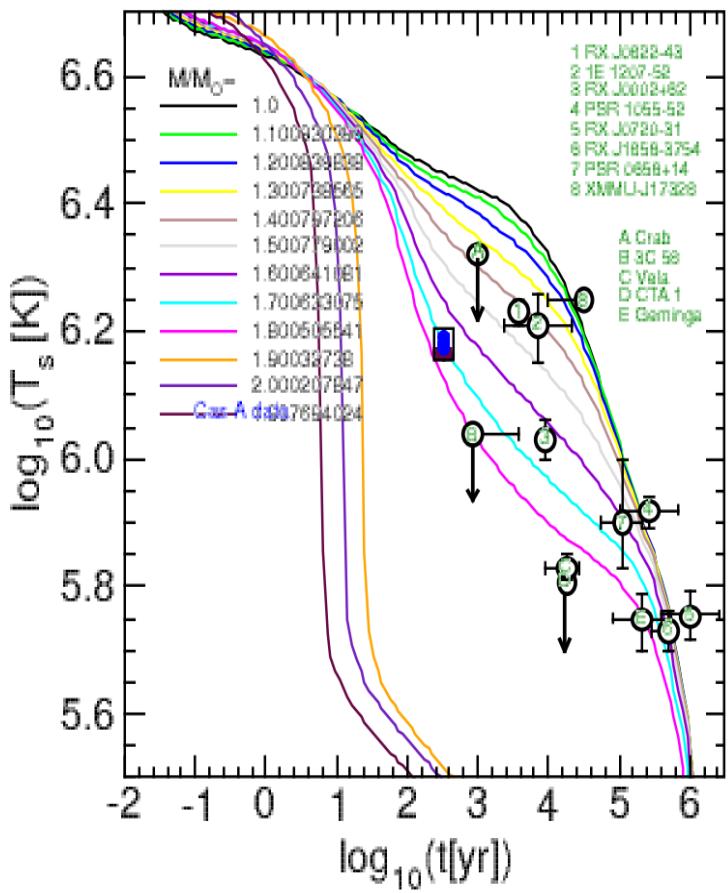


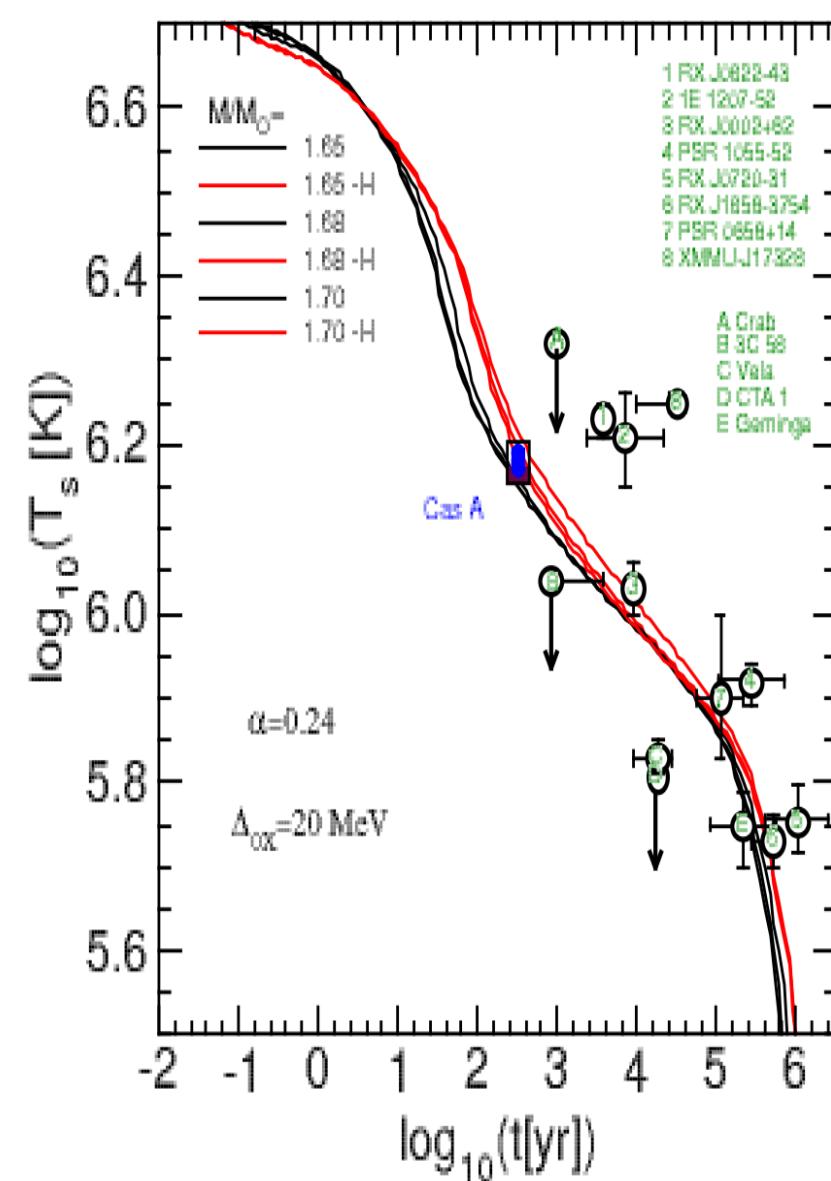
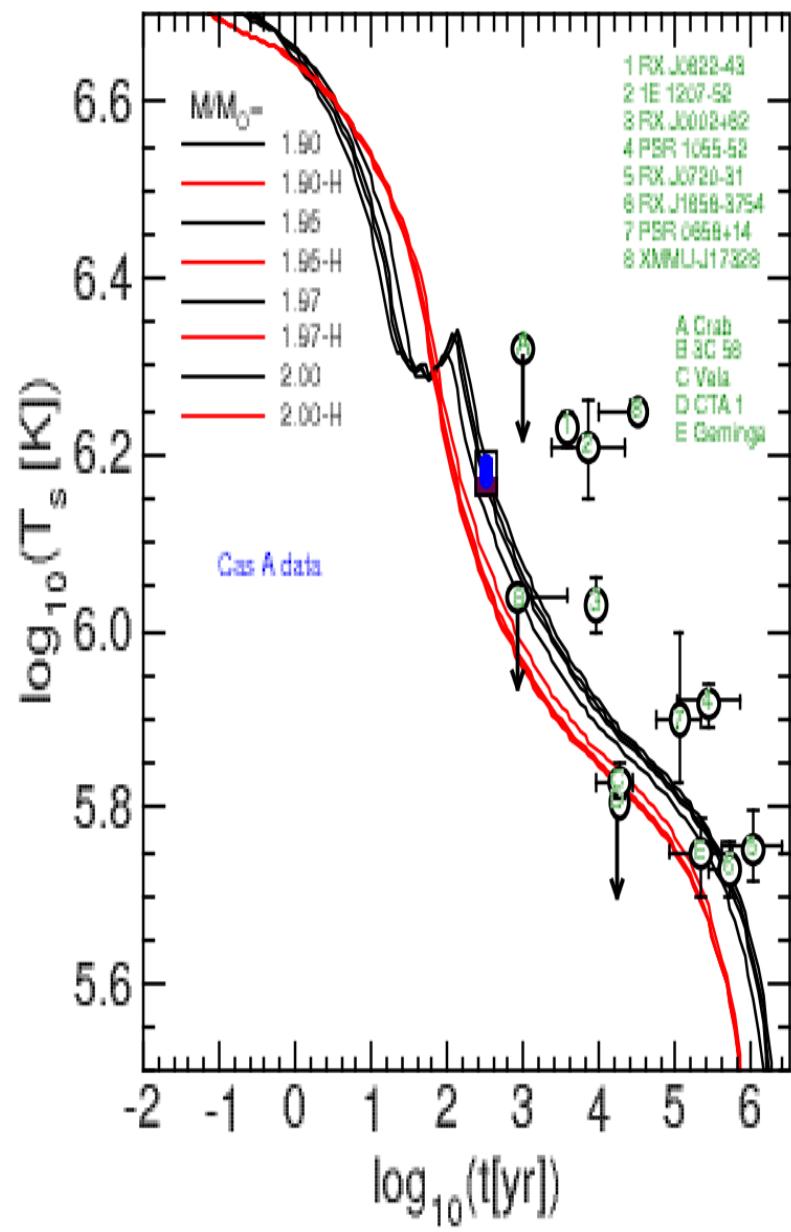
# Conclusions

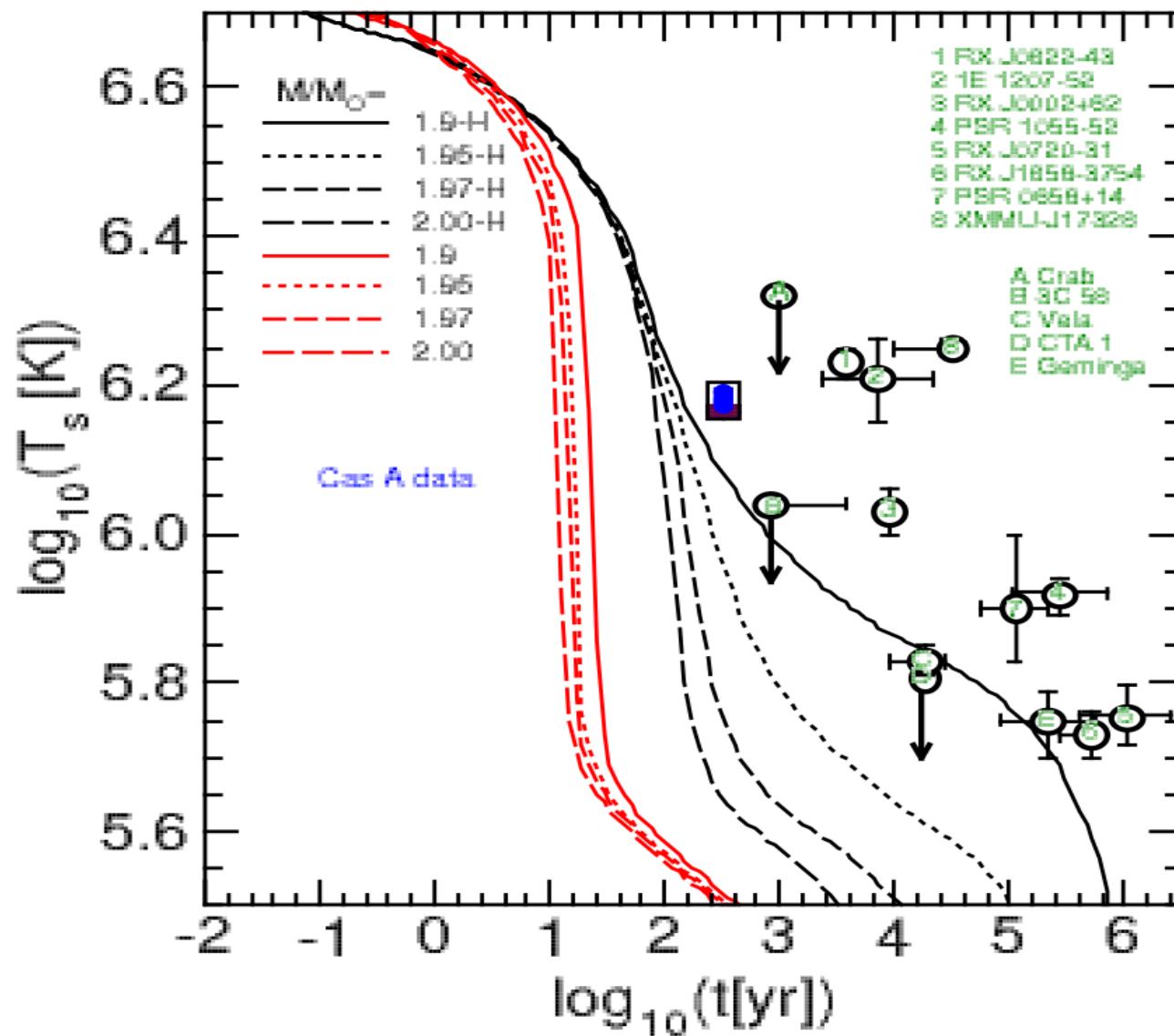
- All known cooling data including the Cas A rapid cooling consistently described by the ``nuclear medium cooling" scenario
- Influence of stiffness on EoS and cooling can be balanced by the choice of corresponding gap model.
- In case of existence of **III CSF** high-mass twin stars could show different cooling behavior depending on core superconductivity

Thank YOU!!!!

# Cooling of Twin CS

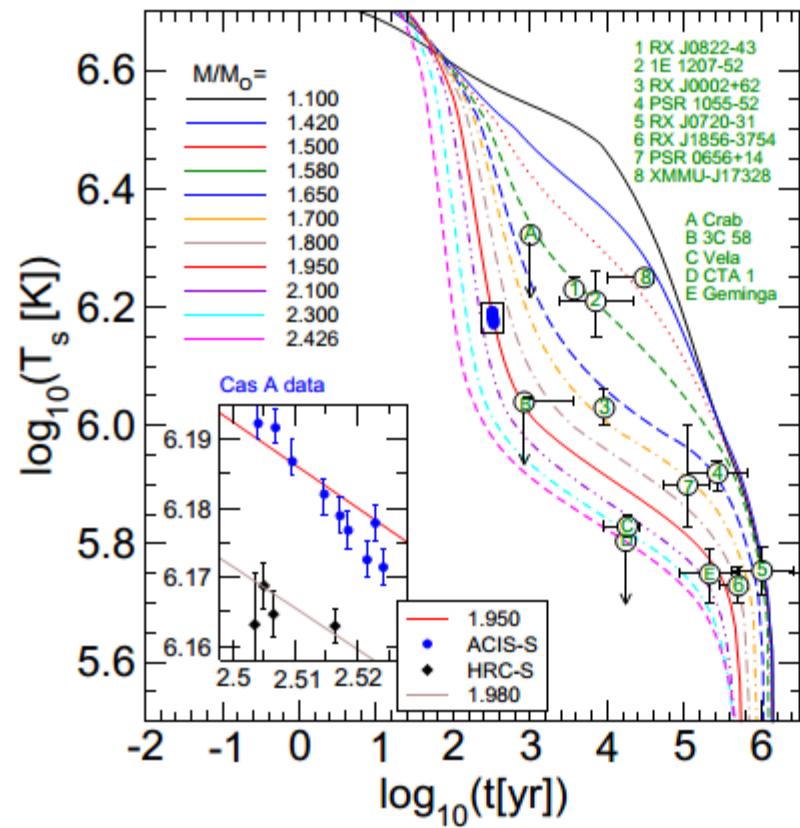
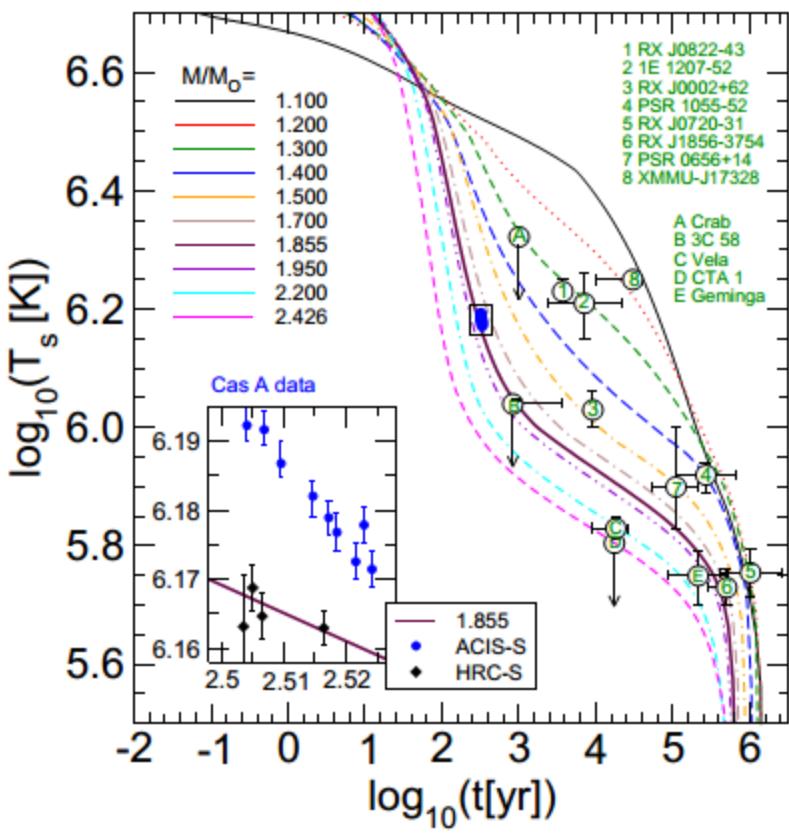






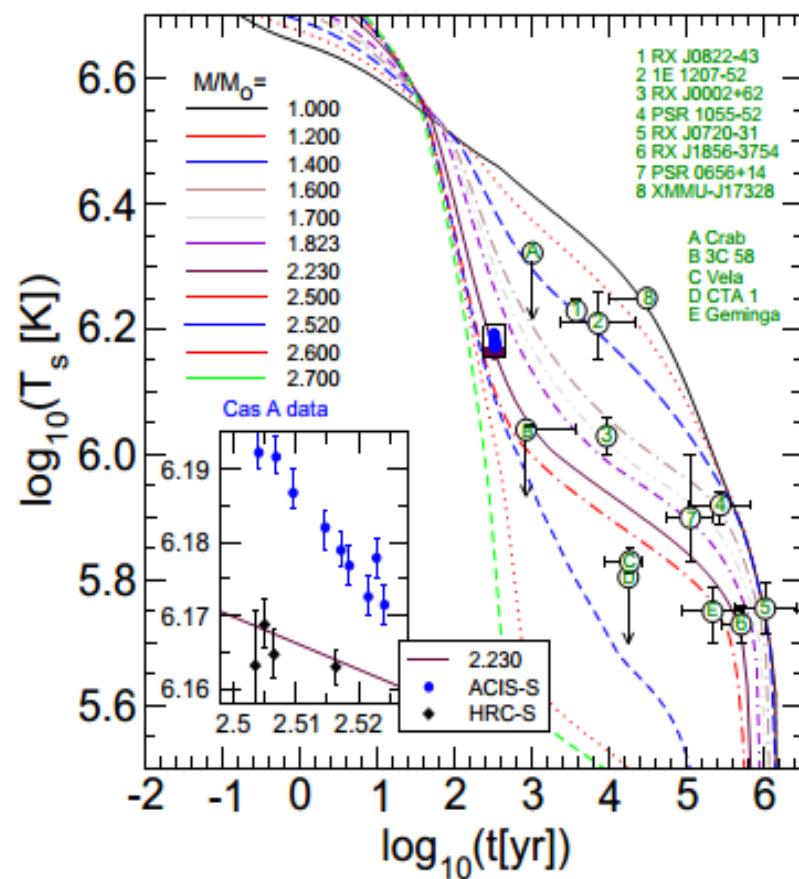
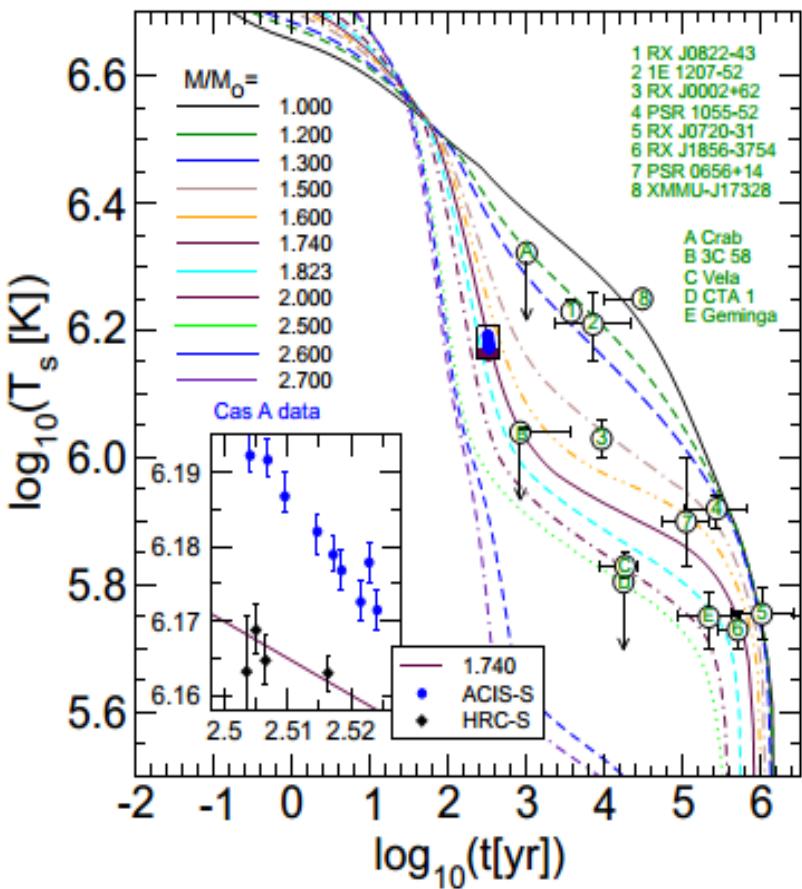
# DD2- ME-nc = 3 n0

## BCLL, EEHOr

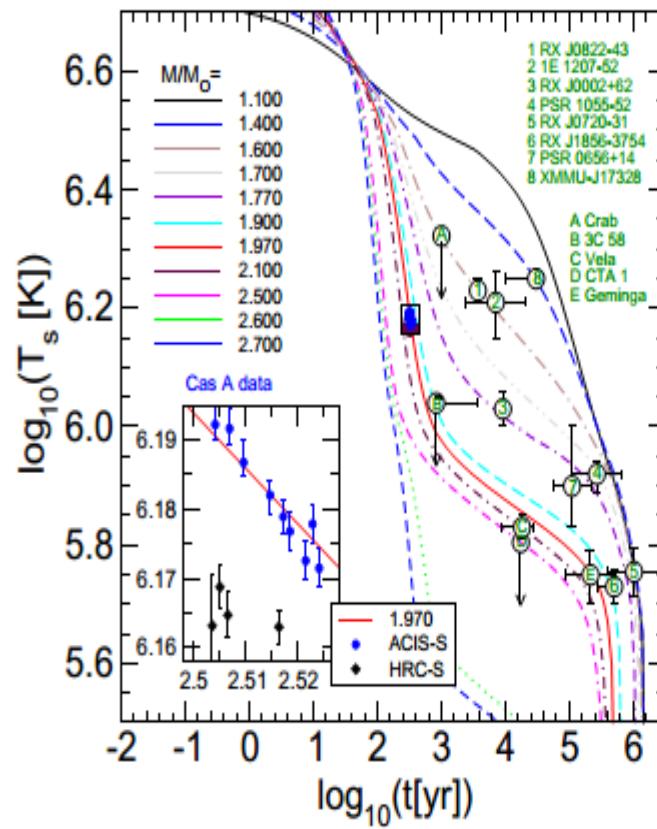
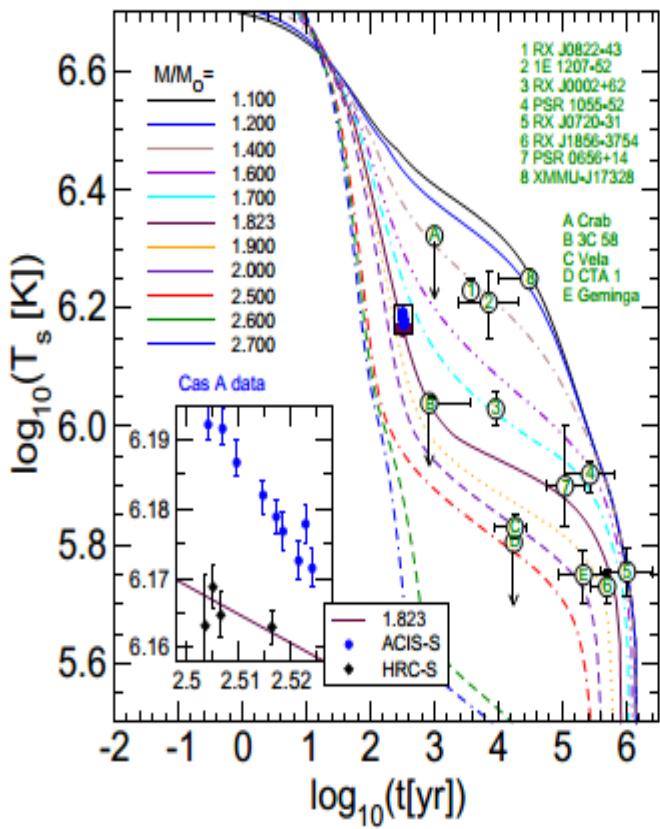


# DD2 vex-p40, AO

## ME-nc = 2.0, 2.5 n0

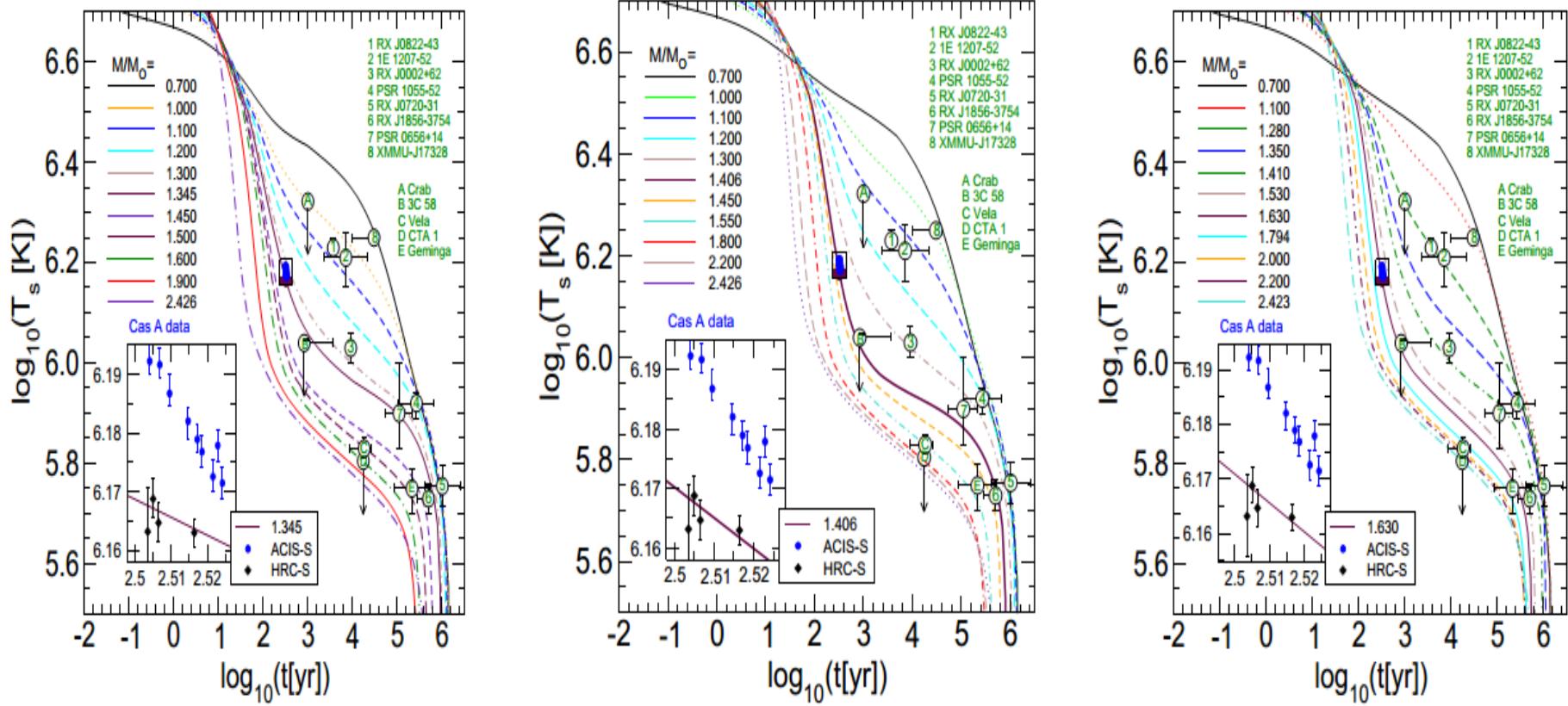


# DD2 vex p40, BCLL ME-nc = 1.5, 2.0 n0

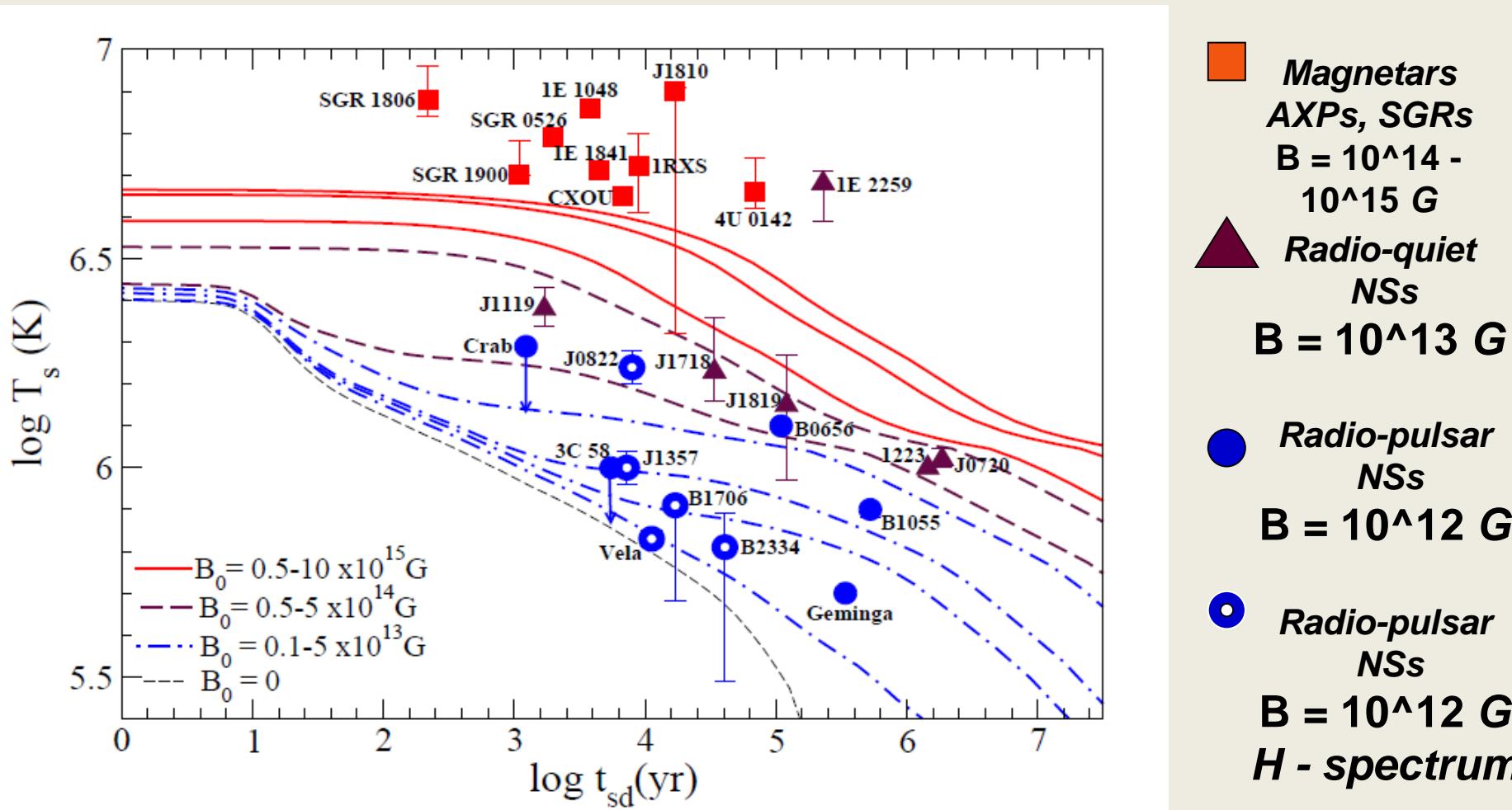


# DD2 - BCLL

## ME-nc = 1.5, 2.0, 2.5n0

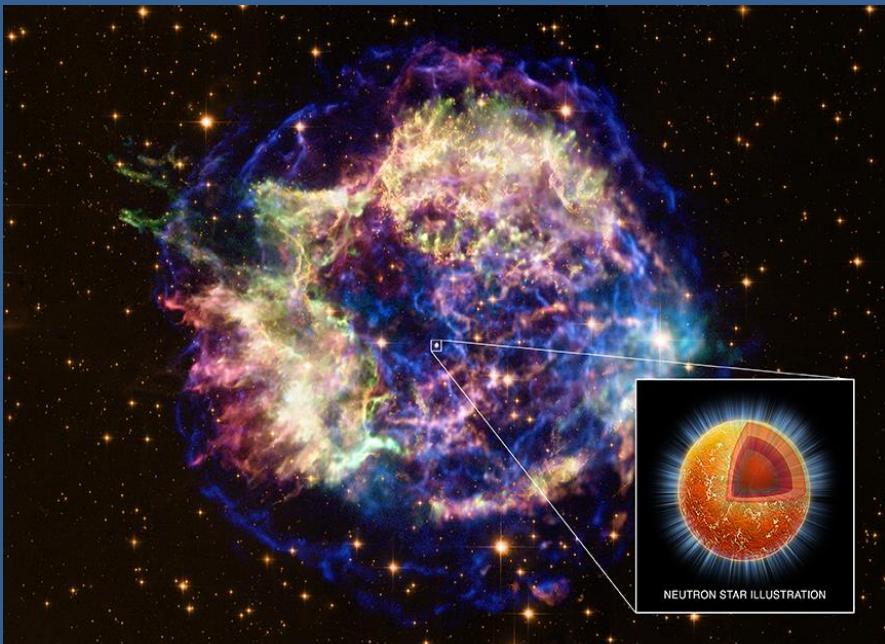


# Data of NS on Magnetic Field



# Neutron Star in Cassiopeia A

- 16.08.1680 John Flamsteed, 6m star 3 Cas
  - 1947 re-discovery in radio
  - 1950 optical counterpart
    - $T \sim 30$  MK
    - $V_{\text{exp}} \sim 4000 - 6000$  km/s
  - distance 11.000 ly = 3.4 kpc

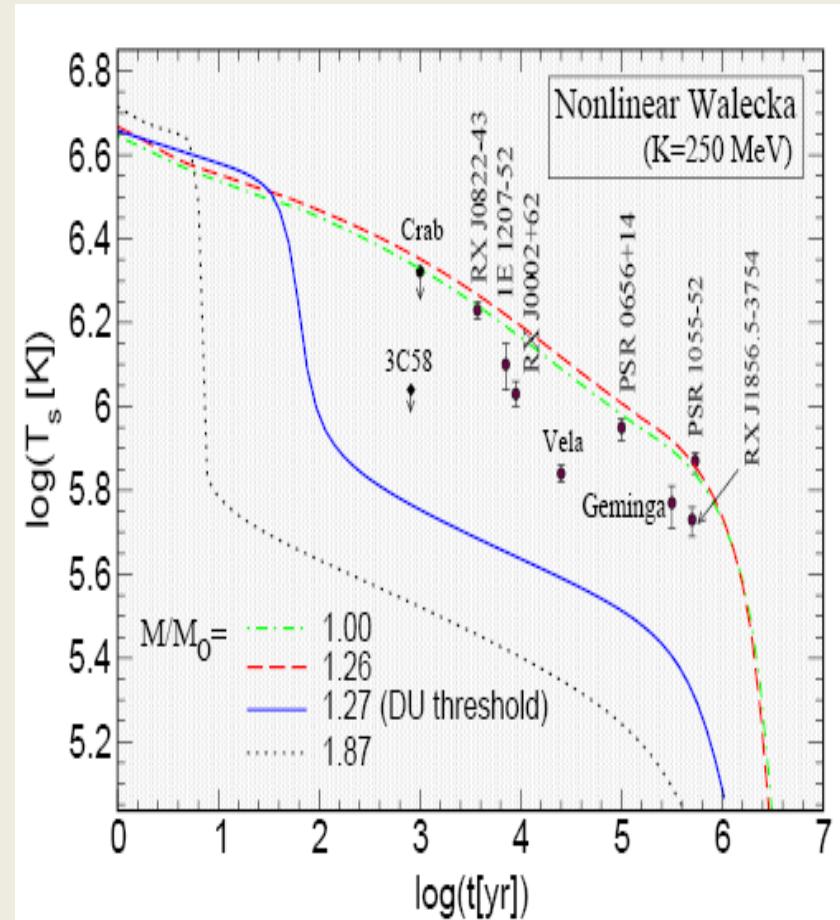
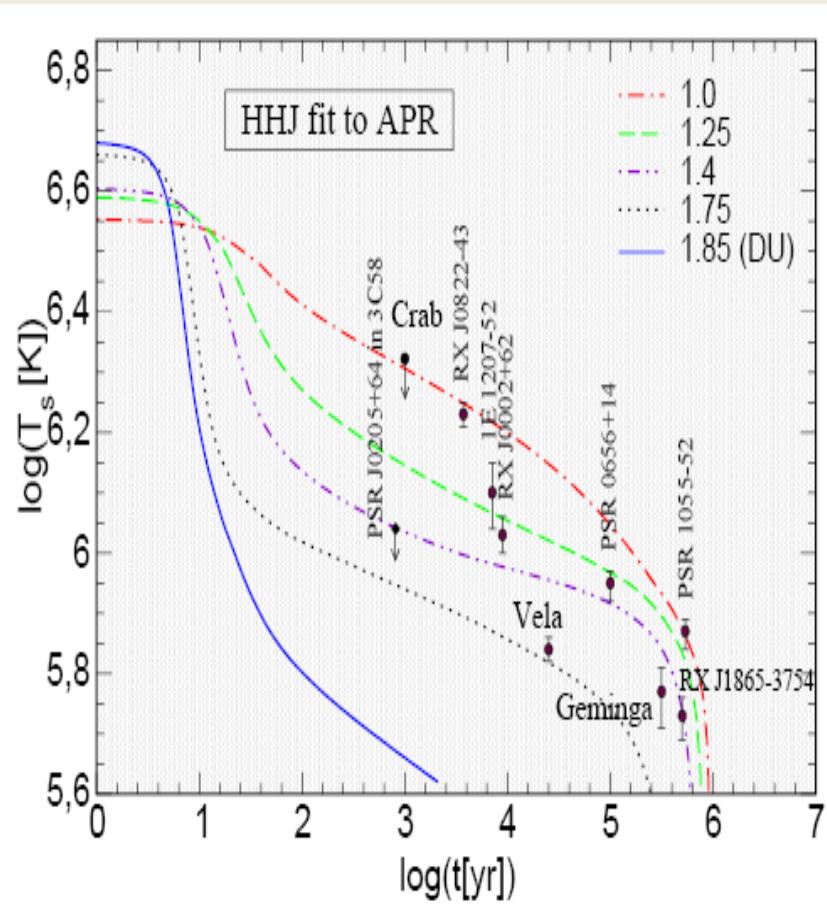


*picture:* spitzer space telescope

D.Blaschke, H. Grigorian, D. Voskresensky, F. Weber,  
Phys. Rev. C 85 (2012) 022802

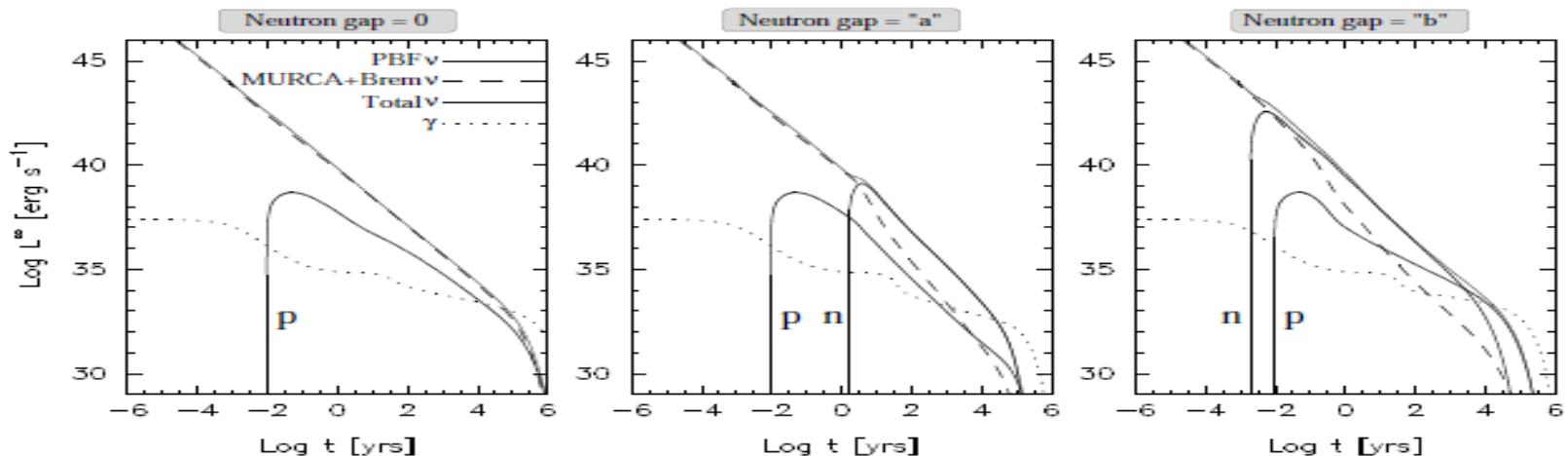
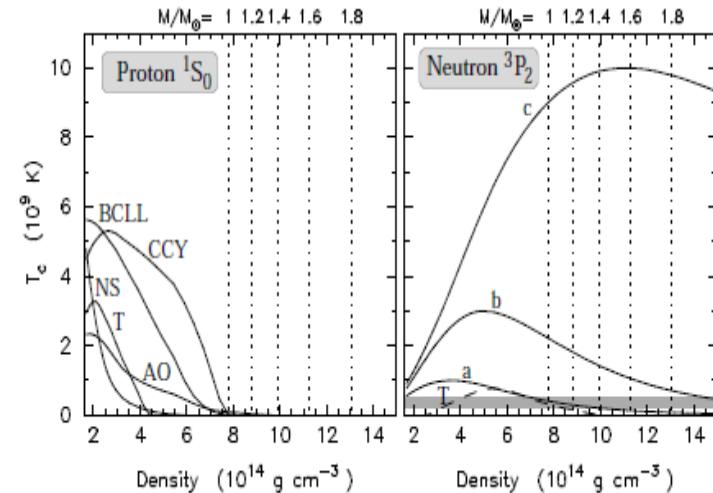
e-Print: arXiv:1108.4125 [nucl-th]

# DU Problem & Constraint



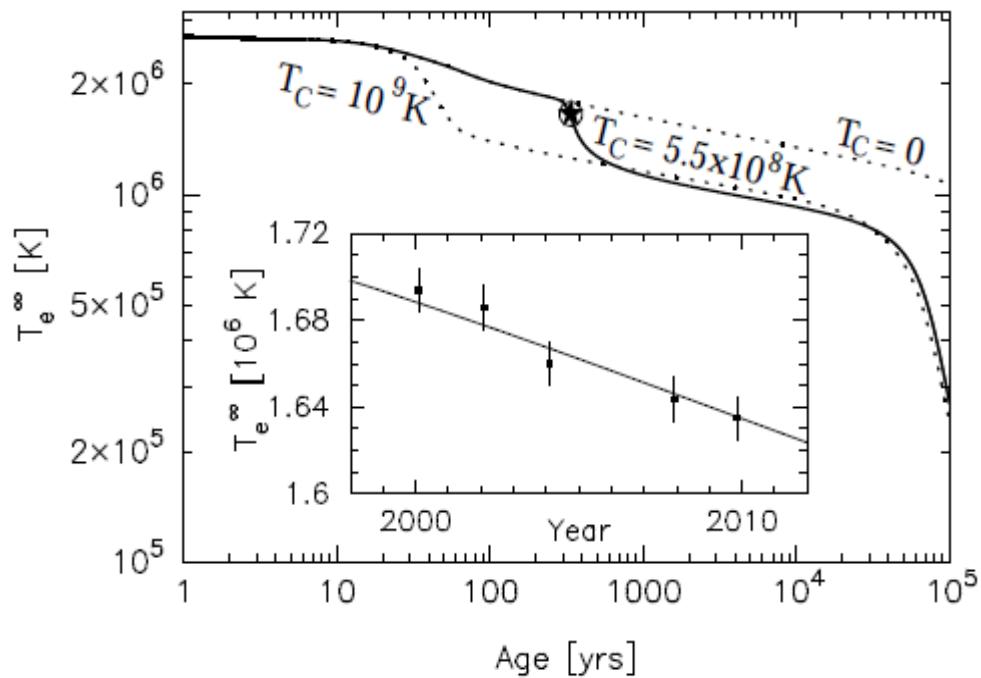
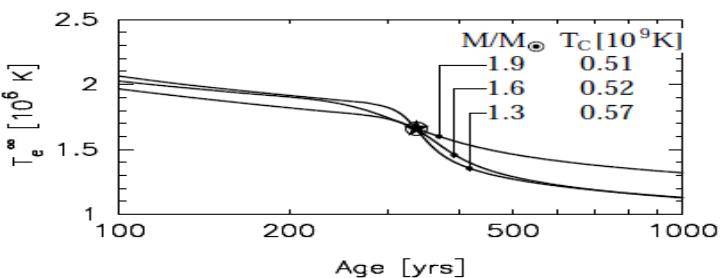
# Influence Of SC On Luminosity

- Critical temperature,  $T_c$ , for the proton  $^1S_0$  and neutron  $^3P_2$  gaps, used in PAGE, LATTIMER, PRAKASH, & STEINER  
Astrophys.J.707:1131 (2009)



# Tc ‘Measurement’ From Cas A

- Assumed to be a star with mass =  $1.4 M_{\odot}$  from the APR EoS
- Rapidly cools at ages  $\sim 30$ - $100$  yrs due to the thermal relaxation of the crust
- Mass dependence



Page, Lattimer, Prakash, & Steiner  
Phys.Rev.Lett.106:081101,2011

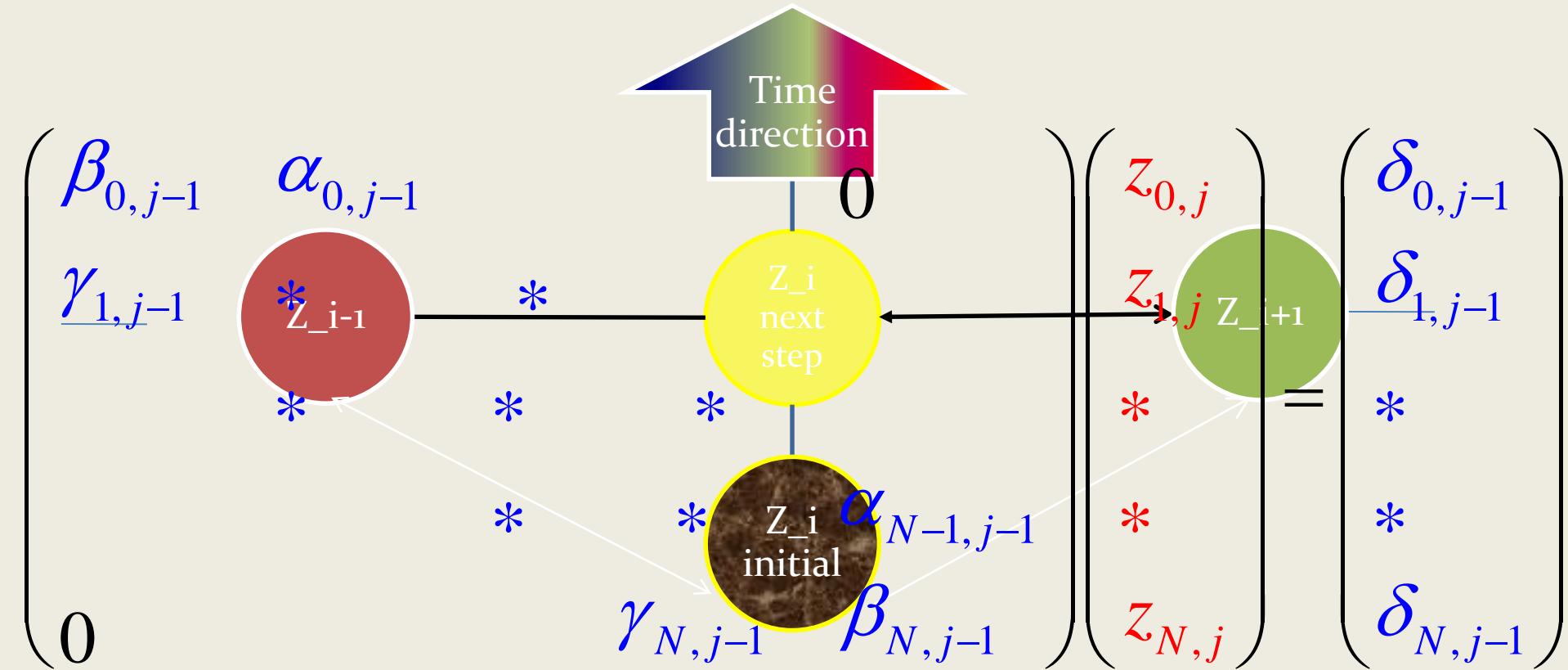
# Equations for Cooling Evolution

$$\begin{cases} \frac{\partial \textcolor{red}{z}(\tau, a)}{\partial \tau} = \textcolor{blue}{A}(z, a) \frac{\partial \textcolor{red}{L}(\tau, a)}{\partial a} + \textcolor{blue}{B}(z, a) \\ \textcolor{red}{L}(\tau, a) = \textcolor{blue}{C}(z, a) \frac{\partial \textcolor{red}{z}(\tau, a)}{\partial a} \end{cases} \quad \textcolor{red}{z}(\tau, a) = \log \textcolor{red}{T}(\tau, a)$$

$$\textcolor{red}{L}_{i\pm 1/2} = \pm \frac{\textcolor{blue}{C}_i + \textcolor{blue}{C}_{i\pm 1}}{2} \frac{\textcolor{red}{z}_{i\pm 1} - \textcolor{red}{z}_i}{\Delta a_{i-1/2(1\mp 1)}}$$

$$\frac{\partial \textcolor{red}{L}_i}{\partial a} = 2 \frac{\textcolor{red}{L}_{i+1/2} - \textcolor{red}{L}_{i-1/2}}{\Delta a_i + \Delta a_{i-1}}$$

# Finite difference scheme



$$\alpha_{i,j-1} z_{i+1,j} + \beta_{i,j-1} z_{i,j} + \gamma_{i,j-1} z_{i-1,i} = \delta_{i,j-1}$$

# Boundary conditions

