The Higgs p_T as a probe to new physics.

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for the ϕ^* -working group

HiggsTools Young Researcher's Meeting, Torino

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Chapter 3: ϕ^* distributions for BSM searches Is ϕ^* more discriminatory of new physics than Higgs p_T ? The set-up

- 1. Pick your favourite Higgs+1 jet process: $gg \rightarrow hg$
- 2. Add loops from your favourite BSM model: MSSM
- 3. Pick your favourite MSSM scenario: lightstop
- 4. Study mass effects from BSM loops on the p_T distribution

5. Repeat for ϕ^*

For results see Matias's talk!

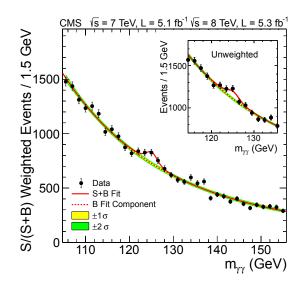
1 Why p_T spectrum?

- ❷ Higgs+1 Jet in the SM
- **8** Higgs+1 Jet in the MSSM

4 Numerical Results

6 Summary

4th July 2012: Higgs discovery completes the Standard Model?



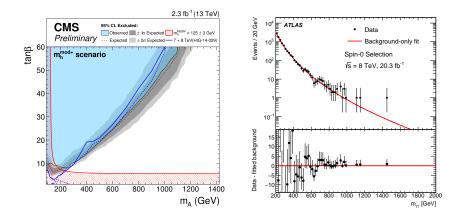
Open Questions

- Unification of gauge couplings?
- ► Baryon Asymmetry: $\Delta N_B - \Delta N_{\bar{B}} \approx 10^9$ \rightarrow missing CP violation
- ► Dark matter → stable, weakly interacting, $m_{DM} \approx 100 \text{ GeV}$
- "Unnatural" Higgs mass
- Tiny neutrino masses
- Quantum theory of gravity
- ▶ etc etc ...



"Frankly, I even find it hard to believe some of the things I've been coming up with."

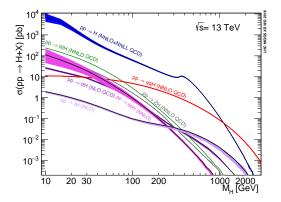
Direct Discovery: Search for new resonances \rightarrow Many blanks and some false leads so far...



Searches for new physics

Indirect Discovery: Look for deviations from SM predictions in known processes

- Largest contribution to SM Higgs production comes from gluon fusion
- Coupling of gluon to Higgs mediated predominantly by a top loop
- Gluon fusion rate can be altered by modified top Yukawa coupling and/or new coloured/scalar particles



Testing nature of Higgs-gluon interaction and its precise measurement can reveal BSM dynamics

Searches for new physics: Why p_T spectrum?

- Successful EWBG requires new states to generate sizeable potential
- ▶ Typically, the states are scalar tops or composite top partners
 - heavy resonances with same quantum no. as top
 - couple strongly to Higgs
- ▶ essential to raise Higgs mass (m_h) to "acceptable" levels
- ▶ Contributions of new heavy loops $(m_h^2/4m_{loop}^2 \ll 1)$ described by effective gluon-gluon-Higgs interaction:

$$\mathcal{L}_{\text{eff}} = c_g \frac{\alpha_s}{12\pi v} G^a_{\mu\nu} G^{a\mu\nu} h$$

 $\rightarrow c_g$ quantifies size of interaction, $c_g = 0 \implies$ SM

- ▶ Modified Yukawa coupling due to top partners effectively scaled into κ_t → $\kappa_t = 1 \implies SM$
- ▶ Inclusive gluon fusion cross section cannot disentangle effects of κ_t, c_g

$$\frac{\sigma_{\rm incl}(\kappa_t, c_g)}{\sigma_{\rm incl}^{\rm SM}} \approx (\kappa_t + c_g)^2$$

New physics models: Why p_T spectrum?

Minimal Composite Higgs Model (MCHM)¹

- ▶ In MCHMs, electroweak symmetry is broken dynamically by a strong interaction \rightarrow based on coset SO(5)/SO(4)
- \blacktriangleright Higgs arises as a pseudo-Nambu-Goldstone boson of the broken symmetry \rightarrow explains the Higgs mass
- Strong sector contains fermionic resonances which
 - contribute to gluon fusion loop diagram
 - mix with SM fermions and modify top Yukawa coupling
- Contributions to the sum $\kappa_t + c_g$ cancel exactly in a broad class of MCHM:

$$\kappa_t + c_g \approx f_g(\xi), \ \xi \equiv v^2/f^2$$

f is the scale of breaking of global symmetry

Gluon fusion XS is independent of the mass spectrum of new fermionic resonances

¹More details in [Schlaffer, Spannowsky, Takeuchi, Weiler, Wymant '14], [Grojean, Salvioni, Schlaffer, Weiler '14], [Schlaffer '15]

New physics models: Why p_T spectrum?

Minimal Supersymmetric Standard Model (MSSM)¹

- ▶ In SUSY, the cancellation between the effects of the modification to the gluon-Higgs vertex takes place less generically.
- ▶ Assuming MSSM is in decoupling limit, inclusive signal strength is

$$\frac{\Gamma(gg \to h)}{\Gamma(gg \to h)_{\rm SM}} = (1 + \Delta_t)^2$$

where

$$\Delta_t \approx \frac{m_t^2}{4} \left(\frac{1}{m_{\tilde{t}_1}^2} + \frac{1}{m_{\tilde{t}_2}^2} - \frac{(A_t - \mu/\tan\beta)^2}{m_{\tilde{t}_1}^2 m_{\tilde{t}_2}^2} \right)$$
(1)

- ▶ For large values of triliniear coupling of Higgs to the stops A_t , deviations from SM value vanish
- A_t dependent parts of the production cross section respond differently to boosts of Higgs than A_t independent ones

Boosted regime breaks degeneracy

¹For a detailed study see:

[[]Brein Hollik '03], [Langenegger, Spira, Starodumov, Trueb '06], [Bagnaschi, Degrassi, Slavich, Vicini '12], [Harlander, Mantler, Wiesemann '14], [Mantler, Wiesemann '15]

Effective description¹

- ▶ Non-trivial structure of Higgs-gluon vertex resolved by introducing scale of large p_T of Higgs \rightarrow Recoil the Higgs against a jet eg, a gluon
- Higgs p_T contains more information than total cross section:
 - richer kinematical structure
 - shape and maximum and normalization can show deviations from SM
 - allows for refined cuts
- ▶ Allowing for $c_g \neq 0$ and $\kappa_t \neq 1$ the differential cross section normalized to SM given by

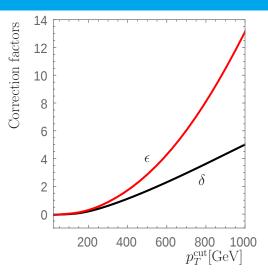
$$\frac{\sigma(p_T^{\text{cut}})}{\sigma^{\text{SM}}(p_T^{\text{cut}})} = (\kappa_t + c_g)^2 + \delta(p_T^{\text{cut}}) \kappa_t \ c_g + \epsilon(p_T^{\text{cut}}) \ c_g^2$$

with $\sigma(p_T^{\text{cut}}) = \int_{p_T > p_T^{\text{cut}}} dp_T \frac{d\sigma}{dp_T}$

¹Inclusion of dim 6 operators: [Grojean, Salvioni, Schlaffer, Weiler '14], [Azatov, Paul '14], [Langenegger, Spira, Stebel '15], dim 8 operators: [Harlander, Neumann '13], [Dawson, Zeng '14], High p_T BSM effects in EFT: [Grazzini, Ilnicka, Spira, Wiesemann '16]

Why p_T spectrum?

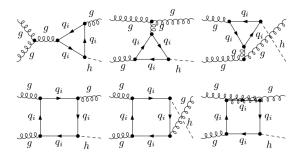
- For small p_T^{cut} , δ, ϵ are small
 - modify the cross section by a few percent
 - less than the uncertainty accepted in inclusive Higgs cross section
- δ, ε grow significantly as p_T^{cut} [Harlander, Liebler, Mantler '16], [Grojean et al. '14]
- New physics should show up at high p_T



Measuing the p_T distribution breaks the degeneracy of the inclusive rate and disentangles c_g, κ_t

Higgs+1 jet in the SM

LO contributions to $gg \rightarrow gh$ [figures: Brein, Hollik '03]



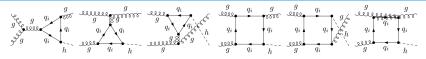
• Higgs production at finite momenta requires additional radiation (g or q)

▶ Partonic subprocesses contributing to $pp \rightarrow h + jet$ are:

$$gg \to hg, \ gq \to h\bar{q}, \ \bar{q}g \to h\bar{q}, \ q\bar{q} \to hg$$

- ▶ Actual breakdown of subprocesses depends on p_T , scale choice, PDFs etc
- ▶ Gluon initiated subprocesses dominate \implies focus on $gg \rightarrow hg$ (~50-70% total rate)

Higgs+1 jet in the SM



- LO (O(α^s_s)) results known since ~ 1990: Ellis, Hinchliffe, Soldate, van der Bij '88; Baur, Glover '90
- ▶ NLO $(\mathcal{O}(\alpha_s^4))$ in HTL came ~ late 90s/early 00s: Schmidt '97; de Florian, Grazzini, Kunszt '99; Ravindran, Smith; Van Neerven '02
 - Estimation of $\mathcal{O}(\alpha_s^4)$ with finite top mass effects: Harlander, Neumann, Oezeren, Wiesemann '12; Neumann, Wiesemann '14
- ► NNLO (O(α⁵_s)) results more recent: Boughezal, Caola, Melnikov, Petriello, Schulze '13, '15; Chen, Gehrmann, Glover, Jacquier '15
- Resummation of large logs needed at low p_T :
 - NLL: Catani et al.'88; Hinchliffe, Novaes '99; Kauffman '91, '92; Balazs et al. '00; Gerger, Qiu '03; Kulesza et al. '04; Gawron, Kwiecinski '04; Watt et al. '04; Lipatov, Zotov '05
 - NNLL: de Florian, Grazzini '00; Catani, de Florian, Grazzini '01; Bozzi, Catani, de Florian, Grazzini '03; Becher, Neubert, Wilhelm '12, '13
 - **N³LL**: Li, Zhu '16; Vladimirov '16
- Resummed results matched to fixed order calculations at high p_T to get predictions for whole p_T range

Higgs bosons in the MSSM

2 Higgs doublets Φ_1 and Φ_2 with $\Phi_i = 1/\sqrt{2}(\phi_i + i\chi_i)$

Physical states

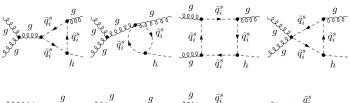
- \mathcal{CP} -even: $\phi_1^0, \phi_2^0 \to h, H$
- $\blacktriangleright \mathcal{CP}\text{-odd: } \chi_1^0, \chi_2^0 \to A, G$
- \blacktriangleright charged: $\phi_1^\pm, \phi_2^\pm \to H^\pm, G^\pm$

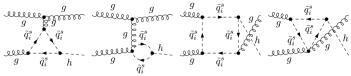
Electroweak Symmetry Breaking \rightarrow 5 physical Higgs states h, H, A, H^{\pm}

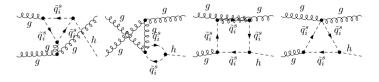
$$\begin{pmatrix} h \\ H \\ A \\ G \end{pmatrix} = \begin{pmatrix} -s_{\alpha} & c_{\alpha} & 0 & 0 \\ c_{\alpha} & s_{\alpha} & 0 & 0 \\ 0 & 0 & s_{\beta_n} & c_{\beta_n} \\ 0 & 0 & -c_{\beta_n} & s_{\beta_n} \end{pmatrix} \begin{pmatrix} \phi_1^0 \\ \phi_2^0 \\ \chi_1^0 \\ \chi_2^0 \end{pmatrix}$$



LO contributions from squarks to $gg \rightarrow gh$ [Brein, Hollik '03]







Higgs+1 jet in the MSSM

- \blacktriangleright The lightest neutral Higgs h is SM-like in the decoupling limit
- ▶ The Higgs+1 jet process is mediated by quarks as well as squarks

 \rightarrow can lead to potentially large mass effects

- ▶ The partonic processes are similar to the SM:
 - gluon fusion $gg \to hg$
 - quark gluon scattering $q(\bar{q})g \rightarrow hq(\bar{q})$
 - quark-antiquark annihilation $q\bar{q} \rightarrow hg$
- ▶ Yukawa couplings of the quarks to the Higgs are different \rightarrow changes overall rate

φ		g_u^ϕ	g^{ϕ}_d	g_V^ϕ
SM	h	1	1	1
MSSM	h	$\cos \alpha / \sin \beta$	$-\sin\alpha/\cos\beta$	$\sin(\beta-\alpha)$
	H	$\sin \alpha / \sin \beta$	$\cos\alpha/\cos\beta$	$\cos(\beta-\alpha)$
	A	$1/\tan\beta$	$\tan\beta$	0

▶ There are additional super partner loops and additional topologies \rightarrow changes incl. XS and angular distributions

The lightstop Scenario

Distributions at LO were plotted using MoRe – SusHi [sushi.hepforge.org] in conjunction with FeynHiggs [feynhiggs.de]

lightstop:

- $\mathbf{1} \ M_{\rm SUSY} = 500 \ {\rm GeV}$
- $2 X_t^{\rm OS} = 2 M_{\rm SUSY}$
- **3** $|A_t| = |A_b| = |A_\tau| \equiv 1017.5$ GeV
- **4** $\mu = 350 \text{ GeV}$
- $5 \tan \beta = 20$
- $M_3 = 1500 \text{ GeV}$
- $M_A = 600 \text{ GeV}$
- **8** $M_2 = 500 \text{ GeV}$

 $M_{\tilde{l}_2} = 1000 \text{ GeV}$

Variations:

- **1** $M_{\rm SUSY} = 600/800 \,\,{\rm GeV}$
- $2 X_t^{\rm OS} = 2 M_{\rm SUSY}$
- $|A_t| = |A_b| = |A_\tau| = X_t + \mu/\tan\beta$
- $4 \ \mu = 350 \text{ GeV}$
- $5 \tan \beta = 20$
- $M_3 = 1500 \text{ GeV}$
- $M_A = 600 \text{ GeV}$
- **8** $M_2 = 500 \text{ GeV}$
- $M_{\tilde{l}_3} = 1000 \text{ GeV}$
- Renormalization scales: $\mu_R = \mu_F = M_T/2; \ M_T = \sqrt{m_h^2 + p_T^2}$
- ▶ Scale variation: $\{\mu_R, \mu_F\} \in \{M_T/4, M_T/4\}, \{M_T, M_T\}$

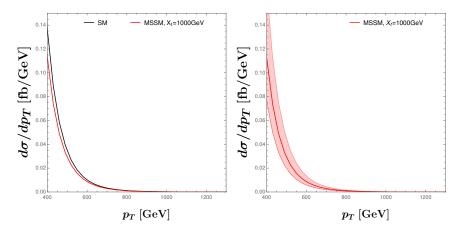
Disclaimer:

- ▶ The lightstop benchmark points were designed for run I of the LHC in 2013 [Carena et al. '13]
- Bounds on light stops have become tighter
- ▶ New MSSM benchmark scenarios compatible with run II are awaited
- Recall eq. (1):

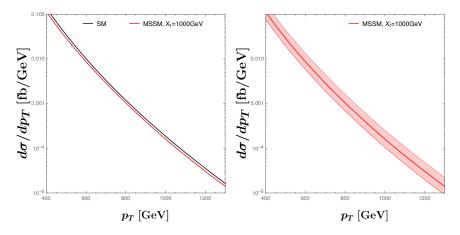
$$\Delta_t = \delta \mathcal{A}_{hgg} / \mathcal{A}_{hgg}^{SM} \approx \frac{m_t^2}{4m_{\tilde{t}_1}^2 m_{\tilde{t}_2}^2} (m_{\tilde{t}_1}^2 + m_{\tilde{t}_2}^2 - X_t^2)$$

- ▶ There is no exact cancellation of stop effects in the total rate
- ▶ When $2M_{SUSY} \le X_t \le 2.5M_{SUSY}$, the gluon fusion rate is reduced by 10-15 %
- From [Carena et al. '13]: "Reduction similar in magnitude to the *current* theoretical uncertainties on the gluon fusion cross section from e.g. the strong coupling constant and parton distribution functions."

LO differential XS for $gg \to hg$ with massive $t, b, c, \tilde{t}, \tilde{b}$ contributions:

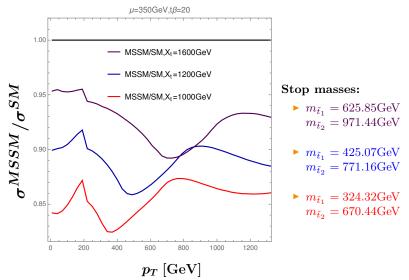


LO differential XS with massive $t, b, c, \tilde{t}, \tilde{b}$ contributions in log scale:



Higgs p_T spectrum in the lightstop Scenario

A comparison of MSSM differential XS $(t,b,c,\tilde{t},\tilde{b}$ in the loops) normalized to the SM (t,b,c) :



Summary

PROS:

- ▶ Mass effects from additional particles in the loop for Higgs+1 jet processes modify the p_T spectrum.
- ▶ For the MSSM, we see clear peaks/valleys as the masses of the stops get resolved

CONS:

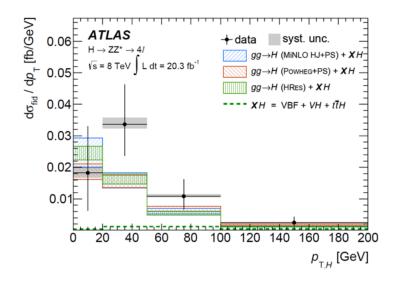
- Missing higher order calculations contribute significantly to the uncertainties
- Deviations can be smaller than the scale uncertainties
- \blacktriangleright Exclusion of light squarks in run II \implies these deviations would be smaller

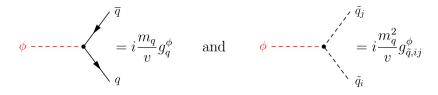
UP NEXT:

▶ For a study of ϕ^* distributions in the MSSM and a comparison to the p_T spectrum, stay tuned for Matias's talk at 11:30 am today!

Thank you for your attention!

APPENDIX





$$v = 2m_W/g = 1/\sqrt{\sqrt{2}G_F} = \sqrt{v_d^2 + v_u^2}.$$

ϕ		g_u^ϕ	g^{ϕ}_d	g_V^ϕ
SM	h	1	1	1
MSSM	h	$\cos \alpha / \sin \beta$	$-\sin lpha / \cos eta$	$\sin(\beta - \alpha)$
	H	$\sin \alpha / \sin \beta$	$\cos\alpha/\cos\beta$	$\cos(\beta - \alpha)$
	A	$1/\taneta$	aneta	0

$$g^{\phi}_{\tilde{q},ij} = g^{\phi,\text{EW}}_{\tilde{q},ij} + g^{\phi,\mu}_{\tilde{q},ij} + g^{\phi,\alpha}_{\tilde{q},ij}$$

$$\begin{split} g^{h,\text{EW}}_{\tilde{t},11} &= c^{\text{EW}}_{\tilde{t},1}c^2_{\theta_{\tilde{t}}} + c^{\text{EW}}_{\tilde{t},2}s^2_{\theta_{\tilde{t}}} & g^{h,\text{EW}}_{\tilde{b},11} = c^{\text{EW}}_{\tilde{b},1}c^2_{\theta_{\tilde{t}}} + c^{\text{EW}}_{\tilde{b},2}s^2_{\theta_{\tilde{b}}} \\ g^{h,\text{EW}}_{\tilde{t},22} &= c^{\text{EW}}_{\tilde{t},1}s^2_{\theta_{\tilde{t}}} + c^{\text{EW}}_{\tilde{t},2}c^2_{\theta_{\tilde{t}}} & g^{h,\text{EW}}_{\tilde{b},22} = c^{\text{EW}}_{\tilde{b},1}s^2_{\theta_{\tilde{b}}} + c^{\text{EW}}_{\tilde{b},2}c^2_{\theta_{\tilde{b}}} \\ g^{h,\text{EW}}_{\tilde{t},12} &= g^{h,\text{EW}}_{\tilde{t},21} = \frac{1}{2} \left(c^{\tilde{t},\text{EW}}_{\tilde{t}} - c^{\tilde{t},\text{EW}}_{1} \right) s_{2\theta_{\tilde{t}}} & g^{h,\text{EW}}_{\tilde{b},12} = g^{h,\text{EW}}_{\tilde{b},21} = \frac{1}{2} \left(c^{\tilde{b},\text{EW}}_{2} - c^{\tilde{b},\text{EW}}_{1} \right) s_{2\theta_{\tilde{b}}} \\ g^{h,\mu}_{\tilde{t},11} &= -g^{h,\mu}_{\tilde{t},22} = \frac{\mu}{m_t} \frac{\cos(\alpha - \beta)}{s^2_\beta} s_{2\theta_{\tilde{t}}} & g^{h,\mu}_{\tilde{b},11} = -g^{h,\mu}_{\tilde{b},22} = -\frac{\mu}{m_b} \frac{\cos(\alpha - \beta)}{c^2_\beta} s_{2\theta_{\tilde{b}}} \end{split}$$

$$\begin{split} g_{\tilde{t},12}^{h,\mu} &= g_{\tilde{t},21}^{h,\mu} = \frac{\mu}{m_t} \frac{\cos(\alpha - \beta)}{s_{\beta}^2} c_{2\theta_{\tilde{t}}} & g_{\tilde{b},12}^{h,\mu} = g_{\tilde{b},21}^{h,\mu} = -\frac{\mu}{m_b} \frac{\cos(\alpha - \beta)}{c_{\beta}^2} c_{2\theta_{\tilde{b}}} \\ g_{\tilde{t},11}^{h,\alpha} &= \frac{c_{\alpha}}{s_{\beta}} \left(2 + \frac{m_{\tilde{t}1}^2 - m_{\tilde{t}2}^2}{2m_t^2} s_{2\theta_{\tilde{t}}}^2 \right) & g_{\tilde{b},11}^{h,\alpha} = -\frac{s_{\alpha}}{c_{\beta}} \left(2 + \frac{m_{\tilde{b}1}^2 - m_{\tilde{b}2}^2}{2m_b^2} s_{2\theta_{\tilde{b}}}^2 \right) \\ g_{\tilde{t},22}^{h,\alpha} &= \frac{c_{\alpha}}{s_{\beta}} \left(2 - \frac{m_{\tilde{t}1}^2 - m_{\tilde{t}2}^2}{2m_t^2} s_{2\theta_{\tilde{t}}}^2 \right) & g_{\tilde{b},22}^{h,\alpha} = -\frac{s_{\alpha}}{c_{\beta}} \left(2 - \frac{m_{\tilde{b}1}^2 - m_{\tilde{b}2}^2}{2m_b^2} s_{2\theta_{\tilde{b}}}^2 \right) \\ g_{\tilde{t},12}^{h,\alpha} &= g_{\tilde{t},21}^{h,\alpha} = \frac{c_{\alpha}}{s_{\beta}} \frac{m_{\tilde{t}1}^2 - m_{\tilde{t}2}^2}{2m_t^2} s_{2\theta_{\tilde{t}}} c_{2\theta_{\tilde{t}}} & g_{\tilde{b},12}^{h,\alpha} = g_{\tilde{b},21}^{h,\alpha} = -\frac{s_{\alpha}}{c_{\beta}} \frac{m_{\tilde{b}1}^2 - m_{\tilde{b}2}^2}{2m_b^2} s_{2\theta_{\tilde{b}}} c_{2\theta_{\tilde{b}}} \end{split}$$

Therein we made use of the abbreviations $s_x = \sin x$ and $c_x = \cos x$ and defined:

$$\begin{split} c_{\tilde{t},1}^{\rm EW} &= -\frac{m_Z^2}{m_t^2} \left(1 - \frac{4}{3} s_{\theta_W}^2 \right) \sin(\alpha + \beta) \qquad c_{\tilde{b},1}^{\rm EW} = \frac{m_Z^2}{m_b^2} \left(1 - \frac{2}{3} s_{\theta_W}^2 \right) \sin(\alpha + \beta) \\ c_{\tilde{t},2}^{\rm EW} &= -\frac{m_Z^2}{m_t^2} \frac{4}{3} s_{\theta_W}^2 \sin(\alpha + \beta) \qquad c_{\tilde{b},2}^{\rm EW} = \frac{m_Z^2}{m_b^2} \frac{2}{3} s_{\theta_W}^2 \sin(\alpha + \beta) \end{split}$$

In the MSSM without flavour mixing in the squark sector, squarks $\tilde{q}_{L,R}$ of one generation mix into mass eigenstates $\tilde{q}_{1,2}$.

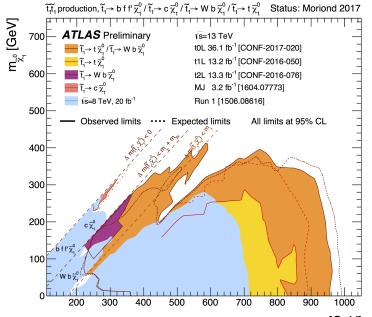
$$\mathcal{L} \supset -(\tilde{q}_{L}^{\dagger}, \tilde{q}_{R}^{\dagger}) M_{\tilde{q}}^{2} \begin{pmatrix} \tilde{q}_{L} \\ \tilde{q}_{R} \end{pmatrix} \quad \text{with} \\ M_{\tilde{q}}^{2} = \begin{pmatrix} M_{\tilde{q}_{L}}^{2} + m_{q}^{2} + M_{Z}^{2} \cos 2\beta (I_{q}^{3} - Q_{q}s_{W}^{2}) & m_{q}X_{q}^{*} \\ m_{q}X_{q} & M_{\tilde{q}_{R}}^{2} + m_{q}^{2} + M_{Z}^{2} \cos 2\beta Q_{q}s_{W}^{2} \end{pmatrix}.$$
(2)

with $X_q := A_q - \mu^* \cdot \{\cot \beta, \tan \beta\}$, where $\cot \beta$ and $\tan \beta$ apply to up- and down-type quarks, respectively.

The soft-breaking masses $M_{\tilde{q}_L}^2$ and $M_{\tilde{q}_R}^2$, the third component of the weak isospin I_q^3 , the electric charge Q_q and the mass of the quark m_q are real parameters.

The squark masses (with $m_{\tilde{q}_1} \leq m_{\tilde{q}_2}$) are eigenvalues of the mass matrix.

Higgs-squark couplings



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The neutral fields of the two Higgs doublets can be decomposed in \mathcal{CP} -even (ϕ_1^0, ϕ_2^0) and \mathcal{CP} -odd (χ_1^0, χ_2^0) components

$$\mathcal{H}_{1} = \begin{pmatrix} h_{d}^{0} \\ h_{d}^{-} \end{pmatrix} = \begin{pmatrix} v_{d} + \frac{1}{\sqrt{2}}(\phi_{1}^{0} + i\chi_{1}^{0}) \\ \phi_{1}^{-} \end{pmatrix} \\
\mathcal{H}_{2} = \begin{pmatrix} h_{u}^{+} \\ h_{u}^{0} \end{pmatrix} = e^{i\xi} \begin{pmatrix} \phi_{2}^{+} \\ v_{u} + \frac{1}{\sqrt{2}}(\phi_{2}^{0} + i\chi_{2}^{0}) \end{pmatrix},$$
(3)

Higgs potential V_H in terms of the neutral Higgs states is given by

$$\begin{split} V_{H}^{0} = &(|\mu|^{2} + m_{\mathcal{H}_{2}}^{2})|h_{u}^{0}|^{2} + (|\mu|^{2} + m_{\mathcal{H}_{1}}^{2})|h_{d}^{0}|^{2} \\ &- [m_{12}^{2}h_{u}^{0}h_{d}^{0} + h.c.] + \frac{g_{1}^{2} + g_{2}^{2}}{8}[|h_{u}^{0}|^{2} - |h_{d}^{0}|^{2}]^{2} \end{split}$$

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