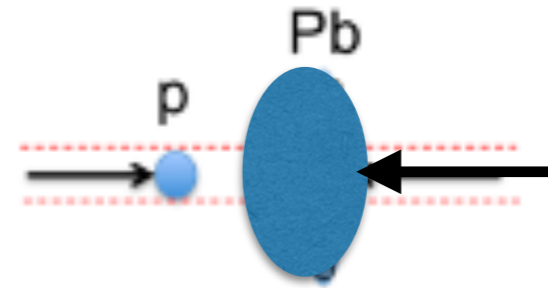
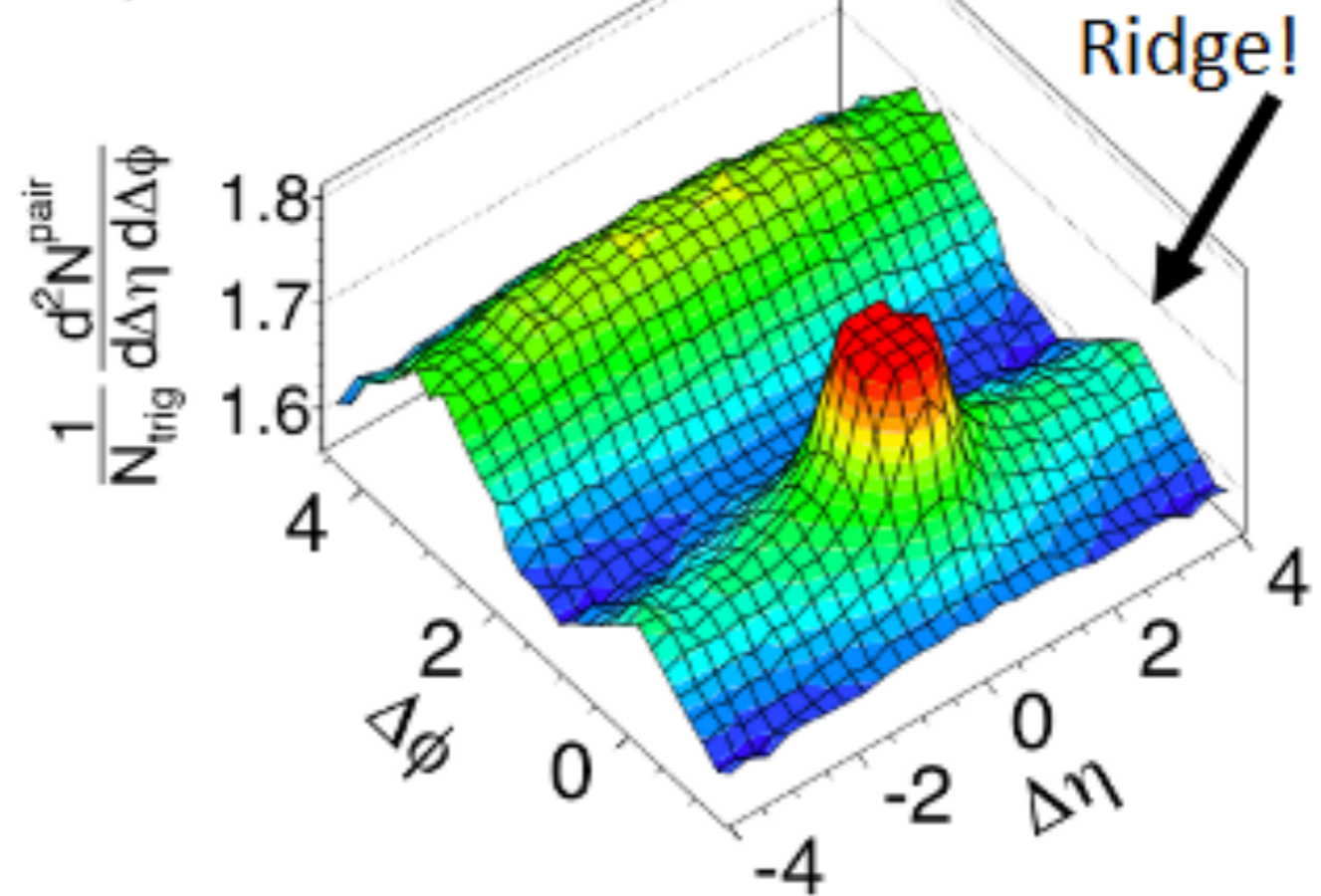


# Ridge phenomena in photon-photon collisions



CMS pPb  $\sqrt{s_{NN}} = 5.02$  TeV,  $N_{trk}^{offline} \geq 110$   
 $1 < p_T < 3$  GeV/c



Stan Brodsky



with Fred Goldhaber, Stan Glazek, Patryk Kubiczek, and Robert Brown

2017 International Conference on the Structure and Interactions of the Photon

22th International Workshop on Photon-Photon Collisions

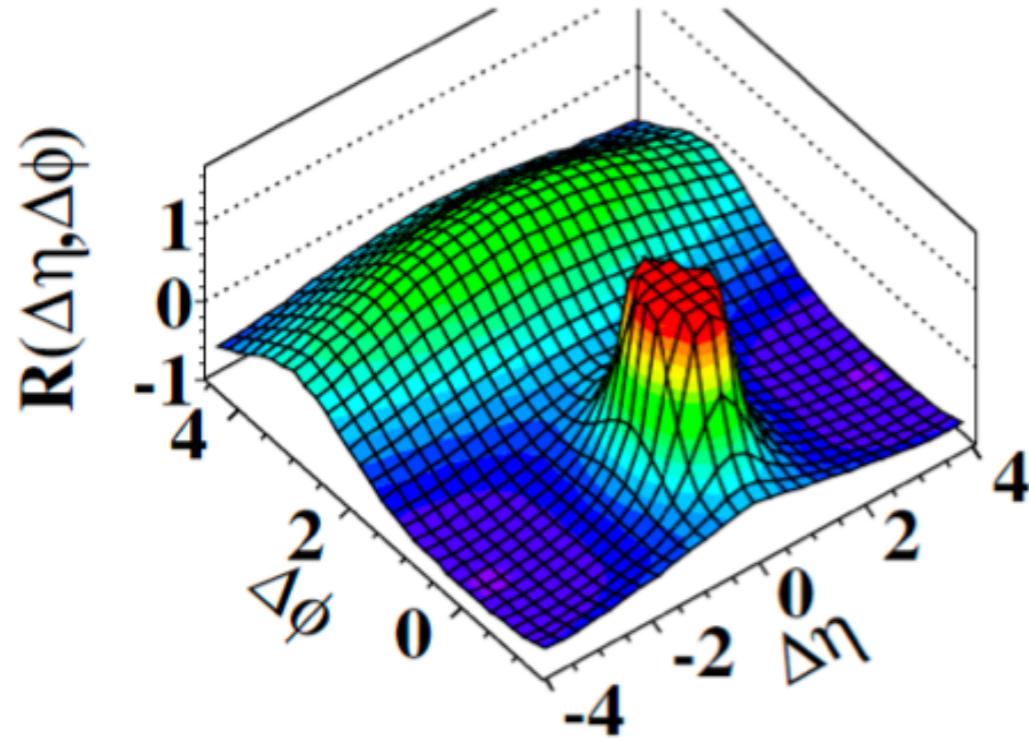
International Workshop on High Energy Photon Colliders

# Ridge in high-multiplicity $pp$ collisions

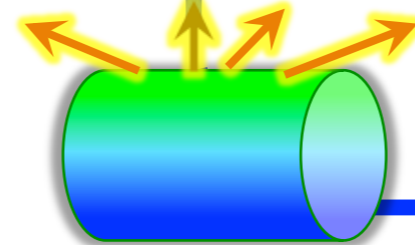
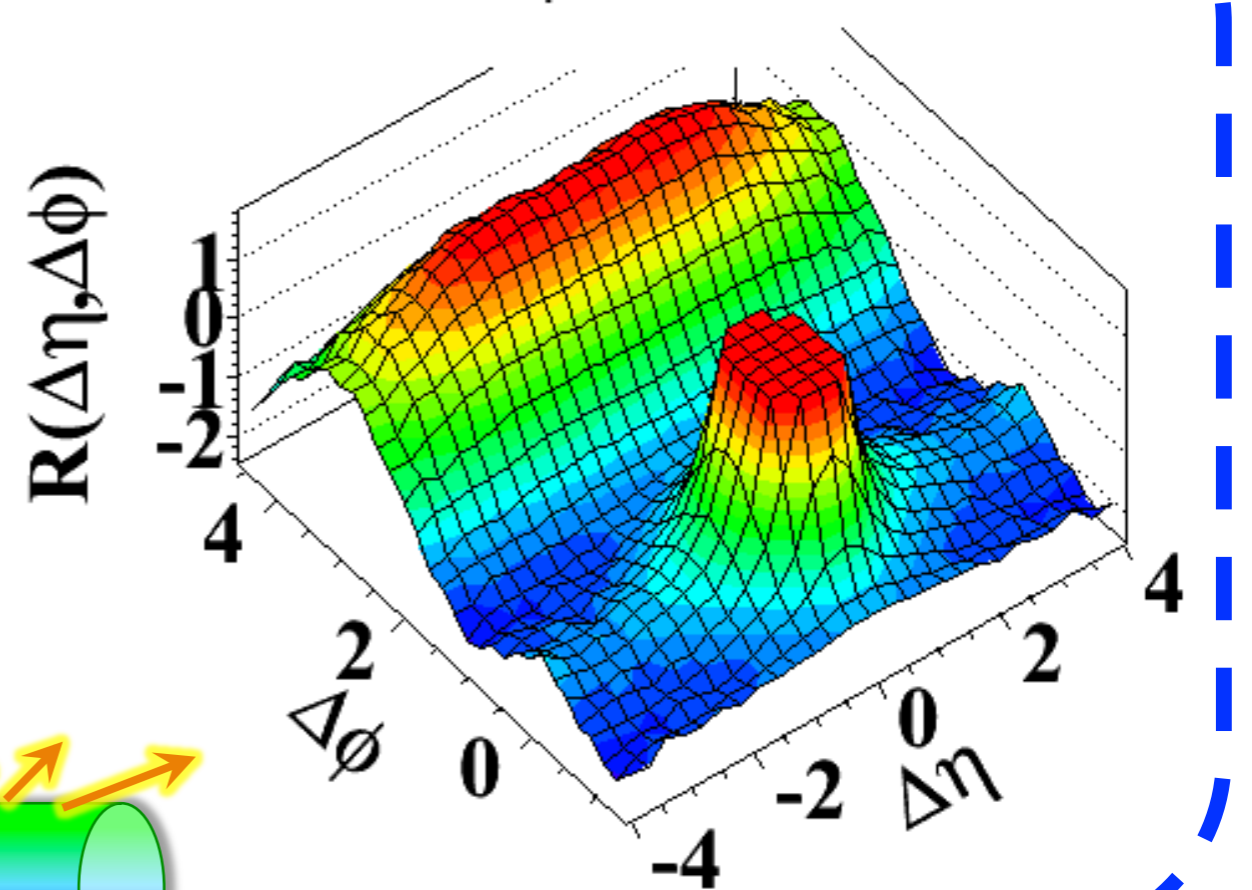
## Two-particle correlations: CMS results

$$pp \rightarrow X$$

CMS Min. Bias ( $1 \text{ GeV} < p_T < 3 \text{ GeV}$ )



(d)  $N > 110$ ,  $1.0 \text{ GeV}/c < p_T < 3.0 \text{ GeV}/c$

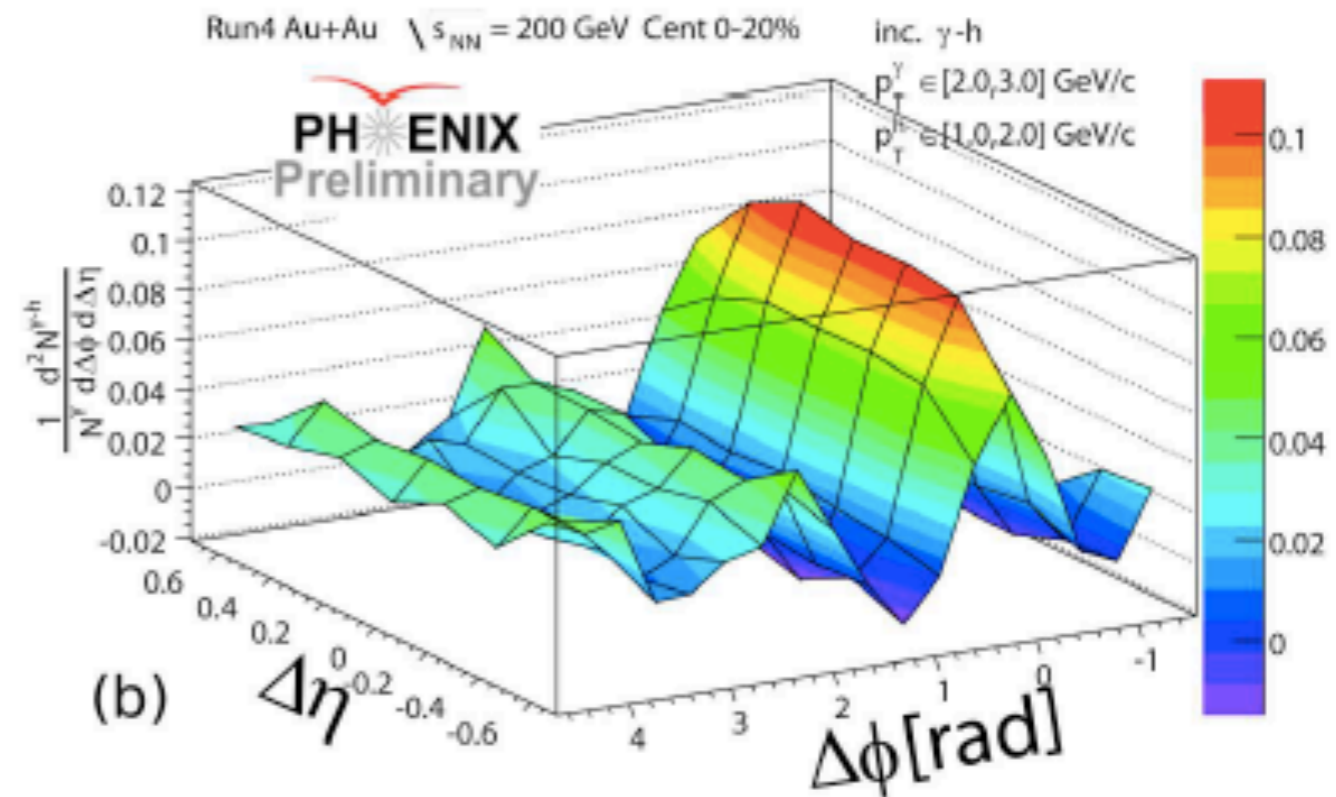
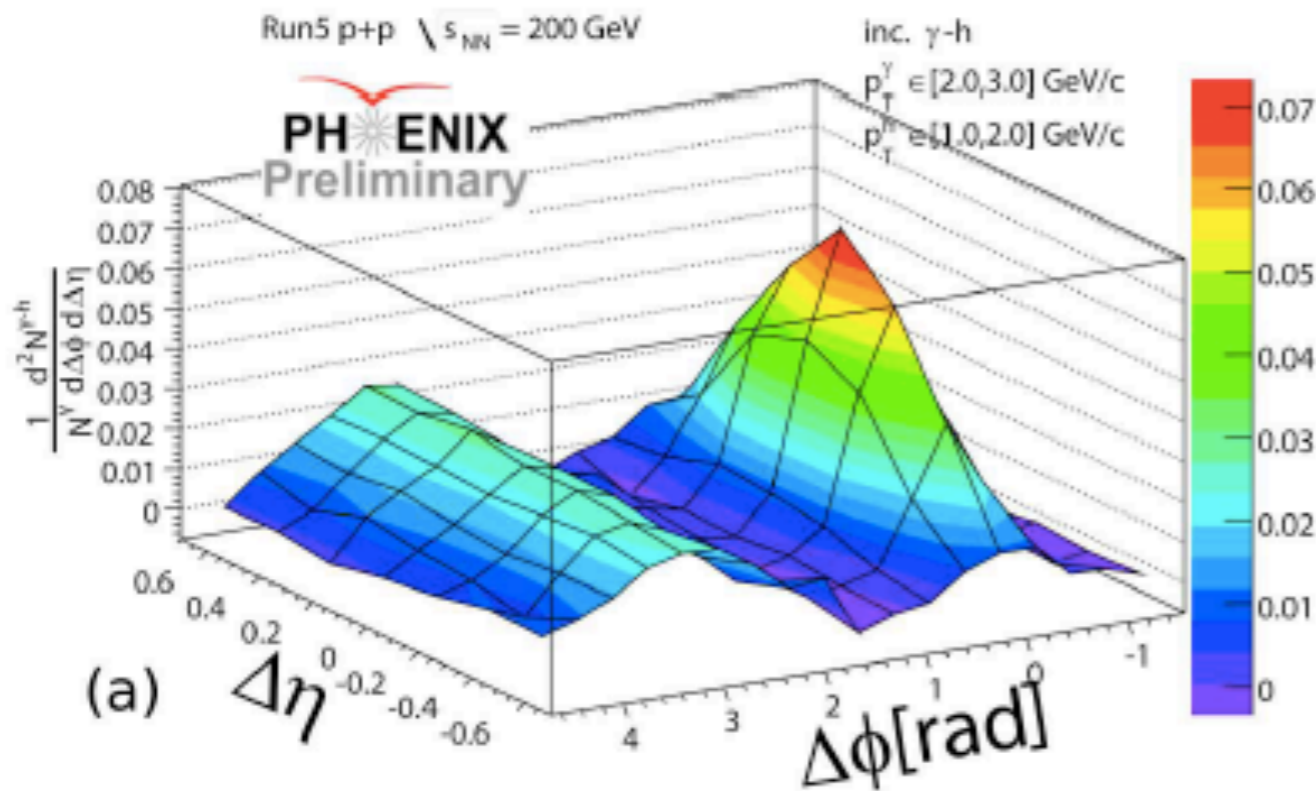


- ◆ Ridge: Distinct long range correlation in  $\eta$  collimated around  $\Delta\Phi \approx 0$  for two hadrons in the intermediate  $1 < p_T, q_T < 3 \text{ GeV}$

*Same-side long-range correlation in rapidity*

$$p + p \rightarrow X, \sqrt{s} = 200 \text{ GeV}$$

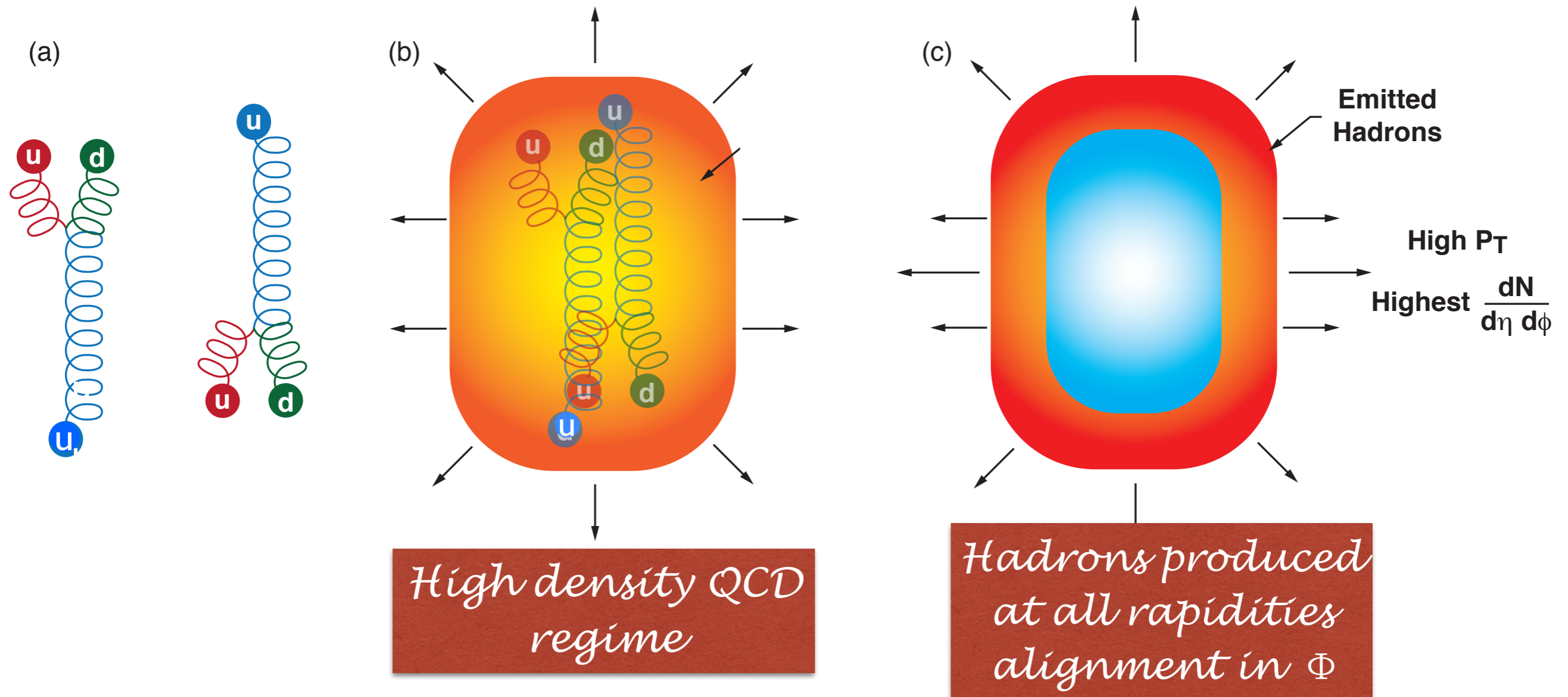
$$Au + Au \rightarrow X, \sqrt{s} = 200 \text{ GeV}$$



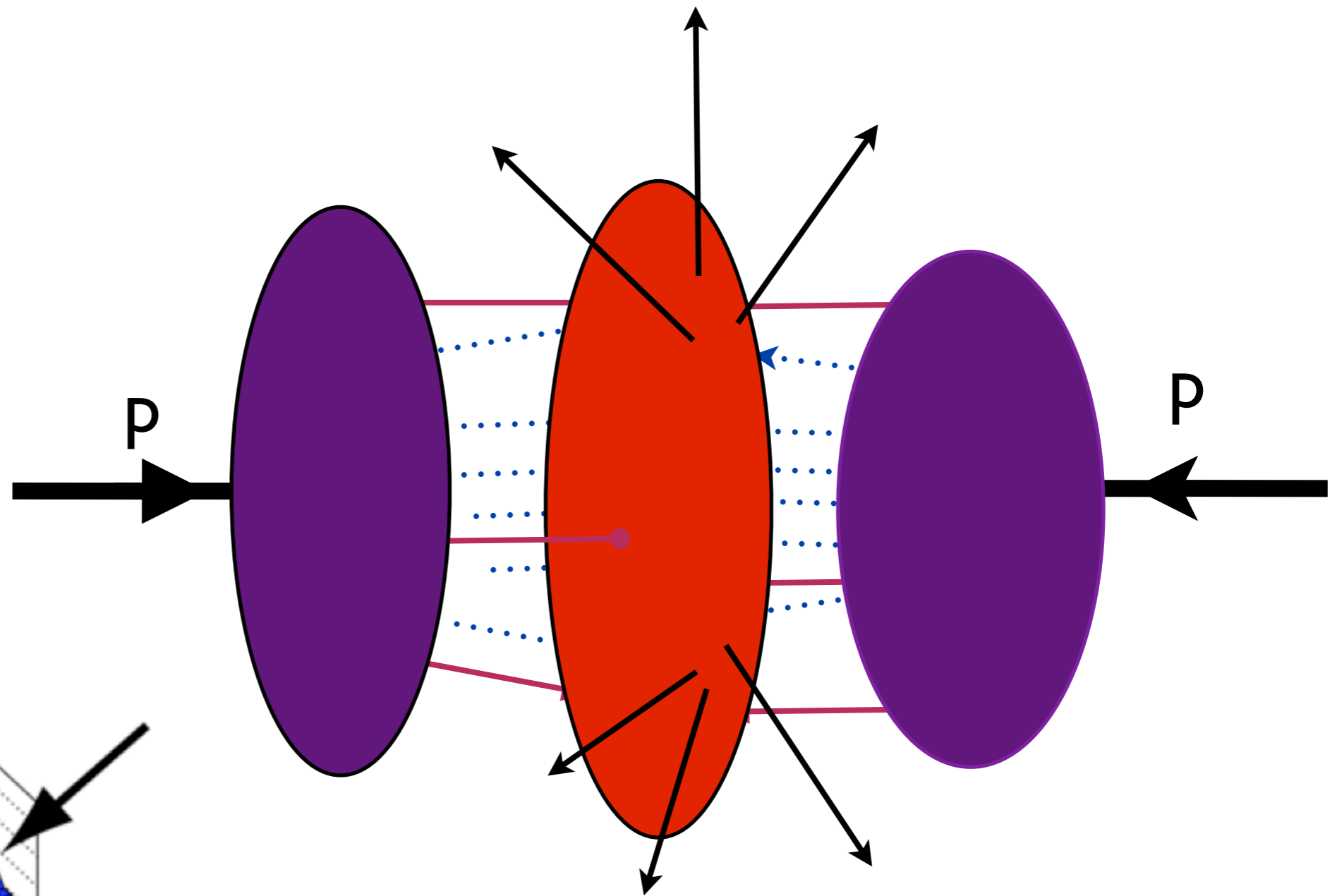
*Ridge phenomena observed in both p-p and Au-Au collisions*

**Collisions of Flux Tubes Can Produce Ridge Phenomena in photon-photon (EIC) and in ultra-peripheral collisions (UPC)**

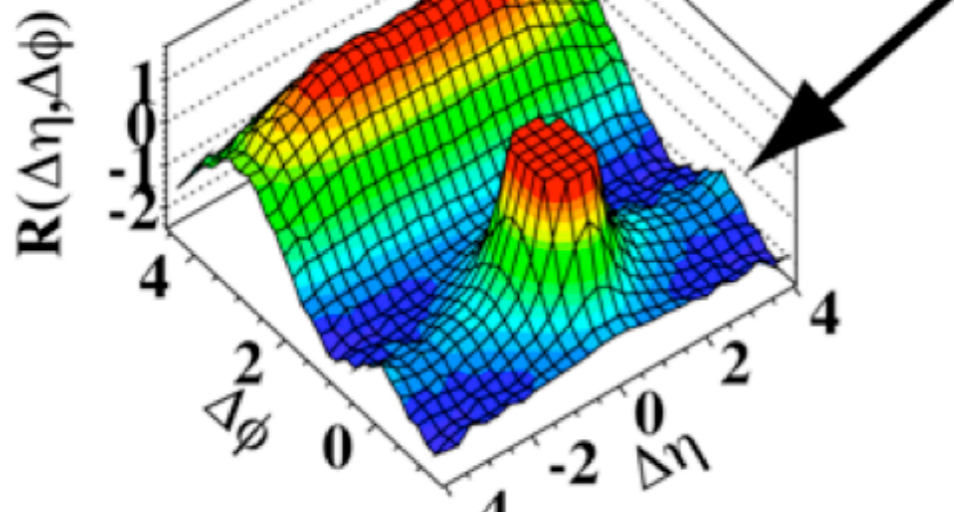
# Ridge may reflect collision of aligned flux tubes



# Collisions of Aligned Flux Tubes Can Produce Ridge Phenomena



$N > 110, 1.0 \text{ GeV}/c < p_T < 3.0 \text{ GeV}/c$



# *Multiparticle ridge-like correlations in very high multiplicity proton-proton collisions*

**Bjorken, Goldhaber, sjb**

***We suggest that the “ridge” correlations may be a reflection of the rare events generated by the collision of aligned flux tubes connecting the valence quarks in the wave functions of the colliding protons.***

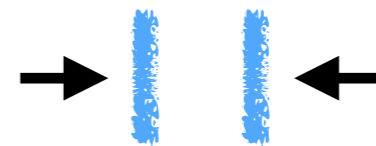
***The “spray” of particles resulting from the approximate line source produced in such inelastic collisions then gives rise to events with a strong correlation between particles produced over a large range of both positive and negative rapidity.***

# Collisions of flux tubes of protons

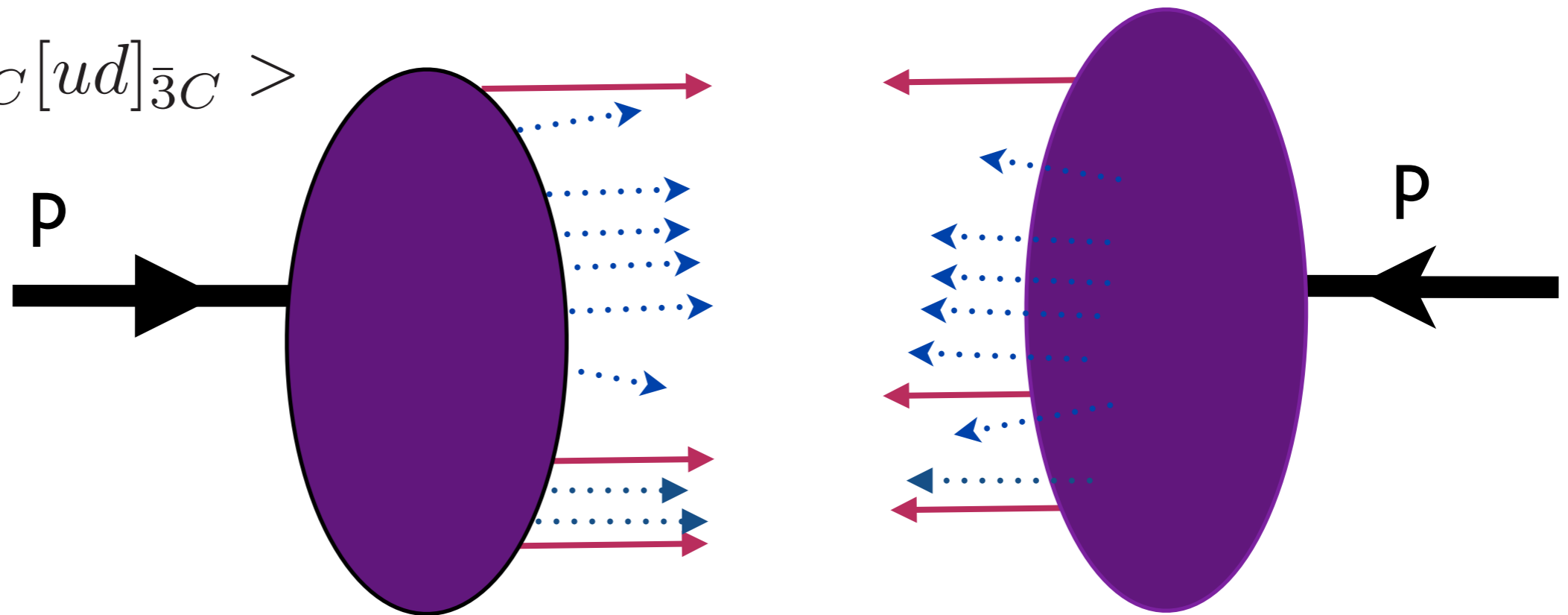
Color confinement potential  $\rightarrow$  high density gluon field: flux tube

Highest hadron multiplicity produced when the two flux tubes are aligned and overlap completely along their length.

Hadrons produced from the collisions of flux tubes



$$|p\rangle = |u_3C [ud] \bar{3}_C\rangle$$



Gluonic distribution reflects quark+diquark color structure of the protons

$v_2$  (dominant) +  $v_3$  (from 'Y' quark + diquark configurations)

# AdS/QCD + Light Front Holography: Proton is bound state of a quark + scalar diquark

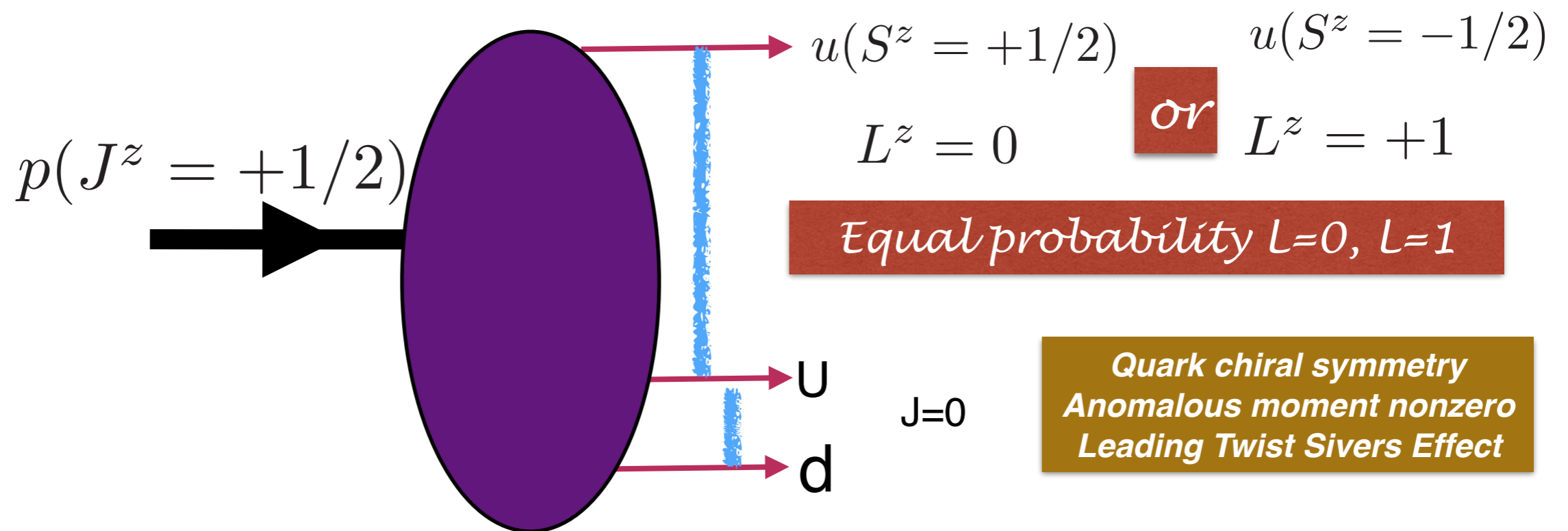
de Teramond, Dosch, Lorce, sjb

Skyrme model: Ellis, Karliner, sjb

LF  $J^z$  conservation: K. Chiu, sjb

$$3_C \times 3_C = \bar{3}_C + \cancel{6_C}$$

$$|p\rangle = |u_{3_C} [ud]_{\bar{3}_C}\rangle$$



**Gluonic distribution reflects quark+diquark color structure of the proton**

**Color confinement potential  $\rightarrow$  high density gluon field: flux tube**



# Collisions of flux tubes of protons

Color confinement potential  $\rightarrow$  high density gluon field: flux tube

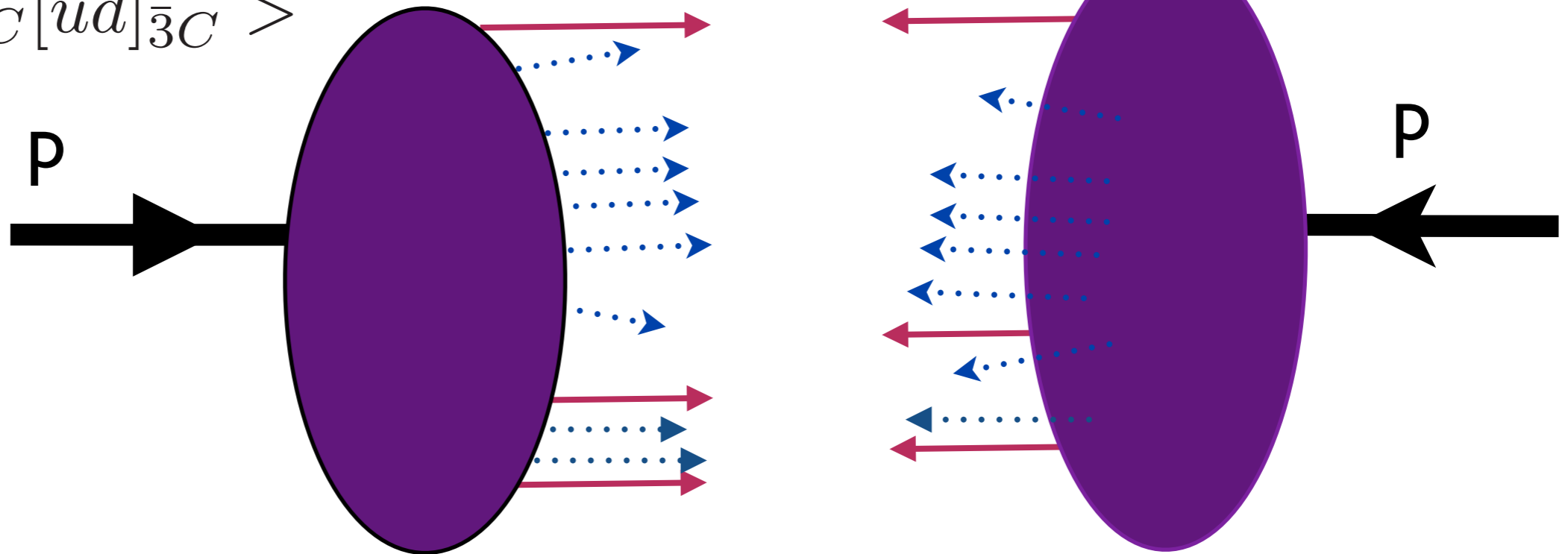
Highest hadron multiplicity produced when the two flux tubes are aligned and overlap completely along their length.

Hadrons produced from the collisions of flux tubes

Bjorken, Goldhaber, sjb



$$|p\rangle = |u_3C [ud] \bar{3}_C\rangle$$



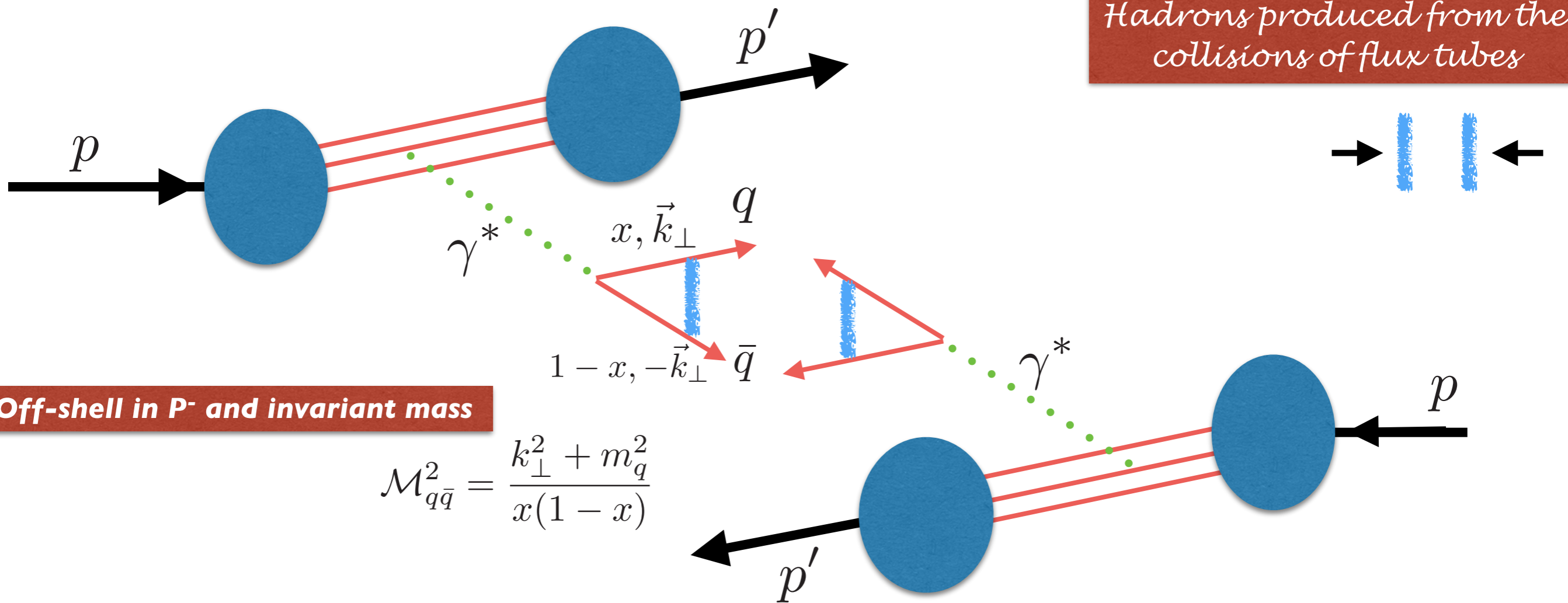
Gluonic distribution reflects quark+diquark color structure of the protons

$v_2$  (dominant) +  $v_3$  (from 'Y' quark + diquark configurations)

- Strangeness and charm enhancements

# Ridge creation in Ultra-Peripheral $pp$ scattering

$$pp \rightarrow \gamma^* \gamma^* p' p' \rightarrow X p' p'$$



Off-shell in  $P^-$  and invariant mass

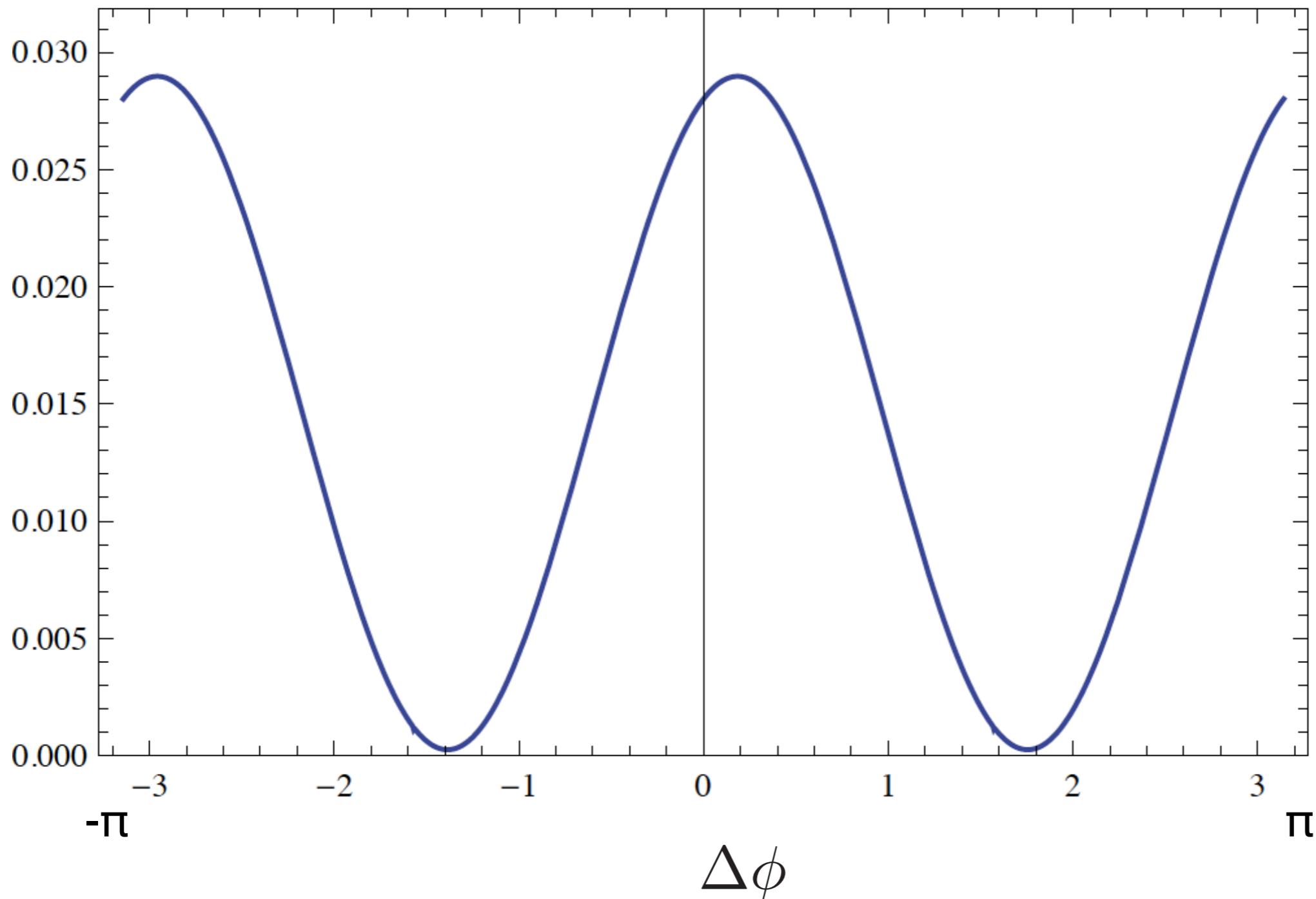
$$\mathcal{M}_{q\bar{q}}^2 = \frac{k_\perp^2 + m_q^2}{x(1-x)}$$

Planes of quark anti-quark and produced ridges aligned with planes of proton scattering!

Correlation of  $q\bar{q}$  and proton scattering planes:  $\sim \cos^2 \Delta\phi$

# Angular correlation $\Delta\phi$ between the proton scattering plane and quark-antiquark production plane

$$\frac{dN}{d\Delta\phi}(\Delta\phi, x, Q^2, \mathcal{M}_{q\bar{q}}^2)$$



$$x = \frac{k_{P'}^+}{k_P^+} = 0.5$$

$$\mathcal{M}_{q\bar{q}} = 8 \text{ GeV}$$

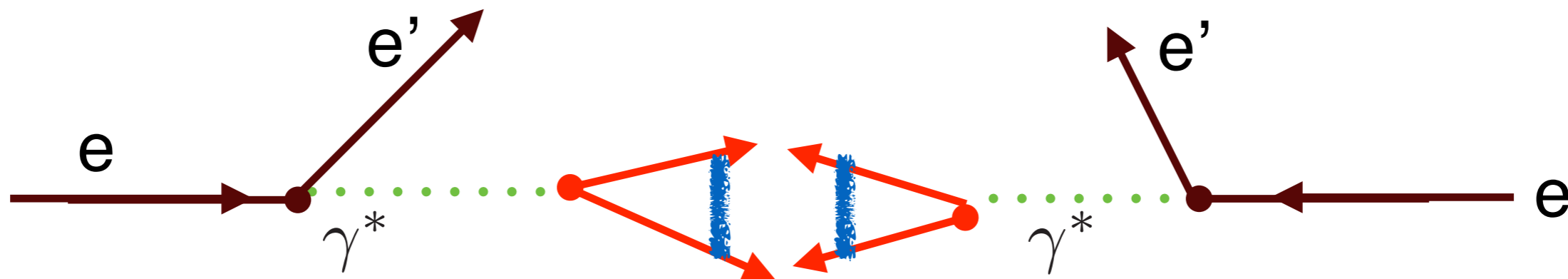
$$Q^2 = 0.94 \text{ GeV}^2$$

(preliminary)

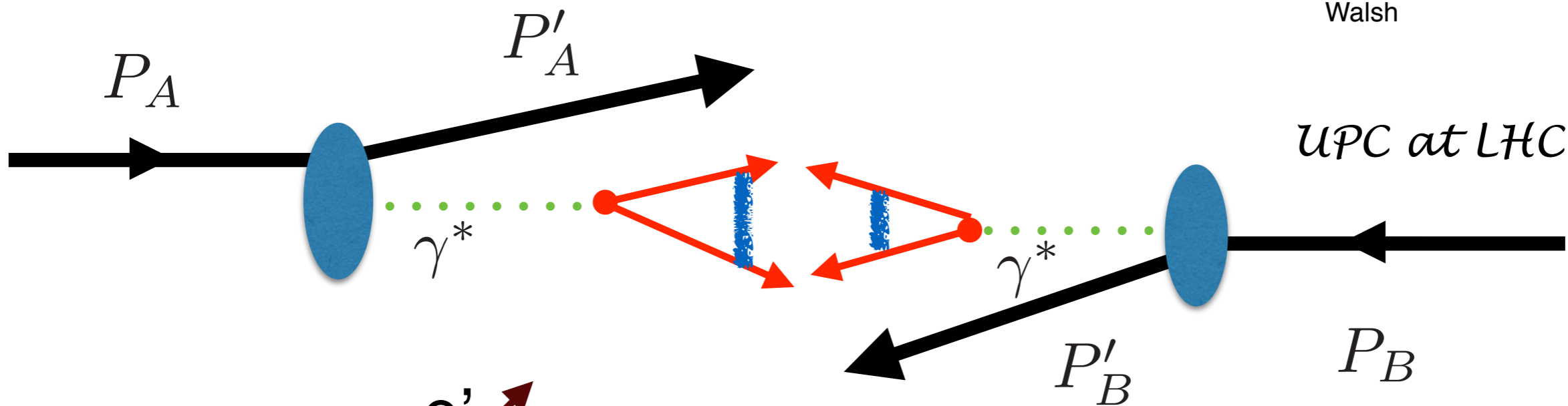
# Collisions of Gluonic Strings in Ultra-Peripheral Collisions

- **Virtual photon polarization correlates quark-antiquark plane with the proton scattering planes**
- **quark-antiquark plane aligned with proton scattering plane  $\sim \cos^2 \Delta\phi$**
- **maximum hadron multiplicity from flux tubes of colliding strings between two aligned quark-antiquark pairs**
- **maximum hadron multiplicity produced when both protons scatter in same plane!**
- **minimum hadron multiplicity when protons scatter at orthogonal angles  $\Delta\phi = \pi/2$**
- **quark-antiquark pair distributions determined from each virtual photon LFWF**
- **Strangeness and charm enhancements**

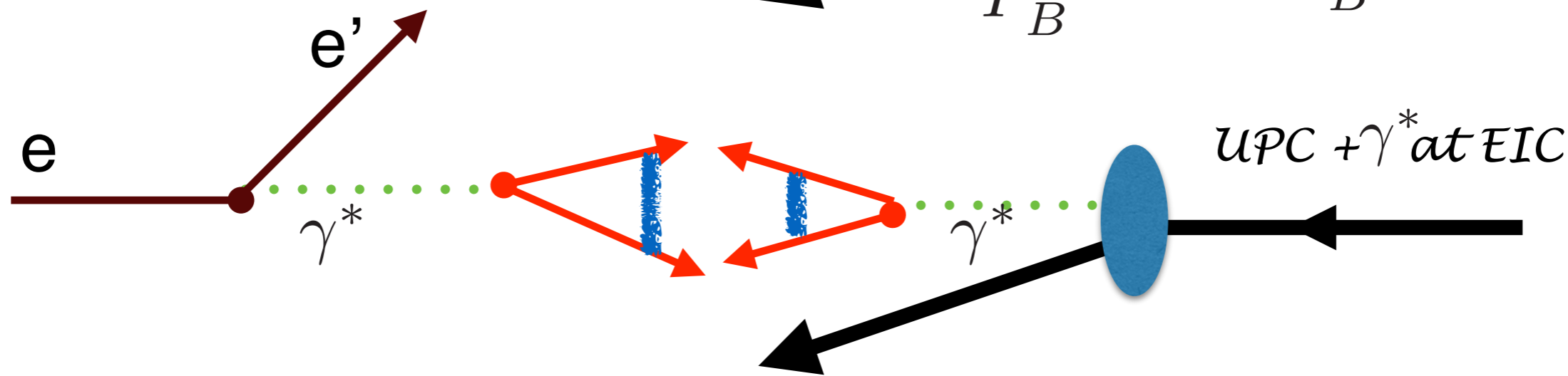
# Collisions of Aligned Flux Tubes in Photon-Photon and UPC Interactions



Kinoshita, Terazawa, sjb  
Budnev, Ginzburg, Meledin, Serbo  
Walsh



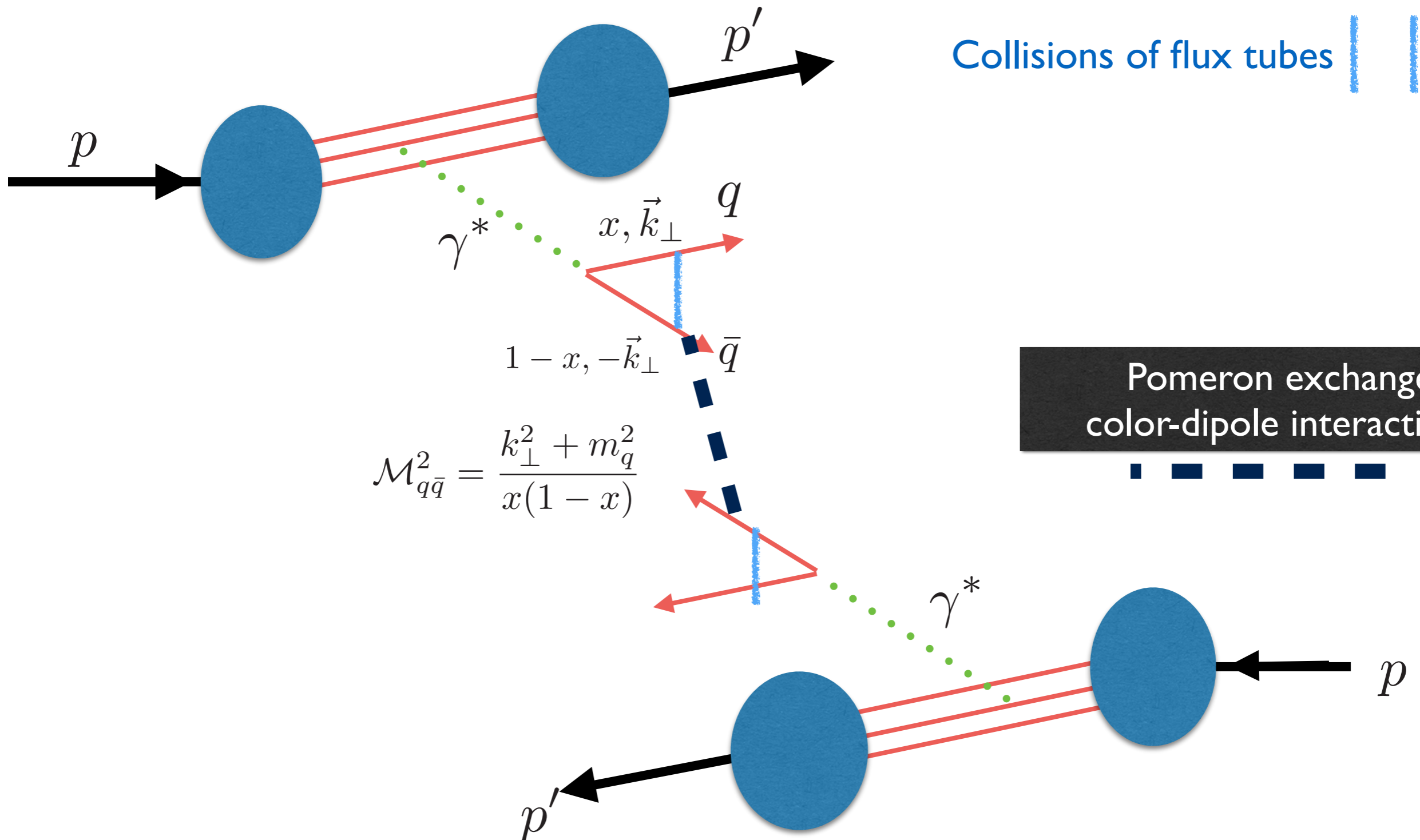
*UPC at LHC*



*UPC +  $\gamma^*$  at EIC*

# Ridge creation in Ultra-Peripheral pp scattering

$$pp \rightarrow \gamma^* \gamma^* p' p' \rightarrow X p' p'$$



Estimate of total cross section:  $\sigma_{\text{UPC}}(pp \rightarrow p' p' \gamma^* \gamma^* \rightarrow p' p' X) \sim 5 \text{ pb}$

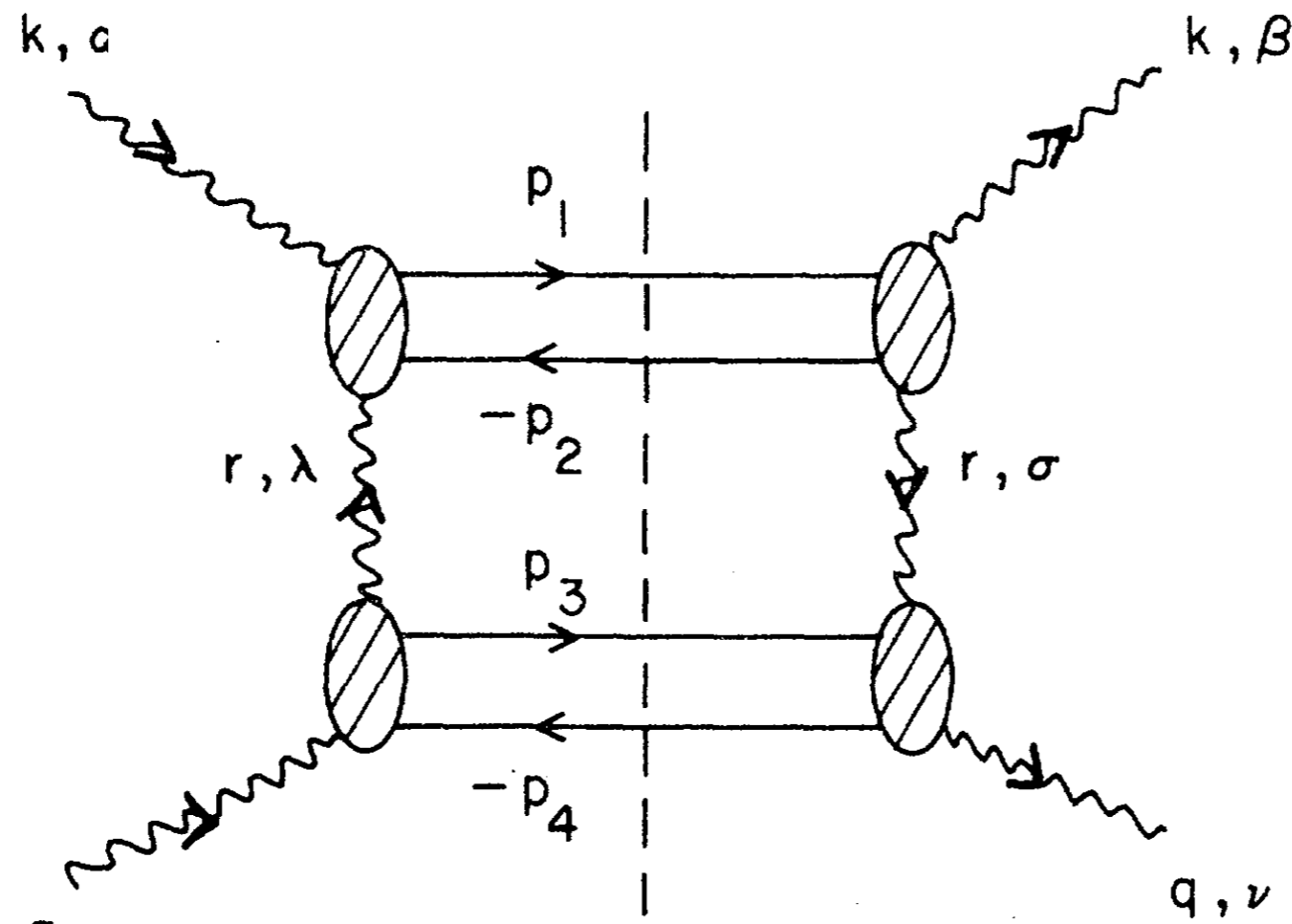
# QED Analog

$$e^- e^+ \rightarrow e^- \gamma^* e^+ \gamma^* \rightarrow e^- (\mu^+ \mu^-) e^+ (\mu^+ \mu^-)$$

## Role of $\gamma+\gamma \rightarrow e^+e^-+e^+e^-$ in Photoproduction, Colliding Beams, and Cosmic Photon Absorption

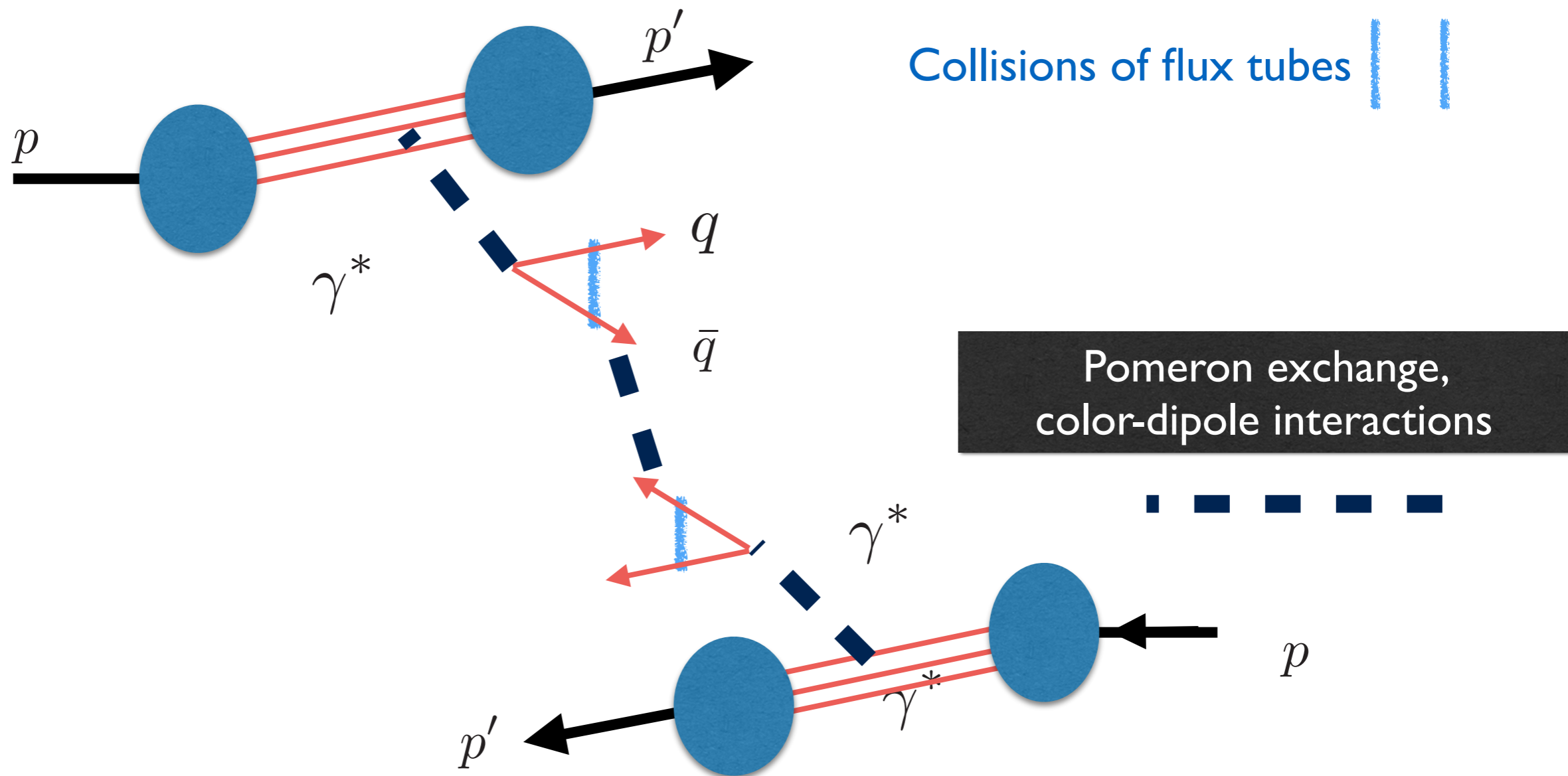
R. W. Brown, W. F. Hunt, K. O. Mikaelian, and I. J. Muzinich

Phys. Rev. D 8, 3083 (1973)



# Ridge creation in Doubly Diffractive $pp$ scattering

$$\sigma_{\text{DD}}(pp \rightarrow p'p'X)$$



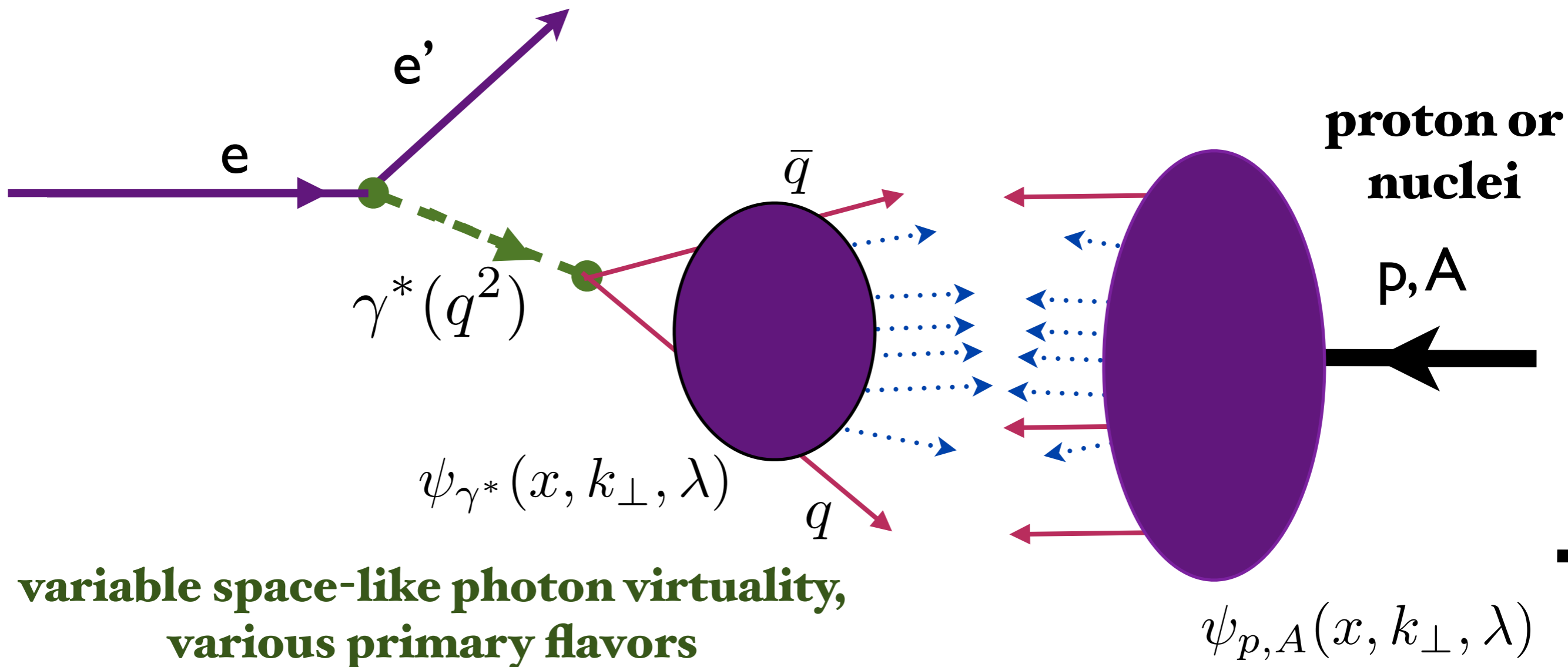
Estimate double diffractive cross section:

$$\sigma_{\text{DD}}(pp \rightarrow p'p'X) \sim \frac{1}{\alpha^4} \sigma_{\text{UPC}}(pp \rightarrow p'p'\gamma^*\gamma^* \rightarrow p'p'X) \sim 50 \mu\text{b}$$



# Electron-Ion Colliders: Virtual Photon-Ion Collider

*Perspective from the e-p collider frame*

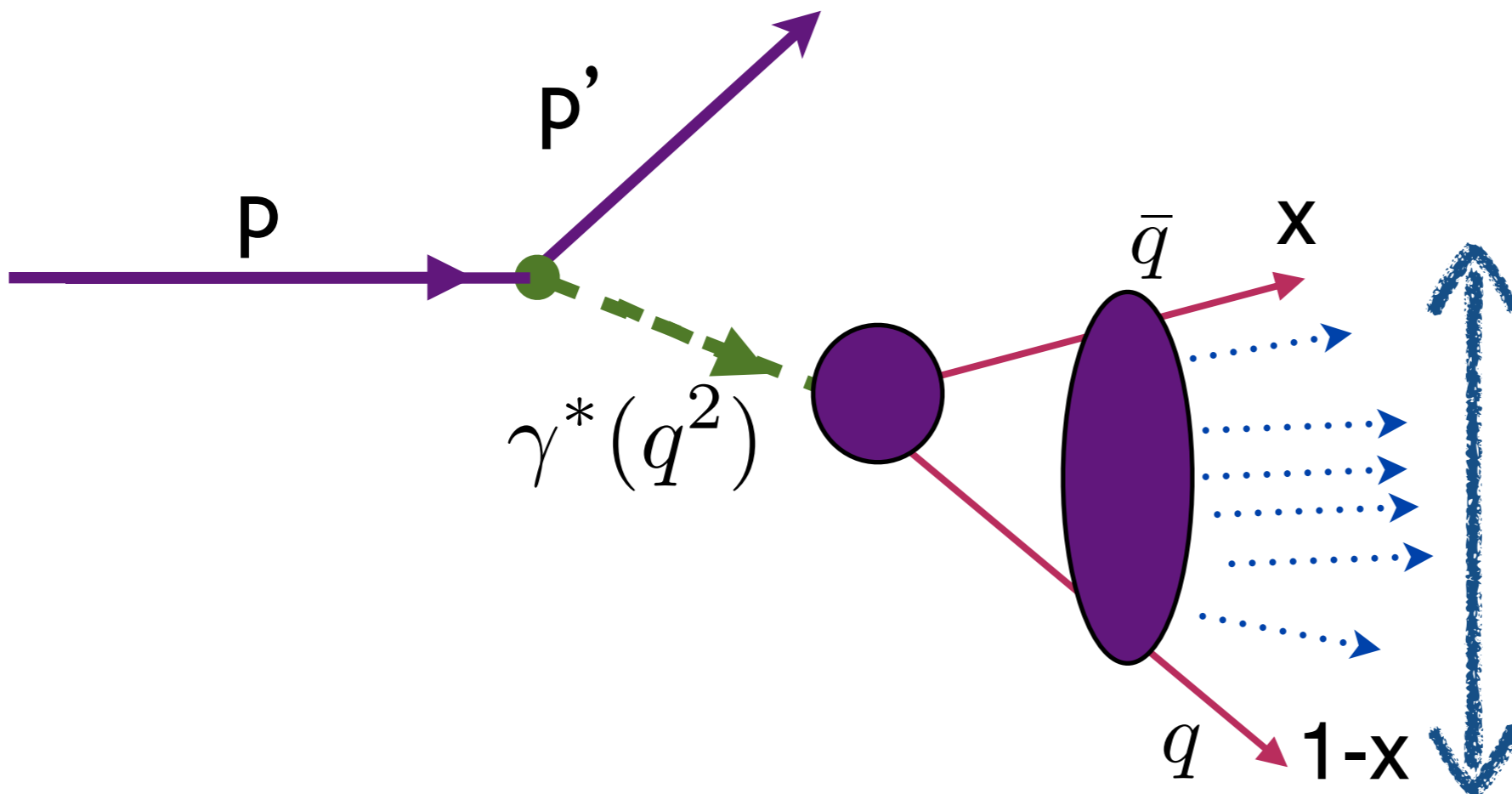


*$\bar{q} q$  plane aligned with lepton scattering plane  $\sim \cos^2\phi$*

*Front-surface nuclear dynamics: shadowing/antishadowing*

# Characteristics of the quark-antiquark flux tube

*Planar structure reflects color-confinement*



*Evolution in Light-Front Time*

$$\tau = x^+ = t + z/c$$

**Off-shell in  $P^- = P^0 + P^z$  and invariant mass**

$$\mathcal{M}_{q\bar{q}}^2 = \frac{k_{\perp}^2 + m_q^2}{x(1-x)}$$

Connection of Gluon Density to Color Confinement  
 Related to Trace (Conformal) Anomaly  $\langle H | G^2 | H \rangle$

# Characteristics of the quark-antiquark flux tube

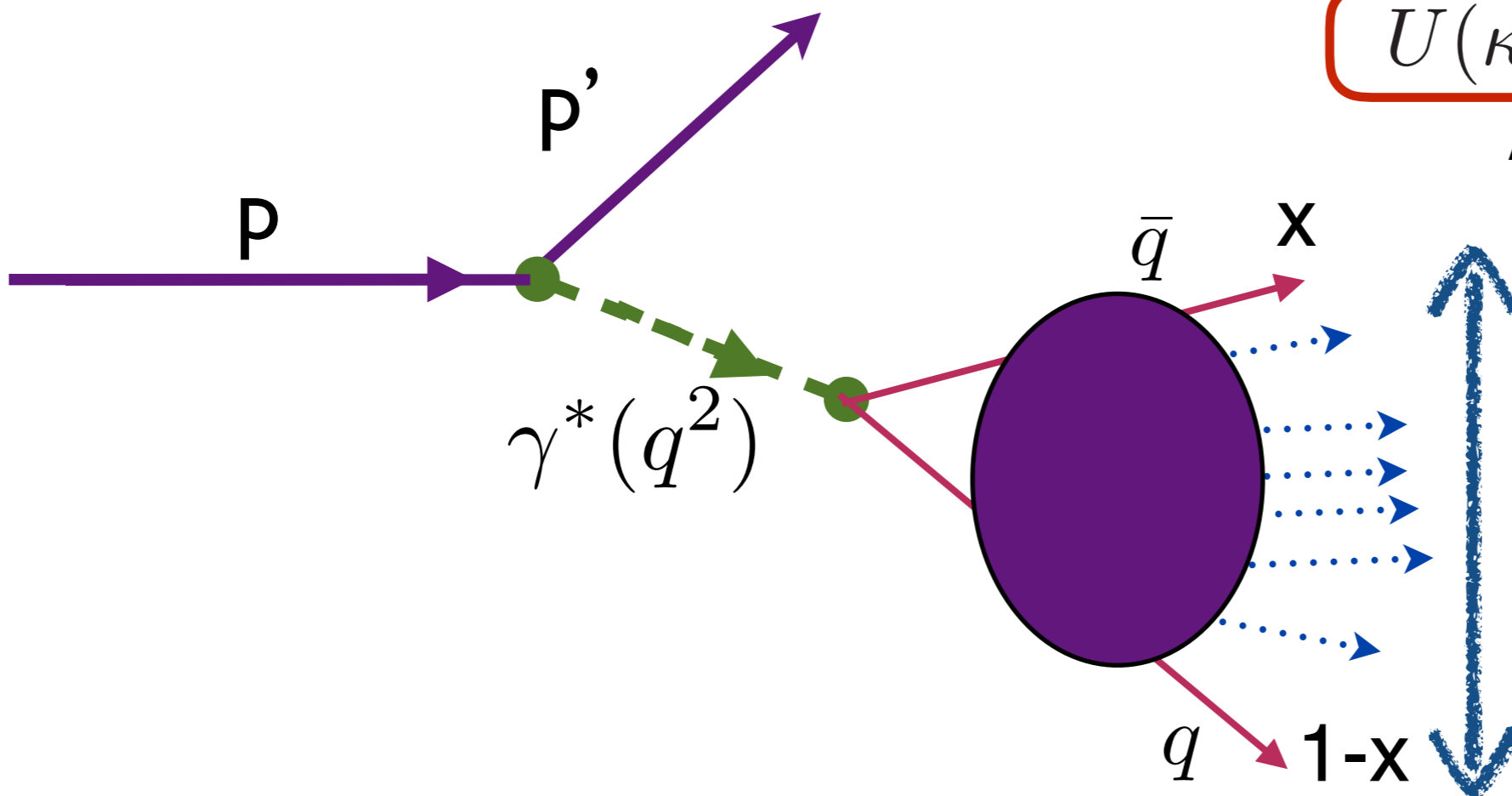
$$\psi(x, b_{\perp}^2, Q^2) \propto \exp -[b_{\perp}^2 x(1-x)(\kappa^2 + Q^2)]$$

*Planar structure reflects color-confinement potential*

$$U(\kappa^2) = \kappa^4 b_{\perp}^2 x(1-x)$$

AdS/QCD + Light-Front Holography

de Teramond, Dosch, Lorce, sjb



$$\langle b_{\perp}^2 \rangle \propto \frac{1}{x(1-x)(\kappa^2 + Q^2)}$$

massless quarks

$$\mathcal{M}^2 = \frac{k_{\perp}^2}{x(1-x)} \propto \frac{1}{b_{\perp}^2 x(1-x)}$$

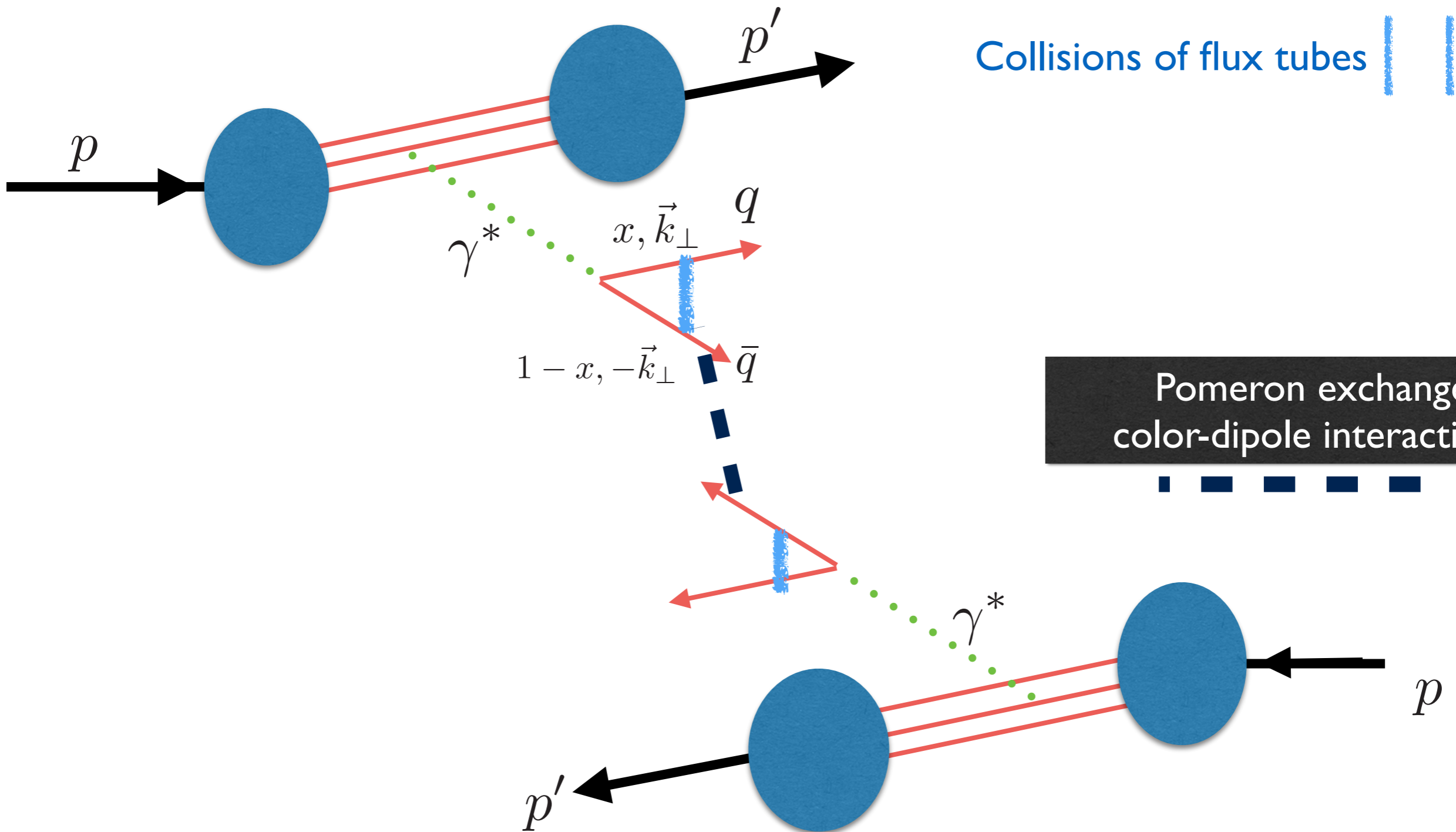
$$\langle b_{\perp}^2 \rangle \rightarrow \infty \text{ if } x \rightarrow 0, 1$$

$$\langle b_{\perp}^2 \rangle \propto \frac{1}{x(1-x)(\kappa^2 + Q^2) + m_q^2}$$

massive quarks

# Ridge creation in Ultra-Peripheral pp scattering

$$pp \rightarrow \gamma^* \gamma^* p' p' \rightarrow X p' p'$$



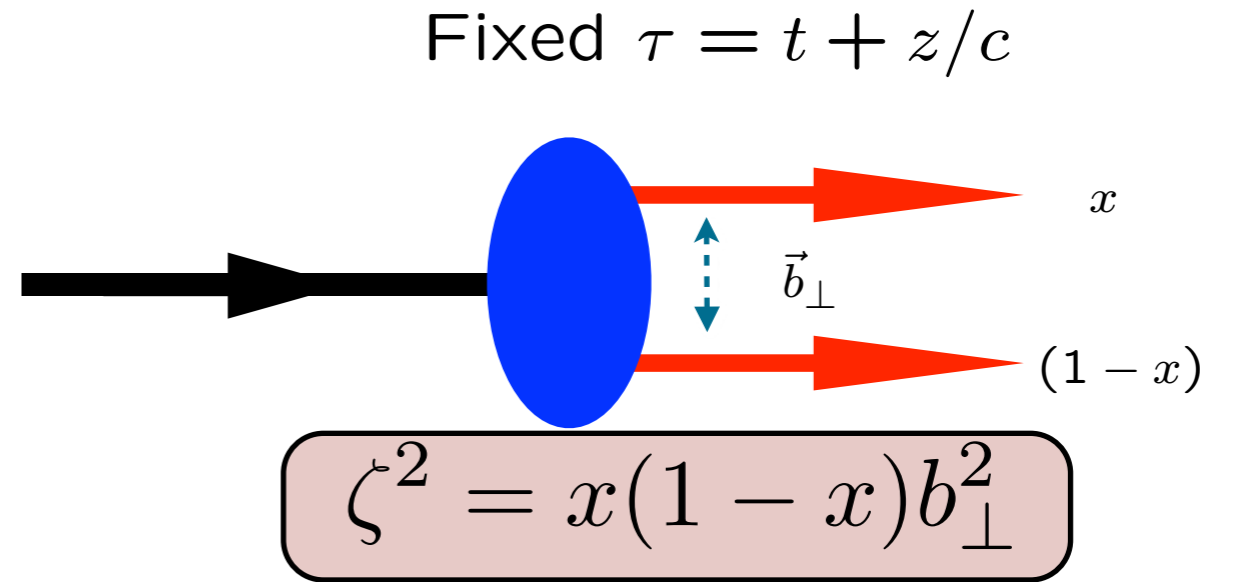
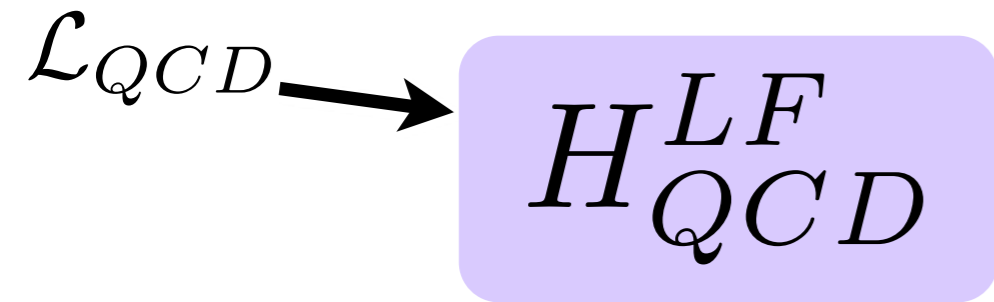
Important Issue: Do interactions modify the planar orientations?

# *Color Confinement and Gluonic Flux Tubes*

## ***Unique Confinement Potential!***

Connection of Gluon Density to Color Confinement  
Related to Trace (Conformal) Anomaly  $\langle H|G^2|H \rangle$

# Light-Front QCD



$$(H_{LF}^0 + H_{LF}^I) |\Psi\rangle = M^2 |\Psi\rangle$$

*Coupled Fock states*

*Eliminate higher Fock states and retarded interactions*

$$\left[ \frac{\vec{k}_{\perp}^2 + m^2}{x(1-x)} + V_{\text{eff}}^{LF} \right] \psi_{LF}(x, \vec{k}_{\perp}) = M^2 \psi_{LF}(x, \vec{k}_{\perp})$$

*Effective two-particle equation*

$$\left[ -\frac{d^2}{d\zeta^2} - \frac{1-4L^2}{4\zeta^2} + U(\zeta) \right] \psi(\zeta) = M^2 \psi(\zeta)$$

*Azimuthal Basis  $\zeta, \phi$*

$$m_q = 0$$

**Single variable  $\zeta$**

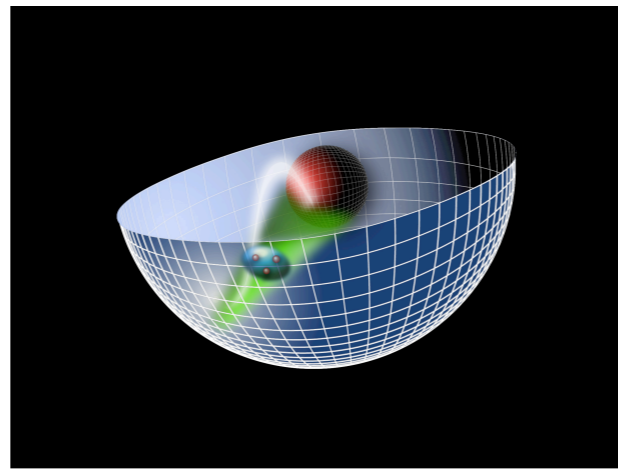
**AdS/QCD:**

$$U(\zeta) = \kappa^4 \zeta^2 + 2\kappa^2 (L + S - 1)$$

*Confining AdS/QCD potential!*

*Semiclassical first approximation to QCD*

*Sums an infinite # diagrams*



*AdS/QCD  
Soft-Wall Model*  
 $e^{\varphi(z)} = e^{+\kappa^2 z^2}$

*Light-Front Holography*

$$\zeta^2 = x(1-x)b_{\perp}^2.$$

$$\left[ -\frac{d^2}{d\zeta^2} + \frac{1-4L^2}{4\zeta^2} + U(\zeta) \right] \psi(\zeta) = \mathcal{M}^2 \psi(\zeta)$$



***Light-Front Schrödinger Equation***

$$U(\zeta) = \kappa^4 \zeta^2 + 2\kappa^2(L + S - 1)$$

$$\kappa \simeq 0.5 \text{ GeV}$$

***Unique Confinement Potential!***  
*Preserves Conformal Symmetry of the action*

***Confinement scale:***

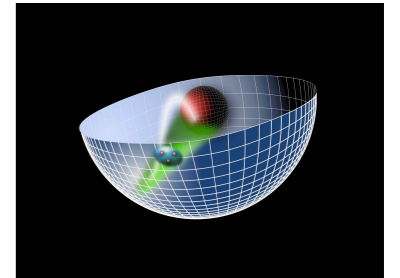
$$1/\kappa \simeq 1/3 \text{ fm}$$

***Scale can appear in Hamiltonian and EQM without affecting conformal invariance of action!***

- **de Alfaro, Fubini, Furlan:**
- **Fubini, Rabinovici:**

# Dilaton-Modified AdS/QCD

$$ds^2 = e^{\varphi(z)} \frac{R^2}{z^2} (\eta_{\mu\nu} x^\mu x^\nu - dz^2)$$

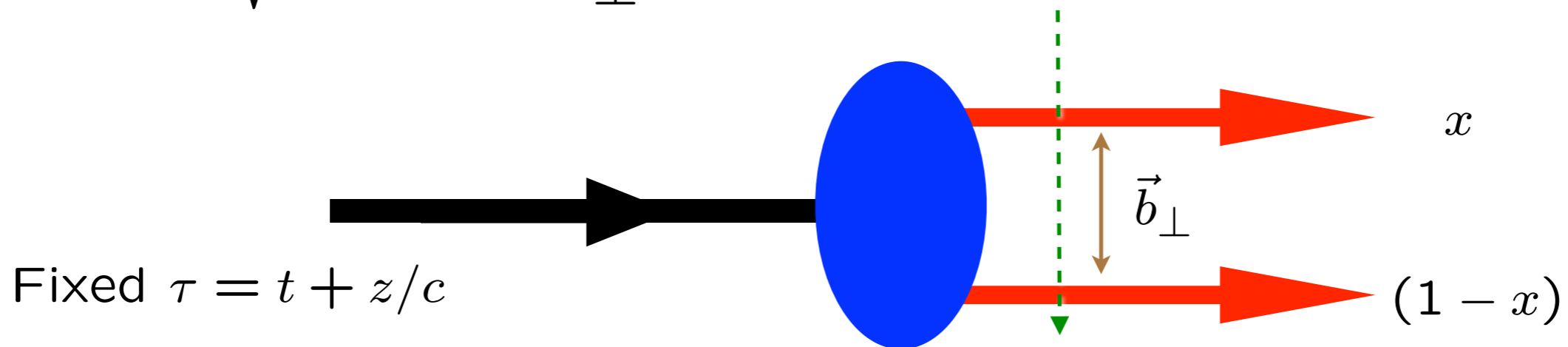


- **Soft-wall dilaton profile breaks conformal invariance**  $e^{\varphi(z)} = e^{+\kappa^2 z^2}$
- **Color Confinement in z**
- **Introduces confinement scale  $\kappa$**
- **Uses AdS<sub>5</sub> as template for conformal theory**



$LF(3+1) \longleftrightarrow AdS_5$ 

# Light-Front Holographic Dictionary

 $\psi(x, \vec{b}_\perp) \longleftrightarrow \phi(z)$ 
 $\zeta = \sqrt{x(1-x)} \vec{b}_\perp^2 \longleftrightarrow z$ 


$$\psi(x, \zeta) = \sqrt{x(1-x)} \zeta^{-1/2} \phi(\zeta)$$

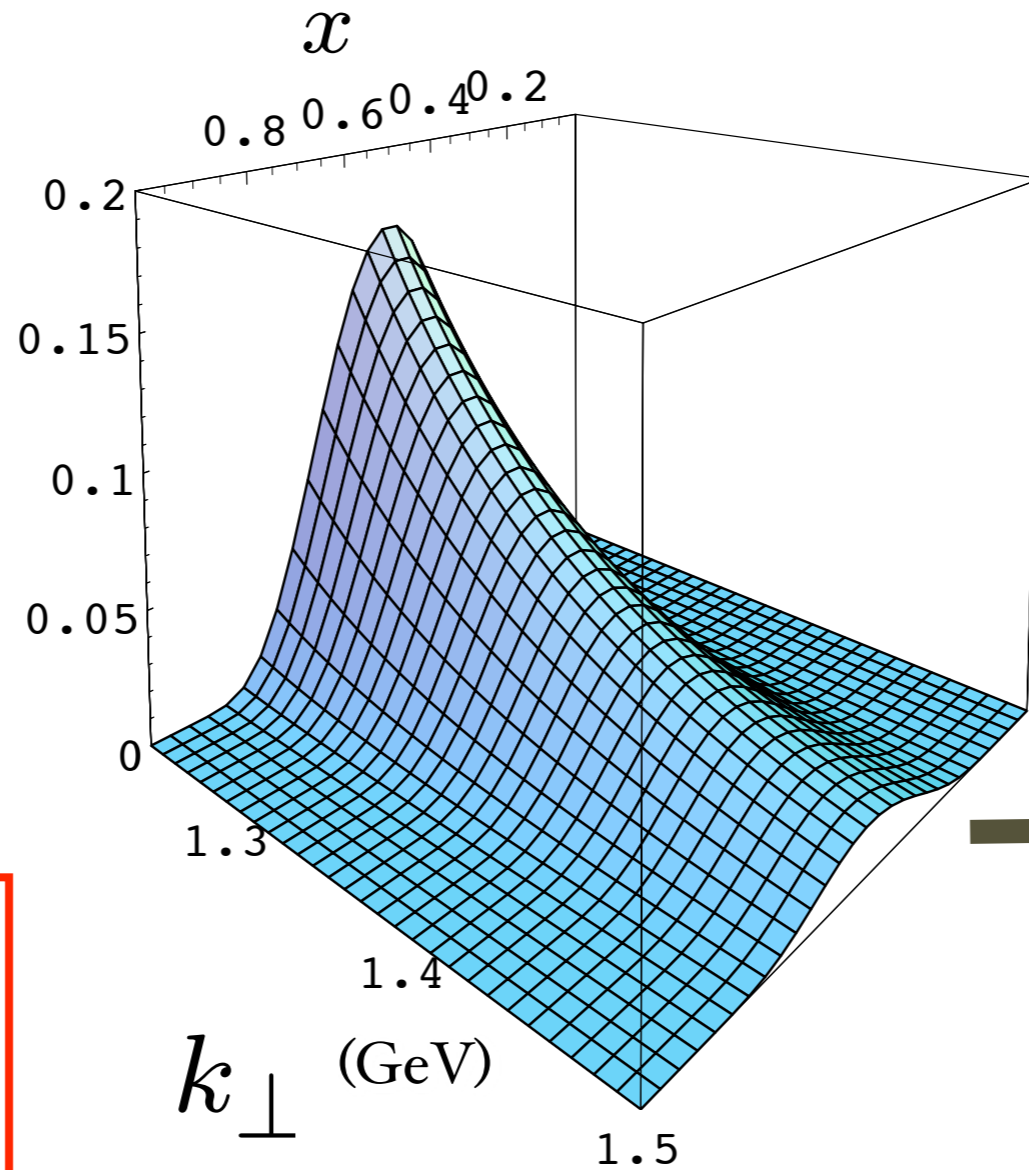
$$(\mu R)^2 = L^2 - (J - 2)^2$$

**Light-Front Holography:** Unique mapping derived from equality of LF and AdS formula for EM and gravitational current matrix elements and identical equations of motion

# Prediction from AdS/QCD: Meson LFWF

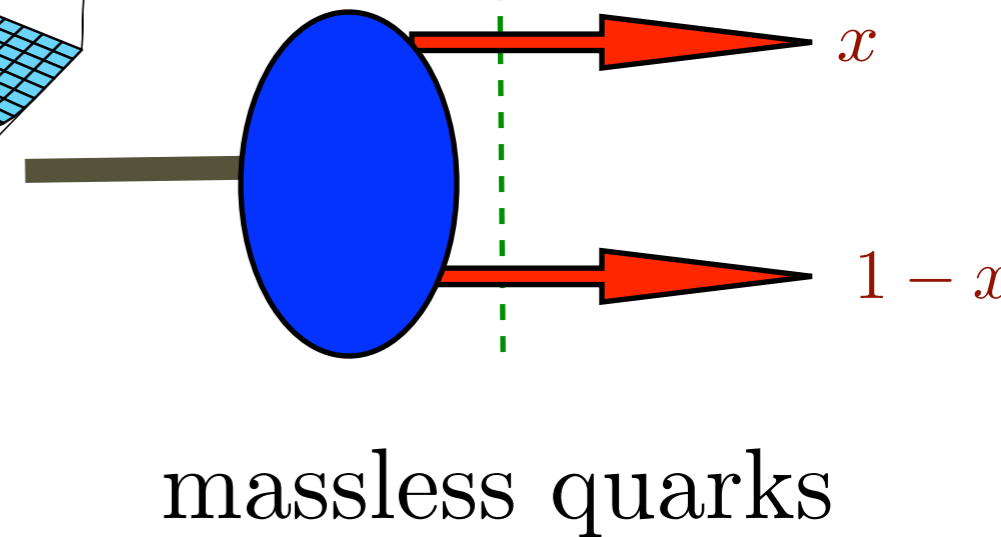
$$e^{\varphi(z)} = e^{+\kappa^2 z}$$

$$\psi_M(x, k_{\perp}^2)$$



de Teramond,  
Cao, sjb

“Soft Wall”  
model



**Note coupling**

$$k_{\perp}^2, x$$

$$\psi_M(x, k_{\perp}) = \frac{4\pi}{\kappa \sqrt{x(1-x)}} e^{-\frac{k_{\perp}^2}{2\kappa^2 x(1-x)}}$$

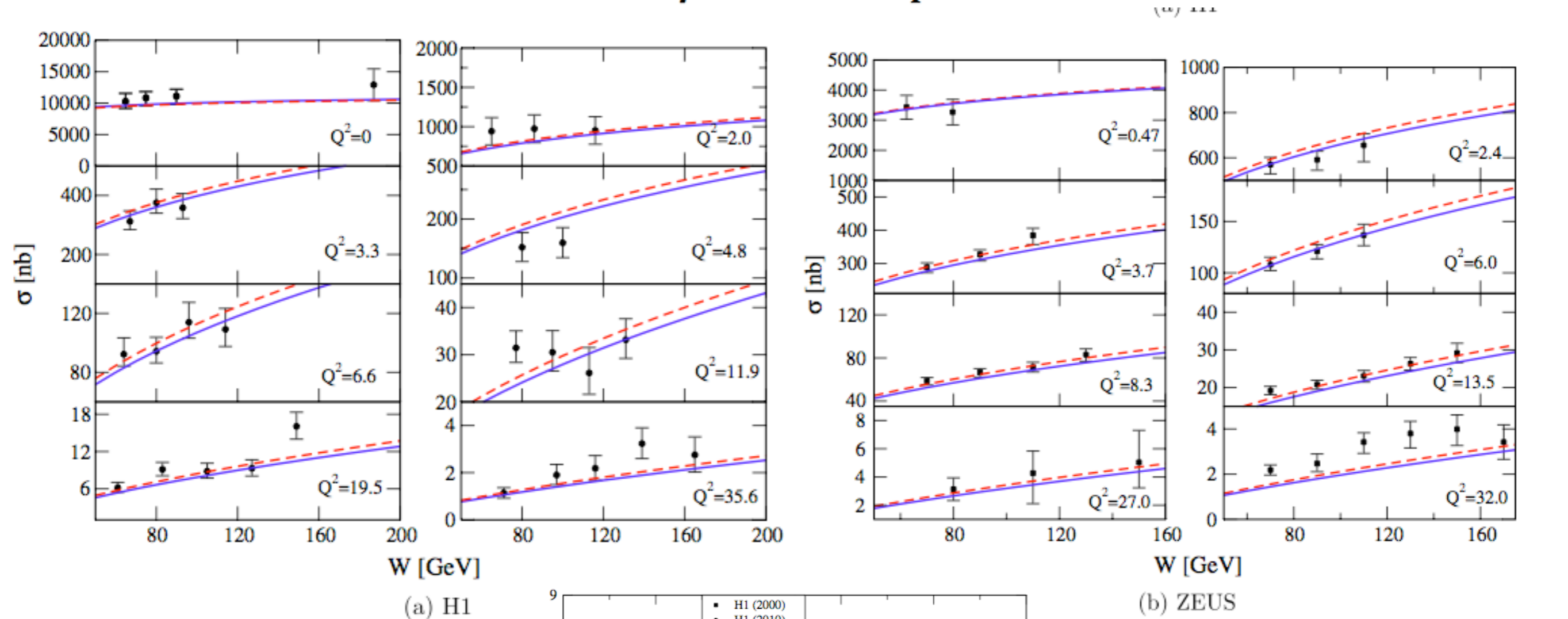
$$\phi_{\pi}(x) = \frac{4}{\sqrt{3}\pi} f_{\pi} \sqrt{x(1-x)}$$

$$f_{\pi} = \sqrt{P_{q\bar{q}}} \frac{\sqrt{3}}{8} \kappa = 92.4 \text{ MeV}$$

**Same as DSE!** C. D. Roberts et al.

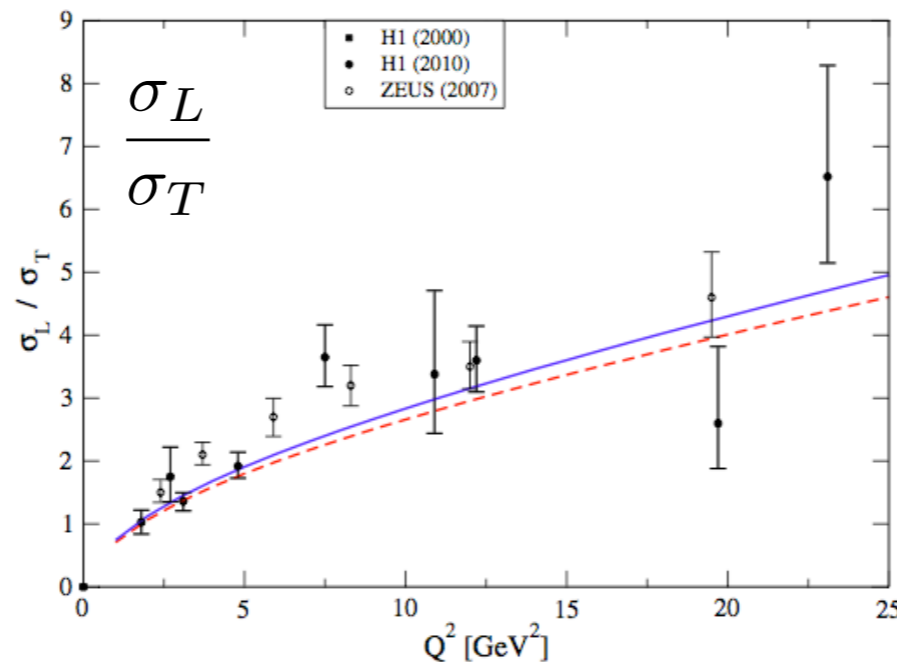
*Provides Connection of Confinement to Hadron Structure*

### AdS/QCD Holographic Wave Function for the $\rho$ Meson and Diffractive $\rho$ Meson Electroproduction

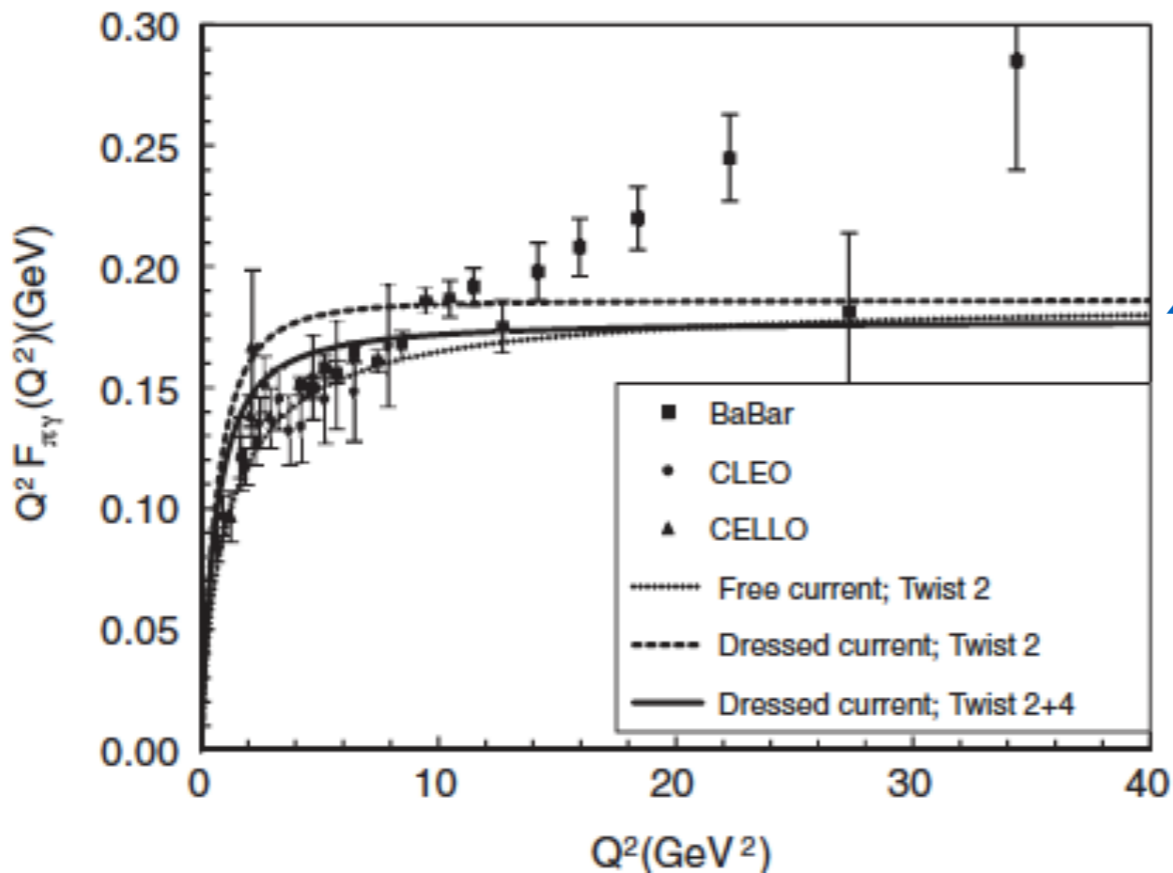


**J. R. Forshaw,  
R. Sandapen**

$$\gamma^* p \rightarrow \rho^0 p'$$



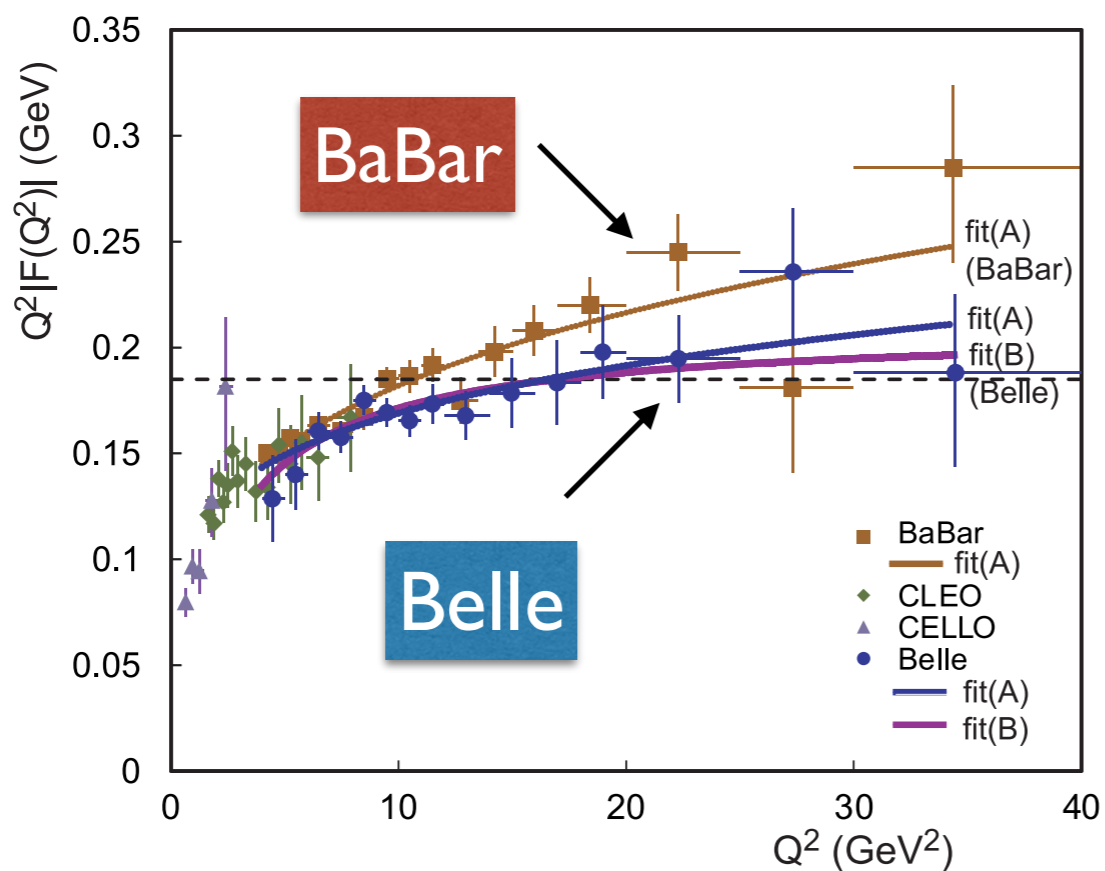
$$\psi_M(x, k_\perp) = \frac{4\pi}{\kappa\sqrt{x(1-x)}} e^{-\frac{k_\perp^2}{2\kappa^2 x(1-x)}}$$



Prediction from AdS/QCD:

$$\phi_\pi(x) = \frac{4}{\sqrt{3}\pi} f_\pi \sqrt{x(1-x)}$$

Cao, de Teramond, sjb

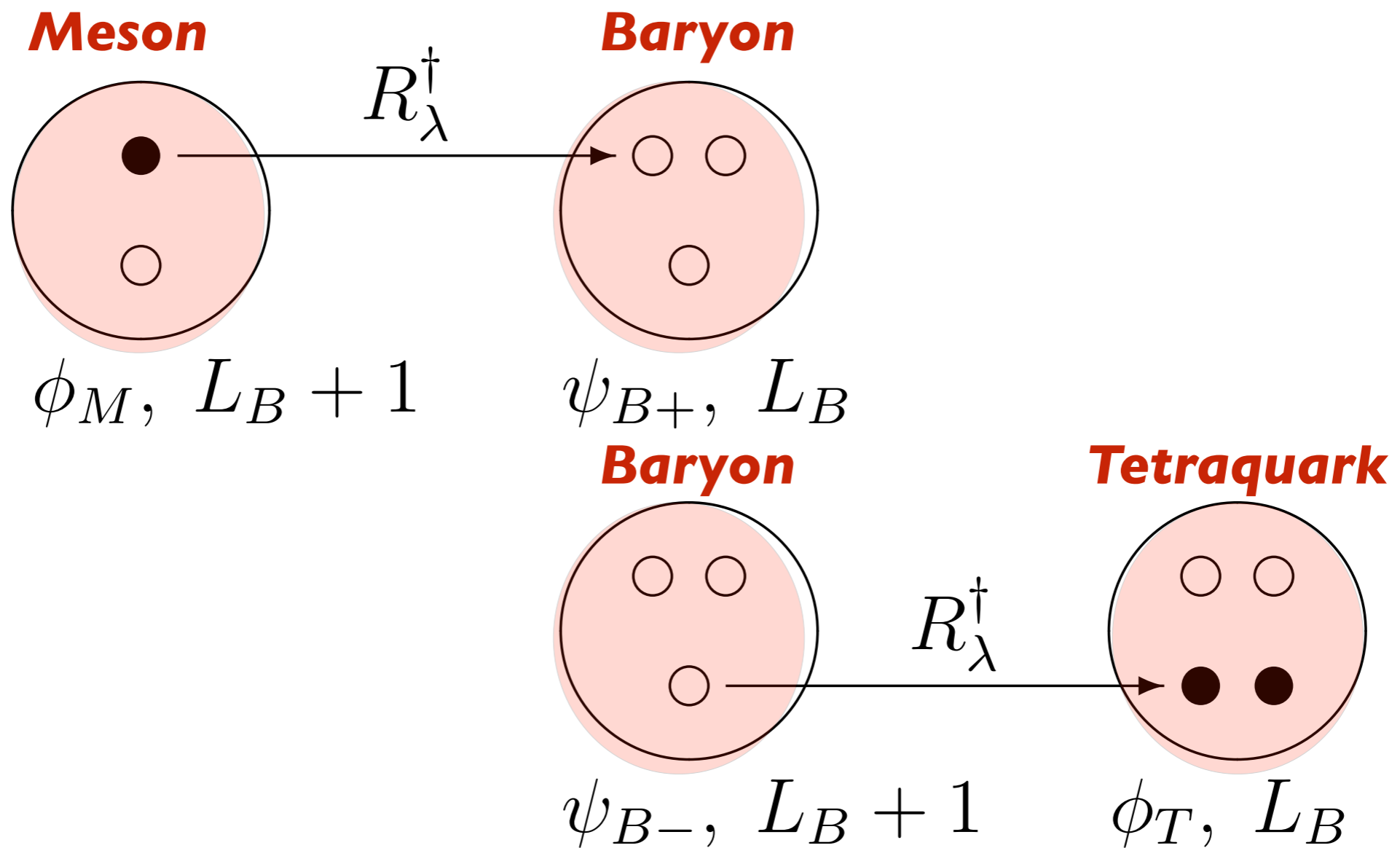


Belle:  
Agreement with  
AdS/QCD and  
pQCD evolution

# Superconformal Algebra

## 2X2 Hadronic Multiplets

Bosons, Fermions with Equal Mass!



Proton: quark + scalar diquark  $|q(qq)\rangle$   
(Equal weight:  $L = 0, L = 1$ )

$$\left( -\partial_{\zeta}^2 + \kappa^4 \zeta^2 + 2\kappa^2(L_B + 1) + \frac{4L_B^2 - 1}{4\zeta^2} \right) \psi_J^+ = M^2 \psi_J^+$$

$$\left( -\partial_{\zeta}^2 + \kappa^4 \zeta^2 + 2\kappa^2 L_B + \frac{4(L_B + 1)^2 - 1}{4\zeta^2} \right) \psi_J^- = M^2 \psi_J^-$$

$$M^2(n, L_B) = 4\kappa^2(n + L_B + 1)$$

**S=1/2, P=+**

*both chiralities*

## Meson Equation

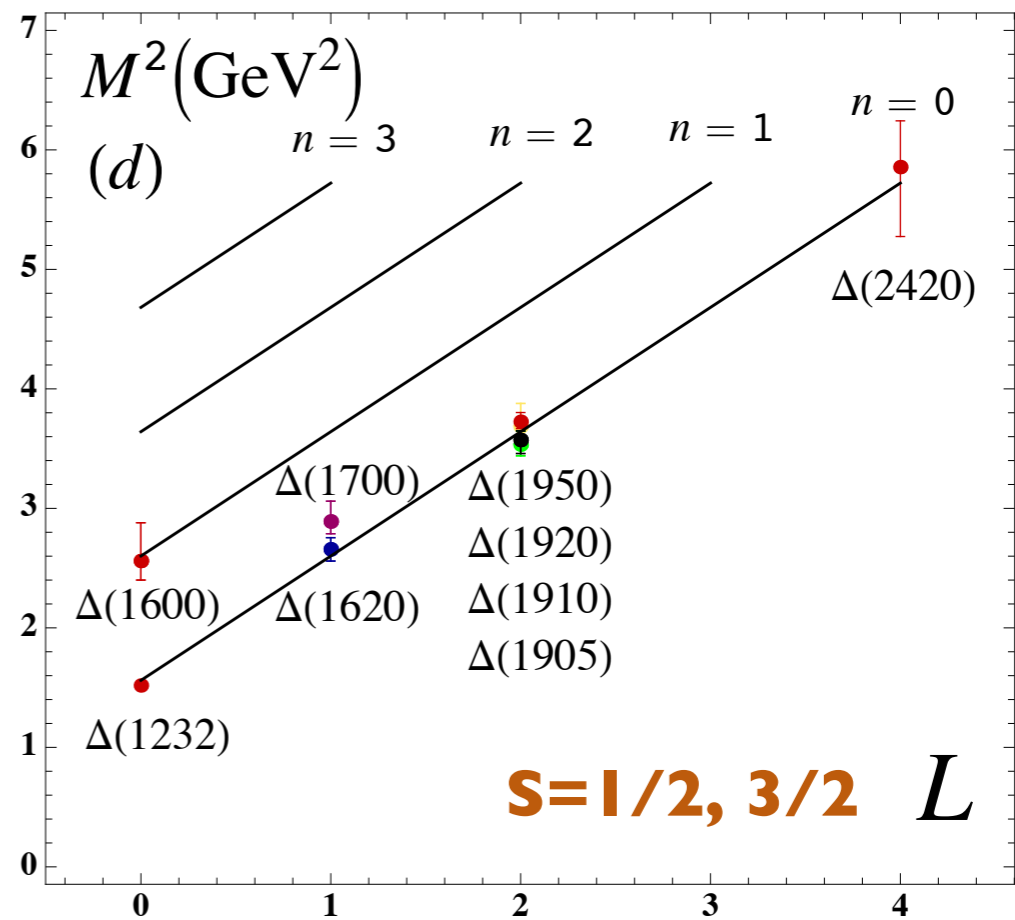
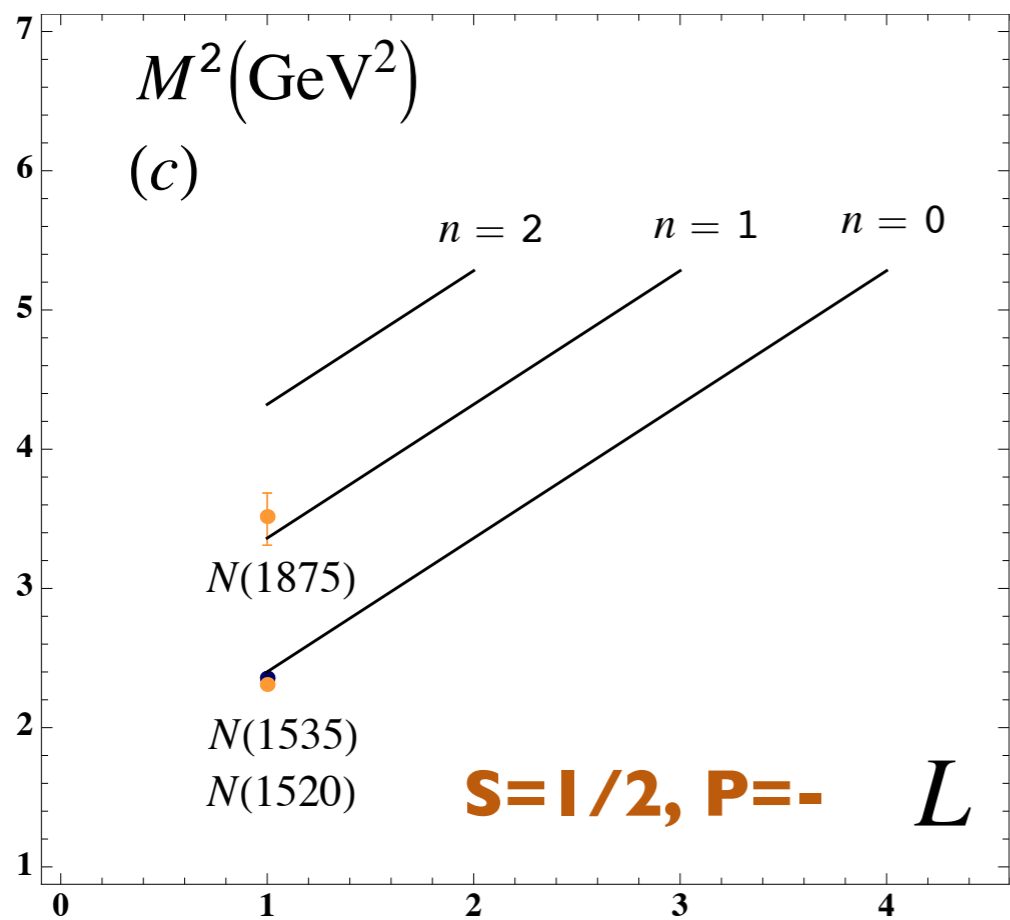
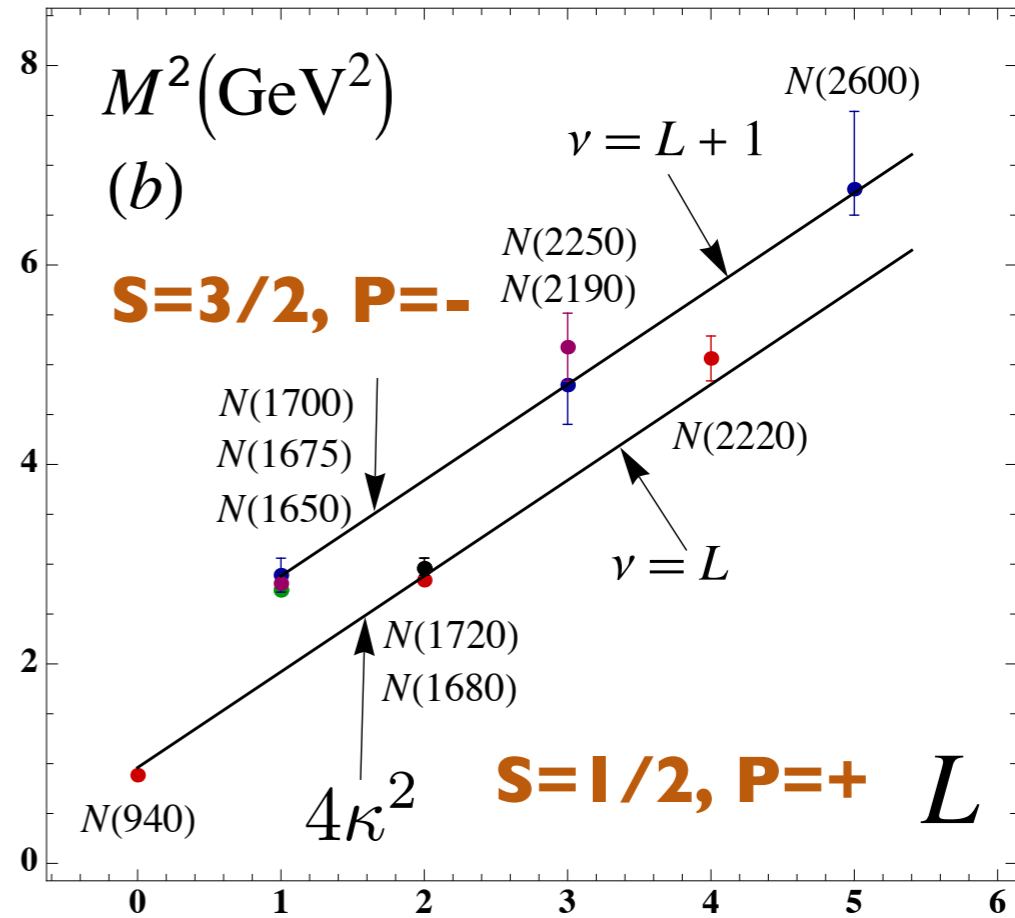
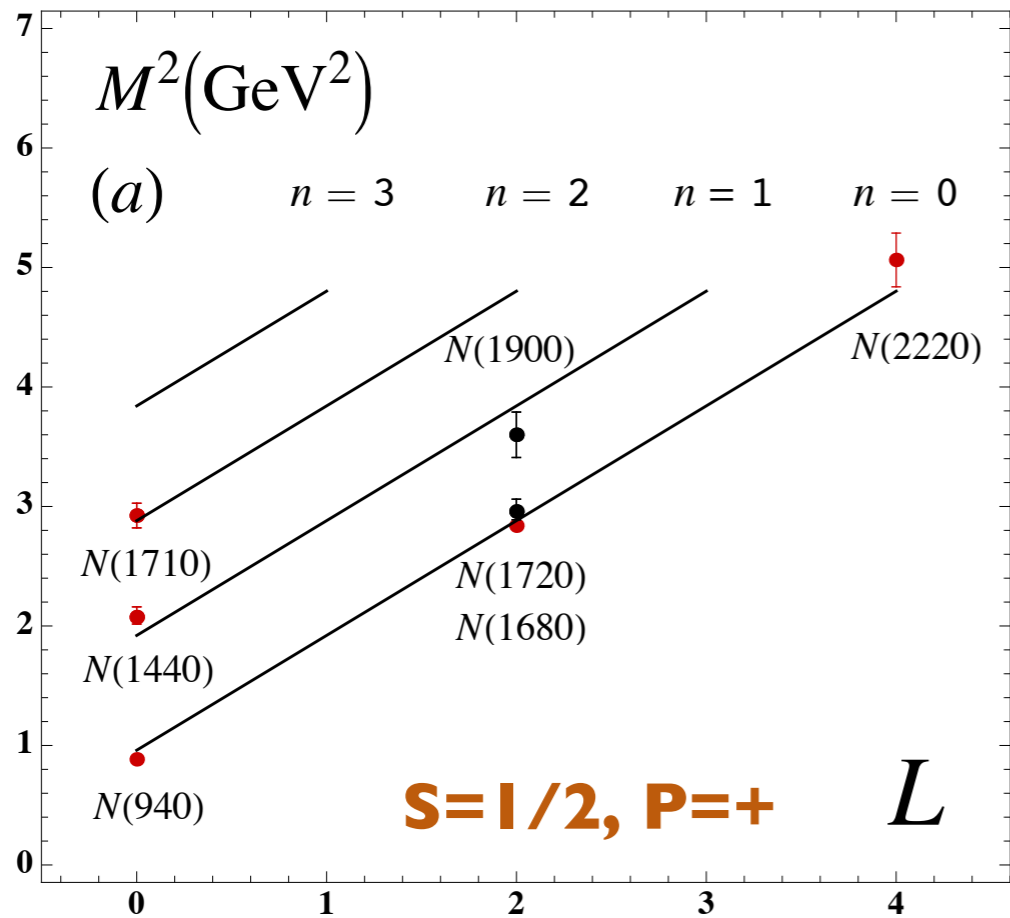
$$\left( -\partial_{\zeta}^2 + \kappa^4 \zeta^2 + 2\kappa^2(J - 1) + \frac{4L_M^2 - 1}{4\zeta^2} \right) \phi_J = M^2 \phi_J$$

$$M^2(n, L_M) = 4\kappa^2(n + L_M)$$

*Same  $\kappa$ !*

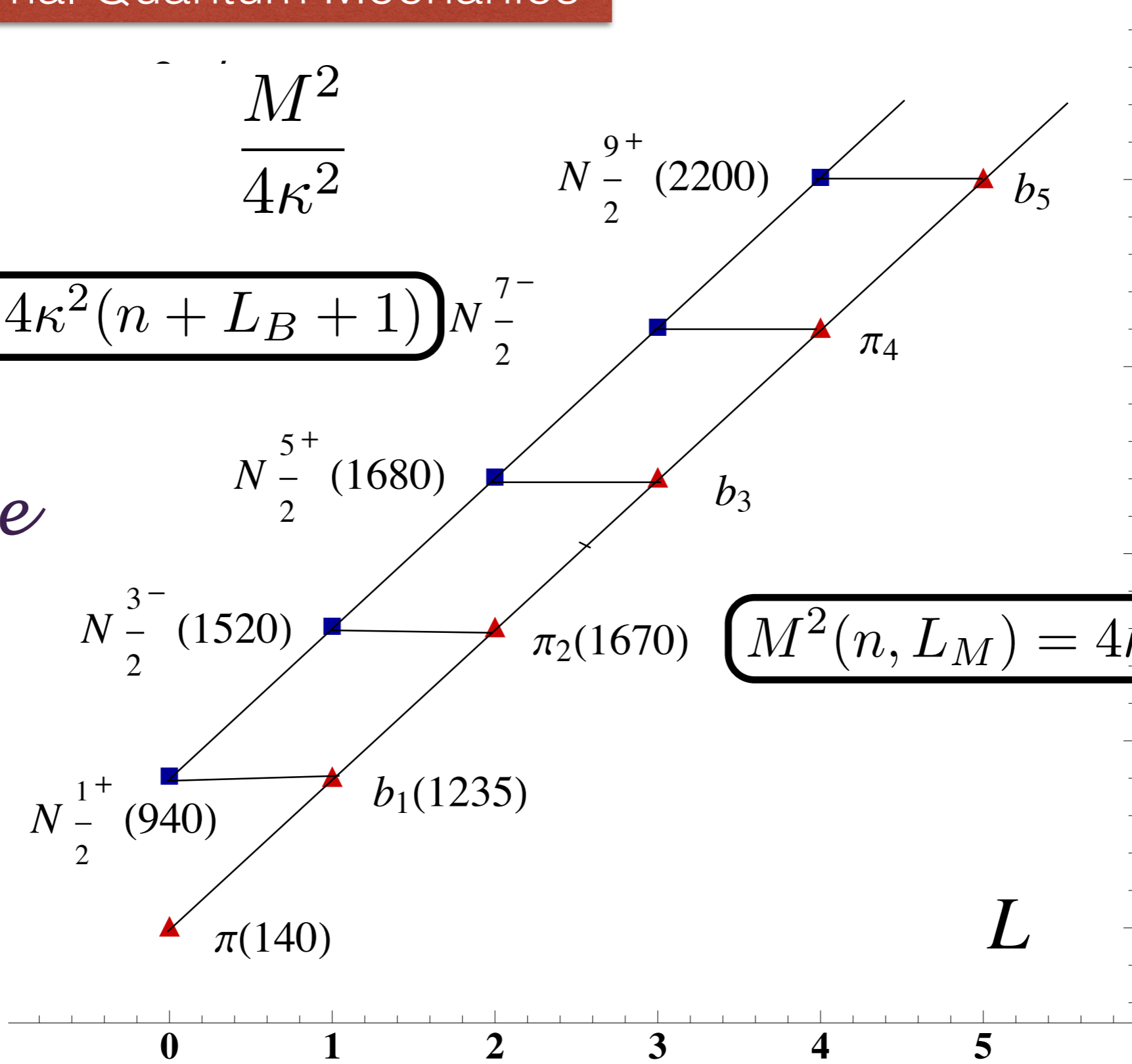
**S=0, I=I Meson is superpartner of S=1/2, I=I Baryon**

**Meson-Baryon Degeneracy for  $L_M=L_B+1$**



$$M^2(n, L_B) = 4\kappa^2(n + L_B + 1)$$

*Same slope*



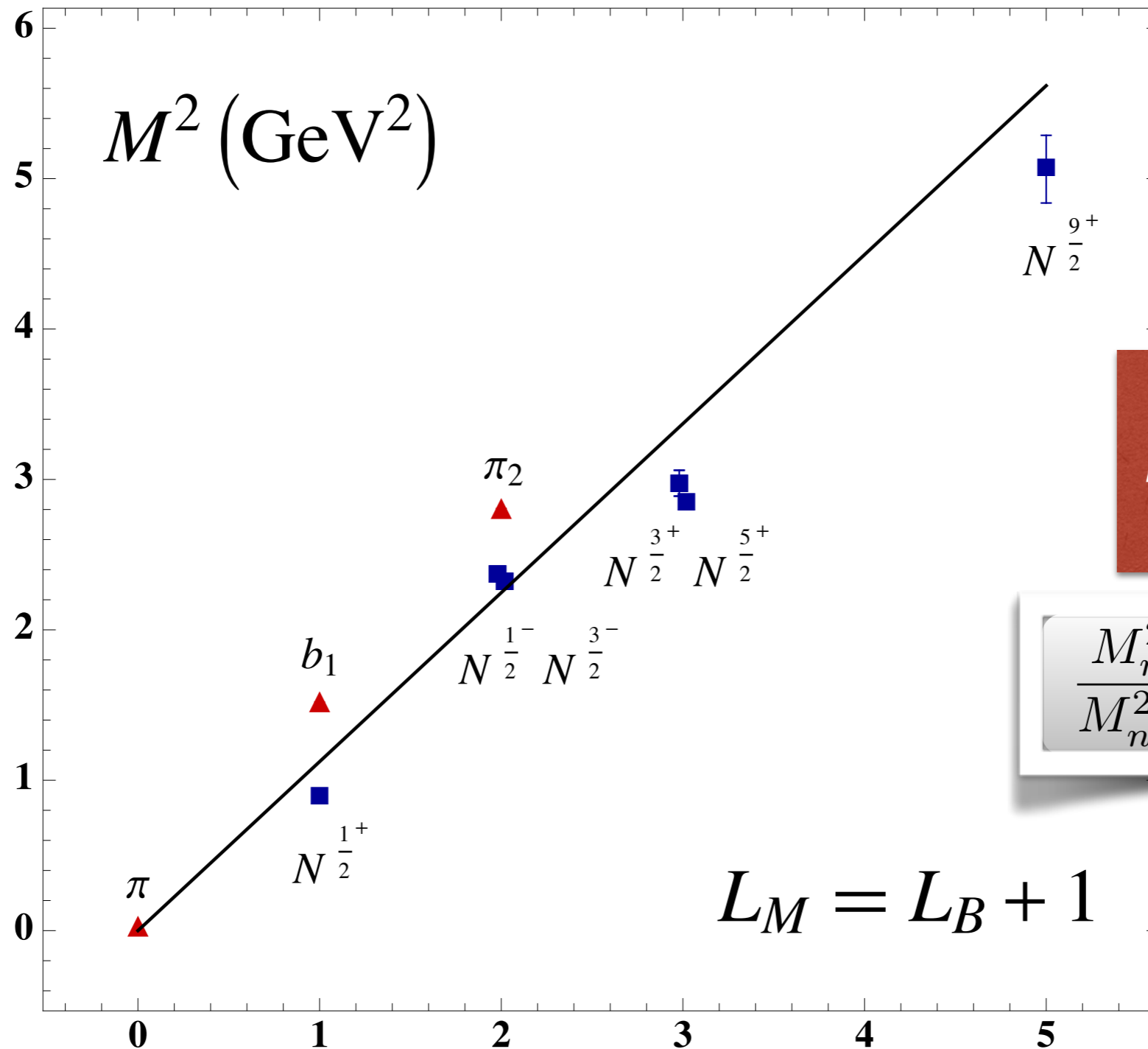
$$M^2(n, L_M) = 4\kappa^2(n + L_M)$$

$$\frac{M_{meson}^2}{M_{nucleon}^2} = \frac{n + L_M}{n + L_B + 1}$$

**Meson-Baryon  
Mass Degeneracy  
for  $L_M=L_B+1$**



# Superconformal AdS Light-Front Holographic QCD (LFHQCD): Identical meson and baryon spectra!



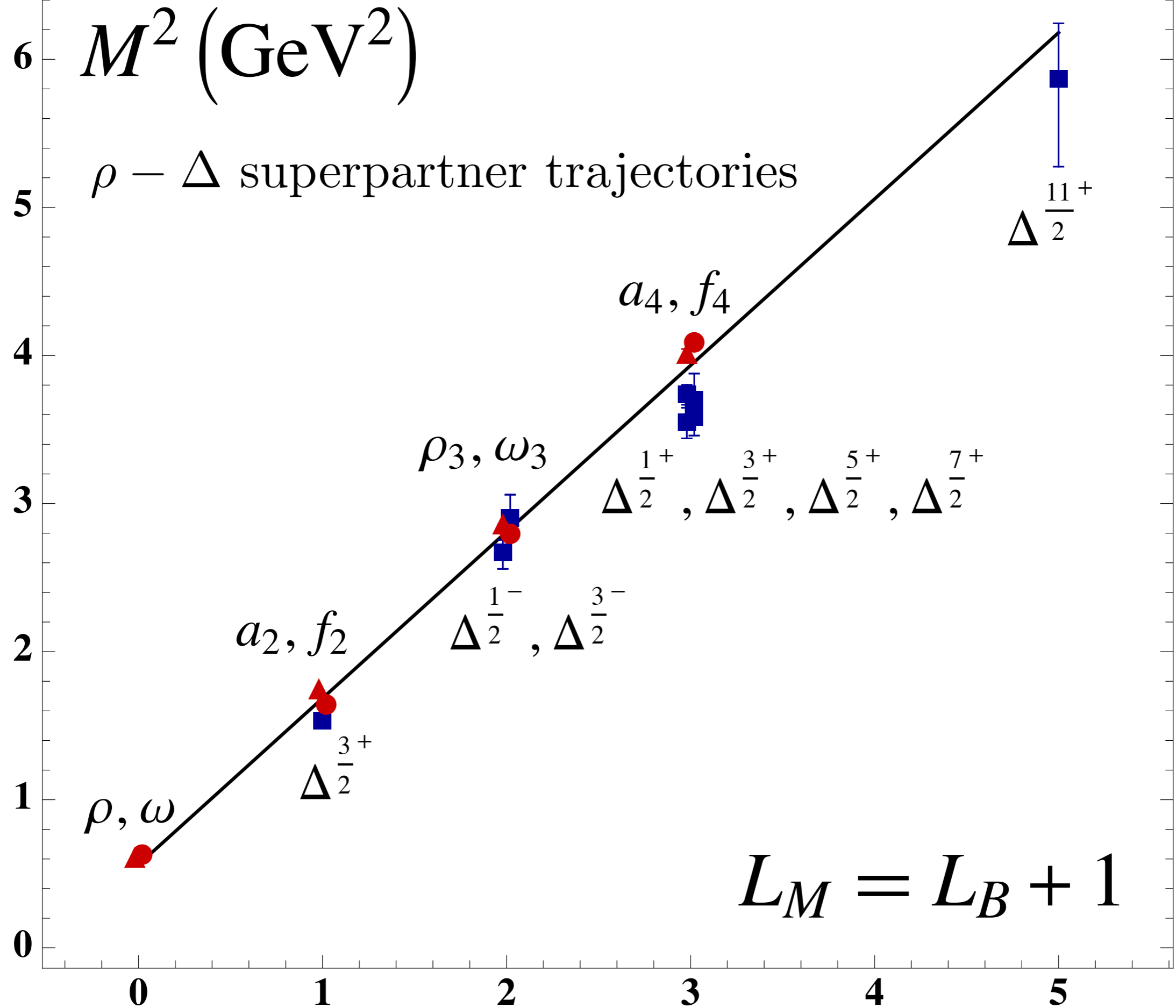
**Meson-Baryon  
Mass Degeneracy  
for  $L_M=L_B+1$**

$$\frac{M_{meson}^2}{M_{nucleon}^2} = \frac{n + L_M}{n + L_B + 1}$$

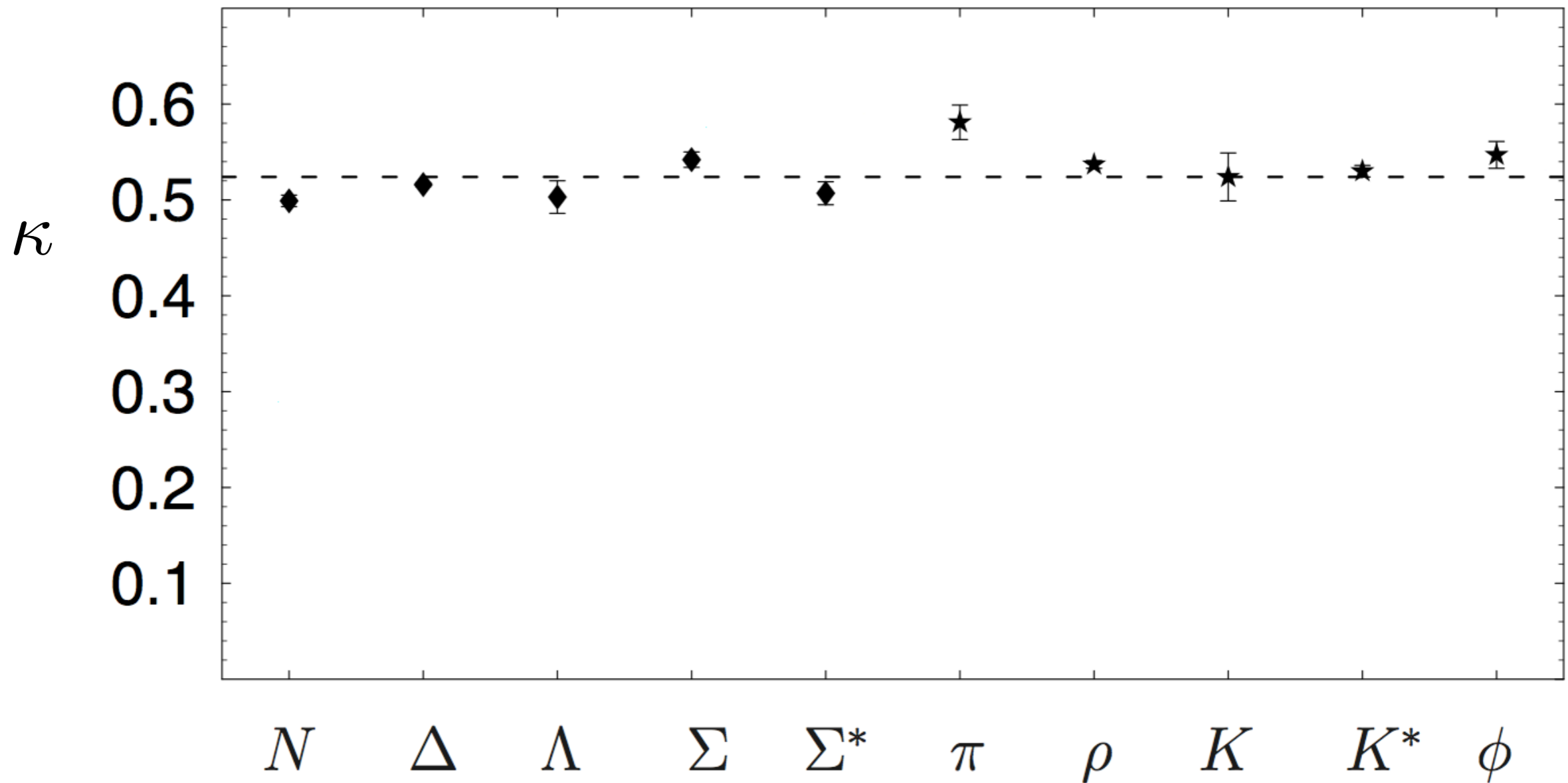
**$S=0, I=I$  Meson is superpartner of  $S=1/2, I=I$  Baryon**

$M^2$  (GeV<sup>2</sup>)

$\rho - \Delta$  superpartner trajectories



$$m_u = m_d = 46 \text{ MeV}, m_s = 357 \text{ MeV}$$



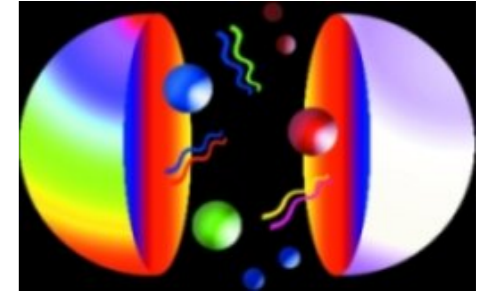
**Fit to the slope of Regge trajectories,  
including radial excitations**

**Same Regge Slope for Meson, Baryons:  
Supersymmetric feature of hadron physics**

# Fermionic Modes and Baryon Spectrum

[Hard wall model: GdT and S. J. Brodsky, PRL **94**, 201601 (2005)]

[Soft wall model: GdT and S. J. Brodsky, (2005), arXiv:1001.5193]



From Nick Evans

- Nucleon LF modes

$$\psi_+(\zeta)_{n,L} = \kappa^{2+L} \sqrt{\frac{2n!}{(n+L)!}} \zeta^{3/2+L} e^{-\kappa^2 \zeta^2 / 2} L_n^{L+1}(\kappa^2 \zeta^2)$$

$$\psi_-(\zeta)_{n,L} = \kappa^{3+L} \frac{1}{\sqrt{n+L+2}} \sqrt{\frac{2n!}{(n+L)!}} \zeta^{5/2+L} e^{-\kappa^2 \zeta^2 / 2} L_n^{L+2}(\kappa^2 \zeta^2)$$

- Normalization

$$\int d\zeta \psi_+^2(\zeta) = \int d\zeta \psi_-^2(\zeta) = 1$$

*Quark Chiral  
Symmetry of  
Eigenstate!*

- Eigenvalues

$$\mathcal{M}_{n,L,S=1/2}^2 = 4\kappa^2 (n+L+1)$$

- “Chiral partners”

$$\frac{\mathcal{M}_{N(1535)}}{\mathcal{M}_{N(940)}} = \sqrt{2}$$

**Nucleon: Equal Probability for L=0, 1**

# Features of Supersymmetric Equations

- $J = L + S$  baryon simultaneously satisfies both equations of  $G$  with  $L$ ,  $L+1$  with same mass eigenvalue

- $J^z = L^z + 1/2 = (L^z + 1) - 1/2 \quad S^z = \pm 1/2$

- Proton spin carried by quark  $L^z$

$$\langle J^z \rangle = \frac{1}{2} (S_q^z = \frac{1}{2}, L^z = 0) + \frac{1}{2} (S_q^z = -\frac{1}{2}, L^z = 1) = \langle L^z \rangle = \frac{1}{2}$$

- Mass-degenerate meson “superpartner” with  $L_M = L_B + 1$ . *“Shifted meson-baryon Duality”*

Mesons and baryons have same  $\kappa$  !

# AdS/QCD + Light Front Holography: Proton is bound state of a quark + scalar diquark

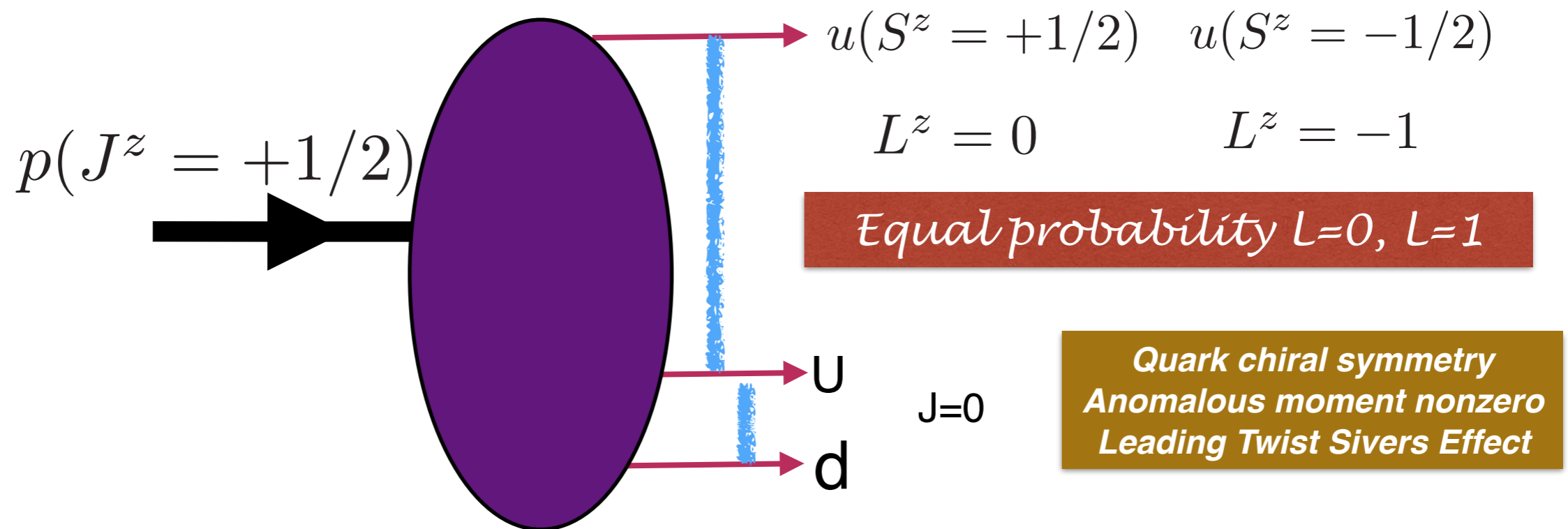
de Teramond, Dosch, Lorce, sjb

Skyrme model: Ellis, Karliner, sjb

LF  $J^z$  conservation: K. Chiu, sjb

$$3_C \times 3_C = \bar{3}_C + \cancel{6_C}$$

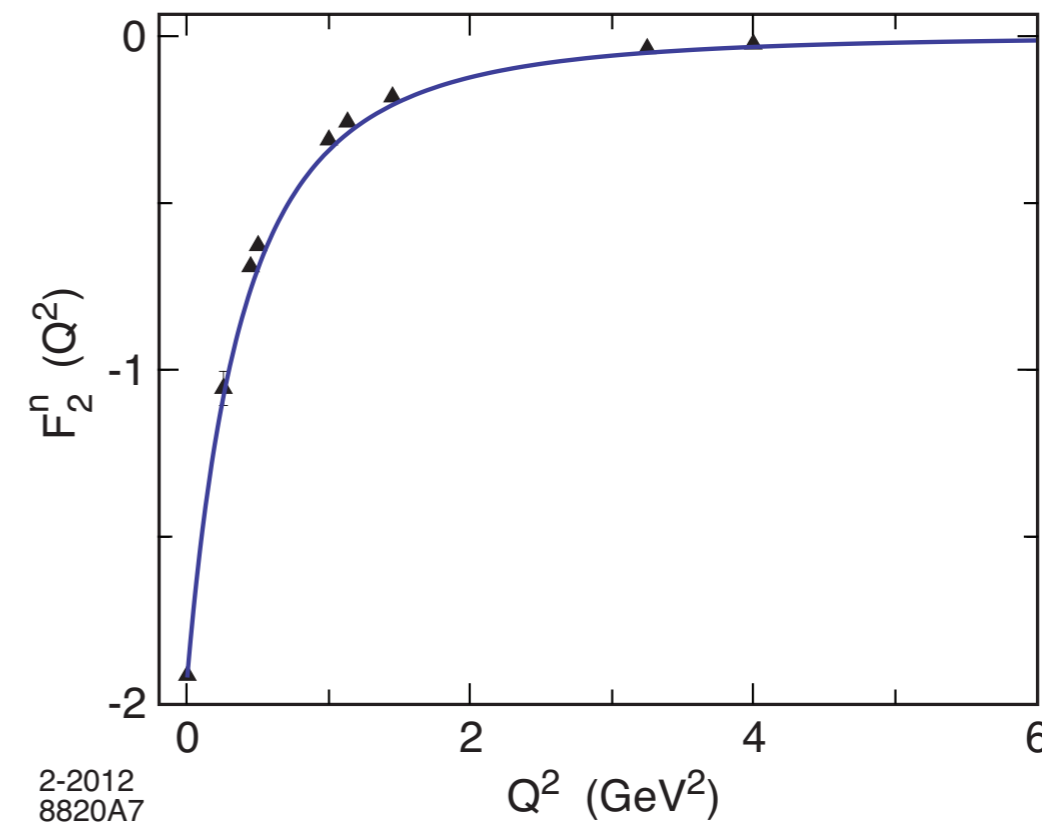
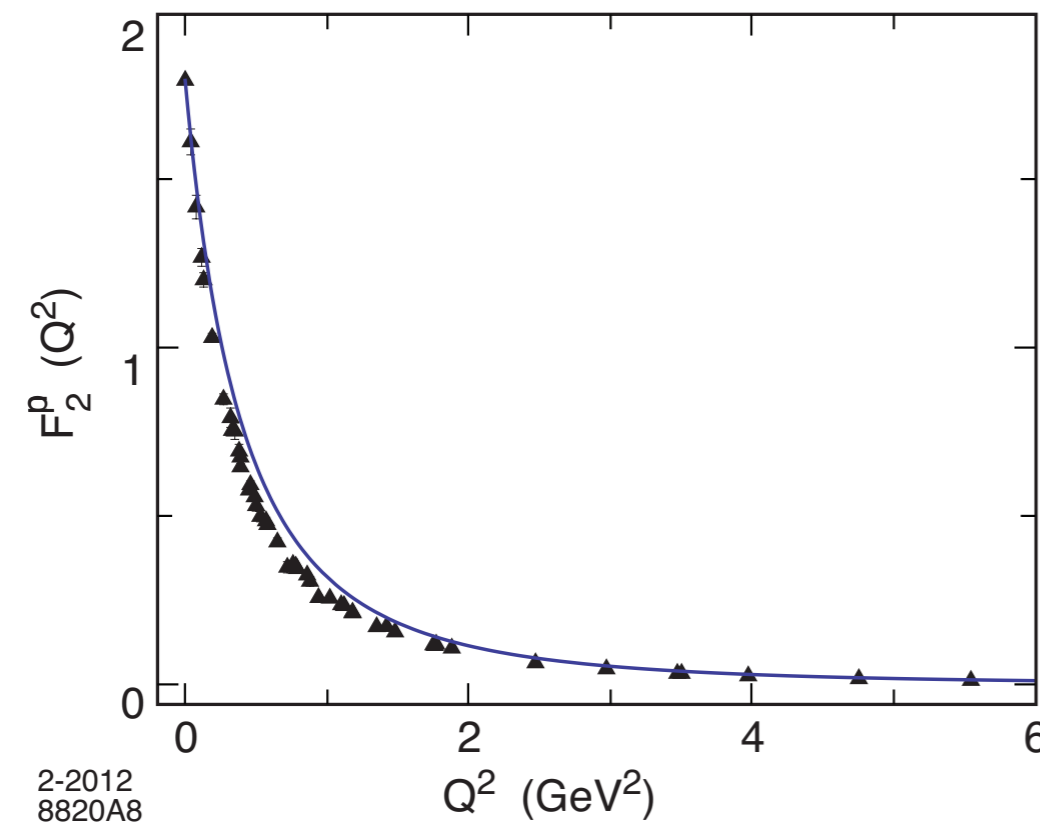
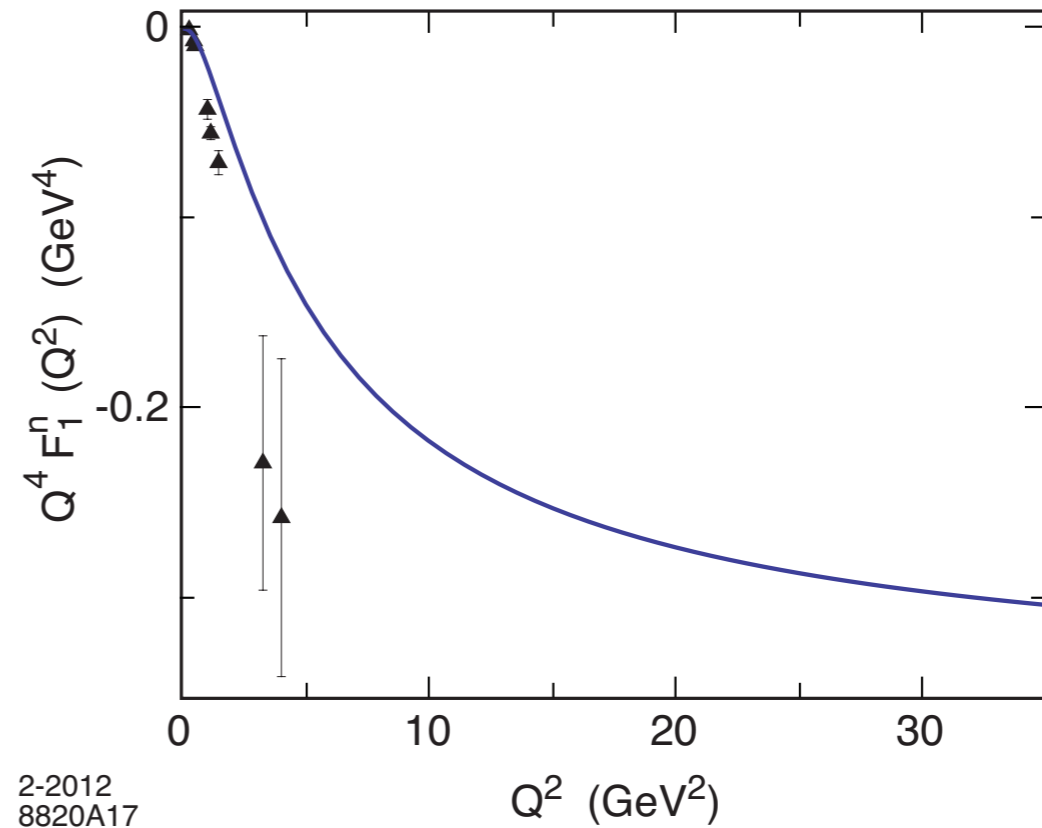
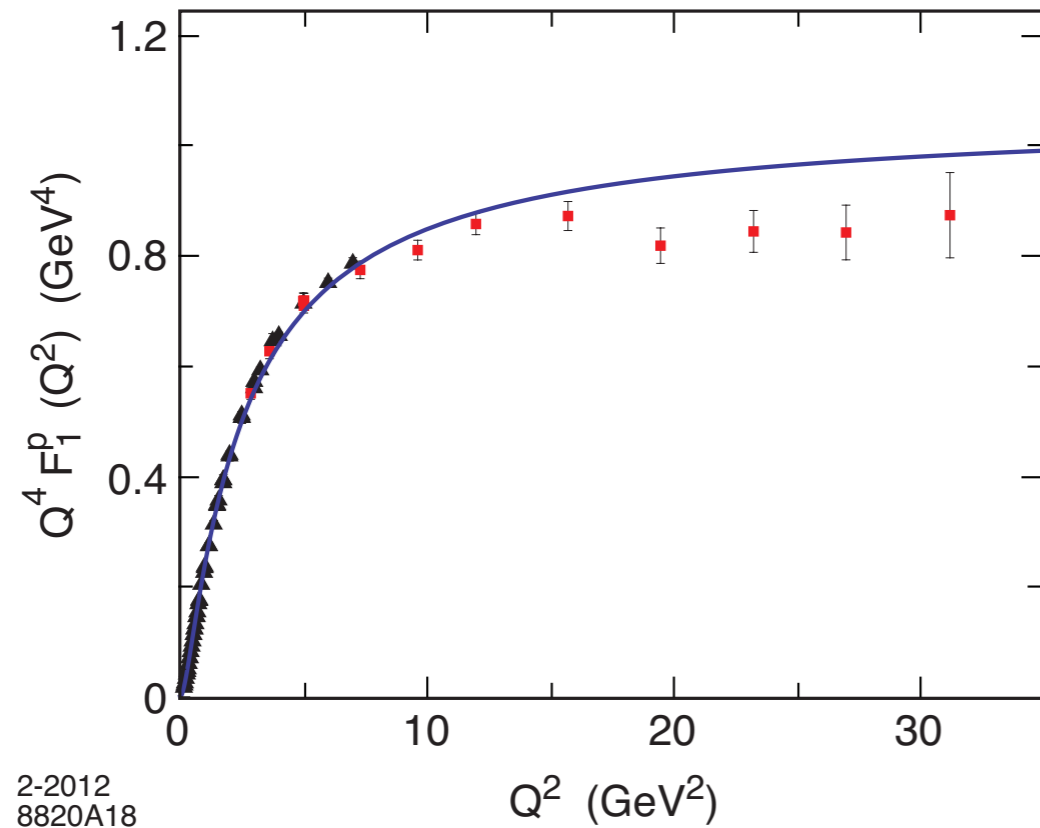
$$|p\rangle = |u_{3_C} [ud]_{\bar{3}_C}\rangle$$



**Gluonic distribution reflects quark+diquark color structure of the proton**

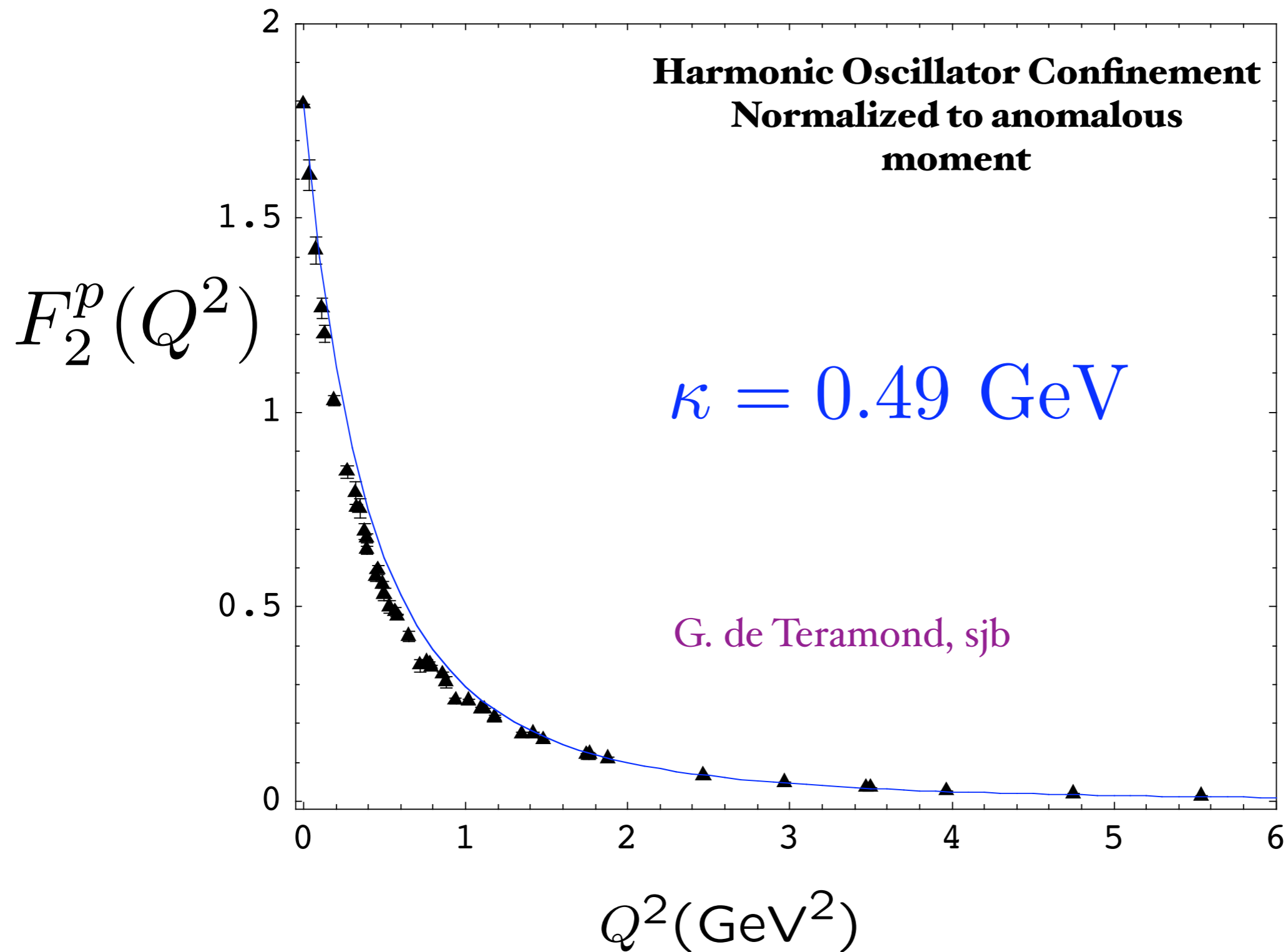
**Color confinement potential  $\rightarrow$  high density gluon field: flux tube**

Using  $SU(6)$  flavor symmetry and normalization to static quantities



# Spacelike Pauli Form Factor

From overlap of  $L = 1$  and  $L = 0$  LFWFs





- Compute Dirac proton form factor using SU(6) flavor symmetry

$$F_1^p(Q^2) = R^4 \int \frac{dz}{z^4} V(Q, z) \Psi_+^2(z)$$

- Nucleon AdS wave function

$$\Psi_+(z) = \frac{\kappa^{2+L}}{R^2} \sqrt{\frac{2n!}{(n+L)!}} z^{7/2+L} L_n^{L+1}(\kappa^2 z^2) e^{-\kappa^2 z^2/2}$$

- Normalization ( $F_1^p(0) = 1$ ,  $V(Q=0, z) = 1$ )

$$R^4 \int \frac{dz}{z^4} \Psi_+^2(z) = 1$$

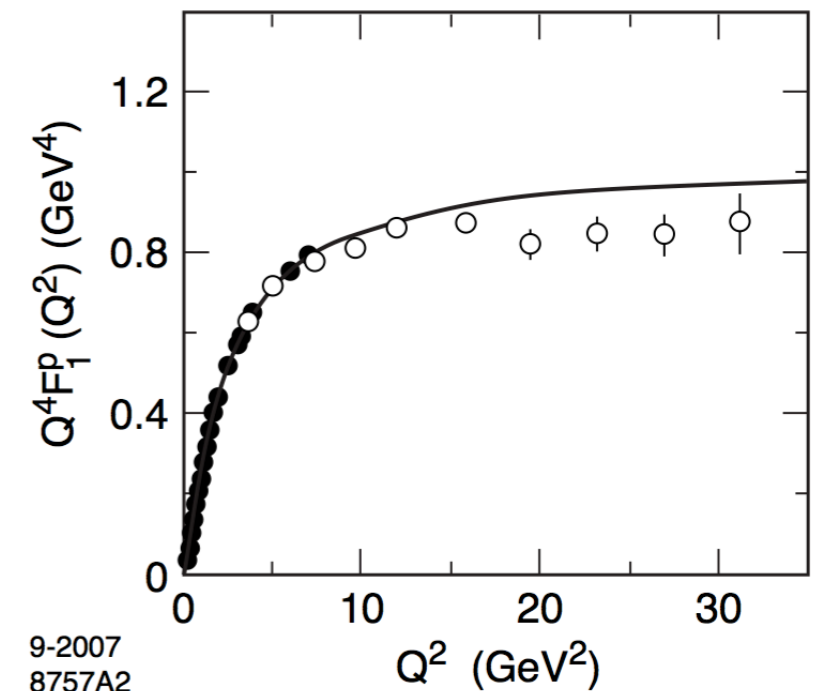
- Bulk-to-boundary propagator [Grigoryan and Radyushkin (2007)]

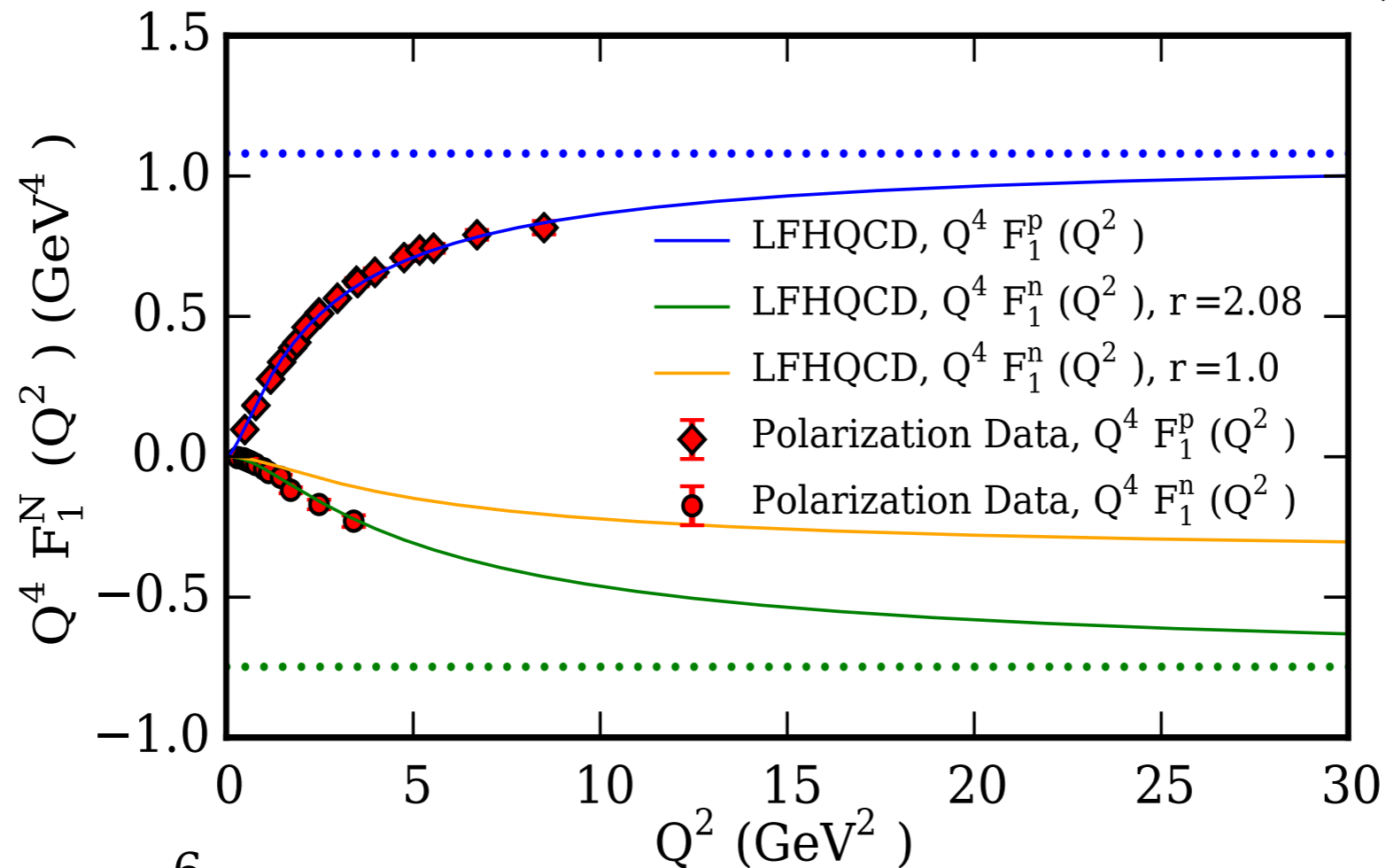
$$V(Q, z) = \kappa^2 z^2 \int_0^1 \frac{dx}{(1-x)^2} x^{\frac{Q^2}{4\kappa^2}} e^{-\kappa^2 z^2 x/(1-x)}$$

- Find

$$F_1^p(Q^2) = \frac{1}{\left(1 + \frac{Q^2}{\mathcal{M}_\rho^2}\right) \left(1 + \frac{Q^2}{\mathcal{M}_{\rho'}^2}\right)}$$

with  $\mathcal{M}_{\rho_n}^2 \rightarrow 4\kappa^2(n + 1/2)$

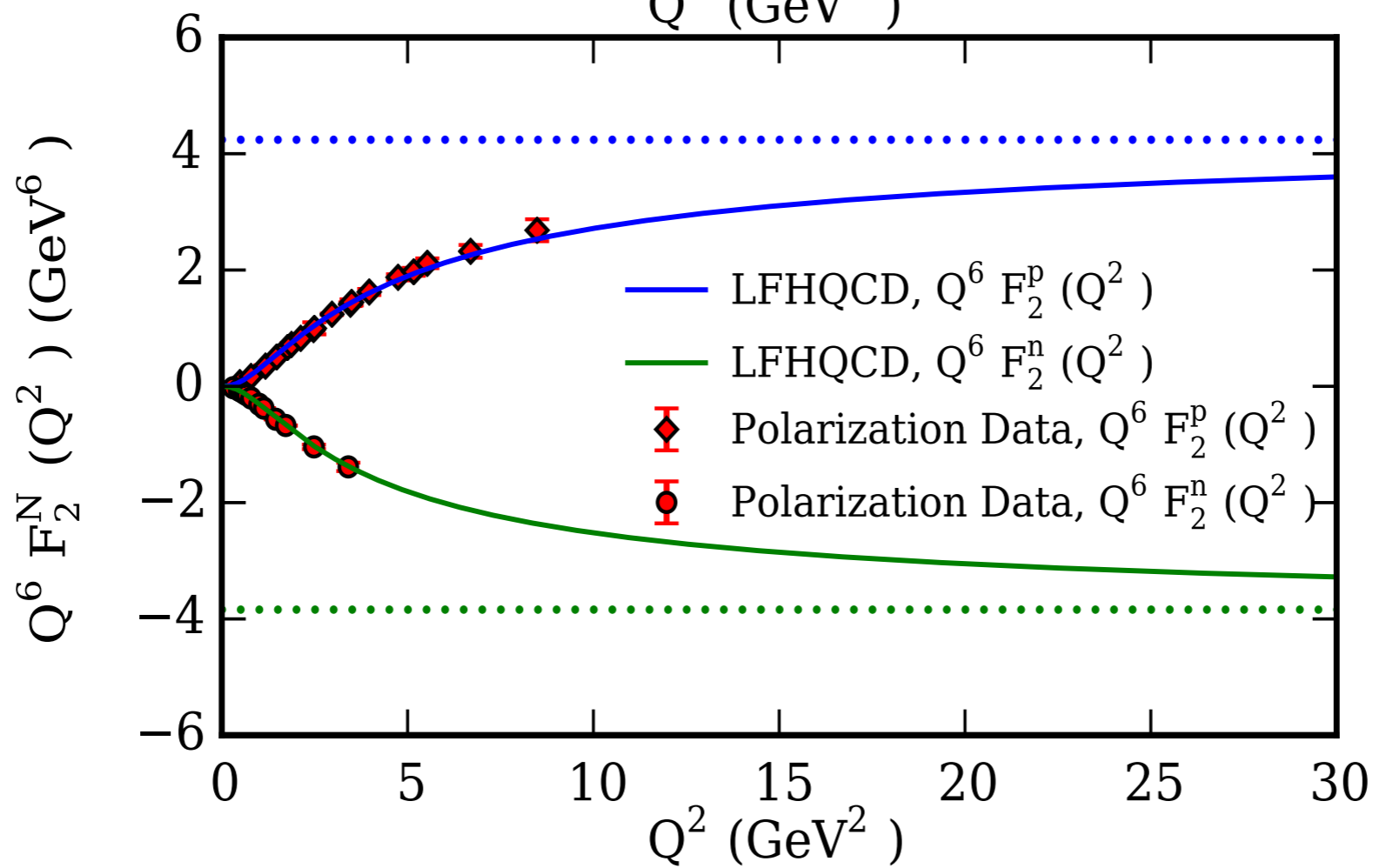




$$Q^4 F_1^p(Q^2)$$

$$Q^4 F_1^n(Q^2)$$

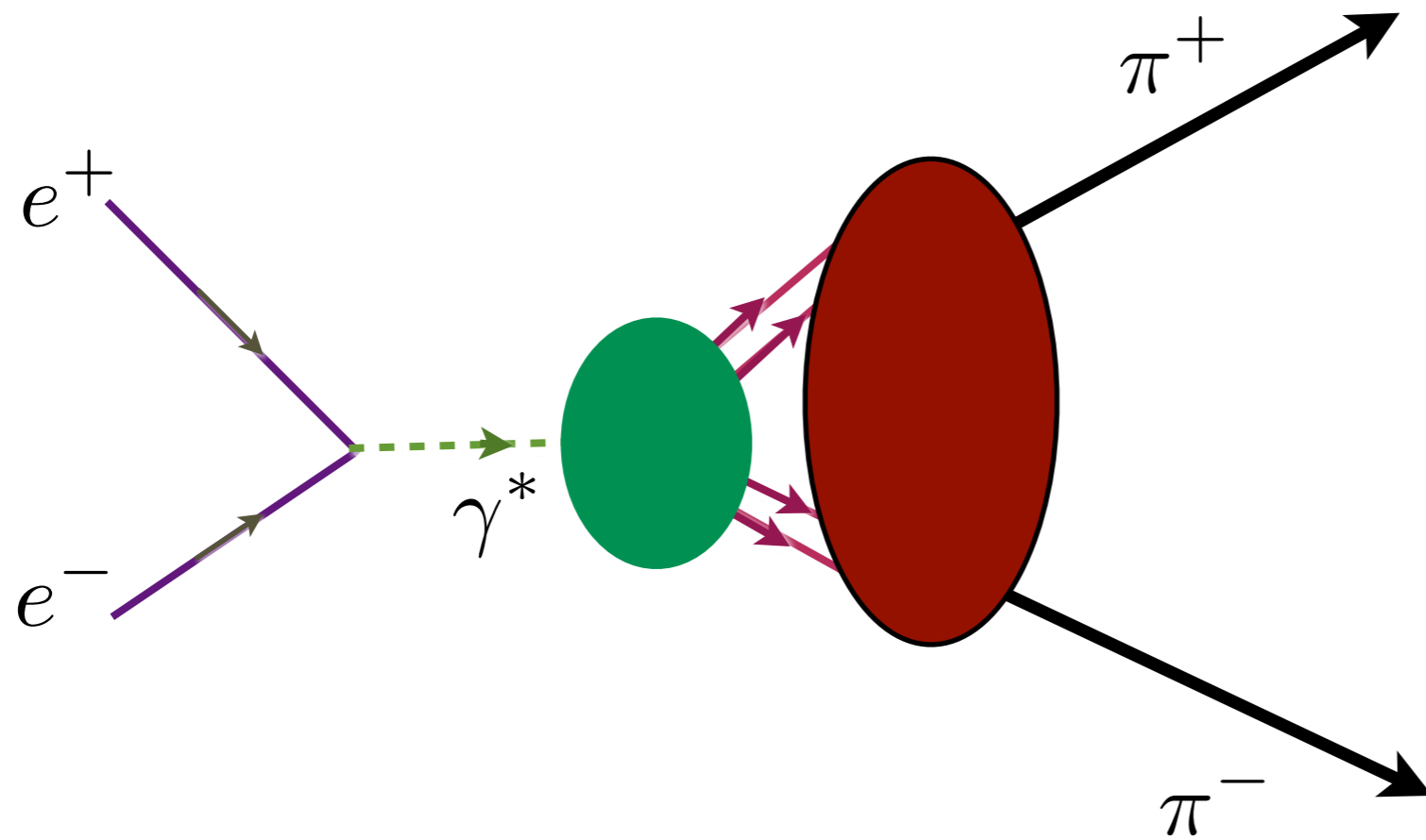
*Includes  
5-quark  
Fock states*



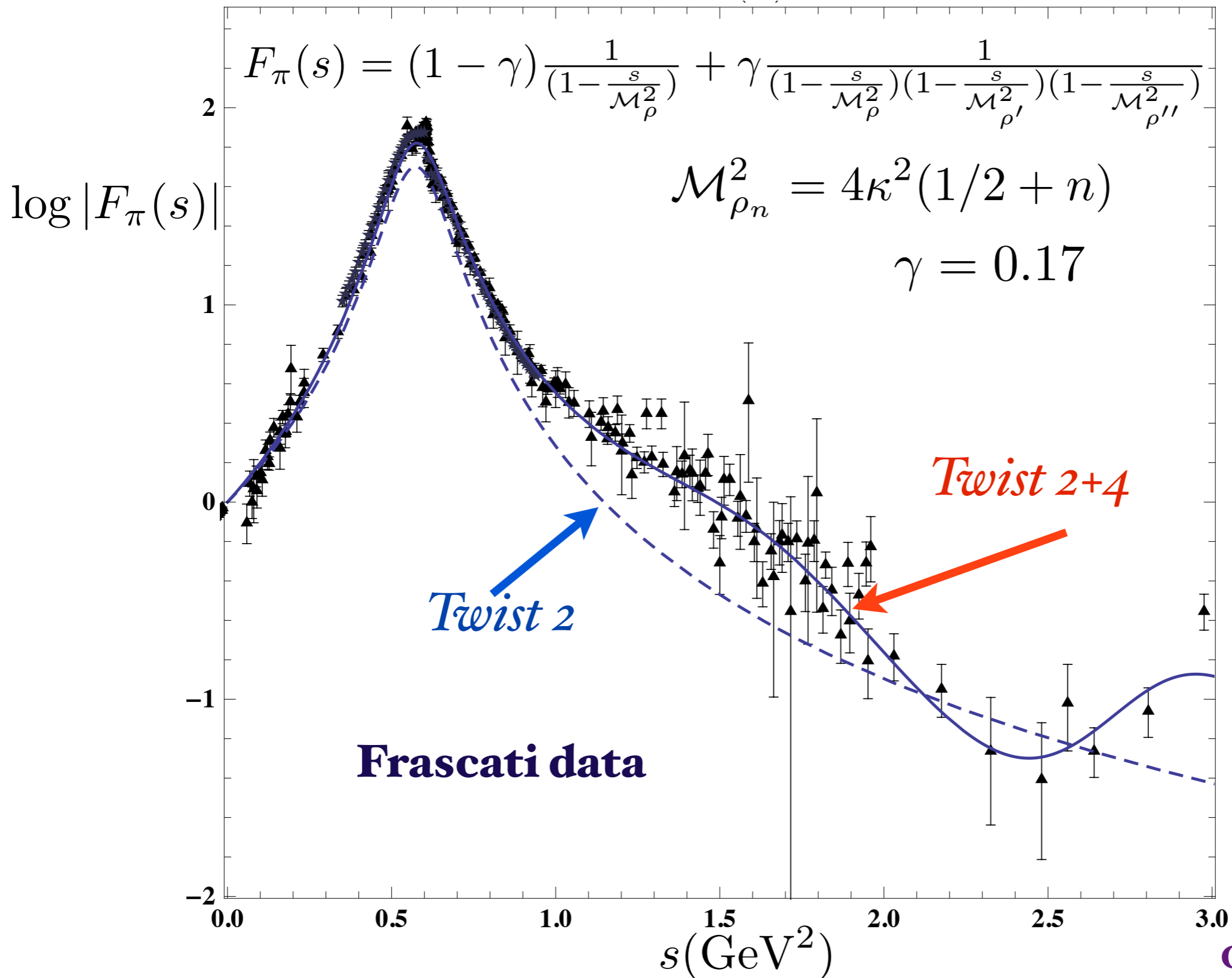
$$Q^6 F_2^p(Q^2)$$

$$Q^6 F_2^n(Q^2)$$

*Dressed soft-wall current brings in higher Fock states and more vector meson poles*



# Timelike Pion Form Factor from AdS/QCD and Light-Front Holography

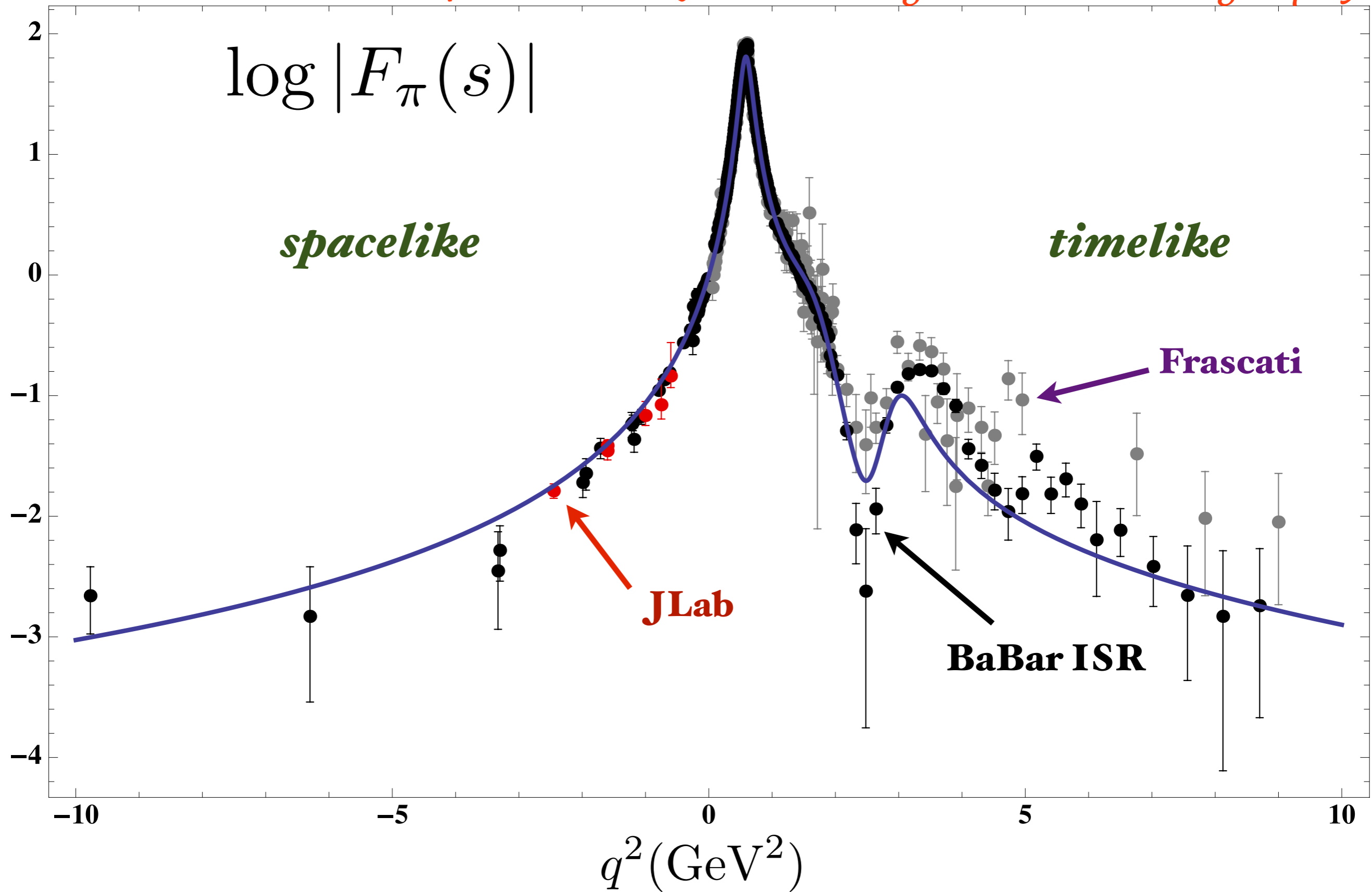


**Prescription for Timelike poles :**

$$\frac{1}{s - M^2 + i\sqrt{s}\Gamma}$$

**14% four-quark probability**

# Pion Form Factor from AdS/QCD and Light-Front Holography



Bjorken sum rule defines effective charge

$$\alpha_{g1}(Q^2)$$

$$\int_0^1 dx [g_1^{ep}(x, Q^2) - g_1^{en}(x, Q^2)] \equiv \frac{g_a}{6} \left[ 1 - \frac{\alpha_{g1}(Q^2)}{\pi} \right]$$

- **Can be used as standard QCD coupling**
- **Well measured**
- **Asymptotic freedom at large  $Q^2$**
- **Computable at large  $Q^2$  in any pQCD scheme**
- **Universal  $\beta_0, \beta_1$**

# Running Coupling from Modified AdS/QCD

Deur, de Teramond, sjb

- Consider five-dim gauge fields propagating in AdS<sub>5</sub> space in dilaton background  $\varphi(z) = \kappa^2 z^2$

$$S = -\frac{1}{4} \int d^4x dz \sqrt{g} e^{\varphi(z)} \frac{1}{g_5^2} G^2$$

- Flow equation

$$\frac{1}{g_5^2(z)} = e^{\varphi(z)} \frac{1}{g_5^2(0)} \quad \text{or} \quad g_5^2(z) = e^{-\kappa^2 z^2} g_5^2(0)$$

where the coupling  $g_5(z)$  incorporates the non-conformal dynamics of confinement

- YM coupling  $\alpha_s(\zeta) = g_{YM}^2(\zeta)/4\pi$  is the five dim coupling up to a factor:  $g_5(z) \rightarrow g_{YM}(\zeta)$
- Coupling measured at momentum scale  $Q$

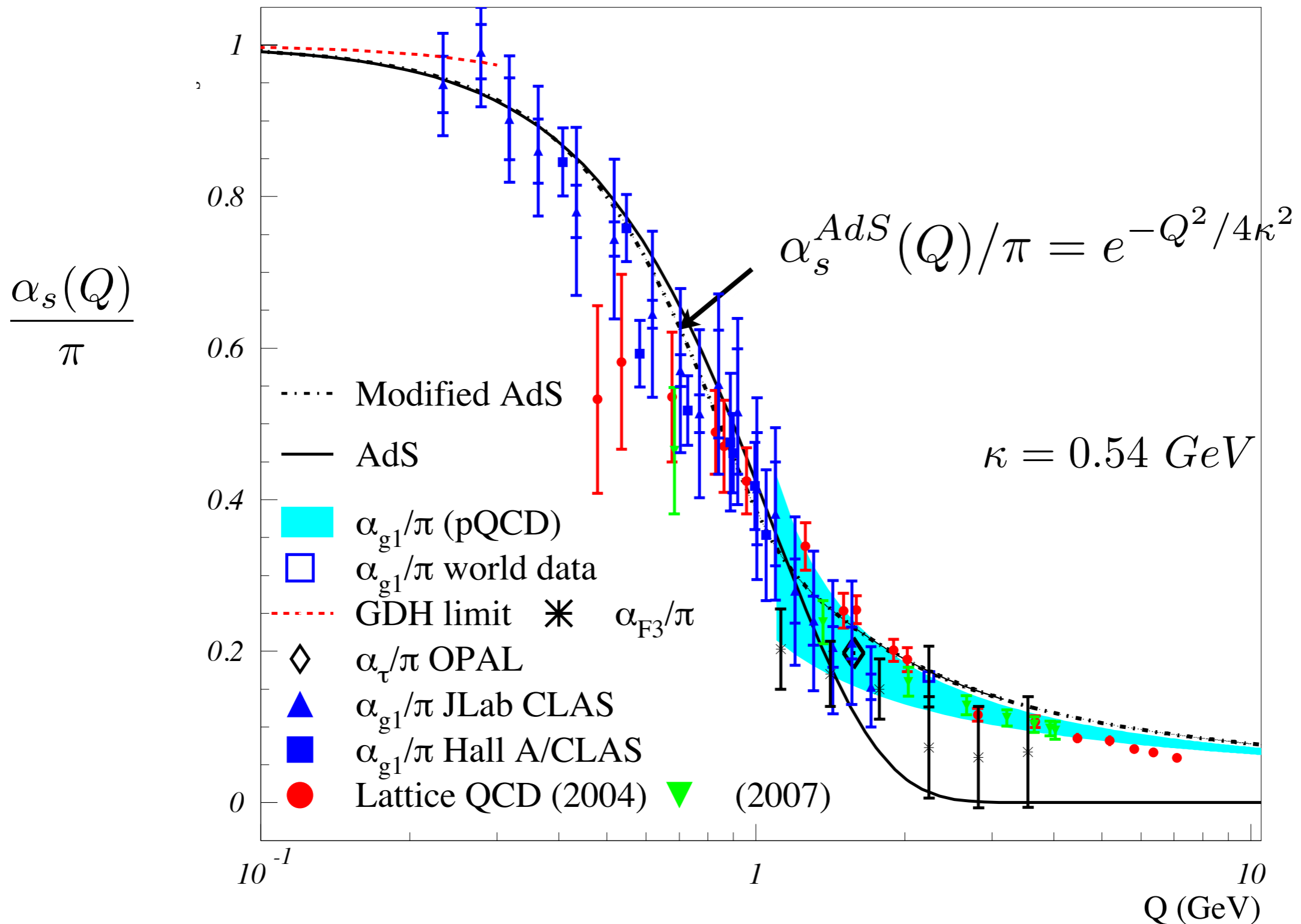
$$\alpha_s^{AdS}(Q) \sim \int_0^\infty \zeta d\zeta J_0(\zeta Q) \alpha_s^{AdS}(\zeta)$$

- Solution

$$\alpha_s^{AdS}(Q^2) = \alpha_s^{AdS}(0) e^{-Q^2/4\kappa^2}.$$

where the coupling  $\alpha_s^{AdS}$  incorporates the non-conformal dynamics of confinement

# Analytic, defined at all scales, IR Fixed Point



**AdS/QCD dilaton captures the higher twist corrections to effective charges for  $Q < 1 \text{ GeV}$**

$$e^\varphi = e^{+\kappa^2 z^2}$$

**Deur, de Teramond, sjb**



$$m_\rho = \sqrt{2}\kappa$$

$$m_p = 2\kappa$$

**All-Scale QCD Coupling**

Fit to Bj + DHG Sum Rules:  
 $\kappa = 0.513 \pm 0.007 \text{ GeV}$

$$\frac{\alpha_{g_1}^s(Q^2)}{\pi}$$

$$e^{-\frac{Q^2}{4\kappa^2}}$$

**World Data:**

$$\Lambda_{\overline{MS}} = 0.332 \pm 0.017 \text{ GeV}$$

Use  $Q_0$  for starting DGLAP and ERBL Evolution

**Perturbative QCD (Asymptotic Freedom)**

**Prediction**

$$\Lambda_{\overline{MS}} = 0.339 \pm 0.019 \text{ GeV}$$

**Transition scale  $Q_0$**

$$Q_0 = 0.87 \pm 0.08 \text{ GeV}$$

$\overline{MS}$  scheme

$$\lambda \equiv \kappa^2$$

$10^{-1}$

1

10

Q (GeV)

# *Future Directions for AdS/QCD*

- **Hadronization at the Amplitude Level**
- **Diffraction dissociation of pion and proton to jets**
- **Factorization Scale for ERBL, DGLAP evolution:  $Q_0$**
- **Calculate Sivers Effect including FSI and ISI**
- **Compute Tetraquark Spectroscopy: Sequential Clusters**
- **Update SU(6) spin-flavor symmetry**
- **Heavy Quark States: Supersymmetry, not conformal**
- **Compute higher Fock states; e.g. Intrinsic Heavy Quarks**
- **Nuclear States — Hidden Color**
- **Basis LF Quantization**      *Vary, sjb*

*Hard Two-Photon Exclusive Processes, Photon Structure Functions, TMDs, C=+ Spectroscopy*

# Characteristics of the quark-antiquark flux tube

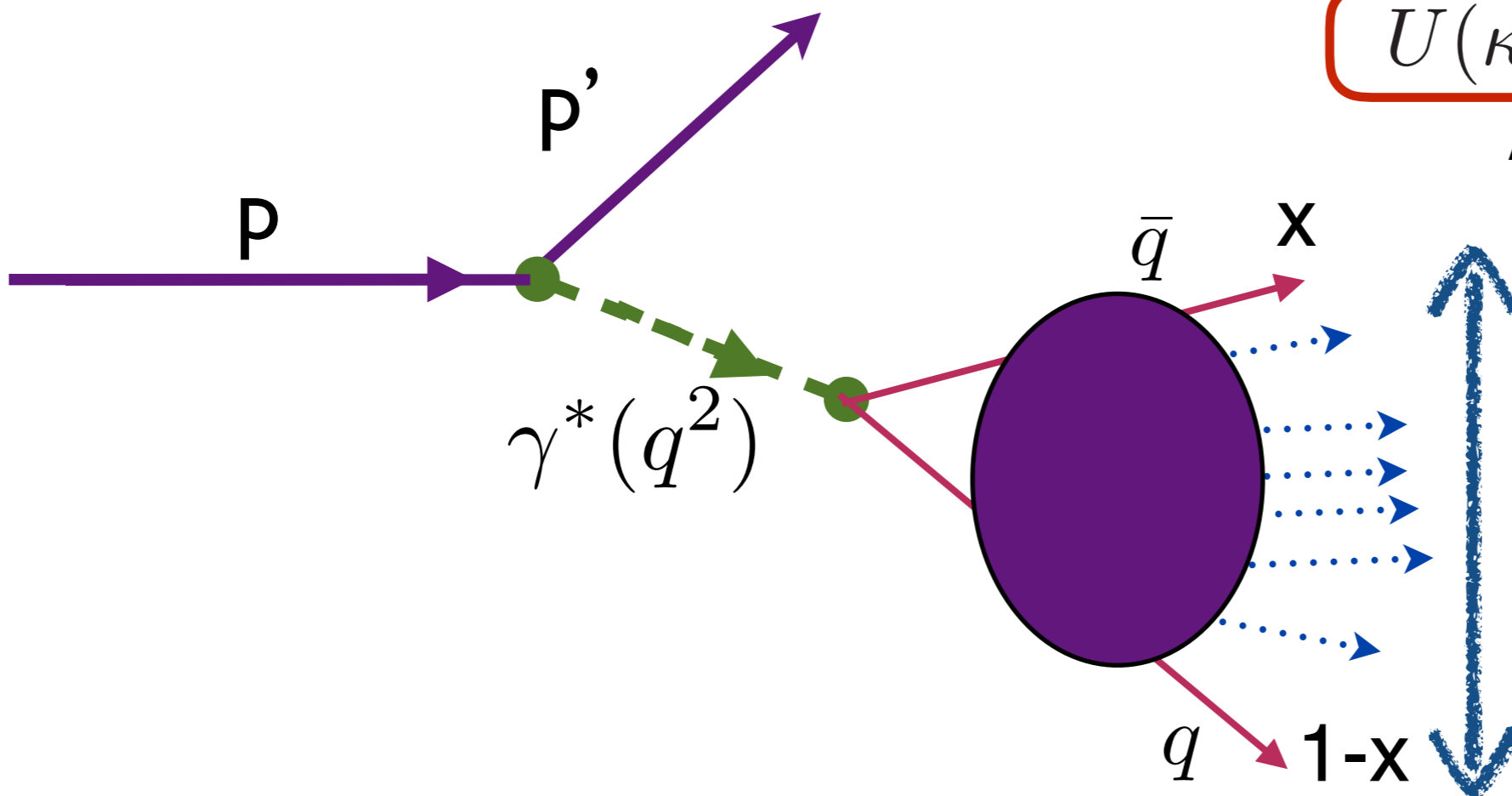
$$\psi(x, b_{\perp}^2, Q^2) \propto \exp -[b_{\perp}^2 x(1-x)(\kappa^2 + Q^2)]$$

*Planar structure reflects color-confinement potential*

$$U(\kappa^2) = \kappa^4 b_{\perp}^2 x(1-x)$$

AdS/QCD + Light-Front Holography

de Teramond, Dosch, Lorce, sjb



$$\langle b_{\perp}^2 \rangle \propto \frac{1}{x(1-x)(\kappa^2 + Q^2)}$$

massless quarks

$$\mathcal{M}^2 = \frac{k_{\perp}^2}{x(1-x)} \propto \frac{1}{b_{\perp}^2 x(1-x)}$$

$$\langle b_{\perp}^2 \rangle \rightarrow \infty \text{ if } x \rightarrow 0, 1$$

$$\langle b_{\perp}^2 \rangle \propto \frac{1}{x(1-x)(\kappa^2 + Q^2) + m_q^2}$$

massive quarks

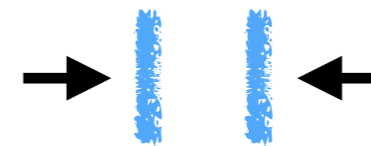
# Collisions of flux tubes of protons

Color confinement potential  $\rightarrow$  high density gluon field: flux tube

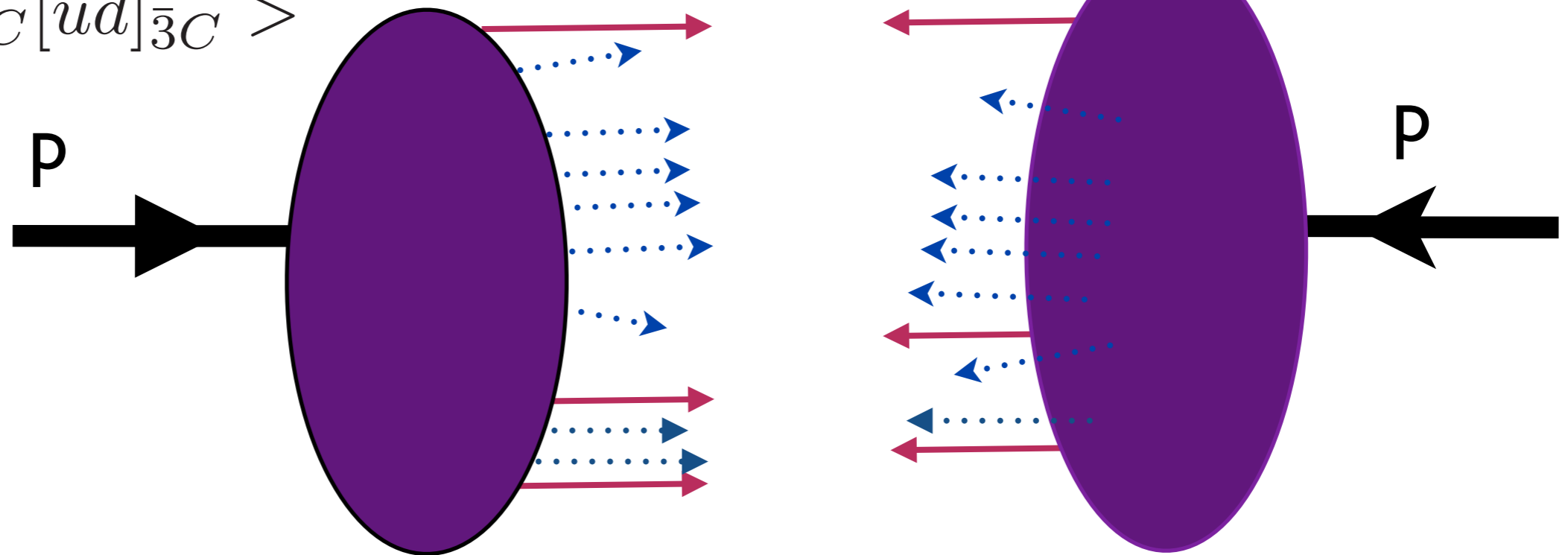
Highest hadron multiplicity produced when the two flux tubes are aligned and overlap completely along their length.

Hadrons produced from the collisions of flux tubes

Bjorken, Goldhaber, sjb



$$|p\rangle = |u_3C [ud] \bar{3}_C\rangle$$



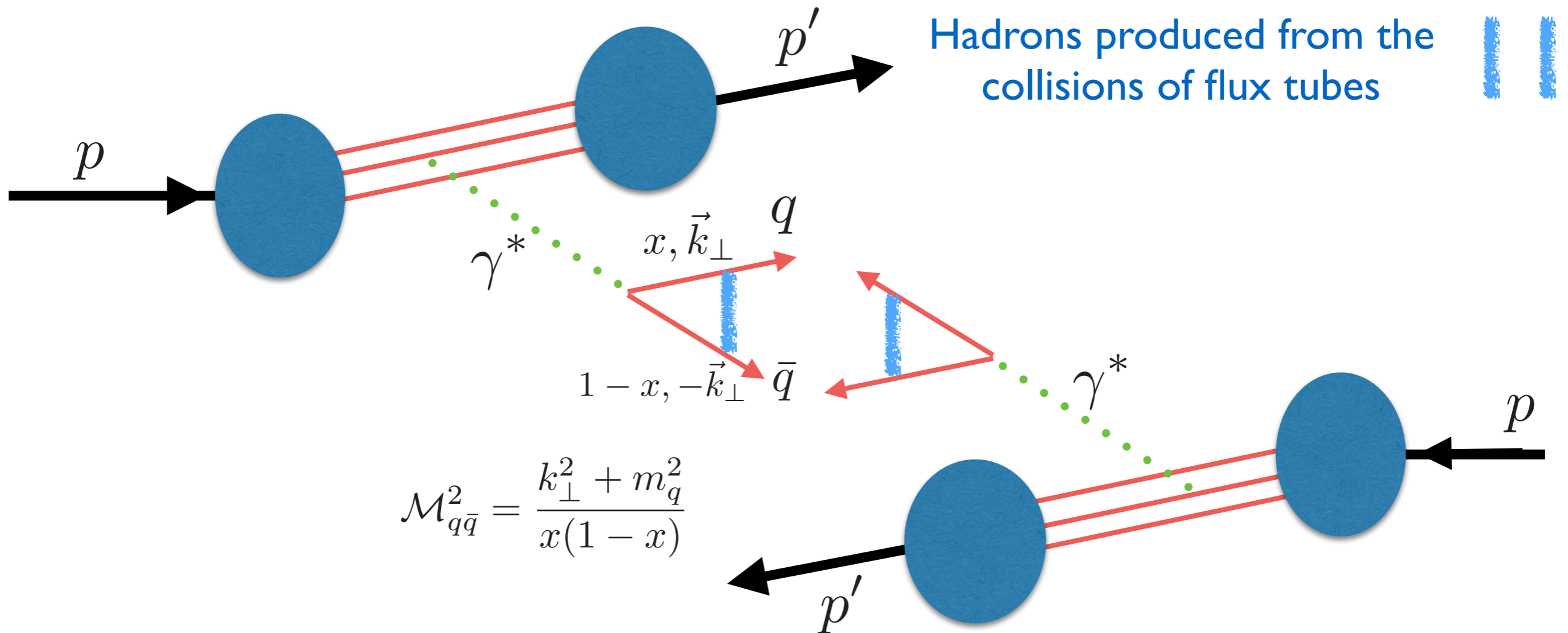
Gluonic distribution reflects quark+diquark color structure of the protons

$v_2$  (dominant) +  $v_3$  (from 'Y' quark + diquark configurations)

- Strangeness and charm enhancements

# Ridge creation in Ultra-Peripheral pp scattering

$$pp \rightarrow \gamma^* \gamma^* p' p' \rightarrow X p' p'$$



Plane of quark anti-quark and produced ridges aligned with plane of electron scattering

Correlation of  $q\bar{q}$  and proton scattering planes:  $\sim \cos^2 \Delta\phi$

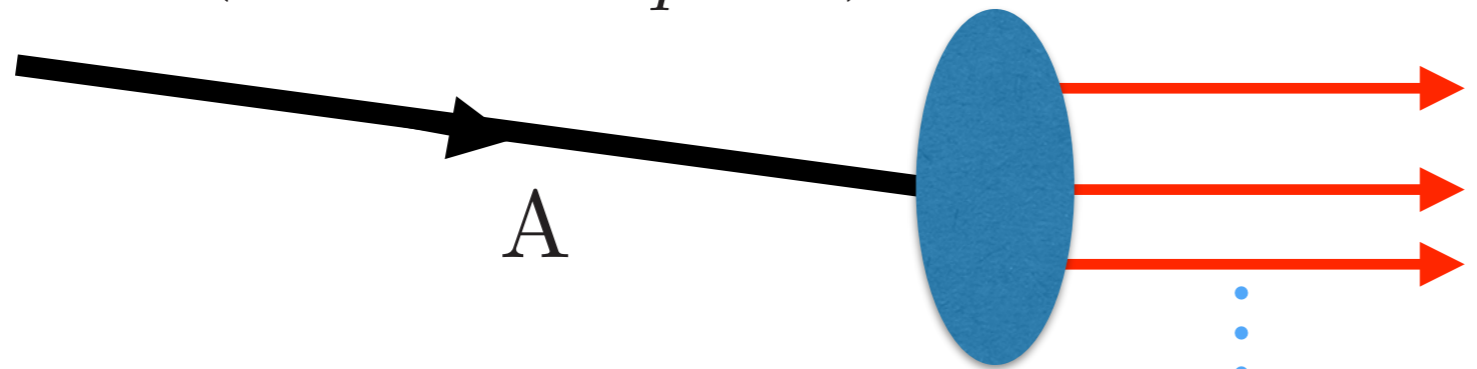
# Collisions of Gluonic Strings in Ultra-Peripheral Collisions

- **quark-antiquark plane aligned with proton scattering plane**
- **maximum hadron multiplicity from flux tubes of colliding strings between two aligned quark-antiquark pairs – flux tubes aligned along their length**  $\sim \cos^2 \Delta\phi$
- **maximum multiplicity produced when both protons scatter in same plane!**
- **minimum multiplicity when protons scatter at orthogonal angles**
- **Control ridge phenomena and multiplicity from orientations of UPC proton scattering planes**
- **Issue: Do the collisions modify the planar correlations?**
- **quark-antiquark pair distributions determined from each virtual photon LFWF**
- **Virtual photon polarization correlates quark-antiquark plane with the proton scattering planes**
- **Dependence on quark flavor, invariant mass of quark-antiquark pair**
- **New Domain for Hadron Dynamics**
- **Connection of Flux Tube to Color Confinement**
- **Similar results for photon-photon collisions**  $\sigma(ee \rightarrow e'e'\gamma^*\gamma^* \rightarrow e'e'X)$

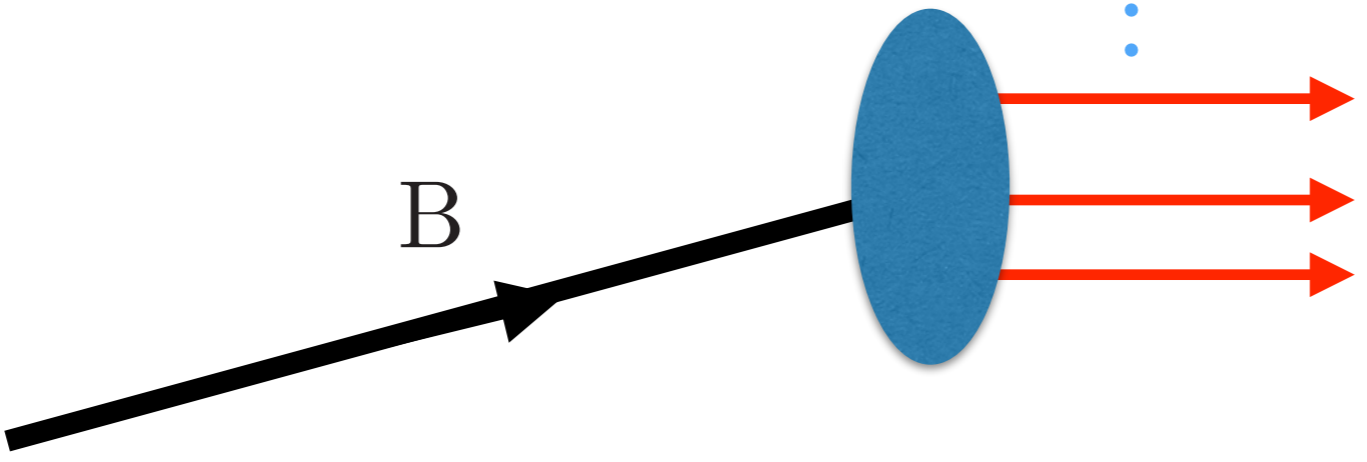
# Useful Theory Tool: "Fool's ISR Frame"

Bjorken

$$p_A = (P^+, \vec{P}_\perp, \frac{M_A^2 + P_\perp^2}{P^+})$$

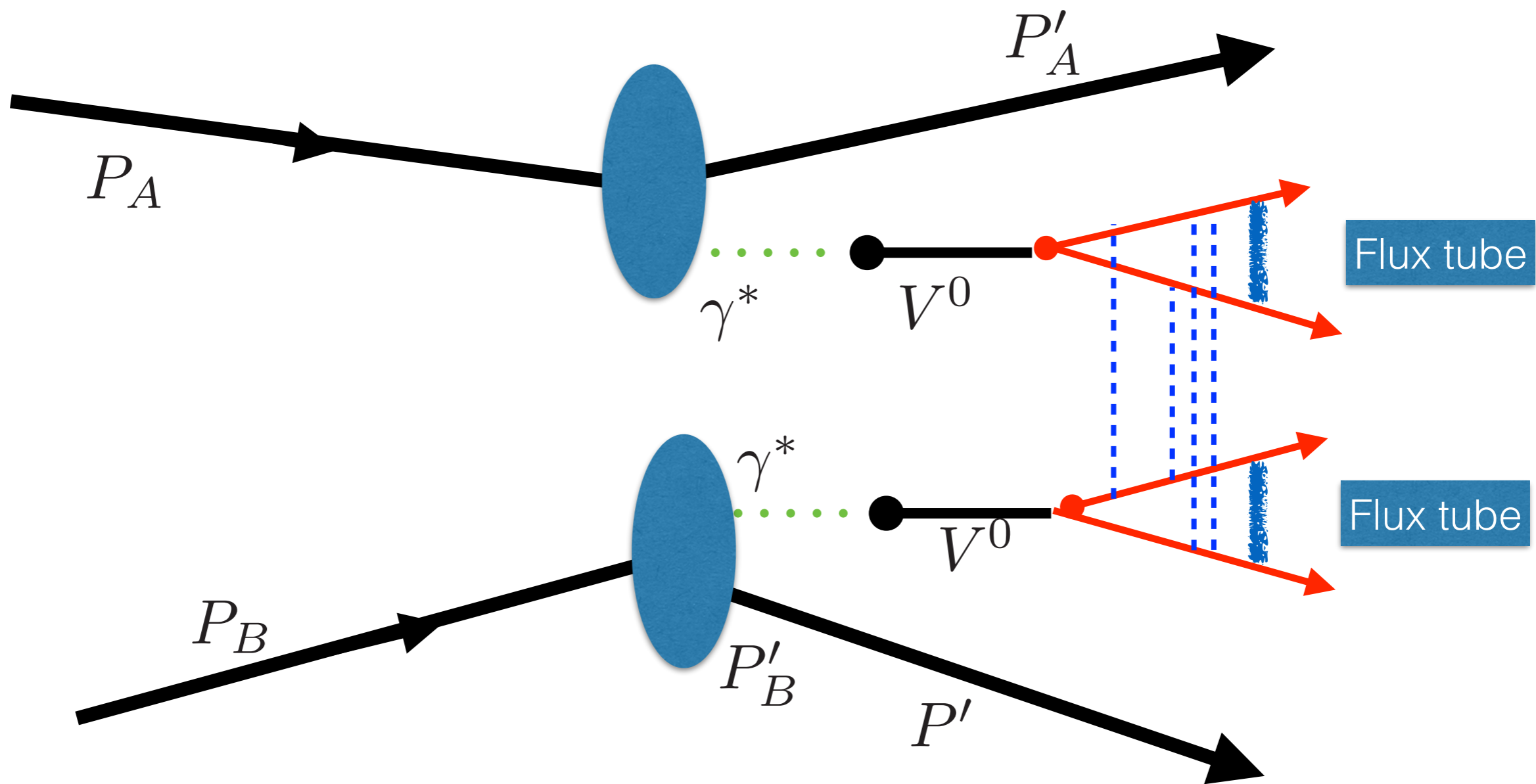


Use  $A^+ = 0$  gauge consistently



$$p_B = (P^+, -\vec{P}_\perp, \frac{M_B^2 + P_\perp^2}{P^+})$$

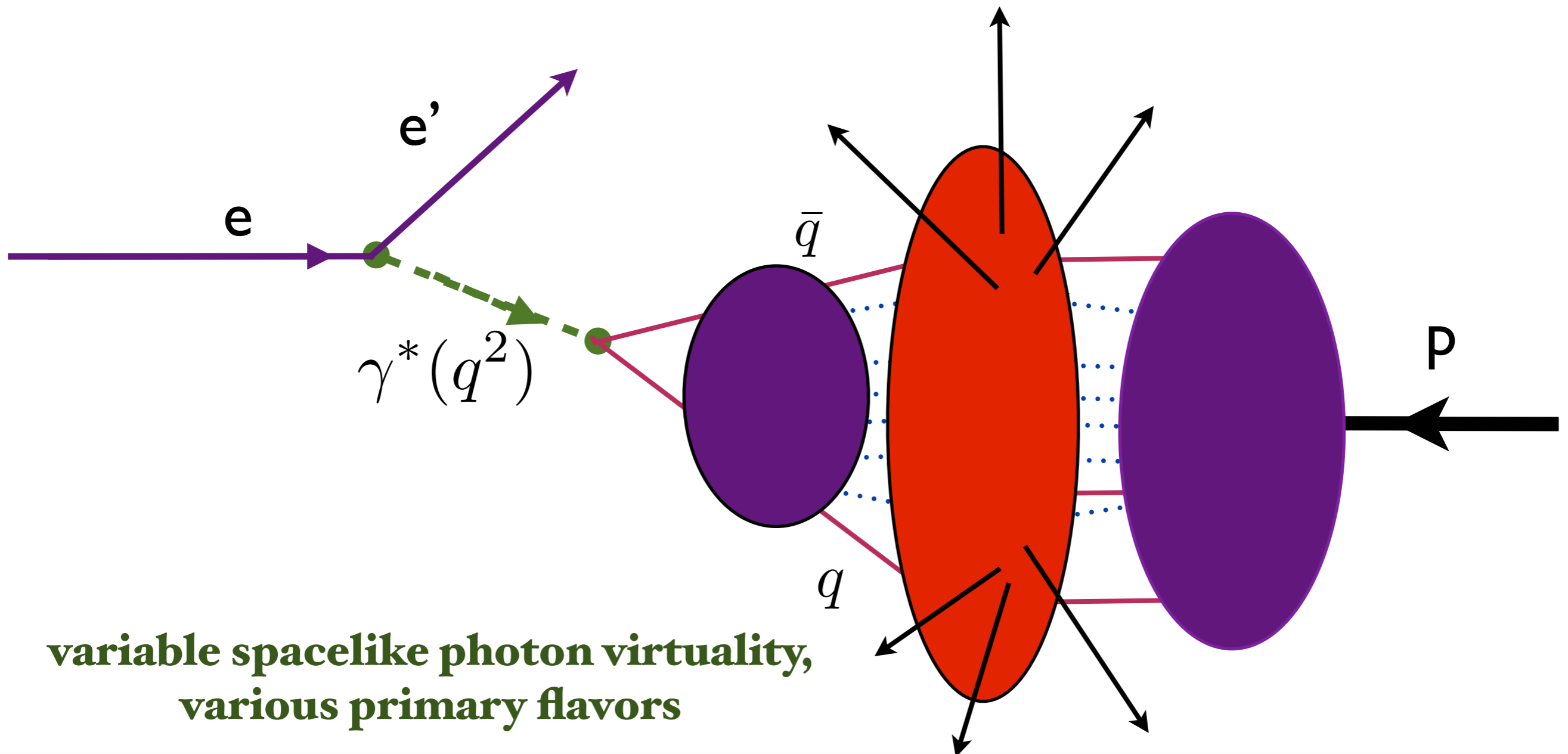
$$s = (p_A + p_B)^2 = M_A^2 + M_B^2 + 2(p_A^+ + p_B^+)(p_A^- + p_B^-) = 2M_A^2 + 2M_B^2 + 4P_\perp^2$$





# LHeC: Virtual Photon-Proton Collider

## Perspective from the e-p collider frame



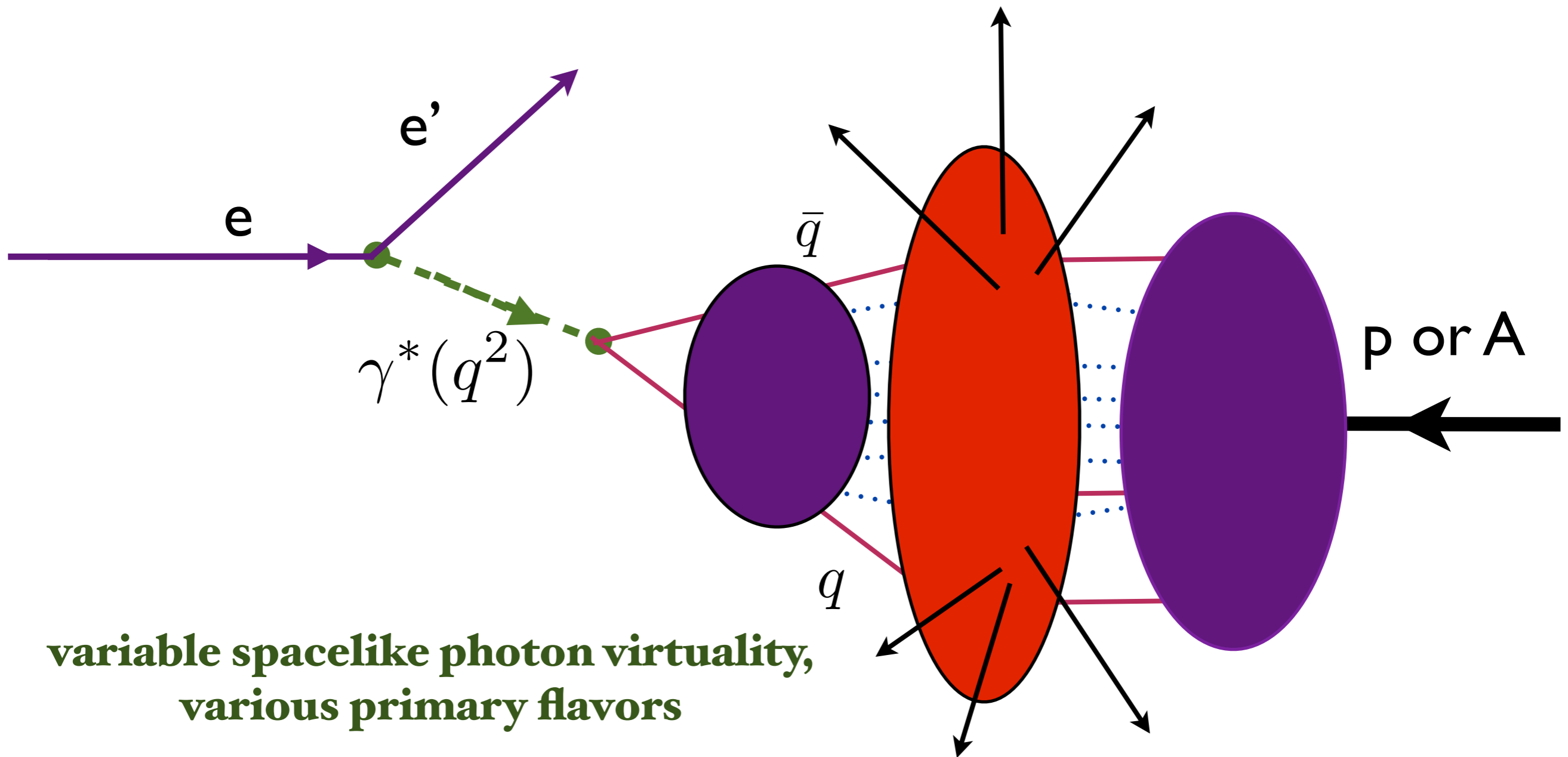
**variable spacelike photon virtuality,  
various primary flavors**

Plane of quark anti-quark and ridges aligned with plane of electron scattering

$$\sim \cos^2 \Delta\phi$$

# *EIC: Virtual Photon-Proton Collider*

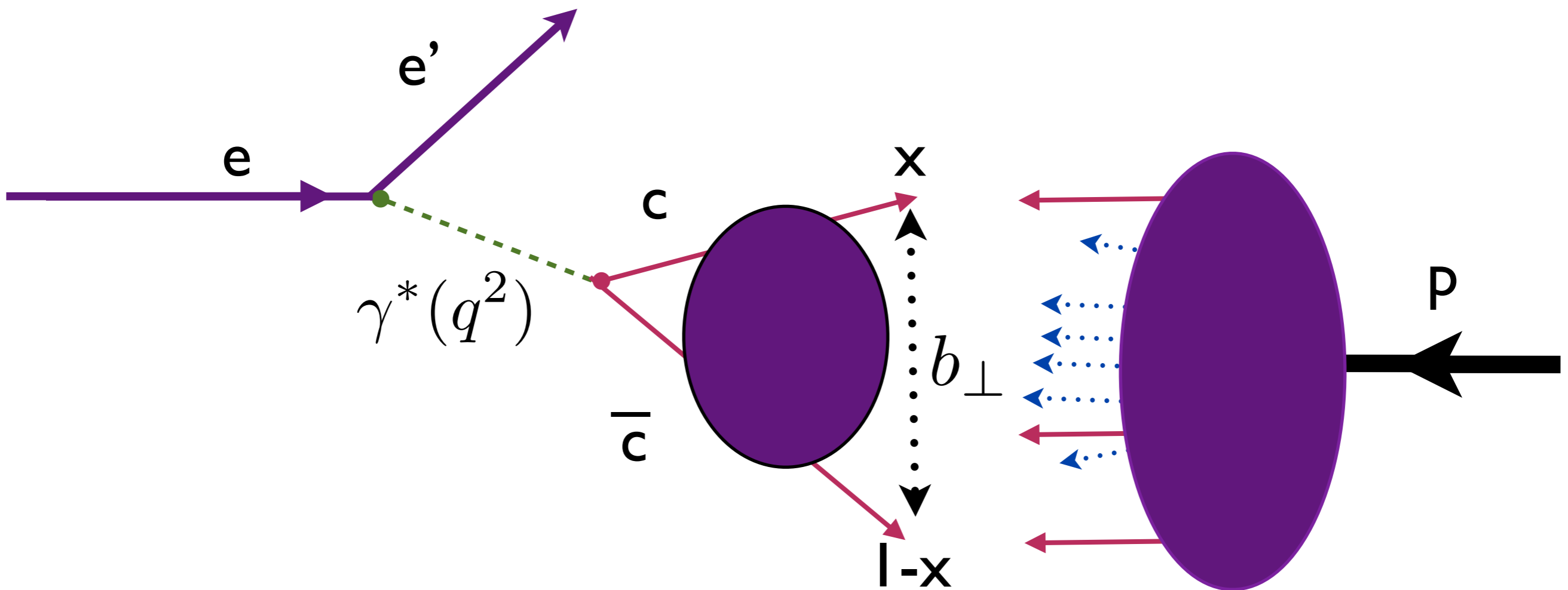
*Perspective from the e-p collider frame*



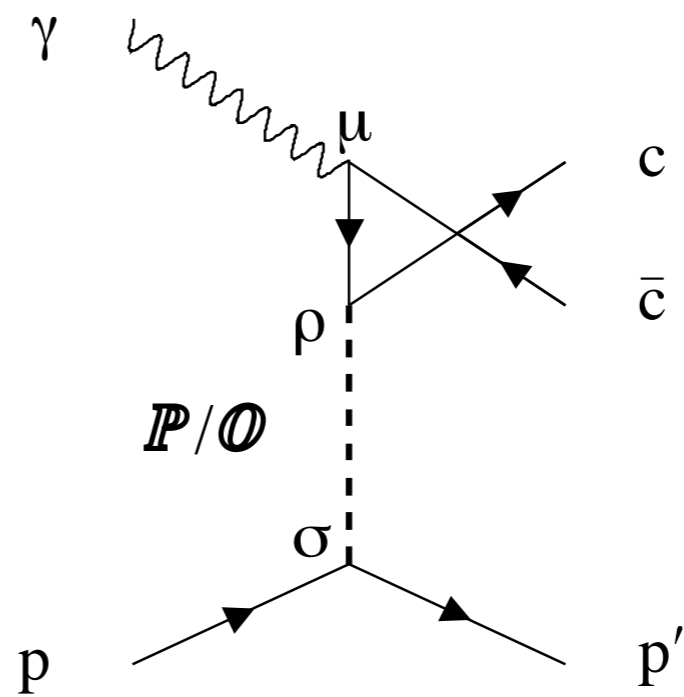
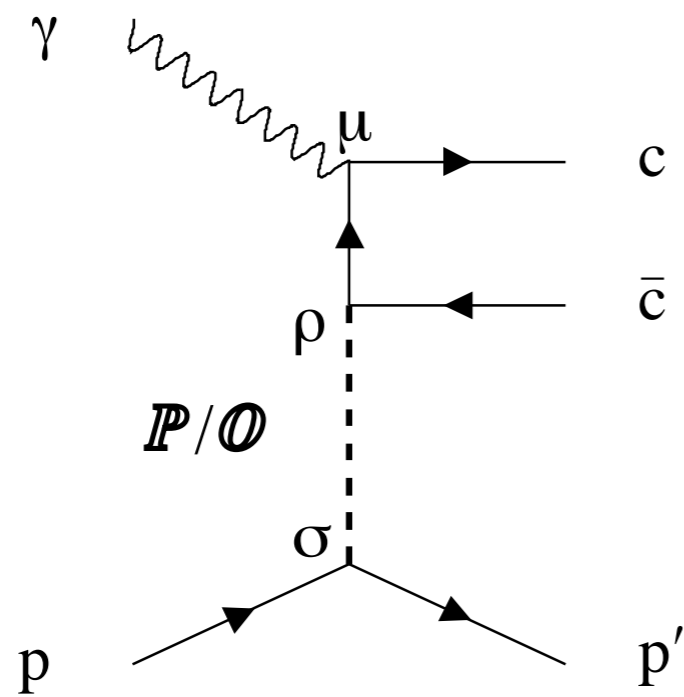
*Saturation, nuclear shadowing, antishadowing*

*$\bar{c}c$  acts as a 'drill'*

$$b_{\perp}^2 \sim \frac{1}{Q^2 x(1-x) + m_c^2}$$

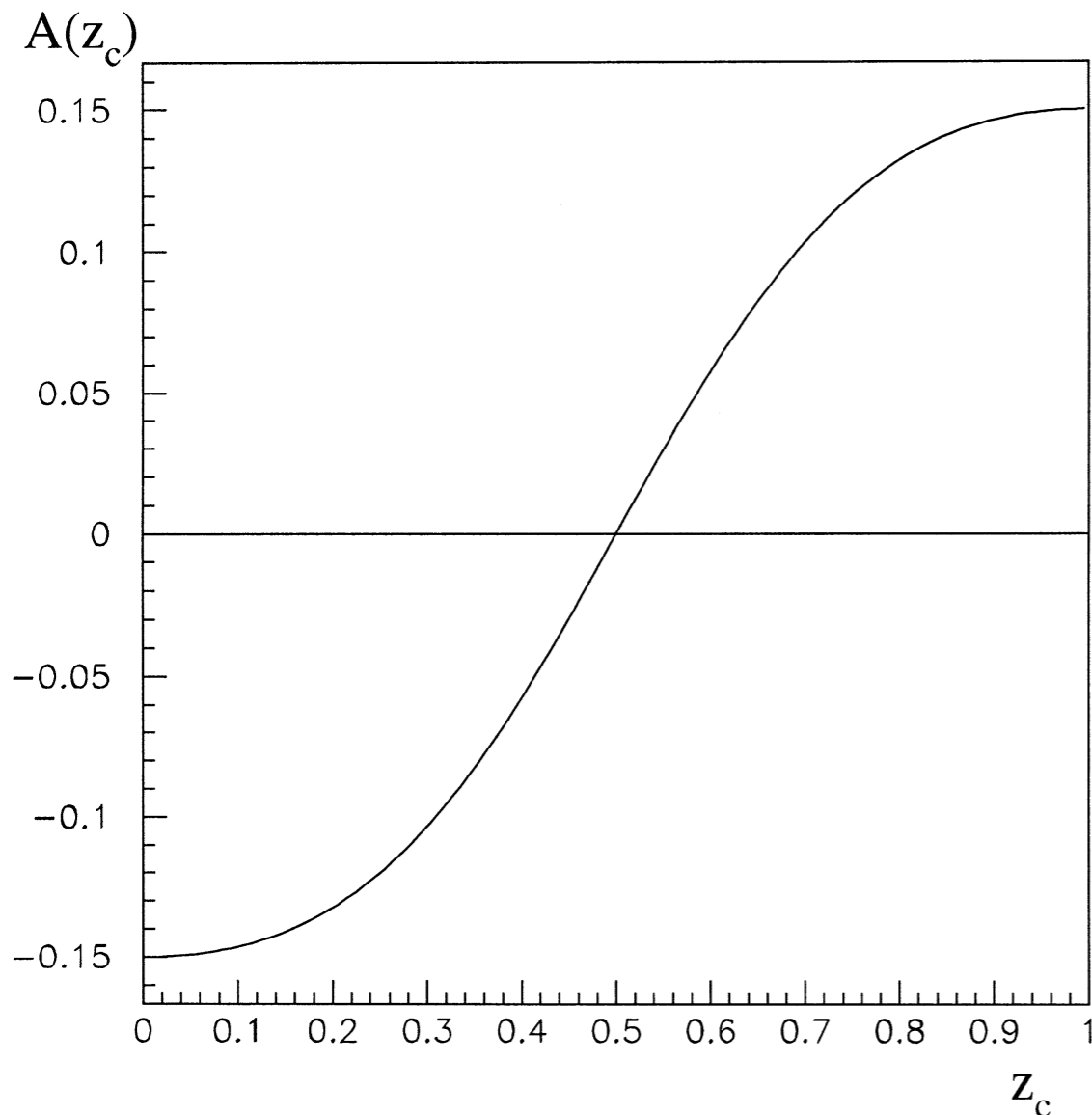


**High  $Q^2$ , high  $M^2_Q$  virtual photon acts as a precision, small bore, linearly oriented, flavor-dependent probe acting on a proton or nuclear target.**  
*Study final-state hadron multiplicity distributions, ridges, nuclear dependence*



$$\gamma^* p \rightarrow c\bar{c}p$$

## Odderon-Pomeron Interference!

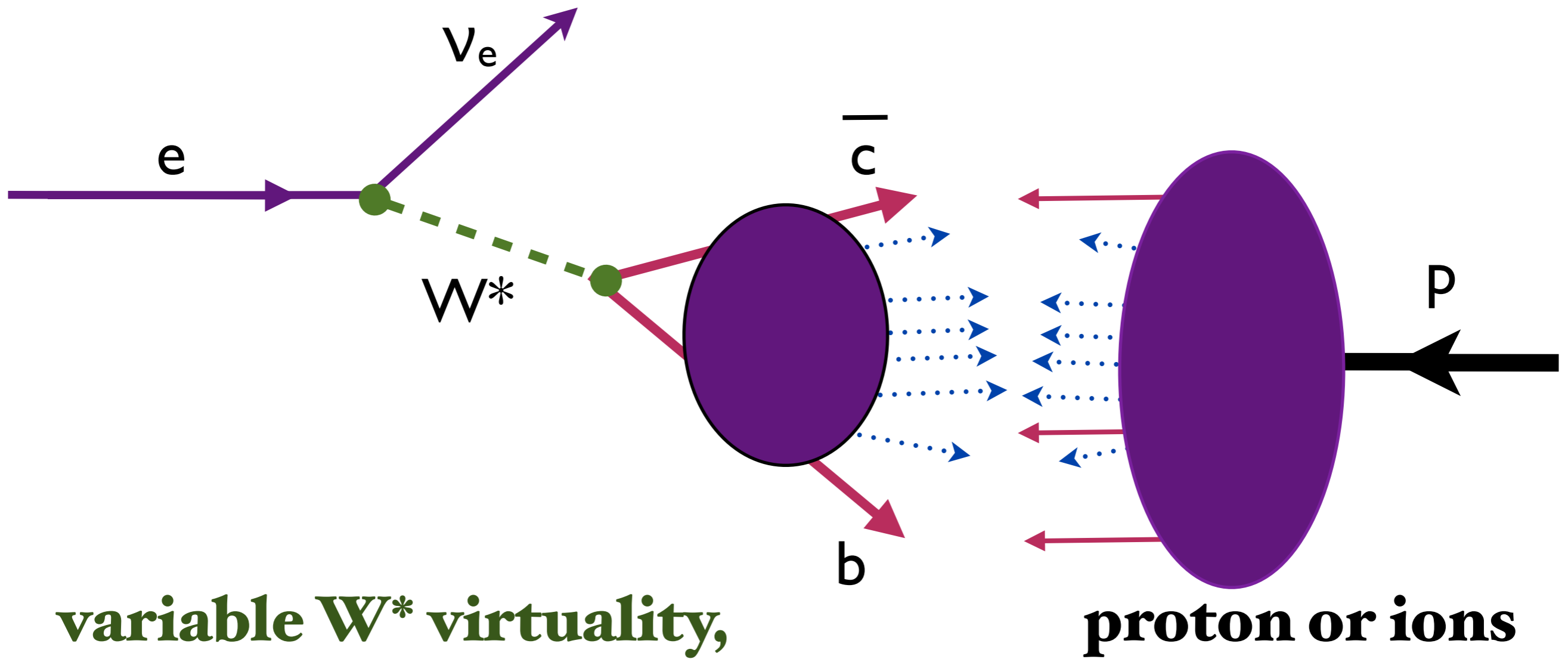


$$\mathcal{A}(t \simeq 0, M_X^2, z_c) \simeq 0.45 \left( \frac{s_{\gamma p}}{M_X^2} \right)^{-0.25} \frac{2z_c - 1}{z_c^2 + (1 - z_c)^2}$$

*Measure charm asymmetry in photon fragmentation region*

**Merino, Rathsmann, sjb**

# *EIC: Virtual Weak Boson-Proton Collider*



**variable  $W^*$  virtuality,  
variable flavors**

**proton or ions**

# ***Novel QCD Physics at the EIC***

- **Control Collisions of Flux Tubes and Ridge Phenomena**
- **Study Flavor-Dependence of Anti-Shadowing**
- **Heavy Quarks at Large  $x$ ; Exotic States**
- **Direct, color-transparent hard subprocesses and the baryon anomaly**
- **Tri-Jet Production and the proton's LFWF**
- **Odderon-Pomeron Interference**
- **Digluon-initiated subprocesses and anomalous nuclear dependence of quarkonium production**
- **Factorization-Breaking Lensing Corrections**



## **Systematic All-Orders Method to Eliminate Renormalization-Scale and Scheme Ambiguities in Perturbative QCD**

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*CP3-Origins, Danish Institute for Advanced Studies, University of Southern Denmark, DK-5230 Odense, Denmark  
and SLAC National Accelerator Laboratory, Stanford University, Stanford, California 94039, USA*

Stanley J. Brodsky†

*SLAC National Accelerator Laboratory, Stanford University, Stanford, California 94039, USA*

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(Received 13 January 2013; published 10 May 2013)*

We introduce a generalization of the conventional renormalization schemes used in dimensional regularization, which illuminates the renormalization scheme and scale ambiguities of perturbative QCD predictions, exposes the general pattern of nonconformal  $\{\beta_i\}$  terms, and reveals a special degeneracy of the terms in the perturbative coefficients. It allows us to systematically determine the argument of the running coupling order by order in perturbative QCD in a form which can be readily automatized. The new method satisfies all of the principles of the renormalization group and eliminates an unnecessary source of systematic error.

# Electron-Electron Scattering in QED

$$\mathcal{M}_{ee \rightarrow ee}(++; ++) = \frac{8\pi s}{t} \alpha(t) + \frac{8\pi s}{u} \alpha(u)$$



$$\alpha(t) = \frac{\alpha(0)}{1 - \Pi(t)}$$

## Gell-Mann--Low Effective Charge

- **Dressed Photon Propagator sums all  $\beta$  (vacuum polarization) contributions, proper and improper**

$$\alpha(t) = \frac{\alpha(t_0)}{1 - \Pi(t, t_0)}$$

$$\Pi(t, t_0) = \frac{\Pi(t) - \Pi(t_0)}{1 - \Pi(t_0)}$$

- **Initial Scale Choice  $t_0$  is Arbitrary!**

- **Any renormalization scheme can be used**  $\alpha(t) \rightarrow \alpha_{\overline{MS}}(e^{-\frac{5}{3}t})$



# Set multiple renormalization scales -- Lensing, DGLAP, ERBL Evolution ...

Choose renormalization scheme; e.g.  $\alpha_s^R(\mu_R^{\text{init}})$

Choose  $\mu_R^{\text{init}}$ ; arbitrary initial renormalization scale

Identify  $\{\beta_i^R\}$  – terms using  $\delta$ -terms  
through the PMC – BLM correspondence principle

Shift scale of  $\alpha_s$  to  $\mu_R^{\text{PMC}}$  to eliminate  $\{\beta_i^R\}$  – terms

Conformal Series

Result is independent of  $\mu_R^{\text{init}}$  and scheme at fixed order

## PMC/BLM

**No renormalization scale ambiguity!**

*Result is independent of  
Renormalization scheme  
and initial scale!*

**QED Scale Setting at  $N_C=0$**

**Eliminates unnecessary  
systematic uncertainty**

**Scale fixed at each order**

**$\delta$ -Scheme automatically  
identifies  $\beta$ -terms!**

*Xing-Gang Wu, Matin Mojaza  
Leonardo di Giustino, SJB*

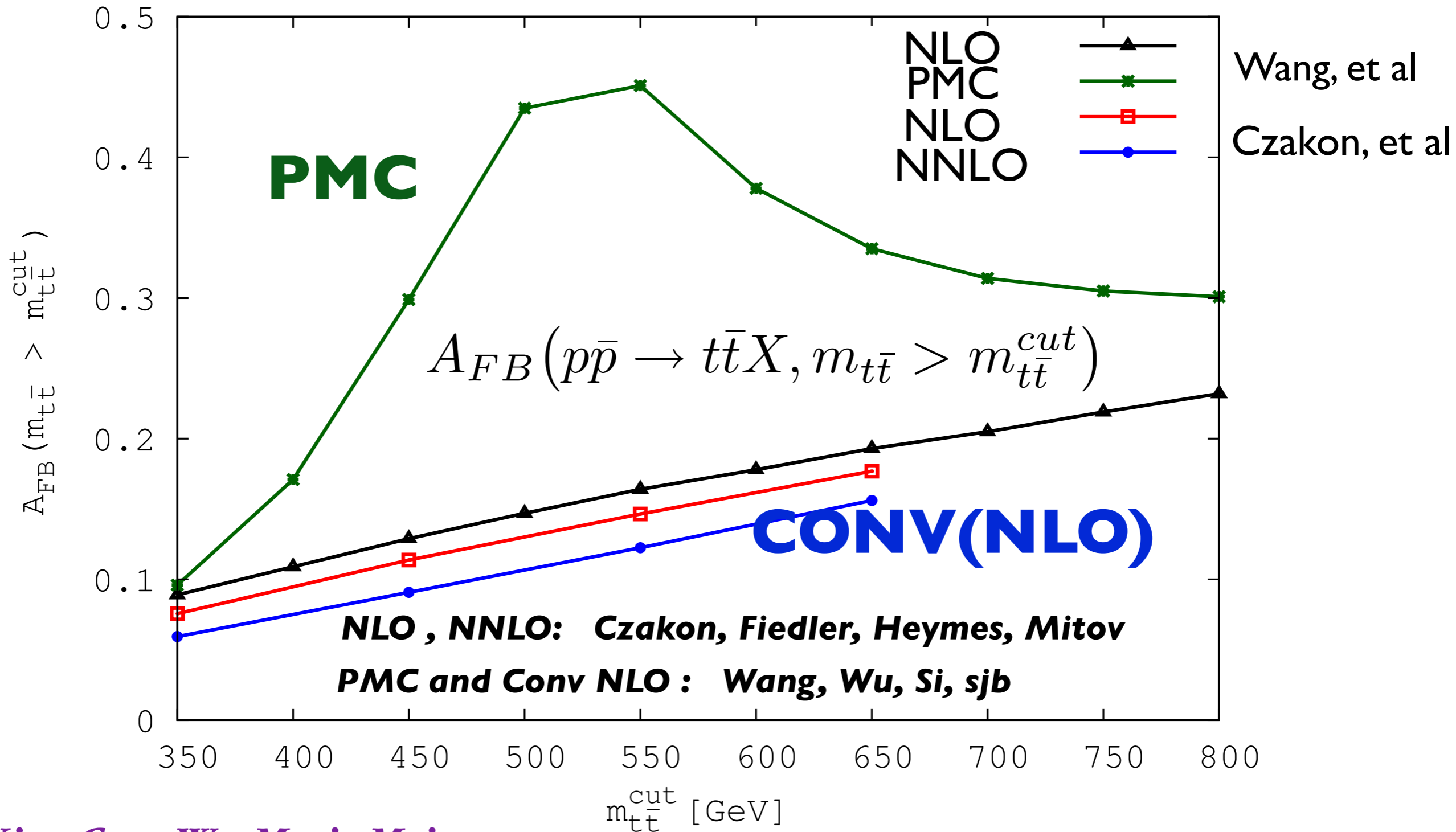
## Principle of Maximum Conformality

*A robot can compute the PMC scales*

NNLO QCD predictions for fully-differential top-quark pair production at the Tevatron

[arXiv:1601.05375](https://arxiv.org/abs/1601.05375)

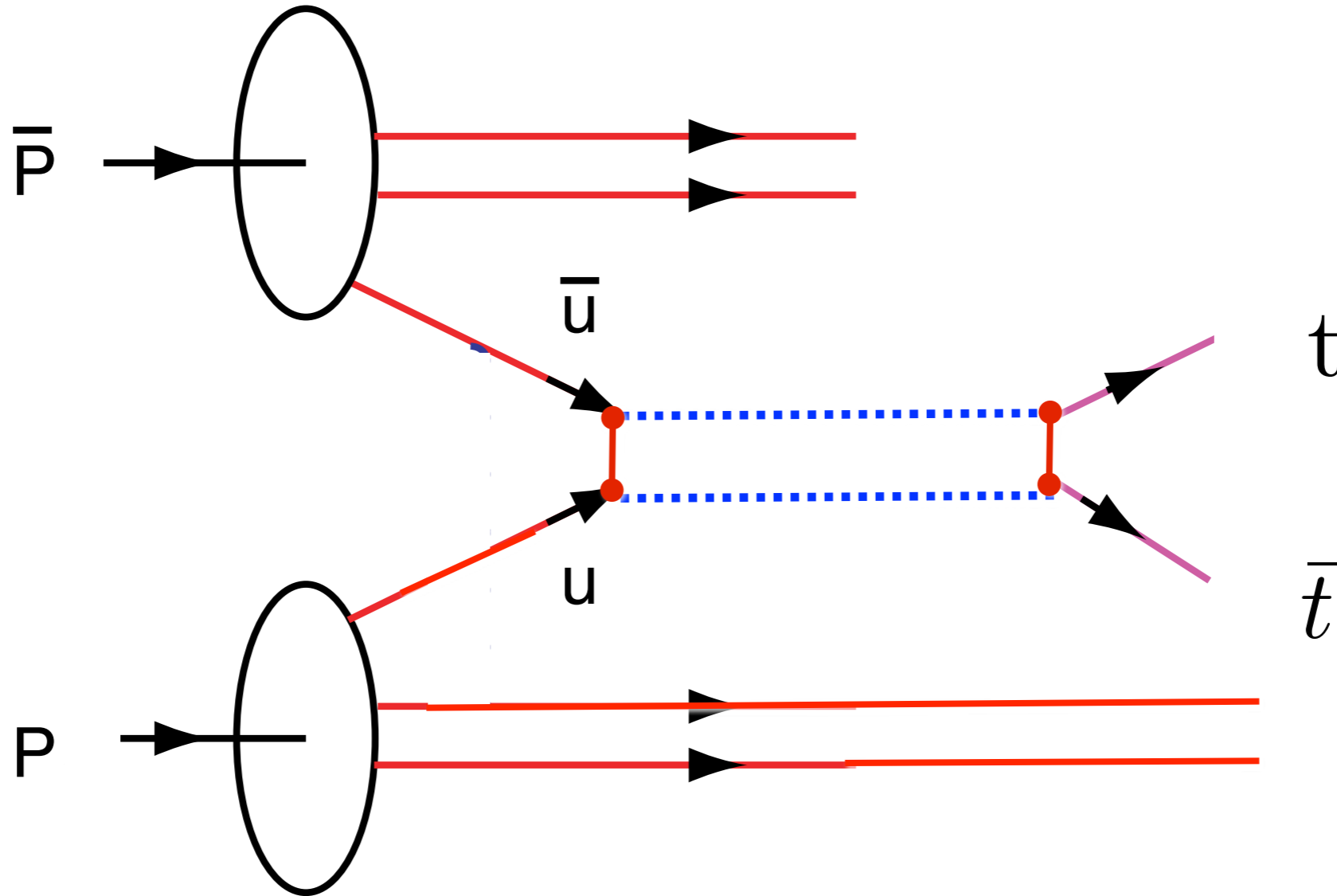
Michał Czakon,<sup>a</sup> Paul Fiedler,<sup>a</sup> David Heymes<sup>b</sup> and Alexander Mitov<sup>b</sup>



*Xing-Gang Wu, Martin Mojaza*  
*Leonardo di Giustino, SJB*

Predictions for the cumulative front-back asymmetry.

# Implications for the $\bar{p}p \rightarrow t\bar{t}X$ asymmetry at the Tevatron



***Interferes with Born term.***

*Small value of renormalization scale increases asymmetry, just as in QED*

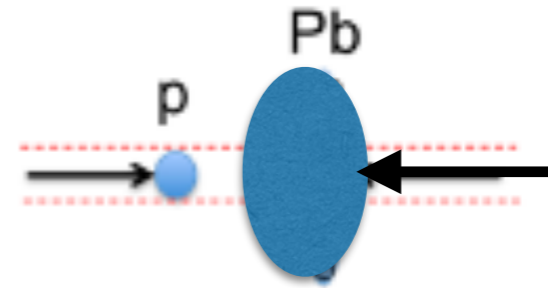
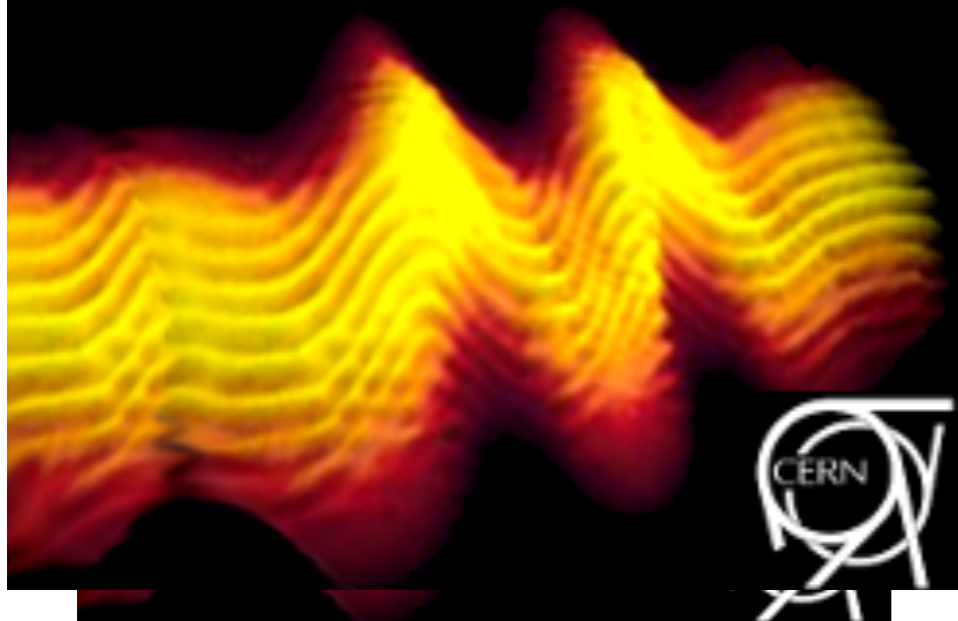
**Xing-Gang Wu, sjb**

# Features of BLM/PMC

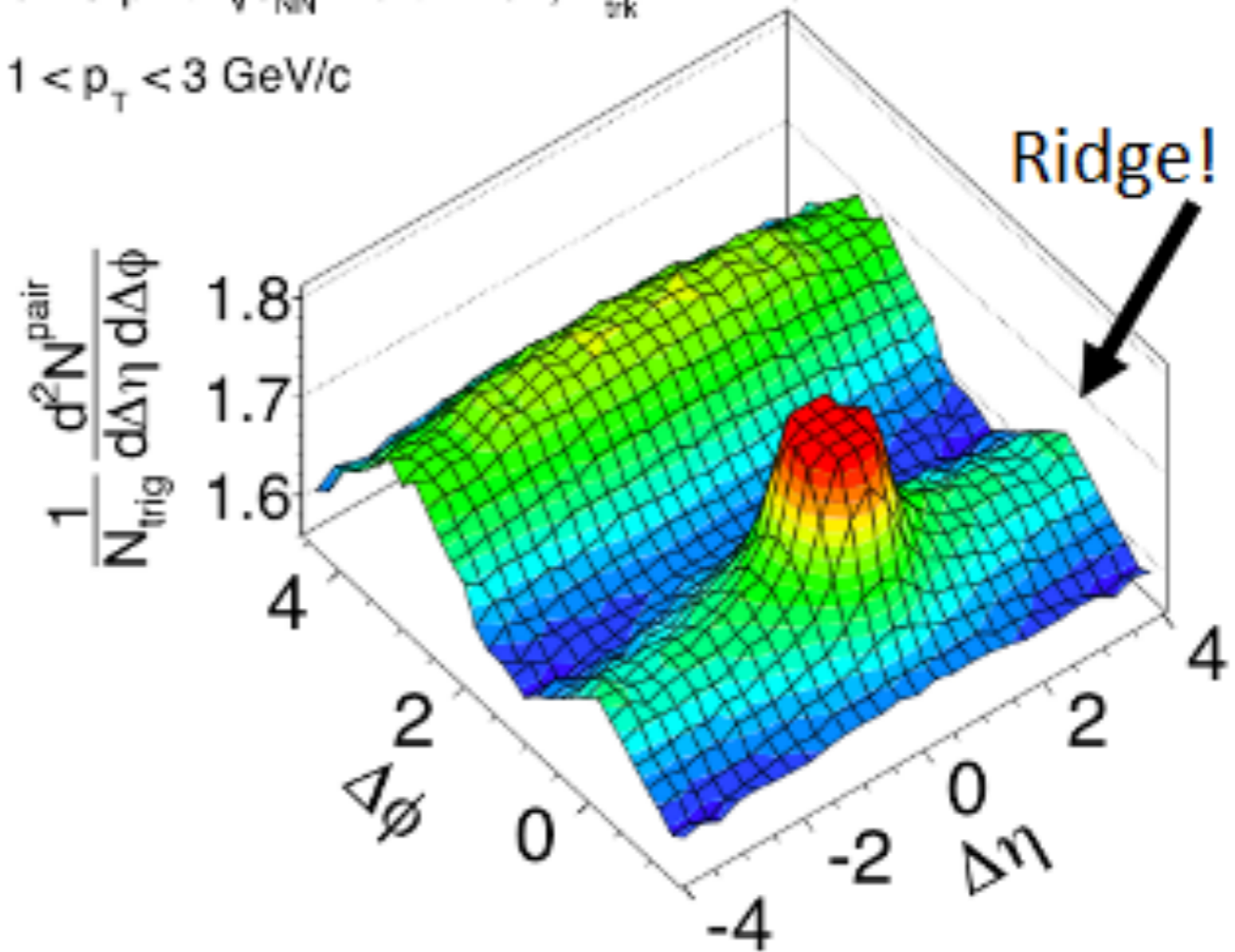
- **Predictions are scheme-independent at every order**
- **Matches conformal series**
- **Commensurate Scale Relations between observables: Generalized Crewther Relation (Kataev, Lu, Rathsmann, [sjb](#))**
- **No  $n!$  Renormalon growth**
- **New scale appears at each order;  $n_F$  determined at each order - matches virtuality of quark loops**
- **Multiple Physical Scales Incorporated (Hoang, Kuhn, Tuebner, [sjb](#))**
- **Rigorous: Satisfies all Renormalization Group Principles**
- **Realistic Estimate of Higher-Order Terms**
- **Same as Gell-Mann Low for QED  $N_C \rightarrow 0$**
- **GUT: Must use the same scale setting procedure for QED, QCD**
- **Eliminates unnecessary theory error**
- **Maximal sensitivity to new physics**
- **Example: BFKL intercept (Fadin, Kim, Lipatov, Pivovarov, [sjb](#))**

# Ridge phenomena in photon-photon collisions

PHOTON 2017  
CERN (Geneva)  
22 - 27 May 2017



CMS pPb  $\sqrt{s_{NN}} = 5.02$  TeV,  $N_{trk}^{offline} \geq 110$   
 $1 < p_T < 3$  GeV/c



Stan Brodsky



with Fred Goldhaber, Stan Glazek, Patryk Kubiczek, and Robert Brown

2017 International Conference on the Structure and Interactions of the Photon

22th International Workshop on Photon-Photon Collisions

International Workshop on High Energy Photon Colliders