



U.S. DEPARTMENT OF  
**ENERGY**

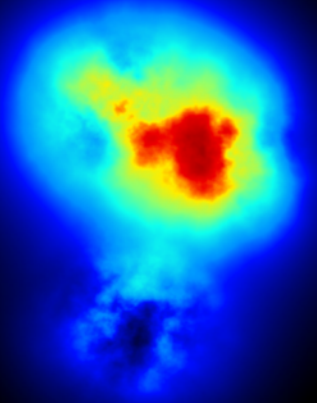
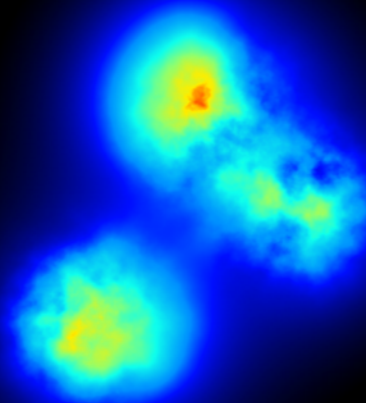
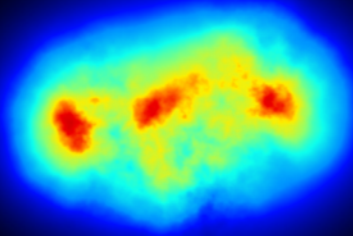
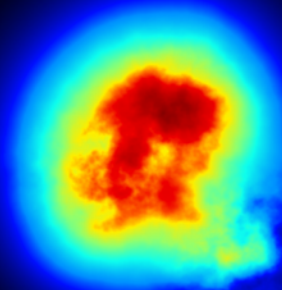
Office of  
Science



# EXCLUSIVE Q-QBAR PHOTOPRODUCTION AND PROTON STRUCTURE

Björn Schenke

Brookhaven National Laboratory



May 24, 2017  
PHOTON 2017  
CERN

# Introduction

Fundamental questions:

How are gluons distributed spatially in the proton?

Do we have access to the fluctuating shape of the proton?

Diffraction  $J/\Psi$  production in  $e+p$  provides access

... so do proton + heavy ion collisions

# Diffractive $J/\Psi$ production

H. Mäntysaari, B. Schenke, Phys. Rev. Lett. 117 (2016) 052301; Phys.Rev. D94 (2016) 034042

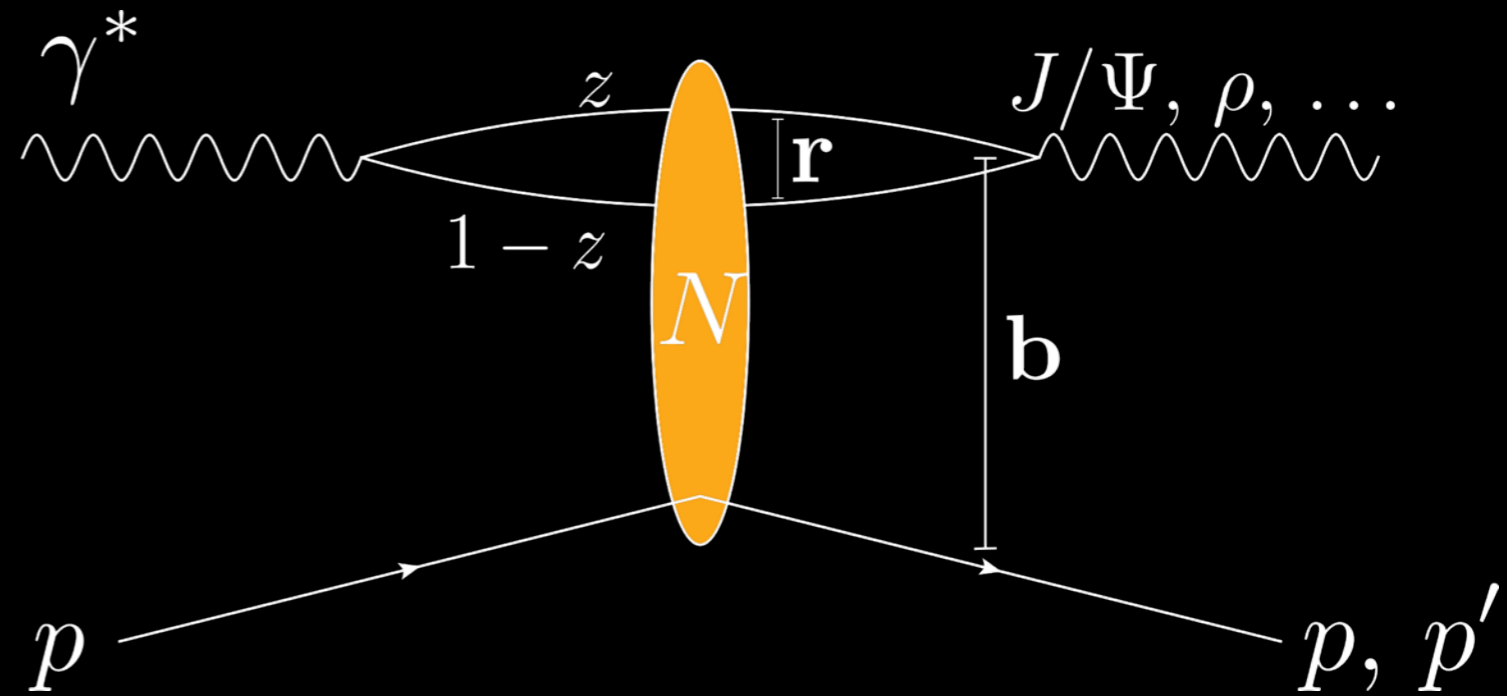
No exchange of color charge  
→ Large rapidity gap

Coherent diffraction:

Proton remains intact, Sensitive to average gluon distribution in the proton

Incoherent diffraction:

Proton breaks up, Sensitive to shape fluctuations



# CGC Framework $J/\Psi$ production

H. Mäntysaari, B. Schenke, *Phys. Rev. Lett.* 117 (2016) 052301; *Phys.Rev.* D94 (2016) 034042

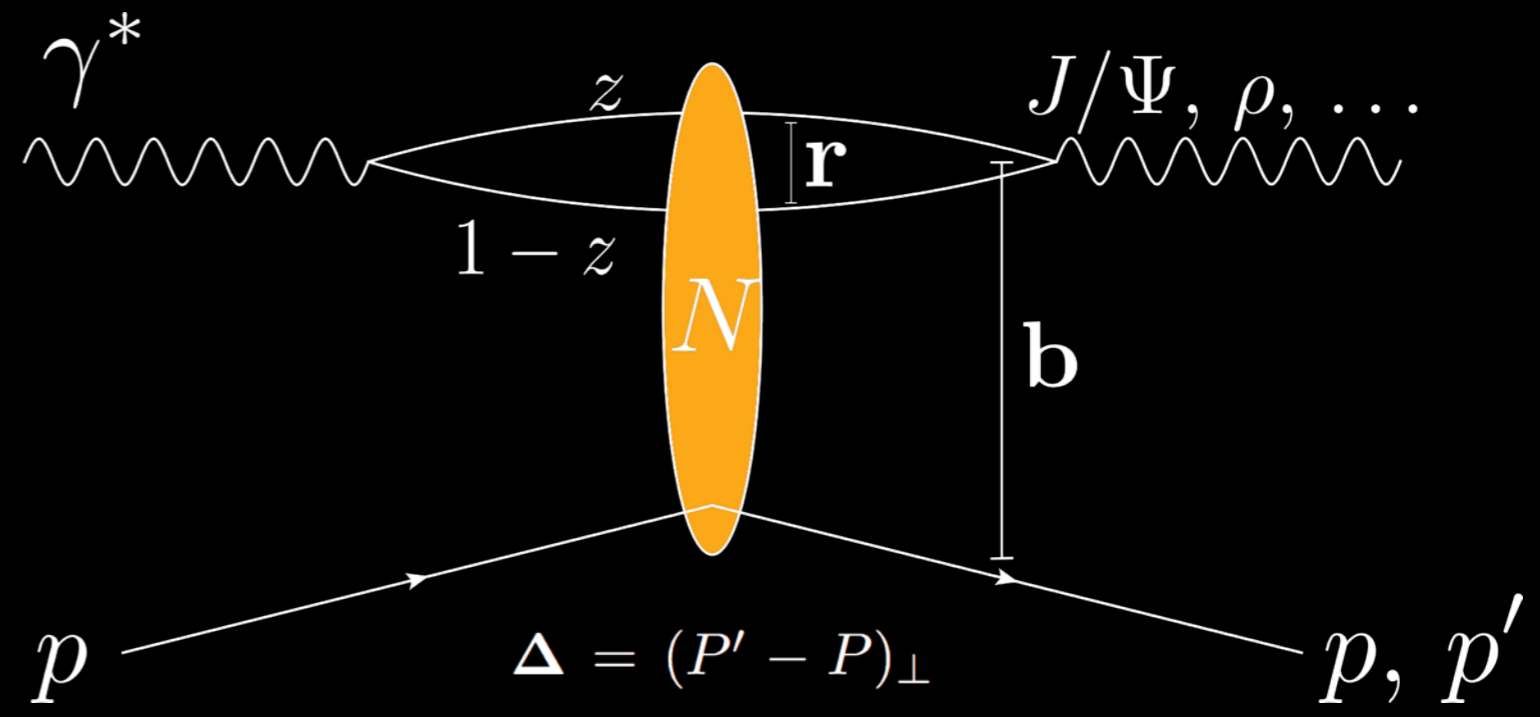
Diffractive eigenstates are color dipoles

at fixed  $r_T$  and  $b_T$

see

M. L. Good and W. D. Walker

*Phys. Rev.* 120 (1960) 1857.



Scattering amplitude

$$A \sim \int d^2 b dz d^2 r \psi^* \psi^V(r, z, Q^2) e^{-ib \cdot \Delta} N(r, x, b)$$

Dipole amplitude  $N$  determined in IPsat or IP-Glasma

# Averaging over the target

H. Mäntysaari, B. Schenke, Phys. Rev. Lett. 117 (2016) 052301; Phys.Rev. D94 (2016) 034042

COHERENT DIFFRACTION:  
TARGET STAYS INTACT

$$\frac{d\sigma^{\gamma^* p \rightarrow V p}}{dt} = \frac{1}{16\pi} \left| \langle \mathcal{A}^{\gamma^* p \rightarrow V p}(x_{\mathbb{P}}, Q^2, \Delta) \rangle \right|^2$$

INCOHERENT DIFFRACTION:  
TARGET BREAKS UP

$$\frac{d\sigma^{\gamma^* p \rightarrow V p^*}}{dt} = \frac{1}{16\pi} \left( \left\langle \left| \mathcal{A}^{\gamma^* p \rightarrow V p}(x_{\mathbb{P}}, Q^2, \Delta) \right|^2 \right\rangle - \left| \langle \mathcal{A}^{\gamma^* p \rightarrow V p}(x_{\mathbb{P}}, Q^2, \Delta) \rangle \right|^2 \right)$$

SENSITIVE TO FLUCTUATIONS!

SEE

H. I. MIETTINEN  
AND J. PUMPLIN  
PHYS. REV. D18 (1978) 1696

Y. V. KOVCHEGOV  
AND L. D. MCLERRAN  
PHYS. REV. D60 (1999) 054025

A. KOVNER AND  
U. A. WIEDEMANN  
PHYS. REV. D64 (2001) 114002

# IPsat model

Kowalski, Teaney, Phys.Rev. D68 (2003) 114005

Parametrize the dipole amplitude as

$$N(\vec{r}, x, \vec{b}) = 1 - \exp[-F(\vec{r}, x, \vec{b})]$$

with

$$F(\vec{r}, x, \vec{b}) = \frac{\pi^2}{2N_c} \vec{r}^2 \alpha_s(\mu^2) x g(x, \mu^2) T_\rho(\vec{b})$$

gluon density  
including DGLAP to  
scale  $\mu^2 = 4/\vec{r}^2 + \mu_0^2$

impact parameter  
dependence

Saturation scale:  $Q_s^2(x, \vec{b}) = 2/r_s^2(x, \vec{b})$

with  $r_s$  defined via  $N(\vec{r}_s, x, \vec{b}) = 1 - e^{1/2}$

# Geometric fluctuations in the IPsat model

Kowalski, Teaney, Phys.Rev. D68 (2003) 114005

All parameters are fit to HERA DIS data

Thickness function  $T_p(\vec{b})$  normally assumed to be Gaussian

Here we introduce a substructure to the proton by defining:

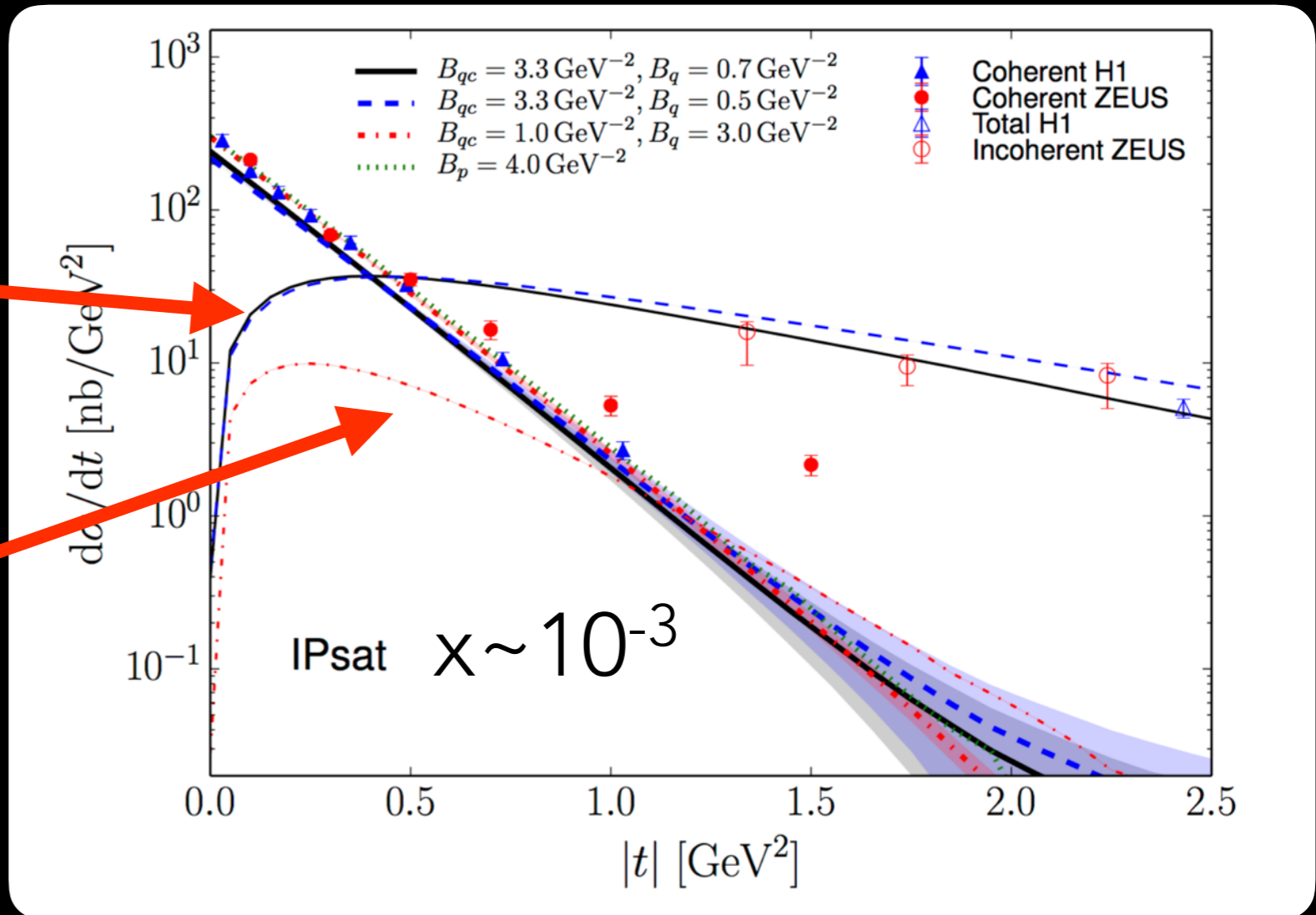
$$T_p(\vec{b}) = \sum_{i=1}^3 T_q(\vec{b} - \vec{b}_i)$$

with  $T_q(\vec{b}) \sim e^{-b^2/2B_q}$

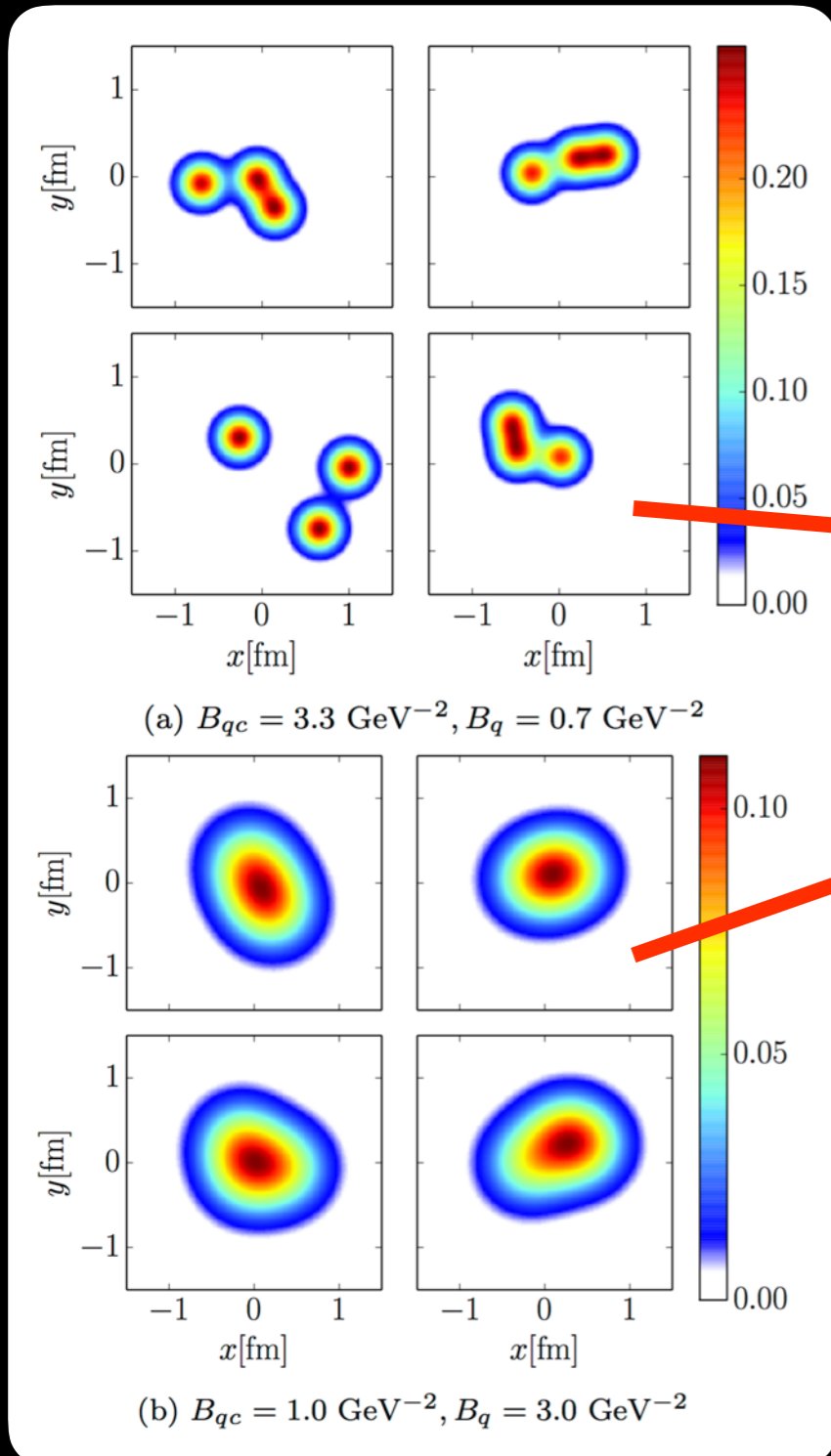
where the positions  $\vec{b}_i$  are sampled from a Gaussian with width  $B_{qc}$

# J/ψ production from fluctuating proton

H. Mäntysaari, B. Schenke, Phys. Rev. Lett. 117 (2016) 052301  
 Phys.Rev. D94 (2016) 034042



H1 collaboration, Eur. Phys. J. C46 (2006) 585,  
 Phys. Lett. B568 (2003) 205  
 ZEUS collaboration, Eur. Phys. J. C24 (2002) 345  
 Eur. Phys. J. C26 (2003) 389





# IP-Glasma model

B.Schenke, P.Tribedy, R.Venugopalan, PRL108, 252301 (2012), PRC86, 034908 (2012)

Take  $Q_s^2(x, \vec{b})$  from IPsat for a given geometry

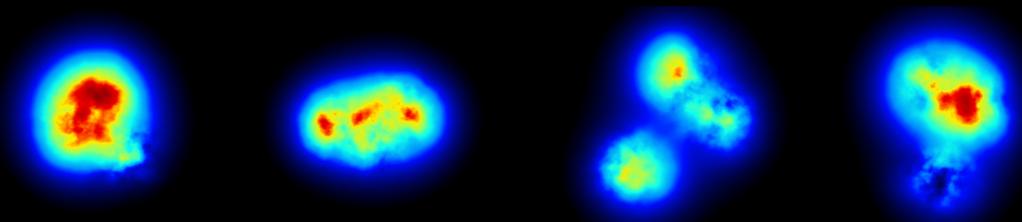
Sample color charges  $\rho(x, \vec{b})$  from distribution with variance  $\sim Q_s^2(x, \vec{b})$

Gluon fields in the proton follow from Yang-Mills eqs.

$$A^i(\vec{b}) = -\frac{i}{g} V(\vec{b}) \partial_i V^\dagger(\vec{b})$$

with Wilson lines:  $V(\vec{b}) = P \exp \left( -ig \int dx^- \frac{\rho(x^-, \vec{b})}{\nabla^2 + m^2} \right)$

Traces of Wilson lines:



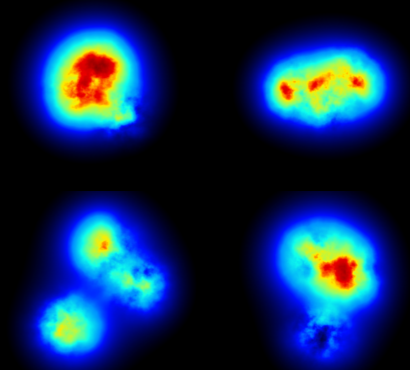
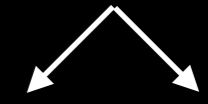
# IP-Glasma results

H. Mäntysaari, B. Schenke, *Phys. Rev. Lett.* 117 (2016) 052301; *Phys.Rev. D*94 (2016) 034042

Geometric + color charge fluctuations

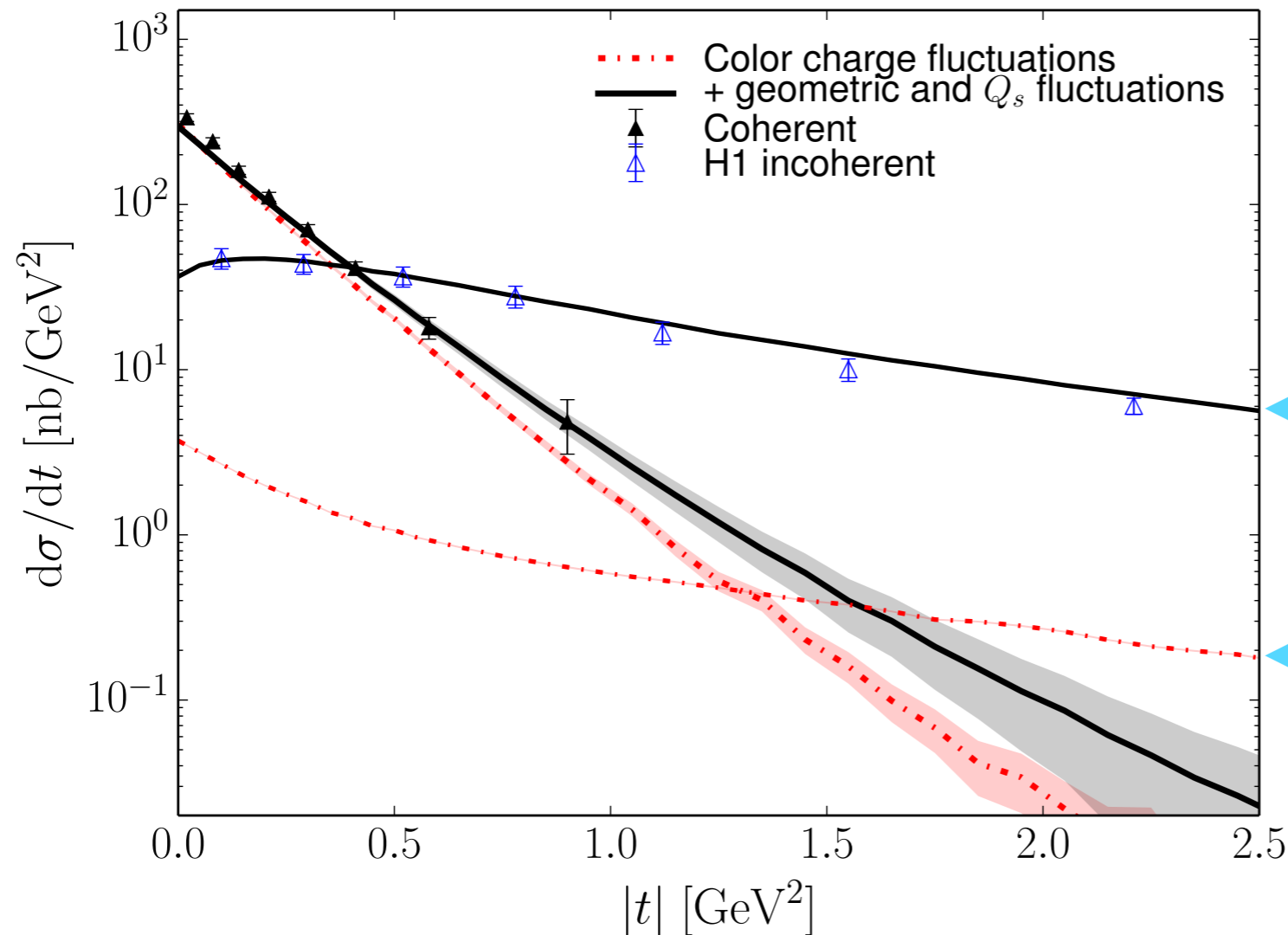
Dipole amp.:  $N(\vec{r}, x_{\mathbb{P}}, \vec{b}) = N(\vec{x} - \vec{y}, x_{\mathbb{P}}, (\vec{x} + \vec{y})/2) = 1 - \text{Tr} V(\vec{x}) V^\dagger(\vec{y}) / N_c$

Wilson lines



tuned shape fluctuations

round proton

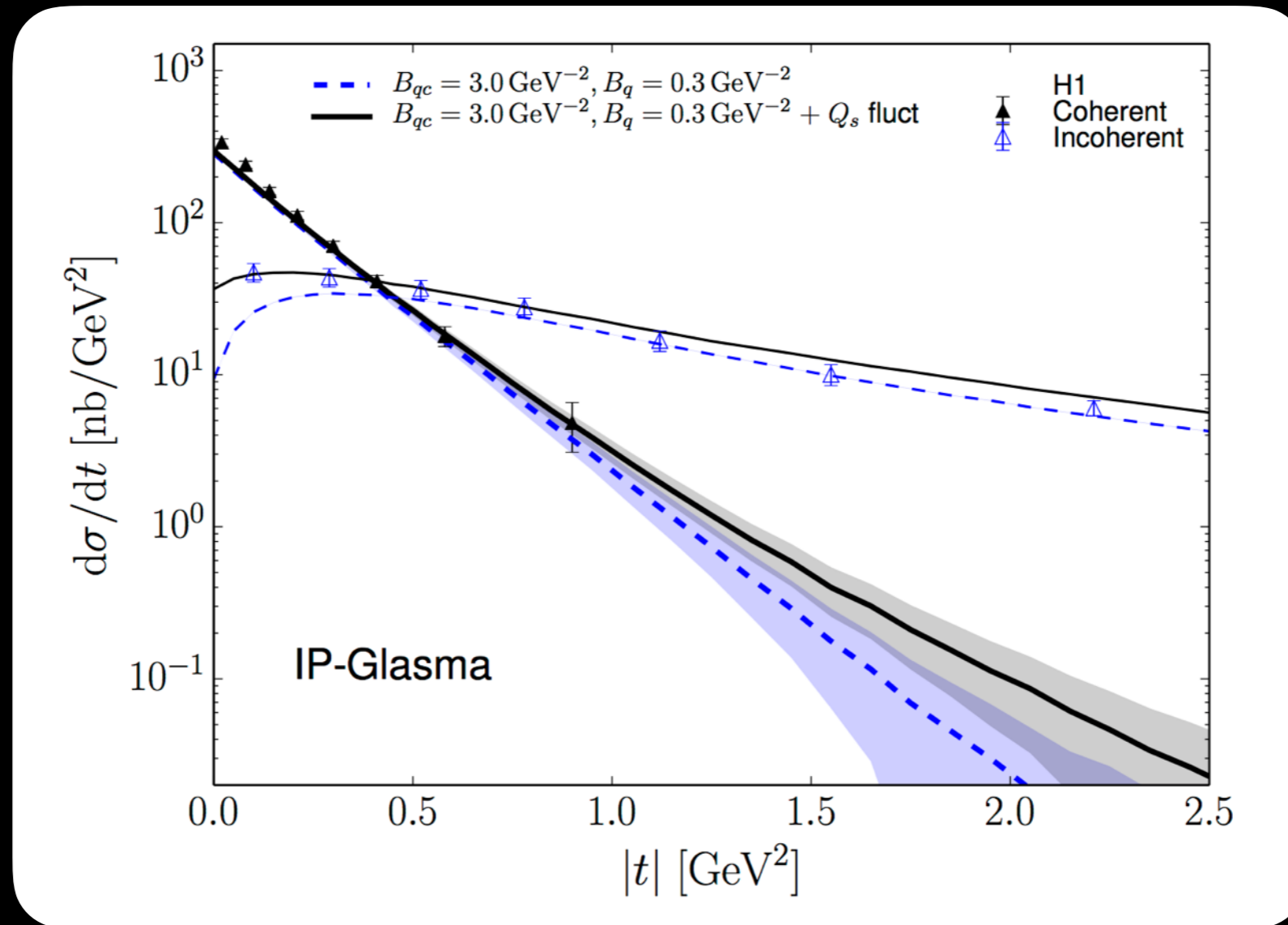


H1 Collaboration, *Eur. Phys. J. C*73 (2013) no. 6 2466

# Effect of $Q_s$ fluctuations

H. Mäntysaari, B. Schenke, Phys. Rev. Lett. 117 (2016) 052301; Phys.Rev. D94 (2016) 034042

$$P(\ln Q_s^2 / \langle Q_s^2 \rangle) = \frac{1}{\sqrt{2\pi}\sigma} \exp \left[ -\frac{\ln^2 Q_s^2 / \langle Q_s^2 \rangle}{2\sigma^2} \right]$$



$\sigma=0.5$

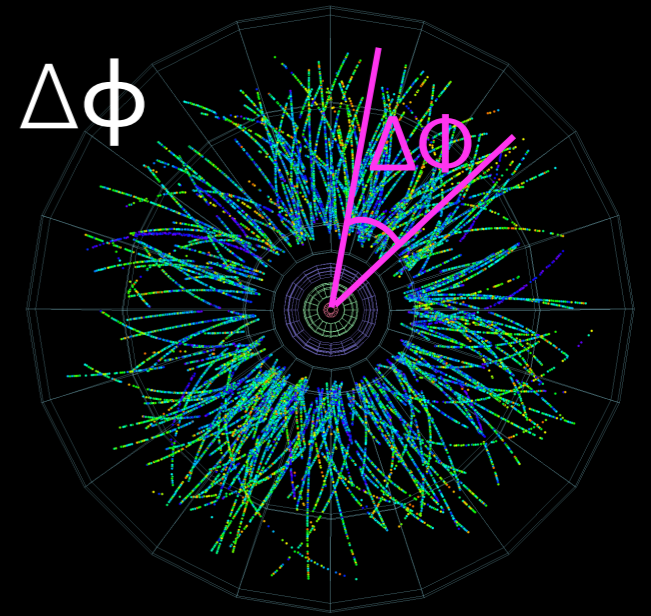
Experimental data: H1 collaboration, JHEP 1005 (2010) 032

# Effect on p+A collisions: Correlations

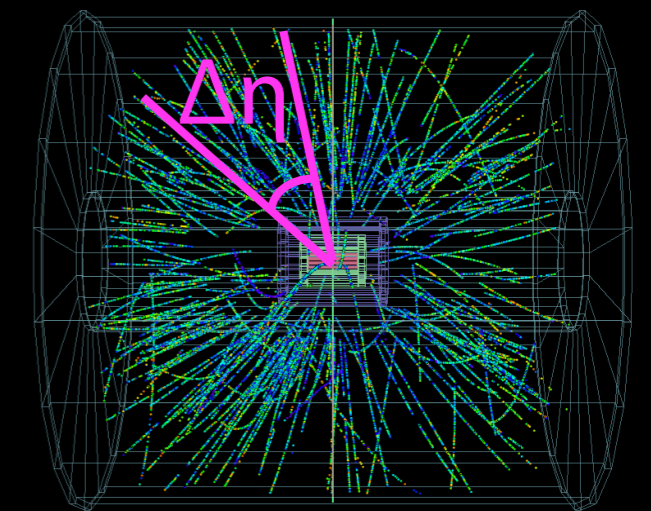
2-particle correlation as a function of  $\Delta\eta$  and  $\Delta\phi$

$\Delta\eta$ : DIFFERENCE IN PSEUDO-RAPIDITY

$\Delta\phi$ : DIFFERENCE IN AZIMUTHAL ANGLE



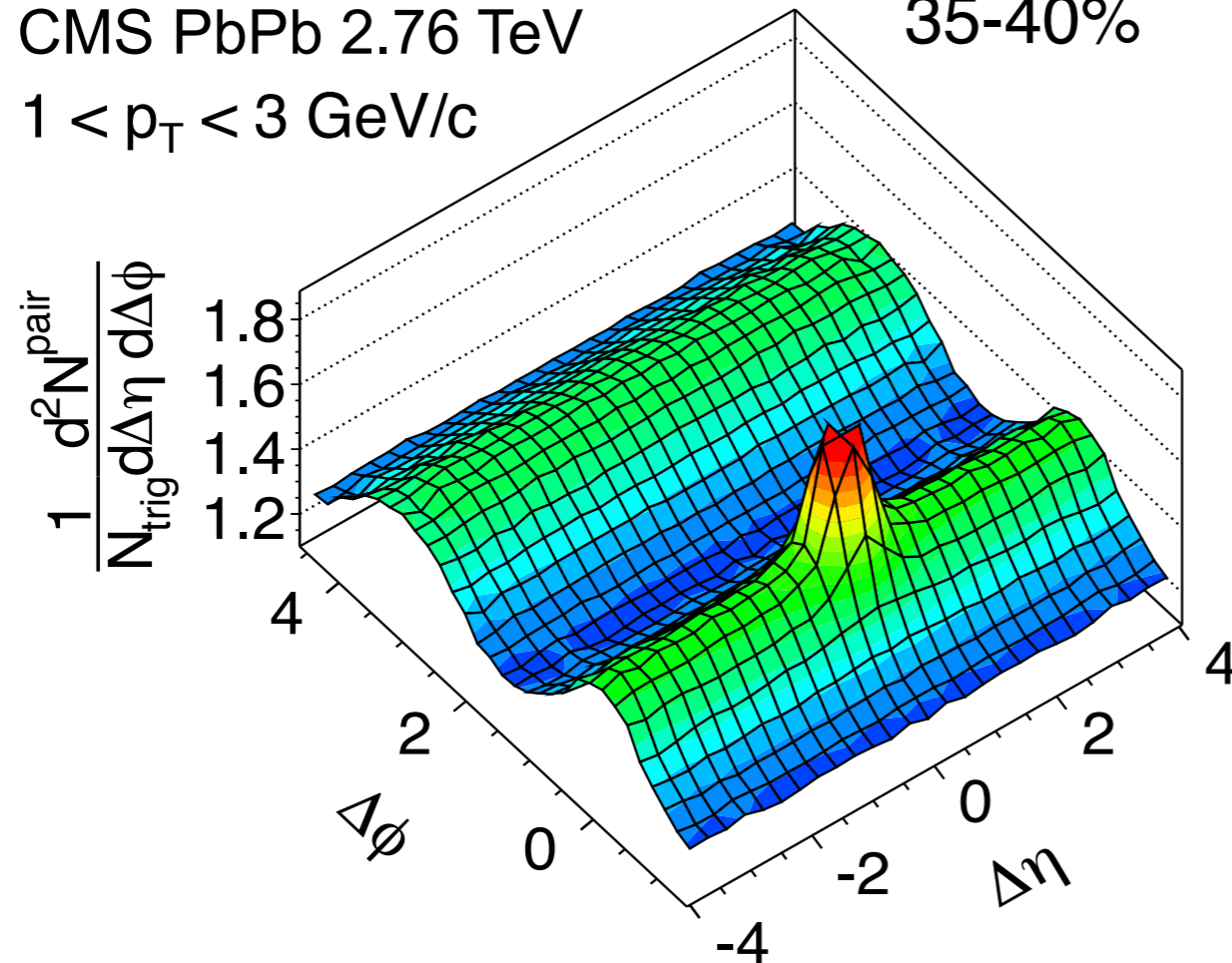
$\Delta\phi$ : DIFFERENCE  
IN AZIMUTHAL ANGLE



$\Delta\eta$ : DIFFERENCE  
IN PSEUDO-RAPIDITY

CMS PbPb 2.76 TeV  
 $1 < p_T < 3$  GeV/c

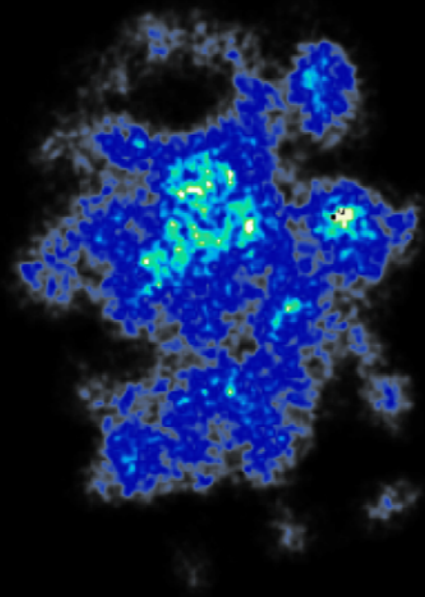
35-40%



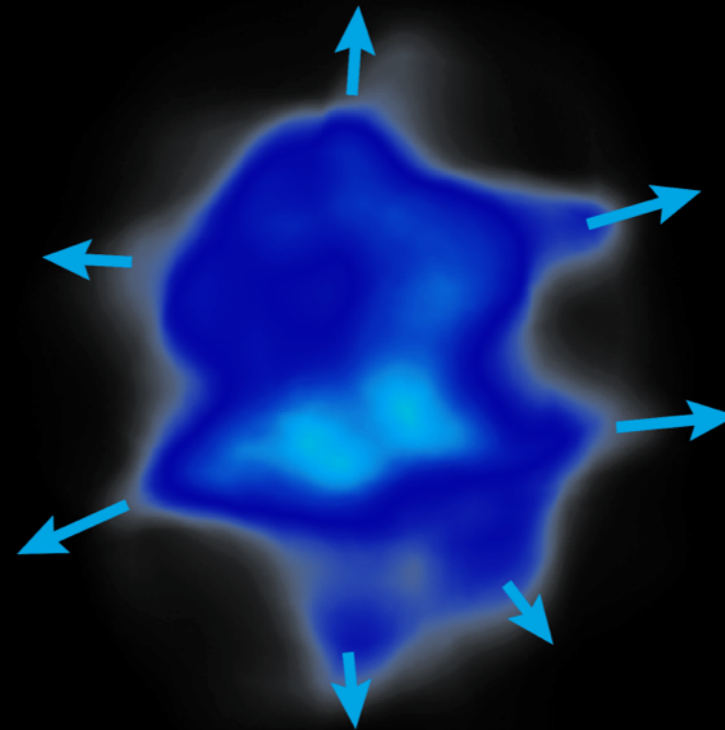
CMS COLL., EUR. PHYS. J. C72 (2012)

# Interpretation: Strong final state effects

- Long range  $\Delta\eta$  correlations emerge from early times (causality)
- Azimuthal structure formed by the medium response to the fluctuating initial transverse geometry



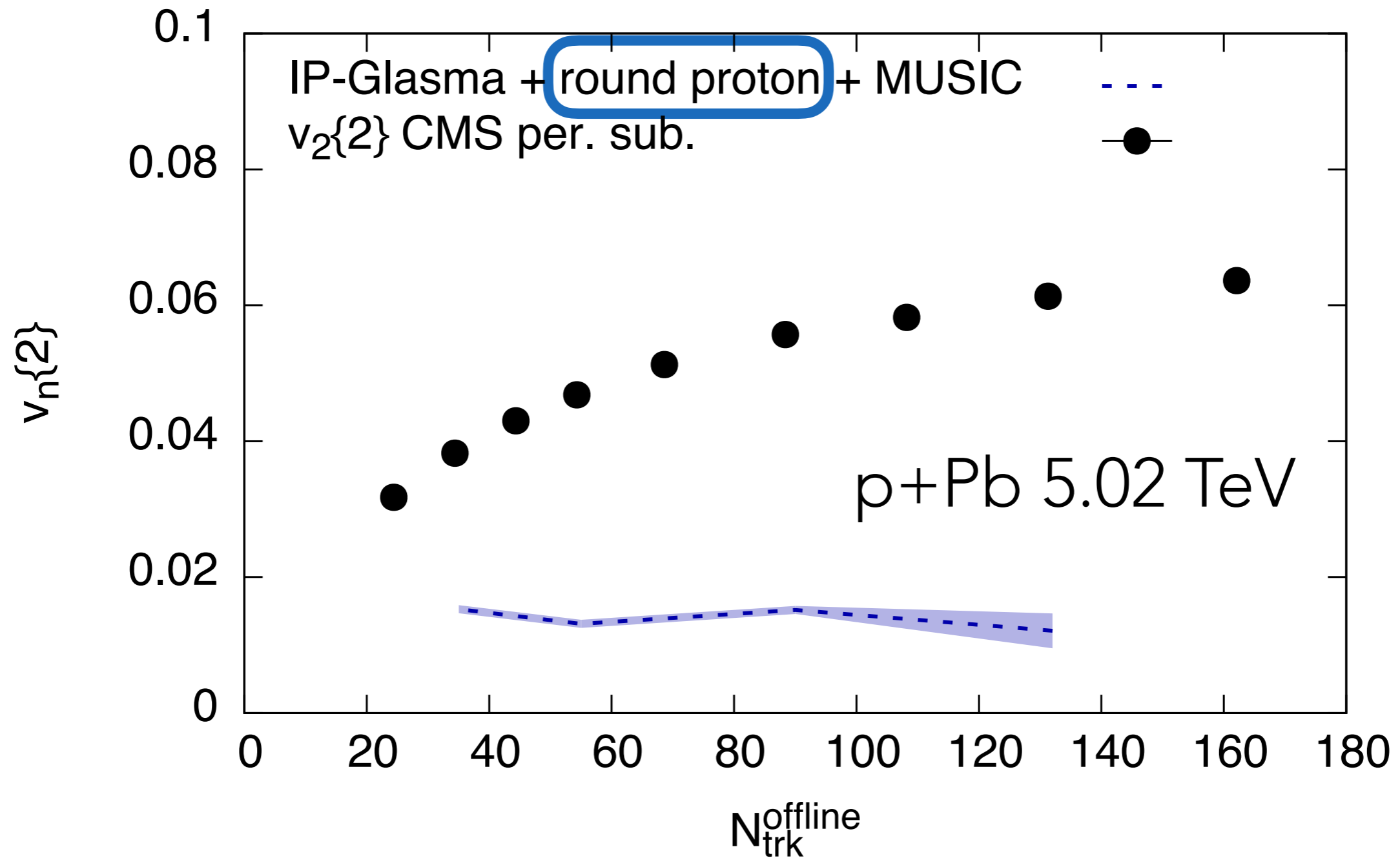
Initial energy density  
distribution



Hydrodynamic  
expansion

# IP-Glasma+MUSIC (hydrodynamics) results

B. Schenke, R. Venugopalan, Phys. Rev. Lett. 113, 102301 (2014)

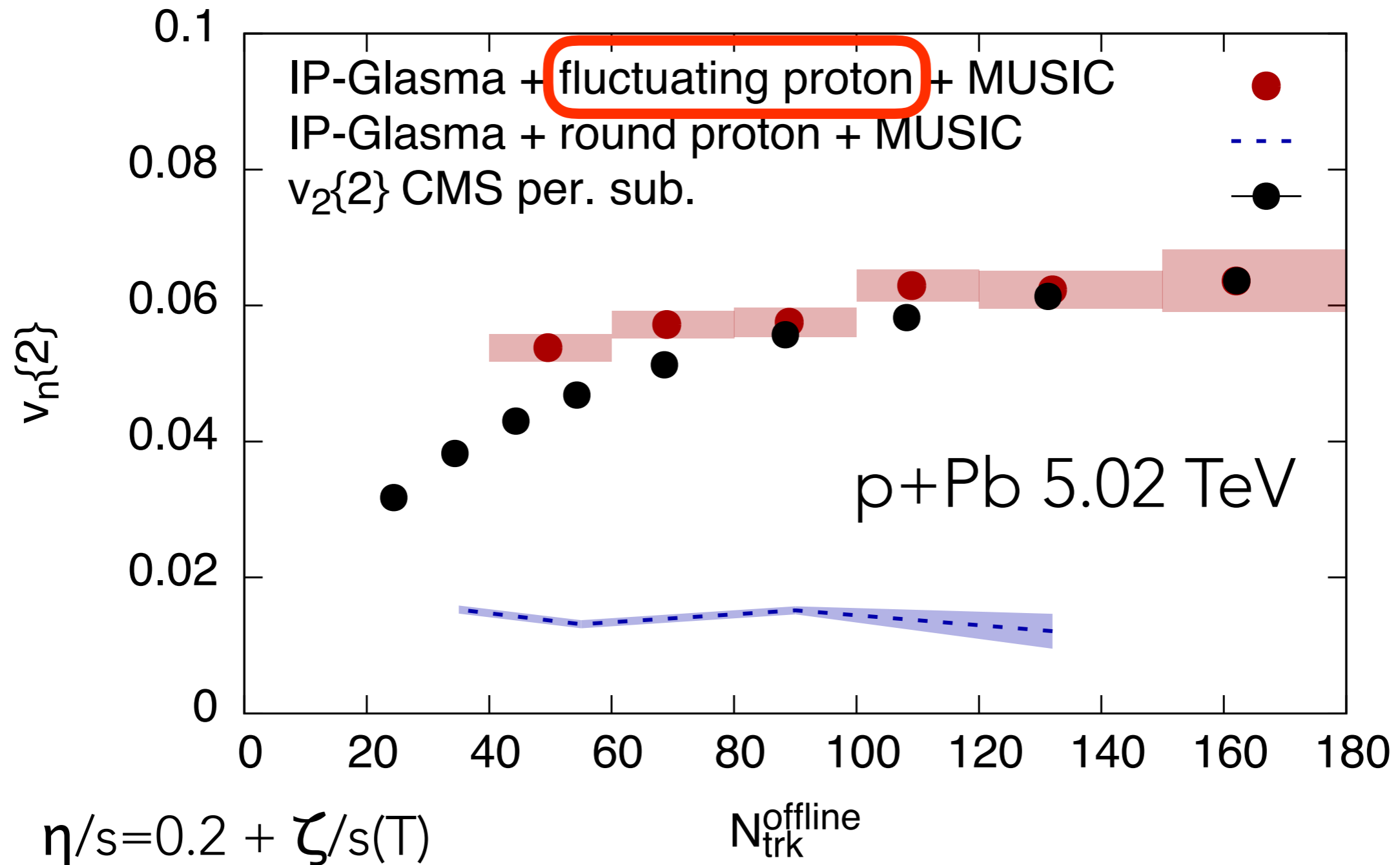


Experimental data: CMS Collaboration, Phys.Lett. B724, 213 (2013)

# IP-Glasma+MUSIC (hydrodynamics) results

B. Schenke, R. Venugopalan, Phys. Rev. Lett. 113, 102301 (2014)

H. Mäntysaari, B. Schenke, C. Shen, P. Tribedy, arXiv:1705.03177



Experimental data: CMS Collaboration, Phys.Lett. B724, 213 (2013)

# Subnucleonic fluctuations in large nuclei

H. Mäntysaari, B. Schenke, arXiv:1703.09256

UltraPeripheral heavy ion Collisions (UPC)

At  $|b_T| > 2R_A$  one nucleus acts as a photon source

Two sources of fluctuations:

Sample nucleon positions from Woods-Saxon

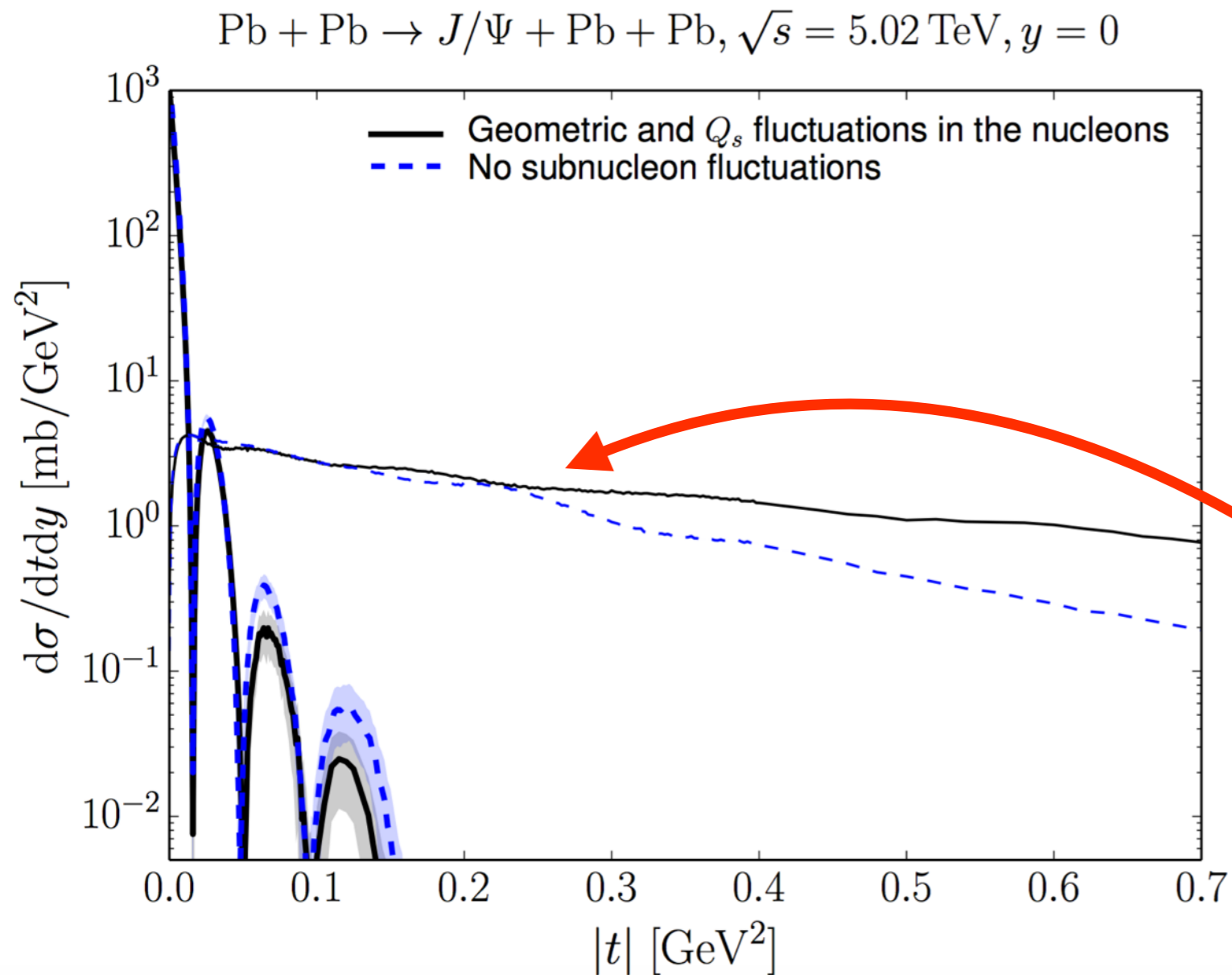
Sample constituent quark structure for each nucleon

We use the IPsat model for this analysis



# Subnucleonic fluctuations in large nuclei

H. Mäntysaari, B. Schenke, arXiv:1703.09256



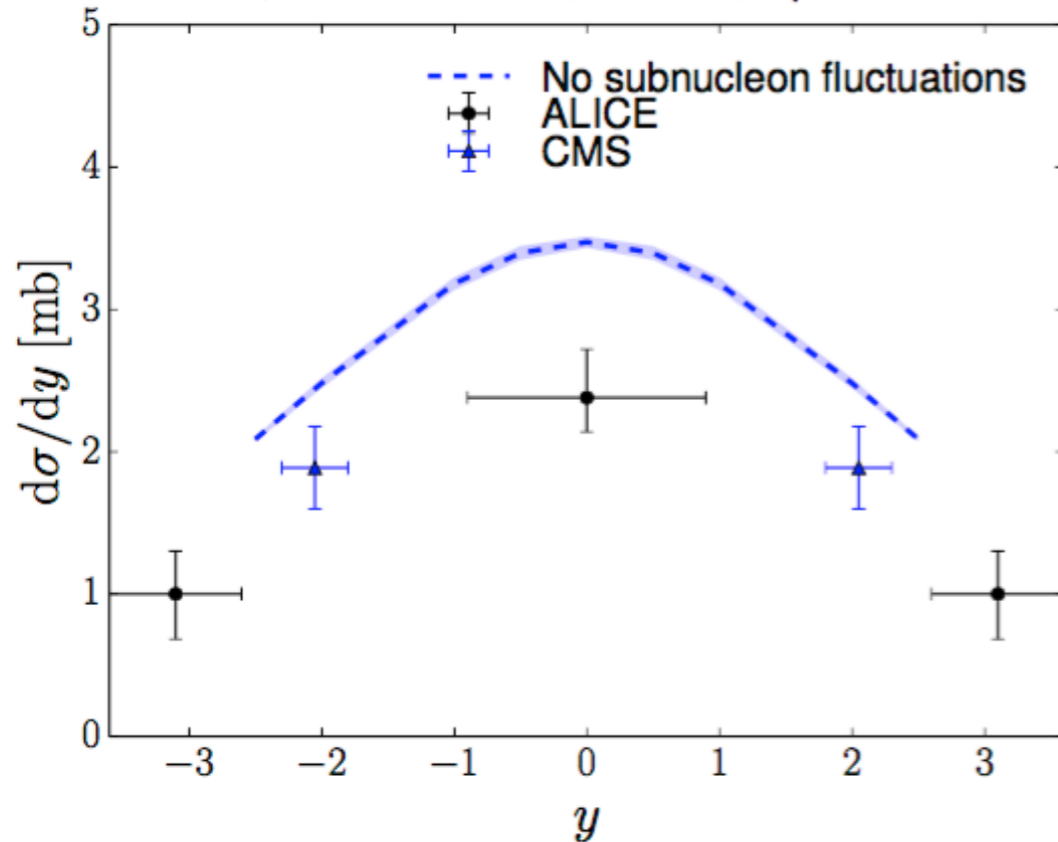
- Small  $|t|$ : fluctuations of nucleon positions
- Large  $|t|$ : fluctuations at subnucleon scale
- **Incoherent slope changes** at  $|t| \approx 0.25$  GeV<sup>2</sup>  $\rightarrow$  0.4 fm which is size of hot spots

Coherent: thick lines  
Incoherent: thin lines

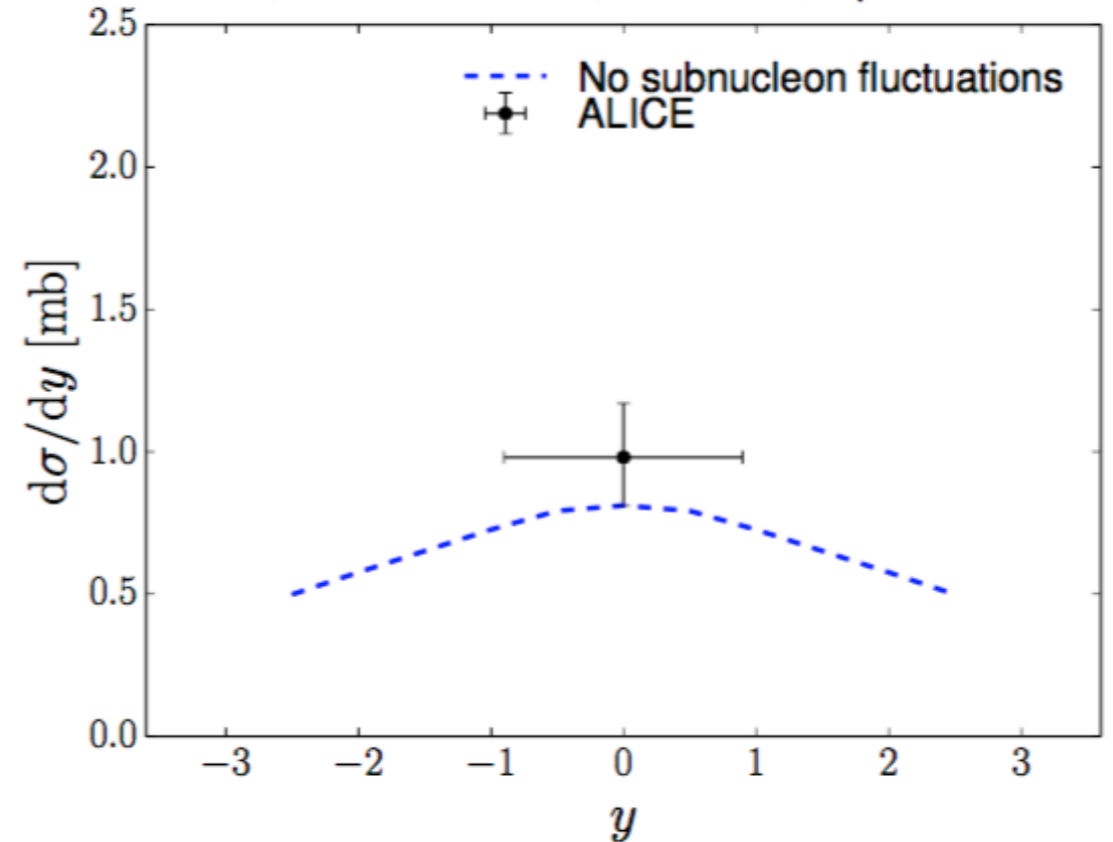
# LHC data - no subnucleonic fluctuations

H. Mäntysaari, B. Schenke, arXiv:1703.09256

Pb + Pb  $\rightarrow$   $J/\Psi$  + Pb + Pb (coherent),  $\sqrt{s_{NN}} = 2760$  GeV



Pb + Pb  $\rightarrow$   $J/\Psi$  + Pb + Pb\* (incoherent),  $\sqrt{s_{NN}} = 2760$  GeV

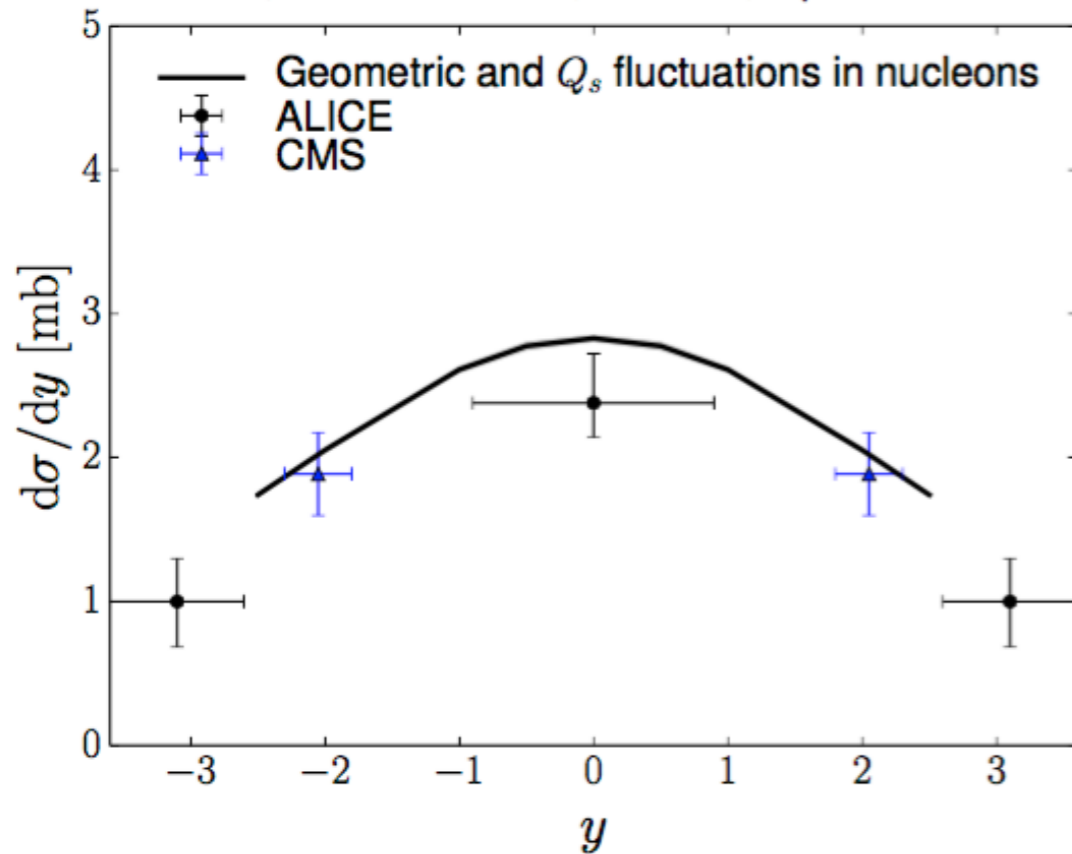


- Only fluctuations of nucleon positions
- Coherent cross section overestimated, incoherent underestimated
- ~ 20-30% normalization uncertainty from the  $J/\Psi$  wave function

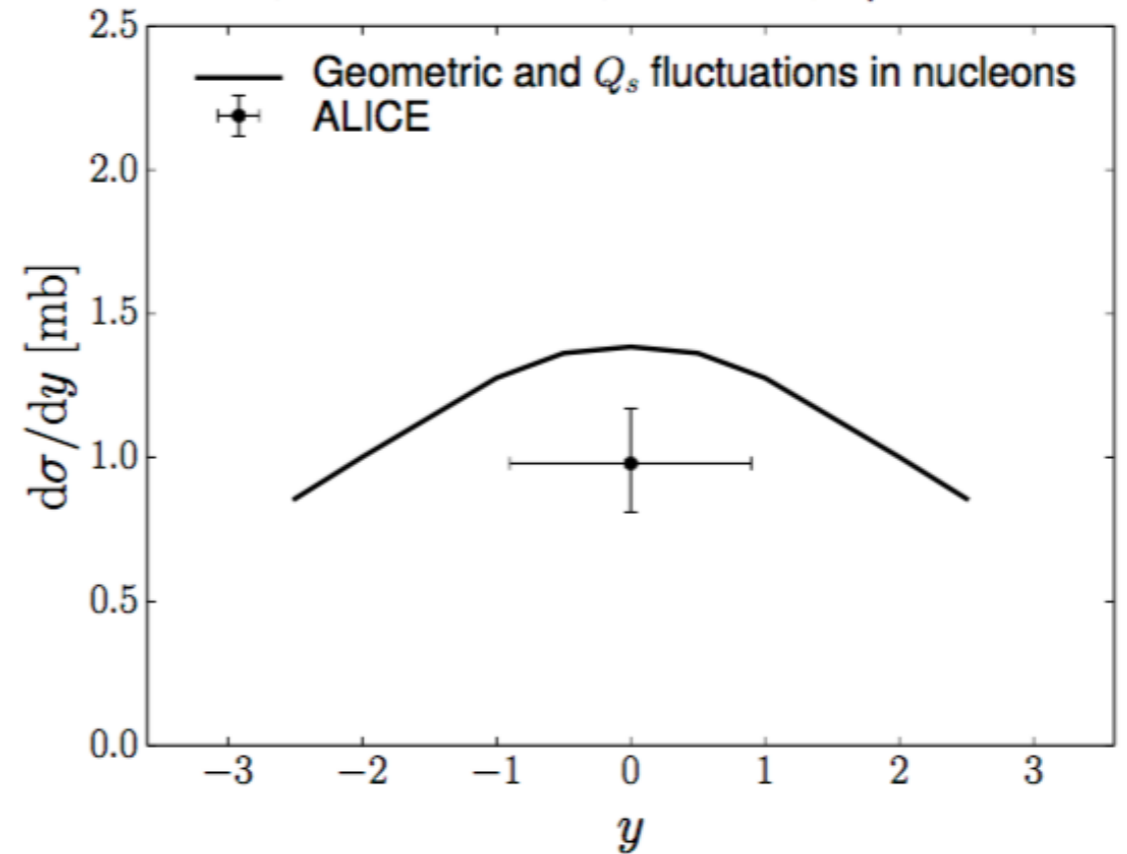
# LHC data - with subnucleonic fluctuations

H. Mäntysaari, B. Schenke, arXiv:1703.09256

Pb + Pb  $\rightarrow$   $J/\Psi$  + Pb + Pb (coherent),  $\sqrt{s_{NN}} = 2760$  GeV



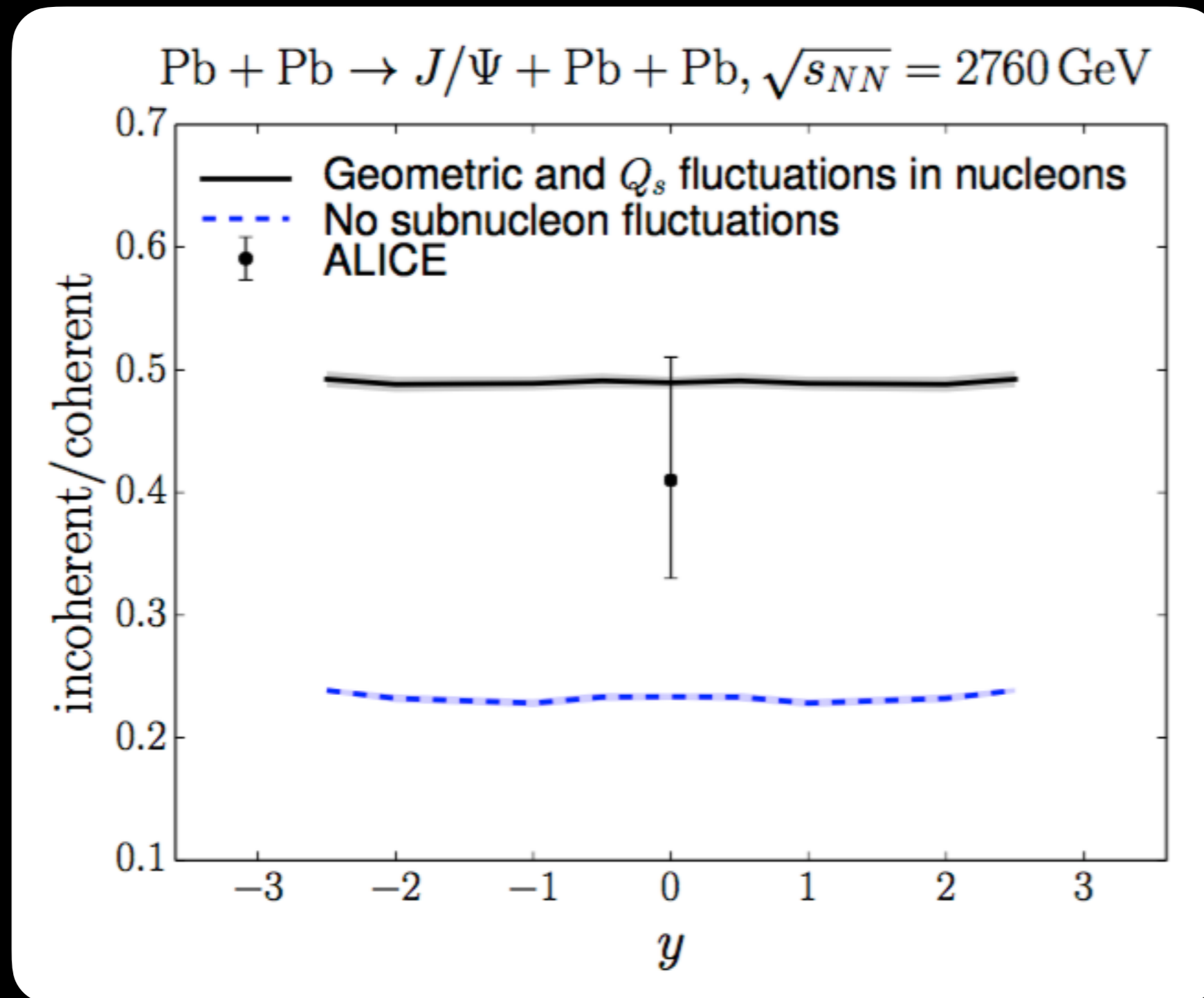
Pb + Pb  $\rightarrow$   $J/\Psi$  + Pb + Pb\* (incoherent),  $\sqrt{s_{NN}} = 2760$  GeV



- Same subnucleonic fluctuations as used for protons earlier
- Both cross sections slightly above the data
- $\sim$  20-30% normalization uncertainty from the  $J/\Psi$  wave function

# Ratio incoherent/coherent cross sections

H. Mäntysaari, B. Schenke, arXiv:1703.09256



# Summary

- Shape fluctuations of the proton's gluon distribution are needed to describe incoherent diffractive vector meson data from HERA
- Constrained fluctuating proton shape compatible with anisotropic flow in p+Pb collisions
- Sub-nucleonic fluctuations also affect incoherent diffractive cross section in ultra-peripheral A+A collisions
- Next step: Go from IPsat to explicit JIMWLK evolution and describe  $F_2$  and diffractive data - Modification of MV initial condition necessary

# BACKUP

# Why a variance?

H. I. Miettinen and J. PumpLin, Phys. Rev. D18 (1978) 1696

Simple model: Target particle  $\rightarrow$  average optical potential

$$|B\rangle = \sum_k C_k |\psi_k\rangle$$

beam particle  $\swarrow$   $\nwarrow$  linear comb. of diffractive eigenstates

$$\text{Im}T |\psi_k\rangle = A_k |\psi_k\rangle$$

Imaginary part of scattering amplitude  $\swarrow$   $\nwarrow$  Probability for  $\psi_k$  to interact with target

$$\langle B|B\rangle = \sum_k |C_k|^2 = 1$$

# Why a variance?

H. I. Miettinen and J. PumpLin, Phys. Rev. D18 (1978) 1696

Total diffractive cross section:

$$\frac{d\sigma_{\text{diff}}}{d^2\vec{b}} = \sum_k |\langle \psi_k | \text{Im}T | B \rangle|^2 = \sum_k |C_k|^2 A_k^2 = \langle A^2 \rangle$$

Elastic scattering amplitude:

$$\langle B | \text{Im}T | B \rangle = \sum_k |C_k|^2 A_k = \langle A \rangle$$

Average over absorption coefficients, weighted according to their probability of occurrence in the particle B

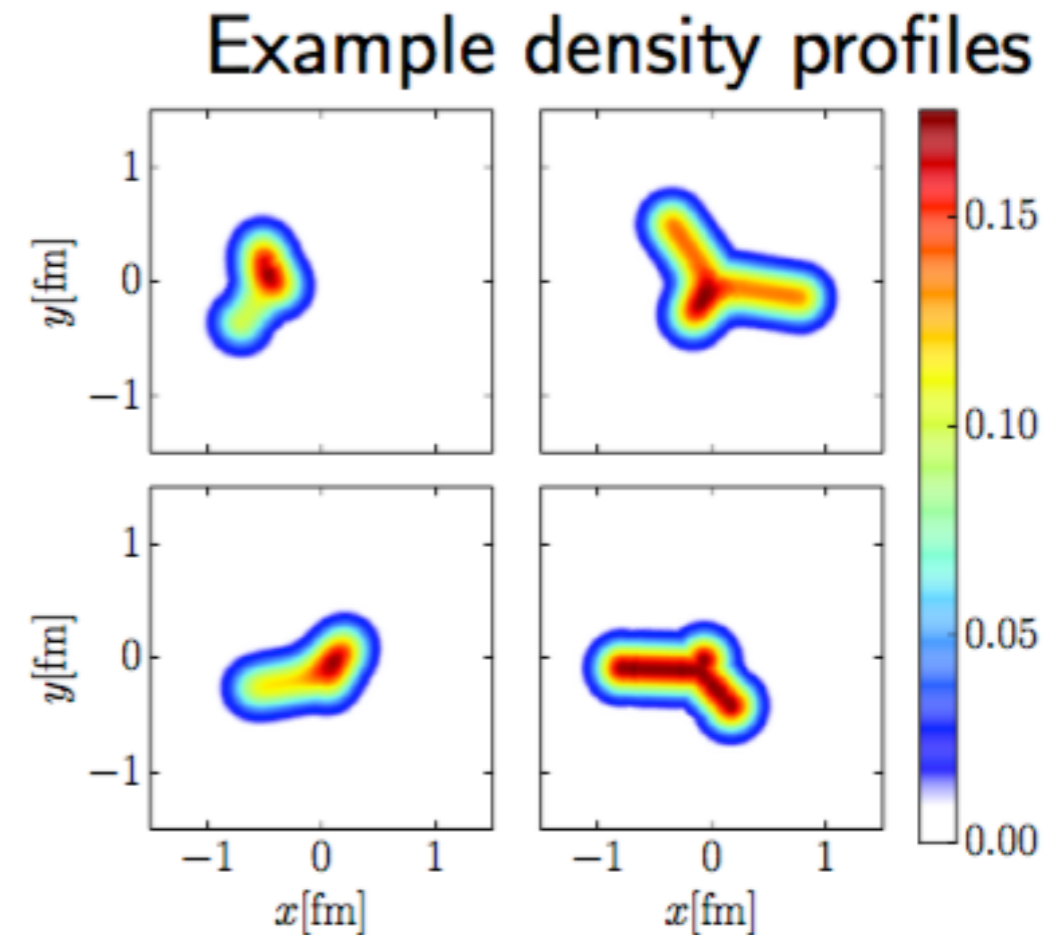
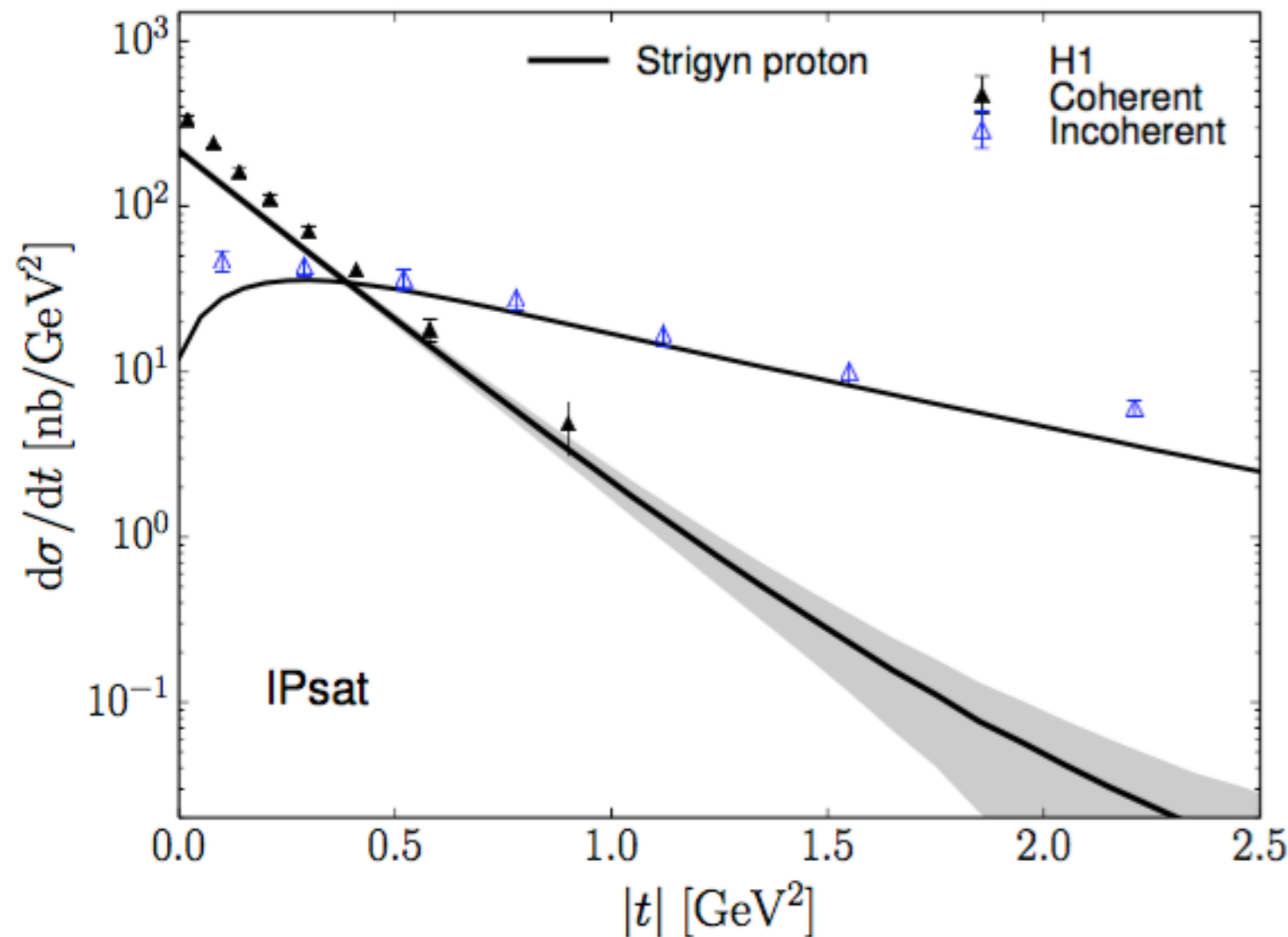
Elastic cross section:  $\frac{d\sigma_{\text{el}}}{d^2\vec{b}} = \langle A \rangle^2$

Inelastic diffractive cross section:  $\frac{d\sigma_{\text{inel}}}{d^2\vec{b}} = \langle A^2 \rangle - \langle A \rangle^2$



# Lumpiness matters, not details of the density profile

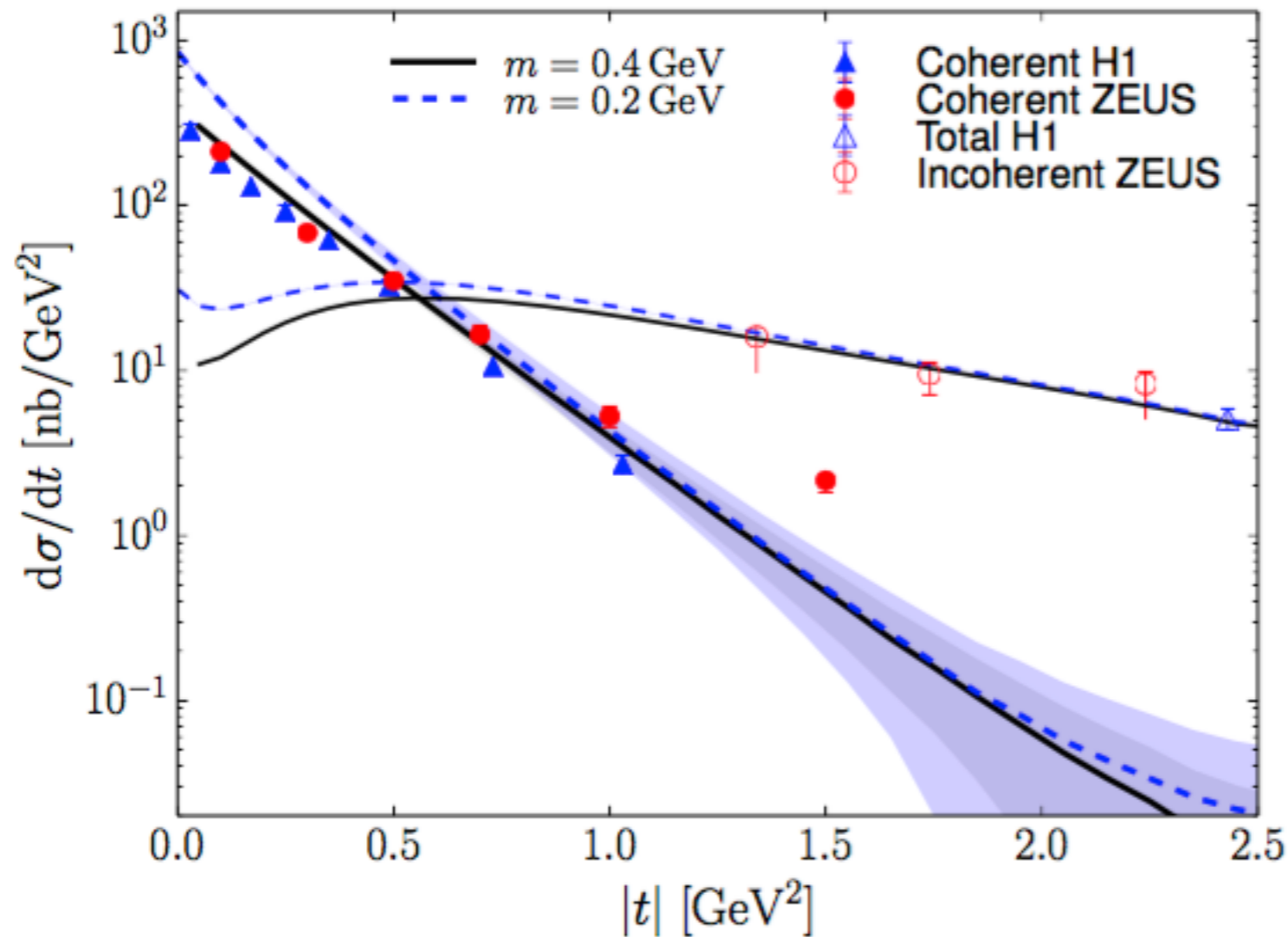
3 valence quarks that are connected by "color flux tubes":  
Gaussian tubes connecting quarks. Also good description of the data



H.M, B. Schenke, PRD94 034042

Flux tubes implementation following results from hep-lat/0606016, used also e.g. in 1307.5911

# Insensitivity on infrared cutoff

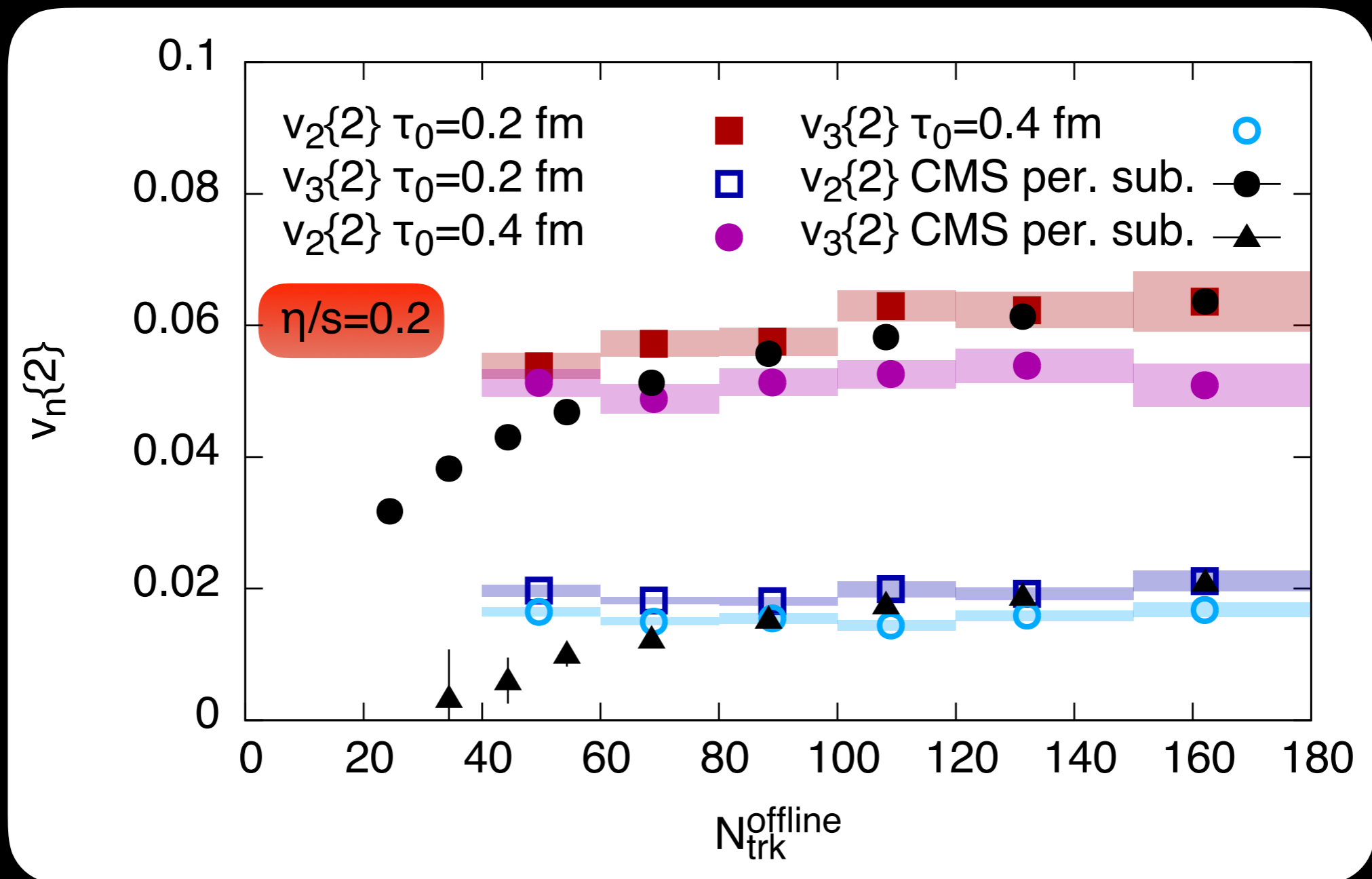


IP-Glasma: IR cutoff  $m \sim \Lambda_{\text{QCD}}$  to regulates long distance coulomb tails

- Proton size depends on  $m$
- No sensitivity at large  $|t|$

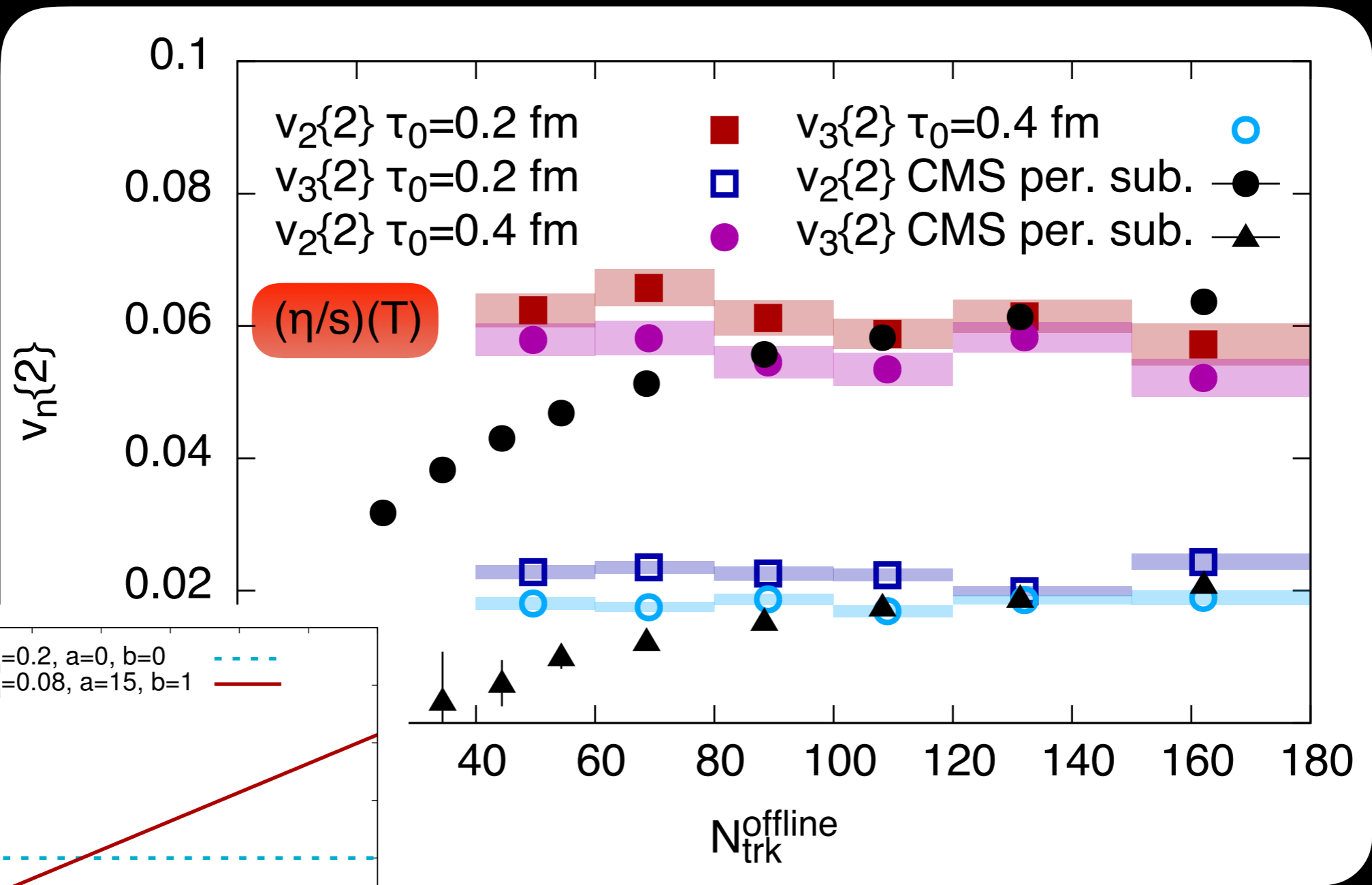
# Integrated anisotropic flow

H. Mäntysaari, B. Schenke, C. Shen, P. Tribedy, arXiv:1705.03177



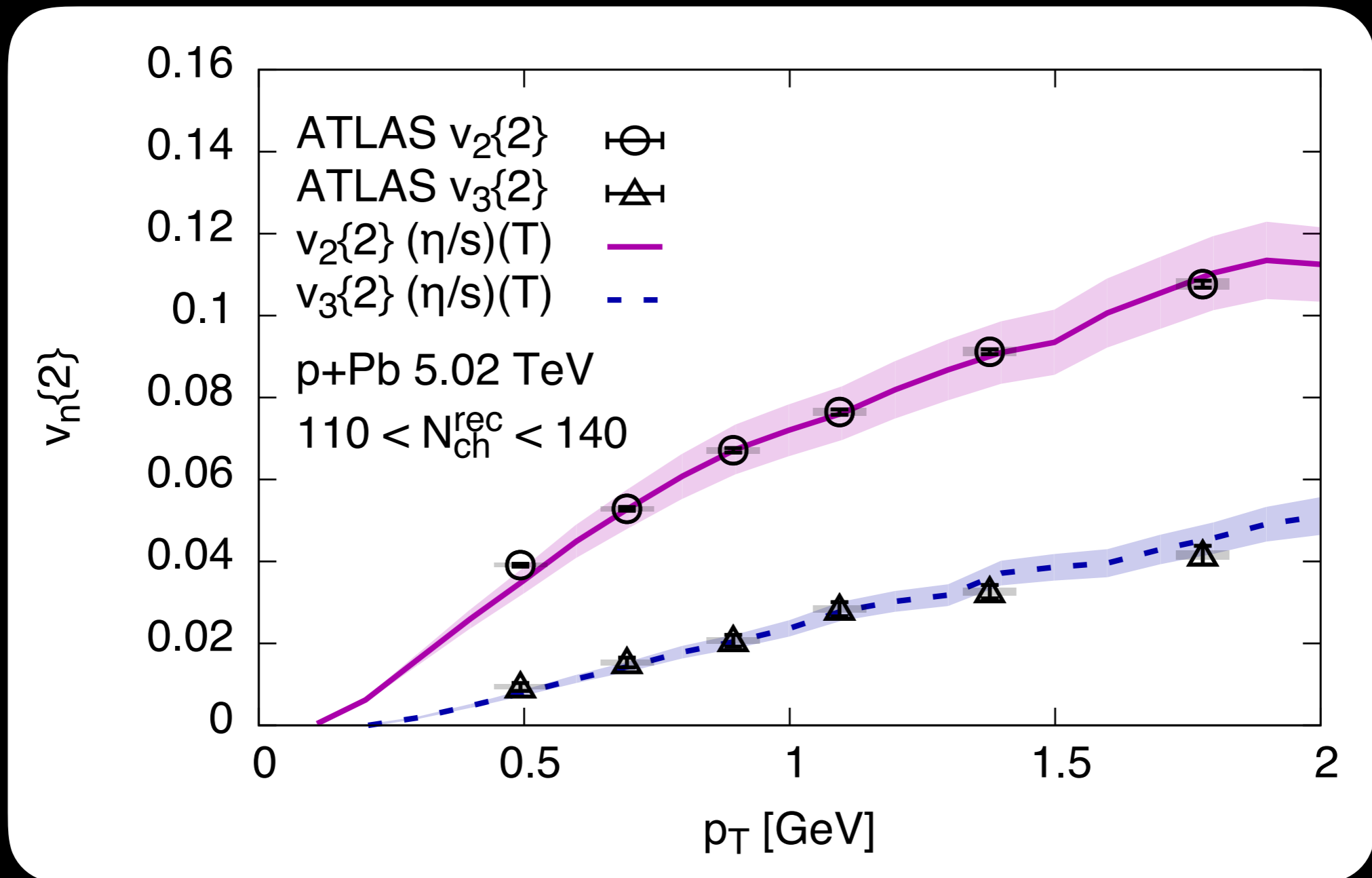
# Integrated anisotropic flow

H. Mäntysaari, B. Schenke, C. Shen, P. Tribedy, arXiv:1705.03177



# $p_T$ -differential anisotropic flow

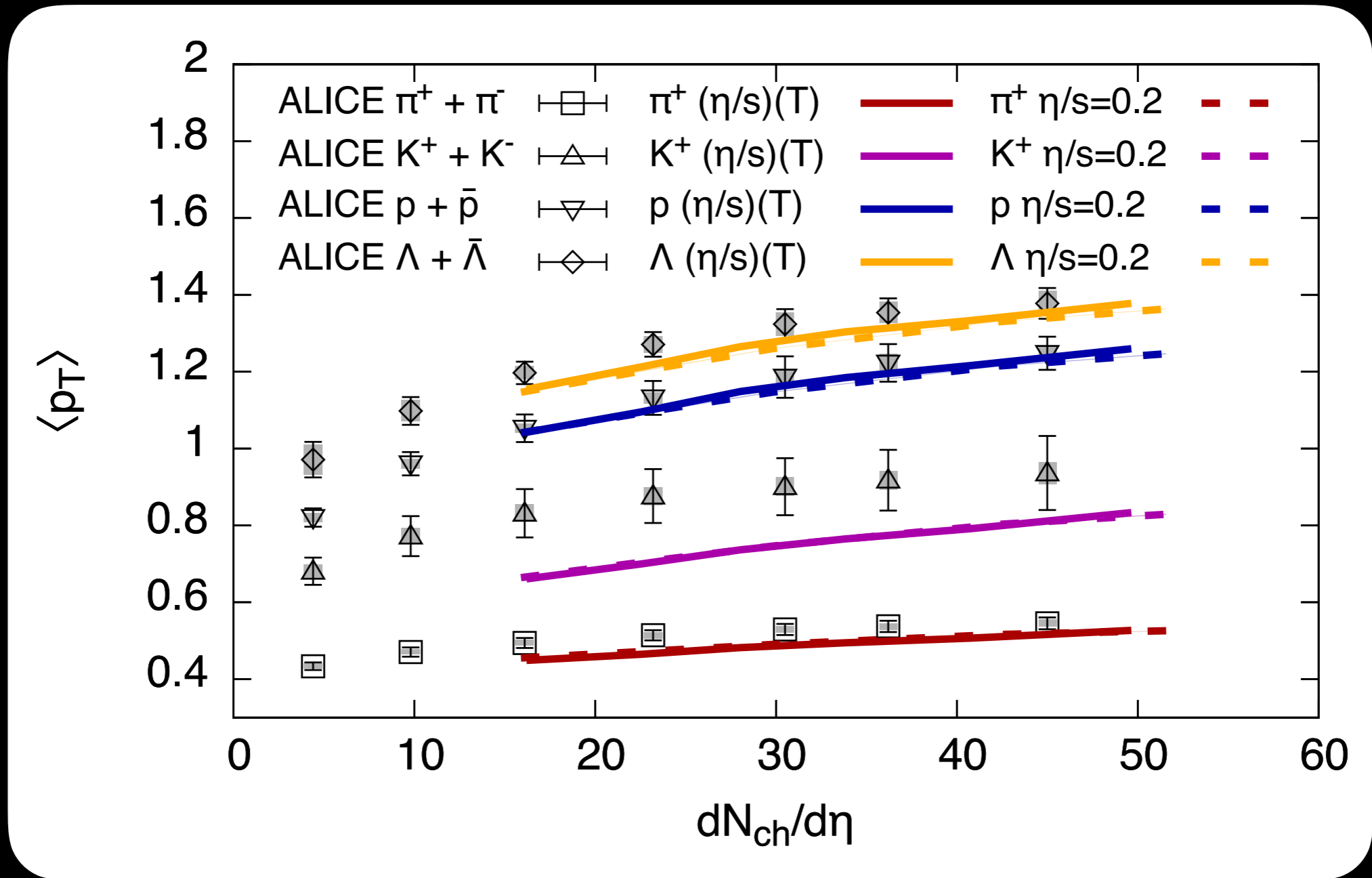
H. Mäntysaari, B. Schenke, C. Shen, P. Tribedy, arXiv:1705.03177



$\tau_0 = 0.4$  fm

# Identified particle mean $p_T$

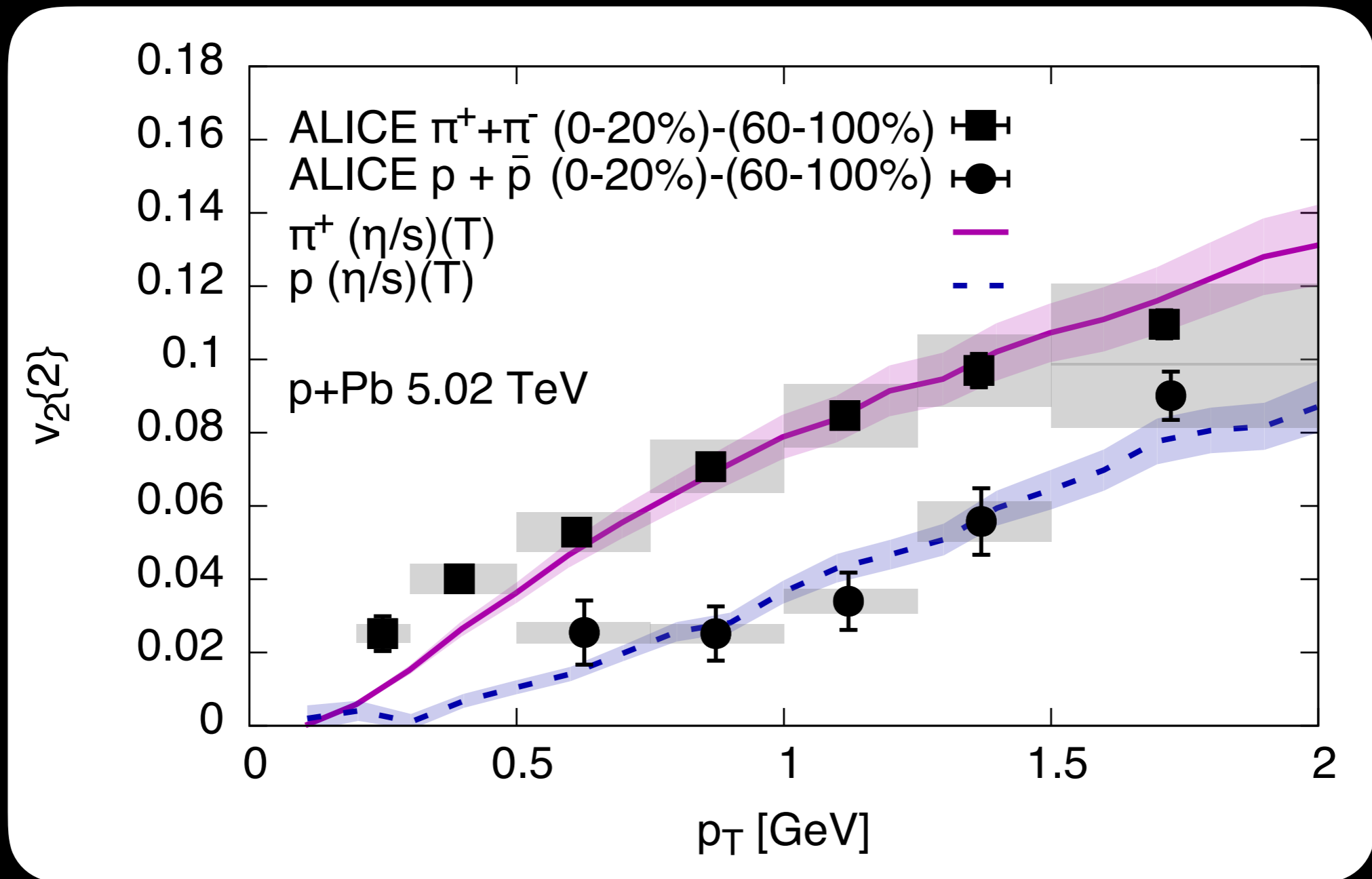
H. Mäntysaari, B. Schenke, C. Shen, P. Tribedy, arXiv:1705.03177



Experimental data: ALICE Collaboration, Phys. Lett. B728, 25 (2014)

# Identified particle flow

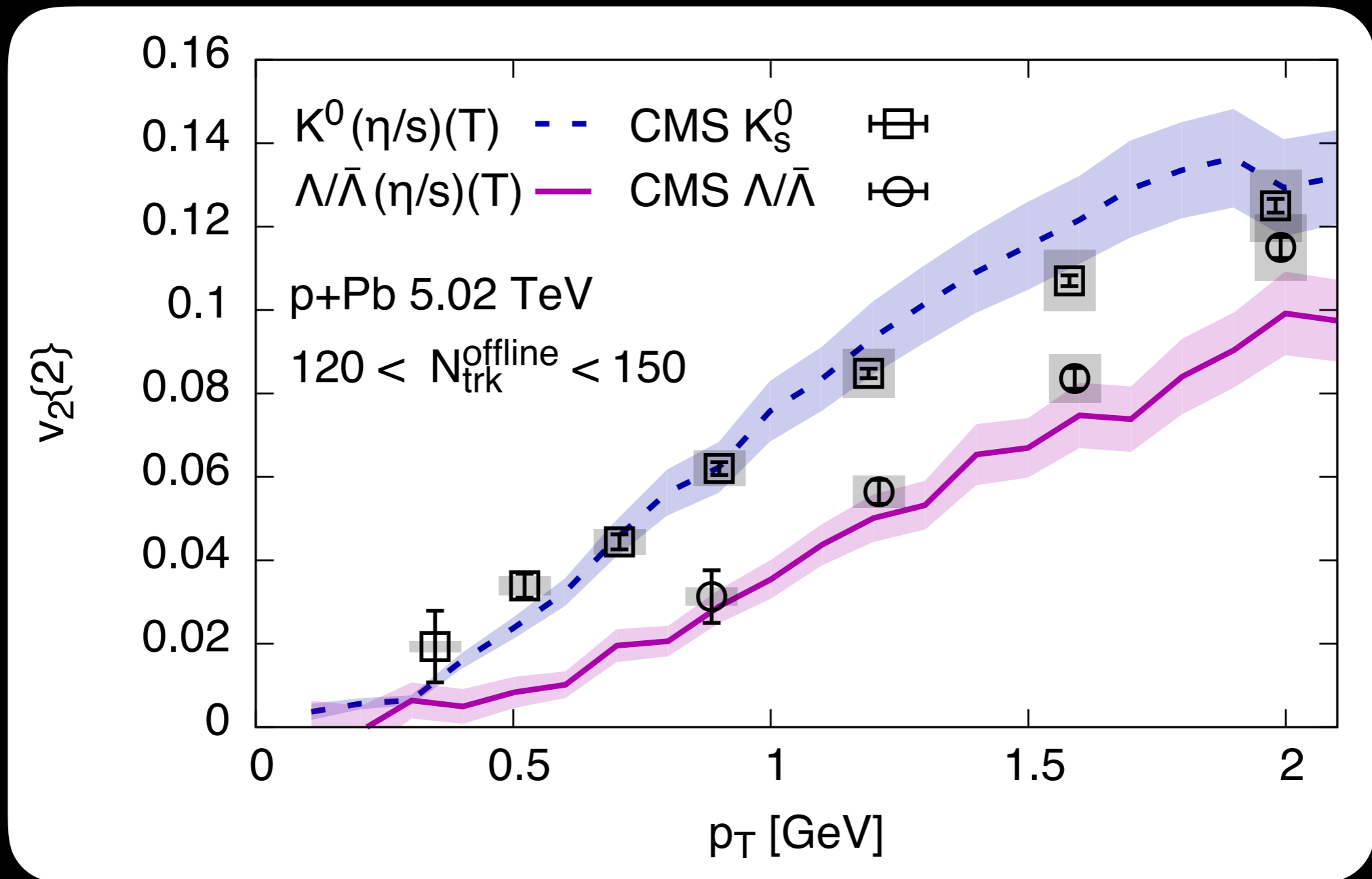
H. Mäntysaari, B. Schenke, C. Shen, P. Tribedy, arXiv:1705.03177



$\tau_0 = 0.4$  fm

# Identified particle flow

H. Mäntysaari, B. Schenke, C. Shen, P. Tribedy, arXiv:1705.03177



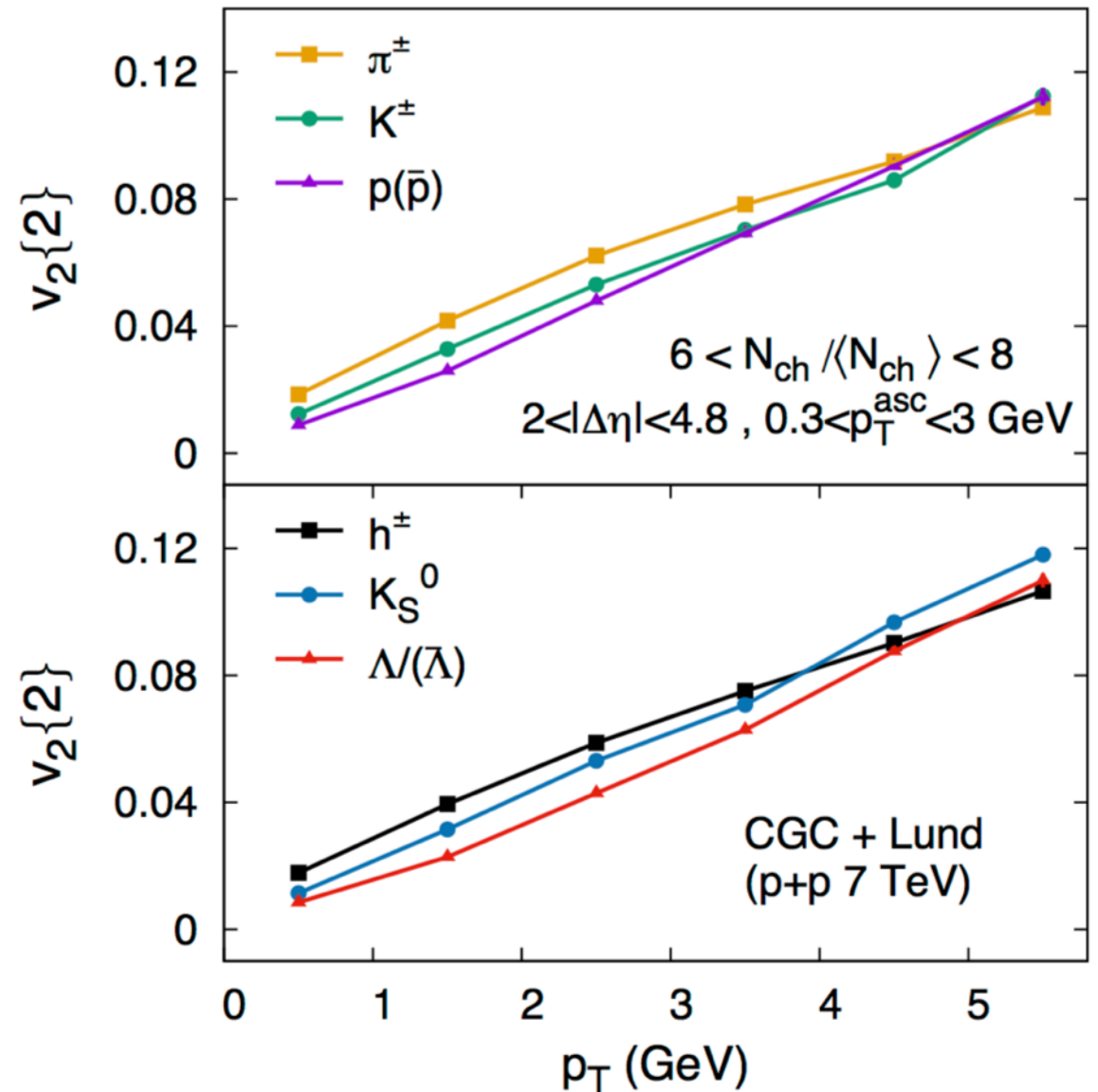
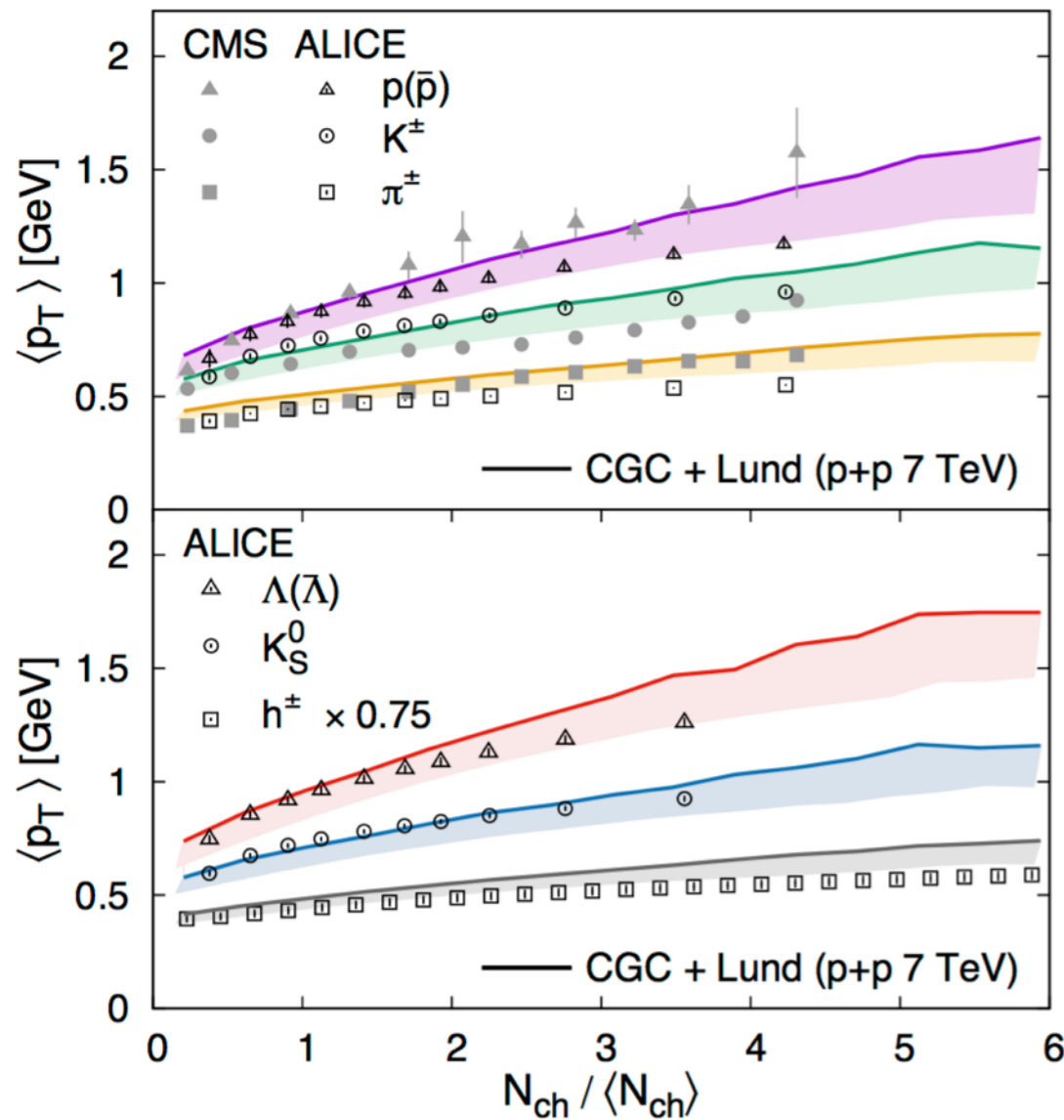
$\tau_0=0.4$  fm



# Mass ordering w/o hydrodynamics

B. Schenke, S. Schlichting, P. Tribedy, R. Venugopalan, Phys. Rev. Lett. 117, 162301 (2016)

## Yang-Mills initial state + Lund fragmentation



Emission from common boosted source

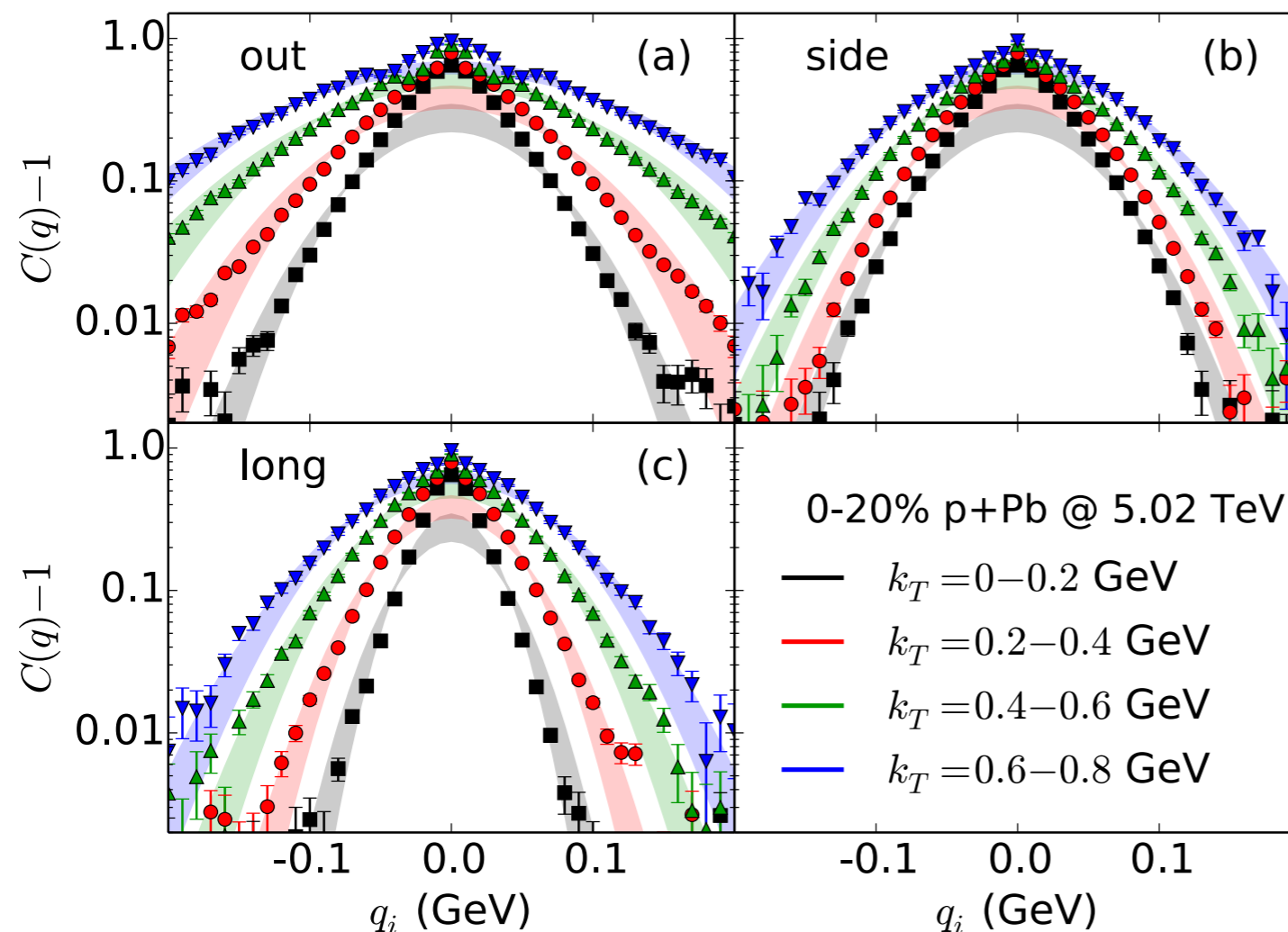
# HBT radii

H. Mäntysaari, B. Schenke, C. Shen, P. Tribedy, arXiv:1705.03177

$$C(\mathbf{q}) = 1 + \frac{\frac{1}{\langle N_{\text{pair}} \rangle} \langle \sum_{ij} \cos(\mathbf{q}_{ij} \cdot \mathbf{x}_{ij}) \rangle}{\frac{1}{\langle N_{\text{mix pair}} \rangle} \langle N_{\text{mix pair}}(\mathbf{q}) \rangle}$$

M. A. Lisa, S. Pratt, R. Soltz, and U. Wiedemann,  
Ann. Rev. Nucl. Part. Sci. 55, 357 (2005)

R. Hanbury Brown and R. Q. Twiss  
Nature 178, 1046 (1956)



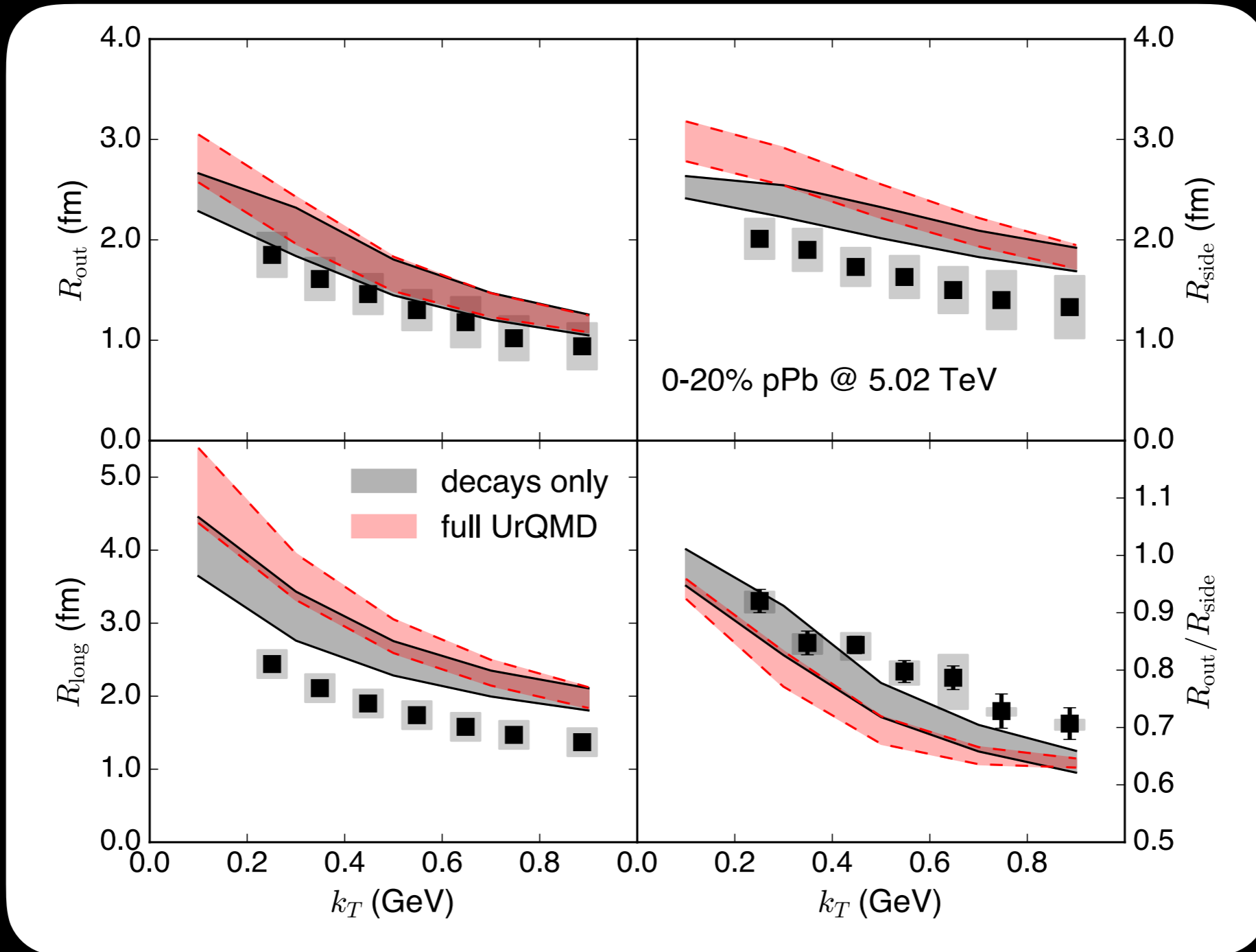
Fit to the Pratt-Bertsch parameterization in the longitudinally co-moving system

S. Pratt, Phys. Rev. D33, 1314 (1986)  
G. Bertsch, M. Gong, and M. Tohyama  
Phys. Rev. C37, 1896 (1988).

# HBT radii

H. Mäntysaari, B. Schenke, C. Shen, P. Tribedy, arXiv:1705.03177

Data: ALICE Collaboration, J. Adam et al. (ALICE), Phys. Rev. C91, 034906 (2015)



$\tau_0 = 0.4 \text{ fm} \quad (\eta/s)(T)$

# JIMWLK evolution

Replace parametrized  $x$ -dependence by renormalization group equation for  $x$ -dependence of probability distribution of Wilson lines

$$\partial_y W_y[V(\vec{x})] = \mathcal{H} W_y[V(\vec{x})]$$

with the JIMWLK Hamiltonian

$$\mathcal{H} = -\frac{1}{2} \frac{\alpha_s}{\pi^2} \int_{\vec{x}\vec{y}\vec{z}} \frac{\delta}{\delta A^{c+}(\vec{x})} \left[ (1 - V^\dagger(\vec{x})V(\vec{z}))^{ca} (1 - V^\dagger(\vec{y})V(\vec{z}))^{ba} \right. \\ \left. \times \frac{(\vec{x} - \vec{z}) \cdot (\vec{y} - \vec{z})}{(\vec{x} - \vec{z})^2 (\vec{y} - \vec{z})^2} \frac{\delta}{\delta A^{b+}(\vec{y})} W_y[V] \right]$$

J. Jalilian-Marian, A. Kovner, A. Leonidov, H. Weigert, Nucl. Phys. B504, 415 (1997), Phys. Rev. D59, 014014 (1999)

E. Iancu, A. Leonidov, and L. D. McLerran, Nucl. Phys. A692, 583 (2001)

E. Ferreiro, E. Iancu, A. Leonidov, and L. McLerran, Nucl. Phys. A703, 489 (2002)

A. H. Mueller, Phys. Lett. B523, 243 (2001)

# Numerical JIMWLK implementation

H. Weigert, Nucl. Phys. A 703, 823 (2002).

T. Lappi and H. Mantysaari, Eur. Phys. J. C 73, 2307 (2013)

## Langevin formulation

$$V_{\mathbf{x}}(Y + dY) = \exp \left\{ -i \frac{\sqrt{\alpha_s dY}}{\pi} \int_{\mathbf{z}} K_{\mathbf{x}-\mathbf{z}} \cdot (V_{\mathbf{z}} \xi_{\mathbf{z}} V_{\mathbf{z}}^\dagger) \right\} \\ \times V_{\mathbf{x}}(Y) \exp \left\{ i \frac{\sqrt{\alpha_s dY}}{\pi} \int_{\mathbf{z}} K_{\mathbf{x}-\mathbf{z}} \cdot \xi_{\mathbf{z}} \right\}$$

$\xi$  is Gaussian noise with zero average and

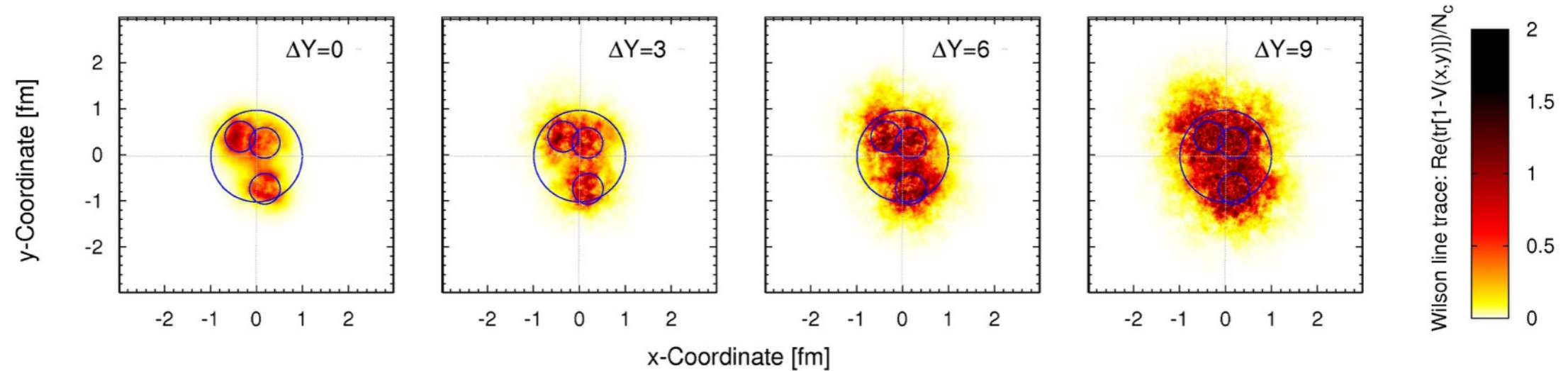
$$\langle \xi_{\mathbf{x},i}^a(Y) \xi_{\mathbf{y},j}^b(Y') \rangle = \delta^{ab} \delta^{ij} \delta_{\mathbf{xy}}^{(2)} \delta(Y - Y')$$

The JIMWLK Kernel is modified to avoid infrared tails:

$$K_{\mathbf{x}-\mathbf{z}}^{\text{mod}} = m |\mathbf{x} - \mathbf{z}| K_1(m |\mathbf{x} - \mathbf{z}|) \frac{\mathbf{x} - \mathbf{z}}{(\mathbf{x} - \mathbf{z})^2}$$

# Shape evolution of the proton

decreasing  $x$ , increasing energy



S. Schlichting, B. Schenke, *Phys. Lett. B* 739, 313-319 (2014)

Proton grows with increasing  $x$

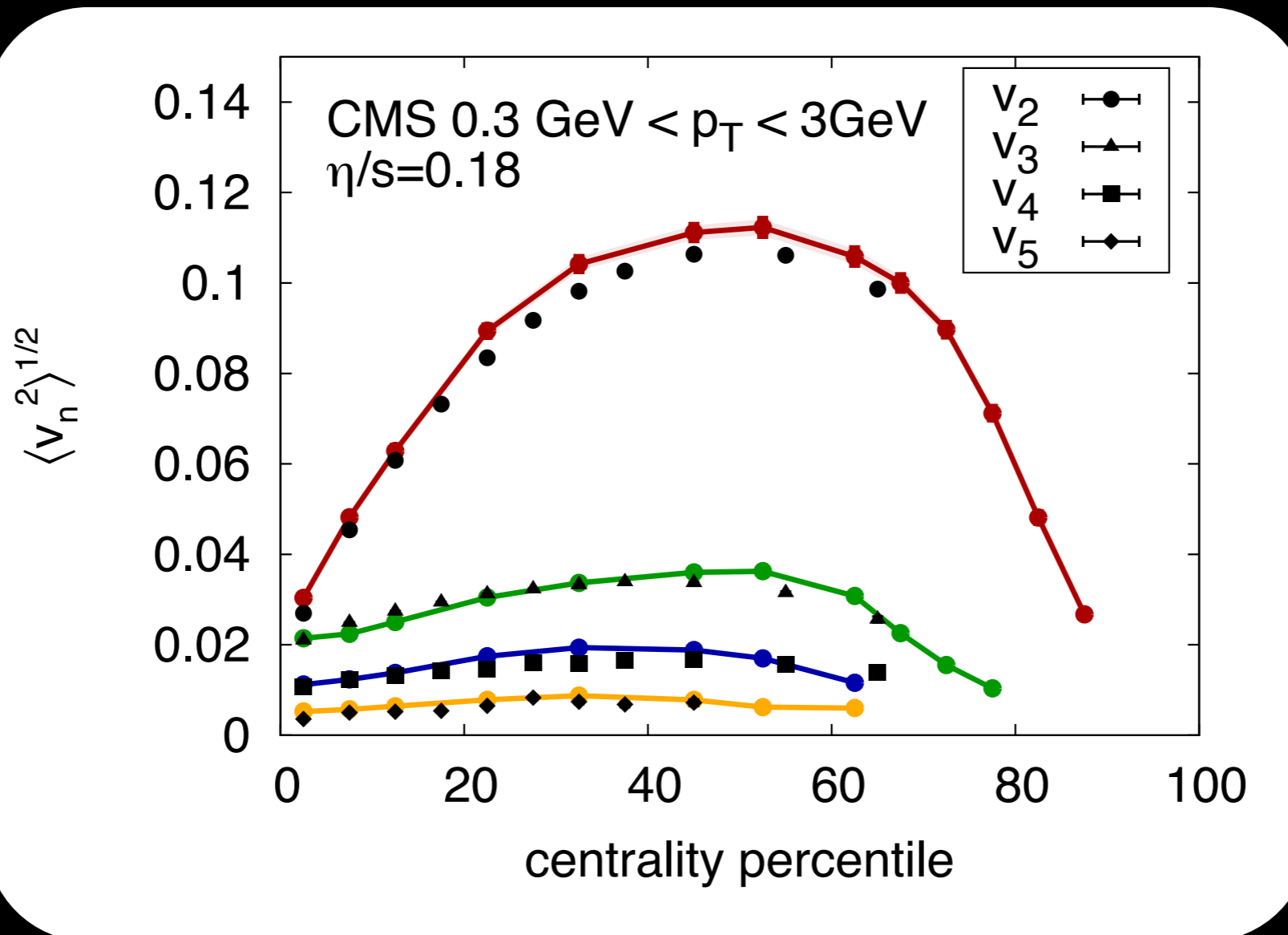
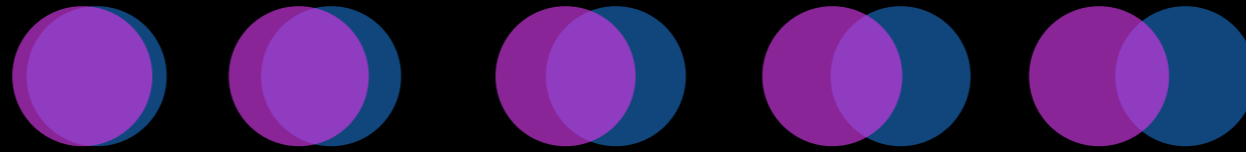
Growth is linear with  $Y$  when infrared regulator is used

Froissart bound not violated

# Flow harmonics $v_n$ from IP-Glasma initial state and MUSIC hydrodynamics

C.Gale, S.Jeon, B.Schenke, P.Tribedy, R.Venugopalan, Phys.Rev.Lett. 110, 012302 (2013)

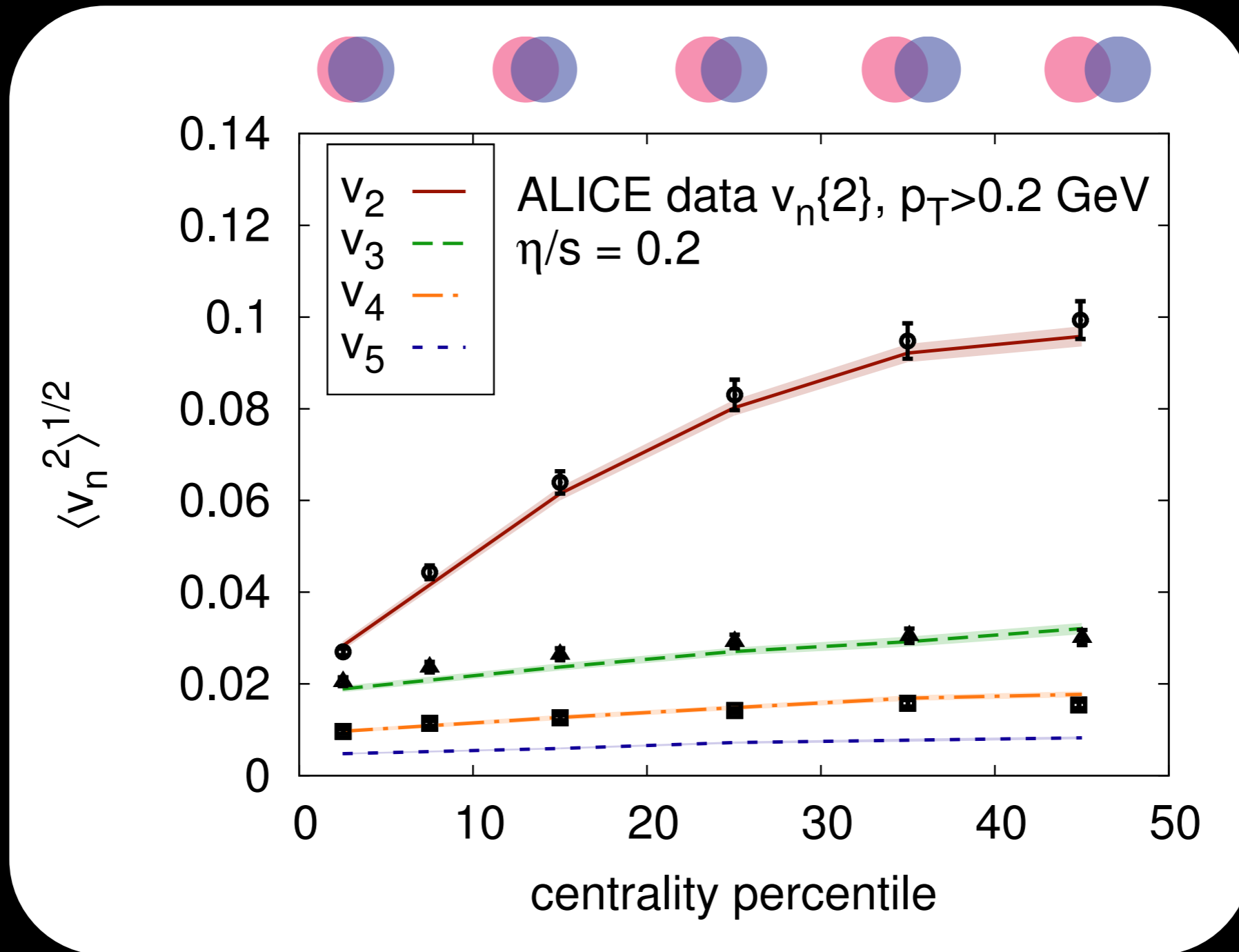
B. Schenke, R. Venugopalan, Phys.Rev.Lett. 113 (2014) 102301



CMS Collaboration, PRC 87(2013) 014902

# COMPARISON OF THEORY TO EXPERIMENT

C. GALE, S. JEON, B.SCHENKE, P.TRIBEDY, R.VENUGOPALAN, PRL110, 012302 (2013)



Quantitative description of the experimental data!

EXP. DATA: ALICE COLLABORATION, PHYS. REV. LETT. 107, 032301 (2011)