

Theory predictions for $t\bar{t} + b$ -jet background to $t\bar{t}H(b\bar{b})$

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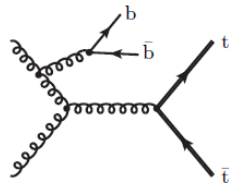
Outline

- 1 NLO+PS $t\bar{t}b\bar{b}$ simulations
- 2 Combination of $t\bar{t} + X$ and $t\bar{t}b\bar{b}$ simulations
- 3 $t\bar{t}b\bar{b}$ uncertainties
- 4 NLO+PS $t\bar{t}b\bar{b}$ tool comparisons

Irreducible $t\bar{t}b\bar{b}$ QCD background at NLO+PS

Nontrivial features of $pp \rightarrow t\bar{t}b\bar{b}$

- 6 external coloured partons
- 34 LO diagrams, multiple scales from 5 to 500 GeV
- dominated by topologies with **FS $g \rightarrow b\bar{b}$ splittings**



⇒ **collinear regions and m_b important** (resummation of IS $g \rightarrow b\bar{b}$ splittings not)

NLO+PS $t\bar{t}b\bar{b}$ 5F scheme ($m_b = 0$) with POWHEL [Garzelli et al '13/'14]

- $t\bar{t}b\bar{b}$ NLO MEs cannot describe collinear $g \rightarrow b\bar{b}$ splittings

NLO merging $t\bar{t} + 0, 1, 2$ jets 5F with SHERPA+OPENLOOPS or MG5AMC@NLO

- challenging for $t\bar{t}$ +HF and still based on $m_b = 0$ MEs + shower in collinear regions

NLO+PS $t\bar{t}b\bar{b}$ 4F scheme ($m_b > 0$) with SHERPA+OPENLOOPS [Cascioli et al '13] or MG5AMC@NLO

- $t\bar{t}b\bar{b}$ NLO MEs cover full b-quark phase space ⇒ **recommended for $t\bar{t}H(b\bar{b})$**

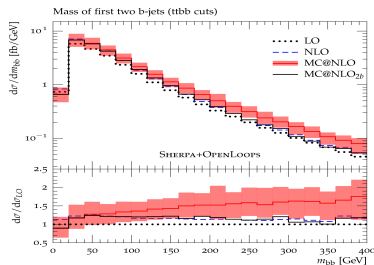
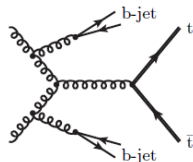
⇒ **NLO accuracy for any inclusive $t\bar{t}$ +b-jet observable with ≥ 1 b-jets!**

S-MC@NLO $t\bar{t}b\bar{b}$ at 8 TeV in 4F scheme [Cascioli et al '13]

Convergence of 4F scheme: no large $\log(m_b)$ in $t\bar{t}b$ region!

| | $t\bar{t}b$ | $t\bar{t}b\bar{b}$ | $t\bar{t}b\bar{b} (m_{b\bar{b}} > 100)$ |
|--|------------------------------------|-----------------------------------|---|
| $\sigma_{\text{LO}} [\text{fb}]$ | $2644^{+71\%+14\%}_{-38\%-11\%}$ | $463.3^{+66\%+15\%}_{-36\%-12\%}$ | $123.4^{+63\%+17\%}_{-35\%-13\%}$ |
| $\sigma_{\text{NLO}} [\text{fb}]$ | $3296^{+34\%+5.6\%}_{-25\%-4.2\%}$ | $560^{+29\%+5.4\%}_{-24\%-4.8\%}$ | $141.8^{+26\%+6.5\%}_{-22\%-4.6\%}$ |
| $\sigma_{\text{NLO}}/\sigma_{\text{LO}}$ | 1.25 | 1.21 | 1.15 |
| $\sigma_{\text{MC@NLO}} [\text{fb}]$ | $3313^{+32\%+3.9\%}_{-25\%-2.9\%}$ | $600^{+24\%+2.0\%}_{-22\%-2.1\%}$ | $181^{+20\%+8.1\%}_{-20\%-6.0\%}$ |
| $\sigma_{\text{MC@NLO}}/\sigma_{\text{NLO}}$ | 1.01 | 1.07 | 1.28 |

MC@NLO enhancement in Higgs region from double $g \rightarrow b\bar{b}$ splittings



One $g \rightarrow b\bar{b}$ splitting from PS

\Rightarrow TH uncertainties related to NLOPS matching and shower crucial!

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Approach proposed in YR4

NLOPS 4F $t\bar{t}b\bar{b}$ sample

- can be applied in its full phase space (no generation cuts)
- ⇒ inclusive description of $t\bar{t} + \geq 1b$ -quarks
- includes also contributions corresponding to $gb \rightarrow t\bar{t}b$ in the 5F scheme

Inclusive $t\bar{t} + X$ sample

- needs to be restricted to $t\bar{t} + 0b$ -quarks to avoid double counting
- ⇒ veto events containing b -quarks not arising from showered top decays or MPI or UE

Possible implementations

- $t\bar{t} + X$ and $t\bar{t}b\bar{b}$ samples **independent samples**
- **reweighting of $t\bar{t} + X$ sample** through $t\bar{t}b\bar{b}$ in the $t\bar{t} + \geq 1b$ -quarks region

Refinement for region of small $p_{T,b}$

Caveat

- $t\bar{t}b\bar{b}$ sample yields (small) contribution to $t\bar{t} + 0 b$ -jet categories of EXP analysis
 - $t\bar{t} + 0 b$ -jet categories (dominated by $t\bar{t}$ +gluons/light-quarks) can bias $t\bar{t}b\bar{b}$ fit
- ⇒ preferable to restrict $t\bar{t}b\bar{b}$ to $t\bar{t} + b$ -jet categories

Proposal: smooth matching of $t\bar{t} + X$ and $t\bar{t}b\bar{b}$ samples

- using smearing function of leading b-jet p_T , such as

$$\xi(p_{T,b}) = \begin{cases} 0 & \equiv \text{pure } t\bar{t} + 0b & \text{for } p_{T,b} < p_{T,\min} \\ \frac{1}{2} \left[1 - \cos \left(\pi \frac{p_{T,b} - p_{T,\min}}{p_{T,\max} - p_{T,\min}} \right) \right] & & \text{for } p_{T,\min} < p_{T,b} < p_{T,\max} \\ 1 & \equiv \text{pure } t\bar{t} + \geq 1b & \text{for } p_{T,b} > p_{T,\max} \end{cases}$$

- with transition region in the vicinity of experimental b-jet threshold, e.g. $[p_{T,\min}, p_{T,\max}] = [15, 25]$ GeV
- same matching procedure should be used in ATLAS and CMS for a transparent comparison and combination of EXP results

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Scale choices (YR4) and uncertainties (no proposal yet)

Factorisation (μ_Q) and resummation (μ_Q) scales

$$E_{T,i} = \sqrt{m_i^2 + p_{T,i}^2}$$

$$\mu_F = \mu_Q = \frac{H_T}{2} = \frac{1}{2} \sum_{i=t,\bar{t},b,\bar{b}} E_{T,i}$$

$\mu_Q \equiv$ shower starting scale is a free parameter in MC@NLO (not in Powheg)

CKKW-like (softer) renormalisation scale

$$\mu_R = \mu_{\text{CKKW}} = \prod_{i=t,\bar{t},b,\bar{b}} E_{T,i}^{1/4}$$

Scale variations (leading uncertainty) $\sim 20\text{-}30\%$

- factor-2 variations of μ_R and $\mu_F \Leftrightarrow$ **normalisation**
- "kinematic" variations of $\mu_R, \mu_F, \mu_Q \Leftrightarrow$ **shape**
- variations of μ_Q in MC@NLO and h_{damp} in Powheg \Leftrightarrow **NLOPS matching**

Other variations

- PDF variations (only few percent)
- shower variations: tune variations, shower recoil scheme, ...

Correlation of TH uncertainties between categories

Categories

- $t\bar{t}h(b\bar{b})$ analyses based on simultaneous fit of MC to data in various categories with different # of light- and b -jets
- correlations crucial to constrain background in signal region (with multiple b -jets)

Between $t\bar{t}$ +light-jet and $t\bar{t}$ + b -jet categories

- uncertainties should be uncorrelated

Between sub-categories (e.g. $t\bar{t}b$, $t\bar{t}bb$, $t\bar{t}B$)

- uncertainties should be correlated

Motivation: independent shower, matching and ME variations account for different types of uncertainties (e.g. related to collinear $g \rightarrow b\bar{b}$ splittings or hard b -production) \Rightarrow no need of separate categories with uncorrelated uncertainties

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Tuned comparison of NLO+PS $t\bar{t}b\bar{b}$ simulations at 13 TeV

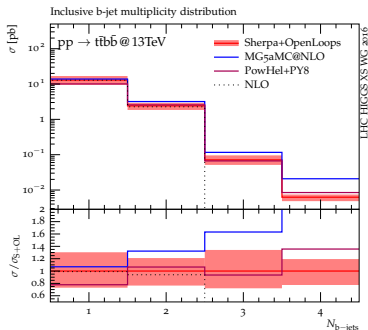
Different NLO+PS methods, showers, and m_b treatments

| Tool | Matching | Shower | m_b [GeV] | gencuts |
|---------------------|----------|------------|-------------|---|
| SHERPA2.1+OPENLOOPS | SMC@NLO | Sherpa 2.1 | 4.75 (4F) | no |
| MG5_AMC@NLO | MC@NLO | Pythia 8.2 | 4.75 (4F) | no |
| POWHEL | Powheg | Pythia 8.2 | 0 (5F) | $p_{T,b} > 4.75$ GeV $\frac{m_{bb}}{2} > 4.75$ GeV |

Detailed setup

- HXSWG's Yellow Report 4 [arXiv:1610.07922]
- <https://twiki.cern.ch/twiki/bin/view/LHCPhysics/ProposalTtbb>

Inclusive $t\bar{t} + b$ -jet multiplicity distribution



- S-MC@NLO (Sherpa+OpenLoops) with $\mu_{R,F}$ variations
- MG5_aMC@NLO+PY8 w.o. variations
- Powhel+PY8 w.o. variations

NLO vs NLO+PS

- decent agreement in NLO accurate bins with ≥ 1 and ≥ 2 b-jets

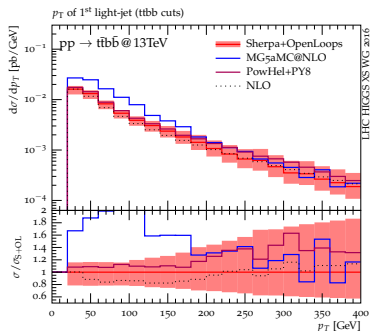
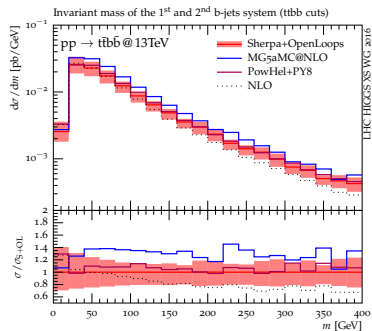
S-MC@NLO vs PowHel+PY8

- **good overall agreement** in spite of differences in matching method, parton shower, N_f -scheme and ad-hoc cuts in Powhel

S-MC@NLO vs MG5aMC@NLO

- **good agreement only for ≥ 1 b-jets** despite similar matching method and same N_f

$t\bar{t}b\bar{b}$ distributions with $\geq 2b$ -jets



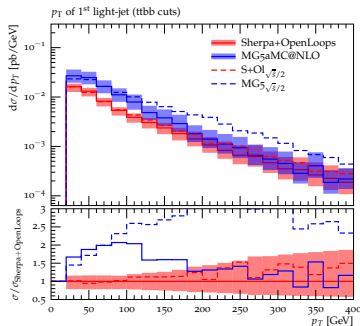
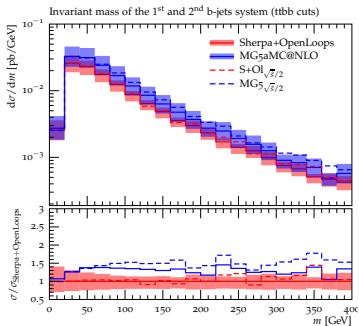
S-MC@NLO vs PowHel+PY8

- **well consistent** also in observables that receive significant shower corrections
- **confirmation of “double-splitting effects”** (see e.g. m_{bb})

S-MC@NLO vs MG5aMC@NLO

- 40% enhancement of $t\bar{t} + 2b$ XS & **sizable differences in NLO radiation pattern**
- related to **strong sensitivity to resummation scale** (shower starting scale) in MG5 . . .

Dependence on resummation scale μ_Q



Nominal MG5_aMC and Sherpa+OpenLoops predictions in YR4

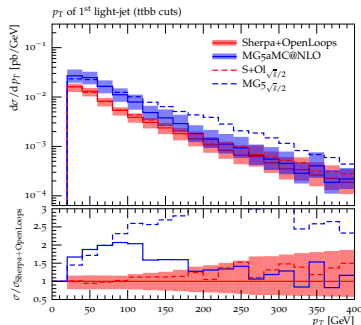
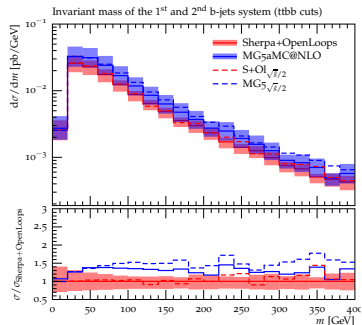
- MG5_aMC supports* only $\mu_Q = f(\xi)\sqrt{\hat{s}} \Rightarrow$ smearing function restricted to $0.1 < f(\xi) < 0.25$ to mimic recommended $\mu_Q = H_T/2$ implemented in Sherpa

New: μ_Q variations enhance the discrepancy

- $\mu_Q = \sqrt{\hat{s}}/2$ in Sherpa to mimic MG5_aMC default choice $0.1 < f(\xi) < 1$
- strong μ_Q -sensitivity of MG5_aMC \Rightarrow much more pronounced deviations

*New: latest MG5aMC@NLO version implements $\mu_Q = H_T/2$ as default resummation scale

Dependence on resummation scale μ_Q



Interpretation of large Sherpa+OpenLoops vs MG5aMC@NLO differences?

- can we exclude bugs or misuse of tools?
- related to **single μ_Q scale in MC@NLO vs multi-scale process** ($M_{tt} \sim 100M_b$)?
- small μ_Q sensitivity and NLOPS/NLO difference in SHERPA+OPENLOOPS suggests **MG5AMC@NO-specific issue (?)**
- **SHERPA+OPENLOOPS $t\bar{t}b\bar{b}$ 4F supported by POWHEL $t\bar{t}b\bar{b}$ 5F**, but should be confirmed by POWHEG $t\bar{t}b\bar{b}$ 4F simulation

Conclusions

NLO+PS $t\bar{t}b\bar{b}$ 4F simulations

- recommended for $t\bar{t}$ +b-jet backgrounds
- technically automated but physically very tricky (many coloured partons and scales, $g \rightarrow b\bar{b}$ splittings)

Matching $t\bar{t} + X$ with $t\bar{t}b\bar{b}$ 4F samples

- veto events with additional b-quarks in $t\bar{t} + X$ sample
- smooth implementation as a function of leading-jet p_T

$t\bar{t}b\bar{b}$ uncertainties

- dominated by μ_R, μ_F, μ_Q scale dependence
- detailed recommendations for shape uncertainties still needed

Discrepancy between Sherpa+OpenLoops and MG5aMC@NLO

- related to μ_Q dependence of MG5aMC@NLO
- calls for thorough investigation/validation

Backup slides

Scale variations for shape (not for normalisation) uncertainties

Consider (aggressive but not fully unreasonable) *kinematic distortions* of μ_R, μ_F, μ_Q using various combinations of the variables

$$\mu_{\text{CMMPS}} = \prod_{i=t, \bar{t}, b\bar{b}} E_{T,i}^{1/4}, \quad m_{b\bar{b}}, \quad H_{T,b(t)} = E_{T,b(t)} + E_{T,\bar{b}(\bar{t})}, \quad H_T = H_{T,t} + H_{T,b}$$

| Scale | default | glo-HT | glo-Mt | glo-soft | R-Mbb | R-HTb | R-HTt | Q-CMMPS | Q-Mt |
|---------------------------|-----------------------|-----------------------|-----------------------|-----------------------|----------------------------|-------------------------|-------------------------|-----------------------|-----------------------|
| μ_R | μ_{CMMPS} | $H_T/2$ | m_t | μ_{CMMPS} | $(m_t m_{b\bar{b}})^{1/2}$ | $(m_t H_{T,b/2})^{1/2}$ | $(m_t H_{T,t/2})^{1/2}$ | μ_{CMMPS} | μ_{CMMPS} |
| μ_F | $H_{T,t}/2$ | $H_T/2$ | m_t | μ_{CMMPS} | $H_{T,t}/2$ | $H_{T,t}/2$ | $H_{T,t}/2$ | $H_{T,t}/2$ | $H_{T,t}/2$ |
| μ_Q | $H_{T,t}/2$ | $H_T/2$ | m_t | μ_{CMMPS} | $H_{T,t}/2$ | $H_{T,t}/2$ | $H_{T,t}/2$ | μ_{CMMPS} | m_t |
| Cuts | $\Delta\sigma/\sigma$ | $\Delta\sigma/\sigma$ | $\Delta\sigma/\sigma$ | $\Delta\sigma/\sigma$ | $\Delta\sigma/\sigma$ | $\Delta\sigma/\sigma$ | $\Delta\sigma/\sigma$ | $\Delta\sigma/\sigma$ | $\Delta\sigma/\sigma$ |
| <i>tbt</i> | 0% | -41% | -27% | +4.7% | +2.3% | 1.1% | -32% | -3.5% | -0.3% |
| <i>tbb</i> | 0% | -33% | -17% | -0.7% | +0.2% | 3.4% | -22% | -6.4% | -1.1% |
| <i>tbb</i> ₁₀₀ | 0% | -29% | -13% | -9.2% | -5.6% | +2.5% | -17% | -14% | -2.9% |

glo single global scale: hard, fixed and softer

R renormalisation scale (dominant!): modify or avoid b-jet dependence

Q resummation-scale (PS uncertainties): softer and fixed

Additional m_b and PDF variations with potential impact on shape (and normalisation)

| | $M_b = 5.0$ | $M_b = 4.5$ | CTEQ 4F | MSTW ₃₇ | MSTW ₃₈ |
|---|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|
| Cuts | $\Delta\sigma/\sigma$ | $\Delta\sigma/\sigma$ | $\Delta\sigma/\sigma$ | $\Delta\sigma/\sigma$ | $\Delta\sigma/\sigma$ |
| <i>ttb</i> | -3.5% | +4.4% | -10% | -0.1% | +2.6% |
| <i>ttbb</i> | -0.7% | +2.7% | -9.3% | +0.2% | +4.2% |
| <i>ttbb₁₀₀</i> | -0.1% | +4.4% | -7.8% | -0.7% | +6.9% |

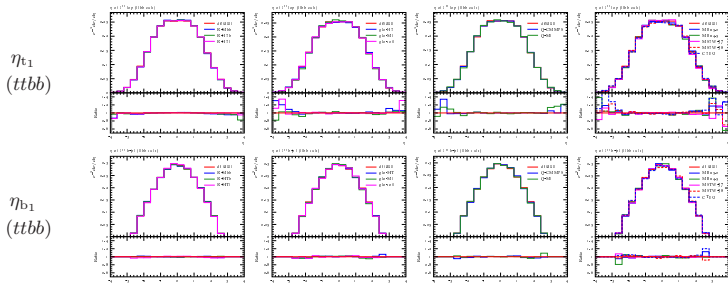
- conservative b-mass variations $m_b = 4.75 \pm 0.25$ GeV (impact on collinear regions)
- compare central MSTW to central CT10 PDF and MSTW variations with large gluon-shape distortion (MSTW eigenvector 19)

Shape variations of differential observables

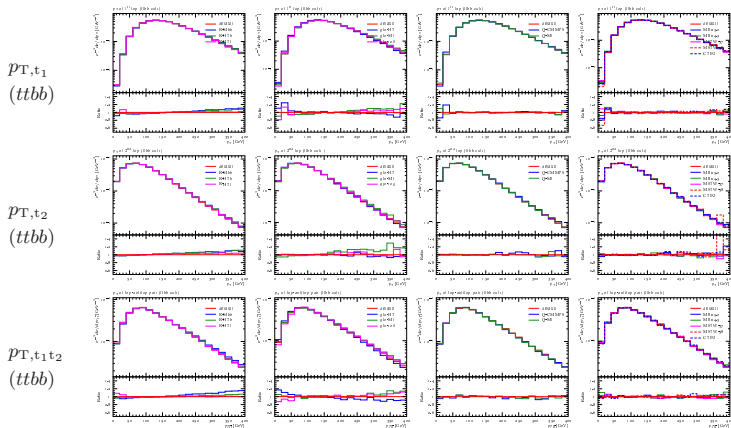
The following plots show a representative selection of shape uncertainties

- normalisation uncertainties removed by normalising all distributions to one
- columns represent (1) R-type (2) glo-type (3) Q-type (4) m_b +PDFs variations

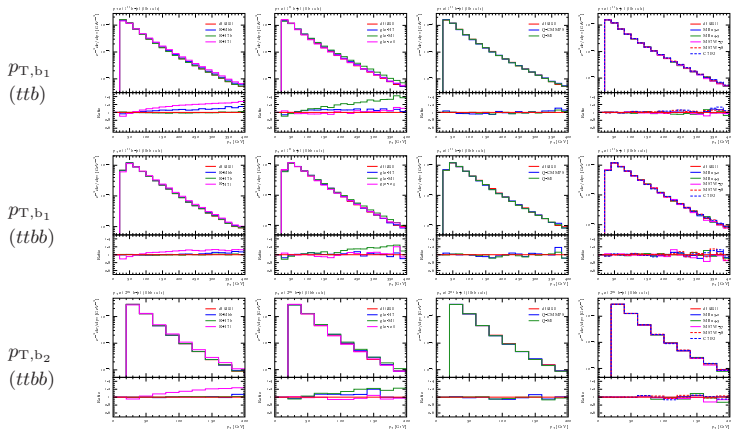
Shape uncertainty of top-quark and b-jet rapidities



\Rightarrow percent-level variations for $|\eta| < 2.5$; η_b very stable

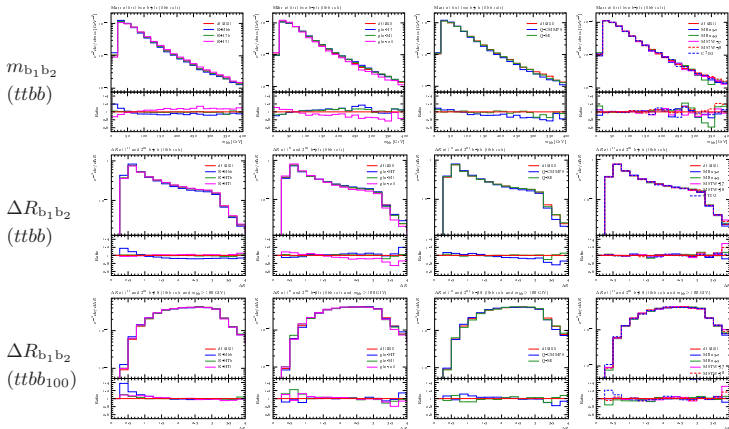
Shape uncertainty of top- p_T 

$\Rightarrow \sim 10\%$ variations (20% in the tails) driven by top-dependence of μ_R

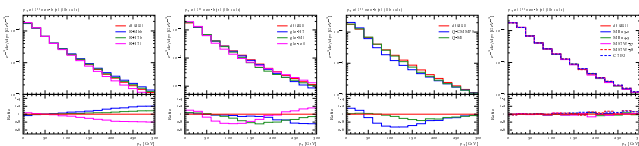
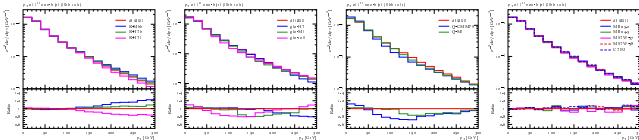
Shape uncertainty of b-jet p_T 

\Rightarrow $\sim 10\text{-}20\%$ variations (40% in the tails) driven by b-dependence of μ_R

Shape uncertainty of b-jet correlations



$\Rightarrow \sim 10\text{-}20\%$ variations driven by b-dependence of μ_R (at small m_{bb} and ΔR) and (aggressive) reduction of μ_Q in the tail

Shape uncertainty of 1st light-jet p_T p_{T,j_1}
($t\bar{t}b$) p_{T,j_1}
($t\bar{t}b\bar{b}$)

⇒ up to $\sim 30\%$ variations at intermediate p_T values. Indicates that the considered variations (dominated by choice of soft resummation scale) are (probably too) conservative