

# The Recursive Jigsaw Reconstruction for SUSY, Higgs and Beyond

Marco Santoni CoEPP 2017

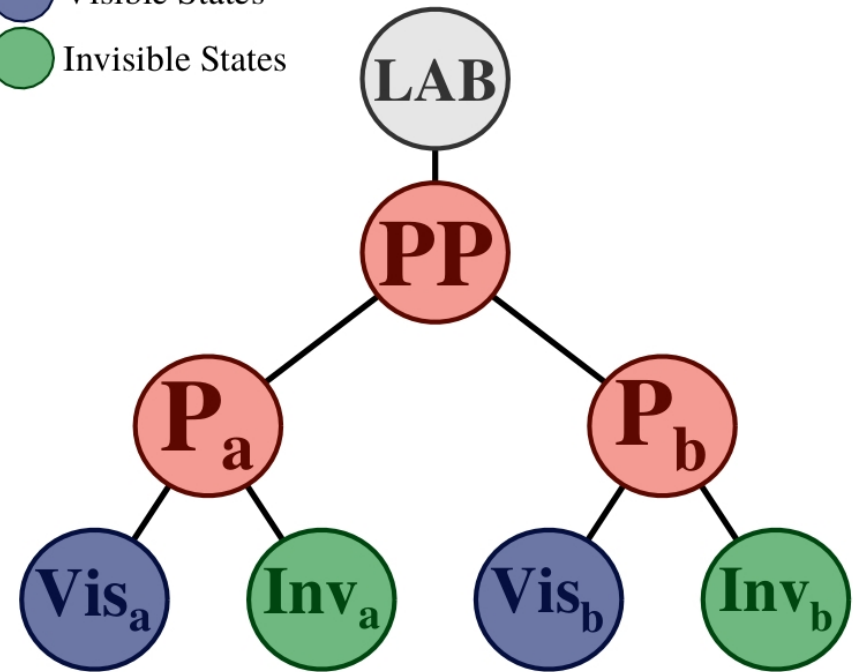
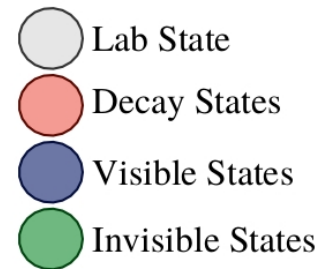
*Supervisors: Paul Jackson and Martin White*

*and with Christopher Rogan*

- What is the Recursive Jigsaw Reconstruction (RJR) technique?
- Example of study: squark and gluino pair production at LHC  
“Sparticles in motion: Analyzing compressed SUSY scenarios with a new method of event reconstruction”  
(arXiv:1607.08307 [hep-ph] – shortly in Phys. Rev. D)
- Other SUSY analyses and beyond
- Summary - Outlook

# What is the Recursive Jigsaw Reconstruction technique?

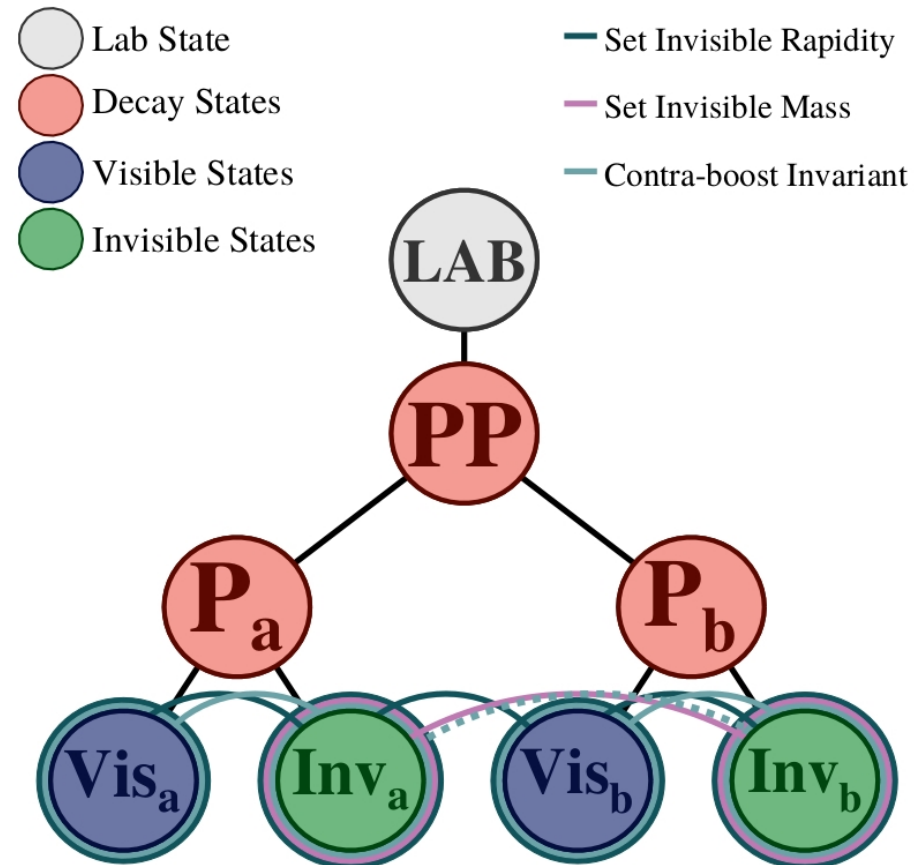
- Original method to **reconstructing** final states with weakly interacting particles
- Transform observable momenta reference-frame to reference-frame
- **Jigsaw rules**: specify the unknown d.o.f. relevant to the transformation (customizable-interchangeable like jigsaw puzzle pieces)
- The procedure is repeated **recursively**, travelling through each of the reference frames relevant to the topology
- Rather than obtaining one observable, get a complete basis of useful variables: angles, energies, masses ...



Developed by Paul Jackson and Christopher Rogan: <http://RestFrames.com>

# What is the Recursive Jigsaw Reconstruction technique?

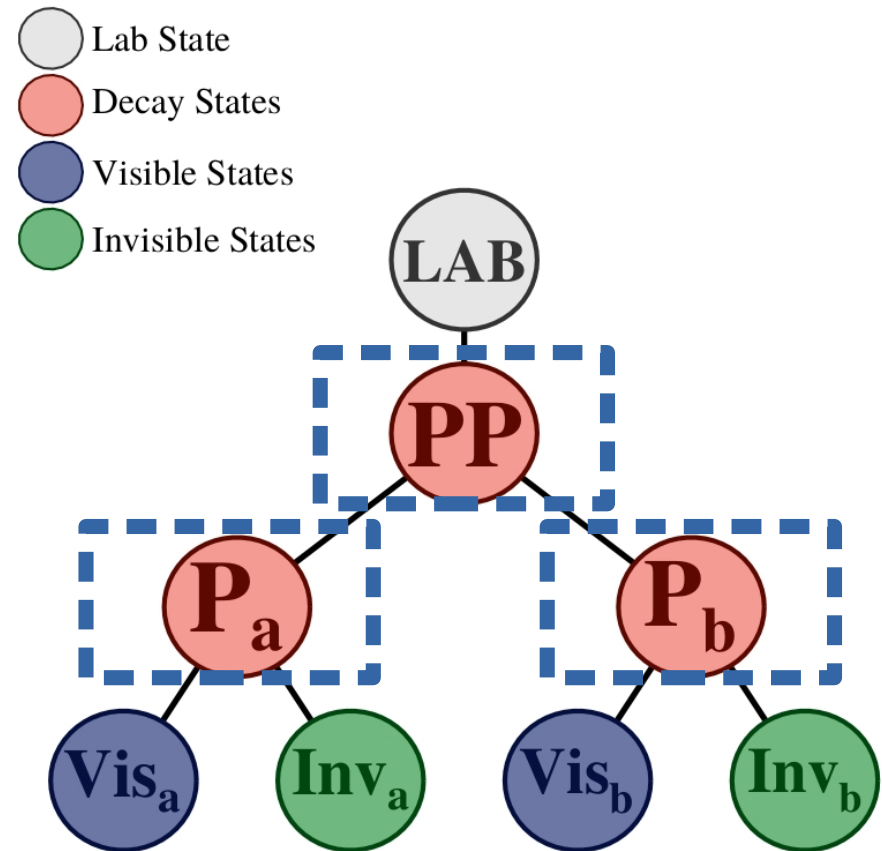
- Original method to **reconstructing** final states with weakly interacting particles
- Transform observable momenta reference-frame to reference-frame
- **Jigsaw rules**: specify the unknown d.o.f. relevant to the transformation (customizable-interchangeable like jigsaw puzzle pieces)
- The procedure is repeated **recursively**, travelling through each of the reference frames relevant to the topology
- Rather than obtaining one observable, get a complete basis of useful variables: angles, energies, masses ...



Developed by Paul Jackson and Christopher Rogan: <http://RestFrames.com>

# What is the Recursive Jigsaw Reconstruction technique?

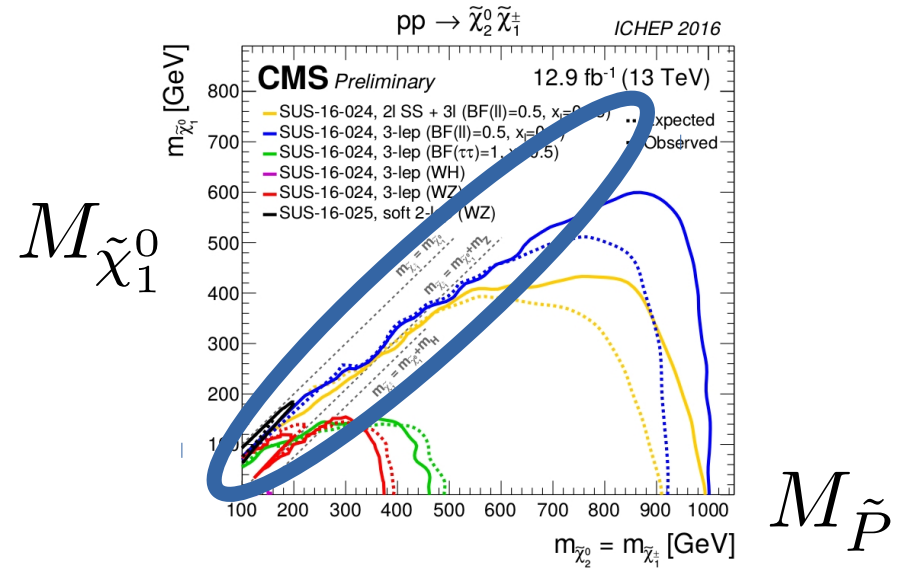
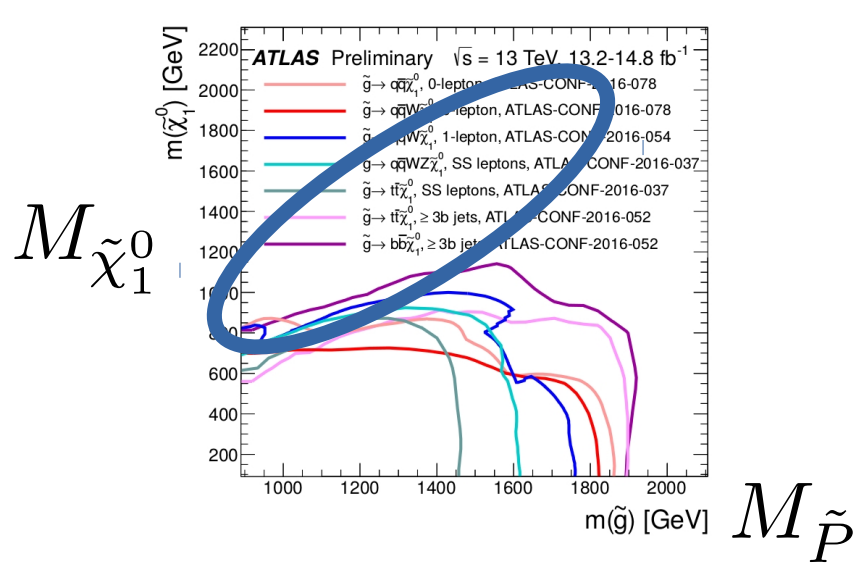
- Original method to **reconstructing** final states with weakly interacting particles
- Transform observable momenta reference-frame to reference-frame
- **Jigsaw rules**: specify the unknown d.o.f. relevant to the transformation (customizable-interchangeable like jigsaw puzzle pieces)
- The procedure is repeated **recursively**, travelling through each of the reference frames relevant to the topology
- Rather than obtaining one observable, get a complete basis of useful variables: angles, energies, masses ...



Developed by Paul Jackson and Christopher Rogan: <http://RestFrames.com>

# Introduction to compressed kinematics

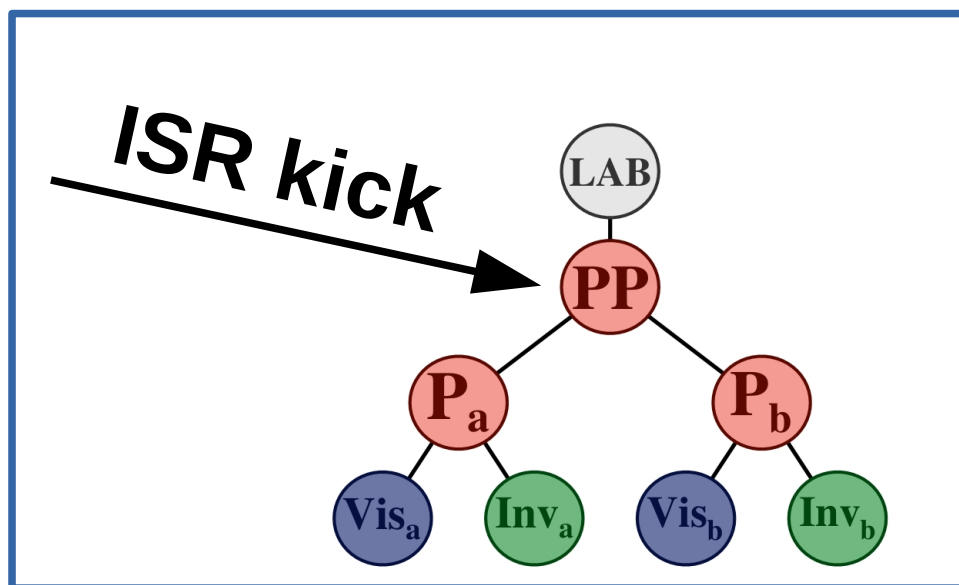
- Compressed scenarios refer to **small mass-splittings**  $M_{\tilde{P}} - M_{\tilde{\chi}_1^0}$  between the parent superparticle  $\tilde{P}$  and the lightest supersymmetric particle (LSP)  $\tilde{\chi}_1^0$



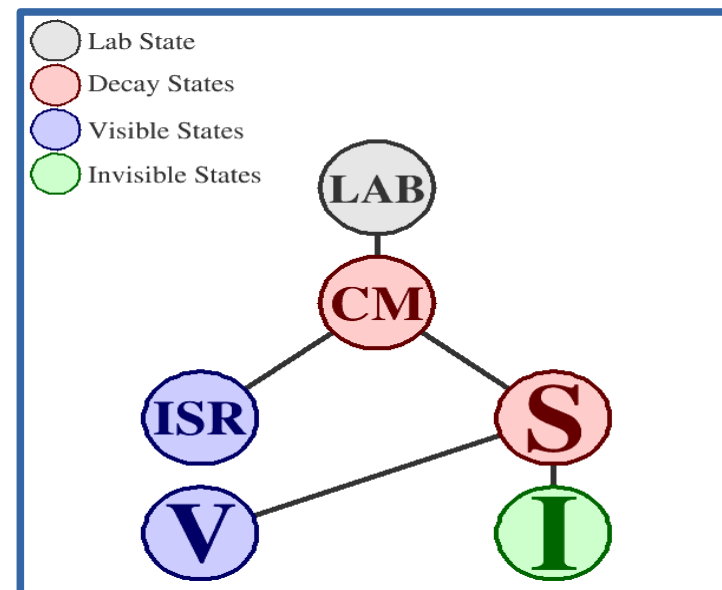
- Challenge**
  - Low momentum decay products are hard to detect
  - The LSPs result in a low value of the transverse missing momentum  $\vec{E}_T$
- To separate signal from BGs, consider only events with a high **momentum** of the **initial state radiation (ISR) system**
- In the limit where the LSPs receive no momentum from their parents' decays:

$$\vec{E}_T \sim -\vec{p}_T^{\text{ISR}} \times \frac{M_{\tilde{\chi}_1^0}}{M_{\tilde{P}}}$$

# Sparticles in motion



=



- A *simple transverse* decay view of the event:
  - **CM**: centre-of-mass system including all visible objects and MET
  - **ISR**: radiation not coming from sparticle decays
  - **S**: the Signal/SUSY system decaying in
  - **V**: Visible system,
  - **I**: Invisible system = missing transverse momentum
- How do we separate initial state radiation from the other decay products?

# The compressed Recursive Jigsaw Reconstruction tree

- **Consider the worst scenario: final states with only light jets and MET**

- We want to **separate** the jets between the visible system (**V**) and those recoiling against it (**ISR**)

- *Transverse* view of the event ( $P_z(jet_i) = 0$ )

- Zero mass for **I** system

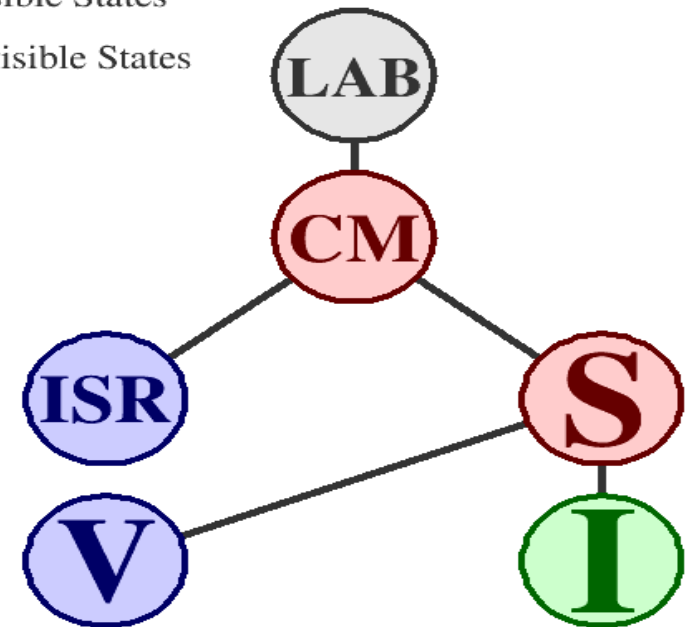
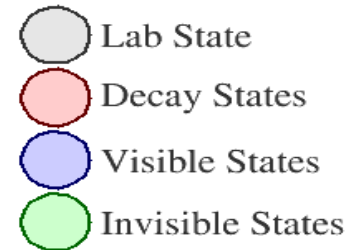
- $\vec{P}_T(\text{CM}) = \vec{P}_T + \sum_i \vec{P}_T(jet_i)$

Boost in the *estimated* **CM** frame

- Combinatoric jigsaw rule based on the minimization of the masses

$$\text{In CM frame } E_{CM} \equiv M_{CM} = \sqrt{M_{ISR} + p^2} + \sqrt{M_S + p^2}$$

Equivalent to maximize  $p$  or find the thrust axis in the CM frame





# A complete basis of variables

Kinematics observables to probe SUSY in the compressed regime

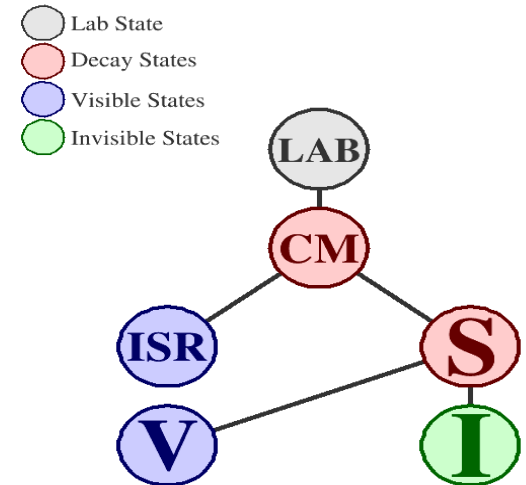
$p_{\text{ISR},T}^{\text{CM}}$  Magnitude of the jets vector-sum transverse momentum of **ISR**-system evaluated in the CM frame (  $\vec{p}_{\text{ISR},T}^{\text{CM}} = -\vec{p}_{\text{S},T}^{\text{CM}}$  )

$R_{\text{ISR}} \equiv \frac{|\vec{p}_{\text{I},T}^{\text{CM}} \cdot \hat{p}_{\text{ISR},T}^{\text{CM}}|}{p_{\text{ISR},T}^{\text{CM}}} \sim \frac{M_{\tilde{\chi}_1^0}}{M_{\tilde{p}}}$  Variable sensitive to the mass ratio

$M_T^{\text{S}}$  Transverse mass of **S** system (**V+I**)

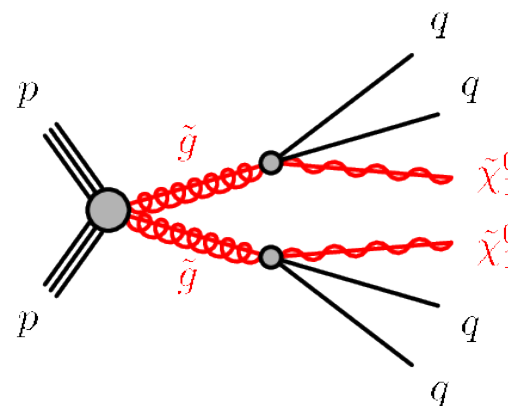
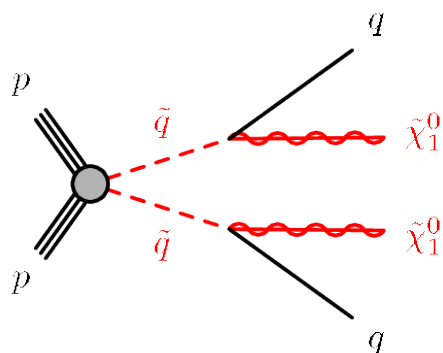
$N_{\text{jet}}^{\text{V}}$  Number of jets assigned to the **V** system (i.e. not associated with the ISR system)

$\Delta\phi_{\text{ISR},\text{I}}$  Opening angle between the ISR system and the I system, evaluated in the CM frame.



# The samples

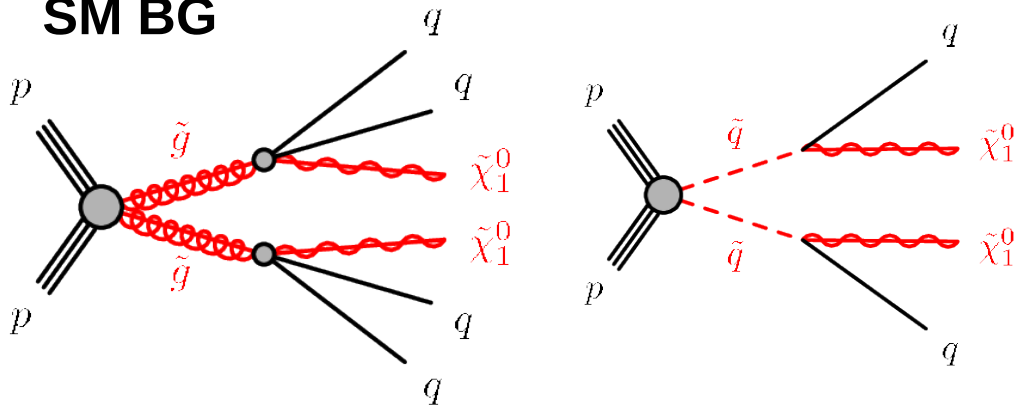
- Samples of all major Standard Model backgrounds as part of the Snowmass study simulated at 14TeV (see arXiv:1308.1636 and 1309.1057 for details)
- All signal and BG samples are generated/simulated using same versions and data\_cards Madgraph+Pythia+Delphes with jet-parton matching and corrections for next-to-leading order (NLO) contributions.
- **Signals: Squark and Gluino pair production** in the compressed-regime



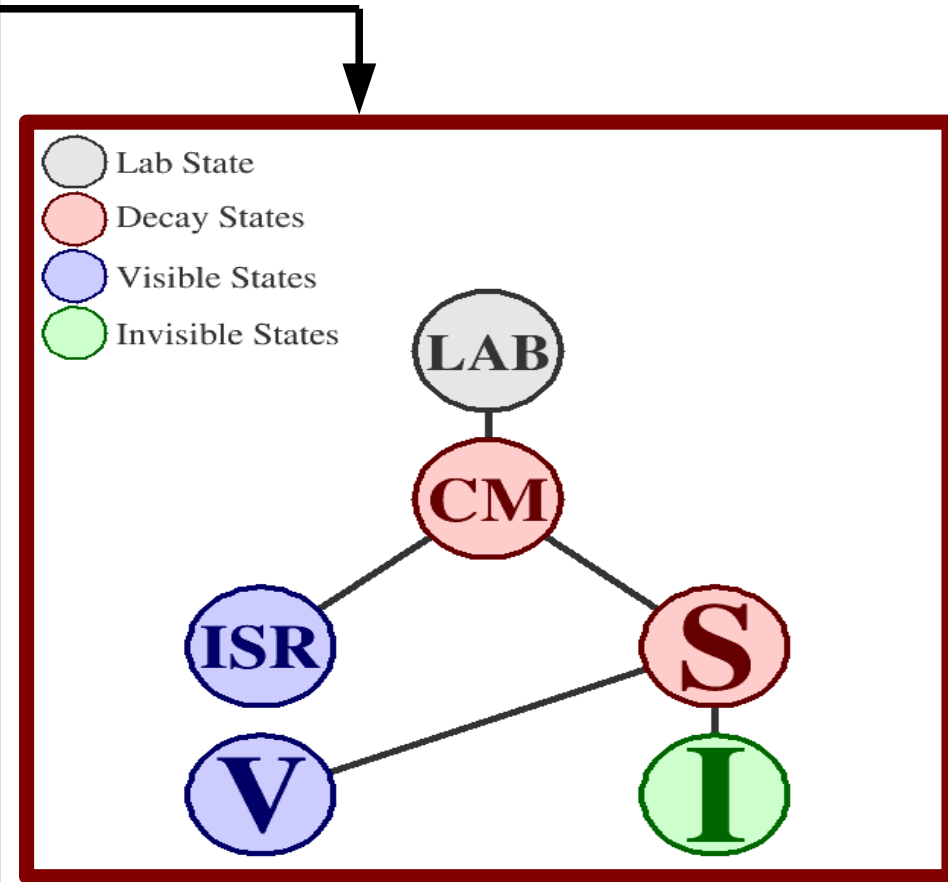
- Mass splittings:  $M_{\tilde{P}} - M_{\tilde{\chi}_1^0} = 25, 50, 100, 200 \text{ GeV}$
- Squark mass  $500 \text{ GeV} \leq M_{\tilde{q}} \leq 1000 \text{ GeV}$       Gluino Mass:  $500 \text{ GeV} \leq M_{\tilde{g}} \leq 1400 \text{ GeV}$
- All samples are scaled to a projection of  $\int L = 100 \text{ fb}^{-1}$       [arXiv:1607.08307 \[hep-ph\]](https://arxiv.org/abs/1607.08307)

# The compressed RJR tree

## SM BG

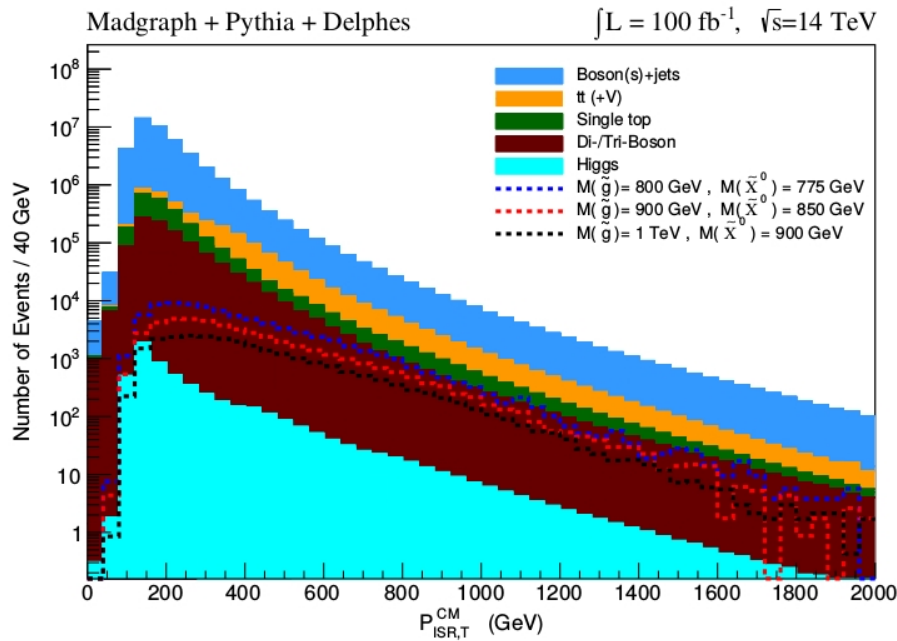


- Pre-selection criteria: final states with
  - Lepton veto (e and mu)
  - $\cancel{E}_T > 100 \text{ GeV}$
  - $p_T(\text{jet}) > 20 \text{ GeV}$



**Complete basis of RJR observables**

# Compressed kinematics for squark/gluino



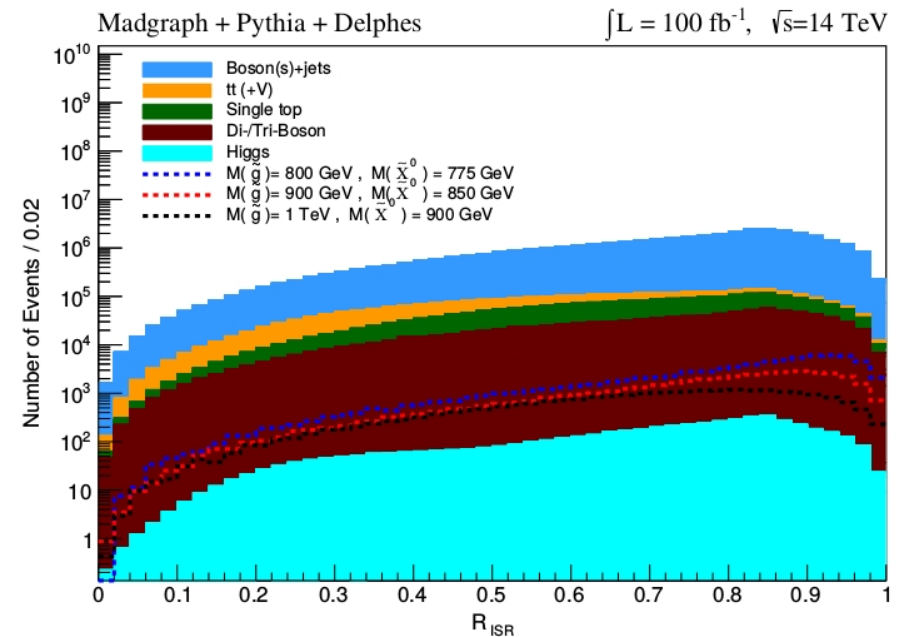
$$p_{ISR,T}^{CM}$$

magnitude of vector-sum transverse momentum of all 'ISR' associated jets evaluated in CM frame

Little discrimination in the absence of other cuts

$$R_{ISR} \equiv \left| \vec{p}_{I,T}^{CM} \cdot \hat{p}_{ISR,T}^{CM} \right| / p_{ISR,T}^{CM}$$

Our choice for  $\frac{M_{\tilde{\chi}_1^0}}{M_{\tilde{P}}}$  sensitive variable

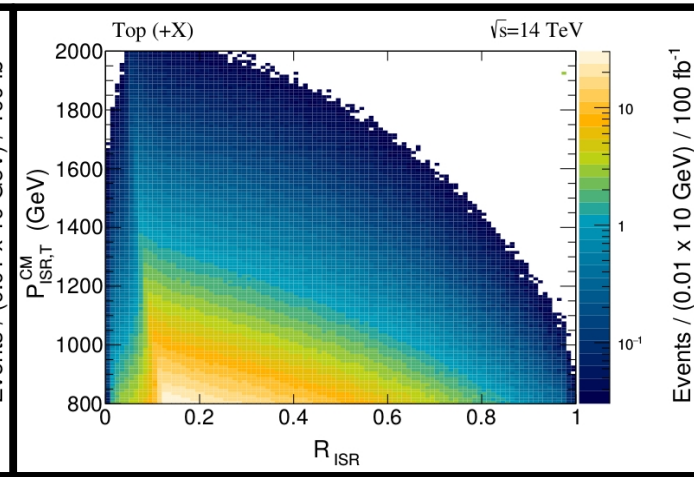
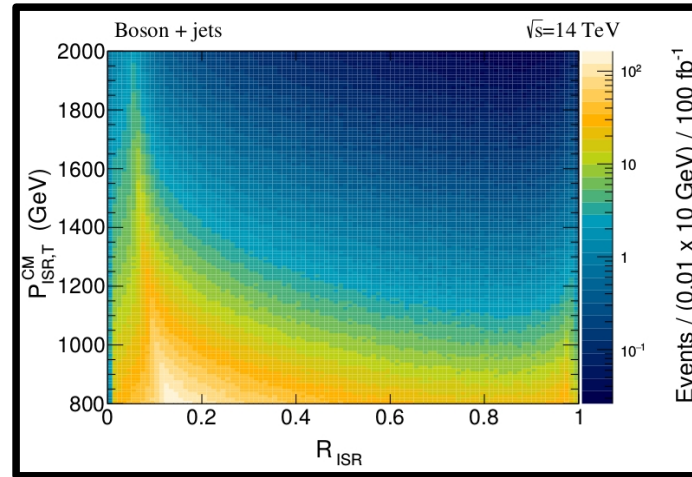
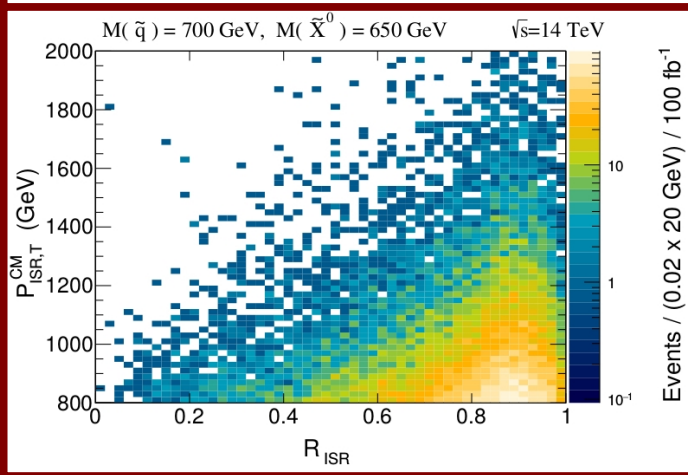
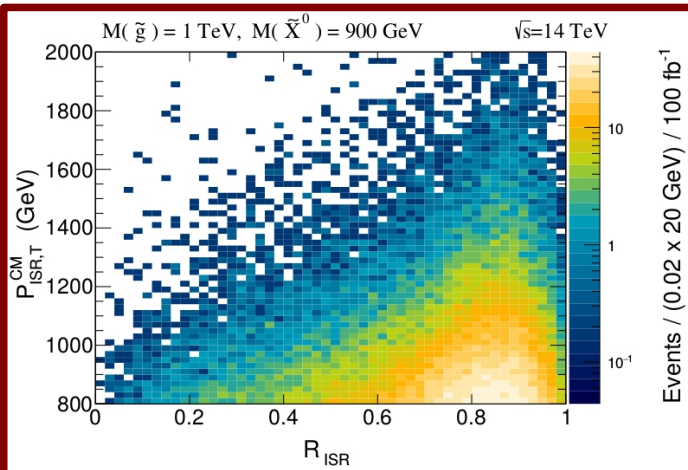


# Complementarity of the ratio and transverse ISR-momentum

Backgrounds

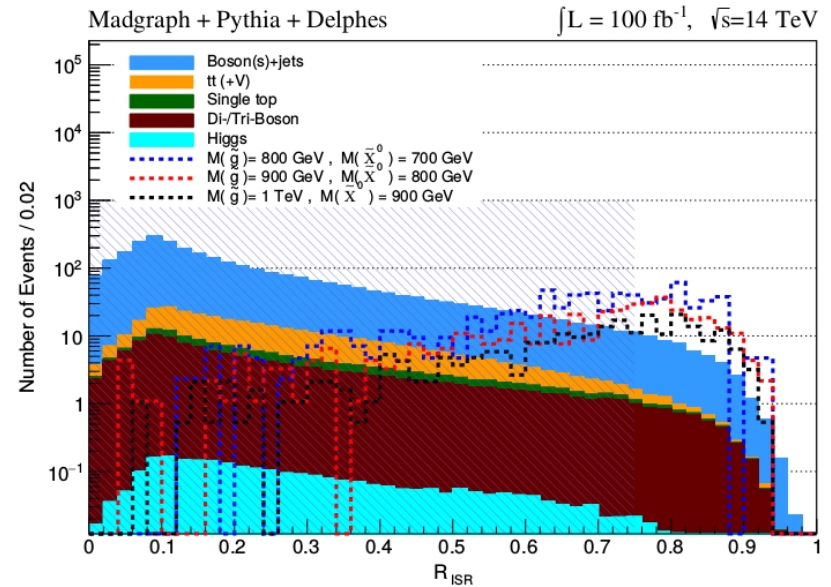
$$R_{\text{ISR}} \text{ vs } p_{\text{ISR},T}^{\text{CM}}$$

Signal



Increasingly hard for backgrounds to have large  $R_{\text{ISR}}$  for higher  $p_{\text{ISR},T}^{\text{CM}}$

$R_{\text{ISR}}$   
Great discrimination  
in the high  
ISR-regime

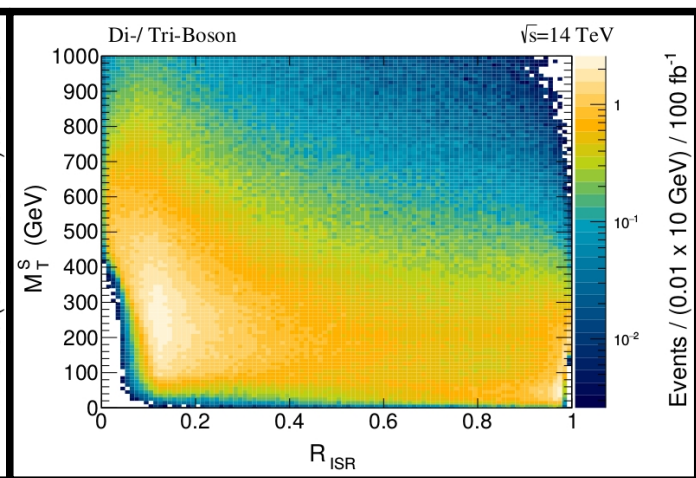
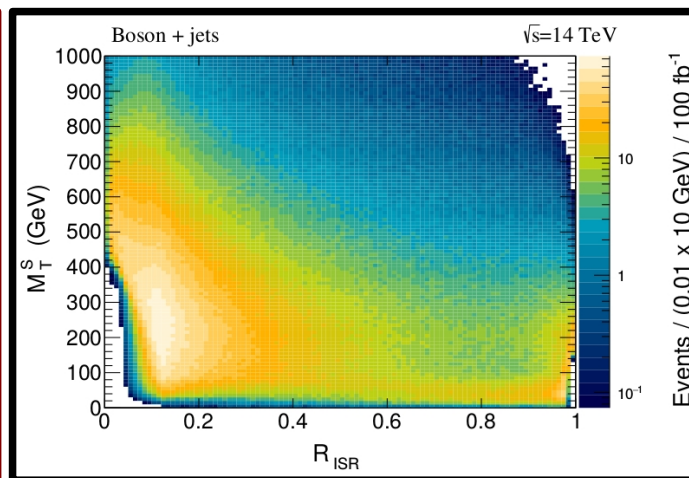
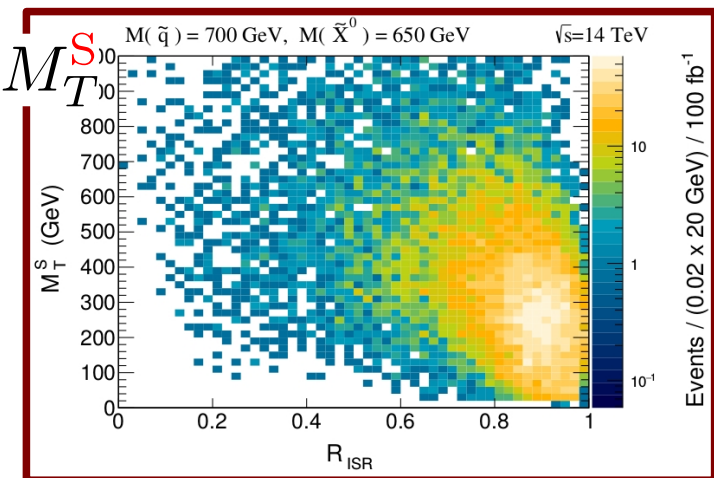
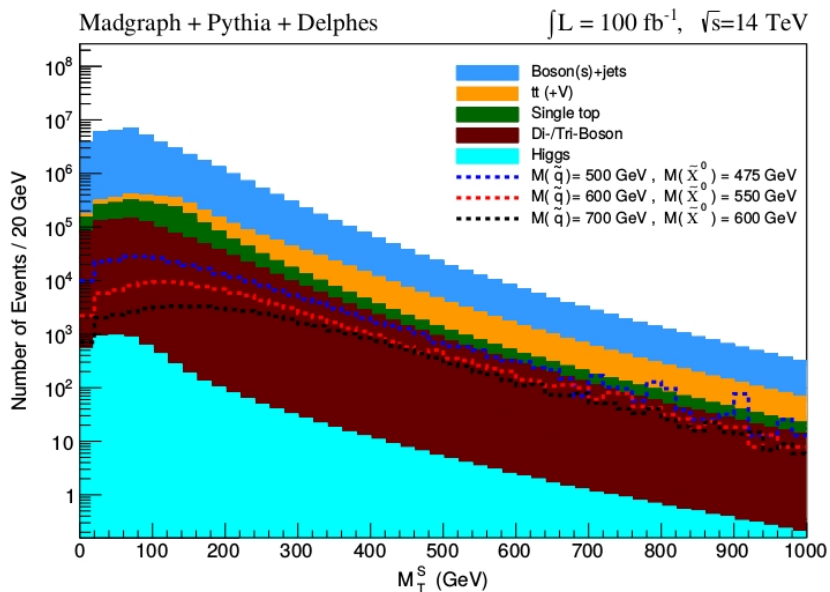


# Transverse mass of the S-system

$$M_T^S$$

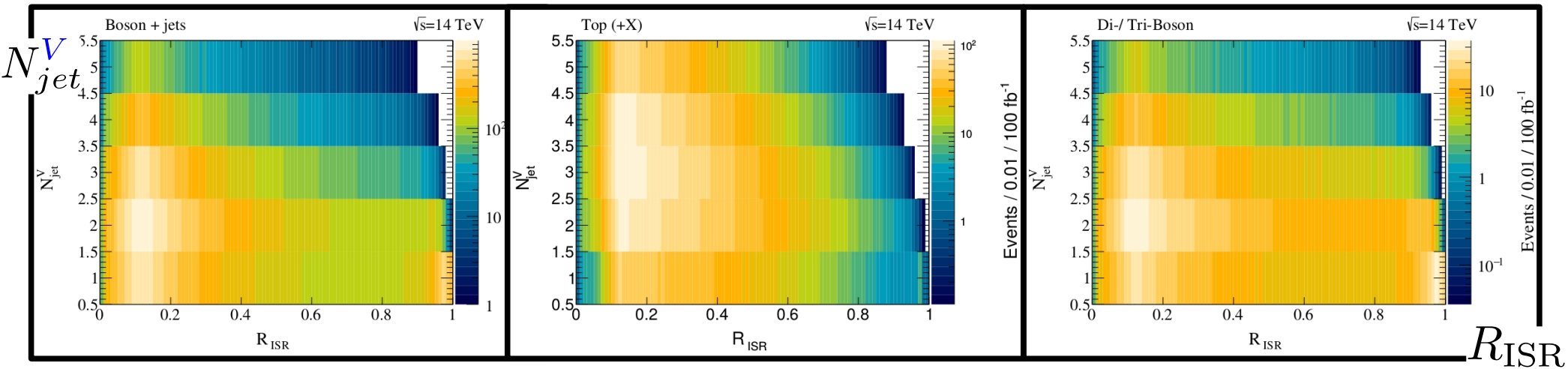
Transverse mass of **S** (V+I) system

- Largely uncorrelated: complementary with other variables
- Good discrimination particularly against V+jets

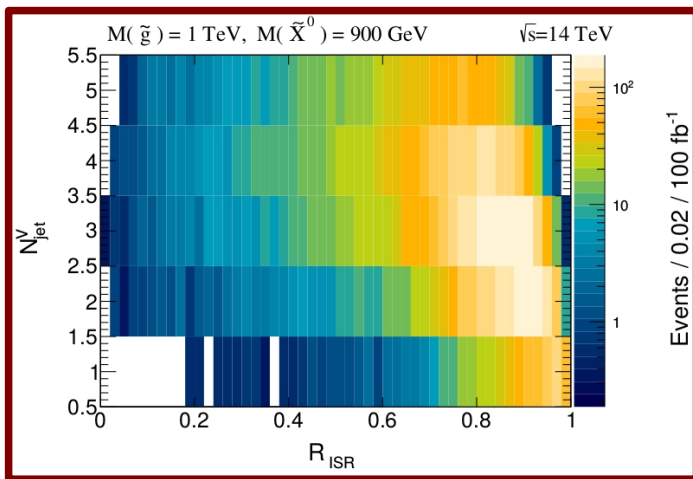


$R_{ISR}$

# Jet multiplicity in the V-system

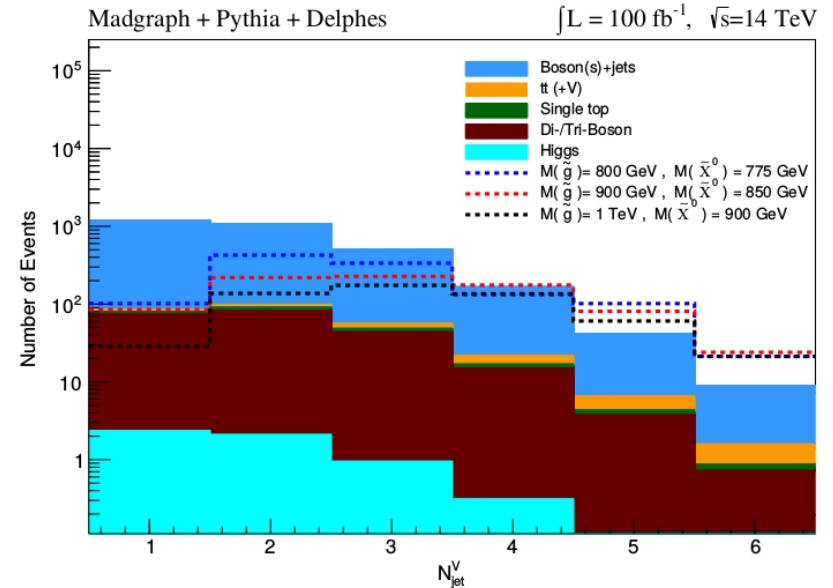


After the high  $p_{ISR,T}^{CM}$  selection criterion, we get excellent performances cutting harder on the jet multiplicity together with the ratio: particularly gluino vs Boson(s) + jets



$N_{jet}^V$

Number of jets  
in V-system



# Inclusive gluino (squark) signal regions

A set of selection criteria for signal regions in the analysis of gluino (squark) pair-production defined targeting the mass splittings.

Variable \ Mass splitting [GeV]	$\Delta M = 25$	$\Delta M = 50$	$\Delta M = 100$	$\Delta M = 200$
Preselection criteria	Lepton (e and mu) and $b$ -jet veto, $\cancel{E}_T > 100$ GeV, $p_T(jet) > 20$ GeV			
$p_{ISR,T}^{CM}$ [GeV]	$> 1000$			
$R_{ISR}$	$> 0.9$	$> 0.85$	$> 0.75$	$> 0.65$
$M_T^S$ [GeV]	-	100	250	400
$N_{jet}^V$	$\geq 3$ ( $\geq 2$ )		$\geq 4$ ( $\geq 2$ )	
$p_T^{jet3,V}$ ( $p_T^{jet2,V}$ ) [GeV]	$> 20$ ( $> 40$ )	$> 30$ ( $> 60$ )	$> 40$ ( $> 120$ )	$> 50$ ( $> 140$ )
$\Delta\phi_{ISR,I}$	$> 3.0$			



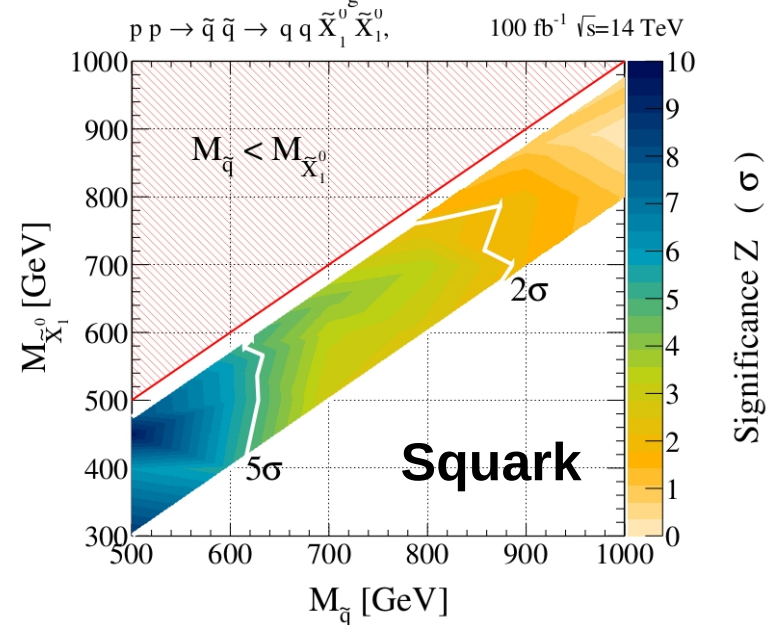
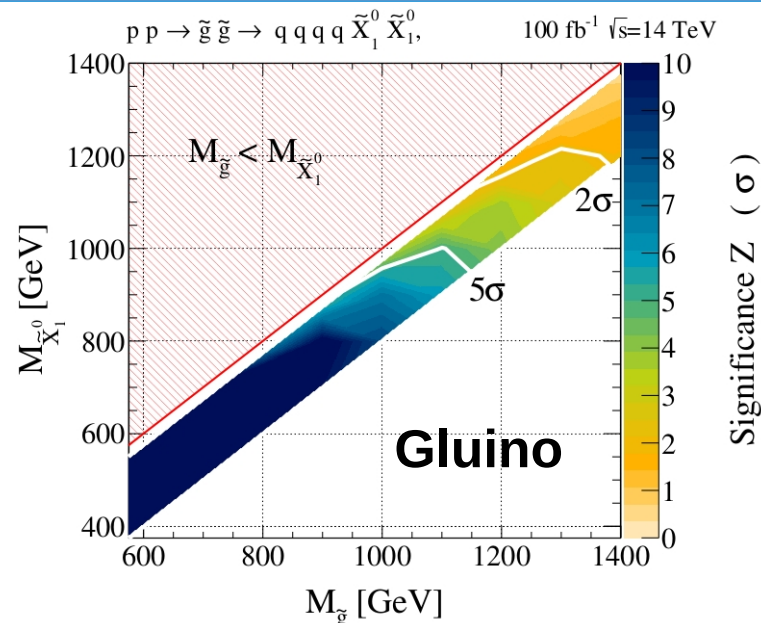
# Results

- Z-score from the RJR inclusive signal regions
- We assume **15%** for the background systematic uncertainty
- **Glino** *Discover:* above 1 TeV  
*Exclusion:* up to 1.4 TeV
- **Squark** *Discover:* above 600 GeV  
*Exclusion:* between 800 and 900 GeV
- Optimisation can be improved using different signal regions for squark and gluino

RJR technique is used by ATLAS collaboration.

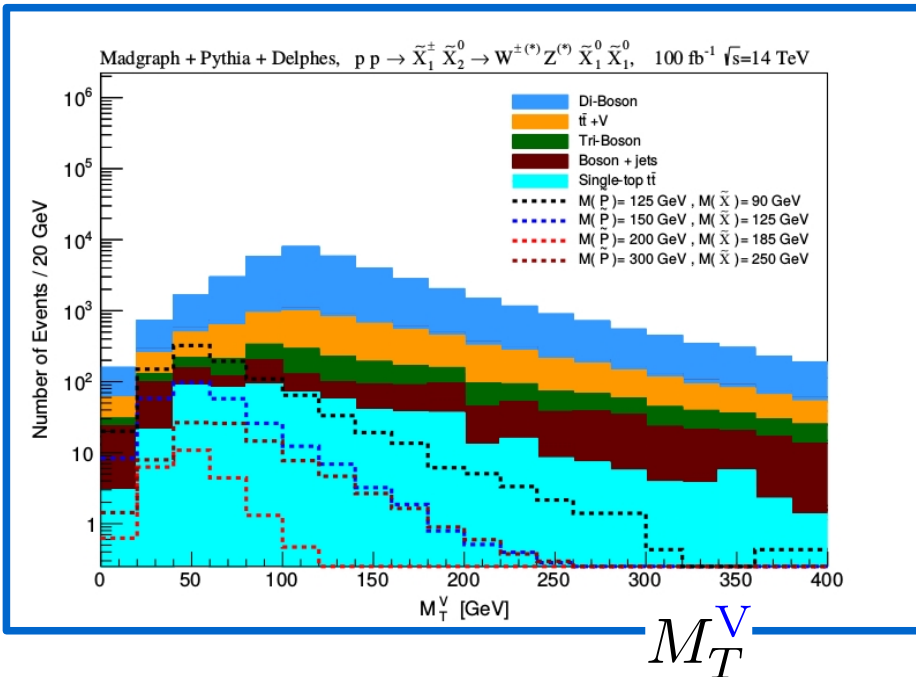
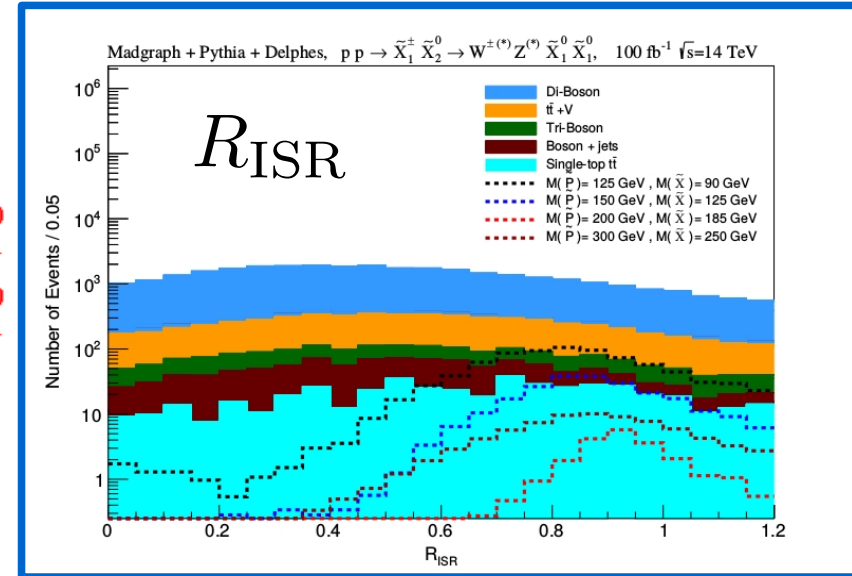
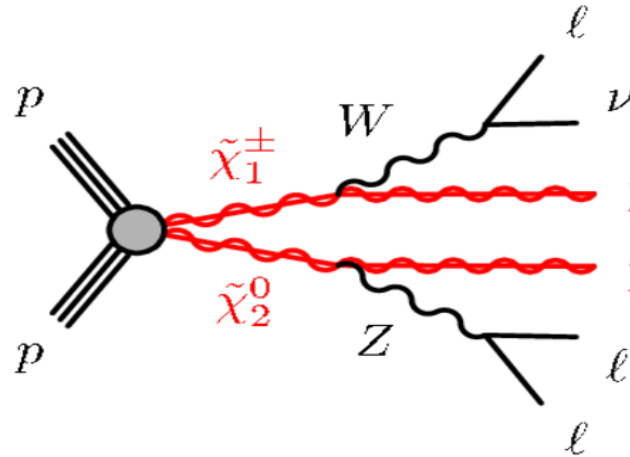
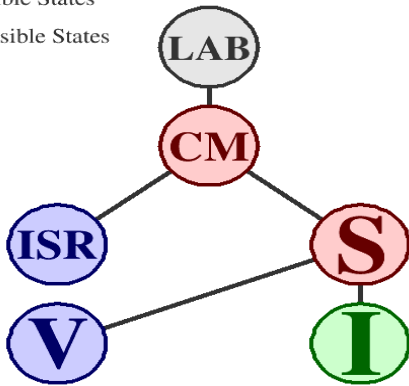
Compressed gluino-squark:

ATLAS-CONF-2016-078 - ATLAS-CONF-2016-077



# SUSY EWK : associated neutralino chargino production

- Lab State
- Decay States
- Visible States
- Invisible States



No ambiguity in the assignment

**V**-system = leptons

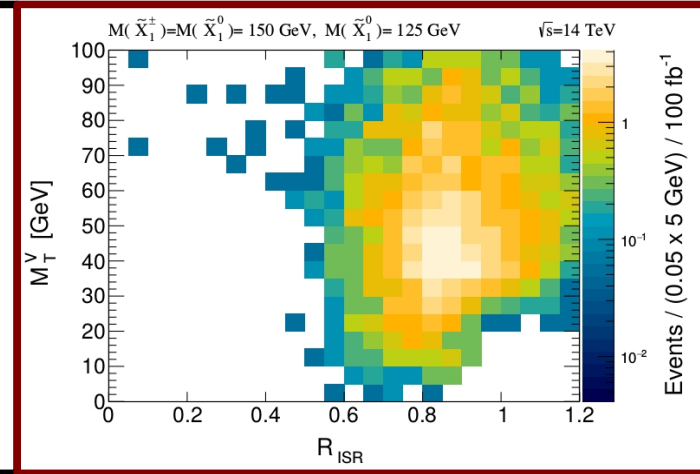
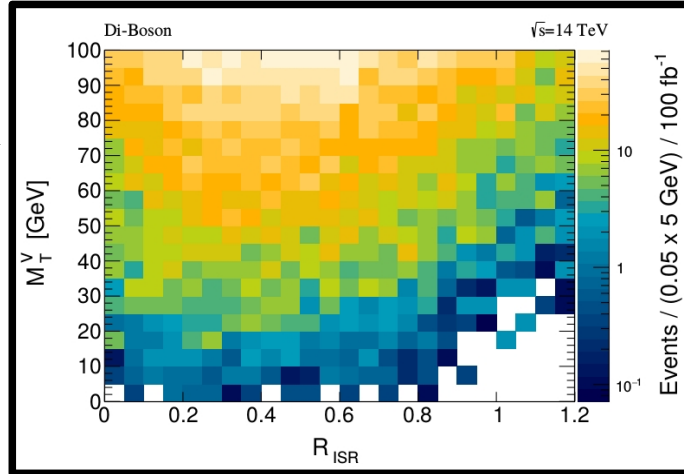
**ISR**-system = jets

$M_T^V$  : Transverse Mass of the Visible system

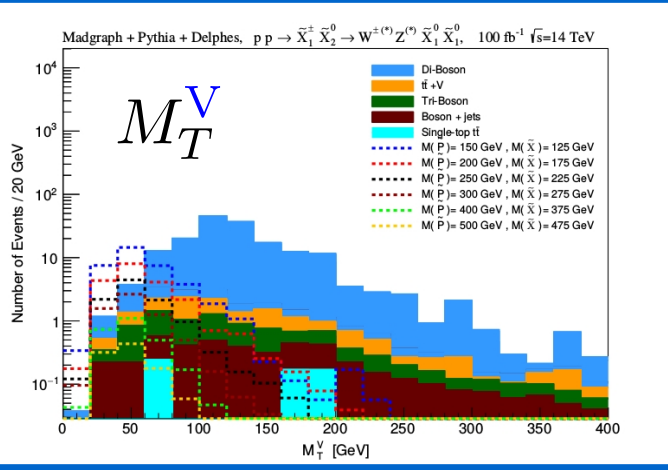
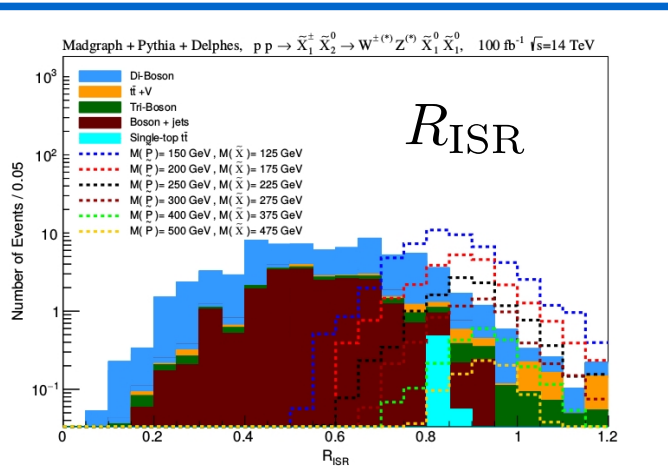
$$M_{\tilde{P}} - M_{\tilde{\chi}_1^0} = 15, 25, 35, 50, 75 \text{ GeV}$$

# EWKino: associated neutralino chargino production

$R_{ISR}$  vs  $M_T^V$

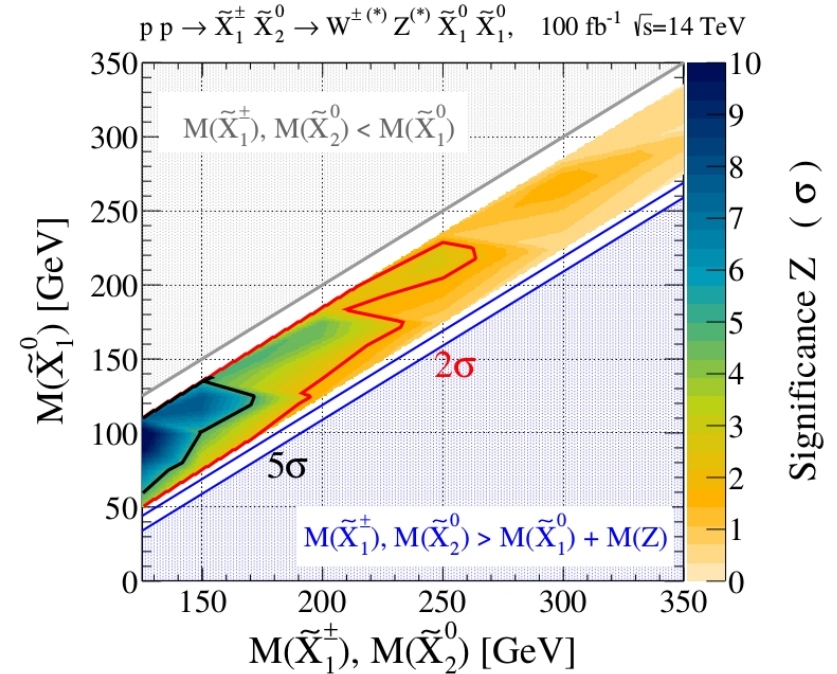


← Applying selection criteria based on RJR observables

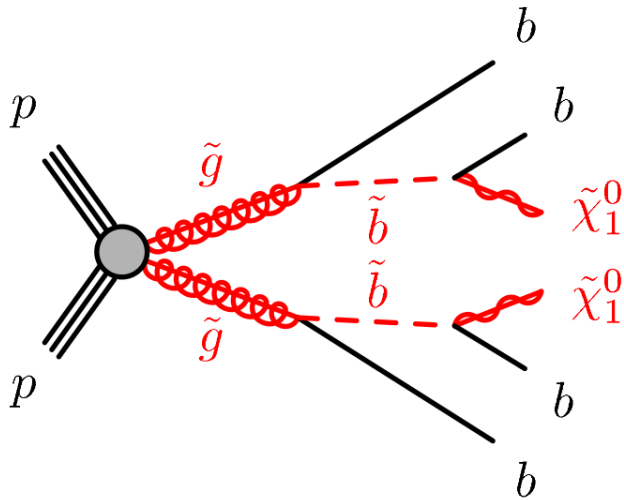


Z-value assuming **15%** of systematic uncertainty and

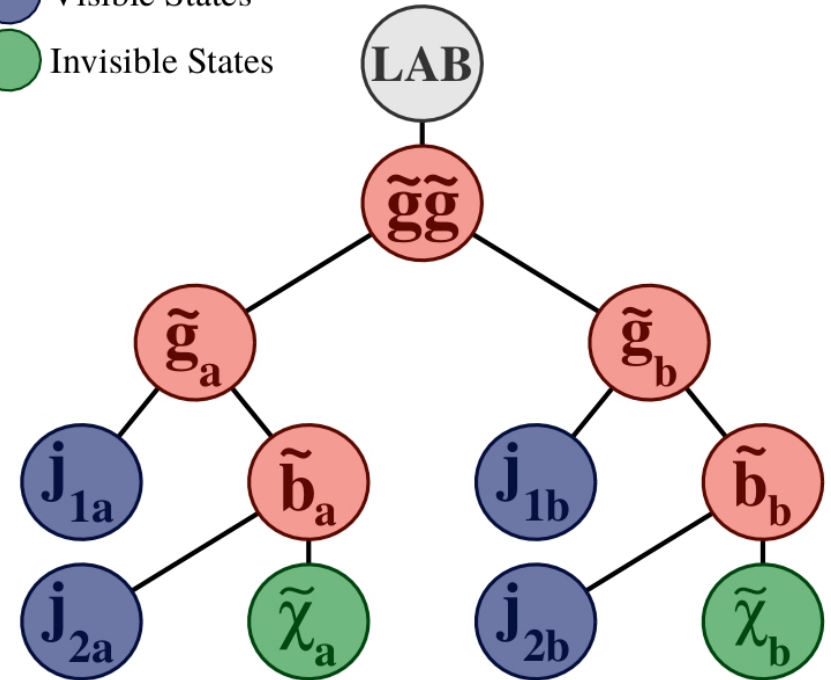
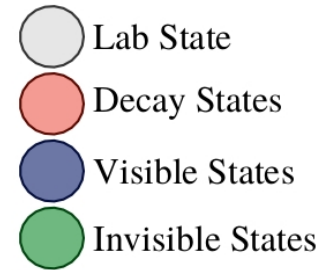
$$\int L = 100\text{fb}^{-1}$$



# Glino mediated sbottom pair production



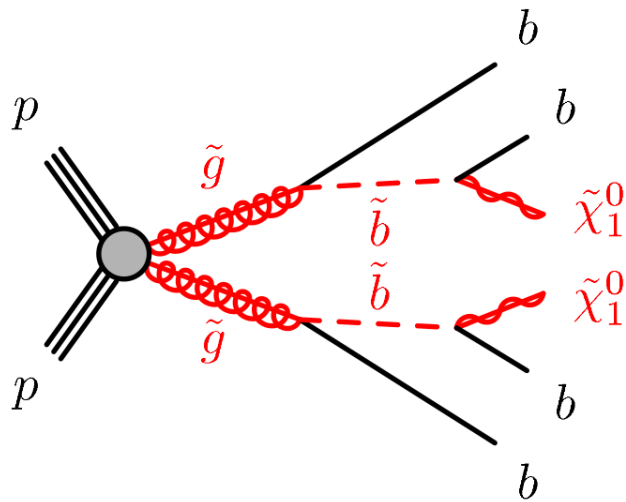
- Open mass spectra: RJR tree describes the SUSY substructure
- Jigsaw rules: **unknown d.o.f. + combinatoric** travelling recursively through the frames
- Complete basis of scale and angular variables computed in the appropriate frame



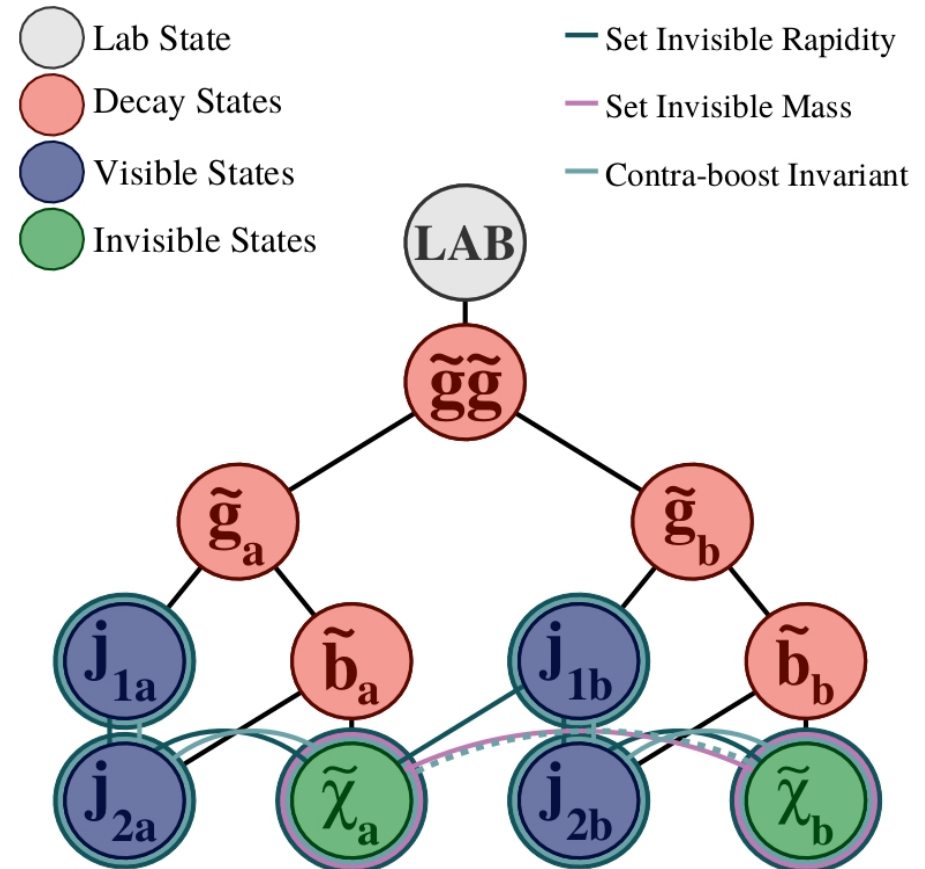
$$M_{\tilde{g}\tilde{g}} \quad E(j_{1a}) \quad E(j_{2a}) \quad E(j_{1b}) \quad E(j_{2b})$$

$$\cos \theta_{\tilde{g}\tilde{g}} \quad \cos \theta_{\tilde{g}_a} \quad \cos \theta_{\tilde{g}_b} \quad \cos \theta_{\tilde{b}_a} \quad \cos \theta_{\tilde{b}_b} \quad \Delta\varphi_{\tilde{g}_a\tilde{g}_b} \quad \Delta\varphi_{\tilde{g}_a\tilde{b}_a} \quad \Delta\varphi_{\tilde{g}_b\tilde{b}_b}$$

# Glauino mediated sbottom pair production



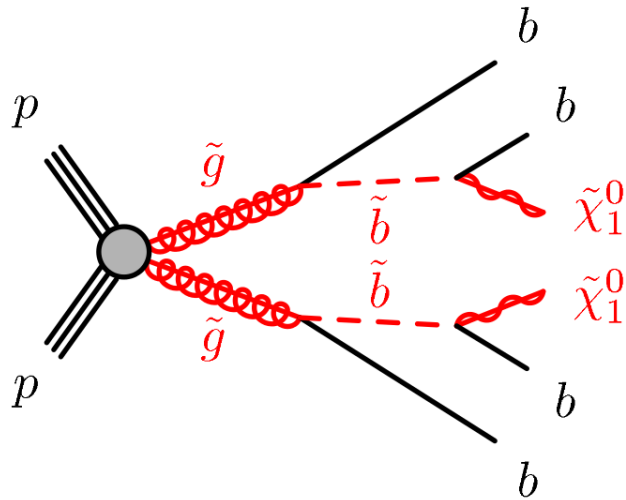
- Open mass spectra: RJR tree describes the SUSY substructure
- Jigsaw rules: **unknown d.o.f. + combinatoric** travelling recursively through the frames
- Complete basis of scale and angular variables computed in the appropriate frame



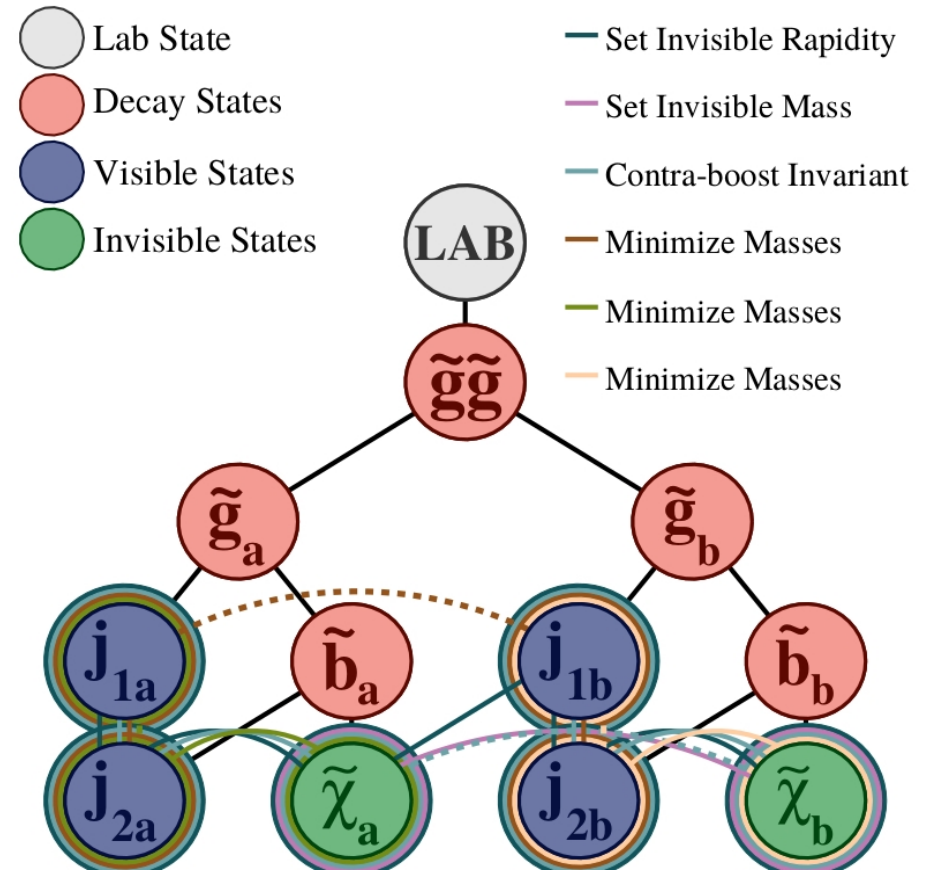
$$M_{\tilde{g}\tilde{g}} \quad E(j_{1a}) \quad E(j_{2a}) \quad E(j_{1b}) \quad E(j_{2b})$$

$$\cos \theta_{\tilde{g}\tilde{g}} \quad \cos \theta_{\tilde{g}_a} \quad \cos \theta_{\tilde{g}_b} \quad \cos \theta_{\tilde{b}_a} \quad \cos \theta_{\tilde{b}_b} \quad \Delta\varphi_{\tilde{g}_a\tilde{g}_b} \quad \Delta\varphi_{\tilde{g}_a\tilde{b}_a} \quad \Delta\varphi_{\tilde{g}_b\tilde{b}_b}$$

# Glino mediated sbottom pair production



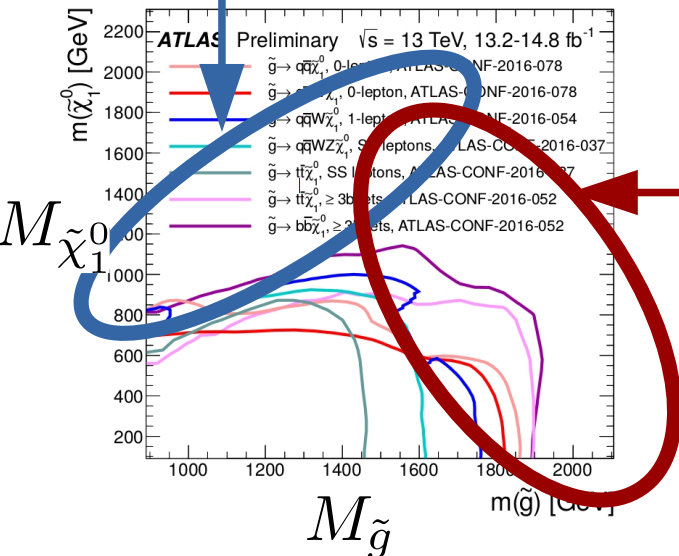
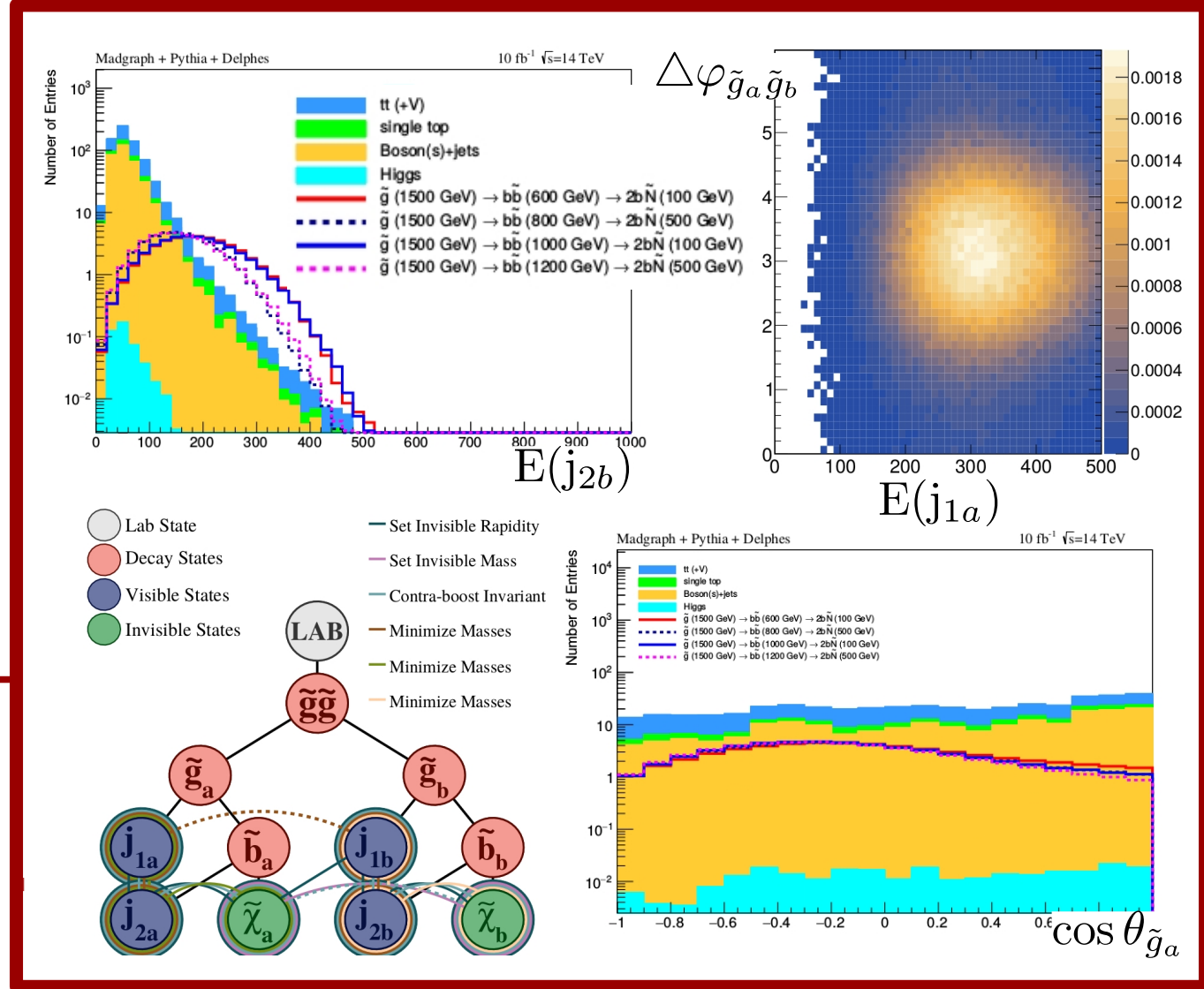
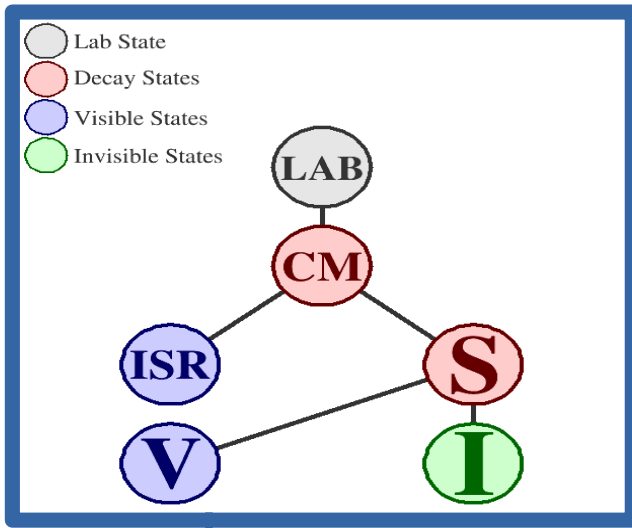
- Open mass spectra: RJR tree describes the SUSY substructure
- Jigsaw rules: **unknown d.o.f. + combinatoric** travelling recursively through the frames
- Complete basis of scale and angular variables computed in the appropriate frame



$$M_{\tilde{g}\tilde{g}} \quad E(j_{1a}) \quad E(j_{2a}) \quad E(j_{1b}) \quad E(j_{2b})$$

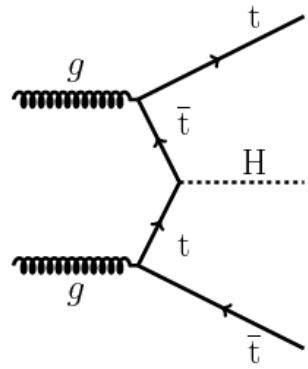
$$\cos \theta_{\tilde{g}\tilde{g}} \quad \cos \theta_{\tilde{g}_a} \quad \cos \theta_{\tilde{g}_b} \quad \cos \theta_{\tilde{b}_a} \quad \cos \theta_{\tilde{b}_b} \quad \Delta\varphi_{\tilde{g}_a\tilde{g}_b} \quad \Delta\varphi_{\tilde{g}_a\tilde{b}_a} \quad \Delta\varphi_{\tilde{g}_b\tilde{b}_b}$$

# Glino mediated sbottom production



Work in progress with Paul Jackson and Chris Rogan

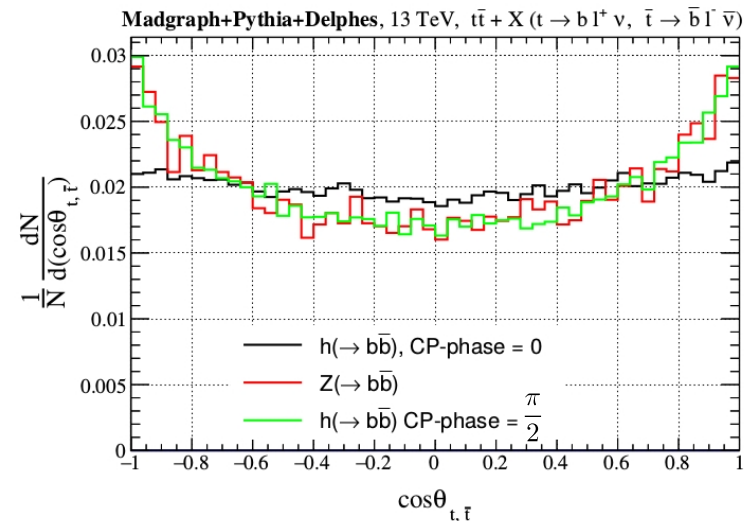
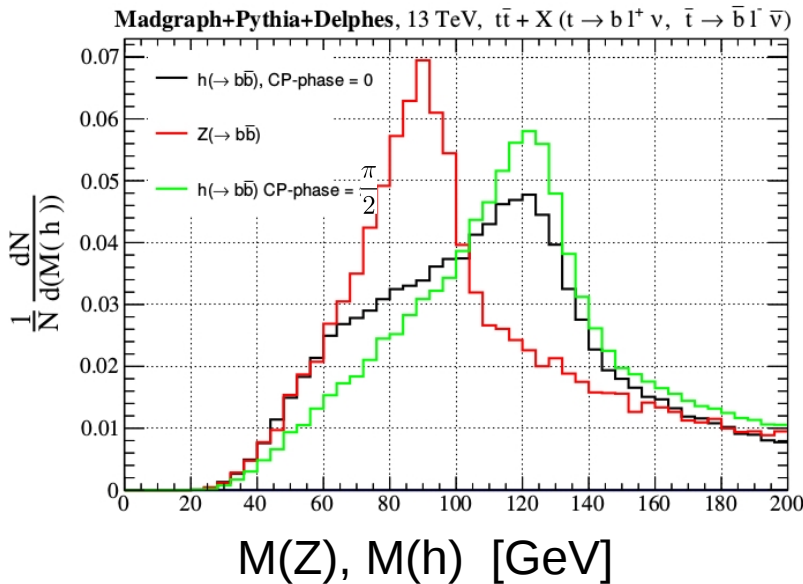
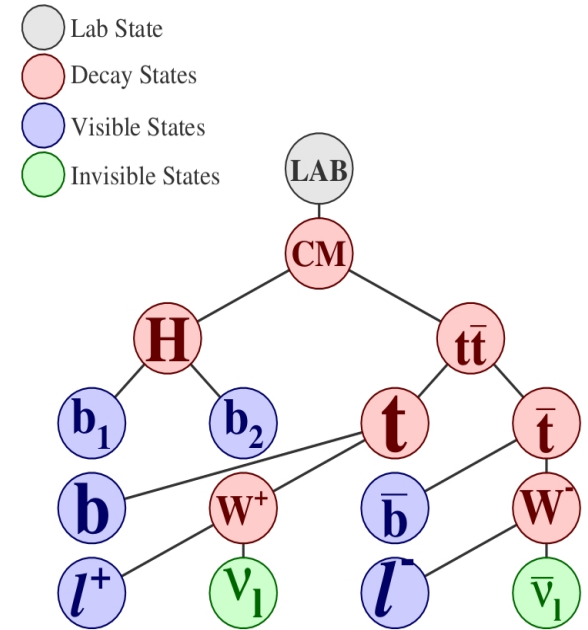
# Higgs + top pair production in di-leptonic channel



RJR tree  $\rightarrow$

Compare the observables that are sensitive to the CP nature of the Higgs

Demonstrate the feasibility of the di-leptonic channel of  $t\bar{t} + h$  at LHC with the RJR method



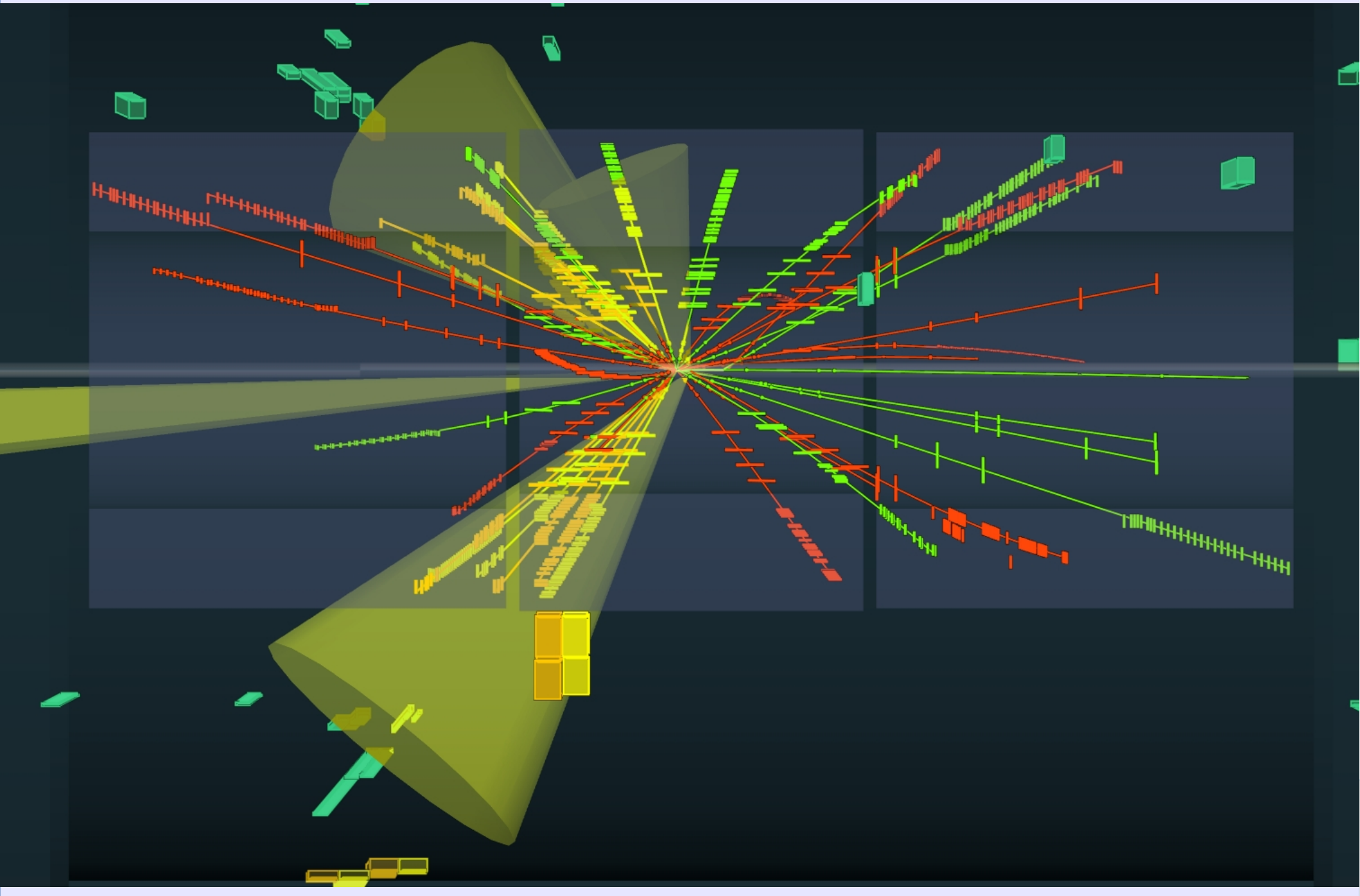
Work in progress with Lei Wu and Jason Yue



# Summary - Outlook

- Demonstrated a new approach for **open** and **compressed** analyses based on the Recursive Jigsaw Reconstruction technique
- **Compressed gluino - squark** scenarios: excellent performance for all mass-splittings and final state topologies studied (arXiv:1607.08307 [hep-ph])
- **Compressed EWKino**: No ambiguity in assignment of leptons and jets to ISR-V system:
  - Excellent performance for associated **neutralino chargino** production
  - In preparation → **chargino pair** production
- RJR can be applied in principle to any open final states: SUSY and beyond
  - **Gluino mediated sbottom production**
  - **Top pair (in di-leptonic channel) + Higgs**
  - ...
- The method is already being used by the ATLAS collaboration

THANKS FOR YOUR ATTENTION

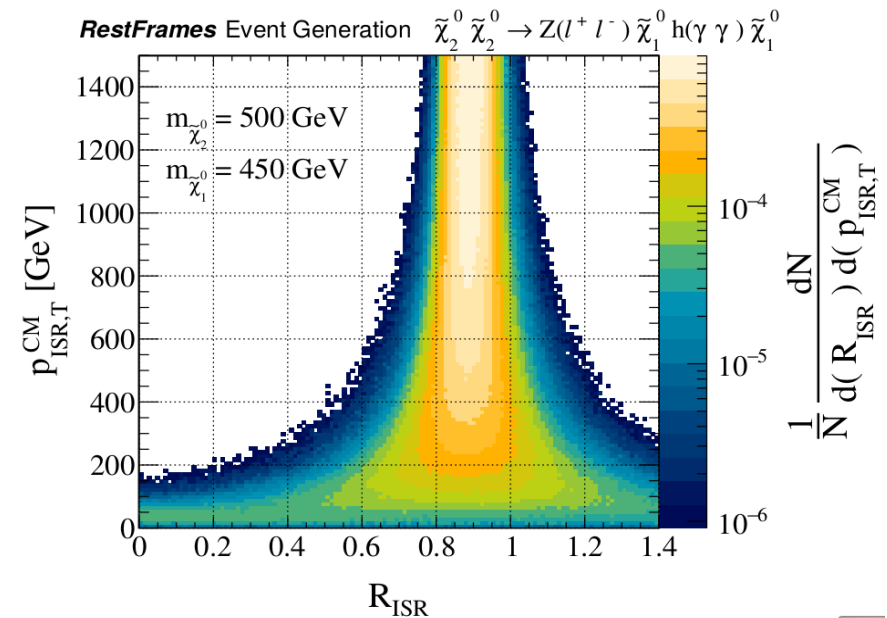
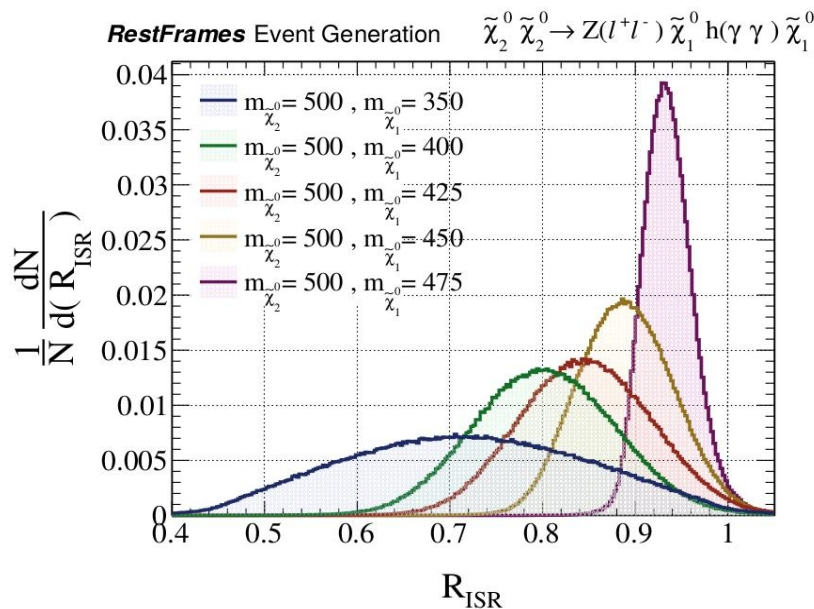


# Backup slides: sparticles in motion

- In the limit of soft momentum of the LSPs in the sparents frame:

$$R_{\text{ISR}} \sim |\cancel{E}_T \cdot \hat{p}_{\text{ISR},T}| / p_{\text{ISR},T} \sim \frac{m_{\tilde{\chi}_1^0}}{m_{\tilde{P}}} \left[ 1 + \mathcal{O} \left( \frac{p_{\tilde{\chi}_1^0}^{\tilde{P}}}{2m_{\tilde{P}}} \right) \left( \frac{\sqrt{p_{\text{ISR},T}^2 + m_{\tilde{P}\tilde{P}}^2}}{p_{\text{ISR},T}} \right) \sin \Omega \right]$$

- R scales nicely with the mass ratio - Width depends on DM - Resolution improves with PTISR



# Backup slides: set rapidity of the invisible particles

$$\beta_z (\text{Lab} \rightarrow \text{Tra}) \quad 0 = \frac{\partial E_\phi^{\text{Tra}}}{\partial \beta_z}$$

$$0 = (1 - \beta_z^2)^{-3/2} (\beta_z E_\phi - p_z(\phi))$$

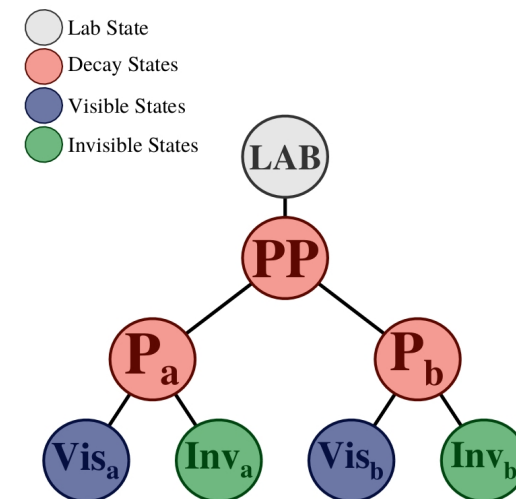
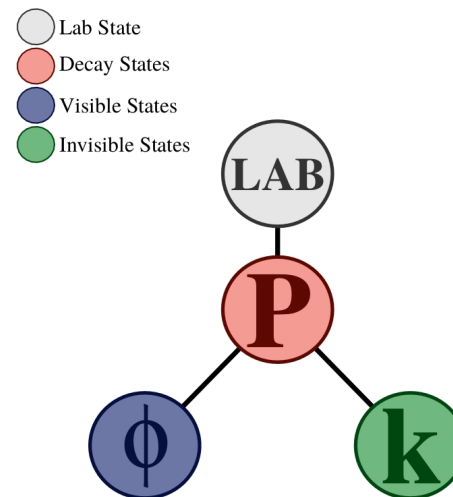
$$\beta_z = \frac{p_z(\phi)}{E_\phi}$$

The guess for  $p_z^{\text{Tra}}(P) = 0$

Being  $p_z^{\text{Tra}}(\phi) = 0 \rightarrow p_z^{\text{Tra}}(k) = 0$

All the observables in the transverse frame and any frames that recursively follow from it are independent from the true value  $\rightarrow$  Generalization

$$\beta_z = \frac{p_z(\text{Vis}_a) + p_z(\text{Vis}_b)}{E_{\text{Vis}_a} + E_{\text{Vis}_b}}$$



# Backup slides: NC signal regions

$\downarrow$ Variable \ $\Delta M$ [GeV] $\rightarrow$	$\Delta M = 15$	$\Delta M = 25$	$\Delta M = 35$	$\Delta M = 50$	$\Delta M = 75$
Objects criteria	3 Leptons (e and mu) $p_T(lep) > 10$ GeV,				
	At least one jet, $p_T(jet) > 20$ GeV, $N_{b-jet}^{ISR} = 0$				
$p_{ISR,T}^{CM} (\cancel{E}_T)$ [GeV]	$> 50$			$> 70$	$> 100$
$N_{jet}^{ISR}$	$< 3$	$< 4$		$< 3$	
$M_T^V$ , for 3 SFL [GeV]	$< 40$	$< 50$	$< 60$	$< 70$	$< 80$
$M_{l+l^-}$ , for 2 SFL [GeV]	$< \Delta M$ with $M_T^V < 100$ GeV				
$\Delta\phi_{CM,I}$	$> 2$				
$\Delta\phi_{ISR,I}$	$> 3$				

# Backup slides NC signal regions

$$R_{\text{ISR}} \sim |\cancel{E}_T \cdot \hat{p}_{\text{ISR},T}| / p_{\text{ISR},T} \sim \frac{m_{\tilde{\chi}_1^0}}{m_{\tilde{P}}} \left[ 1 + \mathcal{O} \left( \frac{p_{\tilde{\chi}_1^0}^{\tilde{P}}}{2m_{\tilde{P}}} \right) \left( \frac{\sqrt{p_{\text{ISR},T}^2 + m_{\tilde{P}\tilde{P}}^2}}{p_{\text{ISR},T}} \right) \sin \Omega \right]$$

GeV $\rightarrow$	$\Delta M = 15$	$\Delta M = 25$	$\Delta M = 35$	$\Delta M = 50$	$\Delta M = 75$
$M_{\tilde{P}}=125$ GeV	0.80 – 1.15	0.80 – 1.15	0.80 – 1.20	0.70 – 1.15	0.65 – 1.10
$M_{\tilde{P}}=150$ GeV	0.85 – 1.05	0.80 – 1.15	0.80 – 1.20	0.70 – 1.15	0.70 – 1.10
$M_{\tilde{P}}=200$ GeV	0.85 – 1.05	0.85 – 1.15	0.80 – 1.20	0.70 – 1.15	0.70 – 1.10
$M_{\tilde{P}}=250$ GeV	0.90 – 1.05	0.85 – 1.15	0.85 – 1.20	0.75 – 1.05	0.75 – 1.10
$M_{\tilde{P}}=300$ GeV	0.90 – 1.05	0.85 – 1.15	0.85 – 1.20	0.75 – 1.05	0.75 – 1.10
$M_{\tilde{P}}=400$ GeV	0.90 – 1.05	0.90 – 1.15	0.85 – 1.20	0.80 – 1.05	0.75 – 1.10
$M_{\tilde{P}}=500$ GeV	0.90 – 1.05	0.90 – 1.15	0.85 – 1.20	0.85 – 1.05	0.80 – 1.10

# Backup slides

- In order to distinguish between signal and backgrounds we need an ISR system to give our sparticles a transverse kick: the response of the sparticle decay products is sensitive to the mass of the LSP
- In the limit where the LSPs receive no momentum from their parents' decays:

$$\vec{E}_T \sim -\vec{p}_T^{\text{ISR}} \times \frac{m_{\tilde{\chi}}}{m_{\tilde{P}}}$$

- Different proxies for pTISR in the recent literature

arXiv:1506.00653  $\frac{E_T}{p_T^{\text{lead jet}}}$  arXiv:1506.07885v1  $\frac{E_T}{\sqrt{H_T}}$   
arXiv:1605.06479 final state jet hierarchy

- Rather than relying on a clean mono-ISR signal or a priori assumption of the sparticles masses we want to separate “ISR objects” from “sparticle objects”

# Backup slides: sparticles in motion

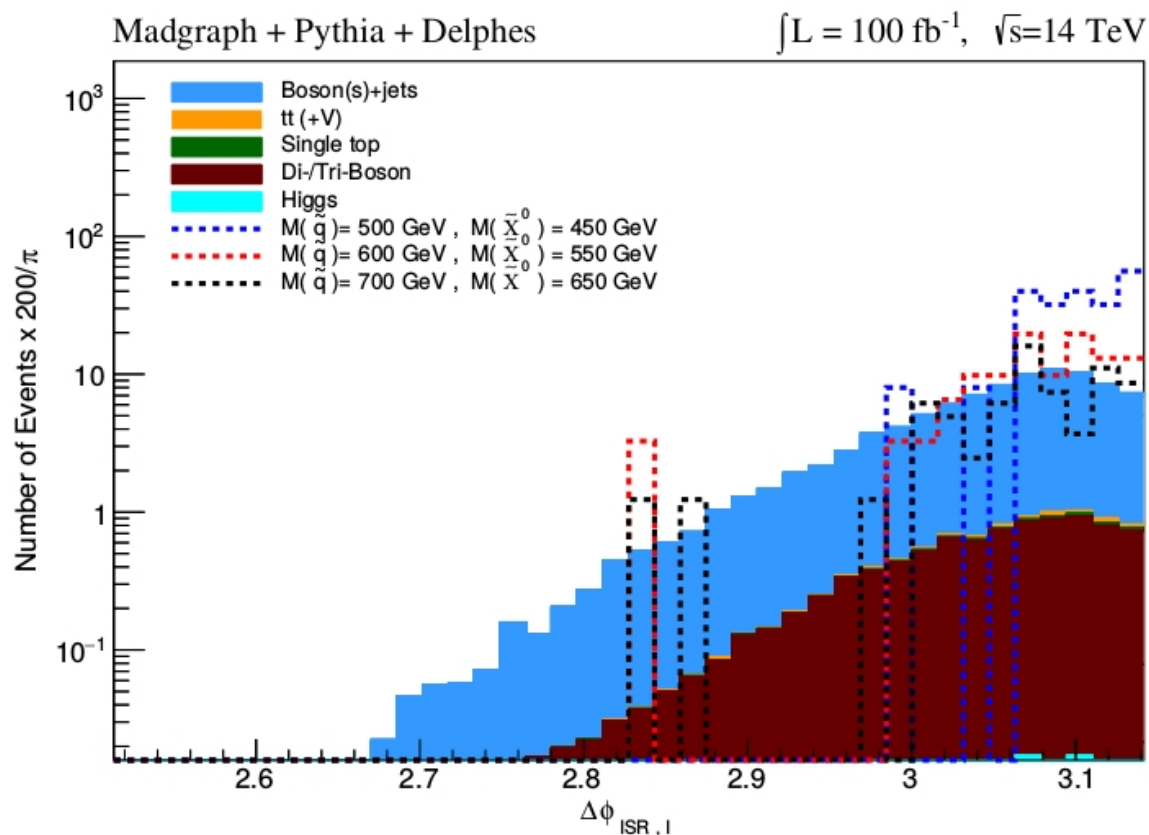
More discrimination from the angular variable

$$\Delta\phi_{ISR, I}$$

N-1 distribution.

Although both signal and background distributions tend towards  $\pi$  the signal has a much stronger tendency to do so.

Good for optimisation





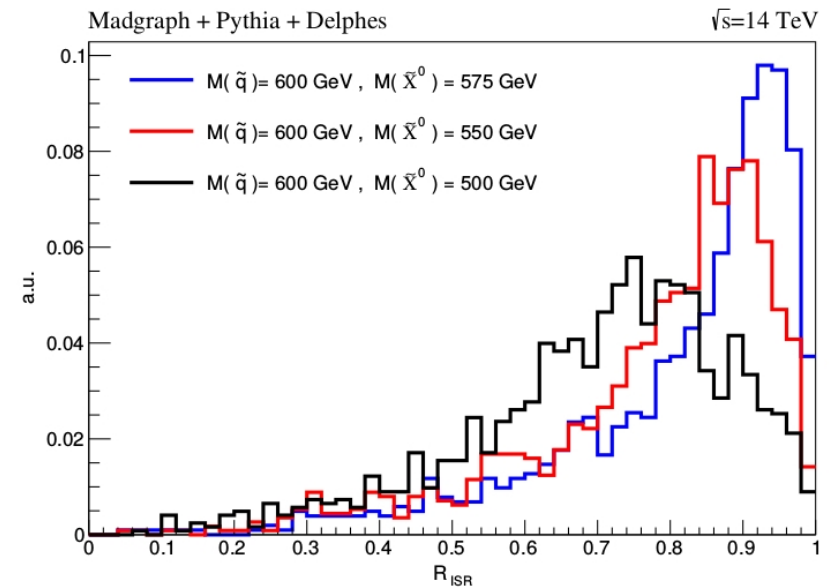
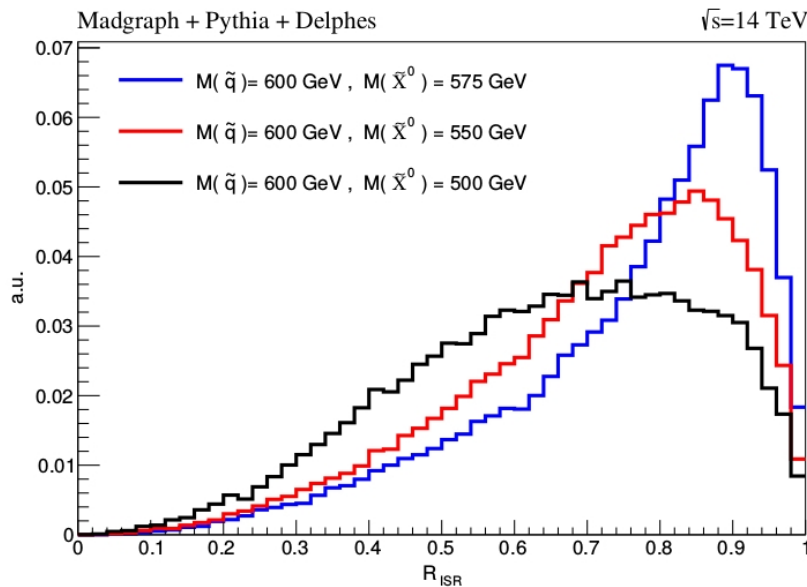
# Backup slides: sparticles in motion

- In the limit of soft momentum of the LSPs in the sparents frame:

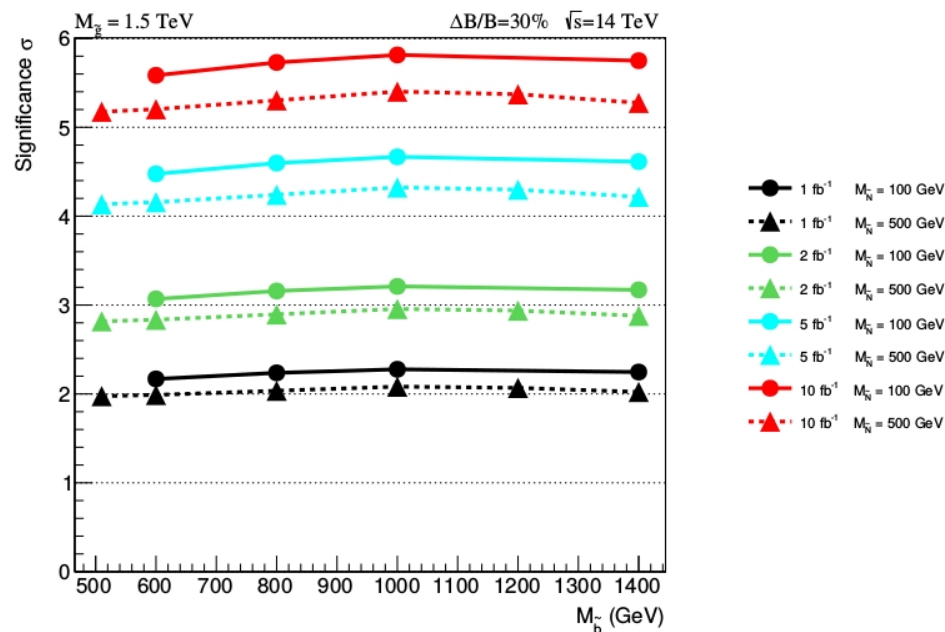
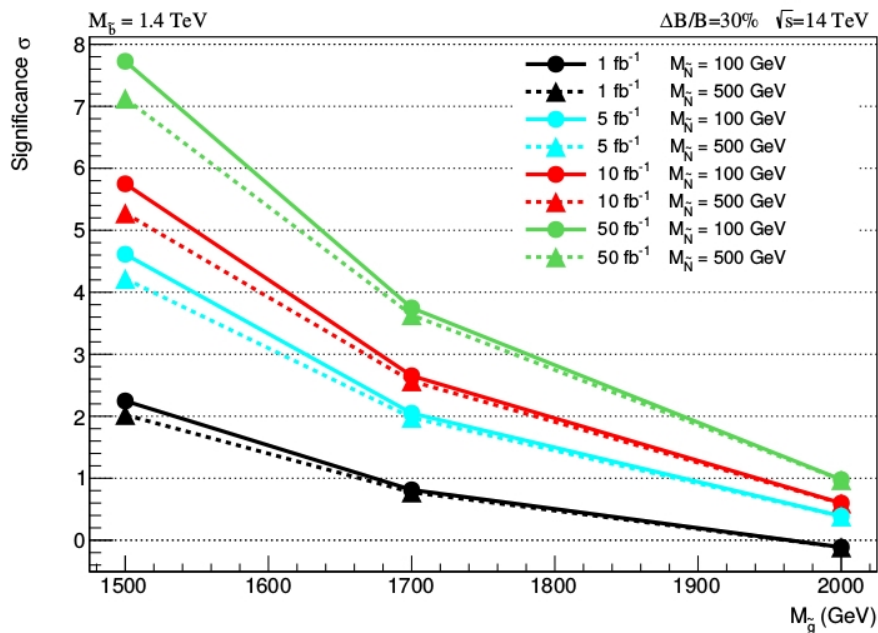
$$R_{\text{ISR}} \sim |\cancel{E}_T \cdot \hat{p}_{\text{ISR},T}| / p_{\text{ISR},T} \sim \frac{m_{\tilde{\chi}_1^0}}{m_{\tilde{P}}} \left[ 1 + \mathcal{O} \left( \frac{p_{\tilde{\chi}_1^0}^{\tilde{P}}}{2m_{\tilde{P}}} \right) \left( \frac{\sqrt{p_{\text{ISR},T}^2 + m_{\tilde{P}\tilde{P}}^2}}{p_{\text{ISR},T}} \right) \sin \Omega \right]$$

- R scales nicely with the mass ratio. Better after some PTISR requirement

- First term 
$$\vec{p}_{1\chi}^{\text{Lab}} + \vec{p}_{2\chi}^{\text{Lab}} \sim \frac{M_\chi}{M_{\tilde{P}}} \vec{p}_{1\tilde{P}}^{\text{Lab}} + \frac{M_\chi}{M_{\tilde{P}}} \vec{p}_{2\tilde{P}}^{\text{Lab}}$$



# Backup slides: preliminary $\sim gg \rightarrow \sim bb$



Sensitivity decreases with gluino-production cross section as expected

- But it's pretty independent of LSP mass (till to the compressed regime)
- And very independent of sbottom mass (also off-shell sbottoms)
- Cutting hard on e.g. jet  $p_T$ s or MET would have killed sensitivity for small mass splittings
- Preliminary, after 5  $\text{fb}^{-1}$  of LHC14,  $>4\sigma$  sensitivity to a 1.5 TeV gluino for low gluino-sbottom and sbottom-LSP mass splittings (30% systematics)

Next  $\rightarrow$  optimization for  $m(\tilde{g})$  1.9- 2 TeV and large  $m(\text{LSP})$