

BESIII



Overview on QCD studies at BESIII

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Outline

- The BESIII experiment
- Baryon structure, form factor measurement
- Hadron spectroscopy
- Precision test on Standard Model, $(g - 2)_\mu$
- Lineshape of J/ψ resonance
- Summary

Beijing Electron Positron Collider

E_{beam} : 1.0-2.3 GeV

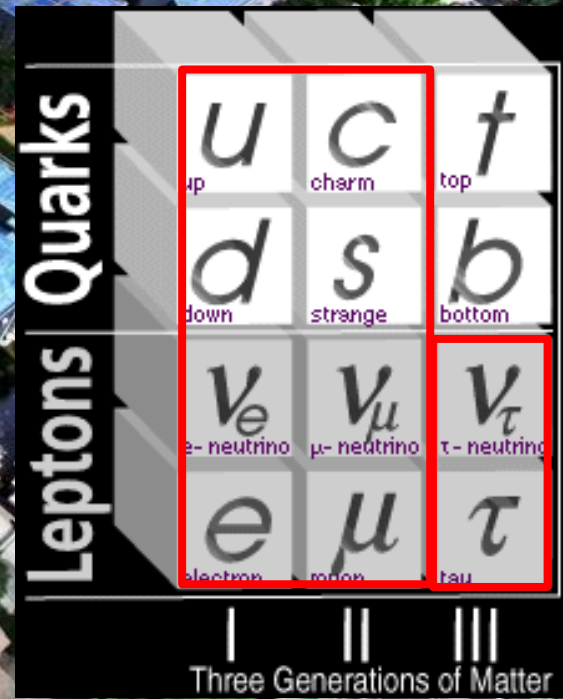
σ_E : 5.16×10^{-4}

L: $1.0 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$ @3770

Linac

BES

Storage ring



BEijing Spectrometer III

Main Drift Chamber

Small cell, 43 layer

$\sigma_{xy} = 130 \mu\text{m}$, $dE/dx \sim 6\%$

$\sigma_p/p = 0.5\%$ at 1 GeV

Muon Counter

Resistive plate chamber

Barrel: 9 layers

Endcaps: 8 layers

$\sigma_{\text{spatial}} = 1.48 \text{ cm}$

Time Of Flight

Plastic scintillator

$\sigma_T(\text{barrel}) = 80 \text{ ps}$

$\sigma_T(\text{endcap}) = 110 \text{ ps}$

Electromagnetic Calorimeter

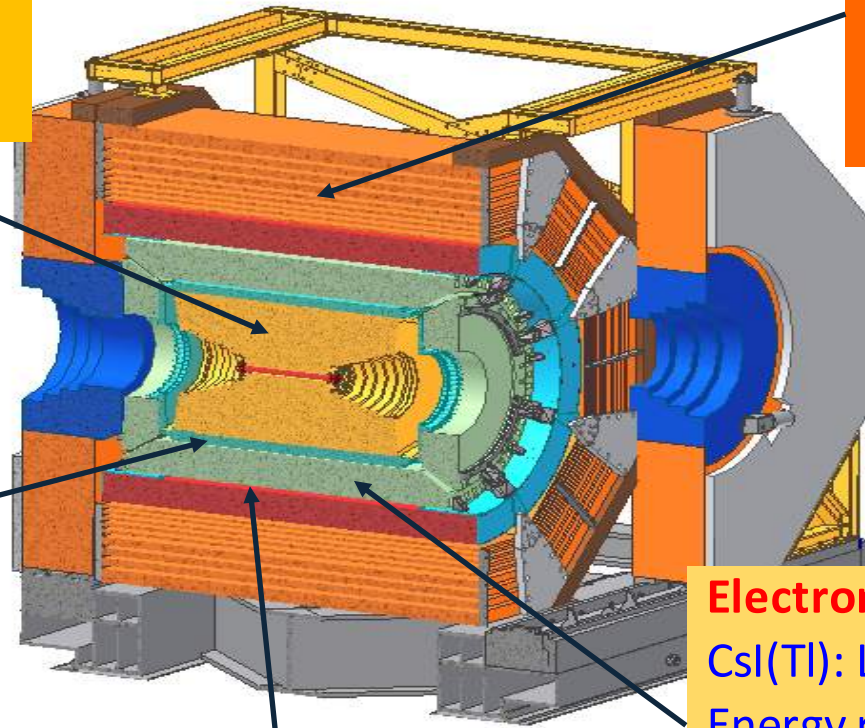
CsI(Tl): $L = 28 \text{ cm}$ ($15X_0$)

Energy range: 0.02-2 GeV

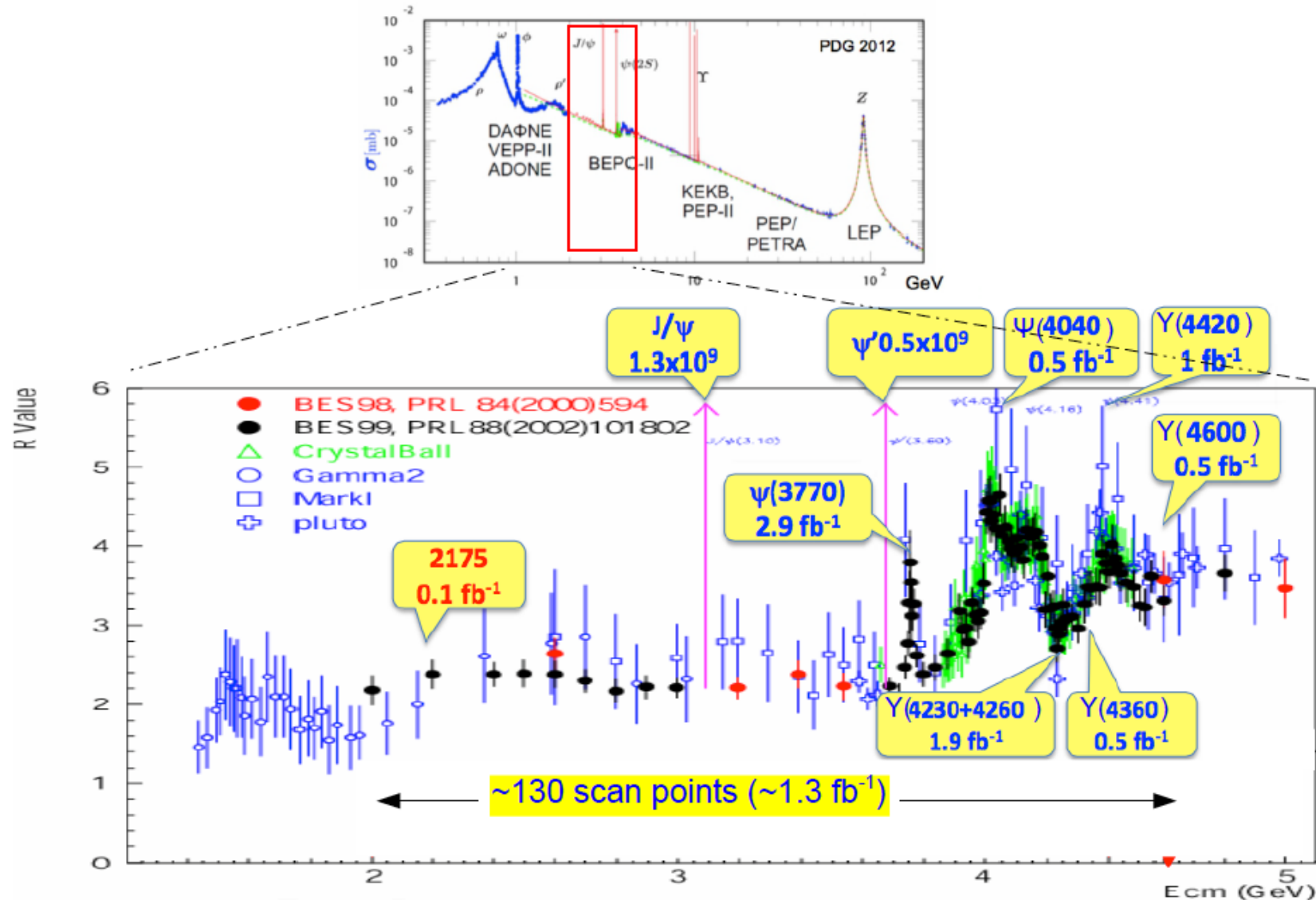
Barrel $\sigma_E = 2.5\%$, $\sigma_l = 6 \text{ mm}$

Endcap $\sigma_E = 5.0\%$, $\sigma_l = 9 \text{ mm}$

SC Magnet 1.0T

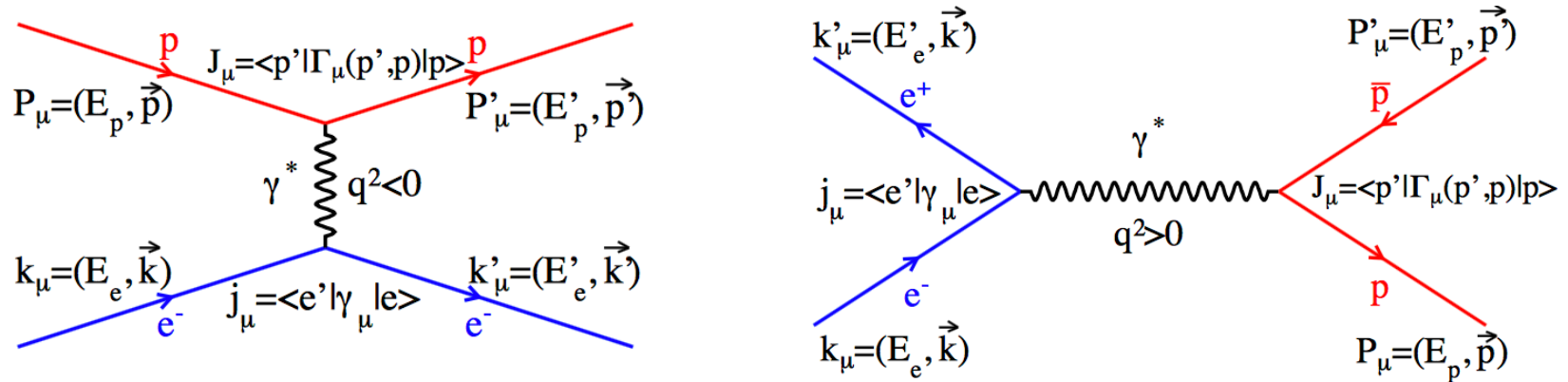


The BESIII data sample



Baryon form factor

- The FFs are measured in space-like (SL) region or time-like (TL) region. The proton electromagnetic vertex Γ_μ describing the hadron current



- $\Gamma_\mu(p', p) = \gamma_\mu F_1(q^2) + \frac{i\sigma_{\mu\nu}q^\nu}{2m_p} F_2(q^2)$
- $G_E(q^2) = F_1(q^2) + \tau \kappa_p F_2(q^2)$
- $G_M(q^2) = F_1(q^2) + \kappa_p F_2(q^2)$
- $\tau = \frac{q^2}{4m_p^2}, \quad \kappa_p = \frac{g_p - 2}{2} = \mu_p - 1$
- At $q^2=0$,
 proton: $F_1=F_2=1, G_E=1, G_M=\mu_p$
 neutron: $F_1=0, F_2=1, G_E=1, G_M=\mu_n$

- G_E and G_M can be interpreted as Fourier transforms of **spatial distributions of charge and magnetization** of nucleon in the **Breit frame**

$$\text{i.e. } \rho(\vec{r}) = \int \frac{d^3q}{2\pi^3} e^{-i\vec{q}\cdot\vec{r}} \frac{M}{E(\vec{q})} G_E(\vec{q}^2)$$

Baryon form factor

- The Born cross section for $e^+ e^- \rightarrow \gamma^* \rightarrow B\bar{B}$, can be expressed in terms of electromagnetic form factor G_E and G_M :

$$\sigma_{B\bar{B}}(q) = \frac{4\pi\alpha^2 C\beta}{3q^2} [|G_M(q)|^2 + \frac{1}{2\tau} |G_E(q)|^2]$$

- The Coulomb factor $C = \begin{cases} \frac{\pi\alpha}{\beta} \frac{1}{1 - \exp(-\frac{\pi\alpha}{\beta})} & \text{for a charged } B\bar{B} \text{ pair} \\ 1 & \text{for a neutral } B\bar{B} \text{ pair} \end{cases}$

	Energy Scan	Initial State Radiation
E_{beam}	discrete	fixed
\mathcal{L}	low at each beam energy	high at one beam energy
σ	$\frac{d\sigma_{p\bar{p}}}{d(\cos\theta)} = \frac{\pi\alpha^2\beta C}{2q^2} [G_M ^2(1 + \cos^2\theta) + \frac{4m_p^2}{q^2} G_E ^2 \sin^2\theta]$	$\frac{d^2\sigma_{p\bar{p}\gamma}}{dq^2 d\theta_\gamma} = \frac{1}{s} W(s, x, \theta_\gamma) \sigma_{p\bar{p}}(q^2)$ $W(s, x, \theta_\gamma) = \frac{\alpha}{\pi x} \left(\frac{2-2x+x^2}{\sin^2\theta_\gamma} - \frac{x^2}{2} \right)$
q^2	single at each beam energy	from threshold to s

Both techniques, energy scan and initial state radiation, can be used at BESIII

$$\sim \frac{1}{400}$$

$e^+ e^- \rightarrow p \bar{p}$

Phys.Rev.D 91, 112004(2015)

■ Using 12 c.m. energies from 2.2324 to 3.671 GeV, total luminosity 156.9 pb^{-1}

■ Cross section

$$\sigma_{\text{Born}} = \frac{N_{\text{obs}} - N_{\text{bkg}}}{L \cdot \epsilon \cdot (1 + \delta)}$$

■ Effective FF

$$\sigma = \frac{4\pi\alpha^2\beta C}{3q^2} (|G_M|^2 + \frac{1}{2\tau} |G_E|^2)$$

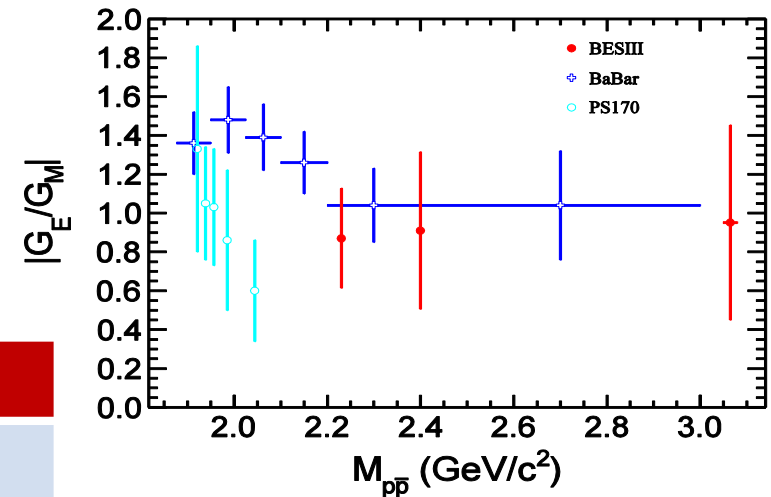
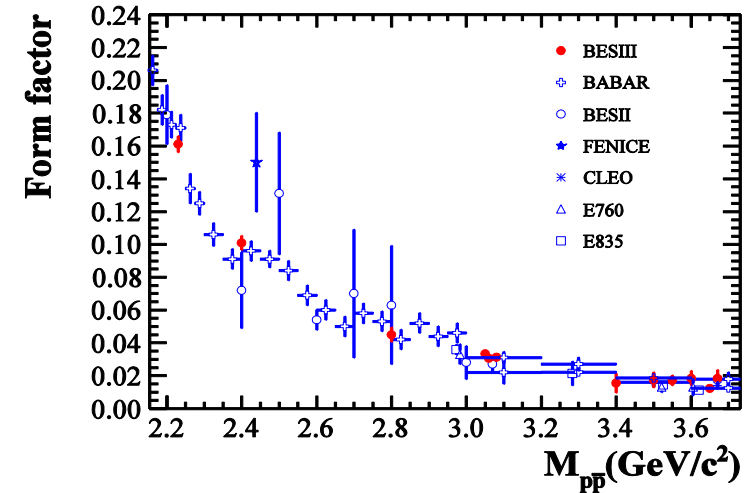
$$G_{\text{eff}} = \sqrt{\frac{3q^2}{4\pi\alpha^2\beta C} \cdot \frac{\sigma}{1 + 1/2\tau}}$$

■ Ratio extraction

➤ Fit function:

$$\frac{dN}{d\cos\theta_p} = N_{\text{norm}} \left[(1 + \cos^2\theta_p) + R_{\text{em}}^2 \frac{1}{\tau} \sin^2\theta_p \right]$$

	$\delta R_{\text{em}}/R_{\text{em}}$	$\delta G_{\text{eff}}/G_{\text{eff}}$
Stat. with Sys.	25% - 50%	3% - 37%



$e^+ e^- \rightarrow \gamma_{ISR} p \bar{p}$

■ Combination of 7 data sets (≥ 3.773 GeV), total luminosity 7.4 fb^{-1} .

■ Event selection:

- Two charged tracks from vertex
- One high energy shower in EMC (ISR-tagged)
- Kinematic constraints applied
- Background subtraction from weighted MC

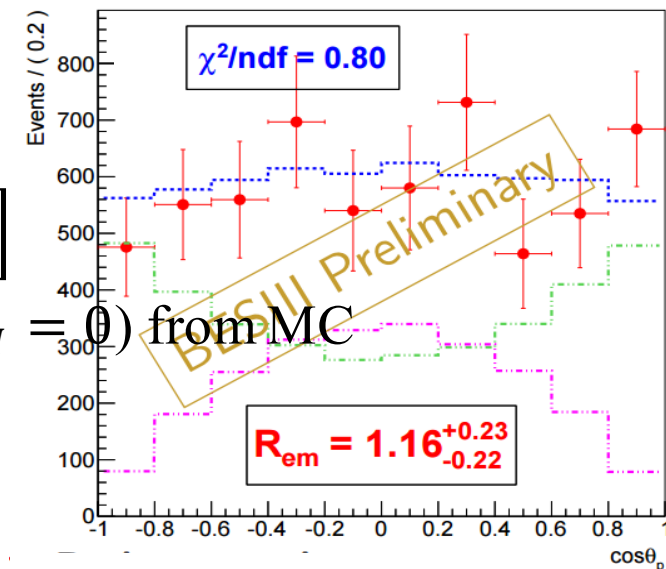
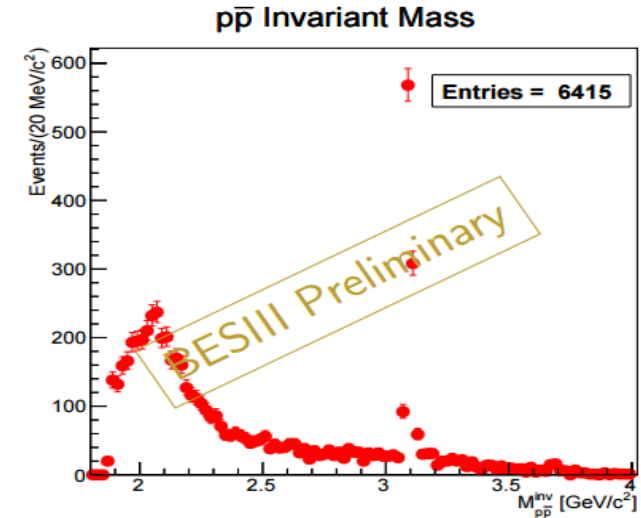
■ Cross section

$$\text{➤ } \sigma_{p\bar{p}}^{\text{Born}}(M_{p\bar{p}}) = \frac{(dN/dM_{p\bar{p}})_{\text{corr}}}{dL/dM_{p\bar{p}}}$$

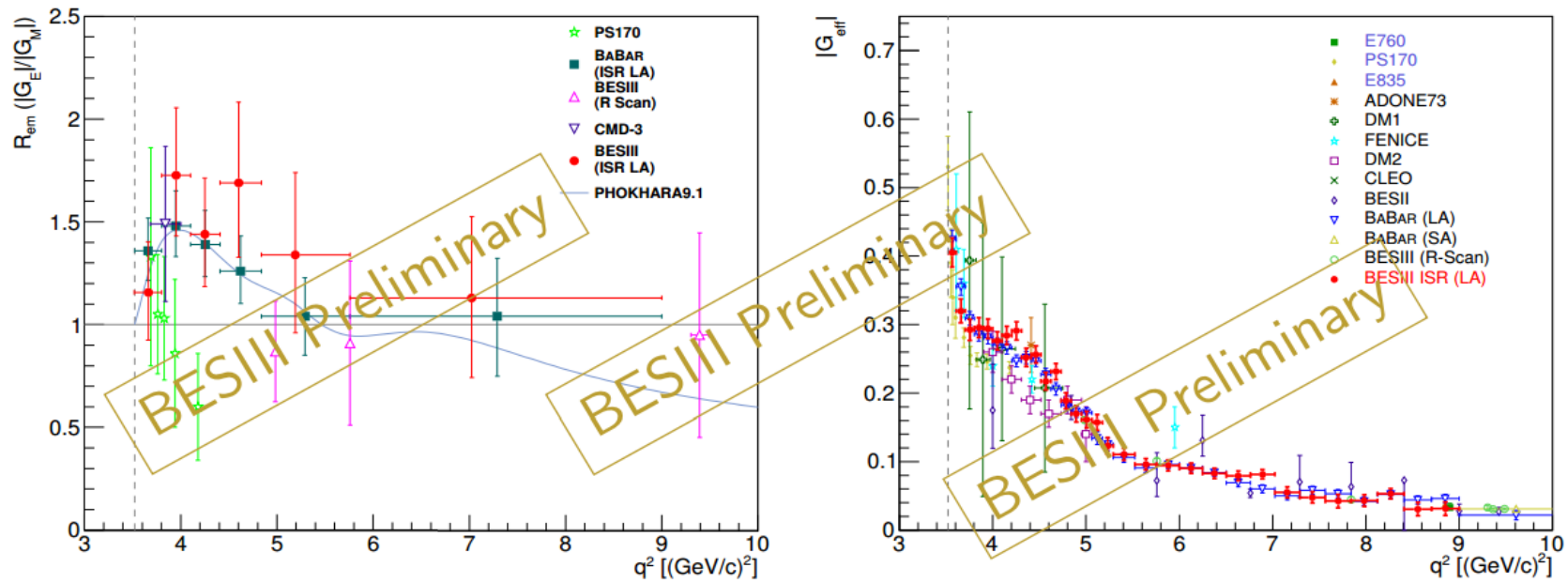
■ Ratio extraction

$$\text{➤ } \frac{d\sigma}{d\cos\theta} = A \left[H_M(\cos\theta, q^2) + \frac{R_{em}^2}{\langle\tau\rangle} H_E(\cos\theta, q^2) \right]$$

➤ $H_M(\cos\theta, q^2)$ ($G_E = 0$) and $H_E(\cos\theta, q^2)$ ($G_M = 0$) from MC



$$e^+ e^- \rightarrow \gamma_{ISR} p \bar{p}$$



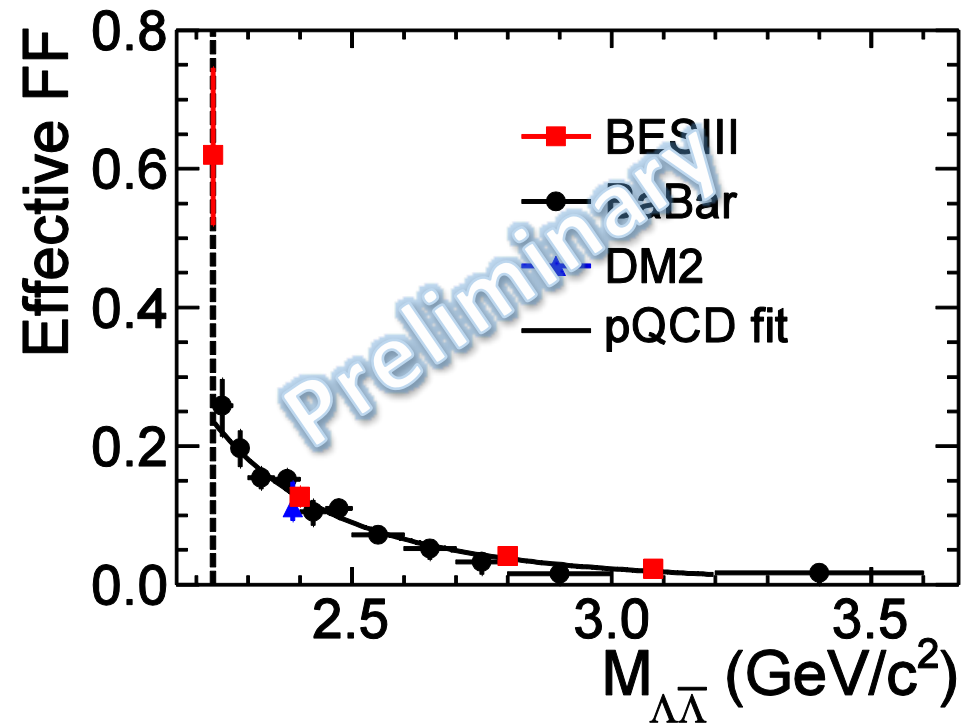
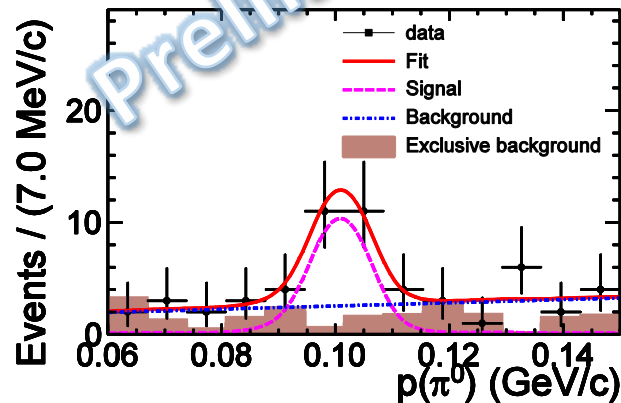
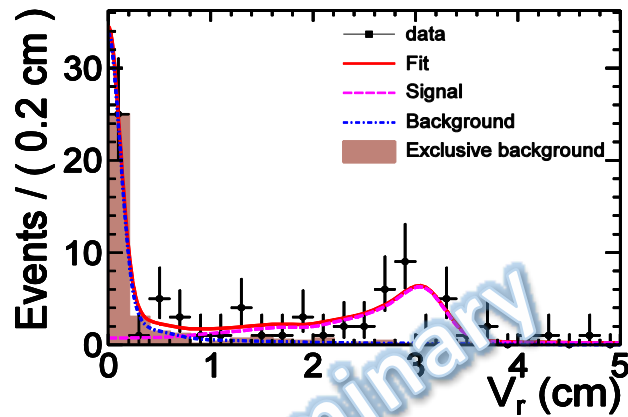
- Background subtraction and efficiency dividing
- The proton FFs extracted between threshold to 3.0 GeV

	$\delta R_{em}/R_{em}$	$\delta G_{eff}/G_{eff}$
Stat.	18.5 – 33.6%	4.1 - 31.6%
Syst.	4.2- 15.6%	1.6 - 12%

$$e^+ e^- \rightarrow \Lambda \bar{\Lambda}$$

■ Using 4 c.m. energies from 2.2324 to 3.08 GeV, total luminosity 40.5 pb^{-1}

■ $e^+ e^- \rightarrow \Lambda \bar{\Lambda}$ at the first energy point, 2.2324 GeV, which is 1.0 MeV above the $\Lambda \bar{\Lambda}$ mass threshold, is reconstructed final final states of $p\bar{p}\pi^+\pi^-$ and $\bar{n}\pi^0 + X$. The Born cross section is measured to be $305 \pm 45^{+66}_{-36} \text{ pb}$



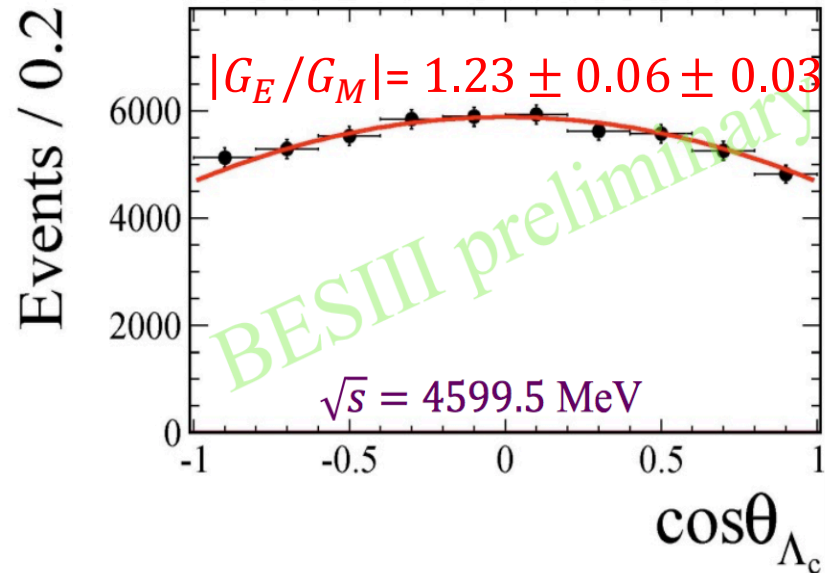
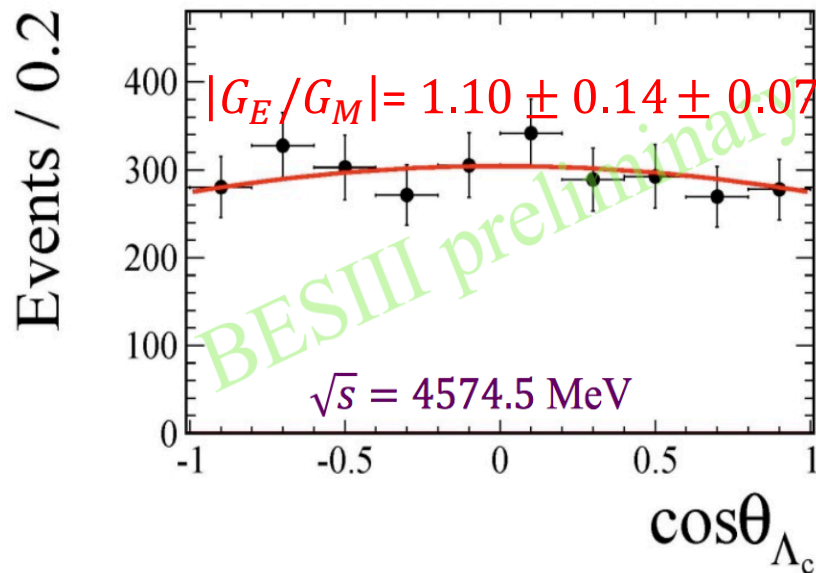
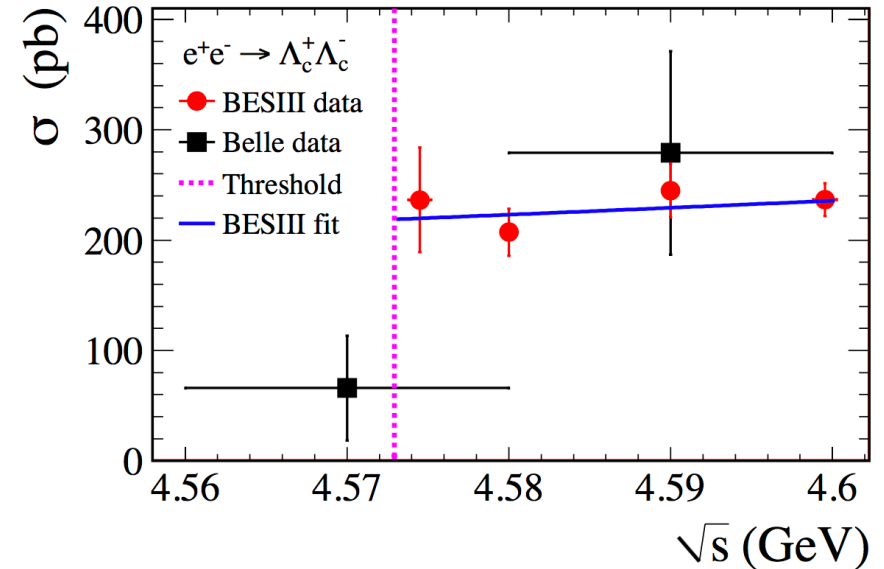
$$e^+ e^- \rightarrow \Lambda_c^+ \bar{\Lambda}_c^-$$

■ Using 4 c.m. energies, 4.575, 4.580, 4.590 and 4.600 GeV, total luminosity

631.3 pb^{-1}

■ $e^+ e^- \rightarrow \Lambda_c^+ \bar{\Lambda}_c^-$ is reconstructed by tagging 10 decay modes of Λ_c^+

■ Angular distribution of Λ_c^+ is studied at 4.575 and 4.600 GeV.



Hadron spectroscopy

➤ Cross section of $e^+e^- \rightarrow K^+K^-$ in BaBar

➤ Possible resonance near 2.2 GeV: $\rho(2150)$, $\phi(2170)/Y(2175)$, ...

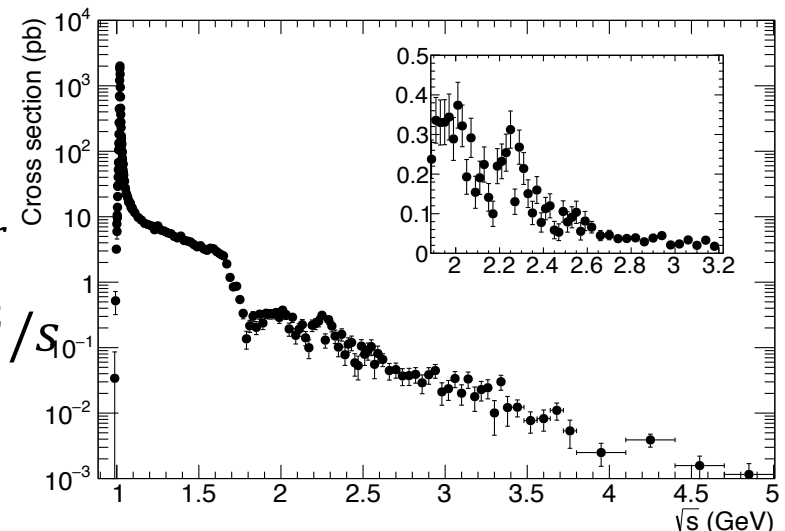
Y(2175)	As $2\ ^3D_1\ s\bar{s}$ quarkonium	As $s\bar{s}g$ hybrid	As $3\ ^3S_1\ s\bar{s}$ quarkonium
	Γ_{LJ} in 3P_0 model	Γ_{LJ} in Flux Tube Model	in Flux Tube Model
$\Gamma_{KK}(\text{MeV})$	9.8	23.1	0
$\Gamma_{\text{tot}}(\text{MeV})$	167.21	211.9	148.7
			in 3P_0 model
			378

[PLB 657 \(2007\) 49](#)

➤ Form factor of kaon

➤ Charge distribution: $F(q^2) = \int d^3r \rho(r) e^{iq \cdot r}$

➤ Check pQCD predictions: $F_K = 16\pi\alpha_s(s)f_K^2/s_0^{-1}$



$e^+ e^- \rightarrow K^+ K^-$

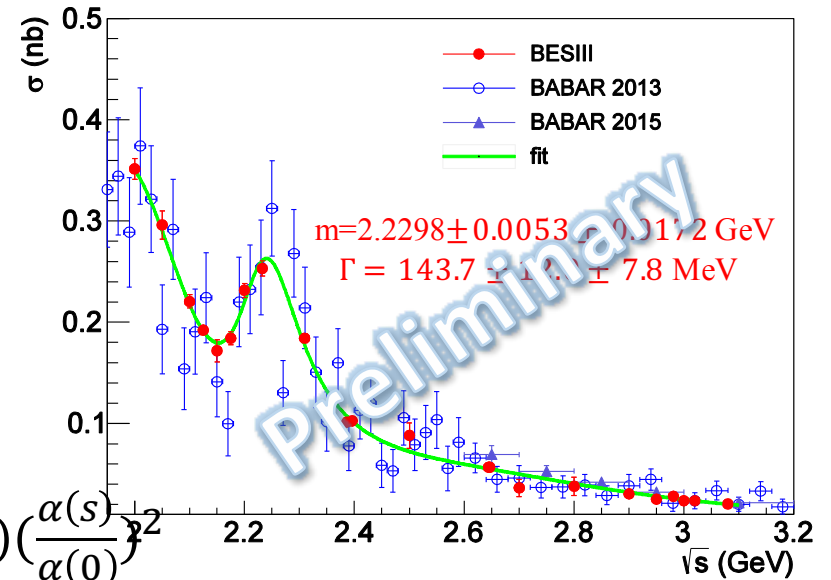
■ R scan data from 2.0 to 3.08 GeV, total luminosity $\sim 651 \text{ pb}^{-1}$

■ A structure near 2.2 GeV is measured by:

$$\sigma = |A_K|^2,$$

$$A_K = \sum_r c_r \cdot BW_r + c_{con} \cdot s^{-\alpha} \cdot e^{i\theta}$$

r : ρ , ω , ϕ and their excited states



■ Form factor extraction:

$$|F_K|^2(s) = \frac{3s}{\pi\alpha(0)^2\beta^3} \frac{\sigma_{KK}(s)}{C_{FS}}; \quad \sigma_{KK}(s) = \sigma_{KK}^0(s) \left(\frac{\alpha(s)}{\alpha(0)} \right)^2$$

$\sigma_{KK}(s)$: dressed cross section; $\sigma_{KK}^0(s)$: bare cross section

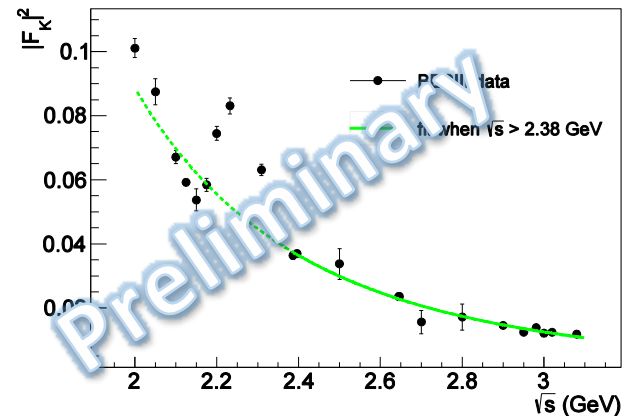
C_{FS} : final-state correction

■ Form factor fitting function:

$$|F_K|^2 = A\alpha_s^2(s)/s^n$$

$$n = 1.94 \pm 0.09$$

(agreement with pQCD prediction $n = 2$)



Precision tests of the Standard Model

■ The anomalous magnetic moment $\alpha_\mu = \frac{g_\mu - 2}{2}$

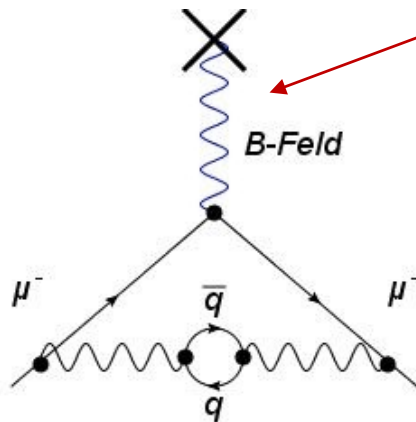
➤ Experimental measurement: $\alpha_\mu^{exp} = (11659208.9 \pm 6.3) \cdot 10^{-10}$ [PRD 73, 072\(2006\)](#)

➤ Theoretical prediction: $\alpha_\mu^{SM} = (11659580.2 \pm 4.9) \cdot 10^{-10}$ [Eur. Phys. J. C71, 1515\(2011\)](#)

=> discrepancy: 3.6 standard deviations

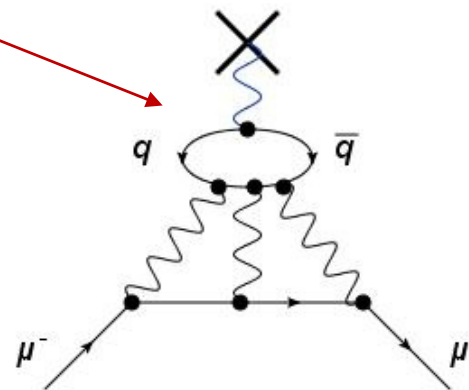
■ $\alpha_\mu^{SM} = \alpha_\mu^{QED} + \alpha_\mu^{weak} + \alpha_\mu^{hadr}$

can not be calculated by means of perturbative calculations



Hadronic vacuum polarization

$$\alpha_\mu^{hadr,VP} = (692.2 \pm 4.2) \cdot 10^{-10}$$



Hadronic light-by-light scattering

$$\alpha_\mu^{hadr,LBL} = (10.5 \pm 2.6) \cdot 10^{-10}$$

Precision tests of the Standard Model

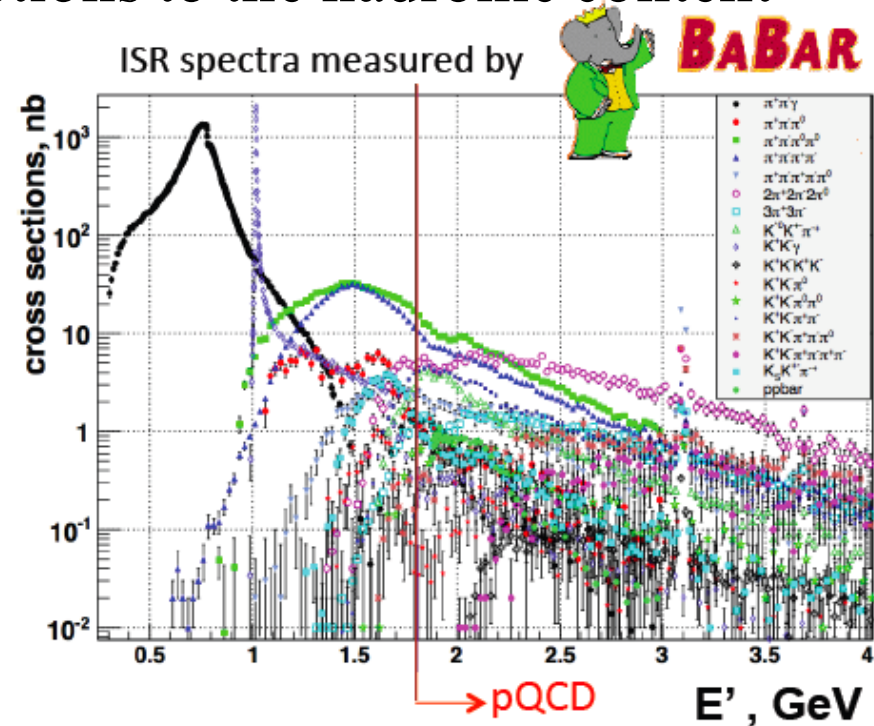
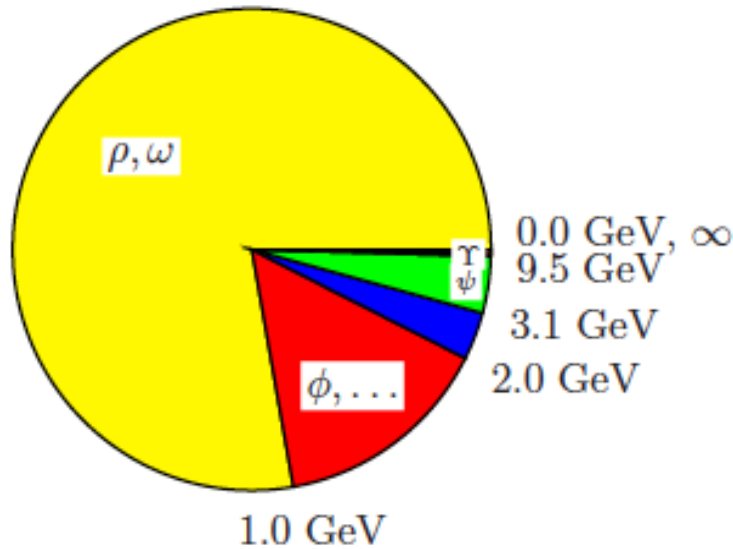
■ Hadronic vacuum polarization

$$\alpha_{\mu}^{had,LO} = \frac{\alpha^2(0)}{3\pi^2} \int_{4m_{\pi}^2}^{\infty} ds \frac{K(s)}{s} R(s)$$

$$R(s) = \frac{\sigma(e^+e^- \rightarrow \text{hadrons})}{\sigma(e^+e^- \rightarrow \mu^+\mu^-)}$$

■ Contributions of hadronic cross sections to the hadronic content

α_{μ}^{hadr}



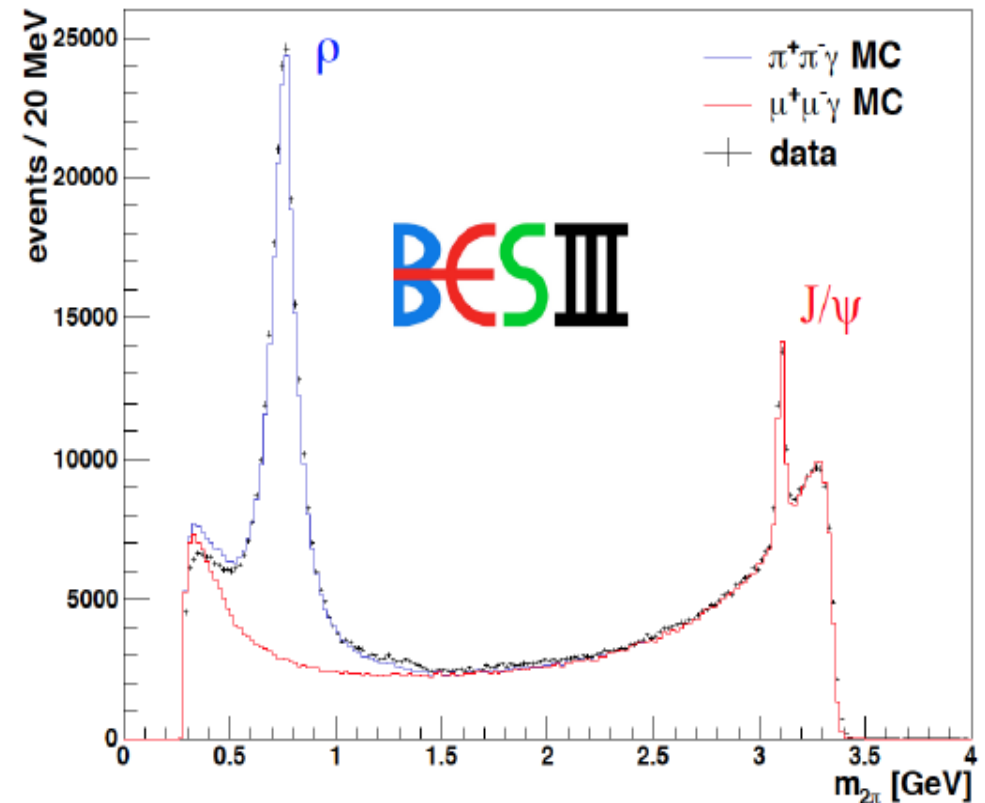
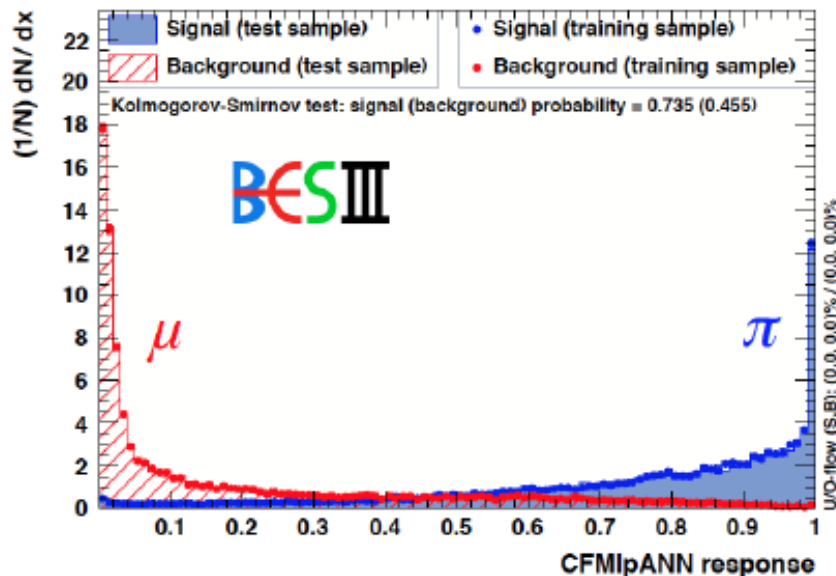
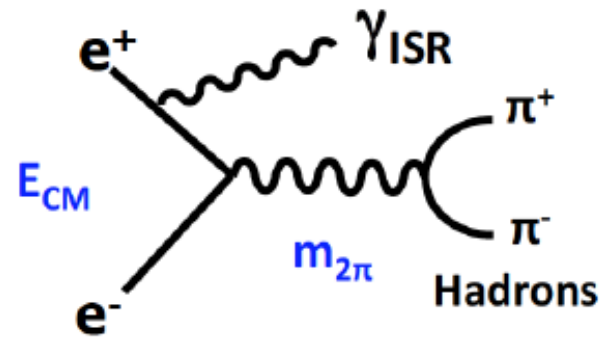
■ The largest contribution is below 1 GeV ($e^+e^- \rightarrow \pi^+\pi^-$)

■ $e^+e^- \rightarrow \pi^+\pi^-\pi^0$ contribution $> 6\%$

$$e^+ e^- \rightarrow \gamma_{ISR} \pi^+ \pi^-$$

Phys. Lett. B 753(2016) 629-631

- Data: 2.9 fb^{-1} @ 3.773 GeV
- Detected ISR photon
- MC produced with Phokhara
- Main background: $\mu^+ \mu^- \gamma$
 - TMVA method (Neutral Network)
- Systematic uncertainty: 0.9%



$$e^+ e^- \rightarrow \gamma_{ISR} \pi^+ \pi^-$$

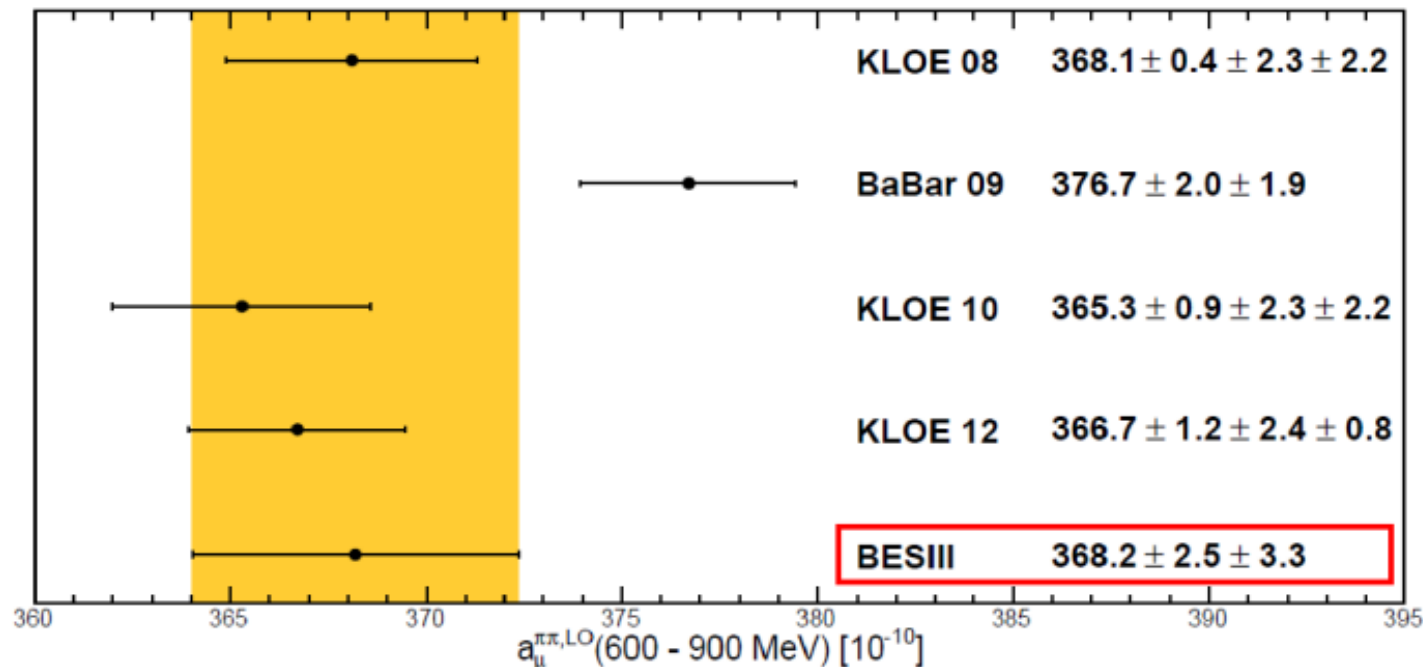
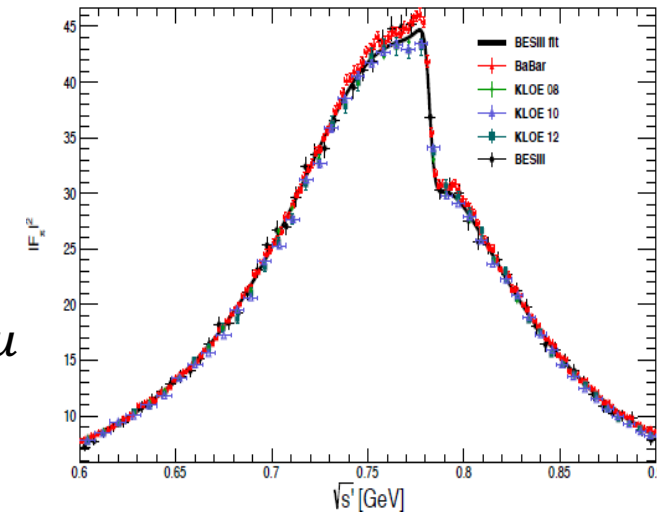
Phy. Lett. B 753(2016) 629-634

■ Cross section: $\sigma_{\pi\pi(\gamma_{FSR})}^{\text{bare}} = \frac{N_{\pi\pi\gamma} \cdot (1 + \delta_{FSR}^{\pi\pi})}{L \cdot \epsilon_{\text{global}} \cdot H(s) \cdot \delta_{\text{vac}}}$

■ Form factor: $|F_\pi|^2 = \frac{3s}{\pi\alpha^2\beta^3} \sigma_{\pi\pi}^{\text{dressed}}$

■ Contribution to the hadronic contribution of α_μ

➤ $\alpha_\mu^{\pi\pi, LO}(0.6 - 0.9 \text{ GeV}) = \frac{1}{4\pi^3} \int_{0.6}^{0.9} ds K(s) \sigma_{\pi\pi}^{\text{bare}}$



$e^+e^- \rightarrow \gamma_{ISR} \pi^+ \pi^- \pi^0$

■ Data: 2.9 fb^{-1} @ 3.773 GeV

■ ISR tagged:

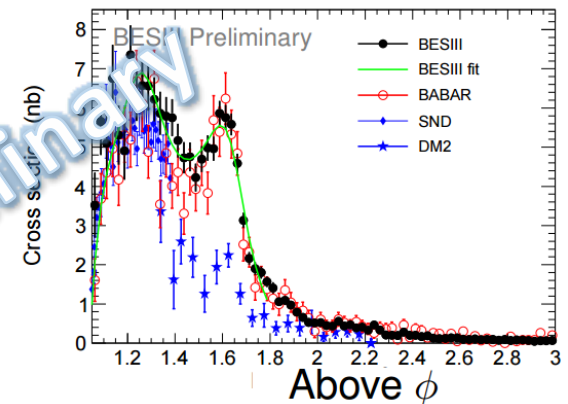
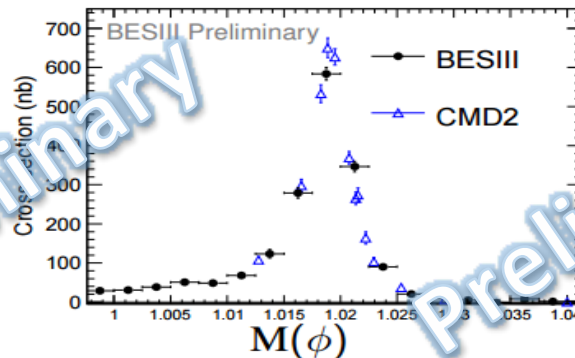
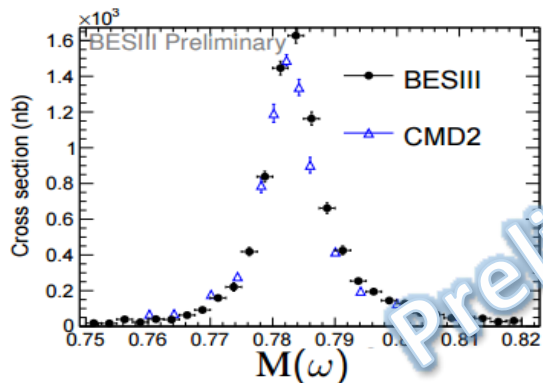
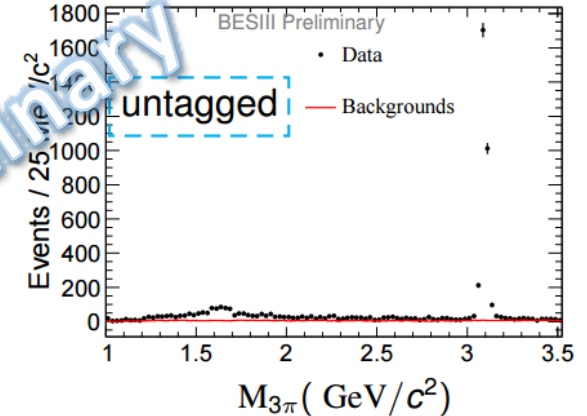
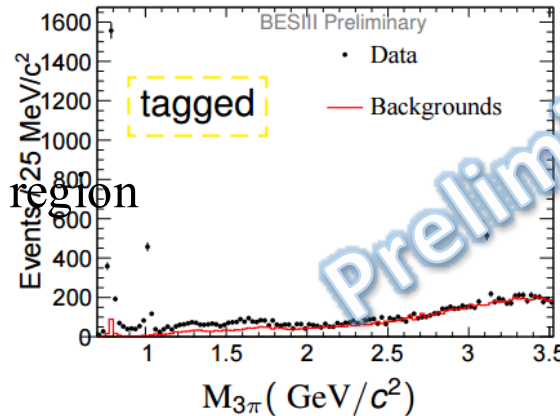
- Clear ω and ϕ signals
- Huge background in high mass region

■ ISR untagged

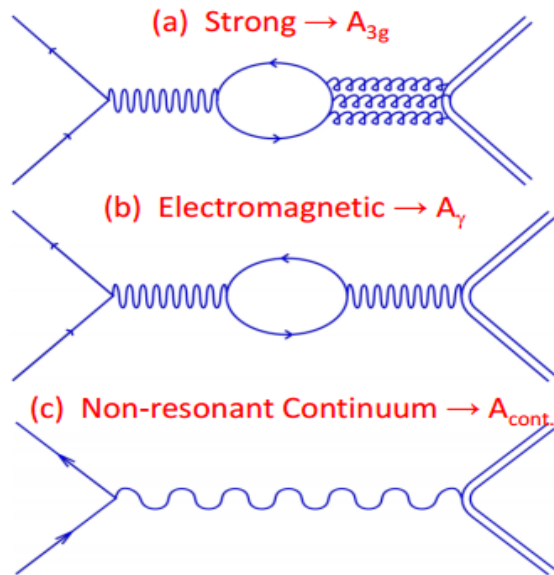
- Limited by acceptance
- Negligible background

■ Below 1.8 GeV , fit with VMD model

- $$\sigma(m) = \frac{12\pi}{m^3} F_{\rho\pi}(m) \left| \sum_{V=\omega, \phi, \omega', \omega''} \frac{\Gamma_V m_V^{3/2} \sqrt{B(V \rightarrow e^+e^-)B(V \rightarrow 3\pi)}}{D_V(m)} \frac{e^{i\phi_V}}{\sqrt{F_{\rho\pi}(m_V)}} \right|^2$$
- Branching fraction for $\omega, \phi, \omega', \omega''$ consistent with PDG



Lineshape of J/ψ resonance



- (a) $e^+e^- \rightarrow J/\psi \rightarrow$ hadrons via strong mechanism;
 (b) $e^+e^- \rightarrow J/\psi \rightarrow$ hadrons via EM mechanism;
 (c) non-resonant $e^+e^- \rightarrow$ hadrons via a virtual photon.

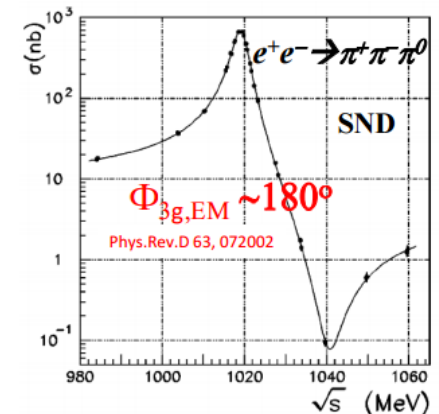
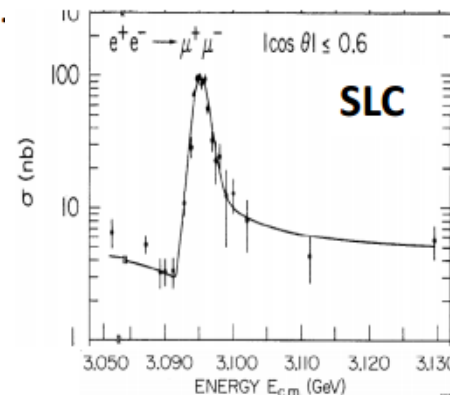
$$\sigma_{\text{Born}} = |A_{3g} + A_{\gamma} + A_{\text{cont}}|^2$$

$$= \left| |A_{3g}| e^{i\Phi_{3g,EM}} + |A_{\gamma}| e^{i\Phi_{\gamma,cont.}} + |A_{\text{cont.}}| \right|^2$$

- [1] M. Suzuki et al., Phys. Rev. D60, 051501 (1999).
 [2] M. Suzuki et al. Phys. Rev. D63, 054021 (2001).
 [3] M. Ablikim et al. (BESIII), Phys. Rev. D86, 032014 (2012).
 [4] K. Zhu et al., Int. J Mod. Phys. A30, 1550148 (2015).

Model dependent experimental evidences:

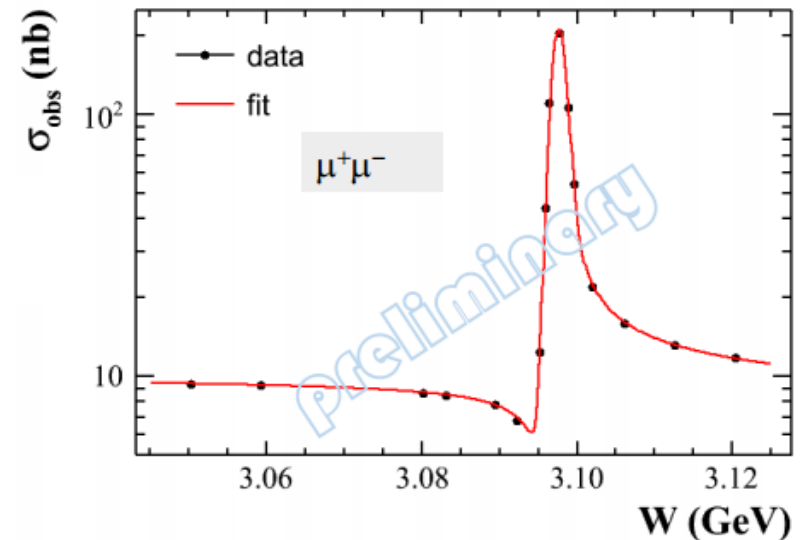
- SU3 and SU3 breaking in $1^-0^-^{[1]}$, $0^-0^-^{[1]}$, $1^-1^-^{[1]}$, $1^+0^-^{[2]}$ decay show the phase between A_{3g} and A_{EM} is $\Phi_{3g,EM} \sim 90^\circ$
- If $A(e^+e^- \rightarrow n\bar{n}) \sim -A(e^+e^- \rightarrow p\bar{p})$, $\frac{B(n\bar{n})}{B(p\bar{p})} = 0.98 \pm 0.08 \rightarrow \Phi_{3g,EM} \sim 89^\circ \pm 8^\circ$ ^[3]
- Other baryon pairs:
 $\Phi_{3g,EM} \sim -85.9^\circ \pm 1.7^\circ$ or $90.8^\circ \pm 1.6^\circ$ ^[4]
- The phase angle between A_{EM} and A_{cont} :
 $\Phi_{\gamma,cont.} = 0^\circ$ from $e^+e^- \rightarrow \mu^+\mu^-$
- The interference between φ and ω was observed at SND, $\Phi_{3g,EM} \sim 180^\circ$



$$e^+ e^- \rightarrow \mu^+ \mu^-$$

- Data at 16 energy points around J/ψ peak, integrated luminosity $\sim 100.5 \text{ pb}^{-1}$
- Observed cross section: $\sigma_i = \frac{N_i}{\epsilon_i L_i (B)}$
- Theoretically prediction of Born cross section: $\sigma^0(W) = \frac{4\pi\alpha^2}{W^2} \left| 1 + \frac{3W^2 \sqrt{\Gamma_{ee}\Gamma_{\mu\mu}} e^{i\gamma, \text{cont}}}{\alpha M (W^2 - M^2 + iM\Gamma)} \right|^2$
- Considering ISR : $\sigma'(W) = \int_0^{1-(\frac{W_m}{W})^2} dx F(x, W) \sigma^0(W)$
- Considering energy spread S_E : $\sigma''(W) = \int_{W-nS_E}^{W+nS_E} \frac{1}{\sqrt{2\pi}S_E} \exp\left(-\frac{W'-W}{2S_E^2}\right) \sigma'(W') dW'$
- Minimization method: $\chi^2 = \sum_{i=1}^{16} \frac{[\sigma^{\text{obs}}(W_i) - \sigma''(W_i)]^2}{(\Delta\sigma^{\text{obs}}W_i)^2 + \left[\Delta W_i \cdot \frac{d\sigma''}{dW}(W_i)\right]^2}$

$\Phi_{\gamma, \text{cont.}} = (-5 \pm 9.7)^\circ$, consistent with zero
 Energy spread: $S_E = (0.911 \pm 0.026) \text{ MeV}$
 Energy shift: $\Delta M = (0.548 \pm 0.041) \text{ MeV}$



$e^+ e^- \rightarrow \pi^+ \pi^- \pi^+ \pi^- \pi^0$

■ For $\pi^+ \pi^- \pi^+ \pi^- \pi^0$ process: $\sigma^0(W) = \left(\frac{A}{W^2}\right)^2 \frac{4\pi\alpha^2}{W^2} \left| 1 + \frac{3W^2 \sqrt{\Gamma_{ee}\Gamma_{\mu\mu}} (1 + Ce^{i\Phi_{3g,EM}})}{\alpha M(W^2 - M^2 + iM\Gamma)} \right|^2$

➤ $\Phi_{3g,EM} = 83.4^\circ \pm 4.3^\circ$ or $-83.5^\circ \pm 4.2^\circ$

➤ $\Gamma_{5\pi} = \left(\frac{A}{W^2}\right)^2 \Gamma_{\mu\mu} |1 + Ce^{i\Phi_{3g,EM}}|^2$

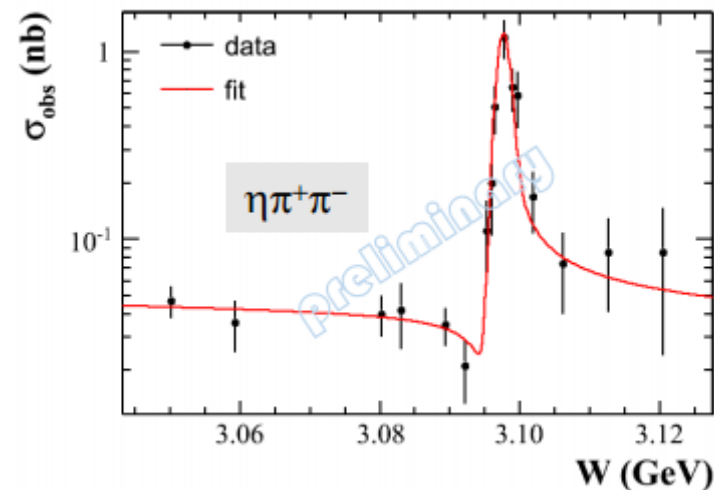
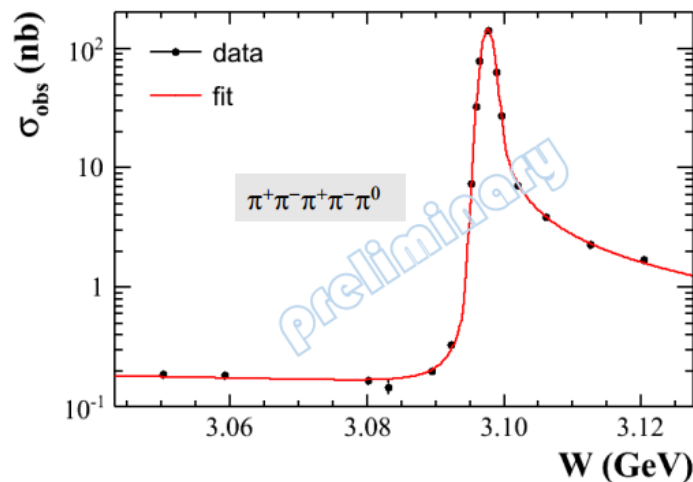
➤ $\text{Br}(J/\psi \rightarrow \pi^+ \pi^- \pi^+ \pi^- \pi^0) = \frac{\Gamma_{5\pi}}{\Gamma} = (4.27 \pm 0.52)\%$, consistent with PDG value

■ For $\eta\pi^+\pi^- (\eta \rightarrow \pi^+\pi^-\pi^0)$ process, the formula is similar with that for $\mu^+\mu^-$

➤ No A_{3g} due to G violation

➤ $\Phi_{\gamma,cont.} = (-2 \pm 39)^\circ$, consistent with zero

➤ $\text{Br}(J/\psi \rightarrow \eta\pi^+\pi^-) = \frac{\Gamma_{\eta\pi^+\pi^-}}{\Gamma} = (3.6 \pm 0.7) \times 10^{-4}$, much improved than PDG value.



J/ψ decay width

- ISR method

- 2.93 fb⁻¹ data at 3.773 GeV

- Channel: e⁺e⁻ → γ_{ISR}μ⁺μ⁻

- Generator: Phokhara

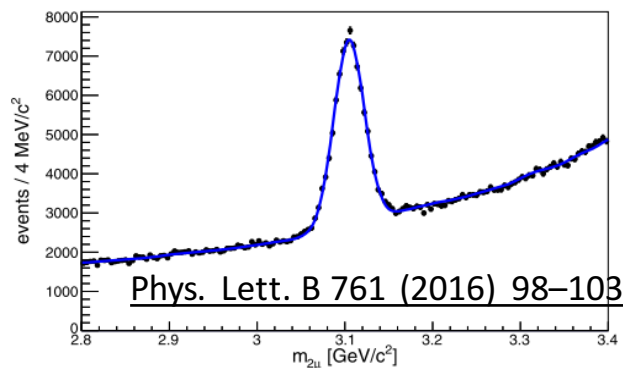
- $\sigma_{J/\psi\gamma}(s) = \frac{N_{J/\psi}}{\epsilon \cdot L} = \Gamma_{ee} \cdot B_{\mu\mu} \cdot I(s)$

$$I(s) = \int_{m_{min}}^{m_{max}} \frac{2m_{2\mu}}{s} W(s, m_{2\mu}) \frac{BW'(m_{2\mu})}{B_{\mu\mu} \Gamma_{ee}} dm_{2\mu}$$

$$BW(m_{2\mu}) = \frac{12\pi B_{\mu\mu} \Gamma_{ee} \Gamma_{tot}}{(m_{2\mu}^2 - m_{J/\psi}^2)^2 + m_{J/\psi}^2 \Gamma_{tot}^2}$$

- Fit function:

$$f(x) = N_{J/\psi} [M(x) \otimes G(x)] + (N_{total} - N_{J/\psi})p(x)$$



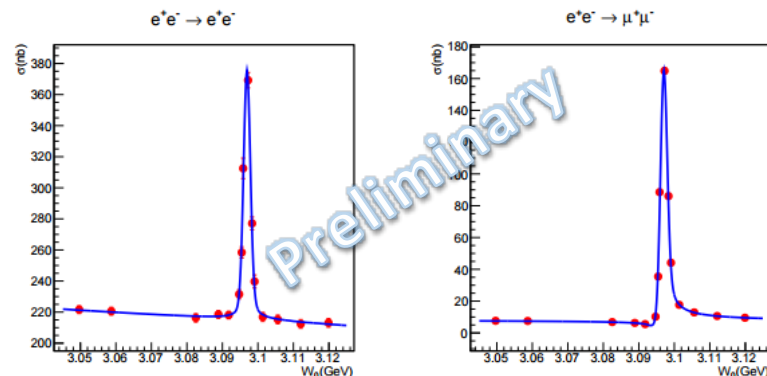
- $\Gamma_{ee} \cdot B_{\mu\mu} = (333.4 \pm 2.5 \pm 4.4) \text{ eV}$

- Energy Scan method

- Data at 15 energy points around J/ψ peak, integrated luminosity ~83 pb⁻¹

- Channels: e⁺e⁻ → e⁺e⁻ and e⁺e⁻ → μ⁺μ⁻

- $\sigma_{ll}^{the} = \sigma_{ll}^{the}(W_0, M, \Gamma_{tot}, \Gamma_{ee} \Gamma_{ll} / \Gamma_{tot}, \sqrt{\Gamma_{ee} \Gamma_{ll}}, \sigma_W)$ with ll = ee or μμ



Collaboration	Year	Γ_{tot} (keV)	Γ_{ll} (keV)
BABAR	2004	94.7 ± 4.4	5.61 ± 0.21
CLEO	2006	96.1 ± 3.2	5.71 ± 0.16
KEDR	2010	94.1 ± 2.7	5.59 ± 0.12
PDG	2014	92.9 ± 2.8	5.55 ± 0.14
BESIII(ISR)	2016	—	5.58 ± 0.09
This Work	2016	94.4 ± 1.9	5.64 ± 0.10

Summary

- Fruitful results from e^+e^- annihilation at BESIII, both energy scan and ISR methods are performed.
- More precise baryon form factor on proton, Λ and Λ_c , threshold effect observed near the mass threshold of baryon pair.
- A vector structure observed in K^+K^- spectrum, with $m=2.2298 \pm 0.0053 \pm 0.0172$ GeV and $\Gamma = 143.7 \pm 12.0 \pm 7.8$ MeV.
- Progress been made in vacuum polarization calculation from $\gamma_{\text{ISR}}\pi^+\pi^-$ and $\gamma_{\text{ISR}}\pi^+\pi^-\pi^0$ processes.
- First measurement for the phase between J/ψ strong and EM amplitude concern multi-hadron final state.
- ISR and ES methods performed to extract Γ_{ll} and Γ_{tot} on J/ψ and achieved the best accuracy.

Thank you!
Obrigado!
谢谢!