



Overview on QCD studies at BESII

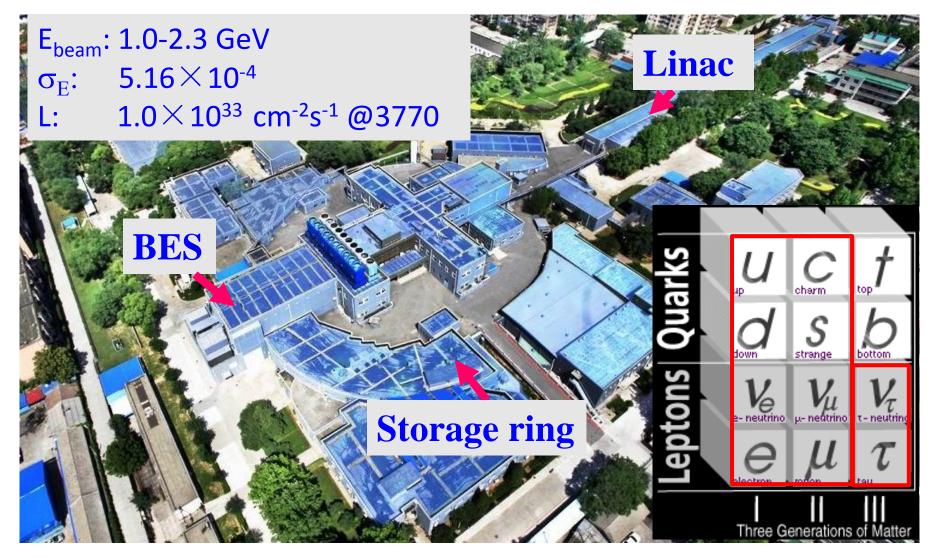
State Key Laboratory of Particle Detection and Decisions University of Science and Technology of China

The 9th International workshop on Excited QCD Sintra, Portugal, May 2017

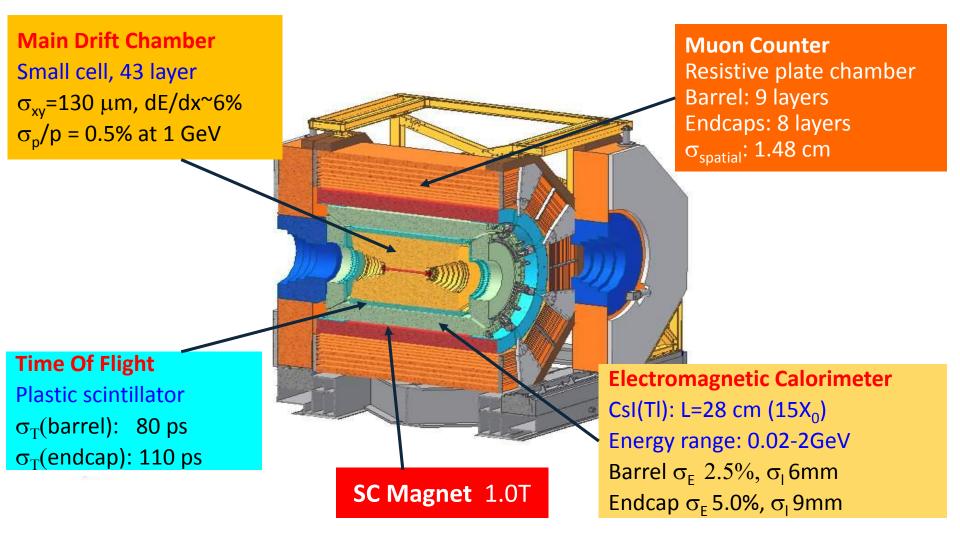
Outline

- The BESIII experiment
- Baryon structure, form factor measurement
- Hadron spectroscopy
- Precision test on Standard Model, $(g 2)_{\mu}$
- Lineshape of J/ψ resonance
- Summary

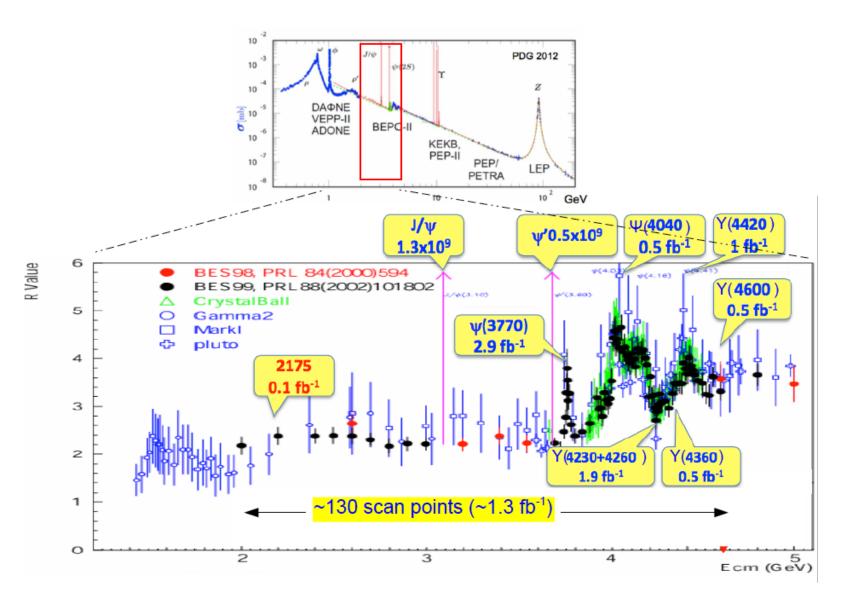
Beijing Electron Positron Collider



BEijing Spectrometer III



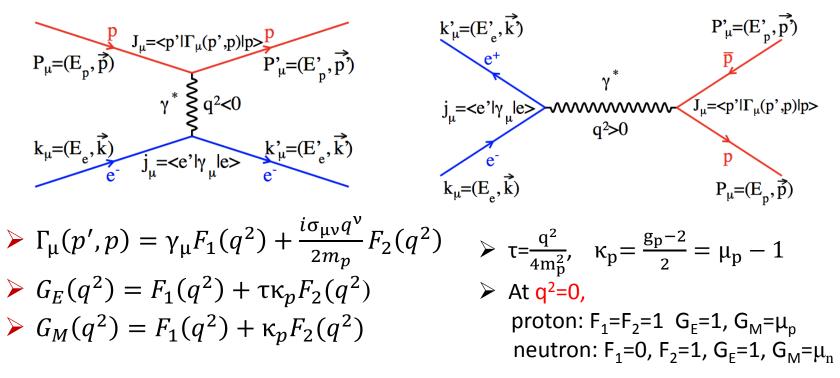
The BESIII data sample



5

Baryon form factor

The FFs are measured in space-like (SL) region or time-like (TL) region. The proton electromagnetic vertex Γ_{μ} describing the hadron current



 G_E and G_M can be interpreted as Fourier transforms of spatial distributions of charge and magnetization of nucleon in the Breit frame

i.e
$$\rho(\vec{r}) = \int \frac{d^3q}{2\pi^3} e^{-i\vec{q}\cdot\vec{r}} \frac{M}{E(\vec{q})} G_E(\vec{q}^2)$$

Baryon form factor

→ The Born cross section for $e^+e^- \rightarrow \gamma^* \rightarrow B\overline{B}$, can be expressed in terms of electromagnetic form factor G_E and G_M:

$$\sigma_{B\bar{B}}(q) = \frac{4\pi\alpha^2 C\beta}{3q^2} [|G_M(q)|^2 + \frac{1}{2\tau} |G_E(q)|^2]$$

$$\blacktriangleright \text{ The Coulomb factor C} = \begin{bmatrix} \frac{\pi\alpha}{\beta} \frac{1}{1 - \exp(-\frac{\pi\alpha}{\beta})} & \text{for a charged } B\bar{B} \text{ pair} \\ 1 & \text{for a neutral } B\bar{B} \text{ pair} \end{bmatrix}$$

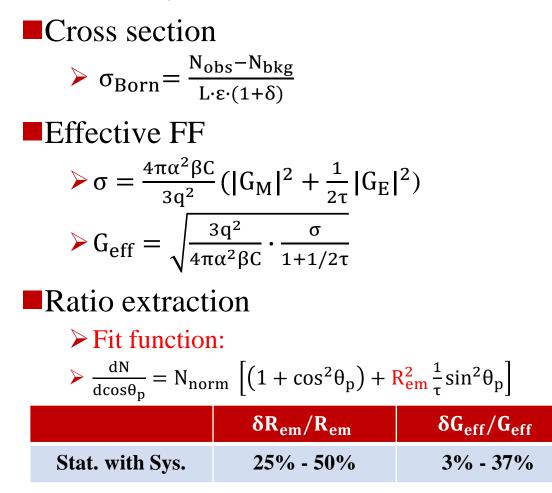
$$\begin{tabular}{|c|c|c|c|c|} \hline Energy Scan & Initial State Radiation \\ \hline E_{beam} & discrete & fixed \\ \hline \mathcal{L} & low at each beam energy & high at one beam energy \\ \hline \sigma & \frac{d\sigma_{p\bar{p}}}{d(\cos\theta)} = \frac{\pi\alpha^2\beta C}{2q^2} [|G_M|^2(1+\cos^2\theta) & \frac{d^2\sigma_{p\bar{p}\gamma}}{dq^2d\theta_\gamma} = \frac{1}{s}W(s,x,\theta_\gamma)\sigma_{p\bar{p}}(q^2) \\ & +\frac{4m_p^2}{q^2}|G_E|^2\sin^2\theta] & W(s,x,\theta_\gamma) = \frac{\alpha}{\pi^x}(\frac{2-2x+x^2}{\sin^2\theta_\gamma}-\frac{x^2}{2}) \\ \hline q^2 & single at each beam energy & from threshold to s \\ \hline \end{array}$$

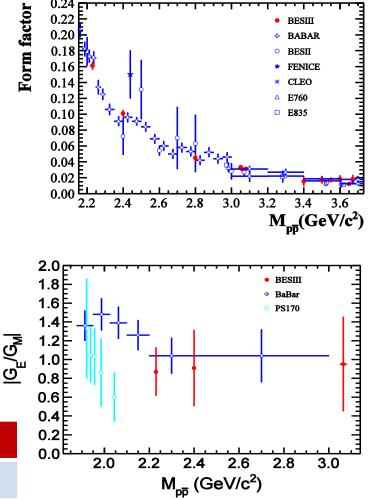
Both techniques, energy scan and initial state radiation. can be used at BESIII

 $e^+e^-
ightarrow p\overline{p}$

Phys.Rev.D 91, 112004(2015)

Using 12 c.m. energies from 2.2324 to 3.671 GeV, total luminosity 156.9 pb⁻¹





$e^+e^- \rightarrow \gamma_{ISR}p\overline{p}$

Combination of 7 data sets (\geq 3.773 GeV), total luminosity 7.4 fb⁻¹.

Event selection:

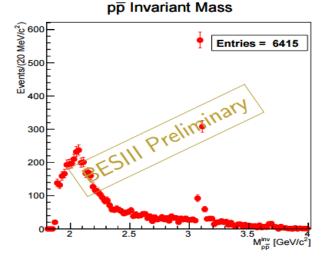
- Two charged tracks from vertex
- ➢ One high energy shower in EMC (ISR-tagged)
- Kinematic constraints applied
- Background subtraction from weighted MC

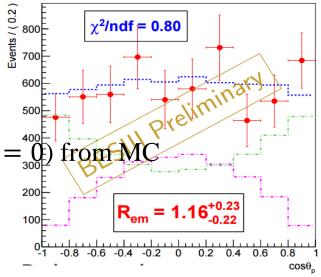
Cross section

 $\succ \sigma_{p\bar{p}}^{Born} \left(M_{p\bar{p}} \right) = \frac{(dN/dM_{p\bar{p}})_{corr}}{dL/dM_{p\bar{p}}}$

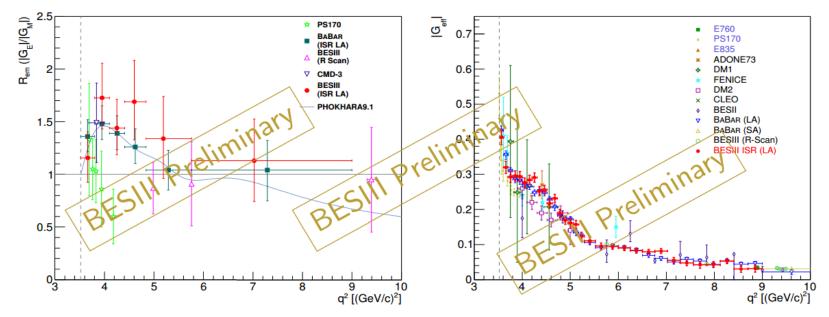
Ratio extraction

$$\ge \frac{d\sigma}{d\cos\theta} = A \left[H_M(\cos\theta, q^2) + \frac{R_{em}^2}{\langle \tau \rangle} H_E(\cos\theta, q^2) \right]$$
$$\ge H_M(\cos\theta, q^2) (G_E = 0) \text{ and } H_E(\cos\theta, q^2) (G_M = 0)$$





 $e^+e^- \rightarrow \gamma_{ISR}p\bar{p}$



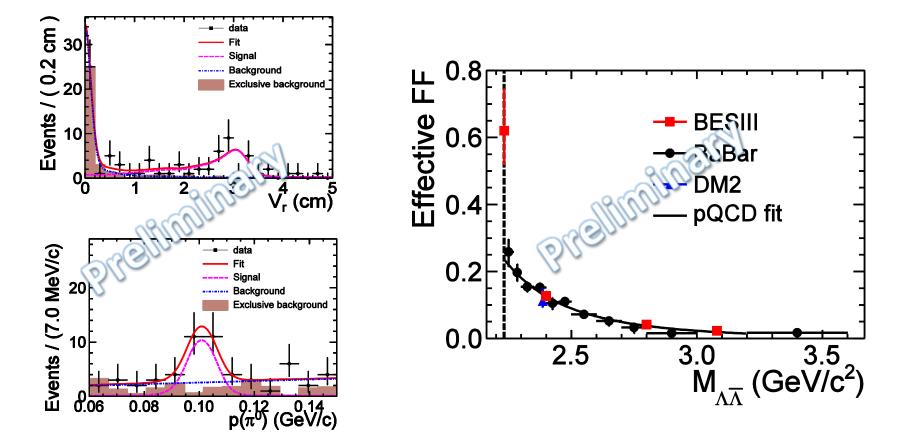
Background subtraction and efficiency dividing

The proton FFs extracted between threshold to 3.0 GeV

	$\delta R_{em}/R_{em}$	δG _{eff} /G _{eff}
Stat.	18.5 - 33.6%	4.1 - 31.6%
Syst.	4.2- 15.6%	1.6 - 12%

$e^+e^- \rightarrow \Lambda \overline{\Lambda}$

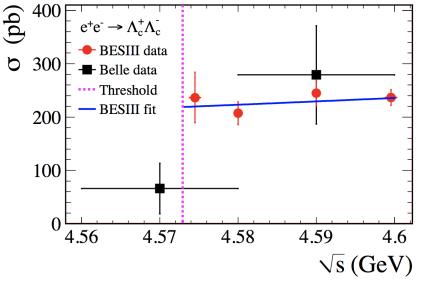
- Using 4 c.m. energies from 2.2324 to 3.08 GeV, total luminosity 40.5 pb⁻¹
- $e^+e^- \rightarrow \Lambda \overline{\Lambda}$ at the first energy point, 2.2324 GeV, which is 1.0 MeV above the $\Lambda \overline{\Lambda}$ mass threshold, is reconstructed final final states of $p\overline{p}\pi^+\pi^$ and $\overline{n}\pi^0 + X$. The Born cross section is measured to be $305 \pm 45^{+66}_{-36}$ pb



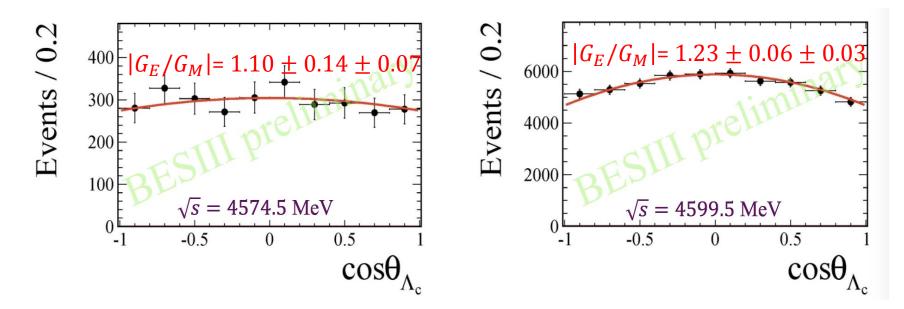
$e^+e^- \rightarrow \Lambda_c^+ \overline{\Lambda}_c^-$

■Using 4 c.m. energies, 4.575, 4.580, 4.590 and 4.600 GeV, total luminosity 631.3 pb⁻¹

■ $e^+e^- \rightarrow \Lambda_c^+ \overline{\Lambda}_c^-$ is reconstructed by tagging 10 decay modes of Λ_c^+



Angular distribution of Λ_c^+ is studied at 4.575 and 4.600 GeV.



Hadron spectroscopy

≻Cross section of $e^+e^- \rightarrow K^+K^-$ inBaBar

 \triangleright Possible resonance near 2.2 GeV:ρ(2150), φ(2170)/Y(2175), ...

Y(2175)	As $2 {}^{3}D_{1} s \overline{s}$ quarkonium		As ssīg hybrid	As 3 ³ S ₁ ss̄ quarkonium
	Γ _{LJ} in ³ P ₀ model	Γ _{LJ} in Flux Tube Model	in Flux Tube Model	in ³ P ₀ model
$\Gamma_{\rm KK}({ m MeV})$	9.8	23.1	0	0
$\Gamma_{\rm tot}({\rm MeV})$	167.21	211.9	148.7	378
PI B 657 (2	007) 49		$rac{10}{2}$ 10 ⁴ error root root root root root root roo	

Form factor of kaon Charge distribution: $F(q^2) = \int d^3 r \rho(r) e^{iq \cdot r}$ Check pQCD predictions: $F_K = 16\pi\alpha_s(s) f_K^2/s_{10^{-1}}$

√s (GeV)

$e^+e^- \rightarrow K^+K^-$

R scan data from 2.0 to 3.08 GeV, total luminosity $\sim 651 \text{ pb}^{-1}$

A structure near 2.2 GeV is measured by:

$$\sigma = |A_K|^2,$$

$$A_K = \sum_r c_r \cdot BW_r + c_{con} \cdot s^{-\alpha} \cdot e^{i\theta}$$

 $r:\rho,\omega,\phi$ a

Form facto

$$r: \rho, \omega, \varphi \text{ and their excited states}$$
orm factor extraction:
$$|F_K|^2(s) = \frac{3s}{\pi\alpha(0)^2\beta^3} \frac{\sigma_{KK}(s)}{c_{FS}}; \quad \sigma_{KK}(s) = \sigma_{KK}^0(s) (\frac{\alpha(s)}{\alpha(0)})^2 = \frac{2.2}{2.2} = \frac{2.4}{2.4} = \frac{2.6}{2.6} = \frac{3}{2.8} = \frac{3}{3} = \frac{3}{\sqrt{s}} (\text{GeV})$$

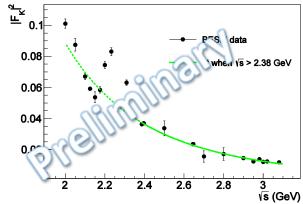
α (up) α

0.4

 $\sigma_{KK}(s)$: dressed cross section; $\sigma_{KK}^0(s)$: bare cross section C_{FS} : final-state correction

Form factor fitting function:

 $|F_K|^2 = A\alpha_s^2(s)/s^n$ n = 1.94 + 0.09(agreement with pQCD prediction n = 2)



BESIII

m=2.2298+0.005?

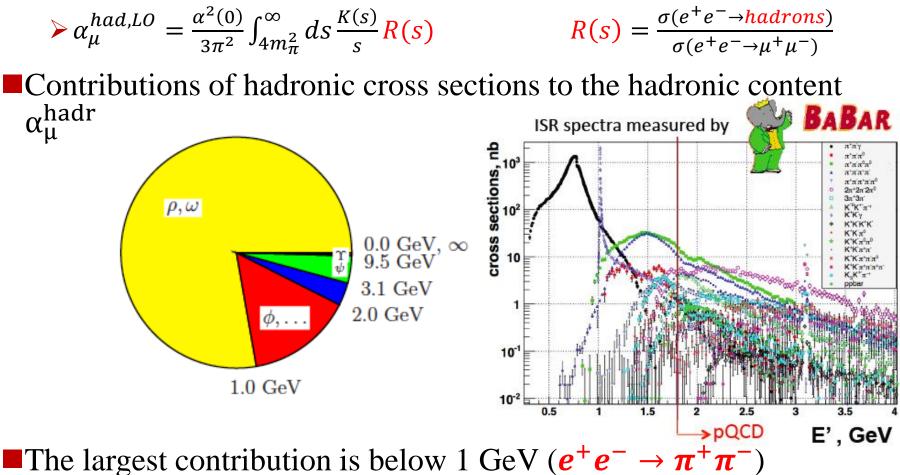
BABAR 2015

Precision tests of the Standard Model

The anomalous magnetic moment $\alpha_{\mu} = \frac{g_{\mu}-2}{2}$ Experimental measurement: $\alpha_{\mu}^{exp} = (11659208.9 + 6.3) \cdot 10^{-10} \frac{10}{PRD 73, 072(2006)}$ Theoretical prediction: $\alpha_{\mu}^{SM} = (11659580.2 + 4.9) \cdot 10^{-10}$ Eur. Phys. J. C71, 1515(2011) =>discrepancy: 3.6 standard deviations $\alpha_{\mu}^{\rm SM} = \alpha_{\mu}^{\rm QED} + \alpha_{\mu}^{\rm weak} + \alpha_{\mu}^{\rm hadr}$ can not be calculated by means of perturbative calculations B-Feld Hadronic light-by-light scattering Hadronic vacuum polarization $\alpha_{\mu}^{hadr,LBL} = (10.5 \pm 2.6) \cdot 10^{-10}$ $\alpha_{\mu}^{hadr,VP} = (692.2 \pm 4.2) \cdot 10^{-10}$

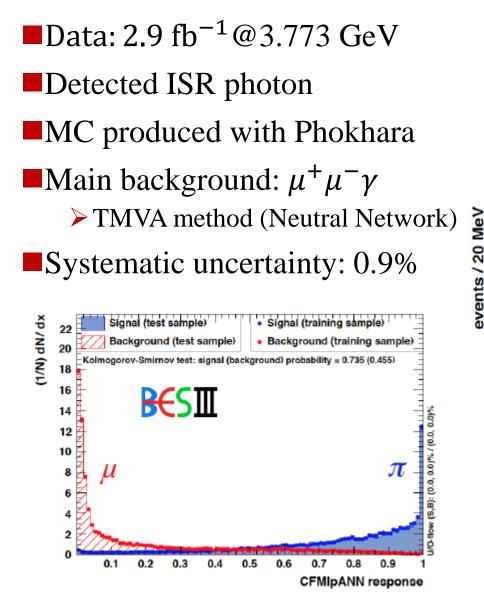
Precision tests of the Standard Model

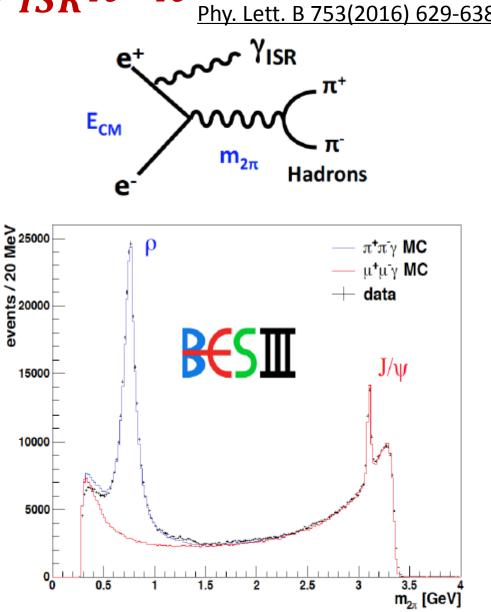
Hadronic vacuum polarization

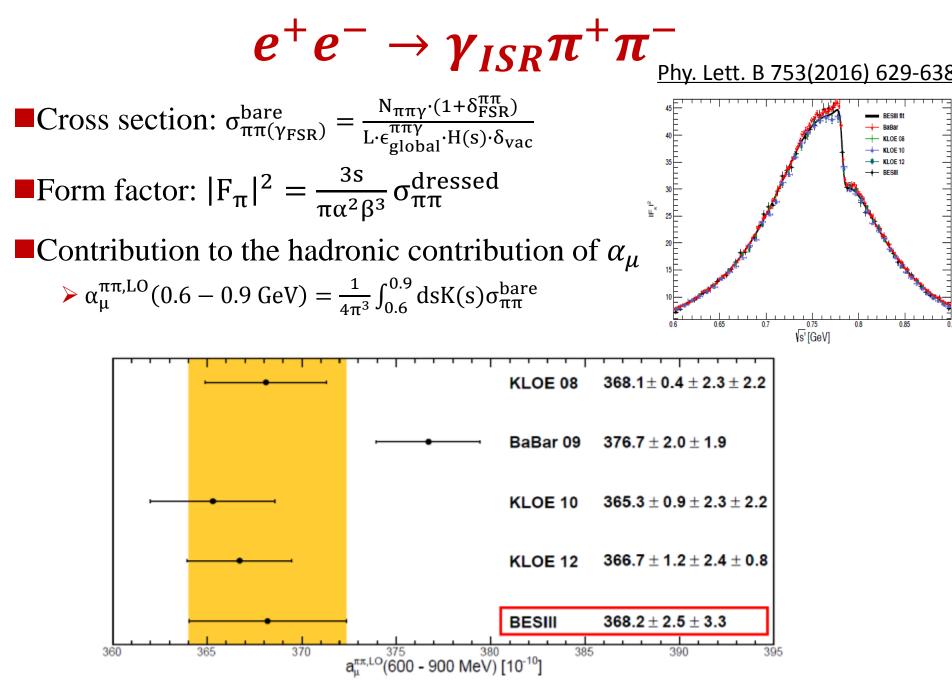


 $e^+e^- \rightarrow \pi^+\pi^-\pi^0$ contribution > 6%

$e^+e^- \rightarrow \gamma_{ISR}\pi^+\pi^-_{_{\rm P}}$





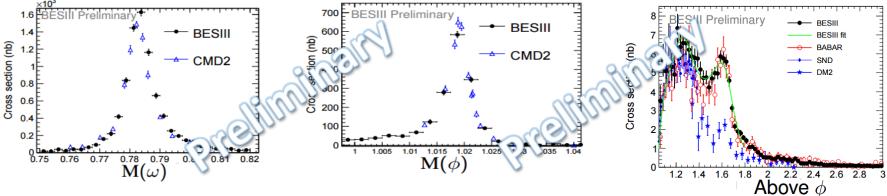


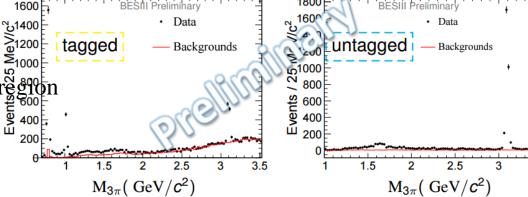
 $e^+e^- \rightarrow \gamma_{ISR}\pi^+\pi^-\pi^0$

- Data: 2.9 fb⁻¹@3.773 GeV
- ISR tagged:
 - \triangleright Clear ω and φ signals
 - \succ Huge background in high mass rgg00
- ISR untagged
 - > Limited by acceptance
 - Negligible background
- Below 1.8 GeV, fit with VMD model

$$\sigma(m) = \frac{12\pi}{m^3} F_{\rho\pi}(m) \left| \sum_{V=\omega,\varphi,\omega'\omega''} \frac{\Gamma_V m_V^{3/2} \sqrt{B(V \to e^+ e^-)B(V \to 3\pi)}}{D_V(m)} \frac{e^{i\varphi V}}{\sqrt{F_{\rho\pi}(m_V)}} \right|$$

 Branching fraction for $\omega, \varphi, \omega' \omega''$ consistent with PDG

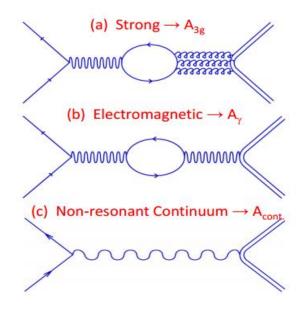




2

3.5

Lineshape of J/ψ resonance



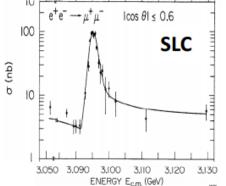
(a) $e^+e^- \rightarrow J/\psi \rightarrow$ hadrons via strong mechanism; (b) $e^+e^- \rightarrow J/\psi \rightarrow$ hadrons via EM mechanism;

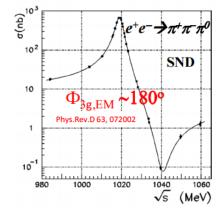
(c) non-resonant $e^+e^- \rightarrow$ hadrons via a virtual photon.

$$\sigma_{\text{Born}} = |A_{3g} + A_{\gamma} + A_{\text{cont}}|^2$$
$$= ||A_{3g}|e^{i\Phi_{3g,\text{EM}}} + |A_{\gamma}|e^{i\Phi_{\gamma,\text{cont.}}} + |A_{\text{cont.}}||^2$$

M. Suzuki et al., Phys. Rev. D60, 051501 (1999).
 M. Suzuki et al. Phys. Rev. D63, 054021 (2001).
 M. Ablikim et al. (BESIII), Phys. Rev. D86, 032014 (2012).
 K. Zhu et al., Int. J Mod. Phys. A30, 1550148 (2015).

- Model dependent experimental evidences:
 - > SU3 and SU3 breaking in $1^{-0^{[1]}}$, $0^{-0^{[1]}}$, $1^{-1^{-[1]}}$, $1^{+0^{-[2]}}$ decay show the phase between A_{3g} and A_{EM} is $\Phi_{3g,EM} \sim 90^{\circ}$
 - $\stackrel{\text{If }A(e^+e^- \to n\overline{n}) \sim -A(e^+e^- \to p\overline{p}),}{\frac{B(n\overline{n})}{B(p\overline{p})} = 0.98 \pm 0.08 \to \Phi_{3g,EM} \sim 89^\circ \pm 8^{\circ[3]} }$
 - > Other baryon pairs: $\Phi_{3g,EM} \sim -85.9^{\circ} \pm 1.7^{\circ} \text{ or } 90.8^{\circ} \pm 1.6^{\circ [4]}$
 - ➤ The phase angle between A_{EM} and A_{cont}: $Φ_{\gamma,cont.} = 0° \text{ from } e^+e^- → μ^+μ^-$
 - ➤ The interference between φ and ω was observed at SND, $Φ_{3g,EM} \sim 180^\circ$





$e^+e^- ightarrow \mu^+\mu^-$

Data at 16 energy points around J/\u03c6 peak, integrated luminosity~100.5 pb⁻¹
 Observed cross section: \u03c6_i = \u03c6_iL_i(B)

Theoretically prediction of Born cross section: $\sigma^{0}(W) = \frac{4\pi\alpha^{2}}{W^{2}} \left| 1 + \frac{3W^{2}\sqrt{\Gamma_{ee}\Gamma_{\mu\mu}}e^{i\gamma,cont}}{\alpha M(W^{2}-M^{2}+iM\Gamma)} \right|^{2}$ Considering ISR : $\sigma'(W) = \int_{0}^{1-(\frac{W_m}{W})^2} dx F(x, W) \sigma^0(W)$ Considering energy spread S_E: $\sigma''(W) = \int_{W-nS_E}^{W+nS_E} \frac{1}{\sqrt{2\pi}S_E} \exp(\frac{W'-W}{2S_E^2}) \sigma'(W') dW'$ $\blacksquare \text{ Minimization method: } \chi^2 = \sum_{i=1}^{16} \frac{\left[\sigma^{\text{obs}}(W_i) - \sigma''(W_i)\right]^2}{\left(\Delta \sigma^{\text{obs}}W_i\right)^2 + \left[\Delta W_i \cdot \frac{d\sigma''}{dW}(W_i)\right]^2}$ (**qu**) م^{ops} 10² ─**•**─ data ── fit $\Phi_{\nu,\text{cont.}} = (-5 \pm 9.7)^{\circ}$, consistent with zero μ+µ⁻ Energy spread: $S_E = (0.911 \pm 0.026) MeV$ Energy shift: $\Delta M = (0.548 \pm 0.041) MeV$ 10 3.06 3.08 3.10 3.12

W (GeV)

$e^+e^- ightarrow \pi^+\pi^-\pi^+\pi^-\pi^0$

For $\pi^+\pi^-\pi^+\pi^-\pi^0$ process: $\sigma^0(W) = \left(\frac{A}{W^2}\right)^2 \frac{4\pi\alpha^2}{W^2} \left|1 + \frac{3W^2\sqrt{\Gamma_{ee}\Gamma_{\mu\mu}}(1+Ce^{i\Phi_{3g,EM}})}{\alpha M(W^2-M^2+iM\Gamma)}\right|^2$

▶ Φ_{3g,EM} = 83.4° ± 4.3° or −83.5° ± 4.2°

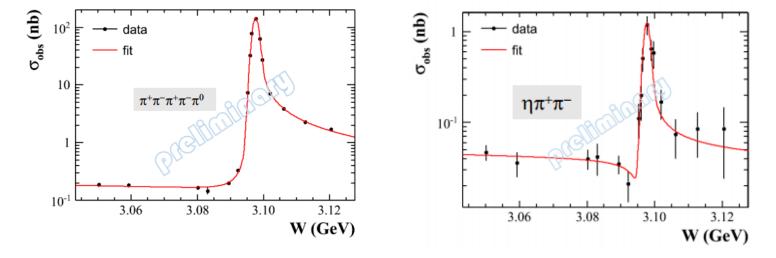
$$\succ \Gamma_{5\pi} = \left(\frac{A}{W^2}\right)^2 \Gamma_{\mu\mu} \left| 1 + C e^{i\Phi 3 g, EM} \right|$$

 $> Br(J/\psi \rightarrow \pi^+\pi^-\pi^+\pi^-\pi^0) = \frac{\Gamma_{5\pi}}{\Gamma} = (4.27 \pm 0.52)\%, \text{ consistent with PDG value}$

For $\eta \pi^+ \pi^- (\eta \to \pi^+ \pi^- \pi^0)$ process, the formula is similar with that for $\mu^+ \mu^-$ > No A_{3g} due to G violation

 $\blacktriangleright \Phi_{\gamma,\text{cont.}} = (-2 \pm 39)^\circ$, consistent with zero

 $\geq \operatorname{Br}(J/\psi \to \eta \pi^+ \pi^-) = \frac{\Gamma_{\eta \pi^+ \pi^-}}{\Gamma} = (\mathbf{3}, \mathbf{6} \pm \mathbf{0}, \mathbf{7}) \times \mathbf{10^{-4}}, \text{ much improved than PDG value.}$

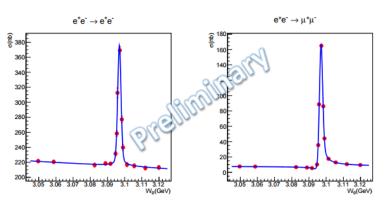


J/ψ decay width

 \sim 2.93 fb⁻¹ data at 3.773 GeV Channel: $e^+e^- \rightarrow \gamma_{ISR}\mu^+\mu^-$ Generator: Phokhara $\sigma_{J/\psi\gamma}(s) = \frac{N_{J/\psi}}{\epsilon I} = \Gamma_{ee} \cdot B_{\mu\mu} \cdot I(s)$ $I(s) = \int_{m_{min}}^{m_{max}} \frac{2m_{2\mu}}{s} W(s, m_{2\mu}) \frac{BW'(m_{2\mu})}{B_{\mu\mu}\Gamma_{ee}} dm_{2\mu}$ $BW(m_{2\mu}) = \frac{12\pi B_{\mu\mu}\Gamma_{ee}\Gamma_{tot}}{(m_{2\mu}^2 - m_{J/\psi}^2)^2 + m_{J/\psi}^2\Gamma_{tot}^2}$ Fit function: $f(x) = N_{I/\Psi}[M(x) \otimes G(x)] + (N_{total} - N_{I/\Psi})p(x)$ 7000 events / 4 MeV/c² 4000 3000 2000 Phys. Lett. B 761 (2016) 98-108 1000 3.1 3.2 3.3 m_{2μ} [GeV/c²] $\blacksquare \Gamma_{ee} \cdot B_{\mu\mu} = (333.4 \pm 2.5 \pm 4.4) \text{ eV}$

ISR method

- Energy Scan method
- Data at 15 energy points around J/ψ peak, integrated luminosity ~83 pb⁻¹
- Channels: $e^+e^- \rightarrow e^+e^-$ and $e^+e^- \rightarrow \mu^+\mu^-$
- $\sigma_{ll}^{the} = \sigma_{ll}^{the}(W_0, M, \Gamma_{tot}, \Gamma_{ee}\Gamma_{ll} / \Gamma_{tot}, \sqrt{\Gamma_{ee}\Gamma_{ll}}, \sigma_W) \text{ with } ll = ee \text{ or } \mu\mu$



Collaboration	Year	Γ_{tot} (keV)	Γ_{ll} (keV)
BABAR	2004	94.7±4.4	5.61±0.21
CLEO	2006	96.1±3.2	5.71±0.16
KEDR	2010	94.1±2.7	5.59 ± 0.12
PDG	2014	92.9 ± 2.8	5.55 ± 0.14
BESIII(ISR)	2016	_	$5.58 {\pm} 0.09$
This Work	2016	94.4±1.9	$5.64{\pm}0.10$

Summary

- Fruitful results from e^+e^- annihilation at BESIII, both energy scan and ISR methods are performed.
- More precise baryon form factor on proton, Λ and Λ_c , threshold effect observed near the mass threshold of baryon pair.
- A vector structure observed in K⁺K⁻ spectrum, with m=2.2298 \pm 0.0053 \pm 0.0172 GeV and Γ = 143.7 \pm 12.0 \pm 7.8 MeV.
- Progress been made in vacuum polarization calculation from $\gamma_{ISR}\pi^+\pi^-$ and $\gamma_{ISR}\pi^+\pi^-\pi^0$ processes.
- First measurement for the phase between J/ψ strong and EM amplitude concern multi-hadron final state.
- ISR and ES methods performed to extract Γ_{ll} and Γ_{tot} on J/ ψ and achieved the best accuracy.

Thank you! Obrigado! 谢谢!