

# $p_\perp$ fluctuations and correlations

Piotr Bożek

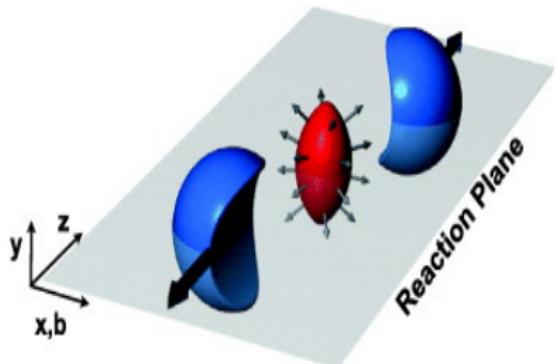
AGH University of Science and Technology, Kraków

with: W. Broniowski, arXiv: 1701.09105  
and S. Chatterjee, arXiv: 1704.02777



asymmetry in the transverse plane at finite impact parameter

$$\text{eccentricity} - \epsilon_2 = -\frac{\int dx dy (x^2 - y^2) \rho(x, y)}{\int dx dy (x^2 + y^2) \rho(x, y)}$$



Snellings 2011

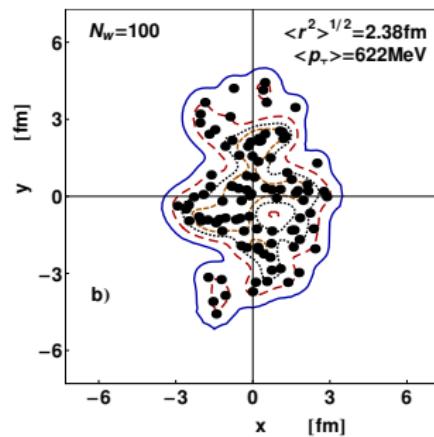
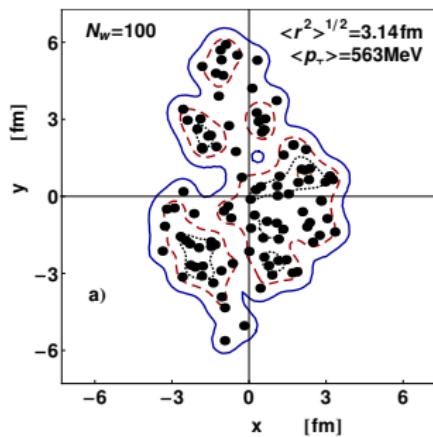
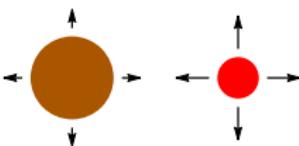
larger gradient and stronger flow in-plane -  $v_2 > 0$  - **elliptic flow**

$$\frac{dN}{d\phi} \propto 1 + 2v_2 \cos(2\phi)$$

$\epsilon_2 + \text{HYDRO RESPONSE} \longrightarrow v_2$

Event Plane (Reaction plane) must be reconstructed in each event

## Size fluctuations $\leftrightarrow p_\perp$ fluctuations

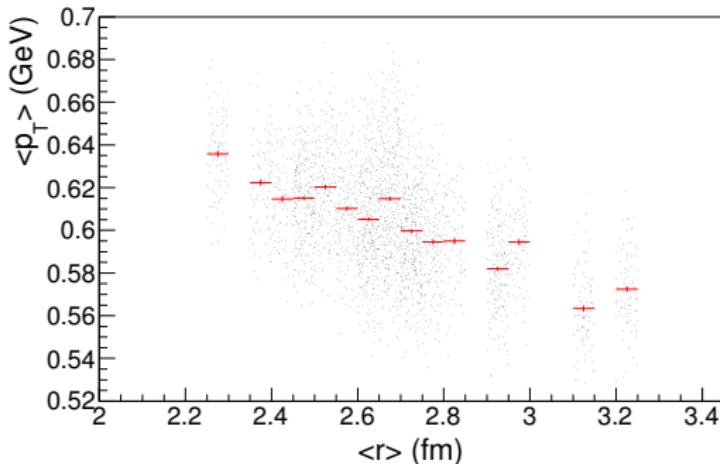


proposed by Broniowski et al. Phys.Rev. C80 (2009) 051902 :

two-shots calculation

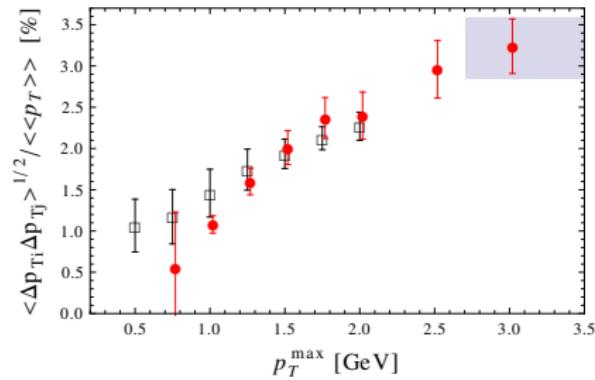
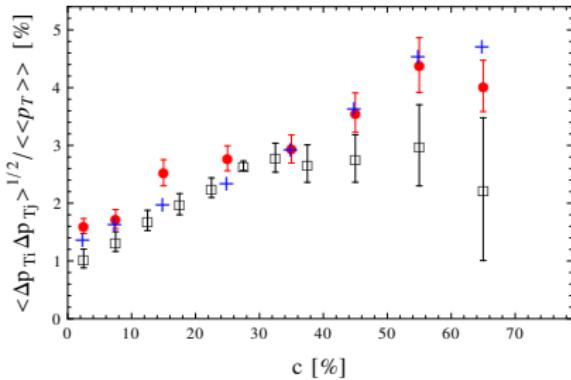
# Physical and statistical fluctuations

$N_w=100$



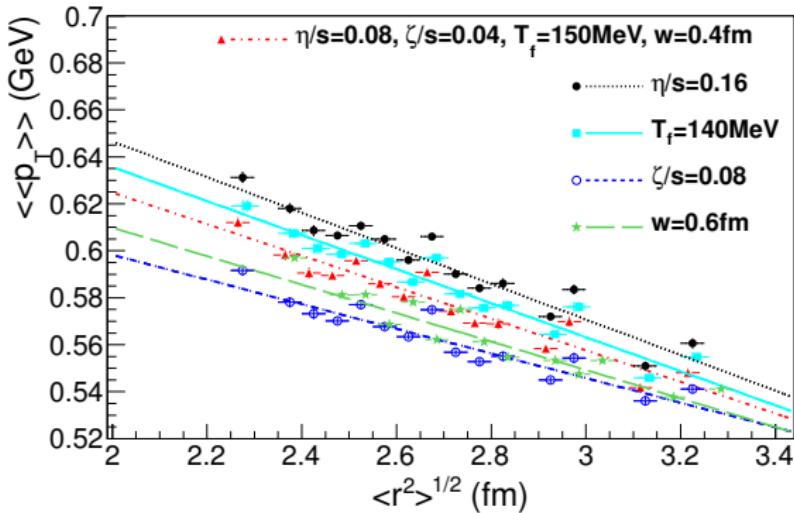
$$C_{p_{\perp}} = \frac{\frac{1}{N(N-1)} \sum_{i \neq j} \langle (p_i - \langle \langle p \rangle \rangle)(p_j - \langle \langle p \rangle \rangle) \rangle}{\langle \langle p_{\perp} \rangle \rangle^2}$$

## PHENIX data vs. hydro.



# Viscosity effects on hydro response

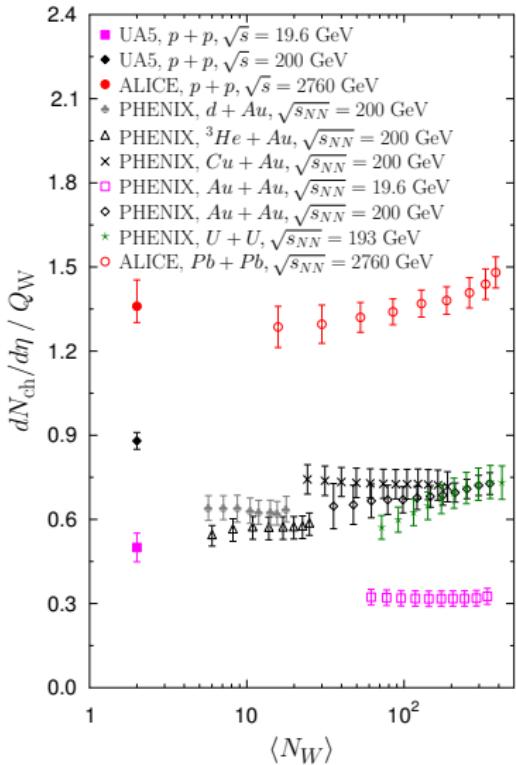
$N_w=100$



$$\frac{\Delta p}{p} \simeq 0.4 \frac{\Delta r}{r}$$

- ▶ size fl.  $\leftrightarrow p_\perp$  fluctuations
- ▶ hydro. response not modified by
  - ▶ viscosity
  - ▶  $T_F$
  - ▶ smearing
  - ▶ core-corona
  - ▶  $P_{tot}$  conservation
  - ▶ centrality def.
- ▶ too much fluctuations?

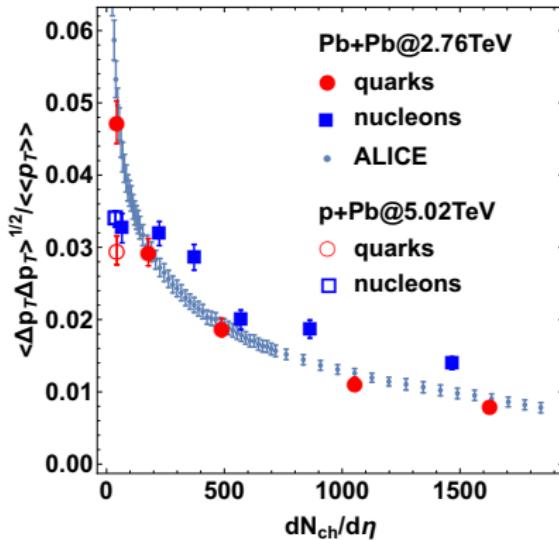
# Wounded quark model in AA



- very good (full) scaling at LHC
- approximate scaling at RHIC
- LHC - 3 partons , RHIC - 2 partons ?

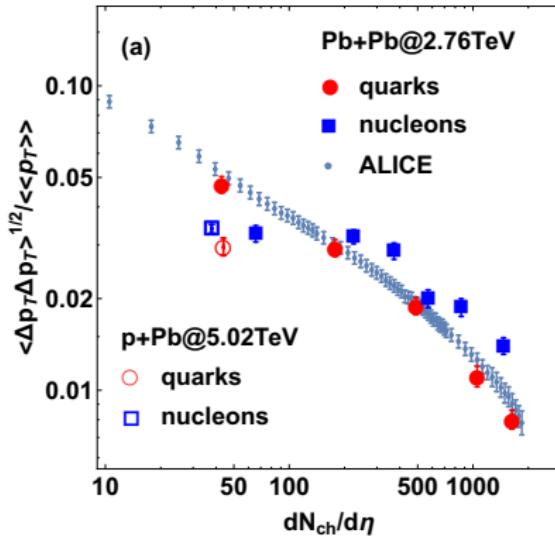
PB, W. Broniowski, M. Rybczyński,  
PRC 2016

## $p_{\perp}$ fluctuation quark Glauber model initial conditions



Quark Glauber model gives better description of initial volume fluctuations

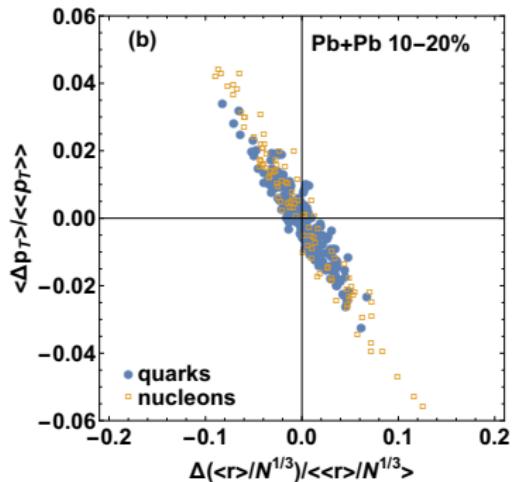
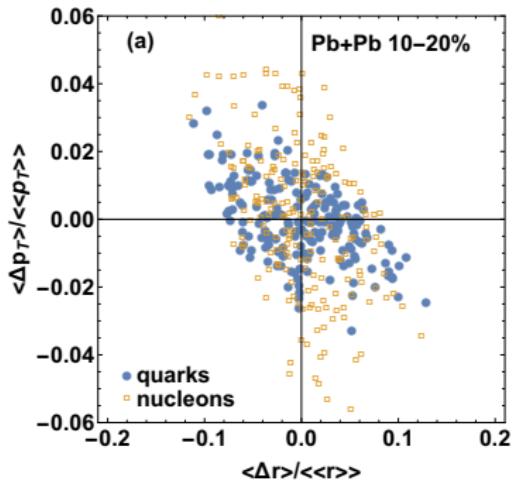
Same in log scale



more than simple  $N^{-1/2}$  scaling

both experiment and theory → not minijets

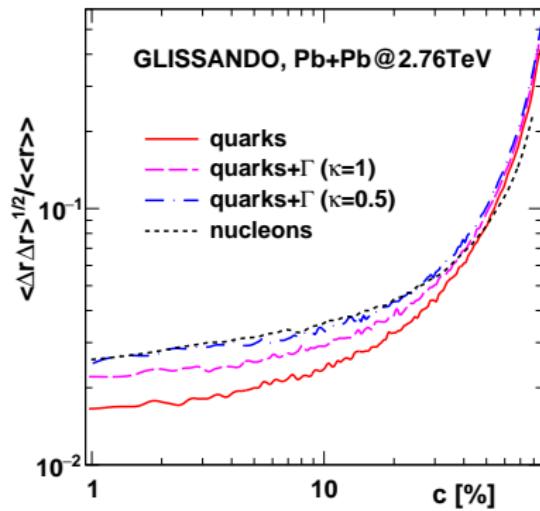
## Size - $p_{\perp}$ correlation



$\frac{N_q^\alpha}{\langle r \rangle}$  - predictor of the final  $p_{\perp}$

consistent with predictor of Mazellauskas-Teaney, PRC 2016

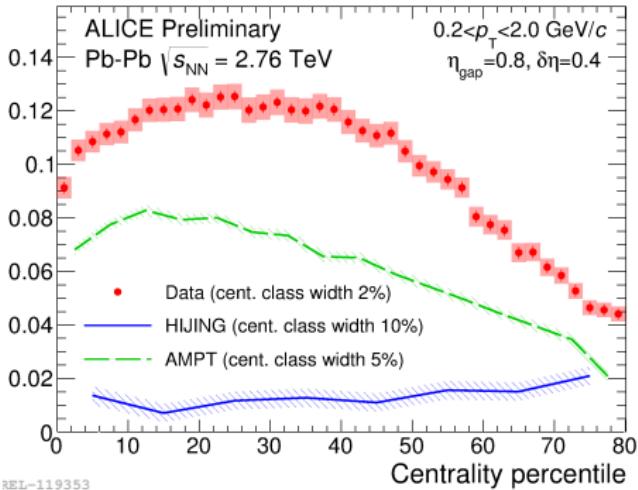
Caution - additional fluctuation may change the results



# $p_\perp - p_\perp$ correlation in rapidity - ALICE preliminary

$$b_{\text{corr}} = \frac{\langle FB \rangle - \langle F \rangle \langle B \rangle}{\langle F^2 \rangle - \langle F \rangle^2}$$

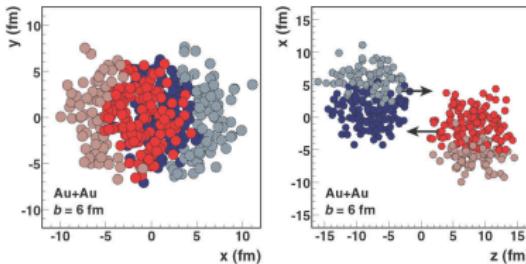
$$B \equiv \bar{p}_{TB} = \frac{\sum_{i=1}^{n_B} p_T^{(i)}}{n_B}$$
$$F \equiv \bar{p}_{TP} = \frac{\sum_{j=1}^{n_F} p_T^{(j)}}{n_F}$$



QM poster I. Altsybeev for ALICE

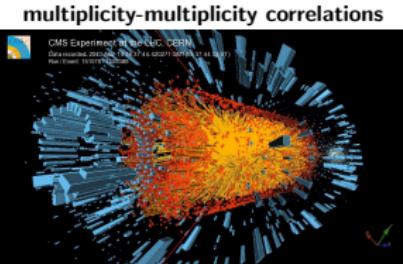
event generators have problems to reproduce data

# Forward and backward assymetry



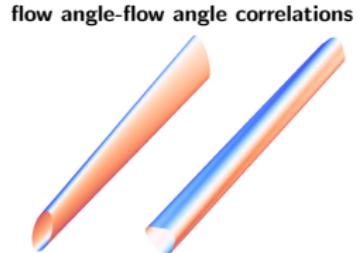
Ann.Rev.Nucl.Part.Sci. 57 (2007) 205

- Glauber Monte Carlo model → different forward and backward distributions
- different fireball shape at forward and backward rapidities



dozens of years, hundreds of papers

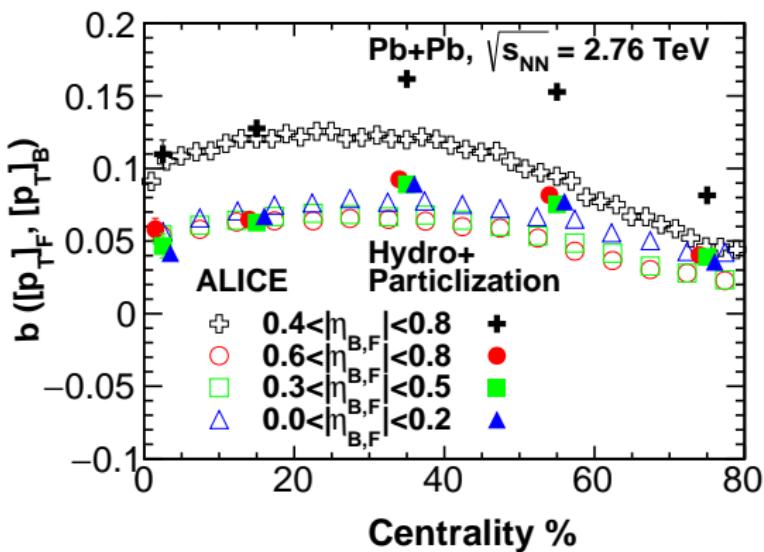
many effects sum up ...



PB, W. Broniowski, J.Moreira : 1011.3354

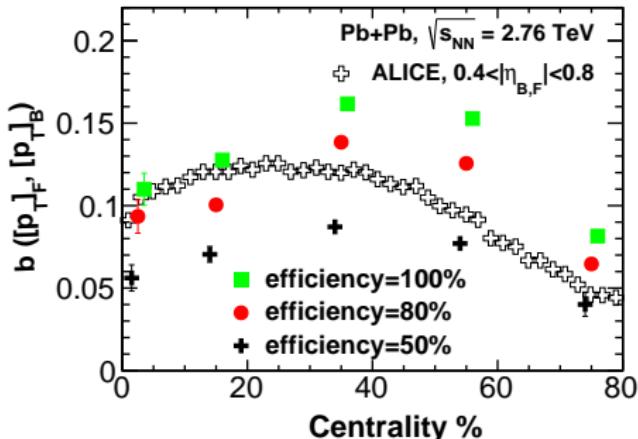
experiment and theory picks up momentum

## $p_{\perp} - p_{\perp}$ correlation in rapidity - hydro



reasonable description of the data

## $p_{\perp} - p_{\perp}$ correlation coefficient - ill defined



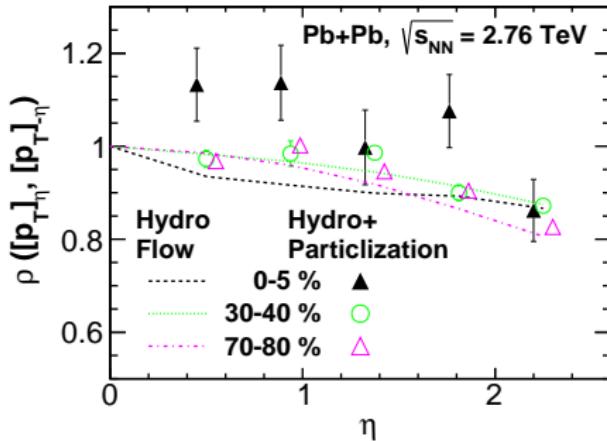
$$b = \frac{<[p_{\perp}]_A[p_{\perp}]_B> - <[p_{\perp}]_A><[p_{\perp}]_B>}{\sqrt{(<p_A^2> - <p_A>^2)(<p_B^2> - <p_B>^2)}} = \frac{\dots}{\sqrt{\frac{1}{n_A^2} \sum_{ij} p_i^A p_j^A \dots}}$$

sensitive to acceptance, particle multiplicity

**dominated by statistical fluctuations!**

## $[p_\perp] - [p_\perp]$ correlation coefficient

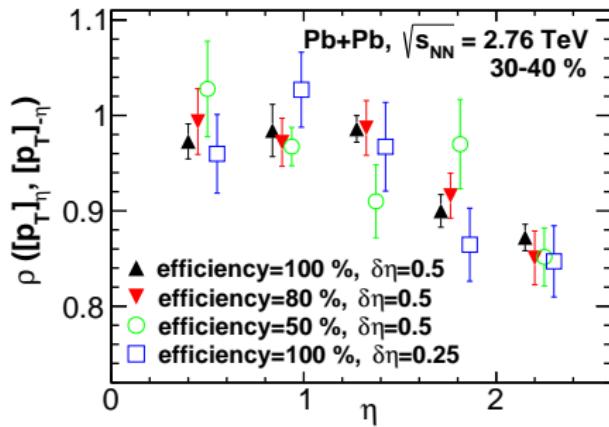
$$\frac{<[p_\perp]_A[p_\perp]_B> - <[p_\perp]_A><[p_\perp]_B>}{\sqrt{C_{p_\perp}^A C_{p_\perp}^B}} = \frac{\dots}{\sqrt{\frac{1}{n_A(n_A-1)} \sum_{i \neq j} p_i^A p_j^A \dots}}$$



$$\rho([p_T], [p_T]) \simeq 1$$

in the current model - strong correlations

## $[p_\perp] - [p_\perp]$ correlation coefficient

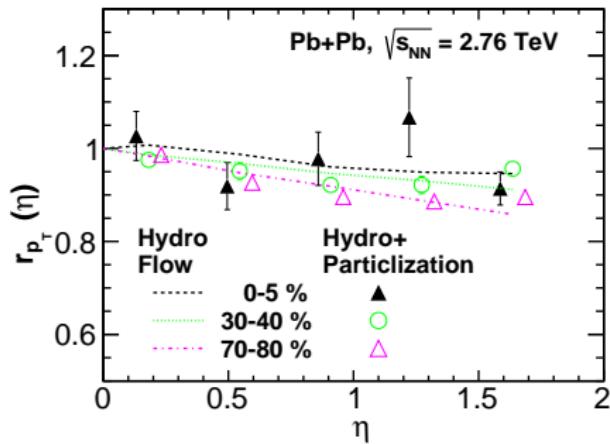


insensitive to acceptance, efficiency, multiplicity

**true measure of flow-flow correlations**

## 3-bin measure of $[p_T]$ decorrelation

$$r_{pT}(\Delta\eta) = \frac{\text{Cov}([p_T], [p_T])(\eta + \Delta\eta)}{\text{Cov}([p_T], [p_T])(\eta - \Delta\eta)}$$



## Measure of $[p_T]$ decorrelation in pseudorapidity

## Summary

- ▶ size fluctuations  $\leftrightarrow p_\perp$  fluctuations
- ▶ Glauber+hydro qualitatively consistent
- ▶ suggest scenarios with less fluctuations (quark Glauber model)
- ▶  $p_\perp$  correlations in  $\eta$  interesting
- ▶ strong  $[p_\perp] - [p_\perp]$  correlations? - should be measured