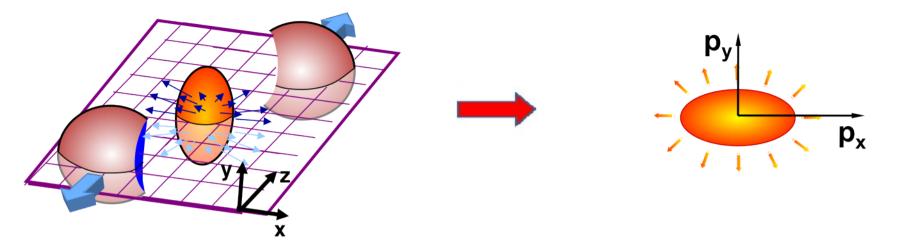
Azimuthal correlations and mixed higher order flow harmonics from CMS at the LHC



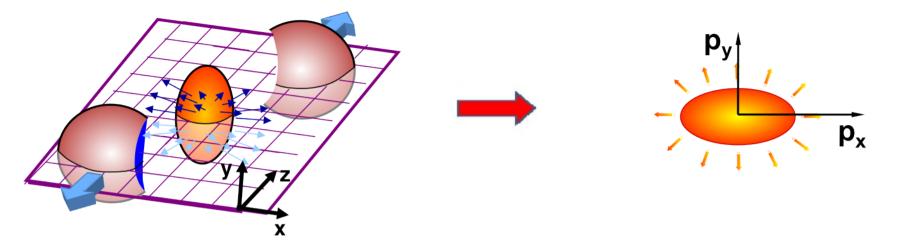
Excited QCD, Sintra, 2017



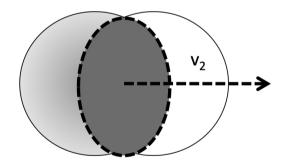




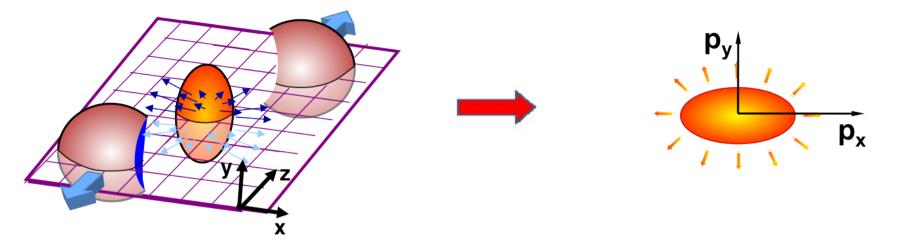
Lenticular overlapping region \rightarrow space anisotropy \rightarrow momentum space anisotropy



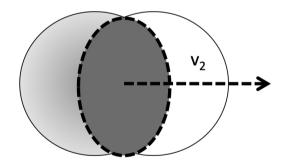
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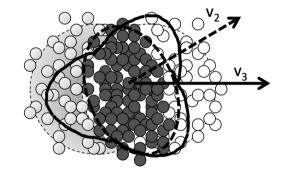


System symmetry \rightarrow elliptic flow



Lenticular overlapping region \rightarrow space anisotropy \rightarrow momentum space anisotropy





System symmetry \rightarrow elliptic flow

Fluctuations \rightarrow non-zero higher order flow

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➢ Particle distribution over azimuthal angle:

$$\frac{dN}{d\phi} \propto 1 + \sum_{n} 2v_n \cos[n(\phi - \Psi_n)]$$

- > v_n coefficients driven by:
 - ♦ Initial geometry;
 - Medium properties.

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 - ◆ Mixed order harmonics,
 - Symmetric cumulant.

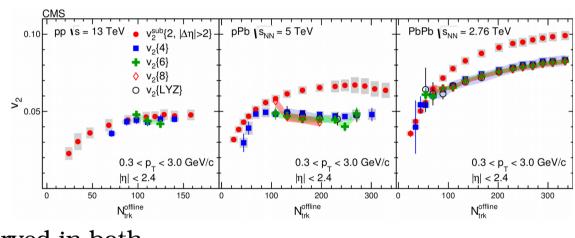
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PLB 765 (2017) 193

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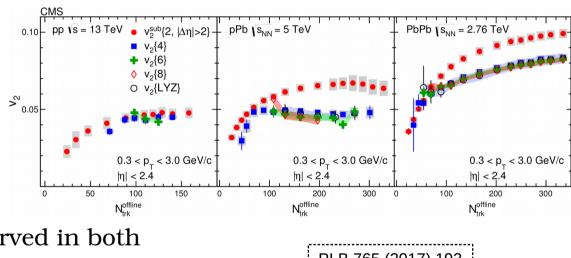
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2.Do the flow correlations can give us better understanding of collectivity in small systems?

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1.Can flow harmonic correlations give us additional constraints?



PLB 765 (2017) 193

> Azimuthal distribution one can write: $P(\phi) = \frac{1}{2\pi} \sum_{n=-\infty}^{+\infty} V_n e^{-in\phi}$ where $V_n \equiv v_n e^{in\Psi_n}$

> The response is <u>linear</u> ($v_n = k_n \epsilon_n$) for n=2,3.

> For higher harmonics (n > 3) there are both, linear and <u>nonlinear</u> part:

$$V_{4} = V_{4L} + \chi_{422}(V_{2})^{2}$$

$$V_{5} = V_{5L} + \chi_{523}V_{2}V_{3}$$

$$V_{6} = V_{6L} + \chi_{6222}(V_{2})^{3} + \chi_{633}(V_{3})^{2}$$

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Phys.Lett. B 744 (2015) 82

Milan Stojanovic

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Phys.Lett. B 744 (2015) 82
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Phys.Lett. B 744 (2015) 82
Linear response (from ε_{n}) Nonlinear response (from $\varepsilon_{2}, \varepsilon_{3}$)

▷ Non linear part can be studied from flow harmonics measured with respect to the lower order event planes (mixed order harmonics): $v_4\{\Psi_{22}\}, v_5\{\Psi_{23}\}, v_6\{\Psi_{33}\}, v_6\{\Psi_{222}\}, v_7\{\Psi_{223}\}, where, for example, v_5\{\Psi_{23}\}$ is:

$$v_{5}\{\Psi_{23}\} \equiv \frac{Re \langle V_{5}V_{2}^{*}V_{3}^{*} \rangle}{\sqrt{\langle |V_{2}|^{2} |V_{3}|^{2} \rangle}} \text{, and nonlinear response coefficient:} \quad \chi_{523} = \frac{v_{5} \{\Psi_{23}\}}{\sqrt{\langle v_{2}^{2}v_{3}^{2} \rangle}}$$

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Standard scalar product approach (linear + nonlinear part):

$$\boxed{v_n\{\Psi_n\}} \equiv \frac{Re\langle V_n V_n^* \rangle}{\sqrt{\langle |V_n|^2 \rangle}} = \frac{\langle v_n v_n \cos(n\Psi_n - n\Psi_n) \rangle}{\sqrt{\langle v_n^2 \rangle}} = \sqrt{\langle v_n^2 \rangle}$$

$$\underbrace{v_n \text{measured with respect to their own event plane } (\Psi_n)}$$

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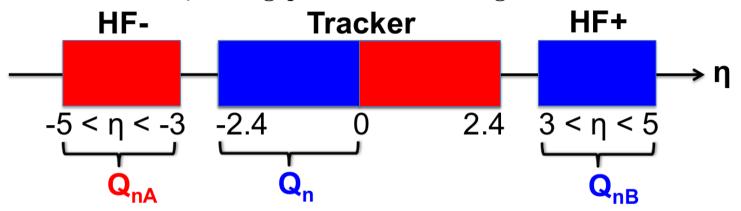
≻ Nonlinear response coefficient:

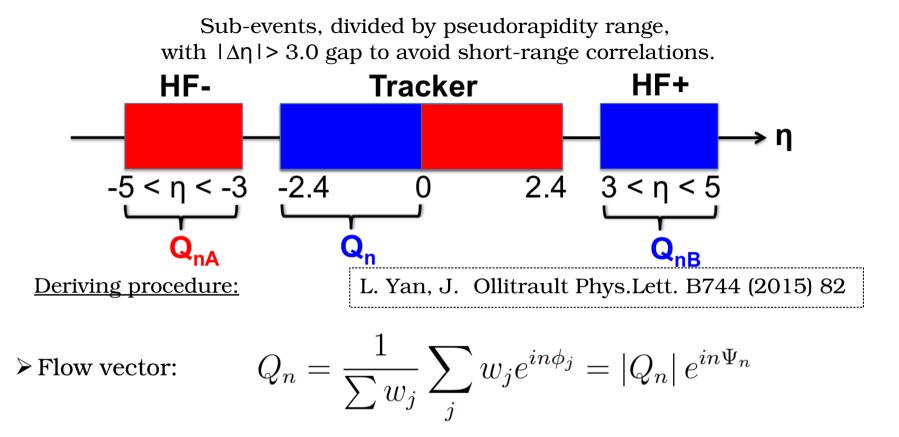
$$\chi_{523} = \frac{Re\langle V_5 V_2^* V_3^* \rangle}{\langle |V_2|^2 |V_3|^2 \rangle} = \frac{\langle v_5 v_2 v_3 \cos(5\Psi_5 - 2\Psi_2 - 3\Psi_3) \rangle}{\langle v_2^2 v_3^2 \rangle} = \frac{v_5 \{\Psi_{23}\}}{\sqrt{\langle v_2^2 v_3^2 \rangle}}$$

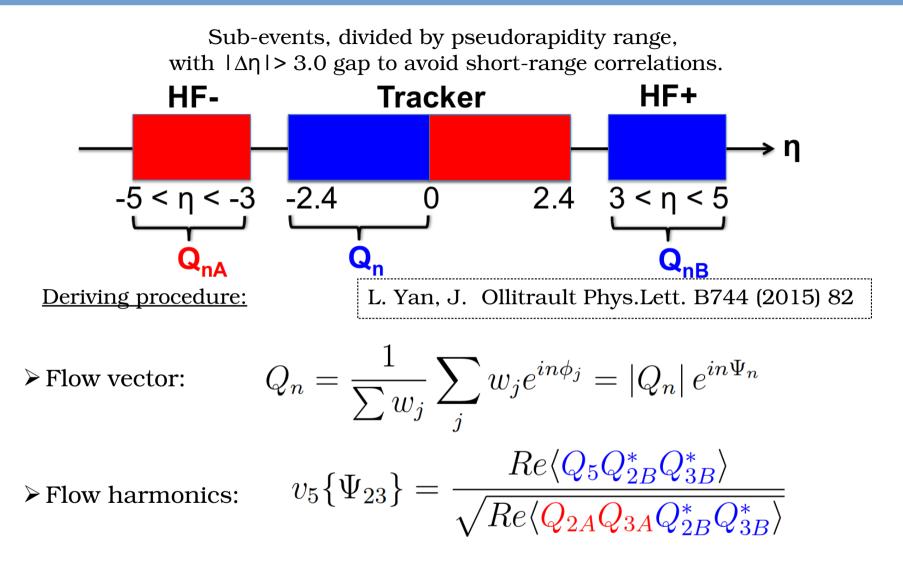
Milan Stojanovic

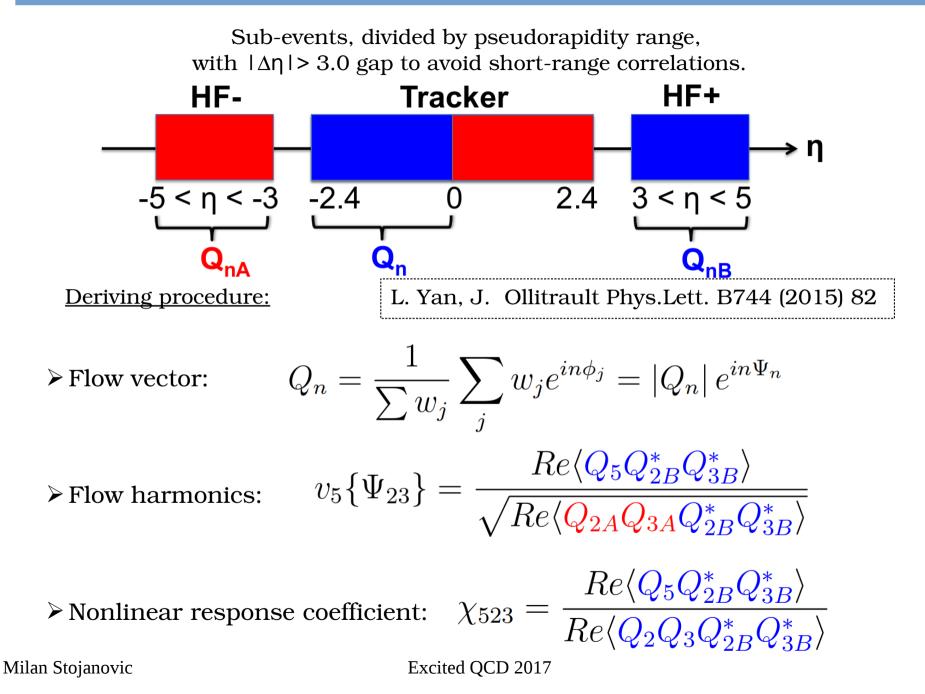
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Sub-events, divided by pseudorapidity range, with $|\Delta \eta| > 3.0$ gap to avoid short-range correlations.







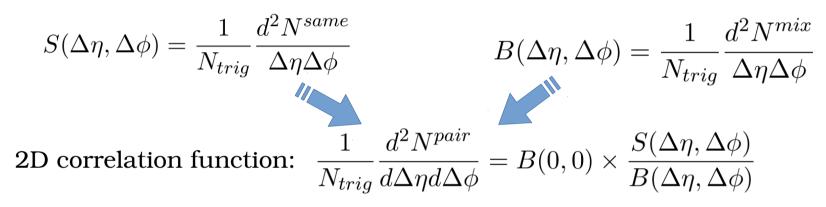


Two-particle correlations

> For $v_n \{\Psi_n\}$ measurement two-particle correlation method has been used.

1. Signal distribution:

2. Background distribution:

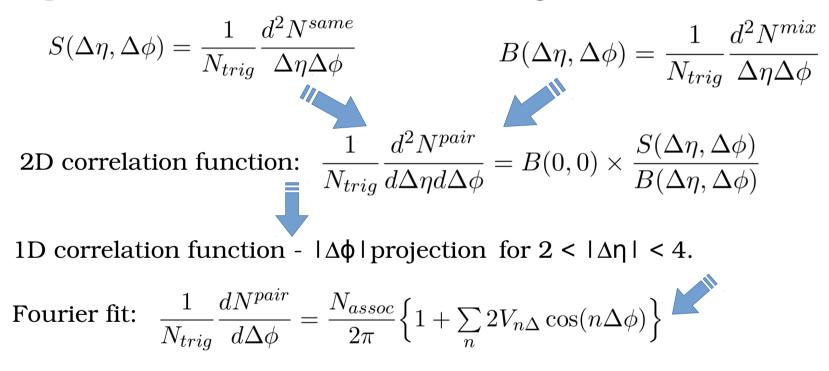


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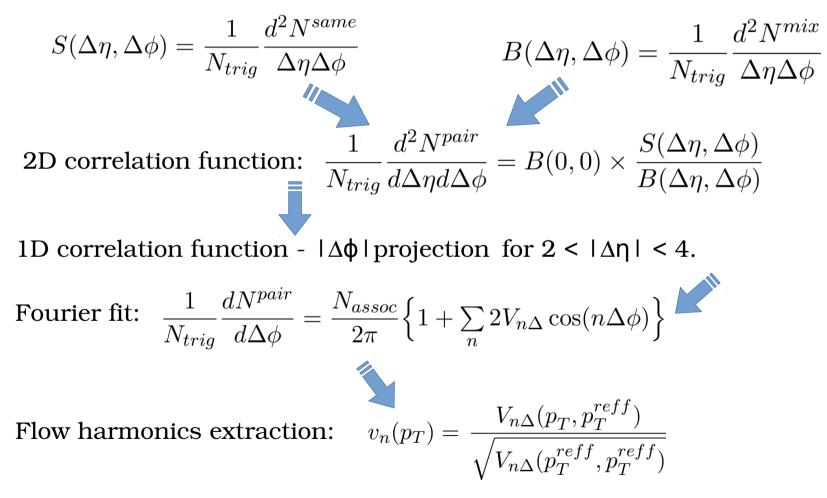


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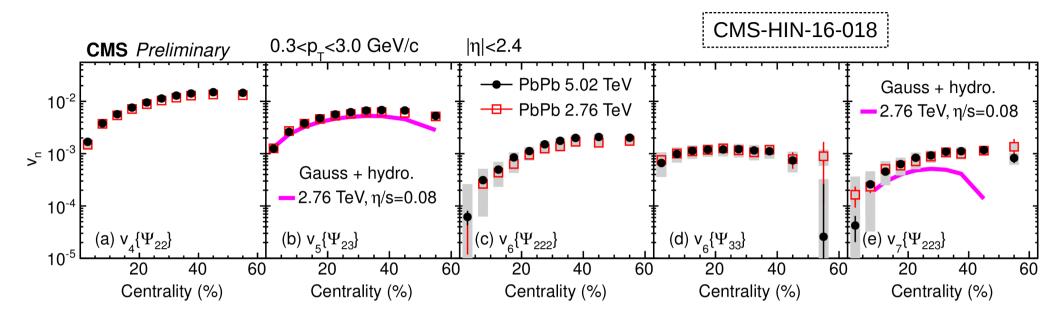
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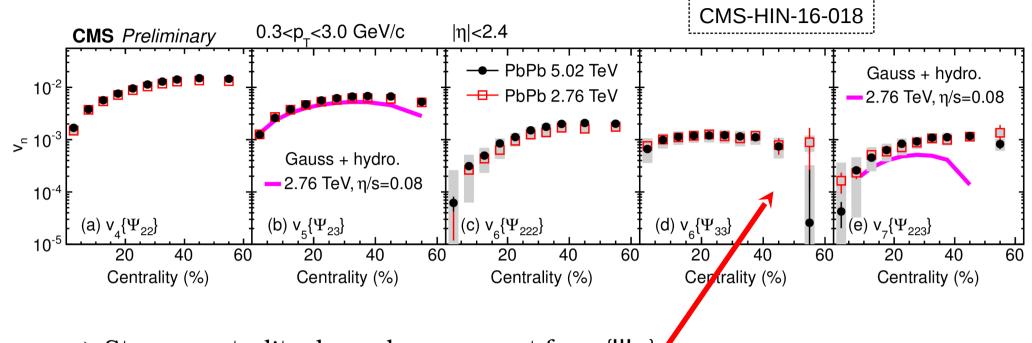
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Mixed order harmonics vs centrality



L. Yan, J. Ollitrault Phys.Lett. B744 (2015) 82

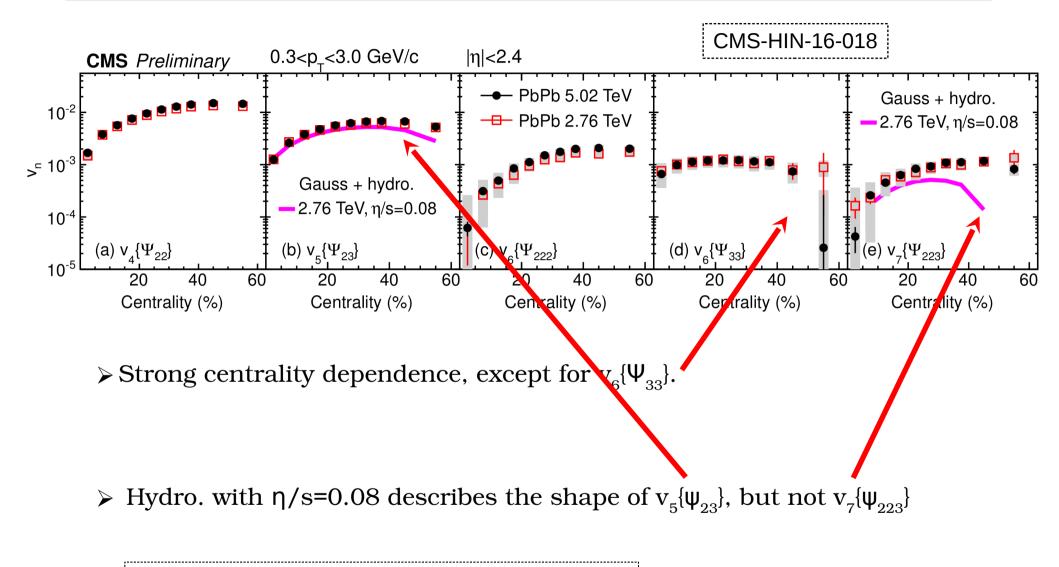
Mixed order harmonics vs centrality



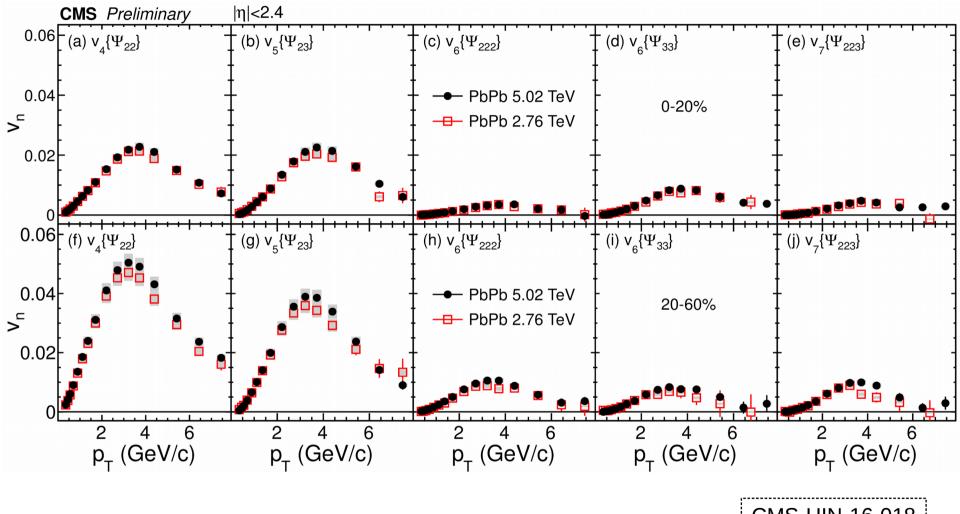
> Strong centrality dependence, except for $v_6^{\{\Psi_{33}\}}$.

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Mixed order harmonics vs centrality

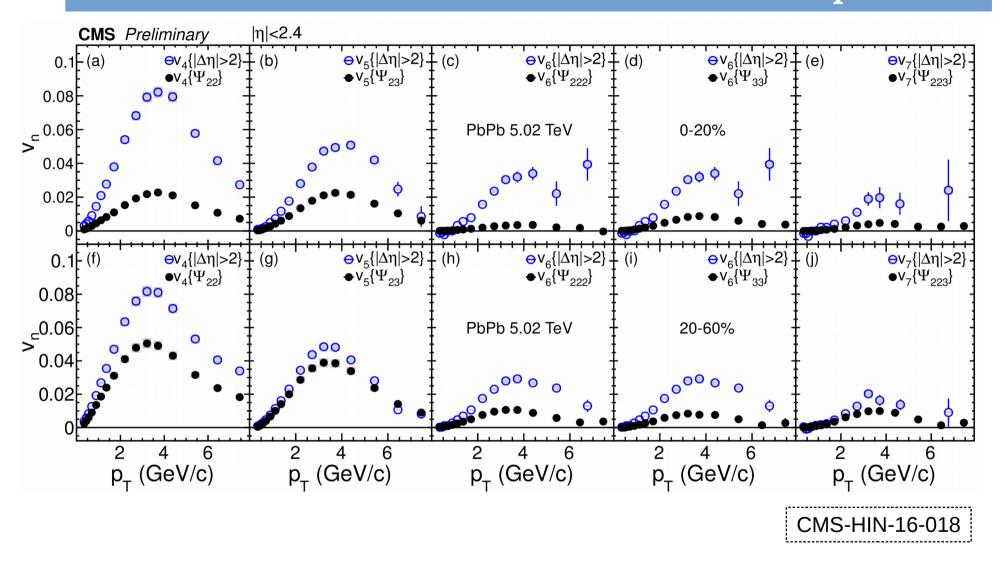


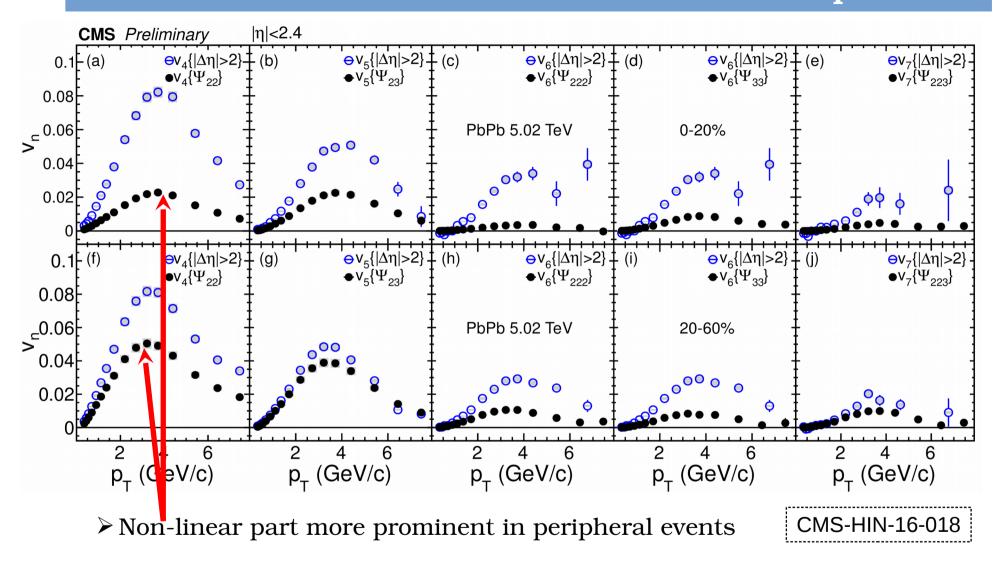
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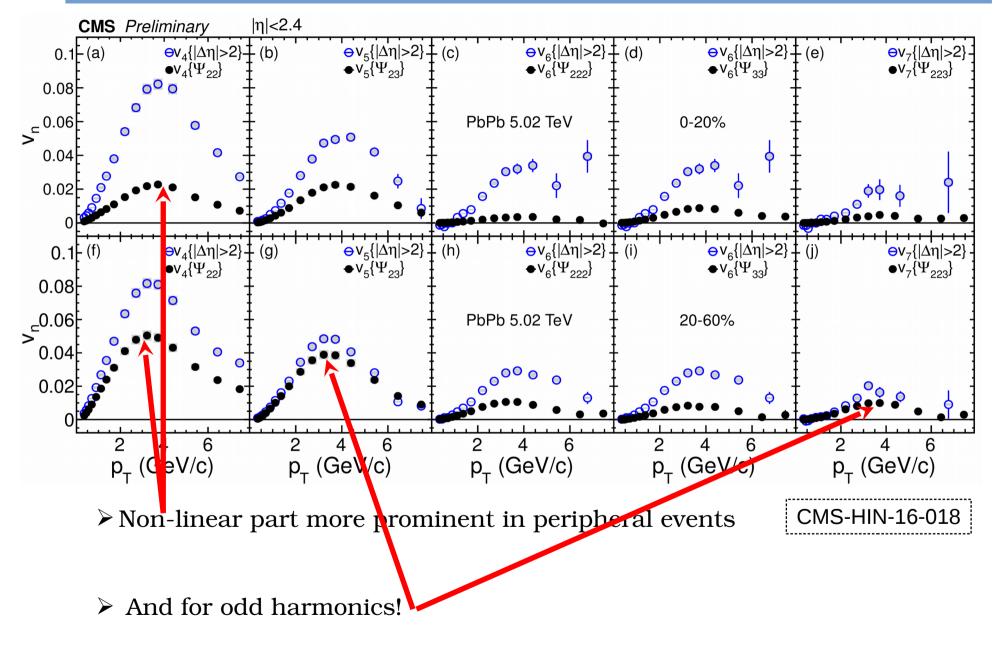


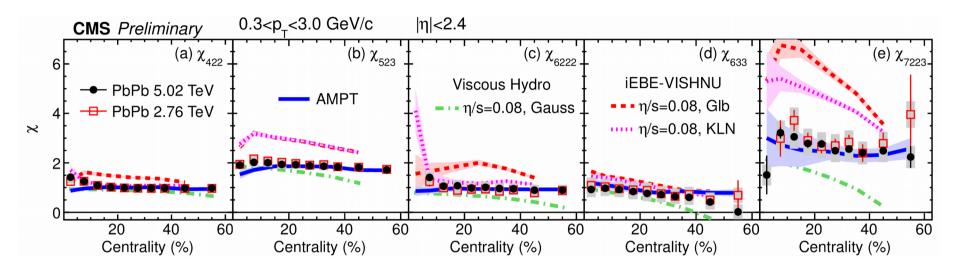
 \succ No strong energy dependence.

CMS-HIN-16-018





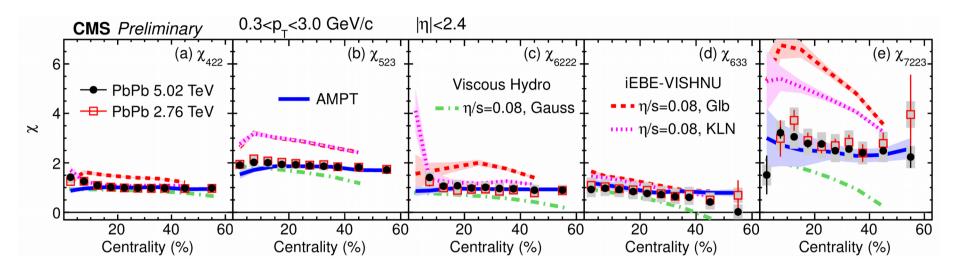




CMS-HIN-16-018

L. Yan, S. Pal, J. Ollitrault, Nucl. Phys. A956 (2016) 340

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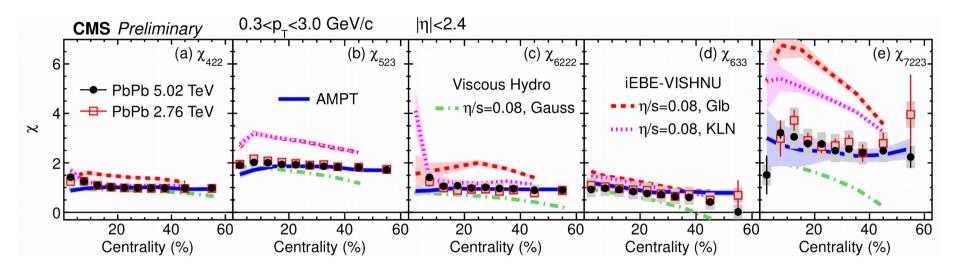


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CMS-HIN-16-018

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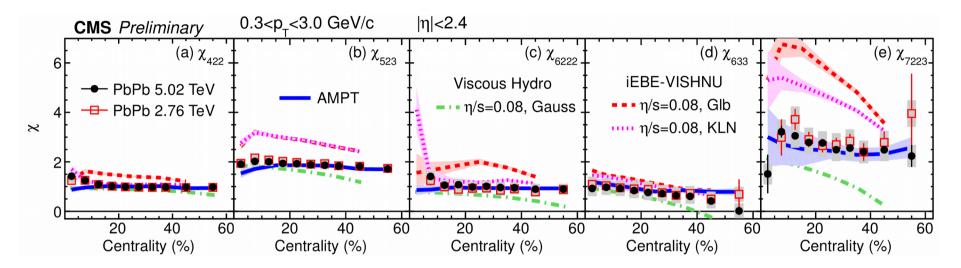
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≻ AMPT favored by data.

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CMS-HIN-16-0



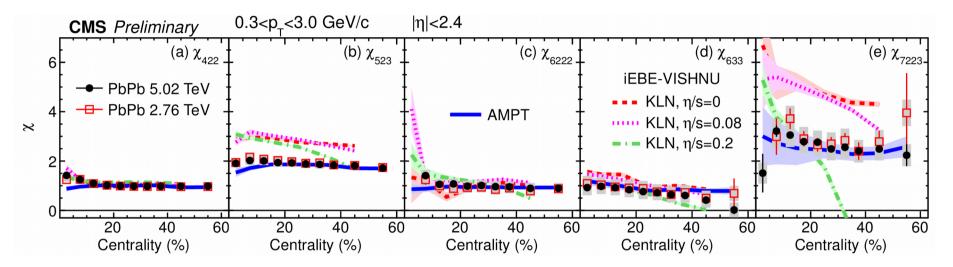
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- Sensitivity to the:
 - ✗ initial conditions

L. Yan, S. Pal, J. Ollitrault, Nucl. Phys. A956 (2016) 340

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CMS-HIN-16-0



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- Sensitivity to the:
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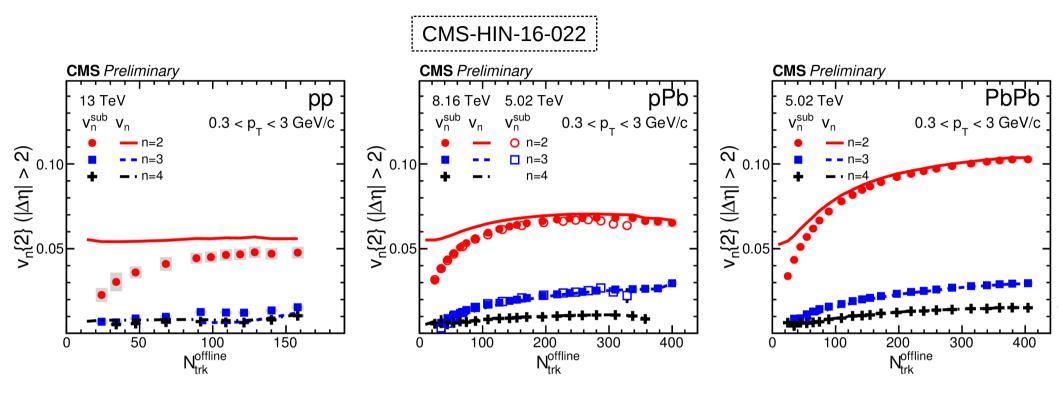
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CMS-HIN-16-0

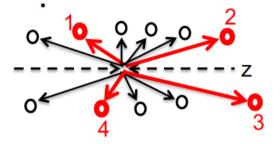
Flow in small systems



 \succ Similar pattern in all systems.

> Weak energy dependence in pPb collisions.

New observable, based on 4-particle cumulant technique, developed by ALICE.



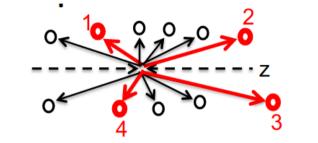
Diagonal terms:

$$\langle \langle 4 \rangle \rangle_{n,n} \equiv \left\langle \left\langle \cos \left[n \left(\phi_1 + \phi_2 - \phi_3 - \phi_4 \right) \right] \right\rangle \right\rangle$$

Non-diagonal terms:

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Symmetric cumulant:

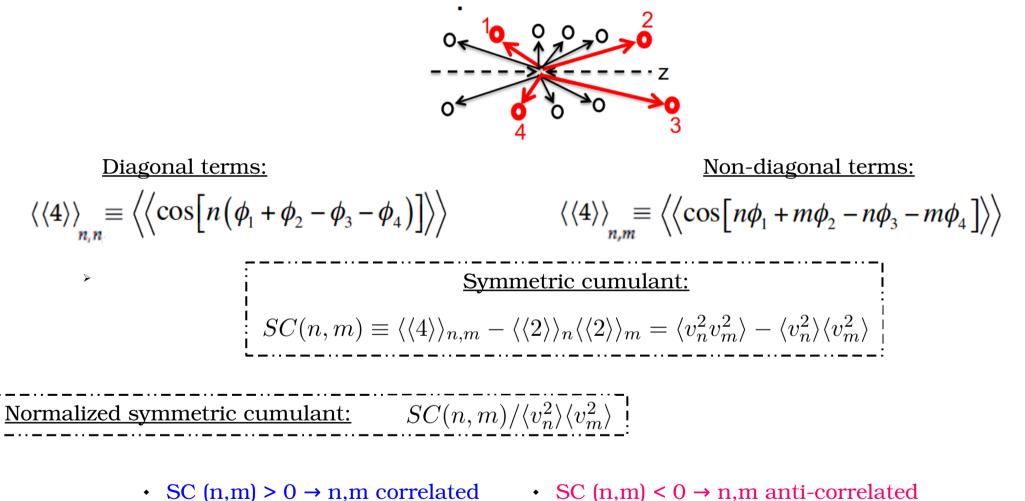
$$SC(n,m) \equiv \langle \langle 4 \rangle \rangle_{n,m} - \langle \langle 2 \rangle \rangle_n \langle \langle 2 \rangle \rangle_m = \langle v_n^2 v_m^2 \rangle - \langle v_n^2 \rangle \langle v_m^2 \rangle$$

• SC $(n,m) > 0 \rightarrow n,m$ correlated • SC $(n,m) < 0 \rightarrow n,m$ anti-correlated

• SC (n,m) =
$$0 \rightarrow$$
 no correlations

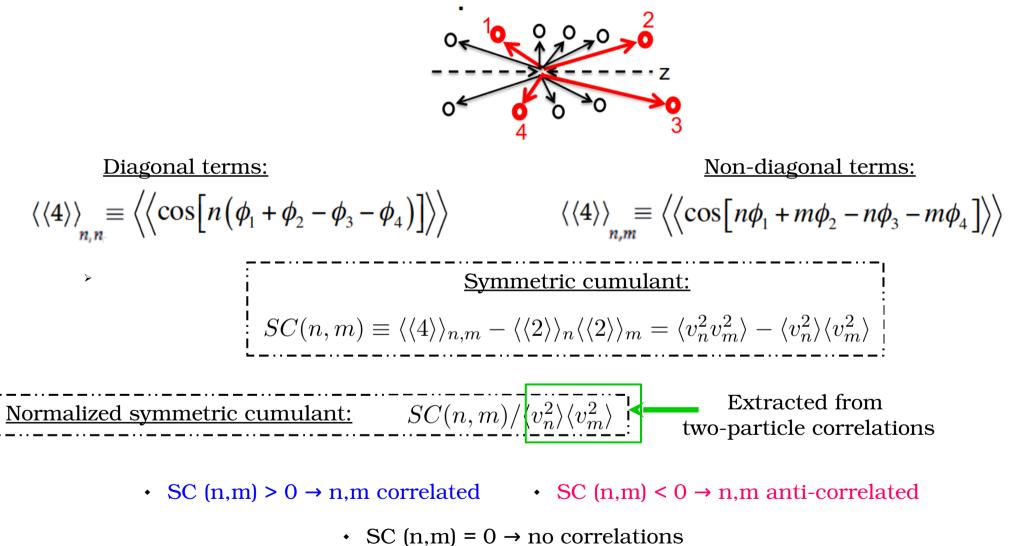
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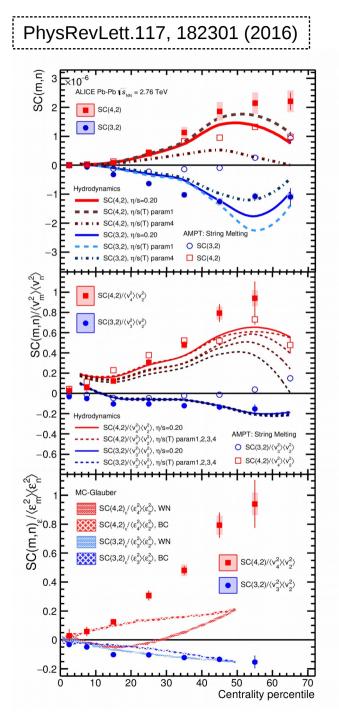
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 \succ Flow harmonics correlations:

- × SC(4,2) < 0 → $v_2 \& v_4$ correlated!
- × SC(3,2) < 0 → $v_2 \& v_3$ anticorrelated!

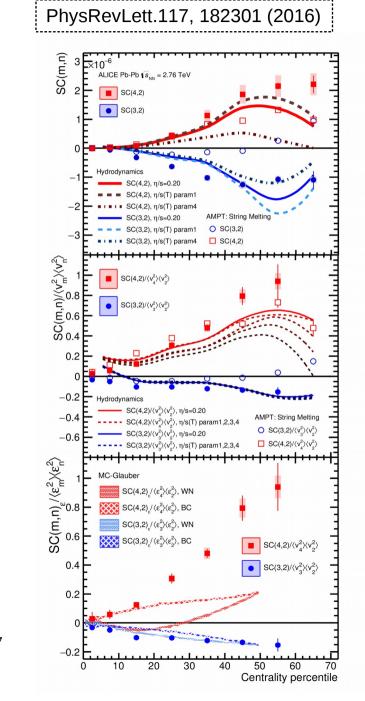


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- > SC(n,m) normalized by $\langle v_2 \rangle \langle v_m \rangle$:
 - Normalized SC(4,2) depends on both IS and medium response;
 - x Normalized SC(3,2) depends only on initial state (IS) fluctuations!



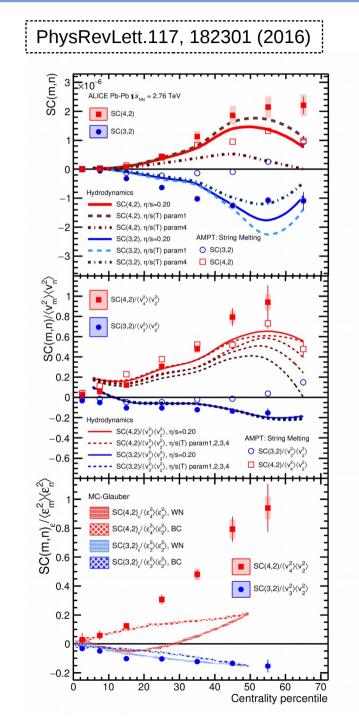
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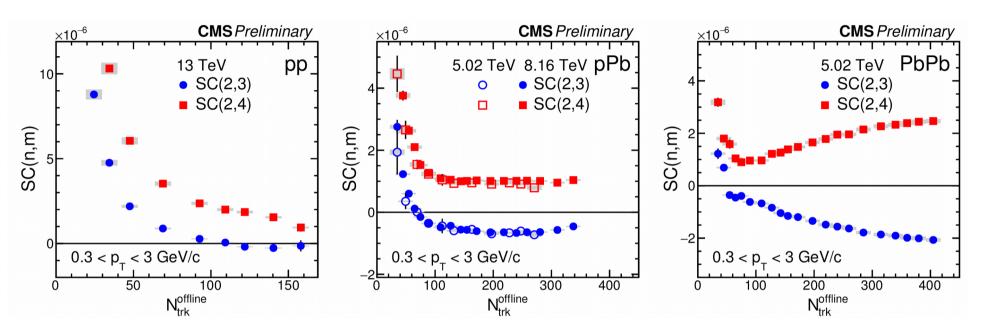
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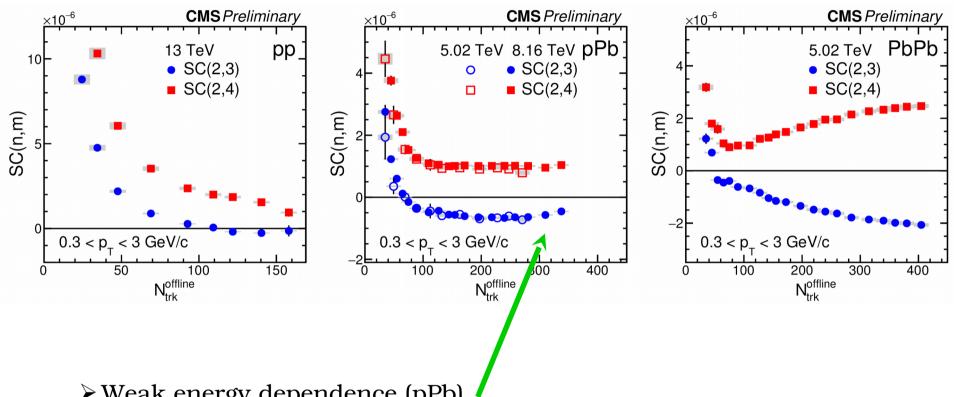
SC – results

CMS-HIN-16-022



SC – results

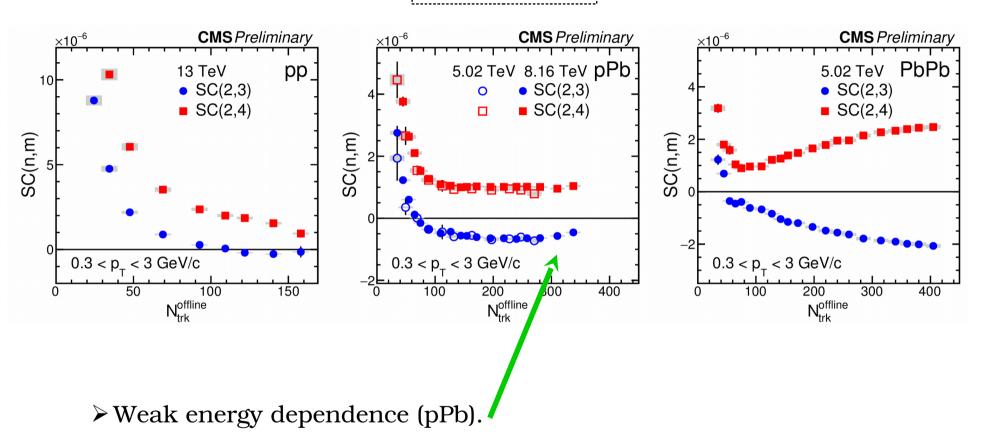
CMS-HIN-16-022



> Weak energy dependence (pPb).

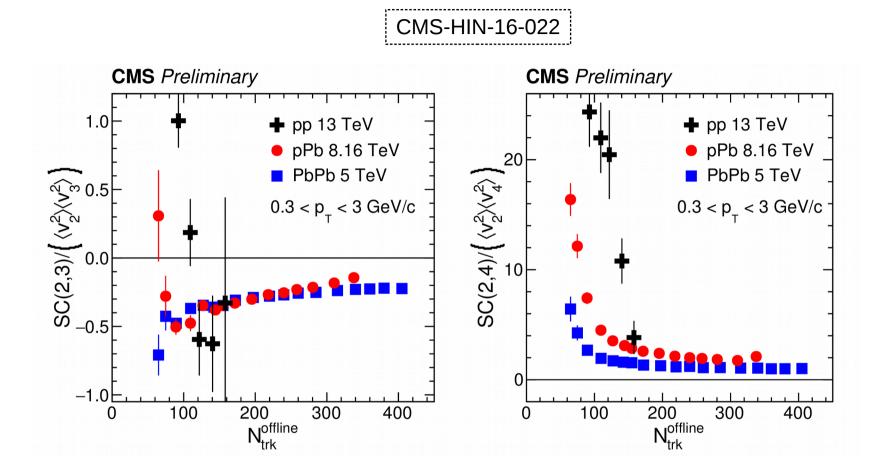
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CMS-HIN-16-022

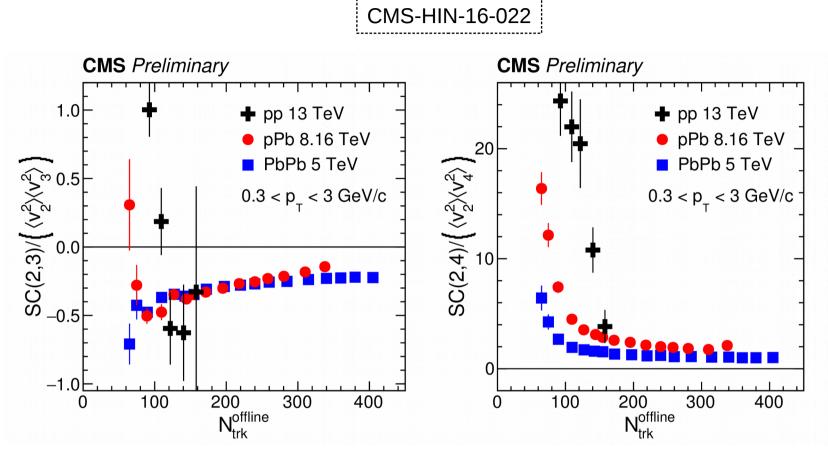


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Normalized SC – results

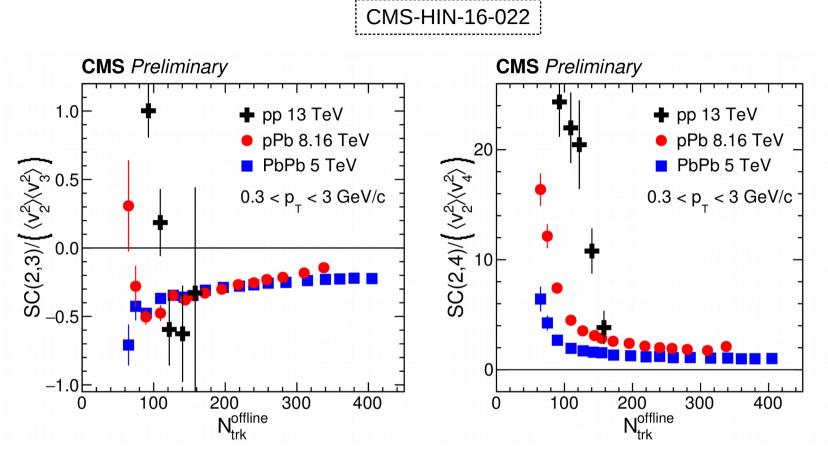


Normalized SC – results



For pPb and PbPb, similar behavior for normalized SC(2,3)
 Suggests similar IS conditions.

Normalized SC – results



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 Suggests similar IS conditions.

Ordering observed for normalized SC(2,4): pp > pPb > PbPb
 May suggests different transport properties.

Summary

➢ Mixed order higher harmonics:

✓ Constraints on transport properties at the freeze-out in PbPb collisions.

Symmetric cumulant in different systems (pp, pPb, PbPb):

- ✓ Suggests <u>similar initial state fluctuation</u> contribution;
- ✓ And may suggest <u>different transport properties</u>.