

Hadronization of highly virtual partons: perturbative vs nonperturbative scenarios

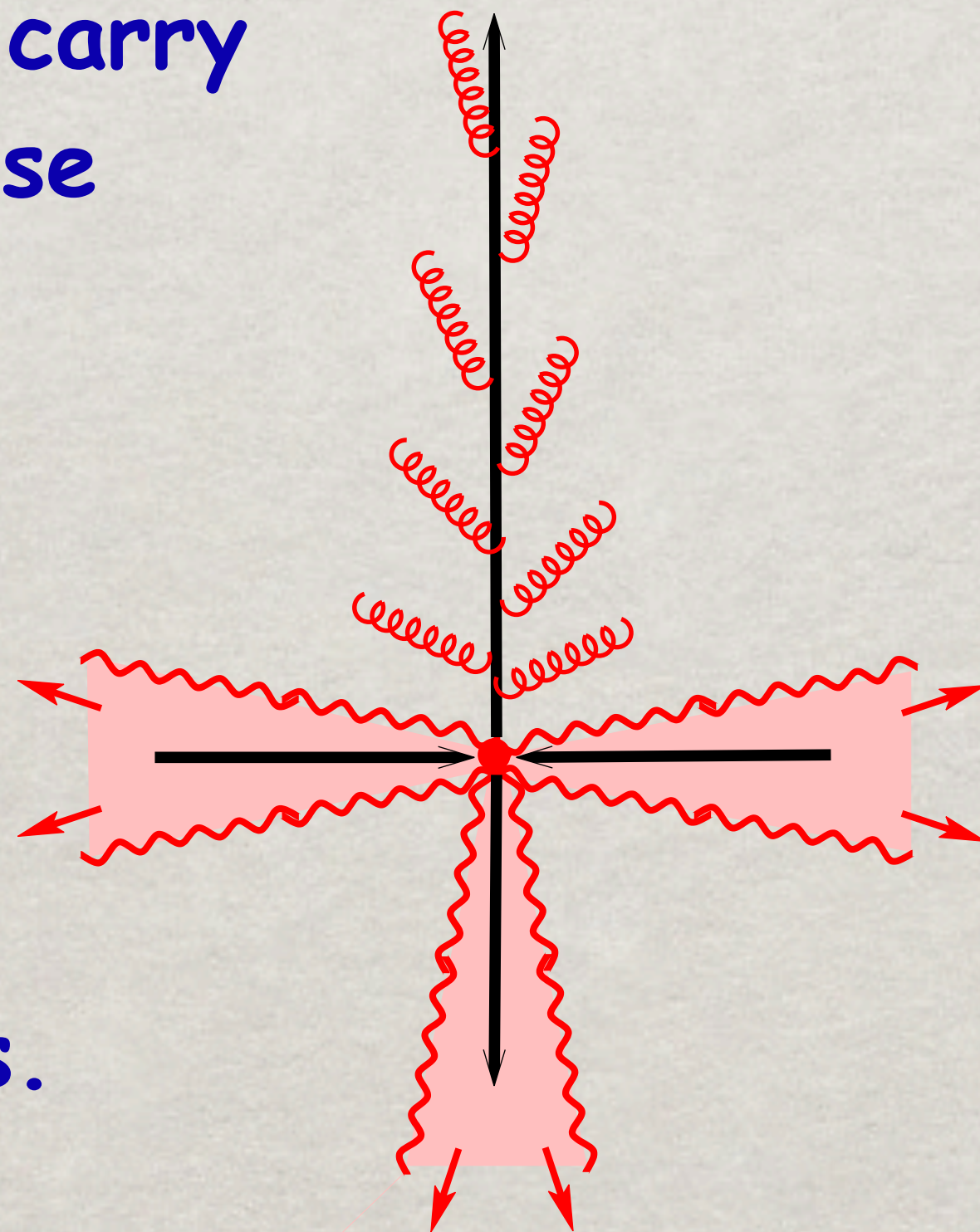
Boris Kopeliovich
Valparaiso

Hard parton collision

High-pt parton scattering leads to formation of **4** cones of gluon radiation:

- (i) the color field of the colliding partons is **shaken off** in forward-backward directions.
- (ii) the scattered partons carry **no field** up to transverse momenta $kt < pt$.

The final state partons are **regenerating** the lost color field by radiating gluons and forming the up-down jets.



The coherence length/time of gluon radiation

$$l_c = \frac{2E x(1-x)}{k_T^2 + x^2 m_q^2} \approx \frac{2\omega}{k_T^2}$$

First are radiated gluons with small longitudinal and large transverse momenta.

Vacuum energy loss

How much energy is radiated over the path length L ?

$$\Delta E(L) = E \int_{\Lambda^2}^{Q^2} dk^2 \int_0^1 dx x \frac{dn_g}{dx dk^2} \Theta(L - l_c)$$

$$\frac{dn_g}{dx dk^2} = \frac{2\alpha_s(k^2)}{3\pi x} \frac{k^2 [1 + (1-x)^2]}{[k^2 + x^2 m_q^2]^2}$$

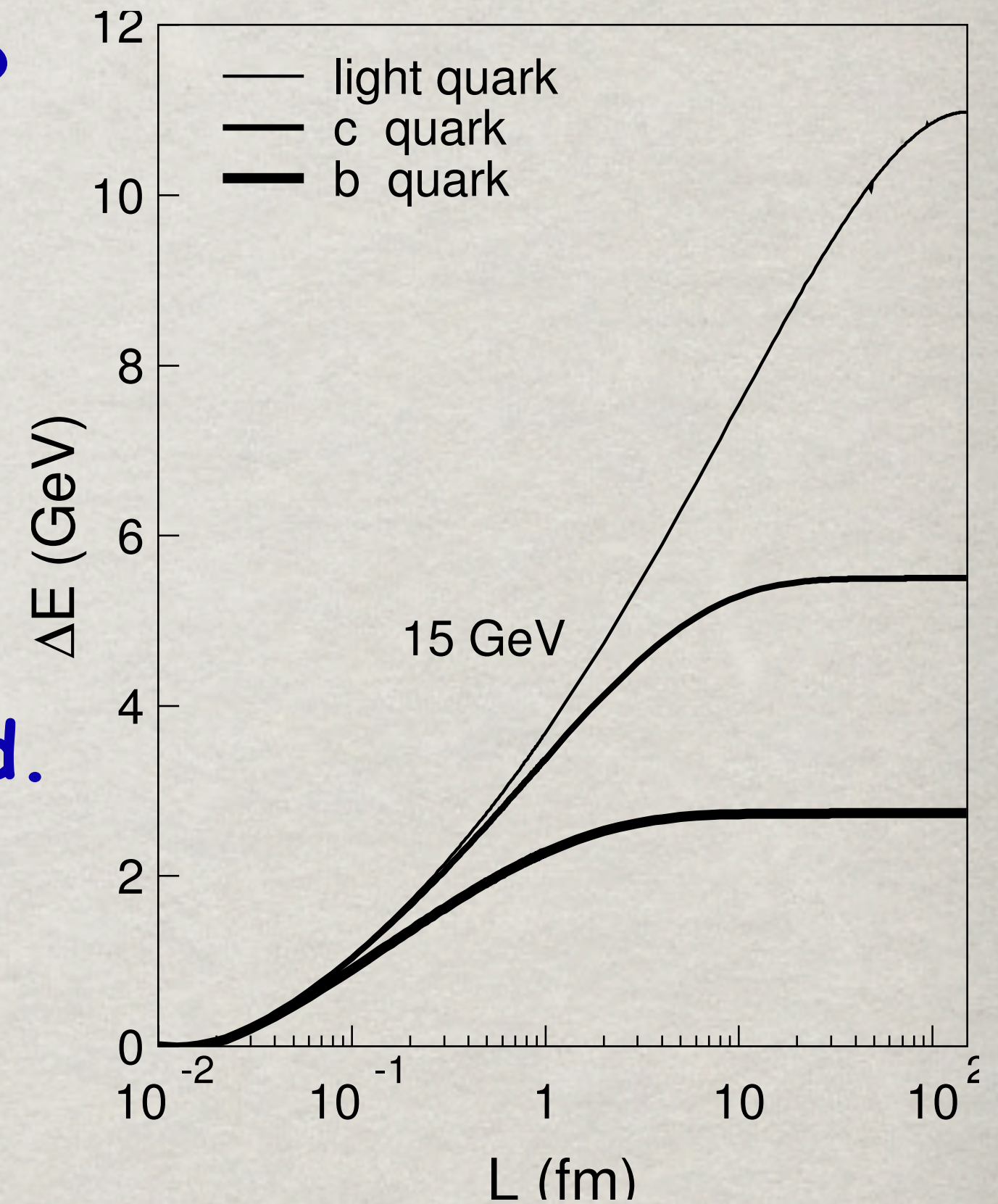
Dead-cone effect: gluons with $k^2 < x^2 m_q^2$ are suppressed.
Heavy quarks radiate less energy than the light ones.

Another dead cone: soft gluons cannot be radiated at short path length

$$k^2 > \frac{2Ex(1-x)}{L} - x^2 m_q^2$$

This is why **heavy and light** quarks radiate with **similar rates**

at short time scales $L \lesssim \frac{Ex(1-x)}{x^2 m_q^2}$



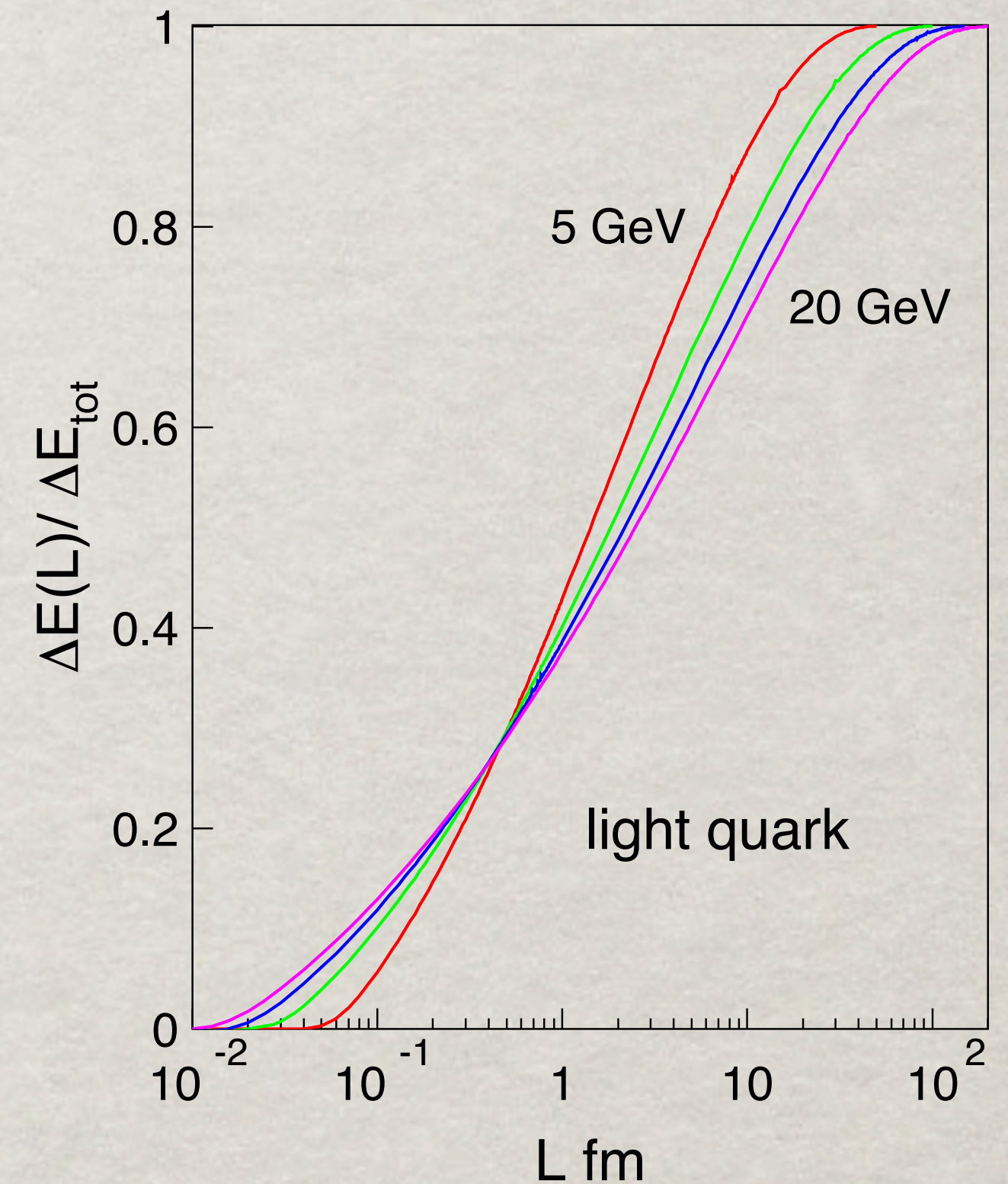
B.K., I.Potashnikova, I.Schmidt,
PRC 82(2010)037901

How fast is energy dissipation?

A light quark loses **40%** of the total radiated energy during the first **1fm**.

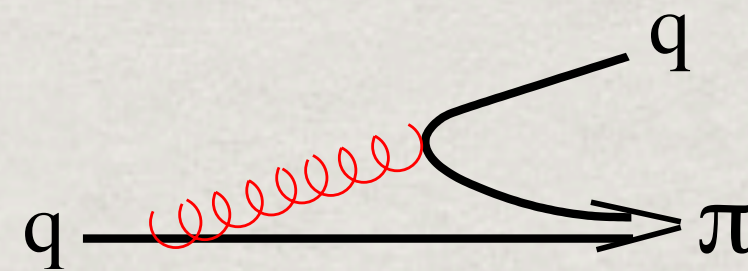
Energy conservation imposes severe restrictions on the **production** length l_p for hadrons with large fractional momentum z_h .

- Gluons with $x > 1 - z_h$ are forbidden, This leads to Sudakov suppression
- The hadron cannot be produced after the parton momentum falls below p_T , i.e. $\Delta E/E > 1 - z_h$



Hadronization in vacuum

Perturbative hadronization at large z

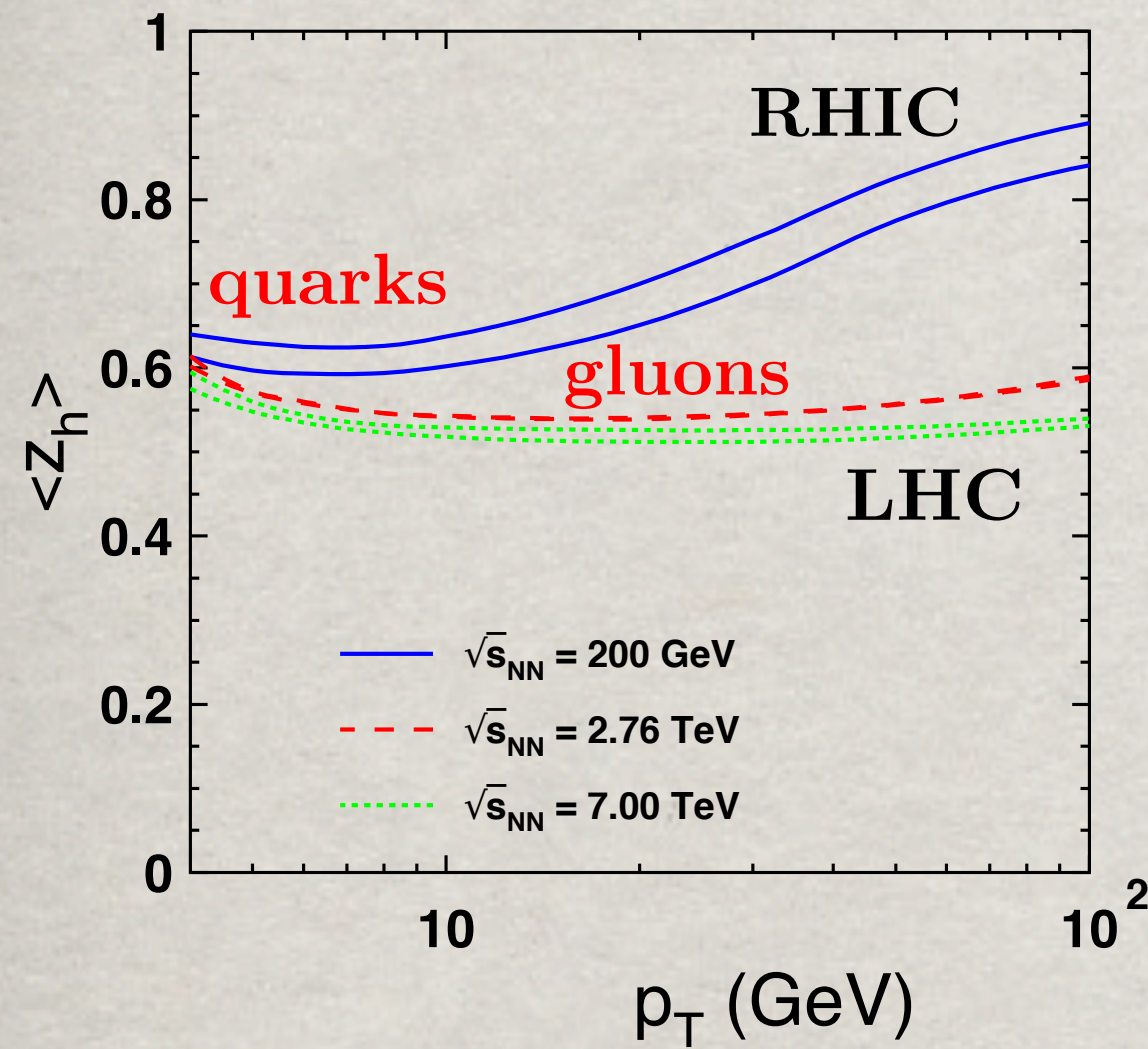


E. Berger, PLB 89(1980)241

B.K., H.J.Pirner, I.Schmidt, A.Tarasov
PRD 77(2008)054004

B.K., H.J.Pirner, I.Potashnikova, I.Schmidt,
PLB 662(2008)117

The mean value $\langle z_h \rangle$

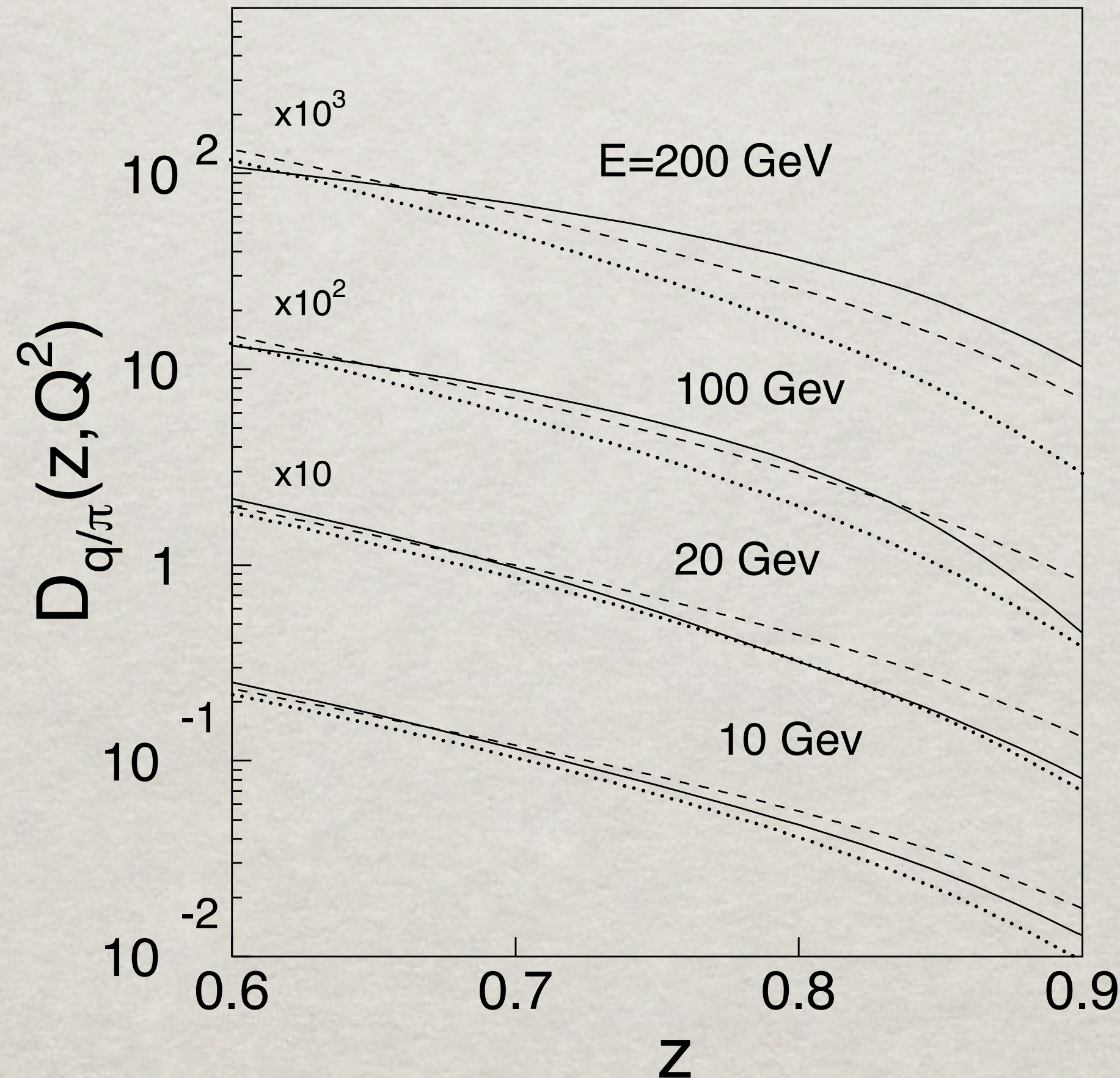


Production of heavy flavored mesons occur with larger z_h

$$\langle z_D \rangle = 0.76$$

$$\langle z_B \rangle = 0.89$$

$$(\sqrt{s} = 7 \text{ TeV})$$



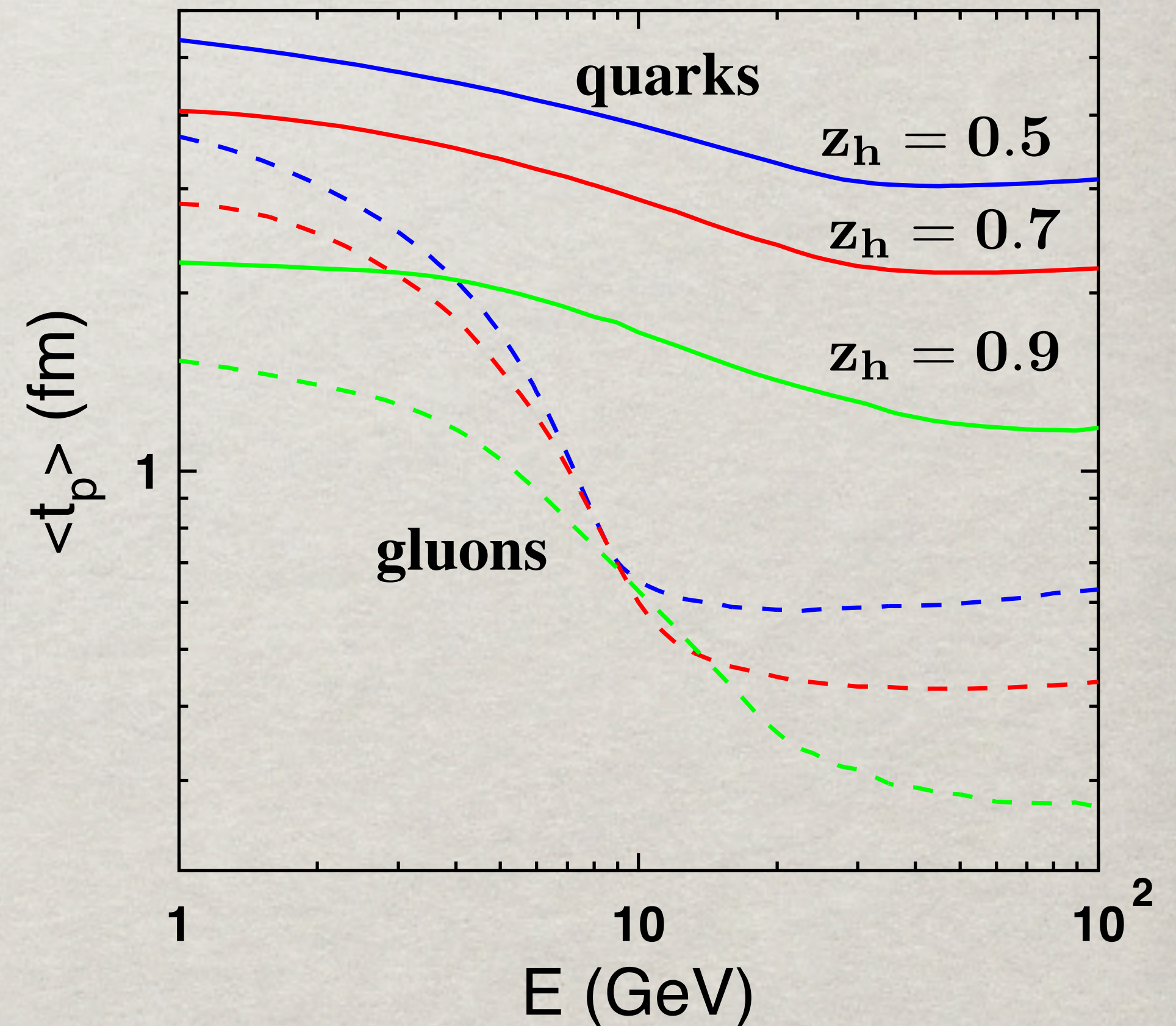
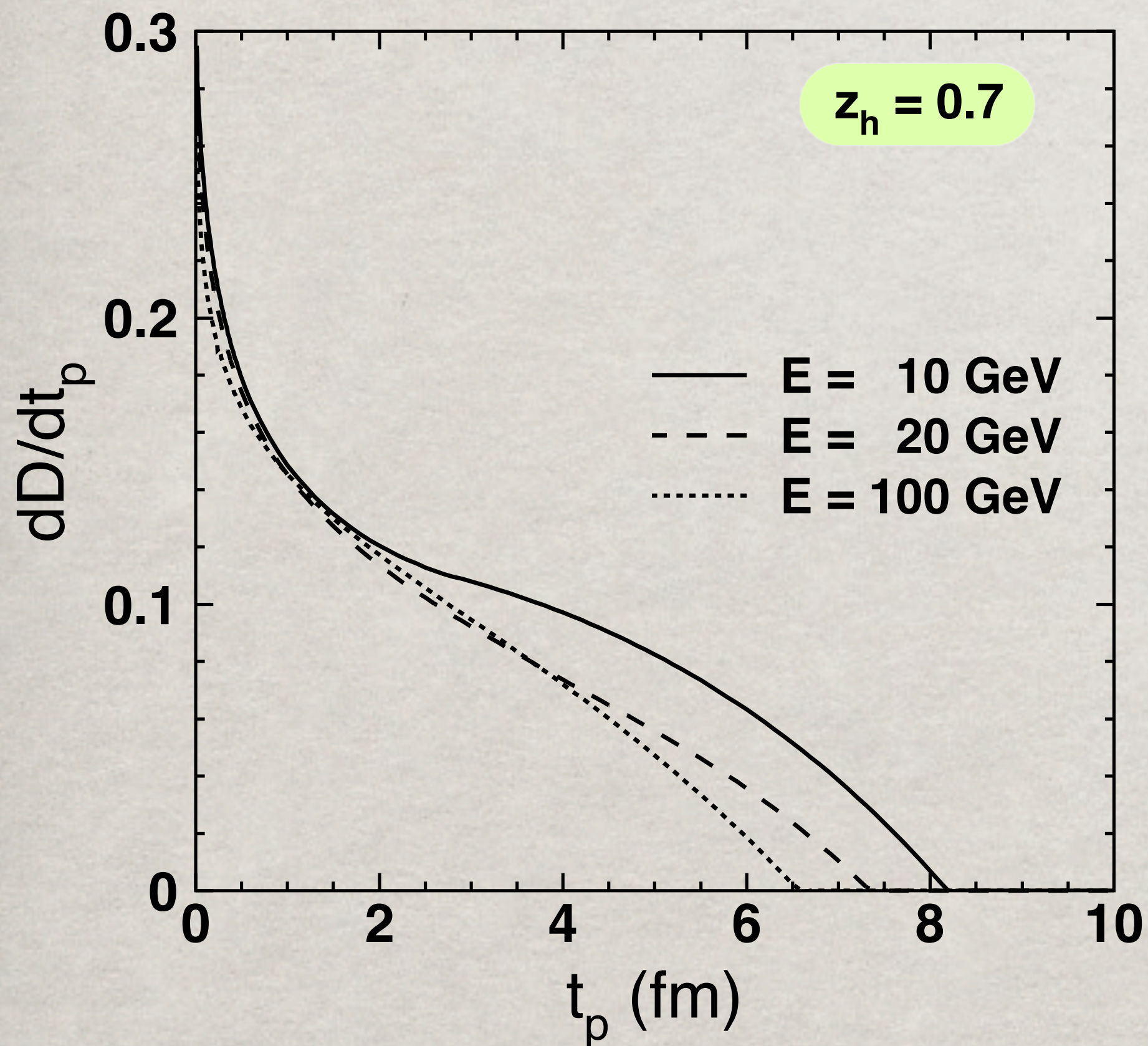
Test vs KKP and BKK:

Production time/length

t_p -dependent fragmentation function

$$\frac{\partial D_{\pi/q}(z_h, \mathbf{E})}{\partial t_p}$$

$$\langle t_p(z_h, \mathbf{E}) \rangle = \frac{1}{D_{\pi/q}} \int dt_p t_p \frac{\partial D_{\pi/q}(z_h, \mathbf{E}^2)}{\partial t_p}$$



Production time/length

Why the Lorentz factor does not make l_p longer at large p_T ?

Jet features depend on two parameters, the hard scale Q^2 and jet energy E .

For the leading hadron energy conservation constraint: $l_p \lesssim \frac{E}{dE/dl} (1 - z_h)$

Energy and scale dependences of l_p in **SIDIS**:

(i) Energy dependence at fixed Q^2

$\langle dE/dl \rangle$ is fixed, so $l_p \propto E$

(ii) Scale dependence at fixed energy

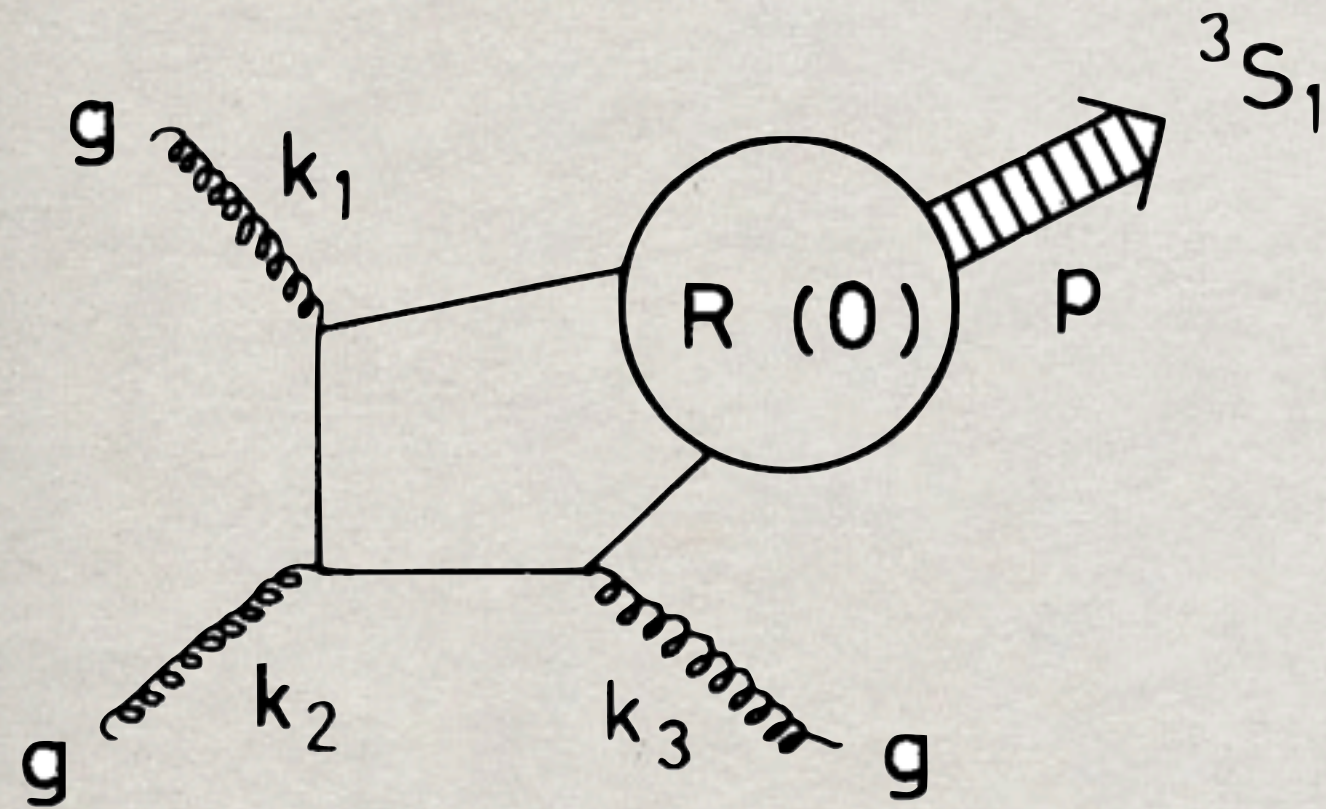
$\langle dE/dl \rangle$ rises with Q^2 , so $l_p(Q^2)$ is falling



Specifics of high- p_T jets: $E = p_T$; $Q^2 = p_T^2$

Charmonium with high p_T

Color singlet mechanism



E.Berger & D.Jones PRD 23(1981)1521

R.Baier & R.Ruckl PLB102(1981)364

collinear factorization

Ph.Hagler, R.Kirschner, A.Schaefer,

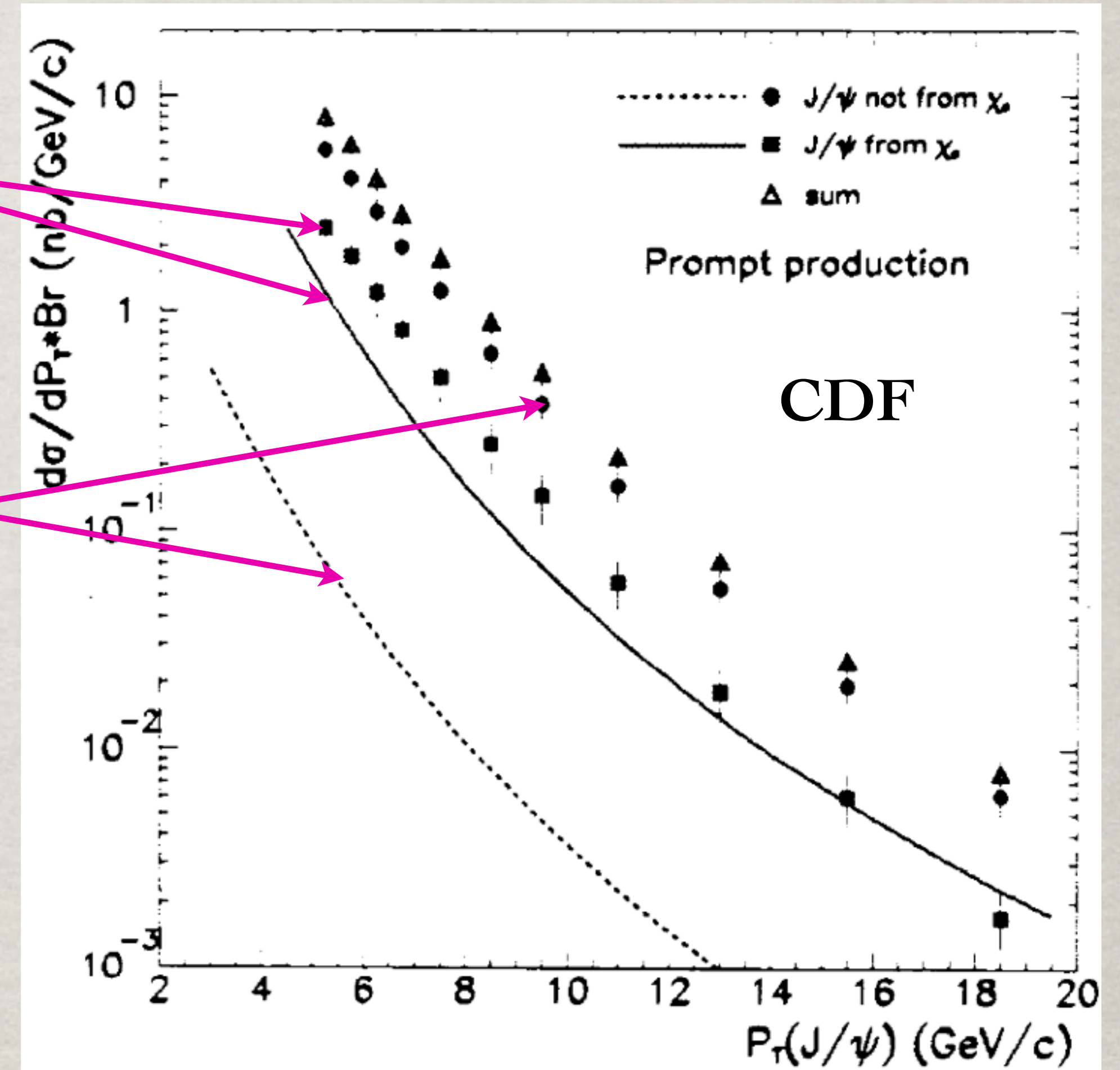
L.Szymanowski, O.Teryaev PRD63(2001)077501

k_T factorization should not be applied

at $k_T \sim p_T$

from χ

direct J/ψ



F. Abe et al., PRL 79(1997)572

Charmonium with high p_T

Color-singlet model fails, because the strong kick from the target breaks-up the c - \bar{c} pair.

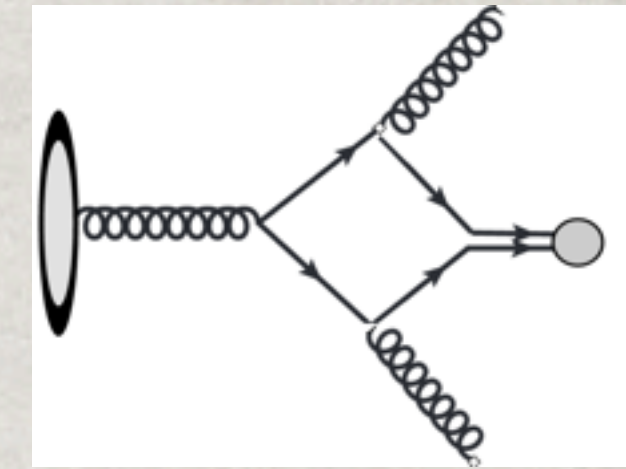
Color-octet model: the projectile gluon can easily accept a strong kick, and then fragment to J/ψ via production of a color-octet c - \bar{c} . Fragmentation is assumed to happen on a long time scale, by a soft mechanism, which cannot be calculated, but fitted.

However, we demonstrated that energy conservation restricts the time of color neutralization and the colorless c - \bar{c} dipole is produced promptly, in the perturbative regime. Therefore this contribution can be evaluated.



Gluon fragmentation

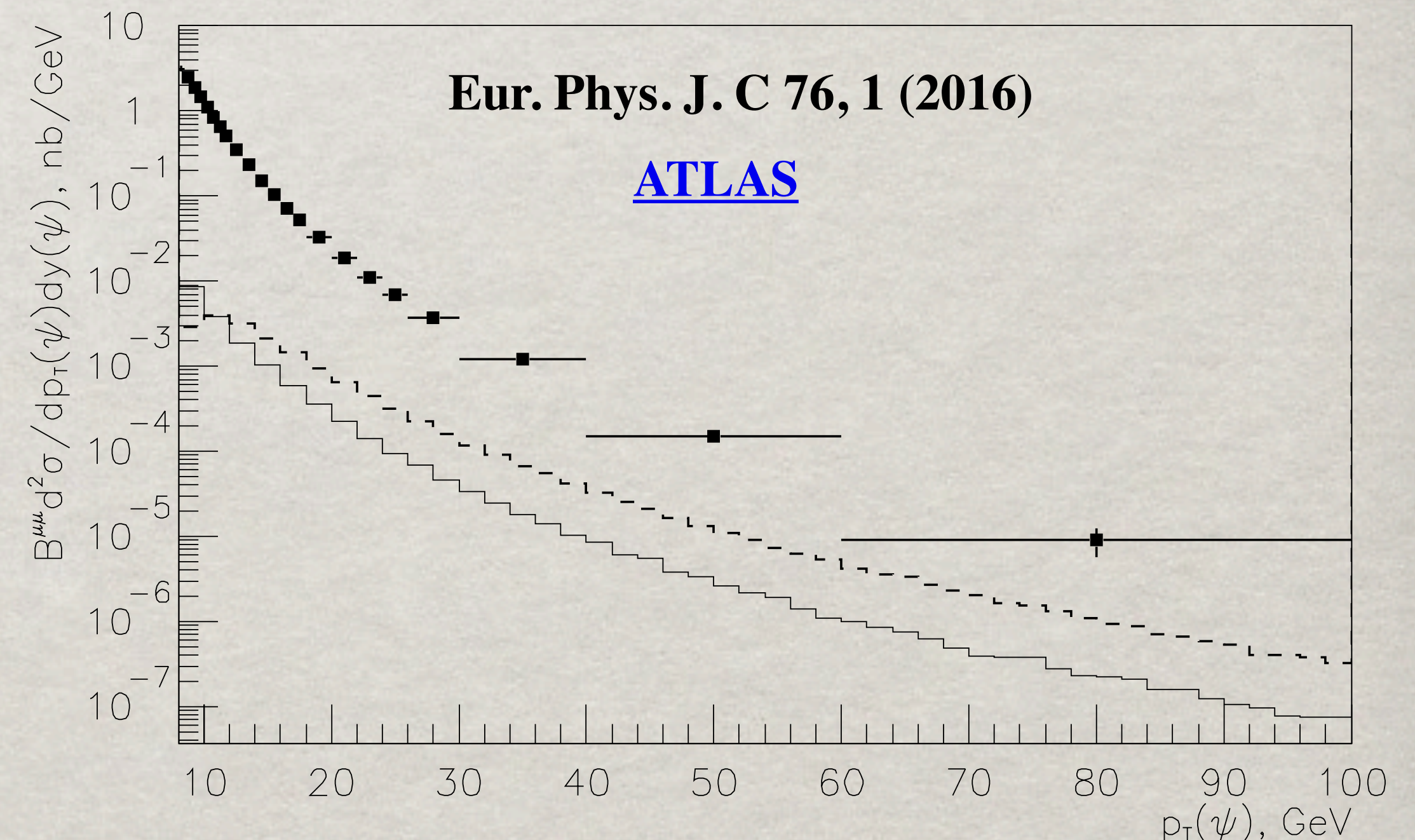
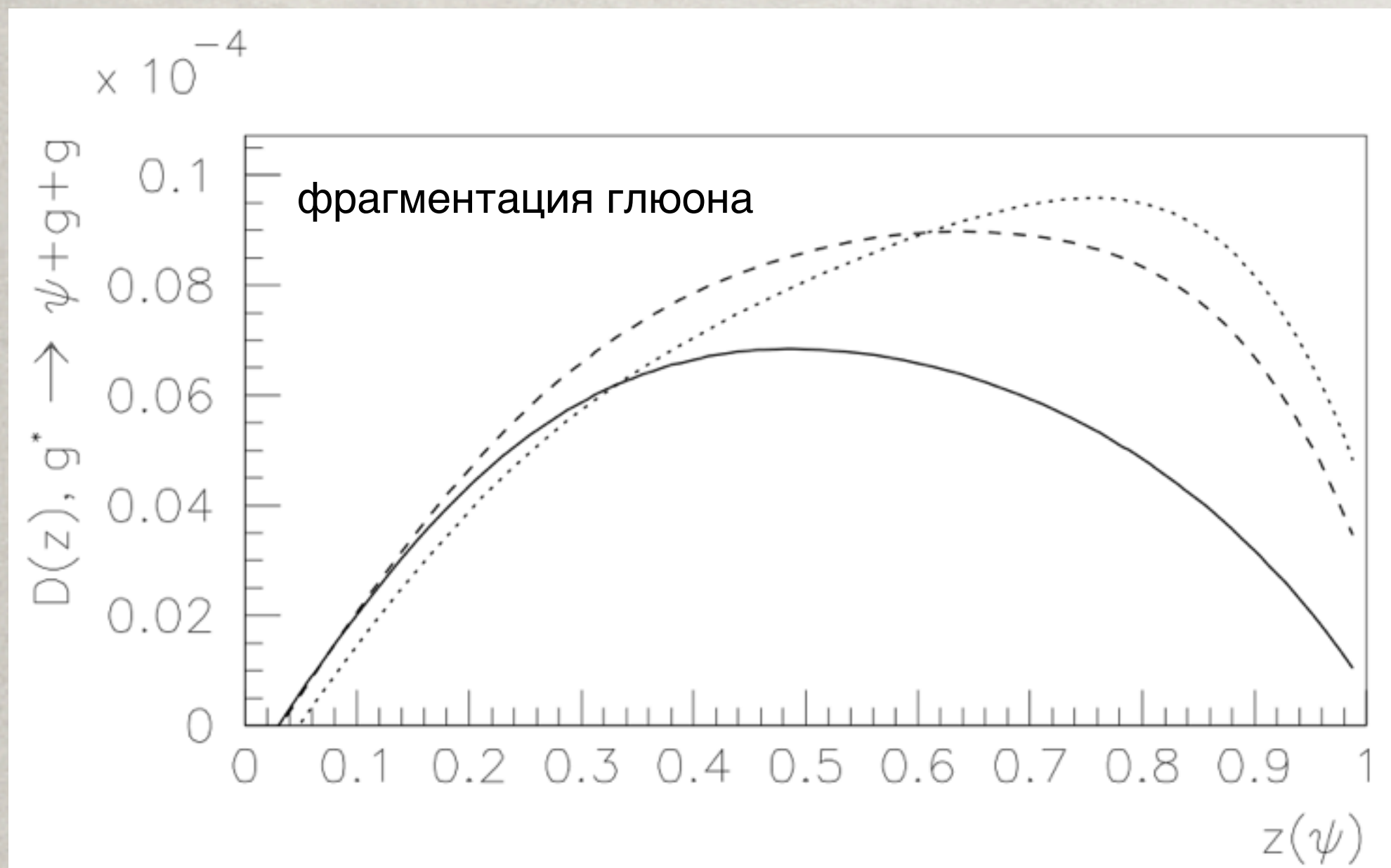
Perturbative fragmentation $g \rightarrow J/\psi + 2g$



S. Baranov & B.K. 2017

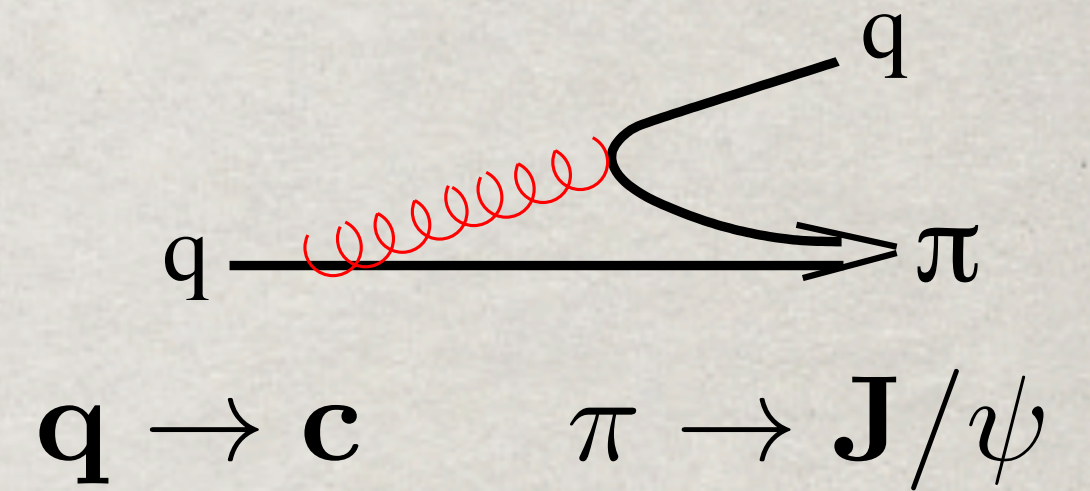
$$dD(g^* \rightarrow \psi gg) = \frac{1}{(2\pi)^6} \frac{1}{32 m_g^6} |\mathcal{M}(g^* \rightarrow J/\psi gg)|^2 dm_g^2 d\Omega_\psi d\phi ds_2 ds_3$$

$$D(z) = \int D(g^* \rightarrow \psi gg) \delta(z - p_\psi^+ / k_1^+) dm_g^2 d\Omega_\psi d\phi ds_2 ds_3.$$

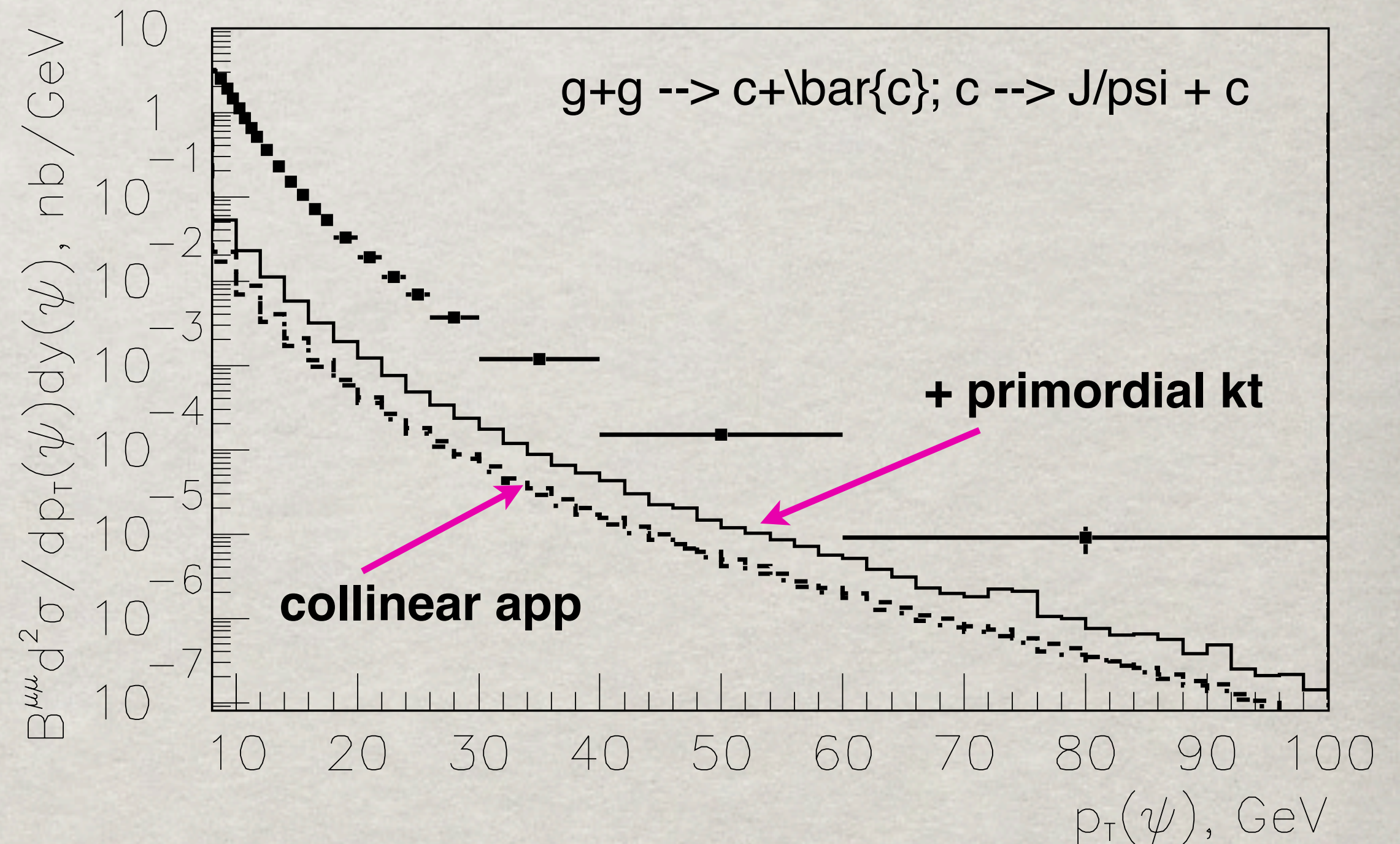
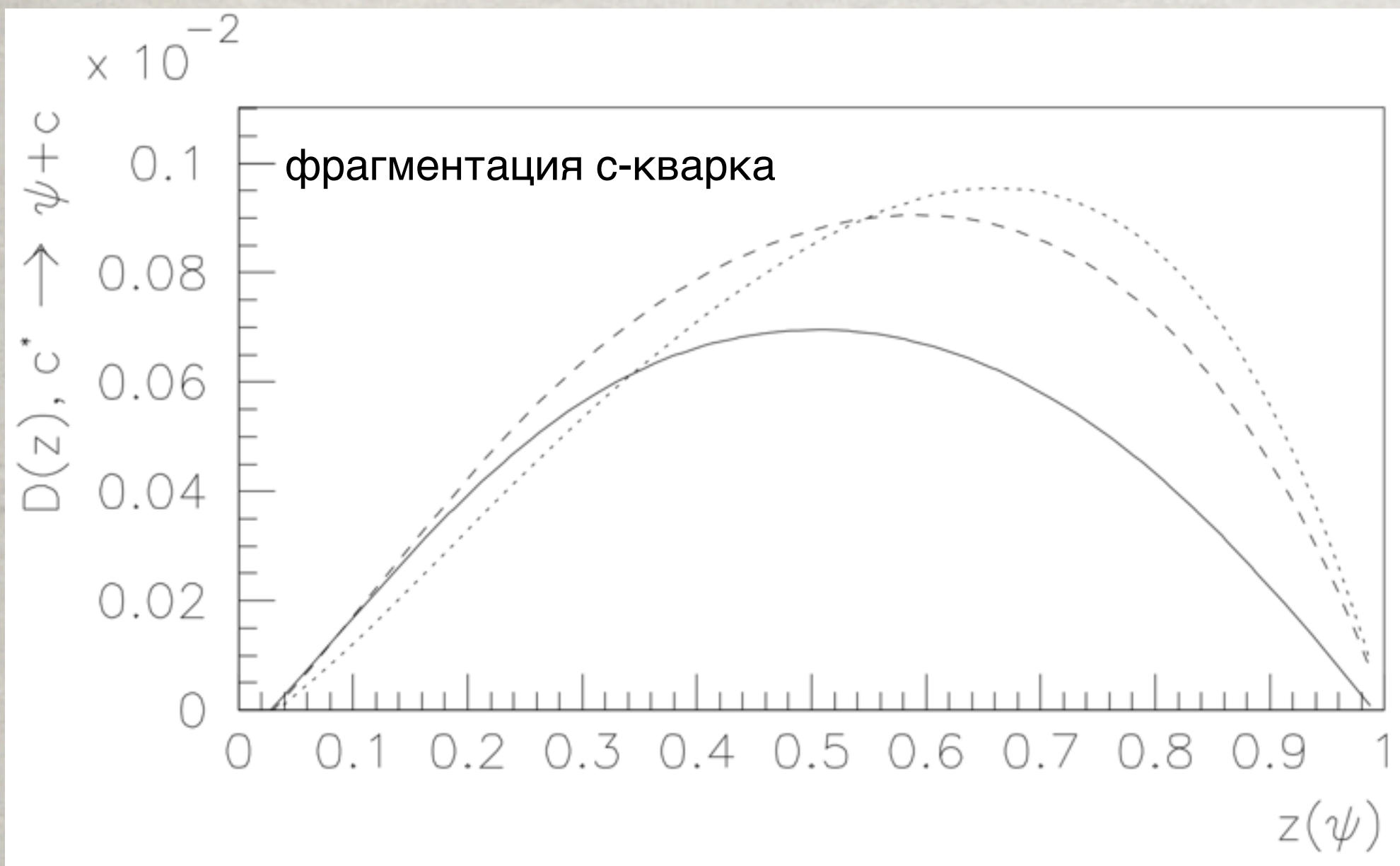


Quark fragmentation

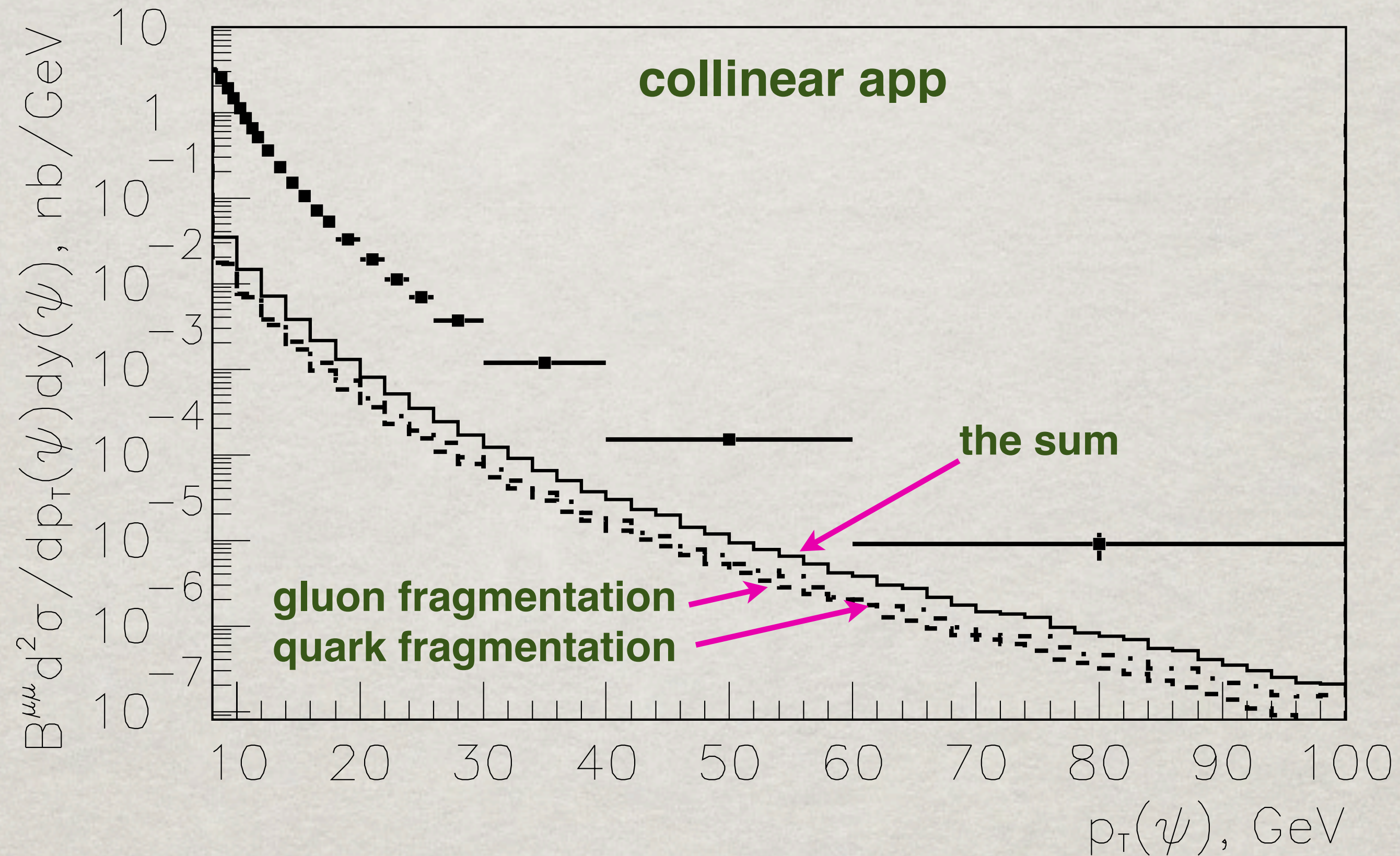
Even if a strong kick breaks-up the c - \bar{c} pair, a single high- p_T c -quark can fragment into J/ψ similar to $q \rightarrow \pi q$ transition



S. Baranov & B.K. 2017



Gluon vs quark fragmentations



Reserves:

kt-factorization pulls the result up by about factor three

J/ ψ 's from X should be excluded from data, pulling it down by about 30%

No severe disagreement remains

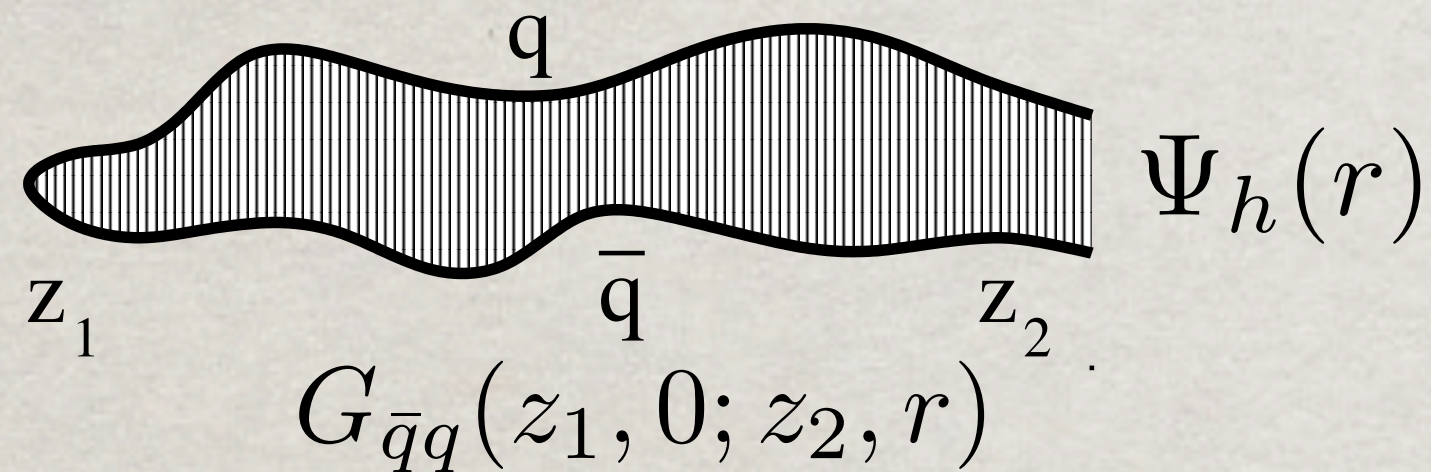
Summary

- A high- p jet with virtuality equal to its energy dissipates energy so intensively, that has to produce a leading hadron (colorless dipole) with large z promptly, on a very short time scale, which does not rise with p_T .
- Production of a dipole on a short time scale can be treated perturbatively.
- A high- p_T J/ψ appears to result from perturbative fragmentation of either a gluon, or a quark
- Reasonable agreement with data at high p_T is achieved.

Exact solution: path integrals

BK, B.Zakharov, Phys.Rev. D44(1991)3466

One has to sum up all quark trajectories.



$$\left[i \frac{d}{dl_2} - \frac{m_q^2 - \Delta_{r_2}}{p_T/2} - V_{\bar{q}q}(l_2, r_2) \right] G_{\bar{q}q}(l_1, r_1; l_2, r_2) = 0$$

$$\text{Im} V_{\bar{q}q}(l, r) = -\frac{1}{4} \hat{q}(l) r^2$$

R_{AA} rises with p_T due to color transparency

The model for time and position dependent \hat{q}

$$\hat{q}(l, \vec{b}, \vec{\tau}) = \frac{\hat{q}_0 l_0}{l} \frac{n_{part}(\vec{b}, \vec{\tau})}{n_{part}(0, 0)}$$

BK, I.Potashnikova, I.Schmidt
Phys.Rev.C83(2011)021901

BK, J.Nemchik, I.Potashnikova, I.Schmidt
Phys.Rev. C86(2012)054904

